

# CP violation and oscillation parameter precision measurements

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Enrique Fernández Martínez



vProbes



in**v**isibles

neutrinos, dark matter & dark energy physics

# Oscillation Parameters

- What we already know ( $1\sigma$ )

- Solar sector  $\begin{cases} \Delta m_{21}^2 = 7.45_{-0.16}^{+0.19} \cdot 10^{-5} \text{ eV}^2 \\ \sin^2 \theta_{12} = 0.306_{-0.012}^{+0.012} \end{cases}$

- Atm. sector  $\begin{cases} \Delta m_{31}^2 = 2.417_{-0.013}^{+0.013} \cdot 10^{-3} / -2.410_{-0.062}^{+0.062} \cdot 10^{-3} \text{ eV}^2 \\ \sin^2 \theta_{23} = 0.446_{-0.007}^{+0.007} / 0.587_{-0.037}^{+0.032} \end{cases}$

$$\sin^2 \theta_{13} = 0.0229_{-0.0019}^{+0.002}$$

M. C. Gonzalez-Garcia, M. Maltoni, J. Salvado, T. Schwetz 1209.3023 [www.nu-fit.org](http://www.nu-fit.org)

See also: D. V. Forero, M. Tortola, J. Valle 1205.4018

G.L. Fogli, E. Lisi, A. Marrone, D. Montanino, A. Palazzo, A.M. Rotunno 1205.5254

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- What we still don't know

- $\delta$

- Mass hierarchy  $s_{atm} = \text{sign}(\Delta m_{31}^2)$

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# The Golden channel in matter

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_\mu) = s_{23}^2 \sin^2 2\theta_{13} \left( \frac{\Delta_{atm}}{\tilde{B}_\mp} \right)^2 \sin^2 \left( \frac{\tilde{B}_\mp L}{2} \right) \quad \text{“atmospheric”}$$

$$+ c_{23}^2 \sin^2 2\theta_{12} \left( \frac{\Delta_{sol} L}{A} \right)^2 \sin^2 \left( \frac{AL}{2} \right) \quad \text{“solar”}$$

$$\text{“interference”} + \tilde{J} \frac{\Delta_{sol}}{A} \frac{\Delta_{atm}}{\tilde{B}_\mp} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{\tilde{B}_\mp L}{2} \right) \cos \left( \pm \delta - \frac{\Delta_{atm} L}{2} \right)$$

Expanded in

$$\sin 2\theta_{13} \sim 0.3 \quad \left( \frac{\Delta_{sol} L}{2} \right) \cong 0.05$$

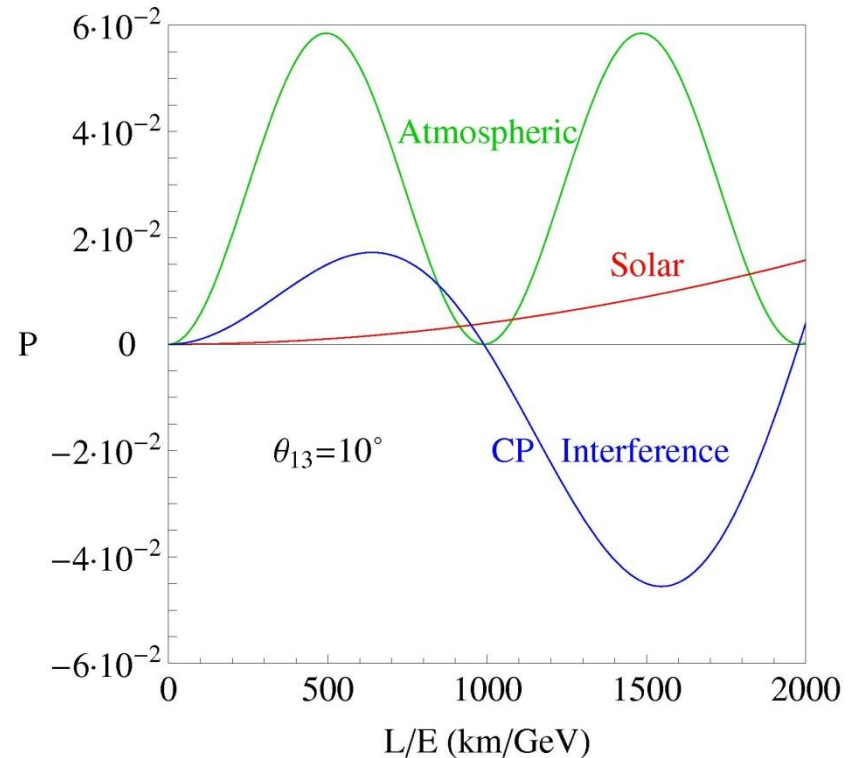
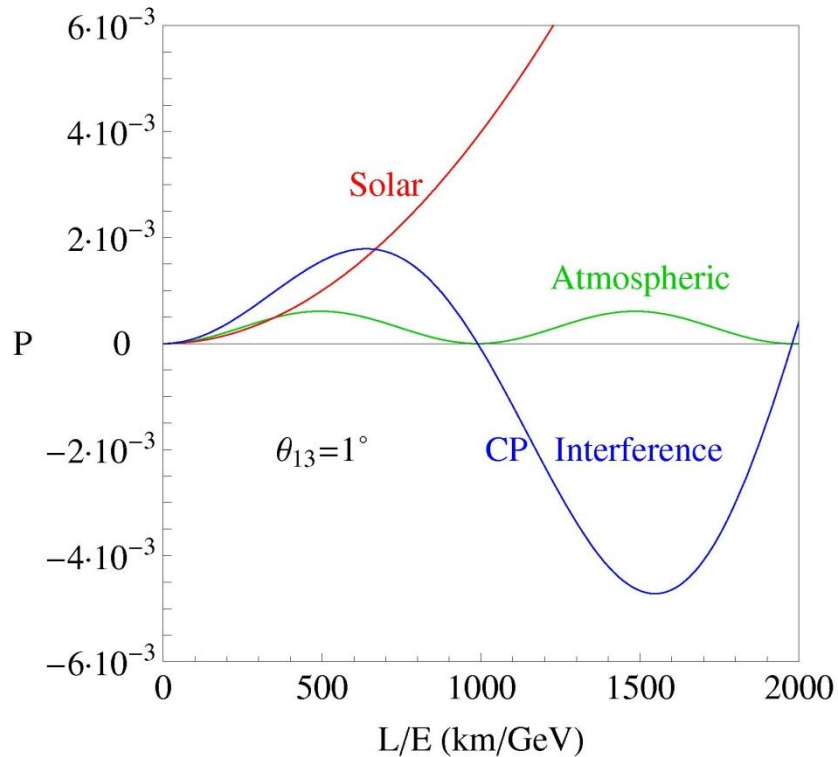
where

$$\tilde{J} = \cos \theta_{13} \sin 2\theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \quad \Delta_{atm} = \frac{\Delta m_{23}^2}{2E} \quad \Delta_{sol} = \frac{\Delta m_{12}^2}{2E}$$

$$A = \sqrt{2} G_F n_e \quad \tilde{B}_\mp = |A \mp \Delta_{atm}|$$

A. Cervera *et al.* hep-ph/0002108

# Optimization of facilities for large $\theta_{13}$

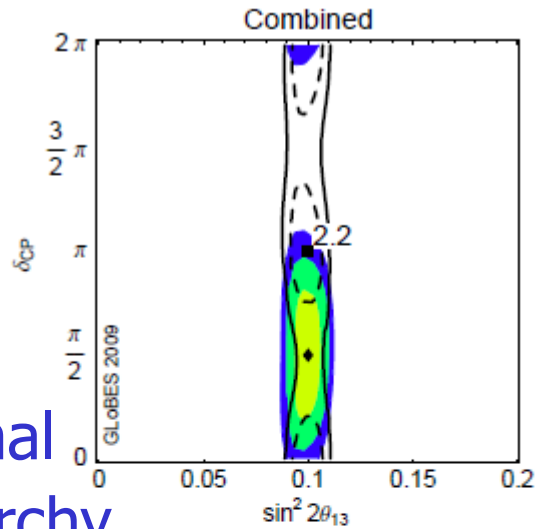


Signal systematics and not stats becomes the bottleneck for large  $\theta_{13}$

P. Coloma and EFM 1110.4583

# Sensitivities with present experiments

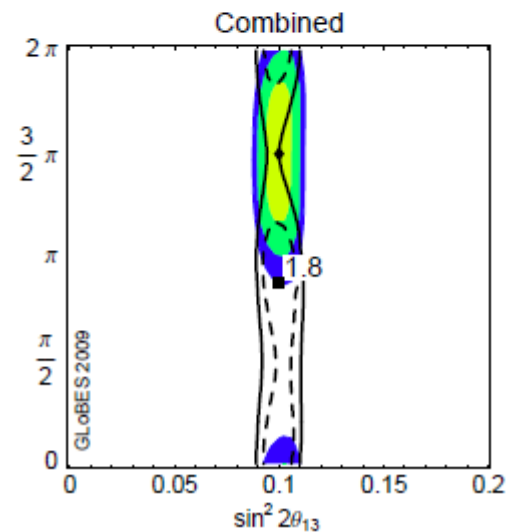
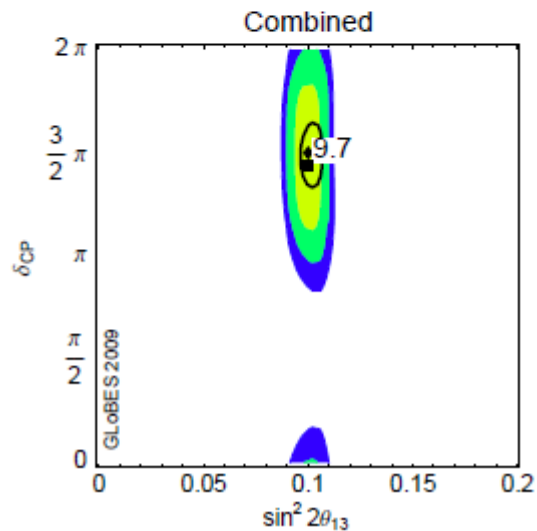
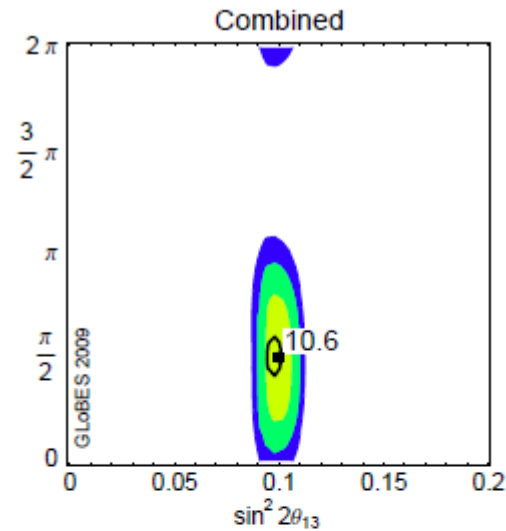
Normal  
hierarchy



