



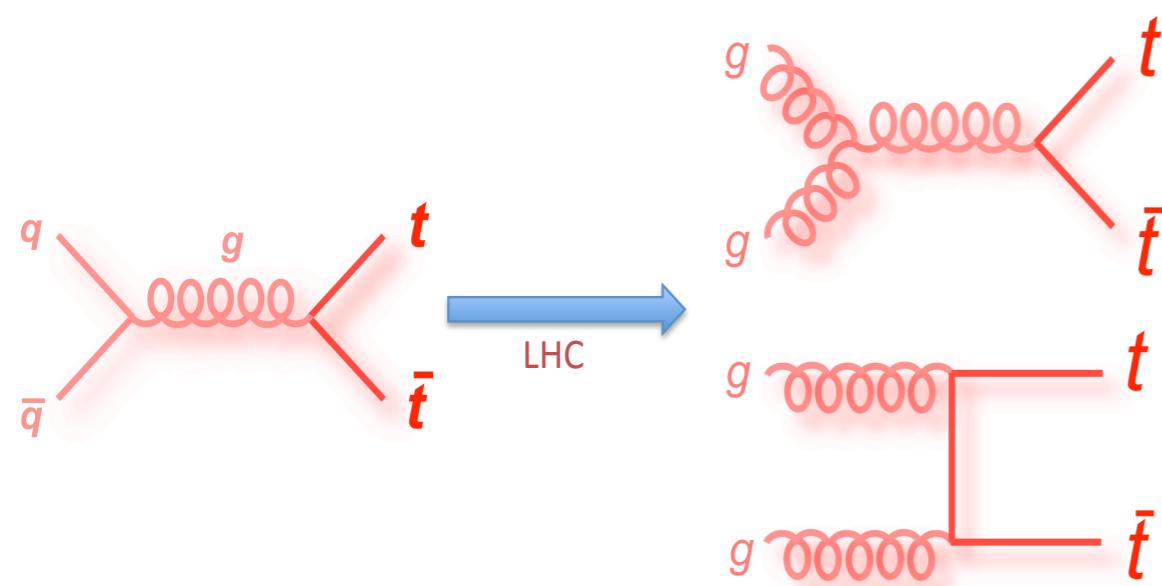
# Measurement of $t\bar{t}$ Production Cross Section Using b-tagged Semileptonic Events

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# Introduction

- Pair production

- ▶  $\sigma \sim 7.5 \text{ pb}$  (Tevatron 1.96 TeV ppbar)
- ▶  $\sigma \sim 165 \text{ pb}$  (LHC 7 TeV) Pair production

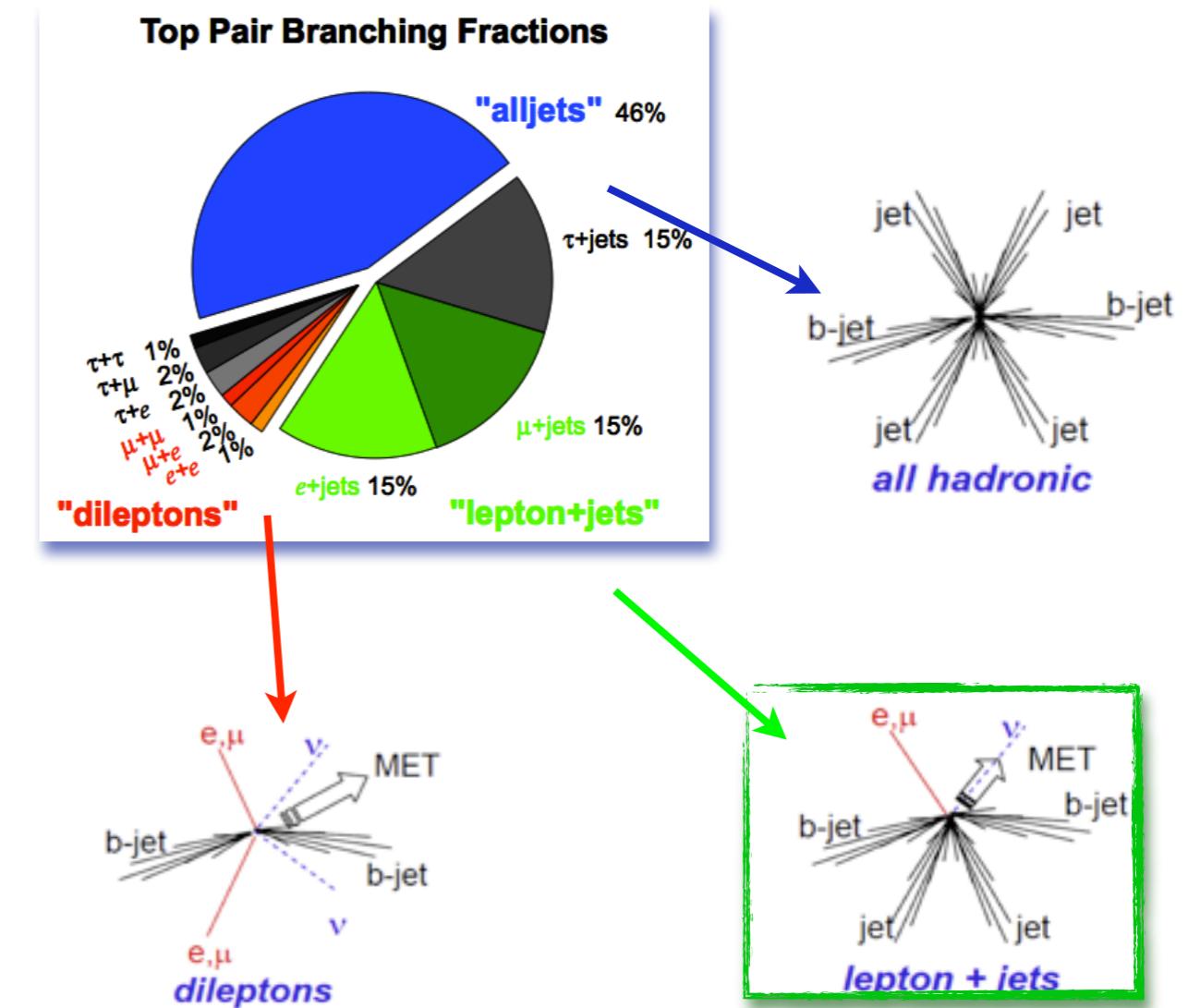


$\sim 90\%$ (Tevatron)  
 $\sim 15\%$ (LHC)

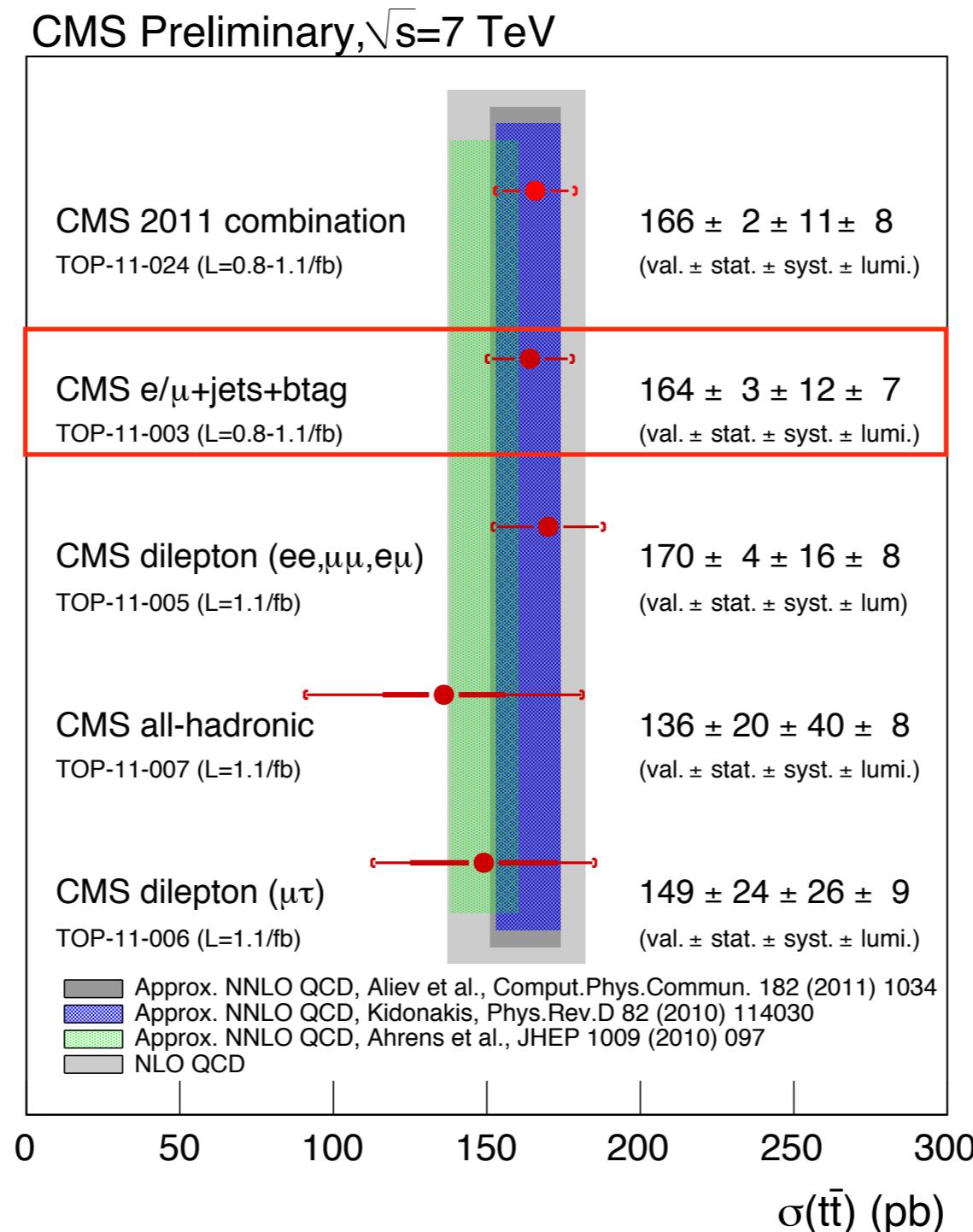
$\sim 10\%$ (Tevatron)  
 $\sim 85\%$ (LHC)

