

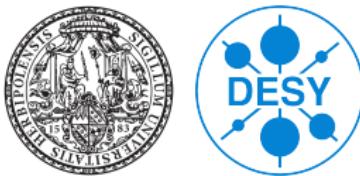


# Improved ultra-high-energy cosmic ray and neutrino predictions from gamma-ray bursts

Mauricio Bustamante

Inst. für Theoretische Physik und Astrophysik, Uni. Würzburg &  
Deutsches Elektronen-Synchrotron DESY, Zeuthen

Gamma-ray bursts in the multi-messenger era  
Paris, June 17, 2014





The origin of UHE CRs ( $\gtrsim 10^9$  GeV) and  $\nu$ 's is still unknown:

- ▶ *how* are they produced?
- ▶ *where* are they produced?

GRBs are among the best candidate sources:

- ▶ radiated energy of  $\sim 10^{52} - 10^{53}$  erg
- ▶ intense magnetic fields of  $\sim 10^5$  G
- ▶ magnetically-confined  $p$ 's shock-accelerated to  $\sim 10^{12}$  GeV

**Problem:** experiments (IceCube, ANTARES) are starting to strongly constrain the simplest emission models

**Solution:** we need to build more realistic models!



Three steps towards improving the GRB neutrino predictions:

Step 1

Refine the calculation of the neutrino yield  
in  $p\gamma$  interactions

Step 2

Go beyond the simplest UHECR-neutrino connection

Step 3

Treat the fireball dynamically (neutrino “light curves”)



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Joint production of UHECRs,  $\nu$ 's, and  $\gamma$ 's:

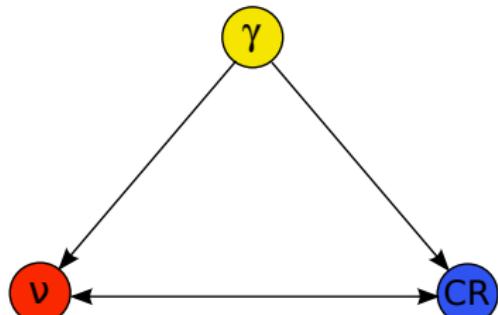
$$p\gamma \rightarrow \Delta^+ (1232) \rightarrow \begin{cases} n\pi^+, & \text{BR} = 1/3 \\ p\pi^0, & \text{BR} = 2/3 \end{cases}$$

$$\pi^+ \rightarrow \mu^+ \nu_\mu \rightarrow \bar{\nu}_\mu e^+ \nu_e \nu_\mu$$

$$\pi^0 \rightarrow \gamma\gamma$$

$$n \text{ (escapes)} \rightarrow p e^- \bar{\nu}_e$$

( $\Delta^+$ : ~50% of all  $p\gamma$  interactions)



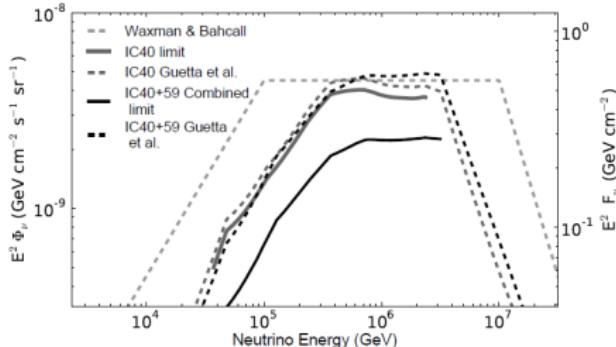
After propagation, with flavour mixing:

$$\nu_e : \nu_\mu : \nu_\tau : p = 1 : 1 : 1 : 1$$

(“one  $\nu_\mu$  per cosmic ray”)

The *simplest* neutron model is now strongly disfavoured ►

# The neutron model under tension?



## IceCube Collaboration:

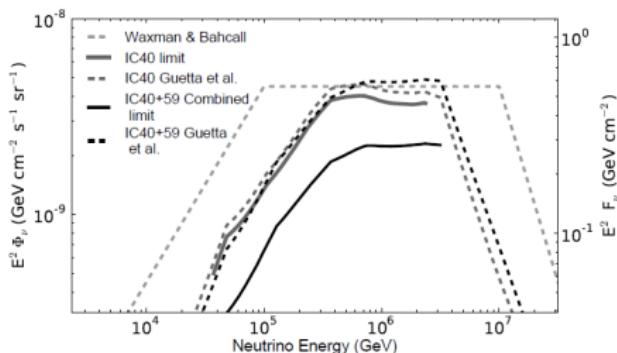
- ▶  $\nu$  flux normalised to GRB  $\gamma$  fluence:
$$\int_0^\infty dE_\nu E_\nu F_\nu (E_\nu) \propto \int_{1 \text{ keV}}^{10 \text{ MeV}} d\varepsilon_\gamma \varepsilon_\gamma F_\gamma (\varepsilon_\gamma)$$
- ▶ quasi-diffuse  $\nu$  flux from 117 GRBs
- ▶ **analytical calculation** – in tension with upper bounds

ICECUBE COLL., *Nature* **484**, 351 (2012)

AHLERS ET AL. *Astropart. Phys.* **35**, 87 (2011)

GUETTA ET AL. *Astropart. Phys.* **20**, 429 (2004)

# The neutron model under tension?



More detailed particle physics (NeuCosmA):

- ▶ extra multi- $\pi$ ,  $K$ ,  $n$  production modes
- ▶ synchrotron losses of secondaries
- ▶ adiabatic cooling
- ▶ full photon spectrum, etc.

$\nu$  flux  $\sim$  one order of magnitude lower

BAERWALD, HÜMMER, WINTER, PRL 108, 231101 (2012)

See also: HE, LIU, WANG, ApJ 752, 29 (2012)

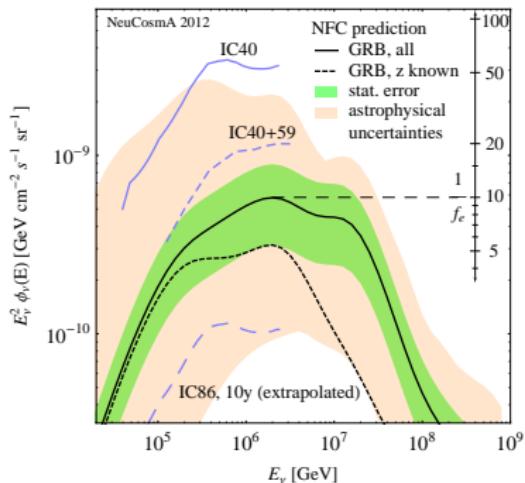
## IceCube Collaboration:

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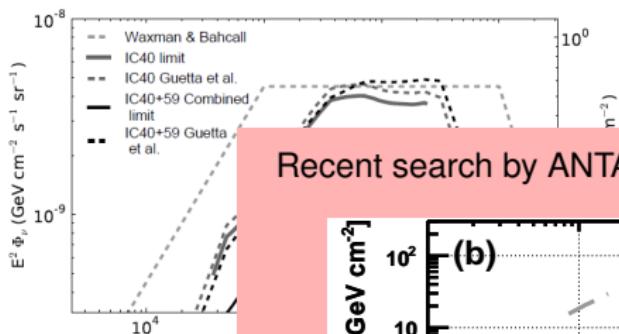
ICECUBE COLL., Nature 484, 351 (2012)

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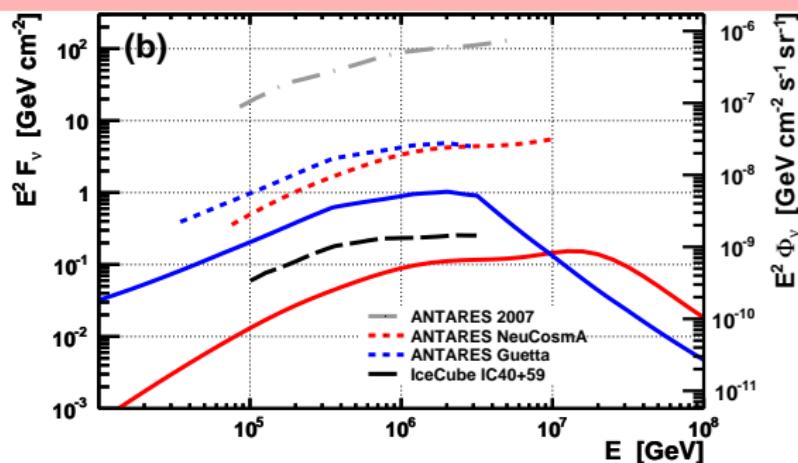
# The neutron model under tension?



More detailed particle physics (NeuCosmA):

- ▶ extra multi- $\pi$ ,  $K$ ,  $n$  production modes
- ▶ synchrotron losses of secondaries

Recent search by ANTARES optimised for NeuCosmA:



ANTARES COLLAB., A & A 559, A9 (2013)

IceCube Collaboration

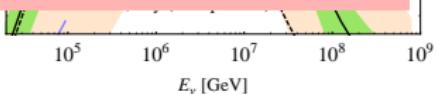
- ▶  $\nu$  flux norm
- ▶  $\int_0^\infty dE_\nu E_\nu I$
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- ▶ analytical c
- ▶ upper bound

ICECUBE COLLAB., Natu

AHLERS ET AL. Astropart. Phys. 35, 87 (2011)

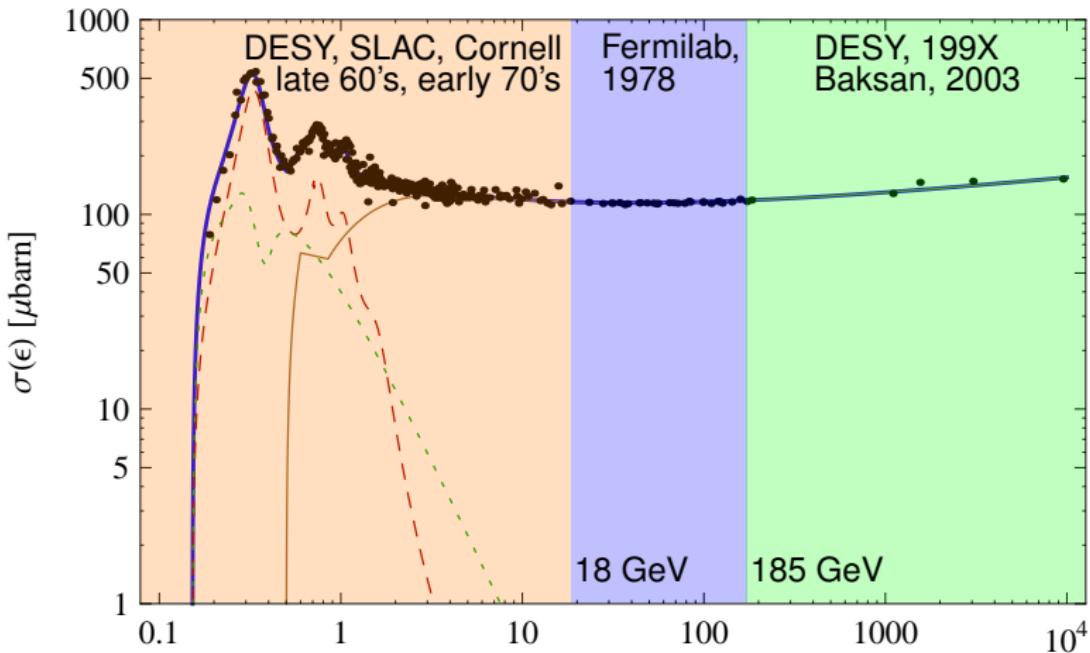
GUETTA ET AL. Astropart. Phys. 20, 429 (2004)

