

# Determining the WIMP mass using the complementarity between direct and indirect searches and the ILC

Andreas Goudelis

Journées Jeunes Chercheurs, 30/11 - 6/12, St Flour, France

Based on N.Bernal, A.G., Y.Mambrini, C.Muñoz,  
Preliminary version: arXiv:0804.1976 [hep-ph]  
Modified version submitted to JCAP

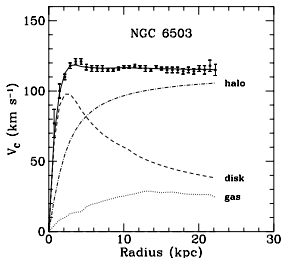
Laboratoire de Physique Théorique - Orsay

# Outline

- 1 Introduction
  - Why Dark Matter
  - WIMP Dark Matter
- 2 DM Detection
  - Detection Methods
  - Direct Detection
  - Indirect Detection
- 3 Direct vs Indirect Detection
- 4 Dark Matter at Colliders
  - The Method
  - Radiative WIMP Production Rate
  - ILC: Results
- 5 Complementarity - Conclusions

# Why Dark Matter?

## Galactic Rotation Curves



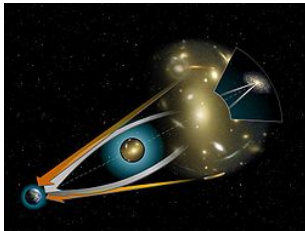
Normally, for  $r > r_{\text{vis}}$  one would expect

$$v(r) = \sqrt{\frac{GM(r)}{r}}$$

instead

$$v(r) \approx \text{const}$$

## Gravitational Lensing

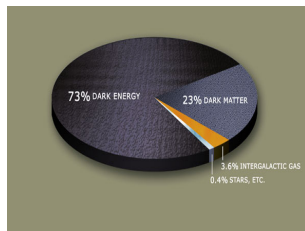


Light bends differently than predicted from GR, if only luminous matter is taken into account.

## And also:

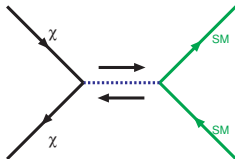
- Primordial Nucleosynthesis
- Large Scale Structure
- Cosmic Microwave Background

At the end of the Day, for  $\Lambda$ CDM



## WIMP DM - Relic Density

Principle of “Thermal Relics”: (The simplest scenario!)



- Begin from a state of thermodynamical equilibrium.
- The universe expands  $\implies$  its temperature falls. SM particles no longer energetic enough to produce  $\chi\chi$  pairs
- $\implies$   $\chi$ 's density falls asymptotically.

A gross estimation of a particle's relic density can be provided by

$$\Omega_{\chi} h^2 \approx \frac{3 \times 10^{-27} \text{cm}^3 \text{s}^{-1}}{\langle \sigma v \rangle}$$

# Weakly Interacting Massive Particles

So:

$$\Omega_\chi \sim \frac{1}{\langle \sigma v \rangle} \sim \frac{m_\chi^2}{g_\chi^4}$$

Substitute

$$(m_\chi, g_\chi) \sim (m_{\text{weak}}, g_{\text{weak}}) \implies \text{Correct relic density!!!}$$

This observation gives rise to the **WIMP hypothesis**.

A number of BSM theories provide very good candidates:

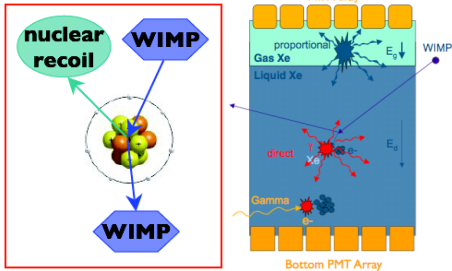
- SUSY: Neutralino, gravitino, right-handed sneutrino
- KKDM: Lightest Kaluza-Klein excitation (UED models)
- Little Higgs Models

A common feature: Impose some kind of discrete symmetry in the Lagrangian to keep the lightest BSM-sector particle stable.

