An up-to-date view of lepton flavour observables

Michele Frigerio Laboratoire Charles Coulomb, CNRS & UM2, Montpellier

MF & Albert Villanova del Moral, JHEP 1307 (2013) 146 MF, Thomas Hambye & Eduard Massó, PRX 1, 021026 (2011)

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Outline

- Lepton physics & the electroweak scale
- Lepton flavour observables: present & future data
- Lepton flavour symmetries: where do we stand
- Minimal flavour structures: a conspiracy for nonmaximal 2-3 mixing
- A connection between neutrinos and very light dark matter candidates

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$$\mathcal{L}_{SM} = \mathcal{L}_{gauge} + \mathcal{L}_{EWSB} + \mathcal{L}_{flavour}$$

$$4 + 2 + 13 \text{ parameters}$$

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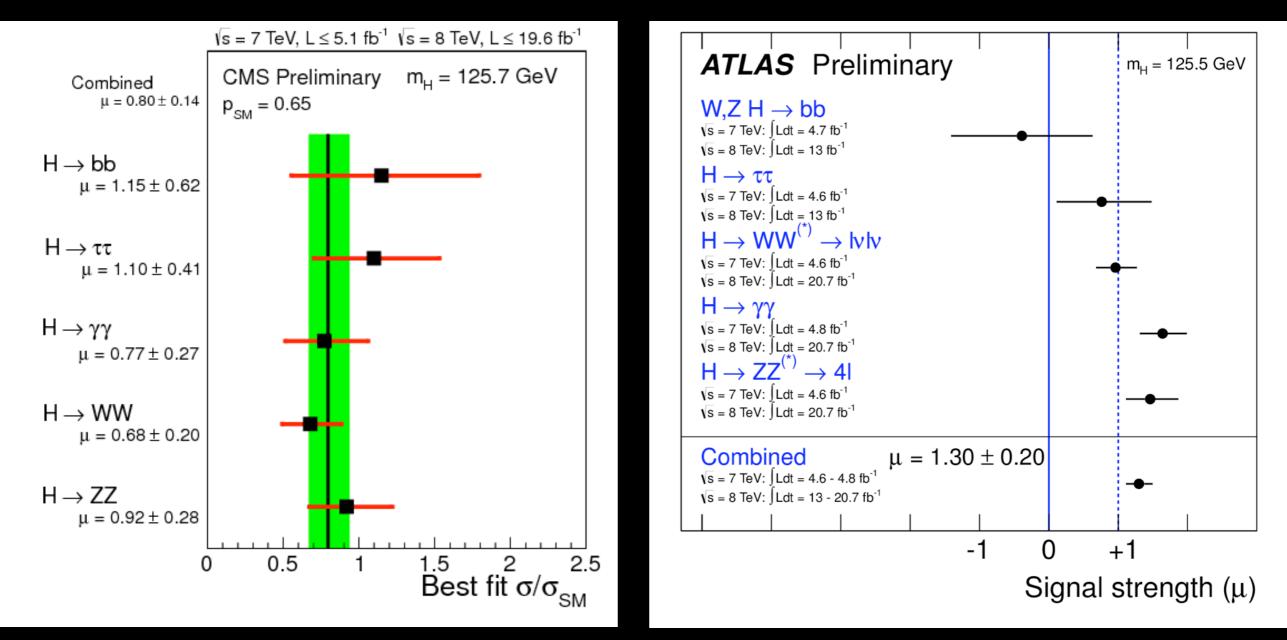
New physics below 100 GeV should be very weakly coupled to the SM: typically gauge singlet states ...

Where should we search?

Definitely, the most motivated new physics signals are expected in the Electroweak Symmetry Breaking Sector... alas, no luck so far

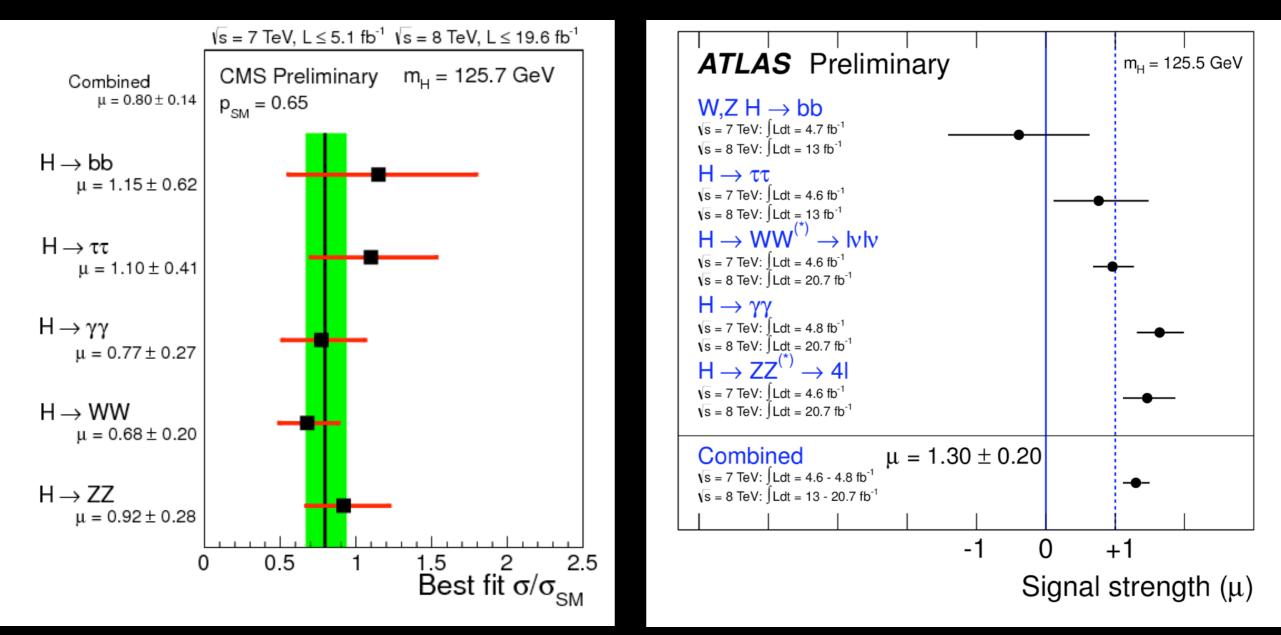
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Still room for natural EWSB, especially one should watch for the top sector observables

The importance of being massive

The discovery of neutrino oscillations amounts to

- a new energy scale, $m_v \sim 0.1 \text{ eV}$, probably associated to another one, $\Lambda = v^2/m_v \sim 10^{14} \text{GeV}$
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$$\frac{1}{\Lambda}\mathcal{L}_{D=5} = \frac{c_{ij}}{2\Lambda}l_{Li}l_{Lj}\phi\phi + h.c.$$

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$$(m_{\nu})_{ij} = c_{ij} \frac{v^2}{\Lambda}$$

The scale of flavour symmetry breaking remains unknown, and possibly out of reach

Charged lepton flavour violation

- Charged lepton flavour violation effects from $I_L \Phi \Phi$ are extremely suppressed, by $(m_v/m_{VV})^4$
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 $R(\mu^{-}\text{Ti} \to e^{-}\text{Ti}) < 4.3 \times 10^{-12} (90\%\text{C.L.})$

SINDRUM II, PLB 317 (1993) 631 improvement by a factor 10⁶ expected with COMET

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- Cosmology may give indications for extra light degrees of freedom. Unfortunately there is no compelling evidence at present. E.g. Planck data require $N_{eff} = 3.3 \pm 0.5$ (95% C.L.)

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Lepton flavour parameters

$$\mathcal{L} \supset \frac{g}{\sqrt{2}} \overline{e_{L\alpha}} \gamma^{\mu} W^{+}_{\mu} \nu_{L\alpha} - m_{\alpha} \overline{e_{L\alpha}} e_{R\alpha} - \frac{1}{2} \nu_{L\alpha} (m_{\nu})_{\alpha\beta} \nu_{L\beta} + h.c.$$

3 charged lepton masses m_e , m_μ , m_τ + Majorana mass matrix for V_e , V_μ , V_τ :

$$m_{\nu} = \begin{pmatrix} m_{ee} & m_{e\mu} & m_{e\tau} \\ m_{e\mu} & m_{\mu\mu} & m_{\mu\tau} \\ m_{e\tau} & m_{\mu\tau} & m_{\tau\tau} \end{pmatrix}$$

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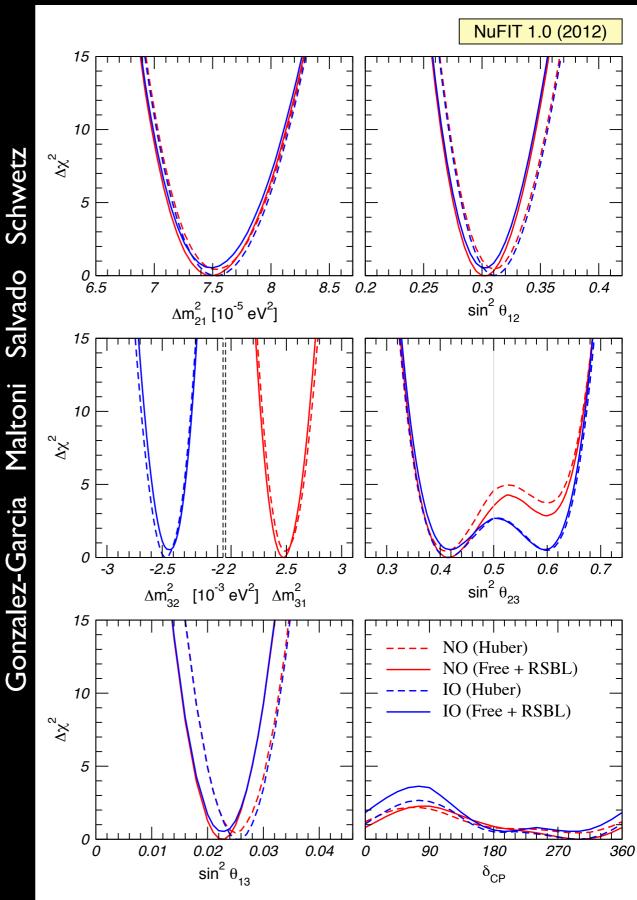
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$$m_{\nu} = U^* \operatorname{diag}(m_1 e^{-2i\rho}, m_2, m_3 e^{-2i\sigma})U^{\dagger}$$

