

# Gauge Mediation beyond MFV

---

Robert Ziegler (LPTHE)

based on JHEP 1306 (2013)  
with L. Calibbi & P. Paradisi

# Overview

---

- Modification of minimal Gauge Mediation with new messenger-matter couplings controlled by same flavor dynamics as Yukawas
- Due to large  $A$ -terms, one can easily accommodate a 125 GeV Higgs for light and predictive SUSY spectrum (one additional parameter wrt GMSB)
- New sources of flavor violation depending on underlying flavor model, but built-in suppression due to loop origin of soft terms

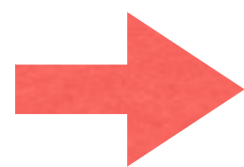
# The Status of Gauge Mediation

---

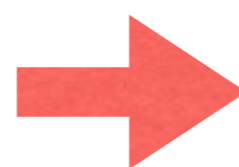
- Gauge Mediation elegant and predictive
- In minimal GM difficult to get large Higgs mass (A-terms are small)

$$\Delta m_h^2 \approx \frac{3m_t^2}{8\pi^2 v^2} \left( \log \frac{M_S^2}{m_t^2} + \frac{X_t^2}{M_S^2} \left( 1 - \frac{X_t^2}{12M_S^2} \right) \right)$$

$$X_t = A_t - \mu \cot \beta$$



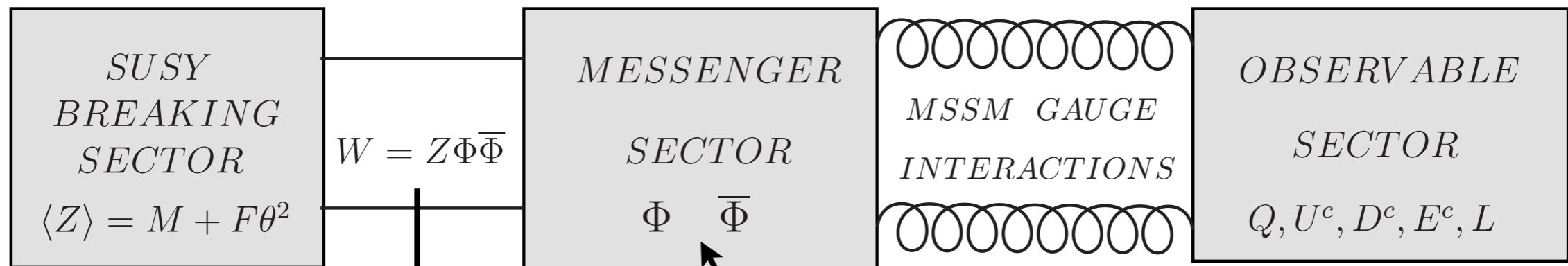
would need very  
large stop masses



all SUSY particles  
very heavy

**Go beyond minimal GM for large A-terms**

# The Structure of Minimal GMSB



complete SU(5) multiplets:  $N \times (\mathbf{5} + \bar{\mathbf{5}})$

$$M_F = M$$

$$(M_S^2)_{1,2} = M^2 \pm F$$

1-loop gaugino masses  $M_a = N \frac{\alpha_a}{4\pi} \Lambda$

2-loop **flavor-universal** sfermion masses  $\tilde{m}_Q^2 = 2N C_a \left( \frac{\alpha_a}{4\pi} \Lambda \right)^2$

Vanishing A-terms  $A = 0$

$\Lambda \equiv F/M$

# Generating large A-terms in GM

---

- Need direct messenger-MSSM couplings  
(usually forbidden by discrete symmetry)

$$\Delta W = \begin{cases} U \bar{\Phi}_5 \bar{\Phi}_5 & \text{Evans, Ibe, Yanagida '11,'12 \quad Craig, Knapen, Shih, Zhao '12} \\ QU \Phi_5 & \text{Albeid, Babu '12 \quad Byakti, Ray '13 \quad Evans, Shih '13 \quad Jelinski '13} \\ H_u \Phi_{10} \Phi_{10} & \dots \\ \dots & \dots \end{cases}$$

- Also new contributions to sfermion masses  
→ need to take care of flavor structure!

new couplings  
proportional to Yukawas

OR

new couplings  
suppressed as Yukawas

- Take  $5, \bar{5}$  messengers with positive R-parity

$$\Delta W = \lambda_{ij}^U Q_i U_j \Phi_{H_u} + \lambda_{ij}^D Q_i D_j \bar{\Phi}_{H_d}$$

- Assume that couplings are controlled by same underlying flavor dynamics as Yukawas  
(flavor symmetries, partial compositeness...)
- Simplest scenario: flavor only from matter fields

$$\Phi, \bar{\Phi} \sim H_u, H_d$$

e.g. not charged under flavor symmetry



$$\lambda^{U,D} \sim y^{U,D}$$

# The Setup

---

- Messengers and Higgs distinguished by symmetry that forbids  $\mu$ -term: H chiral,  $\Phi$  vector-like

→ for  $N=1$  only one messenger can mix with H

e.g.

	$\Phi_{H_u}$	$\Phi_T$	$\bar{\Phi}_{H_d}$	$\bar{\Phi}_T$	$H_u$	$H_d$	$X$	$Q, U, D, E, L$
$U(1)$	1	0	-1	0	1	1	0	-1/2

- Final setup

$$W = (y_U)_{ij} Q_i U_j H_u + (y_D)_{ij} Q_i D_j H_d + (y_E)_{ij} L_i E_j H_d + X (\bar{\Phi}_T \Phi_T + \bar{\Phi}_{H_d} \Phi_{H_u}) + (\lambda_U)_{ij} Q_i U_j \Phi_{H_u}$$

$\lambda_{ij}^U \sim y_{ij}^U \longrightarrow$  only  $\lambda_{33}^U$  relevant for SUSY spectrum

# High-energy Spectrum

---

Evans, Shih '13

- Non-zero squark A-terms

$$A_U = -\frac{\Lambda}{16\pi^2} \left( \lambda_U \lambda_U^\dagger y_U + 2 y_U \lambda_U^\dagger \lambda_U \right) \quad A_D = -\frac{\Lambda}{16\pi^2} \lambda_U \lambda_U^\dagger y_D$$

- New contris to 2-loop squark and soft Higgs masses

$$\Delta m_{Q(U)}^2 \sim \frac{\Lambda^2}{256\pi^4} \left( \lambda_U \lambda_U^\dagger - g_3^2 \right) \lambda_U \lambda_U^\dagger \quad \Delta m_D^2 \sim \frac{\Lambda^2}{256\pi^4} y_D^\dagger \lambda_U \lambda_U^\dagger y_D$$

$$\Delta m_{H_u}^2 \sim -\frac{\Lambda^2}{256\pi^4} \text{Tr} y_U^\dagger \lambda_U \lambda_U^\dagger y_U \quad \Delta m_{H_d}^2 \sim -\frac{\Lambda^2}{256\pi^4} \text{Tr} y_D^\dagger \lambda_U \lambda_U^\dagger y_D$$