- Top Pair final state decays

- ▶ Golden channels: lepton + jets and dilepton
- ▶ Challenging channels: full hadronic, tau + mu



# Cross-section Measurement



<https://twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResultsTOP>

# Event Selection

- Triggers

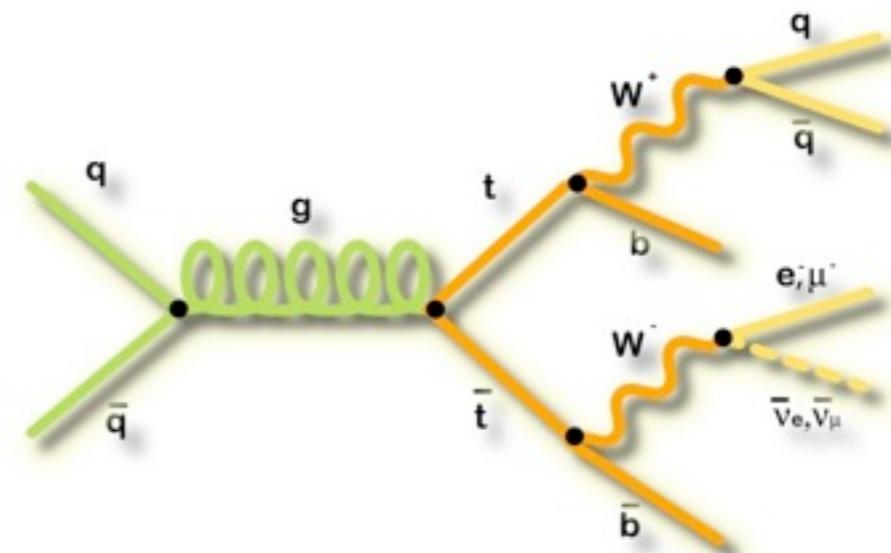
- ▶ Single Electron/Muon

- Electrons

- ▶ Electron ID with 70% (95%) reconstruction efficiency (second electron for dilepton veto)
- ▶ Relative isolation  $<0.01$  and conversion rejection
- ▶  $|\eta| < 2.5$ ,  $P_T > 45$  GeV

- Muons

- ▶ Global and tracker muon, relative isolation  $<0.125$
- ▶  $|\eta| < 2.1$ ,  $P_T > 35$  GeV



- Jets

- ▶ anti- $k_T$  jet clustering algorithm with  $R=0.5$
- ▶  $P_T > 30$  GeV and  $|\eta| < 2.4$ , JetID
- ▶  $\geq 1$  btag jet using standard high efficiency tagger

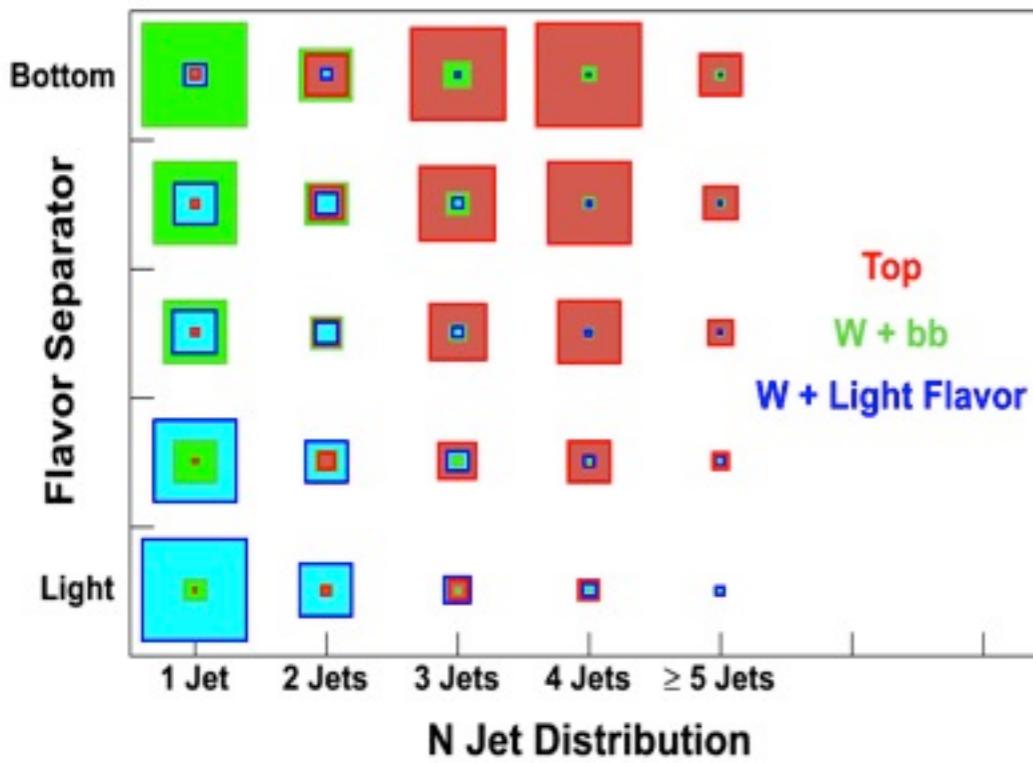
- MET

- ▶ Negative sum of transverse momenta of all reconstructed particles
- ▶ MET  $> 20.0$  GeV

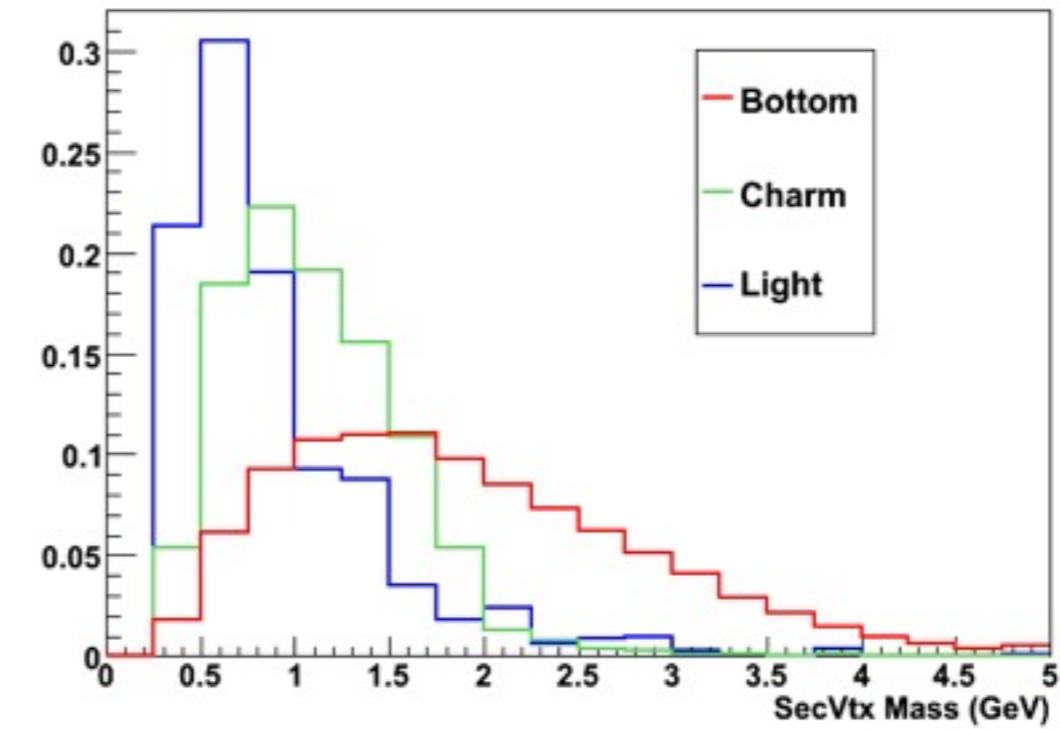
# Simultaneous Heavy Flavor and Top

- Discriminating variables
  - ▶ N-Jet distribution - Distinguish Top from Wbb
  - ▶ “Flavor separator” - Distinguish Wbb from W+charm and W+LF
    - Secondary vertex (secvtx) mass— invariant mass of tracks originating at identified secvtx
    - Good separation of bottom from charm and light flavor jets
- Perform a simultaneous 3D( $N_{\text{Jets}}$ ,  $N_{\text{Tags}}$ , secvtx mass) Maximum Profile likelihood Fit