See talk by J. Schmid tomorrow



## Revising the neutron model: NeuCosmA

- Detailed  $p\gamma$  cross section

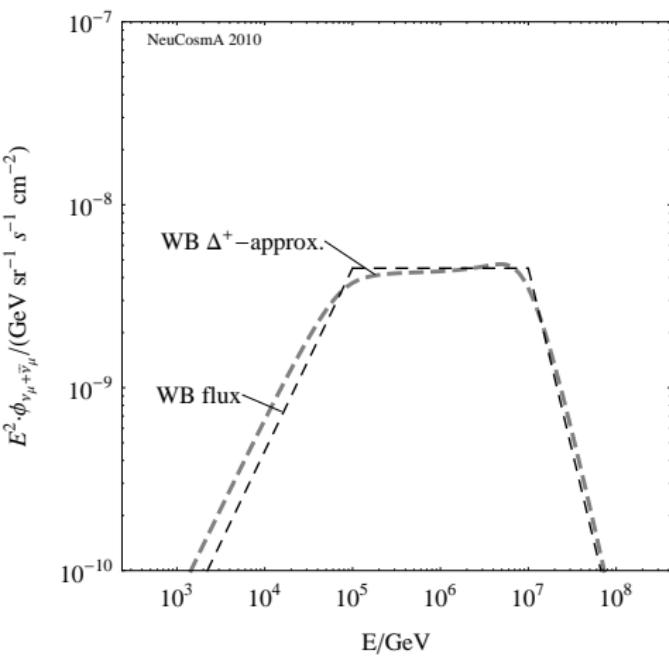


S. HÜMMER, M. RÜGER, F. SPANIER, AND W. WINTER,  
*Astrophys. J.* **721**, 630 (2010)

$\epsilon_r [\text{GeV}]$  Implemented as fast SOPHIA-based parametrisation

# Revising the neutron model: NeuCosmA

- Contributions to the full photohadronic cross section

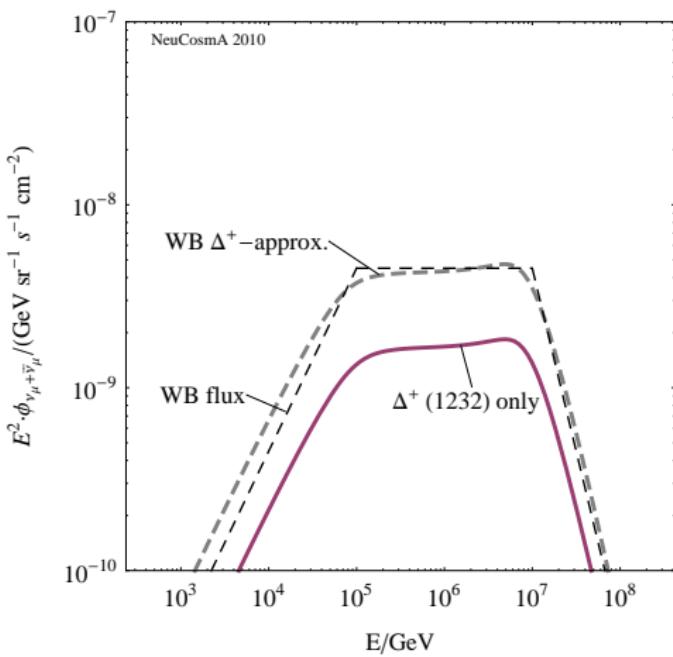


# Revising the neutron model: NeuCosmA

- Contributions to the full photohadronic cross section

Contributions to  $(\nu_\mu + \bar{\nu}_\mu)$  flux from  $\pi^\pm$  decay divided in:

- ▶  $\Delta(1232)$ -resonance



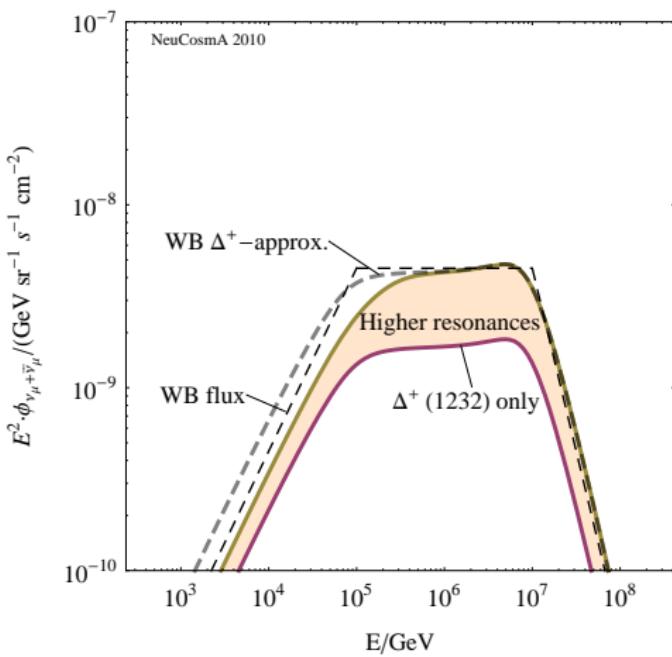
P. BAERWALD, S. HÜMMER, AND W. WINTER,  
*Phys. Rev. D83*, 067303 (2011)

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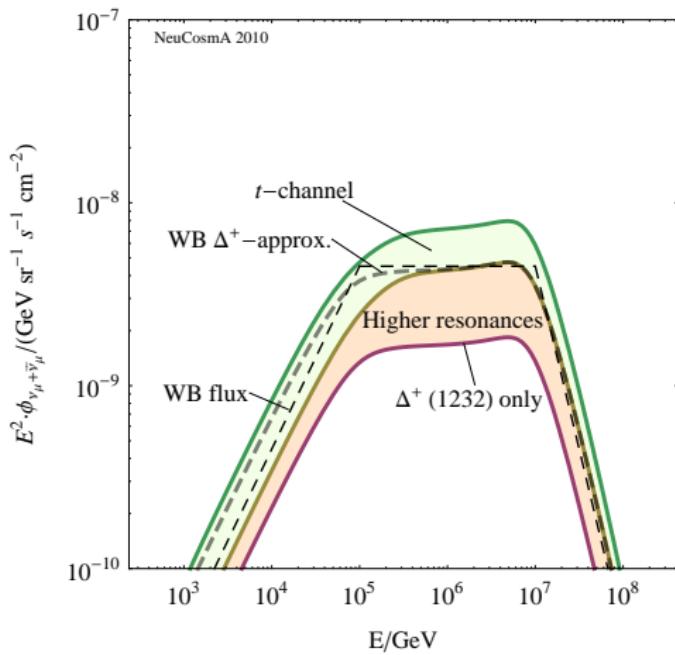
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- ▶  $t$ -channel  
(direct production)

P. BAERWALD, S. HÜMMER, AND W. WINTER,  
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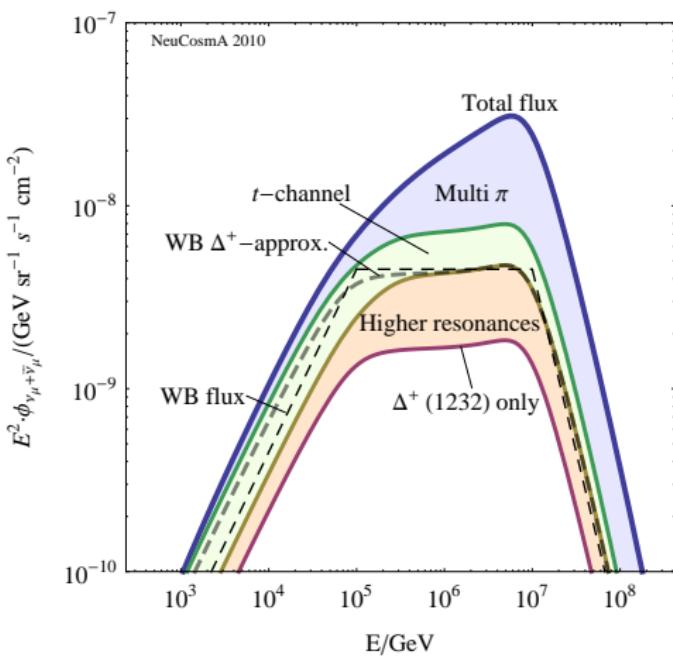
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Contributions to  $(\nu_\mu + \bar{\nu}_\mu)$  flux from  $\pi^\pm$  decay divided in:

- ▶  $\Delta(1232)$ -resonance
- ▶ Higher resonances
- ▶  $t$ -channel  
(direct production)
- ▶ High energy processes  
(multiple  $\pi$ )

P. BAERWALD, S. HÜMMER, AND W. WINTER,  
*Phys. Rev. D83*, 067303 (2011)



Especially "Multi  $\pi$ " contribution leads to **change of flux shape**; neutrino flux higher by up to a factor of 3 compared to WB treatment

$$\begin{aligned}\pi^+ &\rightarrow \mu^+ + \nu_\mu \\ \mu^+ &\rightarrow e^+ + \nu_e + \bar{\nu}_\mu\end{aligned}$$

$$\begin{aligned}\pi^- &\rightarrow \mu^- + \bar{\nu}_\mu \\ \mu^- &\rightarrow e^- + \bar{\nu}_e + \nu_\mu\end{aligned}$$

$$K^+ \rightarrow \mu^+ + \nu_\mu$$

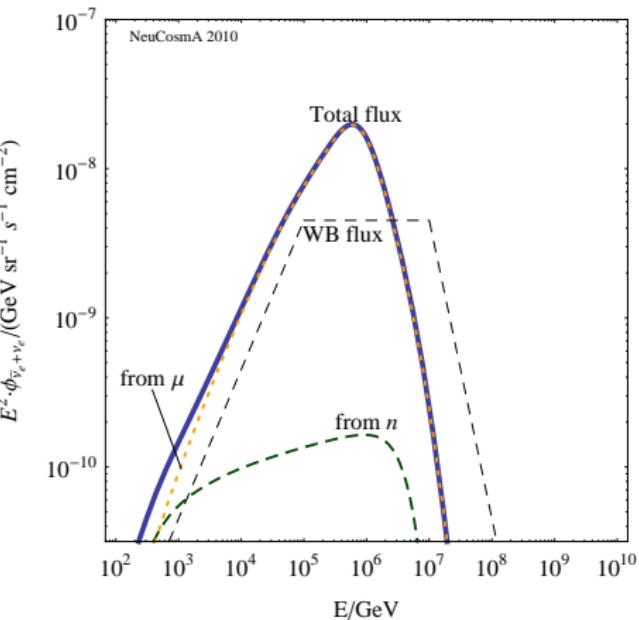
$$n \rightarrow p + e^- + \bar{\nu}_e$$

# Revising the neutron model: NeuCosmA

- Further particle decays

$$\begin{aligned}\pi^+ &\rightarrow \mu^+ + \nu_\mu \\ &\quad \mu^+ \rightarrow e^+ + \textcolor{red}{\bar{\nu}_e} + \bar{\nu}_\mu \\ \\ \pi^- &\rightarrow \mu^- + \bar{\nu}_\mu \\ &\quad \mu^- \rightarrow e^- + \textcolor{red}{\bar{\nu}_e} + \nu_\mu \\ \\ K^+ &\rightarrow \mu^+ + \nu_\mu \\ \\ n &\rightarrow p + e^- + \textcolor{red}{\bar{\nu}_e}\end{aligned}$$

Resulting  $\nu_e$  flux (at the observer)



