



SUSY Model Building for a 126 GeV Higgs

Moritz McGarrie

The MSSM

3-generations:
stops are typically the
lightest
coloured
superpartners



Names		spin 0	spin 1/2	$SU(3)_C, SU(2)_L, U(1)_Y$
squarks, quarks ($\times 3$ families)	Q	$(\bar{u}_L \ \bar{d}_L)$	$(u_L \ d_L)$	$(\mathbf{3}, \mathbf{2}, \frac{1}{6})$
	$\bar{u}$	$\bar{u}_R^*$	$u_R^\dagger$	$(\bar{\mathbf{3}}, \mathbf{1}, -\frac{2}{3})$
	$\bar{d}$	$\bar{d}_R^*$	$d_R^\dagger$	$(\bar{\mathbf{3}}, \mathbf{1}, \frac{1}{3})$
sleptons, leptons ($\times 3$ families)	L	$(\bar{\nu} \ \bar{e}_L)$	$(\nu \ e_L)$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$
	$\bar{e}$	$\bar{e}_R^*$	$e_R^\dagger$	$(\mathbf{1}, \mathbf{1}, 1)$
Higgs, higgsinos	H_u	$(H_u^+ \ H_u^0)$	$(\bar{H}_u^+ \ \bar{H}_u^0)$	$(\mathbf{1}, \mathbf{2}, +\frac{1}{2})$
	H_d	$(H_d^0 \ H_d^-)$	$(\bar{H}_d^0 \ \bar{H}_d^-)$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$

Table 1.1: Chiral supermultiplets in the Minimal Supersymmetric Standard Model. The spin-0 fields are complex scalars, and the spin-1/2 fields are left-handed two-component Weyl fermions.

Names	spin 1/2	spin 1	$SU(3)_C, SU(2)_L, U(1)_Y$
gluino, gluon	$\bar{g}$	g	$(\mathbf{8}, \mathbf{1}, 0)$
winos, W bosons	$\tilde{W}^\pm \ \tilde{W}^0$	$W^\pm \ W^0$	$(\mathbf{1}, \mathbf{3}, 0)$
bino, B boson	$\bar{B}^0$	B^0	$(\mathbf{1}, \mathbf{1}, 0)$

Table 1.2: Gauge supermultiplets in the Minimal Supersymmetric Standard Model.

The superpotential for the MSSM is

$$W_{\text{MSSM}} = \bar{u} \mathbf{y}_u Q H_u - \bar{d} \mathbf{y}_d Q H_d - \bar{e} \mathbf{y}_e L H_d + \mu H_u H_d. \quad (6.1.1)$$

$$\mathbf{y}_u \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_t \end{pmatrix}, \quad \mathbf{y}_d \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_b \end{pmatrix}, \quad \mathbf{y}_e \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_\tau \end{pmatrix}. \quad (6.1.2)$$

A-terms:
Soft terms for each Yukawa

$$\begin{aligned} \mathcal{L}_{\text{soft}}^{\text{MSSM}} = & -\frac{1}{2} \left(M_3 \bar{g} g + M_2 \tilde{W} \tilde{W} + M_1 \bar{B} B + \text{c.c.} \right) \\ & - \left(\bar{u} \mathbf{a}_u \bar{Q} H_u - \bar{d} \mathbf{a}_d \bar{Q} H_d - \bar{e} \mathbf{a}_e \bar{L} H_d + \text{c.c.} \right) \\ & - \bar{Q}^\dagger \mathbf{m}_Q^2 \bar{Q} - \bar{L}^\dagger \mathbf{m}_L^2 \bar{L} - \bar{u} \mathbf{m}_u^2 \bar{u}^\dagger - \bar{d} \mathbf{m}_d^2 \bar{d}^\dagger - \bar{e} \mathbf{m}_e^2 \bar{e}^\dagger \\ & - m_{H_u}^2 H_u^* H_u - m_{H_d}^2 H_d^* H_d - (b H_u H_d + \text{c.c.}) . \end{aligned}$$

$$\mathbf{a}_u \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a_t \end{pmatrix}, \quad \mathbf{a}_d \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a_b \end{pmatrix}, \quad \mathbf{a}_e \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a_\tau \end{pmatrix}, \quad (6.5.28)$$

1. The Higgs mass 126 GeV

The MSSM at one-loop

$$m_h^2 \simeq m_z^2 \cos^2(2\beta) + \frac{3}{(4\pi)^2} \frac{m_t^4}{v_{ew}^2} \left[\log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left(1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right]$$

Diagram illustrating the Higgs mass formula with annotations:

- top mass**: points to m_t
- average stop mass**: points to $m_{\tilde{t}}$

$$126^2 = 91^2 + 81^2$$

$$X_t = A_t - \mu \cot \beta$$

stop mixing

- Radiative corrections are same order as tree level piece
- corrections run logarithmically in SUSY
- MSSM case implies either heavy stops or large $X_t = A_t + \dots$

Fine tuning: little hierarchy problem

$$m_z^2 = -2(m_{H_u}^2 + |\mu|^2) + \dots$$

Light Higgsino

For a natural cancellation these should be of the same order

Light stops

$$\delta m_{H_u}^2 \sim -\frac{3y_t^2 m_{\tilde{t}}^2}{4\pi^2} \text{Log} \left(\frac{\Lambda}{m_{\tilde{t}}} \right) - \frac{3g^2}{8\pi^2} (m_{\tilde{W}}^2 + m_{\tilde{h}}^2) \text{Log} \left(\frac{\Lambda}{m_{\tilde{W}}} \right)$$

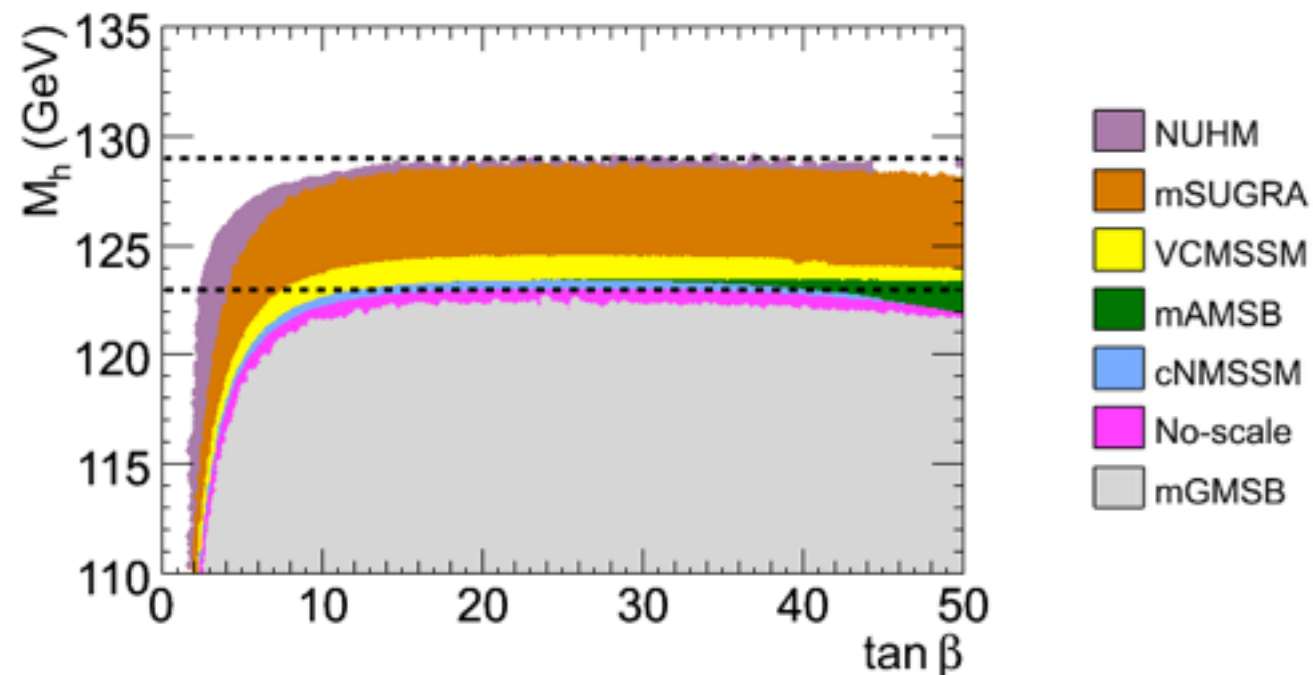
Light(ish) Gluino

$$\delta m_{\tilde{t}}^2 = \frac{8\alpha_s M_3^2}{3\pi} \text{Log} \left(\frac{\Lambda}{M_3} \right)$$

Light wino

Fine tuning (absence of new physics)
appears all models in some way: R-S, composite Higgs, little Higgs, SUSY etc

How do benchmark (minimal) models fair?



1207.1348

Arbey, Battaglia, Djouadi, Mahmoudi

stops less than 2 TeV

The point is that these models all work, but only if the spectrum is very heavy e.g. 5-10 TeV stops: *unnatural and unobservable at LHC/4*.

if you give up on naturalness, is there any reason to see anything at the LHC?

Reasons to (still) believe in SUSY

- Solves big hierarchy problem M_{EW}/M_{Pl}
- Improves GUT unification (and so too, stability of Proton)
- necessary for string theory (unification of all forces)
- radiatively induced EWSB in MSSM-like models.
- Believable dark matter candidate(s)
- It is consistent with low energy EW observables
- Improves fit to muon magnetic moment etc.
- MSSM bounds Higgs < 135 GeV

what are our choices?

The trivial option

Split SUSY, some landscape (multiverse) gives an explanation for Y_u , Λ_{cc} , m_h^2 (maybe more?)

The less likely option?

Generate a large A_t
(vanishing in mGMSB, uncalculable in SUGRA.)

The innovative option

non-minimal....get creative....

In this talk I am going to give 2 examples of models that improve naturalness

Non decoupled D-terms

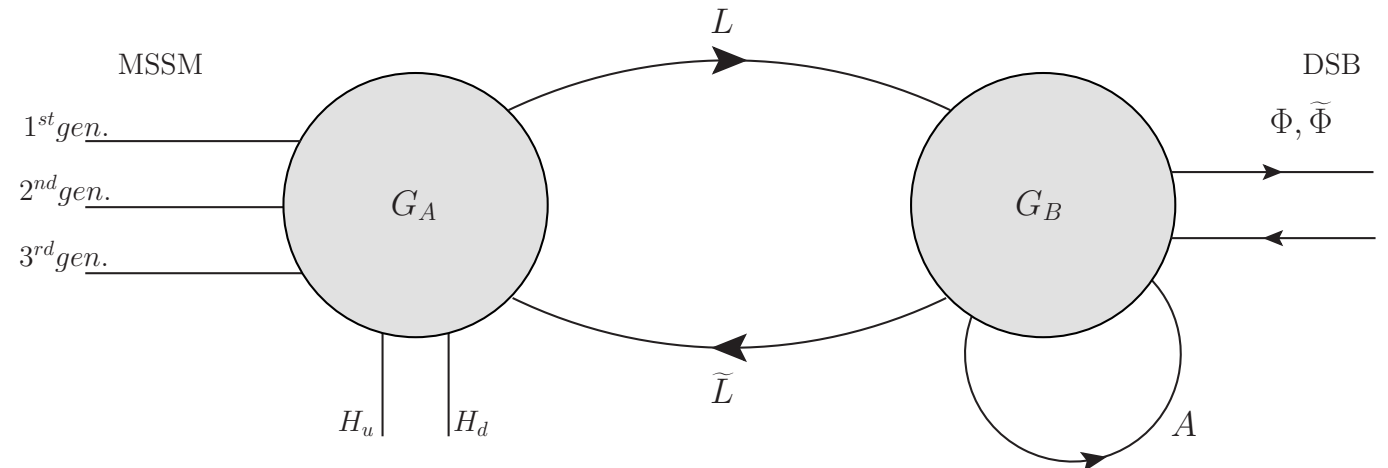
(Aoife Bharucha, Andreas Goudelis & MM) 1310.4500

Large At Without the Desert

(A.Abdalgabar,A.A.Deandrea,A.Cornell, MM) 1405.1038

A quiver model: motivation

- non decoupled D-terms: lifts the Higgs
(sometimes substantially)
Batra, Delgado, Kaplan, Tait 0309149
- extra adjoints of SU(2), SU(3): lifts the Higgs
- More natural than NMSSM?
- embeds into magnetic SQCD
- Deconstructs an extra dimension
- “Split families”: Batra, Kaplan, Tait, Delgado 0404251/0409073



$$m_h^2 \simeq m_z^2 \cos^2(2\beta) + \frac{3}{(4\pi)^2} \frac{m_t^4}{v_{ew}^2} \left[\log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left(1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right] \quad \Delta = \left(\frac{g_A^2}{g_B^2} \right) \frac{2m_L^2}{m_v^2 + 2m_L^2}$$

Related works:

Csaki, Erlich, Grojean, Kribs 0106044

Medina, Shah, Wagner 0904.1625

“GGM and Deconstruction”

M.M. 1009.0012 and 1101.5158

Auzzi, Givon, Gudnason, Shacham

1009.1714

1011.1664

+

...

$$\delta\mathcal{L} = -g_1^2 \Delta_1 (H_u^\dagger H_u - H_d^\dagger H_d)^2 - g_2^2 \Delta_2 \sum_a (H_u^\dagger \sigma^a H_u + H_d^\dagger \sigma^a H_d)^2$$

$$m_z^2 \rightarrow m_z^2 + \left(\frac{g_1^2 \Delta_1 + g_2^2 \Delta_2}{2} \right) v_{ew}^2$$

D-terms Vs NMSSM

$$m_h^2 \simeq m_z^2 \cos^2(2\beta) + \frac{3}{(4\pi)^2} \frac{m_t^4}{v_{ew}^2} \left[\log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left(1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right]$$

$$\Delta = \left(\frac{g_A^2}{g_B^2} \right) \frac{2m_L^2}{m_v^2 + 2m_L^2}$$

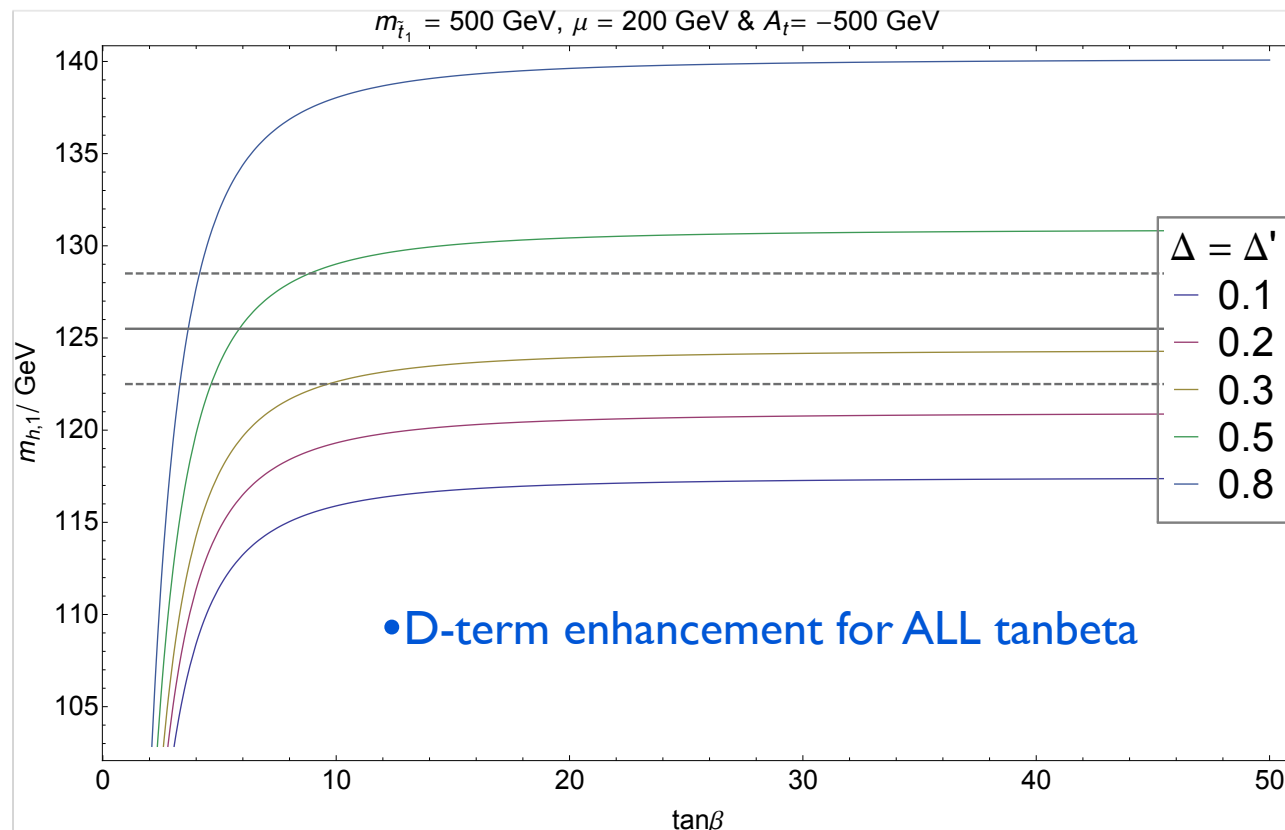
$$\delta\mathcal{L} = -g_1^2 \Delta_1 (H_u^\dagger H_u - H_d^\dagger H_d)^2 - g_2^2 \Delta_2 \sum_a (H_u^\dagger \sigma^a H_u + H_d^\dagger \sigma^a H_d)^2$$

$$m_z^2 \rightarrow m_z^2 + \left(\frac{g_1^2 \Delta_1 + g_2^2 \Delta_2}{2} \right) v_{ew}^2$$

