



Neutrino in Cosmology

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Plan

I. Neutrino decoupling

II. Relativistic neutrinos

- Impact on background evolution
- Relativistic neutrino perturbations
- Effects of N_{eff} on CMB and LSS
- Measuring N_{eff}

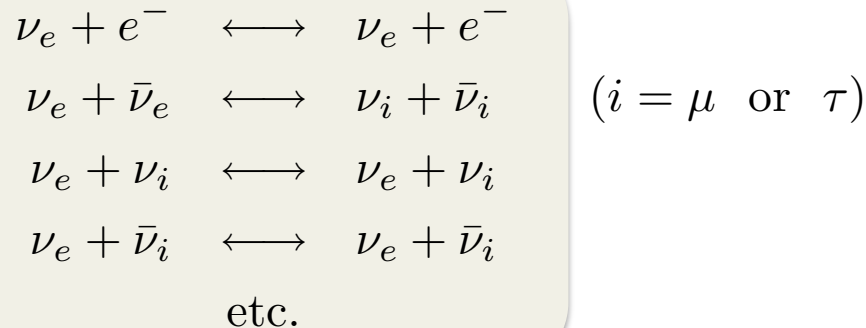
III. Non-relativistic neutrinos

- Impact on background evolution
- Non-relativistic neutrino perturbations
- Effects of masses on CMB and LSS
- Measuring masses (current bounds, future sensitivity)

IV. Other constraints on neutrinos from cosmology

I. Neutrino decoupling

- For $T \sim 10$ MeV:
 - Thermal bath: $\gamma, p, n, e^+, e^-, \{\nu_e, \nu_\mu, \nu_\tau, \bar{\nu}_e, \bar{\nu}_\mu, \bar{\nu}_\tau\}$
 - DM particle
 - All other particles should have decayed when $T \sim m_i$
 - Neutrinos kept in thermal equilibrium through elastic/inelastic weak interactions:



- Exchange of W/Z bosons

I. Neutrino decoupling

- For $T \sim 1$ MeV:
 - thermally averaged cross-section $\langle \sigma v \rangle \sim G_F^2 T^2$
 - Interaction rate $\Gamma = n_{e^-} \langle \sigma v \rangle \sim G_F^2 T^5$
 - Expansion rate $H^2 \sim M_P^{-2} T^4$
 - Ratio $\frac{\Gamma}{H} \sim M_P G_F^2 T^3 \sim \left(\frac{T}{1 \text{ MeV}} \right)^3$
- Decoupling near 1 MeV, then phase-space distributions frozen very close to

$$f_i(p) = \frac{1}{\exp[p/T_\nu] + 1}$$

with $T_\nu \sim a^{-1}$

- Tiny flavor-dependent corrections (e^+e^- annihilation, finite-temperature QED, flavor mixing)

I. Neutrino decoupling

- For $T < 1$ MeV:
 - T_ν scales like a^{-1} but T_γ doesn't ($e^+ + e^- \longrightarrow \gamma + \gamma$)
 - Entropy conservation throughout electron-positron annihilation:
 - Before : $T_\nu = T_\gamma \sim a^{-1}$
 - After : $T_\nu = (4/11)^{1/3} T_\gamma \sim a^{-1}$
 - Given $T_\gamma = 2.726$ K, we know the current neutrino number density

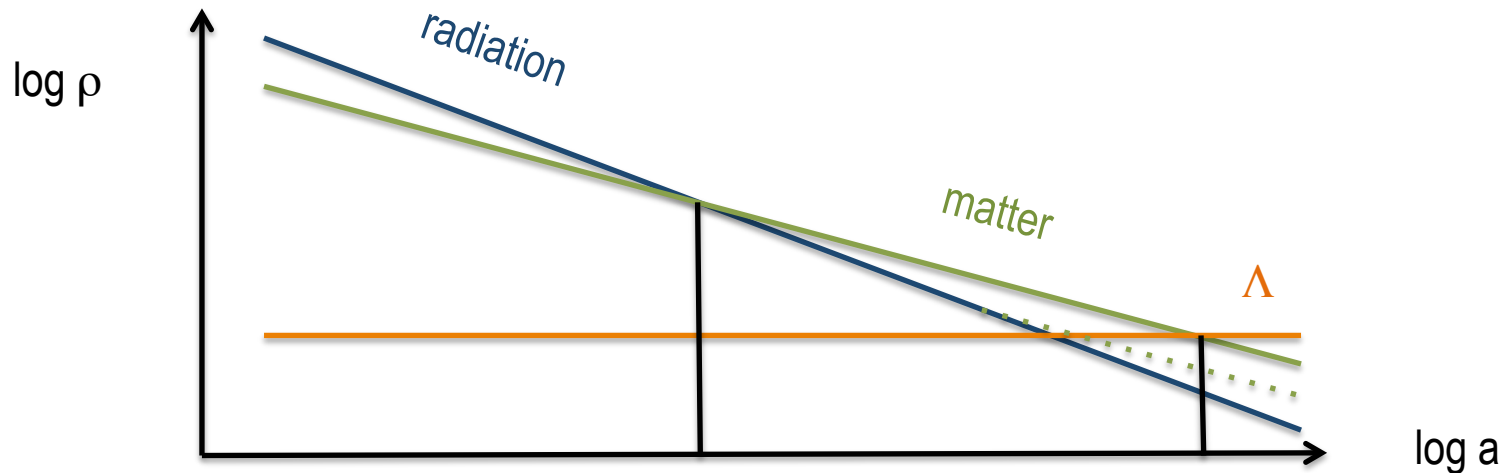
$$n_{\nu_i} = \frac{3}{4} \frac{\zeta(3)}{\pi^2} T_\nu^3 = 56 \text{ cm}^{-3} \quad (\text{for all 6 neutrinos: } 336 \text{ cm}^{-3})$$

- Independent of Majorana/Dirac
- Oscillations irrelevant after decoupling due to nearly equal distributions

I. Neutrino decoupling

- Beyond standard model:
 - Distribution can be modified by neutrino-antineutrino asymmetry (chemical potential). If large flavor-dependent asymmetry, then oscillations become important.
 - Non-thermal enhancement due to decay of unstable particle after neutrino decoupling (e.g. Majoron)
 - Overall suppressed, non-thermal distribution for low-temperature reheating
 - Extra population of sterile neutrinos (thermalised or not)

II. Relativistic neutrinos



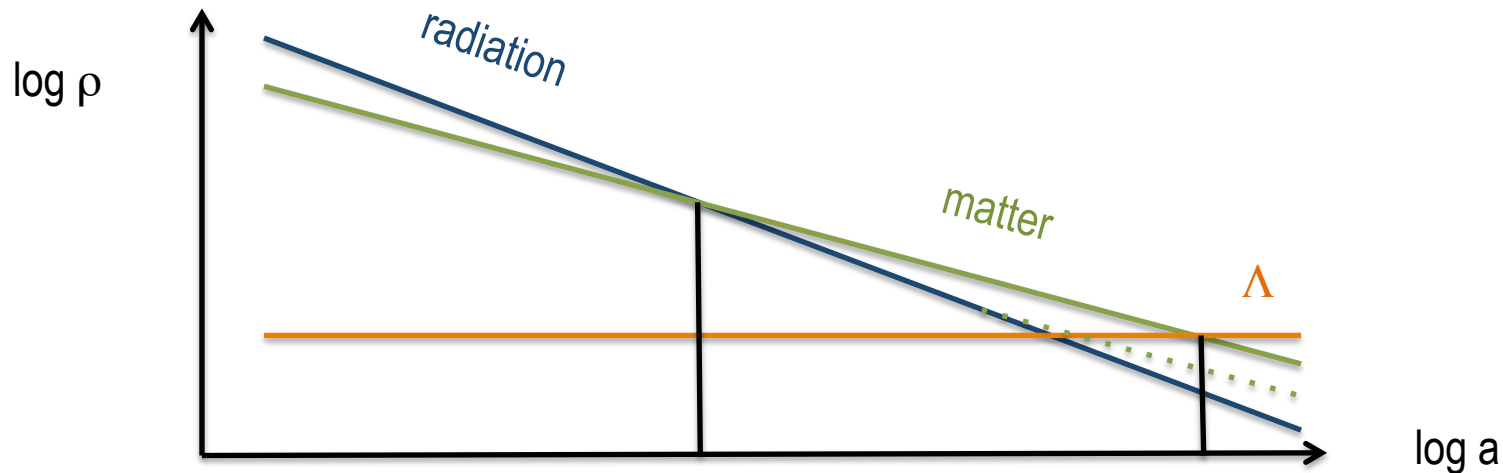
- Background: only $\rho_\nu(a)$ is important

3 standard neutrinos,

Instantaneous decoupling:

$$\rho_R = \rho_\gamma \left(1 + \frac{7}{8} \left(\frac{4}{11} \right)^{4/3} 3 \right).$$

II. Relativistic neutrinos



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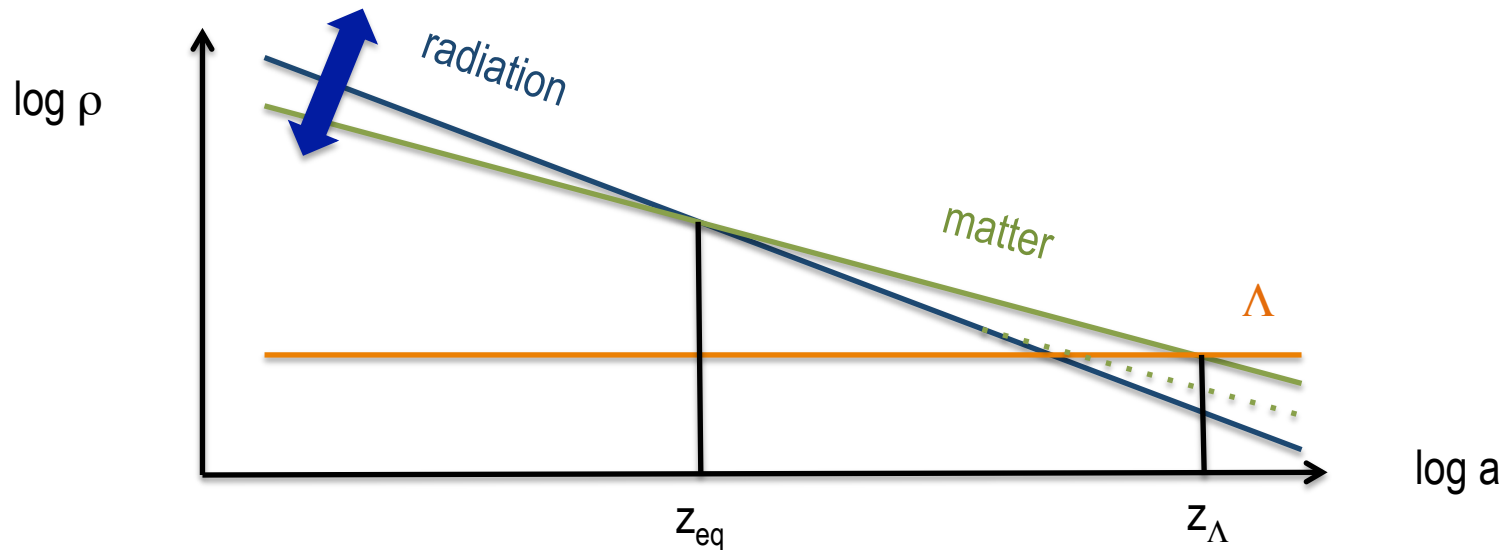
Instantaneous decoupling:

$$\rho_R = \rho_\gamma \left(1 + \frac{7}{8} \left(\frac{4}{11} \right)^{4/3} \textcircled{3} \right) \rightarrow N_{\text{eff}}$$

(= 3.046 in standard model)