1, 2 and 3  $\sigma$

T2K+  
Nova+  
Daya Bay

Inverted  
hierarchy



From P. Huber *et al.* 0907.1896

# List of facilities

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	detector vol. (kt)/type	dist. (km)	power (MW)	proton driver energy (GeV)	years $\nu/\bar{\nu}$
ESS $\nu$ SB-360	500/WC	360	5	2.0/3.0	2/8
ESS $\nu$ SB-540	500/WC	540	5	2.0/3.0	2/8
Hyper-K	560/WC	295	0.75	30	3/7
LBNE-10	10/LAr	1290	0.72	120	5/5
LBNE-PX	34/LAr	1290	2.2	120	5/5
LBNO-EoI	20/LAr	2300	0.7	400	5/5
IDS-NF	100/MIND	2000	4	10*	10**
NuMAX	10/LAr (magnetized)	1300	1	5*	5/5

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Big WC detectors, low energies, small matter effects

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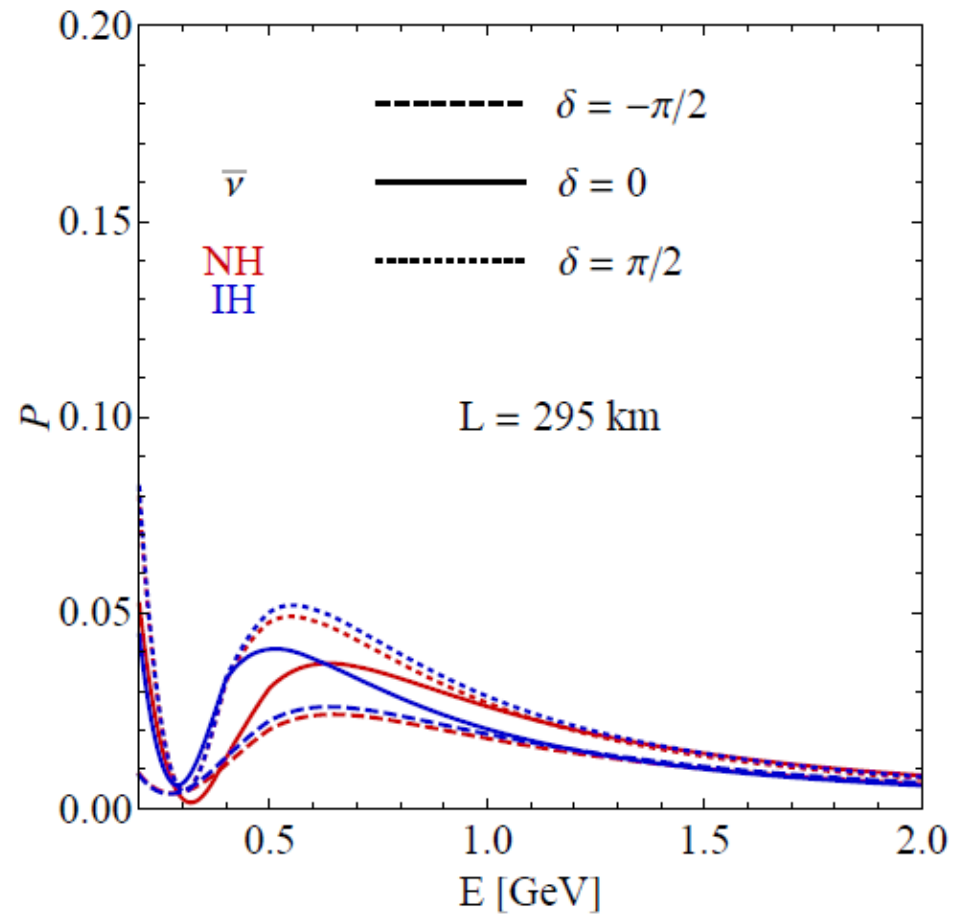
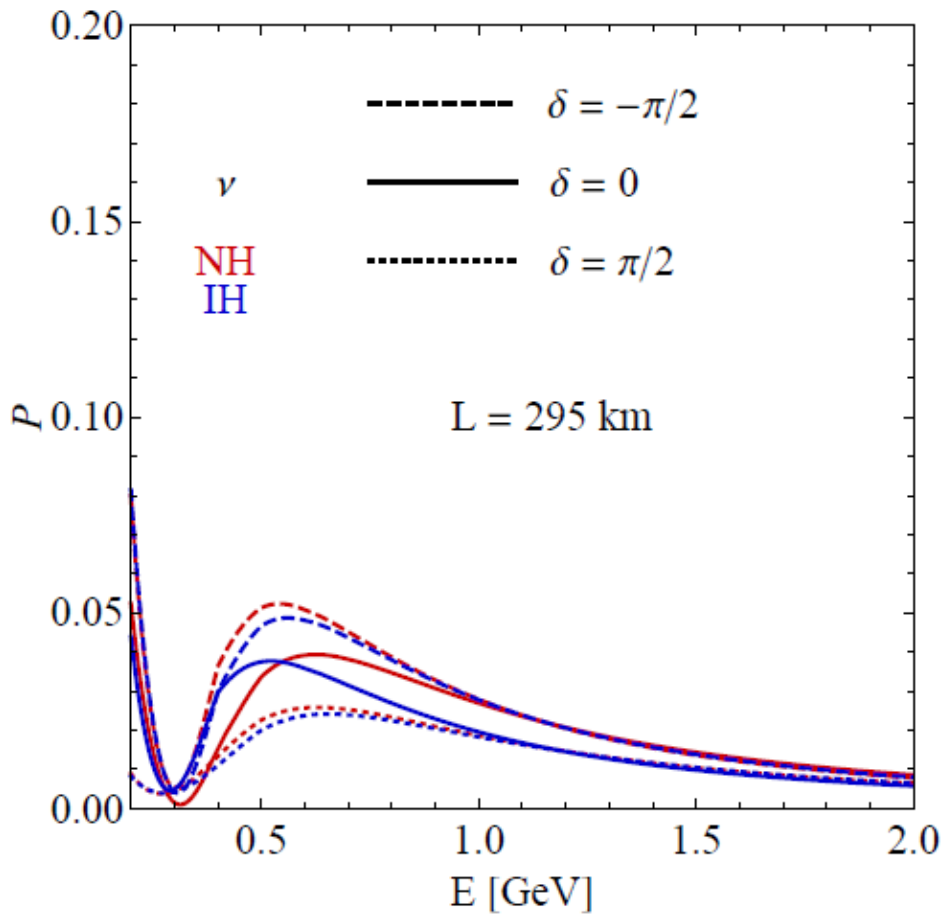
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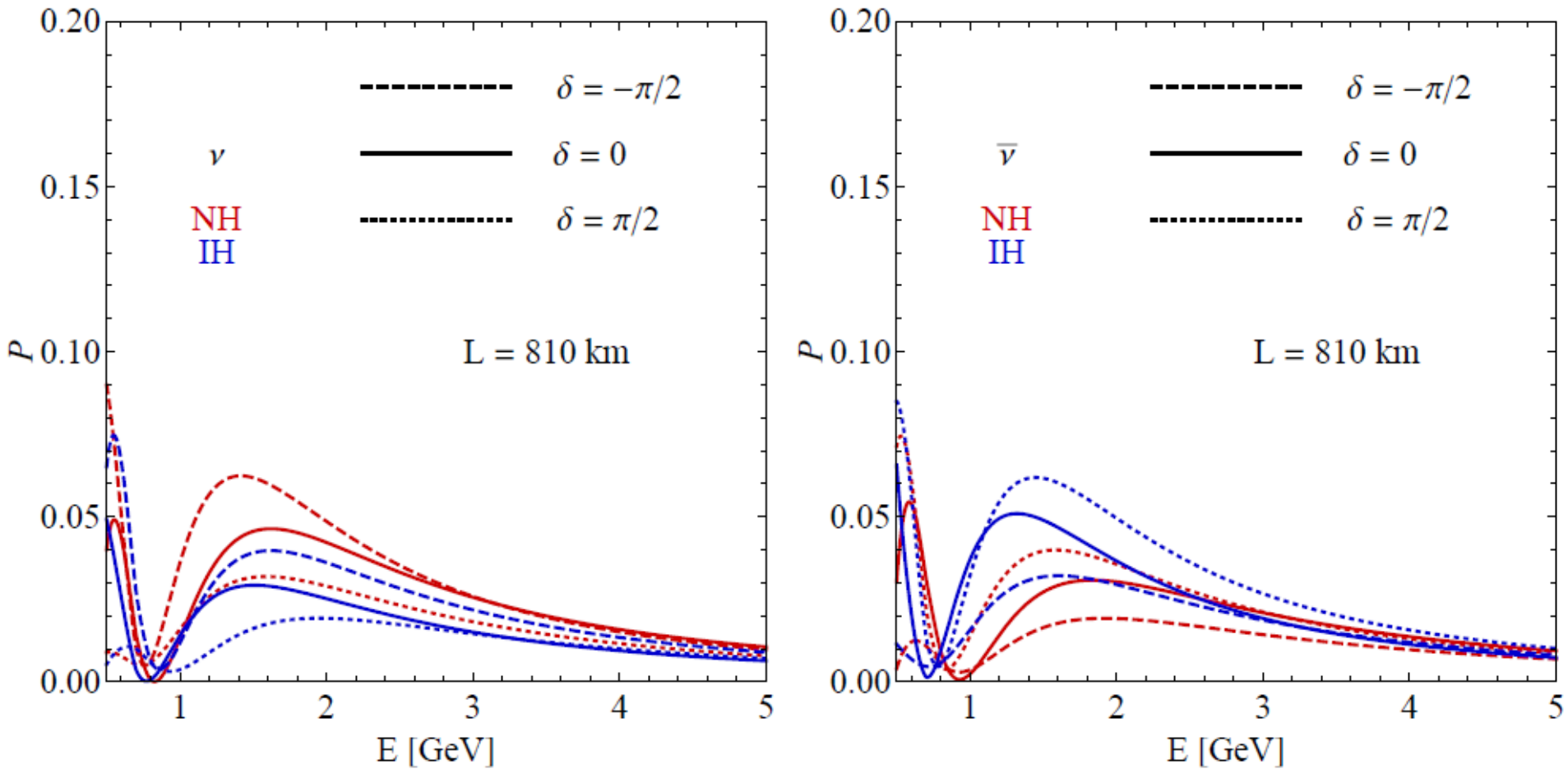
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LAr detectors, high energies and broad beams, big matter effects