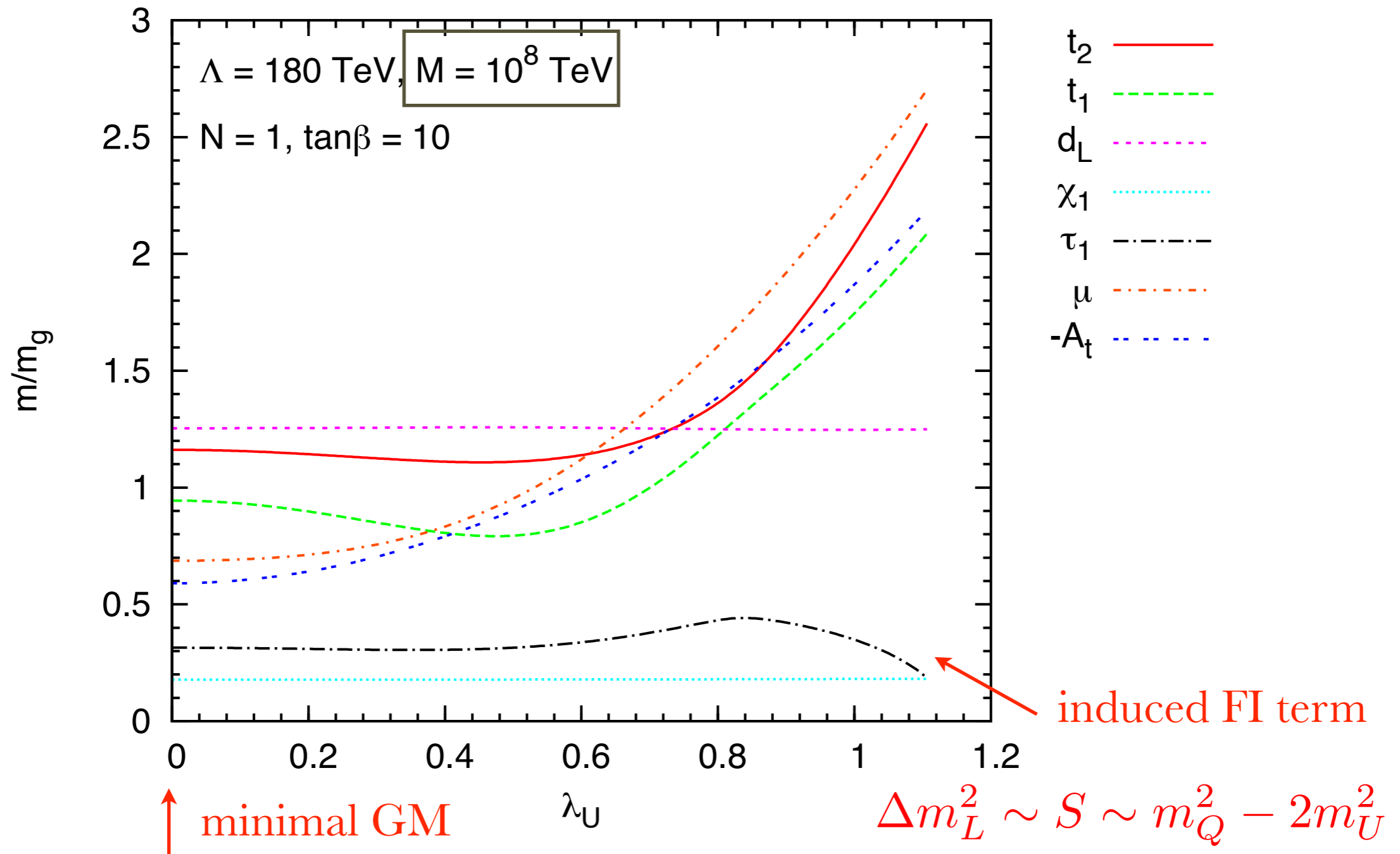
- Negative 1-loop squark masses (for low messenger scales)



