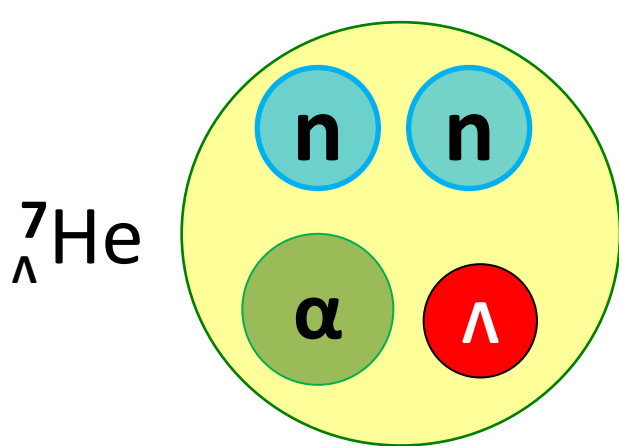


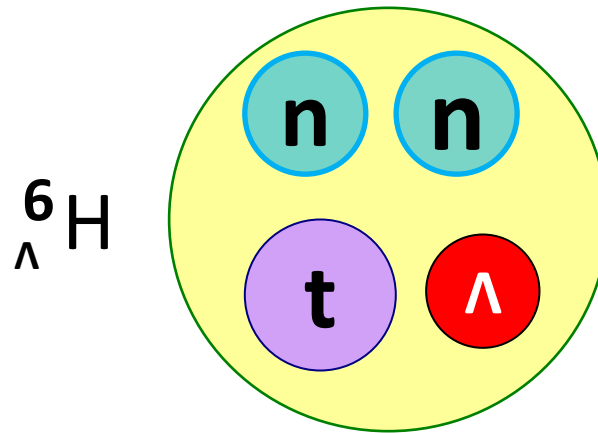
Structure of neutron-rich Λ hypernuclei

E. Hiyama (RIKEN)

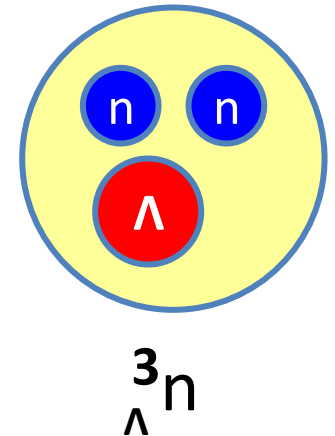
In 2012 and 2013, we had three epoch-making data from the view point of few-body problems.



JLAB experiment-E011,
Phys. Rev. Lett. **110**,
12502 (2013).



FINUDA collaboration & A. Gal,
Phys. Rev. Lett. **108**,
042051 (2012).



C. Rappold et al.,
HypHI collaboration
Phys. Rev. C 88,
041001 (R) (2013)

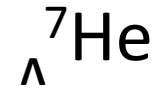
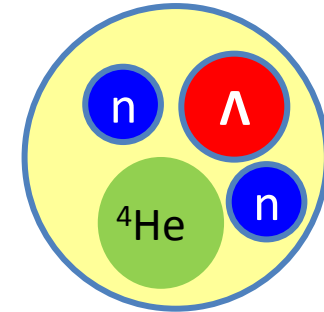
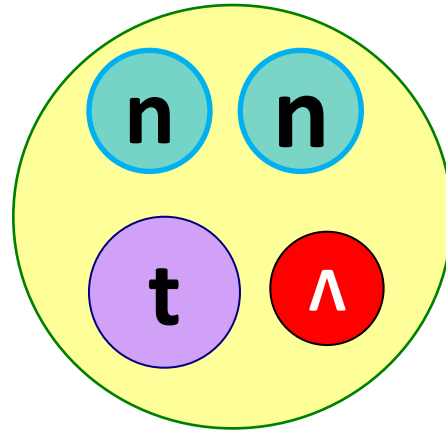
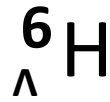
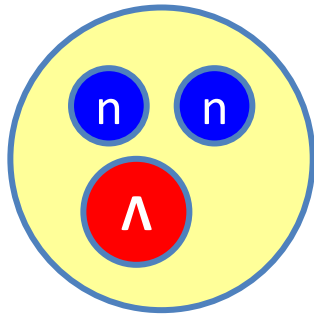
Observation of Neutron-rich Λ -hypernuclei

These observations are interesting from the view points of few-body physics as well as physics of unstable nuclei.

Outline

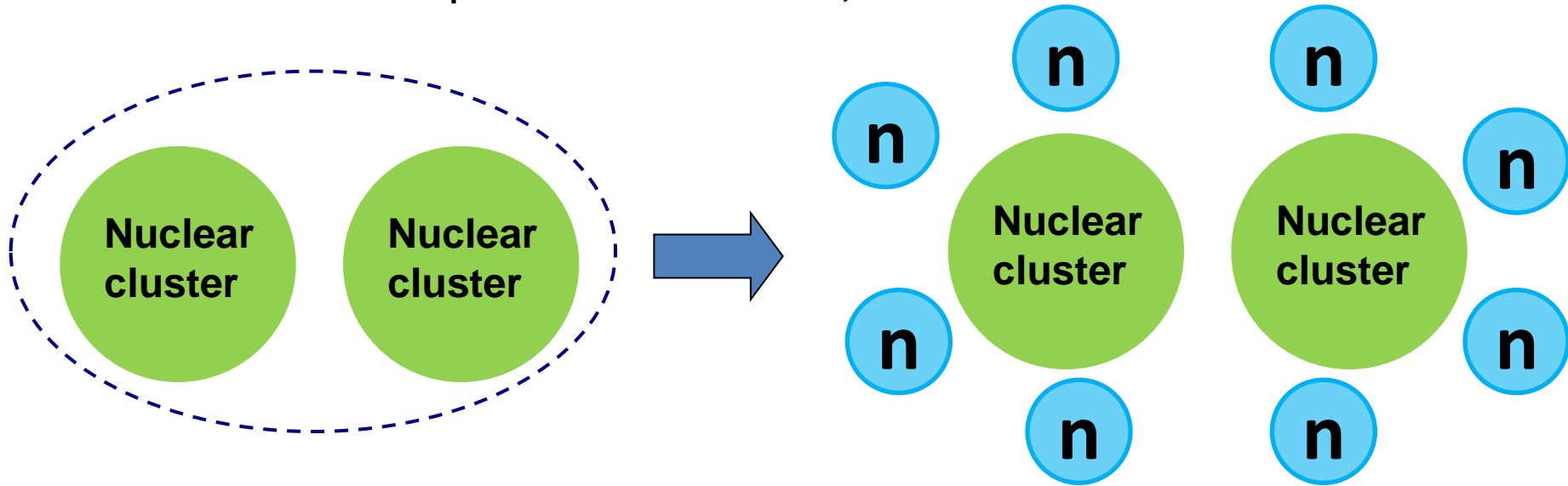
(1) Introduction

(2)



Sec.1 Introduction

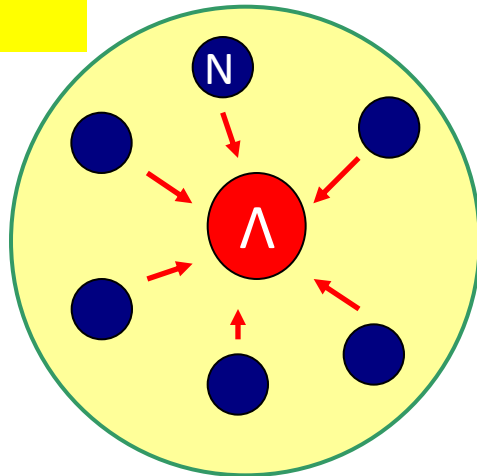
In neutron-rich and proton-rich nuclei,



When some neutrons or protons are added to clustering nuclei, additional neutrons are located **outside** the clustering nuclei due to the Pauli blocking effect.

As a result, we have neutron/proton halo structure in these nuclei. There are many interesting phenomena in this field as you know.

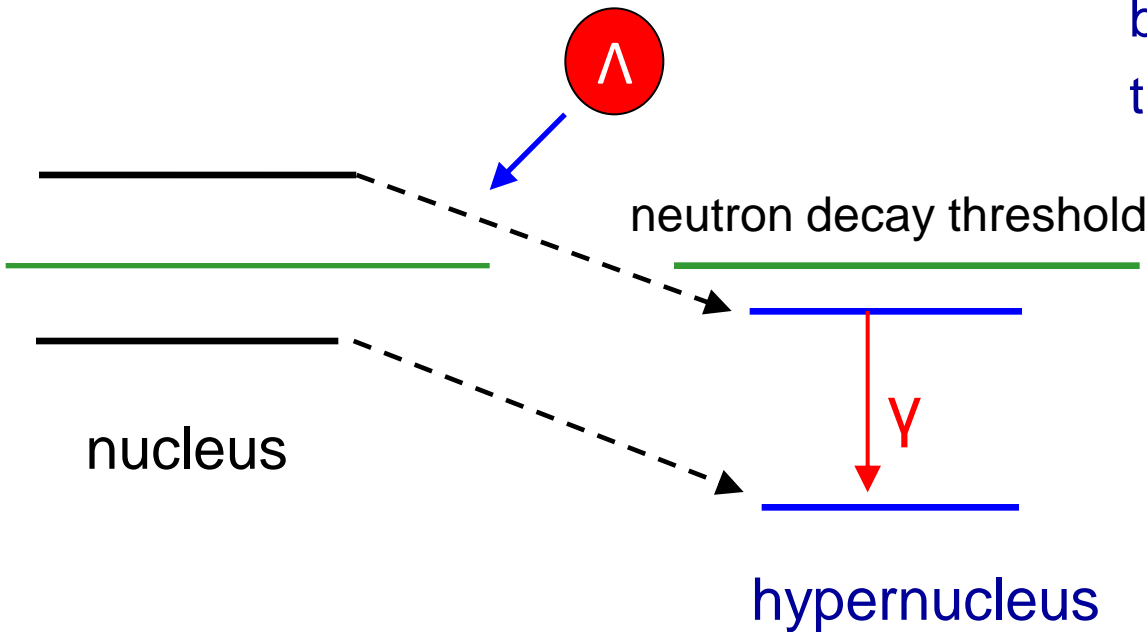
No Pauli principle
Between N and Λ



Hypernucleus

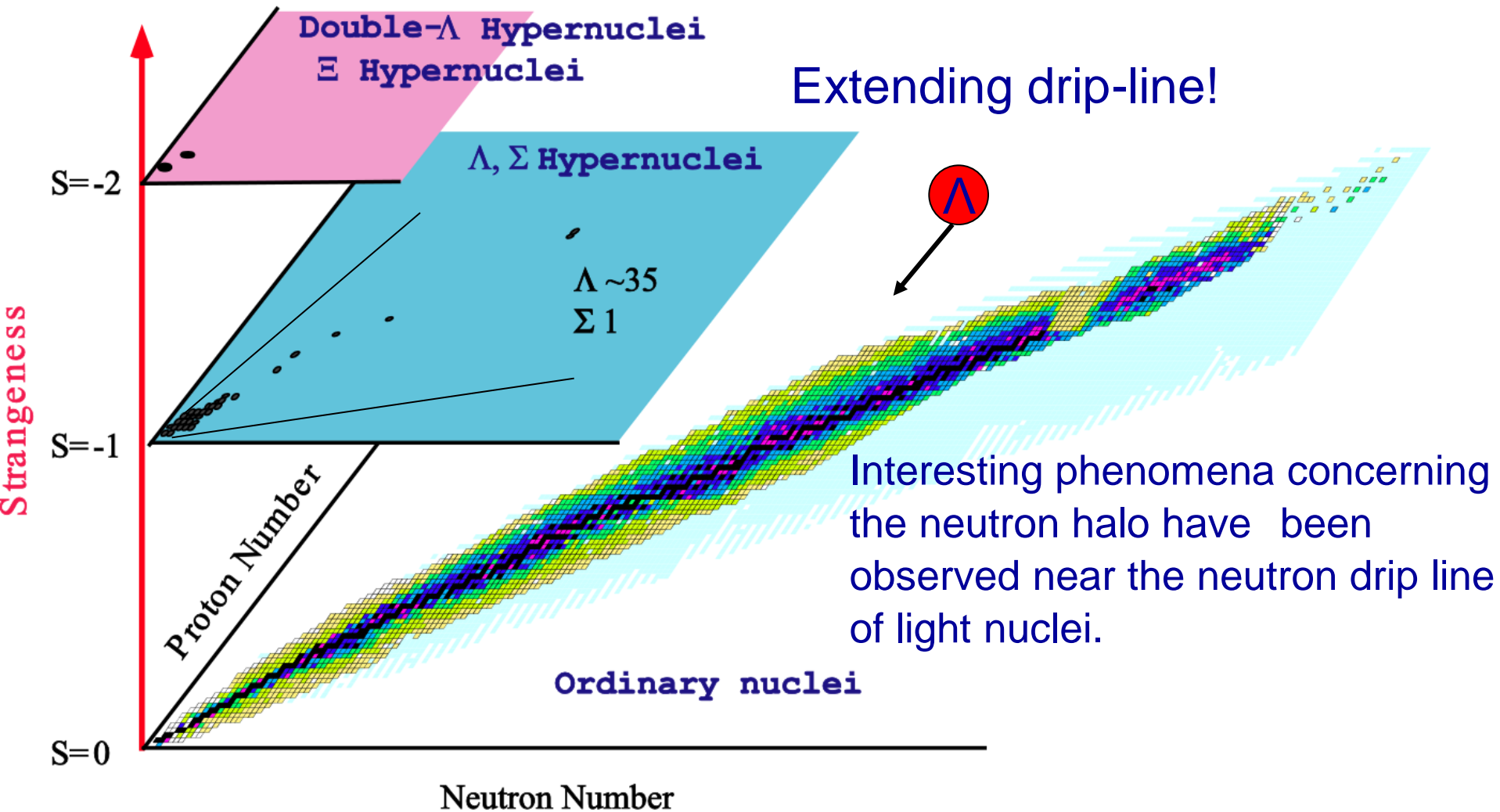
Λ particle can reach deep inside,
and attract the surrounding
nucleons towards the interior
of the nucleus.

Due to the attraction of
 Λ N interaction, the
resultant hypernucleus will
become more stable against
the neutron decay.

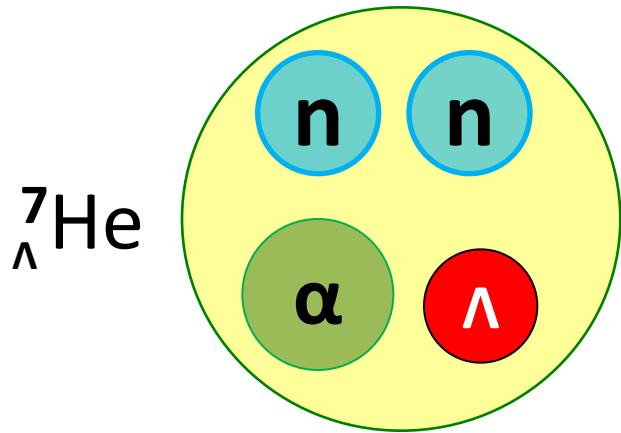


Nuclear chart with strangeness

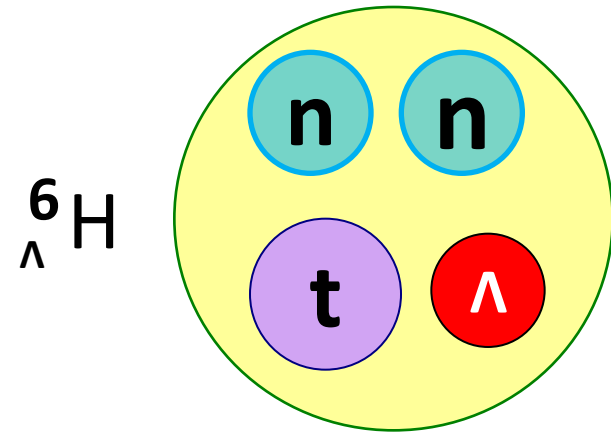
Multi-strangeness system
such as Neutron star



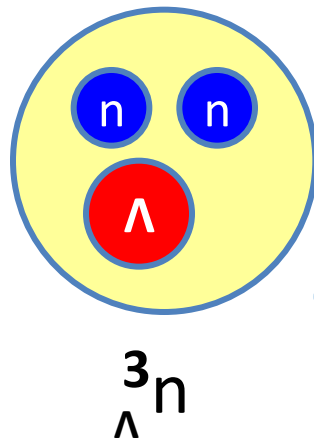
Question : How is structure change when a Λ particle is injected into neutron-rich nuclei?