Flavor Separator versus N-Jet Distribution

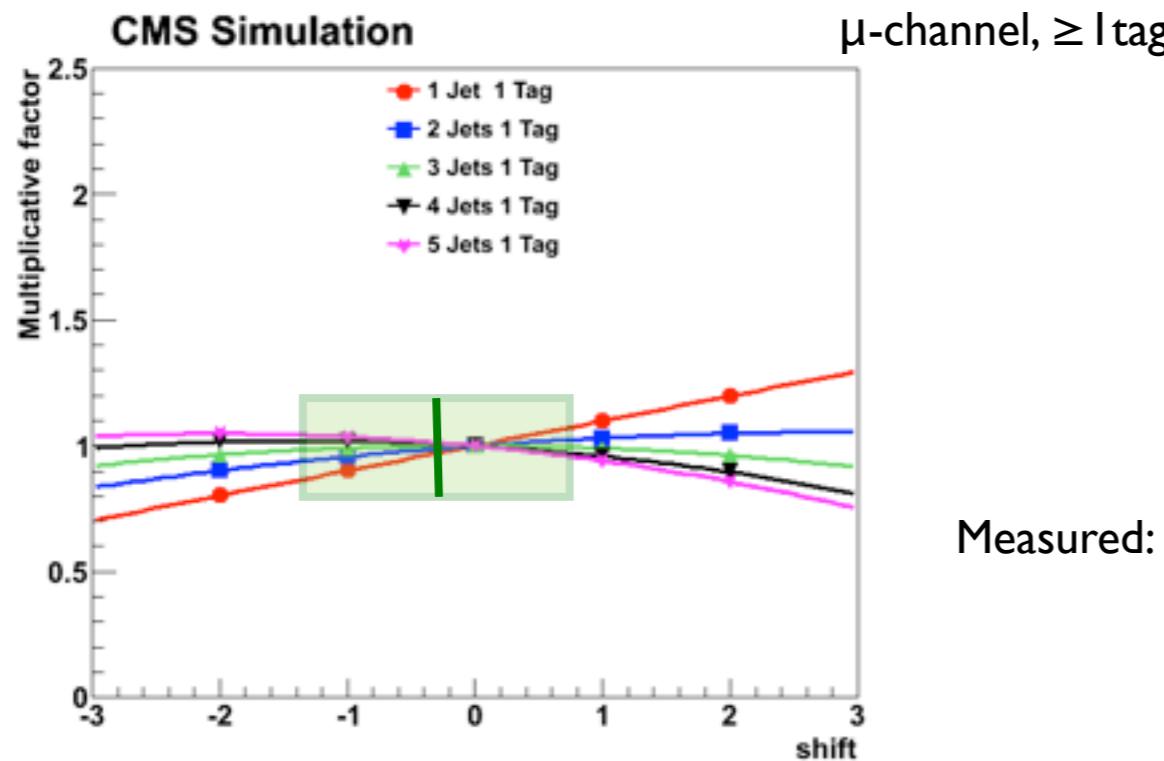


Secondary Vertex Mass Distributions

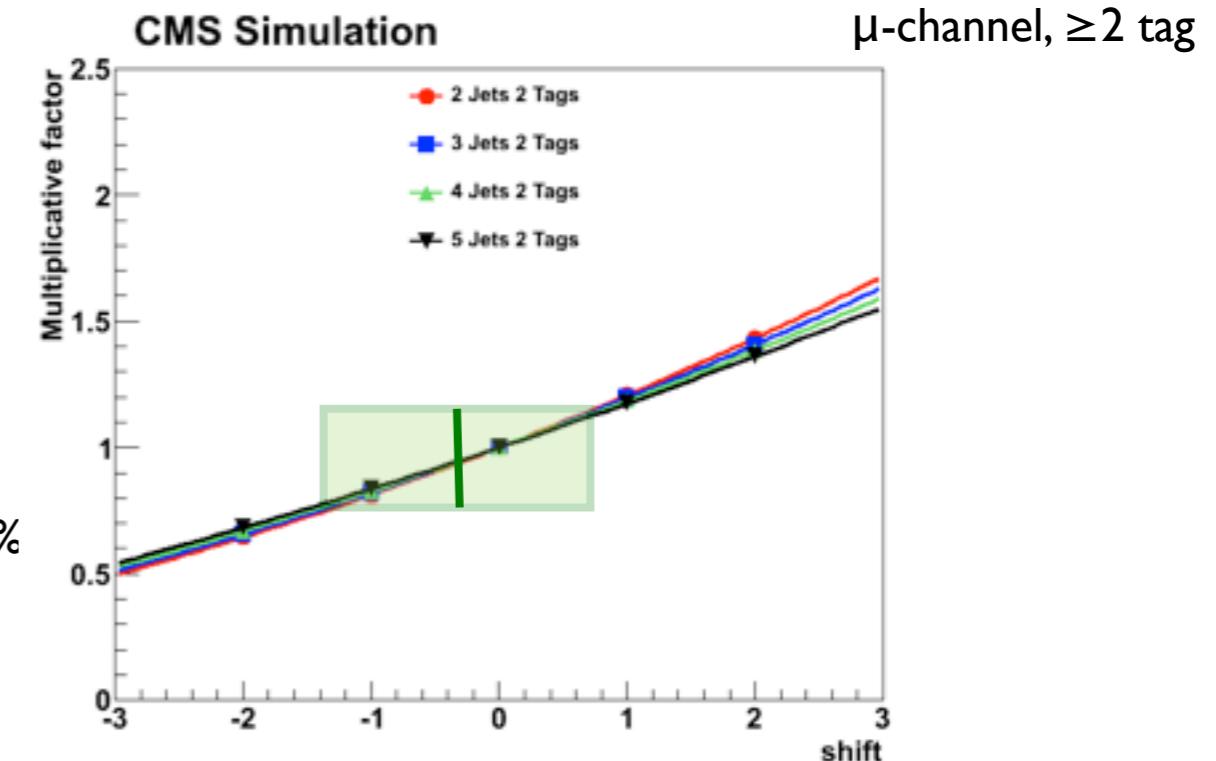


# Systematic Uncertainties (I)

- How do we put systematic uncertainties into fitter?
  - ▶ Create and compare the nominal and shifted MC templates
- All functional forms are parameterized as polynomials
  - ▶ Generally 2<sup>nd</sup> order and are applied as multiplicative factors.
- For example: Able to extract btag efficiency in-situ
  - ▶ Use b-tagging efficiency and mistag SF constrained to  $1.0 \pm 0.1$



Measured:  $97 \pm 1\%$



Btag group measurement of  $95 \pm 1\%$  is covered in our  $1\sigma$  interval

# Systematic Uncertainties (2)

Quantity	Constraint (%)
$b$ -tag Efficiency Scale Factor	$100 \pm 10$
$b$ -tag Mistag Scale Factor	$100 \pm 10$
Jet energy scale relative to nominal	$100 \pm 3$ ( $\eta, p_T$ dependent)
$W+jets$ renormalization/factorization scales	$100^{+100}_{-50}$
$W+jets$ background normalization	unconstrained
QCD background normalization	$100 \pm 100$
Single-top background normalization	$100 \pm 30$
$Z+jets$ background normalization	$100 \pm 30$