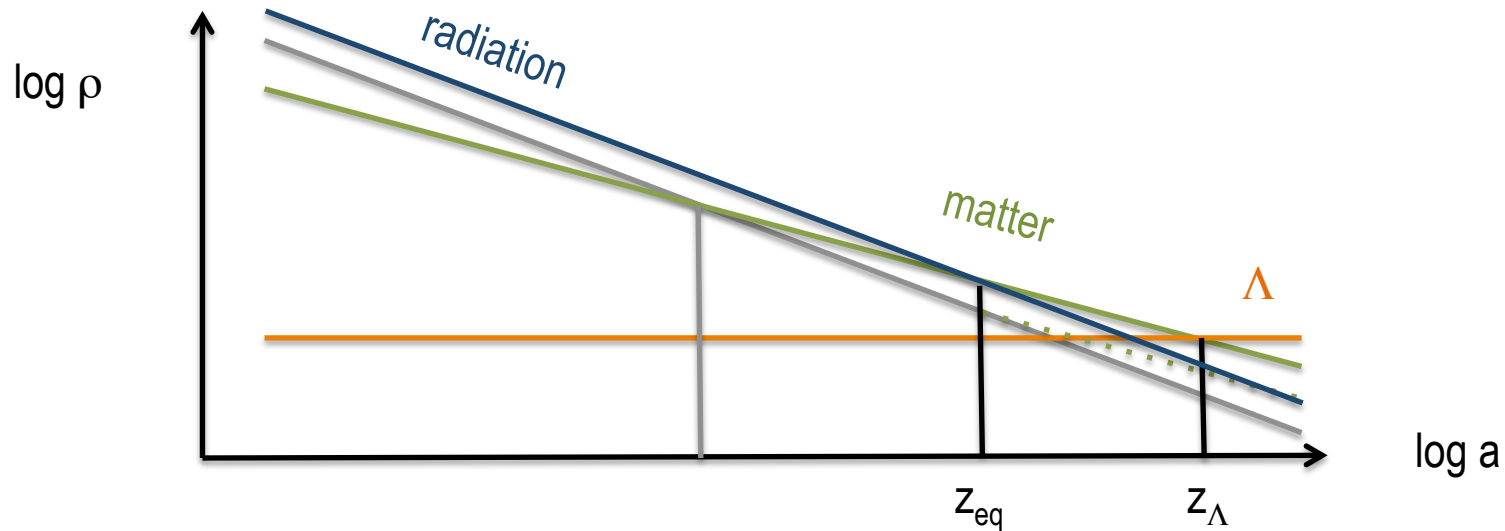
II. Increasing N_{eff}

- Different background evolution affects CMB and LSS power spectrum



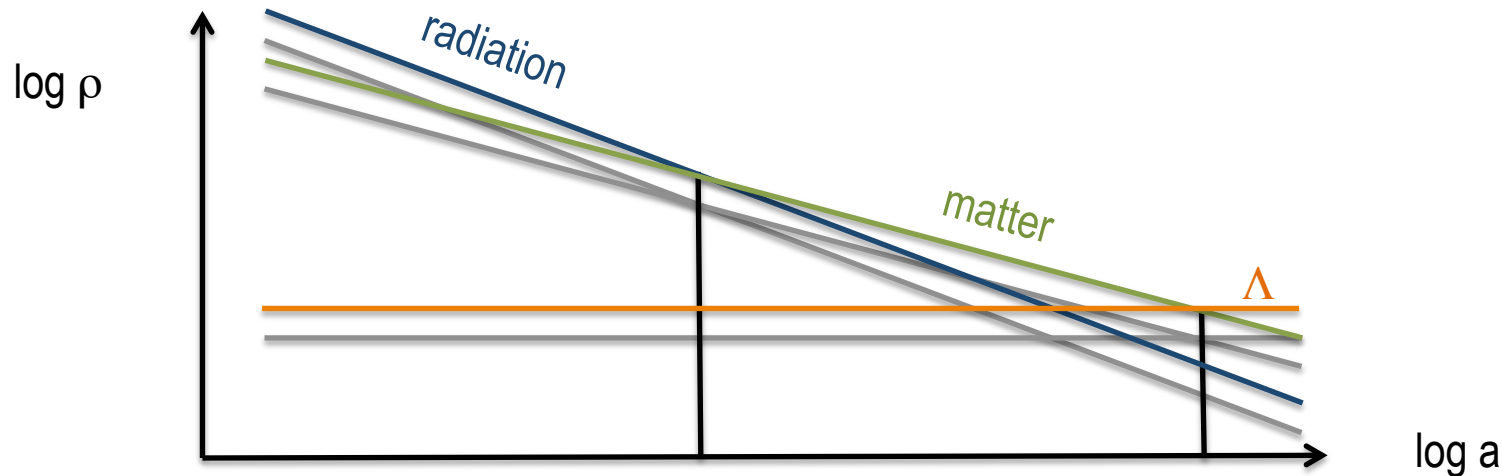
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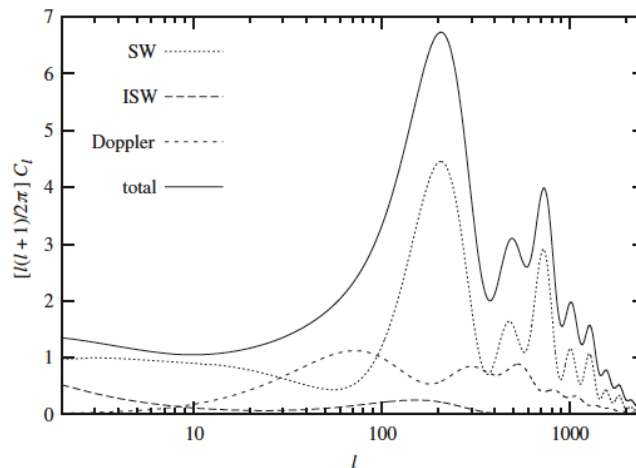
- Different background evolution affects CMB and LSS power spectrum



- Keeping Ω_i fixed and increasing H_0 , N_{eff} preserves characteristic redshifts
- Positive correlation between H_0 , N_{eff}

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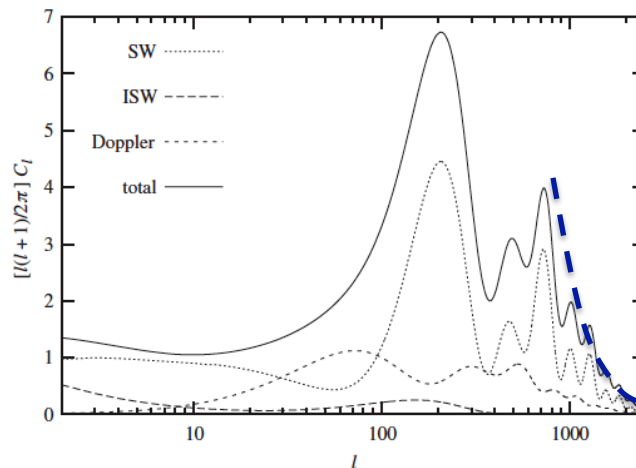
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- Sound horizon at decoupling $\sim H_0$
- Angular diameter distance to decoupling $\sim H_0$

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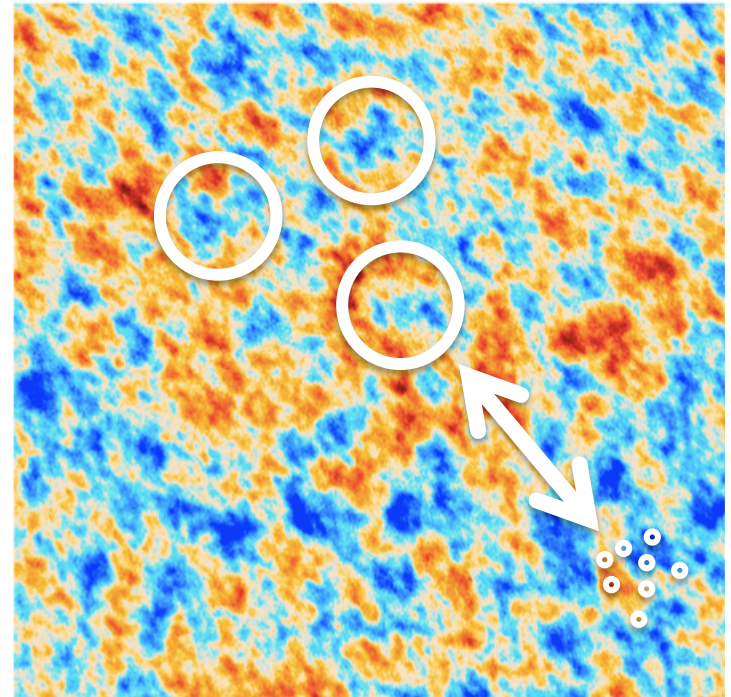
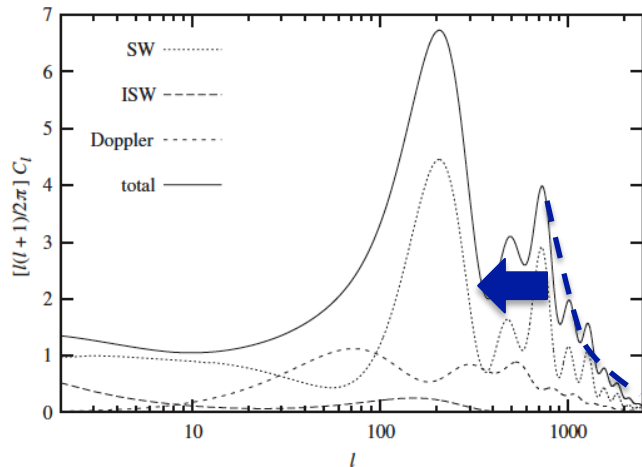


- Sound horizon at decoupling $\sim H_0$
- Angular diameter distance to decoupling $\sim H_0$
- Silk damping scale at decoupling $\sim H_0^2$

II. Increasing N_{eff}

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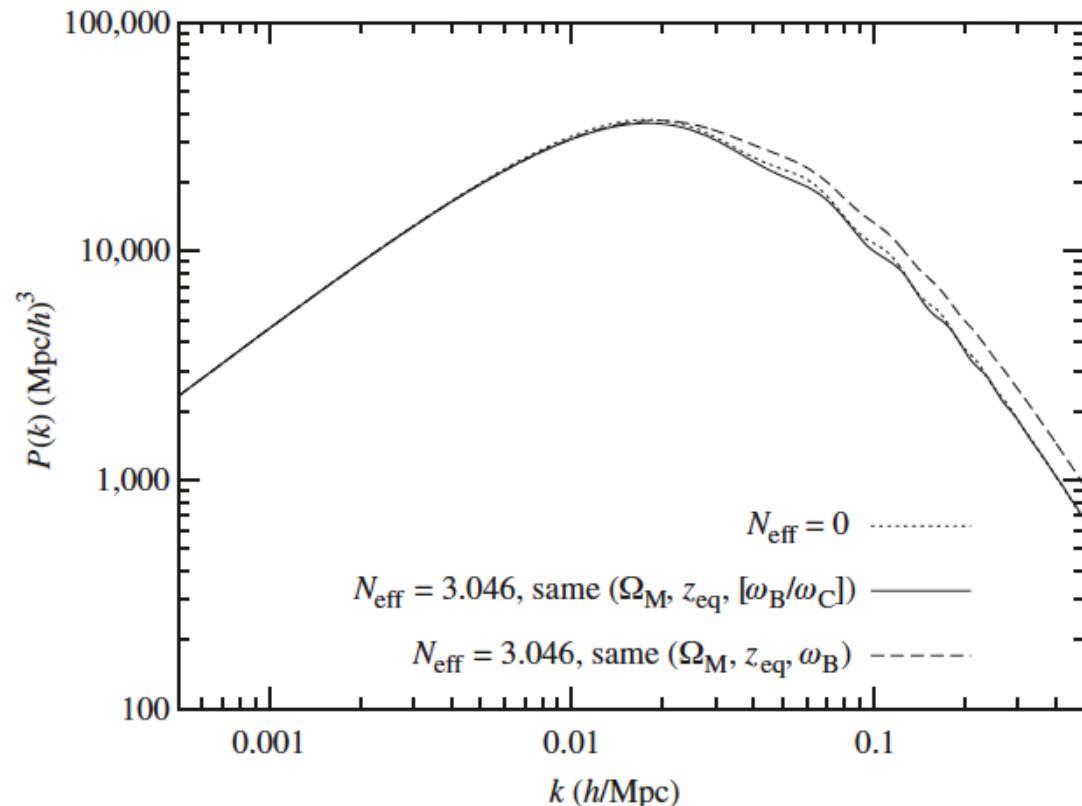
Shift in damping scale relative to peak scale
(larger N_{eff} , more damping)



II. Increasing N_{eff}

- Keeping Ω_i fixed and increasing H_0 , N_{eff} preserves characteristic redshifts
- Positive correlation between H_0 , N_{eff}

But in matter spectrum,
in Fourier space,
shift in sound horizon
visible in BAO scale



II. Perturbations of relativistic neutrinos

- Motivation: gravitational interactions between neutrinos and photons, baryons, cdm

- PSD perturbation $\Psi_v(\eta, \vec{x}, y, \hat{n}) = \frac{f_v(\eta, \vec{x}, y, \hat{n})}{f_{v0}(\eta, y)} - 1$
- Boltzmann in real space $\Psi'_v + \frac{y}{\epsilon} \hat{n} \cdot \vec{\nabla} \Psi_v + \frac{d \ln f_{v0}}{d \ln y} \left[\phi' - \frac{\epsilon}{y} \hat{n} \cdot \vec{\nabla} \psi \right] = 0$
- Fourier + Legendre expansion: Boltzmann hierarchy

$$\begin{aligned}\Psi_{v0}' &= -\frac{yk}{\epsilon} \Psi_{v1} - \phi' \frac{d \ln f_{v0}}{d \ln y} \\ \Psi_{v1}' &= \frac{yk}{3\epsilon} (\Psi_{v0} - 2\Psi_{v2}) - \frac{\epsilon k}{3y} \psi \frac{d \ln f_{v0}}{d \ln y} \\ \Psi_{vl}' &= \frac{yk}{(2l+1)\epsilon} [l\Psi_{v(l-1)} - (l+1)\Psi_{v(l+1)}], \quad \forall l \geq 2.\end{aligned}$$

II. Perturbations of relativistic neutrinos

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- Contributions to $T_{\mu\nu}$ in Einstein equations :

$$\delta\rho_\nu = \bar{\rho}_\nu \delta_\nu = 4\pi a^{-4} \int y^2 dy \epsilon f_{\nu 0}(y) \Psi_0$$

$$\delta P_\nu = \frac{4\pi}{3} a^{-4} \int y^2 dy \frac{y^2}{\epsilon} f_{\nu 0}(y) \Psi_0$$

$$(\bar{\rho}_\nu + \bar{P}_\nu) \theta_\nu = 4\pi a^{-4} \int y^2 dy \epsilon f_{\nu 0}(y) \Psi_1$$

$$(\bar{\rho}_\nu + \bar{P}_\nu) \sigma_\nu = 4\pi a^{-4} \int y^2 dy \frac{y^2}{\epsilon} f_{\nu 0}(y) \Psi_2.$$

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Relativistic particles: shift independent of momentum

PSD remains thermal

Everything can be integrated over momentum!