(But also avoid fast proton decay!)

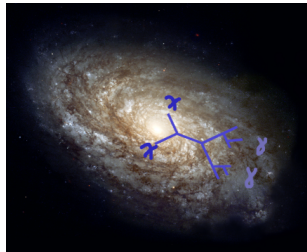
# DM Detection Methods

## Direct Detection



Dark Matter is detected through its collisions with target nuclei of a (typically large) ground-based detector.

## Indirect Detection



DM annihilation into SM particles in the galactic halo. The main detected particles:  $\gamma$ -rays,  $e^+$ , antiprotons as primary or secondary products of WIMP annihilations.

## Direct Detection: The event rate

$$\frac{dN}{dE_r} = \frac{\sigma_{\chi-N} \cdot \rho_0}{2 M_r^2 m_\chi} F(E_r)^2 \int_{v_{\min}(E_r)}^{v_{\text{esc}}} \frac{f(v)}{v} dv$$

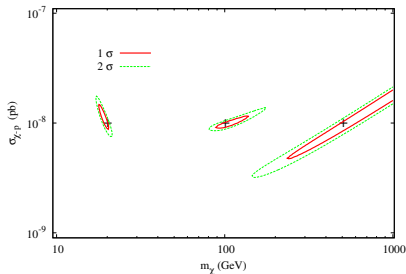
Where:

- $N$ : Number of scatterings ( $\text{s}^{-1}\text{kg}^{-1}$ )
- $E_r$ : Nuclear recoil energy ( $\sim$ few keV)
- $m_\chi$ : WIMP mass
- $M_r = \frac{m_\chi m_N}{m_\chi + m_N}$ : WIMP - Nucleus Reduced Mass
- $\sigma_{\chi-N}$ : WIMP-Nucleus cross-section (Spin-independent coupling)
- $\rho_0$ : Local WIMP density ( $0.3 \text{ GeV cm}^{-3}$ )
- $f(v)$ : WIMP local velocity distribution (Maxwell-Boltzmann)
- $F$ : Nuclear form factor (Woods-Saxon)

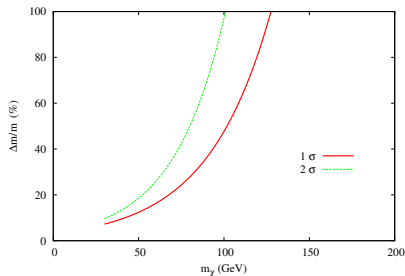
$\Rightarrow$  **Our choice: The XENON 100kg experiment.**

# Direct Detection: Mass Discrimination

## Mass and cross-section discrimination capacity



## Mass Resolution



In fact:

$$m_\chi \ll m_N \Rightarrow \frac{dN}{dE_r} \simeq e^{-E_r/m_\chi^2}$$

$$m_\chi \gg m_N \Rightarrow \frac{dN}{dE_r} \simeq e^{-E_r}$$

⇒ **Better discrimination capacity for small masses**

Here we ignore backgrounds/theoretical uncertainties. For more details, see discussion!



## Indirect Detection: The $\gamma$ -ray flux

$$\Phi_{\gamma}(E_{\gamma}) = 0.94 \cdot 10^{-13} \text{cm}^{-2} \text{sec}^{-1} \text{GeV}^{-1} \text{sr}^{-1} \sum_i Br_i \frac{dN_{\gamma}^i}{dE_{\gamma}} \\ \times \left( \frac{\langle \sigma v \rangle}{10^{-29} \text{cm}^3 \text{sec}^{-1}} \right) \left( \frac{100 \text{GeV}}{m_{\chi}} \right)^2 \bar{J}(\Delta\Omega) \Delta\Omega$$

Where:

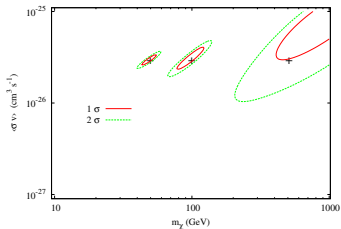
- $Br_i$ : Branching Ratio of annihilation into  $i$ -th SM particle
- $dN_{\gamma}^i/dE_{\gamma}$ : Functions describing SM particles' decays into  $\gamma$ -rays (PYTHIA + fit)
- $\langle \sigma v \rangle$ : Total WIMP self-annihilation cross-section ( $\approx 3 \cdot 10^{-26} \text{cm}^3 \text{sec}^{-1}$ )
- $\bar{J}$ : Astrophysical factor: Depends on DM distribution.

	$a$ (kpc)	$\alpha$	$\beta$	$\gamma$	$\bar{J}(4 \cdot 10^{-3} \text{sr})$
NFW	20	1	3	1	$5.859 \cdot 10^2$
NFW <sub>c</sub>	20	0.8	2.7	1.45	$3.254 \cdot 10^4$
Moore et al.	28	1.5	3	1.5	$2.574 \cdot 10^4$
Moore <sub>c</sub>	28	0.8	2.7	1.65	$3.075 \cdot 10^5$

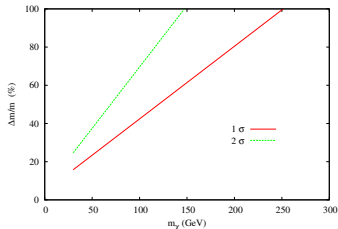
$\Rightarrow$  Our choice: The GLAST experiment

## Indirect Detection: Mass Discrimination

### Mass and cross-section discrimination capacity for a NFW halo profile



### Mass Resolution (95% C.L.)

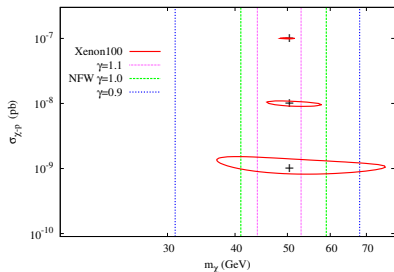


- Again, better resolution for smaller masses (due to strong differences in the spectrum form in the [1, 300]GeV region!).
- Strong dependence on the halo profile.
- No clumpiness included (factor of  $\sim 2 - 10$ )

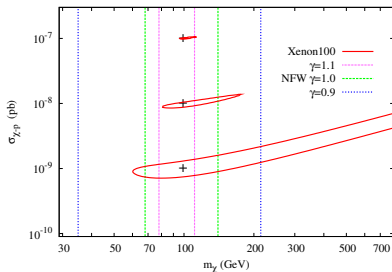
Interesting theoretical/experimental uncertainties, also left for discussion!

## Direct vs Indirect Detection

Example for  $m_\chi = 50\text{GeV}$



Example for  $m_\chi = 100\text{GeV}$



- Comparable precision  $\Rightarrow$  Experiments complementary for low/intermediate masses.
- For higher masses, uncertainties become more important.
- Complementarity more obvious for not too optimistic astrophysical considerations and  $\sigma_{\chi-p}$  cross-sections.

## ILC: The Method

**The General Idea:** Birkedal, Matchev, Perelstein, arXiv:hep-ph/0403004

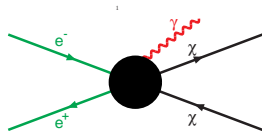
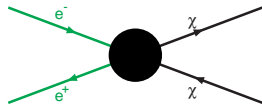
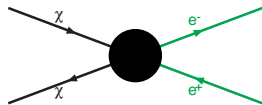
**WIMP Pair - Annihilation (Galaxy - WMAP)**

↓ (Detailed Balancing)

**WIMP Pair - Production (Colliders - Invisible)**

↓ (Collinear Approximation)

