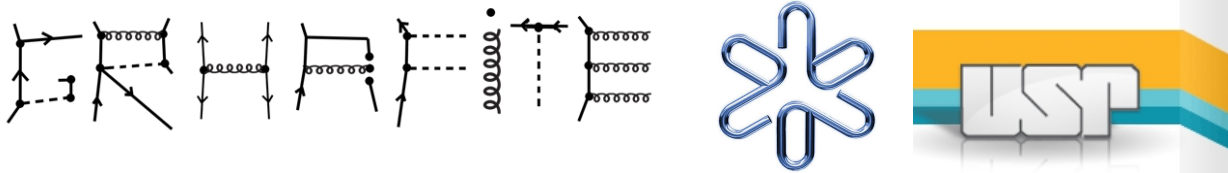


# Capture Reactions with Halo EFT

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collab. with L. Fernando and G. Rupak (Mississippi State University)

Critical Stability

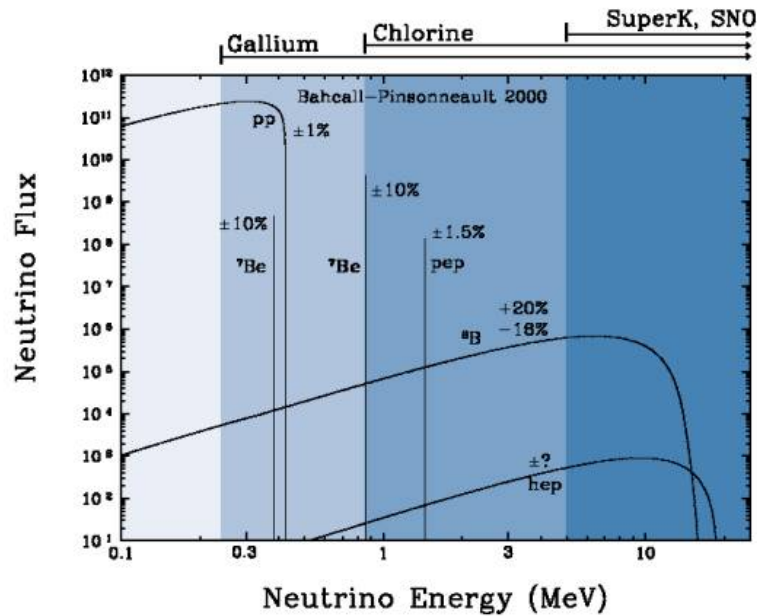
Santos, October 14, 2014

# Capture Reactions with Halo EFT

## Outline

- motivation
- $n$ - ${}^7\text{Li}$  system:
  - low-energy structure
  - low-energy approaches
- halo EFT for  $n + {}^7\text{Li} \rightarrow {}^8\text{Li} + \gamma$ 
  - $E_1$  capture
  - $M_1$  capture
- Summary and outlook

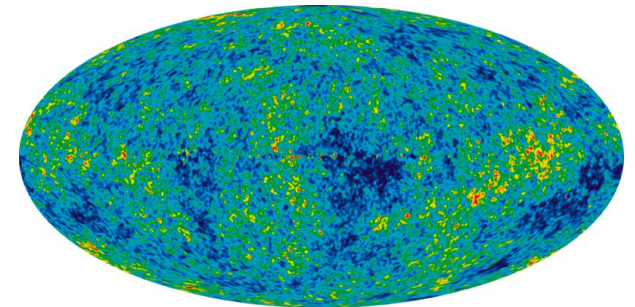
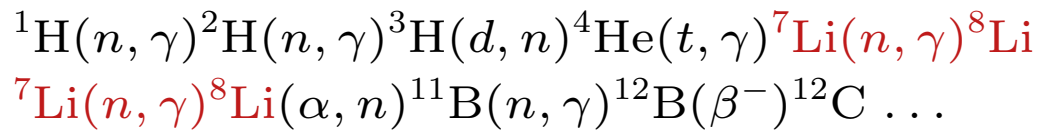




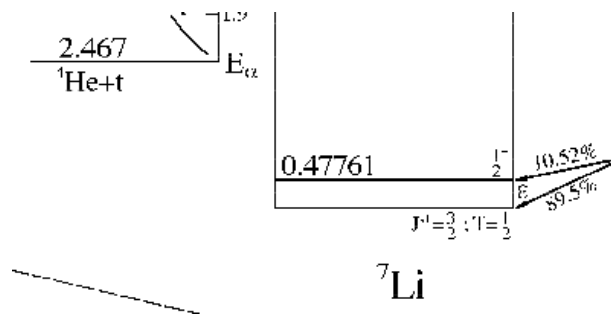
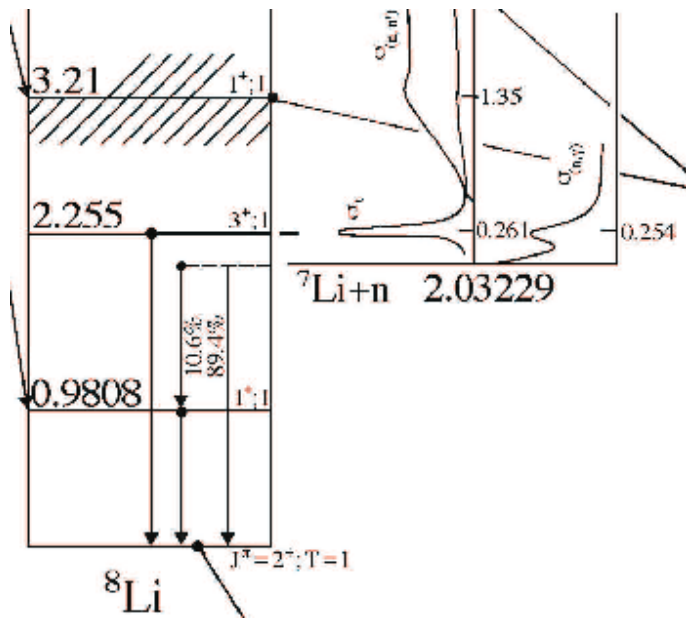
- $p + {}^7\text{Be} \rightarrow {}^8\text{B} + \gamma$   
 $\hookrightarrow {}^8\text{Be} + e^+ + \nu_e$ 
  - $\Rightarrow$  major uncertainty on  $\nu_e$  flux
  - $\Rightarrow S_{17}(0)$ : **low-energy extrapolation**
  - $\Rightarrow$  matter/vacuum oscillations
  - $\Rightarrow$  direct/inverse hierarchy

