

Constraining the CKM Angle γ at LHCb

*Laurence Carson, University of Edinburgh
on behalf of the LHCb Collaboration*

Rencontres de Moriond EW 2014

γ in Tree-Level B Decays

- γ is the least well-constrained angle of the CKM triangle.
- Fits in summer 2012 (before the inclusion of LHCb data) gave:

$$\gamma = 66 \pm 12^\circ \text{ (CKMFitter)}, \quad \gamma = 76 \pm 10^\circ \text{ (UTFit)}$$

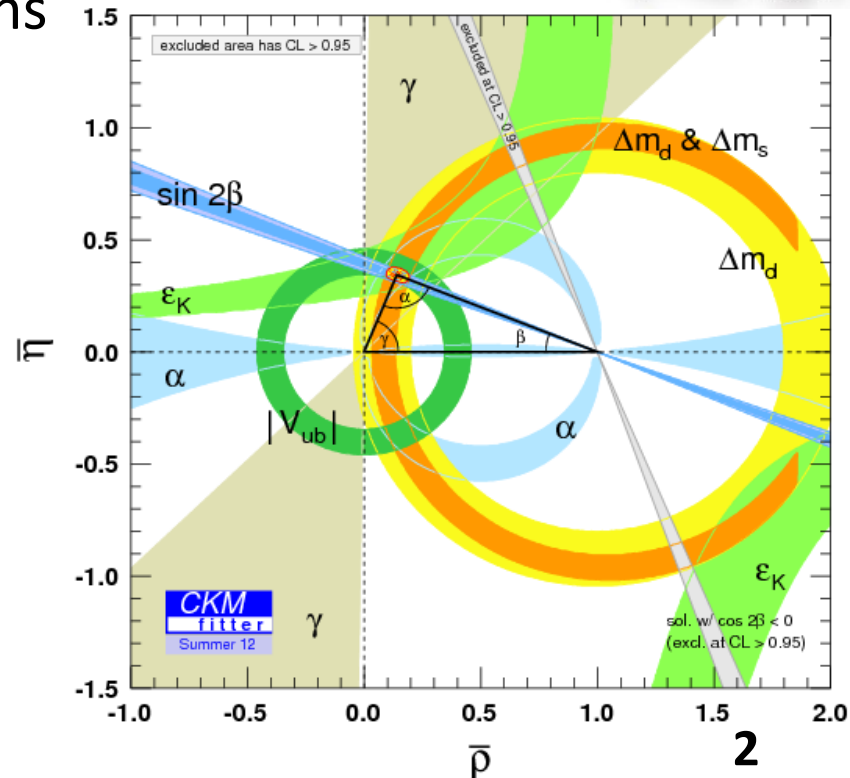
- Measurements of γ from B decays mediated only by tree-level transitions provide an “standard candle” for the Standard Model.

- This can be compared with γ values from B decays involving loop-level transitions

– For example $B^0_{(s)} \rightarrow hh'$ decays

- Significant difference between these would indicate New Physics contribution to the loop process.

$$\gamma = -\arg \left(\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right)$$

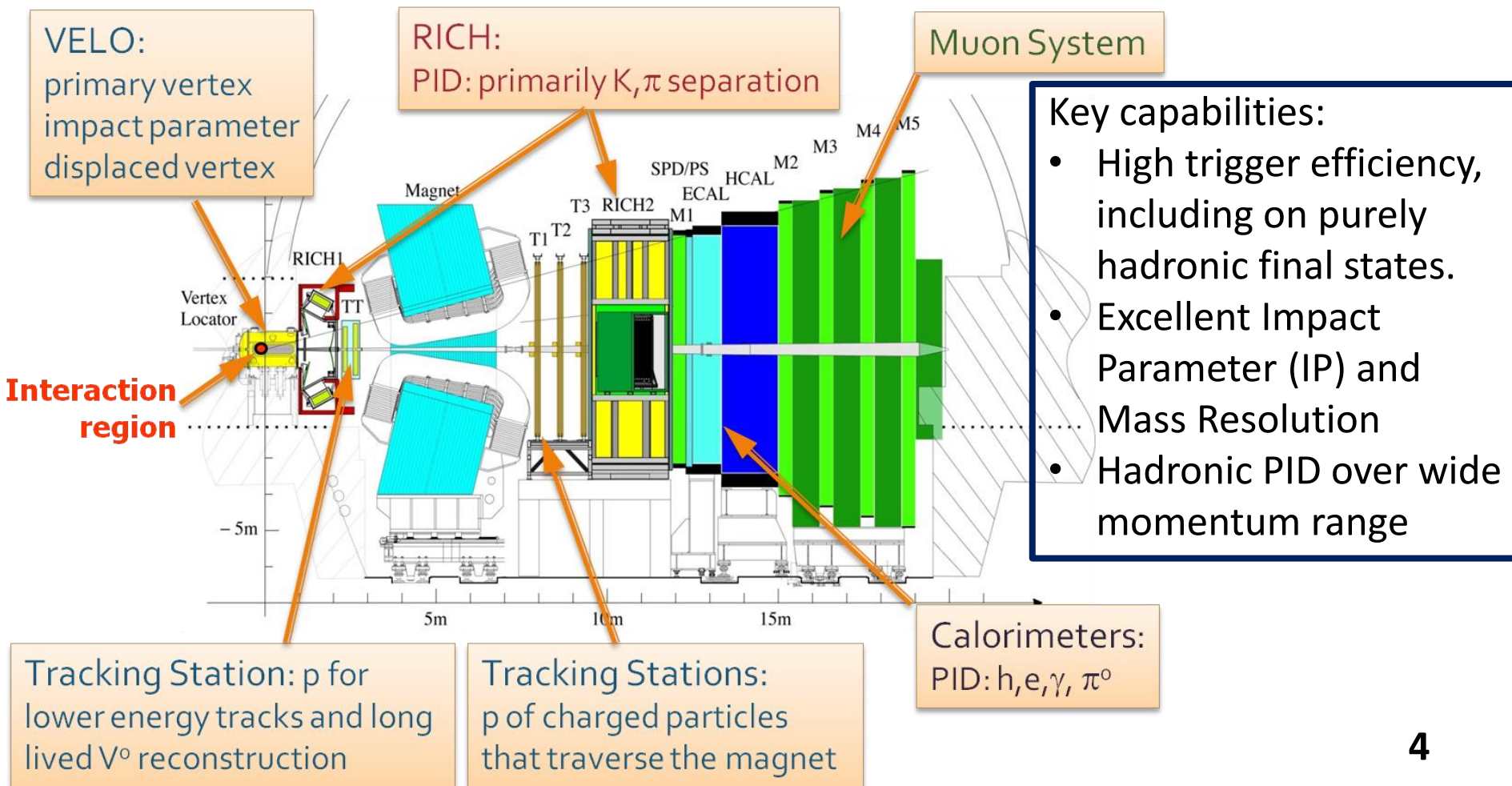


Menu of Results

- LHCb gamma combination from time-independent methods, using $B^+ \rightarrow D^0 K^+$ and $B^+ \rightarrow D^0 \pi^+$ (Phys. Lett. **B 726** (2013) 151), and updated preliminary combination using $B^+ \rightarrow D^0 K^+$ only (LHCb-CONF-2013-006)
- Time-independent γ measurement with 3/fb, using $B^+ \rightarrow D^0 K^+$ and $B^+ \rightarrow D^0 \pi^+$ with $D^0 \rightarrow K_S K \pi$ (LHCb-PAPER-2013-068, submitted to Phys. Lett. **B**) **NEW!**
- First observation of $B_s \rightarrow \bar{D}^0 \varphi$ (Phys. Lett. **B 727** (2013) 403)
- Studies of beauty baryon decays to $D^0 p h$ and $\Lambda_c h$ (Phys. Rev. **D 89** (2014) 032001)
- Studies of beauty baryon decays to pairs of charm hadrons (LHCb-PAPER-2014-002, submitted to Phys. Rev. Lett.) **NEW!**

