

## High SUSY scale and a few-parameter description of the scalar sector

J eremie Quevillon, LPT Orsay

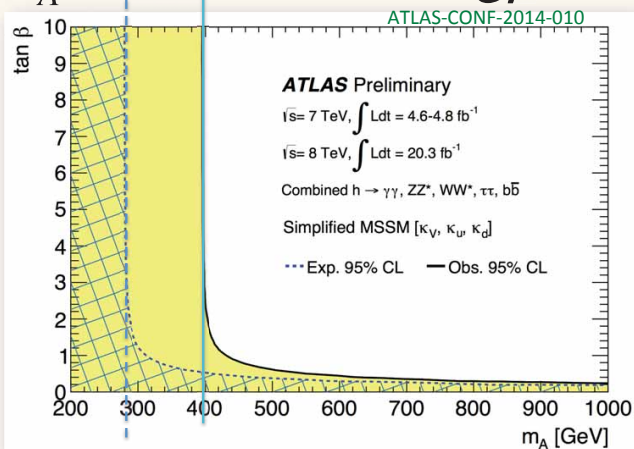
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A. Djouadi, JQ, arXiv:1304.1787

A. Djouadi, L. Maiani, G. Moreau, A. Polosa, JQ, V. Riquer, arXiv:1307.5205

# Simple MSSM Interpretation

$m_A > 400 \text{ GeV}$  for  $\tan\beta > 2$



The post-Higgs MSSM scenario :

- observation of the lighter  $h$  boson at a mass of  $\approx 125$  GeV.
- non-observation of superparticles at the LHC.

MSSM  $\Rightarrow$  SUSY-breaking scale rather high,  $M_S \gtrsim 1$  TeV.

- 1  $M_h \approx 125$  GeV fixes the dominant radiative corrections that enter the MSSM Higgs boson masses  $\Rightarrow$  the Higgs sector can be described by only 2 free parameters (good approximation).
- 2 Main phenomenological consequence of these high  $M_S$  values :
  - reopen the low  $\tan \beta$  region,  $\tan \beta \lesssim 3-5$ , which was for a long time buried under the LEP constraint on the lightest  $h$  mass when a low SUSY scale was assumed.
  - The heavier MSSM neutral H/A states can be searched for in a variety of interesting final states.
- 3 We perform a fit using the LHC data in a model independent way.

In the MSSM to break the electroweak symmetry one need 2 doublets of complex scalar fields :

$$H_d = \begin{pmatrix} H_d^0 \\ H_d^- \end{pmatrix} \text{ with } Y_{H_d} = -1 \quad , \quad H_u = \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix} \text{ with } Y_{H_u} = +1$$

The **tree-level masses** of the CP-even  $h$  and  $H$  bosons depend on  $M_A$ ,  $\tan\beta$  and  $M_Z$ .

However, many parameters of the MSSM such as the SUSY scale  $M_S = \sqrt{m_{\tilde{t}_1} m_{\tilde{t}_2}}$ , the stop/sbottom trilinear couplings  $A_{t/b}$  or the higgsino mass  $\mu$  enter  $M_h$  and  $M_H$  through **radiative corrections**.

In the basis  $(H_d, H_u)$ , the CP-even Higgs mass matrix can be written as:

$$M_S^2 = M_Z^2 \begin{pmatrix} c_\beta^2 & -s_\beta c_\beta \\ -s_\beta c_\beta & s_\beta^2 \end{pmatrix} + M_A^2 \begin{pmatrix} s_\beta^2 & -s_\beta c_\beta \\ -s_\beta c_\beta & c_\beta^2 \end{pmatrix} + \begin{pmatrix} \Delta\mathcal{M}_{11}^2 & \Delta\mathcal{M}_{12}^2 \\ \Delta\mathcal{M}_{12}^2 & \Delta\mathcal{M}_{22}^2 \end{pmatrix}$$

where we have introduced the **radiative corrections** by a  $2 \times 2$  matrix  $\Delta\mathcal{M}_{ij}^2$ .