P. BAERWALD, S. HÜMMER, AND W. WINTER, *Phys. Rev. D* **83**, 067303 (2011)

# Revising the neutron model: NeuCosmA

- Further particle decays

$$\pi^+ \rightarrow \mu^+ + \nu_\mu$$

$$\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$$

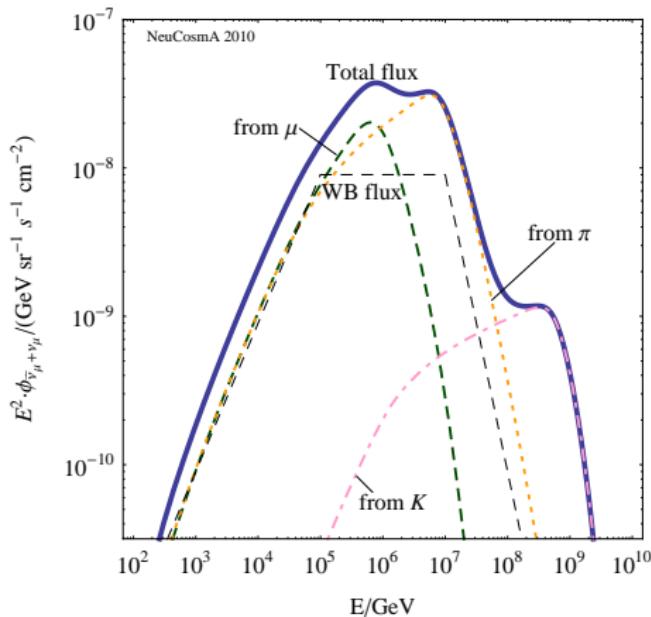
$$\pi^- \rightarrow \mu^- + \bar{\nu}_\mu,$$

$$\mu^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu$$

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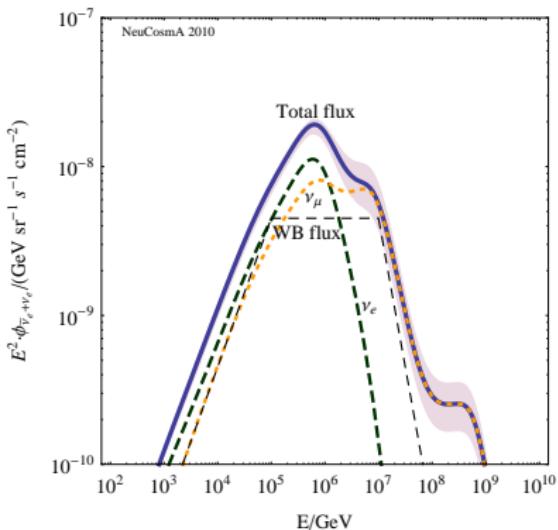


P. BAERWALD, S. HÜMMER, AND W. WINTER, *Phys. Rev.* **D83**, 067303 (2011)

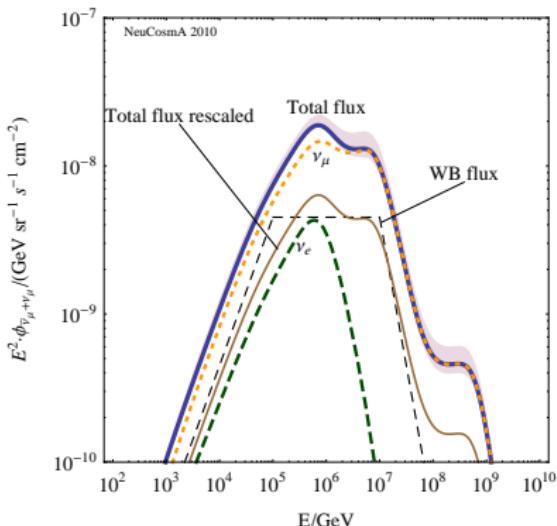
# Revising the neutron model: NeuCosmA

- Neutrino spectra including flavour mixing

Electron neutrino spectrum



Muon neutrino spectrum



P. BAERWALD, S. HÜMMER, AND W. WINTER, *Phys. Rev. D83*, 067303 (2011)

Characteristic double peak structure from  $\mu$  and  $\pi$  decay in both flavours, additional peak from  $K^+$  decay at  $10^8$  to  $10^9$  GeV

# Revising the neutron model: NeuCosmA

- How the spectrum changes...

Corrections to the analytical model:

► shape revised:

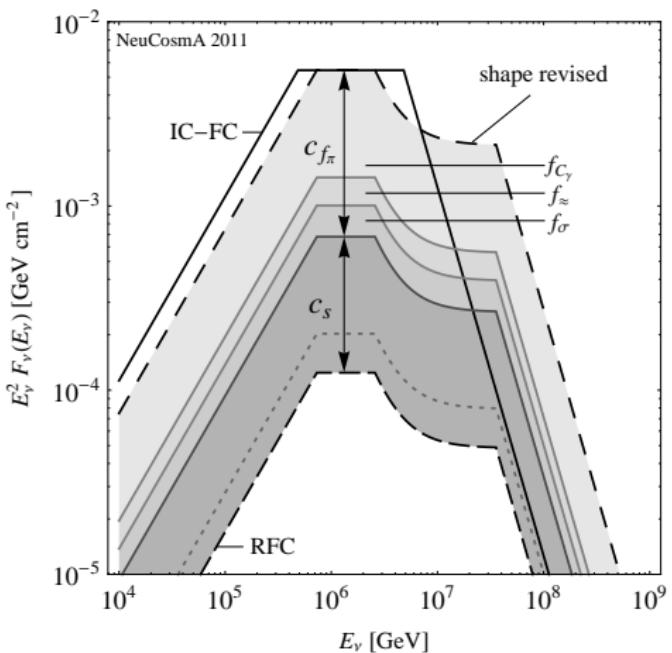
- ▶ shift of first break (correction of photohadronic threshold)
- ▶ different cooling breaks for  $\mu$ 's and  $\pi$ 's
- ▶  $(1+z)$  correction on the variability scale of the GRB

► Correction  $cf_\pi$  to  $\pi$  prod. efficiency:

- ▶  $f_{C\gamma}$ : full spectral shape of photons
- ▶  $f_{\approx} = 0.69$ : rounding error in analytical calculation
- ▶  $f_\sigma \simeq 2/3$ : from neglecting the width of the  $\Delta$ -resonance

► Correction  $c_s$ :

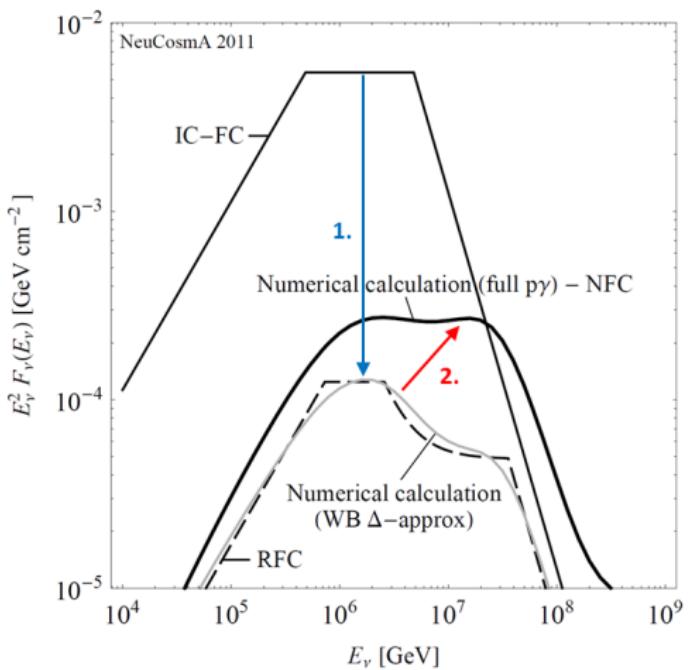
- ▶ energy losses of secondaries
- ▶ energy dependence of the mean free path of protons



S. HÜMMER, P. BAERWALD, AND W. WINTER,  
*Phys. Rev. Lett.* **108**, 231101 (2012)

# Revising the neutron model: NeuCosmA

- How the spectrum changes ... (cont.)



IC-FC: IceCube-Fireball Calculation  
RFC: Revised Fireball Calculation  
NFC: Numerical Fireball Calculation

S. HÜMMER, P. BAERWALD, AND W. WINTER, *Phys. Rev. Lett.* **108**, 231101 (2012)

# Revising the neutron model: NeuCosmA

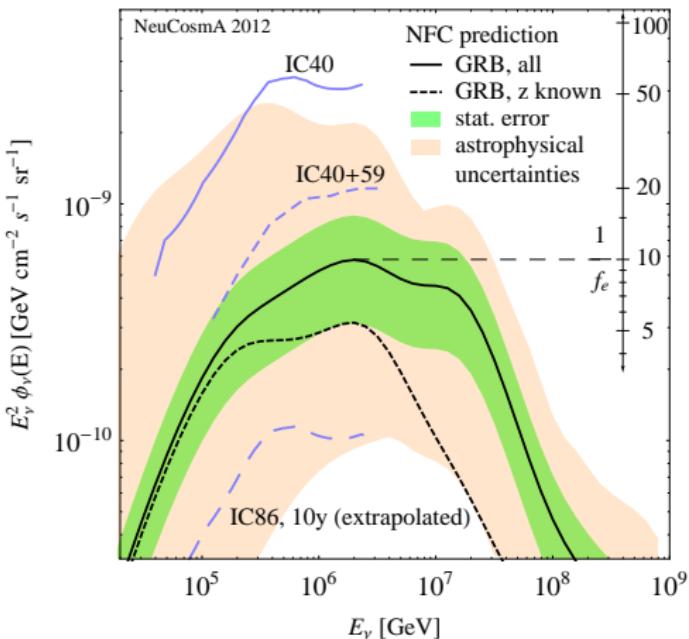
- The new prediction of the quasi-diffuse GRB  $\nu$  flux

- ▶ Same  $n = 117$  GRBs, effective area, and parameters as used by the IC-40 analysis
- ▶ Calculate the associated neutrino flux for each burst and the stacked flux  $F_\nu(E_\nu)$
- ▶ Quasidiffuse flux:

$$\phi_\nu(E_\nu) = F_\nu(E_\nu) \frac{1}{4\pi} \frac{1}{n} \frac{667 \text{ bursts}}{\text{yr}}$$

- ▶ Statistical uncertainty: extrapolation of a few bursts to a quasidiffuse flux
- ▶ Astrophysical uncertainty:

- ▶  $0.001 \leq t_v [\text{s}] \leq 0.1$
- ▶  $200 \leq \Gamma \leq 500$
- ▶  $1.8 \leq \alpha_p \leq 2.2$
- ▶  $0.1 \leq \epsilon_e/\epsilon_B \leq 10$



S. HÜMMER, P. BAERWALD, AND W. WINTER,  
*Phys. Rev. Lett.* **108**, 231101 (2012)



Three steps towards improving the GRB neutrino predictions:

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in  $p\gamma$  interactions

Step 2

Go beyond the simplest UHECR-neutrino connection

Step 3

Treat the fireball dynamically (neutrino “light curves”)

The neutron model hinges on:

- ①  $p$ 's magnetically confined, only  $n$ 's escape
- ②  $p$ 's interact at most once,  $n$ 's do not (*optically thin source*)

However, under the “one  $\nu_\mu$  per CR” hypothesis, GRBs **are disfavoured** to be the sole source of UHECRs ([AHLERS \*et al.\*](#)).

M. AHLERS, M. GONZÁLEZ-GARCÍA, AND F. HALZEN *Astropart. Phys.* **35**, 87 (2011)

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What if ① and ② are violated?