Observed at JLAB, Phys. Rev. Lett. **110**, 12502 (2013).



Observed by FINUDA group, Phys. Rev. Lett. **108**, 042051 (2012).



C. Rappold et al., HypHI collaboration
Phys. Rev. C 88, 041001 (R) (2013)

In order to solve few-body problem accurately,

Gaussian Expansion Method (GEM) , since 1987,

- A variational method using Gaussian basis functions
- Take all the sets of Jacobi coordinates

Developed by Kyushu Univ. Group,
Kamimura and his collaborators.

Review article :

E. Hiyama, M. Kamimura and Y. Kino,
Prog. Part. Nucl. Phys. 51 (2003), 223.

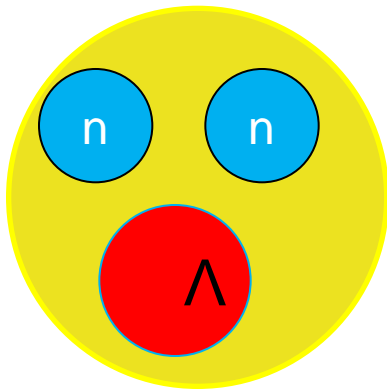
High-precision calculations of various 3- and 4-body systems:

Exotic atoms / molecules ,
3- and 4-nucleon systems,
multi-cluster structure of light nuclei,

Light hypernuclei,
3-quark systems,
⁴He-atom tetramer

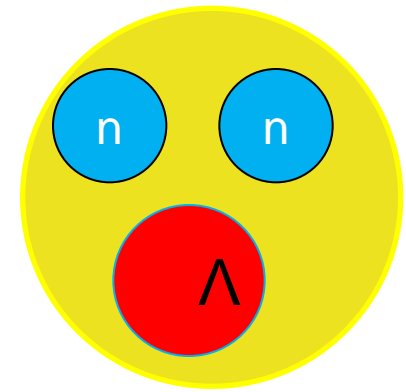
Section 2

three-body calculation of ${}^3_{\Lambda}n$



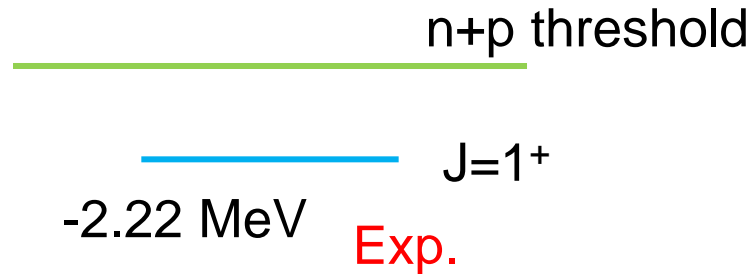
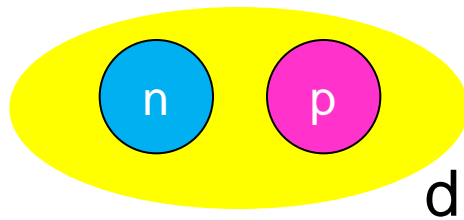
E. Hiyama, S. Ohnishi,
B.F. Gibson, and T. A. Rijken,
PRC89, 061302(R) (2014).

What is interesting to study $nn\Lambda$ system?

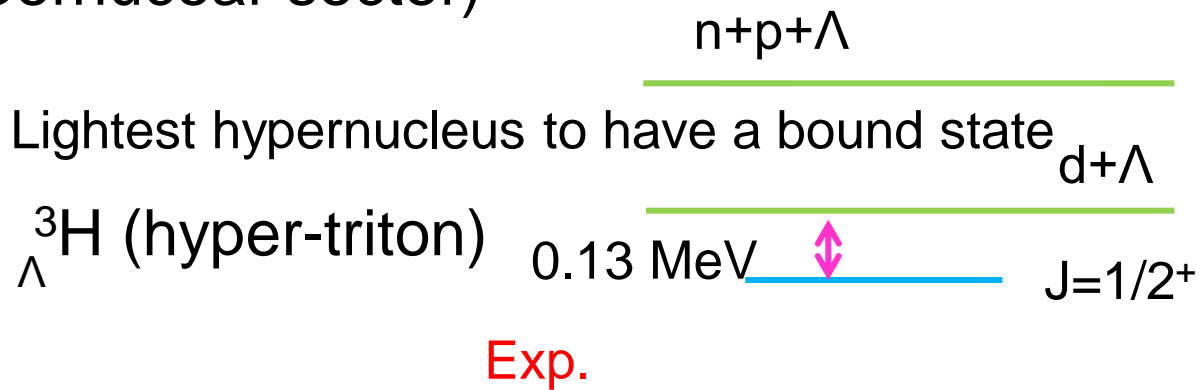
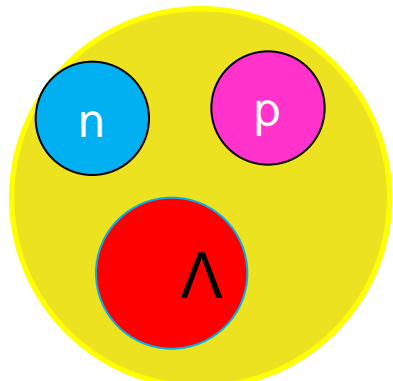


$S=0$

The lightest nucleus to have a bound state is deuteron.

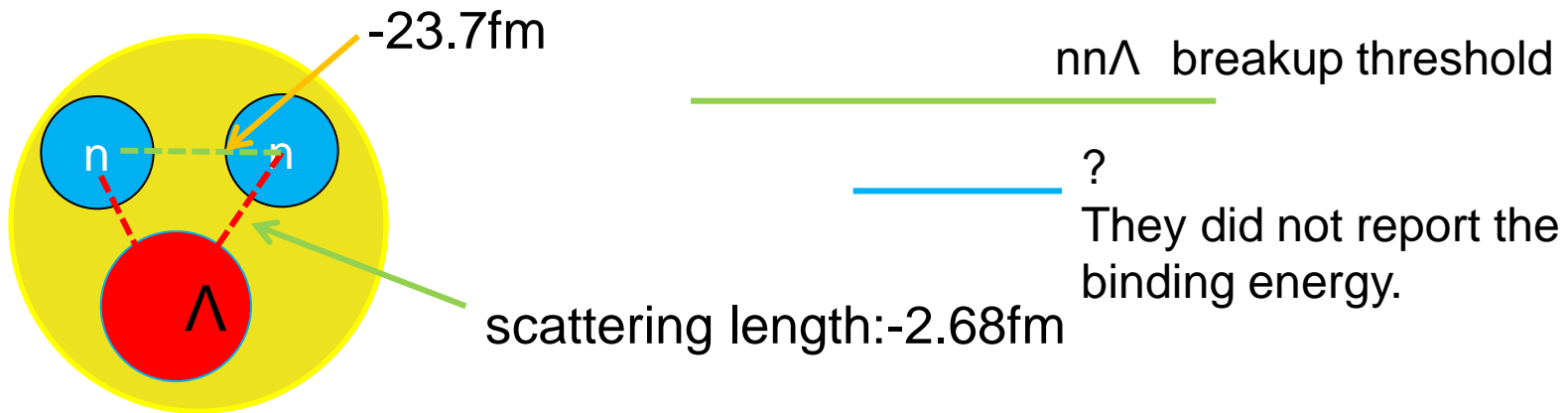


$S=-1$ (Λ hypernuclear sector)



Search for evidence of ${}^3_{\Lambda}n$ by observing $d + \pi^-$ and $t + \pi^-$ final states in the reaction of ${}^6\text{Li} + {}^{12}\text{C}$ at 2 A GeV

C. Rappold,^{1,2,*} E. Kim,^{1,3} T. R. Saito,^{1,4,5,†} O. Bertini,^{1,4} S. Bianchin,¹ V. Bozkurt,^{1,6} M. Kavatsyuk,⁷ Y. Ma,^{1,4} F. Maas,^{1,4,5} S. Minami,¹ D. Nakajima,^{1,8} B. Özel-Tashenov,¹ K. Yoshida,^{1,5,9} P. Achenbach,⁴ S. Ajimura,¹⁰ T. Aumann,^{1,11} C. Ayerbe Gayoso,⁴ H. C. Bhang,³ C. Caesar,^{1,11} S. Erturk,⁶ T. Fukuda,¹² B. Göküzüm,^{1,6} E. Guliev,⁷ J. Hoffmann,¹ G. Ickert,¹ Z. S. Ketenci,⁶ D. Khanef, ^{1,4} M. Kim,³ S. Kim,³ K. Koch,¹ N. Kurz,¹ A. Le Fèvre,^{1,13} Y. Mizoi,¹² L. Nungesser,⁴ W. Ott,¹ J. Pochodzalla,⁴ A. Sakaguchi,⁹ C. J. Schmidt,¹ M. Sekimoto,¹⁴ H. Simon,¹ T. Takahashi,¹⁴ G. J. Tambave,⁷ H. Tamura,¹⁵ W. Trautmann,¹ S. Voltz,¹ and C. J. Yoon³
(HypHI Collaboration)



Observation of $nn\Lambda$ system (2013)

Lightest hypernucleus to have a bound state

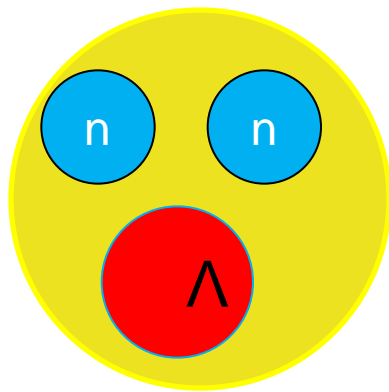
Any two-body systems are unbound. => $nn\Lambda$ system is bound.

Lightest Borromean system.

Theoretical important issue:

Do we have bound state for $nn\Lambda$ system?

If we have a bound state for this system, how much is binding energy?



$nn\Lambda$ breakup threshold



?

They did not report the binding energy.

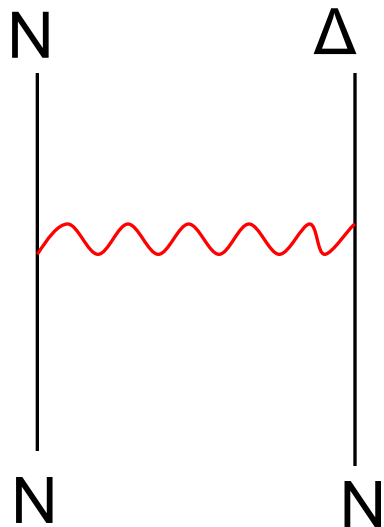
NN interaction : to reproduce the observed binding energies of ${}^3\text{H}$ and ${}^3\text{He}$

NN: AV8 potential

We do not include 3-body force for nuclear sector.

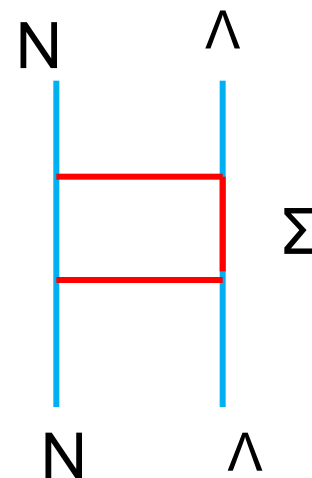
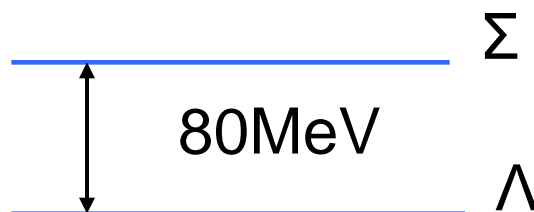
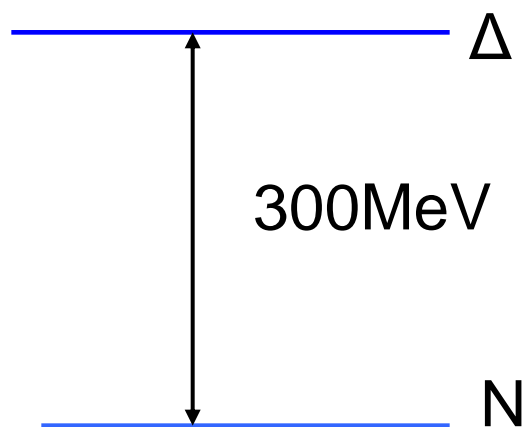
How about YN interaction?

Non-strangeness nuclei

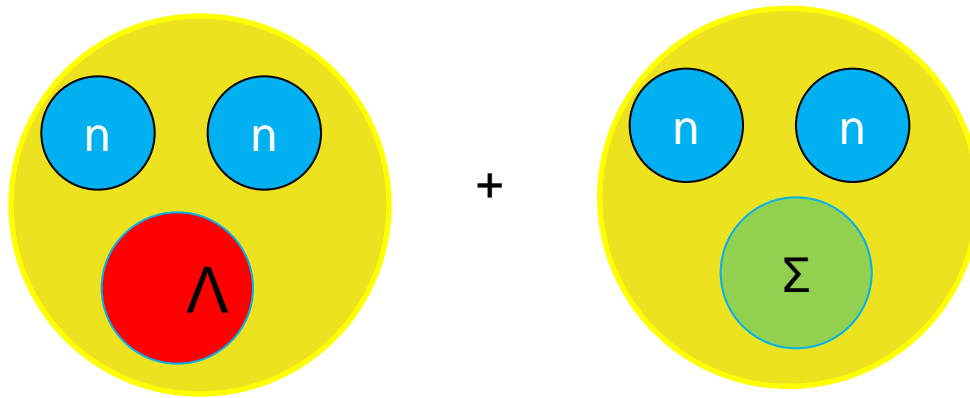


Nucleon can be converted into Δ .
However, since mass difference between nucleon and Δ is large, then probability of Δ in nucleus is not large.

On the other hand, the mass difference between Λ and Σ is much smaller, then Λ can be converted into Σ particle easily.

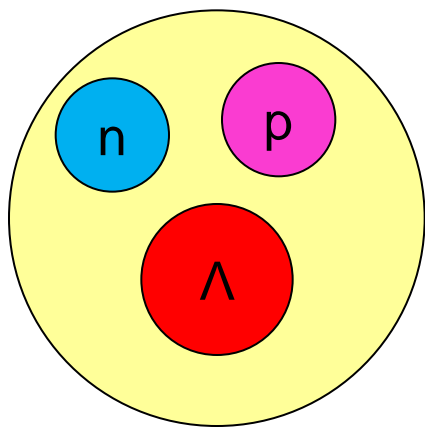


To take into account of Λ particle to be converted into Σ particle, we should perform below calculation using realistic hyperon(Λ)-nucleon(N) interaction.



