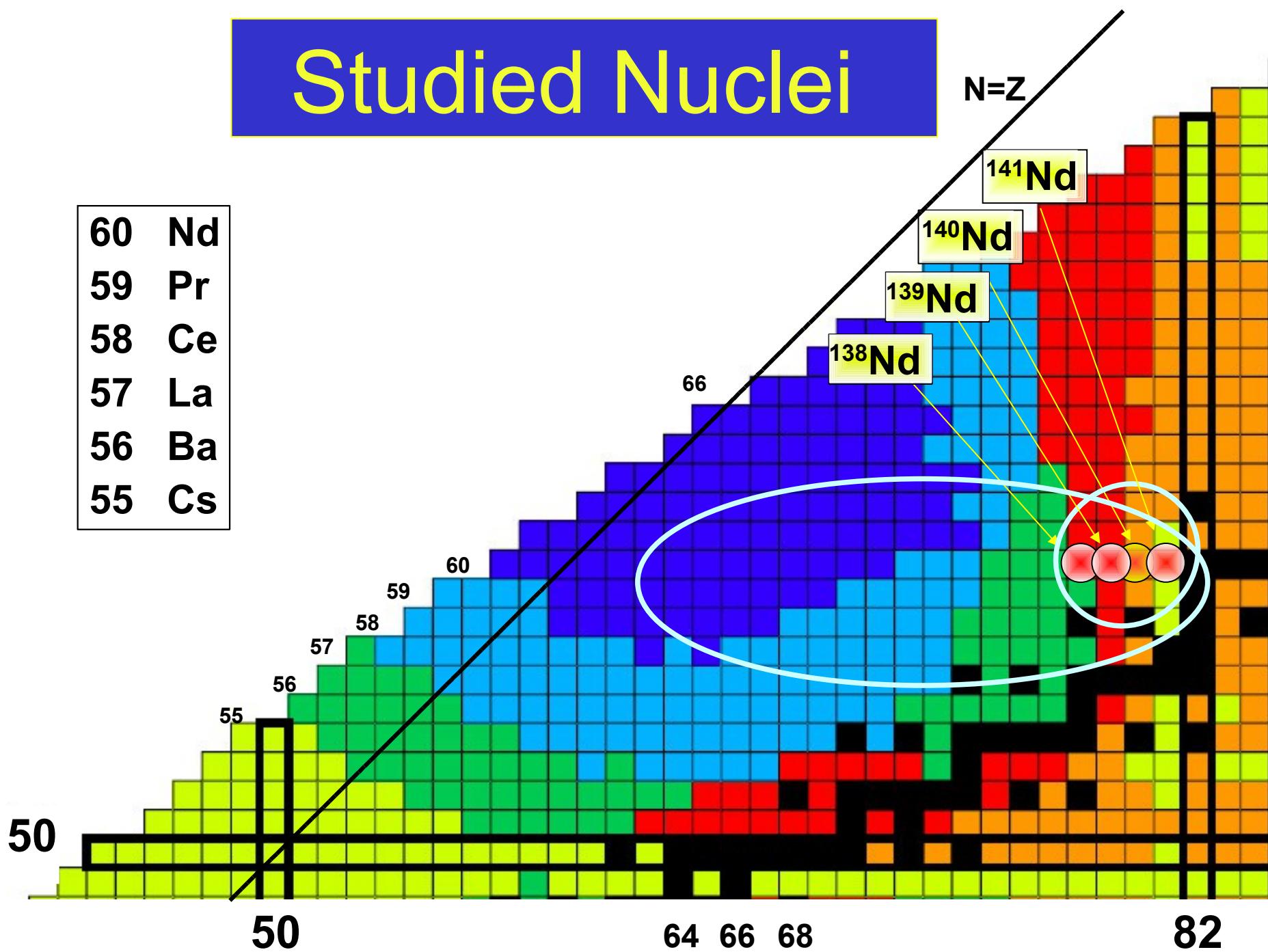


# Exotic rotations and seniority isomers in Nd nuclei

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(Centre de Sciences Nucléaires et Sciences de la Matière)

1. Exotic rotations - GASP, Legnaro (Italy)  
- Euroball, Strasbourg (France)  
- Jurogam+RITU, Jyvaskyla (Finland)
2. Seniority isomers - Jurogam+RITU, Jyvaskyla (Finland)

# Studied Nuclei



# CNS calculations for $^{138}\text{Nd}$ : high spins !

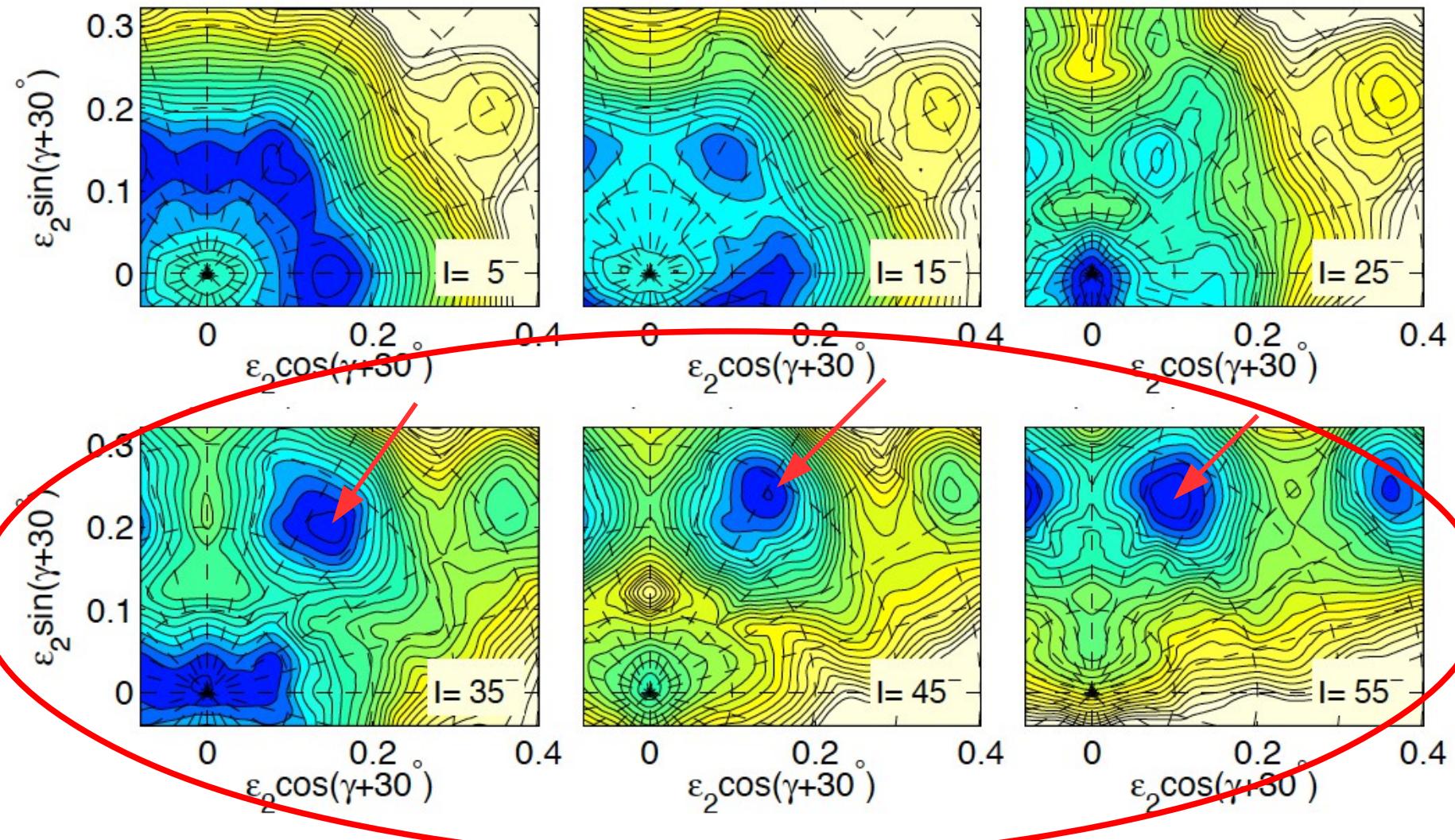


FIG. 3: The PES of the configuration  $\pi_p = -, \alpha_p = 1, \pi_n = +, \alpha_n = 0$  for  $^{138}\text{Nd}$ .