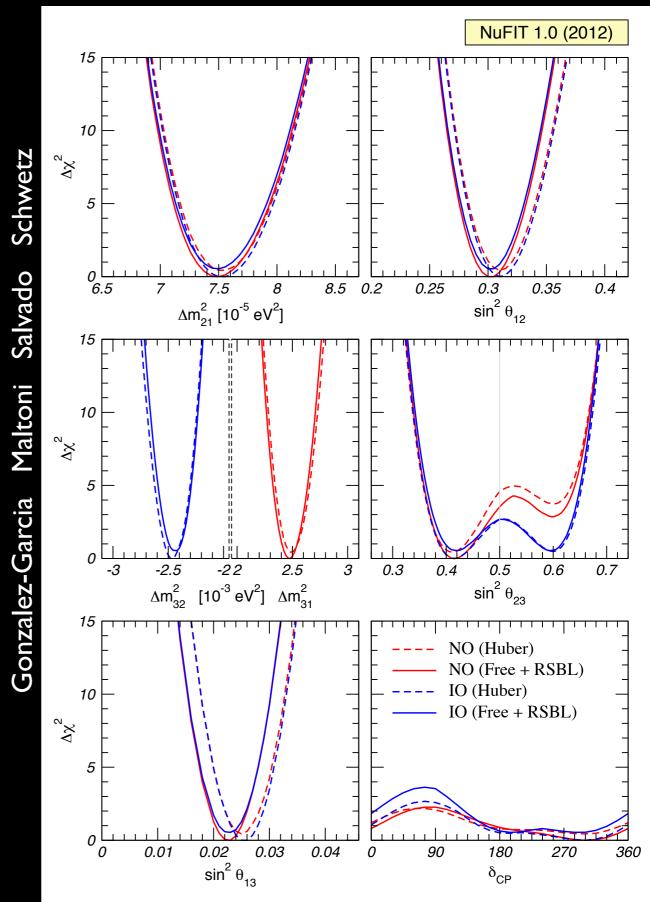
 $U = R(\theta_{23})R(\theta_{13},\delta)R(\theta_{12})$

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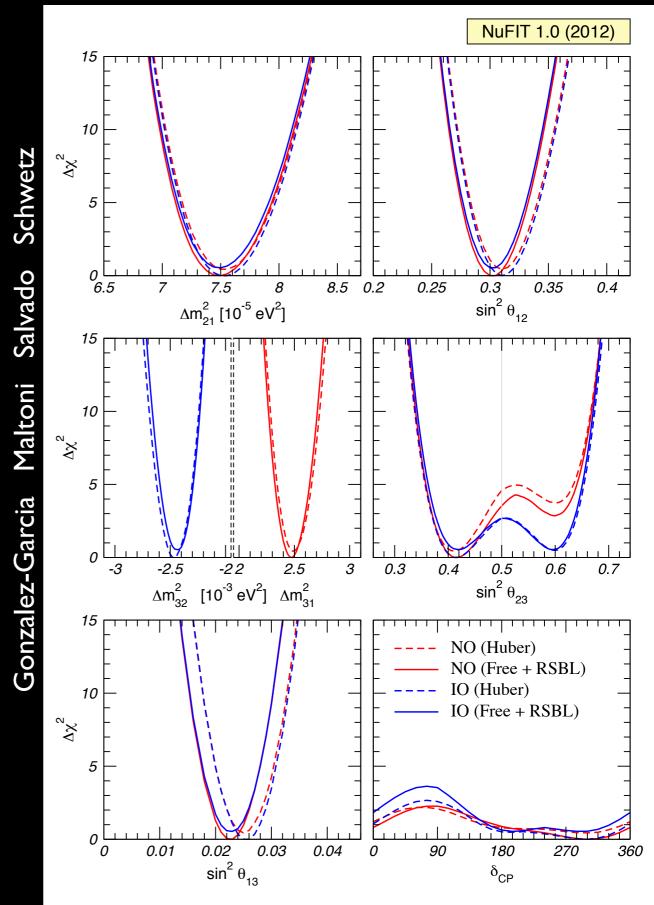


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The 2012 revolution: θ_{13} measured (reactor v's) almost as precisely as θ_{12} (solar v's).

The mixing angle θ_{23} (atmospheric \vee 's) is not precisely determined yet. There is a 2σ preference for a non-maximal value (accelerator \vee 's).



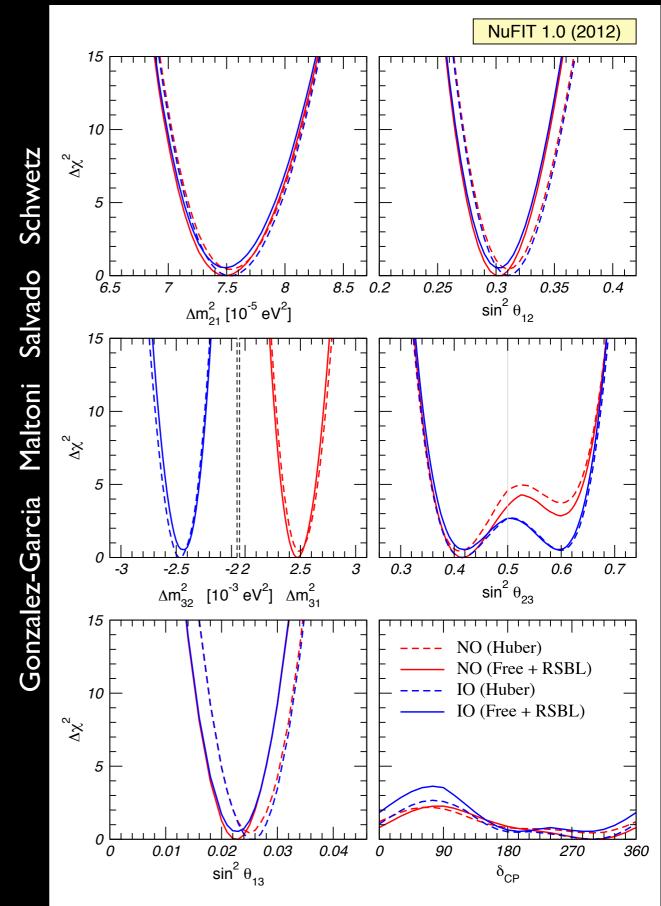
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Lepton CP-violation is behind the corner ? Some values of δ already disfavoured at 1σ



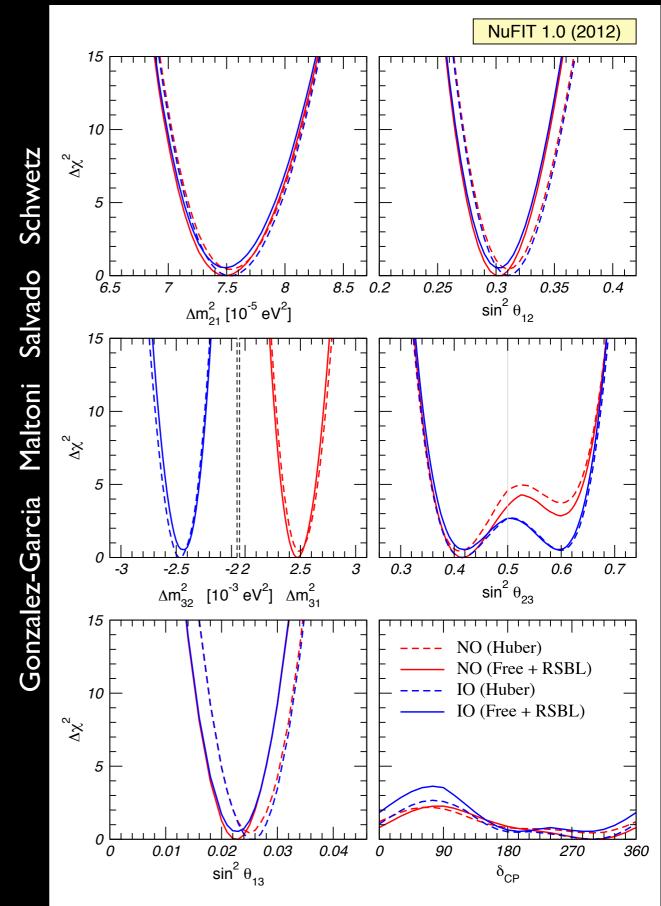
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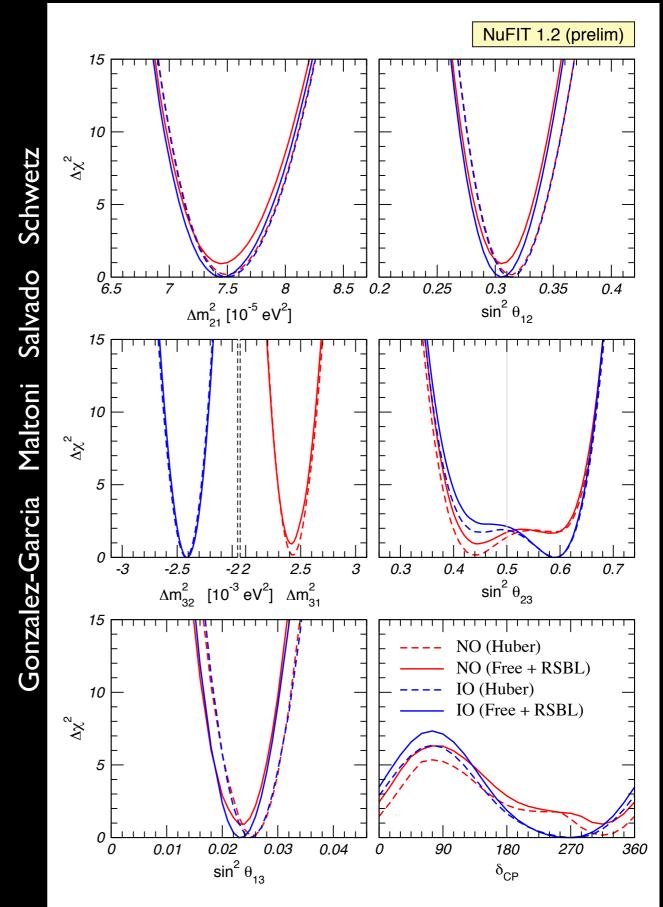
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- Only one realistic observable is sensitive to the two Majoranatype CP-violating phases: the neutrinoless 2 β -decay effective mass, 0 < m_{ee} < 0.38 eV (90% C.L. by EXO-200, KamLAND-Zen pushed down to 0.25 eV; similar bound from a different isotope by GERDA)

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The well-known speaker replied: "It is just you who did not learn anything!"