YN interaction: Nijmegen soft core '97f potential (NSC97f)
proposed by Nijmegen group

reproduce the observed binding energies of ${}^3_{\Lambda}\text{H}$, ${}^4_{\Lambda}\text{H}$ and ${}^4_{\Lambda}\text{He}$



${}^3\text{H}_\Lambda$

$-B_\Lambda$

0 MeV

$d+\Lambda$

$1/2^+$

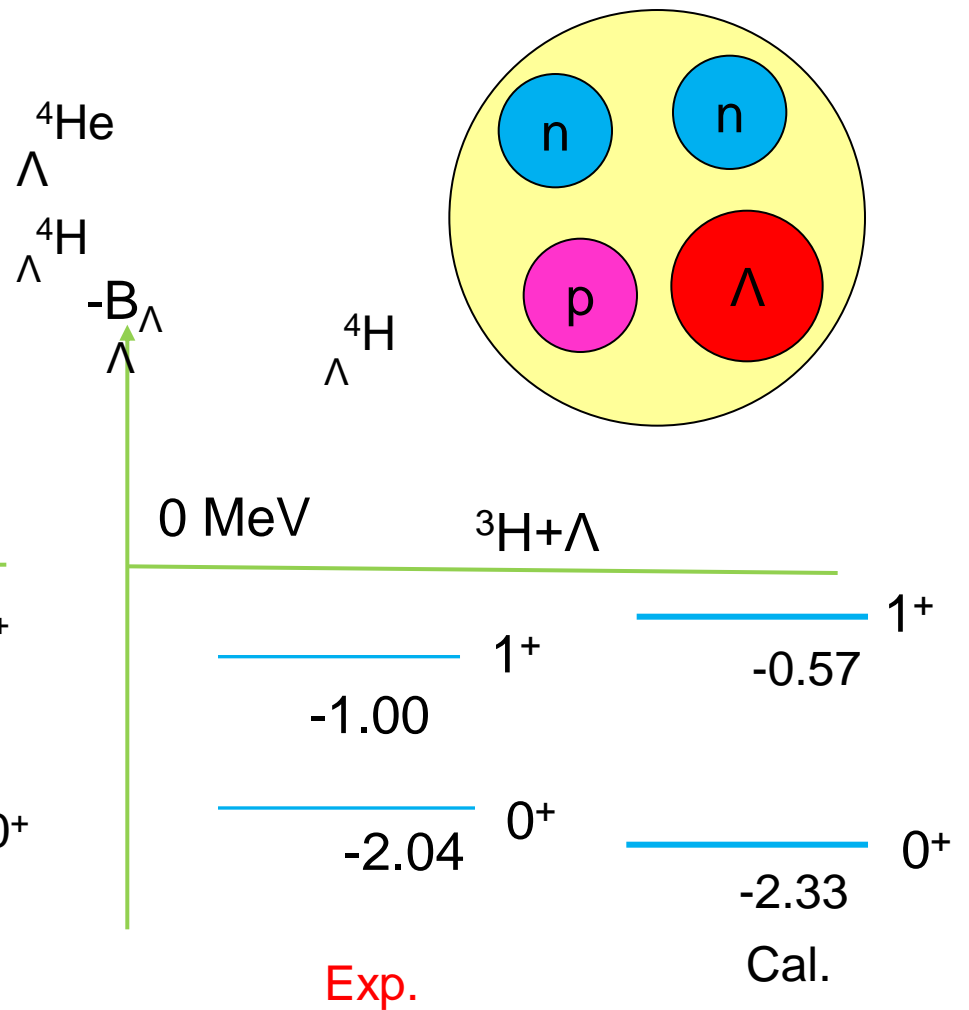
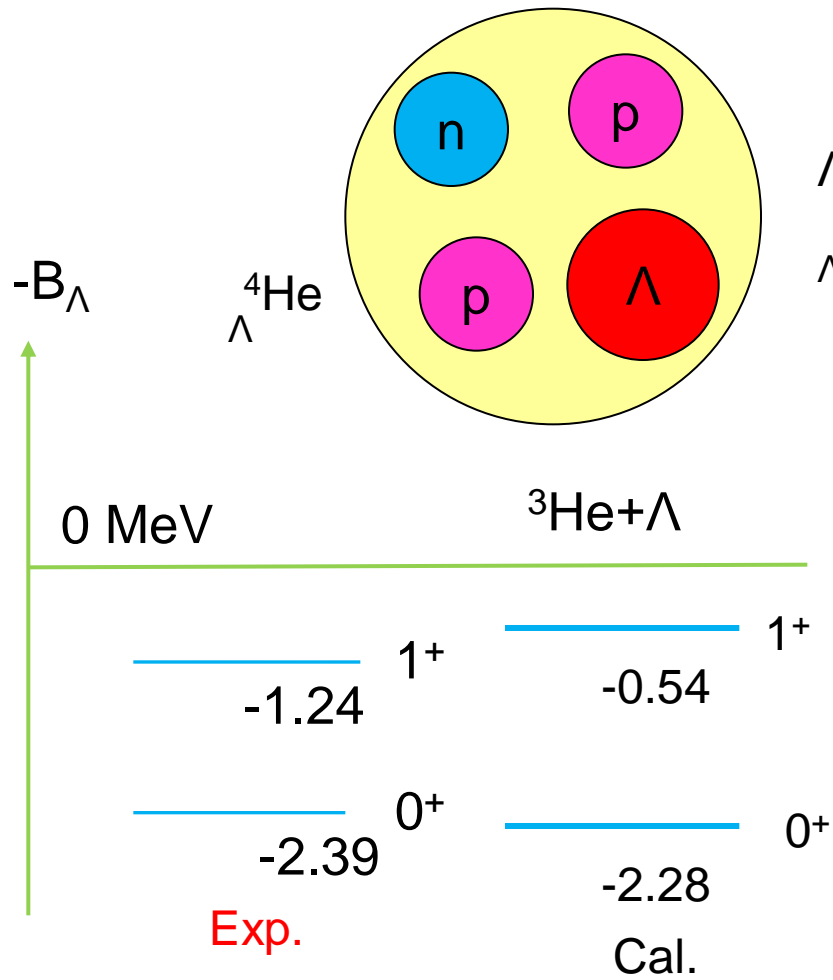
$1/2^+$

$-0.13 \pm 0.05 \text{ MeV}$

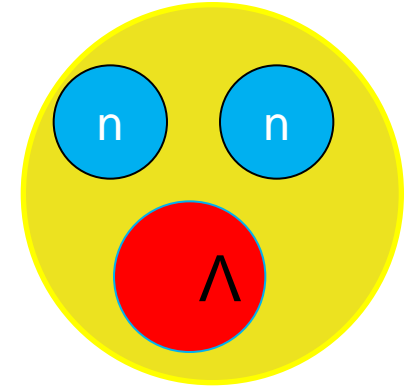
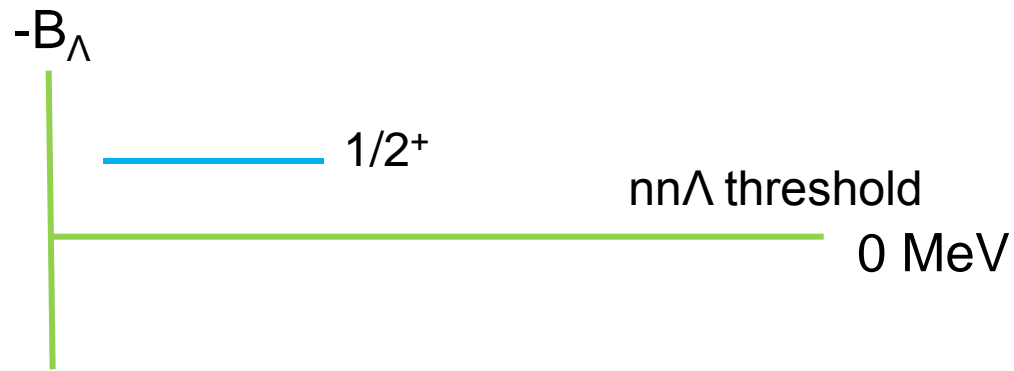
-0.19 MeV

Exp.

Cal.



What is binding energy of $nn\Lambda$?



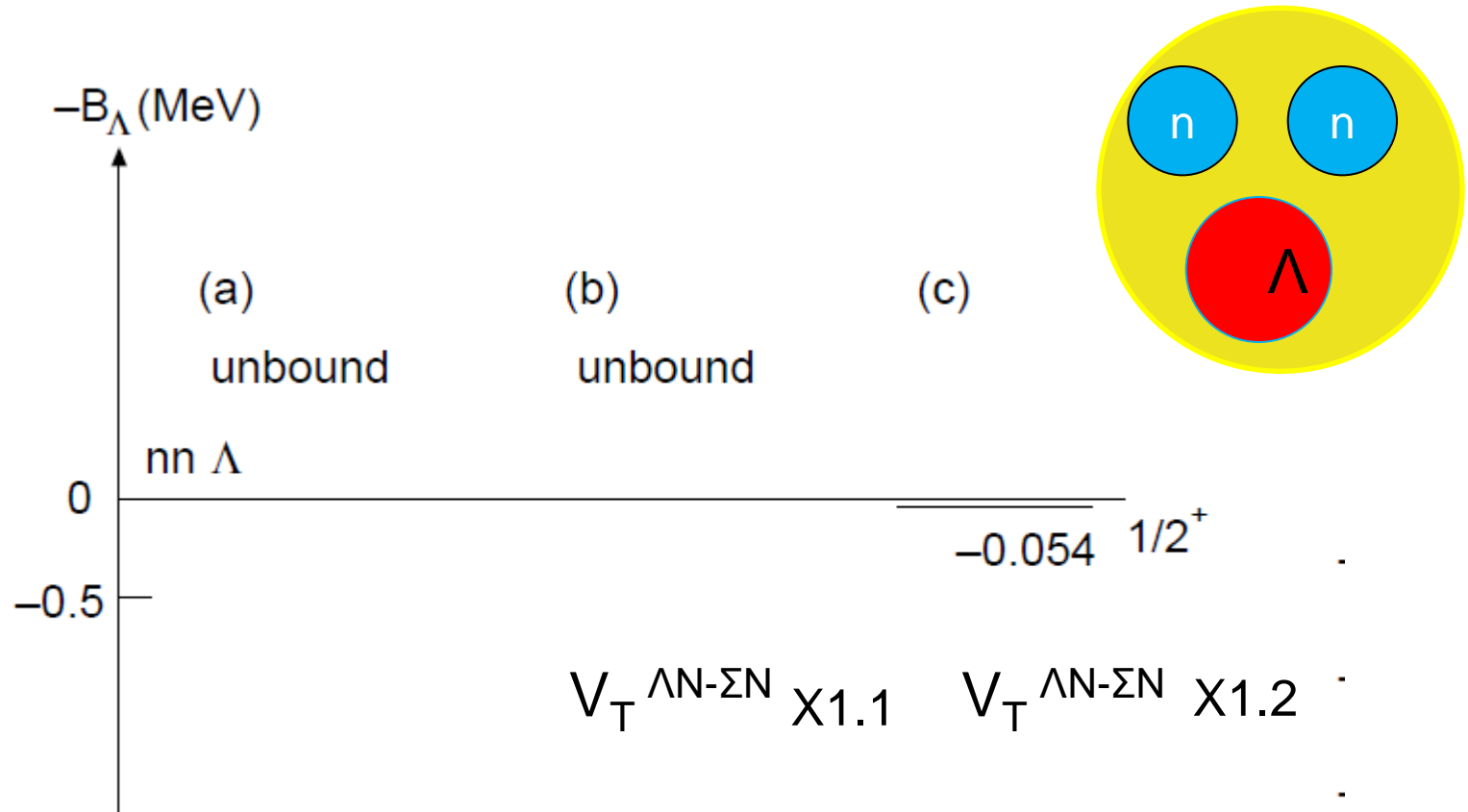
We have no bound state in $nn\Lambda$ system.
This is inconsistent with the data.

Now, we have a question.

Do we have a possibility to have a bound state in $nn\Lambda$ system tuning strength of YN potential ?

It should be noted to maintain consistency with the binding energies of ${}^3_\Lambda\text{H}$ and ${}^4_\Lambda\text{H}$ and ${}^4_\Lambda\text{He}$.

$$V_T^{\Lambda N-\Sigma N} \quad \times 1.1, 1.2$$



When we have a bound state in $nn\Lambda$ system, what are binding energies of ${}^3\text{H}_\Lambda$ and $A=4$ hypernuclei?

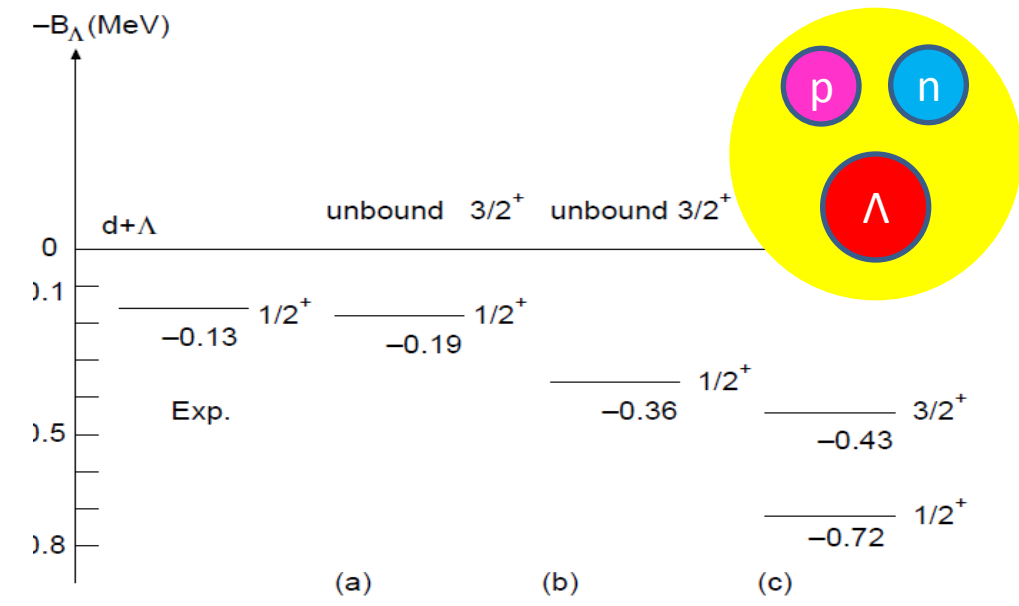
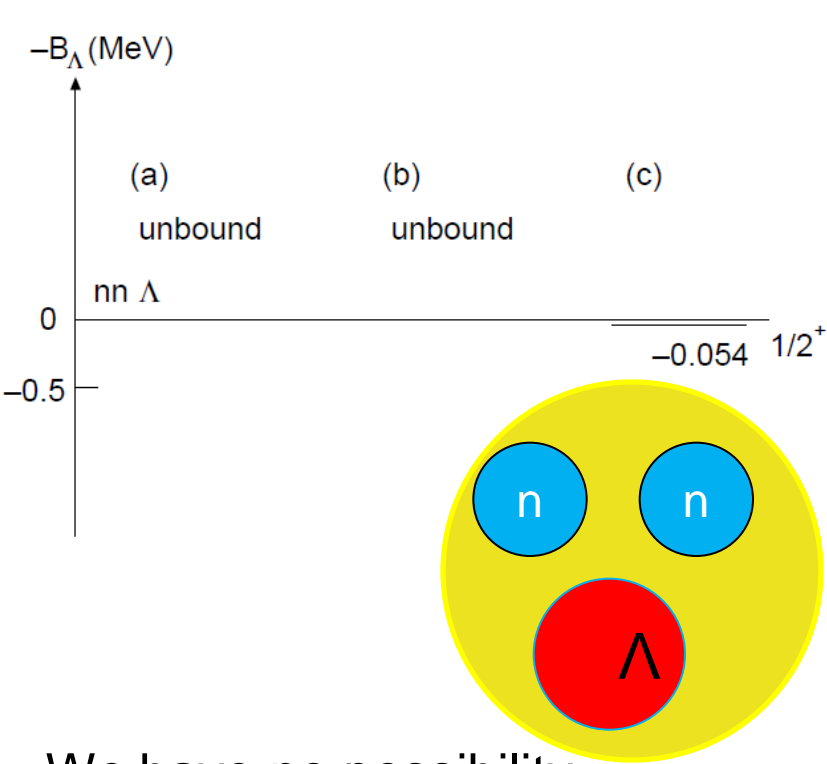
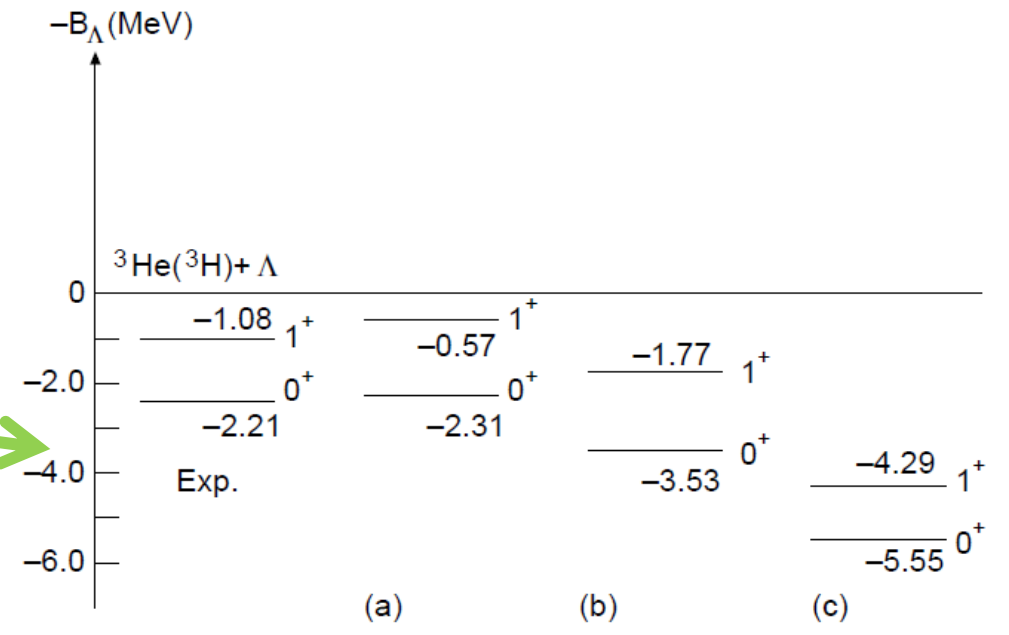
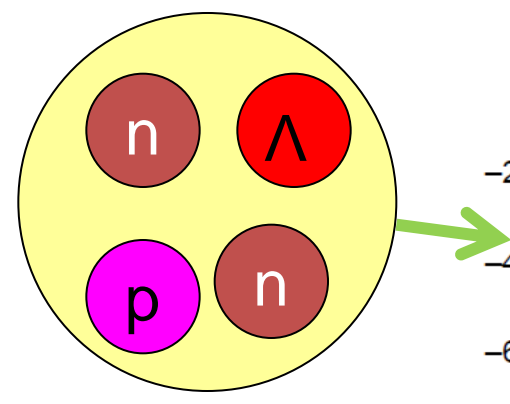


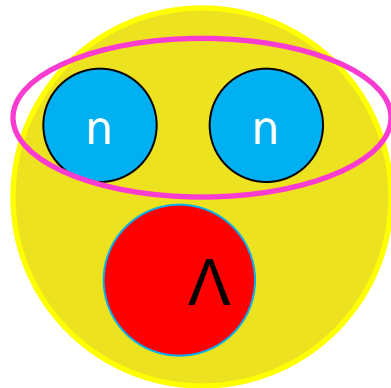
FIG. 3: Calculated Λ -separation energy for ${}^3_\Lambda\text{H}$ with (a) ${}^3V_{N\Lambda-N\Sigma}^T \times 1.00$, (b) ${}^3V_{N\Lambda-N\Sigma}^T \times 1.10$, and (c) ${}^3V_{N\Lambda-N\Sigma}^T \times$

We have no possibility to have a bound state in $nn\Lambda$ system.