# CNS calculations for $^{138}\text{Nd}$

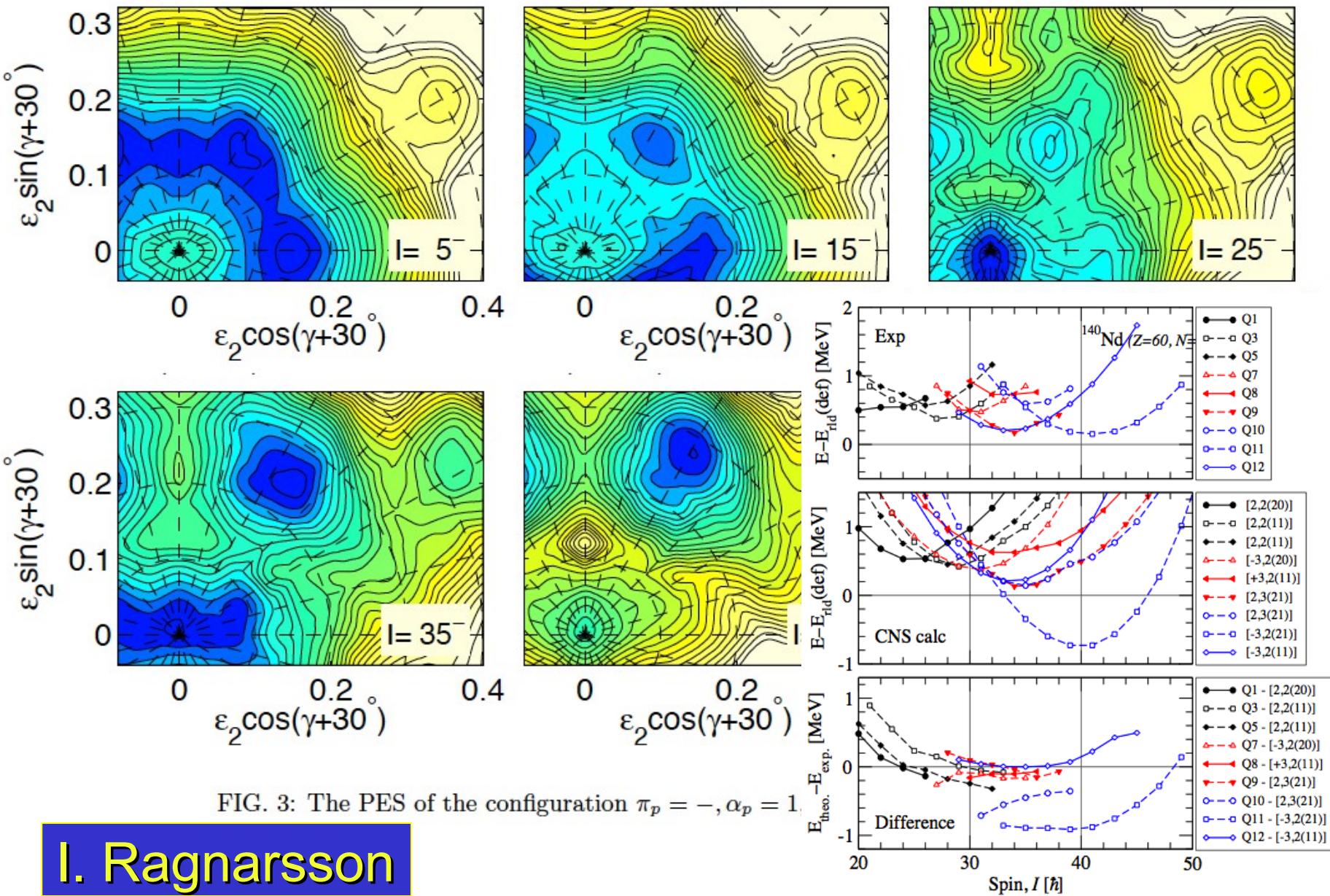
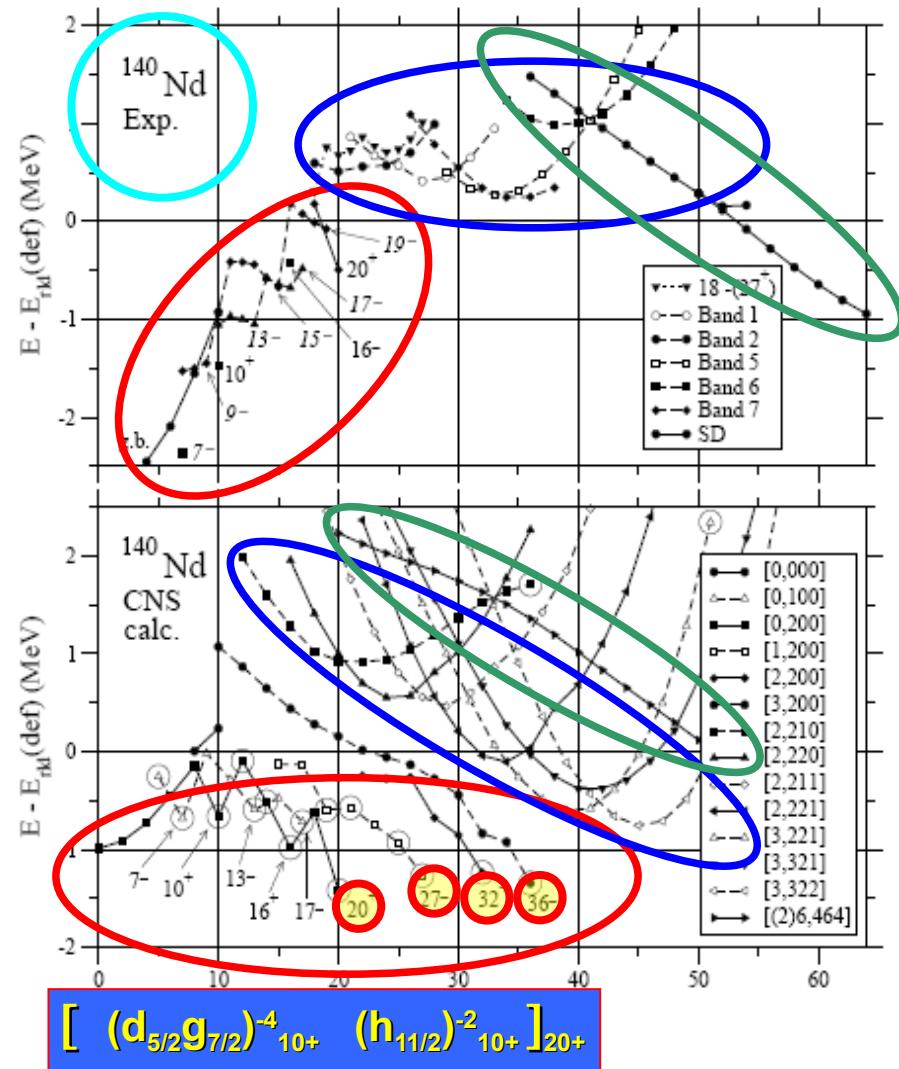
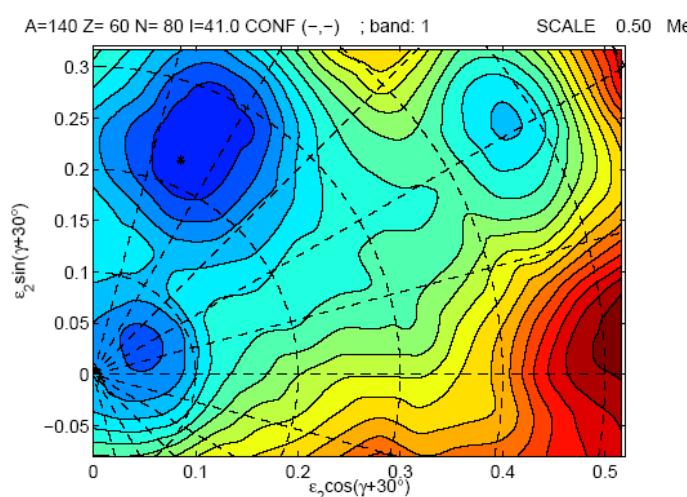
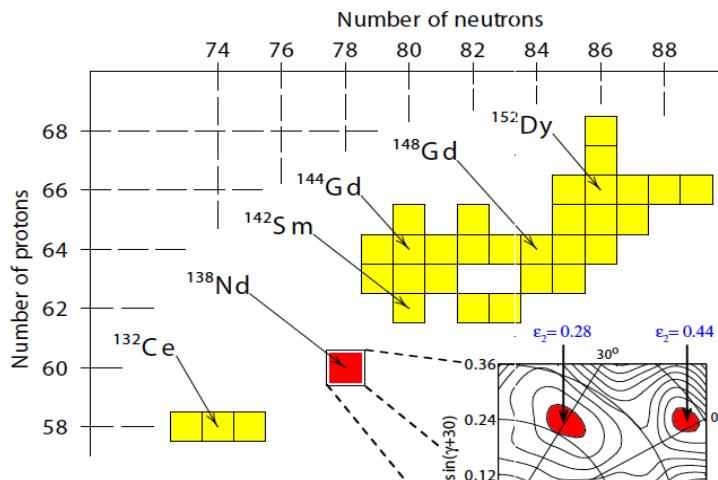


FIG. 3: The PES of the configuration  $\pi_p = -, \alpha_p = 1$

# Stable triaxiality: $\sim +30^\circ$ for $N < 82$



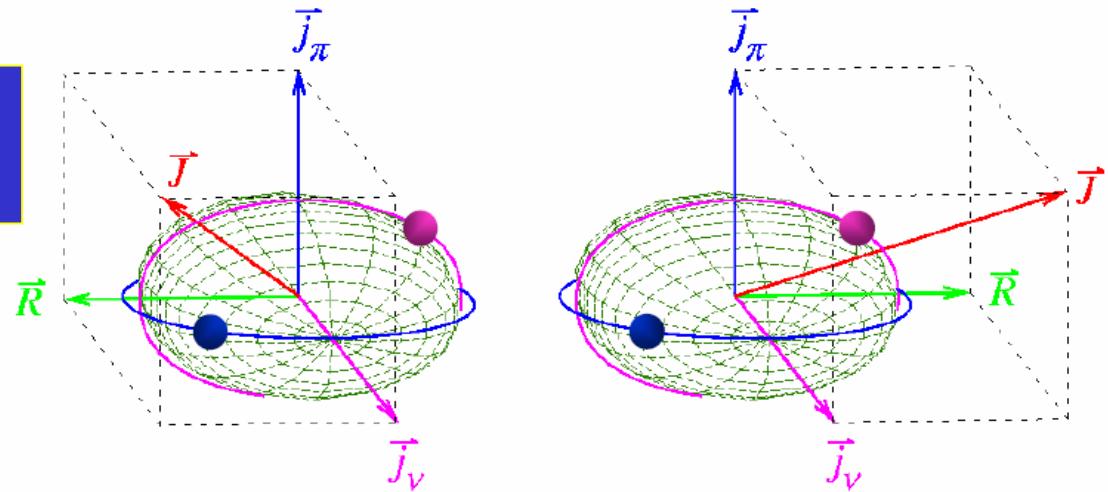
PRC 61 (1999); 69 (2004); 70 (2004); 72 (2005); 74 (2006);  
84 (2011); 86 (2012); 87 (2013); 88 (2013)R

# Triaxiality at high spins

Chiral Geometry in Nuclei

Mutually orthogonal coupling of three angular momenta  
in odd-odd nuclei

## Chiral mode

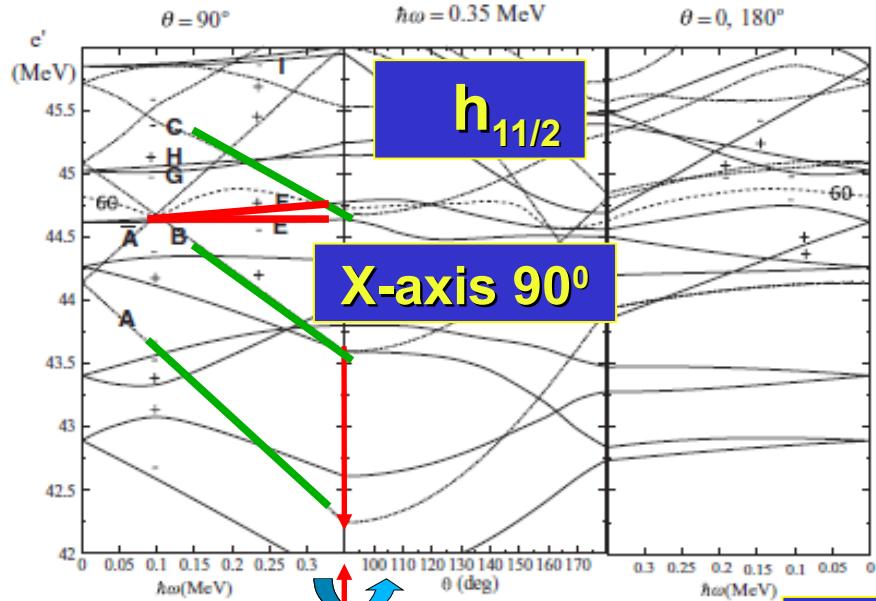


$$E(I, n_{\text{wobb}}) = \frac{I(I+1)}{2\mathcal{J}_x} + \hbar\omega_{\text{wobb}} \left( n_{\text{wobb}} + \frac{1}{2} \right)$$