- mirror symmetry:  ${}^7\text{Li}(n, \gamma){}^8\text{Li}$

- non-homogeneous BBN: bridge the  $A = 8$  gap



# the $n$ - ${}^7\text{Li}$ system



⇒ Bound states:

- $2^+$  ( $-2.03$  MeV):  $\frac{1}{\sqrt{2}}[{}^5P_2 + {}^3P_2]$  ( $p_{3/2}$ )
- $1^+$  ( $-1.05$  MeV):  $\frac{1}{\sqrt{2}}[{}^5P_2 - {}^3P_2]$  ( $p_{1/2}$ )

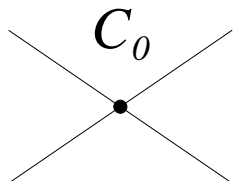
⇒ Scattering states:

- ${}^5S_2$ :  $a_0^{(2)} = -3.63 \pm 0.05$  fm
- ${}^3S_1$ :  $a_0^{(1)} = 0.87 \pm 0.07$  fm
- ${}^3P_3$ :  $E_R = 0.222$  MeV,  $\Gamma_R = 0.031$  MeV

⇒ Radiative capture:

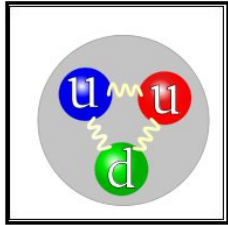
- ${}^5S_2, {}^5S_2 \rightarrow 2^+$  (E1, 89.4%)
- ${}^5S_2, {}^5S_2 \rightarrow 1^+$  (E1, 10.6%)
- ${}^5P_3 \rightarrow 2^+$  (M1)

## potential models vs EFT

	$V_{WS}$	EFT
	$V_{WS}(r) = \frac{-V_0}{1 + \exp\left(\frac{r-R}{d}\right)}$	
bound state	Sch. Eq. for $V_0^B$ , <b>SF/ANC</b>	Feynman graphs, resum., $\mathcal{Z}$
scatt. states	Sch. Eq. for $V_0^{S,\nu}$	Feynman graphs (resum.), $a, r$
EM	$\mathcal{O}_{E1} = Z_C \frac{\mu}{M_C} e r Y_{1m}(\hat{r})$	QED

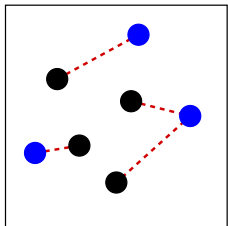


## EFT: basic ideas



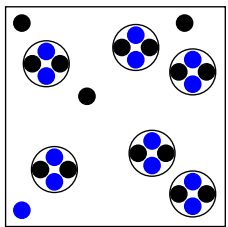
1  $\rightarrow$  10 GeV

- QCD/SM: quarks, gluons vs. hadrons



100 MeV  $\rightarrow$  1 GeV

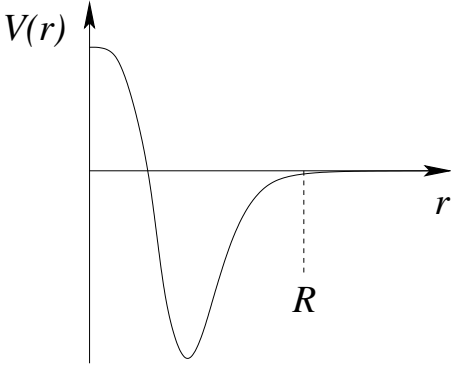
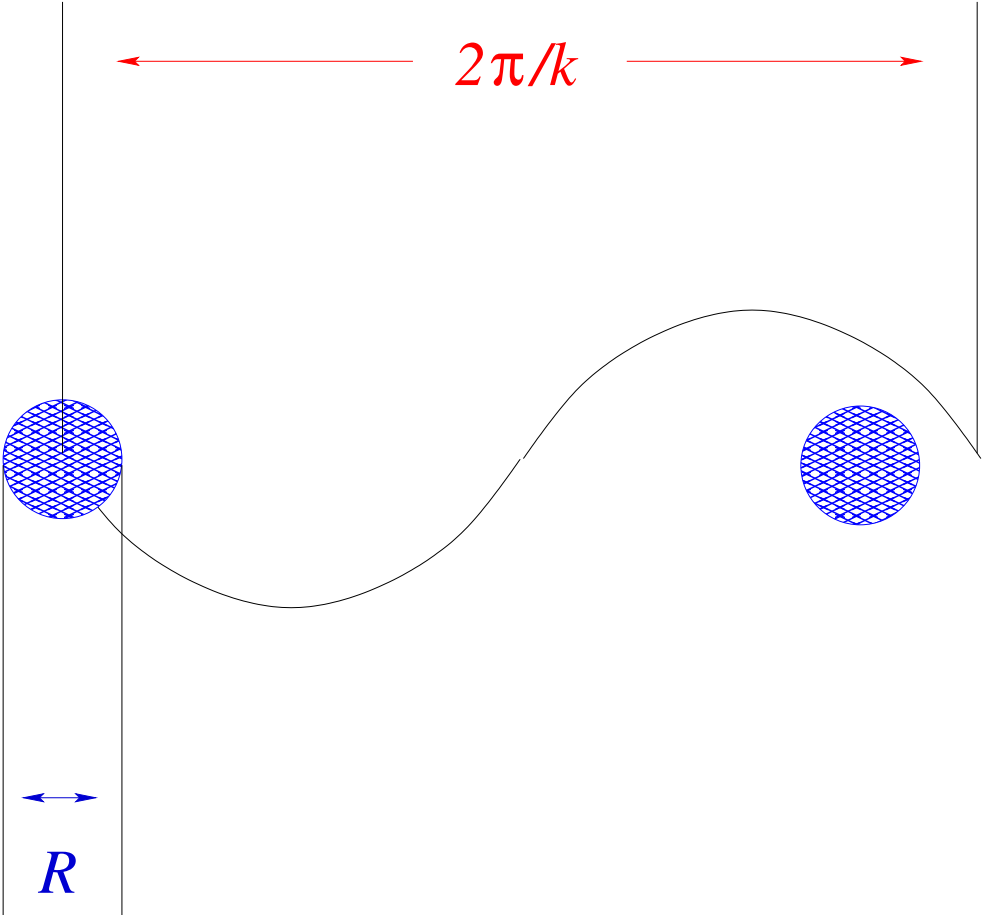
- $\chi$ EFT, phenomenology (meson theory)