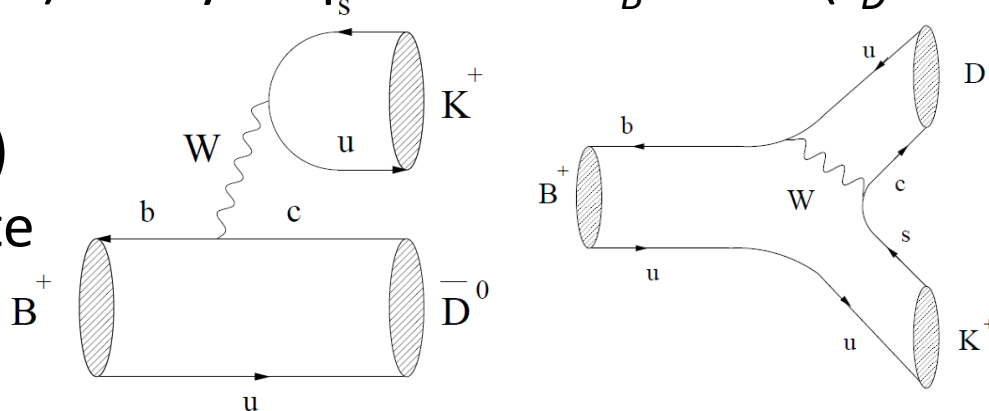
The LHCb Experiment

- Forward arm spectrometer, optimised for study of B and D decays.
- Collected 1/fb of data at $E_{CM} = 7$ TeV in 2011 and 2/fb at 8 TeV in 2012



Time-Integrated Methods

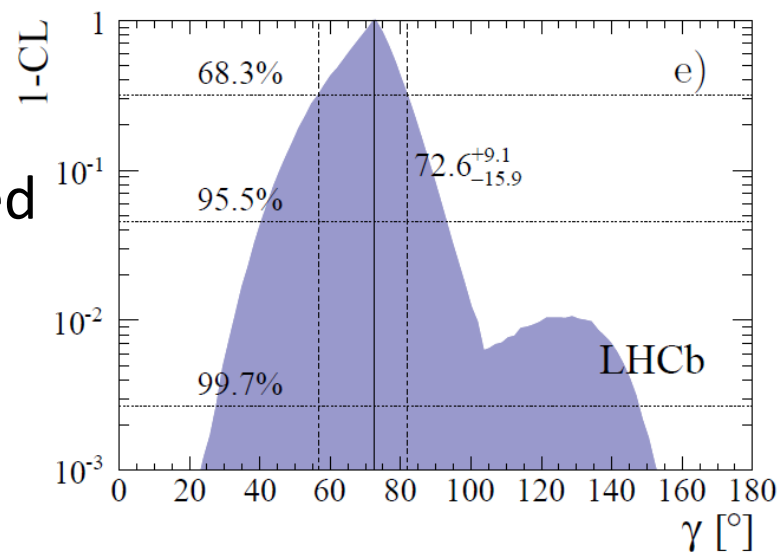
- Sensitivity to γ from interference between $b \rightarrow c$ and $b \rightarrow u$ transitions at tree level, when D final state is accessible to both D^0 and \bar{D}^0
- Aside from γ , have hadronic unknowns $r_{B(D)}$, $\delta_{B(D)}$, where ratio of suppressed to favoured $B(D)$ decay amplitudes is $r_B e^{i(\delta_B - \gamma)} (r_D e^{i\delta_D})$
- Method to extract these hadronic unknowns (and γ) depends on the D final state



- Three main methods:
- **GLW**: $D \rightarrow$ CP-eigenstate, e.g. $\pi\pi$, KK (Phys. Lett. **B 253** (1991) 483, Phys. Lett. **B 265** (1991) 172)
- **ADS**: $D \rightarrow$ quasi-flavour-specific state, e.g. $K\pi$, $K\pi\pi\pi$ (Phys. Rev. Lett. **78** (1997) 257, Phys. Rev. **D 63** (2001) 036005)
- **GGSZ**: $D \rightarrow$ self-conjugate 3-body final state, e.g. $K_S\pi\pi$, $K_S KK$ (Phys. Rev. **D 68** (2003) 054018, Phys. Rev. **D 70** (2004) 072003)

Gamma Combination

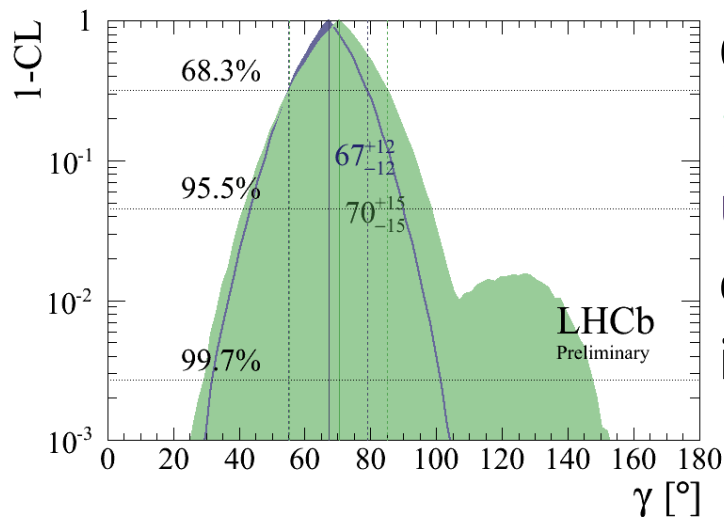
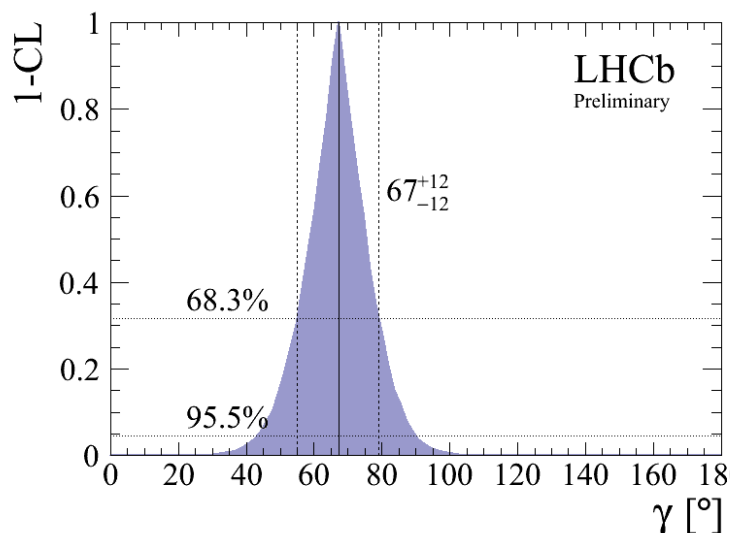
- The published LHCb combination uses analyses of $B \rightarrow Dh$ with:
 - $D \rightarrow K\pi$, KK or $\pi\pi$ using 1/fb (Phys. Lett. **B 712** (2012) 203),
 - $D \rightarrow K\pi\pi\pi$ using 1/fb (Phys. Lett. **B 723** (2012) 44),
 - $D \rightarrow K_S KK$ or $K_S\pi\pi$ using 1/fb (Phys. Lett. **B 718** (2012) 43),
 - Plus CLEO data on $D \rightarrow K\pi\pi\pi$ strong phase (Phys. Rev. **D 80** (2009) 031105)
- The experimental likelihoods are combined as $\mathcal{L}(\vec{\alpha}) = \prod_i f_i(\vec{A}_i^{\text{obs}} | \vec{A}_i(\vec{\alpha}_i))$, where A are the experimental observables (R_{CP} , x_+ , etc) and α are the physics parameters (γ , r_B , etc).
- Confidence intervals are rescaled, to account for undercoverage and neglected correlations between systematics.
- The effects of $D^0-\bar{D}^0$ mixing, and of possible CPV in the D decays, are taken into account.