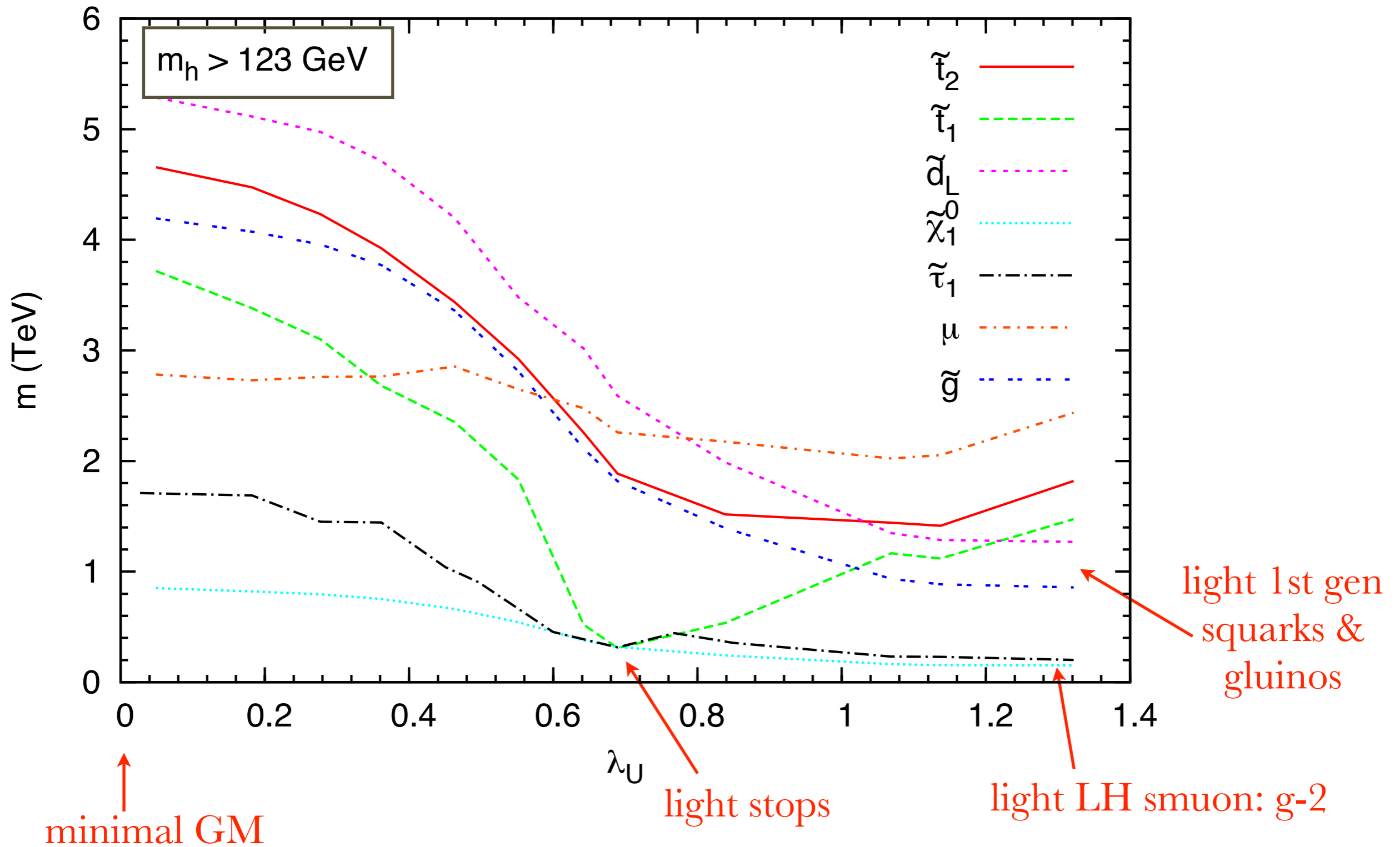
# Low-energy Spectrum

$$\lambda_{33}^U \equiv \lambda_U$$

Evans, Ibe, Yanagida '11,'12



# Low-energy Spectrum



# Sflavor Structure

---

**CKM suppression**  $[(\lambda_U)_{i3} \lesssim V_{i3}]$

$$(\delta_{LL}^u)_{ij} \sim (\lambda_U)_{i3} (\lambda_U^*)_{j3}$$

$$(\delta_{RR}^u)_{ij} \sim (\lambda_U^*)_{3i} (\lambda_U)_{3j}$$

$$(\delta_{LL}^d)_{ij} \sim V_{3i}^* V_{3j},$$

$$(\delta_{RR}^d)_{ij} \sim y_i^D y_j^D V_{3i}^* V_{3j}$$

**Possibly sizable**

**Light Yukawa suppression**

$$(\delta_{LR}^u)_{ij} \sim (\lambda_U)_{i3} (\lambda_U)_{3j}$$

$$(\delta_{LR}^d)_{ij} \sim V_{3i}^* V_{3j} y_j^D$$

**Possibly sizable**

**Additional CKM suppression**

# Flavor constraints

---

Most constraints automatically satisfied for  $\tilde{m} \sim 1$  TeV

$(\delta_{XX}^D)_{12}$	$9.2 \times 10^{-2}$ [Re]	$1.2 \times 10^{-2}$ [Im]
$\langle \delta_{12}^D \rangle$	$1.9 \times 10^{-3}$ [Re]	$2.6 \times 10^{-4}$ [Im]
$(\delta_{LR}^D)_{12}$	$5.6 \times 10^{-3}$ [Re]	$4.0 \times 10^{-5}$ [Im]
$(\delta_{XX}^U)_{12}$	$1.0 \times 10^{-1}$ [Re]	$6.0 \times 10^{-2}$ [Im]
$\langle \delta_{12}^U \rangle$	$6.2 \times 10^{-3}$ [Re]	$4.0 \times 10^{-3}$ [Im]
$(\delta_{LR}^U)_{12}$	$1.6 \times 10^{-2}$ [Re]	$1.6 \times 10^{-2}$ [Im]
$(\delta_{XX}^D)_{13}$	$2.8 \times 10^{-1}$ [Re]	$6.0 \times 10^{-1}$ [Im]
$\langle \delta_{13}^D \rangle$	$4.2 \times 10^{-2}$ [Re]	$1.8 \times 10^{-2}$ [Im]
$(\delta_{LR}^D)_{13}$	$6.6 \times 10^{-2}$ [Re]	$1.5 \times 10^{-1}$ [Im]
$(\delta_{LR}^D)_{11}$	$2.0 \times 10^{-6}$	
$(\delta_{LR}^U)_{11}$	$4.0 \times 10^{-6}$	

$D - \bar{D}$  mixing

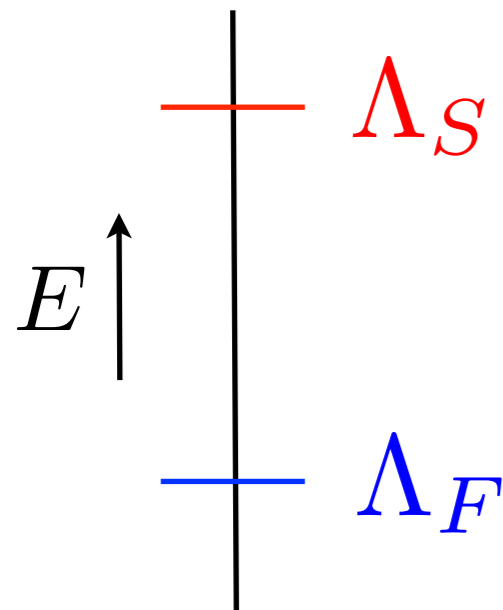
$$(\delta_{RR}^u)_{12} \sim (\lambda_U^*)_{31} (\lambda_U)_{32}$$

