

Global fits to radiative $b \rightarrow s$ transitions

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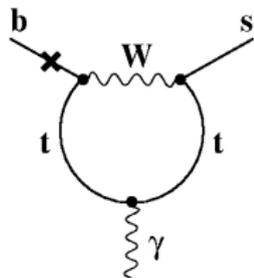


Effective approach to radiative decays

- $b \rightarrow s\gamma$ and $b \rightarrow sl^+\ell^-$ Flavour-Changing Neutral Currents
- enhanced sensitivity to New Physics effects
- analysed in model-independent approach effective Hamiltonian
- integrating out all heavy degrees of freedom

$$b \rightarrow s\gamma(^*) : \mathcal{H}_{\Delta F=1}^{SM} \propto \sum_{i=1}^{10} V_{ts}^* V_{tb} C_i Q_i + \dots$$

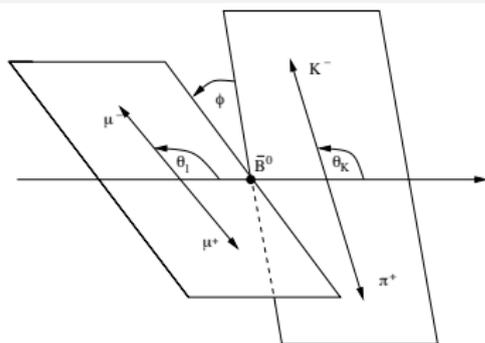
- $Q_7 = \frac{e}{g^2} m_b \bar{s} \sigma^{\mu\nu} (1 + \gamma_5) F_{\mu\nu} b$ [real or soft photon]
- $Q_9 = \frac{e^2}{g^2} \bar{s} \gamma_\mu (1 - \gamma_5) b \bar{\ell} \gamma_\mu \ell$ [$b \rightarrow s\mu\mu$ via Z /hard γ]
- $Q_{10} = \frac{e^2}{g^2} \bar{s} \gamma_\mu (1 - \gamma_5) b \bar{\ell} \gamma_\mu \gamma_5 \ell$ [$b \rightarrow s\mu\mu$ via Z]



NP changes short-distance C_i and/or add new long-distance ops Q'_i

- Chirally flipped ($W \rightarrow W_R$) $Q_7 \rightarrow Q_{7'} \propto \bar{s} \sigma^{\mu\nu} (1 - \gamma_5) F_{\mu\nu} b$
- (Pseudo)scalar ($W \rightarrow H^+$) $Q_9, Q_{10} \rightarrow Q_S \propto \bar{s} (1 + \gamma_5) b \bar{\ell} \ell, Q_P$
- Tensor operators ($\gamma \rightarrow T$) $Q_9 \rightarrow Q_T \propto \bar{s} \sigma_{\mu\nu} (1 - \gamma_5) b \bar{\ell} \sigma_{\mu\nu} \ell$

$B \rightarrow K^* \ell \ell$: angular analysis



- θ_l : angle of emission between K^{*0} and μ^- in di-lepton rest frame
- θ_{K^*} : angle of emission between K^{*0} and K^- in di-meson rest frame.
- ϕ : angle between the two planes
- q^2 : dilepton invariant mass square

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_l d\cos\theta_{K^*} d\phi} = \sum_i f_i(\theta_{K^*}, \phi, \theta_l) \times I_i$$

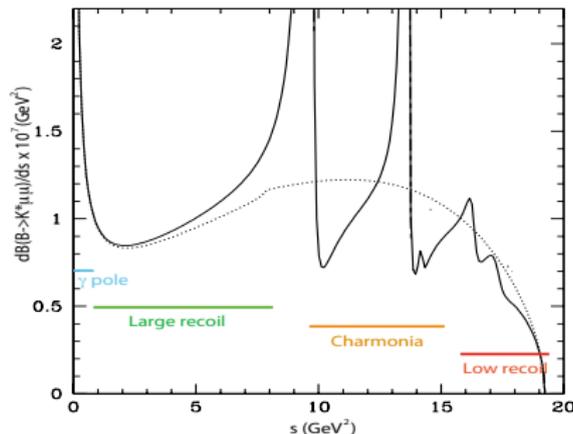
with 12 **angular coeffs** I_i , interferences between 8 **transversity ampl.**

- $\perp, ||, 0, t$ polarisation of (real) K^* and (virtual) $V^* = \gamma^*, Z^*$
- L, R chirality of $\mu^+ \mu^-$ pair

$A_{\perp, L/R}, A_{||, L/R}, A_{0, L/R}, A_t$ + scalar A_S depend on

- q^2 (lepton pair invariant mass)
- Wilson coefficients $C_7, C_9, C_{10}, C_S, C_P$ (and flipped chiralities)
- $B \rightarrow K^*$ **form factors** $A_{0,1,2}, V, T_{1,2,3}$ from $\langle K^* | Q_i | B \rangle$

Four different regions



- Very large K^* -recoil ($4m_\ell^2 < q^2 < 1 \text{ GeV}^2$): γ almost real
(C_7/q^2 divergence and light resonances)
- Large K^* -recoil ($q^2 < 9 \text{ GeV}^2$): energetic K^*
($E_{K^*} \gg \Lambda_{QCD}$: form factors from light-cone sum rules LCSR)
- Charmonium region ($q^2 = m_{\psi, \psi' \dots}^2$ between 9 and 14 GeV^2)
- Low K^* -recoil ($q^2 > 14 \text{ GeV}^2$): soft K^*
($E_{K^*} \simeq \Lambda_{QCD}$: form factors lattice QCD)