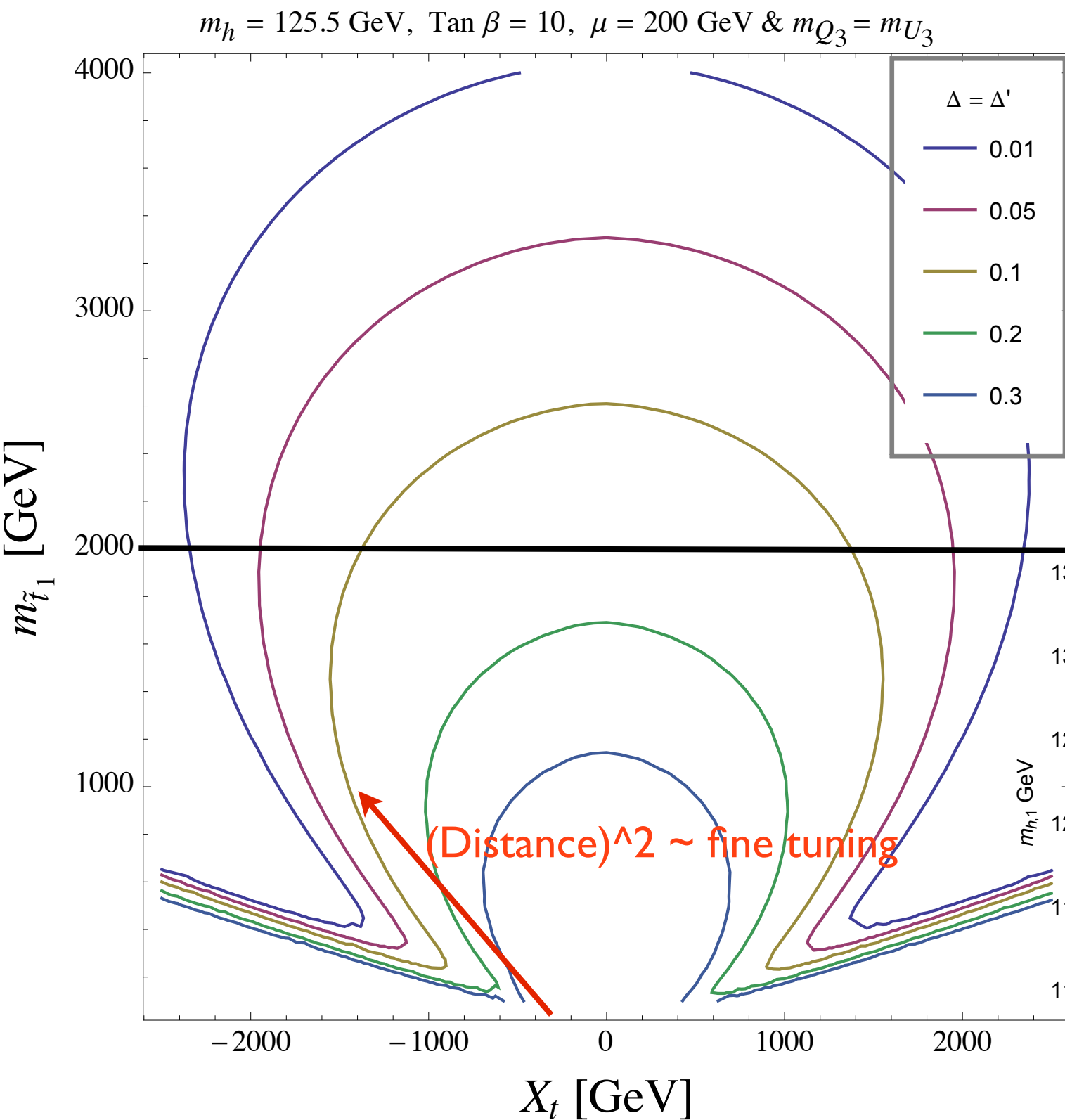
$$W_{NMSSM} \supset \lambda S H_u H_d$$

$$V(\phi's) \supset \lambda^2 |H_u H_d|^2$$

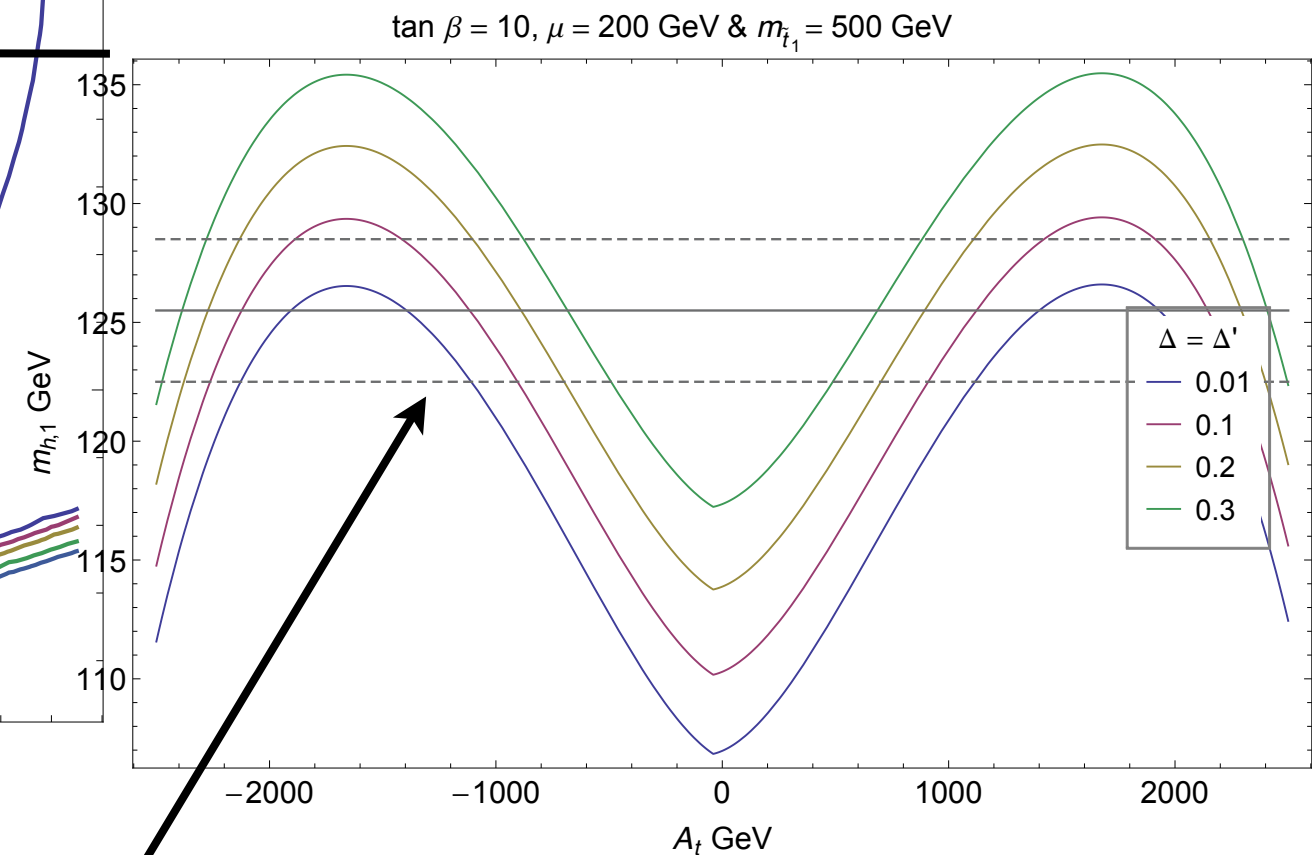
$$m_{h_0}^2 = m_z^2 \cos(2\beta) + \lambda^2 v_{ew}^2 \sin(2\beta)$$



• F-term enhancement only for small tanbeta



Sub 2 TeV stops
for $\Delta \geq 0.1$

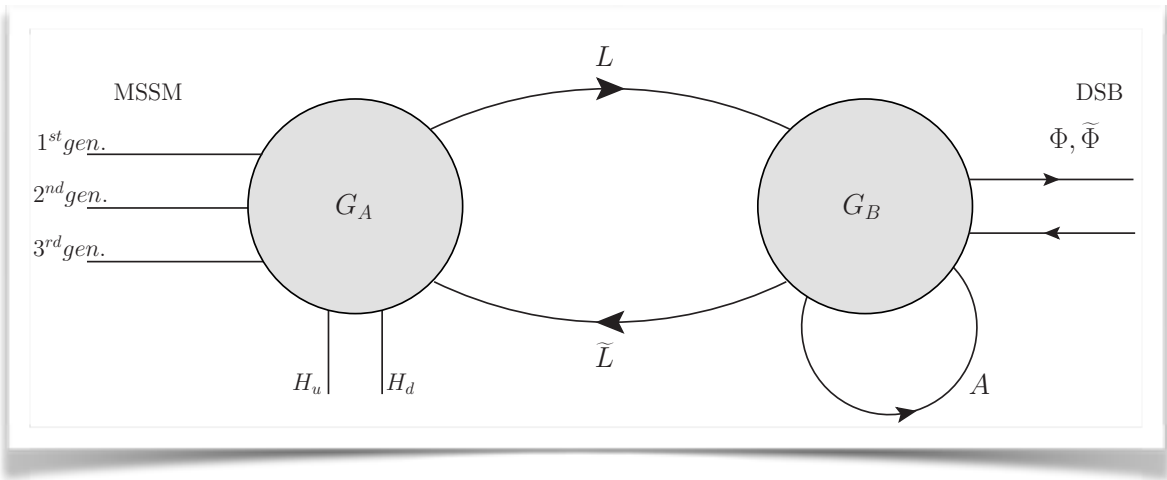


Combination of medium size A_t and Deltas can do the trick! (GMSB back in the game?)

So far most studies of D-terms have been at tree-level and bottom-up

SF	Spin 0	Spin $\frac{1}{2}$	Generations	$(U(1)_A, SU(2)_B, SU(3)_c, U(1)_B, SU(2)_A)$	R-Parity
$\hat{q}$	$\tilde{q}$	q	3	$(\frac{1}{6}, 1, 3, 0, 2)$	-1
$\hat{l}$	$\tilde{l}$	l	3	$(-\frac{1}{2}, 1, 1, 0, 2)$	-1
$\hat{H}_d$	H_d	$\tilde{H}_d$	1	$(-\frac{1}{2}, 1, 1, 0, 2)$	+1
$\hat{H}_u$	H_u	$\tilde{H}_u$	1	$(\frac{1}{2}, 1, 1, 0, 2)$	+1
$\hat{d}$	$\tilde{d}_R^*$	d_R^*	3	$(\frac{1}{3}, 1, \bar{3}, 0, 1)$	-1
$\hat{u}$	$\tilde{u}_R^*$	u_R^*	3	$(-\frac{2}{3}, 1, \bar{3}, 0, 1)$	-1
$\hat{e}$	$\tilde{e}_R^*$	e_R^*	3	$(1, 1, 1, 0, 1)$	-1
$\hat{\tilde{L}}$	L	ψ_L	1	$(-\frac{1}{2}, \bar{2}, 1, \frac{1}{2}, 2)$	+1
$\hat{\tilde{\tilde{L}}}$	$\tilde{L}$	$\psi_{\tilde{L}}$	1	$(\frac{1}{2}, 2, 1, -\frac{1}{2}, \bar{2})$	+1
$\hat{K}$	K	ψ_K	1	$(0, 1, 1, 0, 1)$	+1
$\hat{A}$	A	ψ_A	1	$(0, 3, 1, 0, 1)$	+1

Table 2. Matter fields of the model.



$$W_{\text{SSM}} = Y_u \hat{u} \hat{q} \hat{H}_u - Y_d \hat{d} \hat{q} \hat{H}_d - Y_e \hat{e} \hat{l} \hat{H}_d + \mu \hat{H}_u \hat{H}_d$$

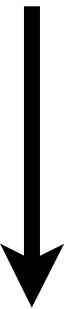
$$W_{\text{Quiver}} = \frac{Y_K}{2} \hat{K} (\hat{L} \hat{\tilde{L}} - V^2) + Y_A \hat{L} \hat{A} \hat{\tilde{L}}$$

The most sophisticated model so far implemented into a spectrum generator (SARAH/SPHENO)
A meta-model i.e. independent of the type of supersymmetry breaking:
AMSB, mSUGRA, GMSB, phenomenological, other?

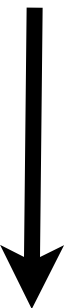
Building a taylor made spectrum generator!

- We used SARAH (written by Florian Staub) mathematica package: “a spectrum generator generator” to write our own spectrum generator.
- We implemented 5 gauge groups with full 2-loop RGE’s and one loop self energies (soon 6 and 9 gauge groups!).
- Higgsing, and breaking to the diagonal 4 gauge groups, including all mixing matrices and assignment of Goldstones, Ghosts, RGEs of vevs, and Bmu at 2 loop.
- All 3 and 4 vertices of all fields computed, and self energies.
- All anomalous dimensions, tadpoles and running of all *additional soft terms and additional Yukawas, at 2 loop level.*
- finite shifts and threshold corrections also accounted for
- Can talk to FeynArts, FormCalc, CalcHep, HiggsSignals, HiggsBounds, WHIZARD, micrOMEGAS, Vevacious and more.