$<$  50 MeV

- $\not\chi$ EFT, Halo/cluster EFT, phenomenology

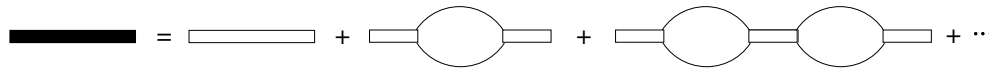
# EFT: basic ideas



## halo/cluster EFT for $n$ - ${}^7\text{Li}$ (scatt. states)

$$\mathcal{L}_{\text{kin}} = N^\dagger \left[ i\partial_0 + \frac{\vec{\nabla}^2}{2M_N} \right] N + C^\dagger \left[ i\partial_0 + \frac{\vec{\nabla}^2}{2M_C} \right] C,$$

$$\mathcal{L}_{\text{int},s} = \phi_i^{(s)\dagger} \left[ \underbrace{i\partial_0 + \frac{\vec{\nabla}^2}{8\mu}}_{\sim C_2} - \underbrace{\Delta}_{\sim C_0} \right] \phi_i^{(s)} + g_0 \left[ \phi_i^{(s)\dagger} N^T \tilde{P}_i^{(s)} C + \text{H.c.} \right] + \dots,$$



$$\Delta \sim \frac{M_{hi}^2}{\mu} \quad \rightarrow \quad iD_s^{(0)} = \frac{i}{-\Delta + i\epsilon} \sim \frac{\mu}{M_{hi}^2} \quad ({}^3S_1)$$

$$\Delta \sim \frac{M_{hi}^2}{\mu} \frac{M_{lo}}{M_{hi}} \quad \rightarrow \quad iD_s^{(0)} = \frac{i}{-\Delta + i\epsilon} \sim \frac{\mu}{M_{hi} M_{lo}} \quad ({}^5S_2)$$



## halo/cluster EFT for $n\text{-}^7\text{Li}$ (bound state)

$p$ -wave: Bertulani, Hammer, van Kolck; Bedaque, Hammer, van Kolck

- two operators at LO!

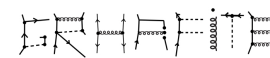
$$\mathcal{L}_{\text{int},p} = \phi_{ij}^{(p)\dagger} \left[ i\partial_0 + \frac{\vec{\nabla}^2}{8\mu} - \Delta \right] \phi_{ij}^{(p)} + g_1 \left[ \phi_{ij}^{(p)\dagger} N^T \tilde{P}_{ij}^{(p)} C + \text{H.c.} \right] + \dots,$$

$$\text{---} = \text{---} + \text{---} \circ \text{---} + \text{---} \circ \text{---} \circ \text{---} + \dots$$

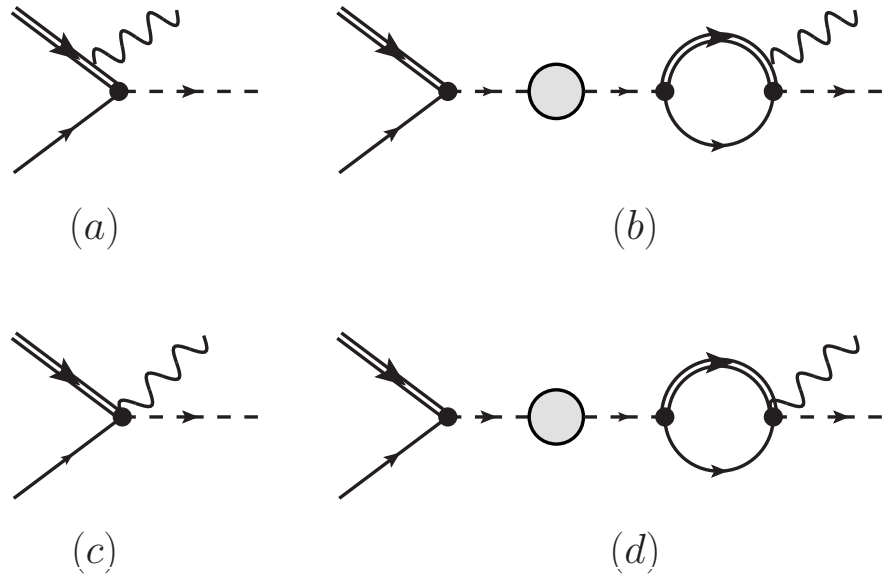
$$\Delta \sim M_{lo}^2/\mu \quad \rightarrow \quad iD_p^{(0)} = \frac{i}{q_0 - \mathbf{q}^2/8\mu - \Delta + i\epsilon} \sim \frac{\mu}{M_{lo}^2} \quad ({}^3P_2, {}^5P_2)$$

$$\mathbf{D}_p = \frac{i}{q_0 - \mathbf{q}^2/8\mu - \Delta - 6g_1^2 L} \quad \Rightarrow \quad \mathcal{Z}^{-1} \equiv \frac{\partial}{\partial q_0} [\mathbf{D}_p^{-1}]_{\text{pole}} = \frac{-2\pi}{3(\gamma_B + r_1)}$$

pole:  $\mathbf{q} = 0$ ;  $q_0 = -\gamma_B^2/2\mu$



## $E_1$ radiative capture



- gauge invariance: cancellation of divergences (Phillips and Hammer)

$$\sigma_{\text{capture}}^{E_1} = \frac{Z}{32\pi M^2} \frac{k_\gamma}{p} \alpha_{em} \left( \frac{Z_C M_N}{M} \right)^2 F(p, \gamma_B, M_C, M_N, a_0^{(1)}, a_0^{(2)})$$