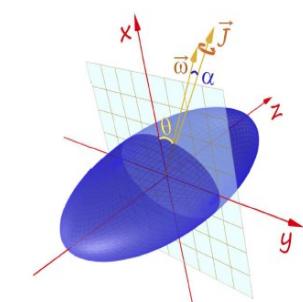
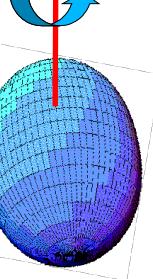
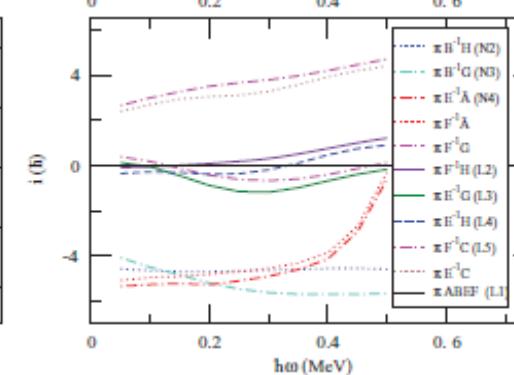
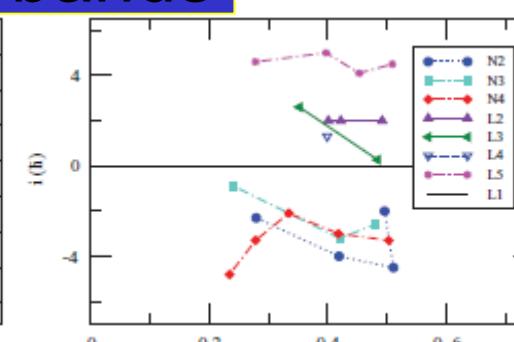
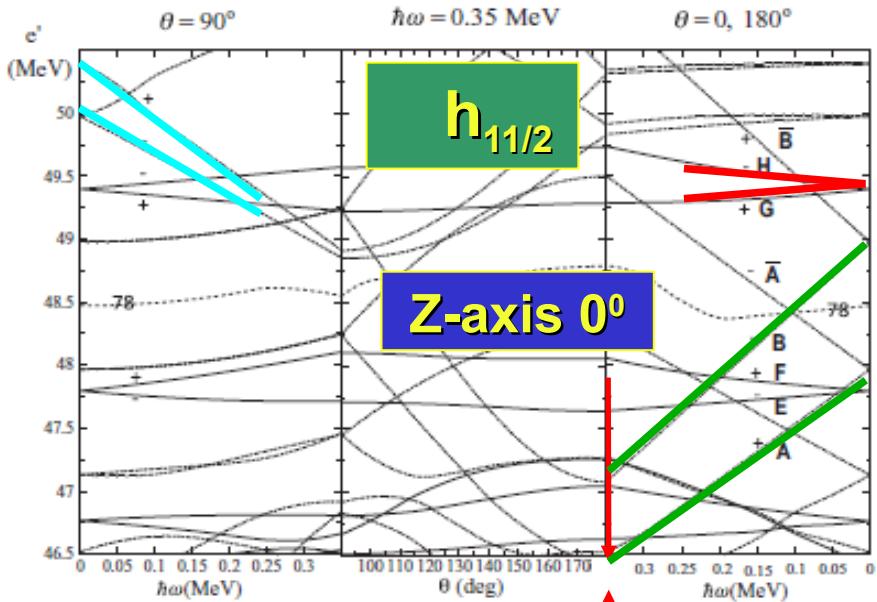
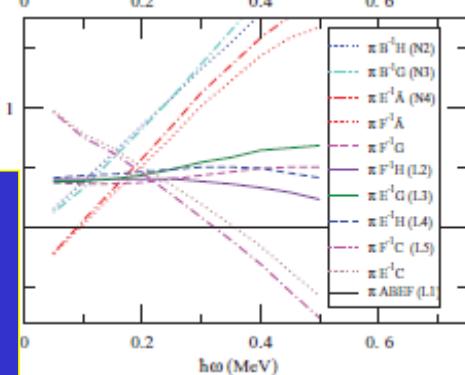
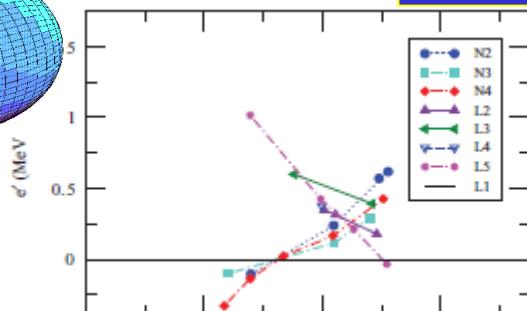
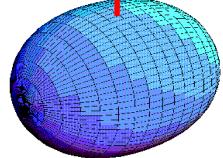
## Wobbling mode

$$\hbar\omega_{\text{wobb}} = \hbar\omega_{\text{rot}} \sqrt{\frac{(\mathcal{J}_x - \mathcal{J}_y)(\mathcal{J}_x - \mathcal{J}_z)}{\mathcal{J}_y \mathcal{J}_z}}$$

$$\hbar\omega_{\text{rot}} = \frac{I}{\mathcal{J}_x}$$



E2 bands

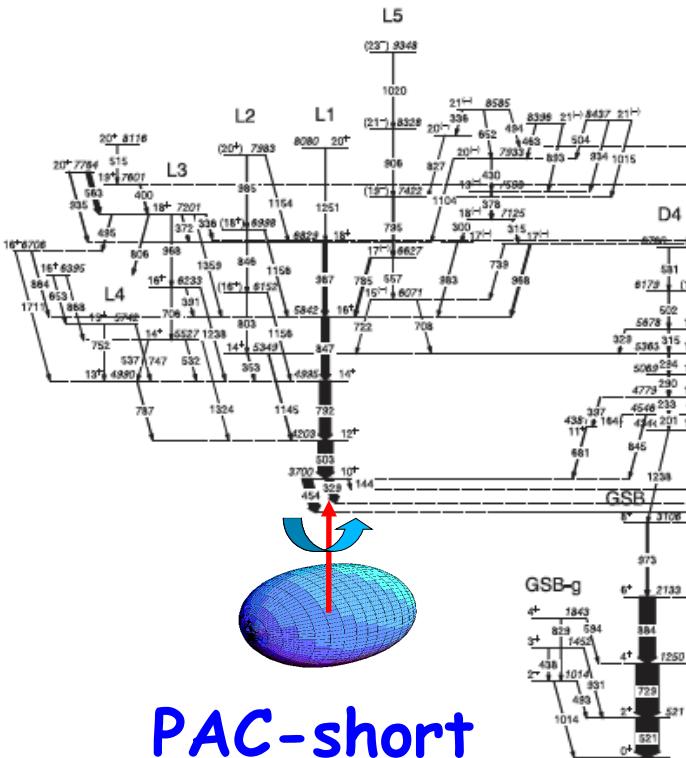


TAC, CSM  
S. Frauendorf

# $^{138}\text{Nd}$ – 21 bands at medium spins !

$(\text{h}_{11/2})^2$

$^{138}\text{Nd}$   
(low- and medium-spin bands)



$(\text{h}_{11/2})^2$

D5  
TAC

D6  
TAC

L8  
TAC

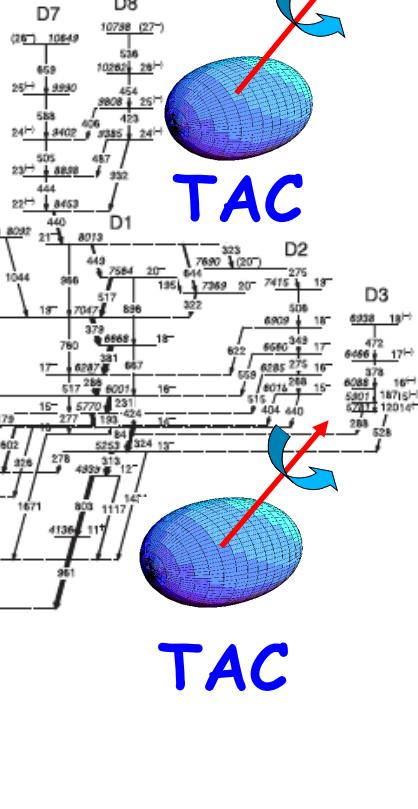
L7  
TAC

N3  
TAC

N4  
TAC

L6  
TAC

PAC-long



C. Petrache et al., PR C86,  
044321 (2012)

# $^{138}\text{Nd}$

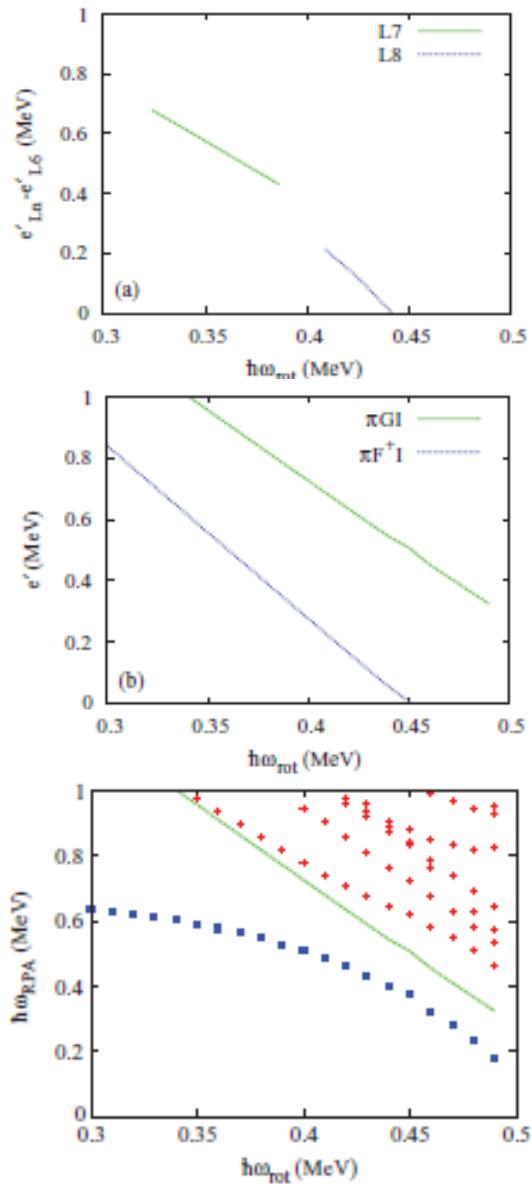
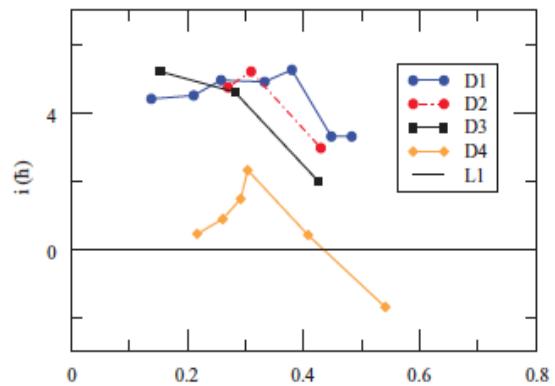
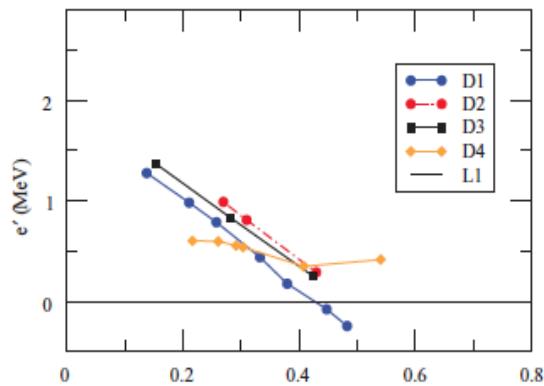
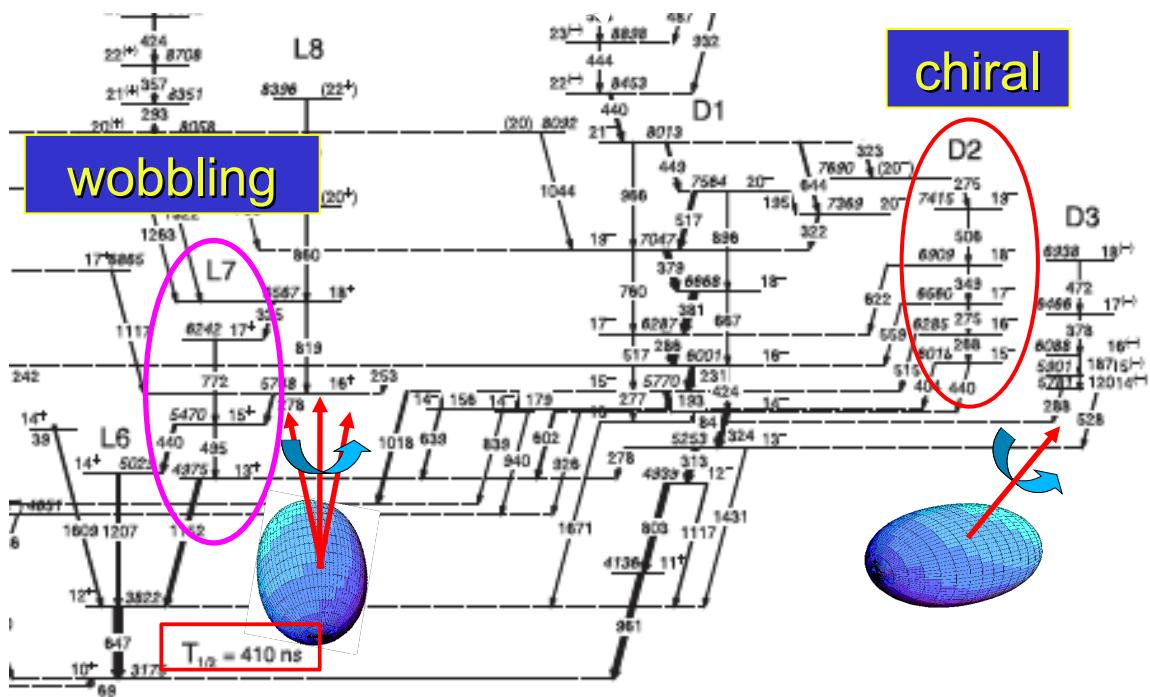


FIG. 18. (Color online) Calculated excitation energies of the RPA solutions built on the aligned  $\nu 10$  configuration as functions of the rotational frequency in  $^{138}\text{Nd}$ . Among them, the collective solution is emphasized by blue squares. Note that noncollective solutions are occasionally overlooked in the present algorithm, which however does not have any consequences for the discussion. The green dotted curve is the unperturbed  $\pi GI$  state.

