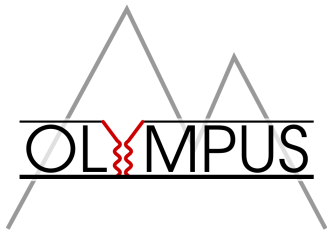


Overview of the Radiative Corrections Plan for



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for the Olympus Collaboration

October 7, 2013

IPN Orsay

Context for this talk

- OLYMPUS aims to measure a radiative correction to elastic ep scattering
 - Hard two photon exchange (TPE) contribution
 - Could solve G_E^p/G_M^p measurement discrepancy

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- Need to ensure all experiments are measuring the same thing
- Need to measure a quantity that's easy to apply to the question of the form factor discrepancy

Corrections to the elastic cross section

$$\frac{d\sigma}{d\Omega} = z^2 \left| \begin{array}{c} \text{tree-level diagram} \end{array} \right|^2$$

Interference terms of order α^3

$$+ 2z^2 \operatorname{Re} \left[\begin{array}{c} \text{tree-level diagram}^\dagger \end{array} \left(\begin{array}{c} \text{tree-level diagram} \\ \text{tree-level diagram with loop} \\ \text{tree-level diagram with self-energy} \\ \text{tree-level diagram with vertex correction} \end{array} \right) \right]$$

$$+ 2z^3 \operatorname{Re} \left[\begin{array}{c} \text{tree-level diagram}^\dagger \end{array} \left(\begin{array}{c} \text{tree-level diagram with exchange} \\ \text{tree-level diagram with exchange} \end{array} \right) \right]$$

$$+ 2z^4 \operatorname{Re} \left[\begin{array}{c} \text{tree-level diagram}^\dagger \end{array} \left(\begin{array}{c} \text{tree-level diagram with exchange} \\ \text{tree-level diagram with exchange} \\ \text{tree-level diagram with exchange} \end{array} \right) \right]$$

$$+ \mathcal{O}(\alpha^4)$$

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 \frac{d\sigma}{d\Omega} = & z^2 \left| \begin{array}{c} \text{tree-level diagram} \end{array} \right|^2 \\
 & + 2z^2 \operatorname{Re} \left[\begin{array}{c} \text{tree-level diagram}^\dagger \end{array} \left(\begin{array}{c} \text{self-energy} + \text{vertex correction} + \text{box diagram} + \text{triangle diagram} \end{array} \right) \right] \\
 & + 2z^3 \operatorname{Re} \left[\begin{array}{c} \text{tree-level diagram}^\dagger \end{array} \left(\begin{array}{c} \text{box diagram} + \text{triangle diagram} \end{array} \right) \right] \\
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Only TPE changes sign for e^+ vs e^-

However, almost all terms are IR divergent...

Corrections from inelastic (bremsstrahlung) processes

- Cancel exactly with divergences from the elastic cross section

$$\begin{aligned}
 \frac{d\sigma_{\text{inel}}}{d\Omega} = & z^2 \left| \begin{array}{c} \text{diagram 1} \\ + \\ \text{diagram 2} \end{array} \right|^2 \\
 & + 2z^3 \text{Re} \left[\left(\begin{array}{c} \text{diagram 1} \\ + \\ \text{diagram 2} \end{array} \right)^\dagger \left(\begin{array}{c} \text{diagram 3} \\ + \\ \text{diagram 4} \end{array} \right) \right] \\
 & + z^4 \left| \begin{array}{c} \text{diagram 3} \\ + \\ \text{diagram 4} \end{array} \right|^2 \\
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 \end{aligned}$$

We cannot separate inelastic *ep* events from elastic *ep* when very little energy is carried away by photons

Standard corrections for ep scattering

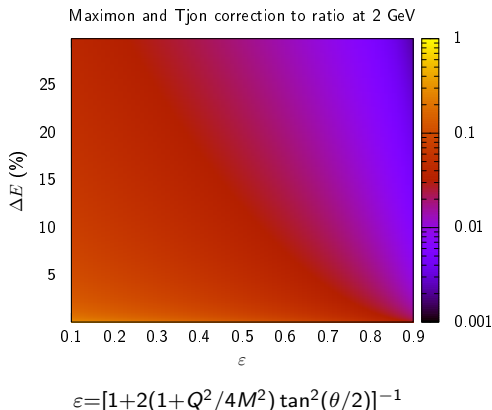
- Mo and Tsai did the first full calculation of the size of these corrections to elastic ep scattering
 - L. W. Mo and Y. S. Tsai, Rev. Mod. Phys. **41**, 205 (1969)
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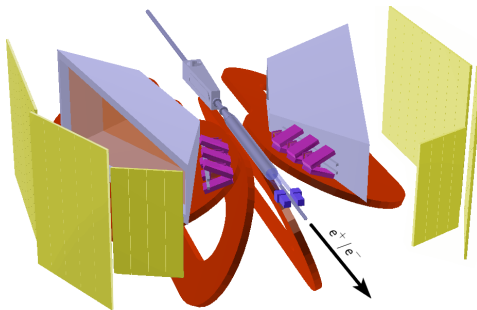
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 - Used for the radiative corrections in most older measurements
- More recently, Maximon and Tjon improved upon the calculations of Mo and Tsai
 - L. C. Maximon and J. A. Tjon, Phys. Rev. C **62**, 054320 (2000)
 - Form for bremsstrahlung given in the soft photon limit without additional approximation
 - Less-severe soft photon approximation in calculation of TPE amplitudes
 - Full calculation of proton vertex