Hadronic quantities: $B \rightarrow K^*$ form factors

7 independent form factors $A_{0,1,2}$, V ($O_{9,10}$) and $T_{1,2,3}$ (O_7)

$$\begin{aligned} \langle K^*(k) | \bar{s} \gamma_\mu (1 - \gamma_5) | B(\epsilon, p) \rangle &= -i \epsilon_\mu (m_B + m_V) A_1(q^2) + i(p+k)_\mu (\epsilon^* \cdot q) \frac{A_2(q^2)}{m_B + m_{K^*}} \\ &\quad + i q_\mu (\epsilon^* \cdot q) \frac{2m_{K^*}}{q^2} \tilde{A}_0(q^2) + \epsilon_{\mu\nu\rho\sigma} \epsilon^{*\nu} p^\rho k^\sigma \frac{2V(q^2)}{m_B + m_{K^*}} \end{aligned}$$

$$\begin{aligned} \langle K^*(k) | \bar{s} \sigma_{\mu\nu} q^\nu (1 + \gamma_5) | B(\epsilon, p) \rangle &= i \epsilon_{\mu\nu\rho\sigma} \epsilon^{*\nu} p^\rho k^\sigma 2T_1(q^2) + \epsilon_\mu^* (m_B^2 - m_V^2) T_2(q^2) \\ &\quad - (p+k)_\mu (\epsilon^* \cdot q) \tilde{T}_3(q^2) + q_\mu (\epsilon^* \cdot q) T_3(q^2) \end{aligned}$$

In the limits of low and large K^* recoil, separation of scales Λ and m_B

- **Large-recoil limit** ($\sqrt{q^2} \sim \Lambda_{QCD} \ll m_B$) [LEET/SCET, QCDF]
 - two soft form factors $\xi_\perp(q^2)$ and $\xi_\parallel(q^2)$
 - $O(\alpha_s)$ corr. from hard gluons [computable], $O(\Lambda/m_B)$ [nonpert]

[Charles et al., Beneke and Feldmann]

- **Low-recoil limit** ($E_{K^*} \sim \Lambda_{QCD} \ll m_B$) [HQET]
 - three soft form factors $f_\perp(q^2)$, $f_\parallel(q^2)$, $f_0(q^2)$
 - $O(\alpha_s)$ corr. from hard gluons [computable] and $O(\Lambda/m_B)$ [nonpert]

[Grinstein and Pirjol, Hiller, Bobeth, Van Dyk...]

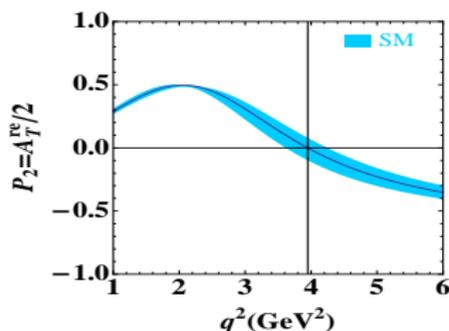
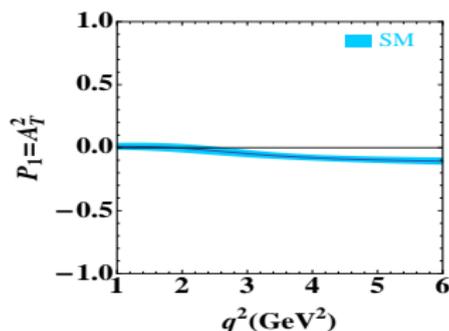
Form-factor “independent” observables

= Obs. where soft form factors cancel at LO

- Zero of forward-back. asym. $A_{FB}(s_0) = 0$: $C_9^{\text{eff}}(s_0) + 2 \frac{m_b M_B}{s_0} C_7^{\text{eff}} = 0$
- Transversity asymmetries

[Krüger, Matias; Becirevic, Schneider]

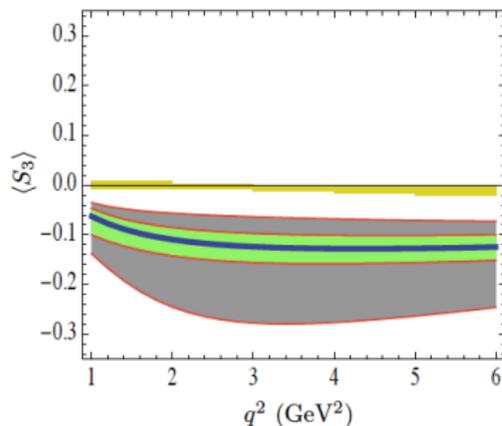
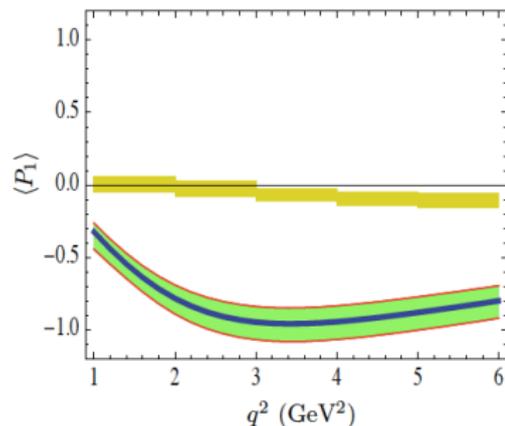
$$P_1 = A_T^{(2)} = \frac{l_3}{2l_{2s}} = \frac{|A_{\perp}|^2 - |A_{\parallel}|^2}{|A_{\perp}|^2 + |A_{\parallel}|^2}, \quad P_2 = \frac{A_T^{\text{re}}}{2} = \frac{l_{6s}}{8l_{2s}} = \frac{\text{Re}[A_{\perp}^L A_{\parallel}^L - A_{\perp}^R A_{\parallel}^{R*}]}{|A_{\perp}|^2 + |A_{\parallel}|^2}$$



- 6 form-factor independ. obs. at large recoil ($P_1, P_2, P_3, P'_4, P'_5, P'_6$) + 2 form-factor dependent obs. ($\Gamma, A_{FB}, F_L \dots$) [$A_{FB} = -3/2 P_2 (1 - F_L)$]
- exhausting information in (partially redundant) angular coeffs l_i

[Matias, Krüger, Mescia, SDG, Virto, Hiller, Bobeth, Dyck, Buras, Altmanshoffer, Straub...]

