

Weak Lensing with Planck



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planck



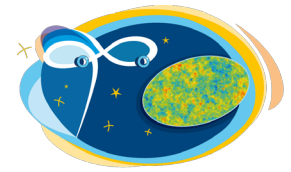
DTU Space
National Space Institute



Science & Technology
Facilities Council



CONSEJO SUPERIOR DE INVESTIGACIONES CIENTÍFICAS
CSIC



HFI PLANCK
a look back to the birth of Universe



National Research Council of Italy



Deutsches Zentrum
für Luft- und Raumfahrt e.V.



UK SPACE
AGENCY



MAX-PLANCK-GESELLSCHAFT



INSU
Observer & comprendre



IN2P3
Les deux infinis



UNIVERSITÀ DEGLI STUDI
DI MILANO



MilliLab



UNIVERSITY OF HELSINKI



UNIVERSITÉ
DE GENÈVE



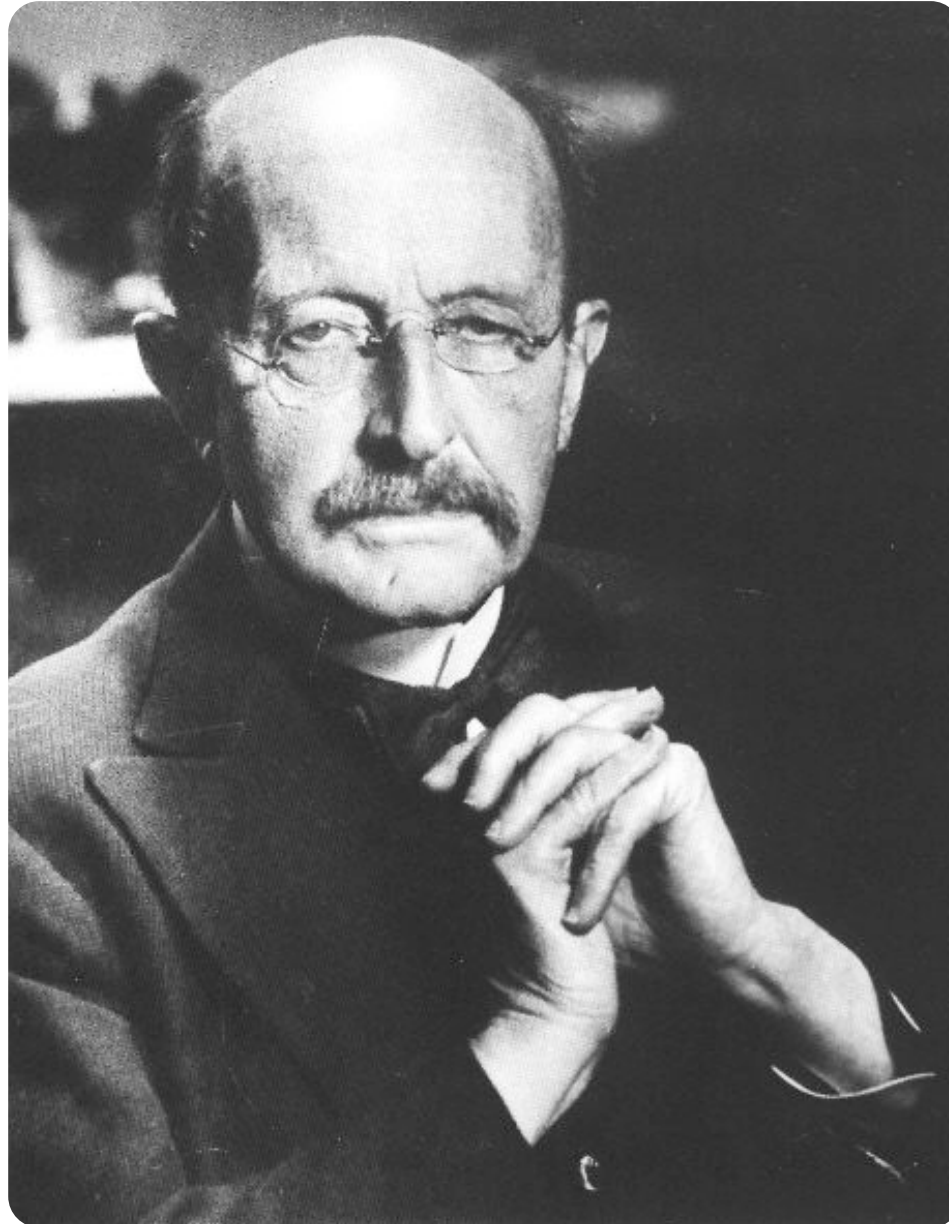
UNIVERSITY OF
TORONTO



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PARIS-SUD XI



Max Planck (1858-1927)