- ▶  $p$ 's “leak out”, not accompanied by (direct)  $\nu$  production
- ▶ multiple  $p$  interactions enhance the  $\nu$  flux
- ▶ in *optically thick sources*, only  $n$ 's at the borders escape

[M. AHLERS, M. GONZÁLEZ-GARCÍA, AND F. HALZEN](#) *Astropart. Phys.* **35**, 87 (2011)

# A two-component model of CR emission

Optical depth:

$$\tau_n = \left. \frac{t_{p\gamma}^{-1}}{t_{\text{dyn}}^{-1}} \right|_{E_{p,\text{max}}} = \begin{cases} \lesssim 1, & \text{optically thin source} \\ > 1, & \text{optically thick source} \end{cases}$$

$E'_{p,\text{max}}$  determined from a competition of processes:

$$t'_{\text{acc}}(E'_{p,\text{max}}) = \min \left[ t'_{\text{dyn}}, t'_{\text{syn}}, t'_{p\gamma}(E'_{p,\text{max}}) \right]$$

Acceleration efficiency,  $\eta$ :

$$t'_{\text{acc}}(E'_p) = \frac{E'_p}{\eta c e B'}$$

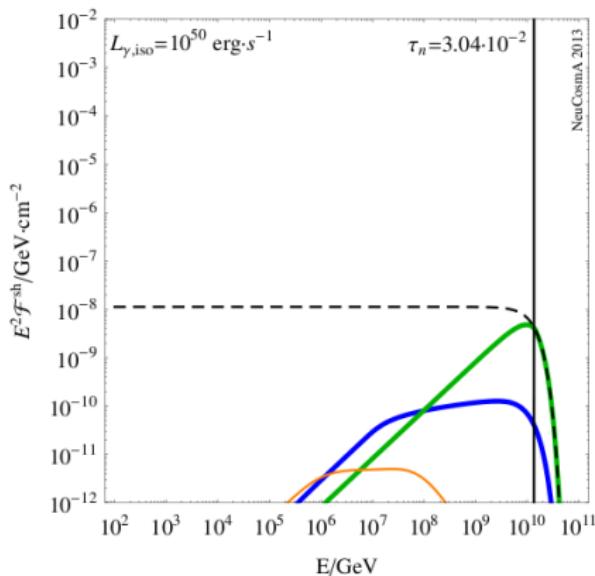
Particles can escape from within a shell of thickness  $\lambda'_{\text{mfp}}$ :

$$\left. \begin{array}{l} \lambda'_{p,\text{mfp}}(E') = \min [\Delta r', R'_L(E'), ct'_{p\gamma}(E')] \\ \lambda'_{n,\text{mfp}}(E') = \min [\Delta r', ct'_{p\gamma}(E')] \end{array} \right\} f_{\text{esc}} = \frac{\lambda'_{\text{mfp}}}{\Delta r'}$$

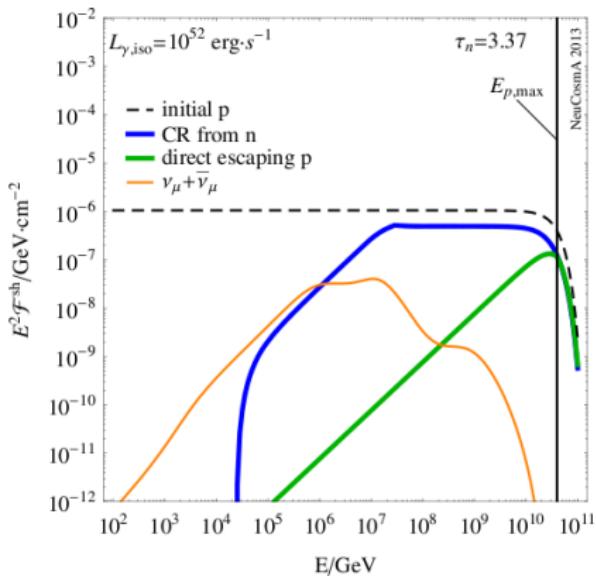
fraction of escaping particles

# A two-component model of CR emission

Optically **thin** source:



Optically **thick** source:



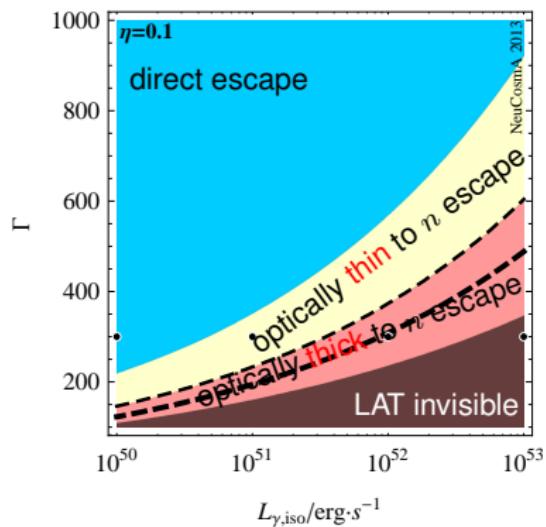
P. BAERWALD, MB, AND W. WINTER, *ApJ* **768**, 186 (2013)

# A two-component model of CR emission

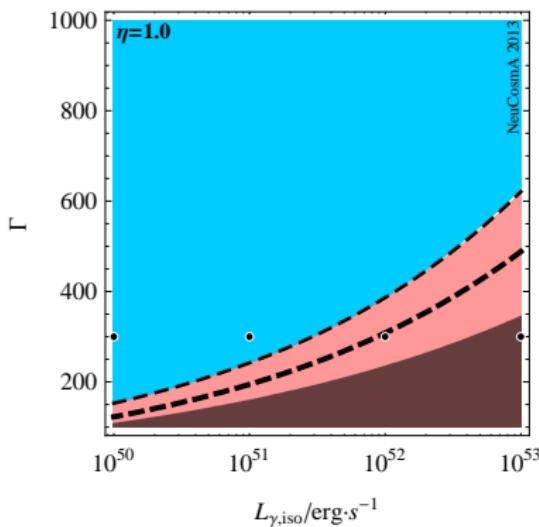
Scan of the GRB emission parameter space:

acceleration  
efficiency

$$\longrightarrow \eta = 0.1$$



$$\eta = 1.0$$



P. BAERWALD, MB, AND W. WINTER, *ApJ* **768**, 186 (2013)

# The UHECR and UHE $\nu$ fluxes at Earth

We use a **Boltzmann equation** to transport protons to Earth:

- ▶ Comoving number density of protons ( $\text{GeV}^{-1} \text{ cm}^{-3}$ ):

$$Y_p(E, z) = n_p(E, z) / (1 + z)^3 ,$$

with  $n_p$  the real number density

- ▶ Transport equation (comoving source frame):

$$\dot{Y}_p = \partial_E (H E Y_p) + \partial_E (b_{e^+ e^-} Y_p) + \partial_E (b_{p\gamma} Y_p) + \mathcal{L}_{\text{CR}}$$

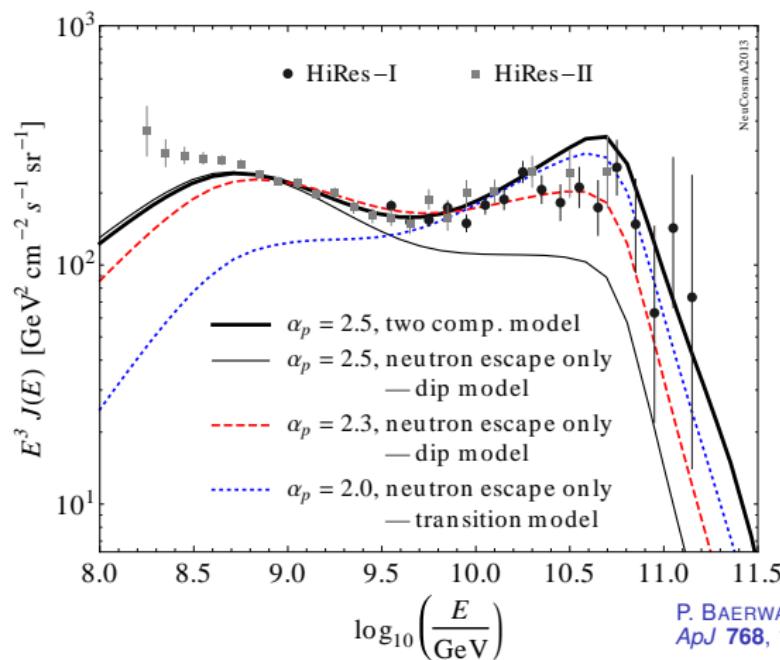
The diagram shows the transport equation  $\dot{Y}_p = \dots$  with four terms in boxes. Arrows point from labels below to each term:

- A blue box labeled "adiabatic losses" points to  $\partial_E (H E Y_p)$ .
- A pink box labeled "pair production losses" points to  $\partial_E (b_{e^+ e^-} Y_p)$ .
- A green box labeled "photohadronic losses" points to  $\partial_E (b_{p\gamma} Y_p)$ .
- An orange box labeled "CR injection from sources" points to  $\mathcal{L}_{\text{CR}}$ .

$$Q_{\text{CR}}(E) \propto E^{-\alpha_p} e^{-E/E_{p,\max}}$$

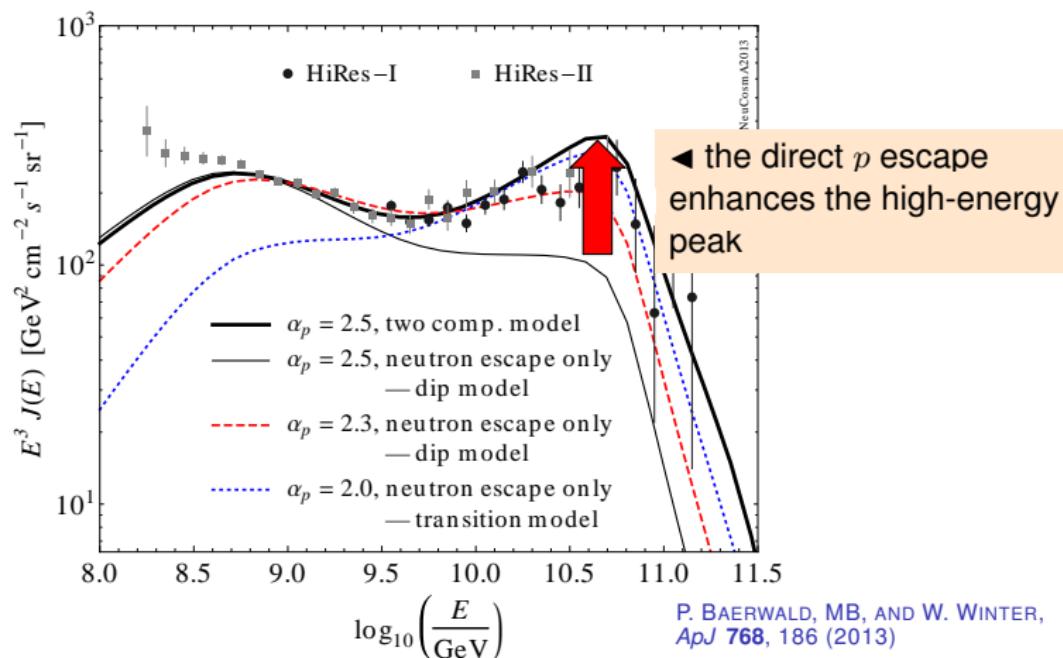
The UHECR and UHE  $\nu$  fluxes at Earth

UHECR flux at Earth from  $n$  and direct  $p$  escape:



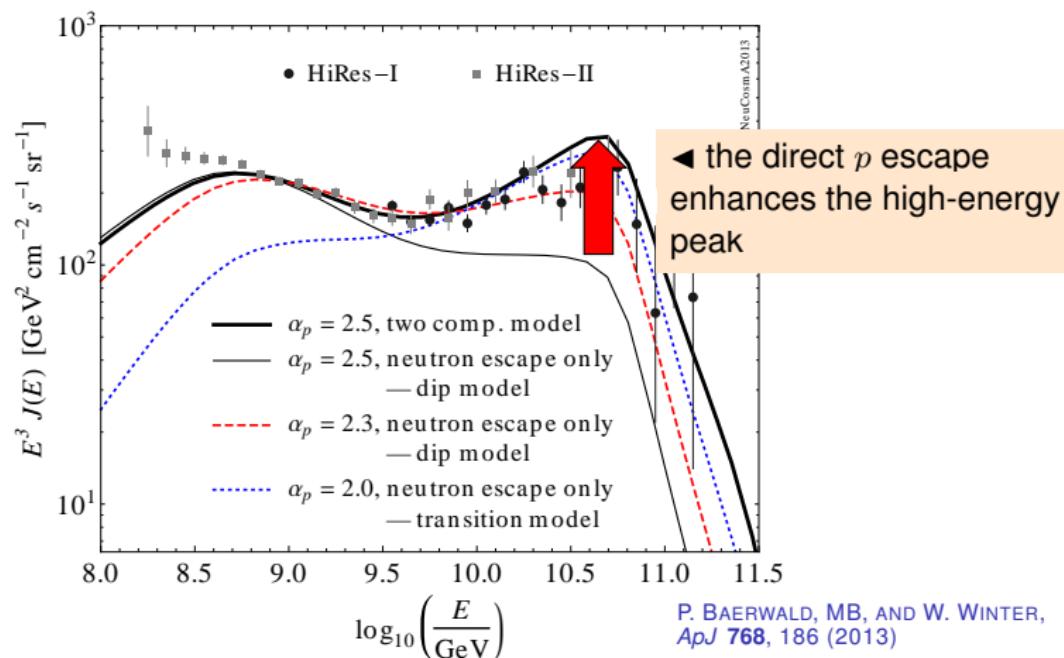
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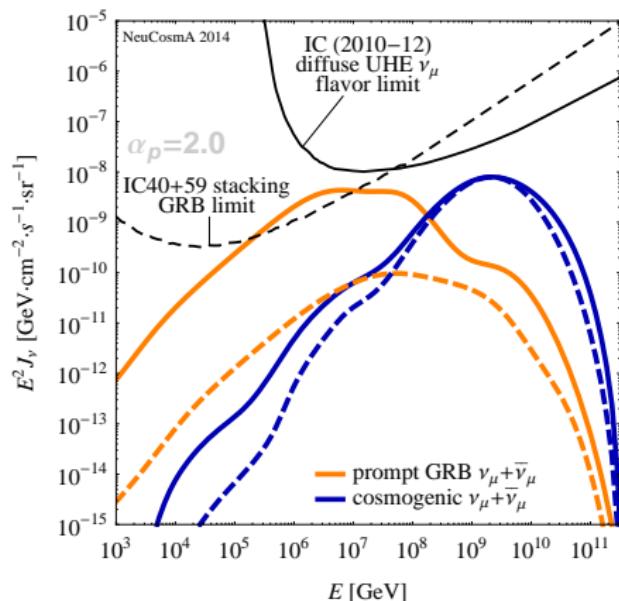
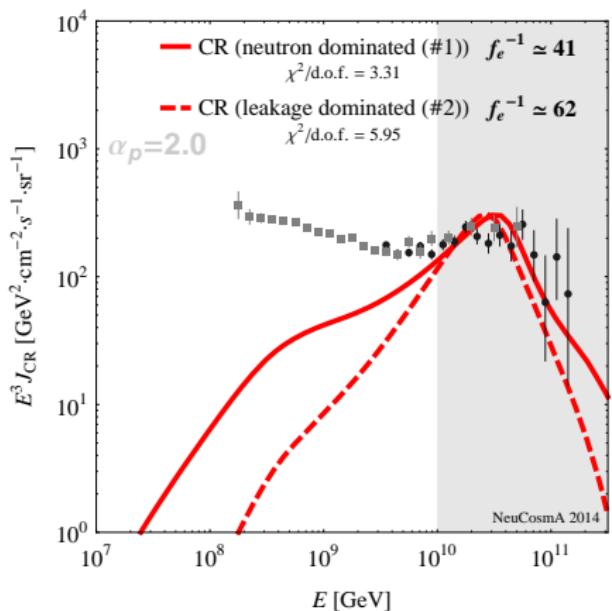
UHECR flux at Earth from  $n$  and direct  $p$  escape:



Our two-component model *is* able to fit the UHECR data

# The UHECR and UHE $\nu$ fluxes at Earth

neutron model vs. two-component model:  
**prompt** and **cosmogenic**  $\nu$ 's



P. BAERWALD, MB, AND W. WINTER, ARXIV:1401.1820

# Where to now? Constraining the connection

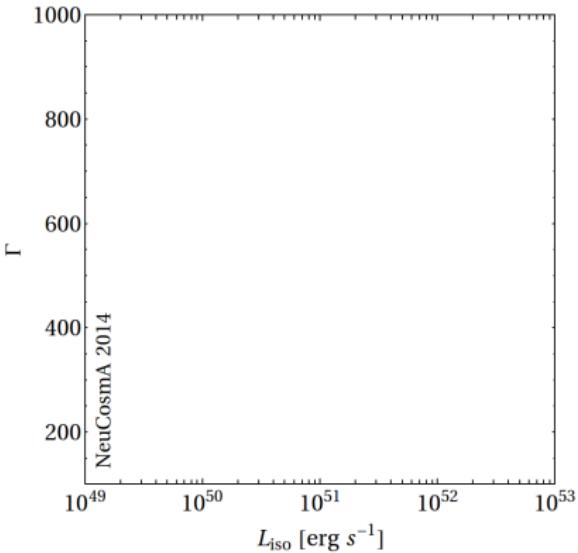
We can already limit the parameter space by using the UHECR observations and  $\nu$  upper bounds:

# Where to now? Constraining the connection

We can already limit the parameter space by using the UHECR observations and  $\nu$  upper bounds:

- 1 Generate the UHECR spectrum at every point in parameter space (e.g., in  $\Gamma$  vs.  $L_{\text{iso}}$ )

direct  $p$  escape,  $\alpha_p = 2$ ,  $\eta = 1.0$

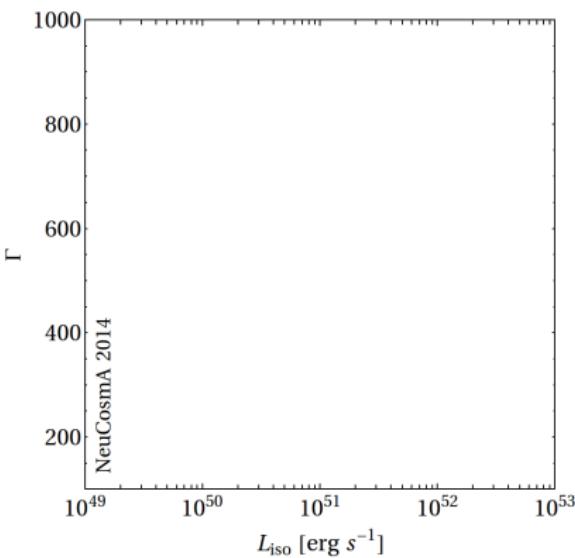


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- 2 Fit each spectrum to HiRes data (or TA, PAO)

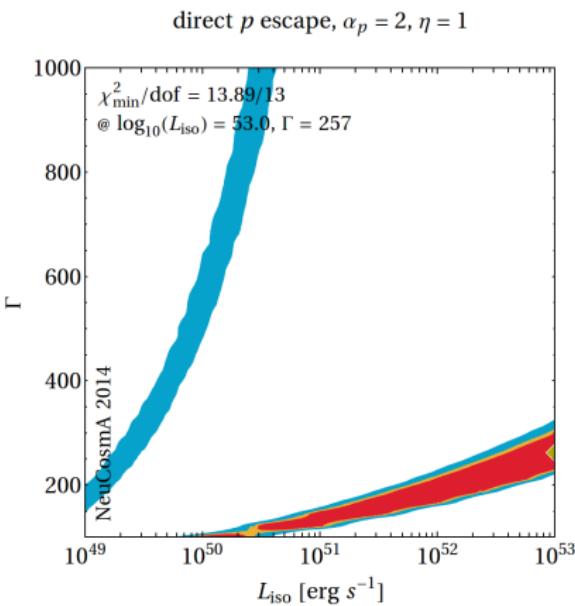
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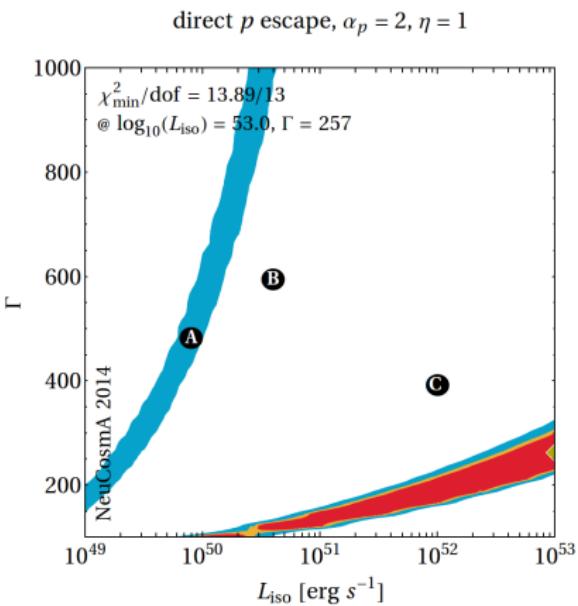
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- 3 Find the best-fit point (diamond), and the 90% (red), 95% (yellow), and 99% (blue) C.L. regions



## Where to now? Constraining the connection

We can already limit the parameter space by using the UHECR observations and  $\nu$  upper bounds:

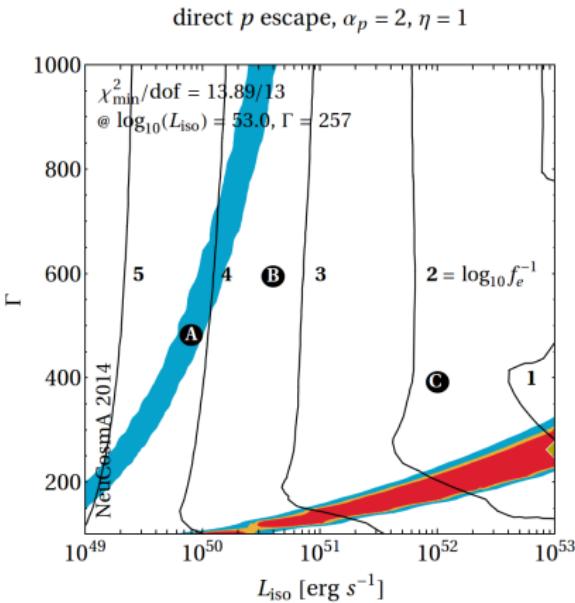
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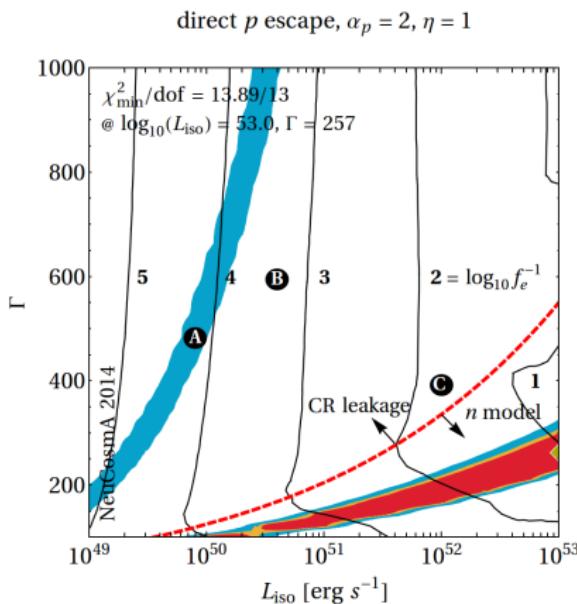
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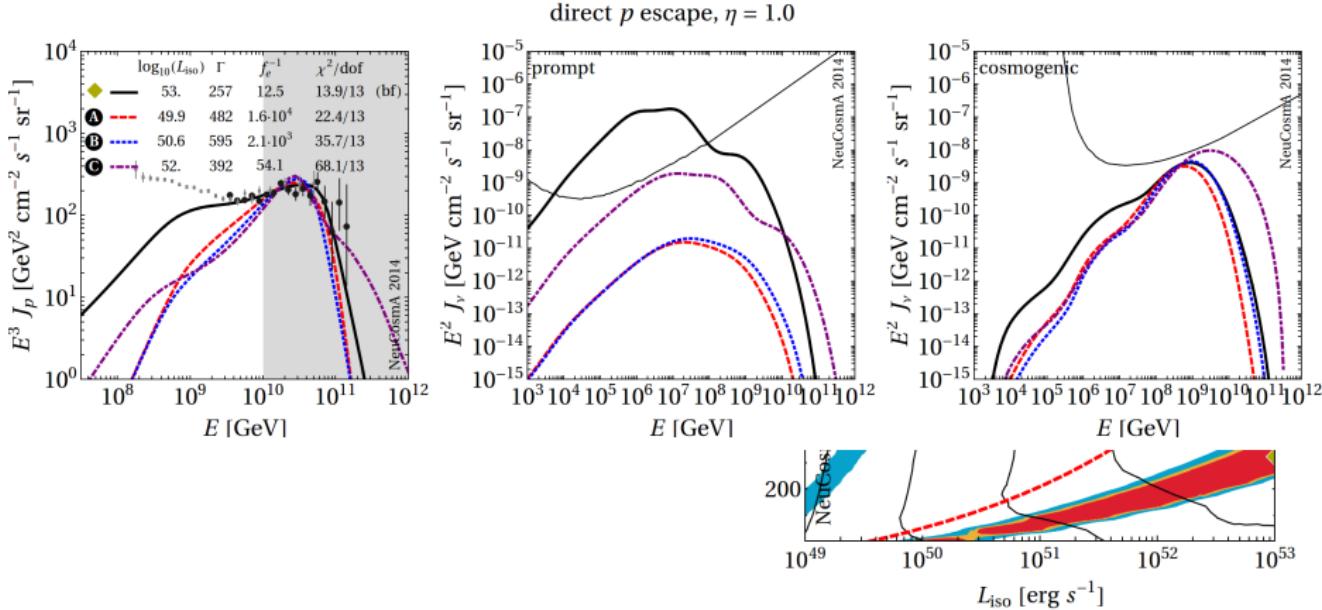
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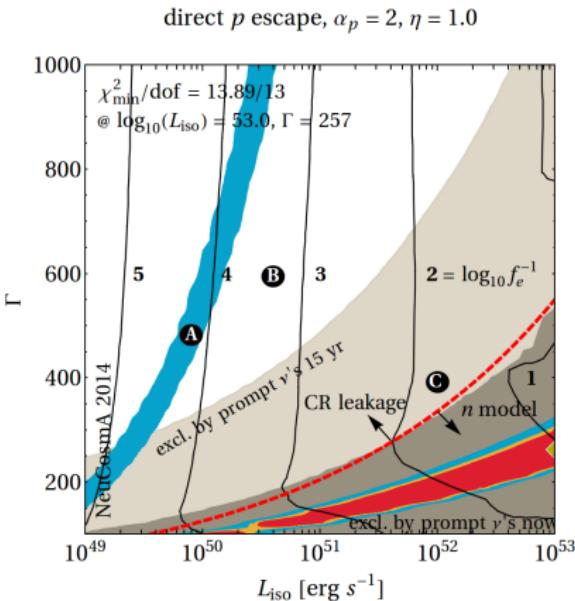
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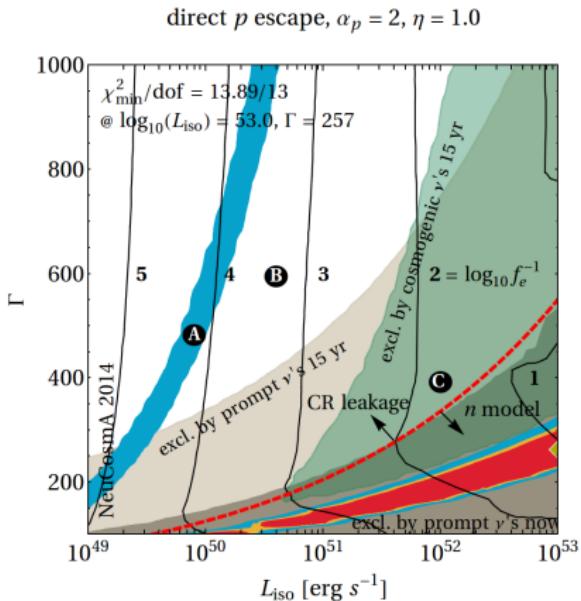
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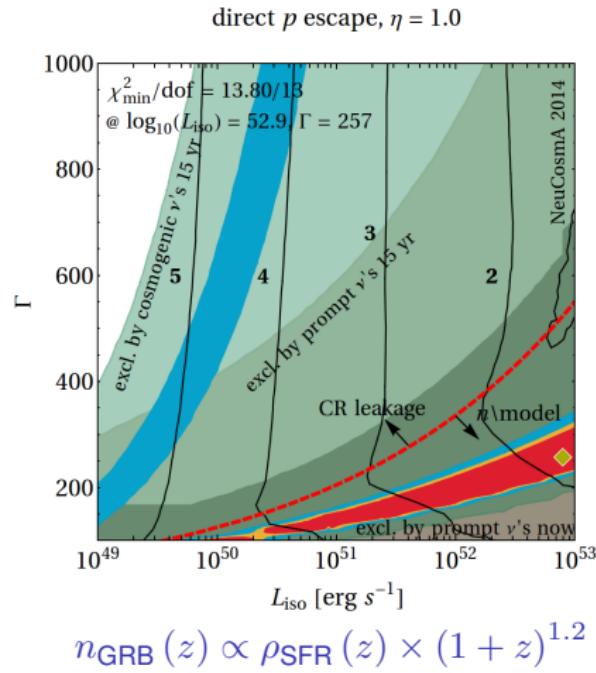
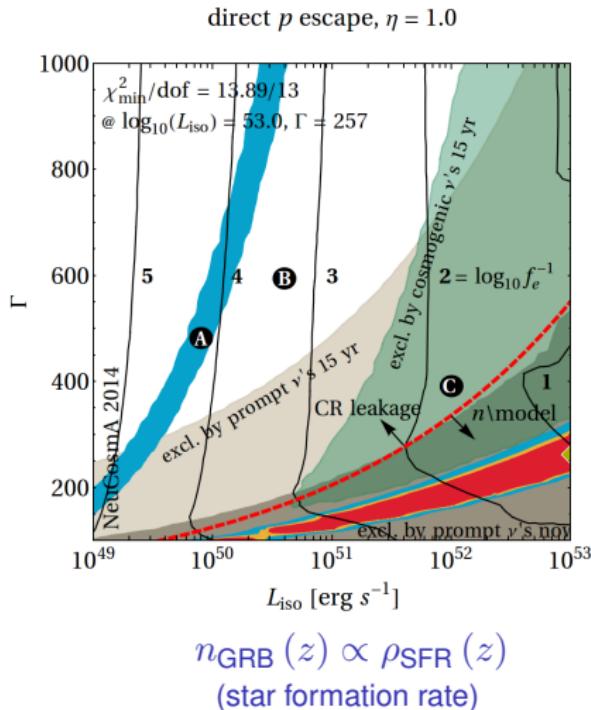
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- 7 After 15 yr of exposure and no detection, cosmogenic neutrinos also exclude



P. BAERWALD, MB, AND W. WINTER, ARXIV:1401.1820

# Where to now? Constraining the connection

The exclusion from cosmogenic  $\nu$ 's grows if the number of GRBs evolves more strongly with redshift:





Three steps towards improving the GRB neutrino predictions:

Step 1

Refine the calculation of the neutrino yield  
in  $p\gamma$  interactions

Step 2

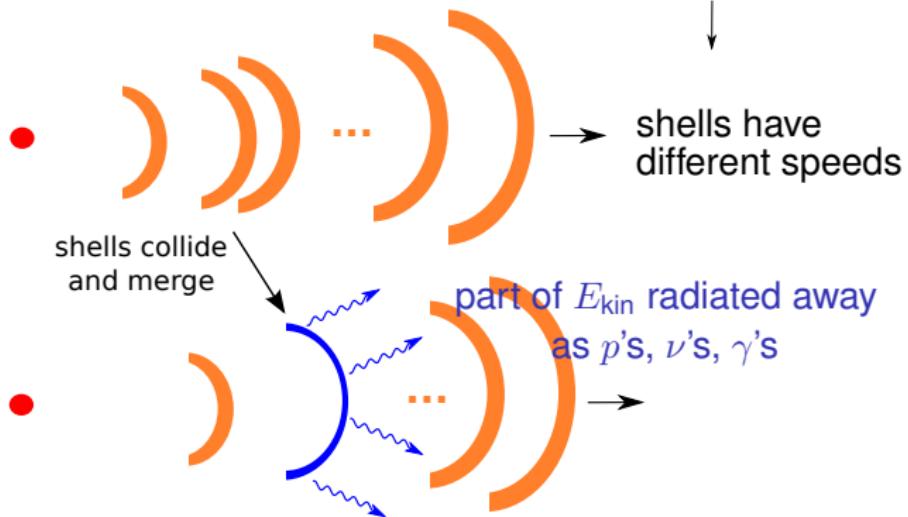
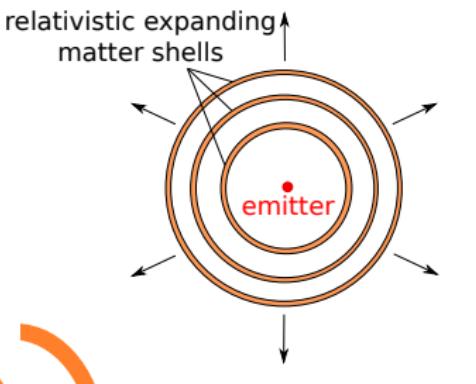
Go beyond the simplest UHECR-neutrino connection

Step 3 ( preliminary)

Treat the fireball dynamically (neutrino “light curves”)

# Internal shocks in the fireball model

**Long-duration GRB ( $\geq 2$  s):**  
a compact object ( $\sim 10^3$  km)  
emits relativistically expanding  
**baryonic-loaded** matter ejecta





Up to now, we have assumed that the burst is made up of  $T_{90}/t_v$  identical internal collisions.