Sensitivity to form factors



- P_i designed to have limited sensitivity to ffs
- S_i CP-averaged version of I_i (A_i for CP-asym)

$$P_1 = \frac{2S_3}{1 - F_L} \quad F_L = \frac{I_{1c} + \bar{I}_{1c}}{\Gamma + \bar{\Gamma}} \quad S_3 = \frac{I_3 + \bar{I}_3}{\Gamma + \bar{\Gamma}}$$

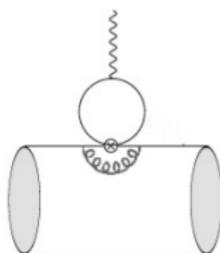
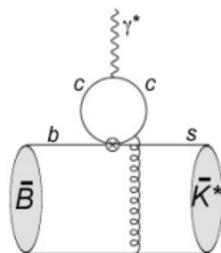
different sensitivity to form factors inputs for given NP scenario
(form factors from LCSR: green [Ball, Zwicky] vs gray [Khodjamirian et al.]

Computation of amplitudes

Large recoil: NLO QCD factorisation

in $A_{\perp,||,0}$ (non-factor.)

in FFs (factor)



- $V, A_i, T_i = \xi_{||,\perp}$
+ factorisable $O(\alpha_s)$
+ nonpert $O(\Lambda/m_b)$
- $A_{0,||,\perp} = C_i \times \xi_{||,\perp}$
+ factorisable $O(\alpha_s)$
+ nonfactorisable $O(\alpha_s)$
+ nonpert $O(\Lambda/m_b)$

- either compute A with $\xi_{||,\perp}$ extracted from V, A_i (check T_i OK)
- or compute A from V, A_i, T_i + nonfactorisable corrections
- nonperturbative corrections $O(\Lambda/m_b) \simeq 10\%$

Low recoil: OPE + HQET

- $A_{0,||,\perp} = C_i \times f_{0,||,\perp} + O(\alpha_s)$ corrections + $O(1/m_b)$ corrections
- $f_{0,||,\perp} \propto CL(A_1, A_2), A_1, V + O(1/m_b)$ corrections
- HQET relations between V, A_i and T_i
- nonperturbative corrections smaller $O(C_7 \Lambda/m_b, \alpha_s \Lambda/m_b)$

SM predictions and LHCb results (1)

- Present bins

- Large recoil: [0.1, 2], [2,4.3], [4.3,8.68] and [1,6] GeV^2
- Low recoil: [14.18,16], [16,19] GeV^2
- $c\bar{c}$ resonances : [10.09, 12.89]

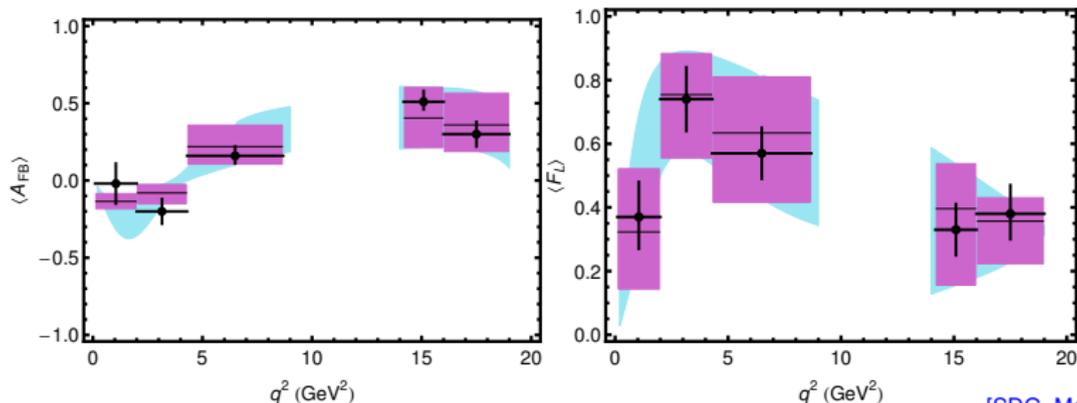
- [0.1, 1] with light resonances, washed out by binning

[Camalich, Jäger]

- $q^2 > 6 \text{ GeV}^2$ may be affected by charm-loop effects

[Khodjamirian et al.]