68% CL confidence interval using DK and $D\pi$ is: $\gamma \in [55.4, 82.3]^\circ$ **6**

Gamma Combination

- There is also a more recent, preliminary LHCb combination.
- This uses analyses of $B \rightarrow DK$ from the same analyses as the published combination, adding the information from an updated analysis with $D \rightarrow K_S KK$ or $K_S \pi \pi$ using the 3/fb dataset (LHCb-CONF-2013-004).
- Preliminary result is $\gamma = 67 \pm 12^\circ$



Comparison of
1/fb-only and
updated
 confidence
 intervals for DK

- These results lead to updated CKM fits:

$$\gamma = 68.0^{+8.0}_{-8.5}^\circ \quad (\text{CKMFitter, FPCP 2013}),$$

$$\gamma = 70.1 \pm 7.1^\circ \quad (\text{UTFit, EPS 2013}).$$

Observables for $B^+ \rightarrow D^0 (\rightarrow K_S K \pi) h^+$

NEW!

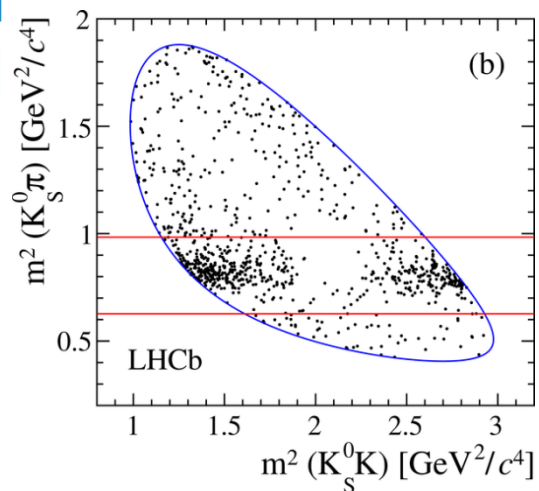
- This is the first ADS-like analysis to use Singly-Cabibbo-Suppressed (SCS) modes. Label final states as OS or SS comparing K^\pm with B^\pm
- Analysing three-body D final state requires knowledge of how the average interference amplitude ($\kappa_{K_S K \pi}$) and strong phase difference ($\delta_{K_S K \pi}$) vary across the D Dalitz plot
 - This is taken from a CLEO-c measurement, Phys. Rev. **D 85** (2012) 092016

- Decay rates for $B^+ \rightarrow D^0 K^+$ are:

$$\Gamma_{SS, DK}^\pm = z \left[1 + r_B^2 r_D^2 + 2 r_B r_D \kappa_{K_S^0 K \pi} \cos(\delta_B \pm \gamma - \delta_{K_S^0 K \pi}) \right]$$

$$\Gamma_{OS, DK}^\pm = z \left[r_B^2 + r_D^2 + 2 r_B r_D \kappa_{K_S^0 K \pi} \cos(\delta_B \pm \gamma + \delta_{K_S^0 K \pi}) \right]$$

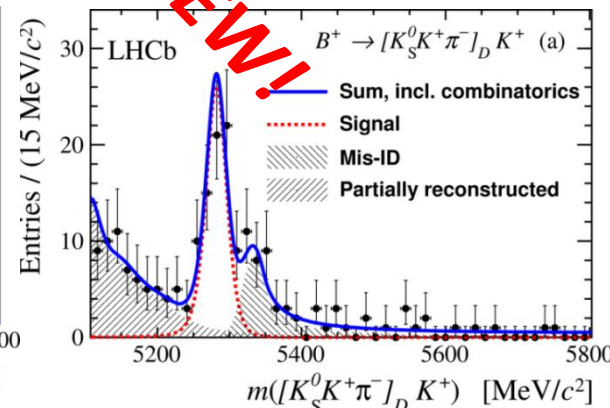
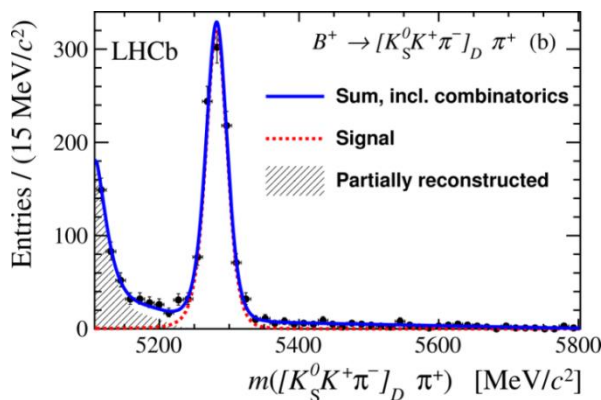
- Measure yield ratios (e.g. $\mathcal{R}_{DK/D\pi, SS}$) and charge asymmetries (e.g. $\mathcal{A}_{SS, DK}$) between the OS and SS samples, and between DK and $D\pi$ final states.
- Analysis is done across whole Dalitz plane, and in a restricted region around the $K^{*\pm}$ resonance, where the coherence factor $\kappa_{K_S K \pi}$ is higher (≈ 1.0 vs ≈ 0.7).



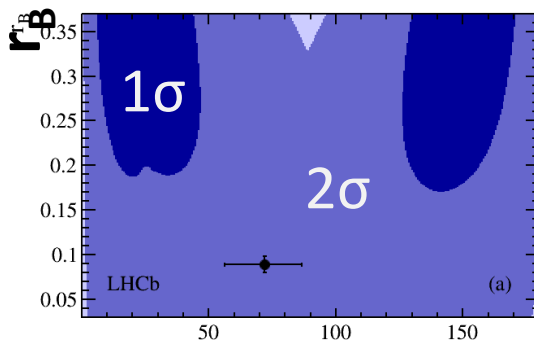
Results for $B^+ \rightarrow D^0(\rightarrow K_S K \pi) h^+$

NEW!

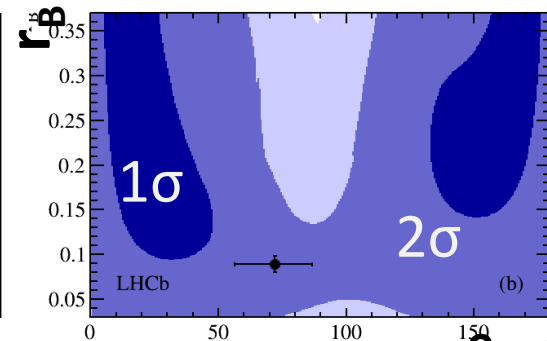
- Measure 8 yields, with $B^+ \rightarrow D^0 K^+$ and $B^+ \rightarrow D^0 \pi^+$ separated by OS/SS and charge of B^\pm
- Charge-summed yields for OS and SS $D^0 K^+$ are 71 and 145 respectively.
- Sensitivity to γ appears to be improved by taking $K^{*\pm}$ region, due to higher coherence factor.
- Good prospects for future analysis of $K^{*\pm}$ region with more statistics.