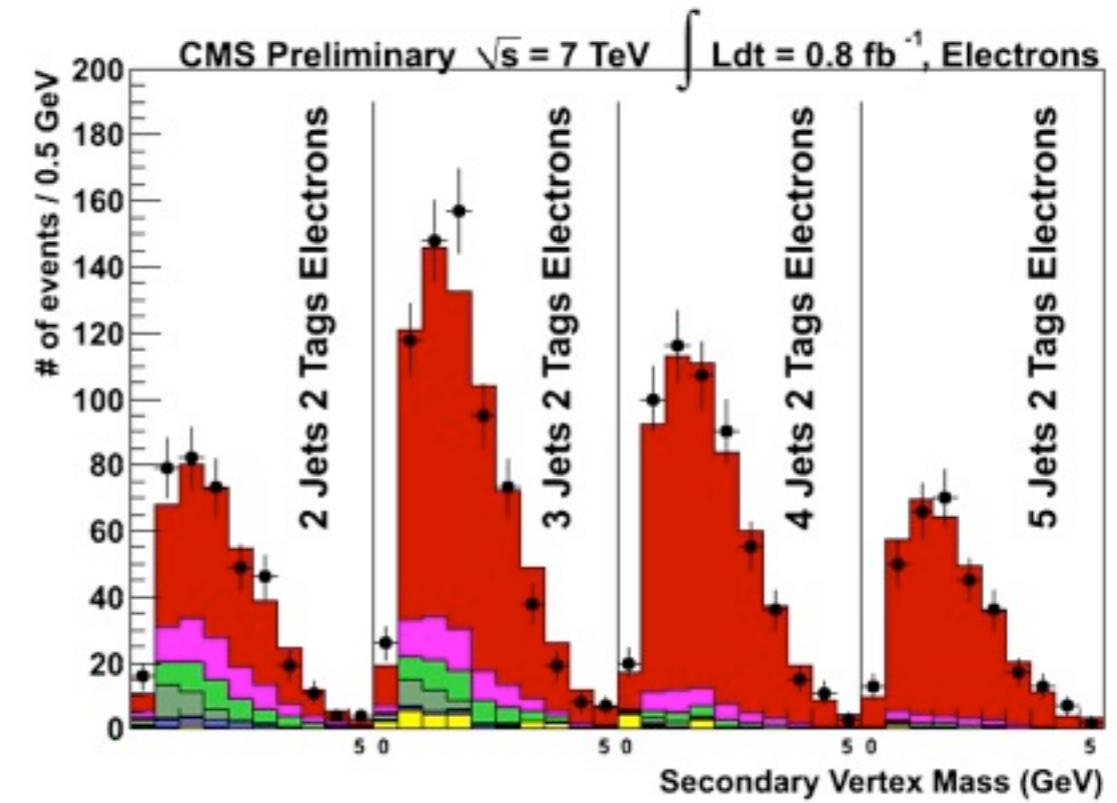
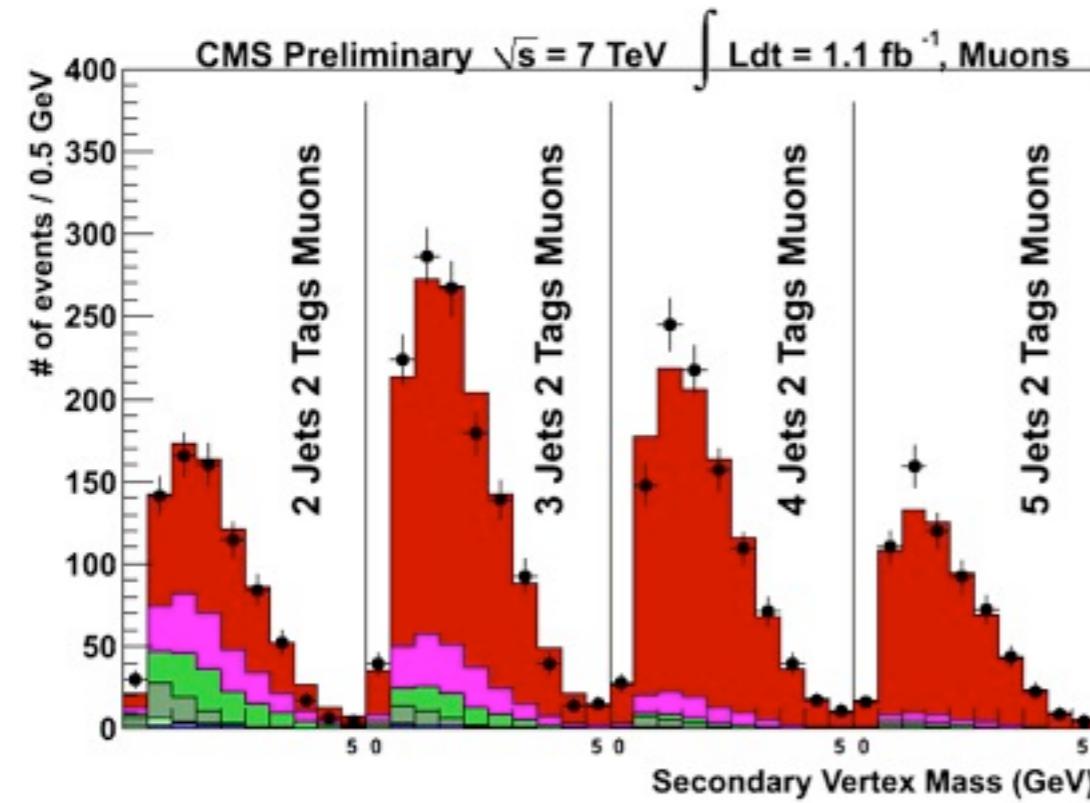
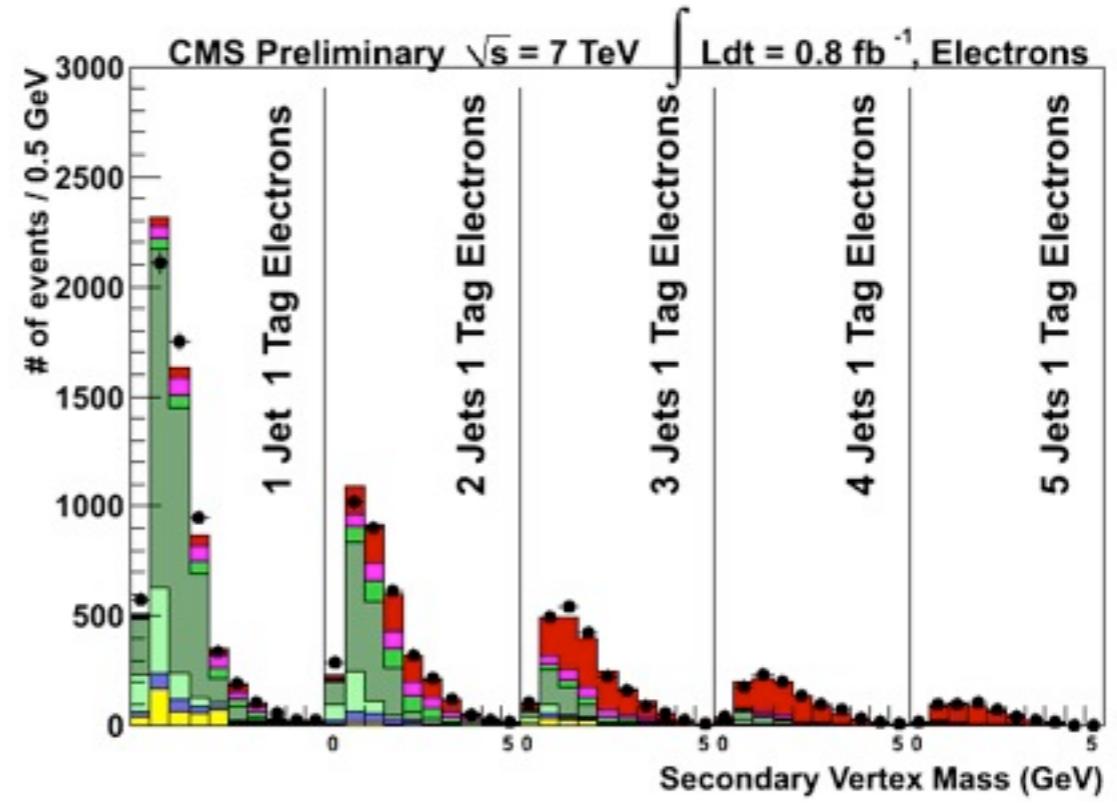
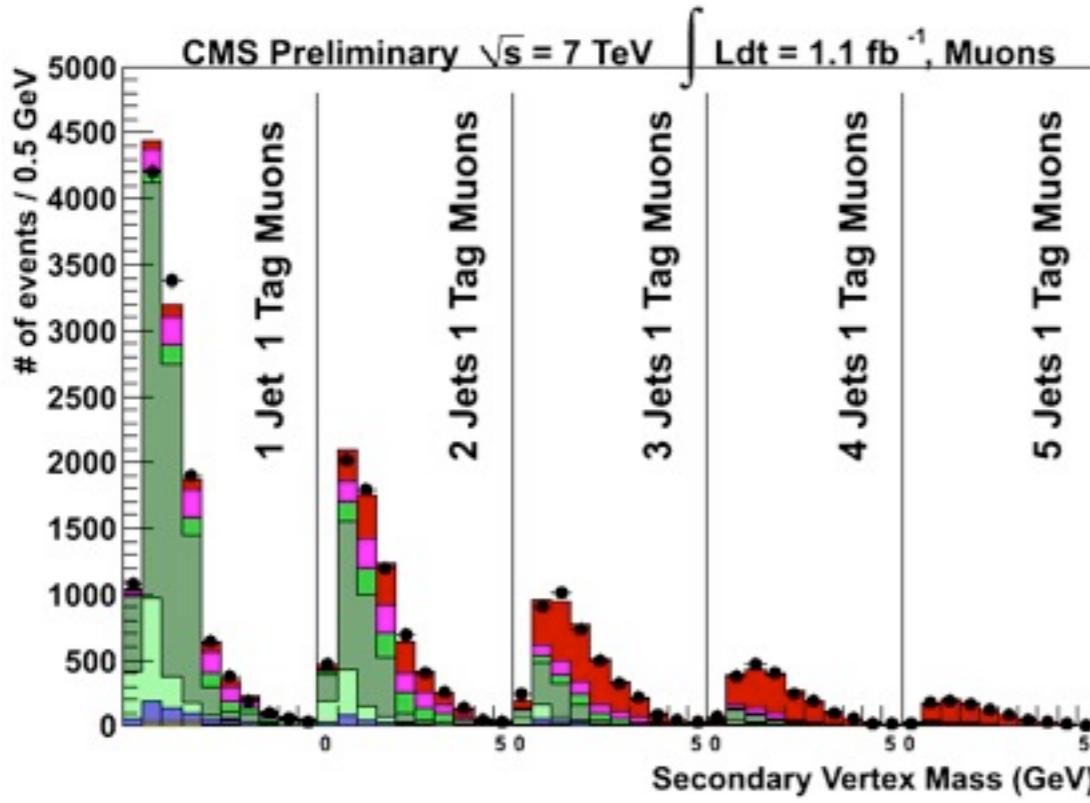
systematic uncertainties  
covered in fit