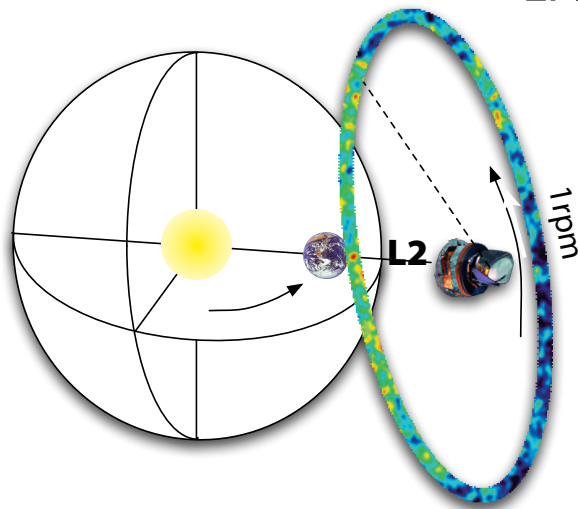
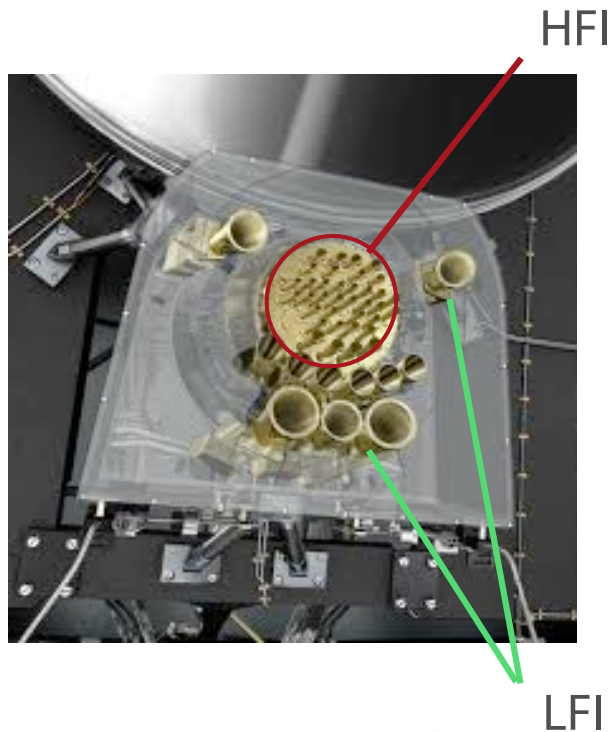
Planck (1993-23/10/2013)





Ariane 5 ECA Launch • HERSCHEL – PLANCK - *May 14, 2009*

Planck

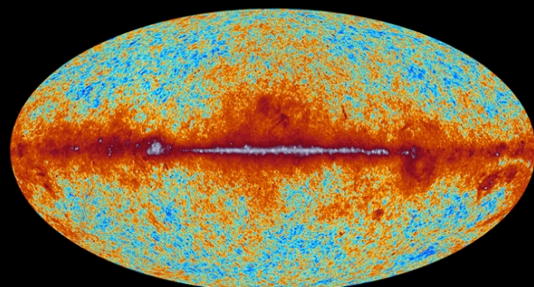


- **Driving goal : The definitive Temperature anisotropies measurement**
- Primary 1.5m
- 2 instruments
 - LFI : 3 bands, 22 radiometers
 - HFI : 6 bands, 50 bolometers
- 4 stage cooler down to 0.1K
 - Last stage is a He3/He4 dilution cooler
- Operated flawlessly since launch
 - HFI (and the dilution cooler) stopped Jan 2012
- ~5 independent surveys (nominal mission 2 surveys)