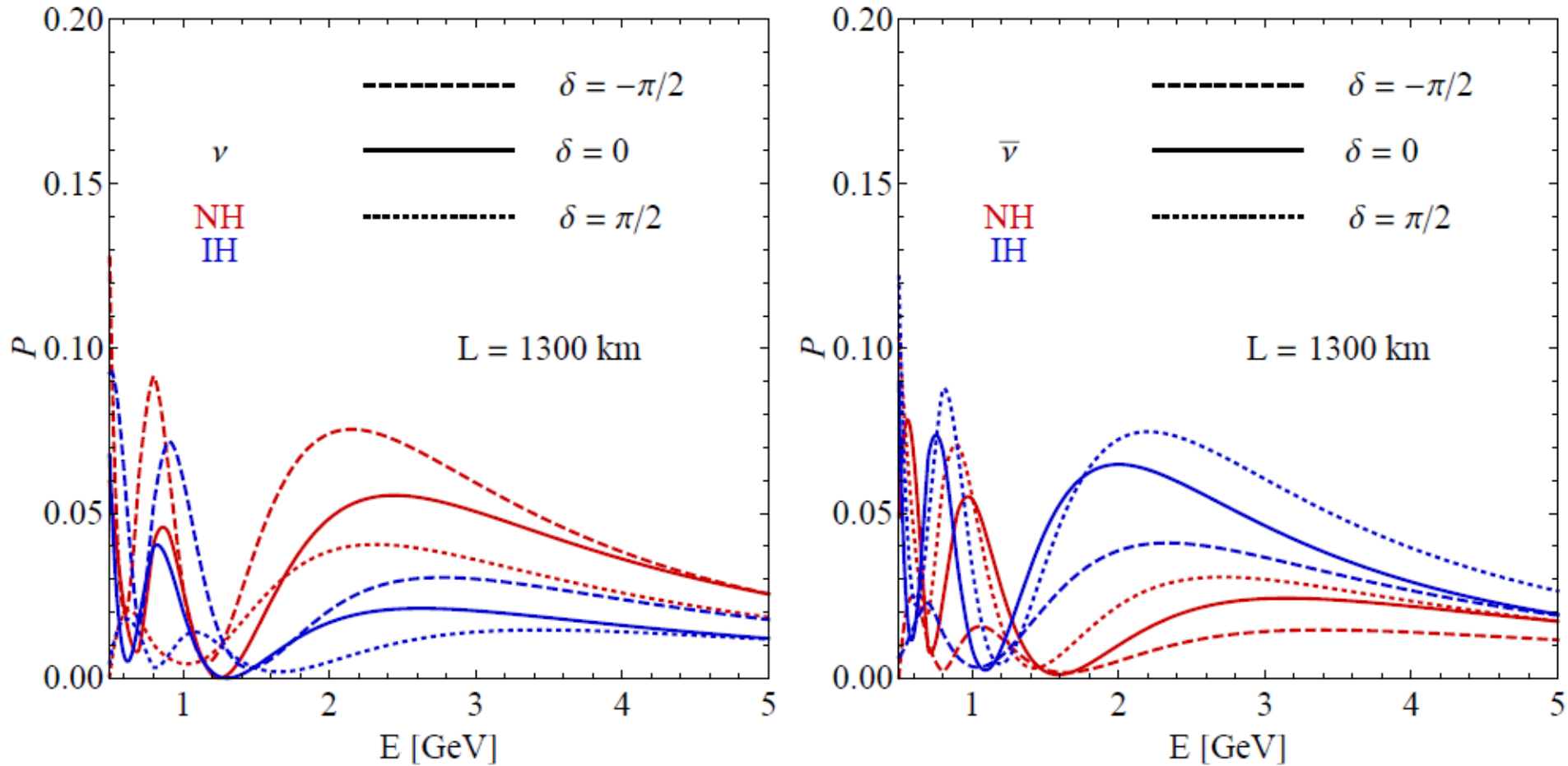
# Probabilities



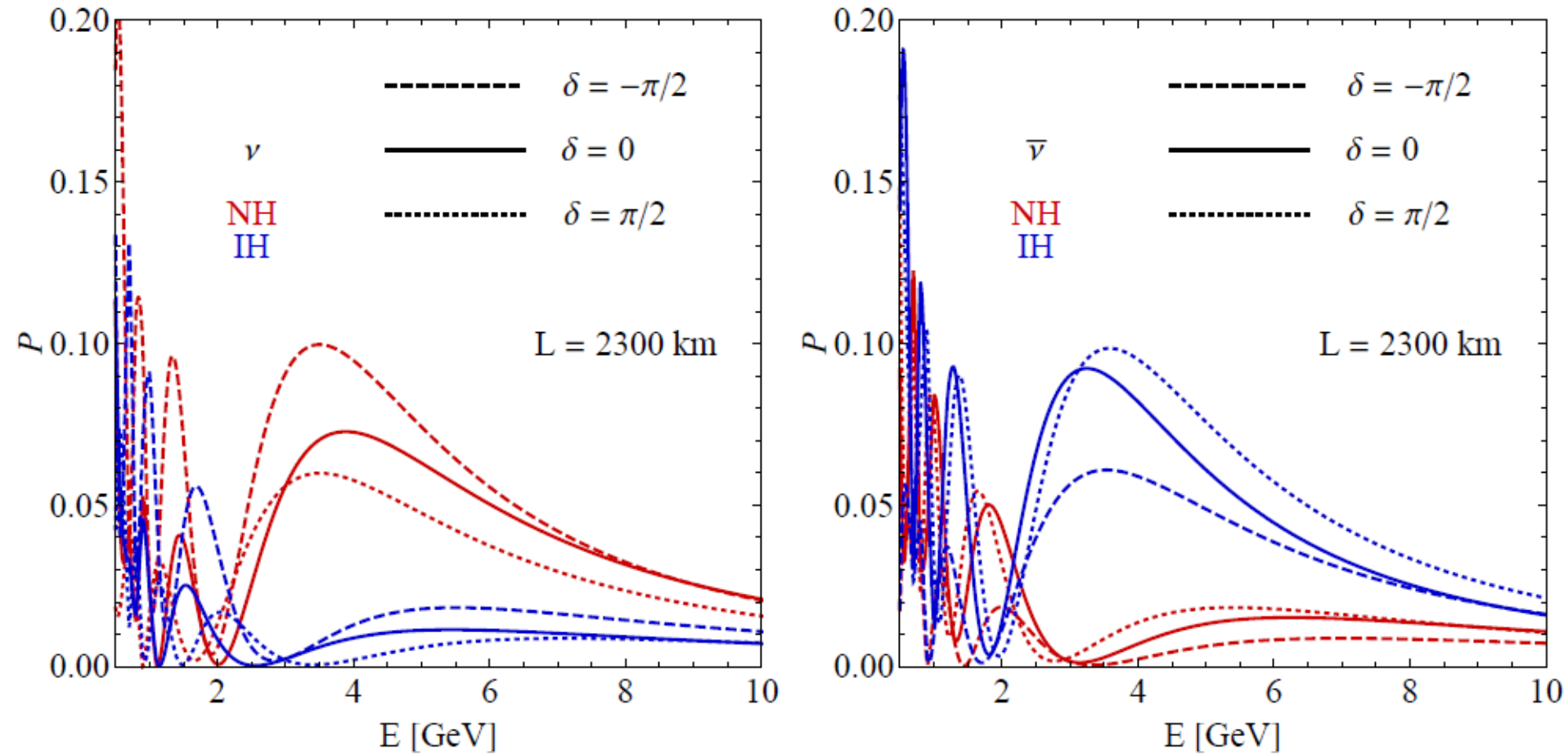
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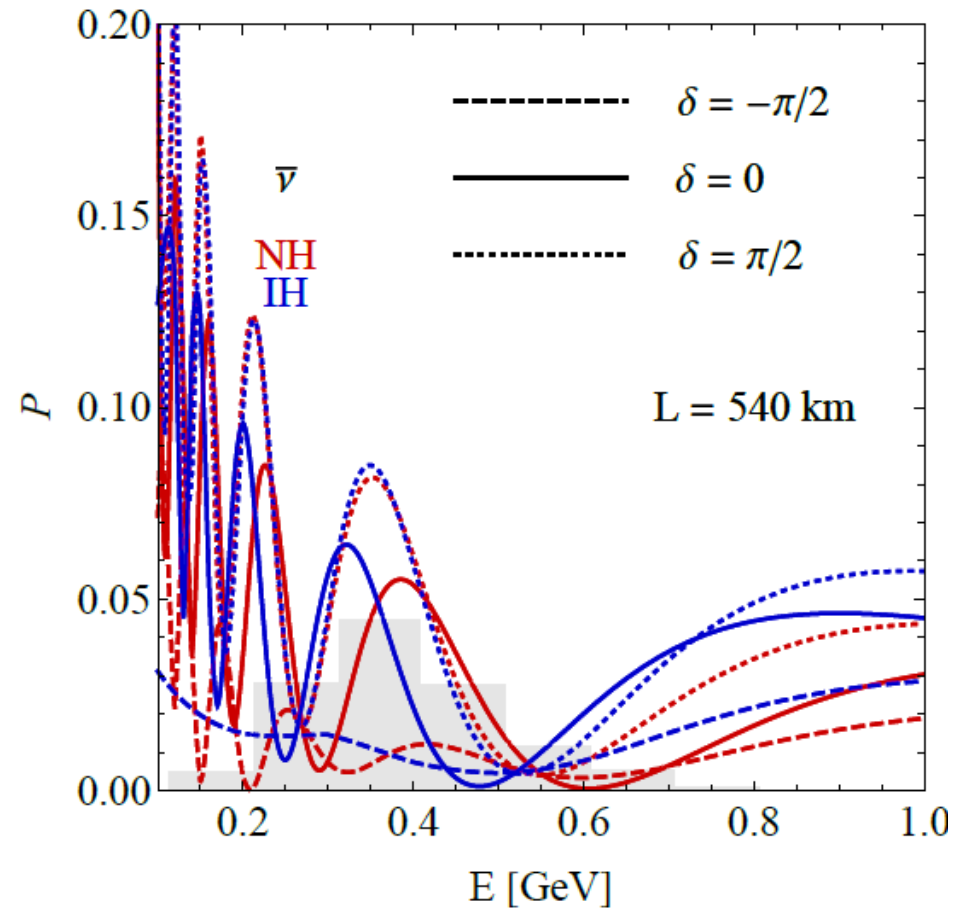
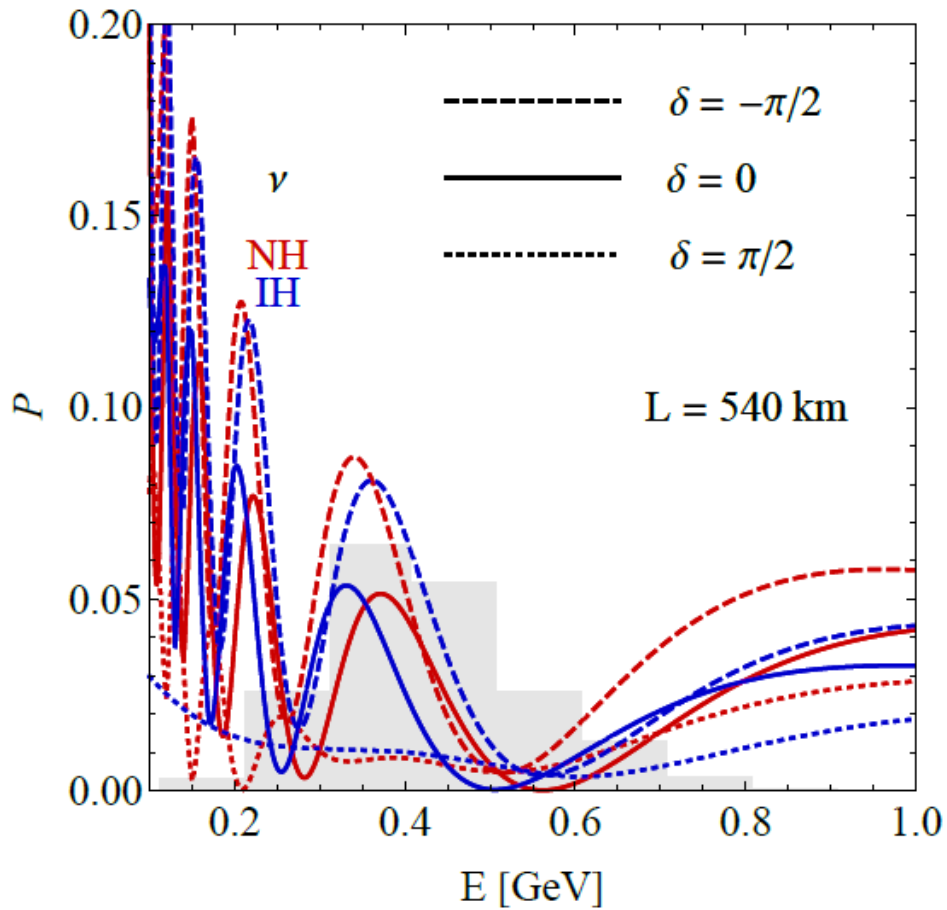