Source	Muon Analysis	Electron Analysis	Combined Analysis
Quantity	Uncertainty (%)		
Lepton ID/reco/trigger	3.4	3	3.4
$E_T$ resolution due to unclustered energy	< 1	< 1	< 1
$t\bar{t}+jets$ $Q^2$ scale	2	2	2
ISR/FSR	2	2	2
ME to PS matching	2	2	2
Pile-up	2.5	2.6	2.6
PDF	3.4	3.4	3.4
Profile Likelihood Parameter	Uncertainty (%)		
Jet energy scale and resolution	4.2	4.2	3.1
$b$ -tag efficiency	3.3	3.4	2.4
$W+jets$ $Q^2$ scale	0.9	0.8	0.7
Combined	7.8	7.8	7.3

systematic uncertainties not  
covered in fit

Important! The full result is not  
the sum of the squares. Have to  
account for correlations (fitter  
does this automatically)

# Results



• Data	$t\bar{t}$	Single Top	$W+b\text{-jets}$	$W+c\text{-jets}$	$W+\text{LF-jets}$	$Z+\text{jets}$	QCD
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# Results

Channel	luminosity	Measurement
$\mu + \text{jets}$	1.1/fb	$163.2 \pm 3.4 \text{ (stat.)} \pm 12.7 \text{ (syst.)} \pm 7.3 \text{ (lum.) pb}$
$e + \text{jets}$	0.8/fb	$163.0 \pm 4.4 \text{ (stat.)} \pm 12.7 \text{ (syst.)} \pm 7.3 \text{ (lumi.) pb}$
combine	0.8-1.1/fb	$164.4 \pm 2.8 \text{ (stat.)} \pm 11.9 \text{ (sys.)} \pm 7.4 \text{ (lumi.) pb}$

- Btag SF
  - ▶  $96.7 \pm 1\%$
- Jet Energy Scale:
  - ▶  $99.2 \pm 1.2\%$  of the nominal in agreement with 100%
- $W+Jets Q^2$ :
  - ▶  $9 \pm 10\%$  in agreement with the nominal value
- $W+b\text{-jets}$ :
  - ▶  $K=1.2 \pm 0.3 * \text{SM expectation}$
- $W+c\text{-jets}$ :
  - ▶  $K=1.7 \pm 0.1 * \text{SM expectation}$

# Extra material

# Results

Fit factors	
Top	$164.2^{+6.1}_{-5.9}$
SingleTop	$1.44^{+0.27}_{-0.27}$
Wbx	$1.21^{+0.28}_{-0.27}$
Wcx	$1.66^{+0.06}_{-0.06}$
Wqq	$0.58^{+0.08}_{-0.07}$
ZJets	$1.34^{+0.29}_{-0.29}$
Fit Shifts	
Q2	$0.09^{+0.10}_{-0.10}$
btag	$-0.33^{+0.11}_{-0.11}$
jes	$-0.28^{+0.39}_{-0.40}$
lftag	$0.11^{+1.00}_{-1.00}$
qcdConstr_1j_el	$0.60^{+0.34}_{-0.33}$
qcdConstr_1j_mu	$-0.78^{+0.25}_{-0.26}$
qcdConstr_2j_el	$-0.65^{+0.27}_{-0.26}$
qcdConstr_2j_mu	$-1.36^{+0.63}_{-0.63}$
qcdConstr_3j_el	$1.27^{+0.59}_{-0.59}$
qcdConstr_3j_mu	$0.09^{+0.86}_{-0.86}$
qcdConstr_4j_el	$-0.21^{+0.38}_{-0.36}$
qcdConstr_4j_mu	$0.19^{+0.85}_{-0.85}$
qcdConstr_5j_el	$-0.46^{+0.45}_{-0.44}$
qcdConstr_5j_mu	$-0.20^{+0.98}_{-0.98}$

*uncorrected*  
 $\sigma(\text{Top})$  in pb

}

fraction of SM

}

shift from nominal  
value [ $\sigma$ ]

constrained to  $0 \pm 1$

}

shift from nominal  
value [ $\sigma$ ]

100% uncert.  
constrained to  $0 \pm 1$

# Results (Correlation Matrix)

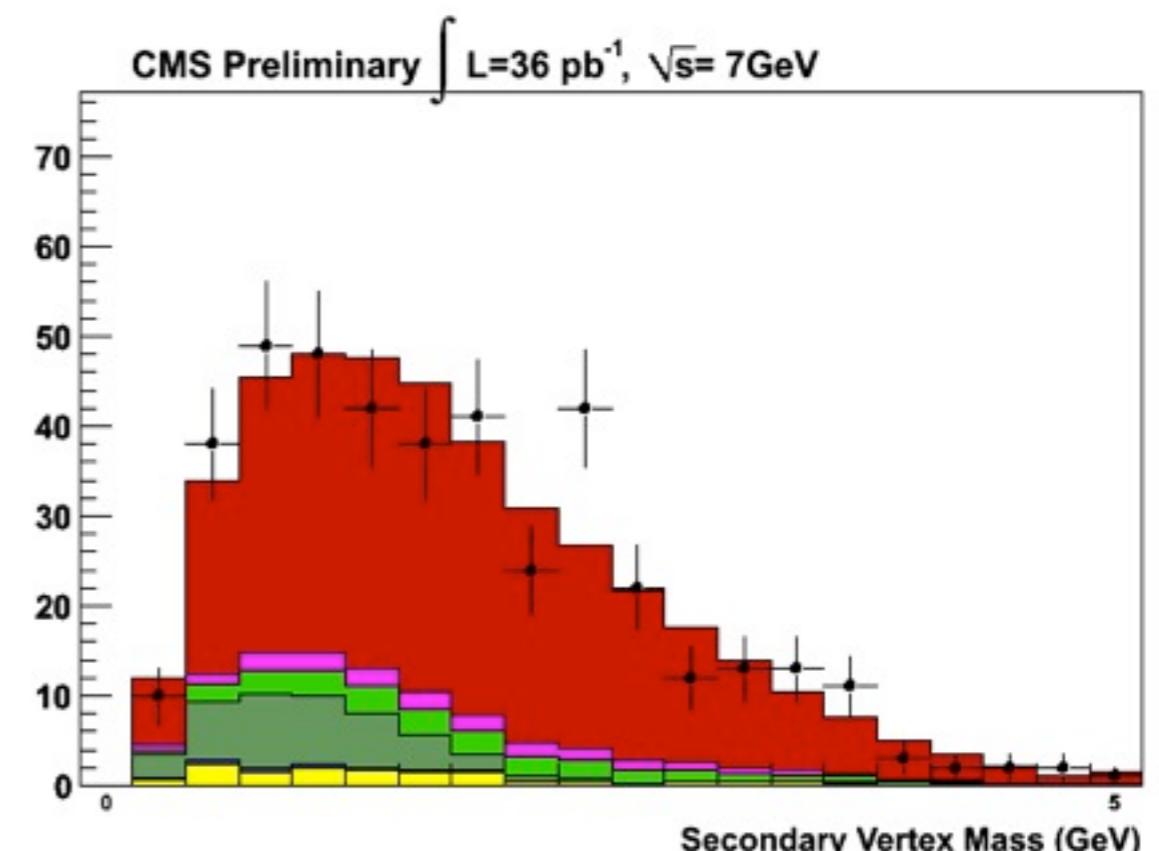
	Top	SingleTop	Wbx	Wcx	Wqq	Zjets	Q2	btag	jes	lftag
Top	1.000	-0.285	-0.180	0.288	0.032	0.074	-0.135	-0.627	-0.835	0.002
SingleTop	-0.285	1.000	-0.731	0.049	0.047	-0.041	0.069	-0.104	0.134	-0.006
Wbx	-0.180	-0.731	1.000	0.068	0.123	-0.145	0.295	0.195	0.269	-0.002
Wcx	0.288	0.049	0.068	1.000	0.053	0.034	0.673	-0.428	-0.204	-0.011
Wqq	0.032	0.047	0.123	0.053	1.000	-0.139	0.311	-0.058	-0.048	-0.763
ZJets	0.074	-0.041	-0.145	0.034	-0.139	1.000	0.129	0.000	-0.100	0.002
Q2	-0.135	0.069	0.295	0.673	0.311	0.129	1.000	-0.022	0.231	-0.016
btag	-0.627	-0.104	0.195	-0.428	-0.058	0.000	-0.022	1.000	0.460	-0.011
jes	-0.835	0.134	0.269	-0.204	-0.048	-0.100	0.231	0.460	1.000	0.003
lftag	0.002	-0.006	-0.002	-0.011	-0.763	0.002	-0.016	-0.011	0.003	1.000