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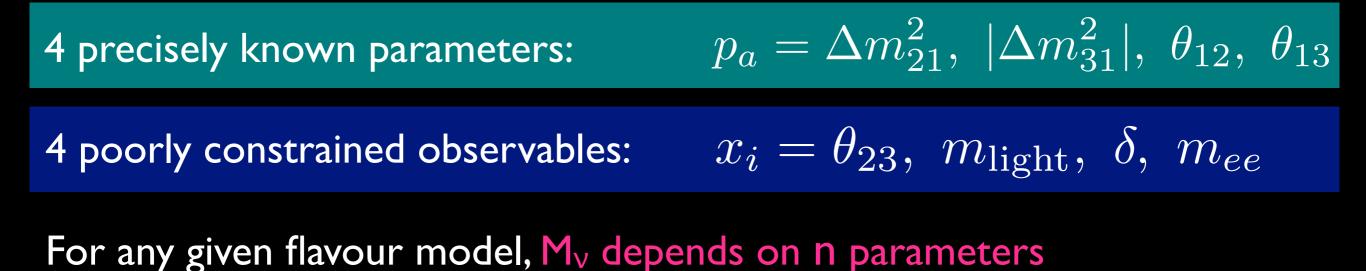
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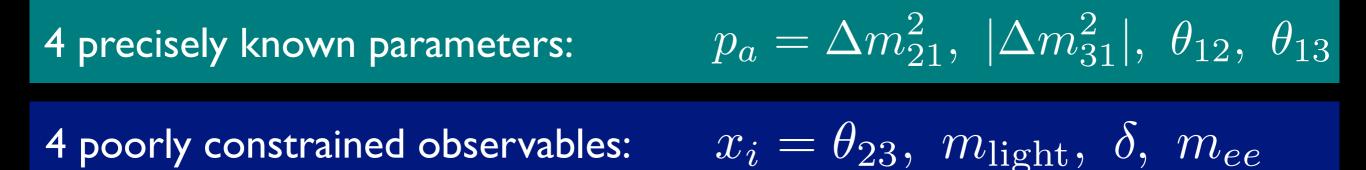
Frigerio & Villanova del Moral, 2013

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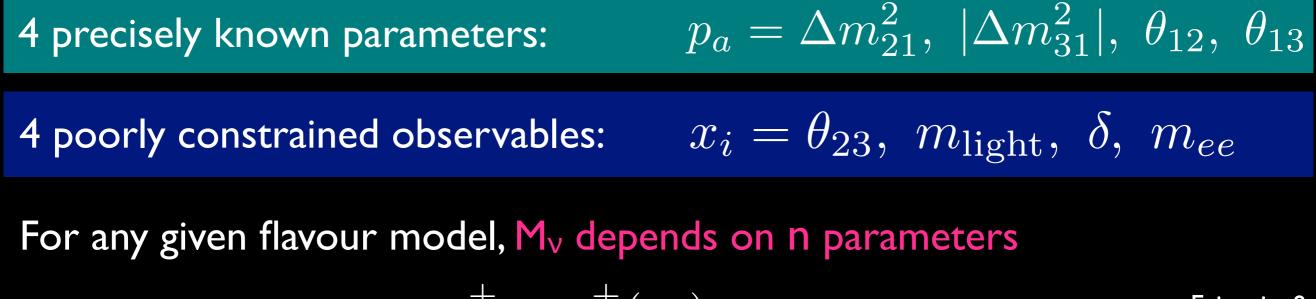


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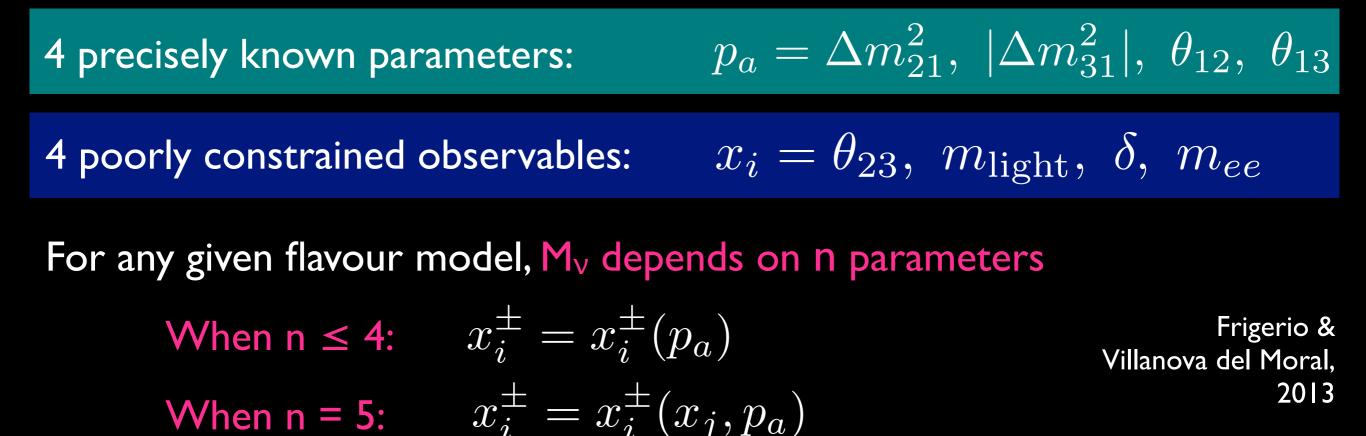
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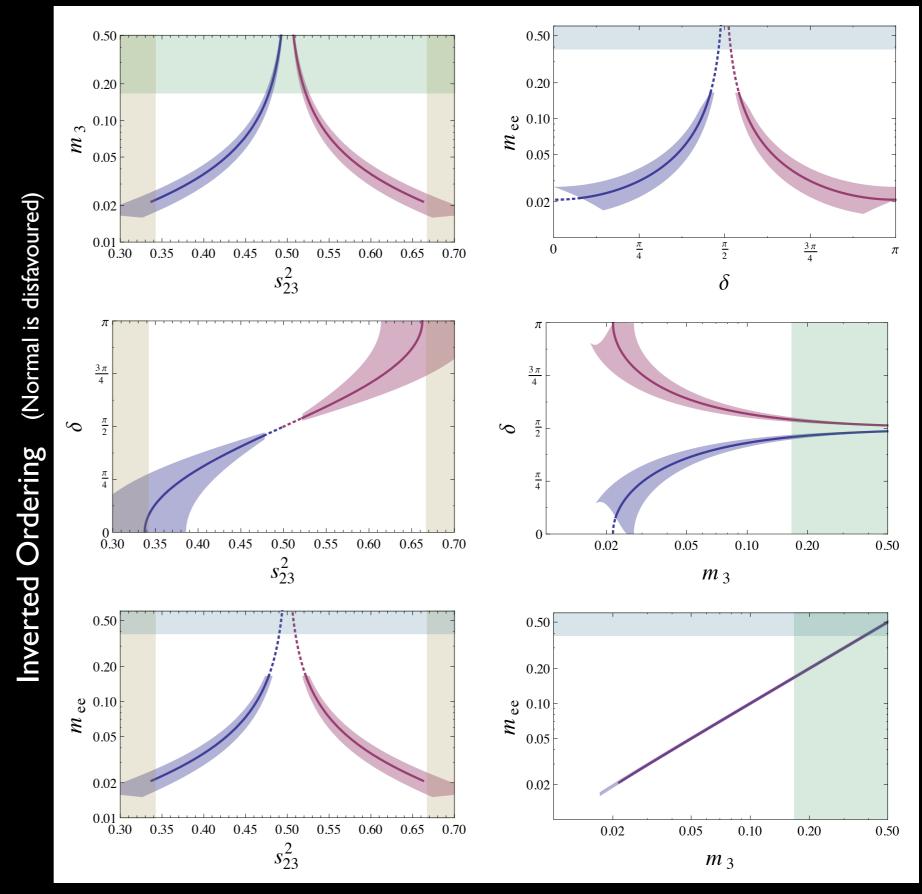
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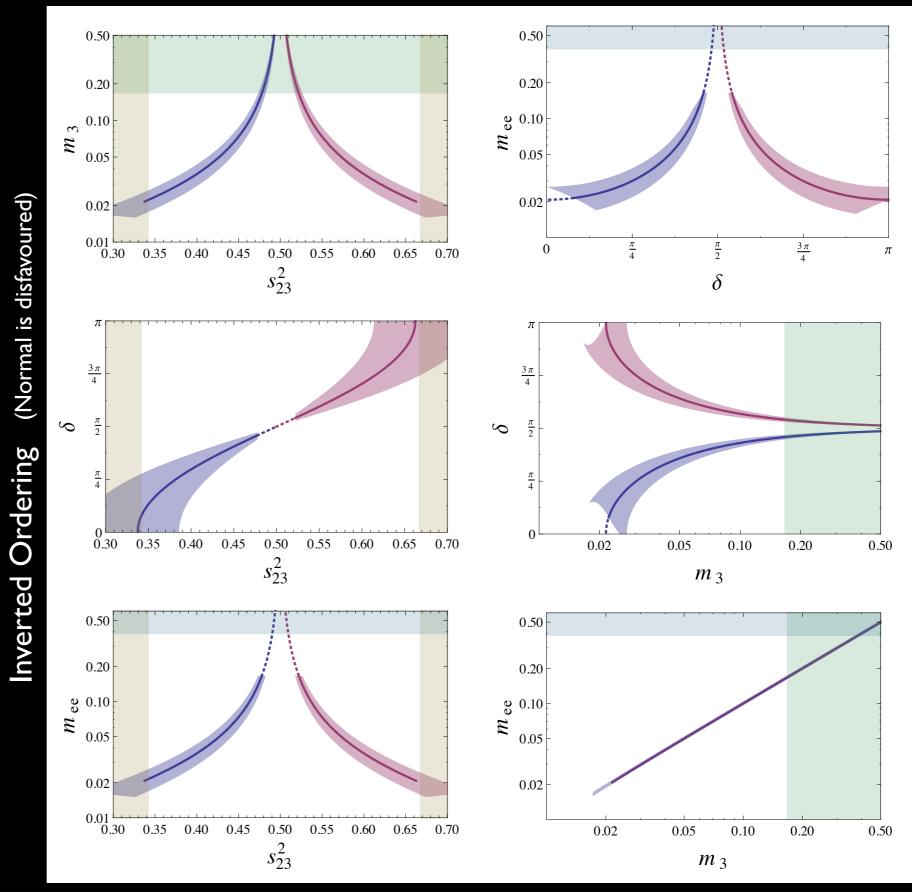
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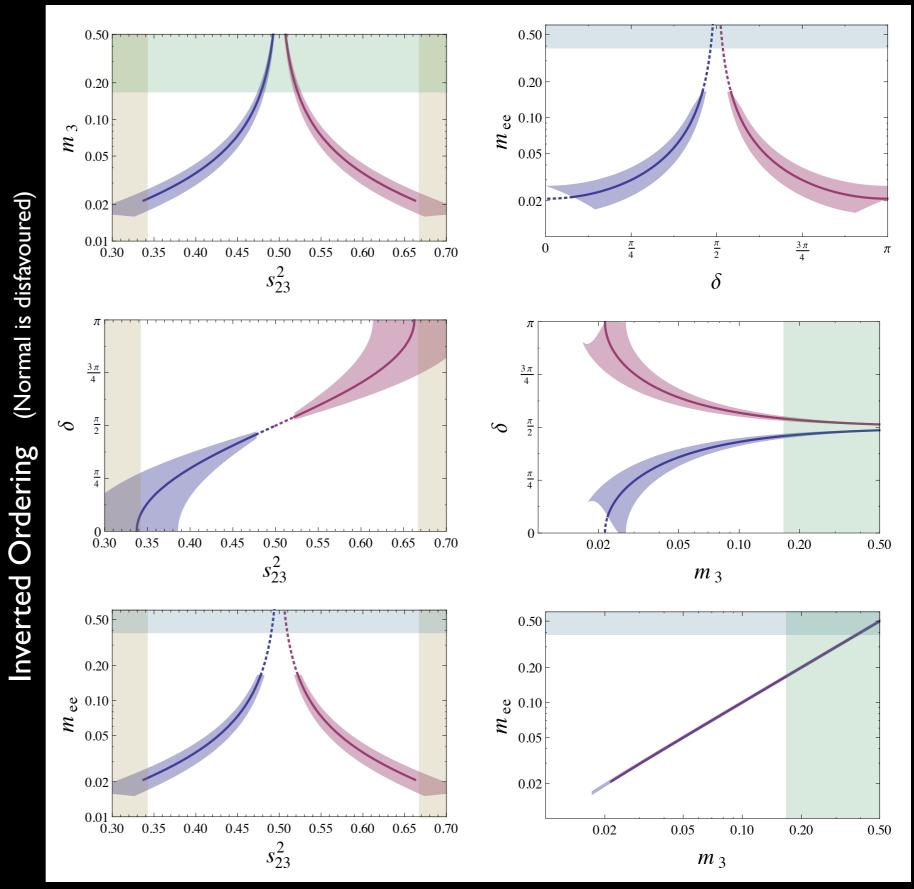
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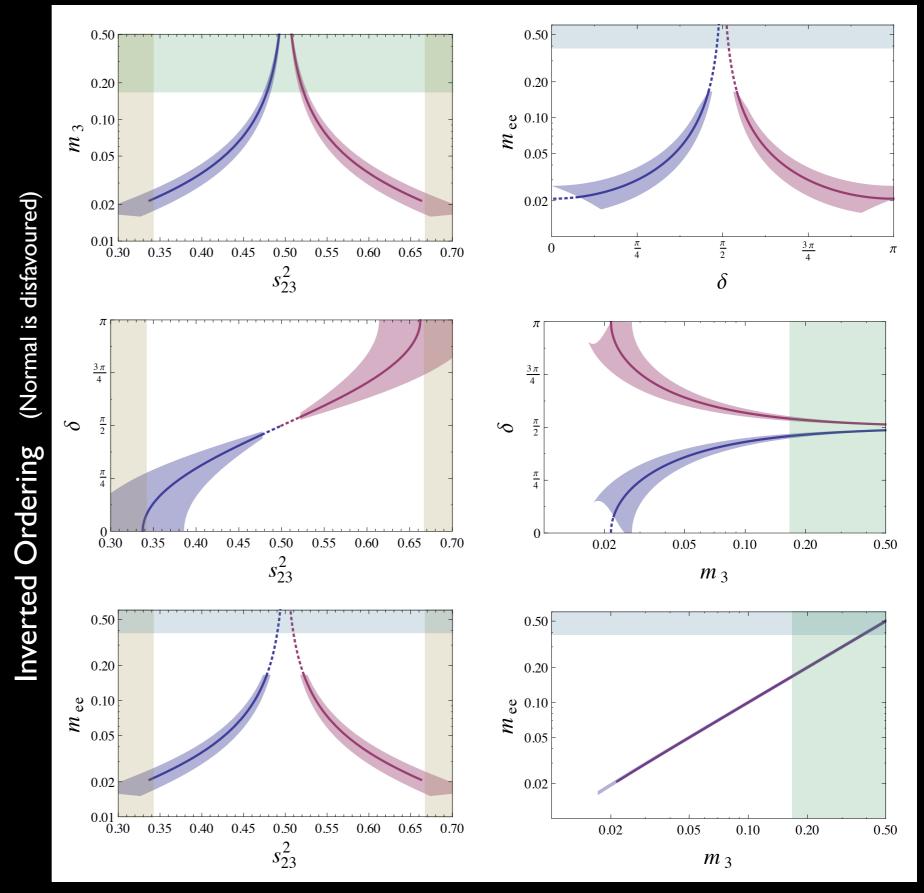