Quiver @
M messenger



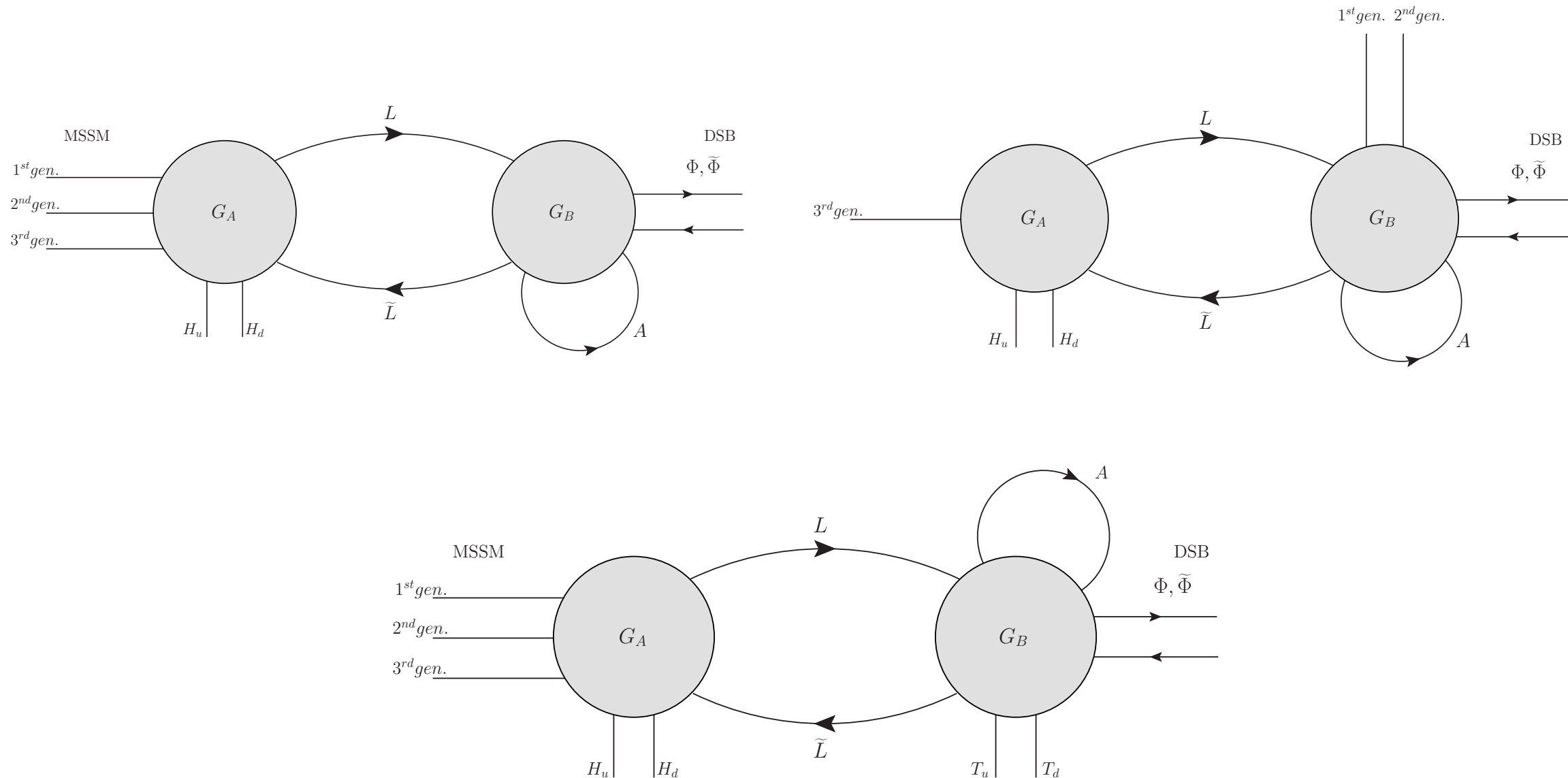
Threshold
scale:
MSSM



LHC

Same precision as SOFTSUSY, SPheno, SUSPECT

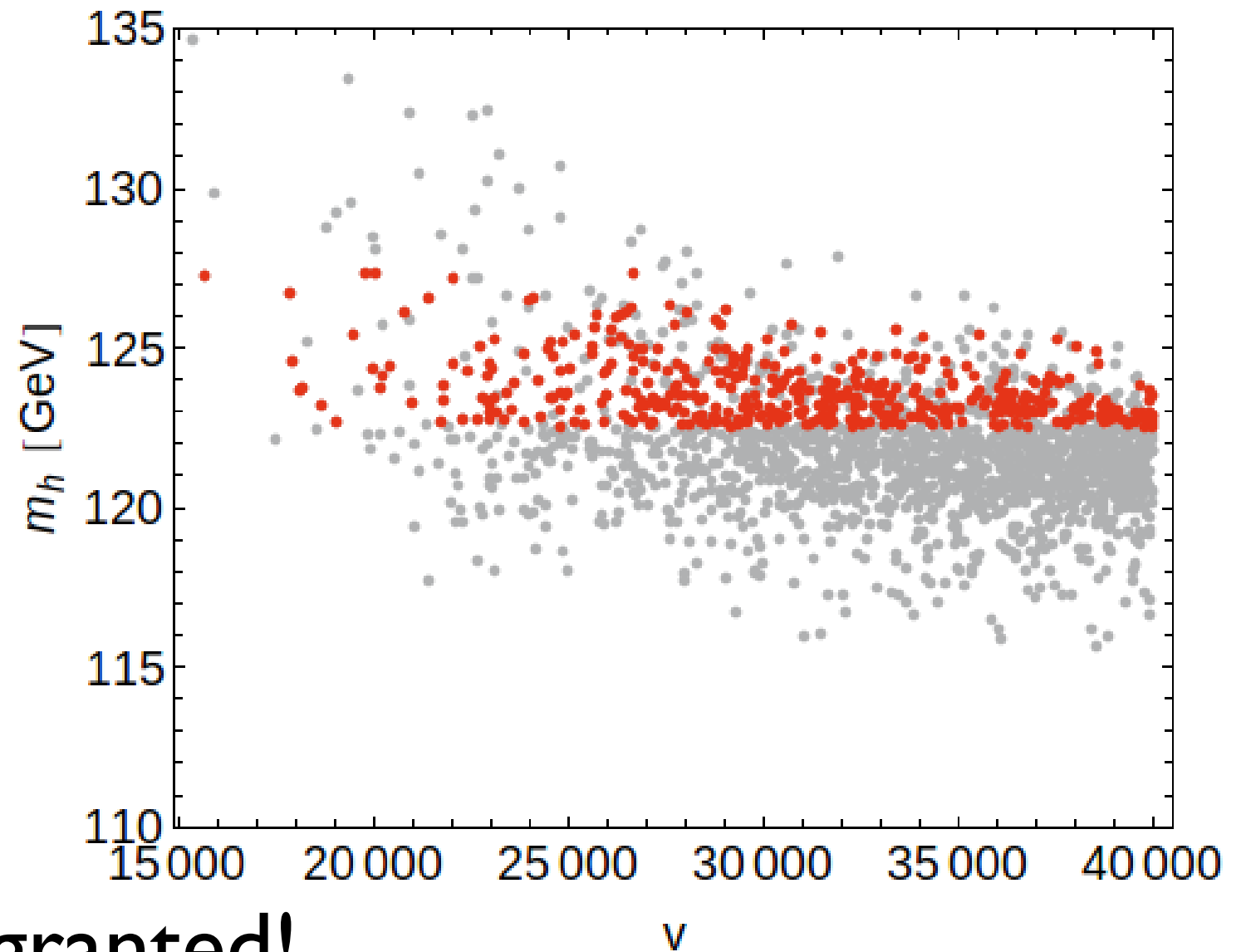
The Quiver Variations



Wish list

- $v < 10\text{TeV}$
 $m_L^2 > m_v^2$

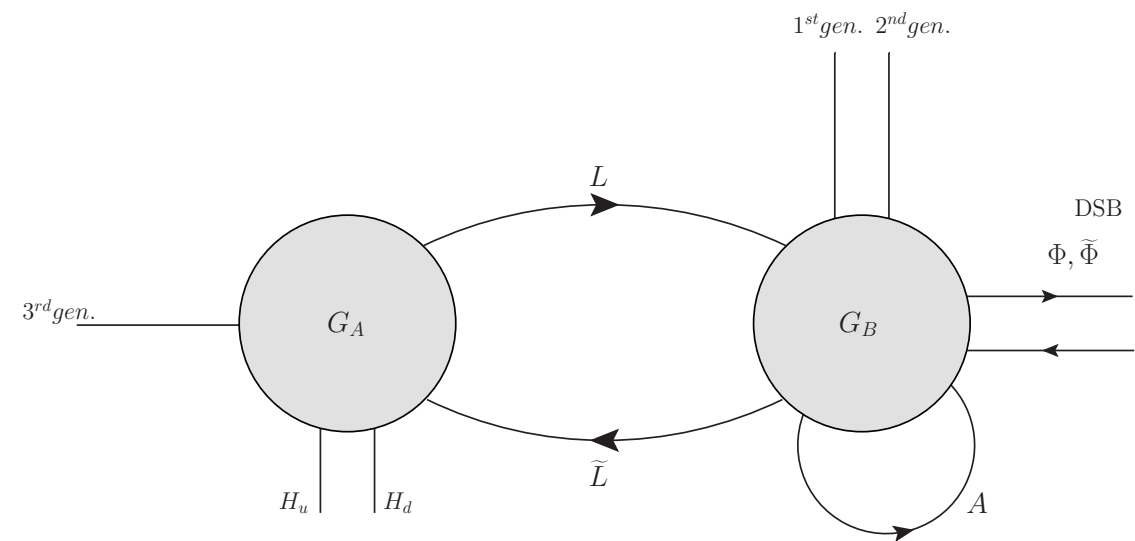
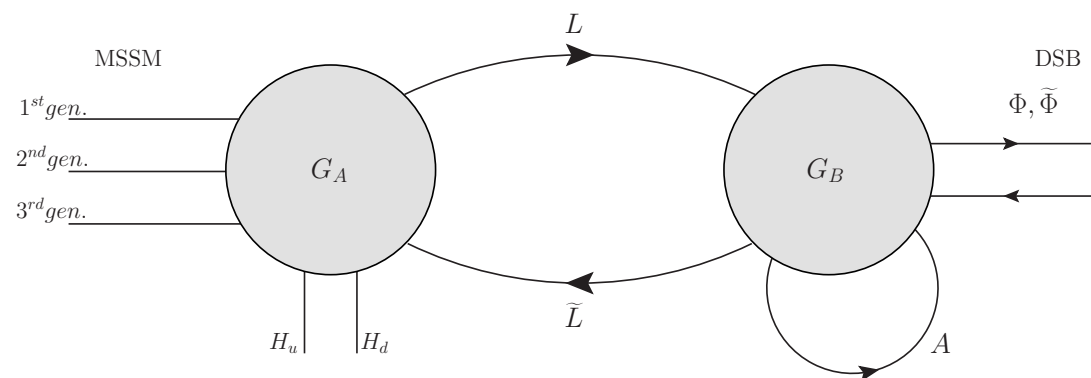
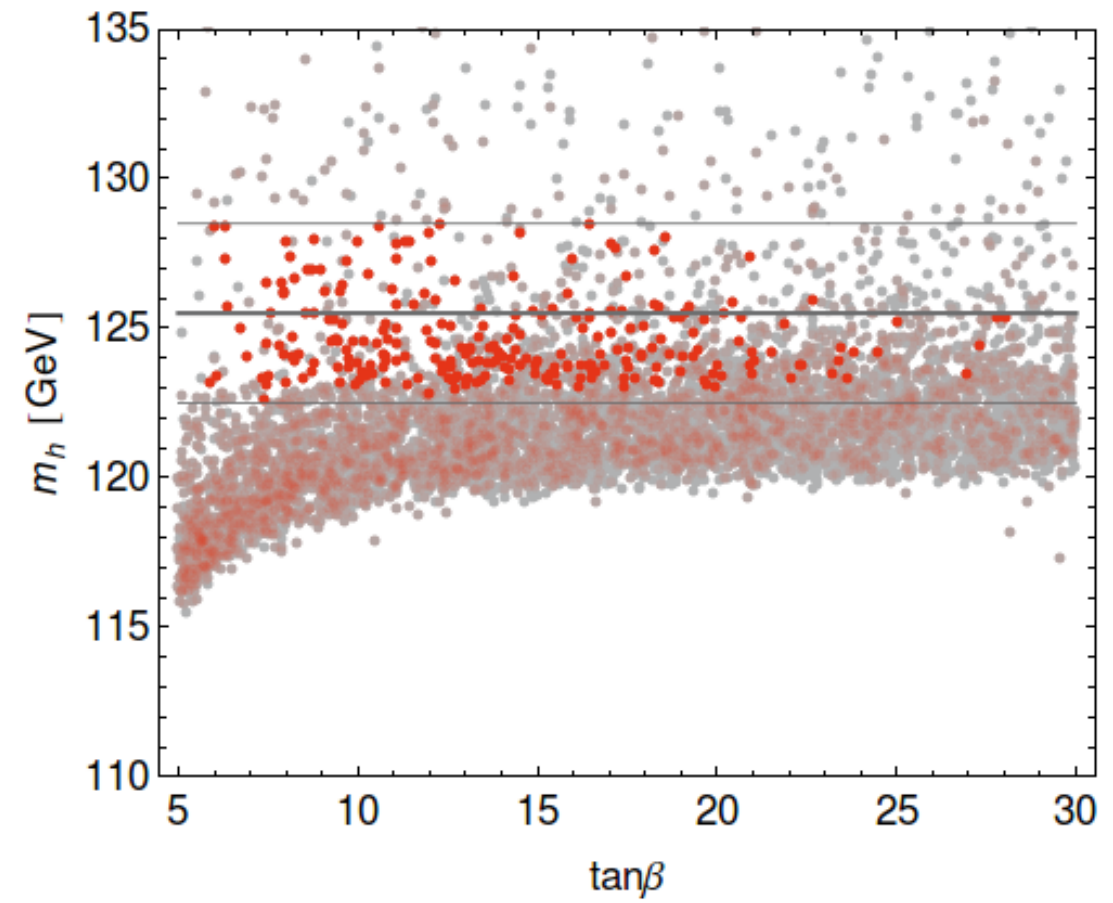
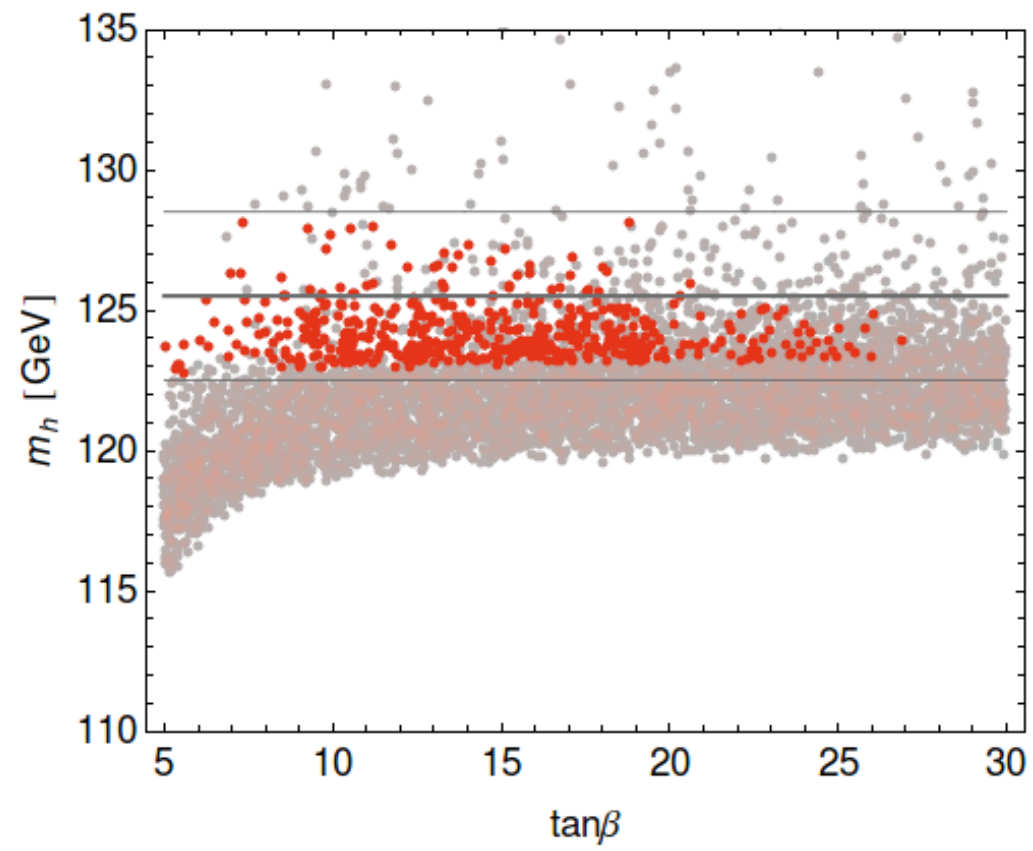
We assumed GMSB
for soft terms!