# Simple Fit For Top Cross Section

- Take all events (electrons and muons) with
  - ▶  $\geq 4$  jets
  - ▶  $\geq 1$  b-tag
- Put secondary vertex mass of leading b jet into fit.
- Constrain
  - ▶ Wbb ( $200\% \pm 200\%$  SM)
  - ▶ Single top ( $100\% \pm 30\%$  SM)
  - ▶ QCD (to MET fits  $\pm 100\%$ )
- Result:
  - ▶  $\sigma_{tt} = 150 \pm 17$  (stat + Wbb)  
 $\pm 11$  (Btag)  $\pm 11$  (JES)  
 $\pm 9$  (Syst) pb  
 $= 150 \pm 22$  pb

Most of this is due  
to uncertainties on Wbb!

How Can We Reduce Uncertainties due to Wbb, B-tagging, and JES?



Theory value  $\sigma_{\text{top pair}} = 157 \text{ pb.}$

# Simultaneous Fit

- Fit separately lepton flavor (electron,muon), number of jets ( $l, 2, 3, 4, \geq 5$ ), and number of tags ( $l, \geq 2$ ).
- Fitter maximizes Poisson likelihood  $P(N_{\text{pred}}|\text{Data})$  for each bin.
  - ▶ It needs to understand how much of each sample ( e.g., top) is there for each lepton flavor, jet, and tag region.
- For example, top:

$$N_{\text{pred}_{t\bar{t}}}(\text{lepton, jet, tag}) = \sigma_{t\bar{t}} \cdot MC_{\text{pred}}(\text{lepton, jet, tag}) \cdot P_{N_{t\bar{t}}}^{\text{Btag}}(\text{lepton, jet, tag} | \mathcal{R}_{\text{Btag}}) \cdot P_{N_{t\bar{t}}}^{\text{JES}}(\text{lepton, jet, tag} | \mathcal{R}_{\text{JES}}) \cdot \dots$$

Number of predicted top pair events for a given lepton, jet, tag region

Top cross section (floats in fit)

MC prediction of events for a given lepton, jet, tags region

Polynomial function that describes fractional change to prediction as a function of  $R_{\text{btag}}$ . Always define to be exactly 1 when  $R_{\text{btag}}=0$ .

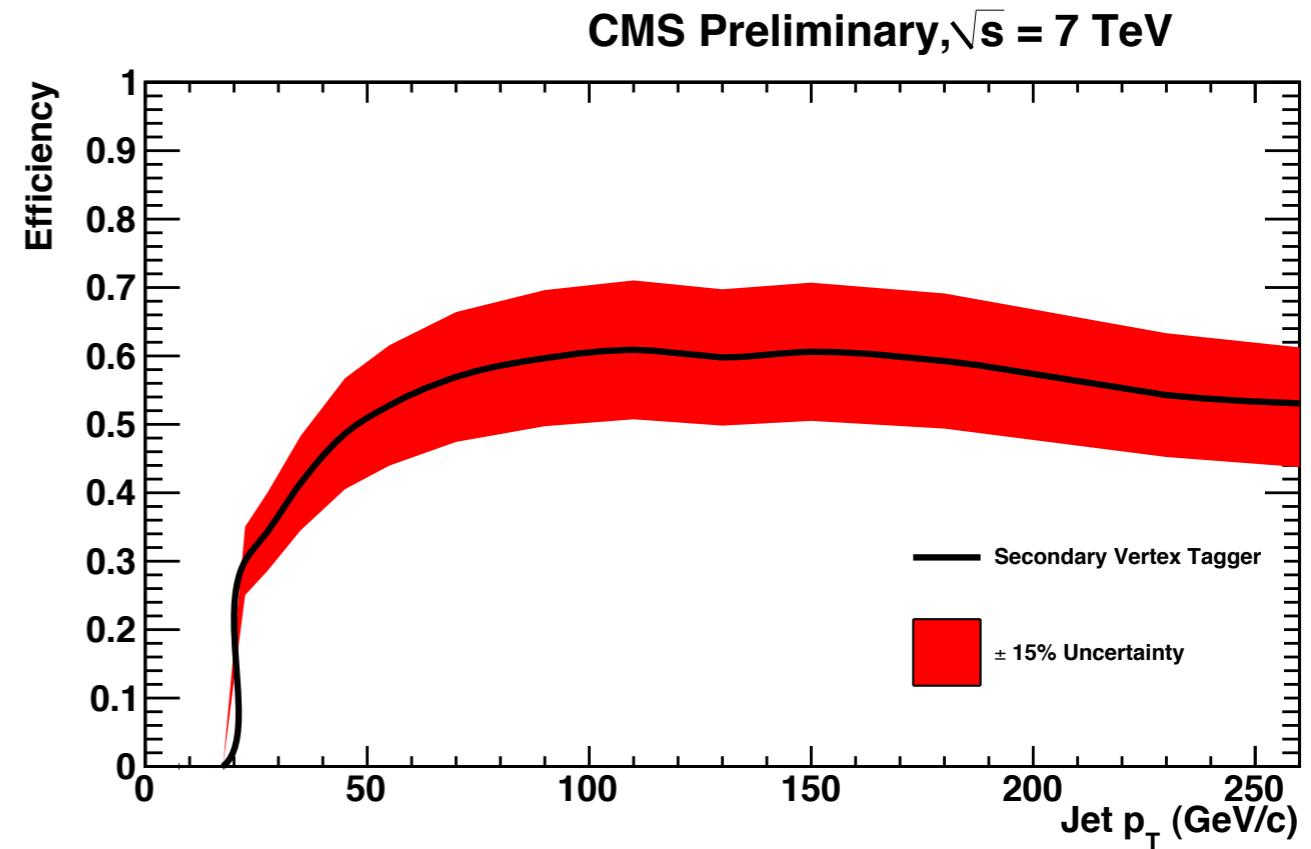
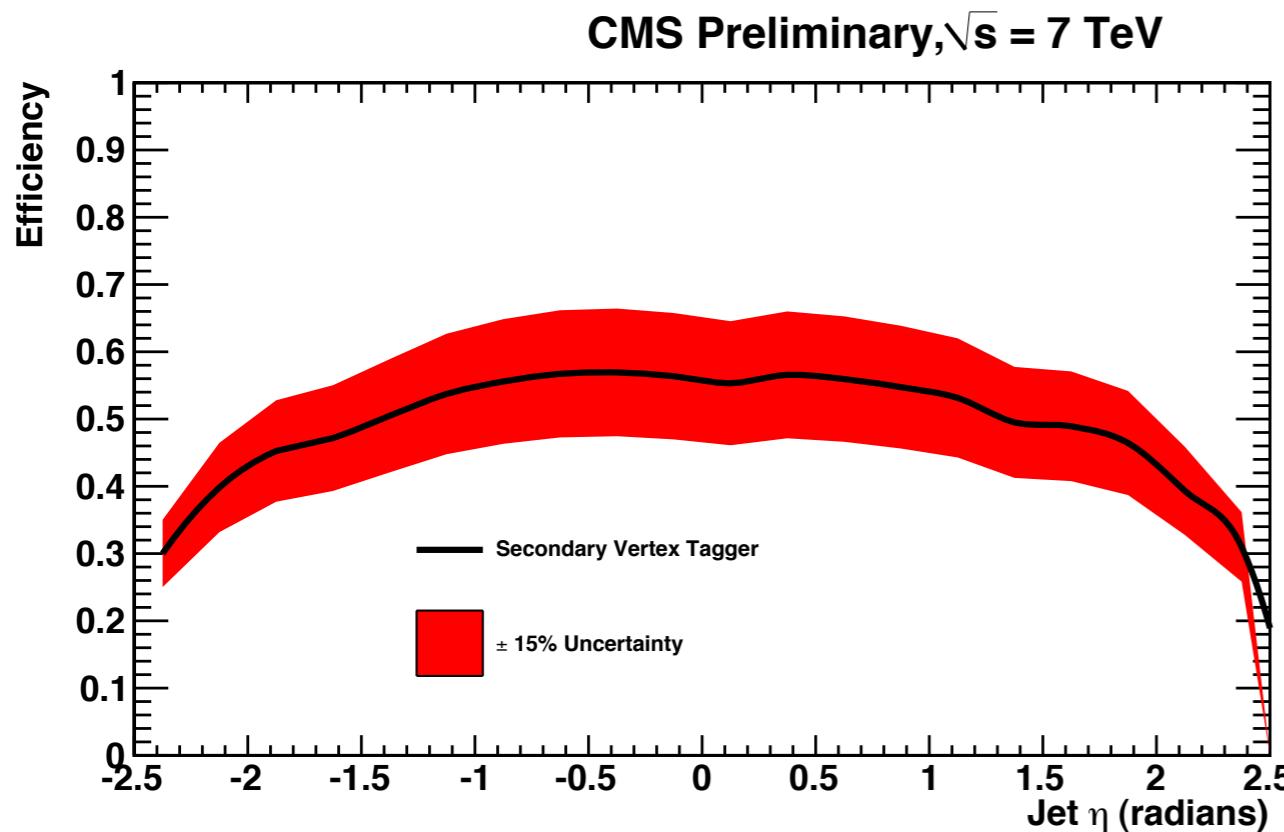
Nuisance parameter for the B-tagging