II. Perturbations of relativistic neutrinos

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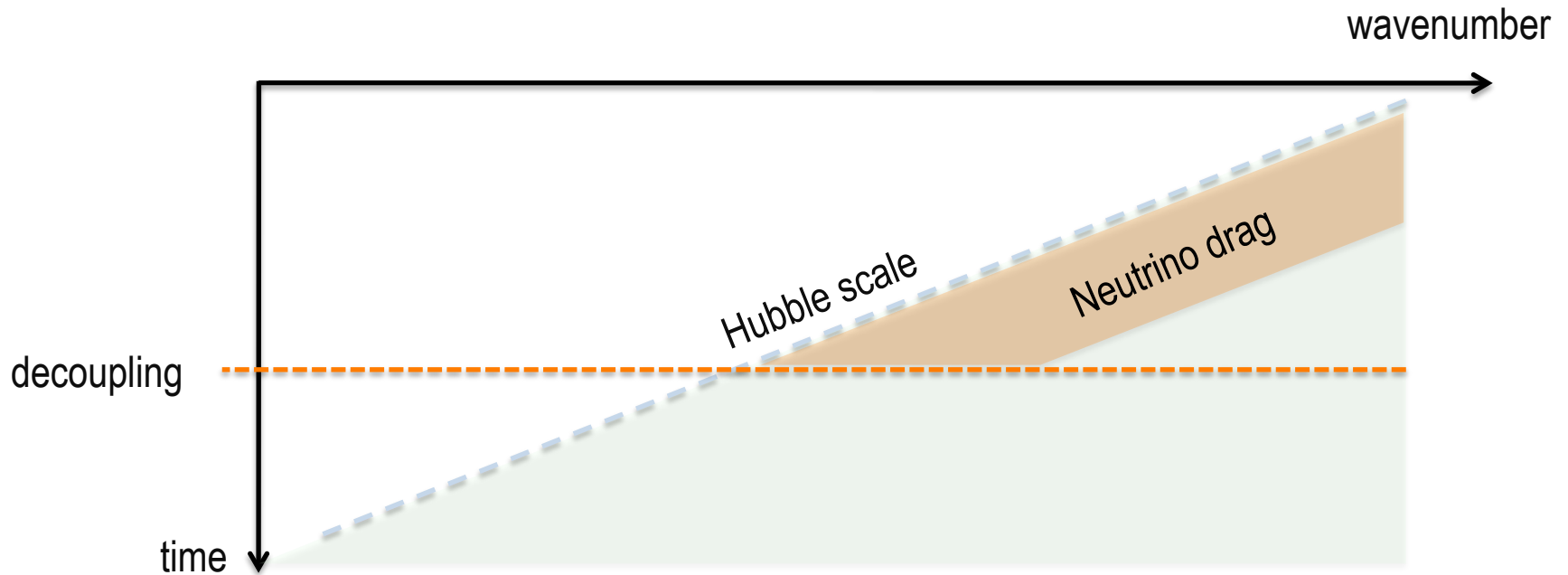
- Boltzmann in Fourier space $F'_\nu + ik\mu F_\nu - 4\phi' - ik\mu 4\psi = 0.$

- Legendre expansion: Boltzmann hierarchy
$$\left\{ \begin{array}{l} F_{\nu 0}' = -k F_{\nu 1} + 4\phi' \\ F_{\nu 1}' = \frac{k}{3} (F_{\nu 0} - 2F_{\nu 2} + 4\psi) \\ F_{\nu l}' = \frac{k}{(2l+1)} [l F_{\nu(l-1)} - (l+1) F_{\nu(l+1)}], \end{array} \right.$$

- Contributions to $T_{\mu\nu}$ $\delta_\nu = F_{\nu 0}, \quad \theta_\nu = \frac{3}{4}k F_{\nu 1}, \quad \sigma_\nu = \frac{1}{2}F_{\nu 2}.$

II. Perturbations of relativistic neutrinos

- N_{eff} increases: more gravitational force ($\delta\rho_{\text{tot}} = \rho_{\nu} \delta_{\nu} + \dots$)
- “neutrino drag”: CMB (and BAO) peaks shifted to larger scales and amplitude reduced



- Summary: CMB and LSS affected through damping tail + shift in peak scale and amplitude. No exact parameter degeneracy with other effects.

II. Measuring N_{eff}

- Ultimately, constraints driven by CMB damping tail
 - WMAP+SPT see anomalously low tail: $N_{\text{eff}} > 3$ at 2 sigma
 - Planck and Planck+BAO well compatible with standard value at 1 sigma
 - Planck (+BAO) + HST : enforce higher H_0 , hence also higher N_{eff}

CMB alone (Planck+WP+HighL)

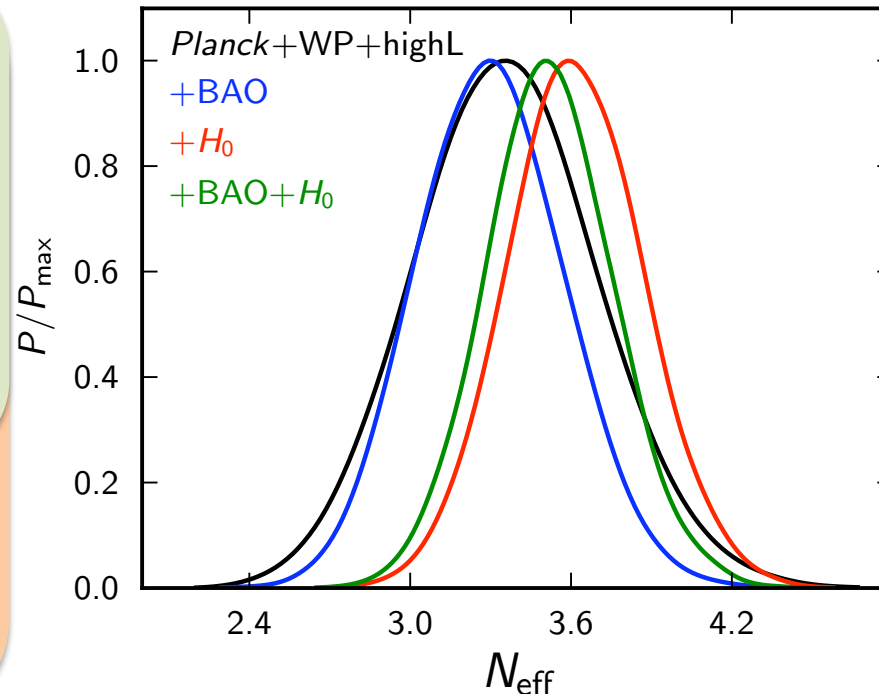
$$N_{\text{eff}} = 3.36 \pm 0.66 \quad (95\% \text{CL})$$

With lensing and BAO:

$$N_{\text{eff}} = 3.30 \pm 0.52 \quad (95\% \text{CL})$$

With H_0 :

$$N_{\text{eff}} = 3.63 \pm 0.49 \quad (95\% \text{CL})$$



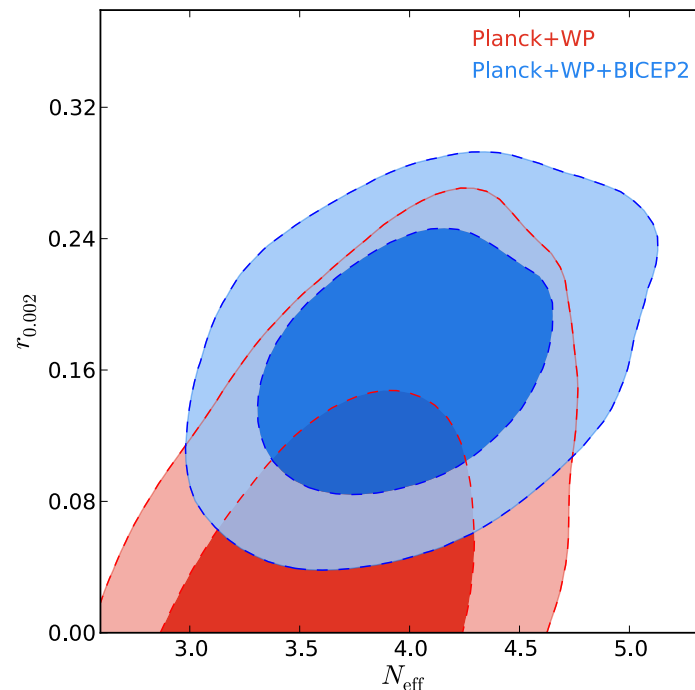
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 - Planck (+BAO) + HST : enforce higher H_0 , hence also higher N_{eff}
 - Planck + BICEP2 : to decrease r tension, also higher N_{eff}

CMB alone (Planck+WP+HighL+BICEP2)

$$N_{\text{eff}} = 4.00 \pm 0.82 \quad (95\% \text{CL})$$

Giusarma et al. 14



Giusarma et al. 1403.4852

II. Future N_{eff} sensitivity

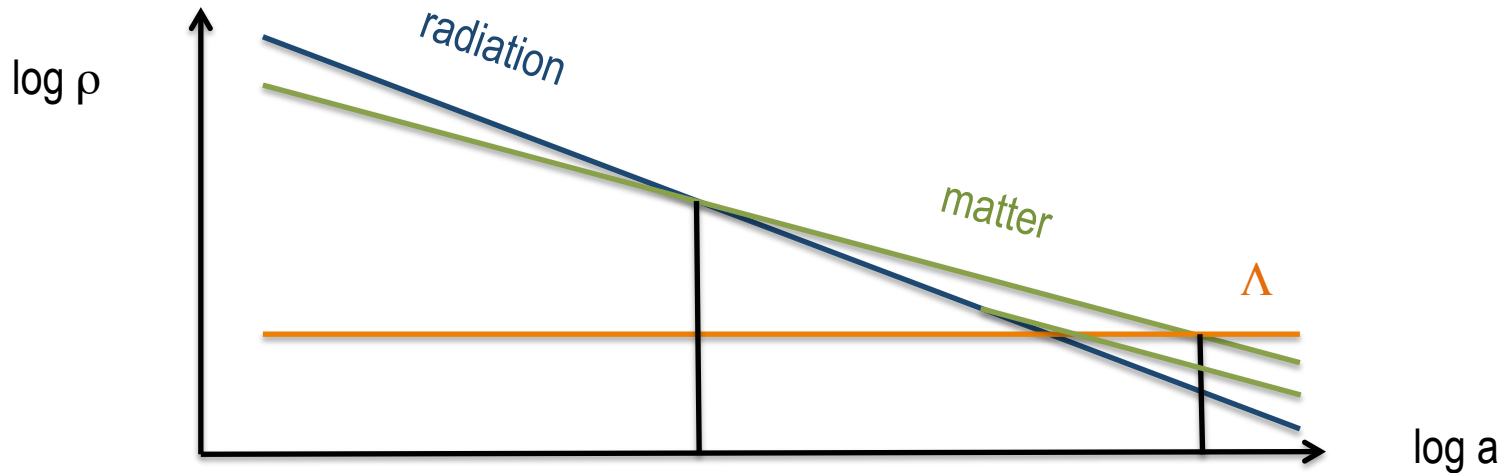
Full Planck data (including lensing) : $\sigma(N_{\text{eff}}) \sim 0.2$ 2014

Planck + LSST, Euclid
(cosmic shear, galaxy correlation) : $\sigma(N_{\text{eff}}) \sim 0.1$ ~ 2022

Post-Planck + Euclid : $\sigma(N_{\text{eff}}) \sim 0.05$ ~ 2030

III. Non-relativistic neutrinos

III. Non-relativistic neutrinos



Non-relativistic transition: $m_\nu = T_\nu \sim (4/11)^{1/3} T_\gamma$, at $z_\nu = (m_\nu/5.3 \text{ eV}) 10^4$

After CMB decoupling for $m_\nu < 0.57 \text{ eV}$ ($M_\nu < 1.7 \text{ eV}$)

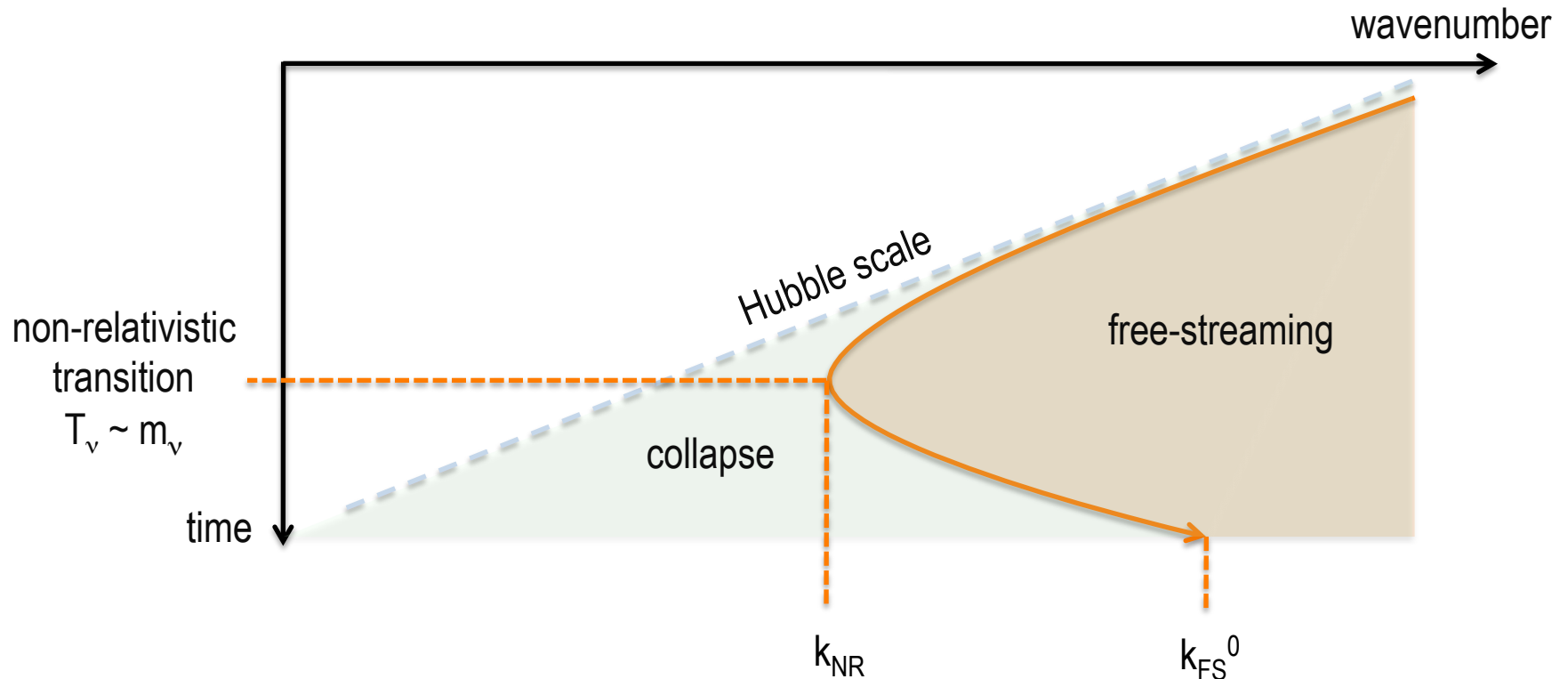
- for fixed $\omega_M = \omega_B + \omega_{\text{CDM}} + \omega_\nu$, change in time of equality
- for fixed $\omega_B + \omega_{\text{CDM}}$ and equality, peak scale affected by $(M_\nu / 0.06 \text{ eV}) \%$
- for fixed equality AND peak scale, effect is on z_Λ