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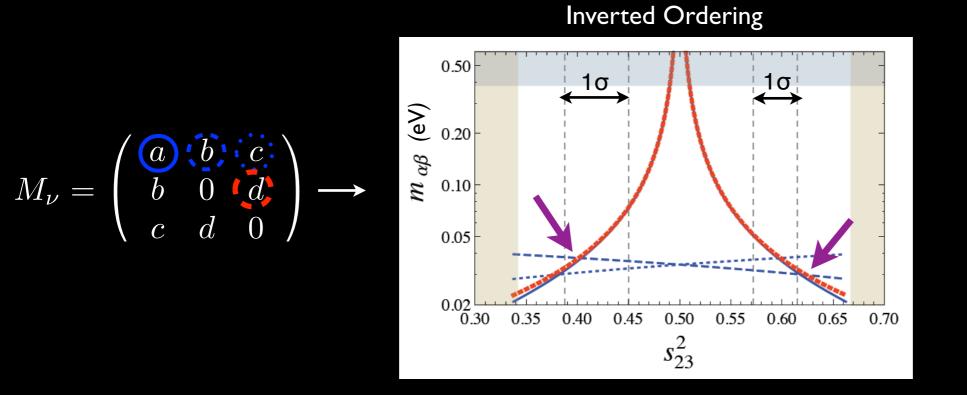
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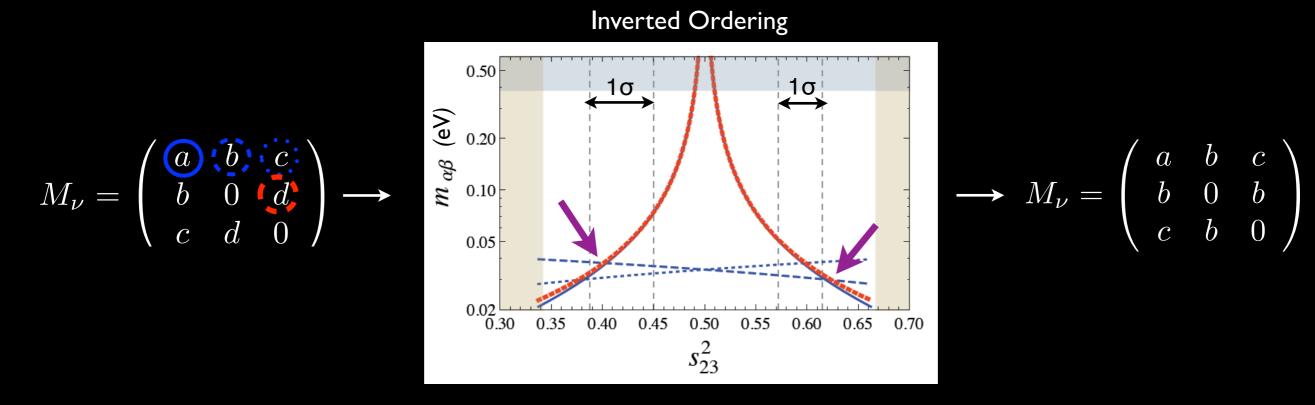
<u>Shaded bands and dashed</u> <u>lines:</u> excluded by bounds on the output parameters