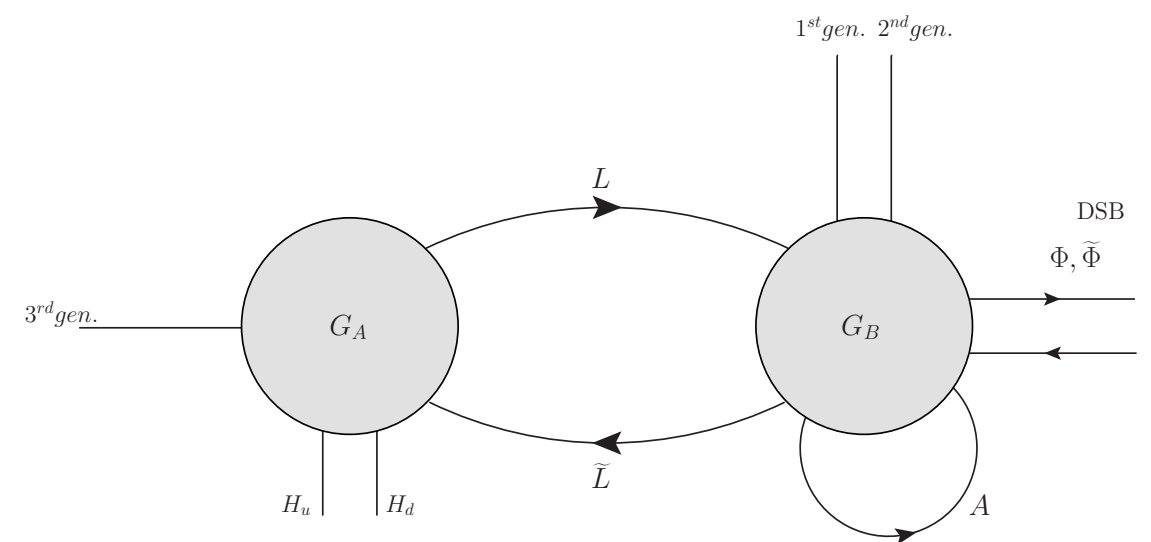
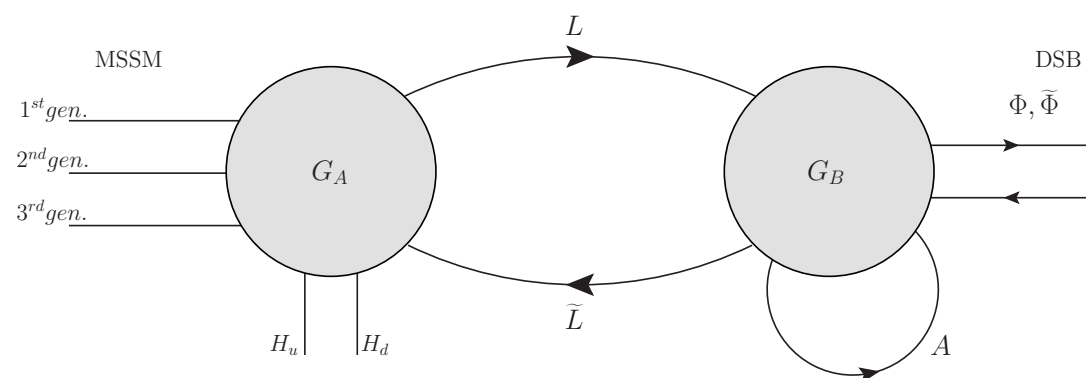
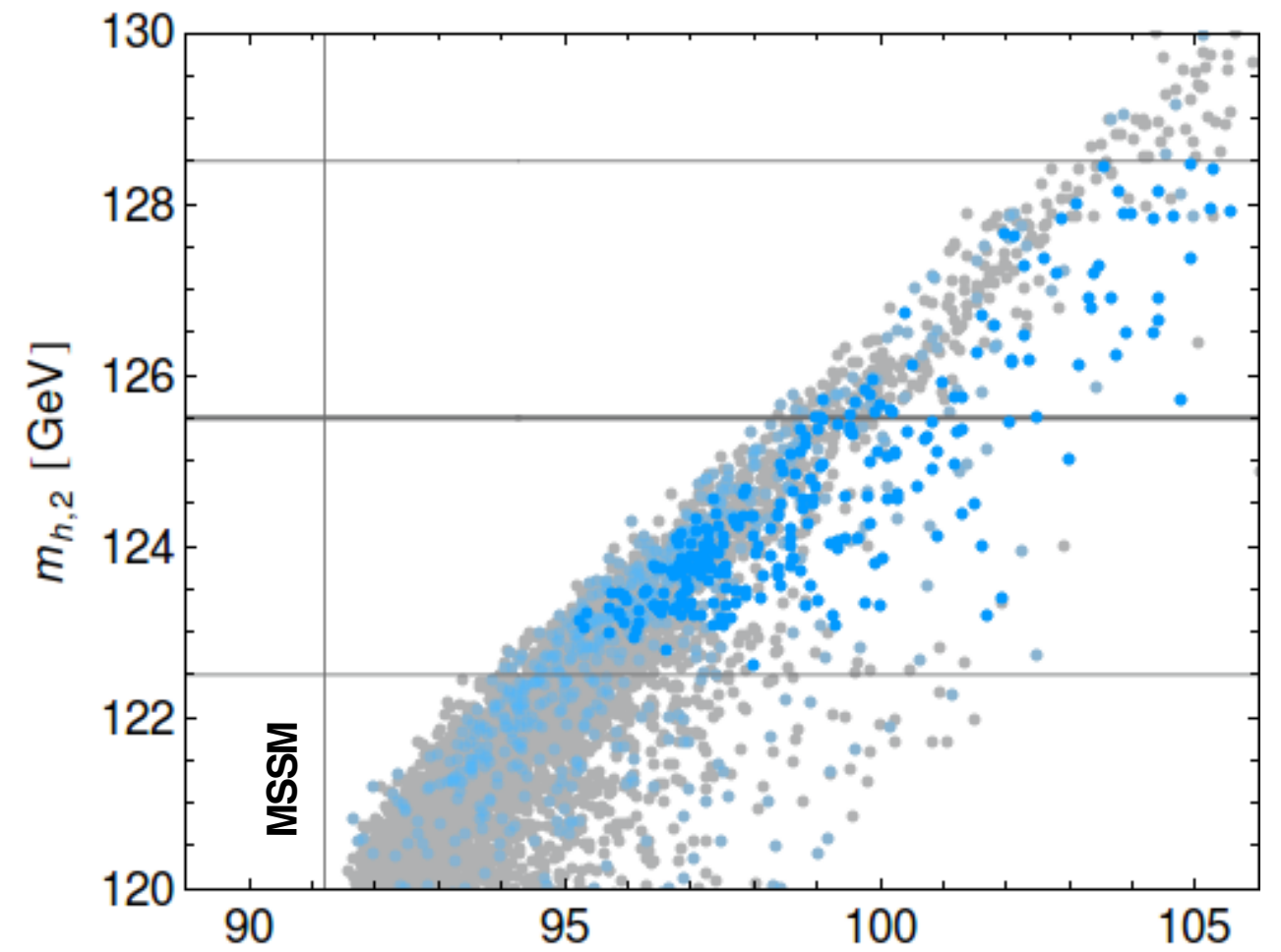
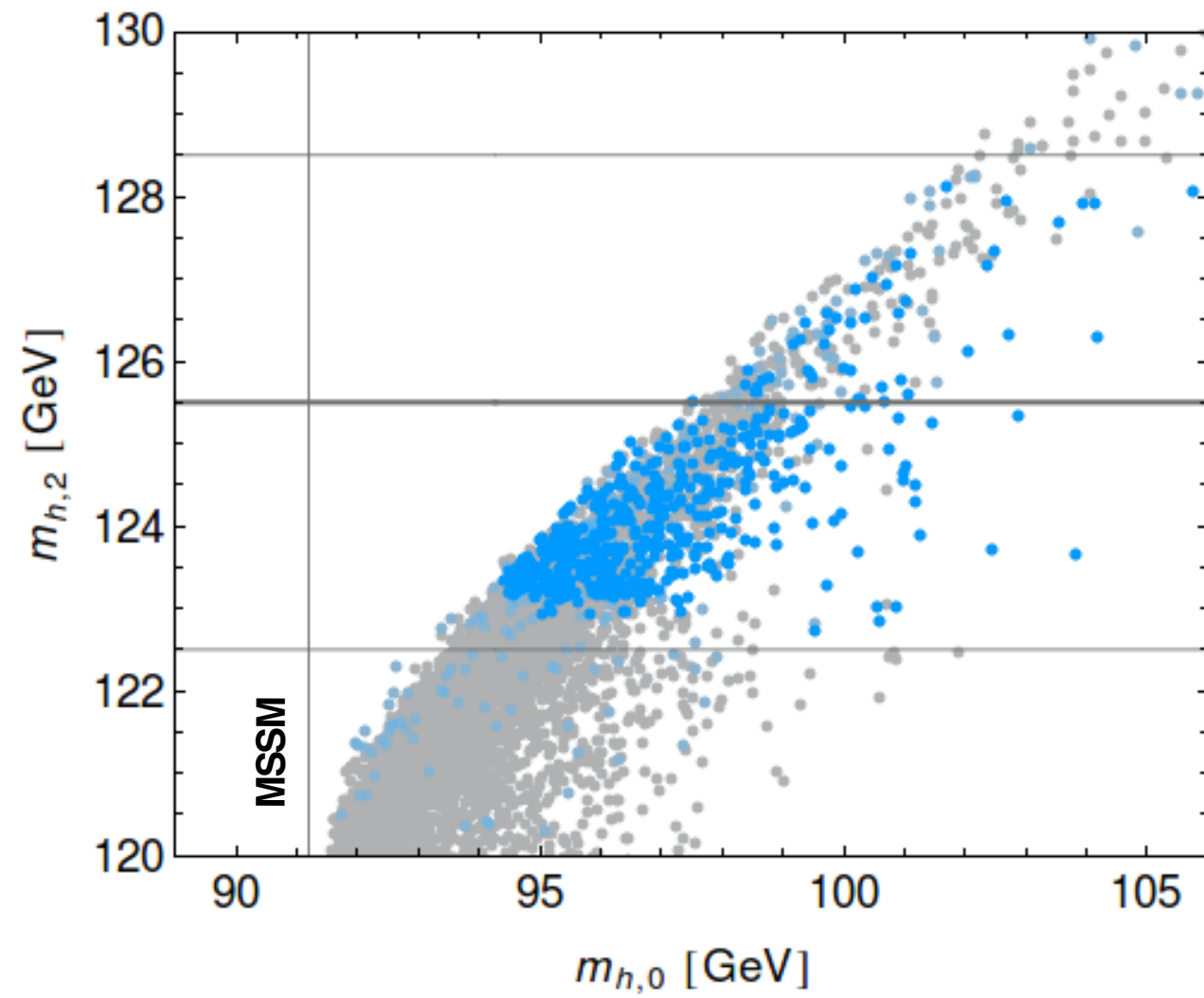


Our wishes were not granted!
we had to enlarge m_L^2 to
make it work

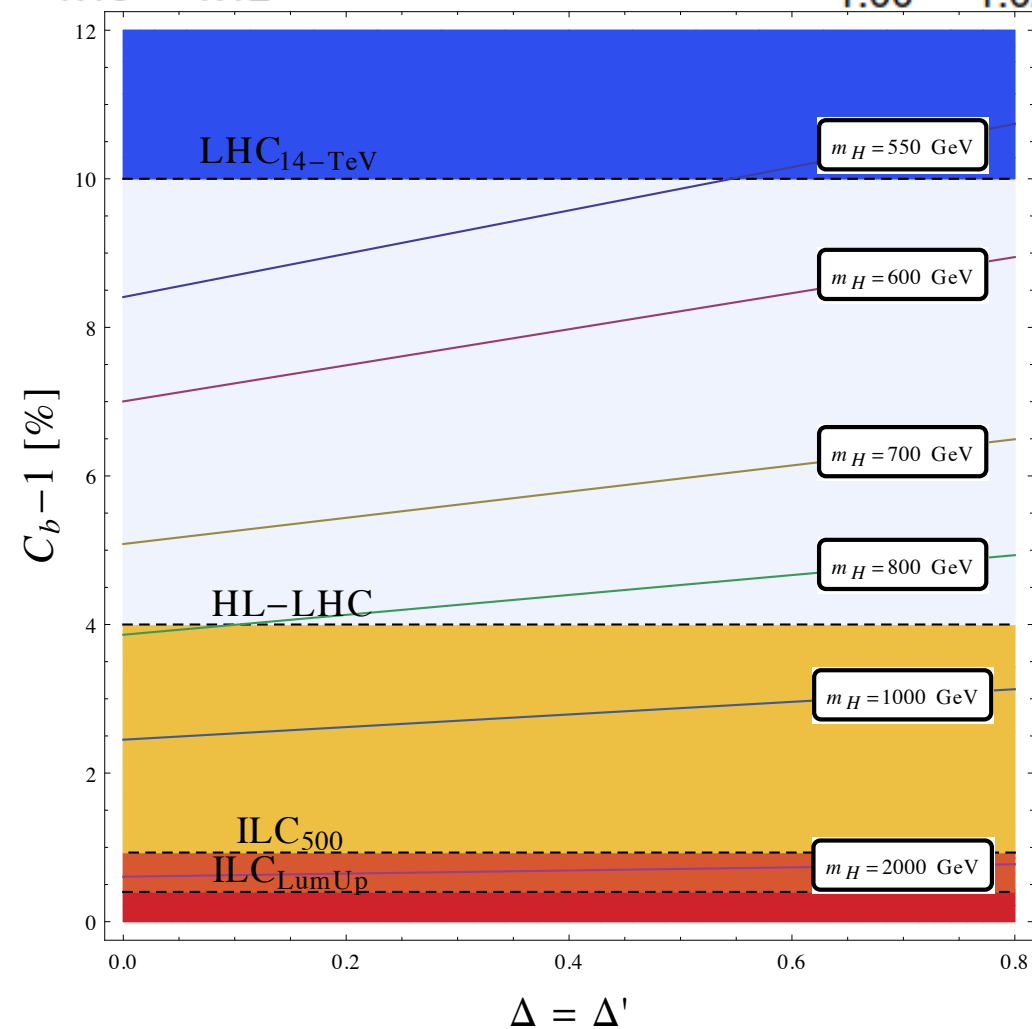
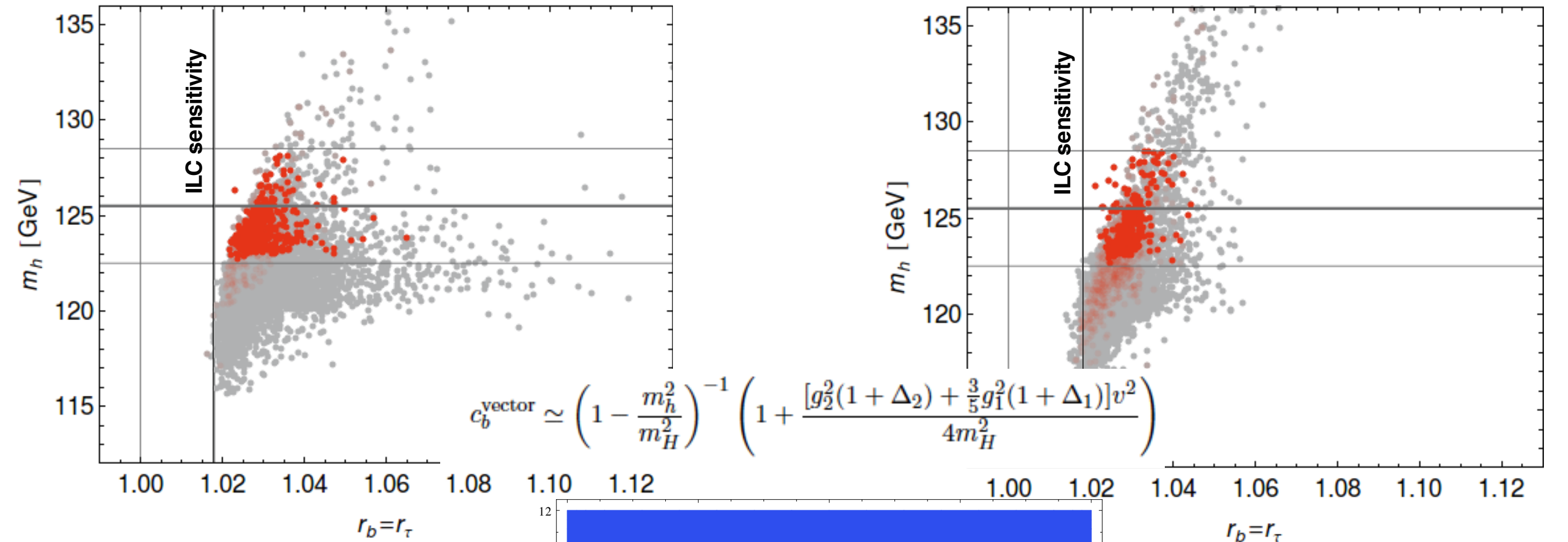
But perhaps this can be improved by
considering
different SUSY breaking scenarios