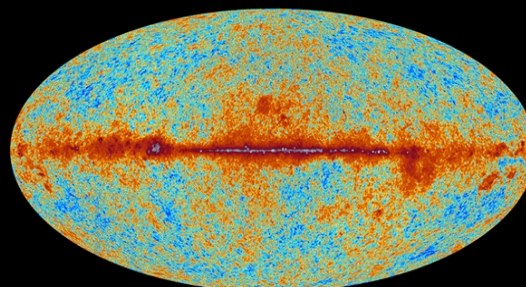


planck

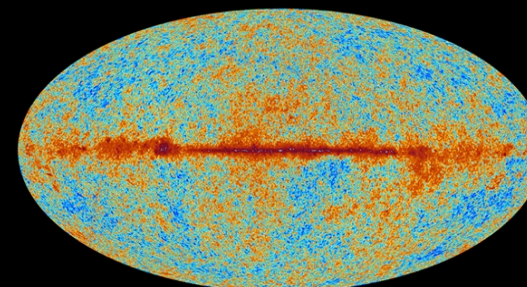
The sky as seen by Planck



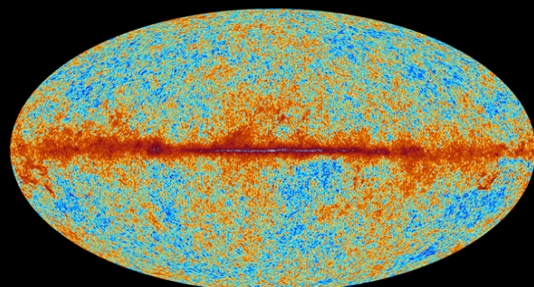
30 GHz



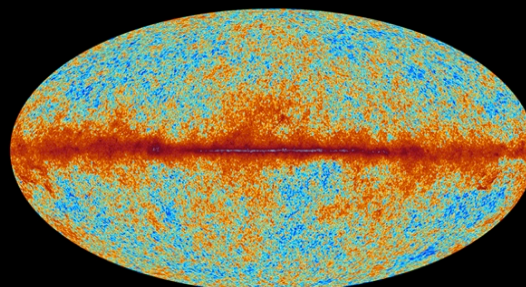
44 GHz