One can then derive the neutral CP even Higgs boson masses and the mixing angle  $\alpha$  that diagonalises the  $h, H$  states,  $H = \cos \alpha H_d^0 + \sin \alpha H_u^0$  &  $h = -\sin \alpha H_d^0 + \cos \alpha H_u^0$

$$M_{h/H}^2 = f_{h/H}(M_A, \tan \beta, \Delta M_{11}, \Delta M_{12}, \Delta M_{22})$$

$$\tan \alpha = f_\alpha(M_A, \tan \beta, \Delta M_{11}, \Delta M_{12}, \Delta M_{22})$$

$M_h$  should be an input now...

$\Delta M_{22}^2$  involves the by far dominant stop-top sector correction,  
 $\Delta M_{22}^2 \gg \Delta M_{11}^2, \Delta M_{12}^2$ .

One can simply trade  $\Delta M_{22}^2$  ( $M_S$ ) for the by now known  $M_h$  using

$$\Delta M_{22}^2 = \frac{M_h^2(M_A^2 + M_Z^2 - M_h^2) - M_A^2 M_Z^2 c_{2\beta}^2}{M_Z^2 c_\beta^2 + M_A^2 s_\beta^2 - M_h^2}$$

In this case, one can simply write  $M_H$  and  $\alpha$  in terms of  $M_A, \tan \beta$  and  $M_h$ :

hMSSM :

$$M_H^2 = \frac{(M_A^2 + M_Z^2 - M_h^2)(M_Z^2 c_\beta^2 + M_A^2 s_\beta^2) - M_A^2 M_Z^2 c_{2\beta}^2}{M_Z^2 c_\beta^2 + M_A^2 s_\beta^2 - M_h^2}$$

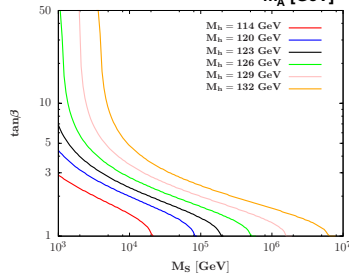
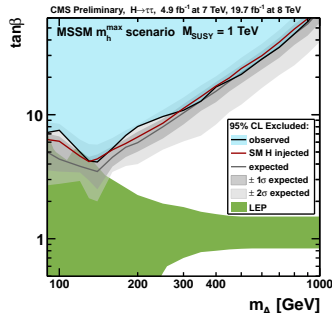
$$\alpha = -\arctan \left( \frac{(M_Z^2 + M_A^2) c_\beta s_\beta}{M_Z^2 c_\beta^2 + M_A^2 s_\beta^2 - M_h^2} \right)$$

- $\tan\beta \lesssim 3$  usually "excluded" by LEP2 ( $M_h \gtrsim 114$  GeV) but it assumes  $M_S \sim 1$  TeV!

- Caveat : ATLAS & CMS constraint apply for a specific benchmark :  $X_t/M_S = \sqrt{6}$  and  $M_S = 1$  TeV (the  $m_h^{max}$  scenario).

- But we can be more relaxed:  
 with  $M_S \gg M_Z$ ,  $\tan\beta \approx 1$  could be allowed!

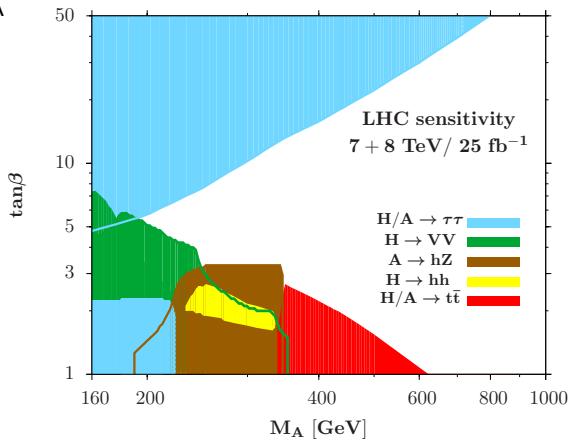
$\Rightarrow$  Let's reopen the low  $\tan\beta$  regime and heavy Higgs searches,  
 but in a benchmark independent approach (hMSSM).