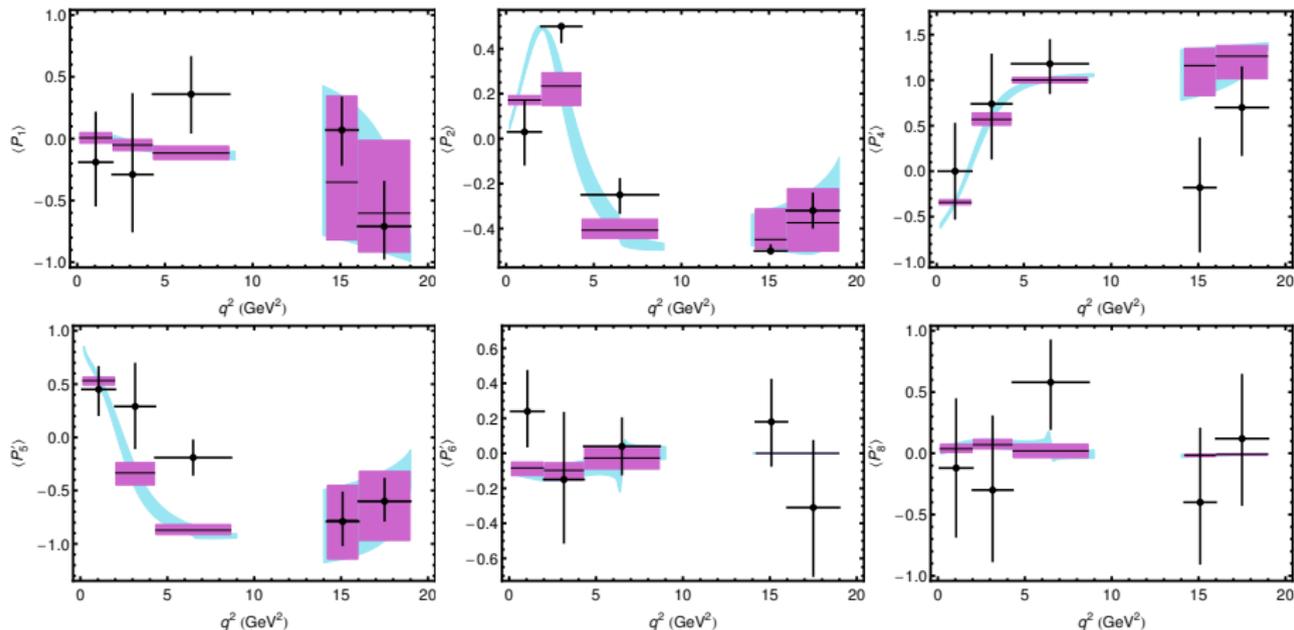
- Beauty 12 and EPS 13 : results from LHCb



[SDG, Matias, Virto]

⇒ blue: SM unbinned, purple: SM binned, crosses: LHCb values

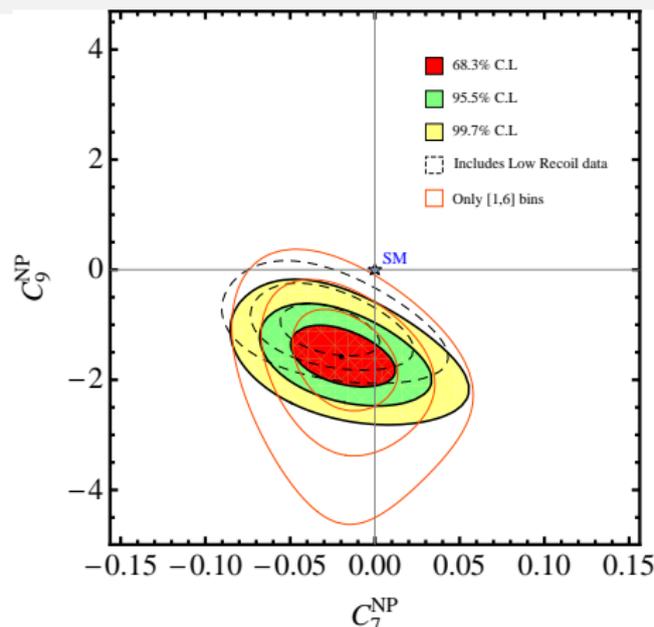
SM predictions and LHCb results (2)



Meaning of the discrepancy in P_2 and P_5' ?

[SDG, Matias, Virto]

- P_2 same zero as A_{FB} , related to C_9/C_7
- $P_5' \rightarrow -1$ as q^2 grows due to $A_{\perp,||}^R \ll A_{\perp,||}^L$ for $C_9^{SM} \simeq -C_{10}^{SM}$
- A negative shift in C_7 and C_9 can move them in the right direction



$$C_i(\mu_{ref}) = C_i^{SM} + C_i^{NP}$$

Standard χ^2 frequentist analysis

- $B \rightarrow K^* \mu \mu$: $P_1, P_2, P_4, P_5, P_6, P_8, A_{FB}$
- $B \rightarrow X_S \gamma, B \rightarrow X_S \mu \mu$: Br
- $B_s \rightarrow \mu \mu$: Br
- $B \rightarrow K^* \gamma$: A_I and $S_{K^* \gamma}$

Several $B \rightarrow K^* \mu \mu$ sets [LHCb]

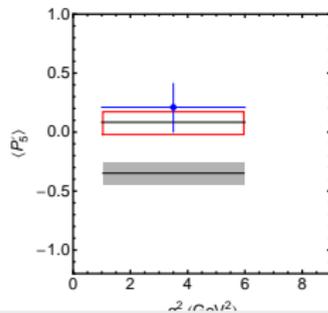
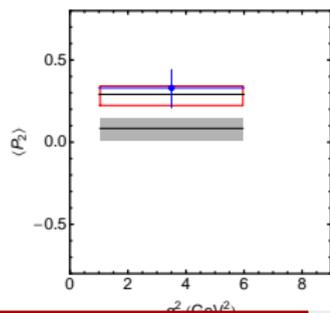
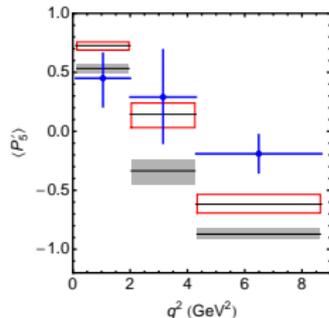
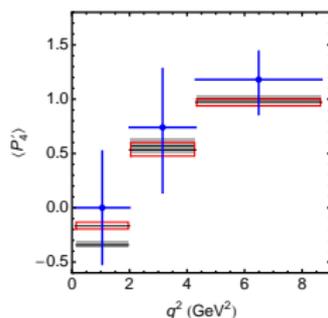
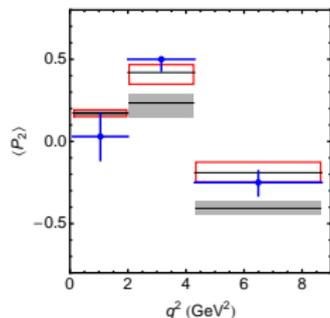
- full: 3 fine large-recoil bins
- dashed: 3 fine large-recoil bins + low-recoil bins
- orange: 1 large recoil-bin only