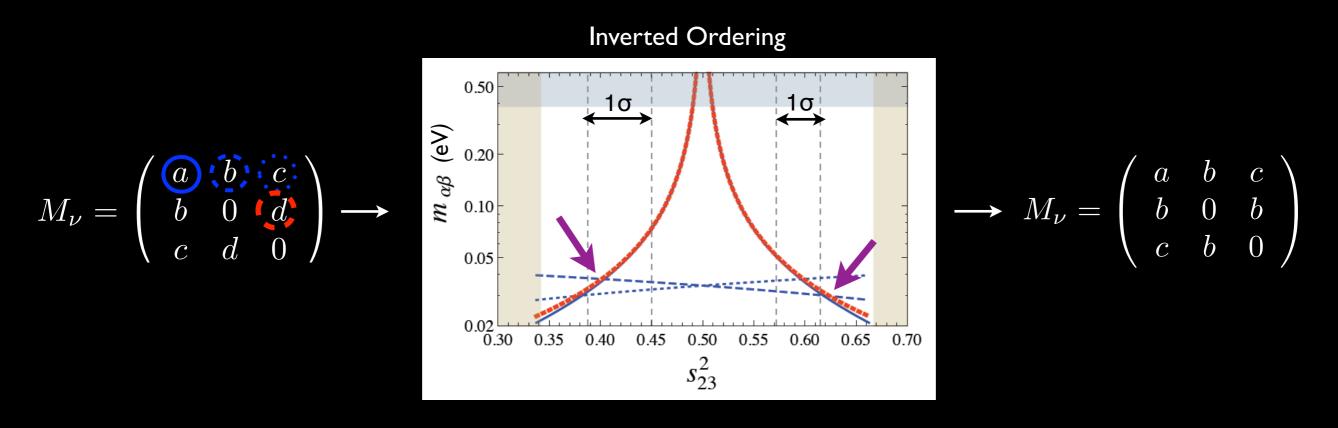


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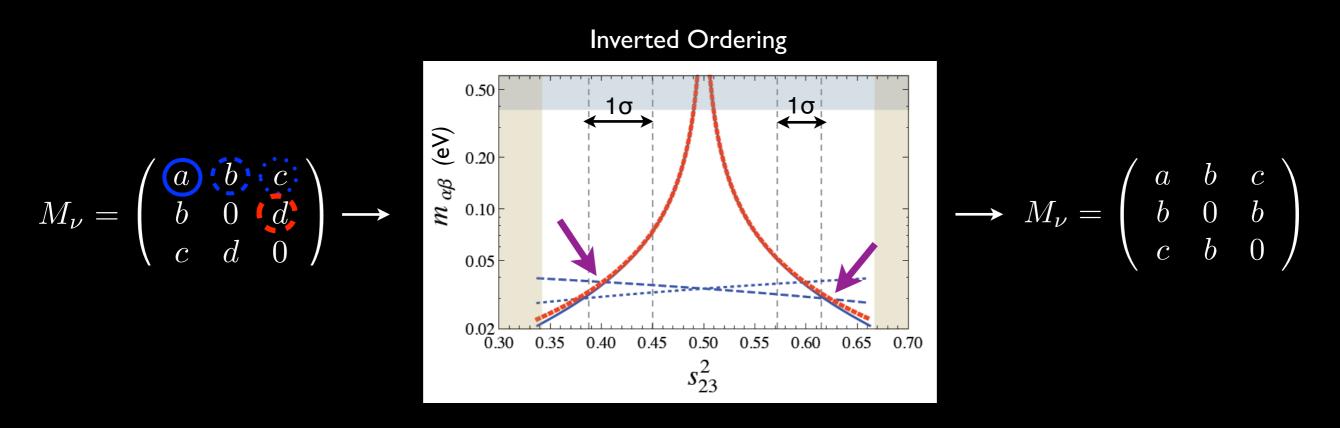
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$$\begin{cases} \sin^2 \theta_{23} = 0.40^{+0.02}_{-0.01} \\ \cos \delta = 0.59^{+0.12}_{-0.14} \\ m_{\text{light}} = m_3 = 0.037^{+0.001}_{-0.002} \text{ eV} \\ m_{ee} = 0.036^{+0.002}_{-0.001} \text{ eV} \end{cases}$$

 $\begin{cases} \sin^2 \theta_{23} = 0.62^{+0.03}_{-0.02} \\ \cos \delta = -0.75^{+0.15}_{-0.12} \\ m_{\text{light}} = m_3 = 0.0289^{+0.0002}_{-0.0001} \text{ eV} \\ m_{ee} = 0.0284^{+0.0000}_{-0.0001} \text{ eV} \end{cases}$

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Can one justify such a matrix structure by a (spontaneously broken) flavour symmetry ?

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- $M_{ee} \neq M_{\tau\tau} = 0$ implies that $2_L \ge 2_L$ couples to a second flavon doublet $2_{\Phi'}$ with $\langle \Phi' \rangle = a(1,0)$, and one needs $2_{\Phi} \neq 2_{\Phi'}$

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- Since L_{μ} transforms as a singlet 1_{L} and $M_{\mu\mu} = 0$, one needs $1_{L} \times 1_{L} \neq 1$

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Can one justify such a matrix structure by a (spontaneously broken) flavour symmetry ?

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All this can be realized with the order-12 group $Q_6 = D'_3$ that has representations $2_1, 2_2, 1, 1', 1'', 1'''$

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One finds $m_1 \ge 0.036$ eV and $m_{ee} \ge 0.012$ eV (the lower bounds corresponding to no CP violation)

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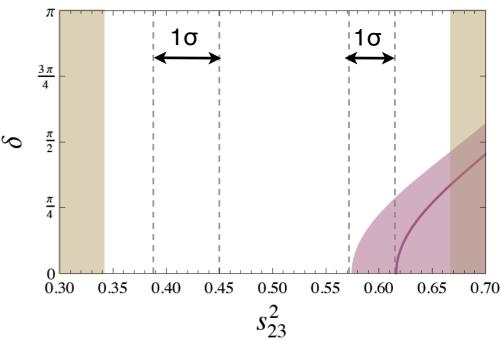
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Is a minimal model convincing ? let us try to find a pretty one

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- To enforce this result a few technicalities are needed.
 A different, economical implementation of the A₄ symmetry can lead to a better agreement with data

Off-diagonal V masses

As in the radiative model by Zee (PLB93,389,1980) and Wolfenstein (NPB175,93,1980)

$$M_{\nu}^{\text{off}} = \begin{pmatrix} 0 & a & b \\ a & 0 & c \\ b & c & 0 \end{pmatrix}$$

This is perfectly A₄-symmetric, if leptons (l_e , l_μ , l_τ) and flavons (ϕ_e , ϕ_μ , ϕ_τ) form A₄-triplets: y^{off} ($\phi_e l_\mu l_\tau + l_e \phi_\mu l_\tau + l_e l_\mu \phi_\tau$) is invariant

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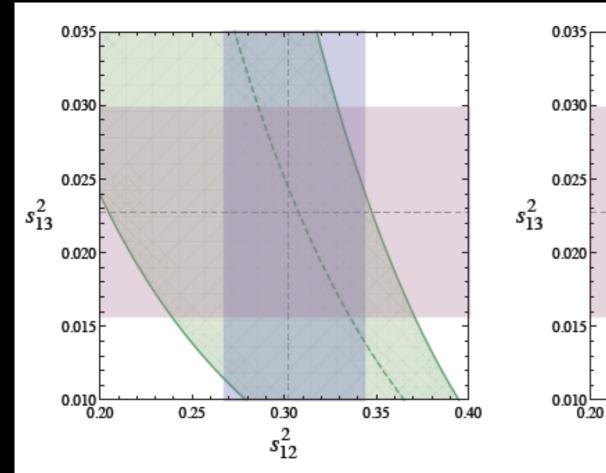


0.30

 s_{12}^2

0.35

0.40



30 range for θ_{12} and 30 range for θ_{13} superimpose perfectly with 10 range for θ_{23}

Off-diagonal + the identity

- Since a decade we know that M_{ν}^{off} alone cannot accommodate Δm^2_{ij}
- However the A₄-triplet of leptons form necessarily another A₄-invariant: $y^{univ}(I_eI_e + I_{\mu}I_{\mu} + I_{\tau}I_{\tau})$
- This does not affect the prediction for θ_{23} (and for δ)
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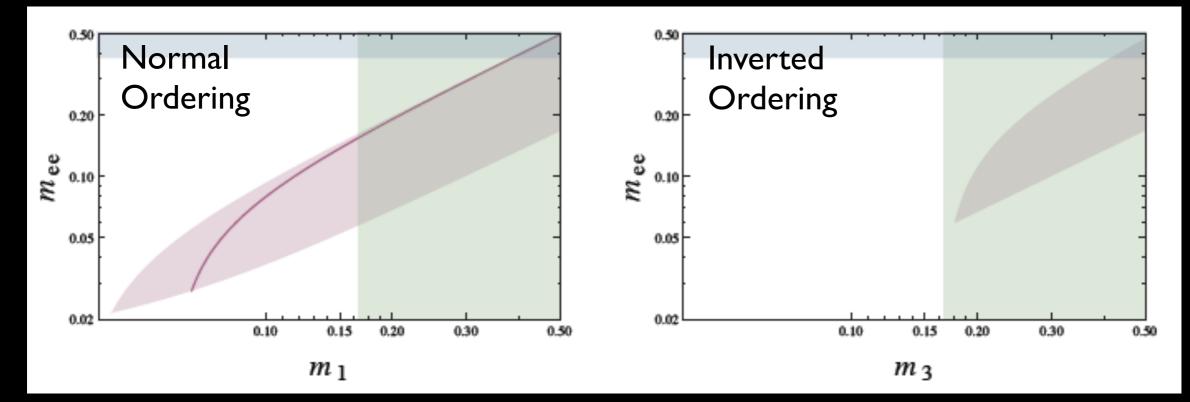
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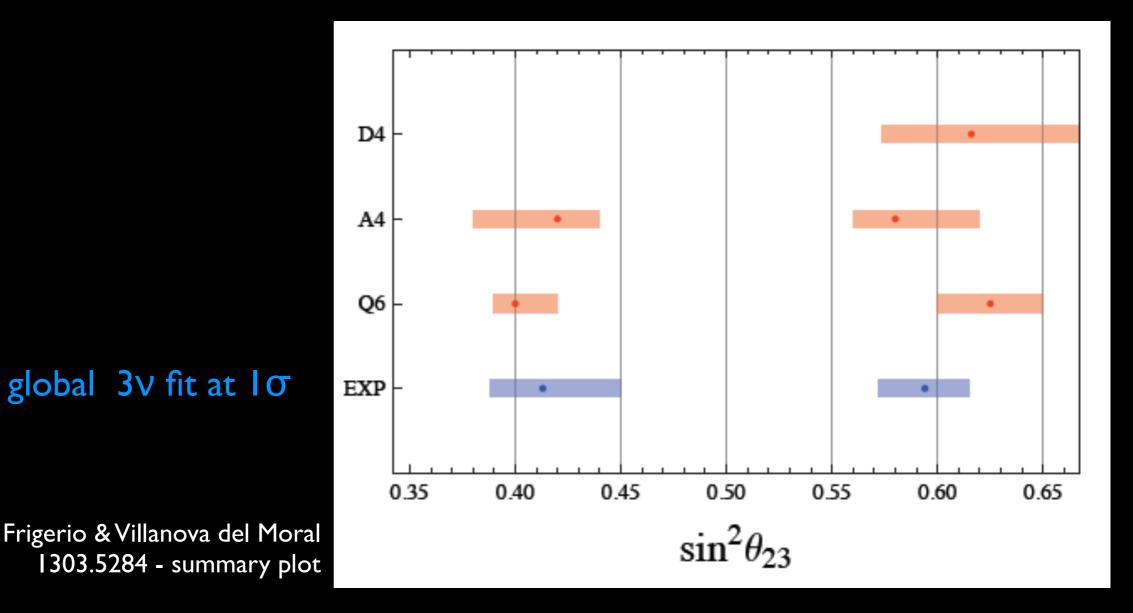