Question: If we tune 1S_0 state of nn interaction, Do we have a possibility to have a bound state in nn Λ ? In this case, the binding energies of ^3H and ^3He reproduce the observed data?

Some authors pointed out to have dineutron bound state in nn system. Ex. H. Witala and W. Gloeckle, Phys. Rev. C85, 064003 (2012).



$T=1, ^1S_0$ state

I multiply component of 1S_0 state by 1.13 and 1.35. What is the binding energies of nn Λ ?

PHYSICAL REVIEW C 85, 064003 (2012)

Di-neutron and the three-nucleon continuum observables

H. Witala

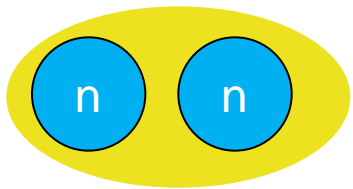
M. Smoluchowski Institute of Physics, Jagiellonian University, PL-30059 Kraków, Poland

W. Glöckle

Institut für Theoretische Physik II, Ruhr-Universität Bochum, D-44780 Bochum, Germany

(Received 24 April 2012; published 25 June 2012)

We investigate how strongly a hypothetical 1S_0 bound state of two neutrons would affect observables in neutron-deuteron reactions. To that aim we extend our momentum-space scheme of solving the three-nucleon Faddeev equations and incorporate in addition to the deuteron also a 1S_0 di-neutron bound state. We discuss effects induced by a di-neutron on the angular distributions of the neutron-deuteron elastic scattering and deuteron breakup cross sections. A comparison to the available data for the neutron-deuteron total cross section and elastic scattering angular distributions cannot decisively exclude the possibility that two neutrons can form a 1S_0 bound state. However, strong modifications of the final-state-interaction peaks in the neutron-deuteron breakup reaction seem to disallow the existence of a di-neutron.



nn unbound

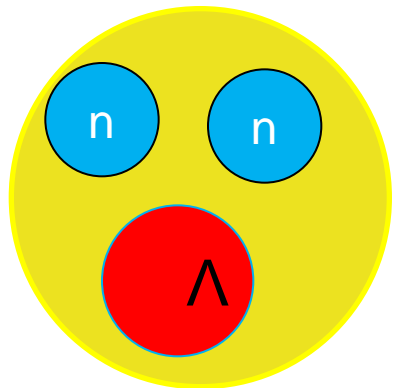
0 MeV

-0.066 MeV

$^1S_0 \times 1.13$

-1.269 MeV

$^1S_0 \times 1.35$



nnΛ unbound

unbound

0 MeV

$1/2^+$

-1.272 MeV

We do not find any possibility to have a bound state in nnΛ.

N+N+N

^3H (^3He)
-8.48 (-7.72)

-7.77 (-7.12)

-9.75 (-9.05)

-13.93 (-13.23) MeV

Exp.

Cal.

Cal.

Cal.

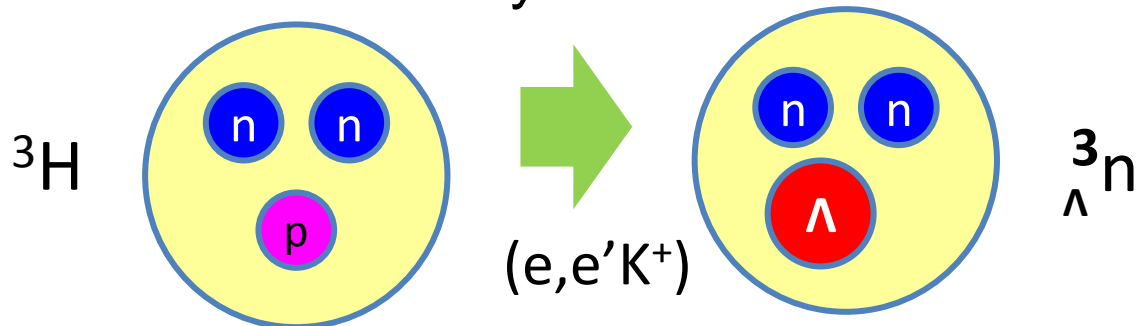
$1/2^+$

$1/2^+$

Summary of $nn\Lambda$ system:

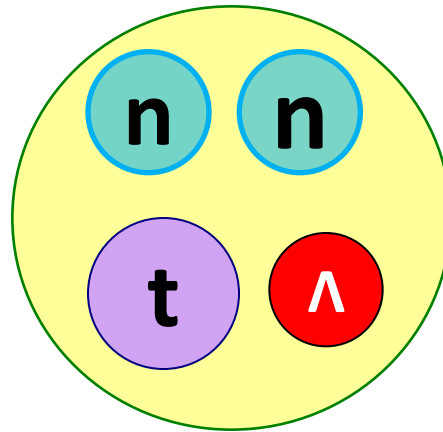
Motivated by the reported observation of data suggesting a bound state $nn\Lambda$, we have calculated the binding energy of this hypernucleus taking into account ΛN - ΣN explicitly. We did not find any possibility to have a bound state in this system. However, the experimentally they reported evidence for a bound state. As long as we believe the data, we should consider additional missing elements in the present calculation. But, I have no idea. Unfortunately, they did not report binding energy.

It might be good idea to perform search experiment of $nn\Lambda$ system at Jlab to conclude whether or not the system exists as bound state experimentally.



Section 3

Four-body calculation of ${}^6_{\Lambda}\text{H}$





Evidence for Heavy Hyperhydrogen ${}^6_{\Lambda}H$

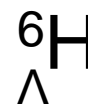
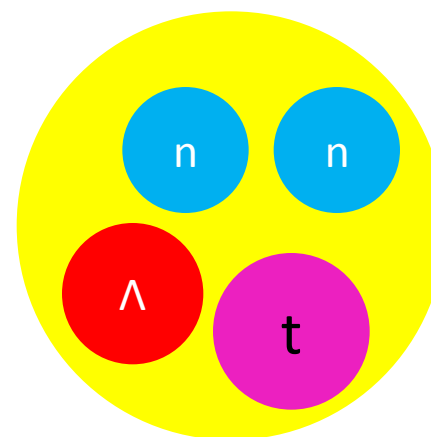
M. Agnello,^{1,2} L. Benussi,³ M. Bertani,³ H. C. Bhang,⁴ G. Bonomi,^{5,6} E. Botta,^{7,2,*} M. Bregant,⁸ T. Bressani,^{7,2} S. Bufalino,² L. Busso,^{9,2} D. Calvo,² P. Camerini,^{10,11} B. Dalena,¹² F. De Mori,^{7,2} G. D'Erasmus,^{13,14} F. L. Fabbri,³ A. Feliciello,² A. Filippi,² E. M. Fiore,^{13,14} A. Fontana,⁶ H. Fujioka,¹⁵ P. Genova,⁶ P. Gianotti,³ N. Grion,¹⁰ V. Lucherini,³ S. Marcello,^{7,2} N. Mirfakhrai,¹⁶ F. Moia,^{5,6} O. Morra,^{17,2} T. Nagae,¹⁵ H. Ota,¹⁸ A. Pantaleo,^{14,†} V. Patricchio,¹⁴ S. Piano,¹⁰ R. Rui,^{10,11} G. Simonetti,^{13,14} R. Wheadon,² and A. Zenoni^{5,6}

(FINUDA Collaboration)

A. Gal

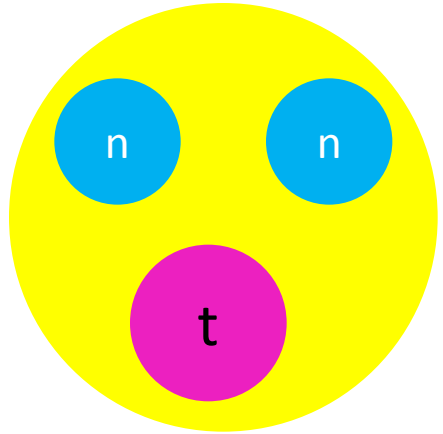
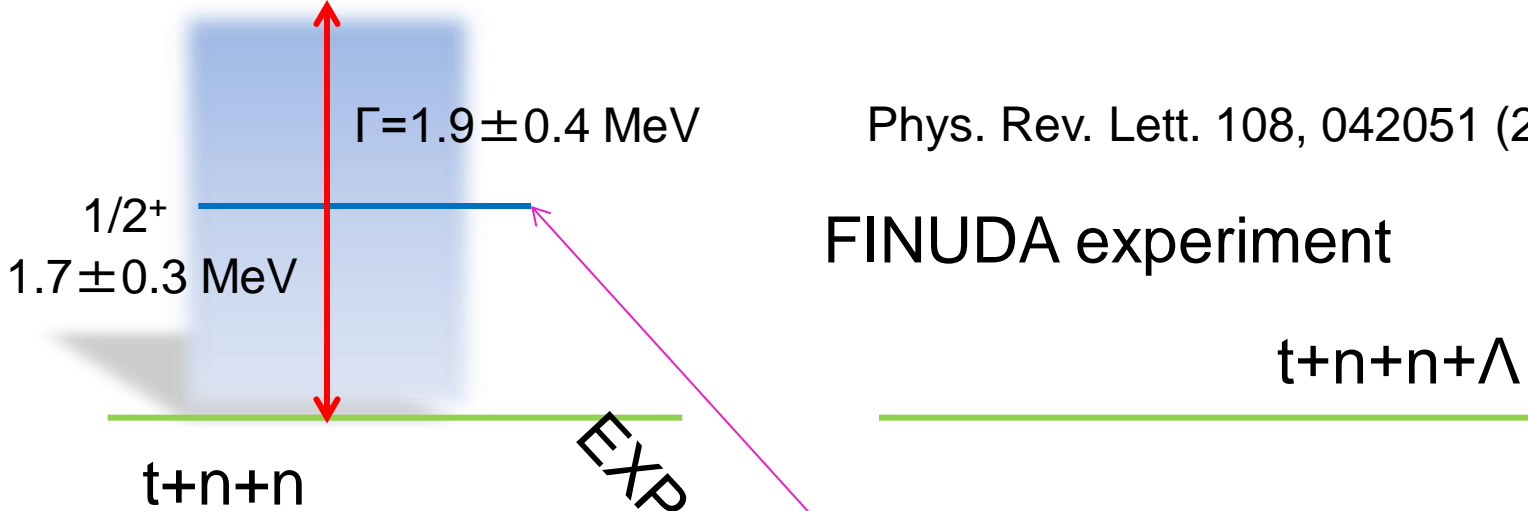
Racah Institute of Physics, The Hebrew University, Jerusalem 91904, Israel

(Received 2 November 2011; published 24 January 2012)

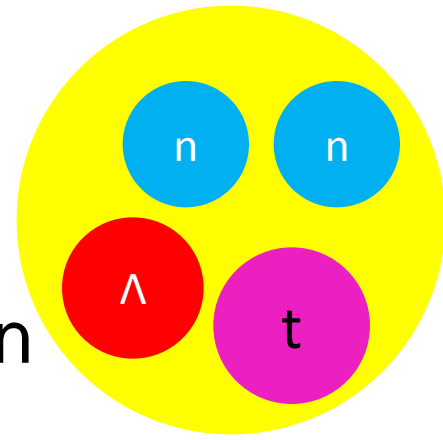
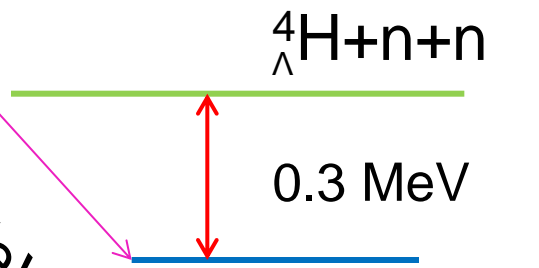


Phys. Rev. Lett. 108, 042051 (2012).

FINUDA experiment



${}^5\text{H}$:super heavy hydrogen



${}^6_\Lambda\text{H}$

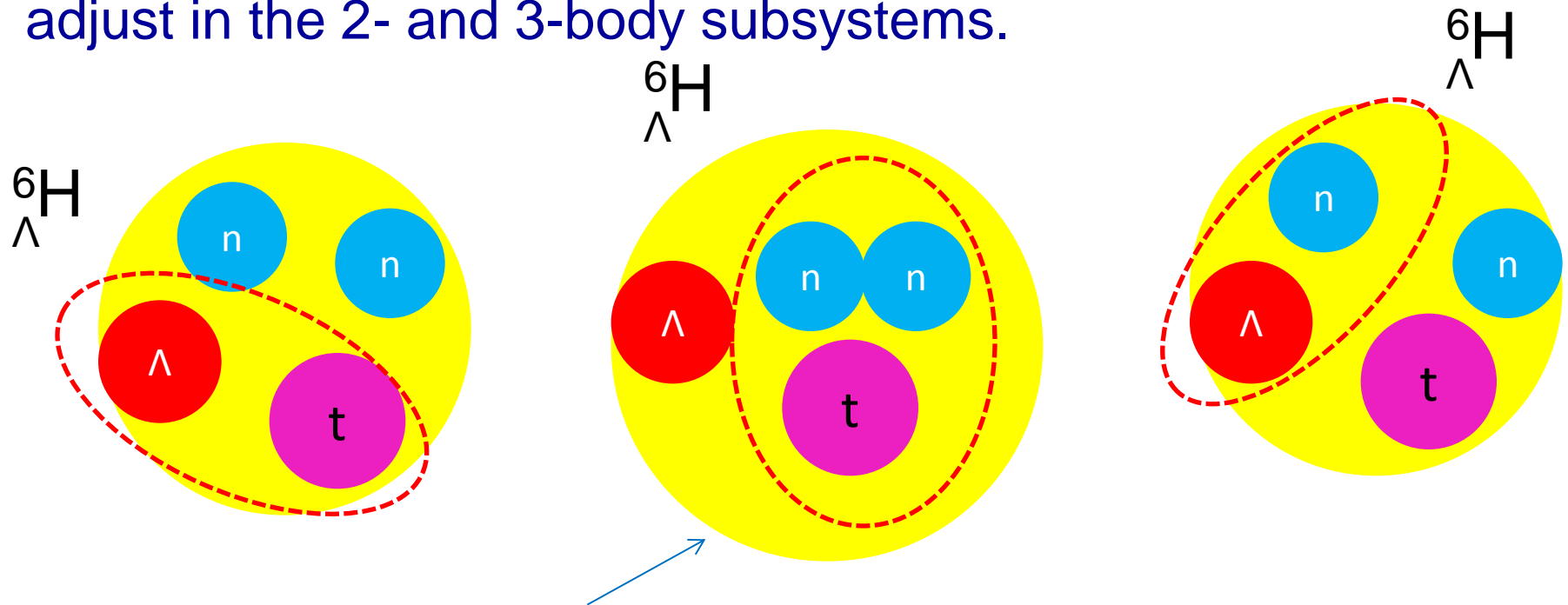
Before experiment, the following authors calculated the binding energies by shell model picture and G-matrix theory.