- Form factors from LCSR [Khodjamirian et al.], extrapolated if needed
- Large recoil: Soft form factors $\xi_{\parallel, \perp}$ + QCDF
- Low recoil: Full form factors V, A_i + HQET for T_i

Only C_7, C_9

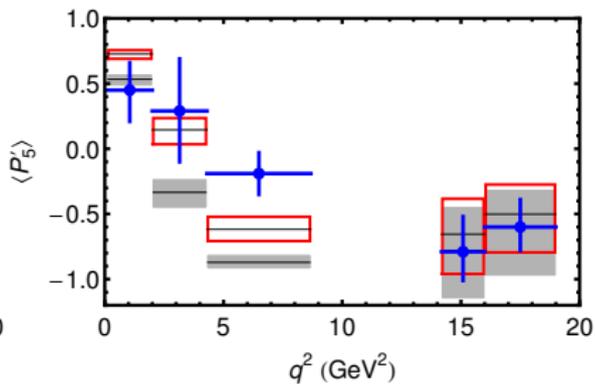
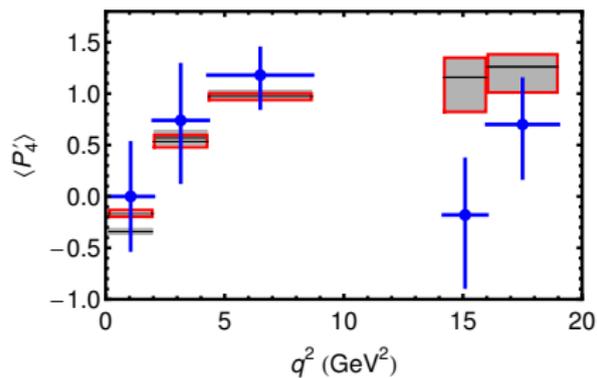
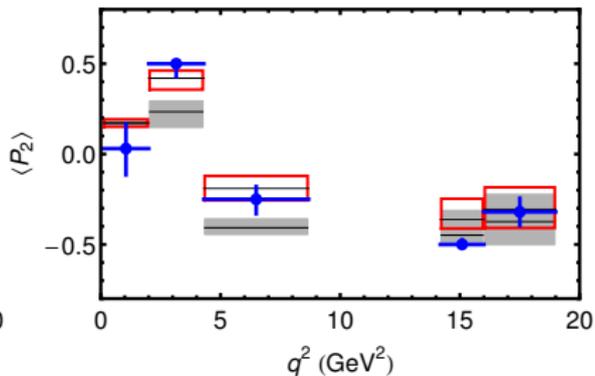
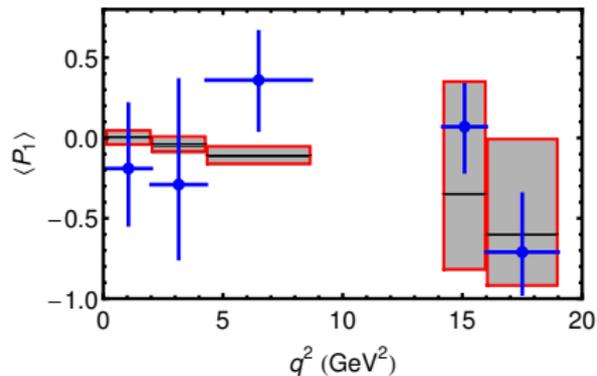
Pull of SM value for each C_i $[\Delta\chi_i^2 = \chi^2(C_i = 0) - \min_{C_i} \chi^2(C_i)]$

- pull for $C_9 \simeq 4\sigma$, pull for $C_7 \simeq 3\sigma$
- once both C_9^{NP} and C_7^{NP} included, low pulls for the other C_i 's
- consistent pattern favouring $C_9^{NP} \simeq -1.5$ [added to $C_9^{SM} \simeq 4.1$]



- grey: SM;
- red: $C_9^{NP} \simeq -1.5$;
- blue: LHCb

$$C_9 = -1.5$$



Other scenarios

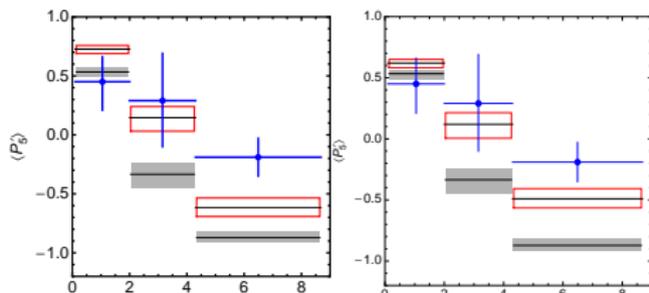
SM operators + chirally flipped

Coefficient	1σ	2σ	3σ
C_7^{NP}	$[-0.05, -0.01]$	$[-0.06, 0.01]$	$[-0.08, 0.03]$
C_9^{NP}	$[-1.6, -0.9]$	$[-1.8, -0.6]$	$[-2.1, -0.2]$
C_{10}^{NP}	$[-0.4, 1.0]$	$[-1.2, 2.0]$	$[-2.0, 3.0]$
$C_{7'}^{NP}$	$[-0.04, 0.02]$	$[-0.09, 0.06]$	$[-0.14, 0.10]$
$C_{9'}^{NP}$	$[-0.2, 0.8]$	$[-0.8, 1.4]$	$[-1.2, 1.8]$
$C_{10'}^{NP}$	$[-0.4, 0.4]$	$[-1.0, 0.8]$	$[-1.4, 1.2]$