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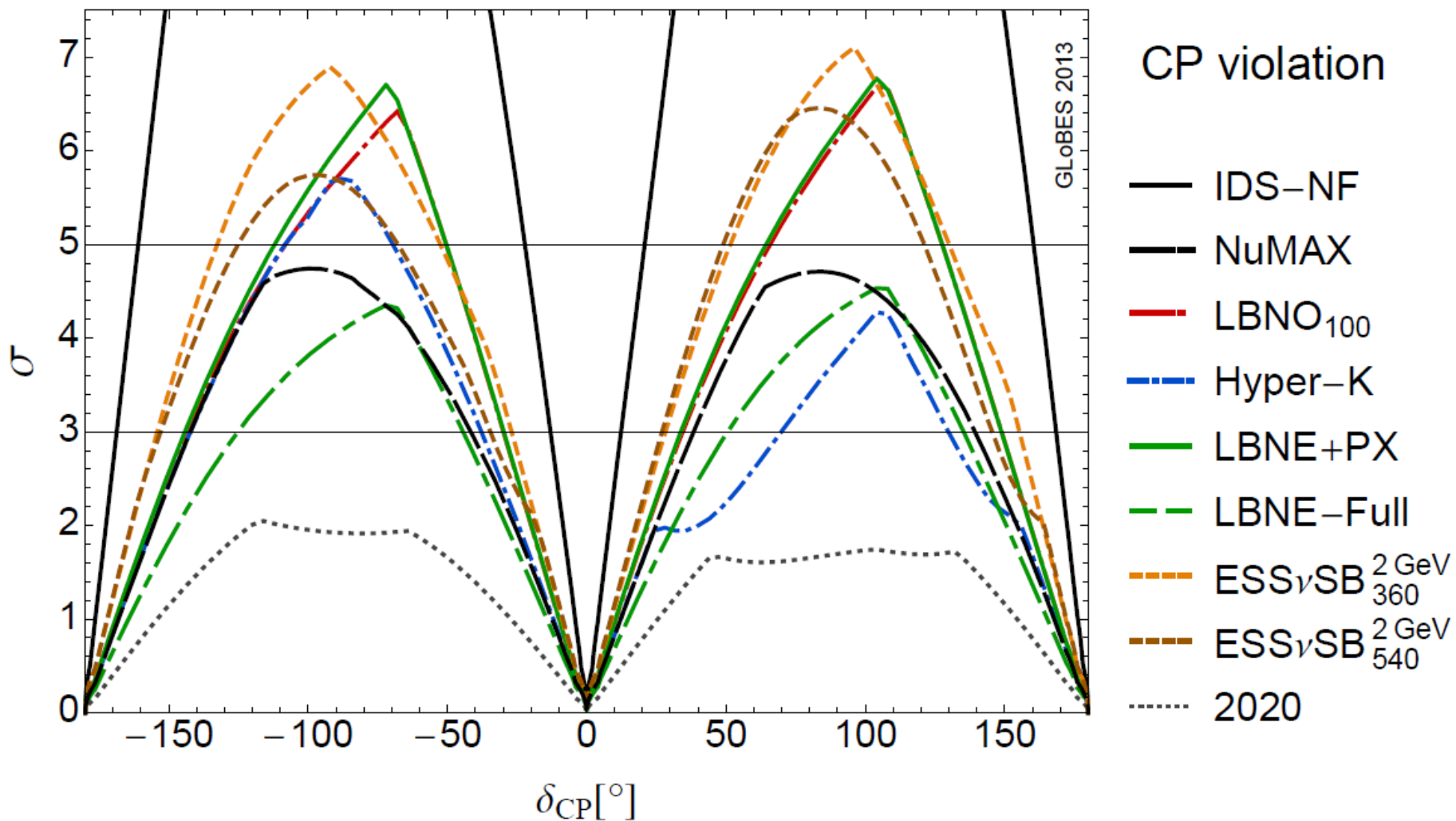
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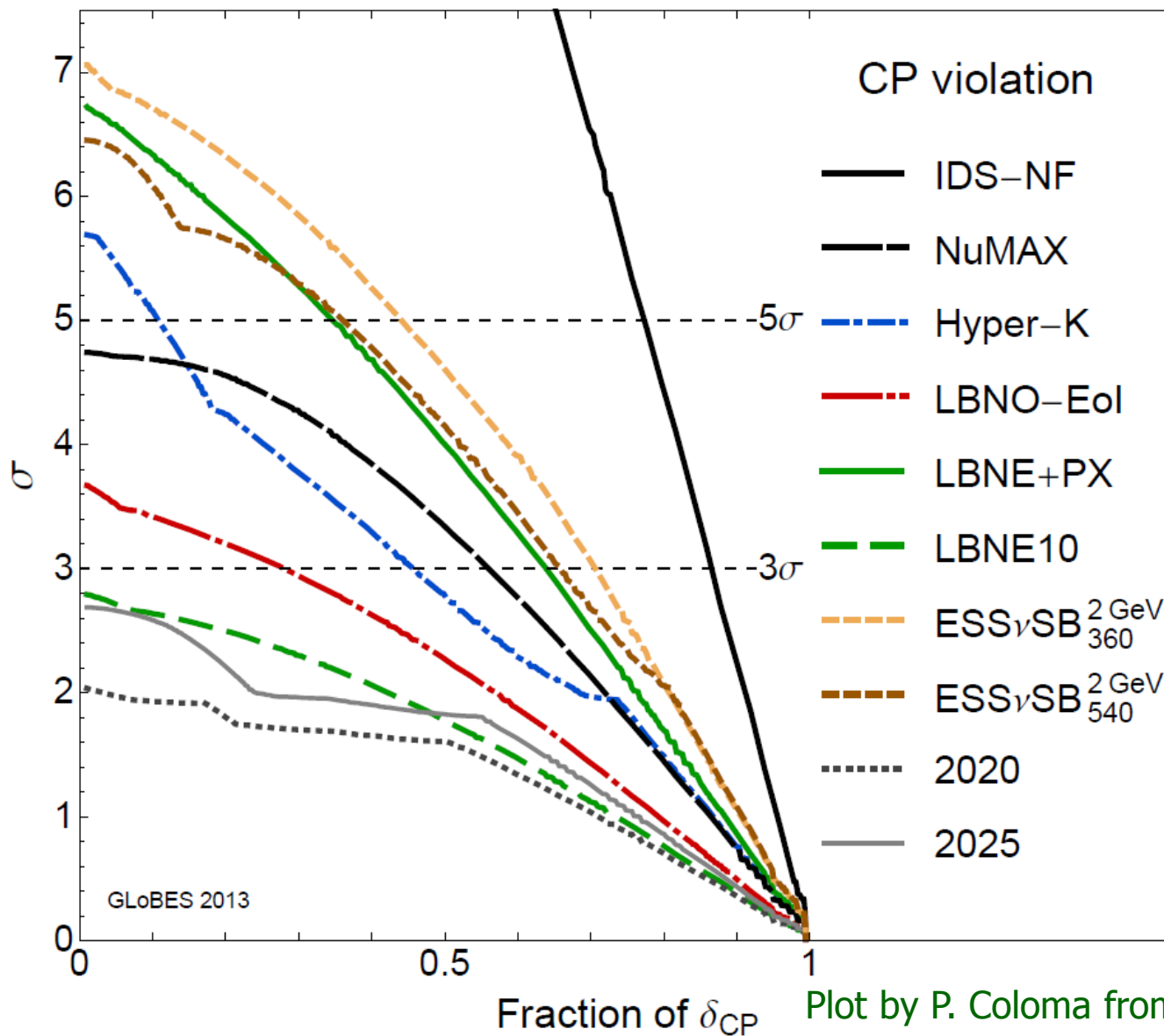
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# Sensitivities to CPV