- (1) R. H. Dalitz and R. Kevi-Setti, Nuovo Cimento 30, 489 (1963).
- (2) L. Majling, Nucl. Phys. A585, 211c (1995).
- (3) Y. Akaishi and T. Yamazaki, Frascati Physics Series Vol. 16 (1999).

Motivating the experimental data, I calculated the binding energy of ${}^6_{\Lambda}\text{H}$ and I shall show you my result.

Before doing full 4-body calculation,
it is important and necessary to reproduce the observed
binding energies of all the sets of subsystems in ${}^6_{\Lambda}\text{H}$.

Namely, All the potential parameters are needed
to
adjust in the 2- and 3-body subsystems.



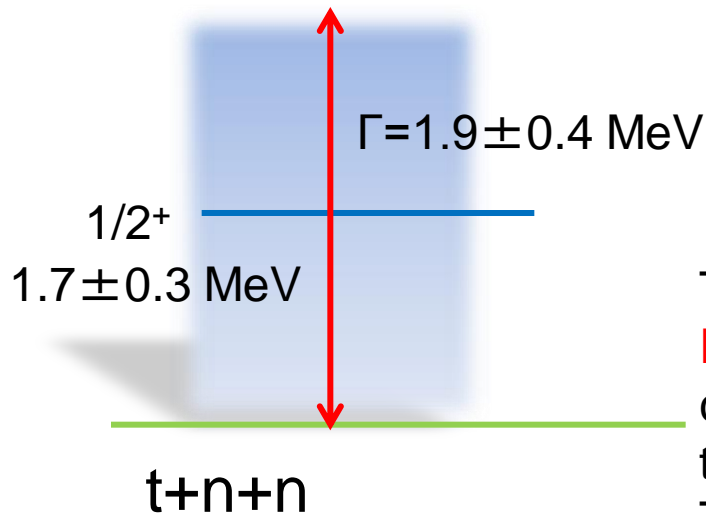
Among the subsystems, it is extremely important to
adjust the energy of ${}^5\text{H}$ core nucleus.

Framework:

To calculate the binding energy of ${}_{\Lambda}^6\text{H}$, it is very important to reproduce the binding energy of the core nucleus ${}^5\text{H}$.

transfer reaction $p({}^6\text{He}, {}^2\text{He}){}^5\text{H}$

A. A. Korcheninnikov, et al. Phys. Rev. Lett. 87 (2001) 092501.

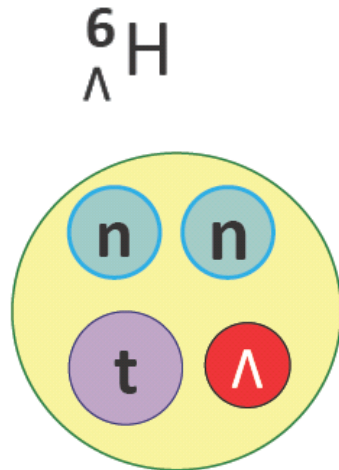
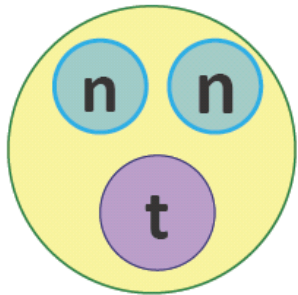
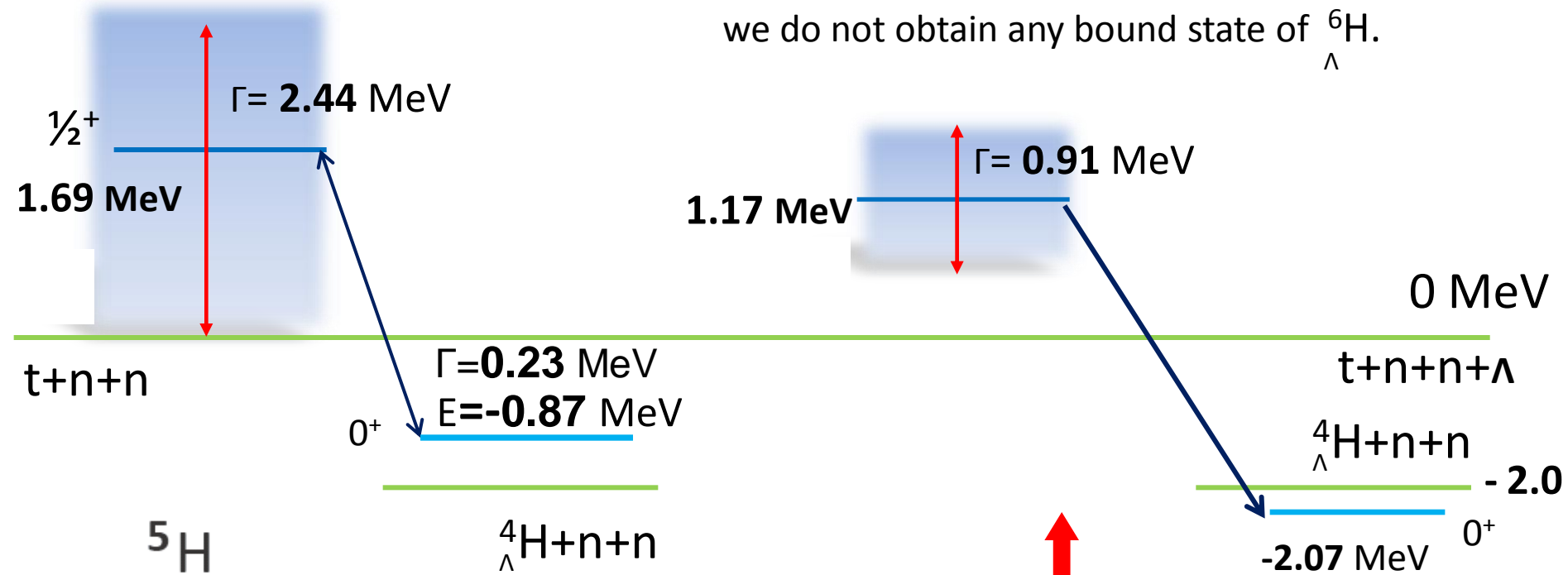


To reproduce the data, for example, [R. De Diego et al, Nucl. Phys. A786 \(2007\), 71.](#) calculated the energy and width of ${}^5\text{H}$ with $t+n+n$ three-body model using complex scaling method. The calculated binding energy for the ground state of ${}^5\text{H}$ is 1.6 MeV with respect to $t+n+n$ threshold and width has 1.5 MeV.

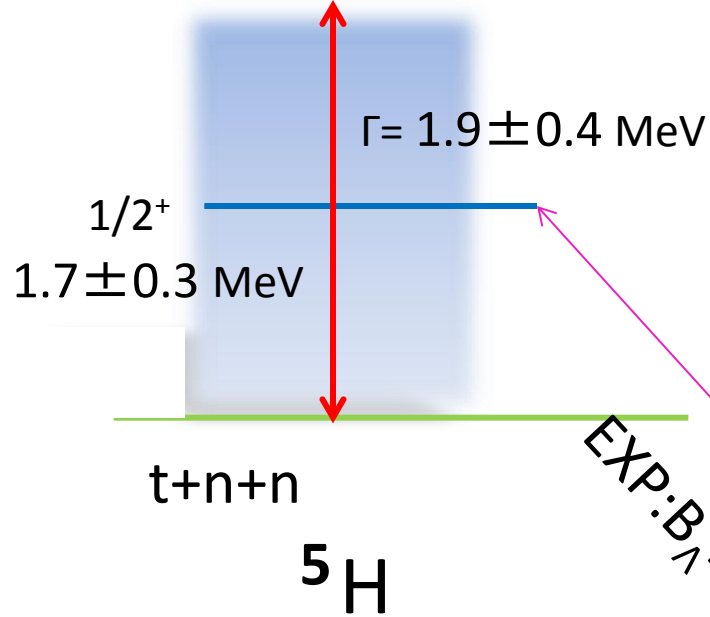
Exp: 1.7 ± 0.3 MeV
 $\Gamma = 1.9 \pm 0.4$ MeV



Even if the potential parameters were tuned so as to reproduce the lowest value of the Exp., $E = 1.4$ MeV, $\Gamma = 1.5$ MeV, we do not obtain any bound state of ${}^6_{\Lambda}\text{H}$.

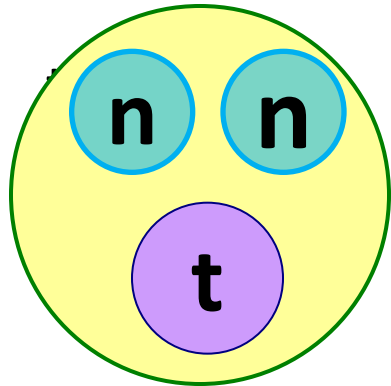
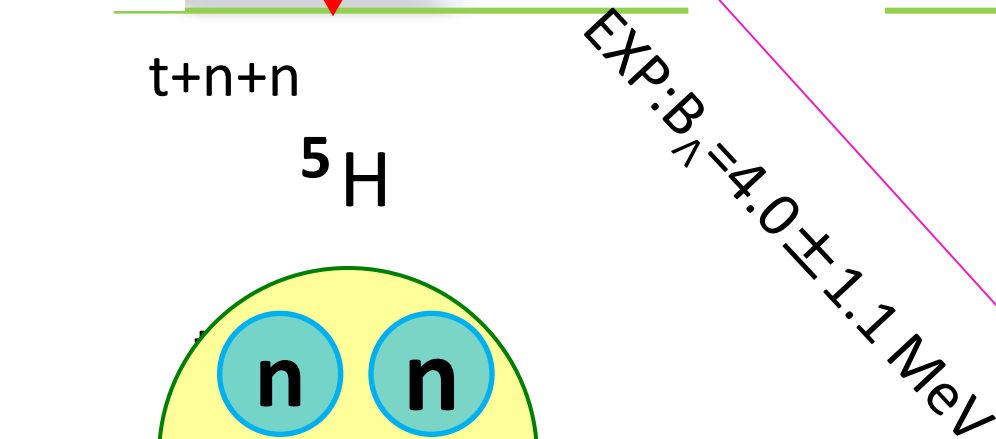


On the contrary, if we tune the potentials to have a bound state in ${}^6_{\Lambda}\text{H}$, then what is the energy and width of ${}^5\text{H}$?

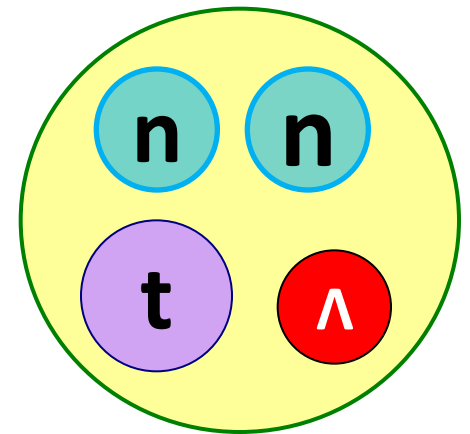


Phys. Rev. Lett. 108, 042051 (2012).

FINUDA experiment



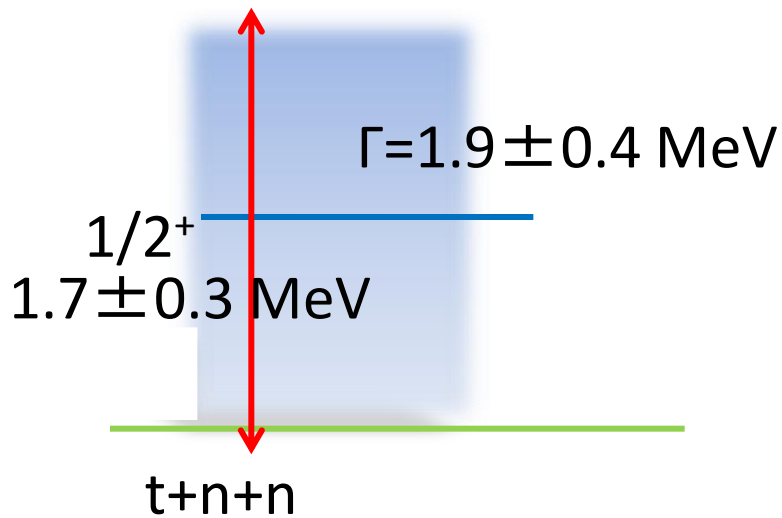
${}^5\text{H}$: super heavy hydrogen



But, FINUDA group provided the bound state of ${}^6_{\Lambda}\text{H}$.

How should I understand the inconsistency between our results and the observed data?

We need more precise data of ${}^5\text{H}$.



A. Korcheninnikov, et al. Phys. Rev. Lett. 87 (2001) 092501.

To get bound state of ${}^6\text{H}$, the energy should be lower than the present data.

It is planned to measure the energy and width of ${}^5\text{H}$ more precisely at RCNP in December in 2014 . We should wait for new data at RCNP.

(E_R, Γ_R) (MeV)

J^π $1/2^+$

^5H (full) (1.57, 1.53)

^5H ($d = 0$) (1.55, 1.35)

Theor. [16] (2.26, 2.93)

Theor. [12] (2.5–3.0, 3–4)

Theor. [13] (3.0–3.2, 1–4)

Theor. [15] (1.59, 2.48)

Exp. [3] ($1.7 \pm 0.3, 1.9 \pm 0.4$) ←

Exp. [8] ($1.8 \pm 0.1, < 0.5$)

Exp. [4] (1.8, 1.3)

Exp. [5] (2, 2.5)

Exp. [6] (3, 6)

Exp. [9] ($5.5 \pm 0.2, 5.4 \pm 0.6$)

We cited this experiment.

However, you have many different decay widths.

width is strongly related to the size of wavefunction.

Then, I hope that

The decay width will be determined at RCNP this year

[3] A.A. Koroshennikov et al., PRL87 (2001) 092501

[8] S.I. Sidorchuk et al., NPA719 (2003) 13

[4] M.S. Golovkov et al. PRC 72 (2005) 064612

[5] G. M. Ter-Akopian et al., Eur. Phys. J A25 (2005) 315.