III. Non-relativistic neutrino perturbations

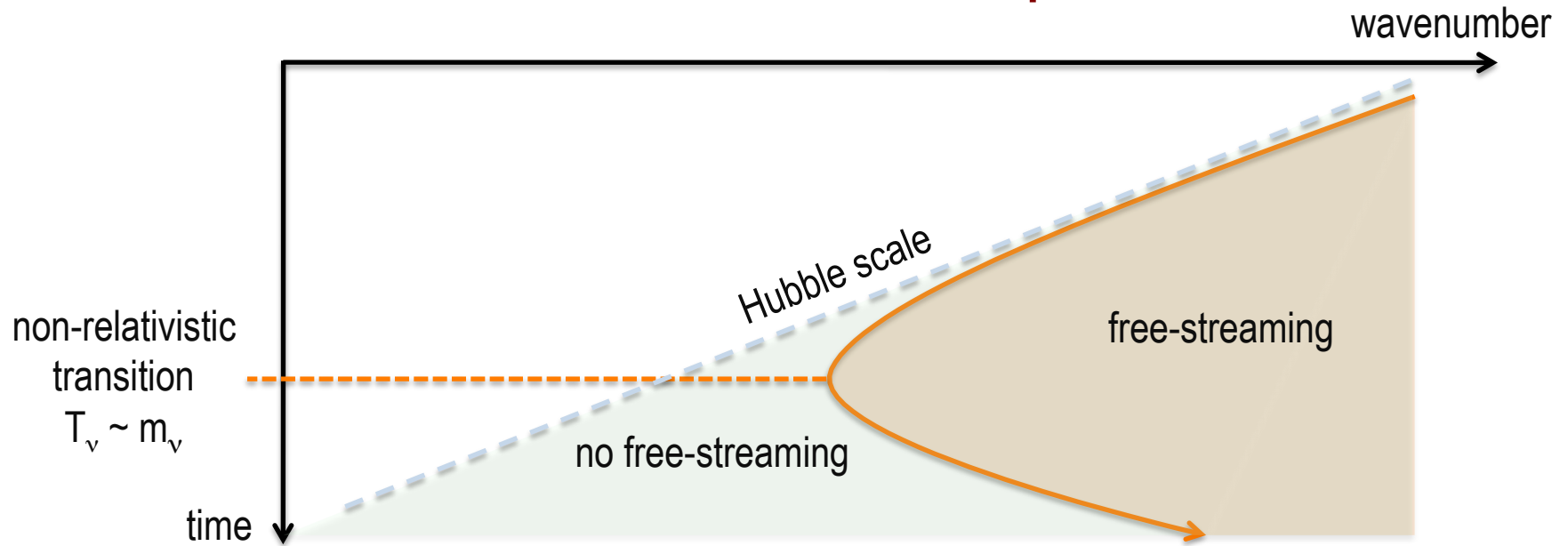
- Non-relativistic regime: importance of free-streaming scale
 - Interacting species with pressure:
 - no gravitational collapse below **Jeans length**
 - $k_J \sim H/c_s$ (sound speed in fluid)
 - Non-interacting species with velocity dispersion:
 - no collapse below **free-streaming length**
 - $k_{FS} \sim H/c_v$ (average particle velocity: $c_v =$ first c , second $\langle p \rangle/m = 3.15 T_v/m_v$)

III. Non-relativistic neutrino perturbations

- Non-relativistic regime: importance of free-streaming scale



III. Non-relativistic neutrino perturbations



- cdm, baryons, neutrino perturbations identical

$$\delta_m'' + H\delta_m' + 3/2H^2 \delta_m = 0$$

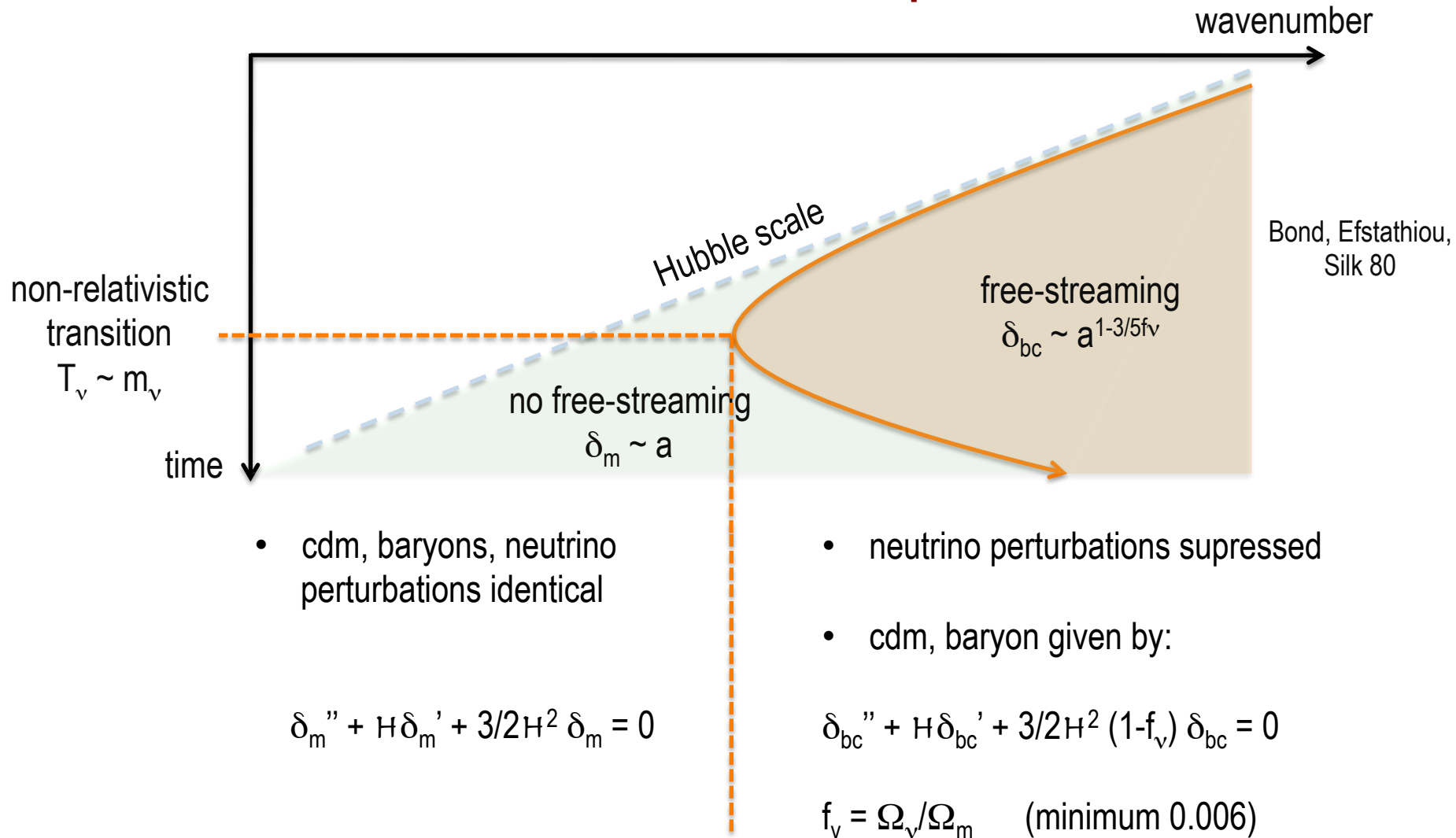
- neutrino perturbations suppressed

- cdm, baryon given by:

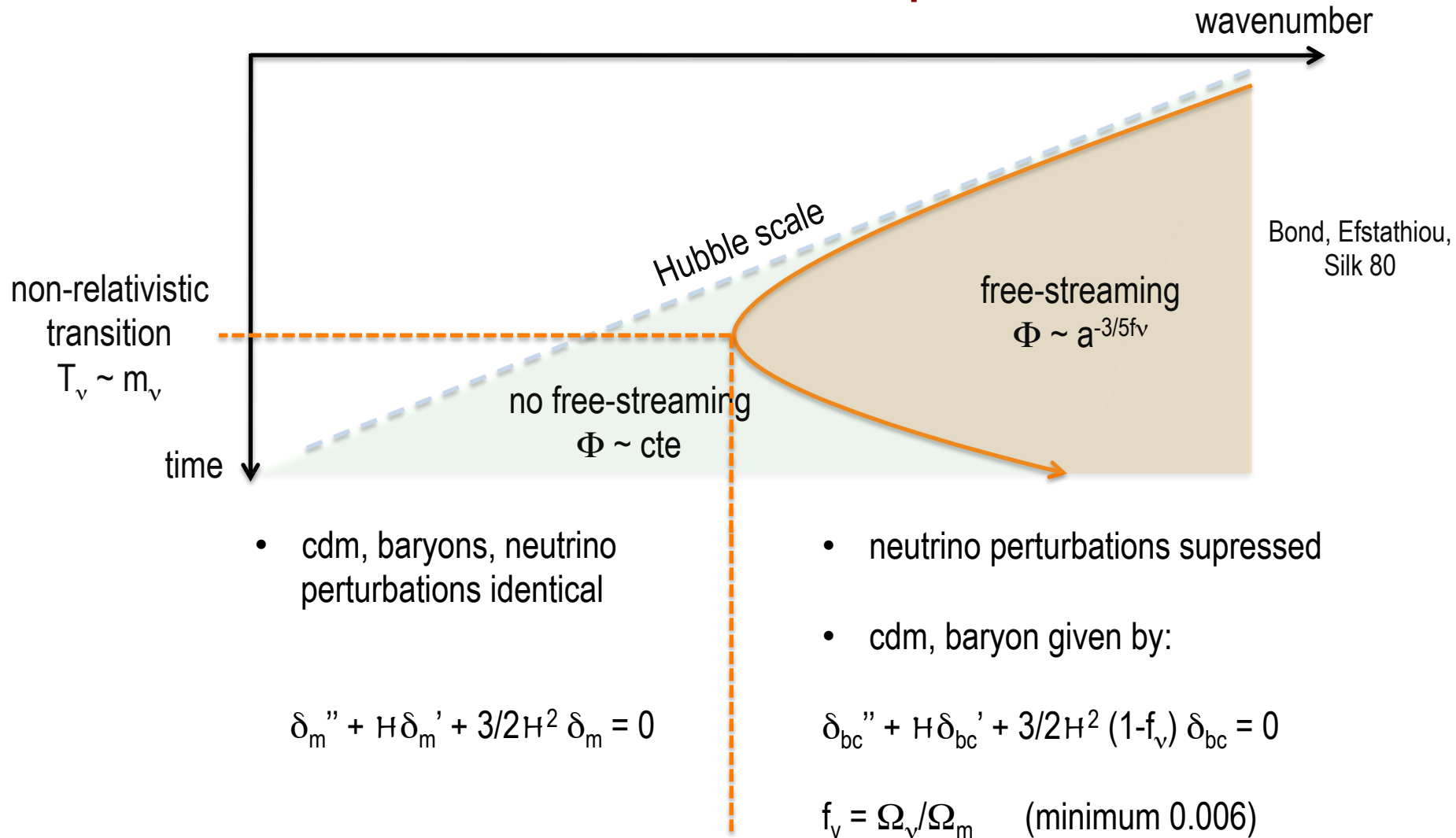
$$\delta_{bc}'' + H\delta_{bc}' + 3/2H^2 (1-f_v) \delta_{bc} = 0$$

$$f_v = \Omega_v/\Omega_m \quad (\text{minimum } 0.006)$$

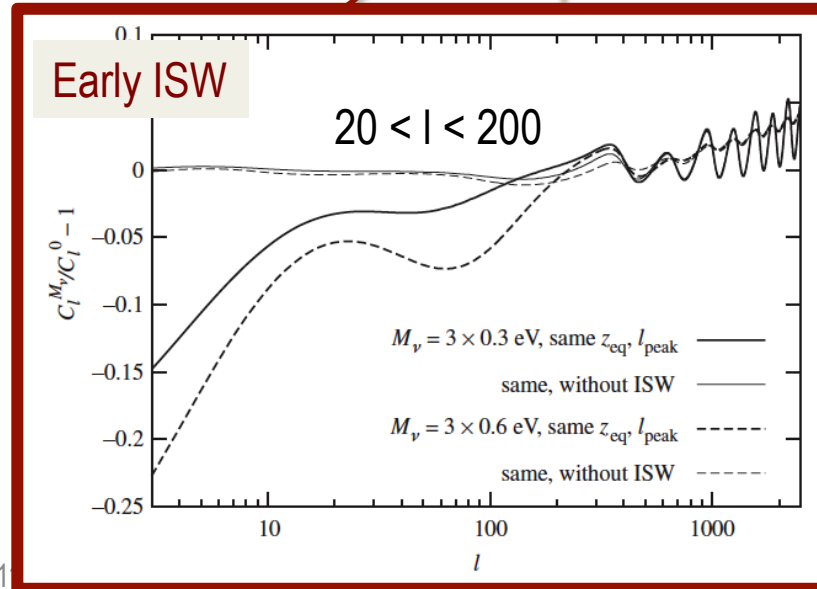
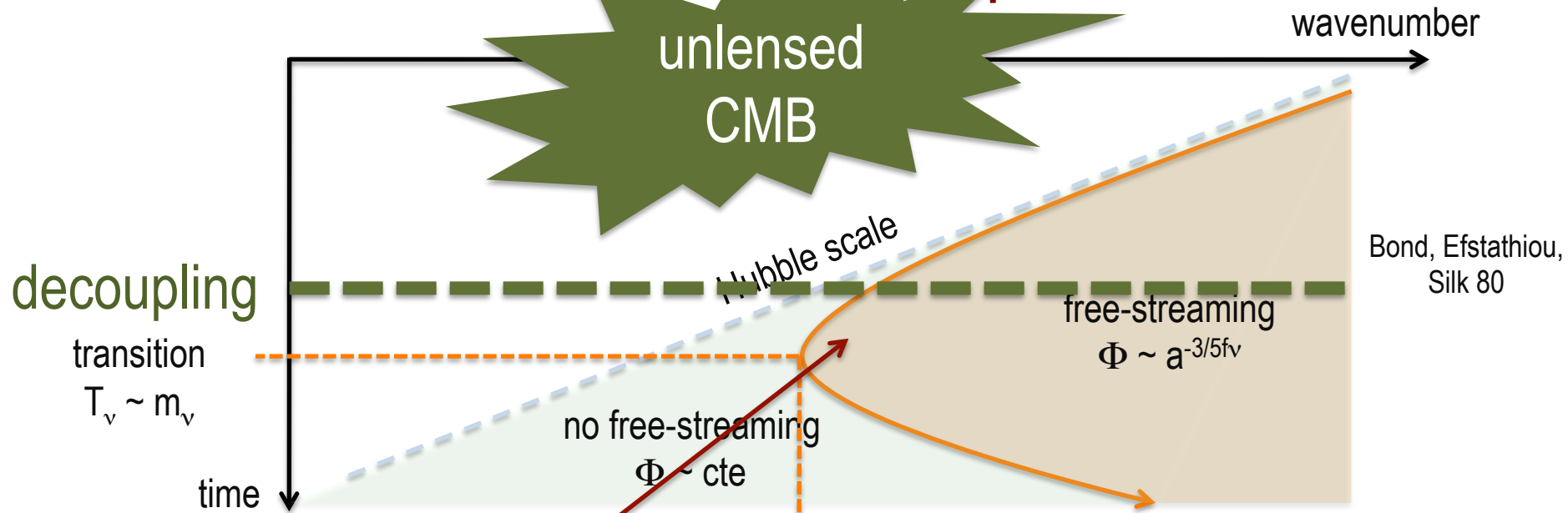
III. Non-relativistic neutrino perturbations