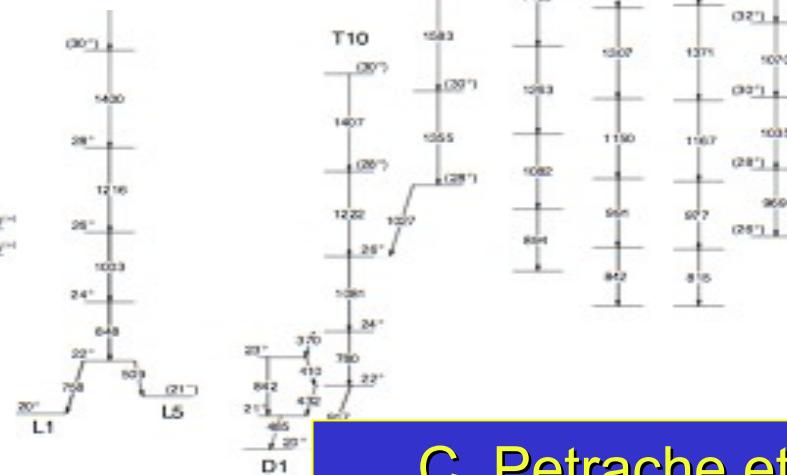
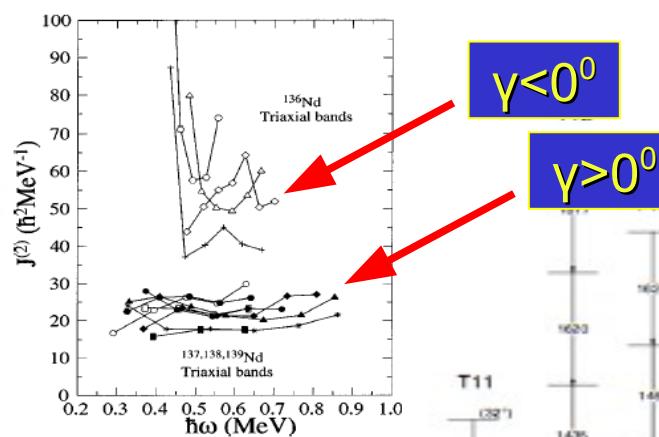
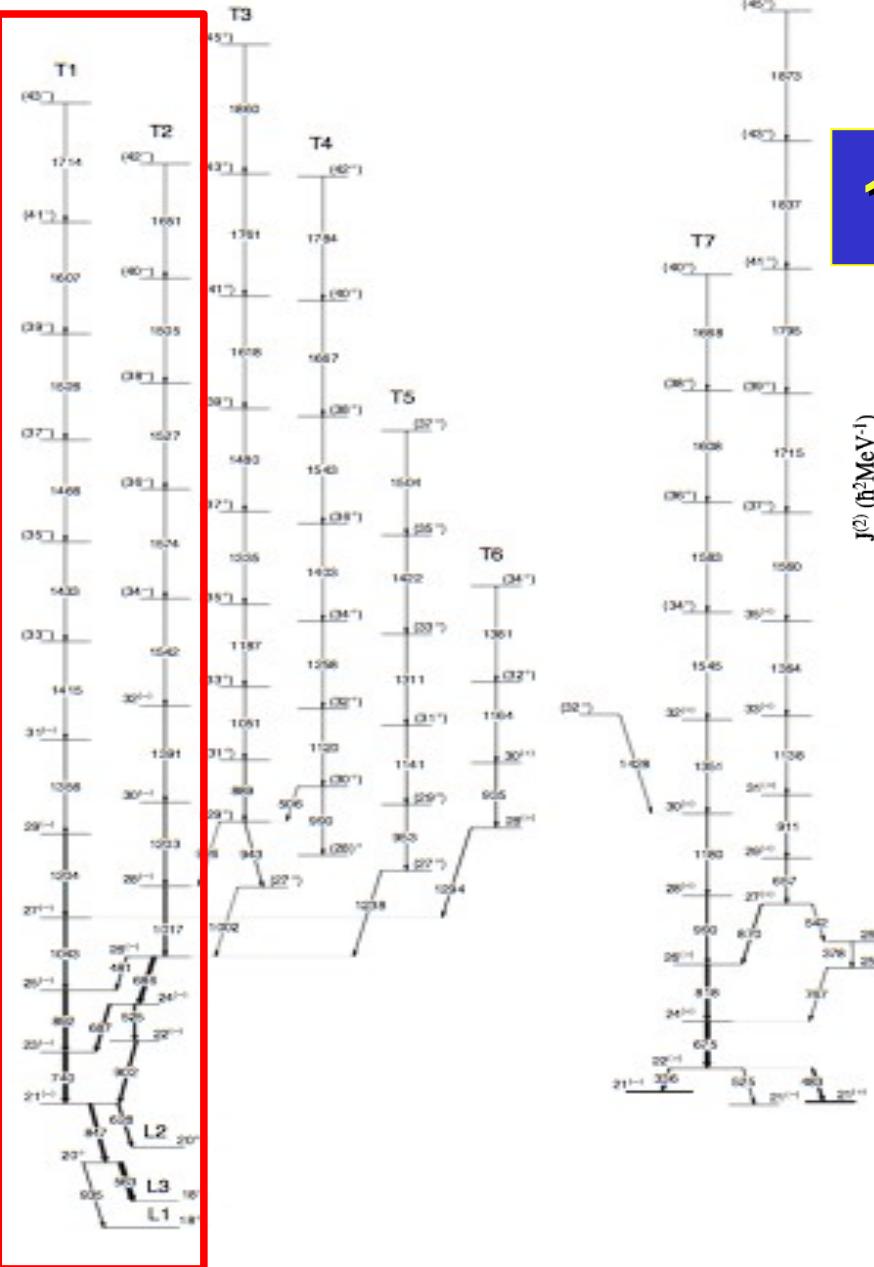
# Configuration assignments for the 21 bands at low and medium spin of $^{138}\text{Nd}$

TABLE IV. Configuration assignments to the low- and medium-spin bands of  $^{138}\text{Nd}$  in terms of particle-hole excitations with respect to the  $\pi ABEF = \pi 10$  reference configuration assigned to band L1 or the corresponding quasiproton vacuum for small finite pairing. The rotation axis is also indicated, which can be tilted (TAC) or parallel to a principal axis (PAC) of the intrinsic reference system of the nucleus. In the case of PAC, l and s indicate the long and short axes, respectively.

Band	Intensity (%)	Configuration	Rotation type	States	Comments
g band	100	$\pi 0 \otimes \nu 0$		$2^+-8^+$	
$\gamma$ band		$\gamma$ band		$2^+-4^+$	Decays to g band
N1	39	$\pi 0 \otimes \nu B^{-1}H\nu 10$	PAC-I	$5_1^- - 15^-$	Decays to g band
N2	14	$\pi B^{-1}H\pi 10 \otimes \nu 0$	PAC-s	$8_2^- - 16^-$	Decays to N1, N3, $8_1^-$
N3	2	$\pi B^{-1}C\pi 10 \otimes \nu 0$	PAC-s	$9_2^- - 15^-$	Decays to N2, N4, $8_1^-$
N4	89	$\pi E^{-1}\bar{A}\pi 10 \otimes \nu 0$	PAC-s	$7_2^- - 15^-$	Decays to N1, N3, GSB
$8_1^-$	17	$\pi F^{-1}\bar{A}\pi 10 \otimes \nu 0$	PAC-s	$8_1^-, 8_2^-$	Decays to N1
L1	64	$\pi 10 \otimes \nu 0$	PAC-s	$10^+ - 20^+$	Decays to N2, N3
L2	6	$\pi F^{-1}H\pi 10 \otimes \nu 0$ or $\pi E^+F^\dagger\pi 10 \otimes \nu 0$	PAC-s	$14^+, 16^+, 18^+$	Decays to L1
L3	2	$\pi E^{-1}G\pi 10 \otimes \nu 0$ or $\pi F^+H\pi 10 \otimes \nu 0$	PAC-s	$14^+ - 20^+$	Decays to L1, L4
L4	2	$\pi E^{-1}H\pi 10 \otimes \nu 0$	PAC-s	$13^+, 15^+$	Decays to L1, L3
L5	8	$\pi F^{-1}C\pi 10 \otimes \nu 0$ or $\pi 10 \otimes \nu h^2$	PAC-s	$15^{(-)} - 23^{(-)}$	Decays to L1, D4
L6	24	$\pi 0 \otimes \nu 10$	PAC-I	$10^+ - 14^+$	Band head is isomeric
L7	11	wobbling or $\pi 0 \otimes \nu F^{-1}G\nu 10$ or $\pi GI\pi 0 \otimes \nu 10$	PAC-I	$13^+ - 17^+$	Decays to L6
L8	2	$\pi 0 \otimes \nu E^{-1}G\nu 10$ or $\pi F^+I\pi 0 \otimes \nu 10$	PAC-I	$16^+ - 22^+$	Decays to L7
D1	21	$\pi F^{-1}\bar{A}\pi 10 \otimes \nu 10$	TAC	$13^- - 21^-$	Decays to N4, L8
D2	2	$\pi E^{-1}\bar{A}\pi 10 \otimes \nu 10$ or chiral	TAC	$15^- - 19^-$	Decays to D1
D3	1	$\pi B^{-1}C\pi 10 \otimes \nu 10$	TAC	$14^- - 18^-$	Decays to nonyrast $\pi = -$
D4	5	$\pi F^{-1}I\pi 10 \otimes \nu 0$ or $\pi F^{-1}\bar{A} \otimes \nu b^{-1}g$	TAC	$10^+ - 17^+$	Decays to L1 and GSB
D5	1	$\pi 10 \otimes \nu 10$	TAC	$16^{(+)} - 23^{(+)}$	Decays to D4 and $\pi = -$
D6	4	$\pi F^{-1}I\pi 10 \otimes \nu 10$ or $\pi E^{-1}H \otimes \nu 10$	TAC	$19^{(+) - (25^+)}$	Decays to L7
D7	3	$\pi F^{-1}C\pi 10 \otimes \nu 10$	TAC	$22^{(-)} - (26^-)$	Decays to D1
D8	2	$\pi E^{-1}C\pi 10 \otimes \nu 10$	TAC	$24^{(-)} - (27^-)$	Decays to D7