Ex. Applying mSUGRA here may get v down



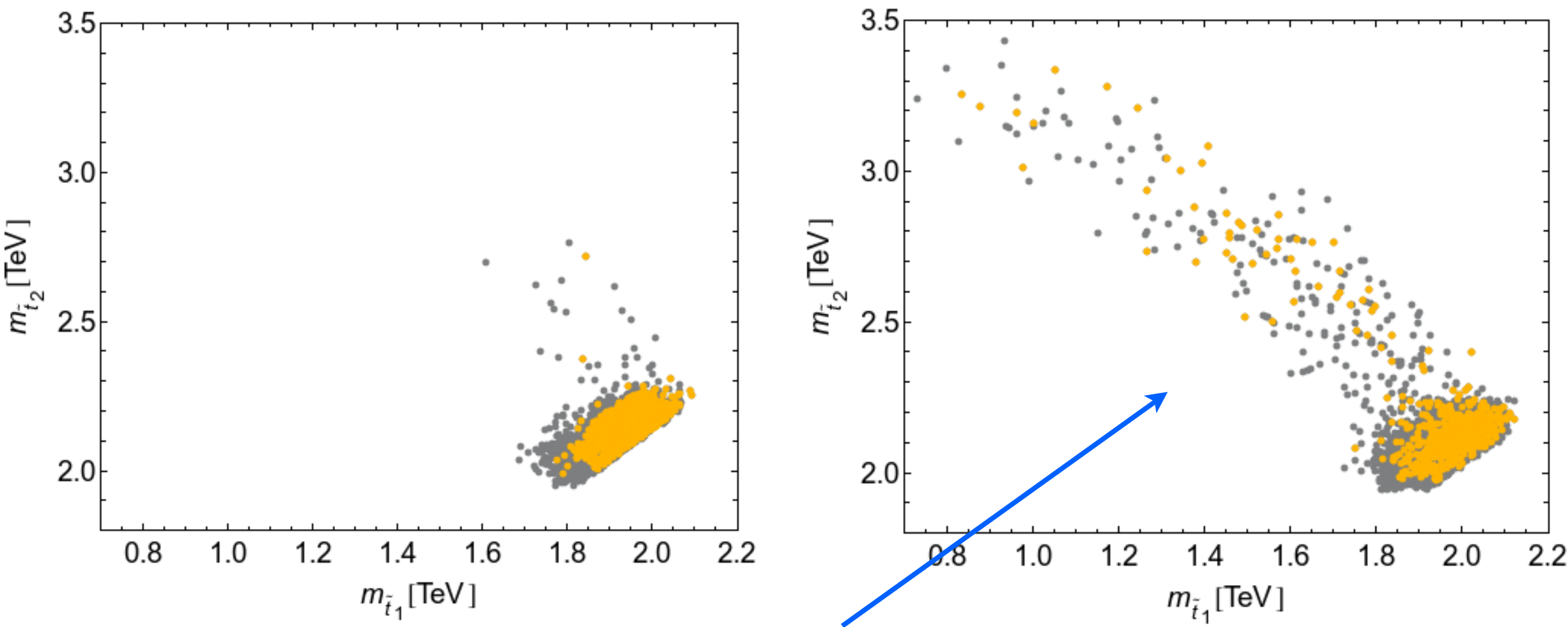


Testable at ILC!

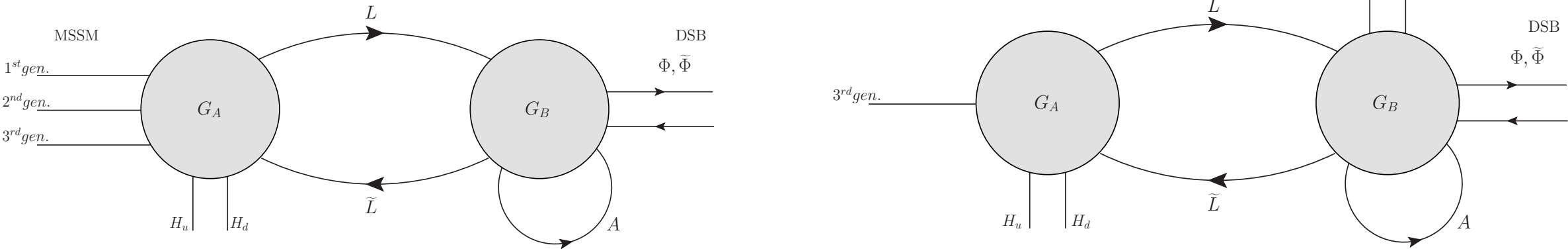


Testing D-terms
@ILC
with S.Porto, G. Moortgat-Pick (DESY)

$$m_h^2 \simeq m_z^2 \cos^2(2\beta) + \frac{3}{(4\pi)^2} \frac{m_t^4}{v_{ew}^2} \left[\log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left(1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right] + \Delta m_{h,1}^2 = \frac{3m_Z^2}{16\pi^2 v_{ew}^2} \left(1 - \frac{8}{3} \sin^2 \theta_W \right) \cos 2\beta m_t^2 \ln \left(\frac{m_{\tilde{q}_L^3}^2}{m_{\tilde{u}_R^3}^2} \right)$$



Stop splitting enhances Higgs mass
@ 1-loop



	MI	MIIa	MI Ib
Input values			
M	233 TeV	288 TeV	260 TeV
$\Lambda_{1,2}$	44.9 TeV	85.6 TeV	111 TeV
Λ_3	190 TeV	206 TeV	208 TeV
m_L^2	47.3 TeV ²	83.3 TeV ²	86.2 TeV ²
v	26.2 TeV	26.5 TeV	25.4 TeV
θ_1, θ_2	1.18, 1.13	1.09, 1.33	1.05, 1.04
$\tan \beta$	16	12	28
Squark sector			
$m_{\tilde{t}_1}$	1.84 TeV	1.99 TeV	409 GeV
$m_{\tilde{t}_2}$	1.98 TeV	2.06 TeV	3.49 TeV
A_t	-442 GeV	-146 GeV	-141 GeV
$m_{\tilde{b}_R}$	1.95 TeV	2.05 TeV	2.56 TeV
$m_{\tilde{q}_{12,L}}$	2.05 TeV	2.12 TeV	2.19 TeV
$m_{\tilde{q}_{12,R}}$	1.97 TeV	2.10 TeV	2.14 TeV
Slepton sector			
$m_{\tilde{l}_{12,L}}$	738 GeV	314 GeV	515 GeV
$m_{\tilde{l}_{3,L}}$	736 GeV	315 GeV	440 GeV
$m_{\tilde{l}_{12,R}}$	901 GeV	183 GeV	262 GeV
$m_{\tilde{l}_{3,R}}$	899 GeV	110 GeV	4.31 TeV
Gaugino sector			
$m_{\tilde{\chi}_1^0}$	53.2 GeV	116 GeV	154 GeV
$m_{\tilde{\chi}_2^0}$	99.3 GeV	242 GeV	306 GeV
$m_{\tilde{\chi}_3^0}$	187 GeV	750 GeV	818 GeV
$m_{\tilde{\chi}_4^0}$	222 GeV	755 GeV	823 GeV
$m_{\tilde{\chi}_1^\pm}$	96.8 GeV	242 GeV	306 GeV
$m_{\tilde{\chi}_2^\pm}$	225 GeV	756 GeV	823 GeV
$m_{\tilde{g}}$	1.62 TeV	1.66 TeV	1.75 TeV
Higgs sector			
m_{h_0}	125 GeV	127 GeV	125 GeV
m_{H_0}	720 GeV	792 GeV	885 GeV
m_{A_0}	721 GeV	796 GeV	894 GeV
$m_{H_{\pm}}$	726 GeV	799 GeV	893 GeV

Extensions:

- 6 gauge groups
- resolve issue of MHu² and V
- Other SUSY breaking parameterisations?
- Single regime spectrum generator
- Add the states to PDG etc....

A renormalisable way to model an extra dimension

Ex. KK gluons, gluinos, Z',
KK W's

Can talk to FeynArts, Formcalc, CalcHep,
HiggsSignals, HiggsBounds,
WHIZARD, microOMEGA, Vevacious and more

“Large A_t Without the Desert”

A.Abdalgabar, A.Cornell, A.Deandrea, MM 1405:1038

$$\mathbf{a}_u \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a_t \end{pmatrix}, \quad \mathbf{a}_d \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a_b \end{pmatrix}, \quad \mathbf{a}_e \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a_\tau \end{pmatrix},$$

UV

In many models $A_t = 0$ in UV



A_t runs negative

IR

typically ends up negative a few 100 GeV

Not sufficient to get correct Higgs mass....

Question: Can we accelerate its running?

1. The Higgs mass 126 GeV

The MSSM at one-loop

$$m_h^2 \simeq m_z^2 \cos^2(2\beta) + \frac{3}{(4\pi)^2} \frac{m_t^4}{v_{ew}^2} \left[\log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left(1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right]$$

top mass

average stop mass

$$126^2 = 91^2 + 81^2$$

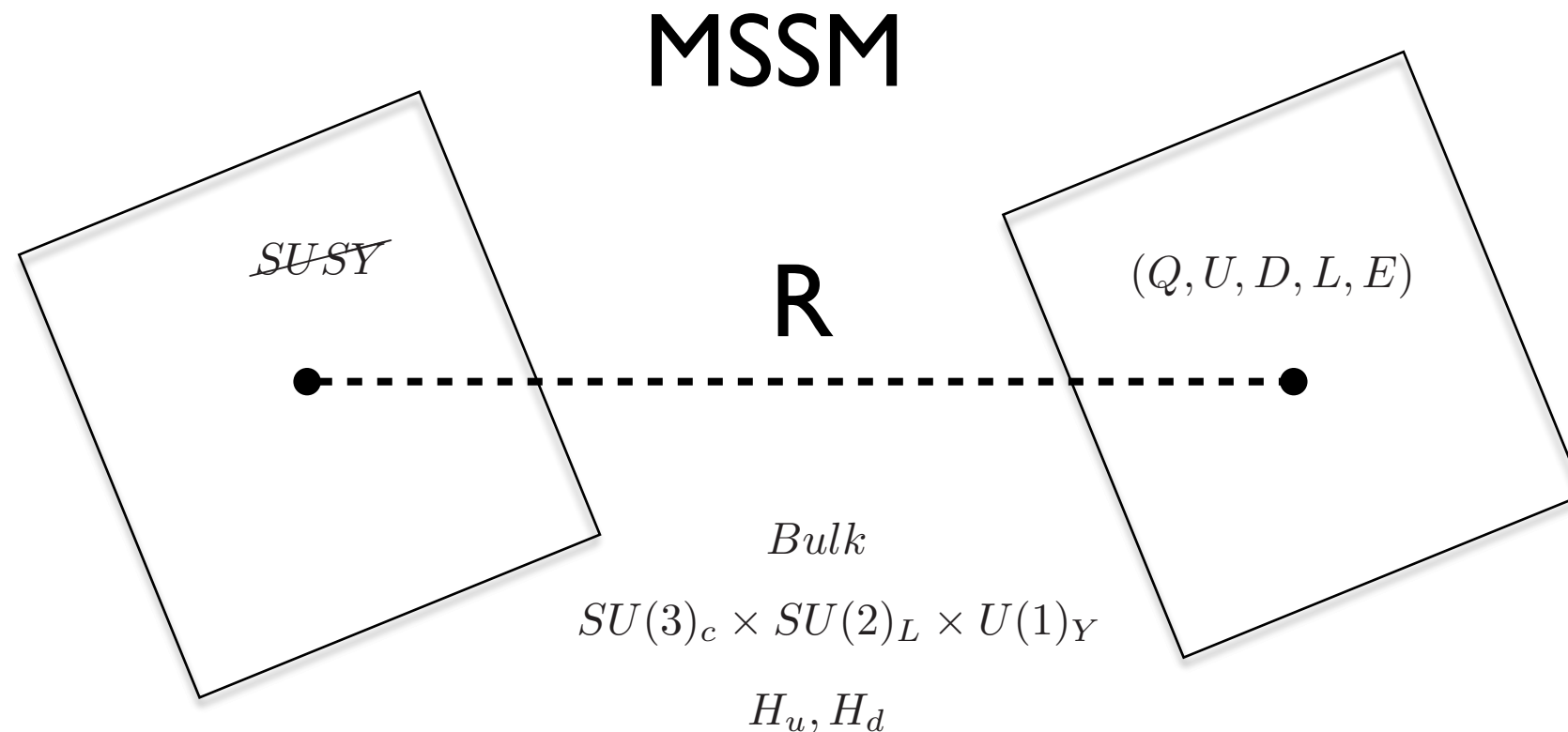
$$X_t = A_t - \mu \cot \beta$$

stop mixing

- Radiative corrections are same order as tree level piece
- corrections run logarithmically in SUSY
- MSSM case implies either heavy stops or large $X_t = A_t + \dots$

In 5D you can get large A_t !