## Wigner bound

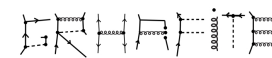
For short-range,  $S$ -wave,  $E$ -independent  $V$ ,

$$r_0 \leq 2 \left( R - \frac{R^2}{a} + \frac{R^3}{3a^2} \right) \quad (\text{Wigner 55'})$$

equivalent to

$$\frac{d}{dE} \left[ \sqrt{2\mu E} \cot \delta(E) \right] \leq 0$$

(Philips *et al.* 1998, Lee and Hammer 2010)



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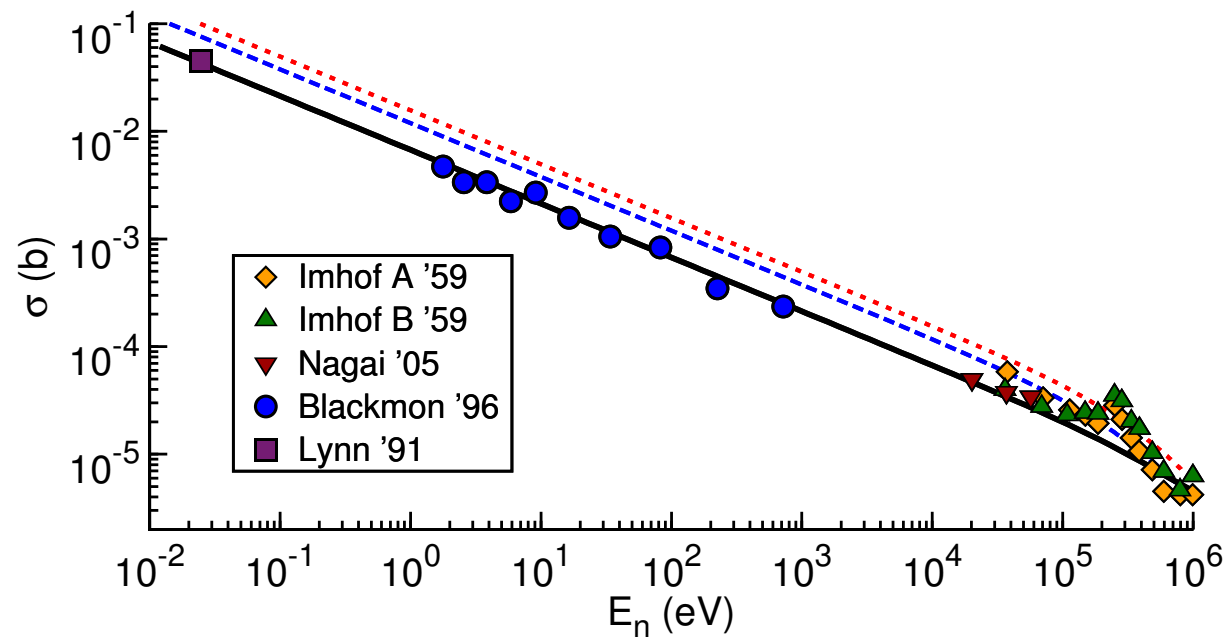
(Philips *et al.* 1998, Lee and Hammer 2010)

Constraints from divergences of loop integrals

**infinities are good!!!**



## $E_1$ radiative capture



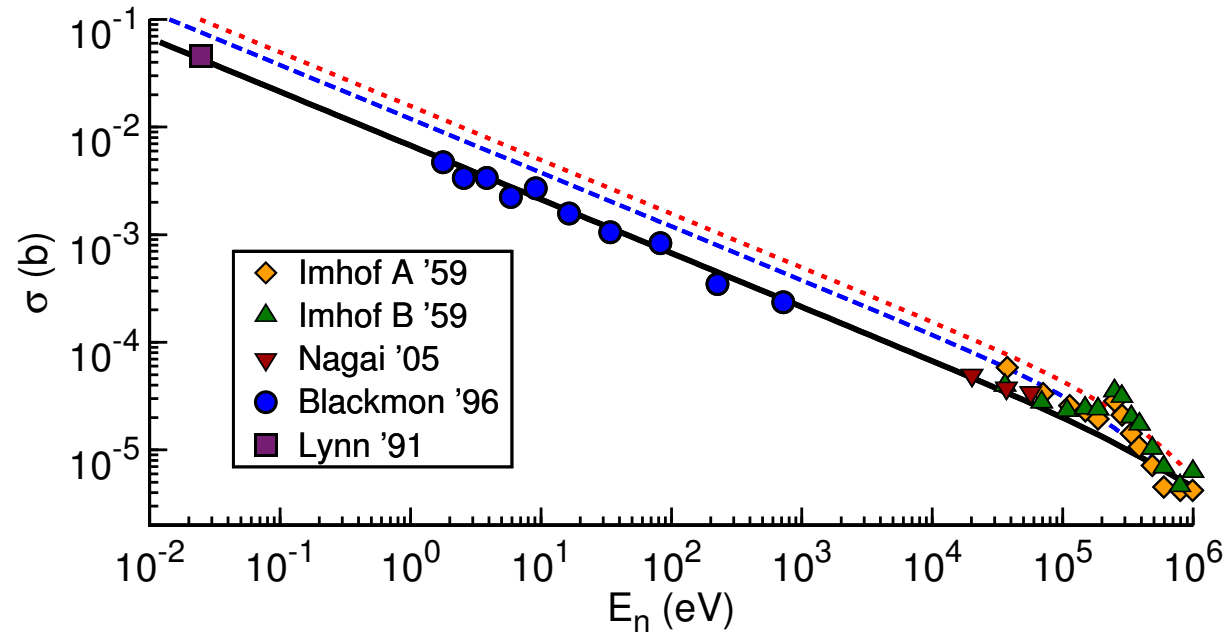
Dauids-Tyep:  $r_1 \approx -0.30 \text{ fm}^{-1}$