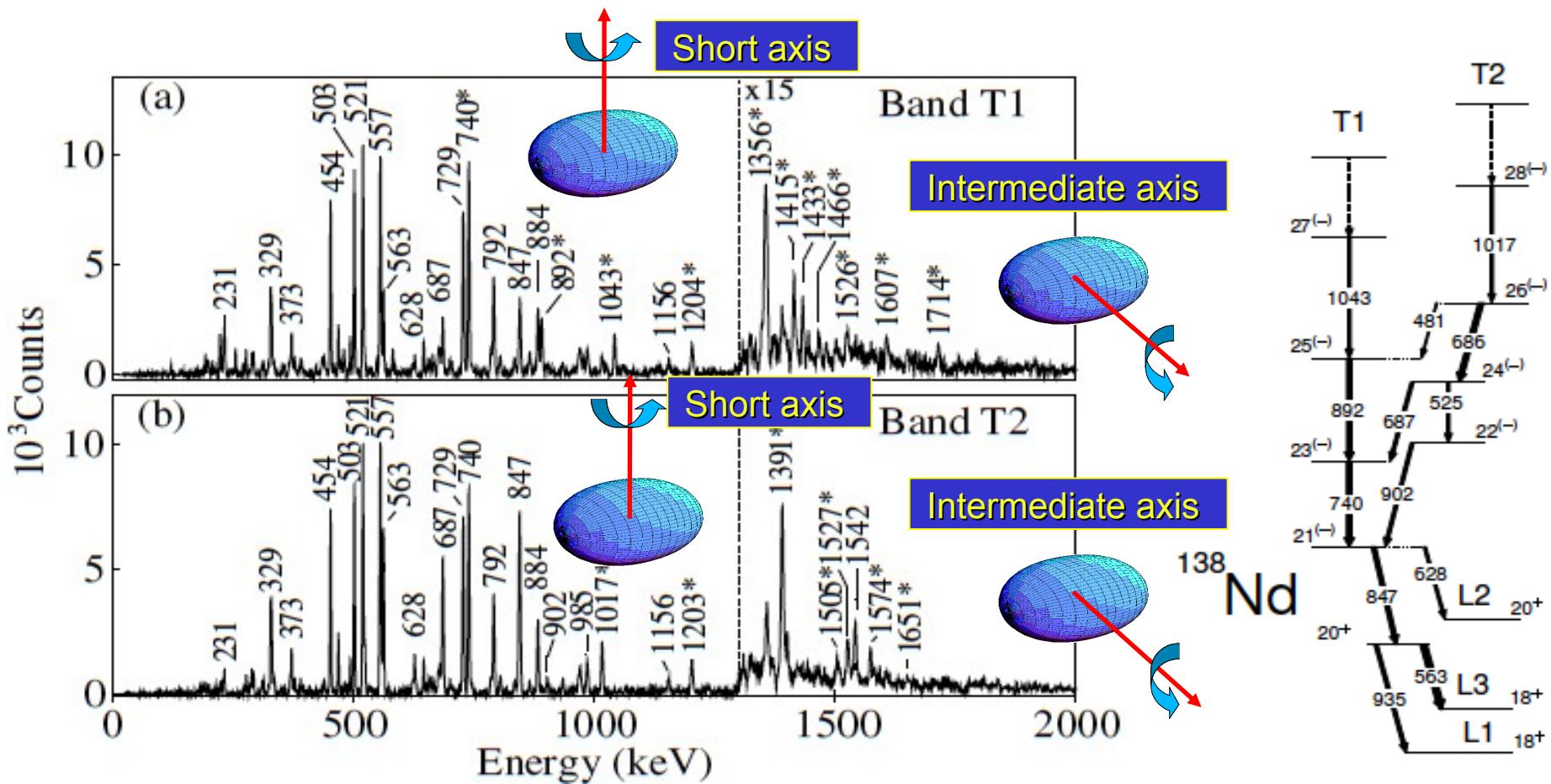
**$^{138}\text{Nd}$**

**15 high-spin bands**



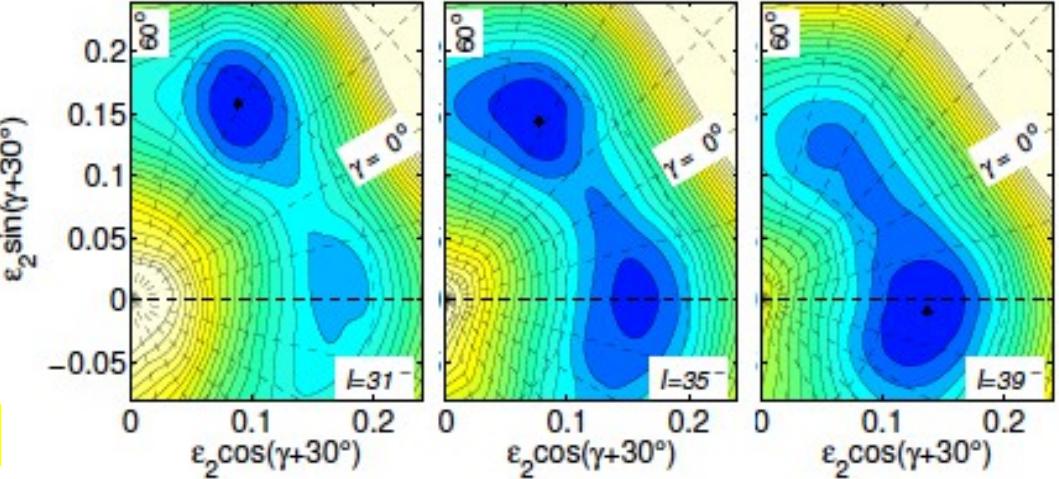
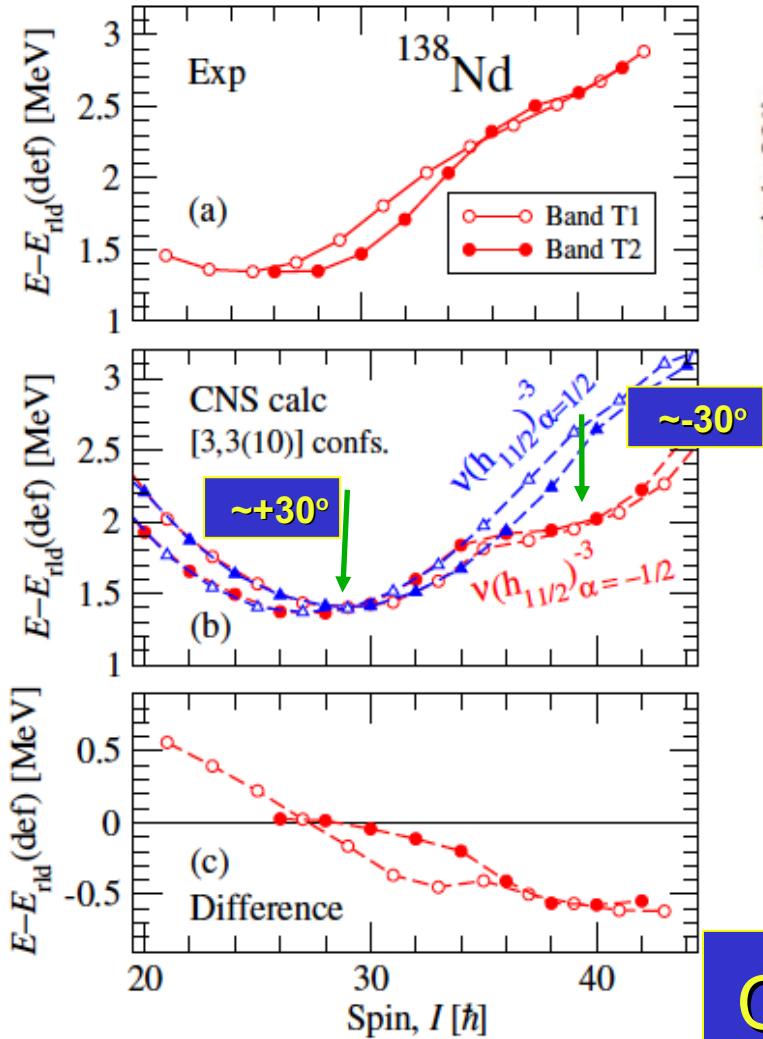
**C. Petrache et al.,  
to be submitted**

# Switch of rotation from short to intermediate axis at high spin in $^{138}\text{Nd}$



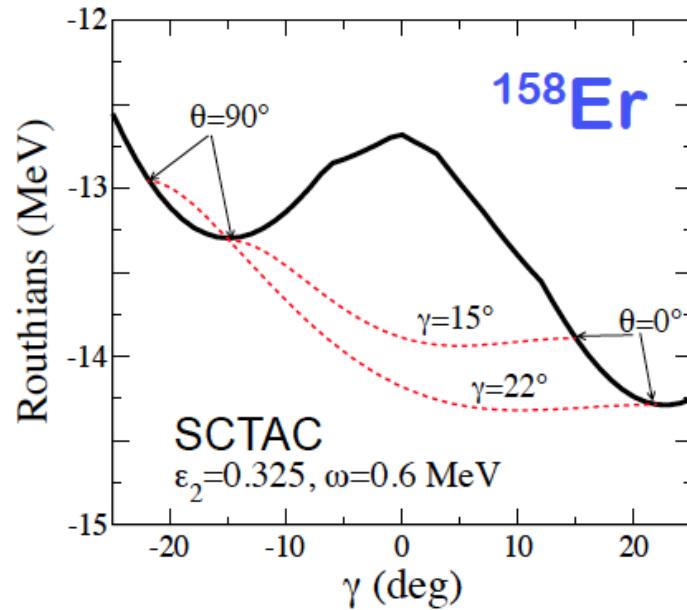
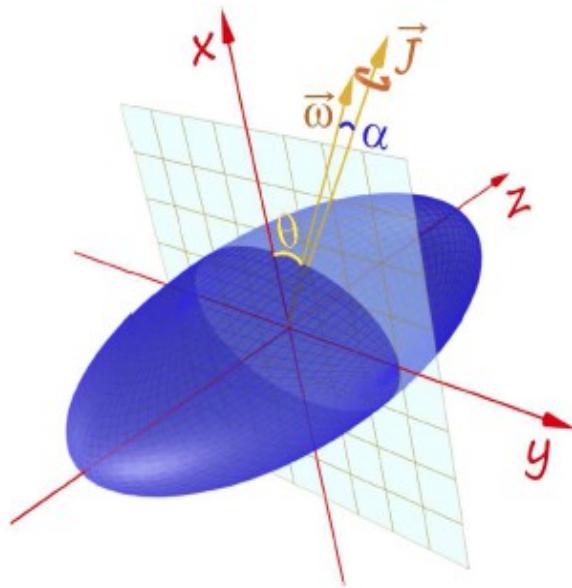
# Existence of triaxial shapes with $\gamma > 0^\circ$ and $\gamma < 0^\circ$

## CNS calculations for $^{138}\text{Nd}$ – I. Ragnarsson



Calculated potential energy surfaces in the  $(\varepsilon_2, \gamma)$ -plane, illustrating the shape change around  $I = 35$  for the  $[3,3(10)]$  configuration assigned to the T1 band. The contour line separation is 0.25 MeV.