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The main search channels for the H/A states :

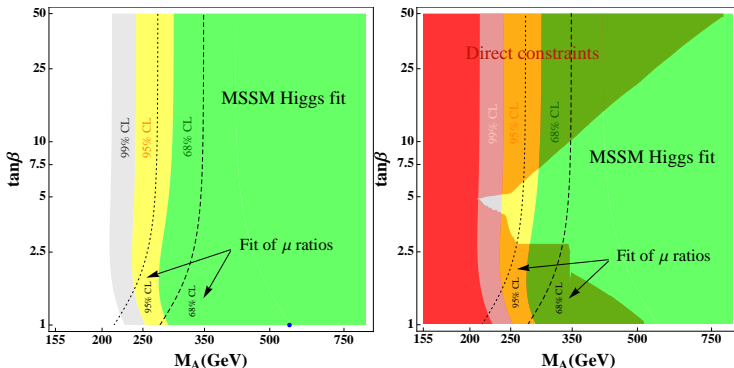
- The  $H/A \rightarrow \tau\tau$  channel (CMS)
- The  $H \rightarrow WW, ZZ$  channels (CMS)
- The  $A \rightarrow Zh$  channel (ATLAS & CMS)
- The  $H \rightarrow hh$  channel (estimate)
- The  $H/A \rightarrow t\bar{t}$  channels (estimate derived from ATLAS & CMS)



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If we neglect **direct corrections** to the h couplings, one can perform a fit of the Higgs signal strengths in the plane  $[\tan\beta, M_A]$  by using the expressions defining the hMSSM:

The best-fit point : **( $\tan\beta=1$  and  $M_A=557$  GeV)** or  
 ( $M_H = 580$  GeV,  $M_{H^\pm} = 563$  GeV,  $\alpha = -0.837$  rad).



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We also superimpose on these indirect limits, the direct constraints on the heavy  $H/A$  boson searches performed by ATLAS and CMS.



## Conclusion :

- We have discussed the MSSM that we seem to have after the discovery of the Higgs boson at the LHC.  
⇒ the MSSM Higgs sector can be described by only  $(\tan \beta, M_A)$  if the information  $M_h = 125$  GeV is used.
- $M_h \approx 125$  GeV and the non-observation of SUSY particles, seems to indicate that the soft-SUSY breaking scale might be large.  
⇒ We have considered the production of the heavier  $H, A$  bosons of the MSSM at the LHC, focusing on the low  $\tan \beta$  regime.
- To describe the  $h$  properties when the direct radiative corrections are also important, we need the 3 couplings  $c_t, c_b$  and  $c_V$ .  
⇒ If we neglect them, the best fit point turns out to be at low  $\tan \beta$ ,  $\tan \beta \approx 1$ , and with a not too high CP-odd Higgs mass,  $M_A \approx 560$  GeV.
- The phenomenology of the low  $\tan \beta$  regime is quite interesting and it will be accessible at the next LHC run.

Bonus slides

- Knowing  $[\tan \beta, M_A]$  and fixing  $M_h = 125$  GeV, the couplings of the Higgs bosons can be derived, including the generally dominant **radiative corrections that enter in the MSSM Higgs masses** :

$$c_V^0 = \sin(\beta - \alpha), \quad c_t^0 = \frac{\cos \alpha}{\sin \beta}, \quad c_b^0 = -\frac{\sin \alpha}{\cos \beta}$$

- However, there are also **direct radiative corrections to the Higgs couplings** not contained in the mass matrix. These can alter this simple picture!
- If large **direct corrections**  $\Rightarrow$  3 independent  $h$  couplings :  
 $c_c = c_t, c_\tau = c_b$  and  $c_V = c_V^0$ .

- To study the  $h$  state at the LHC, we define the effective Lagrangian :

$$\begin{aligned} \mathcal{L}_h = & c_V g_{hWW} h W_\mu^+ W^{-\mu} + c_V g_{hZZ} h Z_\mu^0 Z^{0\mu} \\ & - c_t y_t h \bar{t}_L t_R - c_t y_c h \bar{c}_L c_R - c_b y_b h \bar{b}_L b_R - c_b y_\tau h \bar{\tau}_L \tau_R + \text{h.c.} \end{aligned}$$

- We fit the Higgs signal strengths :  $\mu_X \simeq \frac{\sigma(\mathbf{pp} \rightarrow h) \times \text{BR}(h \rightarrow \mathbf{XX})}{\sigma(\mathbf{pp} \rightarrow h)_{\text{SM}} \times \text{BR}(h \rightarrow \mathbf{XX})_{\text{SM}}}$