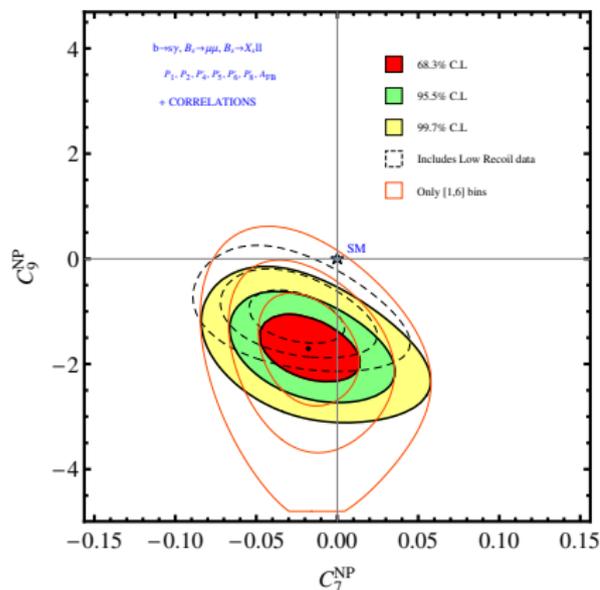
- Large-recoil shape of P_2 and P_5' favours $C_7^{NP} < 0$ and $C_9^{NP} < 0$
- No other NP contrib favoured (small pulls once C_7^{NP} and $C_9^{NP} \neq 0$)

$C_9, C_{9'}$ scenario

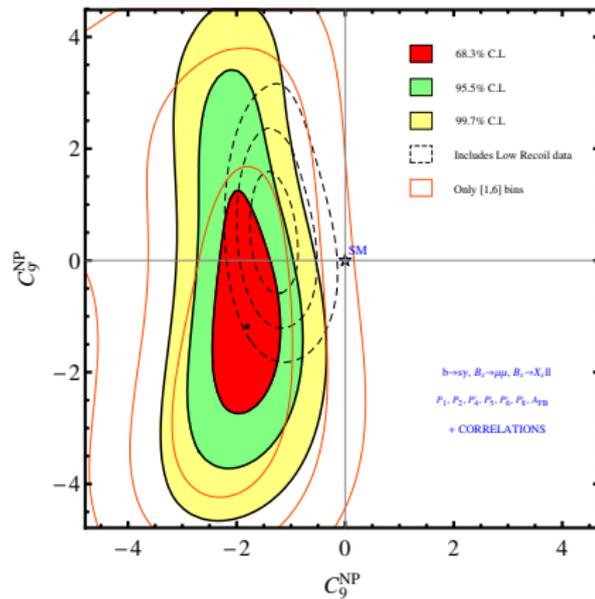
- $C_9^{NP} \sim -1.6, C_{9'}^{NP} \sim -1.5$
improves large-recoil P_5'
- low-recoil dilute effect,
allow $C_{9'} < 0$ or > 0



With exp. correlations: two scenarios



NP in C_7, C_9

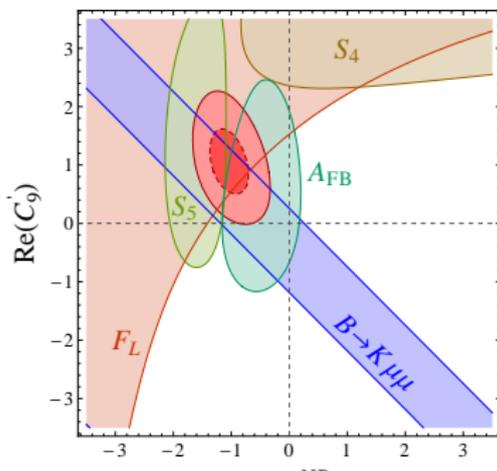


NP in C_9, C_9'

For C_7, C_9 scenario

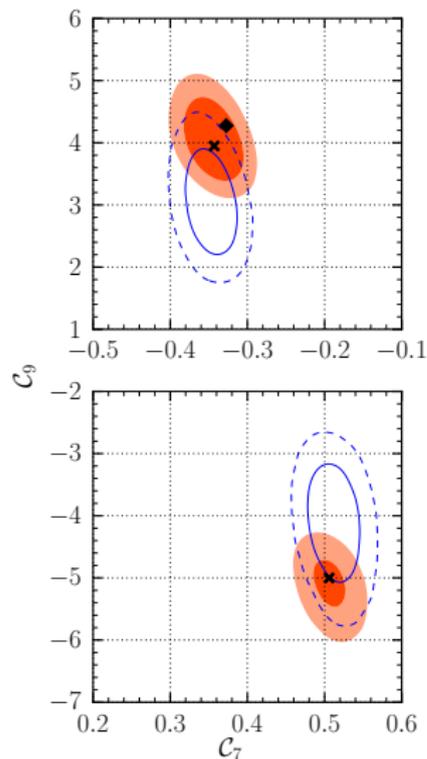
- 4.2σ (large-recoil), 3.5σ (large + low recoil), 2.7σ ([1-6] bin)
- same conclusions hold if P_i, P'_i, F_L rather than P_i, P'_i, A_{FB}

- Frequentist frame: $S_i, A_i, A_{FB}, Br(B \rightarrow K^* \mu \mu), Br(B^- \rightarrow K^- \mu \mu)$, with wide [1-6] at large recoil + low recoil
 $S_{K^* \gamma}, Br(B \rightarrow X_S \gamma), A_{CP}(b \rightarrow s \gamma), Br(B \rightarrow X_S \ell \ell), Br(B_S \rightarrow \mu \mu)$
- Amplitudes from full form factors LCSR [Ball, Zwicky]
 + non-factorisable corrections + $O(\Lambda/m_b)$ non fact.
- $C_9^{NP} \sim -0.9$ with less significance due to use of $S_i, [1,6]$ bins, F_L
- Need for $C_9^{NP} > 0$ due to low-recoil $B(B^- \rightarrow K^- \mu^+ \mu^-)$