# SCTAC calculations for $^{158}\text{Er}$

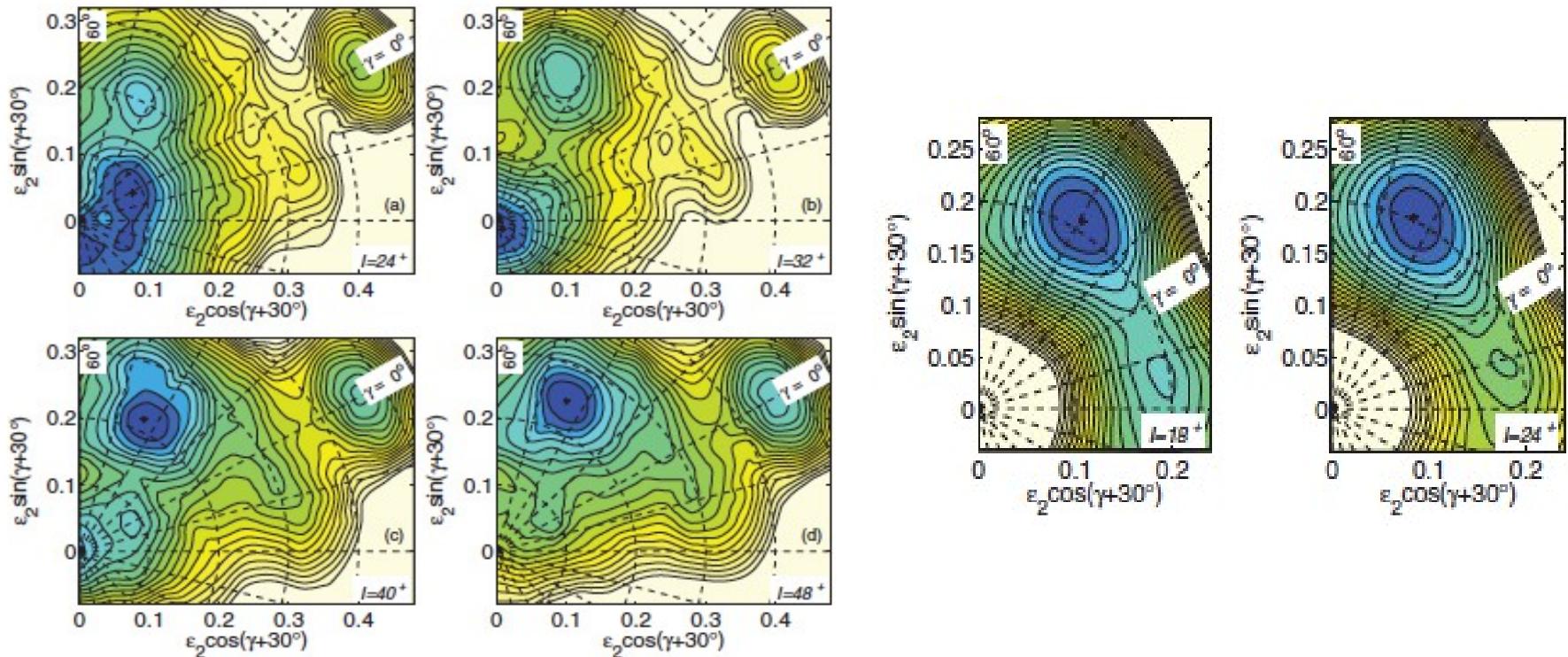


minimum that represents a TSD band. We have thus clarified a long-standing question pertaining to the nature of positive- and negative- $\gamma$  bands associated with the same intrinsic shape in the PAC approach: the rotation of a well-deformed, slightly triaxial configuration can be either about a short or medium axis, but not about both.

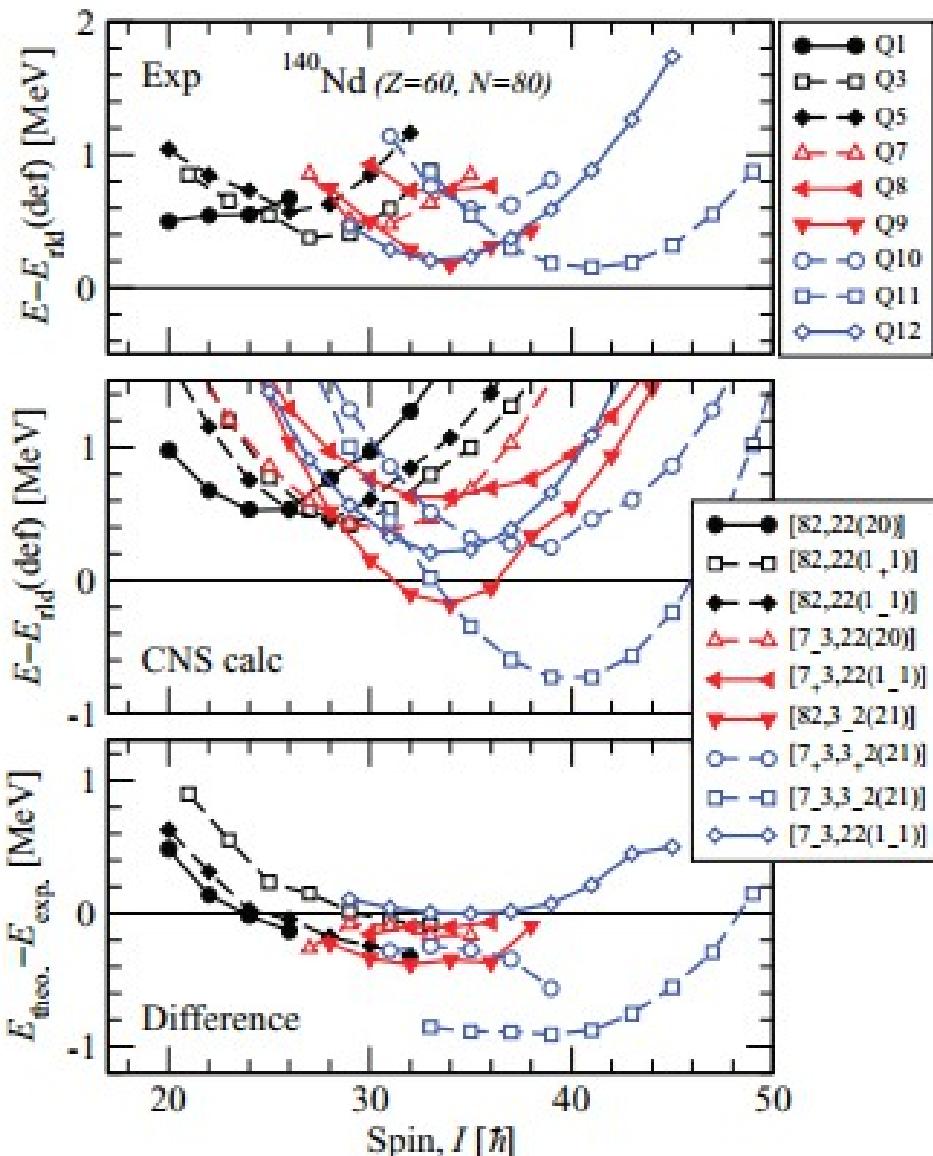
Y. Shi et al.,  
PRL 108,  
092501 (2012)

# Existence of stable triaxial shape at high spins in Lanthanides with $N < 82$ : $^{140}\text{Nd}$

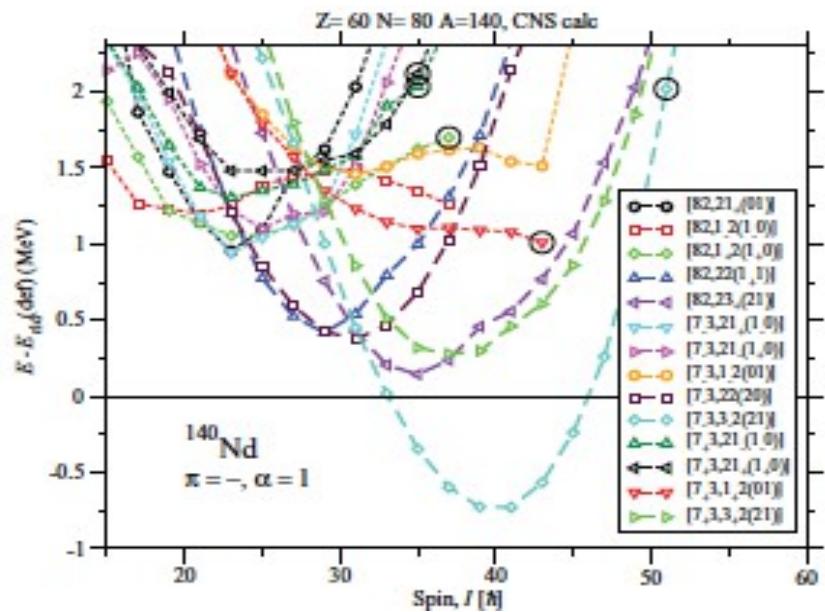
CNS calculations for  $^{140}\text{Nd}$  for  $(I,\pi)=(\text{even},+)$  and for the [82,22(20)] configuration of band Q1