**Best-fit value :  $c_t = 0.89, c_b = 1.01$  and  $c_V = 1.02$  (ATLAS & CMS data).**

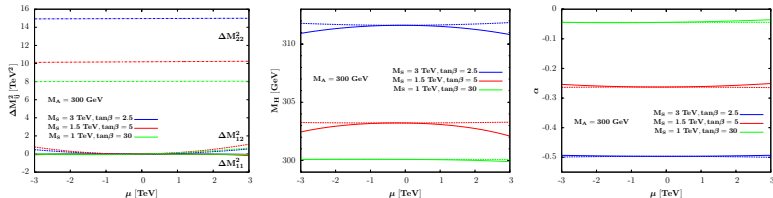
We first consider the radiative corrections when the subleading contributions proportional to  $\mu, A_t/b$  are included in the form of : [Degrassi, Slavich, Zwirner, 2001](#) ; [Carena, Haber, 2003](#)

$$\Delta M_{11}^2 = -\frac{v^2 \sin^2 \beta}{32\pi^2} \bar{\mu}^2 \left[ x_t^2 \lambda_t^4 (1 + c_{11} \ell_S) + a_b^2 \lambda_b^4 (1 + c_{12} \ell_S) \right]$$

$$\Delta M_{12}^2 = -\frac{v^2 \sin^2 \beta}{32\pi^2} \bar{\mu} \left[ x_t \lambda_t^4 (6 - x_t a_t) (1 + c_{31} \ell_S) - \bar{\mu}^2 a_b \lambda_b^4 (1 + c_{32} \ell_S) \right]$$

$$\Delta M_{22}^2 = \frac{v^2 \sin^2 \beta}{32\pi^2} \left[ 6\lambda_t^4 \ell_S (2 + c_{21} \ell_S) + x_t a_t \lambda_t^4 (12 - x_t a_t) (1 + c_{21} \ell_S) - \bar{\mu}^4 \lambda_b^4 (1 + c_{22} \ell_S) \right]$$

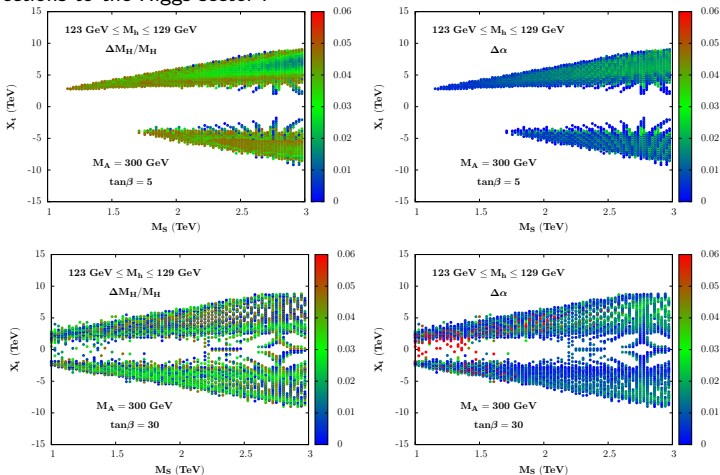
We calculate "approximate" and "exact"  $M_H$  and  $\alpha$  values for  $M_h = 126 \pm 3 \text{ GeV}$ .



- Even for large  $\mu$ ,  $\Delta M_H/M_H < 0.5\%$  and  $\Delta\alpha \lesssim 0.015$ .

⇒ The approximation of determining the parameters  $M_H$  and  $\alpha$  from  $\tan\beta, M_A$  and the value of  $M_h$  is extremely good.

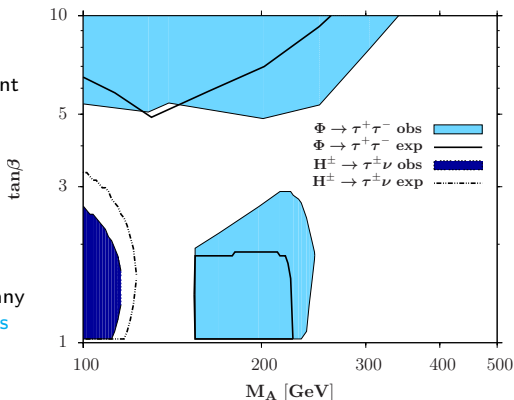
To check more thoroughly the impact of the subleading corrections  $\Delta\mathcal{M}_{11}^2$ ,  $\Delta\mathcal{M}_{12}^2$  :  
 we perform a scan of the MSSM parameter space with the full two-loop radiative  
 corrections to the Higgs sector :



For a chosen  $(\tan\beta, M_A)$  ,  $|\mu| \leq 3 \text{ TeV}$ ,  $|A_t, A_b| \leq 3M_S$ ,  $1 \text{ TeV} \leq M_3 \leq 3 \text{ TeV}$  and  $0.5 \text{ TeV} \leq M_S \leq 3 \text{ TeV}$ .