# b-Tagging Efficiency in Data

- Weight the tag jets in simulation

$$\mathcal{W} = \begin{cases} S_{btag} & \text{heavy flavor jet tagged during simulation} \\ 0 & \text{heavy flavor jet not tagged during simulation} \\ S_{mis} & \text{light flavor jet} \end{cases}$$

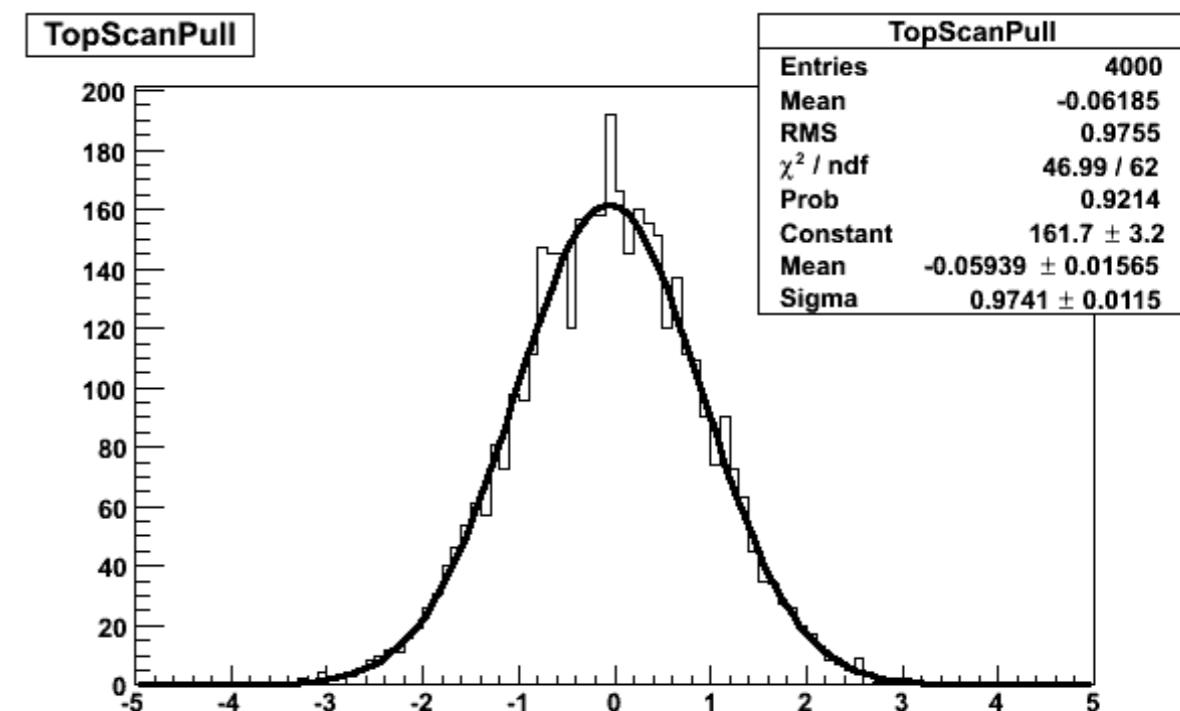
## Efficiency in Data



# Coverage

- How do we know that the fitter doesn't get lost somewhere?
- We run pseudo-experiments to determine 15%, 50% and 84% points for various pull distributions
- We correct for these small under coverage/bias

	Fitted values			PE Corr. [ $\sigma$ ]			Corr. values		
	+ Err	- Err	Bias	+Err	-Err		+Err	-Err	
Electron	162.4	8.9	-8.3	-0.06	1.04	1.01	163.0	9.3	-8.4
Muon	162.9	7.9	-7.7	-0.03	1.01	1.03	163.2	8.0	-7.9
e+mu	164.2	6.1	-5.9	-0.03	1.01	1.03	164.4	6.2	-6.1



Top pull distribution for the combine Mu+Ele channel generated with Q2 systematic uncertainty

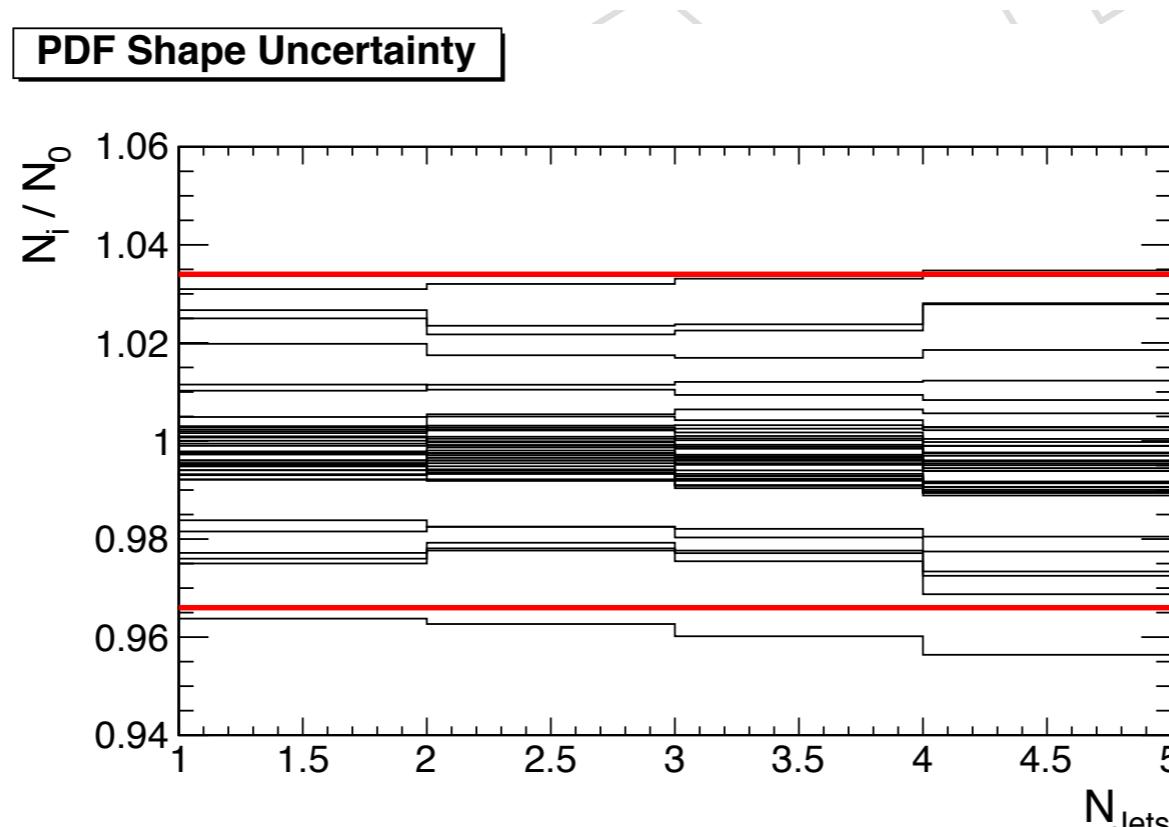
# PDF Uncertainty

- Examine the uncertainties in the PDF set CTEQ6M (default) which are defined in PDF set CTEQ6I
- The systematic uncertainty on the acceptance is estimated (1.004, 0.997)