# Comparison CNS - experiment for $^{140}\text{Nd}$



Energies relative to a  
axially deformed  
rotating liquid drop

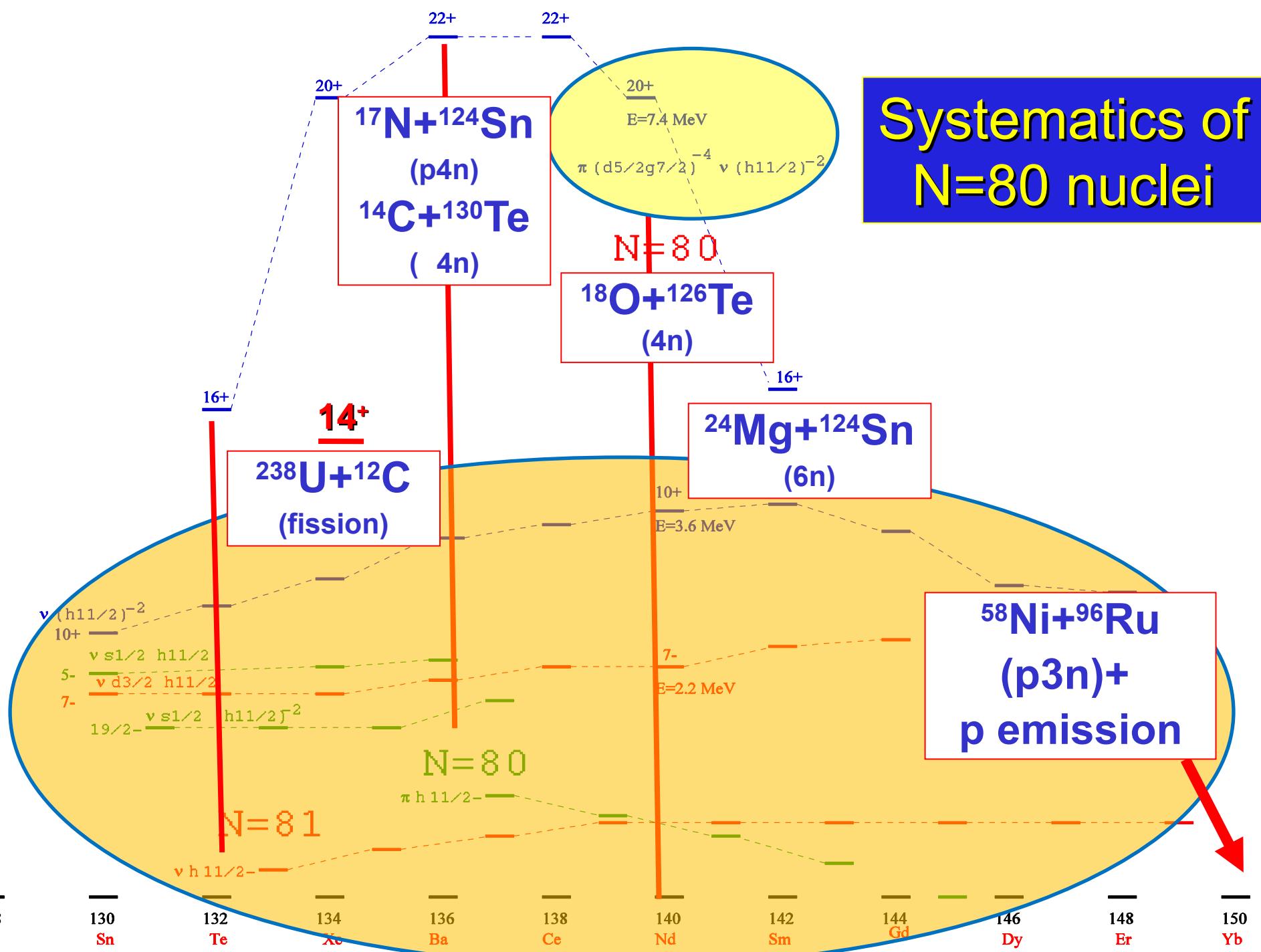


# Seniority isomers in nuclei around the N=82 shell closure

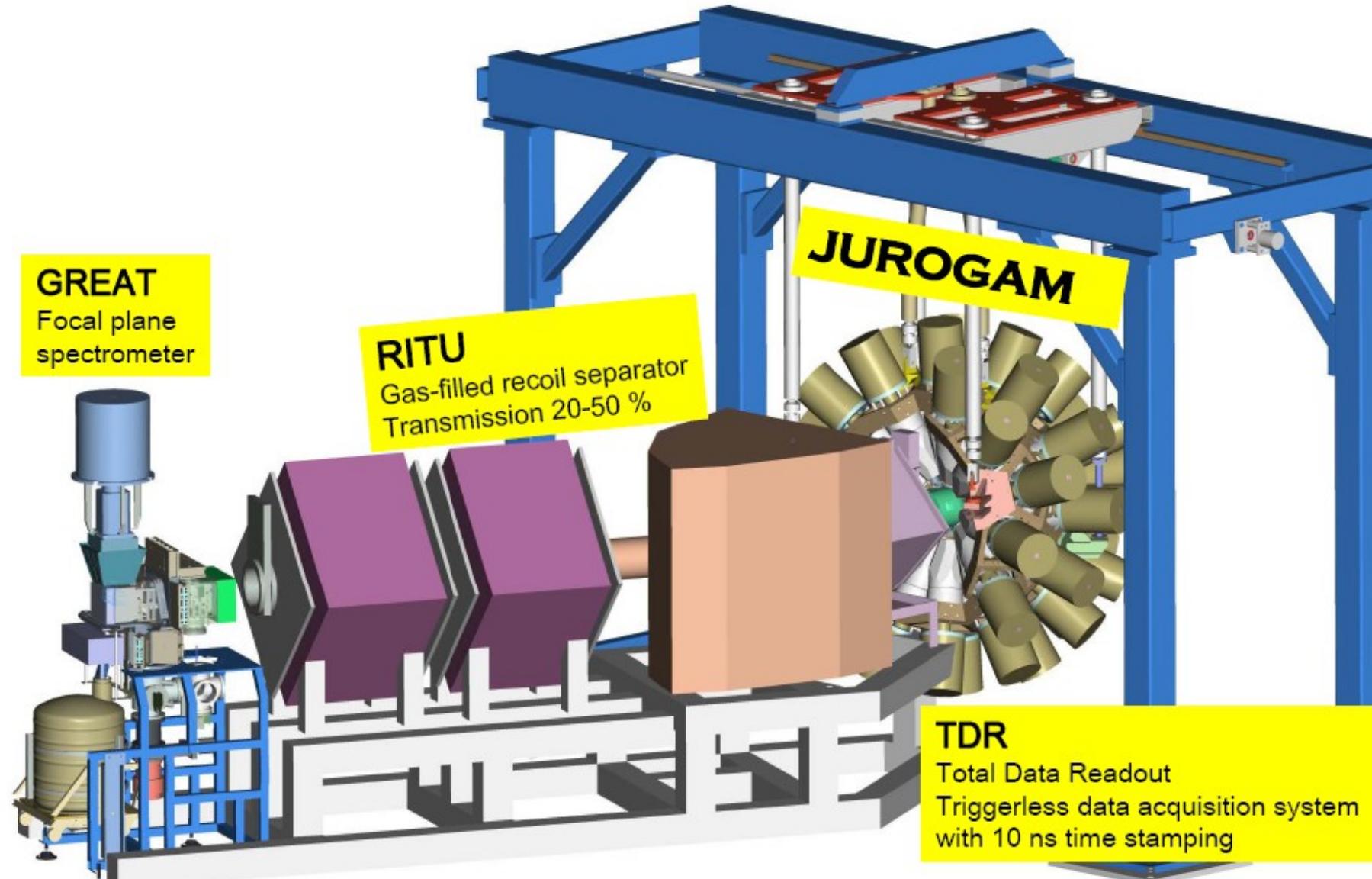
## Why study of isomers ?

- Constraints for matrix elements of effective residual interactions used in the shell-model calculations
- Improve the predictive power of effective interactions for neutron-rich nuclei

# Systematics of N=80 nuclei



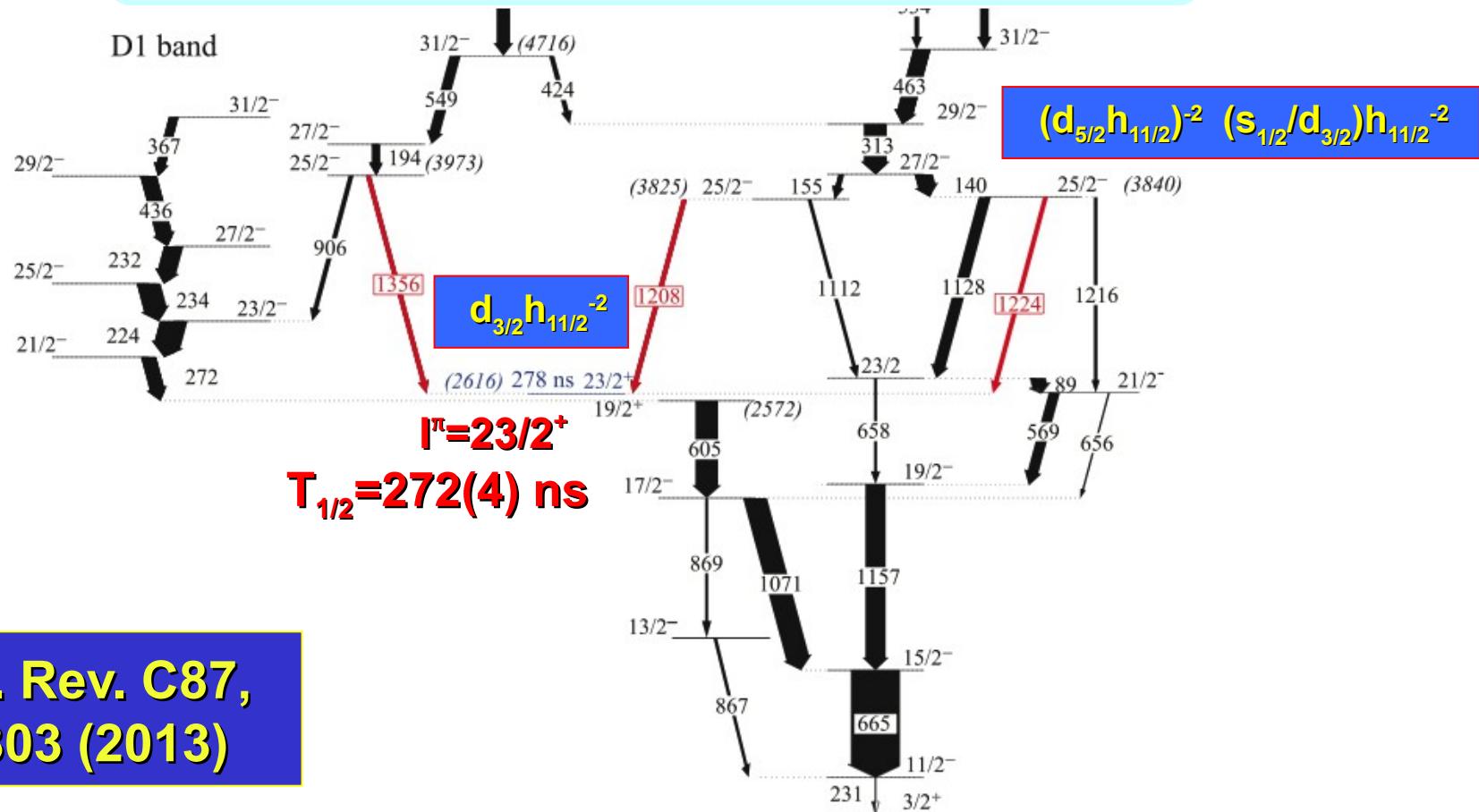
# JUROGAM+RITU at Jyväskylä ( $^{48}\text{Ca} + ^{96}\text{Zr}$ )