Neutron EDM

$$(\delta_{LR}^u)_{11} \sim (\lambda_U)_{13} (\lambda_U)_{31}$$

# Comparison to other Sflavor Models

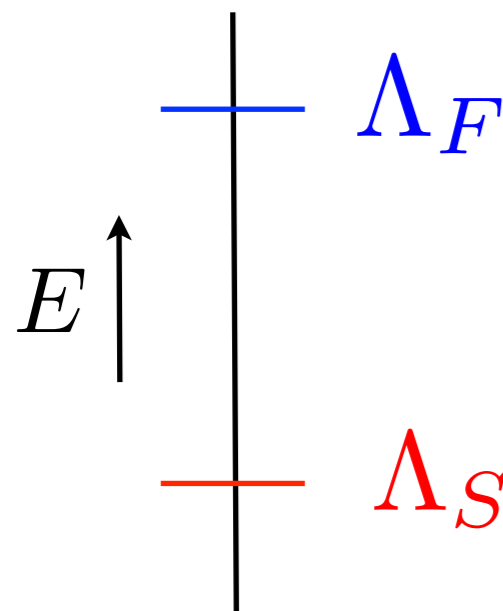
---



**e.g. Gravity Mediation + Flavor Model,  
SUSY Partial Compositeness**

$\delta_{ij}$  controlled by flavor dynamics at  $\Lambda_F$

→ SUSY spectrum not very predictive



**Flavored Gauge Mediation + Flavor Model**

$\delta_{ij}$  controlled by flavor dynamics at  $\Lambda_S$

→ SUSY spectrum very predictive

→ extra suppression FV from loop structure

# Comparison: FGM + U(1) model

	MFV	PC	U(1)	FGM <sub>U,D</sub> + U(1)	FGM <sub>U</sub> + U(1)
$(\delta_{LL}^u)_{ij}$	$V_{i3} V_{j3}^* y_b^2$	$(\epsilon_3^q)^2 V_{i3} V_{j3}^*$	$\frac{V_{i3}}{V_{j3}}  _{i \leq j}$	$V_{i3} V_{j3}^* y_t^2$	$V_{i3} V_{j3}^* y_t^2$
$(\delta_{LL}^d)_{ij}$	$V_{3i}^* V_{3j} y_t^2$	$(\epsilon_3^q)^2 V_{i3} V_{j3}^*$	$\frac{V_{i3}}{V_{j3}}  _{i \leq j}$	$V_{3i}^* V_{3j} y_t^2$	$V_{3i}^* V_{3j} y_t^2$
$(\delta_{RR}^u)_{ij}$	$y_i^U y_j^U V_{i3} V_{j3}^* y_b^2$	$\frac{y_i^U y_j^U}{V_{i3} V_{j3}^*} \frac{(\epsilon_3^u)^2}{y_t^2}$	$\frac{y_i^U V_{j3}}{y_j^U V_{i3}}  _{i \leq j}$	$\frac{y_i^U y_j^U}{V_{i3} V_{j3}^*}$	$\frac{y_i^U y_j^U}{V_{i3} V_{j3}^*}$
$(\delta_{RR}^d)_{ij}$	$y_i^D y_j^D V_{3i}^* V_{3j} y_t^2$	$\frac{y_i^D y_j^D}{V_{i3} V_{j3}^*} \frac{(\epsilon_3^u)^2}{y_t^2}$	$\frac{y_i^D V_{j3}}{y_j^D V_{i3}}  _{i \leq j}$	$\frac{y_i^D y_j^D}{V_{i3} V_{j3}^*}$	$y_i^D y_j^D V_{3i}^* V_{3j} y_t^2$
$(\delta_{LR}^u)_{ij}$	$y_j^U V_{i3} V_{j3}^* y_b^2$	$y_j^U \frac{V_{i3}}{V_{j3}^*}$	$y_j^U \frac{V_{i3}}{V_{j3}^*}$	$y_j^U V_{i3} V_{j3}^* y_t^2 + y_i^U \frac{y_i^U y_j^U}{V_{i3} V_{j3}^*}$ $y_j^U \frac{V_{i3}}{V_{j3}^*} y_t^6$	$y_j^U V_{i3} V_{j3}^* y_t^2 + y_i^U \frac{y_i^U y_j^U}{V_{i3} V_{j3}^*}$ $y_j^U \frac{V_{i3}}{V_{j3}^*} y_t^6$
$(\delta_{LR}^d)_{ij}$	$y_j^D V_{3i}^* V_{3j} y_t^2$	$y_j^D \frac{V_{i3}}{V_{j3}^*}$	$y_j^D \frac{V_{i3}}{V_{j3}^*}$	$y_j^D V_{3i}^* V_{3j} y_t^2 + y_i^D \frac{y_i^D y_j^D}{V_{i3} V_{j3}^*}$ $y_j^D \frac{V_{3i}^*}{V_{3j}} y_t^4 y_b^2$	$y_j^D V_{3i}^* V_{3j} y_t^2$

**Despite weak U(1) suppression FGM looks like PC**

# Application: SUSY $\Delta A_{CP}$

---

- Evidence (?) for direct CPV in charm decays

$$\Delta A_{CP} \equiv A_{CP}(K^+ K^-) - A_{CP}(\pi^+ \pi^-) = -(0.67 \pm 0.16)\%$$

Latest LHCb result:

Naïve average\*

$$\Delta A_{CP} = (-0.33 \pm 0.12)\%$$

- Unclear whether need new Physics

SM needs largish  
hadronic enhancement:

$$\mathcal{O}\left(\frac{V_{cb} V_{ub}}{V_{cs} V_{us}} \frac{\alpha_s}{\pi}\right) \sim 10^{-4}$$

- Can be generated in SUSY from LR transition

$$\Delta A_{CP}^{SUSY} \sim 0.6\% \frac{\text{Im}(\delta_{LR}^u)_{12}}{10^{-3}} \left(\frac{1\text{TeV}}{\tilde{m}}\right)$$

no way in MFV  $(\delta_{LR}^u)_{12} \sim 10^{-7}$

Giudice, Isidori,  
Paradisi '12

# SUSY $\Delta A_{CP}$ in FGM

---

- Constraints on underlying flavor model

$$(\lambda_U)_{31}^* (\lambda_U)_{32} \lesssim 6.0 \times 10^{-2} \left( \frac{M_S}{1 \text{ TeV}} \right) \quad D - \bar{D}$$

$$(\lambda_U)_{13} (\lambda_U)_{31} \lesssim 1.7 \times 10^{-5} \left( \frac{M_S}{1 \text{ TeV}} \right) \left( \frac{M_S}{A} \right) \quad \text{EDM}$$