Observable	Whole Dalitz plot	$K^*(892)^\pm$ region
$\mathcal{R}_{SS/OS}$	$1.528 \pm 0.058 \pm 0.025$	$2.57 \pm 0.13 \pm 0.06$
$\mathcal{R}_{DK/D\pi, SS}$	$0.092 \pm 0.009 \pm 0.004$	$0.084 \pm 0.011 \pm 0.003$
$\mathcal{R}_{DK/D\pi, OS}$	$0.066 \pm 0.009 \pm 0.002$	$0.056 \pm 0.013 \pm 0.002$
$A_{SS, DK}$	$0.040 \pm 0.091 \pm 0.018$	$0.026 \pm 0.109 \pm 0.029$
$A_{OS, DK}$	$0.233 \pm 0.129 \pm 0.024$	$0.336 \pm 0.208 \pm 0.026$
$A_{SS, D\pi}$	$-0.025 \pm 0.024 \pm 0.010$	$-0.012 \pm 0.028 \pm 0.010$
$A_{OS, D\pi}$	$-0.052 \pm 0.029 \pm 0.017$	$-0.054 \pm 0.043 \pm 0.017$



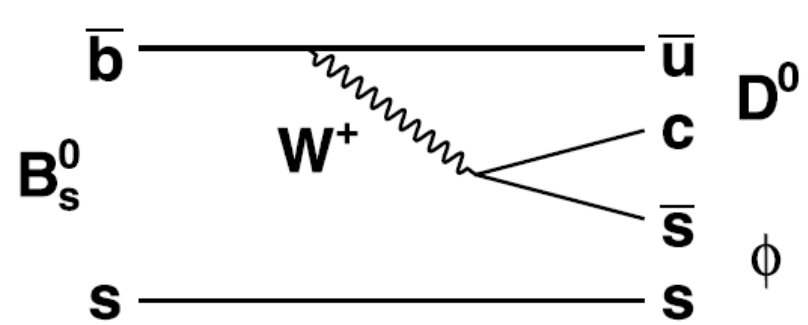
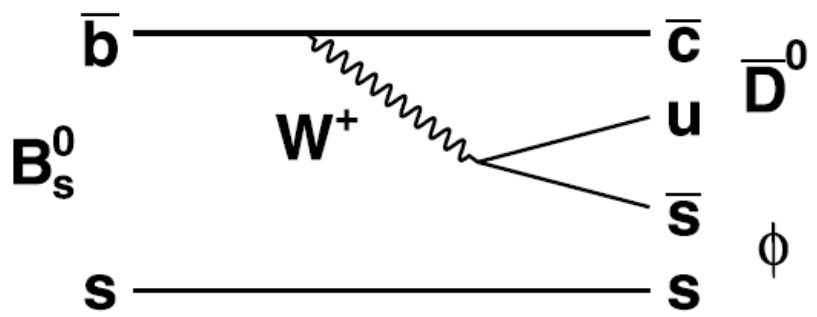
Whole Dalitz plot γ



$K^{*\pm}$ region γ

Observation of $B_s \rightarrow \bar{D}^0 \phi$

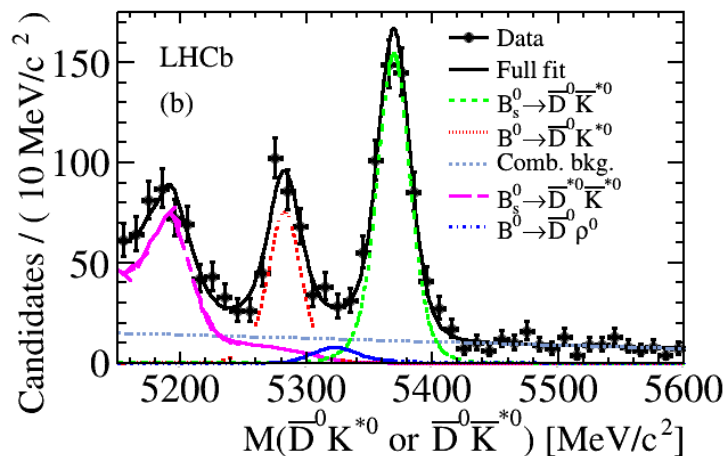
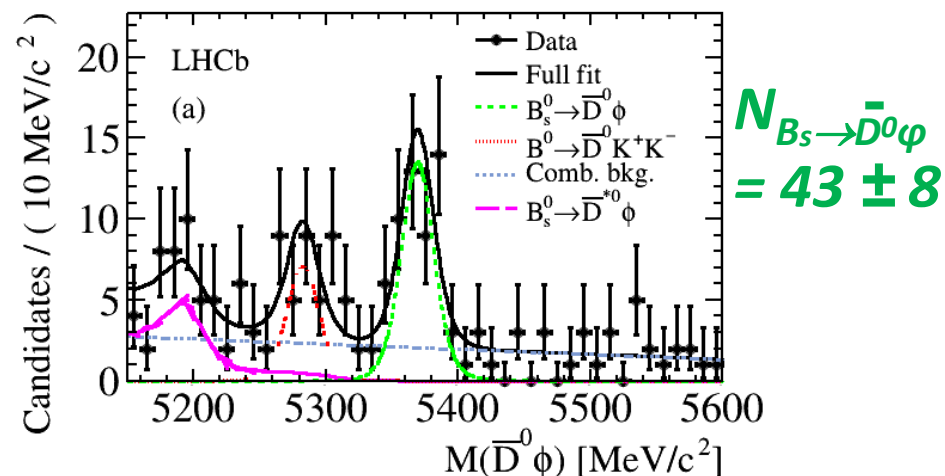
- Time-dependent analysis of the $B_s \rightarrow \bar{D}^0 \phi$ decay can measure γ and φ_s (Phys. Lett. **B 253** (1991) 483).
- Using the now-known sign of $\Delta\Gamma_s$, this determination can be made unambiguous (Phys. Rev. **D 85** (2012) 114015).
- A time-*in*dependent analysis can also measure γ , provided enough D^0 final states are included (Phys. Rev. **D 69** (2004) 113003, Phys. Lett. **B 649** (2007) 61). This has advantages for LHCb, as it means flavour-tagging is not required.



- First step is to make the first observation of the decay, using the Cabibbo-favoured $\bar{D}^0 \rightarrow K^+ \pi^-$ decay mode.

Observation of $B_s \rightarrow \bar{D}^0 \phi$

- LHCb searched for $B_s \rightarrow \bar{D}^0 \phi$ with a blind analysis of 1/fb of data.
- First observation of $B_s \rightarrow \bar{D}^0 \phi$ is made, with significance of 6.5σ .



- Branching fraction (\mathcal{B}) is measured relative to the $B_d \rightarrow \bar{D}^0 K^{*0}$ decay. Also improve the measurement of $\mathcal{B}(B_s \rightarrow \bar{D}^0 \bar{K}^{*0})$ relative to $B_d \rightarrow \bar{D}^0 K^{*0}$:

$$\mathcal{B}(B_s^0 \rightarrow \bar{D}^0 \phi) = [2.3 \pm 0.4 \text{ (stat)} \pm 0.2 \text{ (syst)} \pm 0.2 (f_s/f_d) \pm 0.3 (\mathcal{B}(B^0 \rightarrow \bar{D}^0 K^{*0}))] \times 10^{-5},$$

$$\mathcal{B}(B_s^0 \rightarrow \bar{D}^0 \bar{K}^{*0}) = [3.3 \pm 0.3 \text{ (stat)} \pm 0.1 \text{ (syst)} \pm 0.3 (f_s/f_d) \pm 0.5 (\mathcal{B}(B^0 \rightarrow \bar{D}^0 K^{*0}))] \times 10^{-4}.$$

- With more data, can add more D^0 final states, such as KK , $\pi\pi$, $K_S\pi\pi$, ...