“Power law running”



An extra dimension of radius R .
Additional Kaluza Klein modes enter RGEs @ $Q > 1/R$

Large A_t : Independent of the details of SUSY breaking

Split families: Locate different generations in brane or bulk

$$m_{(Q,U,D)3}^2 \ll m_{(Q,U,D)1,2}^2$$

Power law running

$$\alpha^{-1}(Q) = \alpha^{-1}(m_z) - \frac{b}{2\pi} \log \frac{Q}{m_z} + \frac{\tilde{b}}{2\pi} \log \frac{Q}{m_{KK}} - \frac{\tilde{b}}{2\pi} \left(\frac{Q^d}{m_{KK}} - 1 \right) c_d$$

(K.Dienes, E.Dudas, T. Gherghetta) 9803466

(K.Dienes, E.Dudas, T. Gherghetta) 9806292

“The finite power-law corrections to the Yukawa couplings have the right sign and magnitude to cancel the tree-level terms. This can help to explain the hierarchical structure of the fermion Yukawa couplings.”

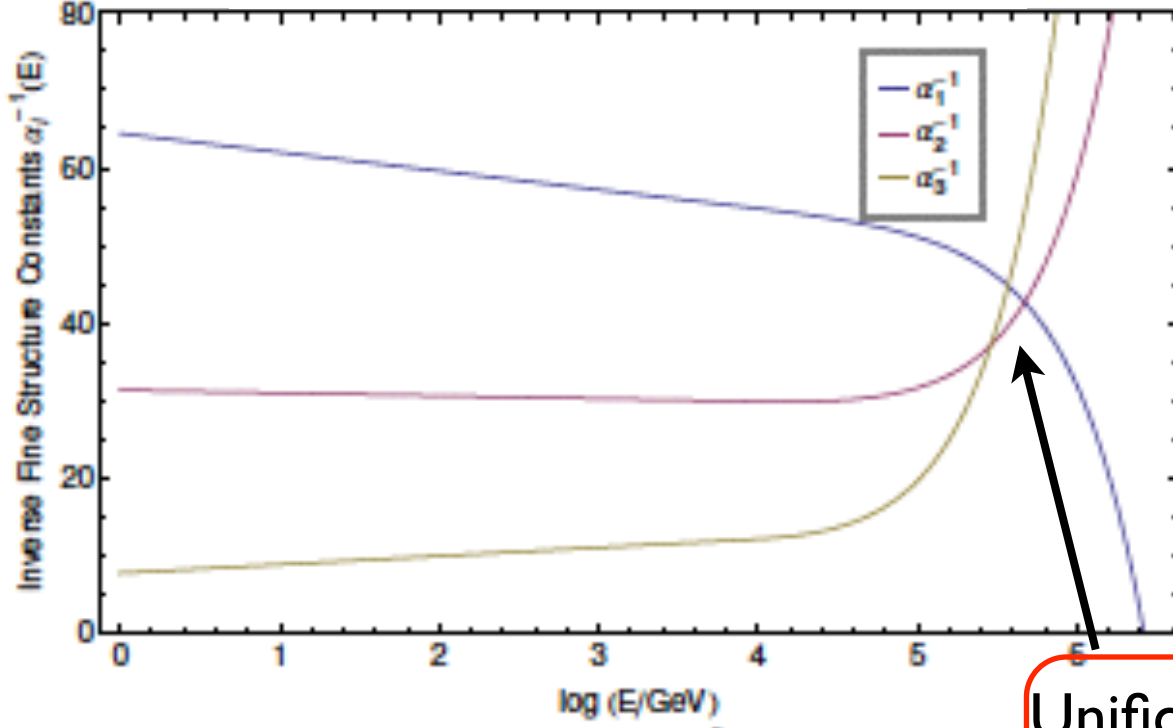
(A.Abdalagbar, A.Cornell, A.Deandrea, MM) 1405:1038

“Perhaps we can use this to accelerate the value of A_t ?”

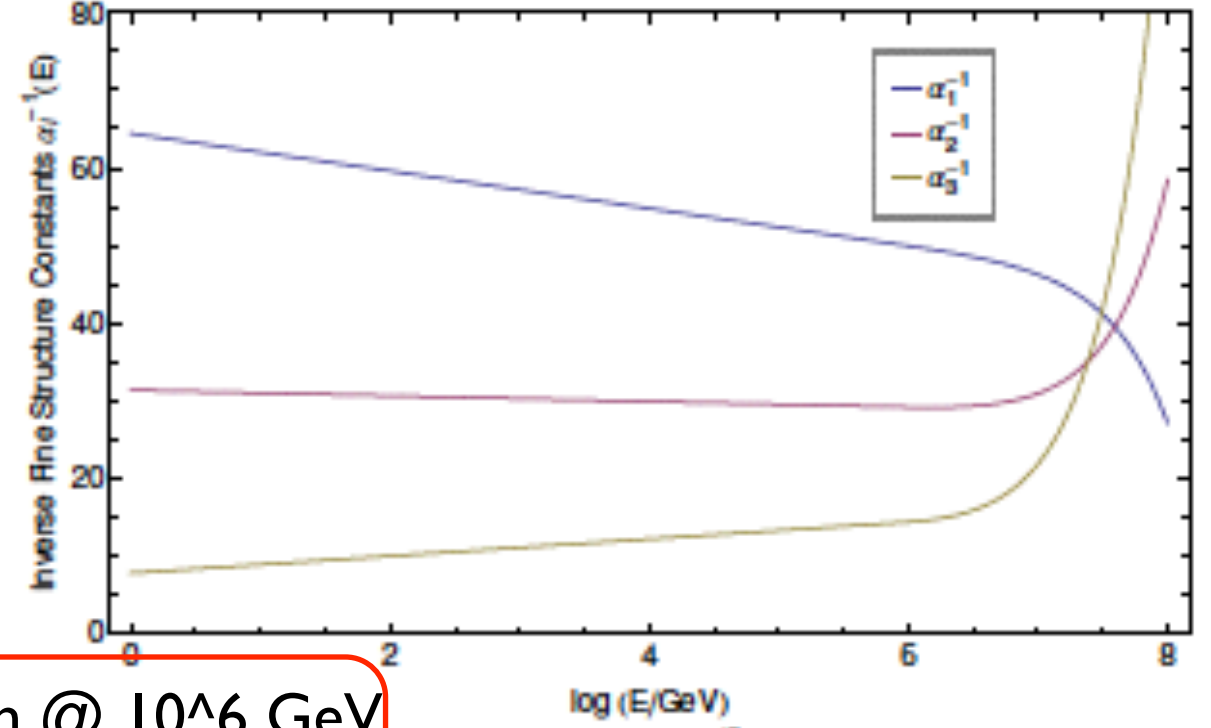
4+d dimensional MSSM

- ✓ Always unify
- ✓ No proton decay
- ✓ Explains flavour
- ✓ Large A_t

Compactification scale 10 TeV

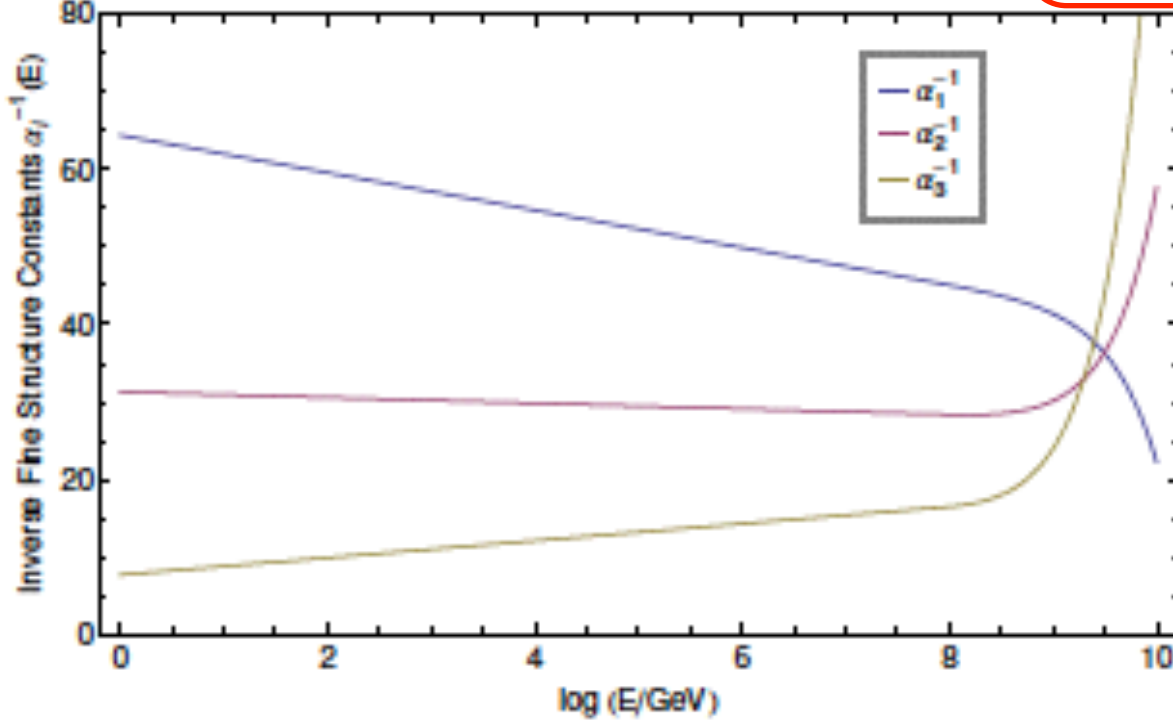


Compactification scale 10^3 TeV



Unification @ 10^6 GeV

Compactification scale 10^5 TeV



Compactification scale 10^{12} TeV

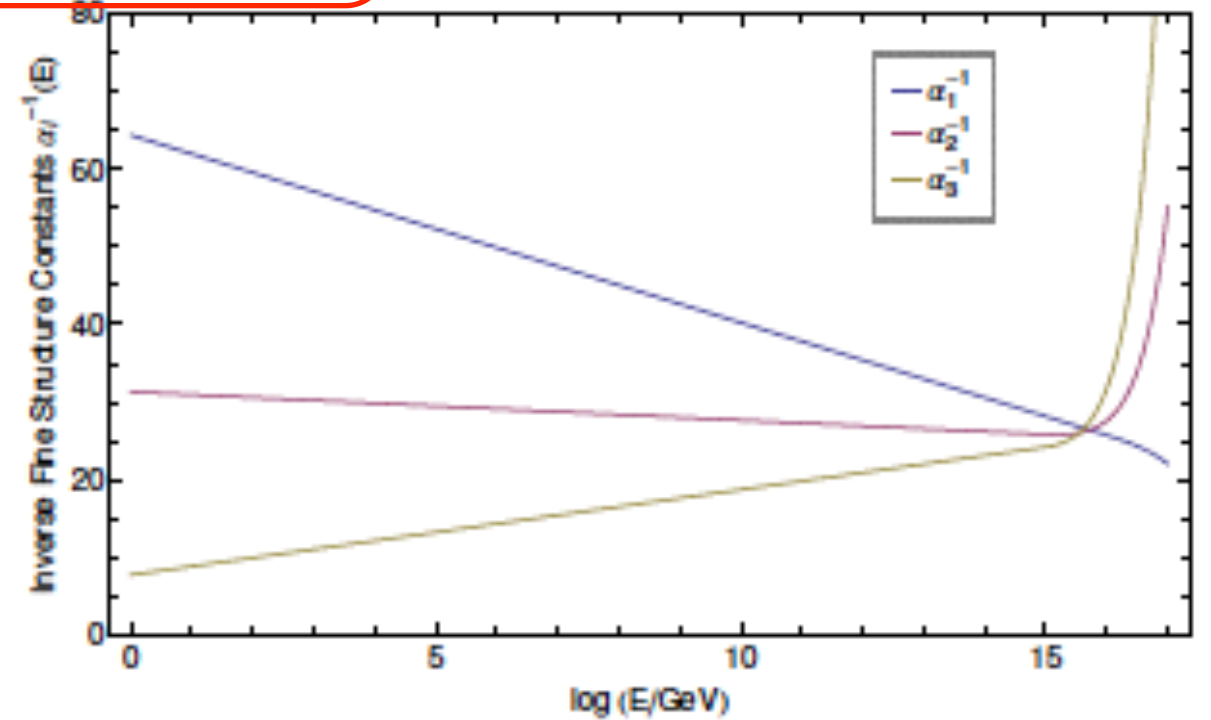
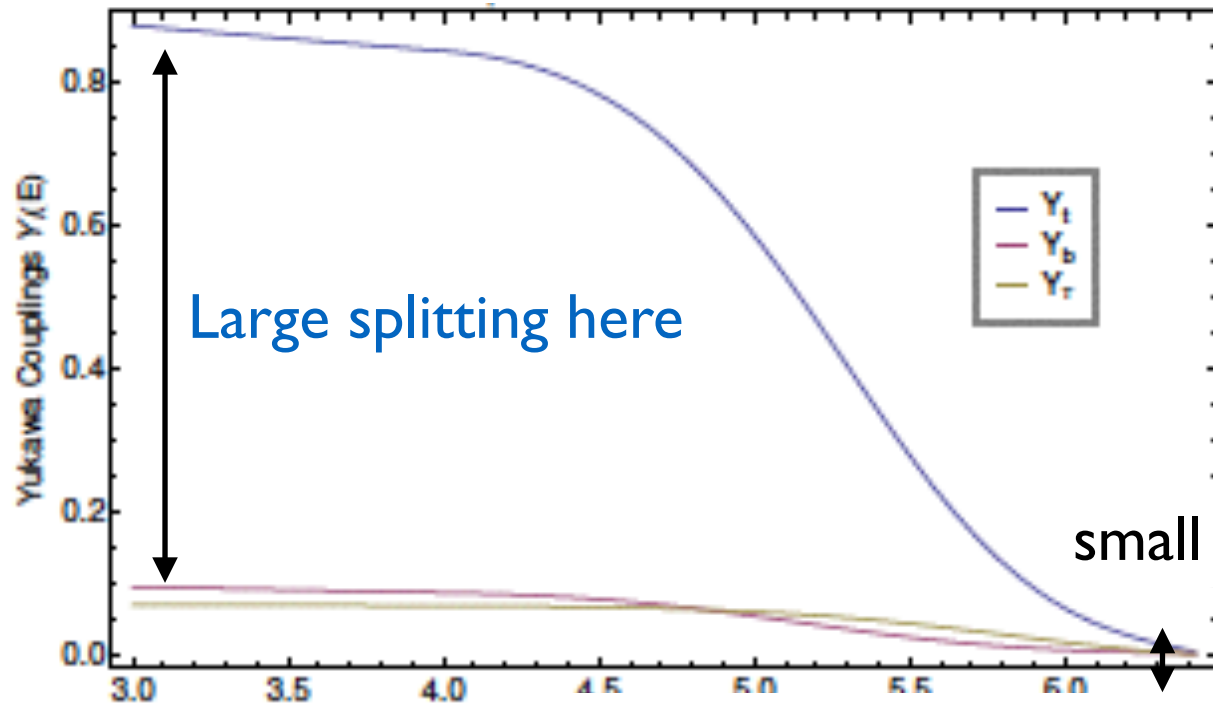
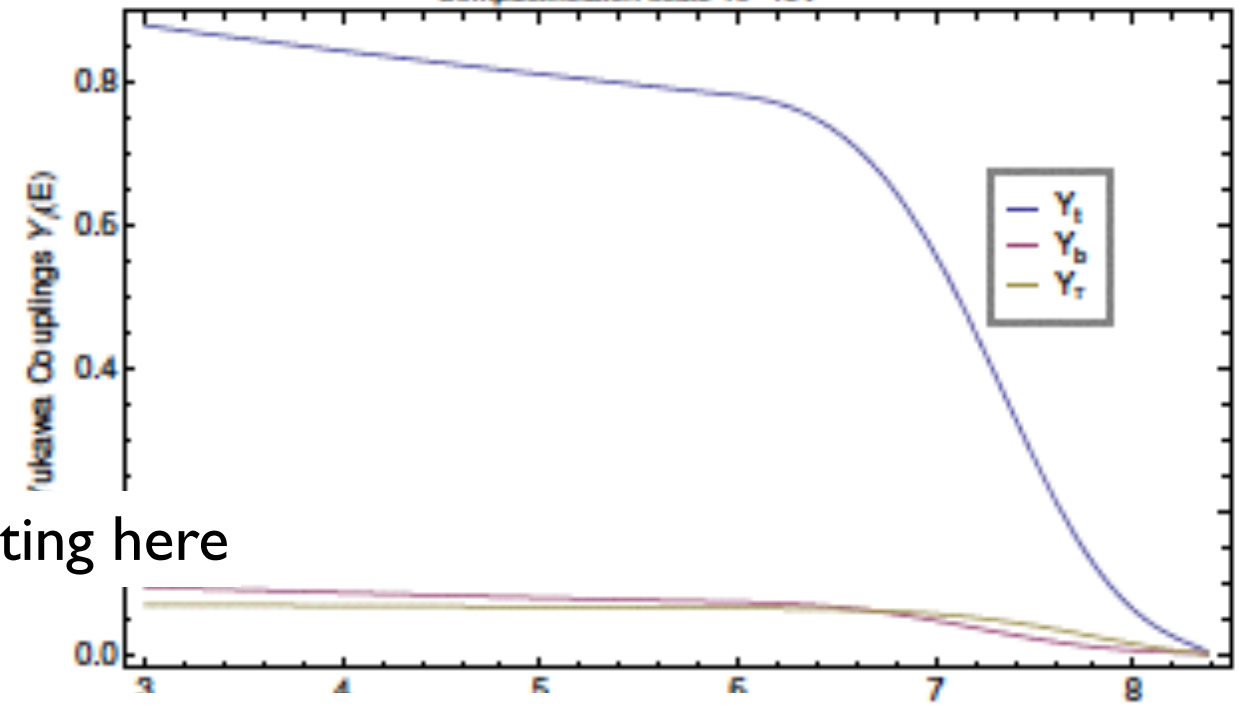


Figure 1. Running of the inverse fine structure constants $\alpha^{-1}(E)$, for three different values of the compactification scales 10 TeV (top left panel), 10^3 TeV (top right), 10^5 TeV (bottom left) and 10^{12} TeV (bottom right), with M_3 of 1.7 TeV, as a function of $\log(E/\text{GeV})$.