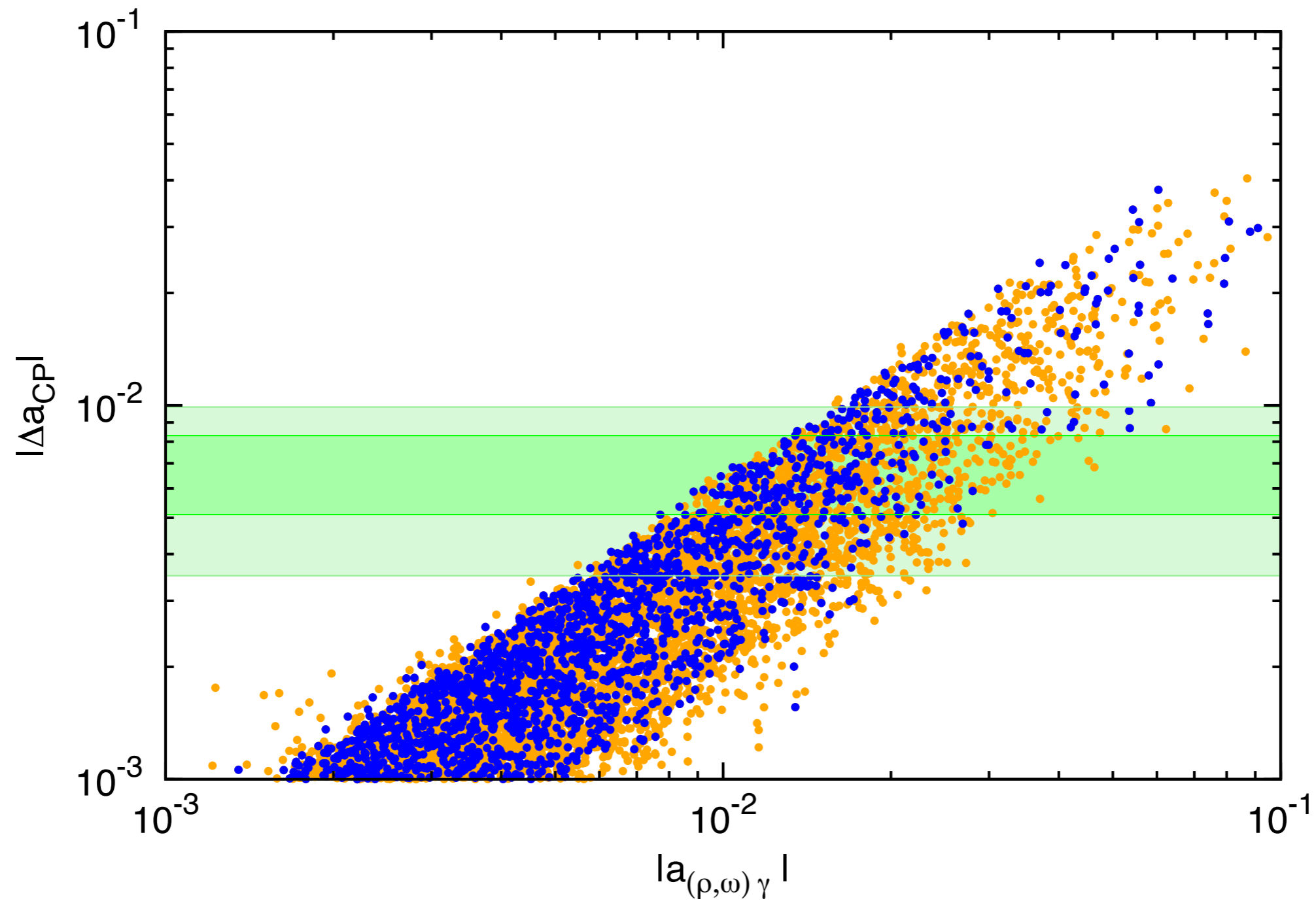
- $\Delta A_{CP}$  depends on different combination  $\lambda_U$  entries

$$(\delta_{LR}^u)_{12}^{eff} \sim (\lambda_U)_{13} (\lambda_U)_{32}$$

**Large  $\Delta A_{CP}$  possible for suitable flavor model**



# Testable with $\Delta A_{CP}$ vs. $D \rightarrow V\gamma$ Isidori, Kamenik '12



●  $>123$  GeV Higgs

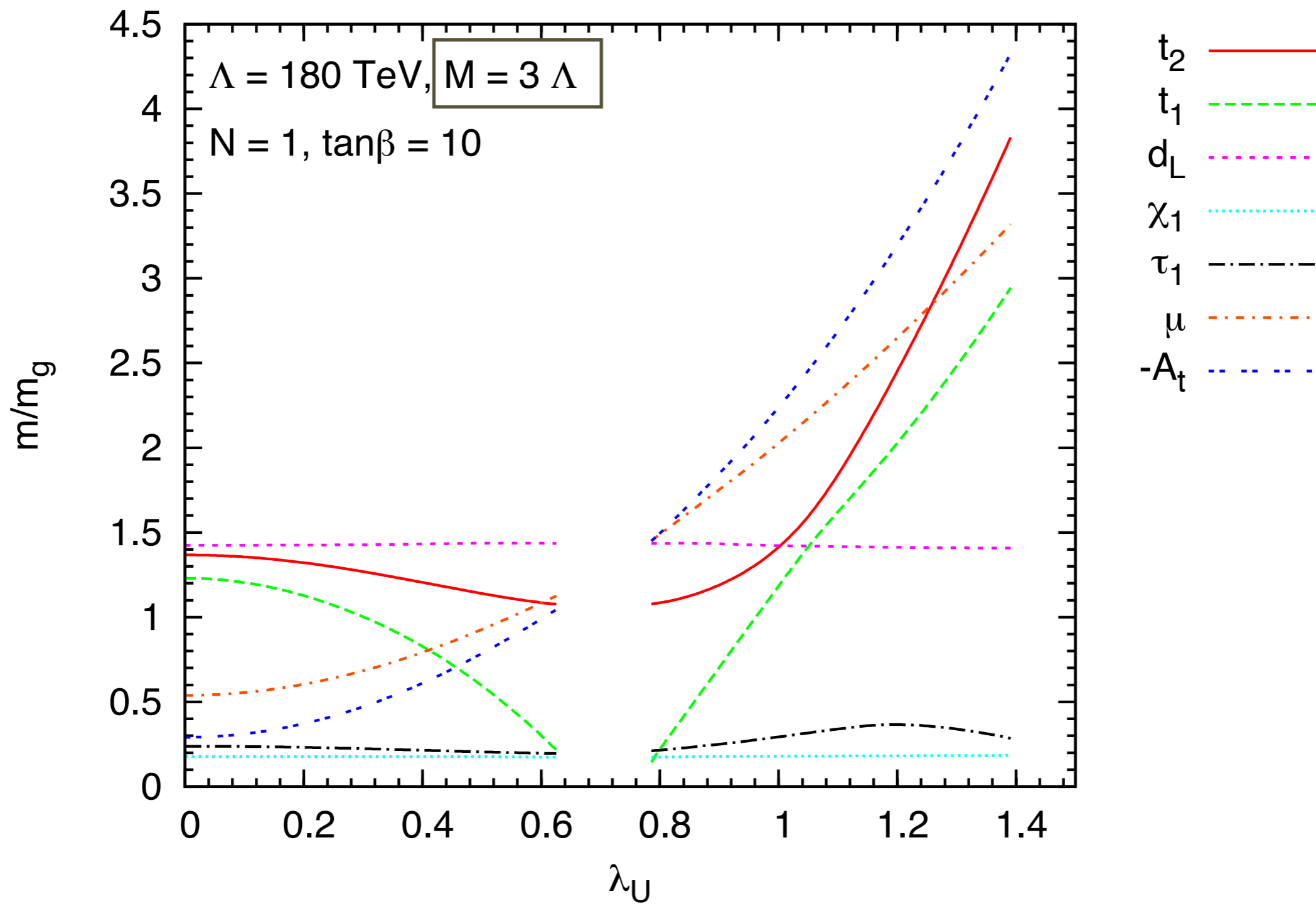
# Summary

---

- Consider couplings of GM messenger to MSSM that are parametrically small as Yukawas
- Leads to large misaligned  $A$ -terms
- Large Higgs mass with light, calculable spectrum
- Flavor pheno non-MFV, depends on flavor model
- LL&RR transitions small, dominant effects from LR
- Perfect framework to address direct CPV in charm