### Constraints from the heavier Higgs searches at high $\tan\beta$ :

- CMS  $H/A \rightarrow \tau\tau$  analysis : constraint very restrictive for  $M_A \lesssim 250$  GeV, excludes  $\tan\beta \gtrsim 5$ .
- Caveat : ATLAS&CMS constraint apply for a specific benchmark :  $X_t/M_S = \sqrt{6}$  and  $M_S = 1$  TeV.
- Exclusion limit can be obtained in any MSSM scenario, CMS search limit is effective and excludes low  $\tan\beta$ .



A. Djouadi, J. Q., arXiv:1304.1787

→ Low  $\tan\beta$  areas, thought to be buried under the LEP2 exclusion bound on  $M_h$ , are now open territory for heavy MSSM Higgs hunting!

→ This can be done not only in these 2 channels but also in a plethora of channels...

$\Phi$	$g_{\Phi\bar{u}u}$	$g_{\Phi\bar{d}d}$	$g_{\Phi VV}$	$g_{\Phi AZ}/g_{\Phi H^+W^-}$
$h$	$\cos\alpha/\sin\beta$	$-\sin\alpha/\cos\beta$	$\sin(\beta-\alpha)$	$\propto \cos(\beta-\alpha)$
$H$	$\sin\alpha/\sin\beta$	$\cos\alpha/\cos\beta$	$\cos(\beta-\alpha)$	$\propto \sin(\beta-\alpha)$
$A$	$\cot\beta$	$\tan\beta$	0	$\propto 0/1$

The decoupling limit is controlled by  $g_{HVV} = \cos(\beta-\alpha)$  :

$$g_{HVV} \xrightarrow{M_A \gg M_Z} \chi \equiv \frac{1}{2} \frac{M_{22}^2}{M_A^2} \sin 4\beta - \frac{1}{2} \frac{M_{22}^2}{M_A^2} \sin 2\beta \rightarrow 0$$

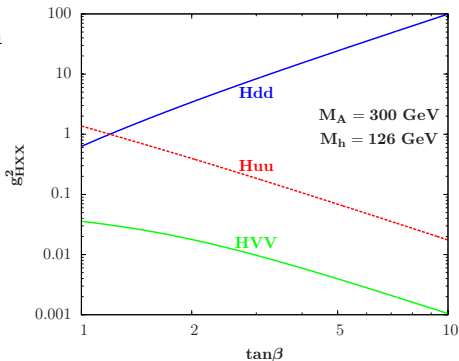
**Tree-level part**: doubly suppressed in both the  $\tan\beta \gg 1$  and  $\tan\beta \sim 1$  cases.

$$\sin 4\beta = \frac{4 \tan\beta(1 - \tan^2\beta)}{(1 + \tan^2\beta)^2} \rightarrow \begin{cases} -4/\tan\beta & \text{for } \tan\beta \gg 1 \\ 1 - \tan^2\beta & \text{for } \tan\beta \sim 1 \end{cases} \rightarrow 0$$

**The radiative part** : behave as  $-\mathcal{M}_{22}^2/M_A^2 \times \cot\beta$ , also vanishes at high  $\tan\beta$  values  $\Rightarrow$  the decoupling limit  $g_{HVV} \rightarrow 0$  is reached very quickly at high  $\tan\beta$ , as soon as  $M_A \gtrsim M_h^{\max}$ . Instead, for  $\tan\beta \approx 1$ , this radiatively generated component is maximal. **Departure from the decoupling limit!**

$$\begin{aligned} g_{huu} &\xrightarrow{M_A \gg M_Z} 1 + \chi \cot\beta \rightarrow 1 \\ g_{hdd} &\xrightarrow{M_A \gg M_Z} 1 - \chi \tan\beta \rightarrow 1 \\ g_{Hu u} &\xrightarrow{M_A \gg M_Z} -\cot\beta + \chi \rightarrow -\cot\beta \\ g_{Hd d} &\xrightarrow{M_A \gg M_Z} +\tan\beta + \chi \rightarrow +\tan\beta \end{aligned}$$

At low  $\tan\beta$  :  $g_{HVV}$  is non-zero,  $g_{Htt}$  and  $g_{Att}$  are significant.  
 $\Rightarrow H/A/H^\pm$  bosons can have sizable couplings to top quarks and massive gauge bosons if  $\tan\beta \sim 3$ .