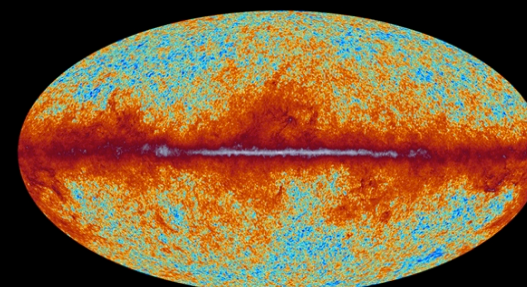
70 GHz



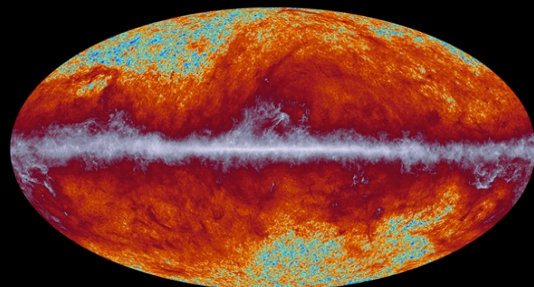
100 GHz



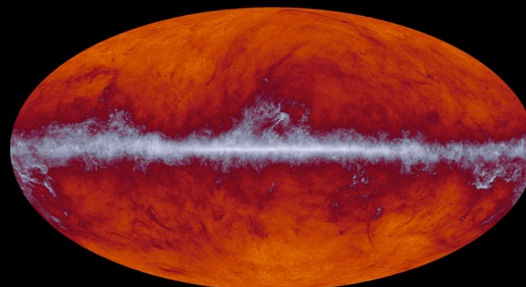
143 GHz



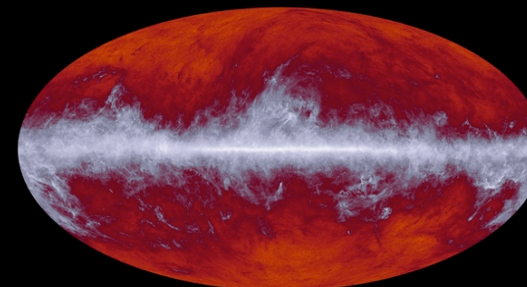
217 GHz



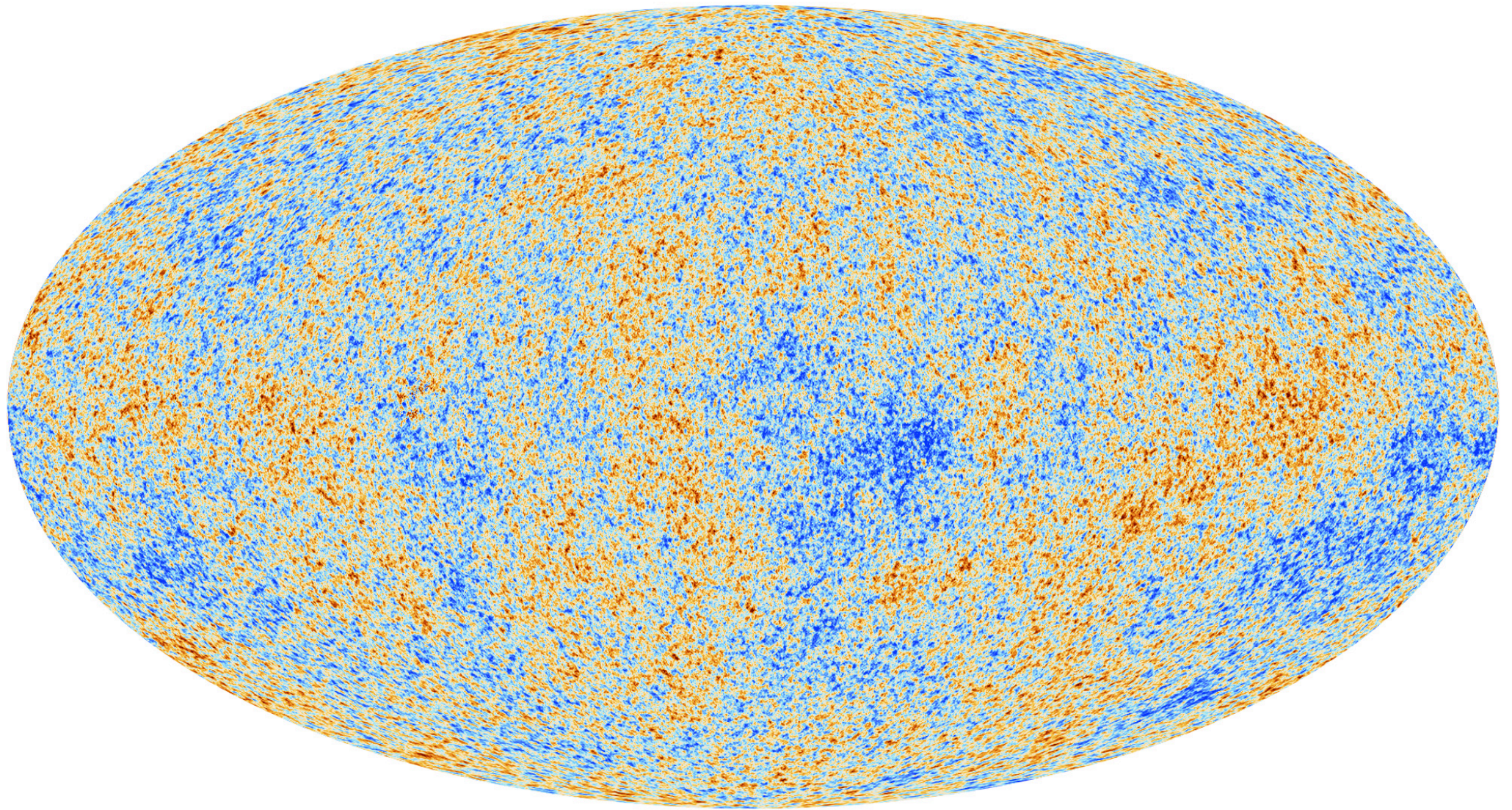