Backup

# Low-energy Spectrum



# NMSSM for mu-term

---

	$\Phi_{H_u}$	$\bar{\Phi}_{H_d}$	$H_u$	$H_d$	$X$	$Q, U, D, E, L$
U(1)	1	-1	1	1	0	-1/2



add S and break U(1) to Z3

	$\Phi_{H_u}$	$\bar{\Phi}_{H_d}$	$H_u$	$H_d$	$X$	$Q, U, D, E, L$	$S$
Z3	1	-1	1	1	0	1	1

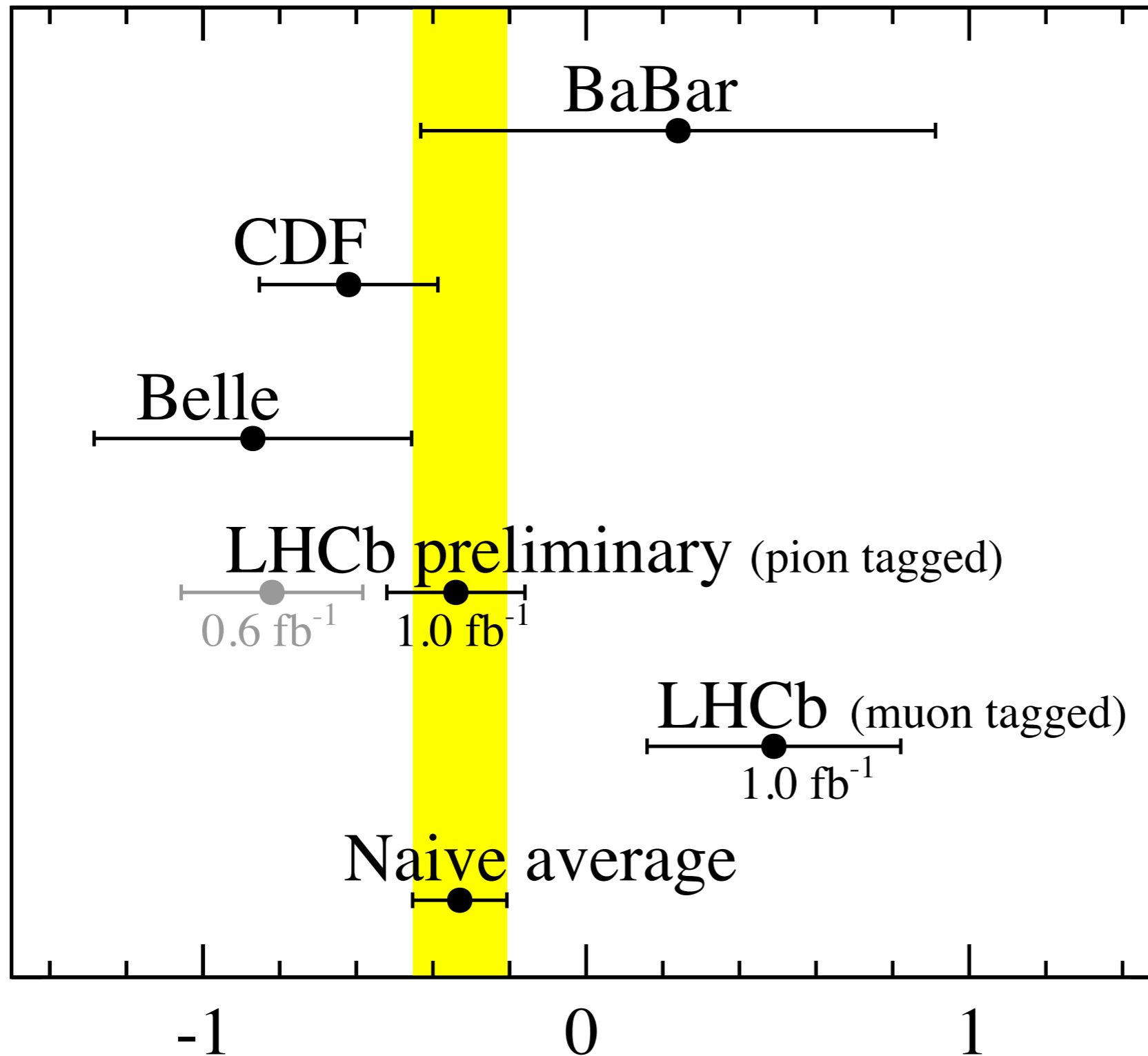
$$W \sim X \bar{\Phi}_{H_d} (\Phi_{H_u} + H_u) + QU (\Phi_{H_u} + H_u) + SH_d (\Phi_{H_u} + H_u) + S^3$$