**Radiative WIMP Production (Colliders - Visible!)**



## ILC: Radiative WIMP Production Rate

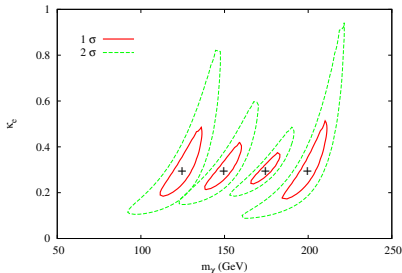
$$\frac{d\sigma(e^+e^- \rightarrow 2\chi + \gamma)}{dx d\cos\theta} \approx \frac{\alpha\kappa_e\sigma_{an}}{16\pi} \frac{1+(1-x)^2}{x} \frac{1}{\sin^2\theta} 2^{2J_0} \times (2S_\chi + 1)^2 \left(1 - \frac{4m_\chi^2}{(1-x)s}\right)^{1/2+J_0}$$

Where:

- $x = 2E_\gamma/\sqrt{s}$
- $\theta$ : Photon emission angle
- $\sigma_{an}$ : Total annihilation cross-section (WMAP) ( $\sim 7\text{pb}$ )
- $J_0$ : Dominant (s- or t-) annihilation channel
- $S_\chi$ : WIMP's spin
- $\kappa_e = \sigma_e^{(J_0)}/\sigma_{an}$ : Annihilation fraction into  $e^+e^-$  pairs.

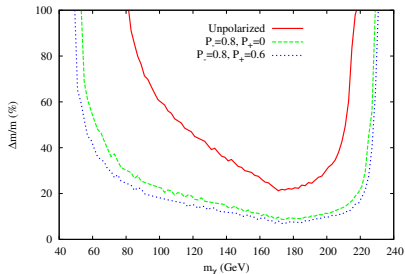
## ILC: Mass Discrimination

### WIMP mass - annihilation fraction discrimination capacity



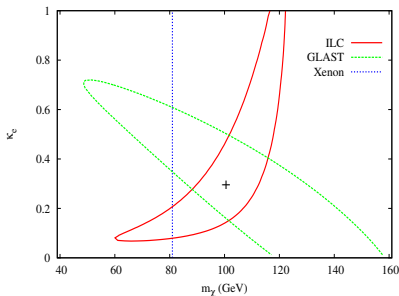
(500GeV Unpolarized beams,  $500\text{fb}^{-1}$  integrated luminosity)

### Relative error in WIMP's mass discrimination



- Discrimination capacity peaks significantly for  $m_\chi = 175\text{GeV}$  (optimal combination of uncut spectrum - phase space).
- Significant improvement in mass resolution for polarized beams.

## DM Experiments/ILC complementarity



An example at 95% CL:

- $m_\chi = 100\text{GeV}$
- 3 years of exposure,
- $\sigma_{\chi-p} = 10^{-8}\text{ pb}$
- NFW profile and a
- 500 GeV unpolarized linear collider with an integrated luminosity of  $500\text{fb}^{-1}$

$m_\chi$	XENON	GLAST	ILC
50 GeV	-5/ + 7 GeV	$\pm 10$ GeV	-
100 GeV	-19/ + 75 GeV	-33/ + 39 GeV	-40/ + 20 GeV
175 GeV	-65/ GeV	-125 GeV	-20/ + 15 GeV
500 GeV	-	-	-

## Summarizing...

- We presented a simple way to exploit simultaneously different kinds of experiments to extract **model-independent** information on WIMP Dark Matter.
- For quite reasonable (i.e. not too optimistic) considerations on the WIMP-nucleus scattering cross-section and the DM halo profile we saw that different kinds of experiments can act highly complementary:
  - The precision is comparable.
  - Possibility to cover different regions in the parameter space.

### ... in preparation:

- Can **PAMELA/ATIC** observations come in terms with **SUSY** models?
- And on a totally different subject:  **$Z'$  at the LHC**





Merci !!!