Search for ${}^6_{\Lambda}\text{H}$ hypernucleus by the ${}^6\text{Li}(\pi^-, K^+)$ reaction at $p_{\pi^-} = 1.2 \text{ GeV}/c$

H. Sugimura^{a,b,*}, M. Agnello^{c,d}, J.K. Ahn^e, S. Ajimura^f, Y. Akazawa^g, N. Amano^a, K. Aoki^h, H.C. Bhangⁱ, N. Chiga^g, M. Endo^j, P. Evtoukhovitch^k, A. Feliciello^d, H. Fujioka^a, T. Fukuda^l, S. Hasegawa^b, S. Hayakawa^j, R. Honda^g, K. Hosomi^g, S.H. Hwang^b, Y. Ichikawa^{a,b}, Y. Igarashi^h, K. Imai^b, N. Ishibashi^j, R. Iwasaki^h, C.W. Jooⁱ, R. Kiuchi^{i,b}, J.K. Lee^e, J.Y. Leeⁱ, K. Matsuda^j, Y. Matsumoto^g, K. Matsuoka^j, K. Miwa^g, Y. Mizoi^l, M. Moritsu^f, T. Nagae^a, S. Nagamiya^b, M. Nakagawa^j, M. Naruki^a, H. Noumi^f, R. Ota^j, B.J. Roy^m, P.K. Saha^b, A. Sakaguchi^j, H. Sako^b, C. Samantaⁿ, V. Samoilov^k, Y. Sasaki^g, S. Sato^b, M. Sekimoto^h, Y. Shimizu^l, T. Shiozaki^g, K. Shirotori^f, T. Soyama^j, T. Takahashi^h, T.N. Takahashi^o, H. Tamura^g, K. Tanabe^g, T. Tanaka^j, K. Tanida^l, A.O. Tokiyasu^f, Z. Tsamalaidze^k, M. Ukai^g, T.O. Yamamoto^g, Y. Yamamoto^g, S.B. Yang^l, K. Yoshida^j,
(J-PARC E10 Collaboration)

arXiv:1310.6104v1 [nucl-ex] 23 Oct 2013

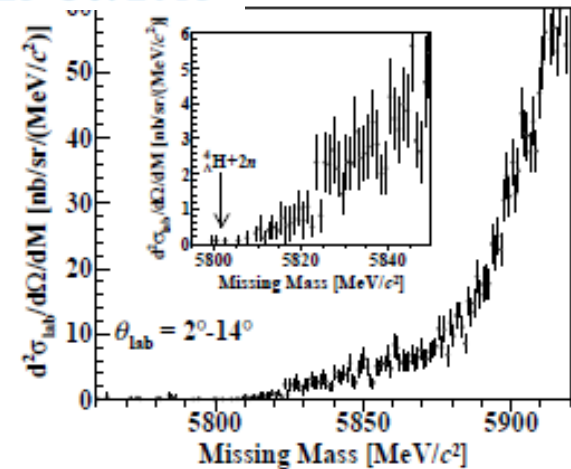
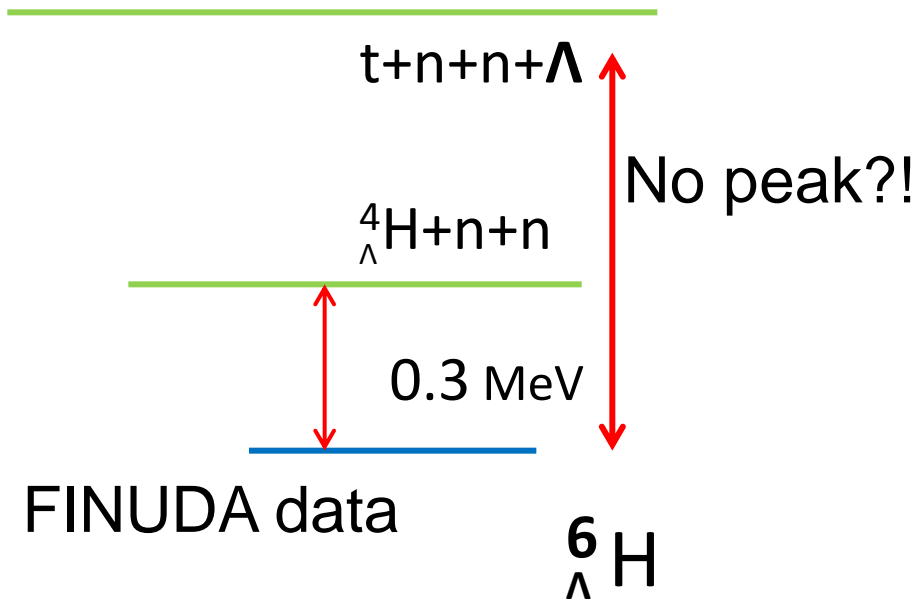
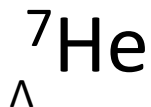
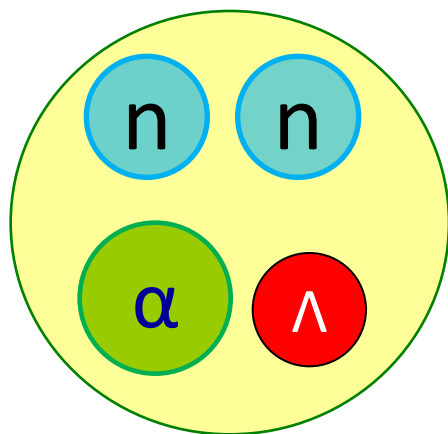


Figure 5: Missing-mass spectrum of the ${}^6\text{Li}(\pi^-, K^+)$ reaction at $1.2 \text{ GeV}/c$. A magnified view around the Λ bound region is shown in the inset. The arrow labeled as ${}^4_{\Lambda}\text{H}+2n$ shows the particle decay threshold (5801.7 MeV/c²).

Theoretically, we might understand by the following reason.
If the state is resonant state, the reaction cross section would be much smaller than that we expect. => I should calculate reaction cross section ${}^6\text{Li}(\pi, K){}^6_{\Lambda}\text{H}$.



To be submitted
in PRC



Resonant states of neutron-rich Λ hypernucleus, ${}^7_{\Lambda}\text{He}$

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¹*Nishina Center for Accelerator-Based Science, Institute for Physical and Chemical Research (RIKEN), Wako 351-0198, Japan*

^{1,2}M. Kamimura

²*Department of Physics, Kyushu University, Fukuoka, 812-8581, Japan*

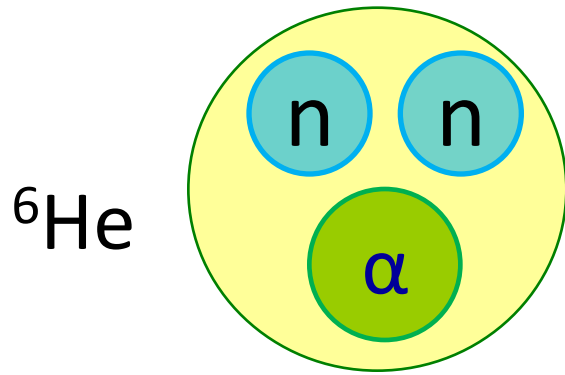
T. Myo

General Education, Faculty of Engineering, Osaka Institute of Technology, Osaka, 535-8585, Japan

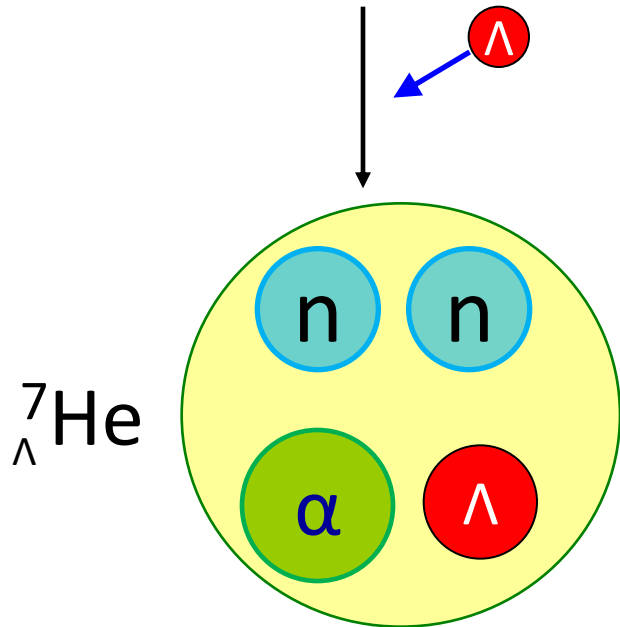
T. Motoba

Laboratory of Physics, Osaka Electro-Communication University, Neyagawa 572-8530, Japan
Yukawa Institute for Theoretical Physics, Kyoto University, Kyoto 606-8317, Japan

The structure of neutron-rich Λ hypernucleus, ${}^7_{\Lambda}\text{He}$ is studied within the framework of $\alpha + \Lambda + n + n$ four-body cluster model. We predict second $3/2^+$ and $5/2^+$ states as narrow resonant states to be 0.03 MeV and 0.07 MeV with width $\Gamma \sim 1$ MeV with respect to $\alpha + \Lambda + n + n$ threshold which correspond to the second 2^+ state of ${}^6\text{He}$ coupled to $0s \Lambda$. By estimation of differential cross section of ${}^7\text{Li}(\gamma, K^+) {}^7_{\Lambda}\text{He}$, there is a possibility to observe these state at JLab in the future. We also calculate second 2^+ state of ${}^6\text{He}$ as resonant state within the framework of $\alpha + n + n$ three-body cluster model. Our result is 2.81 MeV with $\Gamma = 4.63 \text{ MeV}$ with respect to $\alpha + n + n$ threshold, which is inconsistent with the recent SPIRAL data. It is suggested that search experiment at JLab of the second $3/2^+$ and $5/2^+$ states of ${}^7_{\Lambda}\text{He}$ would provide an opportunity to confirm the second 2^+ state of the core nucleus ${}^6\text{He}$.



${}^6\text{He}$: One of the lightest
n-rich nuclei

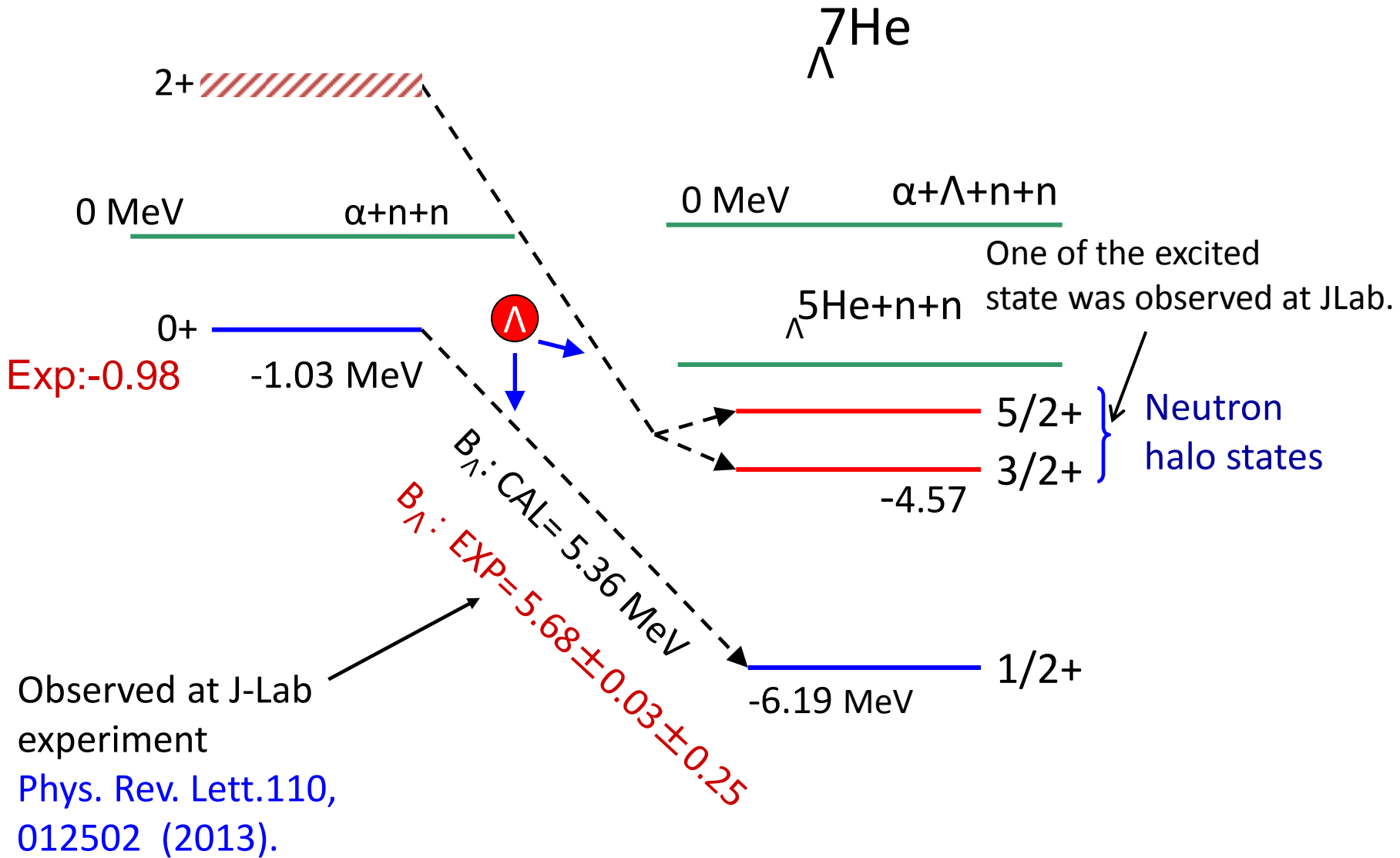


${}^7_{\Lambda}\text{He}$: One of the lightest
n-rich hypernuclei

Observed at JLAB,
Phys. Rev. Lett. 110, 12502 (2013).

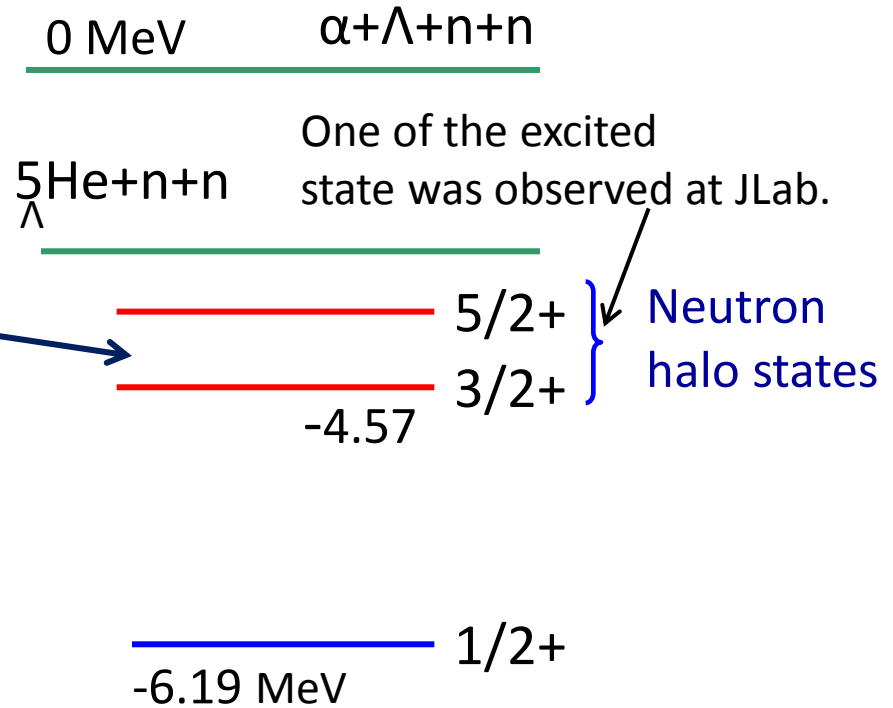
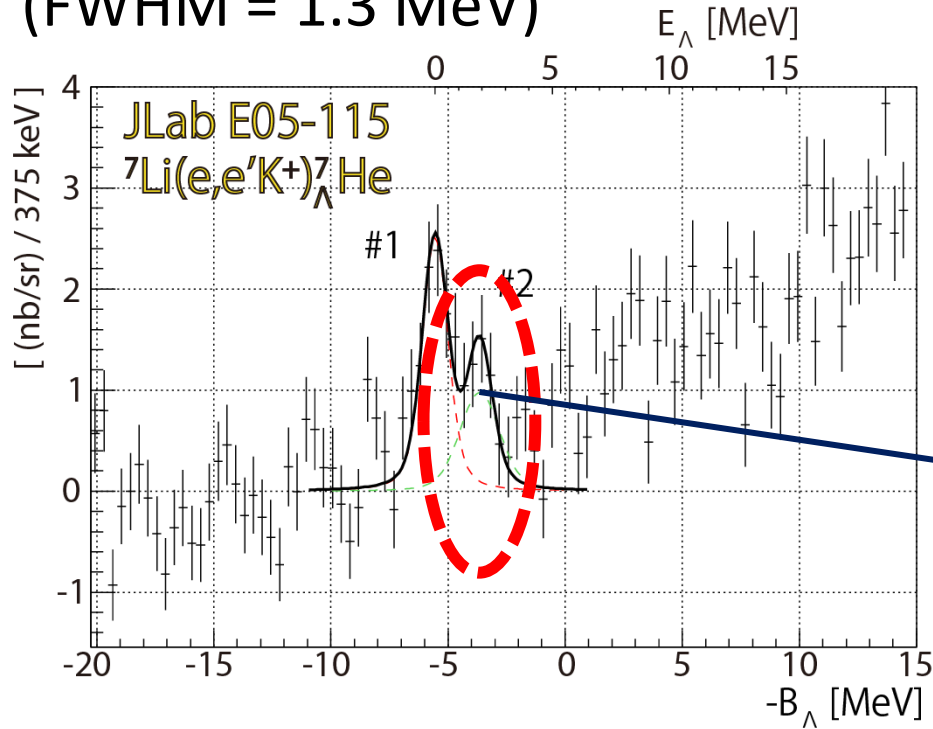
CAL: E. Hiyama et al., PRC 53, 2075 (1996), PRC 80, 054321 (2009)

6He Another interesting issue is to study the excited states of ${}^7_{\Lambda}\text{He}$.