353 GHz



545 GHz



857 GHz

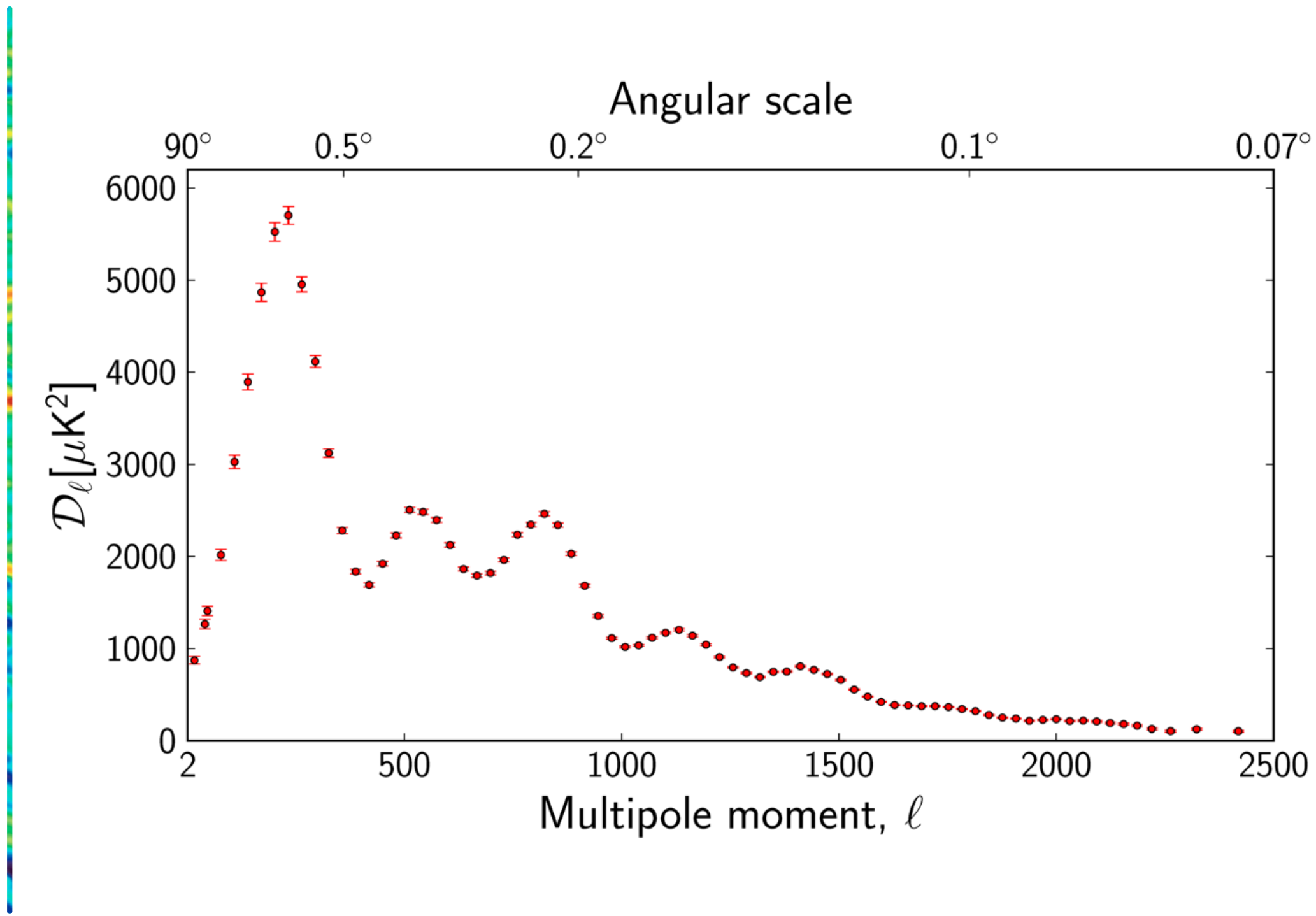


First Planck (almost) full sky CMB Temperature Map

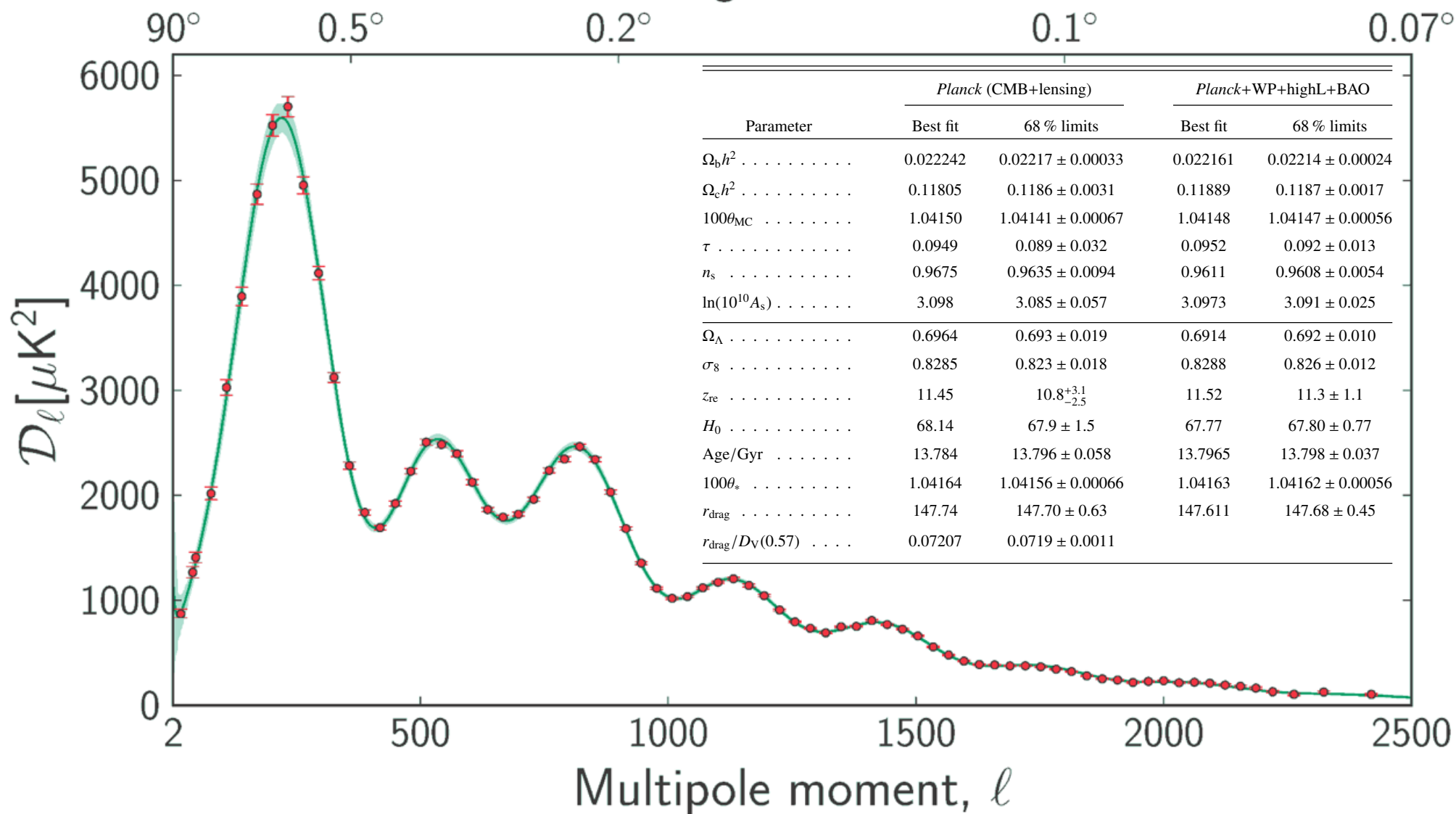
Released March 2013, along with 28 articles