Compactification scale 10 TeV



Compactification scale 10^3 TeV



Flavour hierarchy just an RGE effect?

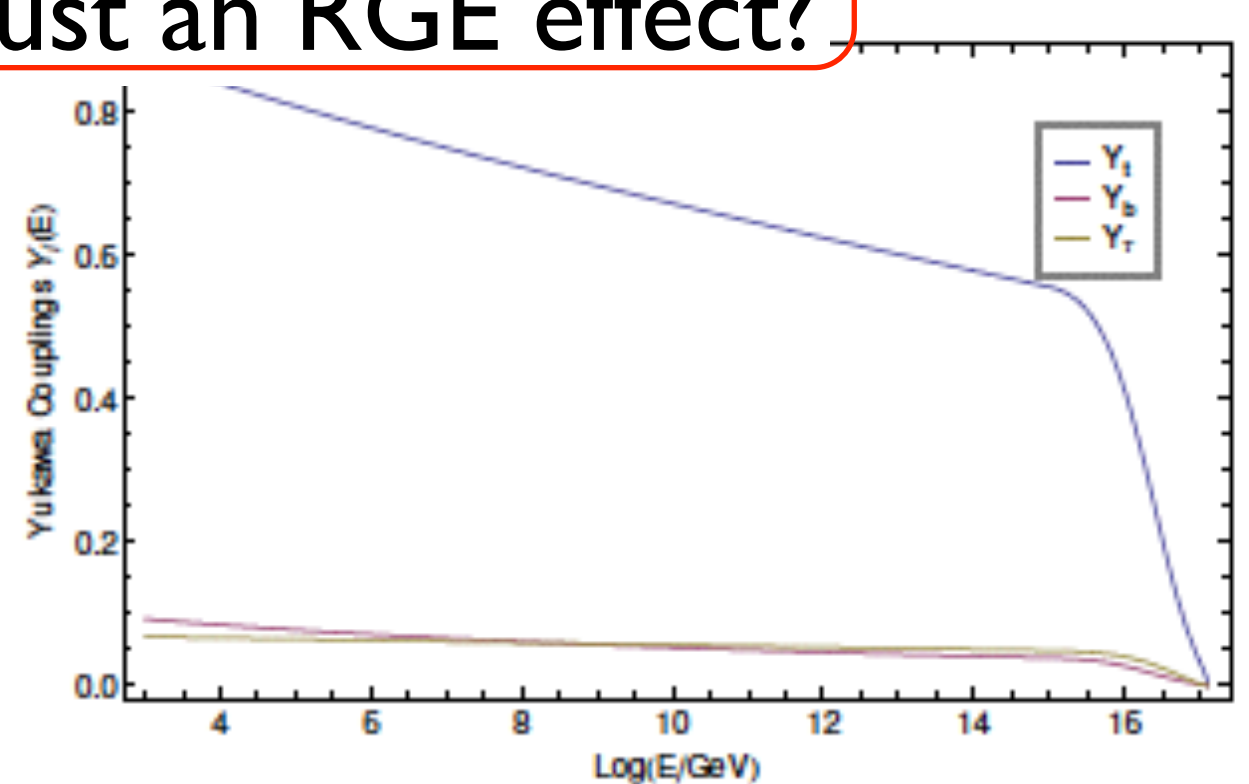
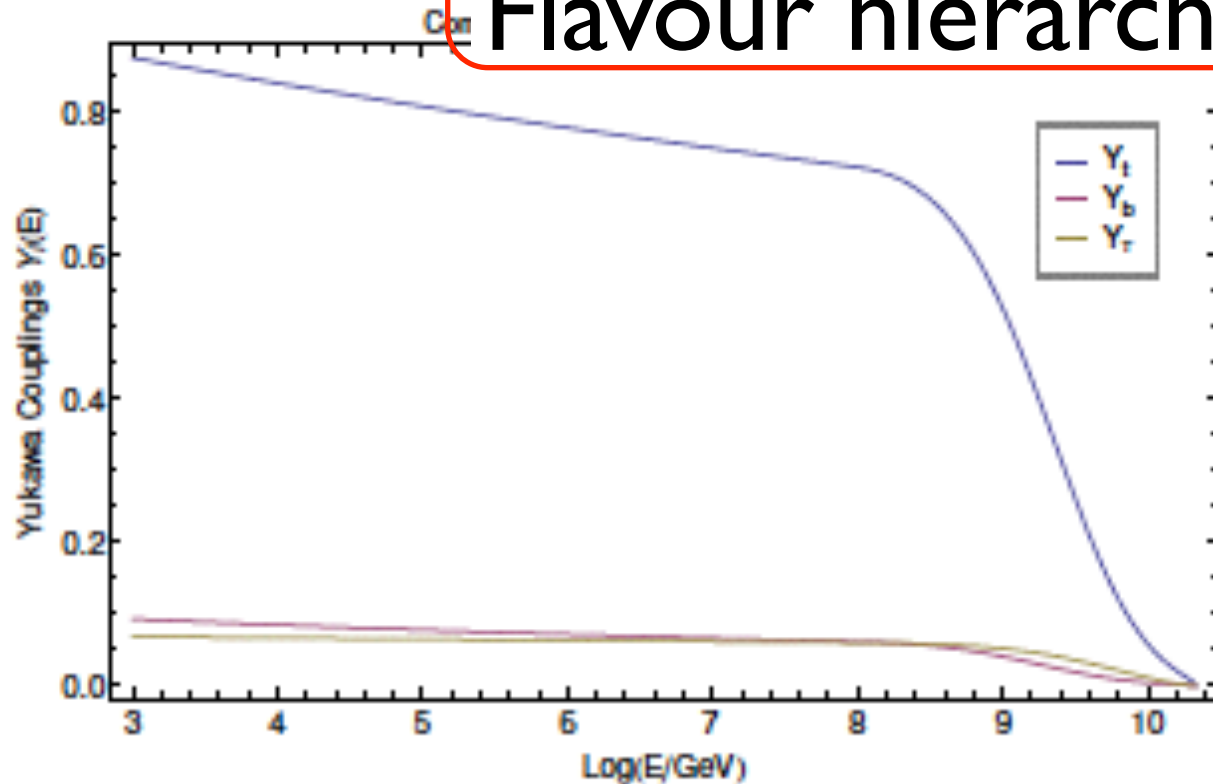


Figure 2. Running of Yukawa couplings Y_i , for three different values of the compactification scales: 10 TeV (top left panel), 10^3 TeV (top right), 10^5 TeV (bottom left) and 10^{12} TeV (bottom right), with $M_3[10^3]$ of 1.7 TeV, as a function of $\log(E/\text{GeV})$.