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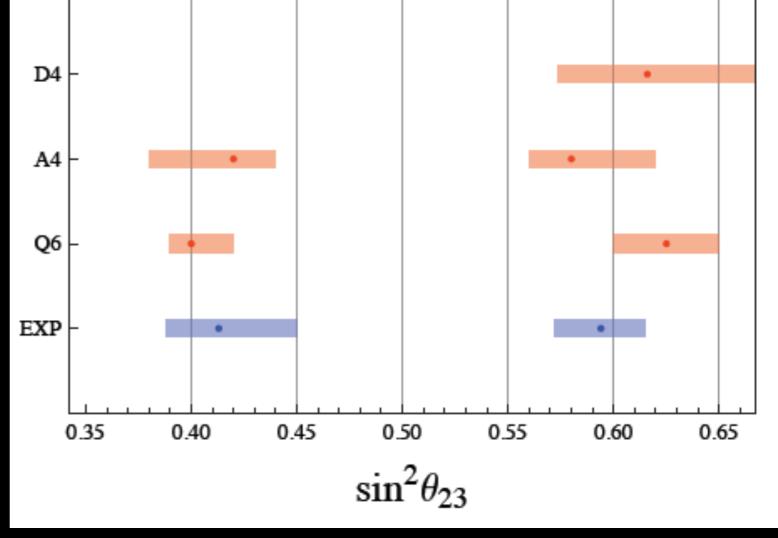
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top-down I+2 model

off-diagonal + identity model

bottom-up I+2 model

global 3v fit at 1σ



Frigerio & Villanova del Moral 1303.5284 - summary plot

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- What is the mechanism inducing the off-diagonal & the identity terms? Radiative, seesaw, both? At what energy scale(s)?





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- Minimal models can sharply predict future observables
- With the least possible assumptions, we found a preference for a deviation from maximal θ_{23} of the presently preferred size

Addendum

- Lepton physics & the electroweak scale
- Lepton flavour observables: present & future data
- Lepton flavour symmetries: where do we stand
- Minimal flavour structures: a conspiracy for nonmaximal 2-3 mixing
- A connection between neutrinos and very light dark matter candidates

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- approximate symmetry: the scale of spontaneous SB is much larger than the scale of explicit SB