Data available : first year maps and map characterisation

<http://pla.esac.esa.int/pla/aio/planckProducts.html>



Angular scale



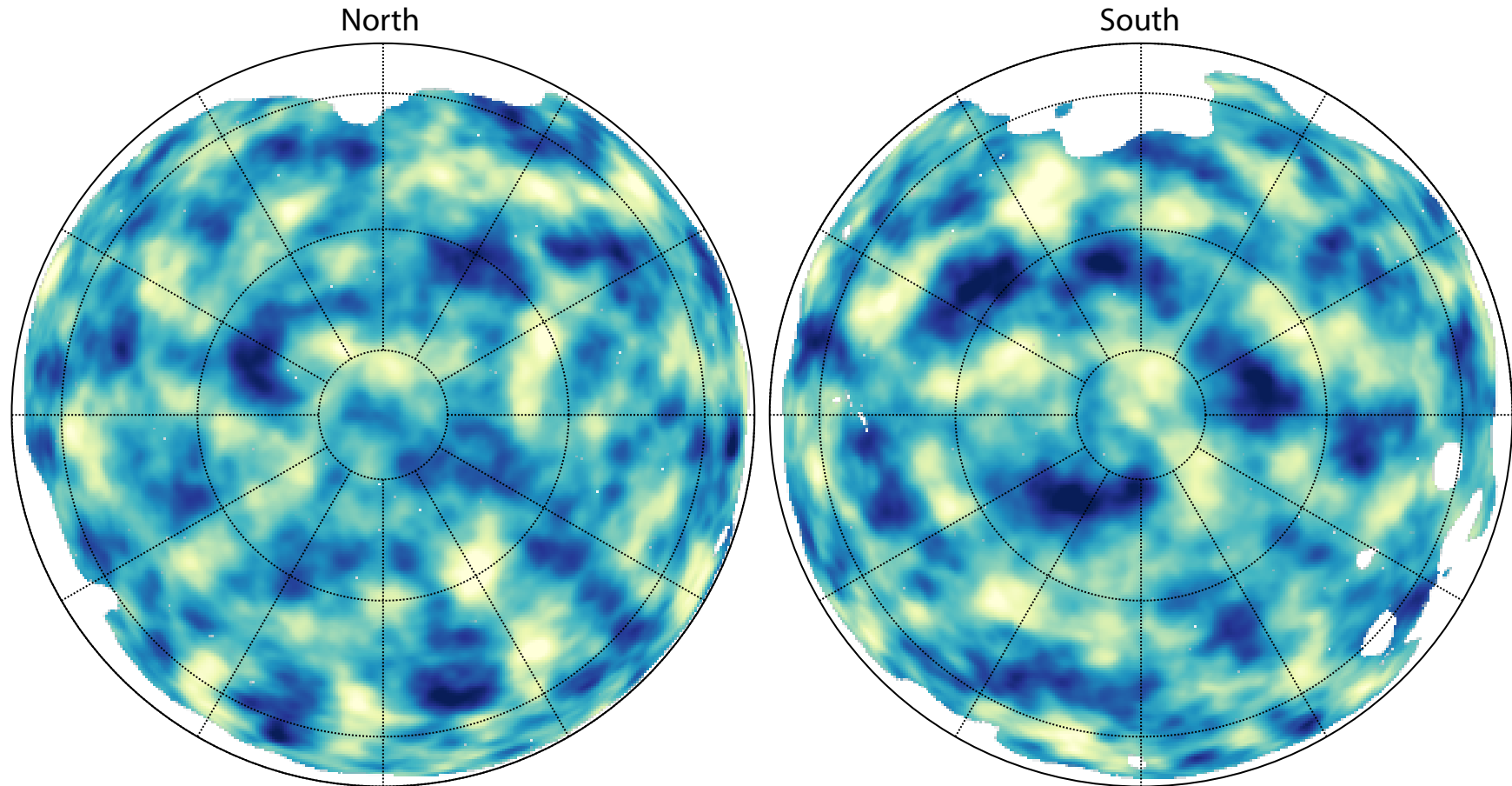
**Amazing fit to the theory
6 parameter model!**