Compactification scale 10 TeV

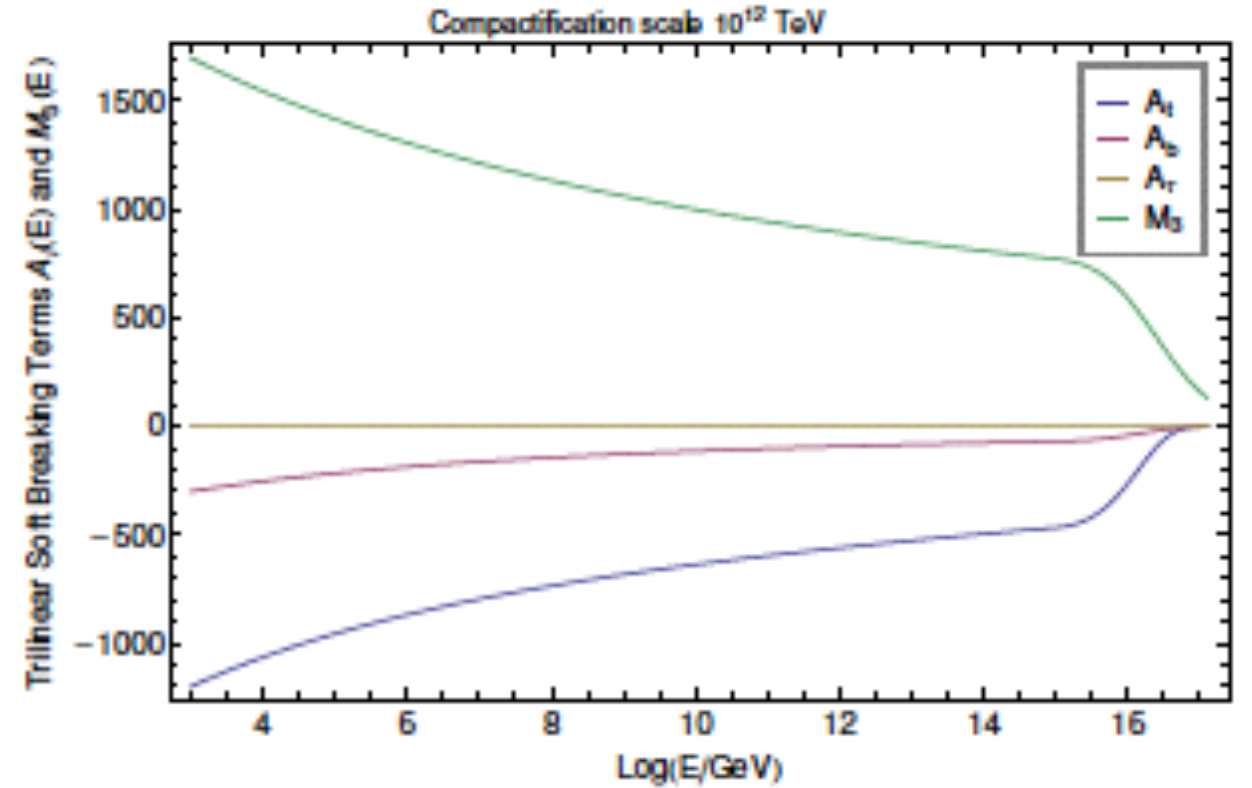
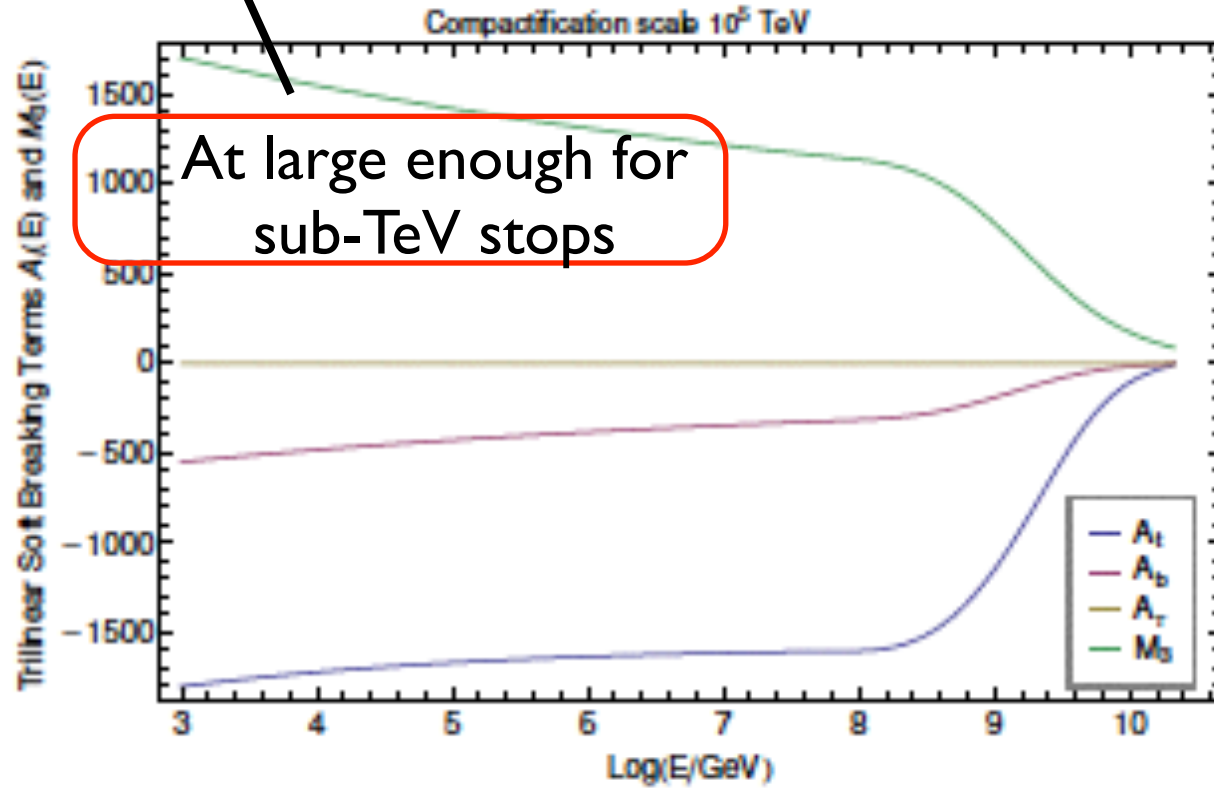
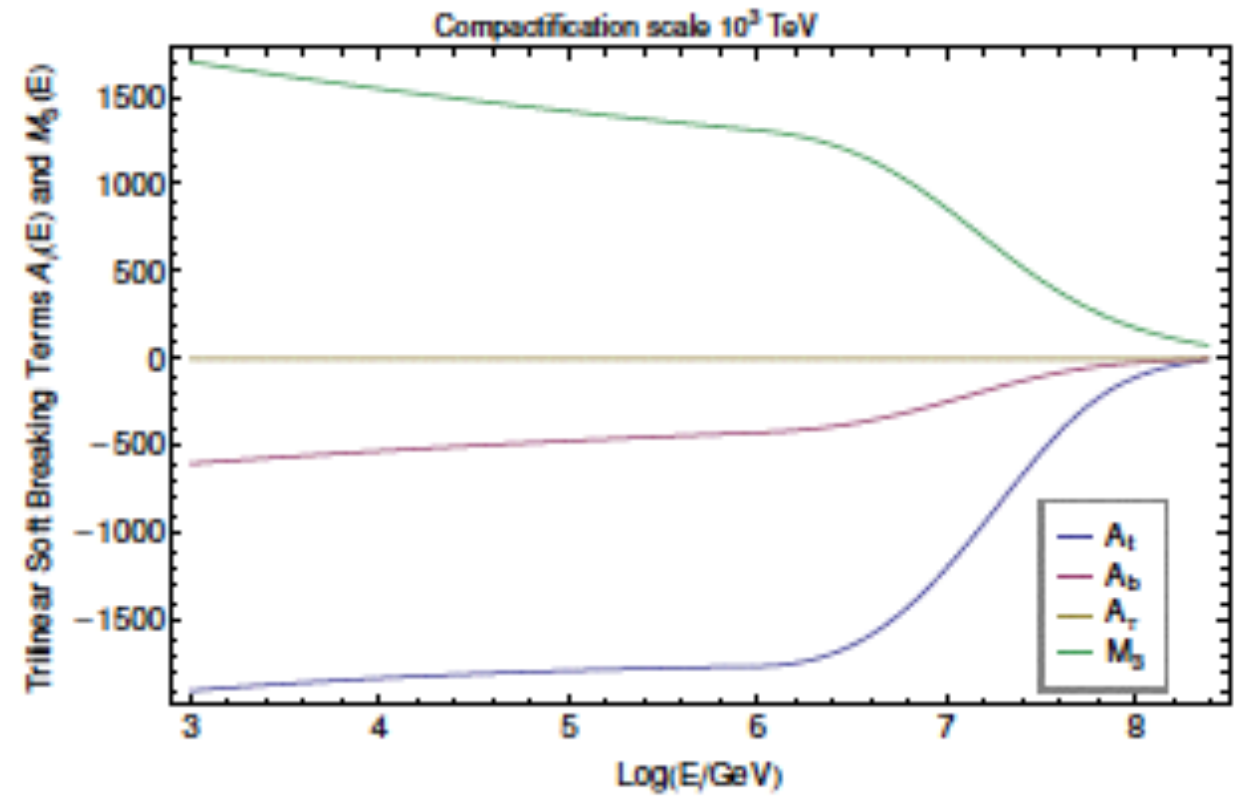
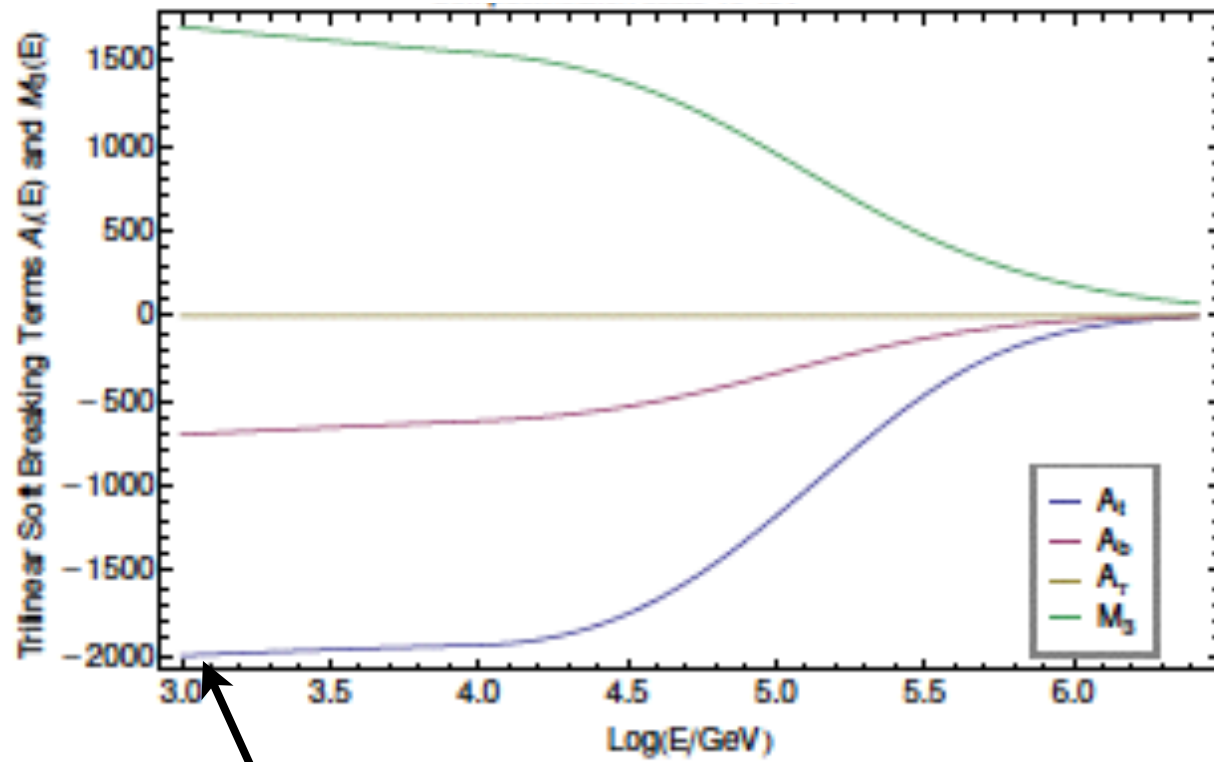
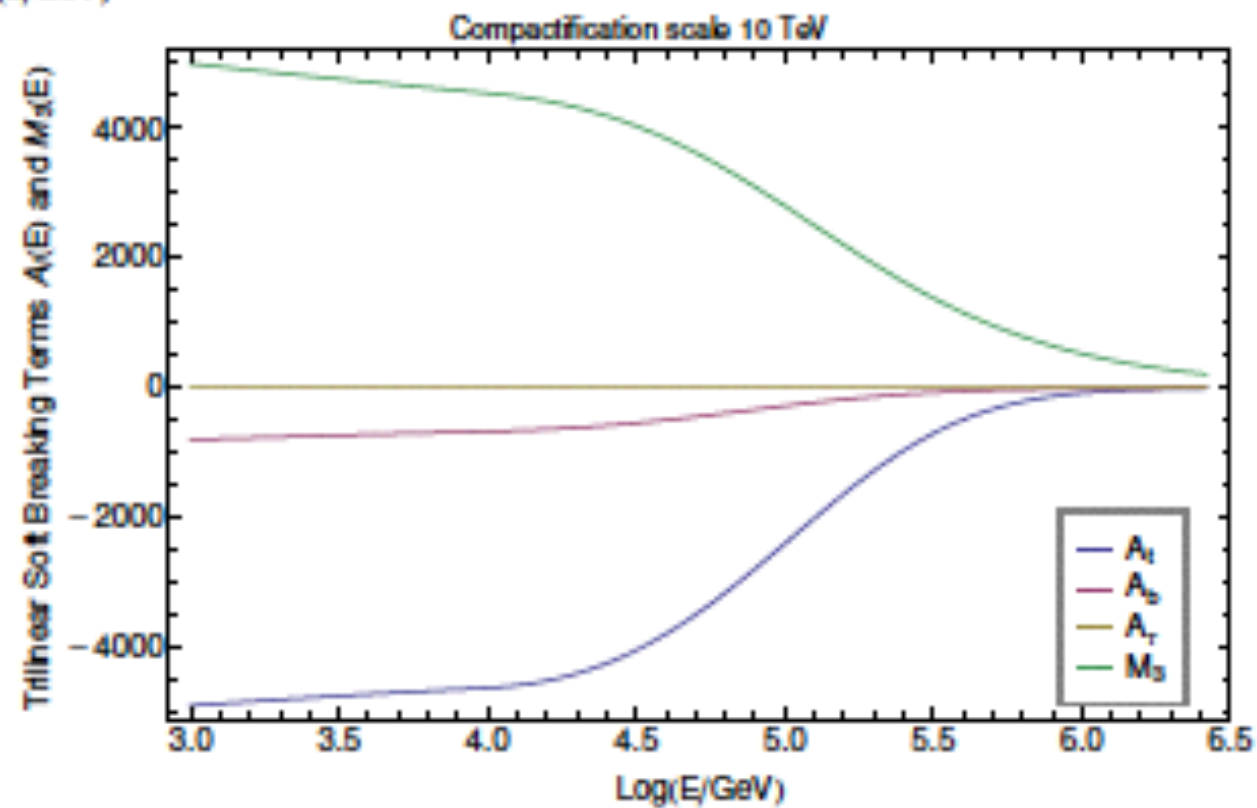
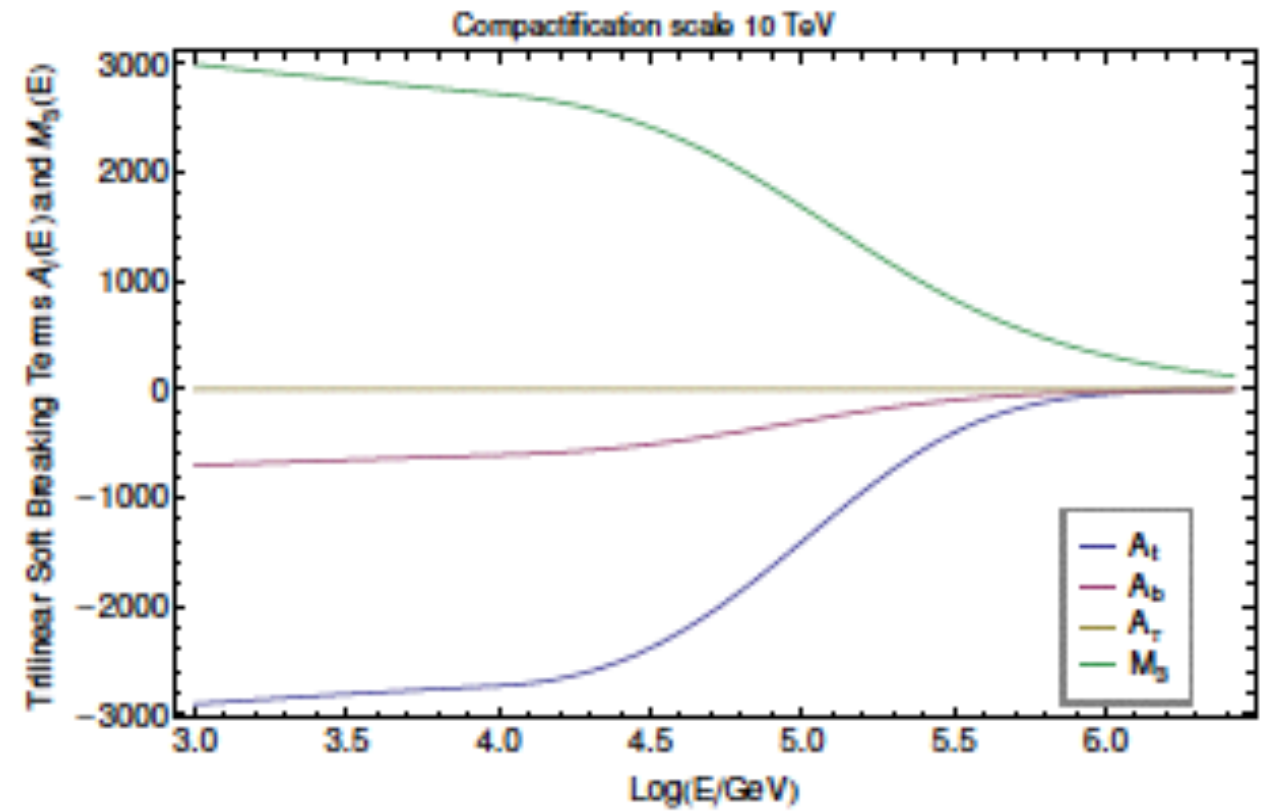
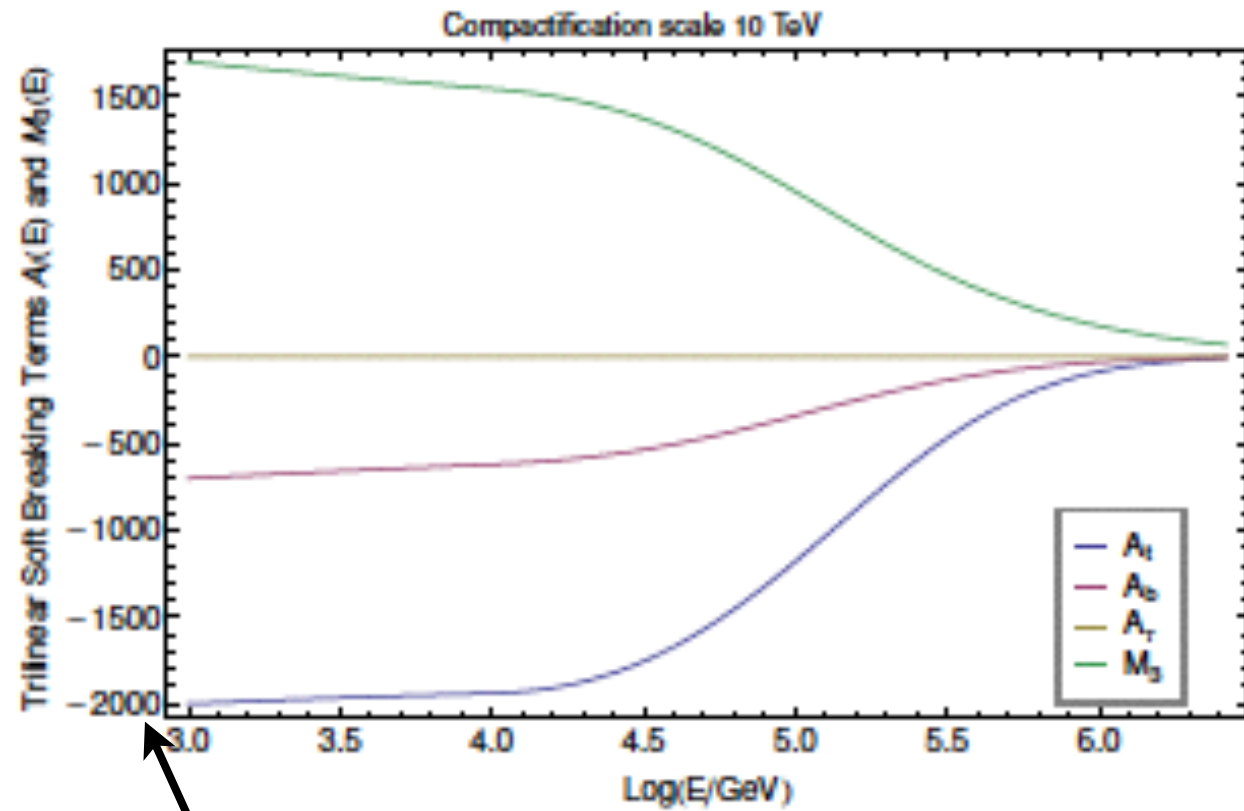


Figure 3. Running of trilinear soft terms $A_i(3,3)(E)$, for three different values of the compactification scales 10 TeV (top left panel), 10^3 TeV (top right), 10^5 TeV (bottom left) and 10^{12} TeV (bottom right), with $M_3[10^3]$ of 1.7 TeV, as a function of $\log(E/\text{GeV})$.



At large enough for
sub-TeV stops

Larger gluino gives larger A_t

Conclusions

- Traditional models are in bad shape
- Perhaps it is time to panic?
- Natural SUSY is motivated from bottom up
- These can have exciting top-down motivations too
- It does mean sacrificing minimality!