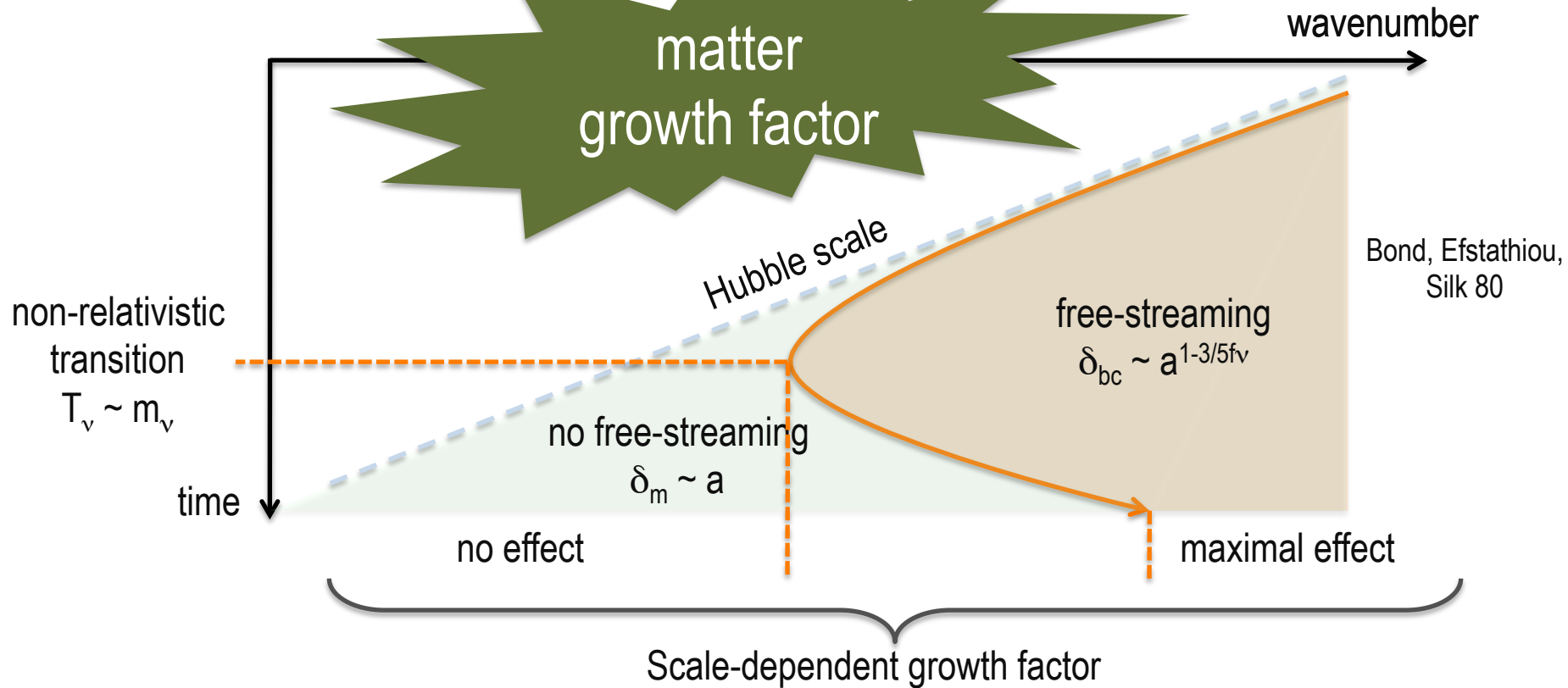
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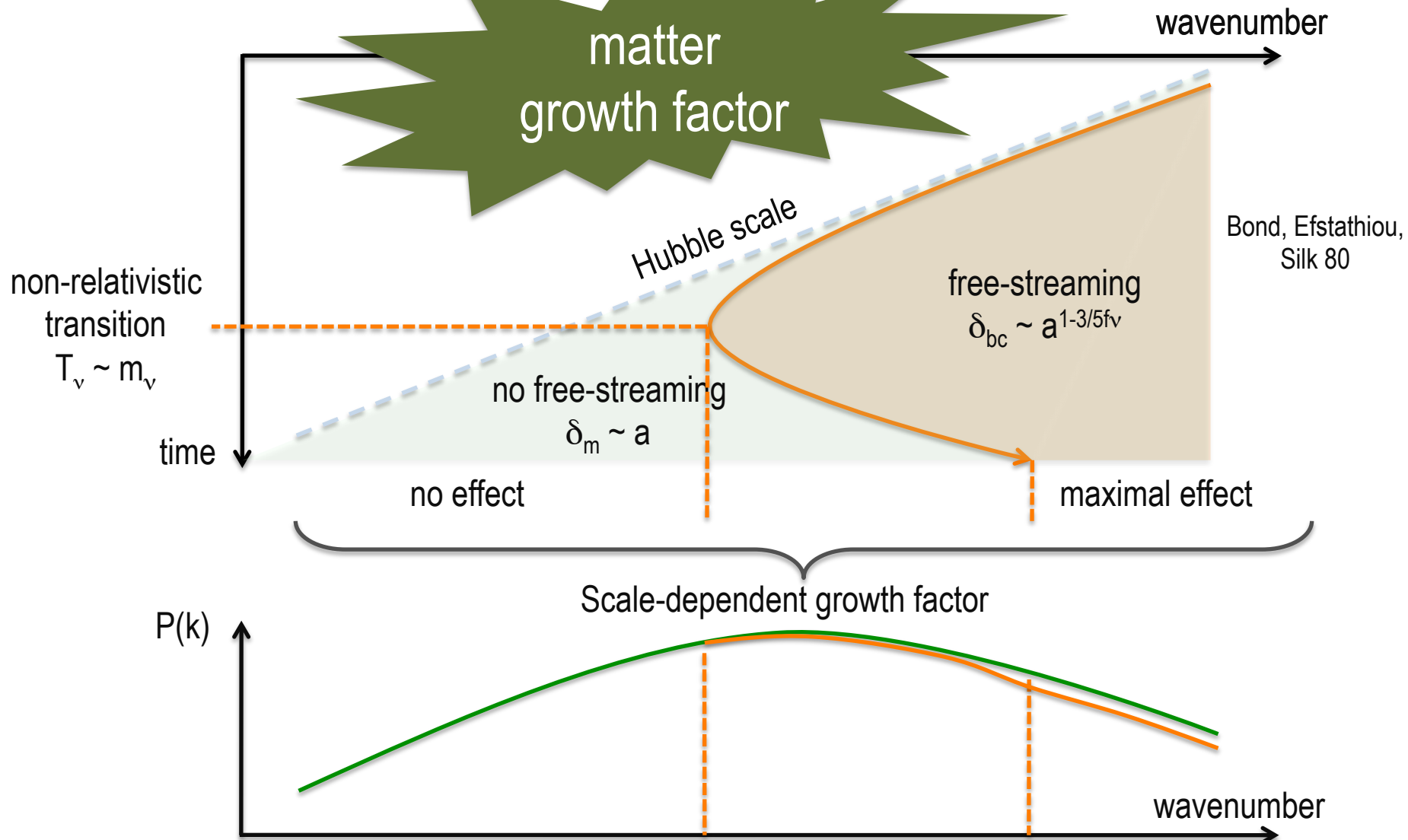
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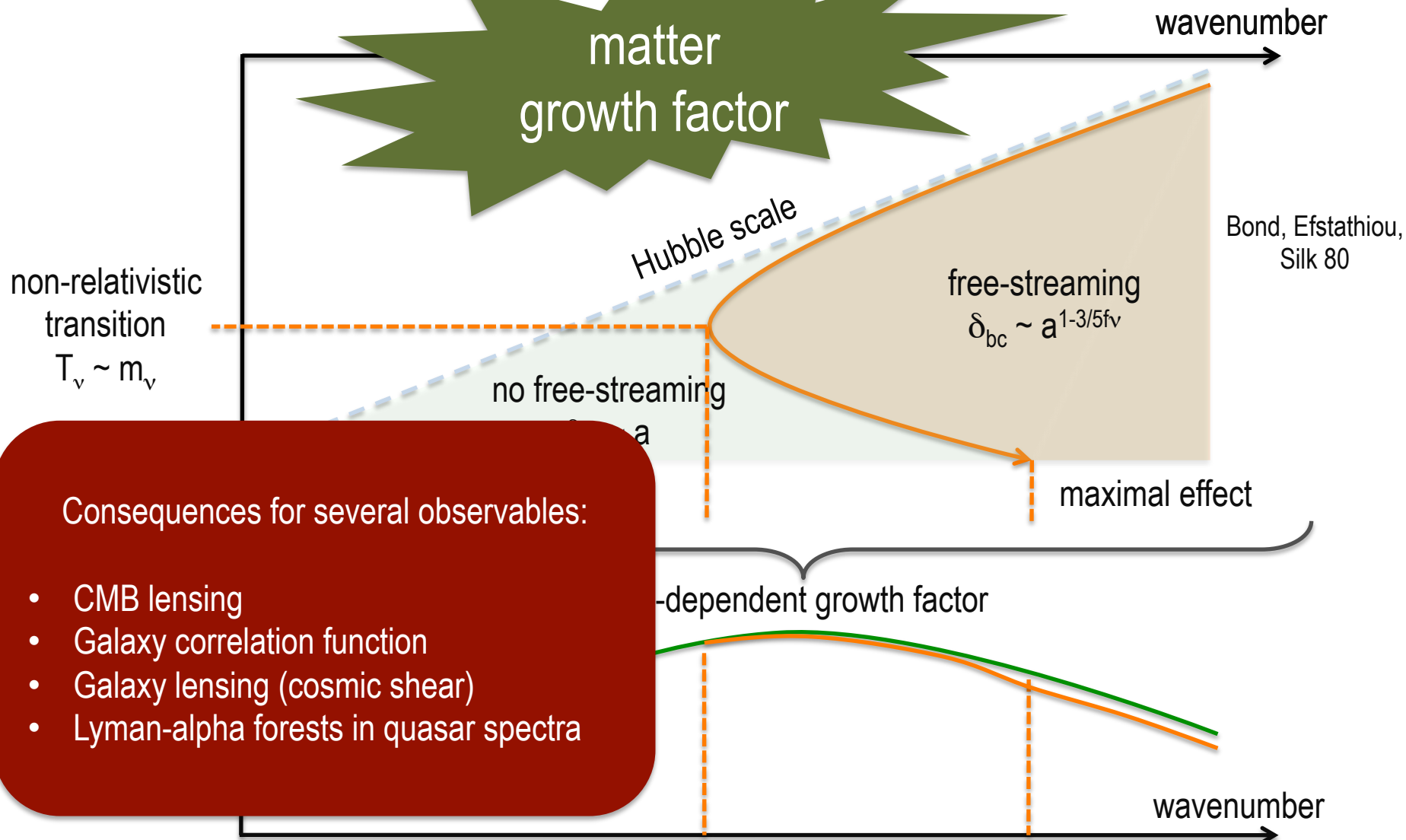
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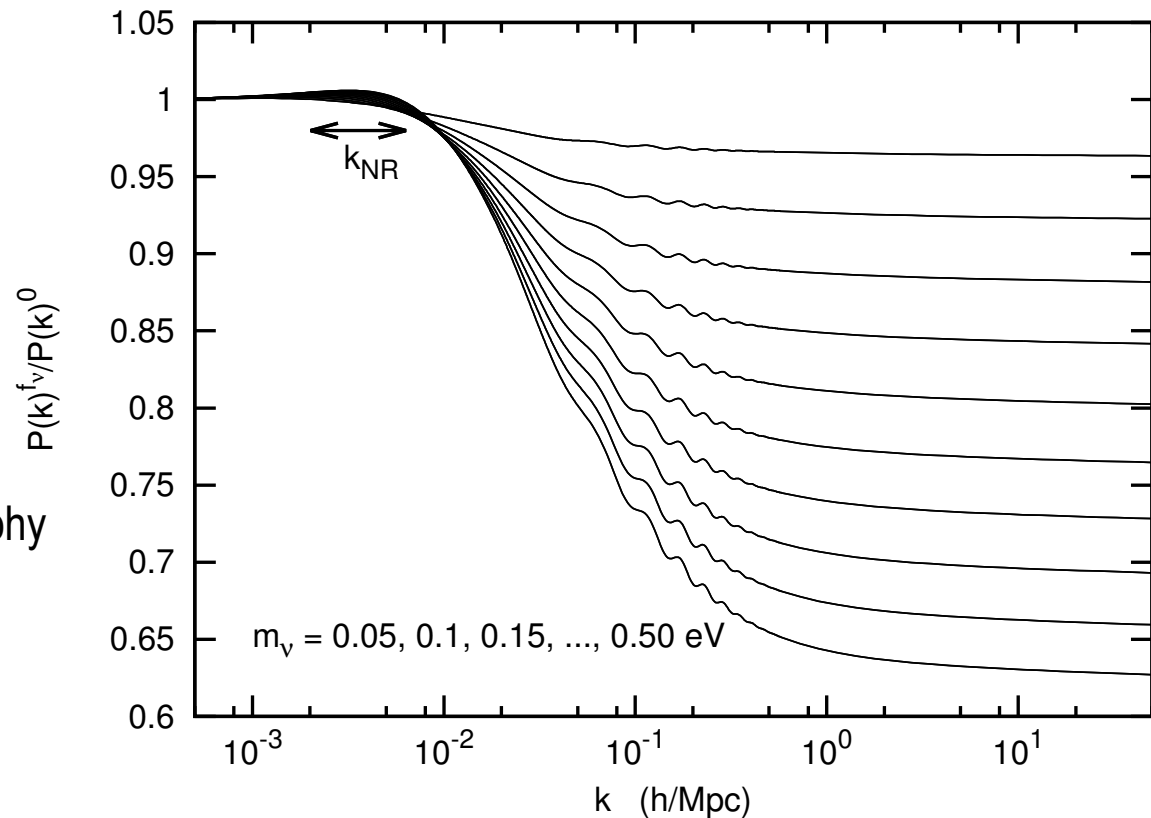