Virtues of pNGBs as dark matter

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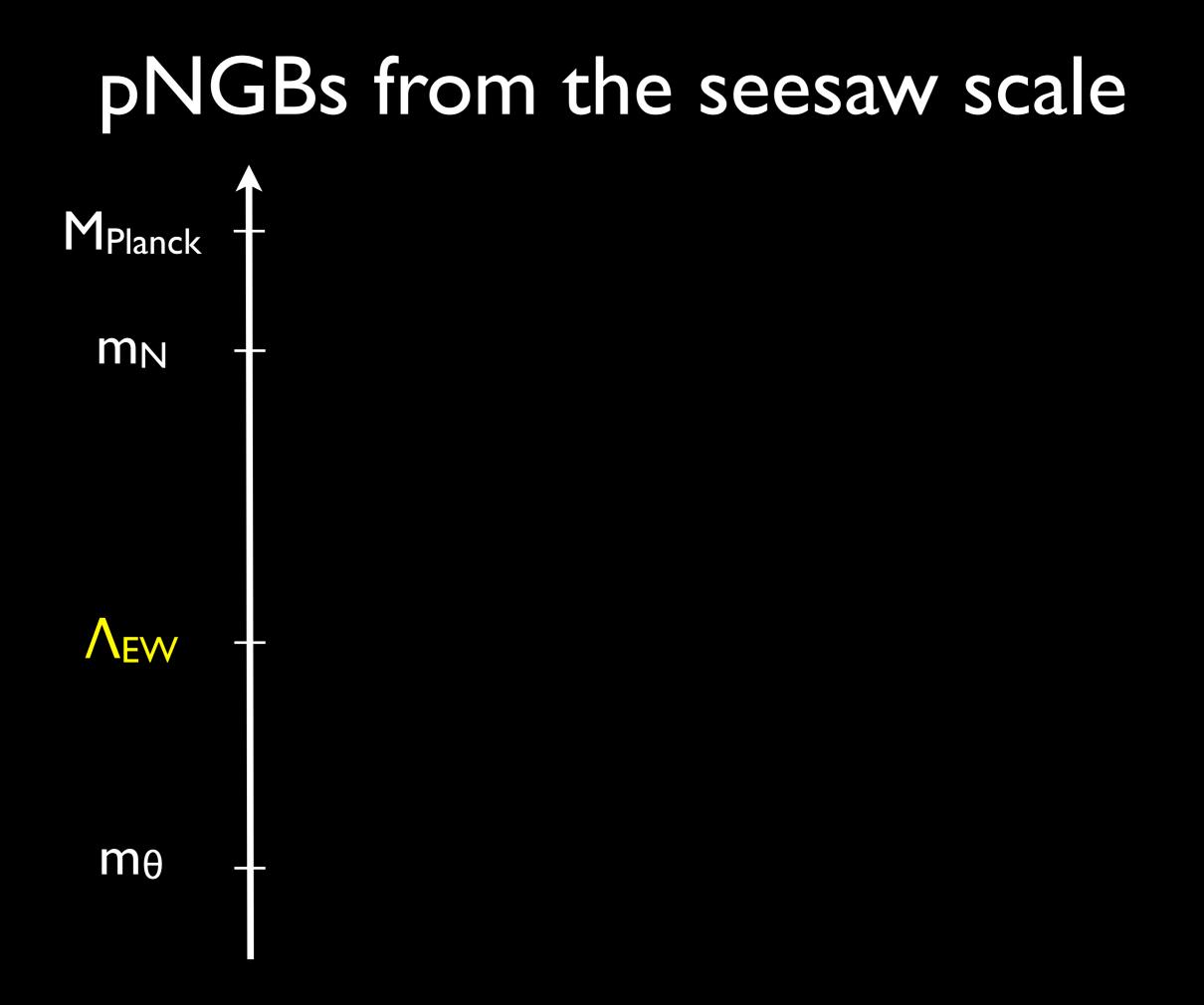
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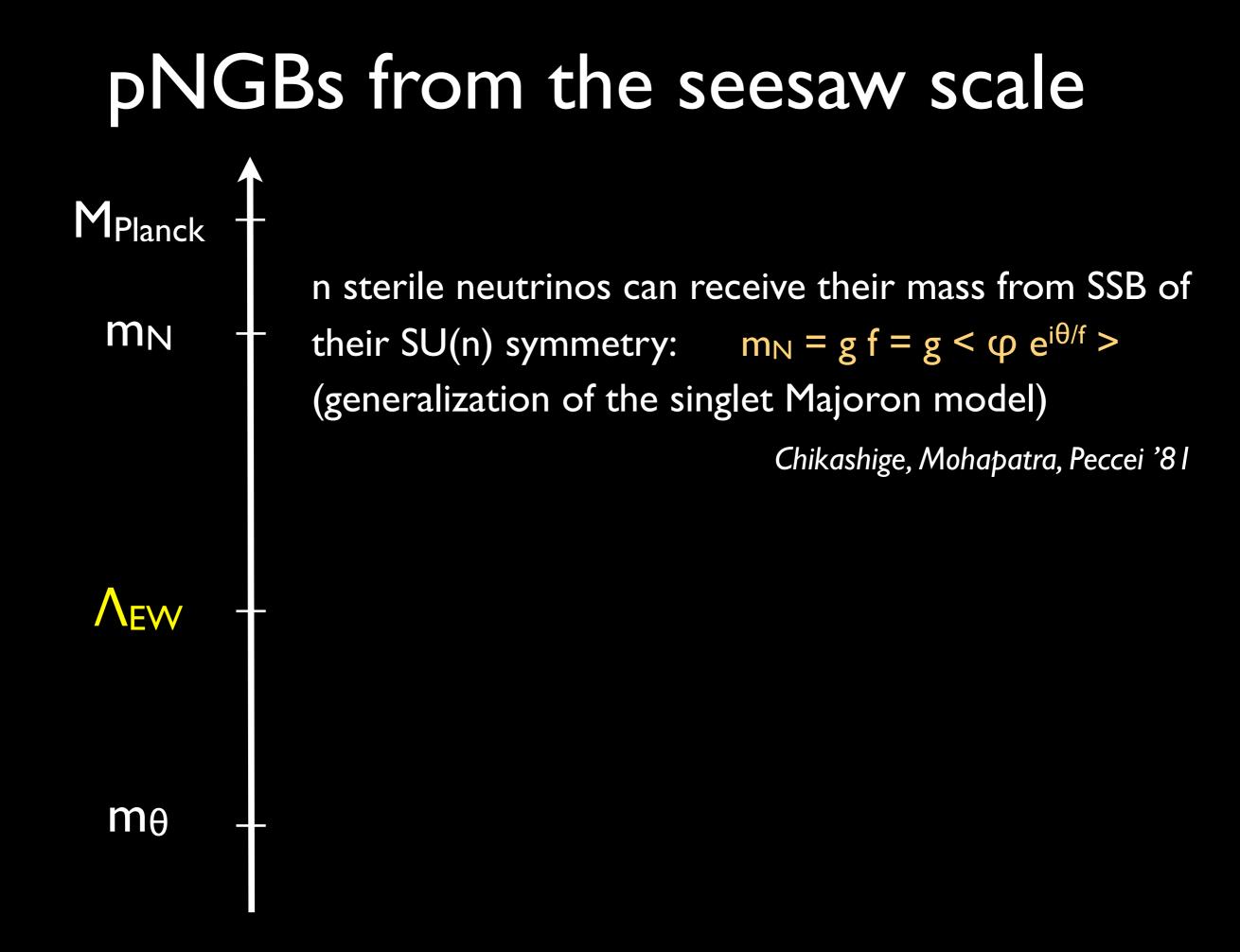
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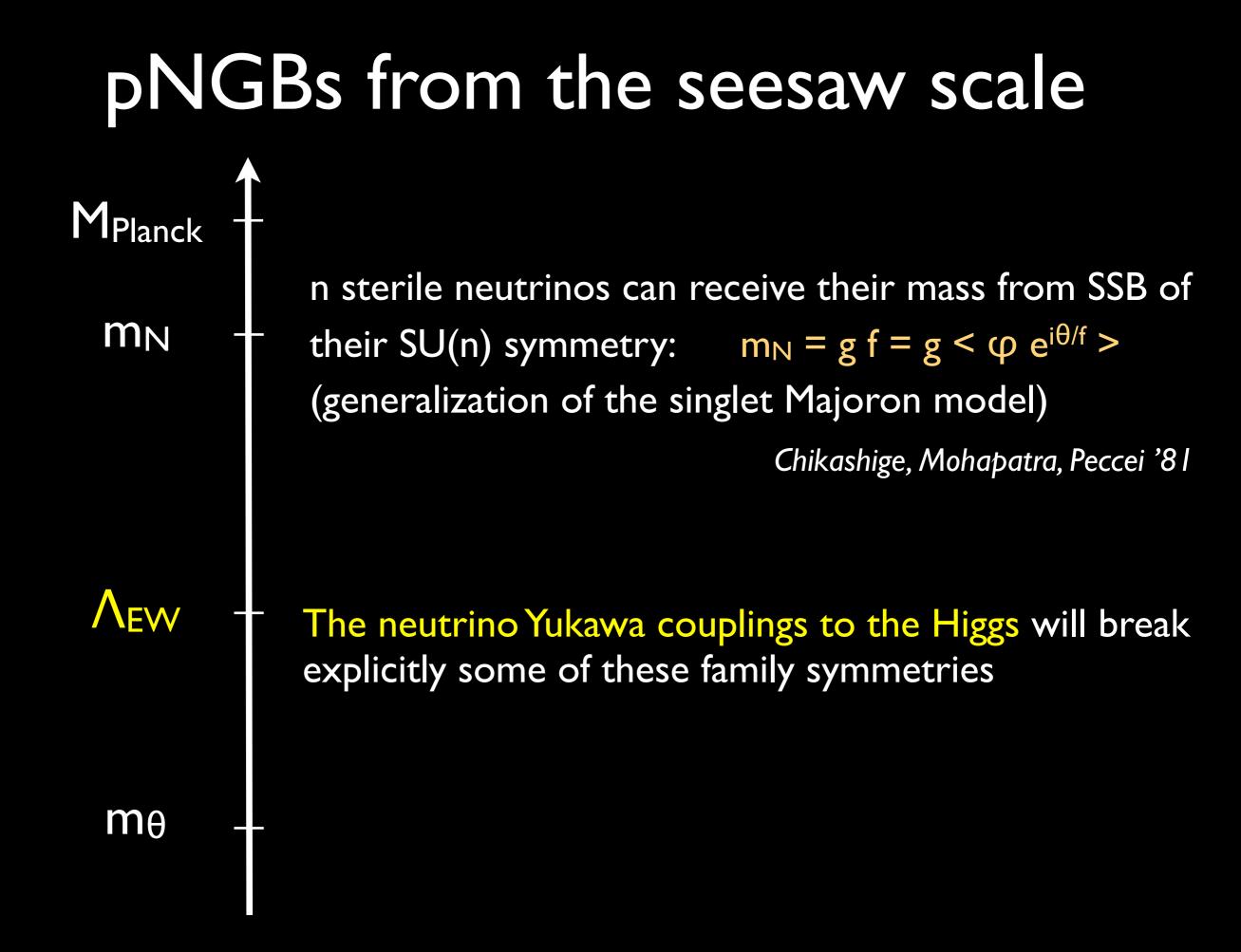
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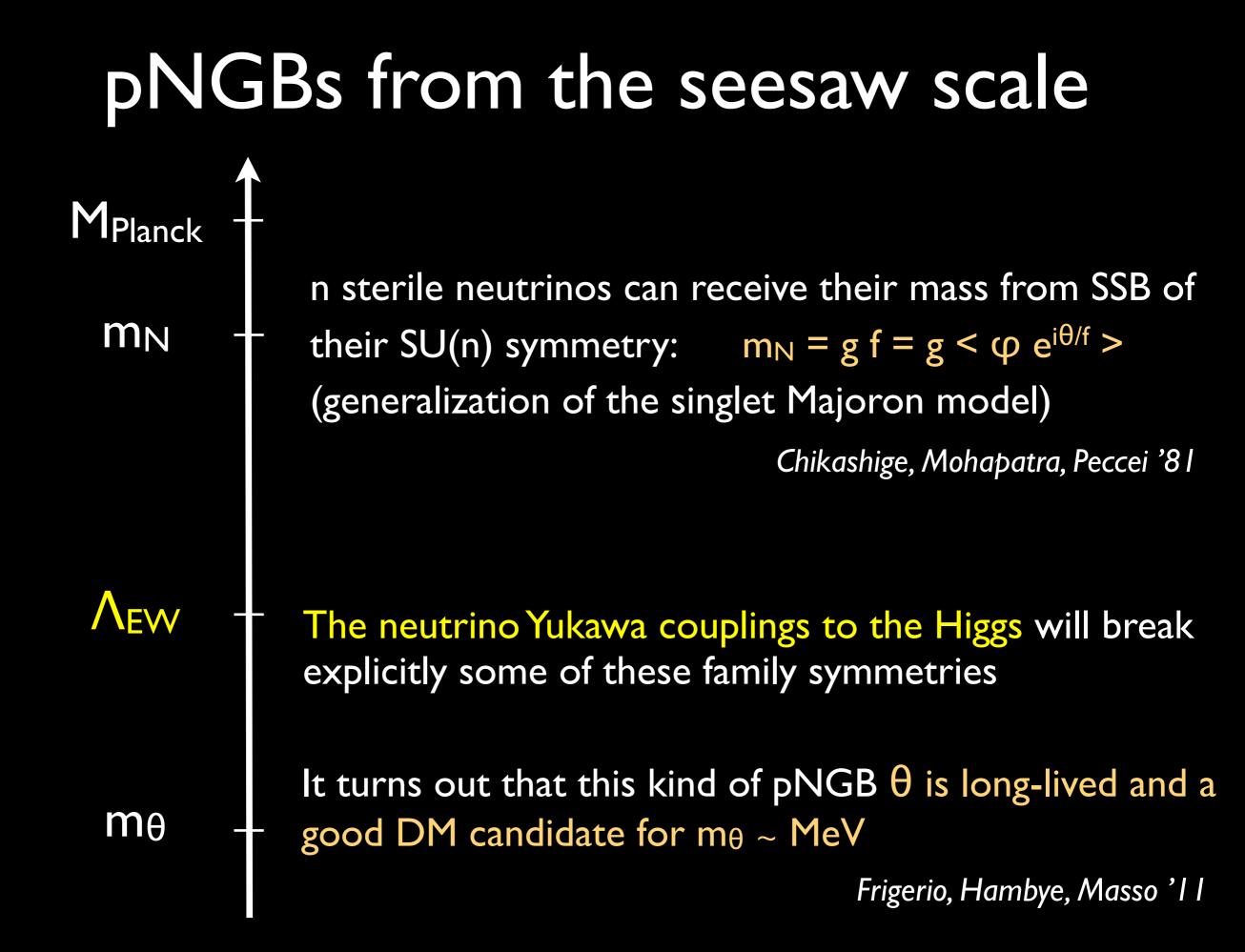
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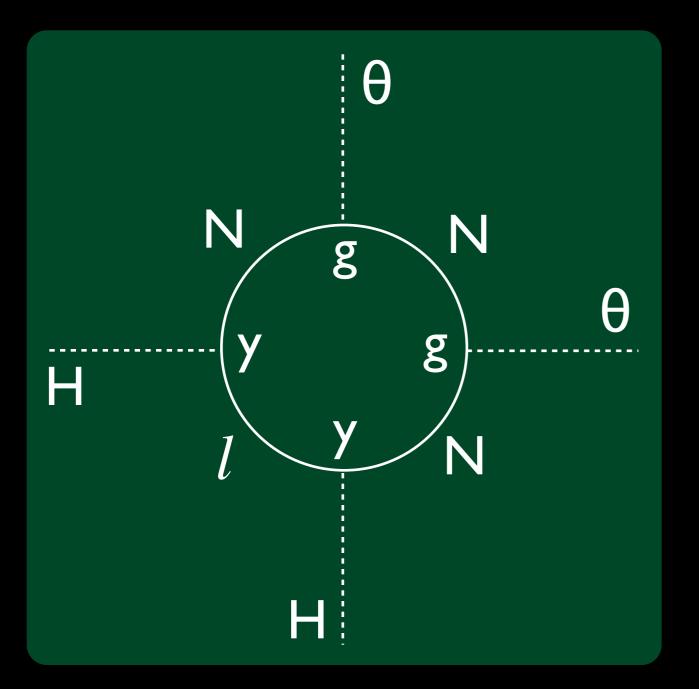
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- If the spontaneous SB scale f is very large, the pNGB is automatically long-lived: its lifetime grows with f². For DM one needs $\tau_{DM} > \tau_0 = 5 \cdot 10^{17} \text{s} [\tau(DM \rightarrow e^+e^-) > 10^{26} \text{s}]$