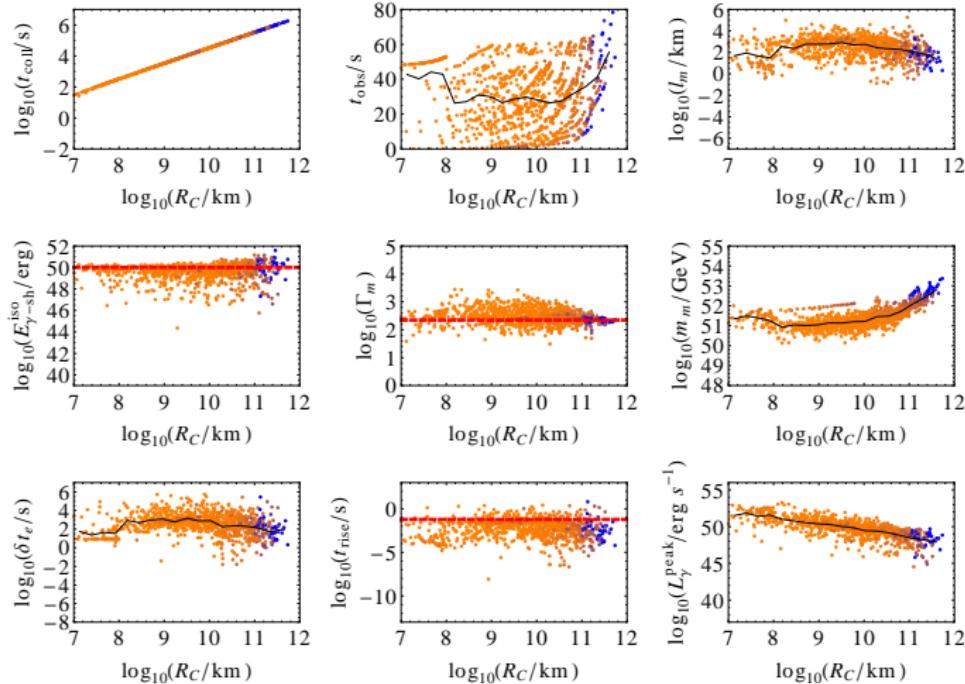
Let us go beyond that:

- 1 Start with  $\sim 1000$  initial baryon-loaded shells, each with a different speed  $\Gamma_i$
- 2 Propagate them until an internal collision occurs
- 3 A new merged shell is created, with  $\Gamma_m \simeq \sqrt{\Gamma_s \Gamma_f}$ ; it continues moving
- 4 Part of the kinetic energy of the former shells is radiated away as gamma-rays, protons, and neutrinos
- 5 Continue until there are no more shells left to collide, or the ISM is reached

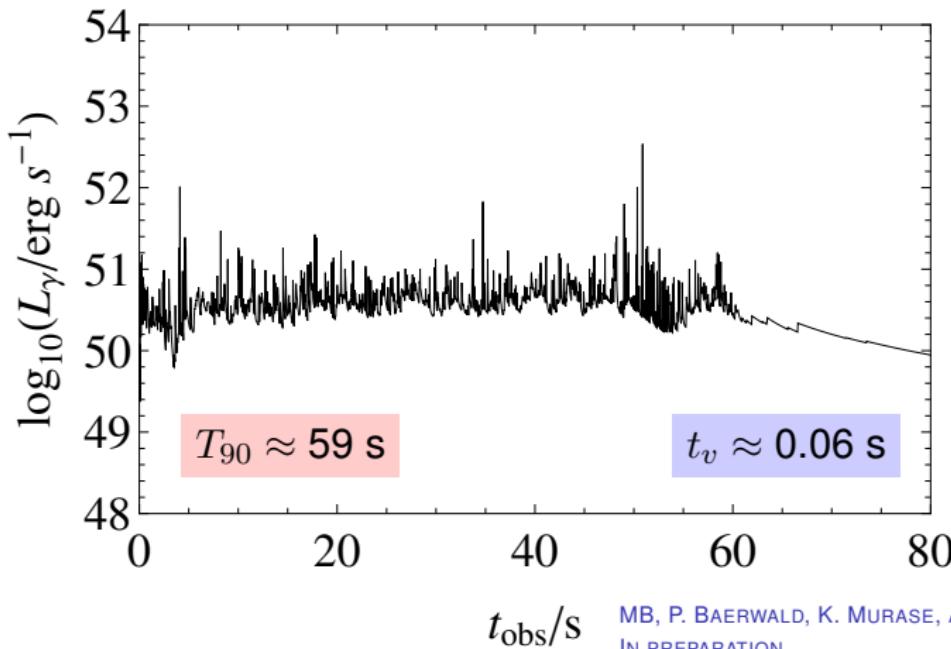
S. KOBAYASHI, T. PIRAN, AND R. SARI, *ApJ* **490**, 92 (1997)

F. DAIGNE AND R. MOCHKOVITCH, *MNRAS* **296**, 275 (1998)

We can track how the parameters change with collision radius:

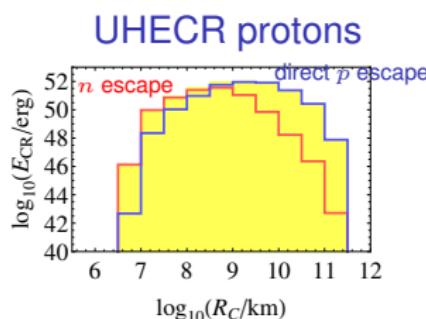
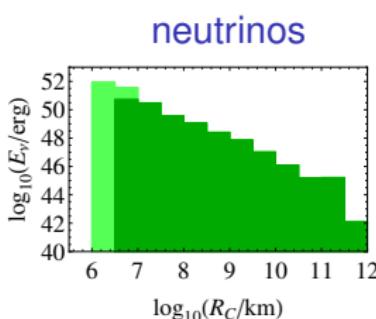
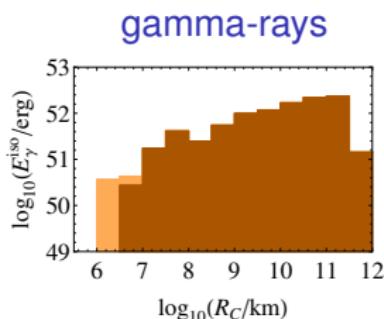


A fast-rise-exponential-decay (FRED) pulse is assigned to each collision; their superposition yields a **synthetic light curve**:



$t_{\text{obs}}/\text{s}$  MB, P. BAERWALD, K. MURASE, AND W. WINTER,  
IN PREPARATION

The gamma-ray, neutrino, and proton emission peak at different collision radii:

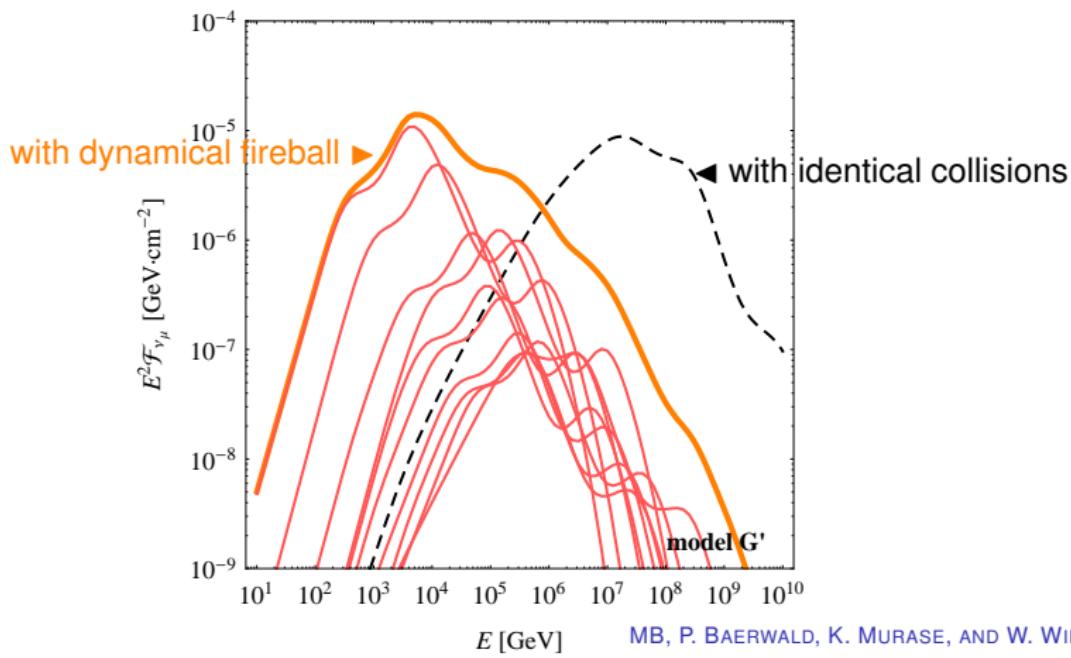


MB, P. BAERWALD, K. MURASE, AND W. WINTER, IN PREPARATION

- ▶ **Light colours:** sub-photospheric collisions
- ▶ Total gamma-ray emission normalised to  $E_{\gamma-\text{tot}}^{\text{iso}} = 10^{53}$  erg

As the burst expands, the photon and proton densities fall, and this affects the relative emission of the different particle species

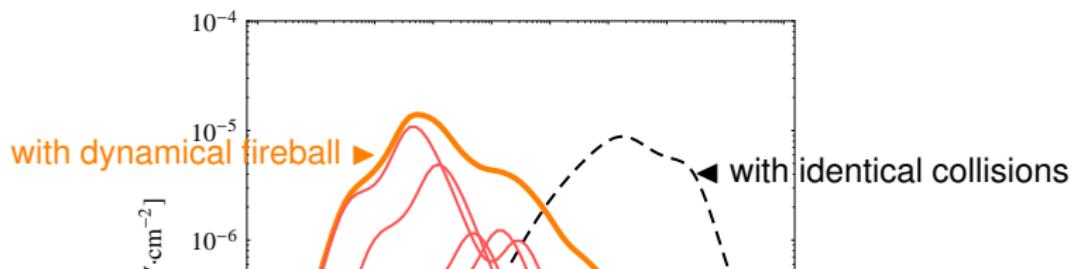
Total  $\nu$  fluence of the burst built up from the individual collisions:



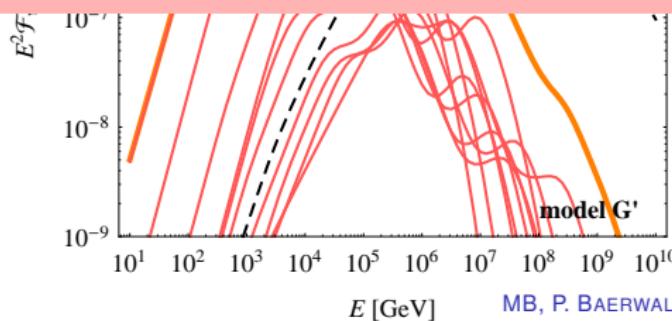
MB, P. BAERWALD, K. MURASE, AND W. WINTER,  
IN PREPARATION

The prompt  $\nu$  emission peaks at energies  $\ll$  the typical  $\sim \text{PeV}$ !

Total  $\nu$  fluence of the burst built up from the individual collisions:



We might be looking for neutrinos in the wrong energies ...



MB, P. BAERWALD, K. MURASE, AND W. WINTER,  
IN PREPARATION

The prompt  $\nu$  emission peaks at energies  $\ll$  the typical  $\sim$  PeV!



We have revised the GRB neutrino predictions of  $\nu$  emission:

- 1 Refine the  $\nu$  yields from  $p\gamma$  interactions
  - ▶ corrected, full numerical calculation with detailed particle physics
  - ▶ quasi-diffuse flux  $\sim 1$  order magnitude below analytical one by IceCube
- 2 Go beyond the neutron model of UHECR-neutrino production
  - ▶ the standard  $n$  escape component, plus a direct  $p$  escape component
  - ▶ prompt  $\nu$  flux affected; cosmogenic  $\nu$  flux not much
  - ▶ fits to UHECR observations yield values of baryonic loading
  - ▶ IceCube bounds exclude large parts of parameter space
- 3 Dynamical fireball model
  - ▶ track burst parameters as the fireball expands
  - ▶ photon, proton, and neutrino emissions peak at different radii
  - ▶ total neutrino fluence peaks at lower energies ( $\ll$  PeV)

The current (IceCube, ANTARES) and upcoming (KM3NeT, IceCube+) experiments force us to refine our predictions



# Backup slides

UHE  $\nu$ 's in the GRB internal shock modelSecondary injection of neutrons, neutrinos ( $\text{GeV}^{-1} \text{ cm}^{-3} \text{ s}^{-1}$ )

$$Q' (E') = \int_{E'}^{\infty} \frac{dE'_p}{E'_p} N'_p (E'_p) \int_0^{\infty} c d\varepsilon' N'_{\gamma} (\varepsilon') R (E', E'_p, \varepsilon')$$

Normalisation to the observed GRB photon flux  $F_{\gamma}$ 

$$\int \varepsilon' N'_{\gamma} (\varepsilon') d\varepsilon' = \frac{E'_{\text{iso}}^{\text{sh}}}{V'_{\text{iso}}} \propto F_{\gamma}, \quad \int E'_p N'_p (E'_p) dE'_p = \frac{1}{f_e} \frac{E'_{\text{iso}}^{\text{sh}}}{V'_{\text{iso}}} \propto \frac{F_{\gamma}}{f_e}$$