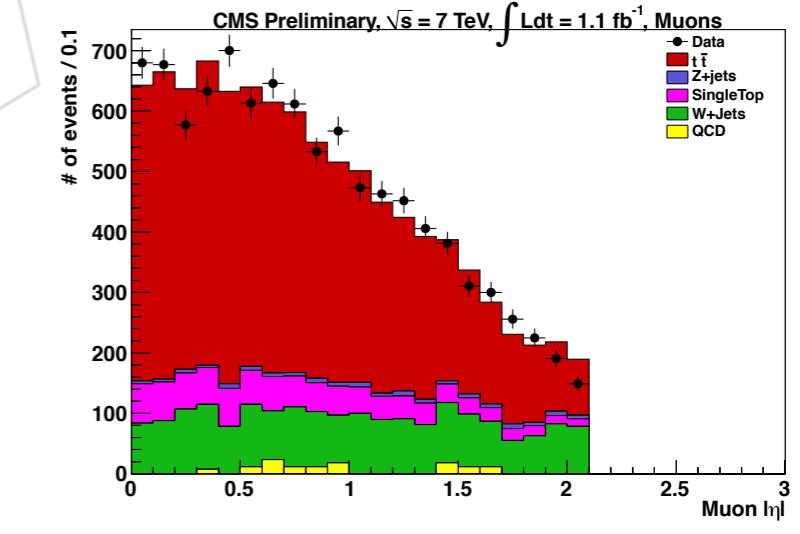
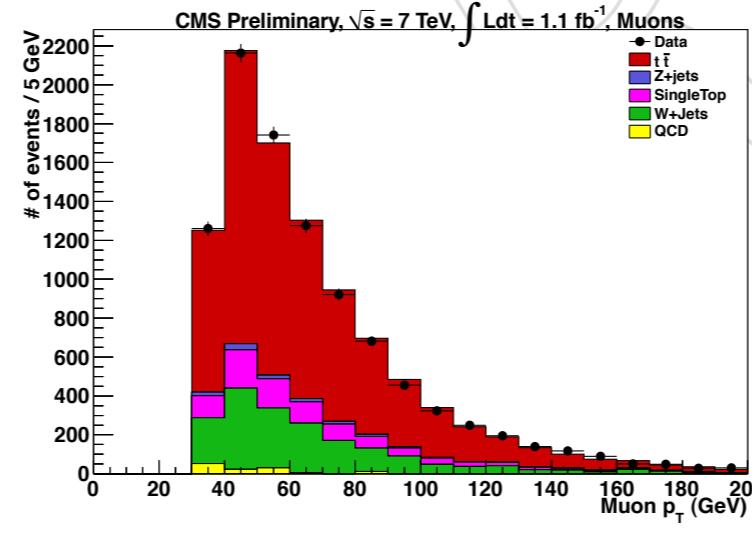
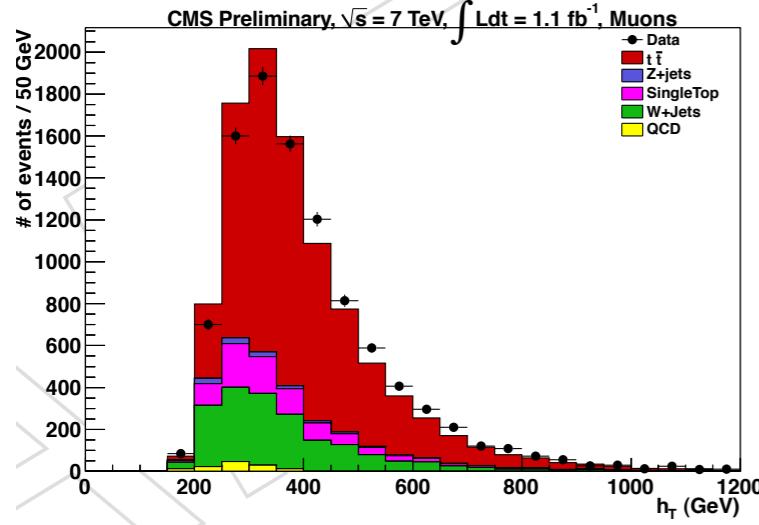
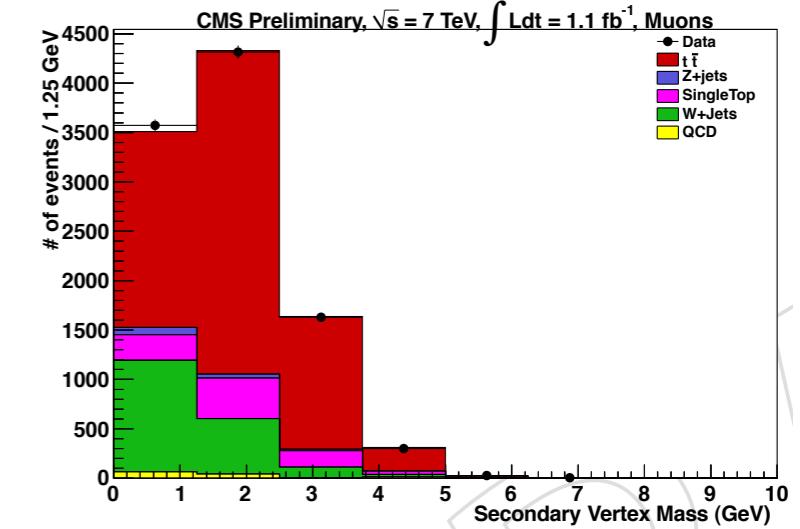
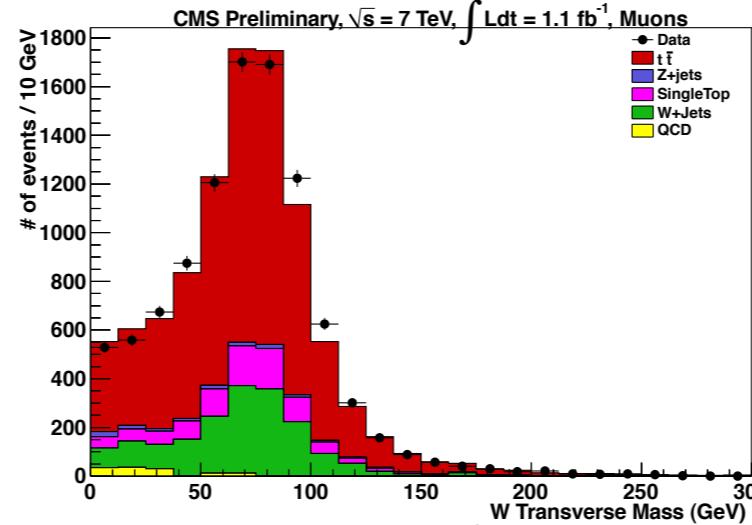
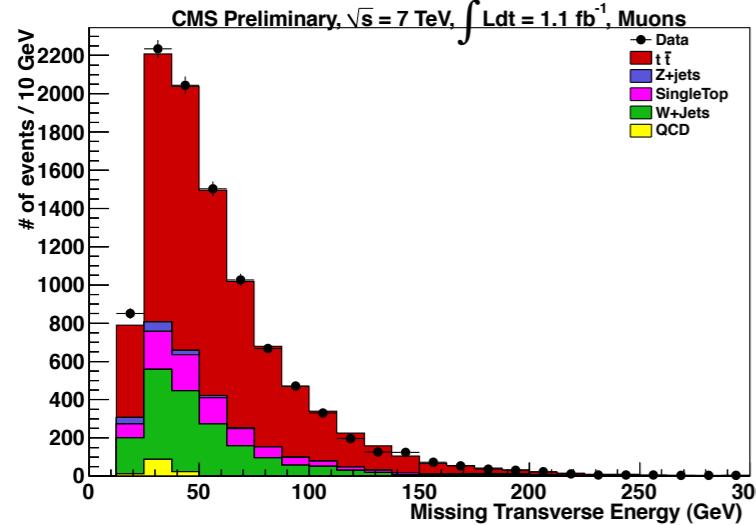
$$\Delta = \frac{1}{N_{\text{events}}} \sum_{\text{events}} \left[ \sum_{i=1}^{22} \left( \frac{\text{PDF}_+^i}{\text{PDF}_0} \right)^2 + \sum_{j=1}^{22} \left( \frac{\text{PDF}_-^j}{\text{PDF}_0} \right)^2 \right]$$

PDF uncertainty eigenvector weights

- The additional uncertainty due to Njets shape is estimated by examining the ratio between each of the Njet distribution corresponding to 44 eigenvectors in CTEQ6I and the nominal
- A flat 3.4% uncertainty for the 68% C.L. brackets the variation seen conservatively



# $\mu + \text{jets}$ kinematic distributions



# e+jets kinematic distributions