Planck as a Matter tracer machine



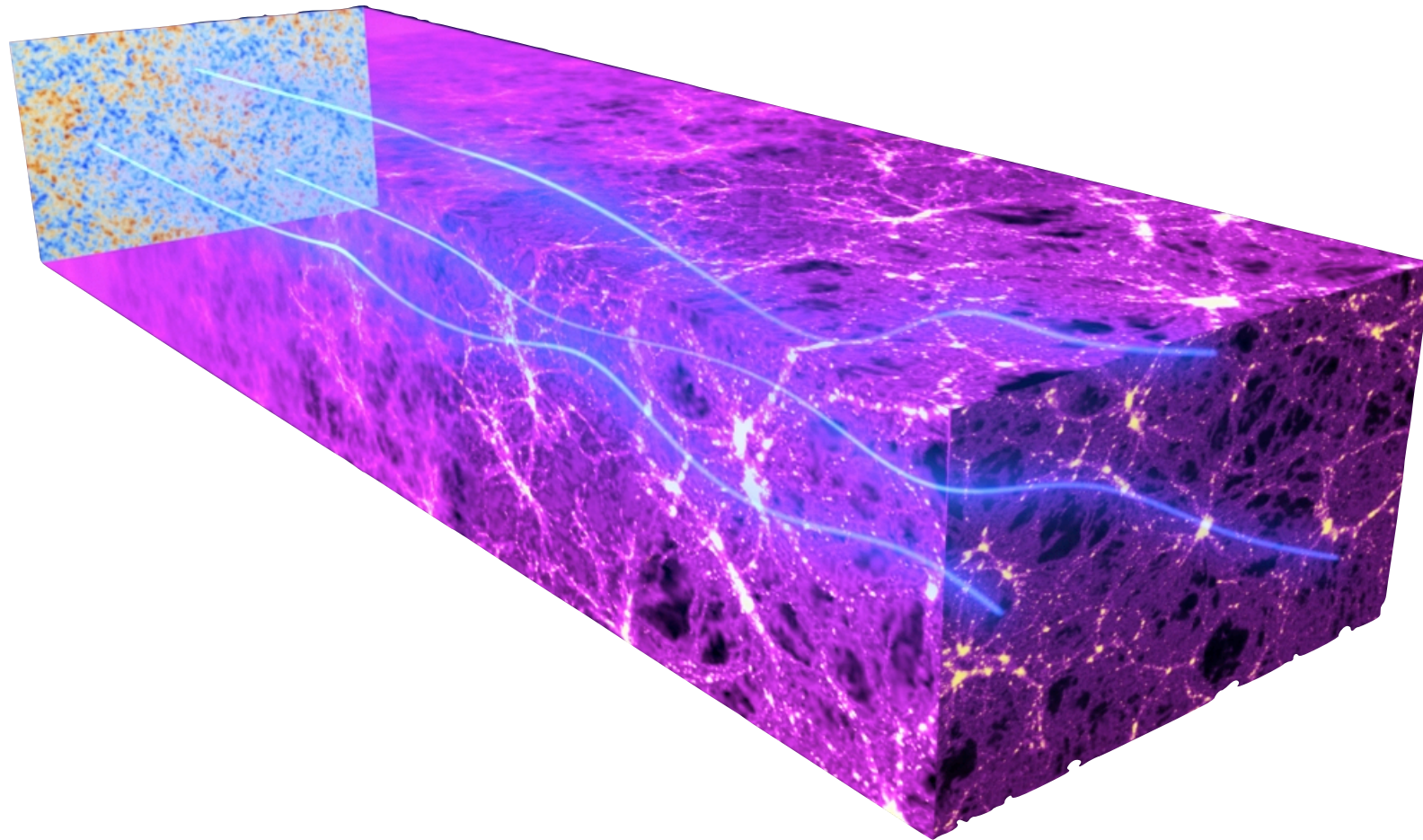
- Planck is the first full sky mission capable of measuring secondary anisotropies & small scale foregrounds
 - Tracer of the large scale structure at lower redshift
- Dark matter and baryons
 - **Weak lensing**
 - ISW
 - SZ clusters
 - CIB

Planck map of the large scale structures

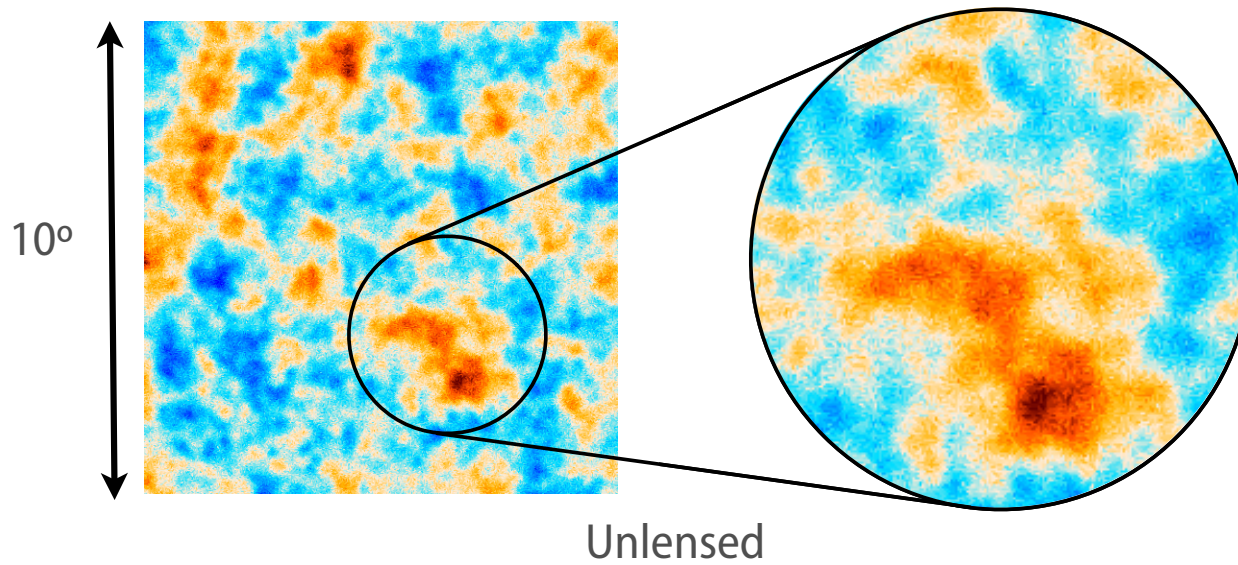
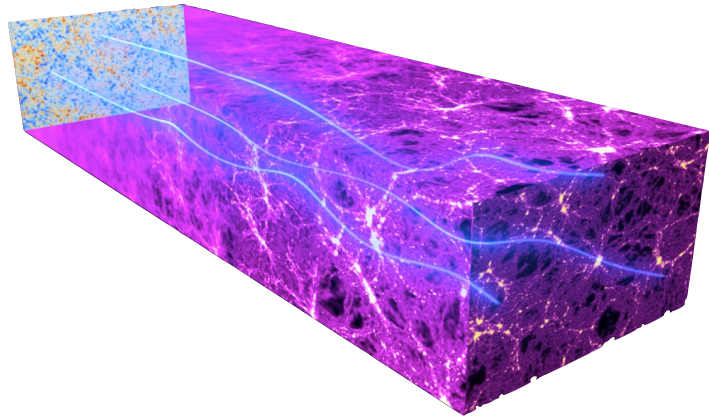