Standard corrections for ep scattering

- Both formulations express the correction to the cross section in terms of a parameter ΔE
 - ΔE is the maximum energy loss an inelastic electron can have and still be measured as elastic
 - Determined by detector resolution
- Size of correction increases with decreasing ΔE

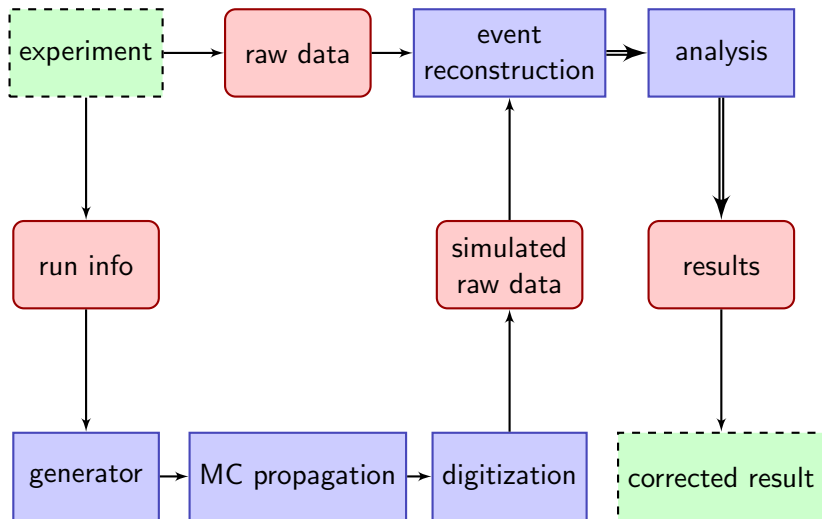


Monte Carlo



- ΔE far too crude of a quantization of our ability to separate elastic and inelastic events
- Need to take into account efficiencies, cuts, and acceptances of the detectors
- Monte Carlo is the clear solution
 - Allows us to go beyond Maximon and Tjon
 - Can do a full calculation of bremsstrahlung with no soft-photon approximation

Analysis plan



Luminosity Monitors

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- 12° $ep \rightarrow ep$ luminosity monitors
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- Symmetric Møller/Bhabha luminosity monitor
 - Currently using tree level generator
 - Need a radiative one for the final result
 - $e^- + e^- \rightarrow e^- + e^-$
 $e^+ + e^- \rightarrow e^+ + e^-$
 $e^+ + e^- \rightarrow 2\gamma$

OLYMPUS generator plugin

- Outer “interfacing” part:
 - Gets the beam position, slope, charge, and energy from run info
 - Passes the beam charge (e^+ or e^-) and energy to the inner part
 - Generates appropriate target distribution

OLYMPUS generator plugin

■ Outer “interfacing” part:

- Gets the beam position, slope, charge, and energy from run info
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- Generates appropriate target distribution

■ Inner “physics” part:

- Contains the differential cross section and event generation
- Easy to swap in and out
- Born, isotropic, pion, Novosibirsk radiative, OLYMPUS radiative (testing)
 - Pion: MAID2007
(<http://wwwkph.kph.uni-mainz.de/MAID/maid2007/>)
 - Novosibirsk radiative: ESEPP by Alexander Gramolin
(<http://www.inp.nsk.su/~gramolin/esepp/>)
- Can add other radiative generators...