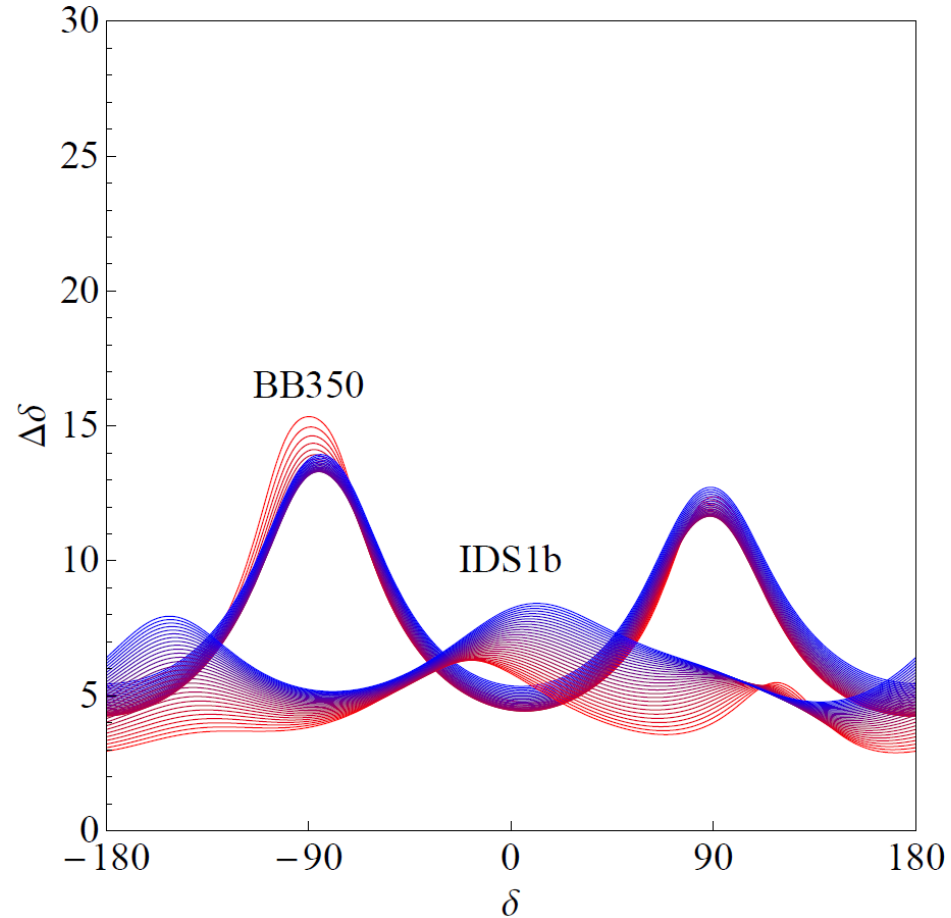
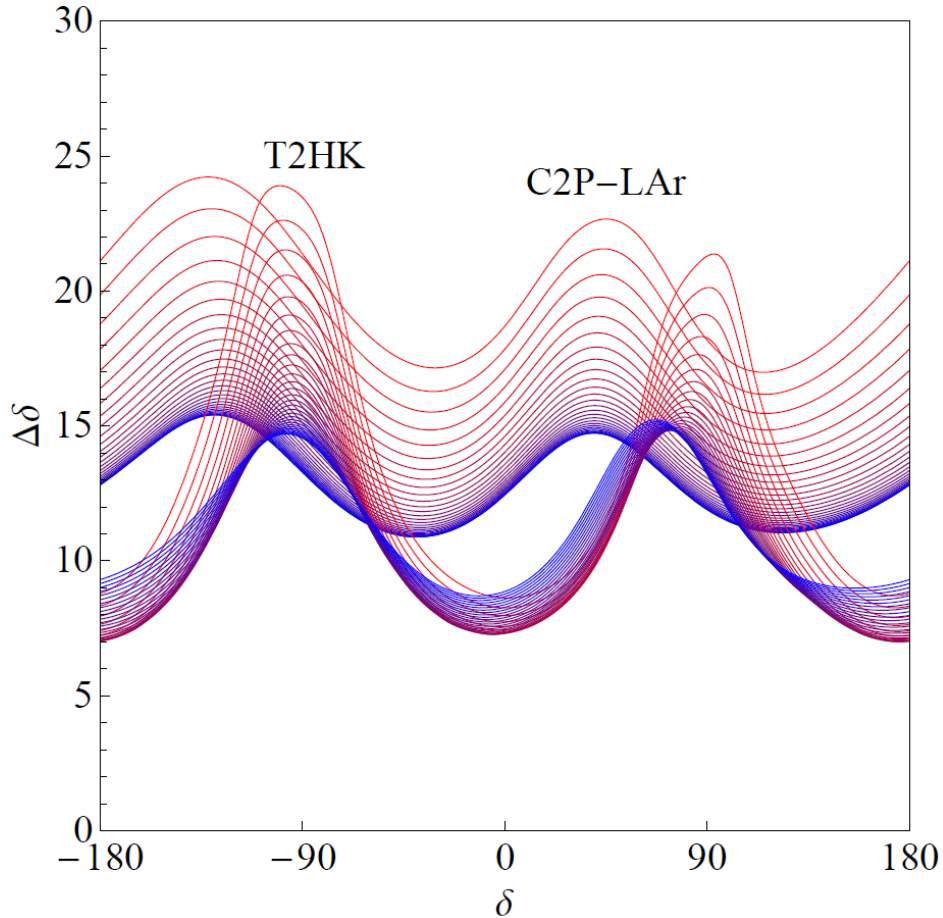


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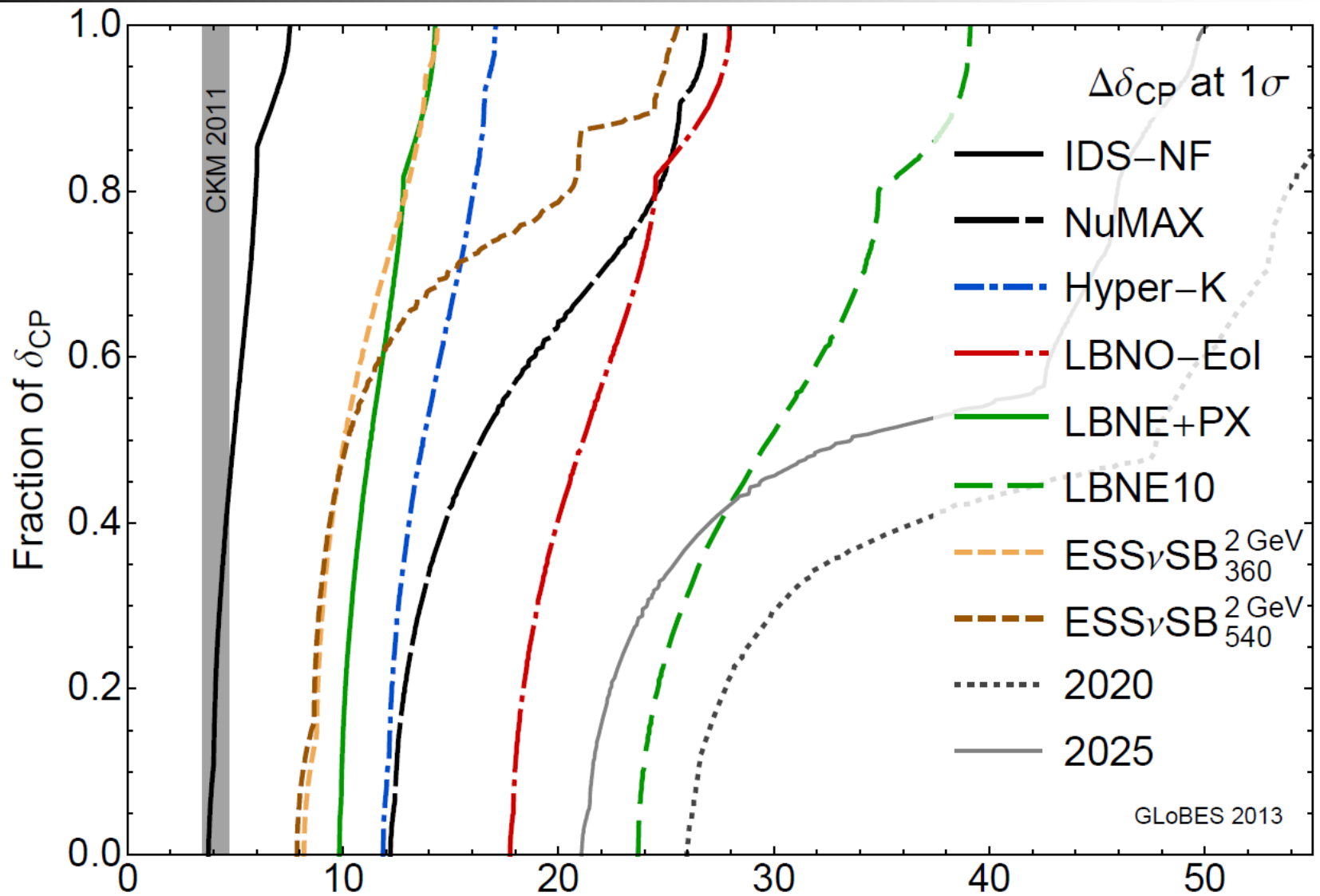