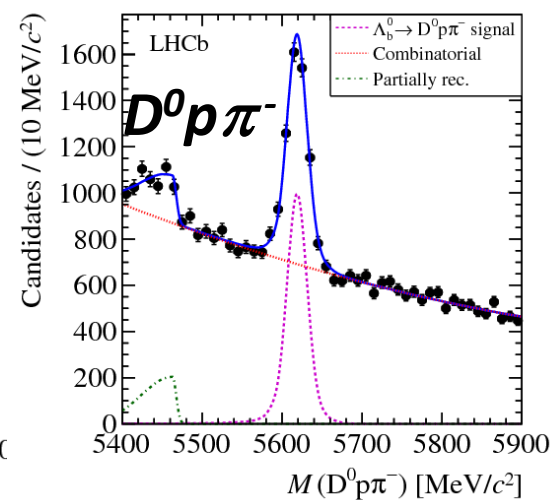
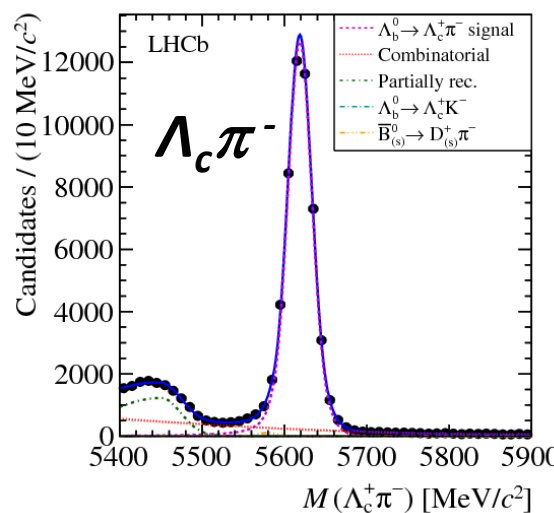
Baryon Decays to $D^0 p h$, $\Lambda_c h$

- Beauty baryon sector remains largely unexplored.
- Decays such as $\Lambda_b \rightarrow D^0 \Lambda$ and $\Lambda_b \rightarrow D^0 p K^-$ can be used to measure γ (Z. Phys. C **56** (1992) 129, Mod. Phys. Lett. A **14** (1999), Phys. Rev. D **65** (2002) 073029)
- LHCb has studied beauty baryon decays to $D^0 p h^-$ and $\Lambda_c h^-$ final states, using 1/fb of data.
- The Cabibbo-favoured final states $D^0 \rightarrow K^- \pi^+$ and $\Lambda_c \rightarrow p K^- \pi^+$ are used.
- Common $p K^- \pi^+ h$ final state reduces systematic uncertainties.

• Firstly, use a loose, cut-based selection to measure:

$$\begin{aligned} & \frac{\mathcal{B}(\Lambda_b^0 \rightarrow D^0 p \pi^-) \times \mathcal{B}(D^0 \rightarrow K^- \pi^+)}{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^-) \times \mathcal{B}(\Lambda_c^+ \rightarrow p K^- \pi^+)} \\ & = 0.0806 \pm 0.0023 \pm 0.0035 \end{aligned}$$

(factoring out poorly-known $\mathcal{B}(\Lambda_c \rightarrow p K^- \pi^+)$)



Baryon Decays to $D^0 p h$, $\Lambda_c h$

- Tighter selection (with BDT) used to make the first observations of $\Lambda_b \rightarrow D^0 p K^-$ (9.0σ) and $\Xi_b \rightarrow D^0 p K^-$ (5.9σ), and measure:

$$\frac{\mathcal{B}(\Lambda_b^0 \rightarrow D^0 p K^-)}{\mathcal{B}(\Lambda_b^0 \rightarrow D^0 p \pi^-)} = 0.073 \pm 0.008^{+0.005}_{-0.006},$$

$$\frac{f_{\Xi_b^0} \times \mathcal{B}(\Xi_b^0 \rightarrow D^0 p K^-)}{f_{\Lambda_b^0} \times \mathcal{B}(\Lambda_b^0 \rightarrow D^0 p K^-)} = 0.44 \pm 0.09 \pm 0.06$$

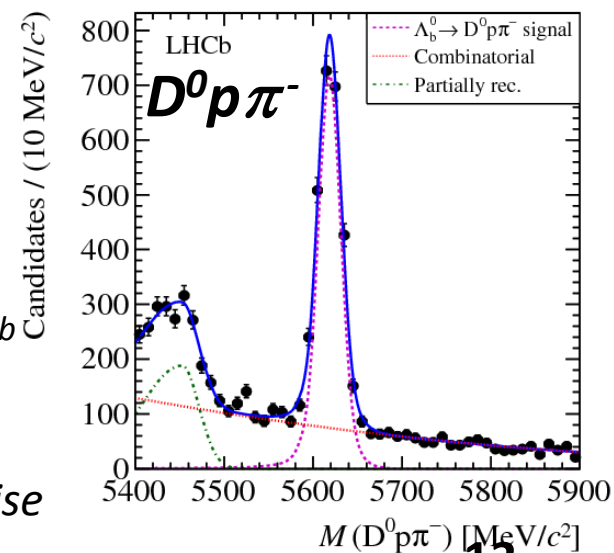
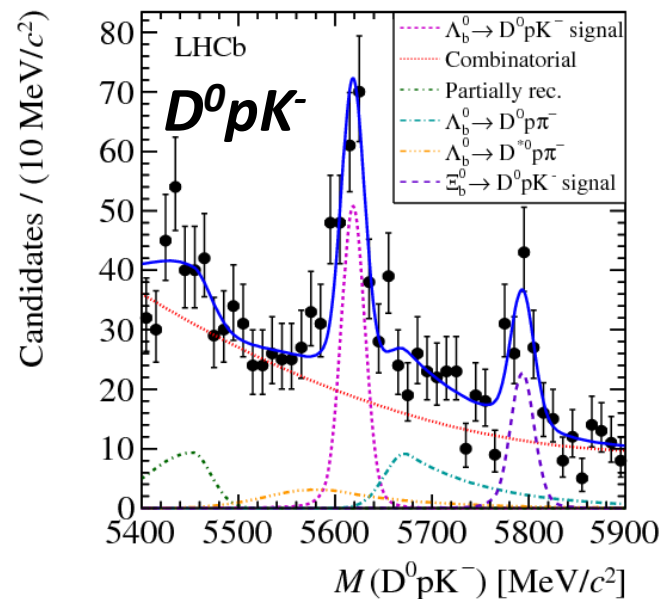
- The $D^0 p K^-$ spectrum can also be used to measure the mass difference:

$$m_{\Xi_b^0} - m_{\Lambda_b^0} = 174.8 \pm 2.4 \pm 0.5 \text{ MeV}/c^2$$

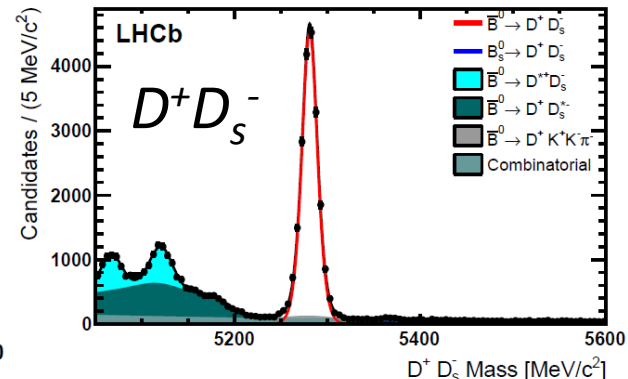
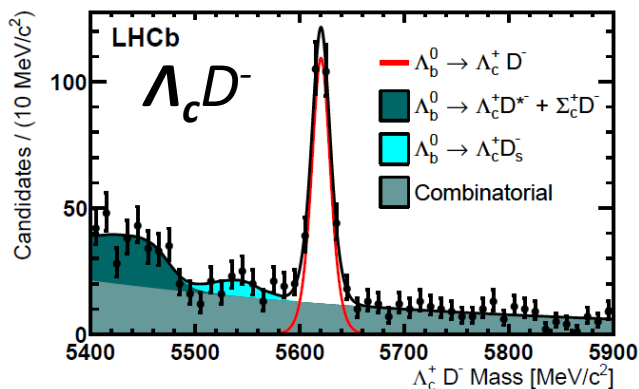
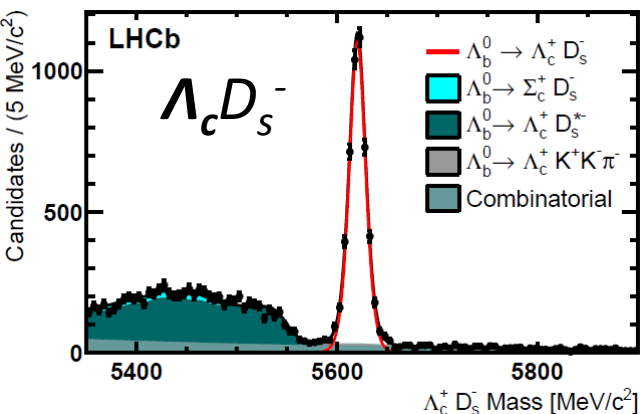
(Systematic is dominated by background modelling in mass fit)