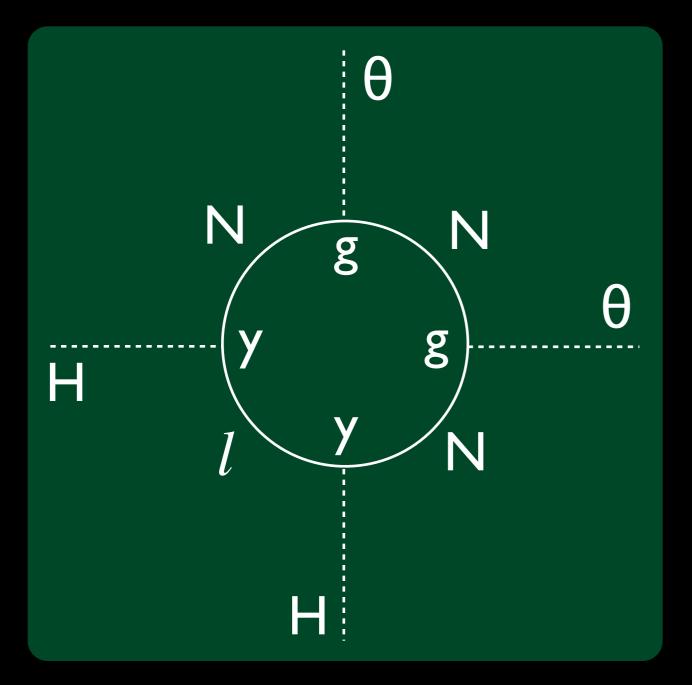




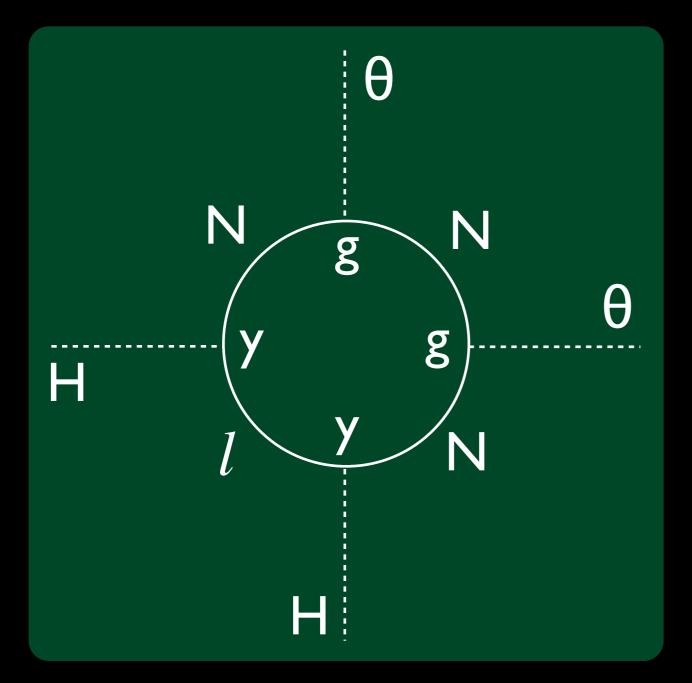






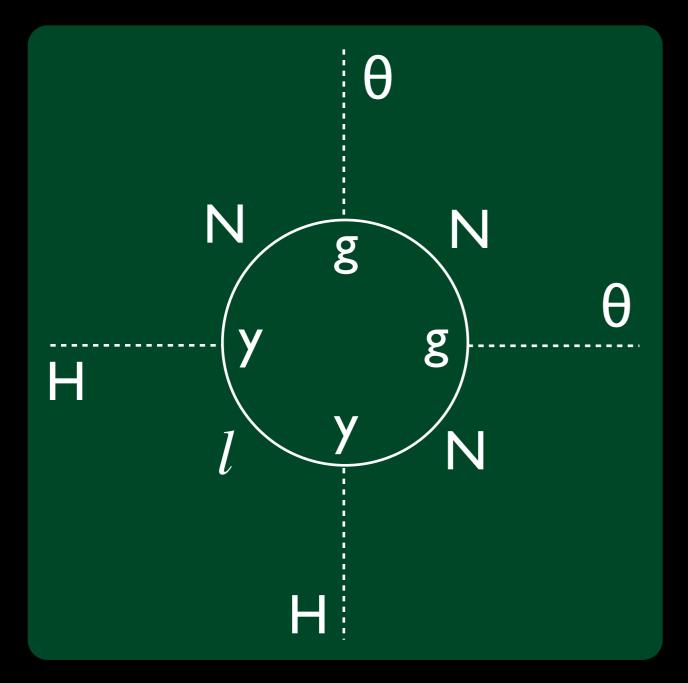


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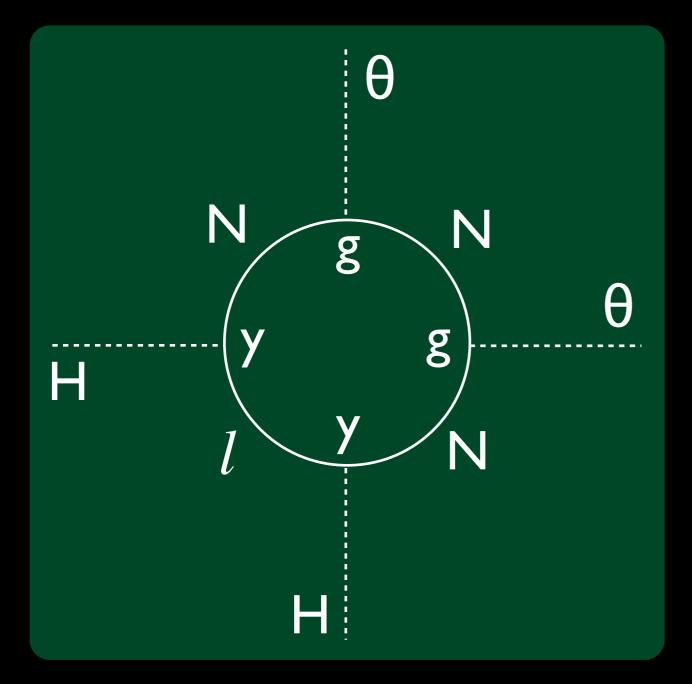


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**$$\theta$$
-Higgs coupling in a nutshell**
 $-\mathcal{L} \supset l_{\alpha}(y_{\alpha j}v)N_{j}\left(\frac{H}{v}\right) + \frac{1}{2}N_{i}(g_{ij}f)N_{j}\exp\left(i\frac{\theta}{f}\right)$



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Many details & subtleties ... Hill, Ross '88; Little Higgs models; Frigerio, Hambye, Masso '11



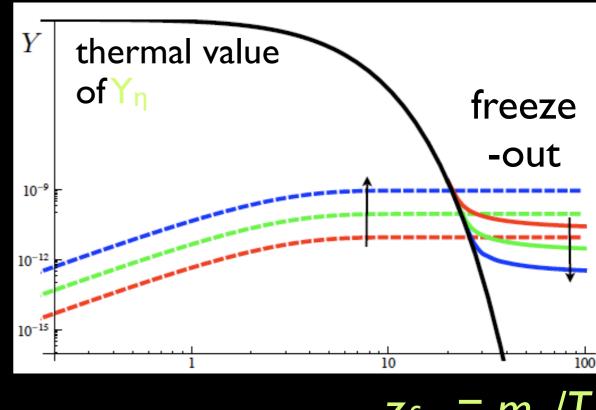
Freeze-out: **n** thermalizes and later decouples, at $T \leq m_{\eta}$. To obtain the correct Ω_{DM} one needs $m_{\eta} \approx 50$ GeV.

e.g. Farina, Pappadopulo, Strumia, 2010

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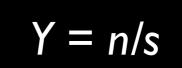


 $z_{f.o.} = m_{\eta}/7$

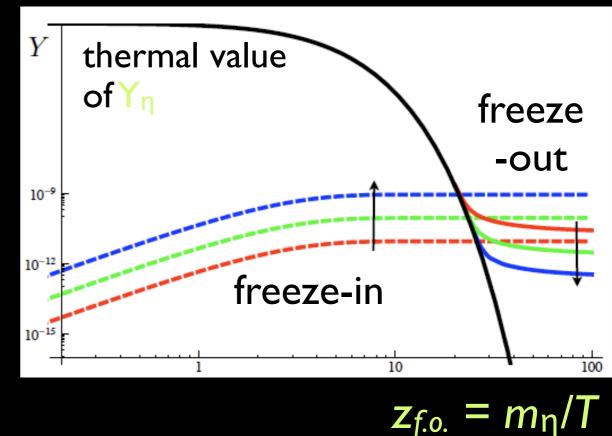
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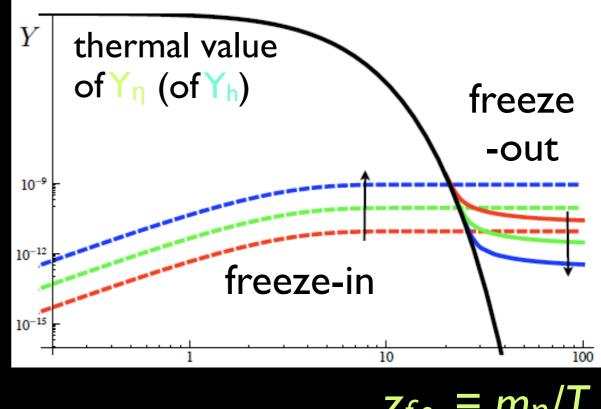
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Freeze-in: a less-than-thermal population of η 's is produced by the annihilation/decay of heavier particles, X = h, W, Z. The η number density reaches a plateau at T \approx m_X. We found that Ω_{DM} is reproduced for $m_{\eta} \approx 3$ MeV ($\lambda \approx 10^{-10}$).

Frigerio, Hambye, Masso 2011

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 $\frac{z_{f.o.}}{z_{f.i.}} = \frac{m_{\eta}}{T}$

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θ-couplings to SM fermions

Since θ has the coupling $g\theta NN$, and since N mixes with V, θ decays into light neutrinos at tree-level

$$\Gamma(\theta \to \nu\nu) = \frac{1}{16\pi} g_{\theta\nu\nu}^2 m_{\theta} \qquad \left(g_{\theta\nu\nu} \simeq 10^{-21} \left(\frac{\text{MeV}}{m_{\theta}}\right)^2 \left(\frac{g}{10^{-3}}\right)^3 \left(\frac{m_{\nu}}{\text{eV}}\right)^2\right)$$

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Since v couples to Z and W, at one-loop θ couples also to charged fermions, both leptons and quarks

Allowed regions for θ dark matter