Tombrello:  $r_1 \approx -0.46 \text{ fm}^{-1}$

Wigner bound:  $r_1 \lesssim -1 \text{ fm}^{-1}$



## $E_1$ radiative capture



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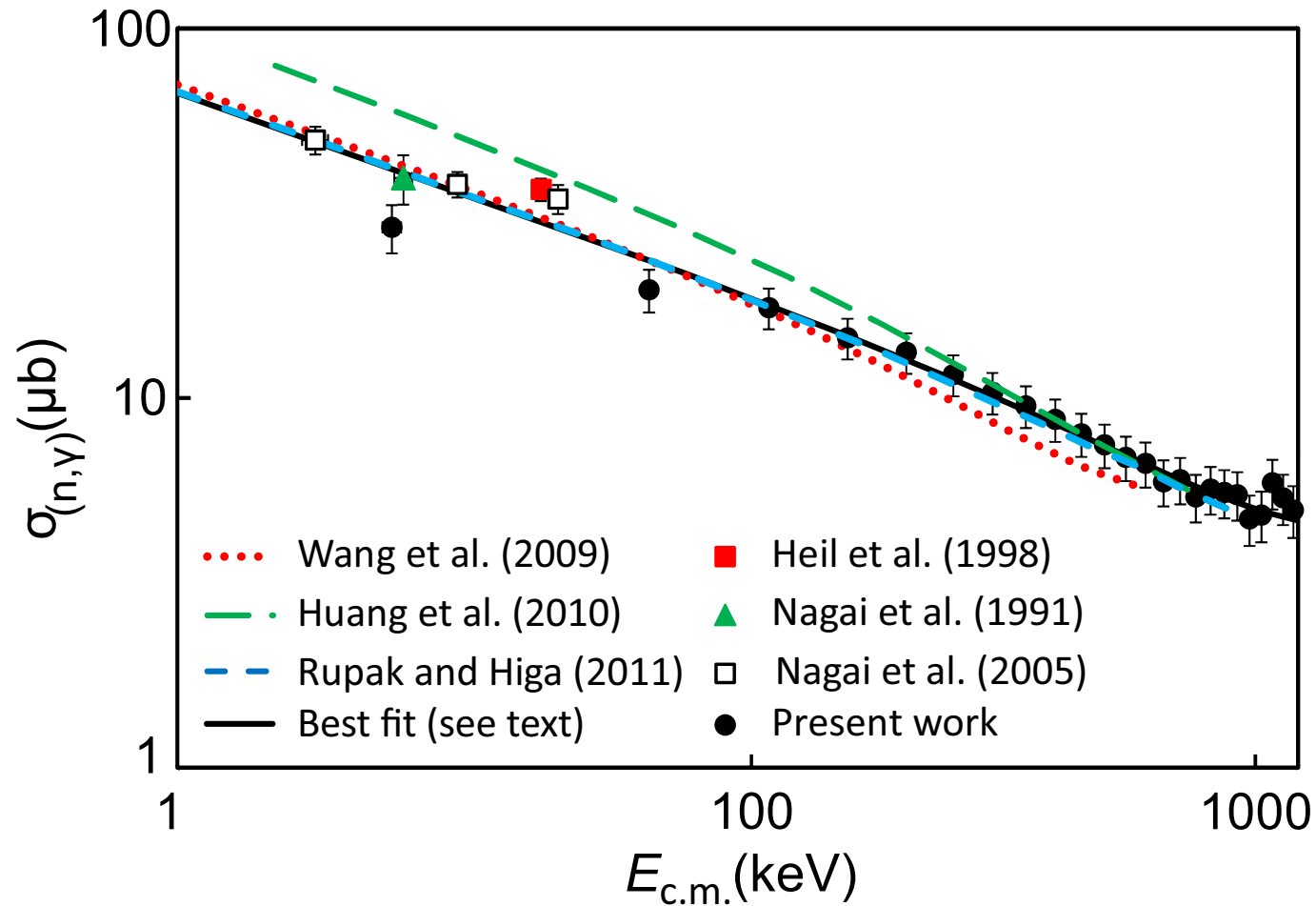
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**EFT:**  $r_1 = -1.47 \text{ fm}^{-1}$

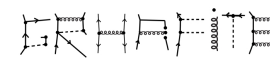
(G. Rupak, RH, PRL 106, 222501, 2011)



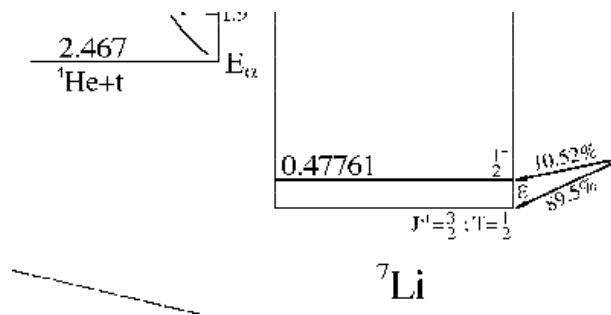
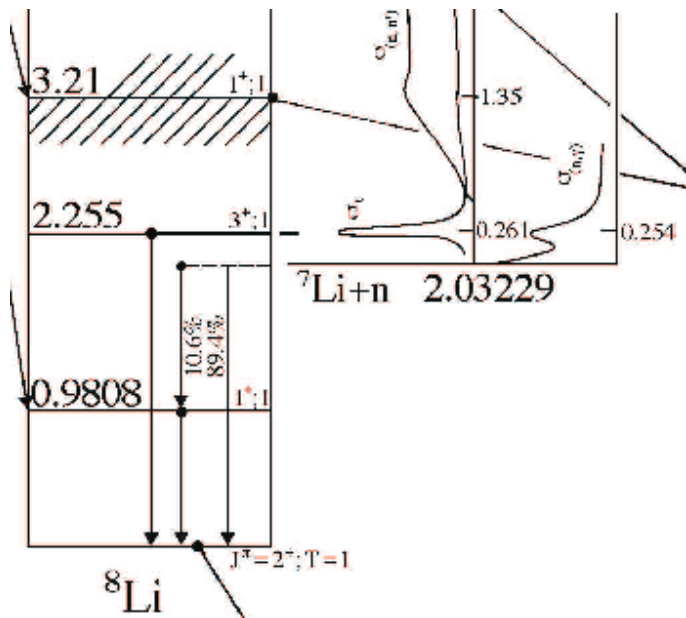
## $E_1$ radiative capture