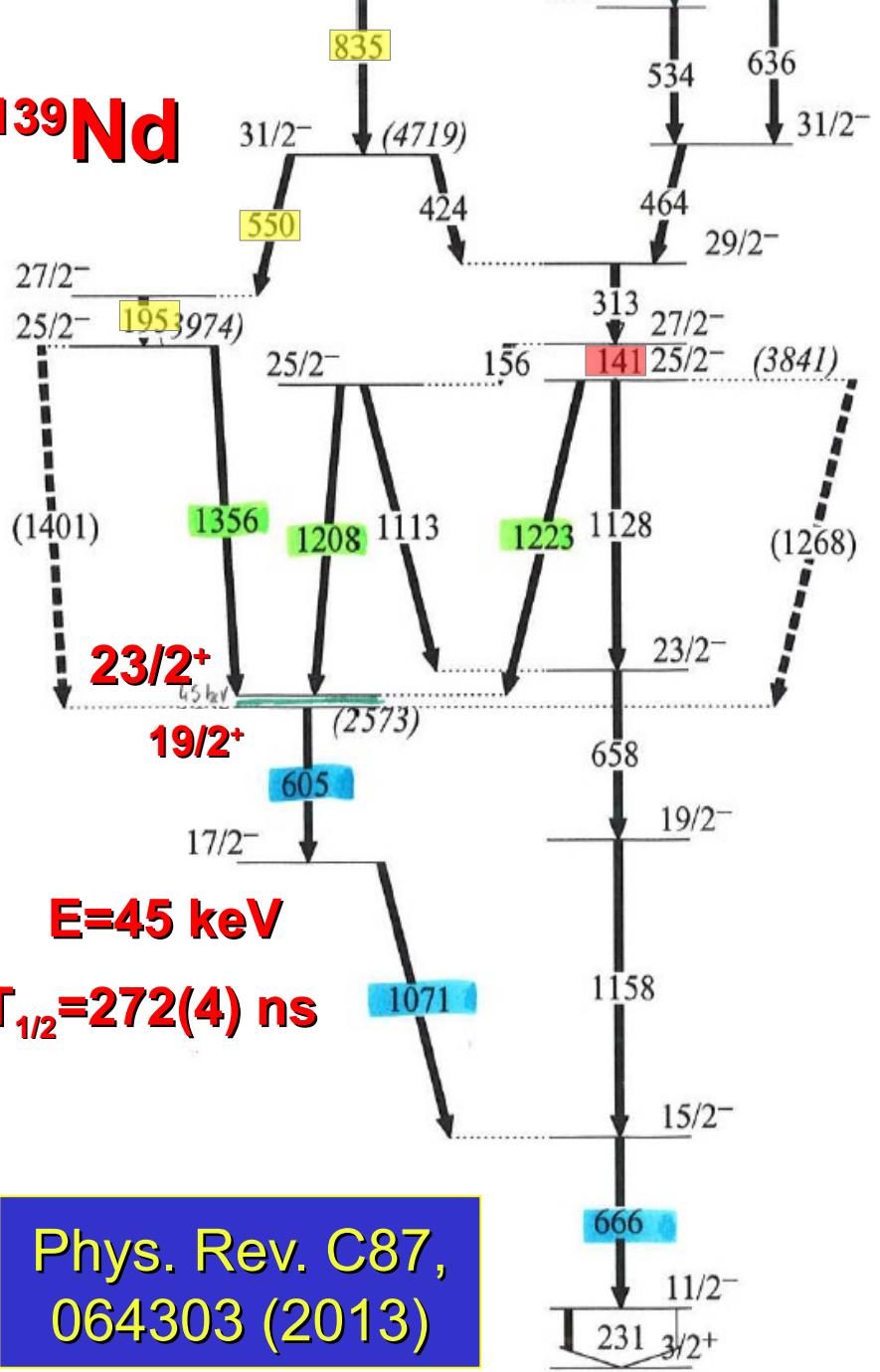
# Isomers in nuclei close to N=82

## Level scheme of $^{139}\text{Nd}$

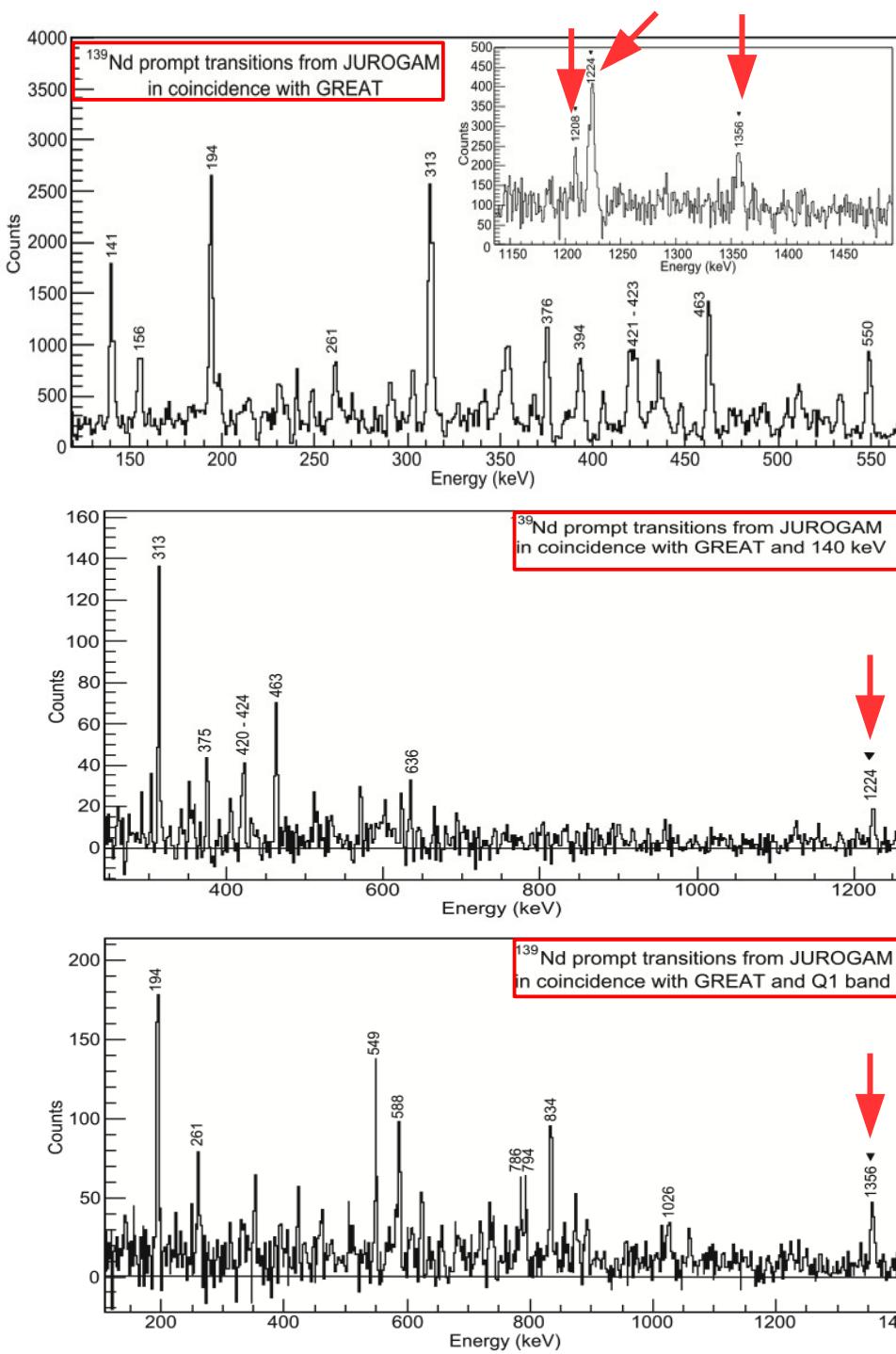
JUROGAM II + RITU  
Prompt  $\gamma$ -rays + recoil selection



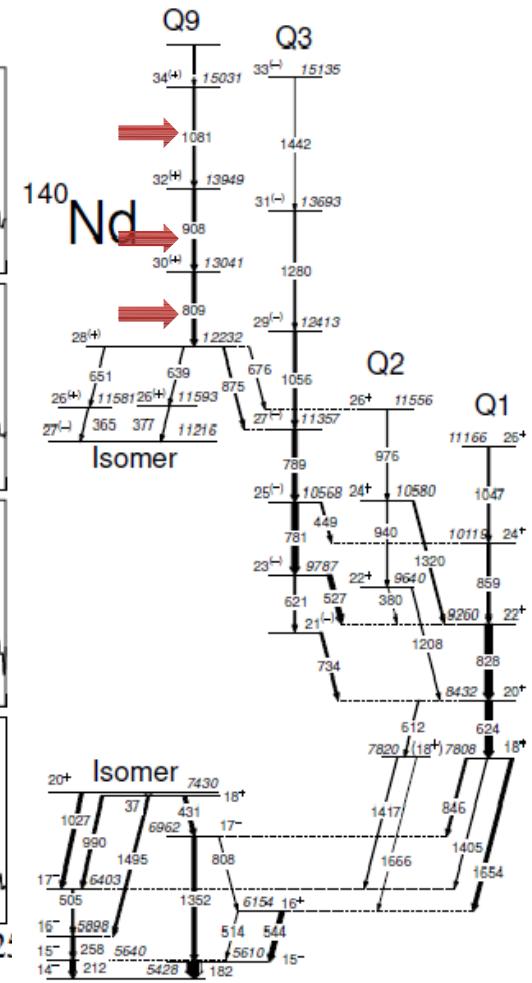
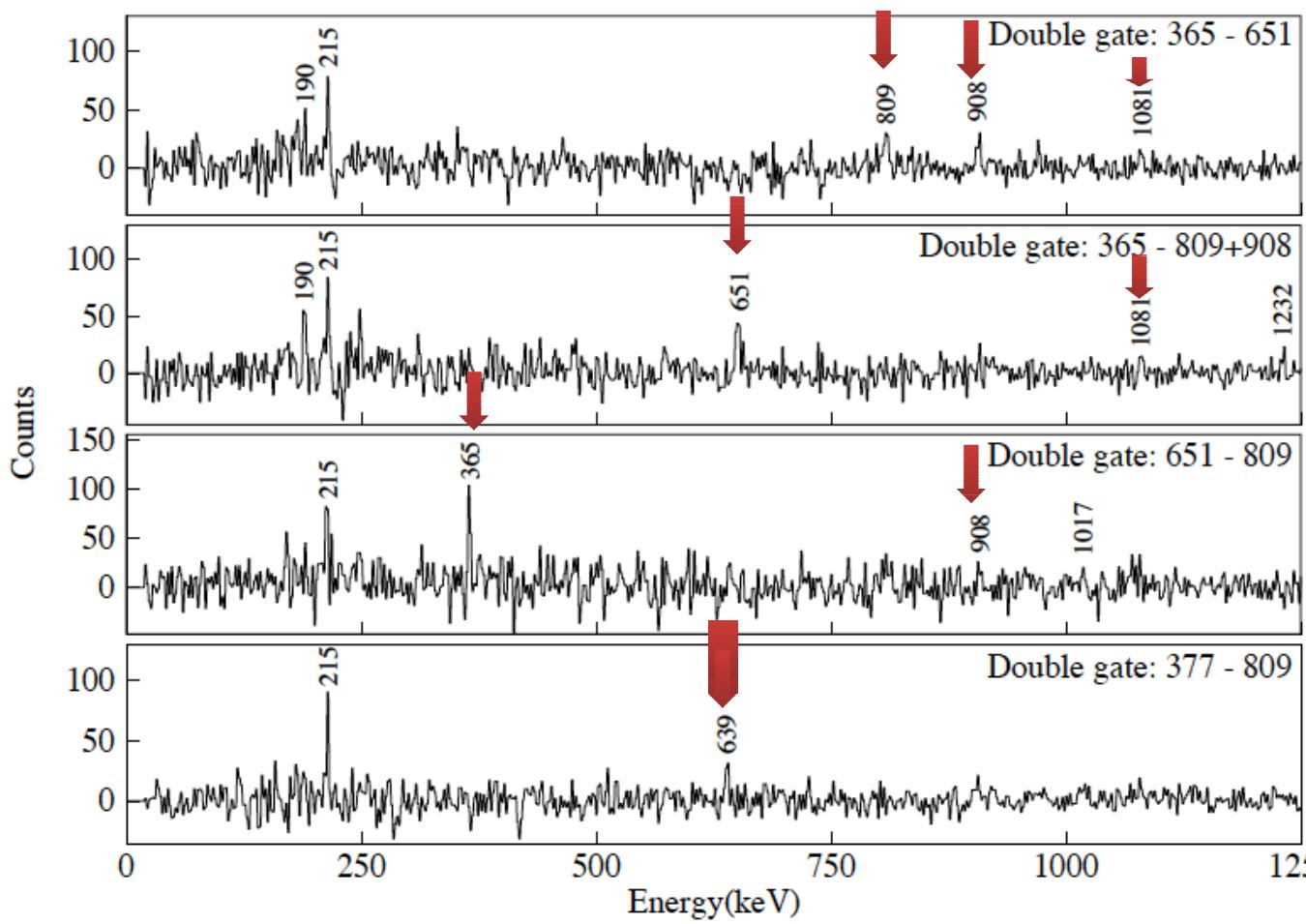
# $^{139}\text{Nd}$



Phys. Rev. C87,  
064303 (2013)



# Prompt coincidence spectra between transitions above the $27^-$ isomer



# Collaboration

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A. Astier, T. Konstantinopoulos

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IPN Lyon – N. Redon, O. Stezowski, D. Guinet, A. Vancrayenest

LTH Lund – I. Ragnarsson

Notre Dame University – S. Frauendorf

Fukuoka University – M. Matsuzaki

University of Jyväskylä – P. Greenlees et al.

University of Padova – S. Lunardi et al.