$\underbrace{\hspace{10em}}_{\Phi'_{H_u}}$

helps to get negative  $m_S^2$

$\mu$  - term

# Experimental situation



Naïve average\*

$$\Delta A_{CP} = (-0.33 \pm 0.12)\%$$

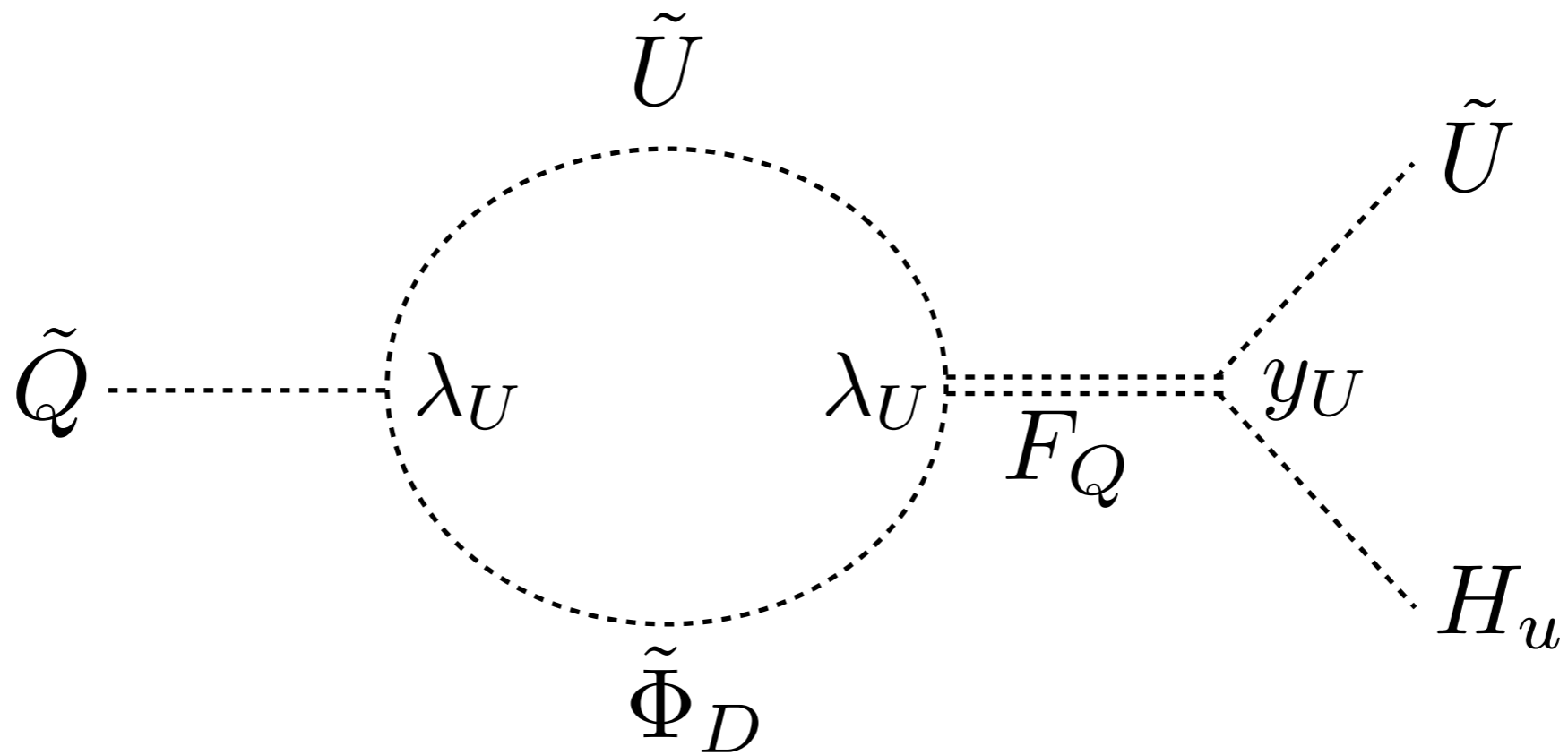
\*) Does not account for indirect CP violation.  
No scaling of errors.

CERN-LHC seminar, 12 March 2013

Jeroen van Tilburg

# A-terms

---



# 1-loop contributions

---

$$\Delta m_{Q,1-loop}^2 \sim -\frac{\Lambda^2}{16\pi^2} \frac{\Lambda^2}{M^2} \lambda_U \lambda_U^\dagger$$
$$\Delta m_{U,1-loop}^2 \sim -\frac{\Lambda^2}{16\pi^2} \frac{\Lambda^2}{M^2} \lambda_U^\dagger \lambda_U$$

# Tree-level contributions

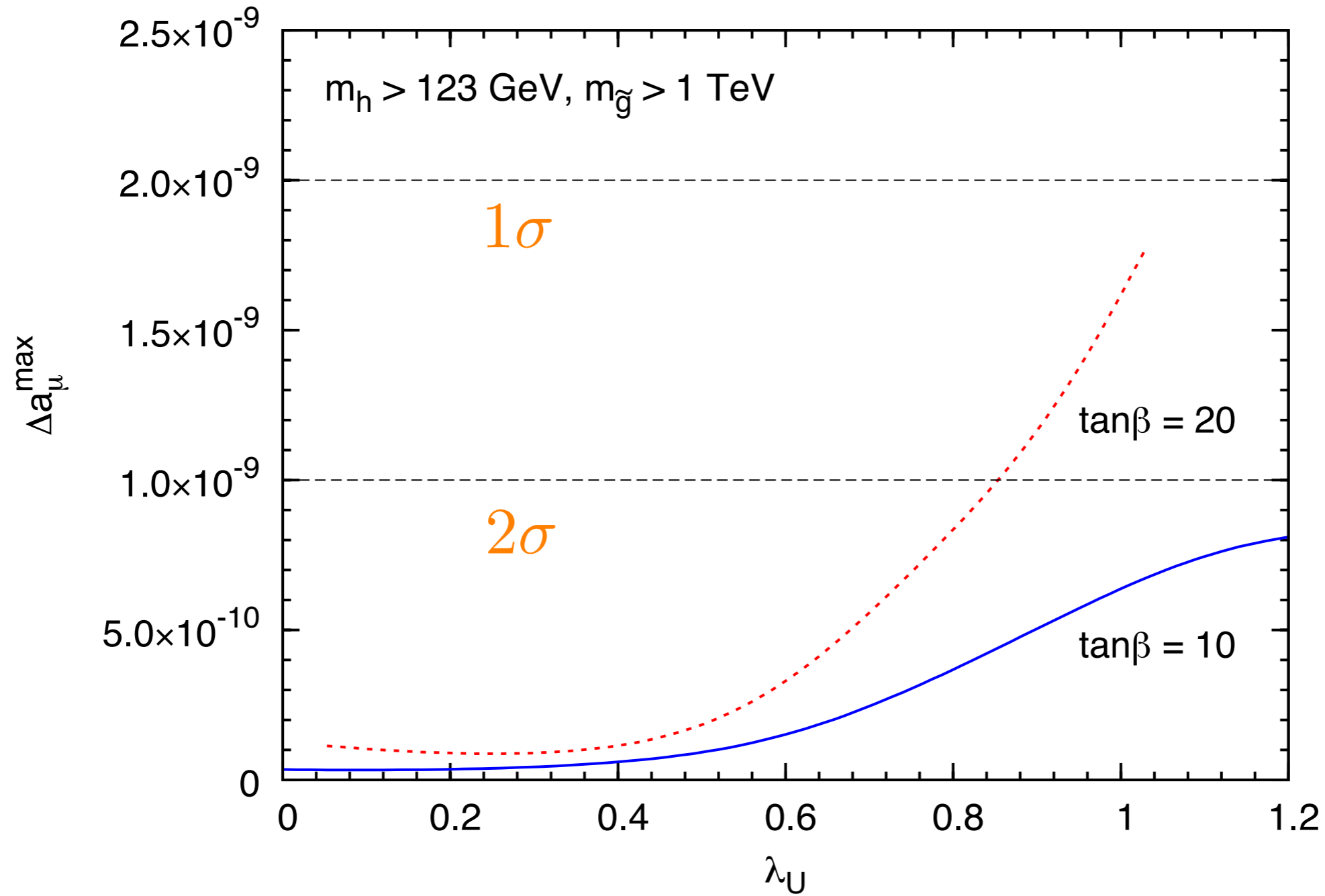
---

$$\Delta W = \mu H_u H_d + \mu' \Phi_{H_u} H_d$$

$$\Delta m_{H_d,tree}^2 = -\frac{\mu'^2}{M^2} \frac{\Lambda^2}{1 - \Lambda^2/M^2}$$