# Precision



$\theta_{13}$ :  $3^\circ$  -  $10^\circ$

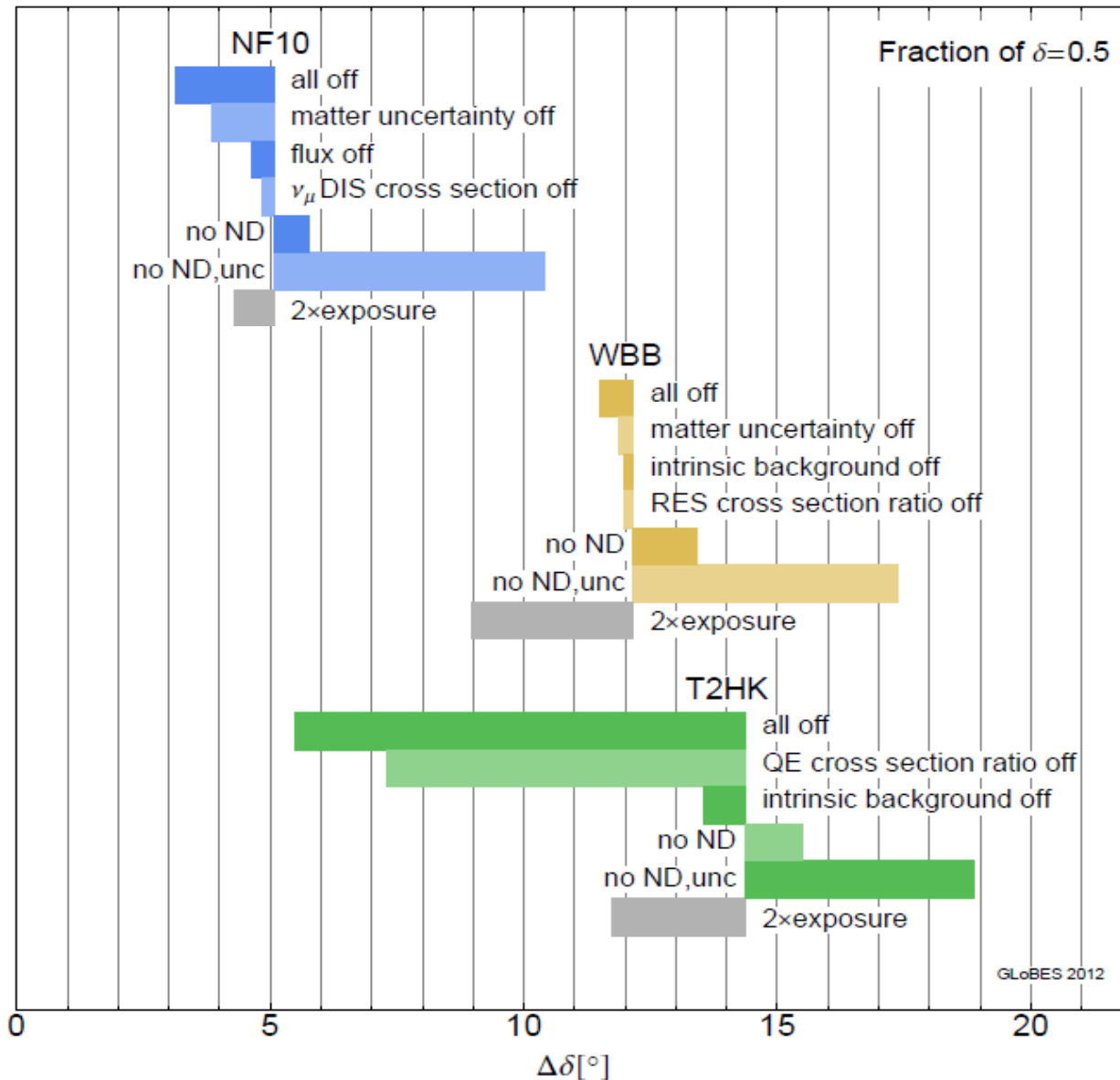
# Precision in $\delta$



# Systematics

Systematics	SB			NF		
	Opt.	Def.	Cons.	Opt.	Def.	Cons.
Fiducial volume ND	0.2%	0.5%	1%	0.2%	0.5%	1%
Fiducial volume FD (incl. near-far extrap.)	1%	2.5%	5%	1%	2.5%	5%
Flux error signal $\nu$	5%	7.5%	10%	0.1%	0.5%	1%
Flux error background $\nu$	10%	15%	20%	correlated		
Flux error signal $\bar{\nu}$	10%	15%	20%	0.1%	0.5%	1%
Flux error background $\bar{\nu}$	20%	30%	40%	correlated		
Background uncertainty	5%	7.5%	10%	10%	15%	20%
Cross secs $\times$ eff. QE <sup>†</sup>	10%	15%	20%	10%	15%	20%
Cross secs $\times$ eff. RES <sup>†</sup>	10%	15%	20%	10%	15%	20%
Cross secs $\times$ eff. DIS <sup>†</sup>	5%	7.5%	10%	5%	7.5%	10%
Effec. ratio $\nu_e/\nu_\mu$ QE <sup>*</sup>	3.5%	11%	–	–	–	–
Effec. ratio $\nu_e/\nu_\mu$ RES <sup>*</sup>	2.7%	5.4%	–	–	–	–
Effec. ratio $\nu_e/\nu_\mu$ DIS <sup>*</sup>	2.5%	5.1%	–	–	–	–
Matter density	1%	2%	5%	1%	2%	5%

# Systematics

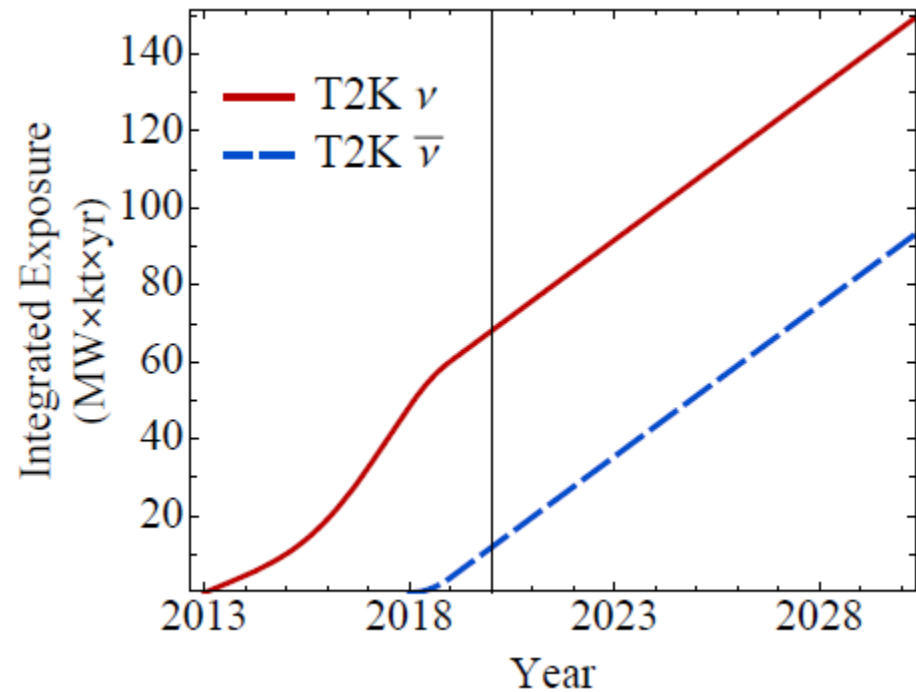
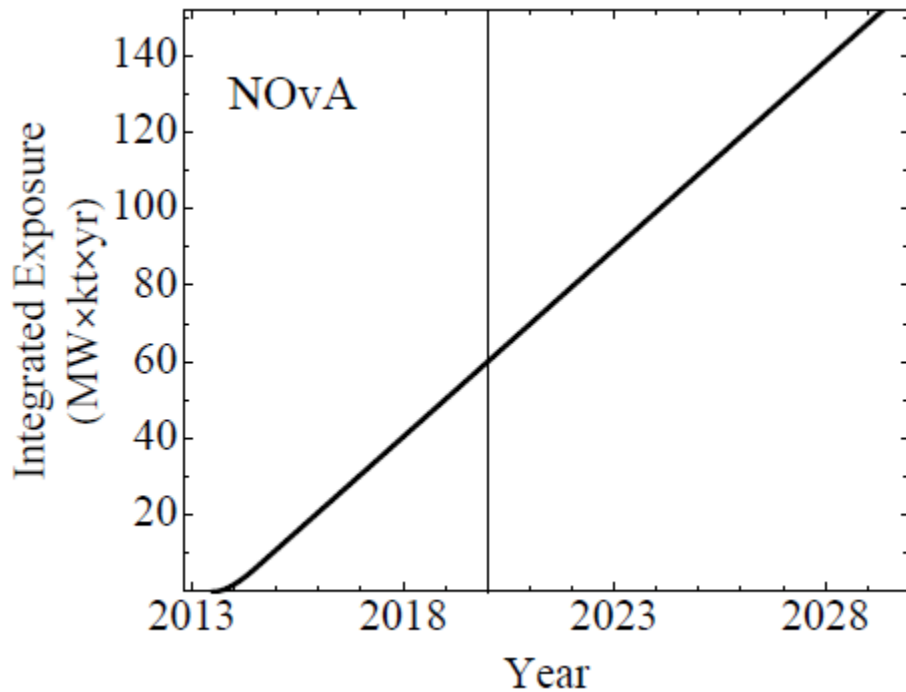


# Conclusions

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- The large value of  $\theta_{13}$  discovered opens the window to the measurement of the neutrino mass hierarchy and leptonic CP violation.
- T2K and Nova will provide the first  $\sim 90\%$  CL indications over the next 8 years. In order to reach discovery, upgraded or new facilities will be needed.
- The optimization strategy for CPV also changes for large  $\theta_{13}$ : importance of systematic errors and the second oscillation peak over statistics and backgrounds.

# T2K+NO $\nu$ A Running time



# Sensitivities with future experiments

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4. Repeat for as many **"true values"** as you want and plot

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But, will a **single** realization of the experiment actually reach the **expected** sensitivity?