Fluence per shell, at Earth ( $\text{GeV}^{-1} \text{ cm}^{-2}$ )

$$\mathcal{F}^{\text{sh}} = t_v V'_{\text{iso}} \frac{(1+z)^2}{4\pi d_L^2} Q'$$

Secondary injection of neutrons, neutrinos ( $\text{GeV}^{-1} \text{ cm}^{-3} \text{ s}^{-1}$ )

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► Photon density, shock rest frame ( $\text{GeV}^{-1} \text{ cm}^{-3}$ ):

$$N'_\gamma (\varepsilon') \propto \begin{cases} (\varepsilon')^{-\alpha_\gamma}, & \varepsilon'_{\gamma,\min} = 0.2 \text{ eV} \leq \varepsilon' \leq \varepsilon'_{\gamma,\text{break}} \\ (\varepsilon')^{-\beta_\gamma}, & \varepsilon'_{\gamma,\text{break}} \leq \varepsilon' \leq \varepsilon'_{\gamma,\max} = 300 \times \varepsilon'_{\gamma,\min} \end{cases}$$

$$\varepsilon'_{\gamma,\text{break}} = \mathcal{O}(\text{keV}), \alpha_\gamma \approx 1, \beta_\gamma \approx 2$$

► Proton density:

$$N'_p (E'_p) \propto (E'_p)^{-\alpha_p} \times \exp \left[ - \left( E'_p / E'_{p,\max} \right)^2 \right] \quad (\alpha_p \approx 2)$$

Maximum proton energy limited by energy losses:

$$t'_{\text{acc}} (E'_{p,\max}) = \min [t'_{\text{dyn}}, t'_{\text{syn}} (E'_{p,\max}), t'_{p\gamma} (E'_{p,\max})]$$

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UHE  $\nu$ 's in the GRB internal shock model

Secondary injection of neutrons, neutrinos ( $\text{GeV}^{-1} \text{ cm}^{-3} \text{ s}^{-1}$ )

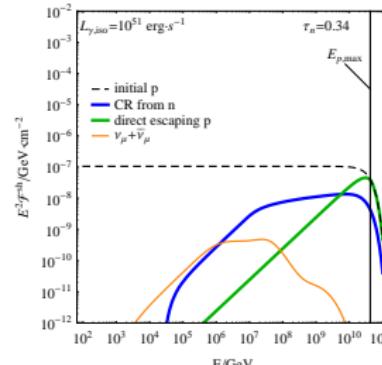
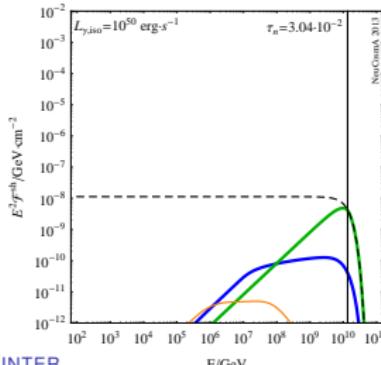
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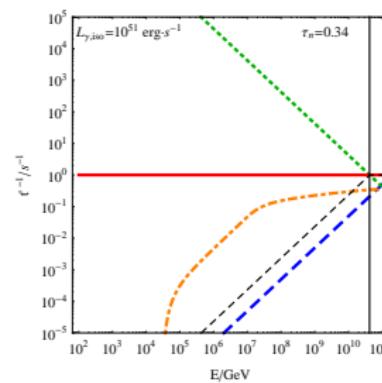
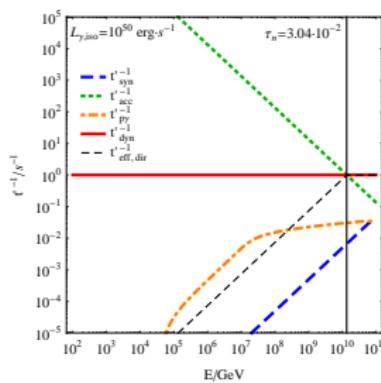
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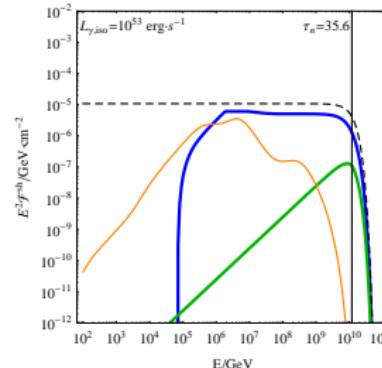
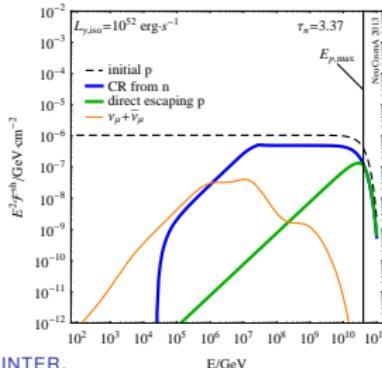
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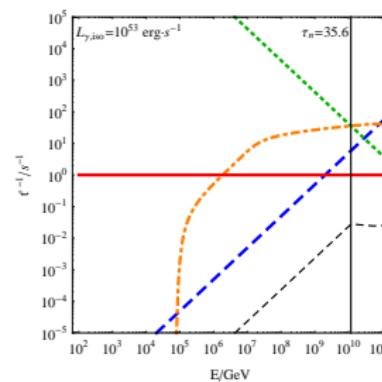
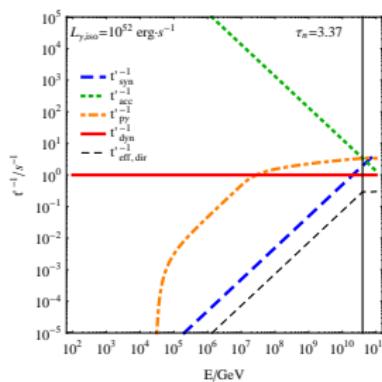
Optically **thin** sources ( $\tau_n < 1$ ):

P. BAERWALD, MB, W. WINTER,  
*ApJ* 768, 186 (2013)



Optically **thick** sources ( $\tau_n > 1$ ):

P. BAERWALD, MB, W. WINTER,  
*ApJ* 768, 186 (2013)



### Optically thin to neutron escape regime

- ▶ the standard emission scenario
- ▶  $p$ 's magnetically confined:  $n$ 's and  $\nu$ 's from  $p\gamma$  interactions
- ▶  $n$ 's escape and decay to produce UHECRs

### Direct escape regime

- ▶ directly-escaping  $p$ 's from the borders dominate
- ▶ subdominant  $n$  production
- ▶ more CRs emitted, so “one  $\nu_\mu$  per CR” no longer valid

### Optically thick to neutron escape regime

- ▶  $n$ 's and  $p$ 's in the bulk trapped by multiple  $p\gamma$  interactions
- ▶ they only escape from the borders
- ▶  $\nu$  production enhanced

- ▶ Energy loss rate ( $\text{GeV s}^{-1}$ ):

$$b(E) \equiv \frac{dE}{dt}$$

- ▶ For pair production  $p\gamma \rightarrow pe^+e^-$ :

$$b_{e^+e^-}(E, z) = -\alpha r_0^2 (m_e c^2)^2 c \int_2^\infty d\xi n_\gamma \left( \frac{\xi m_e c^2}{2\gamma}, z \right) \frac{\phi(\xi)}{\xi^2}$$

- ▶  $n_\gamma$ : isotropic photon background ( $\text{GeV}^{-1} \text{ cm}^{-3}$ )
- ▶  $\xi$ : photon energy in units of  $m_e c^2$
- ▶ proton energy:  $E = \gamma m_p c^2$  ( $\gamma \gg 1$ )
- ▶  $\phi(\xi)$ : (tabulated) integral in energy of outgoing  $e^-$

G. BLUMENTHAL, *Phys. Rev.* **D 1**, 1596 (1970)

H. BETHE, W. HEITLER, *Proc. Roy. Soc.* **A146**, 83 (1934)

# Interaction with the photon backgrounds

Photohadronic interactions –  $p\gamma$  interaction rate ( $\text{s}^{-1}$  per particle):

$$\Gamma_{p\gamma \rightarrow p'b}(E, z) = \frac{1}{2} \frac{m_p^2}{E^2} \int_{\epsilon_{\text{th}} m_p / 2E}^{\infty} d\epsilon \frac{n_{\gamma}(\epsilon, z)}{\epsilon^2} \int_{\epsilon_{\text{th}}}^{2E\epsilon/m_p} d\epsilon_r \epsilon_r \sigma_{p\gamma \rightarrow p'b}^{\text{tot}}(\epsilon_r)$$

- For given values of  $E$  and  $z$ , NeuCosmA calculates the cooling rate  $t_{p\gamma}^{-1} \equiv - (1/E) b_{p\gamma} (\text{s}^{-1})$  as

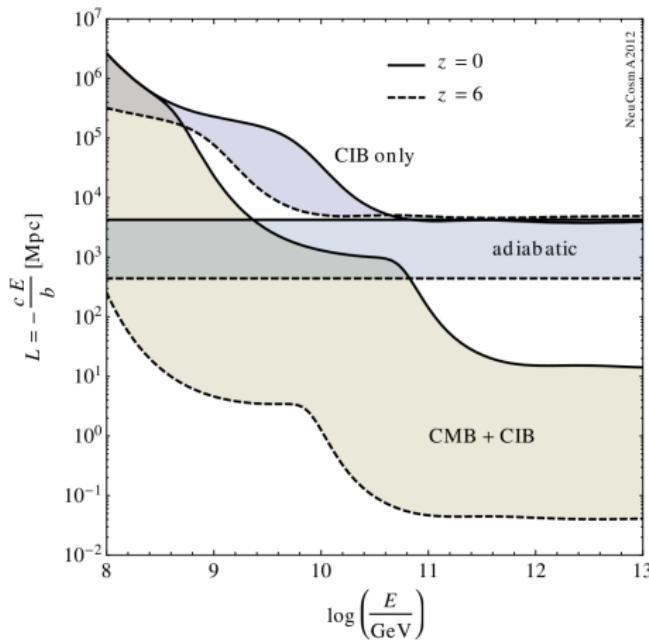
$$t_{p\gamma}^{-1}(E, z) = \sum_i^{\text{all channels}} \Gamma_{p \rightarrow p}^i(E, z) K^i,$$

with  $K^i E$  the loss of energy per interaction

- From this, we calculate back  $b_{p\gamma} (\text{GeV s}^{-1}) \dots$
- $\dots$  and the corresponding energy-loss term in the transport equation,  $\partial_E(b_{p\gamma} Y_p)$ .

S. HÜMMER, M. RÜGER, F. SPANIER, W. WINTER, *Astrophys. J.* **721**, 630 (2010) [1002.1310]

Note that  $L_{\text{CIB}} \gg L_{\text{CMB}}$ :



Matches, e.g., H. TAKAMI, K. MURASE, S. NAGATAKI, K. SATO, *Astropart. Phys.* **31**, 201 (2009) [0704.0979]

Comoving source density:  $\dot{\rho}_{\text{CR}}(z) [\text{Mpc}^{-3} \text{ yr}^{-1}]$

$\mathcal{H}$ : normalised to the local rate, i.e.,  $\mathcal{H}(z) \equiv \dot{\rho}_{\text{CR}}(z) / \dot{\rho}_{\text{CR}}(0)$

$$\mathcal{H}_{\text{SFR}}(z) = \begin{cases} (1+z)^{3.4} & , z < 1, \\ N_1 (1+z)^{-0.3} & , 1 \leq z < 4 , \quad \mathcal{H}_{\text{GRB}}(z) = (1+z)^\alpha \mathcal{H}_{\text{SFR}}(z) \\ N_1 N_4 (1+z)^{-3.5} & , z \geq 4 \end{cases}$$