# Muon g-2



$$\Delta a_\mu \approx 1.3 \times 10^{-9} \left( \frac{\tan\beta}{10} \right) \left( \frac{500 \text{ GeV}}{\tilde{m}_{\mu R}} \right)^2 \left( \frac{\mu/\tilde{m}_{\mu L}}{10} \right)$$

Evans, Ibe, Shirai, Yanagida '12

# SU(5) invariant charge assignment

---

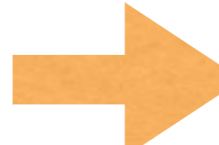
	$\Phi_{H_u}$	$\Phi_T$	$\bar{\Phi}_{H_d}$	$\bar{\Phi}_T$	$H_u$	$H_d$	$X$	$Q, U, D, E, L$
$U(1)$	1	<del>0</del> 1	-1	<del>0</del> -1	1	1	0	-1/2

$$\Delta W = (\lambda_{QQ})_{ij} Q_i Q_j \Phi_T + (\lambda_{UE})_{ij} U_i E_j \Phi_T$$

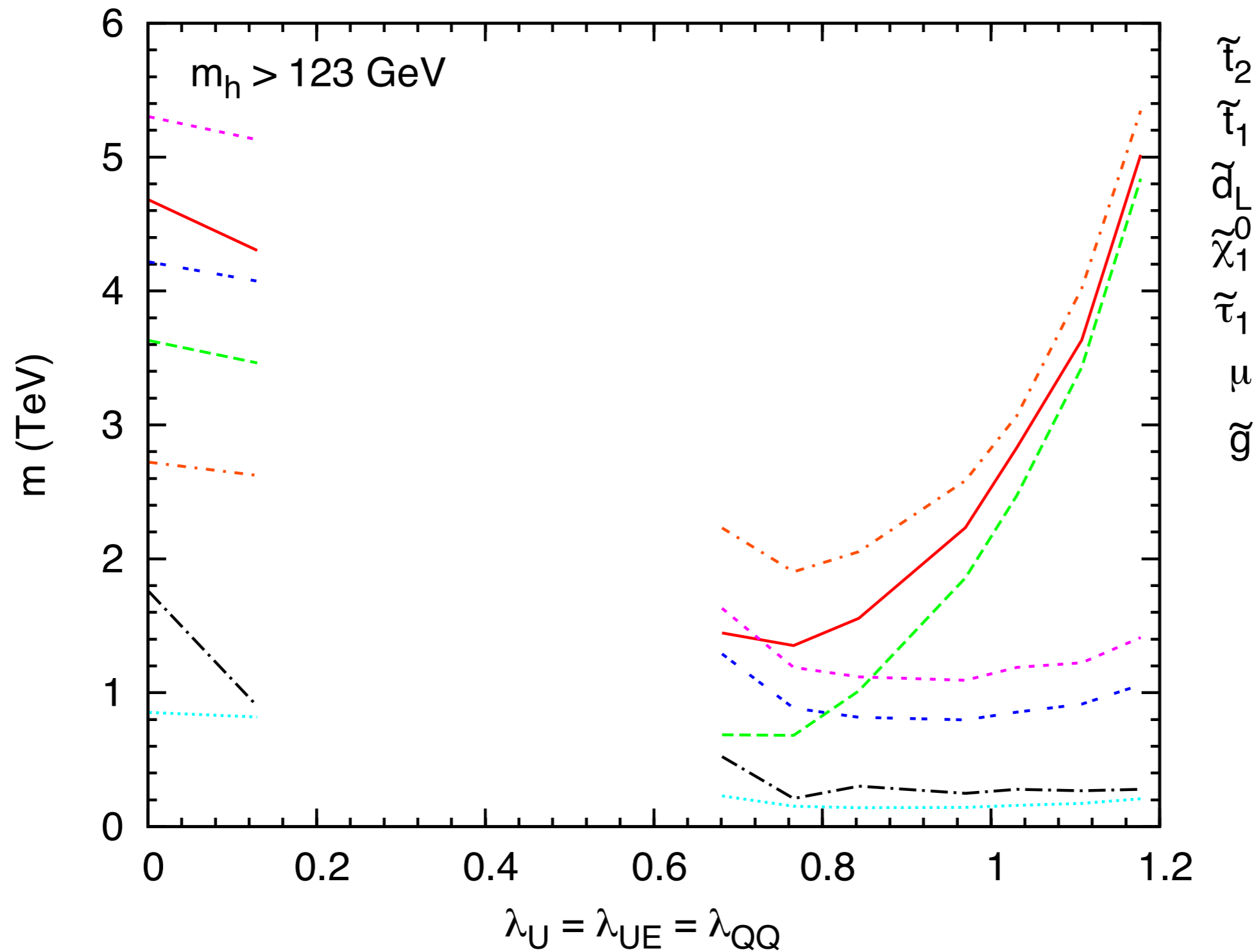
with  $\lambda_{QQ} \sim \lambda_{UE} \sim \lambda_U \sim y_U$

no dim 5 proton decay operators

$$K_{eff} \sim \underbrace{\frac{(\lambda_{QQ})_{11}(\lambda_{UE})_{11}}{M^2}}_{1/M_{eff}^2} Q_1^\dagger Q_1^\dagger U_1 E_1 \quad M_{eff} \gtrsim 10^{15} \text{ GeV}$$


M ≳ 10<sup>10</sup> GeV

# SU(5) invariant charge assignment



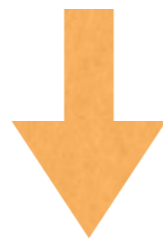
# $\Delta A_{CP}$ in U(1) Flavor Models

---

maximal effect bounded from EDM constraint

$$(\delta_{LR}^u)_{11} \lesssim 3 \times 10^{-6} \frac{\tilde{m}}{\text{TeV}}$$

$$(\delta_{LR}^u)_{12} \sim \frac{m_c}{m_u} V_{us} (\delta_{LR}^u)_{11}$$



$$(\delta_{LR}^u)_{12} \lesssim 3 \times 10^{-4} \frac{\tilde{m}}{\text{TeV}}$$

$$\text{need indeed } 5 \times 10^{-4} \frac{\tilde{m}}{\text{TeV}}$$

better situation than Gravity Mediation + U(1)

$$(\delta_{LR}^u)_{12} \lesssim 8 \times 10^{-5} \frac{\tilde{m}}{\text{TeV}}$$

Hiller, Nir '12