- Combining with the LHCb measurement of m_{Λ_b} using $\Lambda_b \rightarrow J/\psi \Lambda$ (PRL 110 (2013) 182001) gives:

$$m_{\Xi_b^0} = 5794.3 \pm 2.4 \pm 0.7 \text{ MeV}/c^2 \quad \text{Most precise to date!}$$



- Another showcase for LHCb's capabilities with beauty baryons is the analysis of their decays to pairs of charm hadrons, using 3/fb.
- Events are selected using a BDT trained on signal decays to the relevant single charm hadron: $B_d \rightarrow D^- \pi^+$, $B_s \rightarrow D_s^- \pi^+$ or $\Lambda_b \rightarrow \Lambda_c \pi^-$.
- Clear first observations are made of the decays $\Lambda_b \rightarrow \Lambda_c D_s^-$ (CF) and $\Lambda_b \rightarrow \Lambda_c D^-$ (SCS), with:
$$\frac{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ D^-)}{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ D_s^-)} = 0.042 \pm 0.003 \text{ (stat)} \pm 0.003 \text{ (syst)}$$



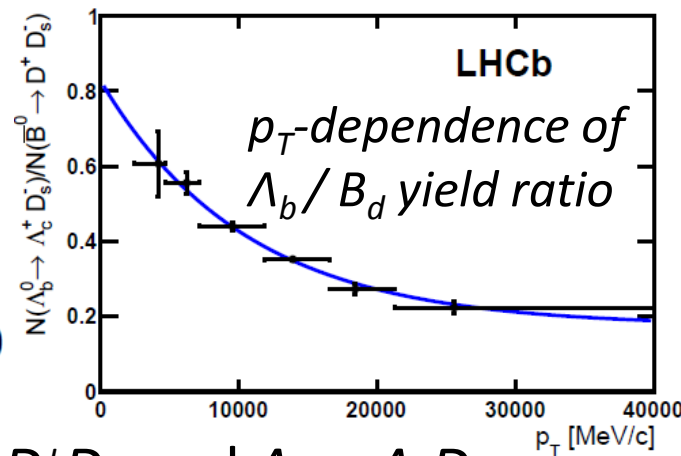
- The Λ_b branching fractions can be normalised to $\bar{B}_d \rightarrow D^+ D_s^-$, but the fragmentation fraction ratio f_{Λ_b}/f_d is known to depend on the p_T of the b-hadron (LHCb, Phys. Rev. **D 85** (2012) 032008)...

- Adopting the p_T -dependence of f_{Λ_b}/f_d measured by LHCb using $B_d \rightarrow D^- \pi^+$ and $\Lambda_b \rightarrow \Lambda_c^- \pi^+$ (LHCb-PAPER-2012-004, in preparation), the double ratio is measured:

$$\left[\frac{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ D_s^-)}{\mathcal{B}(\bar{B}^0 \rightarrow D^+ D_s^-)} \right] / \left[\frac{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^-)}{\mathcal{B}(\bar{B}^0 \rightarrow D^+ \pi^-)} \right] = 0.96 \pm 0.02 \text{ (stat)} \pm 0.06 \text{ (syst)}.$$

- In addition, the modes $B_{\{d,s\}} \rightarrow \Lambda_c^+ \Lambda_c^-$ are searched for, and no significant signal is found. The following 95% C.L. limits are set:

$$\frac{\mathcal{B}(\bar{B}^0 \rightarrow \Lambda_c^+ \Lambda_c^-)}{\mathcal{B}(\bar{B}^0 \rightarrow D^+ D_s^-)} < 0.0022, \quad \frac{\mathcal{B}(B_s^0 \rightarrow \Lambda_c^+ \Lambda_c^-)}{\mathcal{B}(B_s^0 \rightarrow D^+ D_s^-)} < 0.30$$



- Finally, the very similar Q-values of the $\bar{B}_d \rightarrow D^+ D_s^-$ and $\Lambda_b \rightarrow \Lambda_c^- D_s^-$ decays allows a precise measurement of the mass difference:

$$M(\Lambda_b^0) - M(\bar{B}^0) = 339.72 \pm 0.24 \text{ (stat)} \pm 0.18 \text{ (syst)} \text{ MeV}/c^2.$$

Dominant syst is due to $\tau(D^+) \gg \tau(\Lambda_c)$

- Using the World Average B_d mass gives the most precise result to date for the absolute Λ_b mass: $M(\Lambda_b^0) = 5619.30 \pm 0.34 \text{ MeV}/c^2$

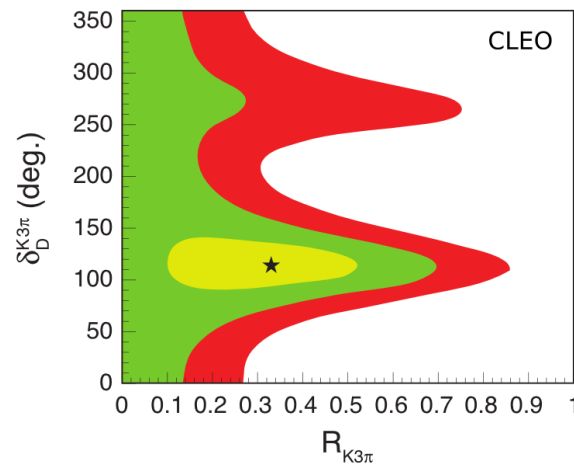
Summary & Prospects

- Preliminary LHCb γ combination with $B^+ \rightarrow D^0 K^+$ decays, using various methods (ADS, GLW, GGSZ) gives $\gamma = 67 \pm 12^\circ$, more precise than the B-factory measurements.
- At the moment, no one method dominates the sensitivity.
- Always looking to add new B decays, and new D final states
 - First constraints on γ with $B^+ \rightarrow D^0 (\rightarrow K_S K \pi) h^+$ just submitted to PLB
 - Promising new mode $B_s \rightarrow \bar{D}^0 \varphi$ now observed
- Wealth of measurements now being done with b -baryons, may throw up some interesting surprises.
- Stay tuned for more results in the future!
 - Many measurements are awaiting the inclusion of the 2.0/fb collected at 8 TeV in 2012

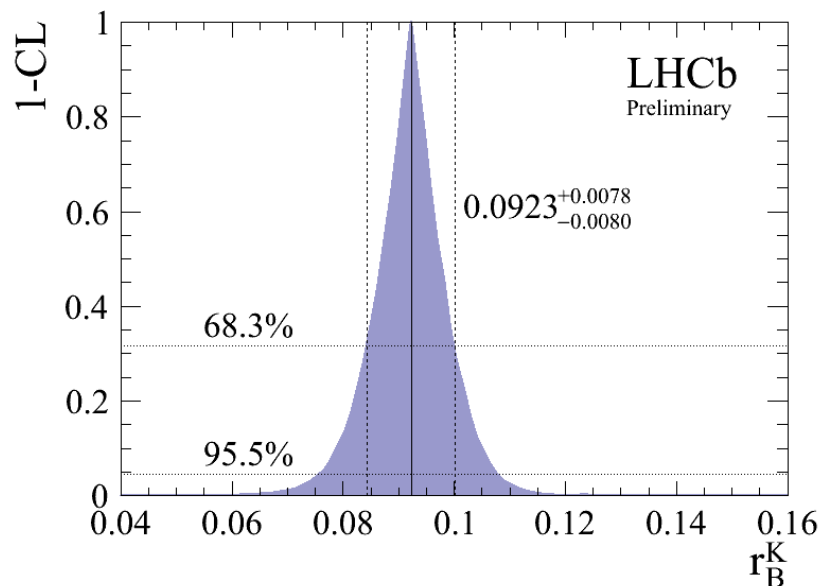
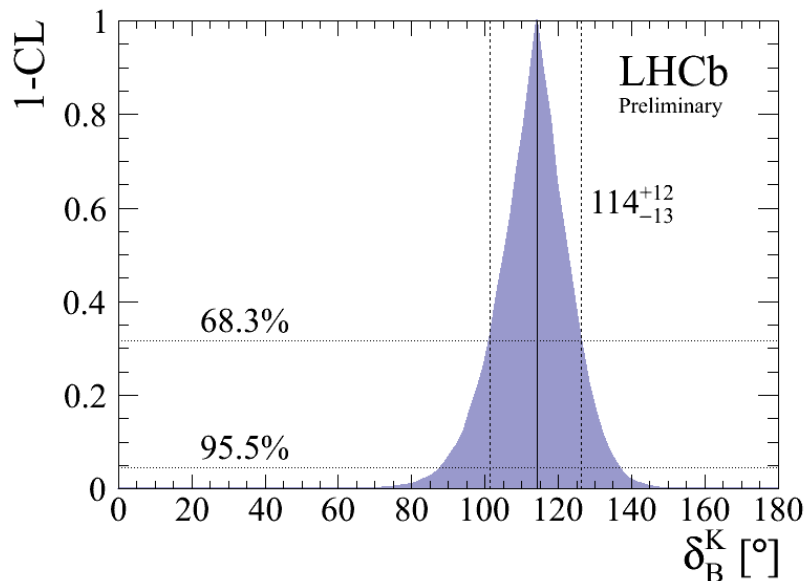
Backup