III. Non-relativistic neutrino perturbations



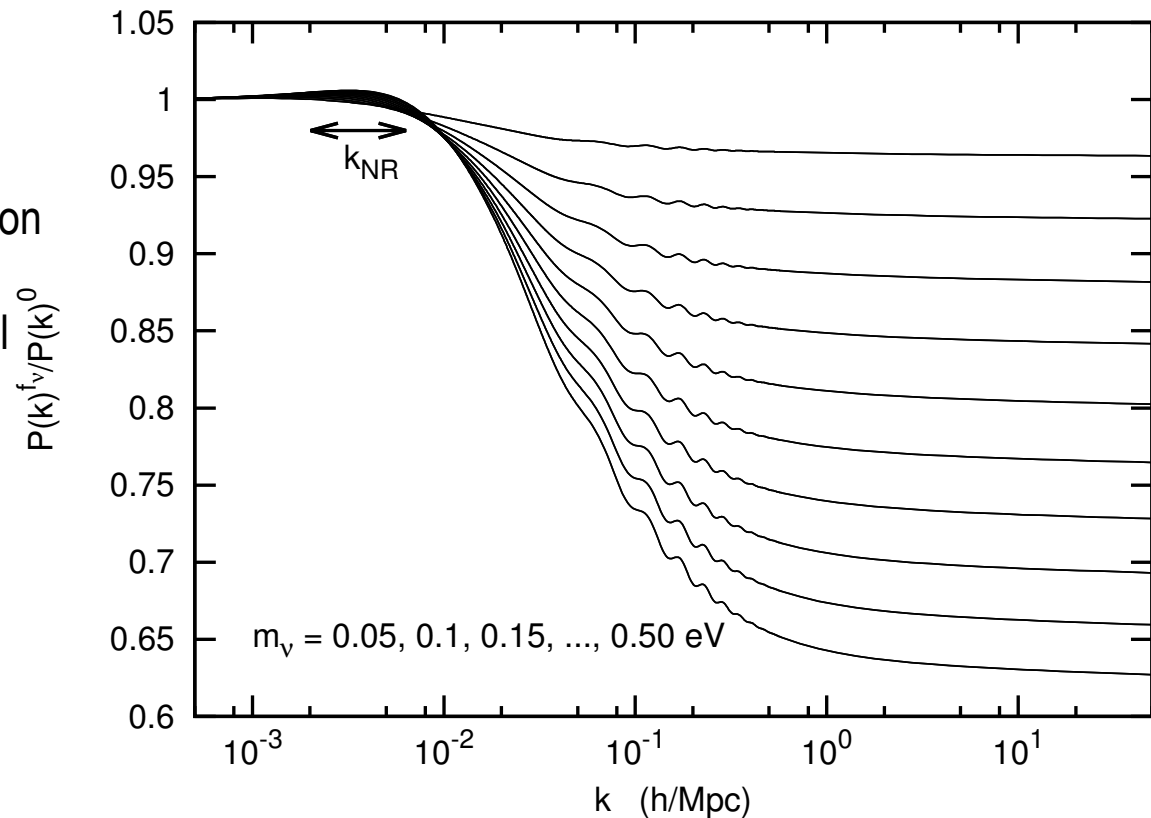
III. Neutrino masses and linear growth of structure

- Step-like effect
- Depends on redshift!
Smaller at high z
- Importance of tomography



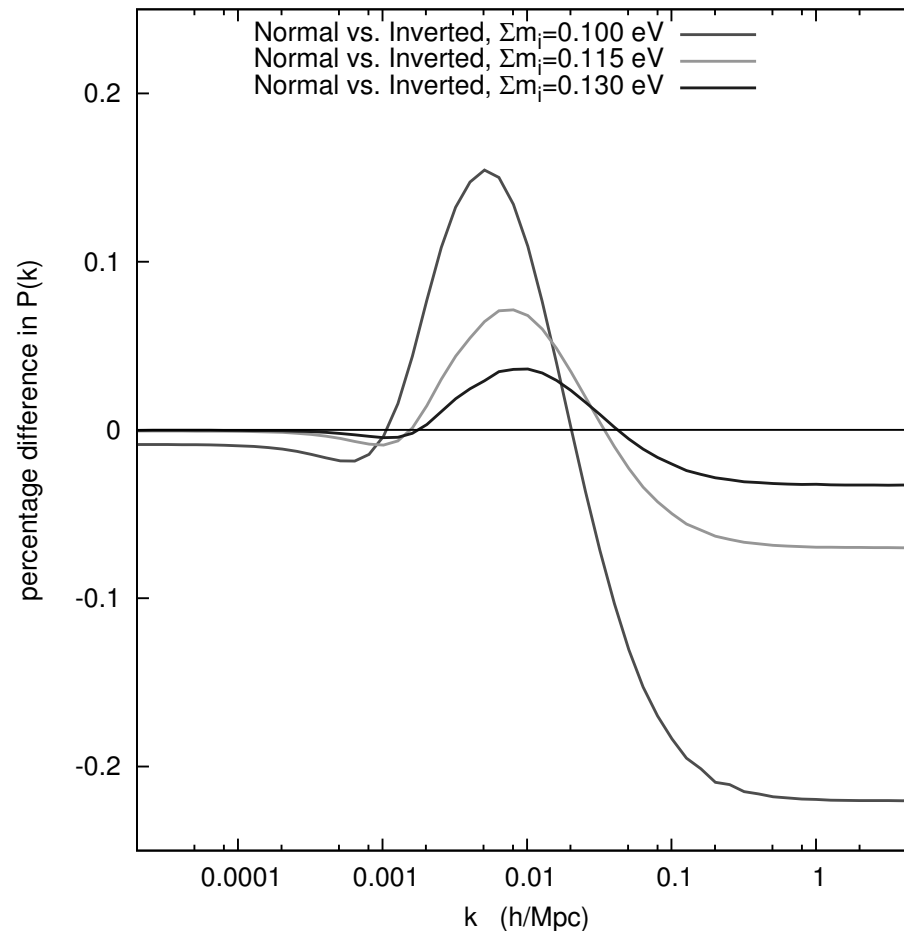
III. Neutrino masses and linear growth of structure

- Today: $\Delta P/P \sim 1-8f_v$
- At least **4.5%** suppression
- Depends mainly on total mass.
- But k_{NR} depends on individual mass



III. Neutrino masses and linear growth of structure

- Mass splitting: effects of order 0.1%
- Undetectable

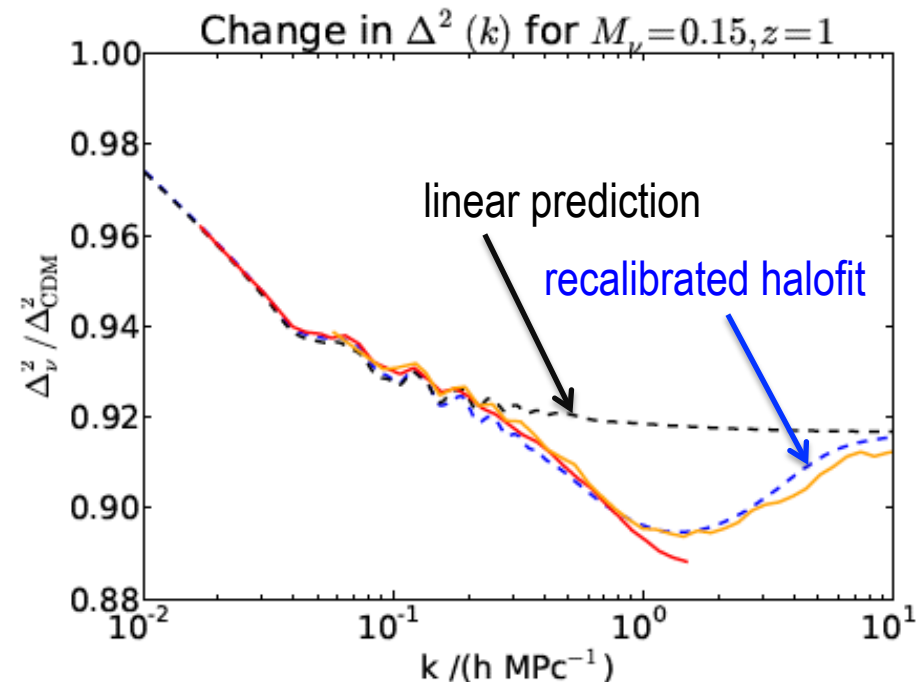
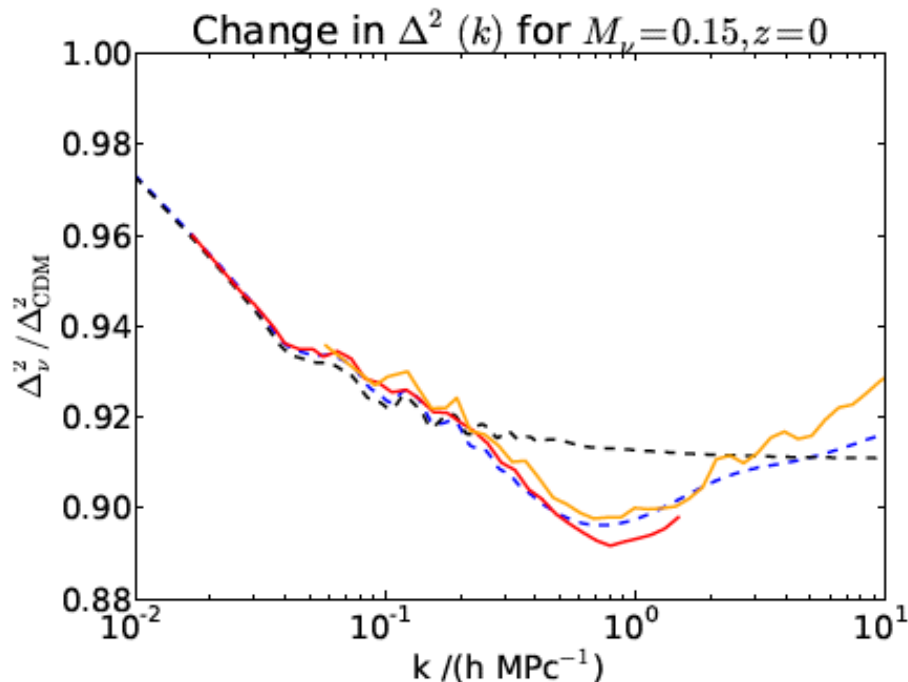


III. Neutrino masses and non-linear growth of structure

- Effect enhanced by non-linear evolution

Bird et. al 2011, see also

Brandbyge et al., Hannestad et al., Wagner et al.



- Tree-PM, $N_\nu \gg N_{\text{cdm}}$, ν in tree only
- (or SPH with imperfect fluid)

III. So what do we actually measure?

Assuming three standard active neutrinos, and no other light relic:

- Equivalently: $\rho_\nu, \omega_\nu, \Sigma m_i = M_\nu = 93.14 \omega_\nu \text{ eV}$
- Mass splitting inaccessible
- No sensitivity to Dirac/Majorana, mixing angles, CP phases, etc.

Assuming three standard active neutrinos, and no other light relic:

- Equivalently: $\rho_{\text{HDM}}, \omega_{\text{HDM}}, M_{\text{veff}} = 93.14 \omega_{\text{HDM}} \text{ eV}$
- plus N_{eff} defined during radiation domination
- Mass splitting could be accessible : depends on model

III. Measuring M_ν

CMB:

- Not observed by Planck (within error bars)!
- Planck + WP alone: $M_\nu < 0.66 \text{ eV}$ (95% CL)
- adding BAO: $M_\nu < 0.23 \text{ eV}$

Planck XVI paper, 2013

CMB + LSS:

- Contradictions: compatible with $M_\nu < 0.23 \text{ eV}$ or pointing at $\sim 0.3\text{-}0.4 \text{ eV}$

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CMB + LSS:

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Any experiment seeing low amplitude favors high neutrino mass but conflicts CMB TT

- CMB lensing,
- (SZ) clusters,
- CFHTLens weak lensing,
- BOSS red.-space dist.