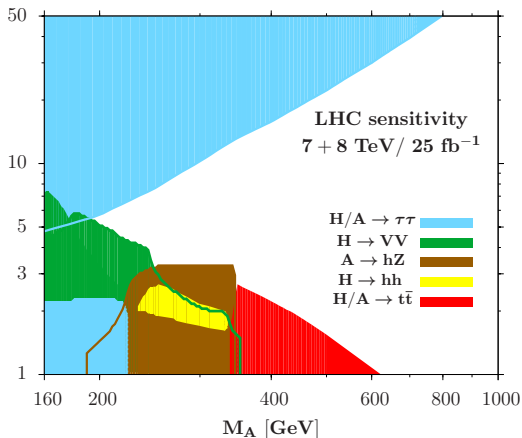


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## The $H/A \rightarrow t\bar{t}$ channels

- It has not been considered in the case of the SM Higgs for 2 reasons :
  - For  $M_{H_{SM}} \gtrsim 350$  GeV,  $H_{SM} \rightarrow WW, ZZ$  dominate over the  $H_{SM} \rightarrow t\bar{t}$ .
  - The  $t\bar{t}$  background was thought to be overwhelmingly large (it had to be evaluated in a large mass window because of the large  $\Gamma_H$ ).
- Situation different in the MSSM :  $\Gamma_{H/A} \lesssim 20$  GeV for  $\tan\beta \gtrsim 1$  and  $M_{H,A} \lesssim 500$  GeV (and grow linearly with the Higgs masses beyond this value)
 

$\Rightarrow$  one can integrate the  $t\bar{t}$  continuum background in a smaller invariant mass bin and enhance the S/B ratio.
- $BR(H/A \rightarrow t\bar{t}) \approx 100\%$  for  $\tan\beta \lesssim 3$  if kinematically open.



Search for  $H/A \rightarrow t\bar{t}$  will be more favorable for the MSSM at low  $\tan\beta$  than in the SM.



- Knowing  $[\tan \beta, M_A]$  and fixing  $M_h = 125$  GeV, the couplings of the Higgs bosons can be derived, including the generally dominant **radiative corrections that enter in the MSSM Higgs masses** :

$$c_V^0 = \sin(\beta - \alpha) , \quad c_t^0 = \frac{\cos \alpha}{\sin \beta} , \quad c_b^0 = -\frac{\sin \alpha}{\cos \beta}$$

- However, there are also **direct radiative corrections to the Higgs couplings** not contained in the mass matrix. These can alter this simple picture!

- The  $hb\bar{b}$  coupling : modified by additional one-loop vertex corrections,

$$c_b \approx c_b^0 \times [1 - \Delta_b / (1 + \Delta_b) \times (1 + \cot \alpha \cot \beta)]$$

$\Delta_b$  : SUSY-QCD corr. with sbottom-gluino loops

- The  $ht\bar{t}$  coupling : derived indirectly from  $\sigma(gg \rightarrow h)$  and  $BR(h \rightarrow \gamma\gamma)$ ,

$$c_t \approx c_t^0 \times \left[ 1 + \frac{m_t^2}{4m_{\tilde{t}_1}^2 m_{\tilde{t}_2}^2} (m_{\tilde{t}_1}^2 + m_{\tilde{t}_2}^2 - (A_t - \mu \cot \alpha)(A_t + \mu \tan \alpha)) \right]$$

- $c_c = c_t^0$  and  $c_\tau = c_b^0$ .

- Invisible decays? ([Djouadi,Falkowski,Mambrini,JQ, arXiv:1205.3169](#))

$\Rightarrow$  neutralinos are relatively light and couple significantly to  $h \rightarrow$  rather unlikely.