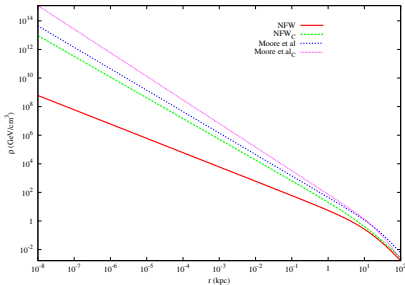
... to use in emergency ...

# Halo Profiles

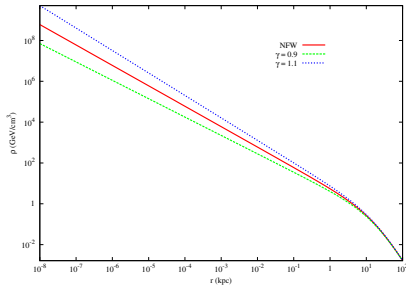
The most usual parametrization:

$$\rho(r) = \frac{\rho_0 [1 + (R_0/a)^\alpha]^{(\beta-\gamma)/\alpha}}{(r/R_0)^\gamma [1 + (r/a)^\alpha]^{(\beta-\gamma)/\alpha}}$$

Some well motivated profiles

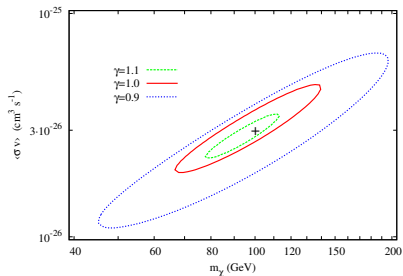


Fun with  $\gamma$ !!!



## Halo Profiles: Influence on observations

### More fun with $\gamma$ !!!



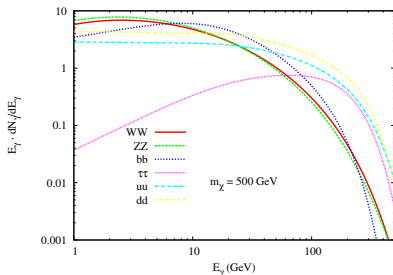
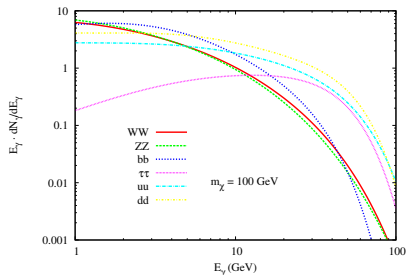
- Among the most important uncertainties: Flux can be enhanced/suppressed by orders of magnitude!
- Estimations based on N-body simulations. Open question: role of baryons?
- Observations seem to favour rather small  $\gamma$  values ( $\gamma \leq 1$ )

## Spectral Functions

PYTHIA result fit performed through functions of the form:

$$\frac{dN_{\gamma}^i}{dx} = \exp[F_i(\ln(x))]$$

with  $x = E_{\gamma}/m_{\chi}$  and  $F$  being 7th order polynomial functions.



- The  $\tau$  spectrum has a characteristic hard form, other leptons have zero contribution.

## Some Points on the ILC Treatment

- The detailed balancing equation:

$$\frac{\sigma(\chi + \chi \rightarrow X_i + \bar{X}_i)}{\sigma(X_i + \bar{X}_i \rightarrow \chi + \chi)} = 2 \frac{v_X^2 (2S_X + 1)^2}{v_\chi^2 (2S_\chi + 1)^2}$$

We can expand the total thermally averaged CS:

$$\sigma_i v = \sum_{J=0}^{\infty} \sigma_i^{(J)} v^{2J} \xrightarrow{v \ll c} \sigma_{an} = \sum_i \sigma_i^{(J_0)}$$

For soft/collinear photons:

$$\frac{d\sigma(e^+ e^- \rightarrow 2\chi + \gamma)}{dx d\cos\theta} \approx \mathcal{F}(x, \cos\theta) \tilde{\sigma}(e^+ e^- \rightarrow 2\chi)$$

## Form Factor and Stuff...

- Woods-Saxon form factor:

$$F(E_r) = \frac{3j_1(qR_1)}{qR_1} e^{-(qs)^2}$$

- WIMP-Nucleus and WIMP-proton CS:

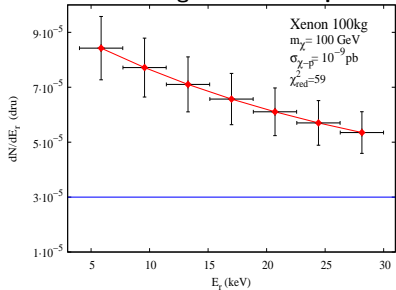
$$\sigma_{\chi-N} = \sigma_{\chi-p} (Am_r/M_r)^2$$

where

$$M_r = \frac{m_\chi m_p}{m_\chi + m_p}$$
$$m_r = \frac{m_\chi m_N}{m_\chi + m_N}$$

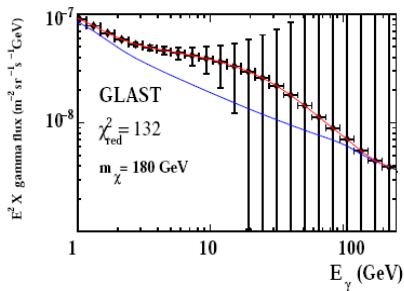
## Signal Examples

**XENON 100kg event rate expectation:**



(7 energy bins [4.5, 26.9] keV)

**GLAST  $\gamma$ -ray flux expectation:**

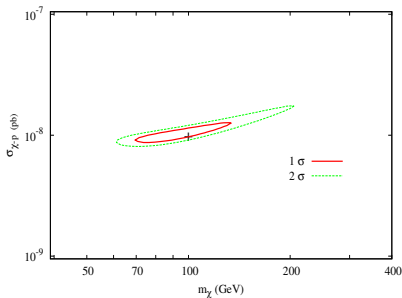


An NFW halo profile has been supposed.

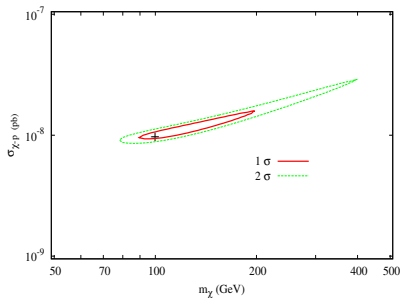


## Direct Detection: Background Uncertainties

Constant bkg equal to maximal signal value



Exponential bkg that mimics signal

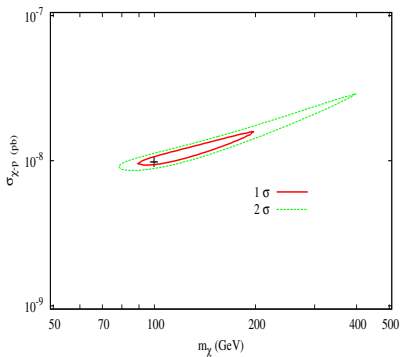


- Good knowledge of backgrounds is essential!!!
- Experiments claim to be practically background-free...

## Direct Detection: Uncertainties in velocity distribution

The general form:

$$f(v_\chi) d^3 v_\chi = \frac{1}{(v_\chi^0)^3 \pi^{3/2}} e^{-(v_\chi/v_\chi^0)^2} d^3 v_\chi$$

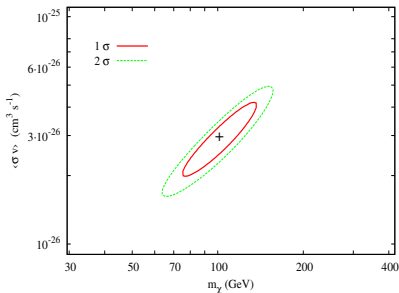


## Indirect Detection: Background Uncertainties

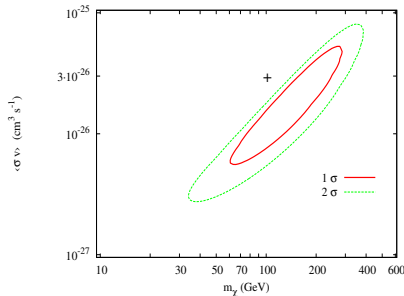
The main background uncertainty at low energies: **EGRET**