“Equivalent analysis” for with LHCb
 $F_L, A_{FB}, S_{3,4,5,7,8}$ with three
 low-recoil bins (but no $B \rightarrow K \mu \mu$)

- 2.7σ for C_7^{NP}, C_9^{NP}
- Best fit point
 $C_7^{NP} = -0.02, C_9^{NP} = -1.76$
- No need for $C_9^{NP} \neq 0$

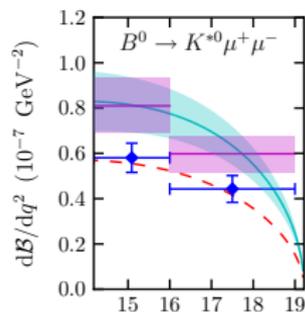


- Bayesian analysis: $P_i, F_L, A_{FB}, Br(B \rightarrow K^* \mu\mu), Br(B \rightarrow K \mu\mu), Br(B \rightarrow K^* \gamma), C_{K^* \gamma}, S_{K^* \gamma}, Br(B \rightarrow X_S \gamma), A_{CP}(b \rightarrow s \gamma), Br(B \rightarrow X_S \ell\ell), Br(B_S \rightarrow \mu\mu)$
 wide [1-6] at large recoil + low recoil
- Priors on nuisance parameters (form factors, Λ/m_b corrections)
- SM with decent p -values from χ^2_{\min} if shift of 10 – 20% Λ/m_b corrections to amplitudes (but N_{dof} ? asymptotic ?)
- 2 σ dev. from SM for NP in 7,9,10 only
 $C_7^{NP} = 0 \pm 0.02, C_9^{NP} = -0.3 \pm 0.4, C_{10}^{NP} = -0.4 \pm 0.3$
- Bayes factors favour NP in SM operators + chirally flipped operators, either generic or restricted to $(C_9, C_{9'})$

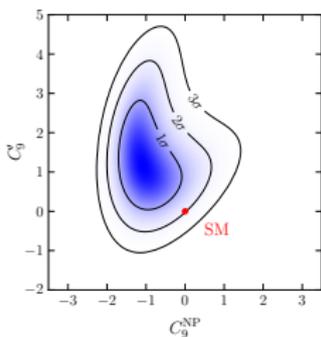
Analysis based on lattice QCD form factors

$B \rightarrow K^* ll$ and $B_s \rightarrow \phi ll$ form factors

[Horgan et al.]



- Lattice simulations (staggered + NRQCD)
- Main problem in BRs [\neq previous studies]
SM predictions 30% higher than experiment
(similar to results using [Ball, Zwicky])
(blue and pink : SM, dashed: $C_9^{NP} = -C_{9'}^{NP} = 1.1$)

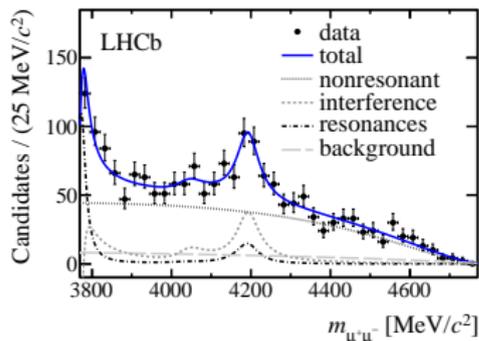
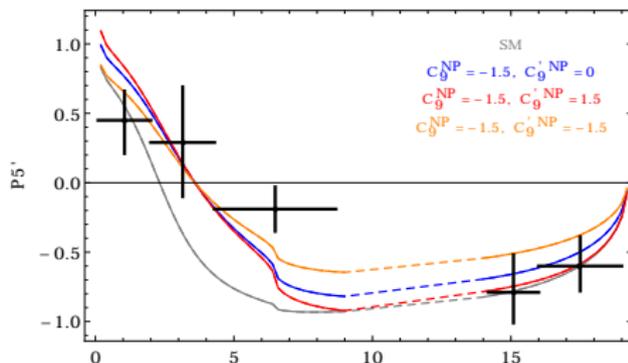


- Frequentist with only large-recoil $B_q \rightarrow V ll$:
 $d\Gamma/dq^2, F_L, S_3, S_4, S_5, A_{FB}$ for $B \rightarrow K^* ll$;
 $d\Gamma/dq^2, F_L, S_3$ for $B_s \rightarrow \phi ll$
- 2 low-recoil bins: $C_9^{NP} = -1.1 \pm 0.5, C_{9'}^{NP} = 1.1 \pm 1.0$
- Last low-recoil bin: $C_9^{NP} = -1.1 \pm 0.7, C_{9'}^{NP} = 0.4 \pm 0.7$

$C_{9'}^{NP} \sim 0$ or $C_{9'}^{NP} > 0$?

[1-6] bins for $B \rightarrow K^* \mu \mu$

- q^2 dependence of $P_{5'}$
- $C_{9'}^{NP} < 0$ better agreement for 1st and 3rd bins of $P_{5'}$
- $C_{9'}^{NP} > 0$ worse agreement for 1st and 3rd bins of $P_{5'}$
- integrated value over [1, 6] almost same: no sensitivity



Low-recoil $B(B^- \rightarrow K^- \mu^+ \mu^-)$

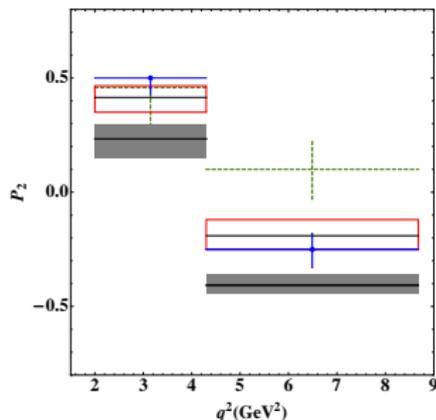
- [14,18,22] good agreement with SM
- favours $C_9^{NP} + C_{9'}^{NP} \simeq 0$, $C_{9'}^{NP} > 0$
- in [Altmannshofer, Straub], low-recoil 3 bins with 20% uncertainty to account for $\psi(4160)$ in first large-recoil bin