Claims for $M_\nu \sim 0.3 \text{ eV} - 0.8 \text{ eV}$

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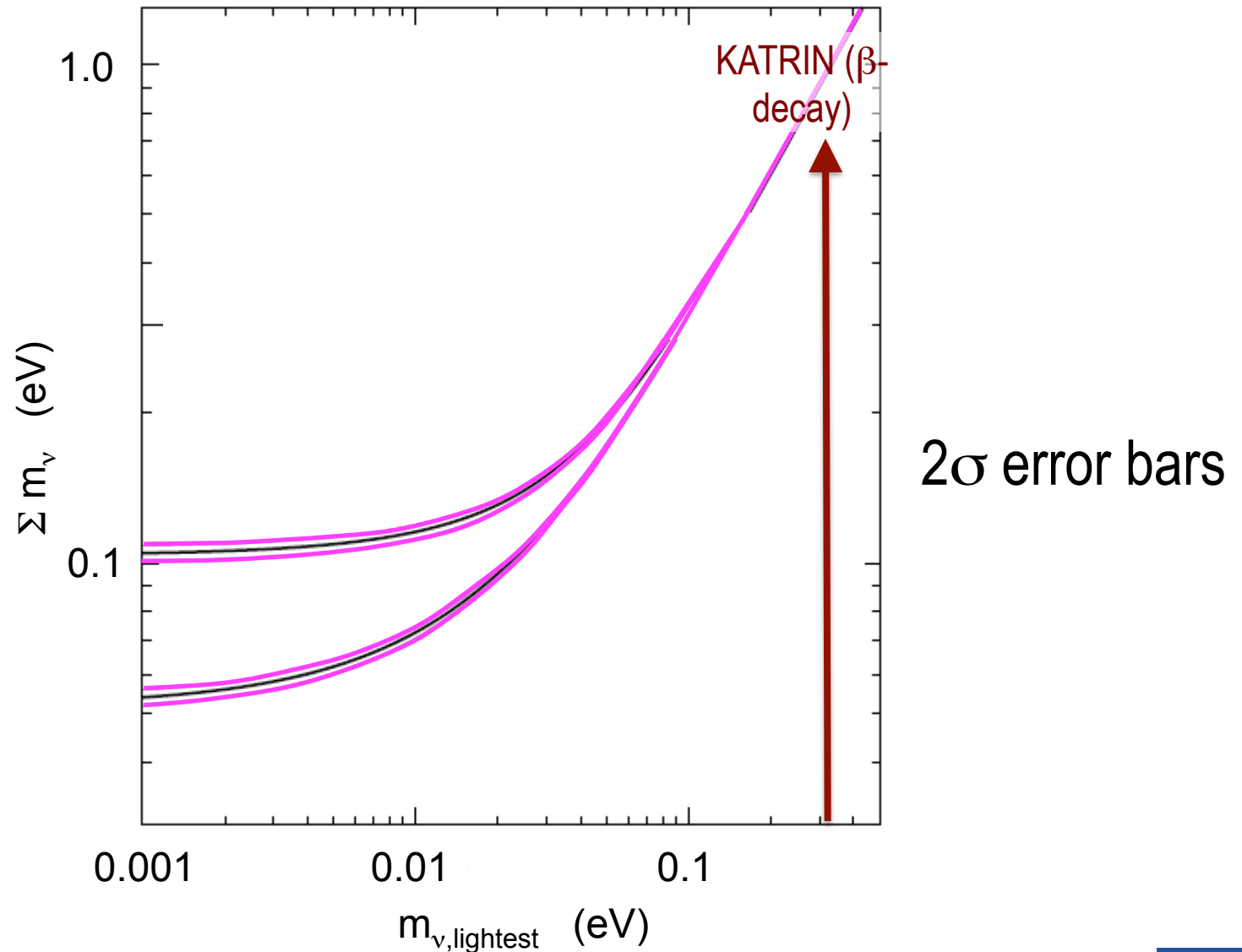
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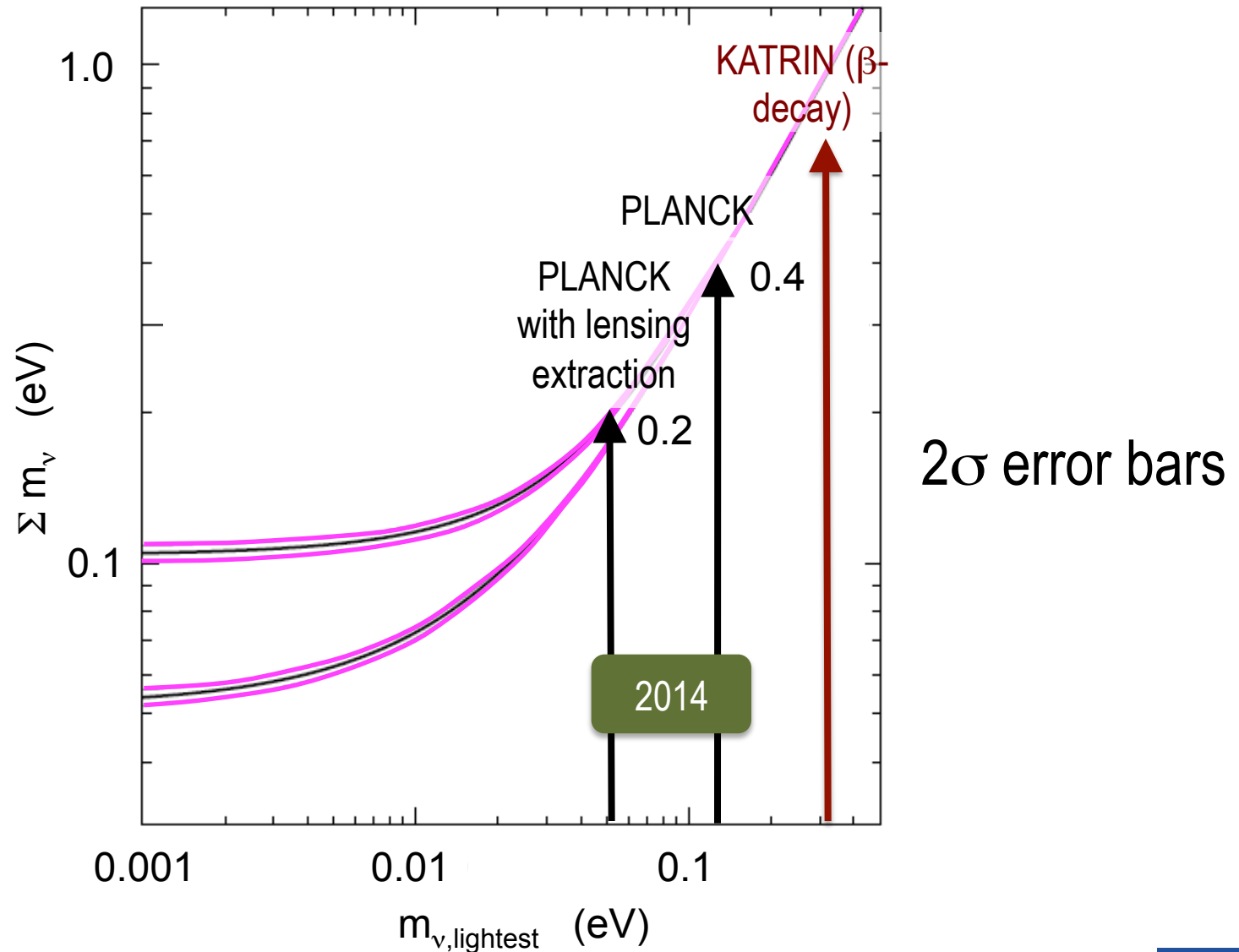
Any experiment seeing high amplitude disfavors high neutrino mass:

- SDSS Ly- α of 2006
 $M_\nu < 0.17 \text{ eV}$ (95%)

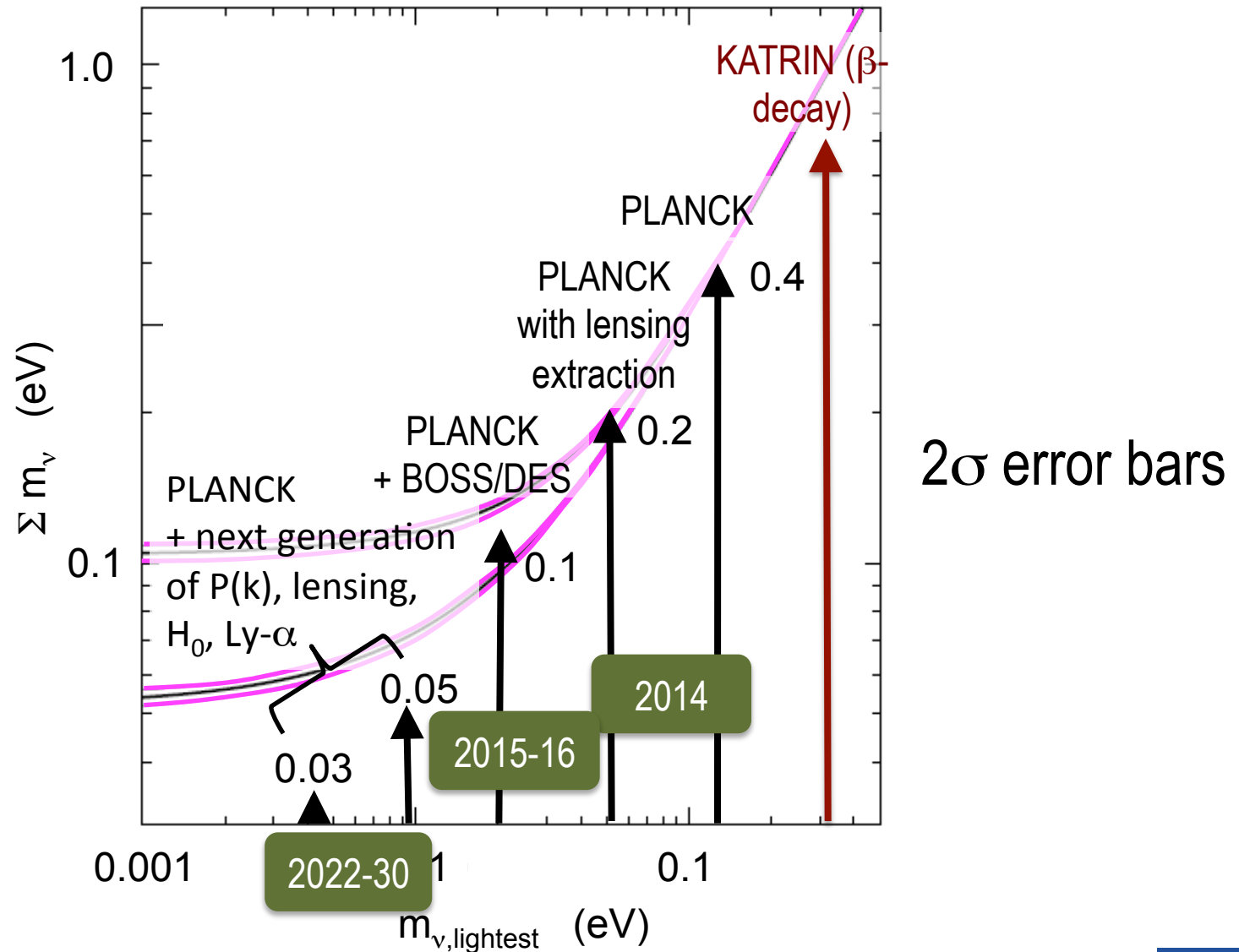
III. Future mass sensitivity



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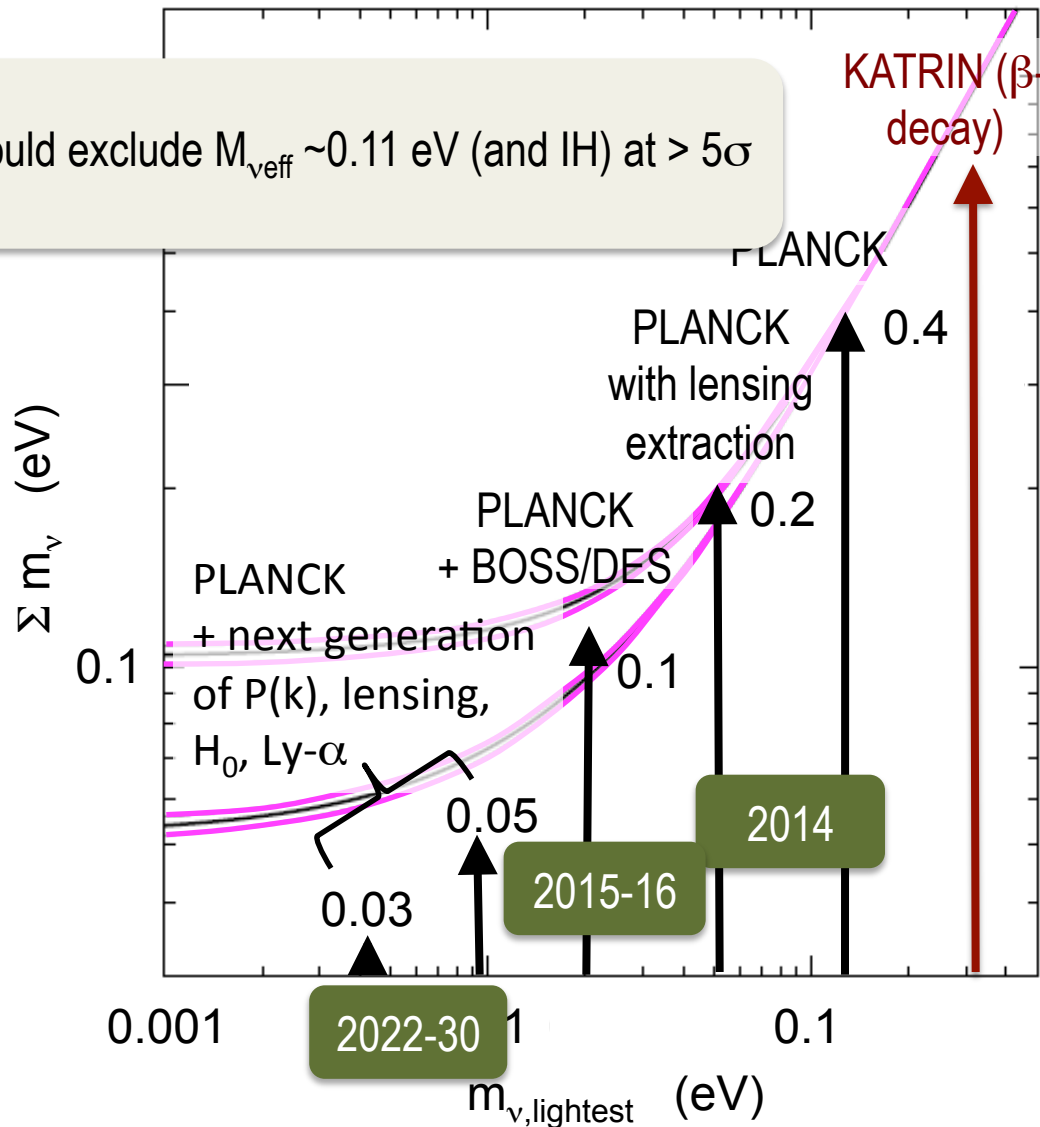