- Uncertainties in the spectrum overall normalisation
- Uncertainties in the power-law spectral index

Varying the normalisation



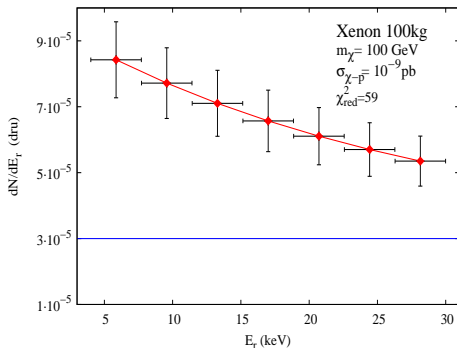
Varying the spectral index



**!!! Uncertainties important: At low energies, maximal signal statistics !!!**

## Direct Detection: The XENON experiment

- Situated at the Gran Sasso NL, Italy
- Currently: 15kg of liquid Xenon. Goal: 1T. Simultaneous measurement of scintillation and ionization.



## Indirect Detection: The GLAST experiment

### Generalities...

- Detects  $\gamma$ -rays coming from DM annihilations in the GC.
- Scheduled for launch in May 2008 for a 5-year mission.
- Will perform an all-sky survey in the energy range [1,300]GeV.
- Effective Area:  $\sim 10^4 \text{cm}^2$ , Angular Resolution:  $0.1^0 \times 0.1^0$ .
- Will examine the inner  $\sim 7\text{pc}$  of the Milky Way.

### GLAST's Background

- Diffuse  $\gamma$ -ray measurements from HESS.
- HESS point-source ( $\sim \text{Sgr A}^*$ ,  $E_\gamma \geq 160\text{GeV}$ )  
→ Possibly related to some astrophysical accelerator.
- HESS might be underestimating the low-energy background from the GC.  
(Zaharijas and Hooper, arXiv:astro-ph/0603540)
- EGRET point source (Near the galactic center)  
→ Difficult to interpret as coming from DM annihilation.  
(Dodelson, Hooper and Serpico, arXiv:0711.4621[astro-ph])

Our choice: Interpolation between HESS and EGRET data.

## ILC: Subtleties

Approach valid for soft/collinear photons → **Undetectable!**

- Nevertheless, it gives satisfactory results outside the soft/collinear region for **nonrelativistic** WIMPs.

To ensure the WIMPs' non-relativistic nature we impose the following kinematical cuts:

$$\frac{\sqrt{s}}{2} \left( 1 - \frac{8m_\chi^2}{s} \right) \leq E_\gamma \leq \frac{\sqrt{s}}{2} \left( 1 - \frac{4m_\chi^2}{s} \right).$$

- Main background process: Radiative neutrino production (CalcHEP 2.5).

## Discrimination Method

Analysis based on extended likelihood function:

$$L = \frac{(N_{th}^{scan})^{N_{Exp}}}{N_{Exp}!} \exp(-N_{th}^{scan}) \prod_{i=1}^{N_{Exp}} f(E; m_{\chi}, \sigma_{\chi-p})$$

- Calculate the theoretical number of events,  $N_{th}$ , for the input mass and cross-section.
- Draw an “experimental” nb of events,  $N_{Exp}$ , from a Poisson distribution.
- Scan the  $(m_{\chi}, \sigma_{\chi-N})$  parameter space and find the experiment’s estimation, taking into account the theoretical nb of events of every point in the PS,  $N_{th}^{scan}$ .
- Generate a large number of experiments, repeat the procedure, pick the one that averages all experiments’ results.
- From this experiment, plot  $(m_{\chi}, \sigma_{\chi-N})$  non-discrimination regions.

⇒ This method allows to account for random deviations from the expected number of events.