Gamma Combination

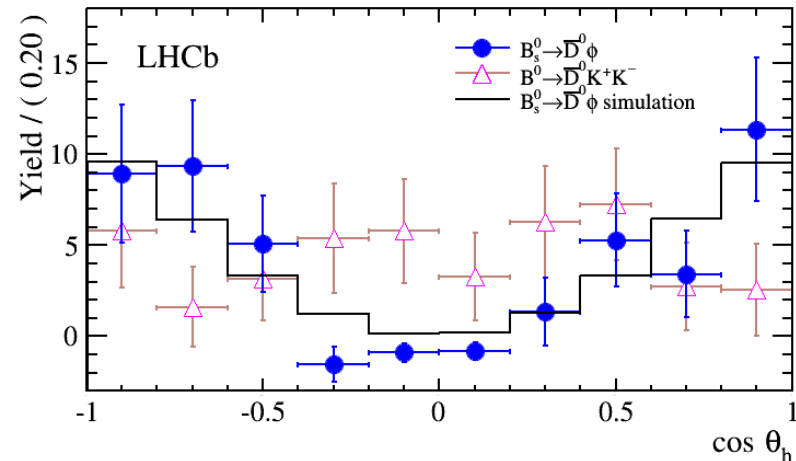
- CLEO-c result on $D \rightarrow K \pi \pi \pi$:



- Other parameters measured:

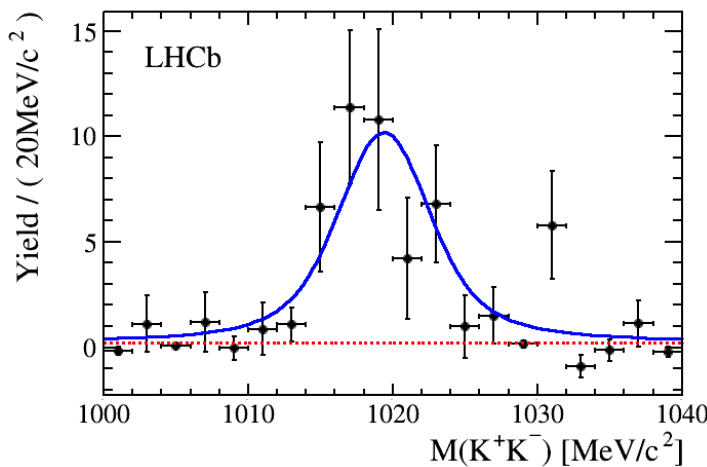


- Distribution of the helicity angle for selected signal events shows that the B_s mass region is dominated by a vector resonance, as expected for a final state. In contrast in the B_d mass region is not.



- The B_d distribution supports what was seen in the LHCb paper on the discovery of the $B_d \rightarrow \bar{D}^0 K^+ K^-$ decay, Phys. Rev. Lett. **109** (2012) 131801.

- The B_s distribution is reinforced by the $m(KK)$ distribution in the B_s region:

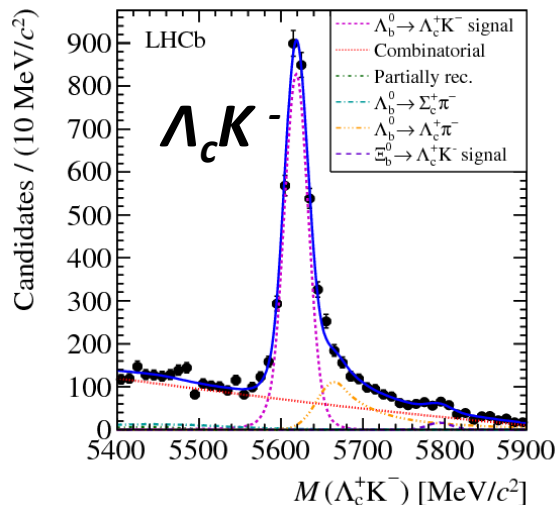
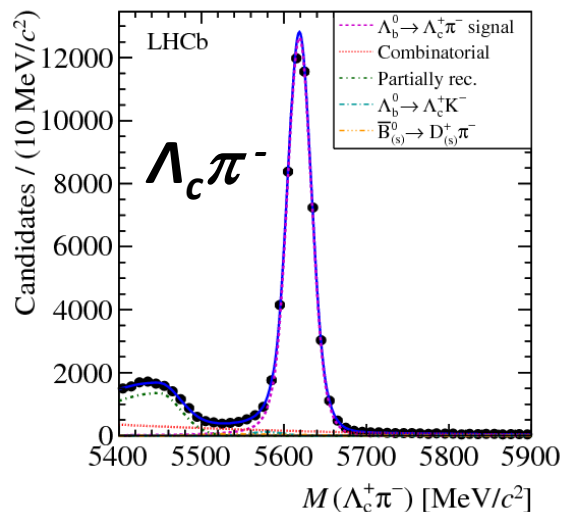


Baryon Decays to $D^0 p h$, $\Lambda_c h$

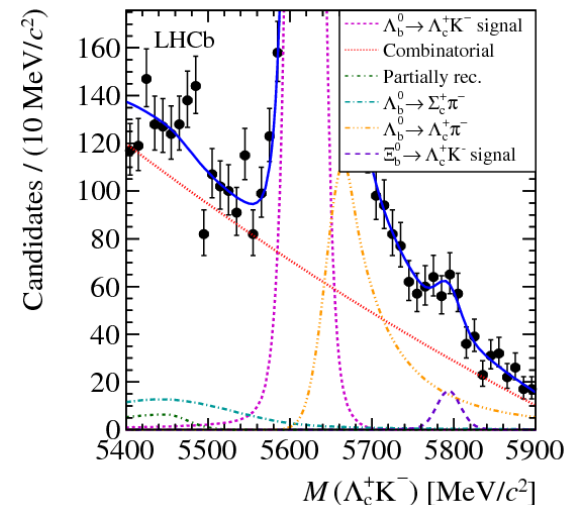
- The tighter selection is also applied to the $\Lambda_c h^-$ spectra, to clearly observe $\Lambda_b \rightarrow \Lambda_c K^-$, and find evidence for $\Xi_b \rightarrow \Lambda_c K^-$ (3.3σ):

$$\frac{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ K^-)}{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^-)} = 0.0731 \pm 0.0016 \pm 0.0016,$$