${}^7\text{Li}(e,e'K^+){}^7_{\Lambda}\text{He}$

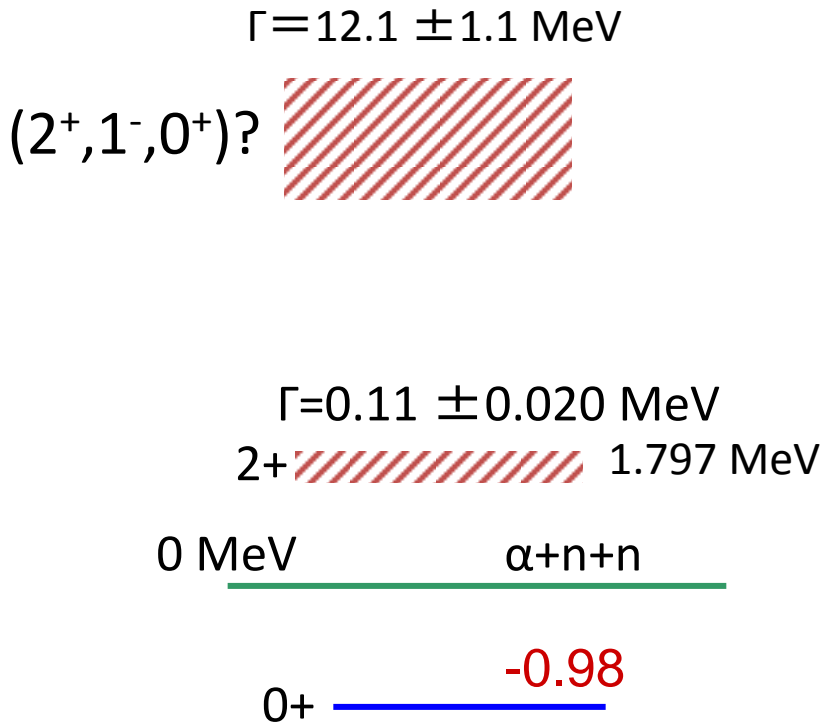
(FWHM = 1.3 MeV)



The calculated energy of the excited state is in good agreement with the data.

Question: In ${}^7\Lambda\text{He}$, do we have any other new states?
If so, what is spin and parity?

First, let us discuss about energy spectra of ${}^6\text{He}$ core nucleus.

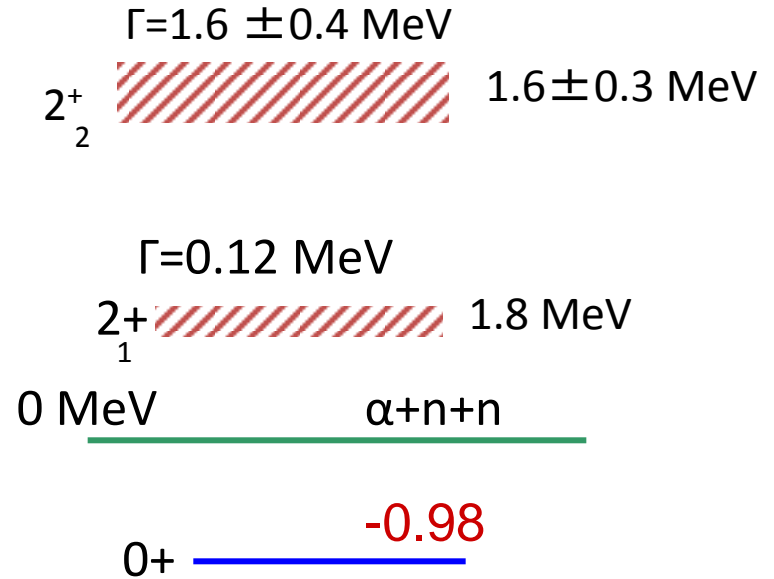


${}^6\text{He}$

Exp.

Data in 2002

Core nucleus



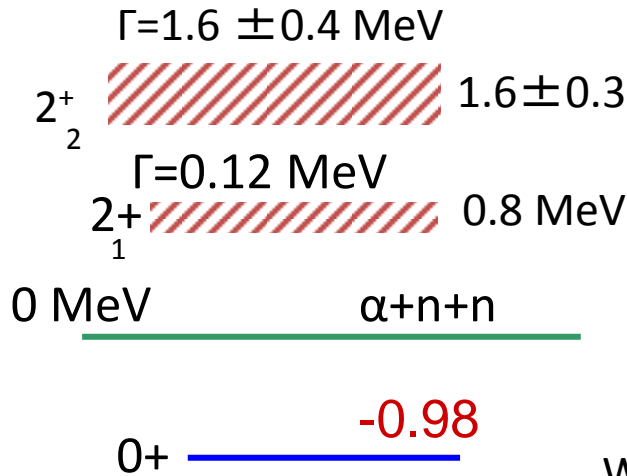
${}^6\text{He}$

Exp.

Data in 2012

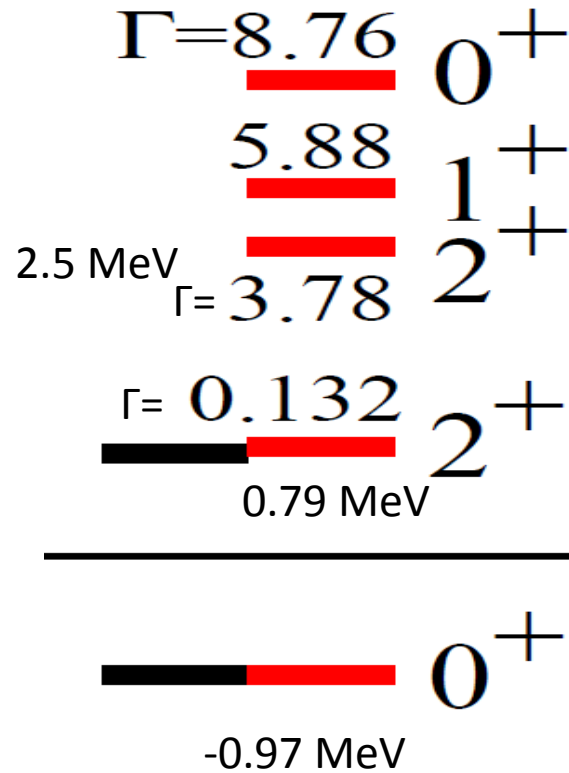
X. Mougeot et al., Phys. Lett. B
718 (2012) 441. p(${}^8\text{He}$, t) ${}^6\text{He}$

How about theoretical result?



Decay with is smaller than the calculated width.

What is my result?



theory

Myo et al., PRC 84, 064306 (2011).

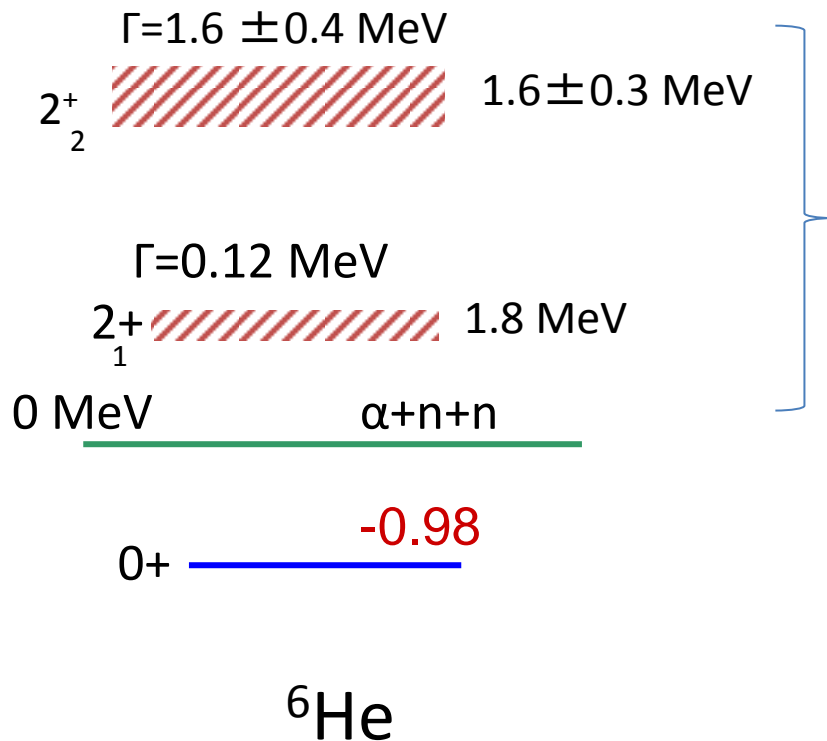
${}^6\text{He}$

Exp.

Data in 2012

X. Mougeot et al., Phys. Lett. B 718 (2012) 441. $p({}^8\text{He}, t){}^6\text{He}$

Question: What are theoretical results?



These are resonant states.

I should obtain energy position and decay width.

To do so, I use complex scaling method which is one of powerful method to get resonant states. I will not explain about this method.

Exp.

Data in 2012

X. Mougeot et al., Phys. Lett. B
718 (2012) 441. $p({}^8\text{He}, t){}^6\text{He}$

The Hamiltonian for ${}^6\text{He}$ is written as

$$H = T + V_{NN} + \sum_{i=1}^2 [V_{\alpha N_i} + V_{\alpha N_i}^{\text{Pauli}}] \quad ,$$

and for ${}^7_{\Lambda}\text{He}$ is written as

$$H = T + V_{NN} + V_{\Lambda\alpha} + \sum_{i=1}^2 [V_{\Lambda N_i} + V_{\alpha N_i} + V_{\alpha N_i}^{\text{Pauli}}] \quad .$$

Complex scaling is defined by the following transformation.

$$U(\theta)f(\mathbf{x}) = \exp\left(i\frac{3}{2}\theta\right)f(\exp(i\theta)\mathbf{x})$$

$$H(\theta) = U(\theta)HU(\theta)^{-1} \quad ,$$

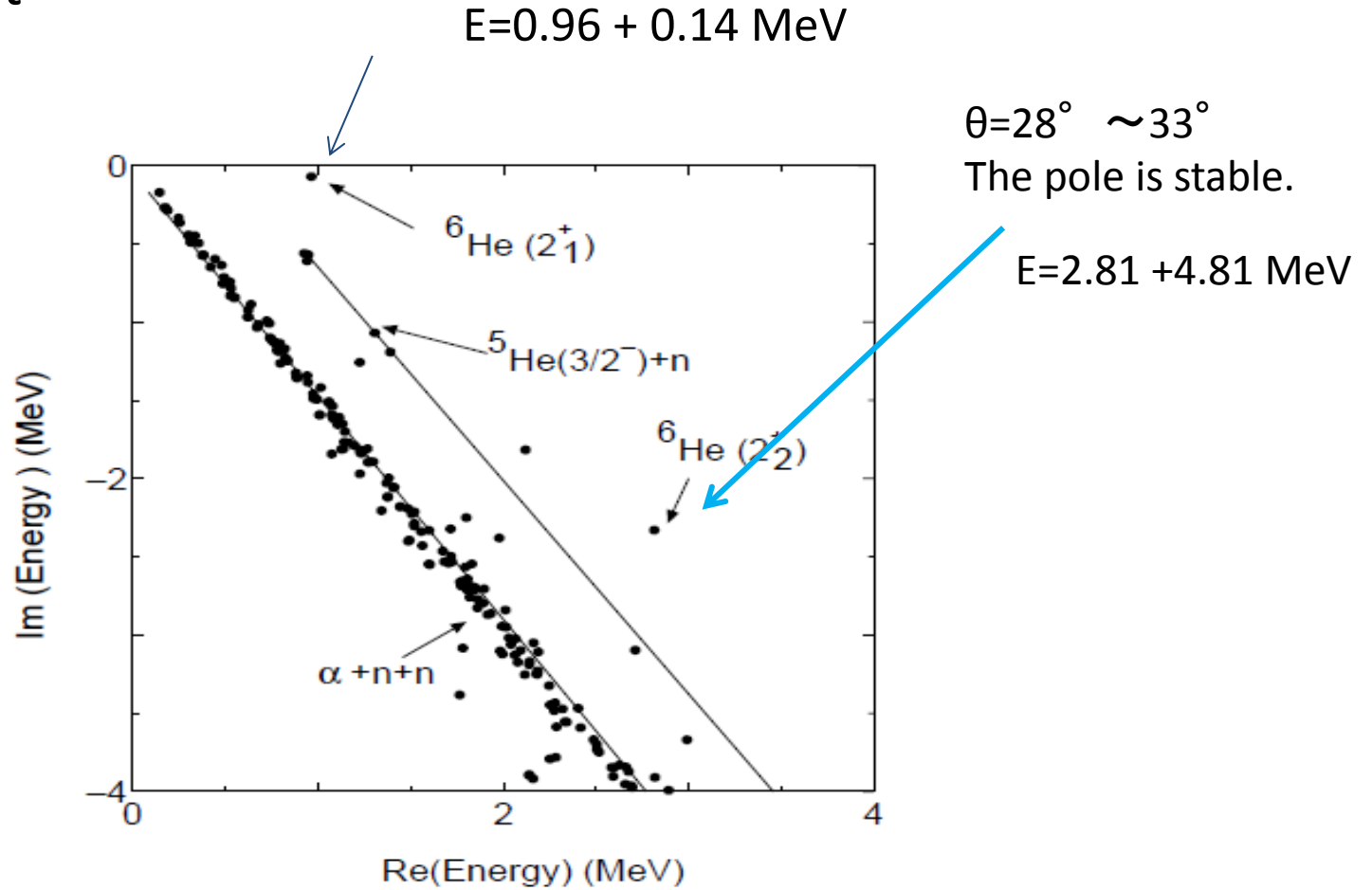
$$|\Psi_{\theta}\rangle = U(\theta)|\Psi\rangle \quad .$$

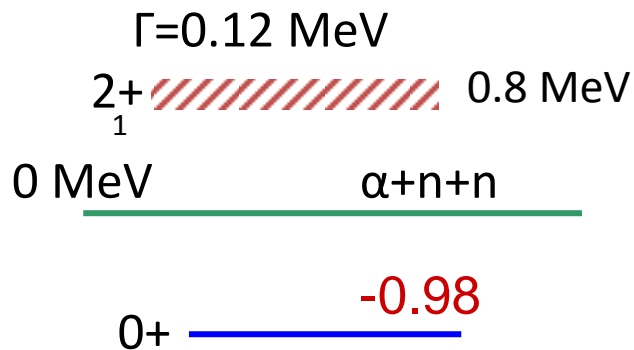
As a result, I should solve this Schroediner equation.

$$H(\theta)|\Psi_{\theta}\rangle = E(\theta)|\Psi_{\theta}\rangle$$

$$E = E_r + i\Gamma/2$$

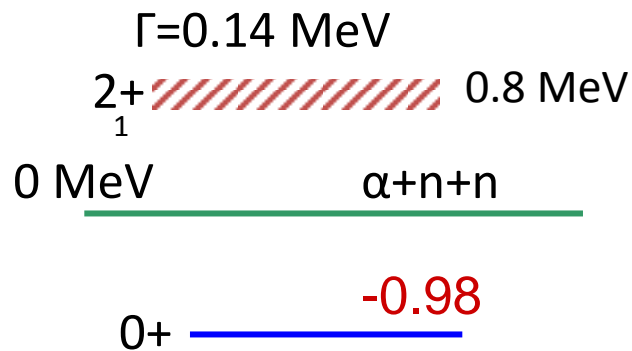
My result





${}^6\text{He}$

Exp.