(Izsák *et al.*, arXiv:1312.3498 [nucl-ex], to appear @ PRC)



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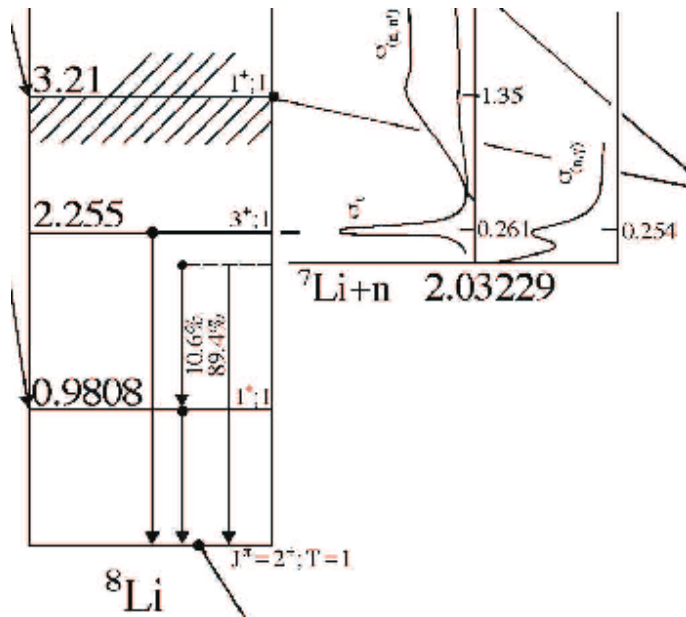
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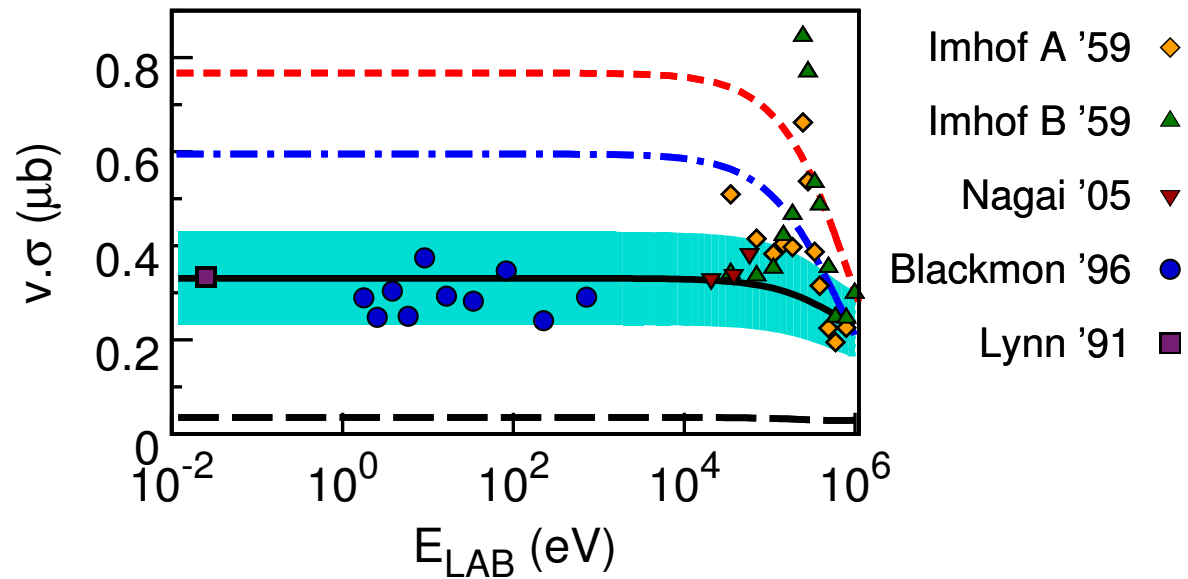
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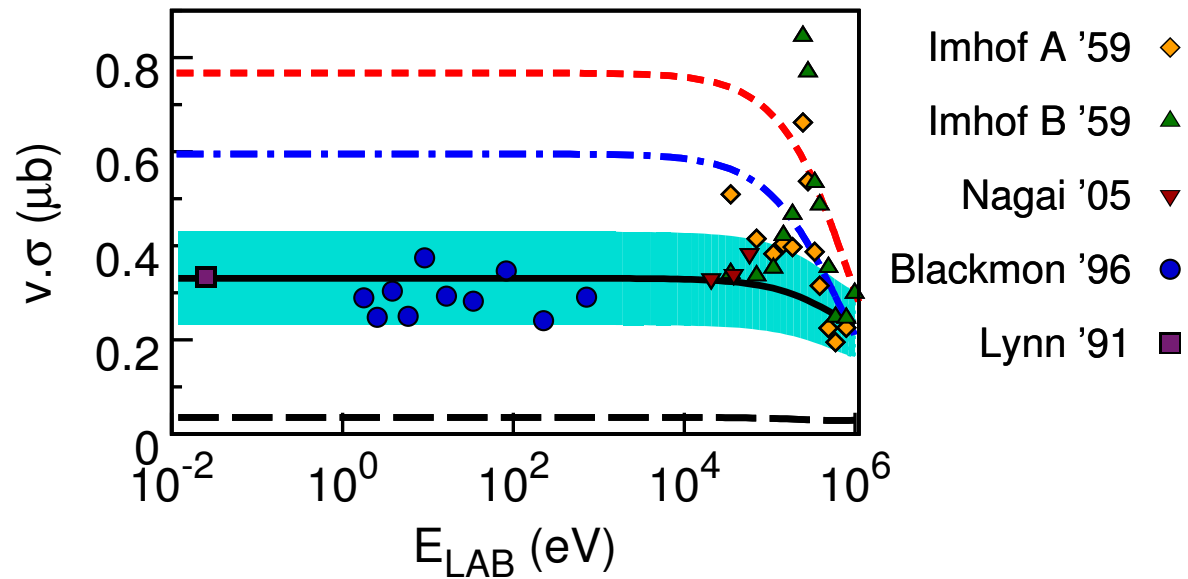
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(L. Fernando, RH, G. Rupak, EPJA 48, 24, 2012)