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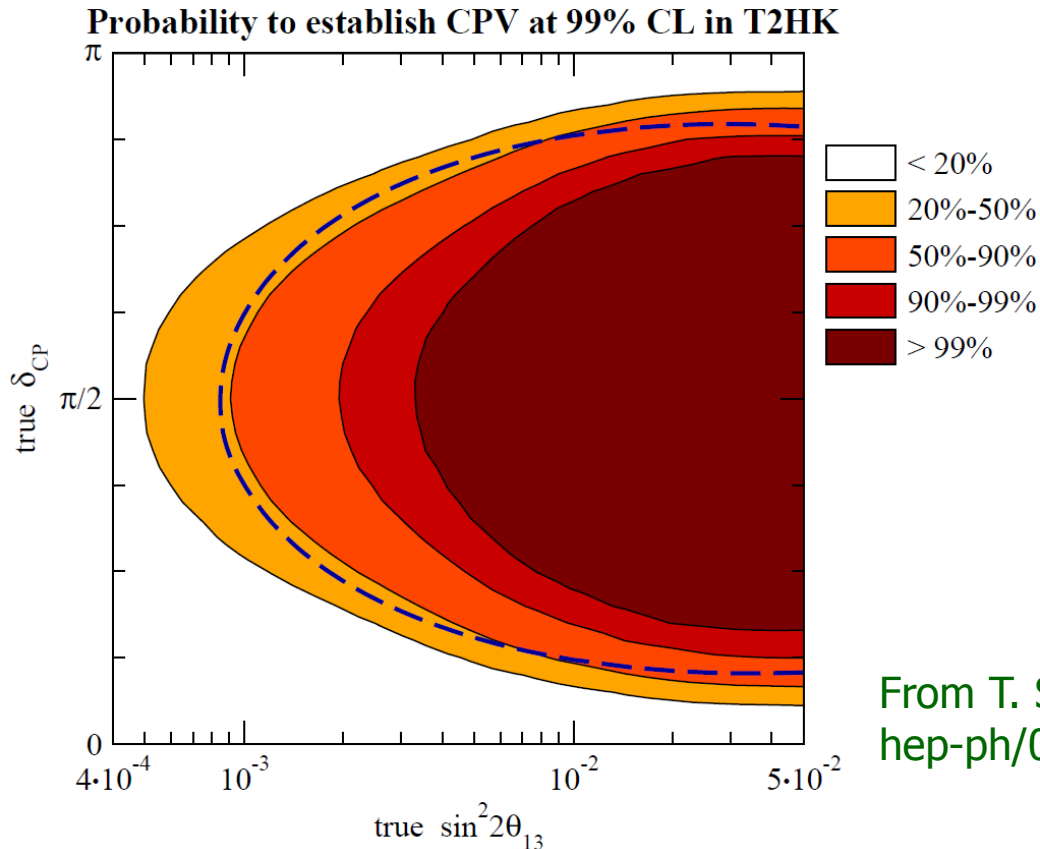
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From T. Schwetz  
hep-ph/0612223

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The first could get lucky, the second unlucky...

Naturally the two things are correlated

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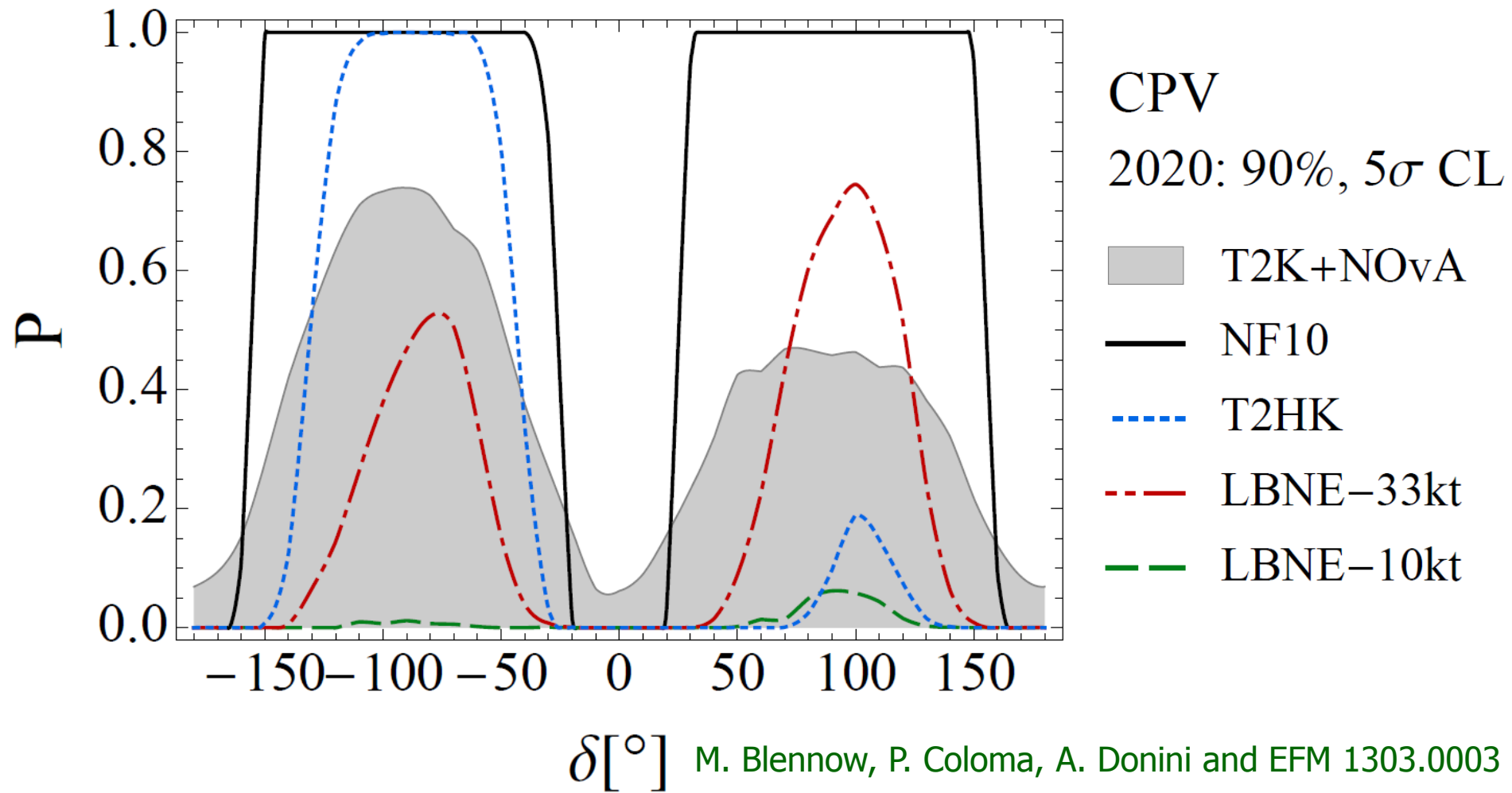
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3. Compute the  $\chi^2$  between each realization and the **"null hypothesis"** and check if the target CL was reached for that realization. Count how many, that gives an estimation of the success probability.
4. Repeat for as many **"true values"** as you want and plot

# Probabilities for CPV discovery



90 % CL for T2K+NO $\nu$ A,  $5\sigma$  for the rest  
Sensitivity peaked around  $\pm 90^\circ$  for all

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- $\sin^2 \theta_{13} = 0.0229_{-0.0019}^{+0.002}$

- What we still don't know

- $\delta = -95_{-61}^{+56}$

- Mass hierarchy  $s_{atm} = \text{sign}(\Delta m_{31}^2)$

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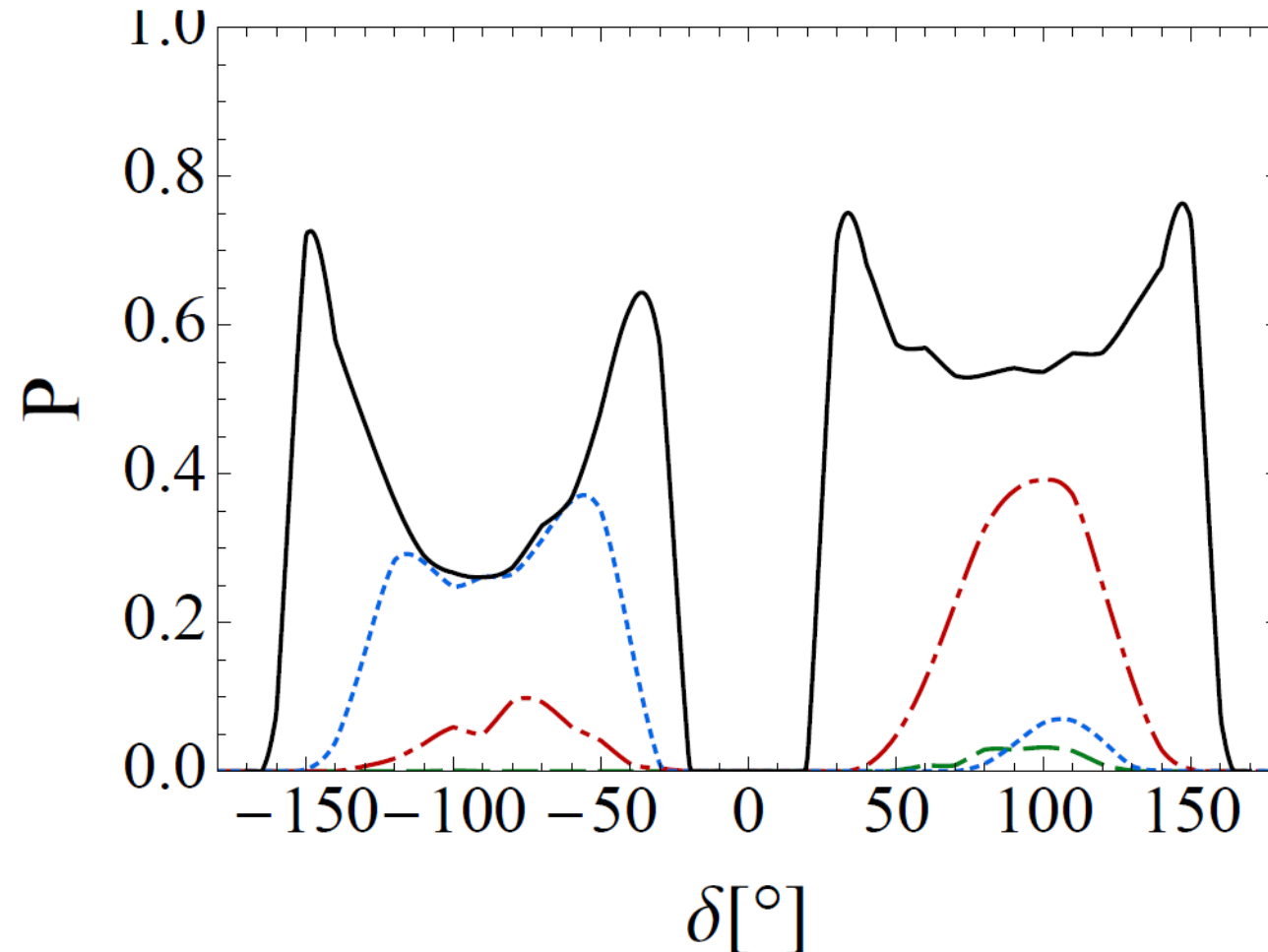
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# Probabilities for CPV discovery

Sensitivity peaked around  $\pm 90^\circ$  for all  
If T2K+NO $\nu$ A dont see, will the others see?