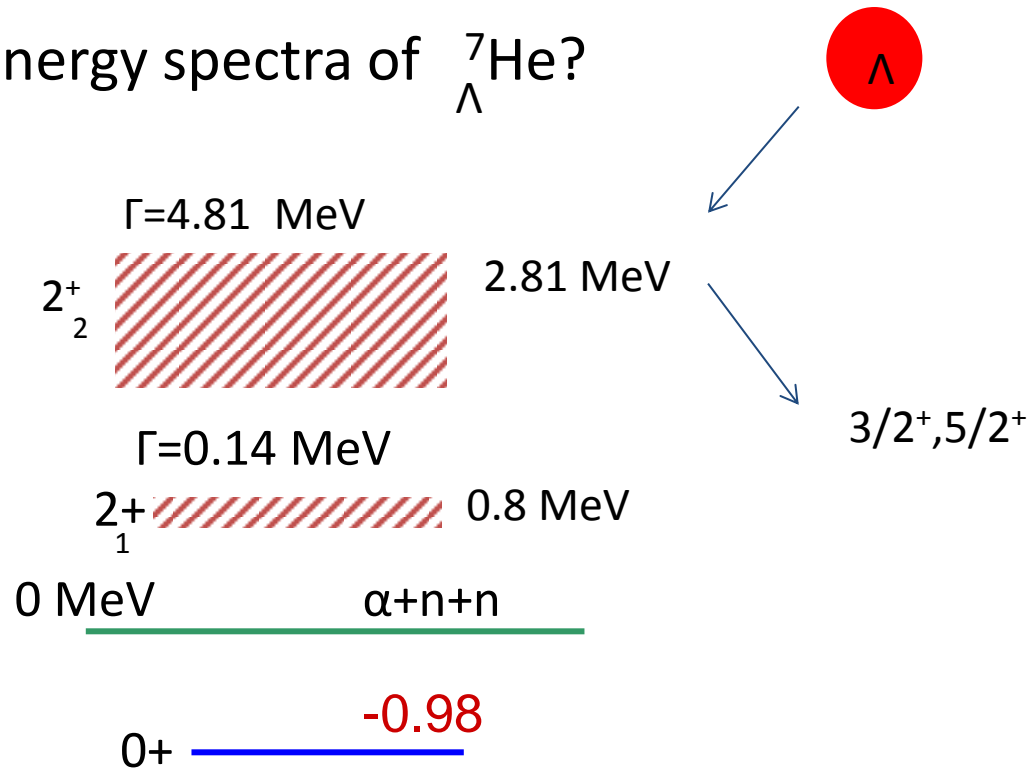
${}^6\text{He}$

Cal.

Data in 2012

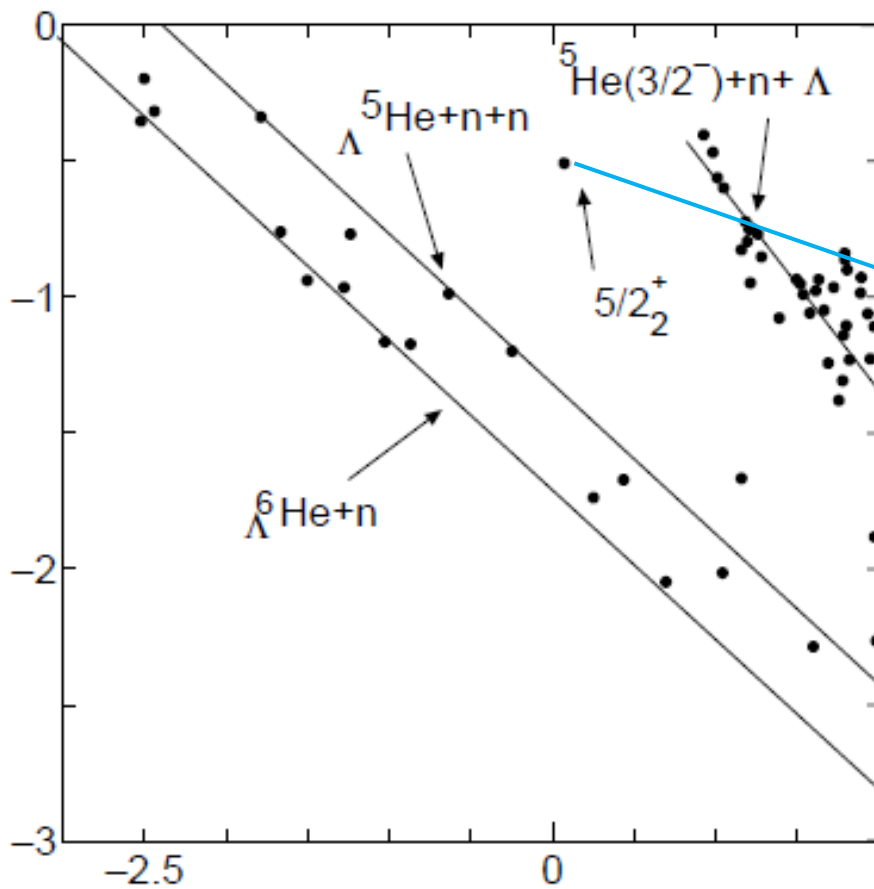
X. Mougeot et al., Phys. Lett. B
 718 (2012) 441. $p({}^8\text{He}, t){}^6\text{He}$

How about energy spectra of ${}^7_{\Lambda}\text{He}$?

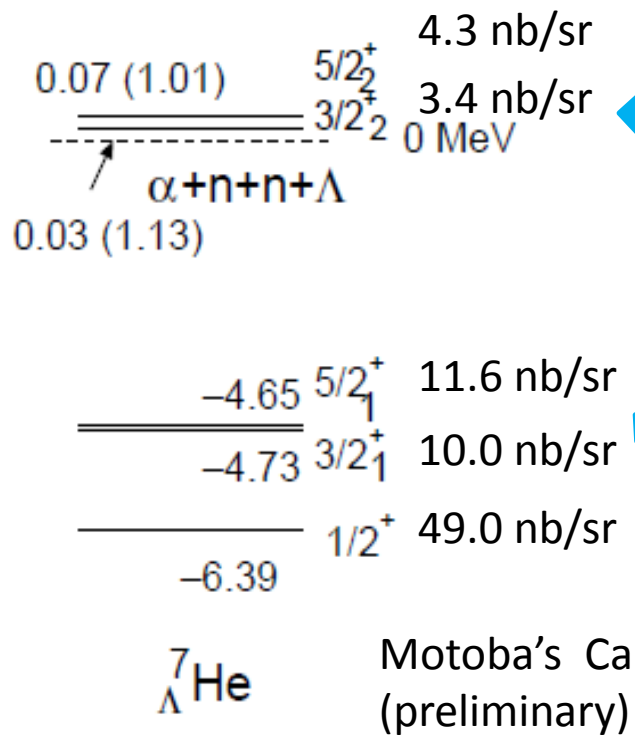
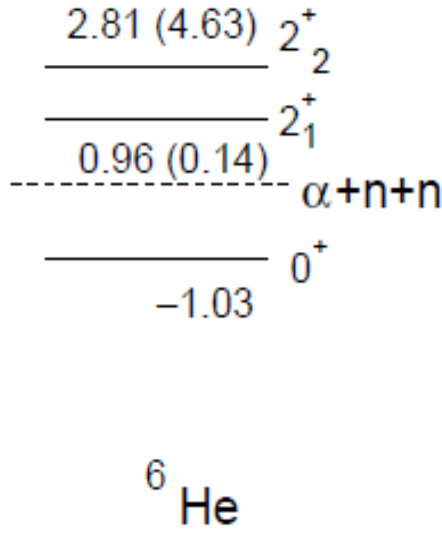


${}^6\text{He}$

Cal.



$E=0.07\text{ MeV}+1.13\text{ MeV}$
The energy is measured
with respect to
 $\alpha+\Lambda+n+n$ threshold.



I propose to experimentalists to observe these states.

40% reduction

I think that
It is necessary to estimate
reaction cross section
 ${}^7\text{Li} (e, e' K^+)$.

Motoba san recently
estimated differential cross
sections for each state.

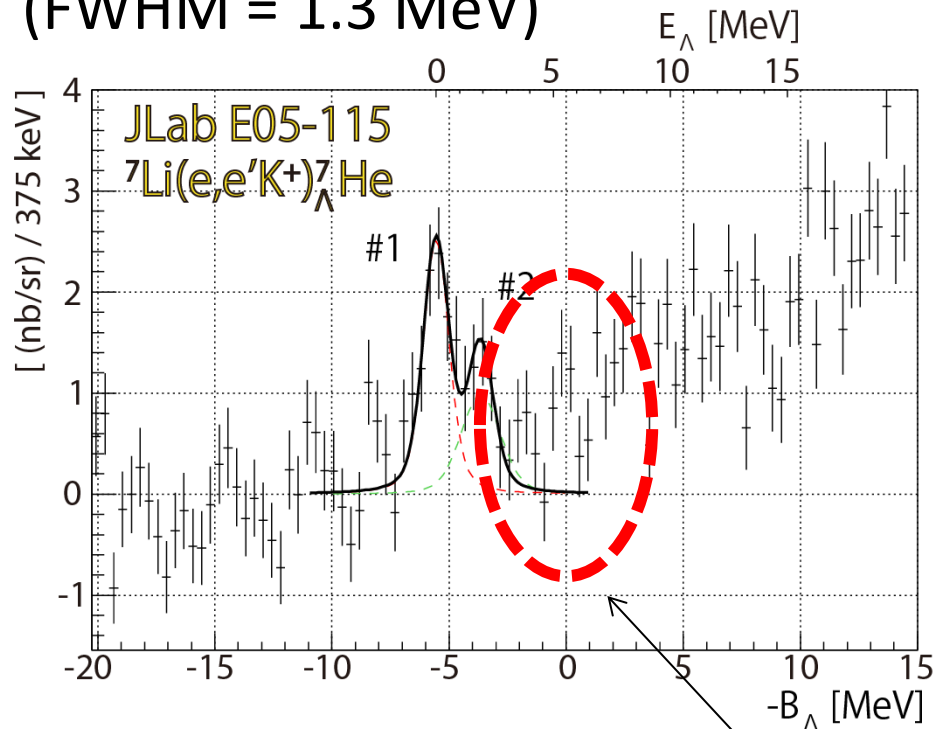
At $E^{\text{lab}}=1.5 \text{ GeV}$ and $\theta=7 \text{ deg}$ (E05-115 experimental kimenatics)

Motoba's Cal.
(preliminary)

${}^7\text{Li}(e,e'K^+){}^7_{\Lambda}\text{He}$

At present, due to poor statics,
It is difficult to have the third peak.
But, I hope that next experiment
at Jlab will observe the third peak.

(FWHM = 1.3 MeV)



Fitting results

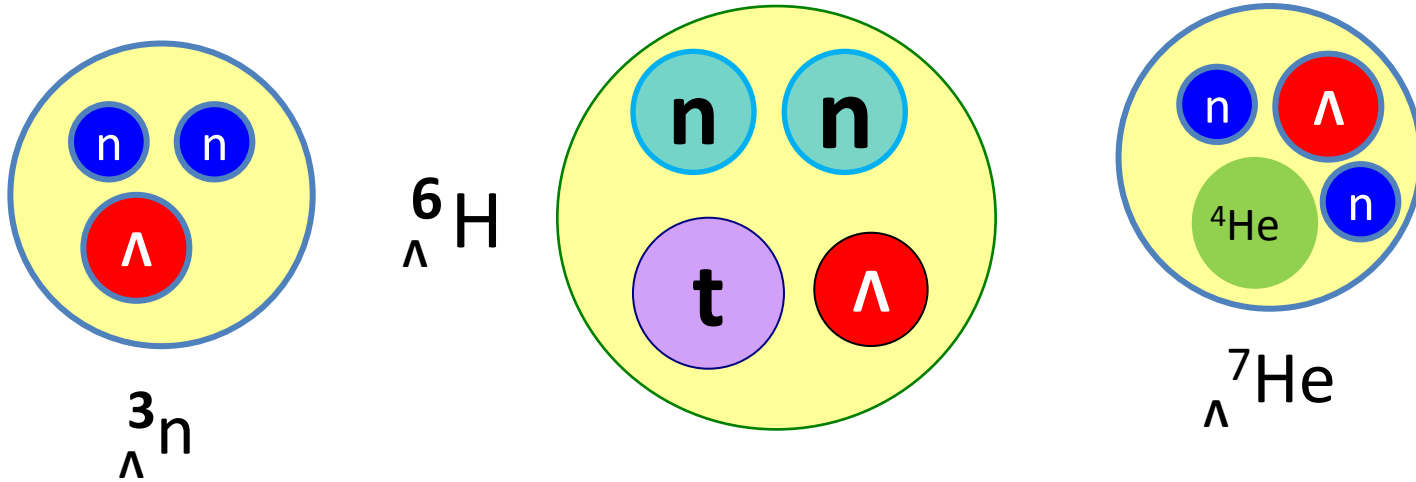
Peak number	State ${}^6\text{He}[J_C] \otimes j^\Lambda$	Number of events	$-B_\Lambda$ [MeV] (E_Λ)	$\left(\frac{d\sigma}{d\Omega_K}\right)_{1^\circ-13^\circ}$ [nb/sr]
1	$1/2^+$ $[0^+; \text{g.s.}] \otimes s_{1/2}^\Lambda$	413 ± 20	$-5.55 \pm 0.10 \pm 0.11$ (0.0)	$10.7 \pm 0.5 \pm 1.7$
2	$3/2^+, 5/2^+$ $[2^+; 1.80] \otimes s_{1/2}^\Lambda$	239 ± 15	$-3.65 \pm 0.20 \pm 0.11$ ($1.90 \pm 0.22 \pm 0.05$)	$6.2 \pm 0.4 \pm 1.0$

Good agreement with my prediction

Third peak???

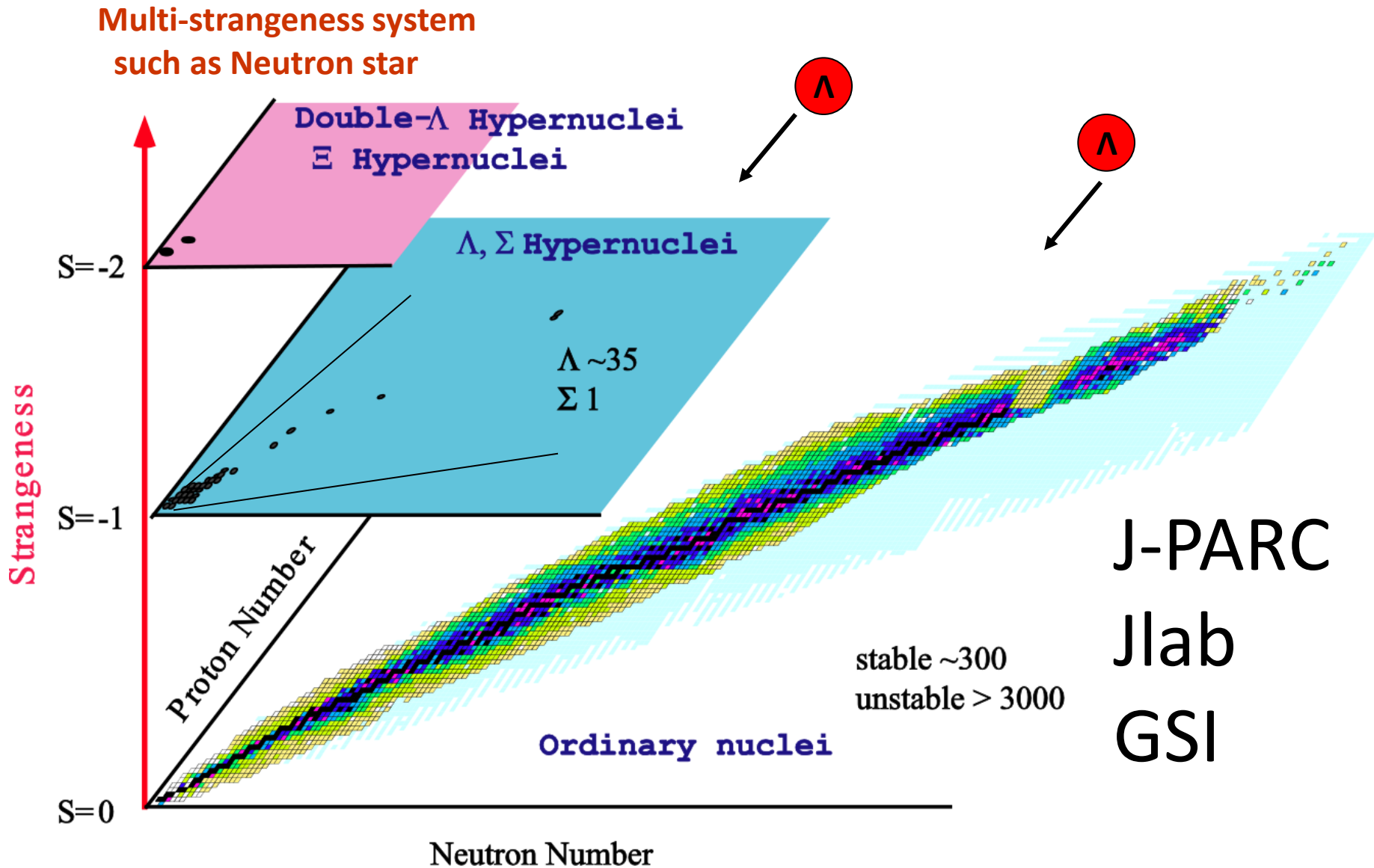
They plan to submit their proposal for ${}^7_{\Lambda}\text{He}$ to JLab next June.

Summary



Neutron-rich Λ hypernuclei

Nuclear chart with strangeness



Thank you!