- Redundancy in angular coefficients

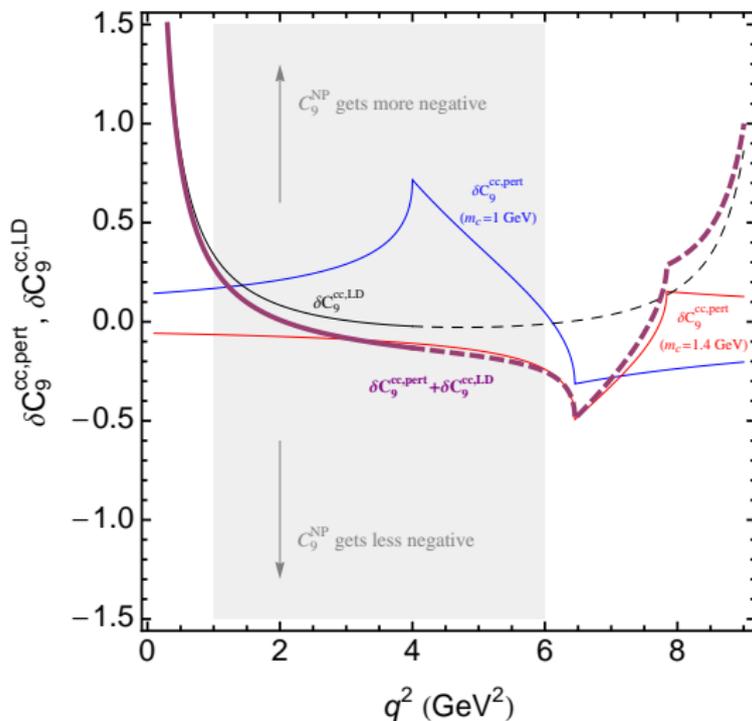
$$P_2 = \frac{1}{2} \left[P_4' P_5' + \frac{1}{\beta_\ell} \sqrt{(-1 + P_1 + P_4'^2)(-1 - P_1 + \beta_\ell^2 P_5'^2)} \right]$$

if no new CPV phase in C_i 's and negligible $P_{3,5',8'}$ ($Im[A_i A_j^*]$)

- Corrections from binning can be computed and are small, apart from [0.1-2] and [1-6] bins



- $\langle P_2 \rangle$: Gray: SM prediction, blue: data, red: $C_9^{NP} = -1.5$, green: relation
- [2.4,3]: 0.2σ measured vs relation
- [4.3,8.68]: 2.4σ measured vs relation, 1.9σ rel. vs NP best fit, 3.6σ rel. vs SM
- More consistent for (P_2, P_5') in the future if third-bin P_5' goes down (closer to SM) and third-bin P_2 goes up (away from SM)

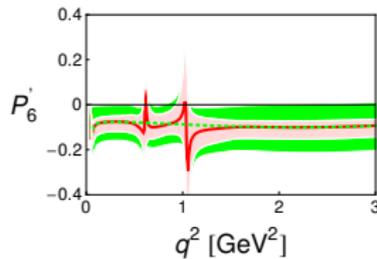
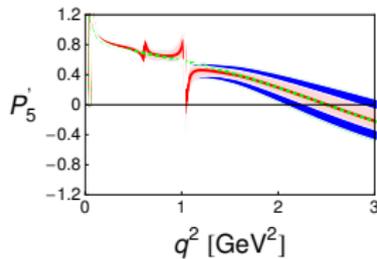
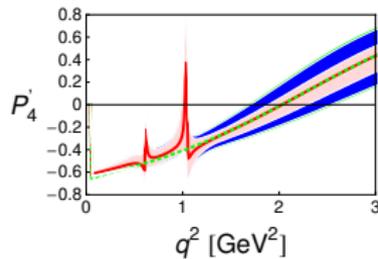


Shifts induced by change in m_c and long-distance gluons in $c\bar{c}$ loops

$1/m_b$ corrections

[Camalich, Jäger] SM preds with same central values but larger errors

- FF=soft form factor + $O(\alpha_s)$ corrections + $O(\Lambda/m_b)$
- Fix soft form factors $\xi_{\perp}, \xi_{\parallel}$ from 2 form factors [LCSR]
- Then compare predictions for the other form factors



- [Camalich, Jäger] assume $C_7 = C_7^{SM}$ and extract from $B(B \rightarrow K^* \gamma)$ the very accurate value $\xi_{\perp}(0) = T_1(0) = 0.277 \pm 0.013$
 \implies Need large $O(\Lambda/m_b)$ to predict other form factors in agreement with other approaches (LCSR, Dyson-Schwinger eqs. . . .)
- [SDG, Matias, Virto] $\xi_{\perp}(0) = 0.31^{+0.20}_{-0.10}$ from LCSR
10% $O(\Lambda/m_b)$ enough for QCDF and LCSR to agree for all FFs

Outlook

$b \rightarrow s\gamma(*)$ transition

- Very interesting playing ground for FCNC studies
- Many observables, more or less sensitive to hadronic unc.
- Intriguing LHCb results for $B \rightarrow K^* \mu\mu$, supporting $C_9^{NP} \neq 0$
- And a lot theoretical discussions on accuracy of computations and/or interpretation in terms of NP

How to improve ?

- Exp: finer binning in $[1, 6]$ region, other expts (ATLAS and CMS ?)
- Exp: refine $B \rightarrow K \mu\mu$ and impact of $\psi(4160)$
- Th: form factors from lattice on a larger q^2 range ?
- Th: $c\bar{c}$ loops, soft-gluon exchanges, quark/hadron duality
- Both: cross check with other modes/observables

Only the beginning of the story... more very soon !