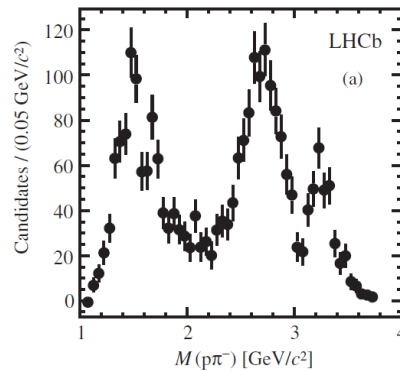
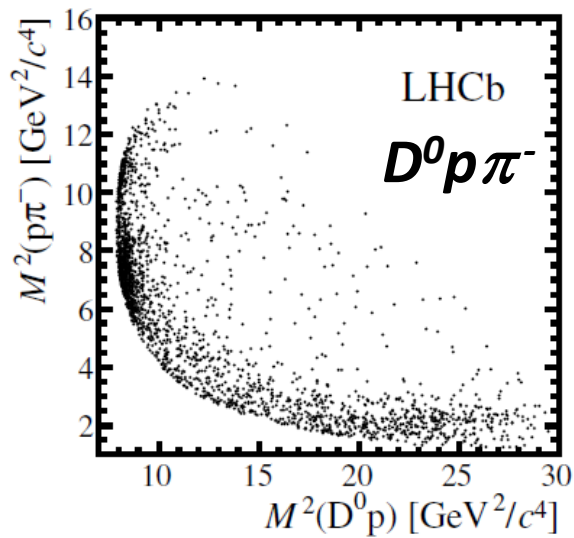
$$\frac{\mathcal{B}(\Xi_b^0 \rightarrow \Lambda_c^+ K^-) \times \mathcal{B}(\Lambda_c^+ \rightarrow p K^- \pi^+)}{\mathcal{B}(\Xi_b^0 \rightarrow D^0 p K^-) \times \mathcal{B}(D^0 \rightarrow K^- \pi^+)} = 0.57 \pm 0.22 \pm 0.21$$



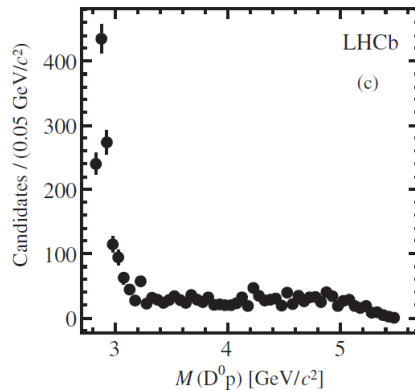
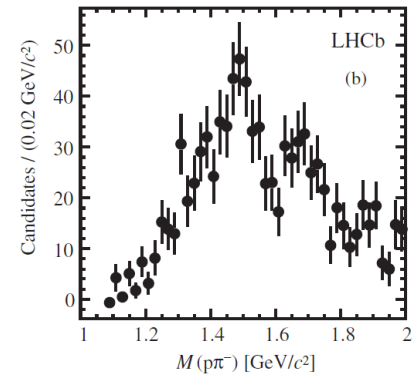
zoom
 $\Lambda_c K^-$
→



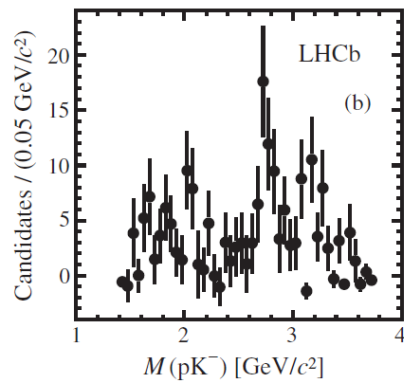
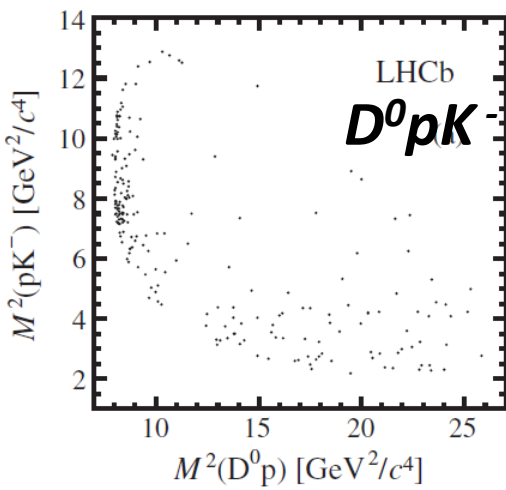
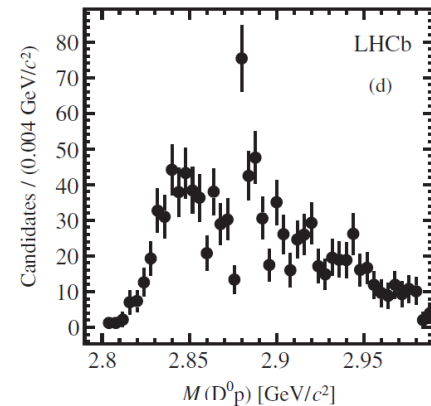
$\Lambda_b \rightarrow D^0 p h^-$ Dalitz Plots



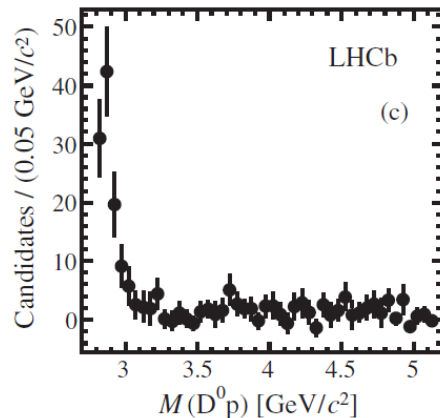
zoom to low-mass



zoom to low-mass



$m(pK^-)$



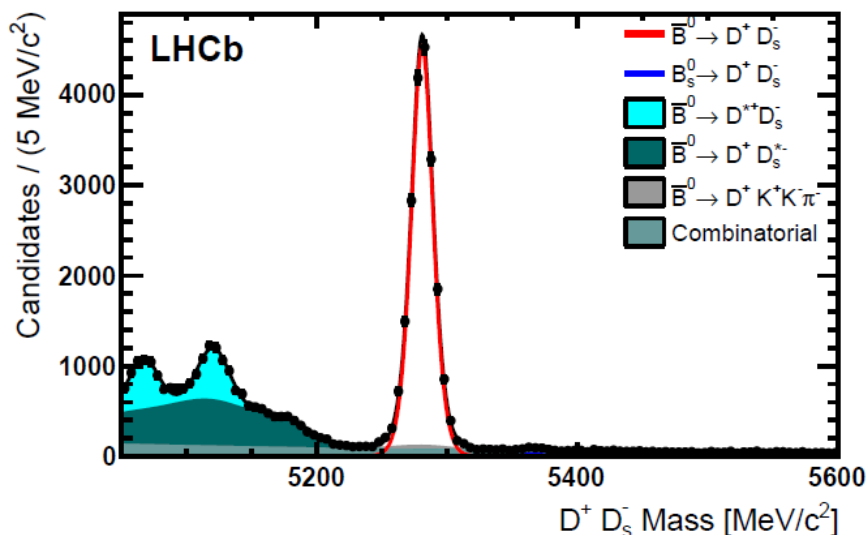
$m(D^0 p)$ 21

$\mathcal{B}(B_s \rightarrow D^+ D_s^-)$ Measurement

- The “two charm hadrons” analysis also makes the most precise measurement of $\mathcal{B}(B_s \rightarrow D^+ D_s^-)$:

$$\frac{\mathcal{B}(B_s^0 \rightarrow D^+ D_s^-)}{\mathcal{B}(\bar{B}^0 \rightarrow D^+ D_s^-)} = 0.038 \pm 0.004 \text{ (stat)} \pm 0.003 \text{ (syst)}.$$

$$\mathcal{B}(B_s^0 \rightarrow D^+ D_s^-) = (2.7 \pm 0.5) \times 10^{-4}$$



zoom
y-axis
→