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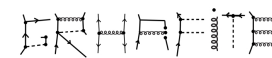


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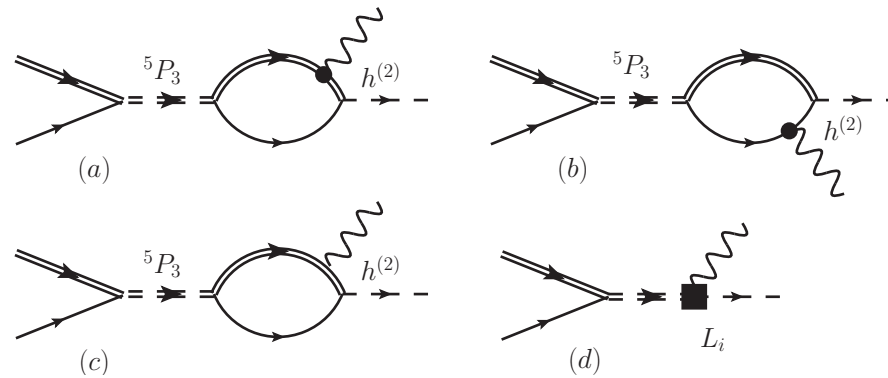
(L. Fernando, RH, G. Rupak, EPJA 48, 24, 2012)

**EFT+*ab-initio*:**  $^5P_2 - ^3P_2$  weights,  $^7\text{Li}^*$

(X. Zhang *et al.*, PRC 89, 024613, 2014)



# $M_1$ radiative capture

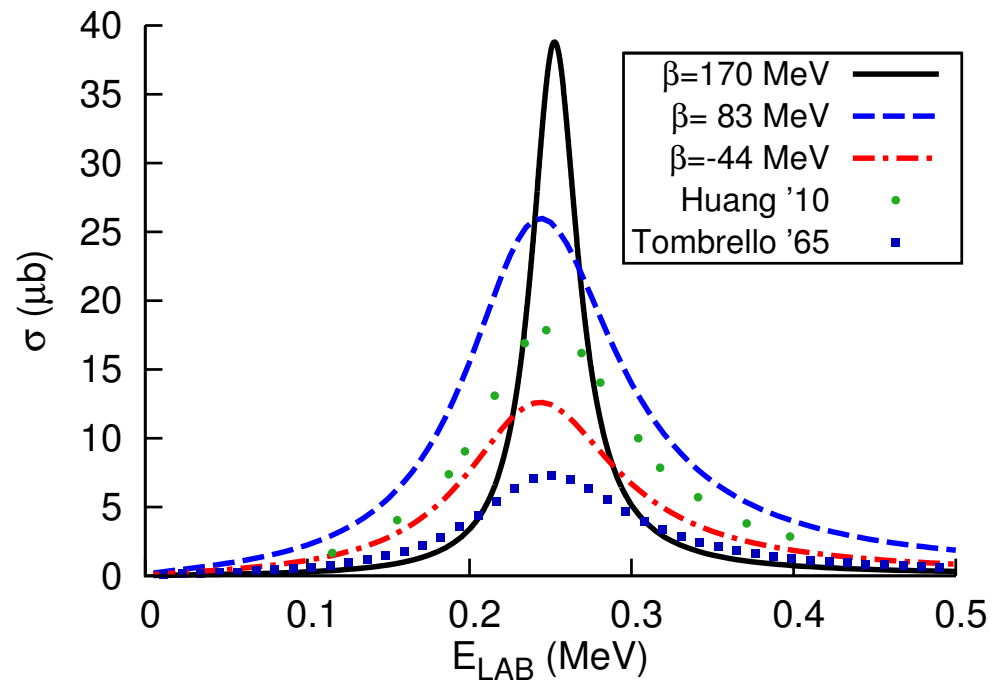


$$\sigma_{\text{capture}}^{M_1} = \frac{Z}{32\pi M^2} \left[ \frac{k_\gamma}{p} \right]^3 p^4 G(p, \gamma_B, M_C, M_N, a_0^{(1)}, a_0^{(2)}, K^{(1)}, K^{(2)}, \beta)$$

$$K^{(1)} = \sqrt{\frac{3}{2}} \left( \frac{3}{2} g_c - \frac{3}{2} g_n \right), \quad K^{(2)} = \sqrt{\frac{3}{2}} \left( \frac{3}{2} g_c + \frac{1}{2} g_n + \frac{2\mu Z_c M_n}{M_c^2} \right),$$

$$\left( \frac{\mu M_n Z_c}{M_c^2} \vec{L} + g_c \vec{S}_C + g_n \vec{S}_N \right)_z$$