Unweighted vs. Weighted

Different approaches to event generation:

- Our radiative generator is weighted
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 - Can easily use regular counting statistics
 - Looks just like data
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Different approaches to event generation:

- Our radiative generator is weighted
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- Unweighted:
 - Can easily use regular counting statistics
 - Looks just like data
 - Non-trivial to generate from a high-dimensional distribution
- Weighted:
 - Easier to change energy on an event-to-event basis
 - Choice of what distribution to sample from
 - Can have multiple weights while propagating each event

Options with weighted generators

- Importance sampling
 - Choose a distribution that's easy to sample from
 - Should approximate cross section in range you care about
 - Almost constant weights
 - Can slightly suppress events that we probably don't care about
 - For more: Talk tomorrow by Axel Schmidt

Options with weighted generators

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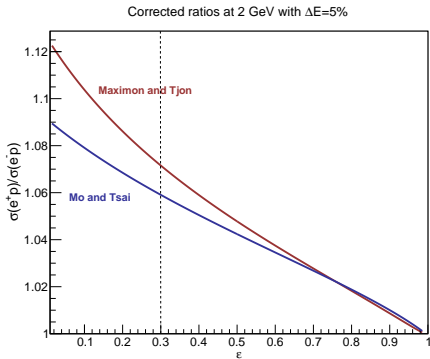
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■ Multiple weights

- Slowest step of analysis is propagation of generated events through Monte Carlo
- Want to propagate as few events as possible
- Can carry weights from many different cross section calculations simultaneously
- Allows us to break the final radiative correction into components

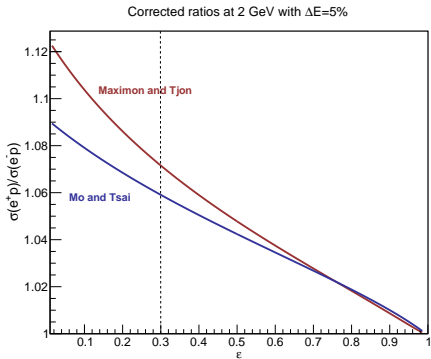
“Hard” vs “soft” two photon exchange

- Hard TPE has not been accounted for in Rosenbluth experiments
 - Mo and Tsai and Maximon and Tjon calculate “soft” two photon exchange differently
 - “Hard” two photon exchange is everything else...



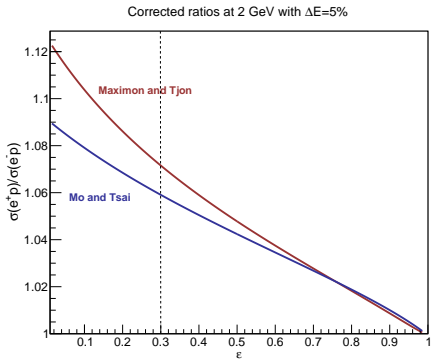
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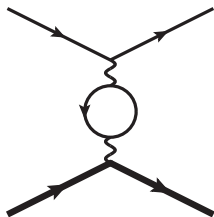


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- For us, this is just a definitional difference
- Carry two weights for each simulated event, and easily generate two final results



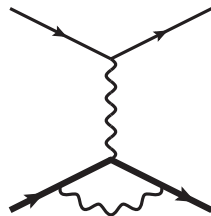
Vacuum polarization



- Maximon and Tjon and Mo and Tsai use just electrons/positrons in the loop
 - Easy to extend to more leptons
 - Detailed theoretical calculations exist
 - Can use experimental measurement
- Once again, we can carry a bunch of weights through our whole analysis to see how big of an effect this might have

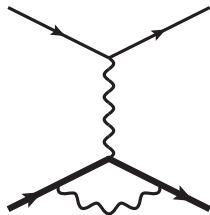
Form factor dependence

- We're trying to solve a form-factor discrepancy



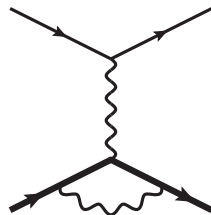
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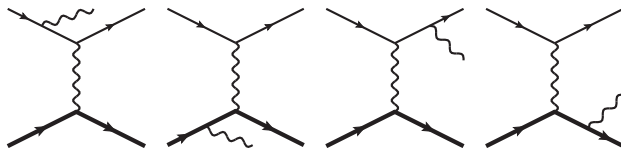


Form factor dependence

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 - Negligible for our experiment...
- Bremsstrahlung
 - Probably not totally negligible
 - Can use several choices: dipole, more sophisticated parameterizations
 - Can use different weights to see if choice makes a difference



The most challenging part of our radiative corrections



- Detailed calculation of bremsstrahlung to the order of α^3 without any soft photon approximation or peaking approximation for most of parameter space
- Use Maximon and Tjon formulation for cross section with elastic kinematics very close to the elastic curve
- See: Talk by Axel Schmidt tomorrow

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- Radiative generator is mostly written
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- Check to make sure it produces similar results to Novosibirsk generator
 - Need to understand any differences
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- Geant4 Monte Carlo development is complete
 - Detectors and materials positioned by surveys done before and immediately after data taking
- Digitization is not yet completed for all detectors

Conclusion

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 - Extensive options that can be propagated in parallel through use of weights
 - Can use this weighting to report size of various contributions in final result (suggestions?)
- Working with the other TPE experiments to ensure consistent radiative corrections