III. Future mass sensitivity



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cosmology could exclude $M_{\text{veff}} \sim 0.11$ eV (and IH) at $> 5\sigma$



III. Model-dependence of bounds ?

- Bounds obtained by fitting **given model** (minimal 6-parameter Λ CDM, extensions with curvature, dark energy, more freedom in primordial spectrum, etc.)
- Effect of N_{eff} , M_ν could be **confused** with that of other parameters
 - true with past experiments (e.g. degeneracies $N_{\text{eff}}-M_\nu$, $N_{\text{eff}}-H_0$, $w-M_\nu$, etc.)
 - Less and less true: thousands of independent data points, at many different scales AND redshift; only ~ 10 -20 model parameters
 - Unique effect of M_ν : scale-dependent growth factor, signature of free-streaming particles (different from changing primordial spectrum)
 - Unique effects of N_{eff} : e.g. baryon drag shifting peaks because $c > c_s$, signature of ultra-relativistic particles

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- **Unique effect of M_ν** : **scale-dependent growth factor**, signature of free-streaming particles (different from changing primordial spectrum)
- **Unique effects of N_{eff}** : e.g. **baryon drag** shifting + damping tail

III. Complementarity with laboratory ?

- assuming $N_{\text{eff}} = 3$, $M_{\text{veff}} = m_1 + m_2 + m_3$, independently of mixing angles, CP phases, Dirac/Majorana mass : different from β - and double β -decay
- What if there is a tension between cosmology and laboratory bounds? E.g. KATRIN find $m_\beta \sim 0.3$ eV and cosmology $M_\nu < 0.1$ eV?
- After checking for systematics and degeneracies, would bring evidence for non-standard ν interactions (decay into lighter species, effective mass from coupling with other fields, etc...) or strong deviation from standard cosmological model (low-scale reheating / entropy production after BBN and conspiracy with other light relics ...) : NEW PHYSICS

III. Complementarity with laboratory ?

- assuming $N_{\text{eff}} = 3$, $M_{\text{veff}} = m_1 + m_2 + m_3$, independently of mixing angles, CP phases, Dirac/Majorana mass : different from β - and double β -decay
- What if there is a tension between cosmology and laboratory bounds? E.g. KATRIN find $m_\beta \sim 0.3$ eV and cosmology $M_\nu < 0.1$ eV?
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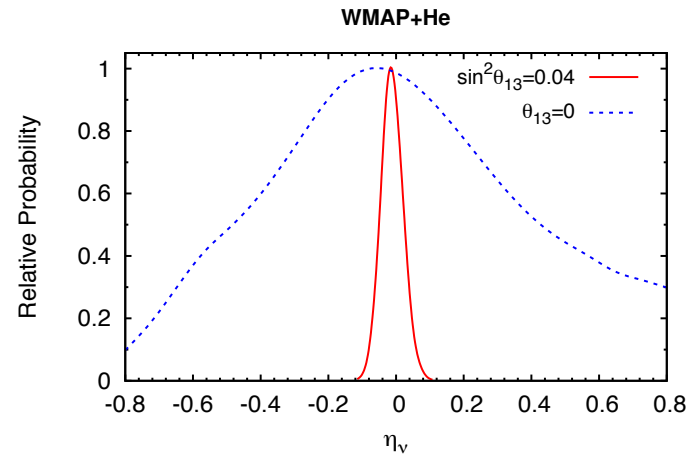
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IV. Beyond minimal model

- Extra production of neutrinos; low temperature reheating;
 - N_{eff} constraints from CMB, LSS, BBN

- **Neutrino-antineutrino asymmetry**

- Similar, but non-trivial effects from oscillations and BBN leading to much stronger bound!
- Very constrained by θ_{13}
- At $T \sim 10$ MeV, $\eta_\nu < 0.06$
- $\Delta N_{\text{eff}} < 0.4$

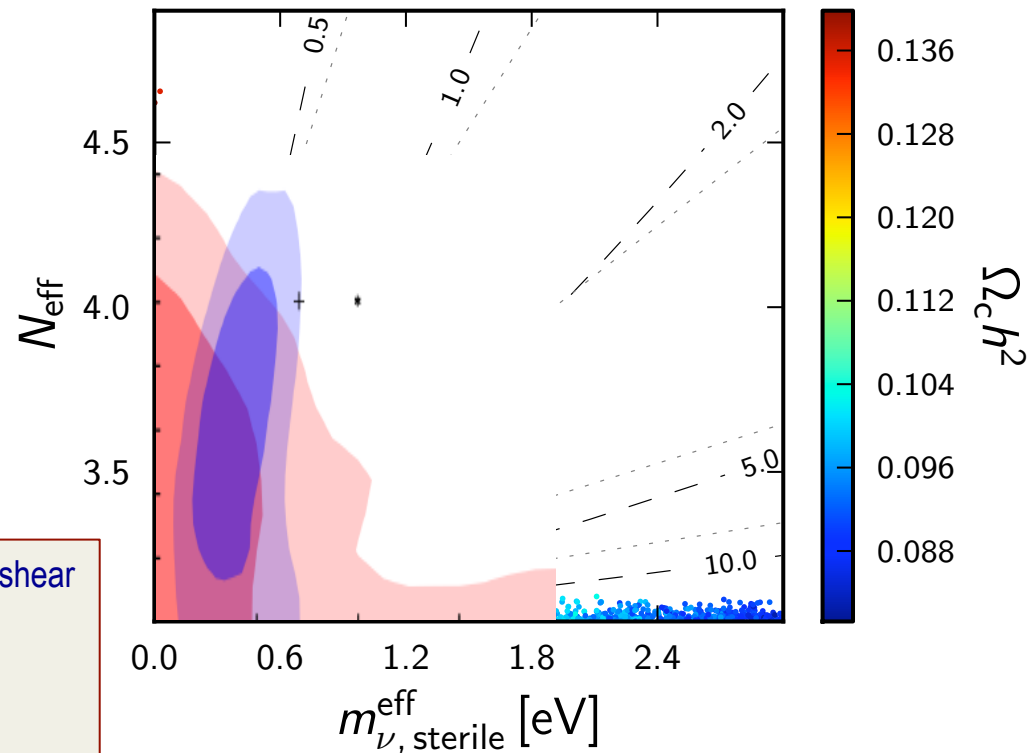


Franca et al., PRD86 023517 (2012)

- **Non-standard neutrino interactions: very model-dependent**
 - Interactions with themselves, dark matter, scalar field, quintessence, dark radiation
 - (see e.g. Archidiacono & Hannestad 13, Wilkinson et al. 13, Serra 10, ...)
- **Light sterile neutrinos: see next**

IV. Light sterile neutrinos

CMB only (Planck + WP + highL) analysis for 3+1 case:



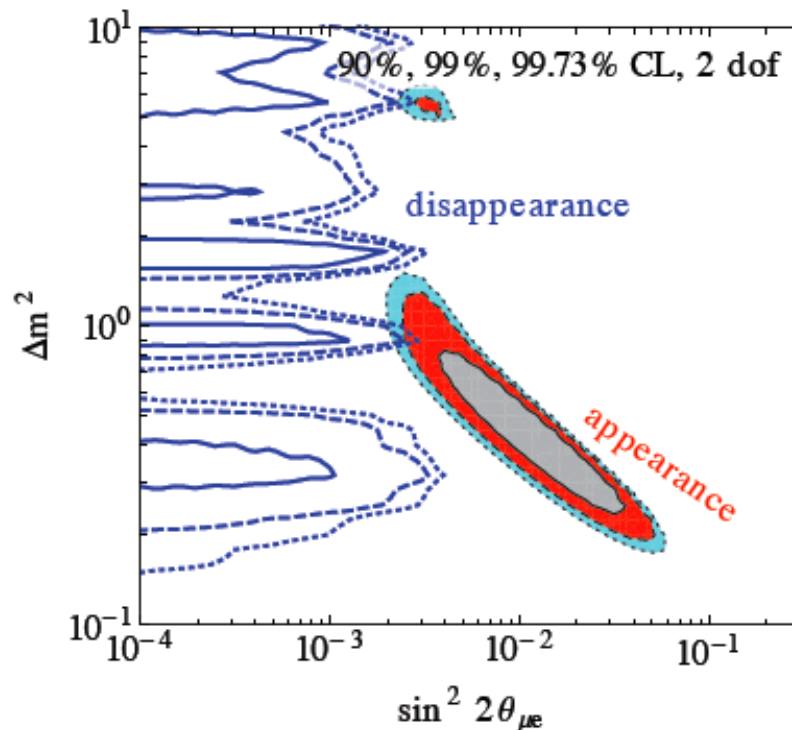
Using H0 + BAO + clusters + gal.shear

From Hamann & Hasenkamp
See also Wyman et al.,
Archidiacono et al.,
Giusarma et al.

IV. Light sterile neutrinos

Motivations: anomalies in short-baseline neutrino oscillation experiments

3+1 analysis in
Kopp et al. 2013



Appearance: LSND, MiniBoone, NOMAD, KARMEN, ICARUS, E776

Disappearance: reactor, Gallium, MiniBoone, CDHS, Minos, KARMEN

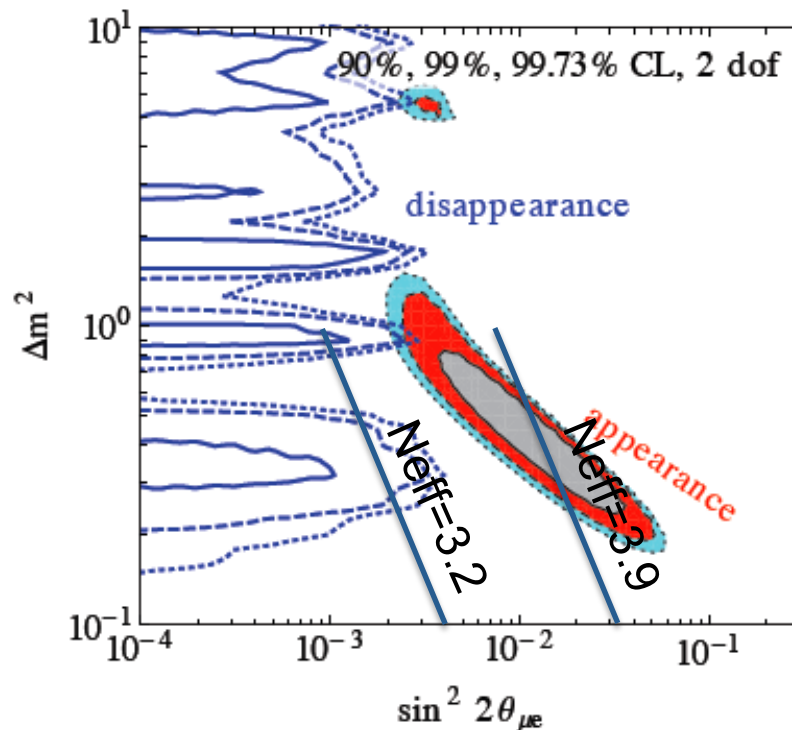
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N_{eff} isocontours are model-dependent
(leptonic asymmetry: Saviano et al.,
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NSI: Archidiacono et al.,...)



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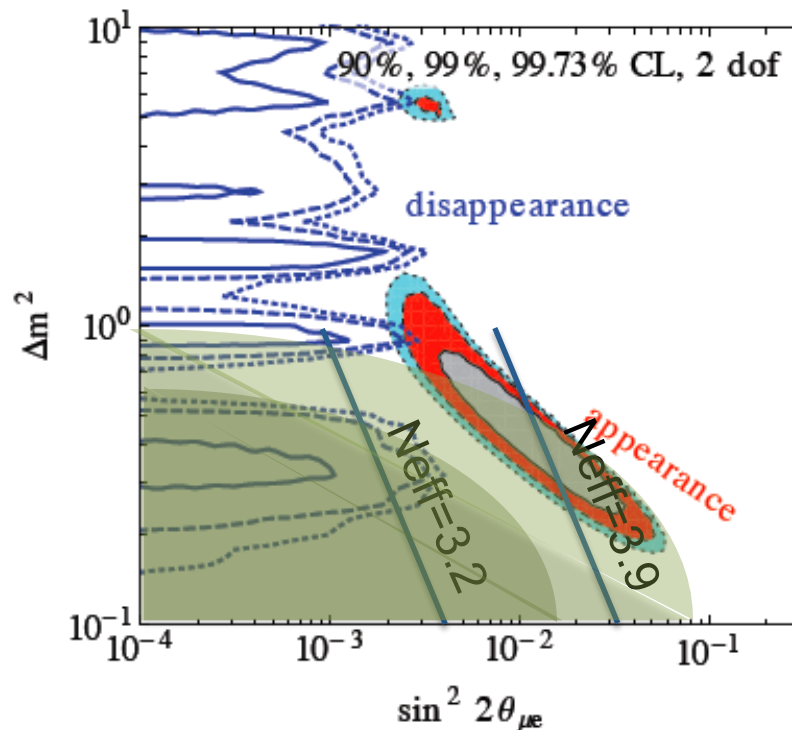
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