# $M_1$ radiative capture

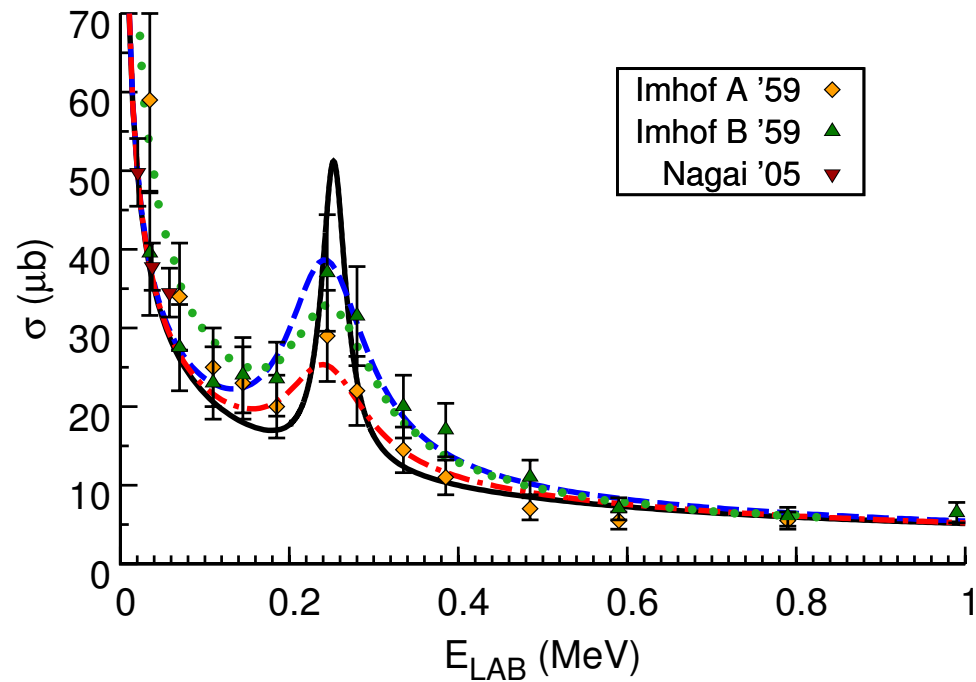


$$\Gamma_{exp} \approx 30 \text{ keV}; \Gamma_{pot} \approx 110 \text{ keV}$$

(L. Fernando, RH, G. Rupak, EPJA 48, 24, 2012)



## $M_1$ radiative capture



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(L. Fernando, RH, G. Rupak, EPJA 48, 24, 2012)

see also Bennaceur *et al.*, NPA 651, 289, 1999



# Summary

- **halo/cluster EFT**: systematic way of implementing EM currents
- gauge invariance: cancellation of power divergences
- ${}^7\text{Li}(n, \gamma){}^8\text{Li}$ :
  - **two** operators at LO
  - “normalization” is very sensitive to  $r_1$  (not well-known from elastic scatt.)
  - $r_1 = -1.47 \text{ fm}^{-1}$ : excellent description of previous data, respect the Wigner bound
  - **potential models**: not so reliable extrapolations at low energies, uncontrolled theoretical uncertainties
  - **excellent agreement** with most recent MSU data (**CD**)
  - $M_1$  capture: missing some structure (degrees of freedom)

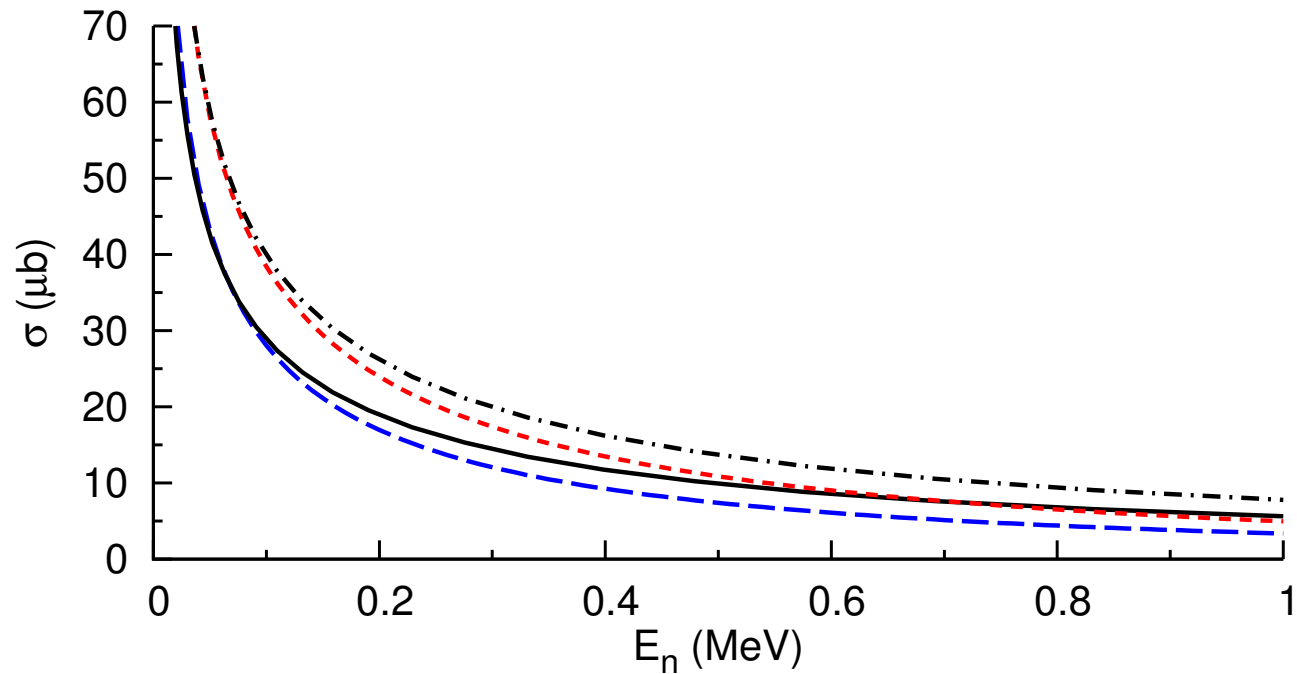


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## $E_1$ radiative capture (theory: ${}^5P_2$ only)



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Tombrello:  $r_1 \approx -0.46 \text{ fm}^{-1}$

**Wigner bound:**  $r_1 \lesssim -1 \text{ fm}^{-1}$  (Lee and Hammer)