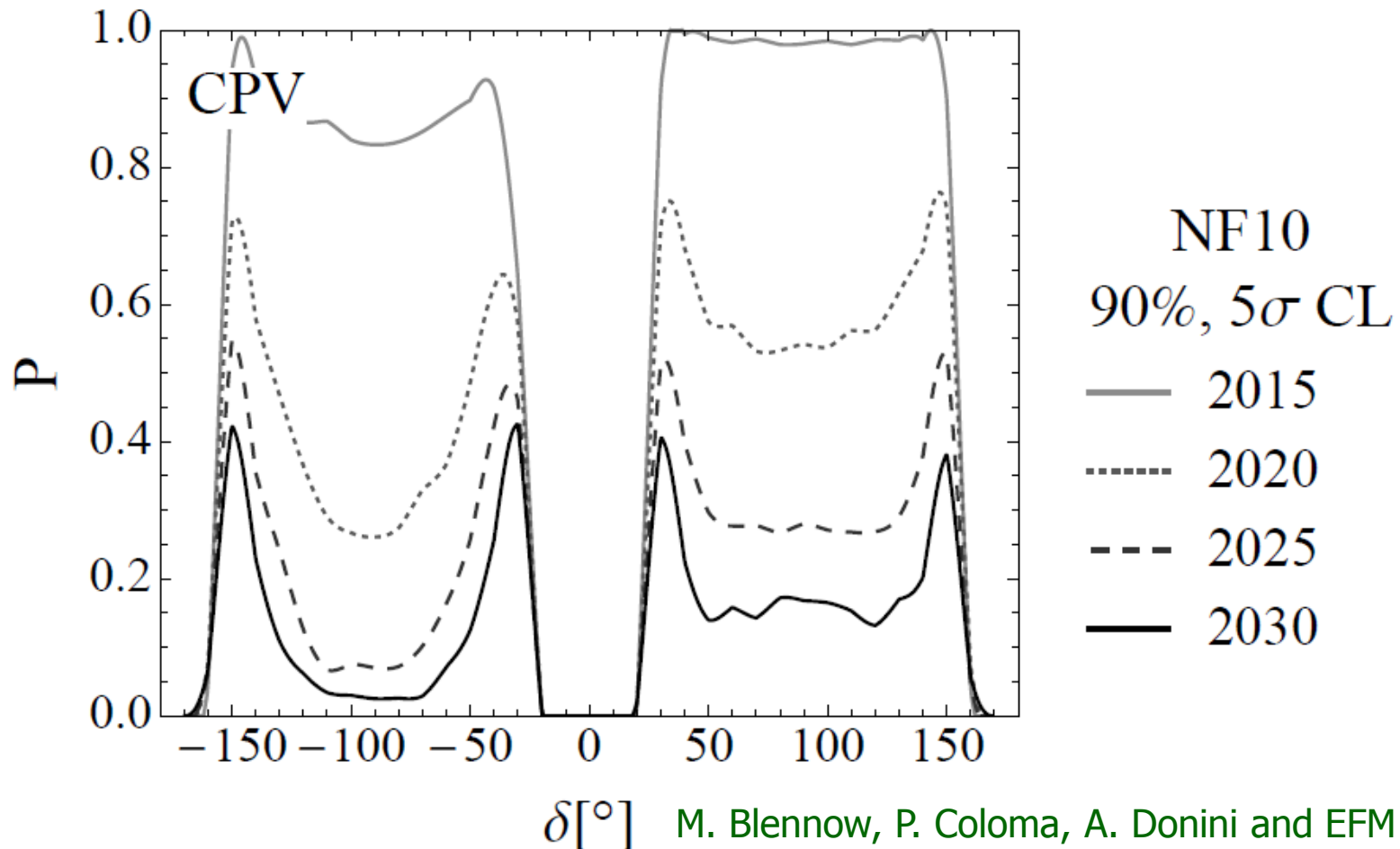
CPV  
2020: 90%,  $5\sigma$  CL



Joint probability  
of not having a  
90% CL hint at  
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 $5\sigma$  discovery at  
new facility



# Probabilities for CPV discovery



Joint probability of **not** having a **90% CL** hint at **T2K+NO $\nu$ A** and **5  $\sigma$**  discovery at new facility. Less and less likely when increasing **T2K+NO $\nu$ A** running time if no hint.

# Conditional probability

---

The results from **T2K+NO<sub>v</sub>A** will constrain our prior knowledge of  $\delta$  for the next facilities

Negative results will make CPV values of  $\delta$  less likely

$$P(\delta | T2K + NO_{\nu A})$$

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$$P(\text{disc} | T2K + NO\nu A) = \int P(\text{disc} | T2K + NO\nu A, \delta) P(\delta | T2K + NO\nu A) d\delta$$

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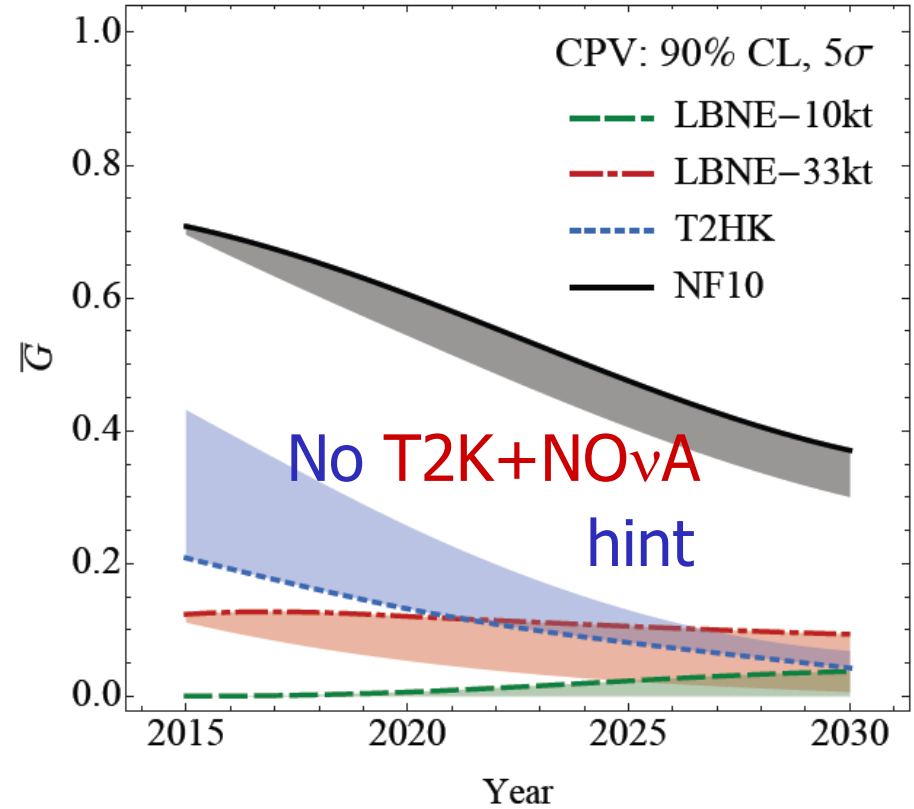
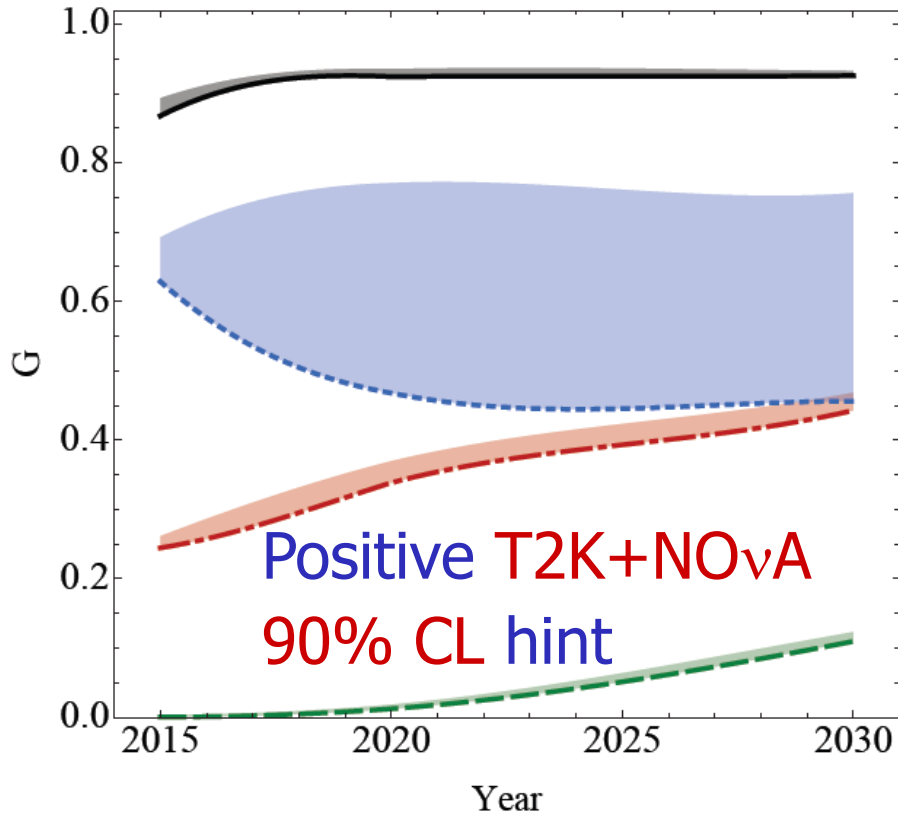
$$P(\text{disc} | T2K + NO\nu A) = \int P(\text{disc} | T2K + NO\nu A, \delta) P(\delta | T2K + NO\nu A) d\delta$$

Can be easily computed

from the joint prob:

$$P(\text{disc} | T2K + NO\nu A) = \frac{P(\text{disc}, T2K + NO\nu A)}{P(T2K + NO\nu A)}$$

# Conditional probability



# Precision