According to our reconstruction of the lensing effect
25sigma detection
Almost full sky map of LSS at $z \sim 2$

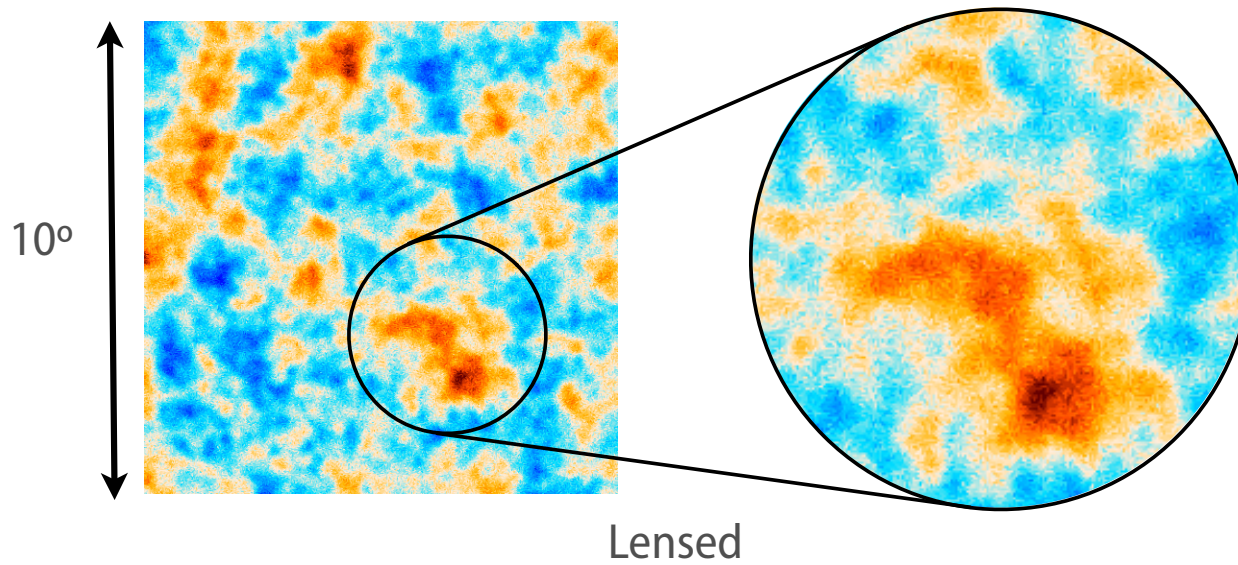
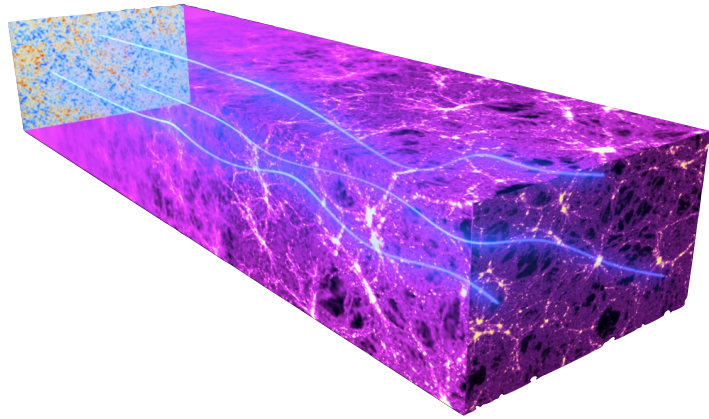
CMB lensing reconstruction



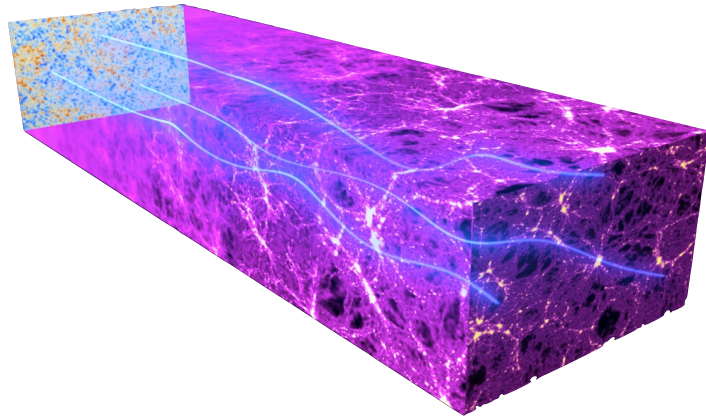
CMB lensing reconstruction



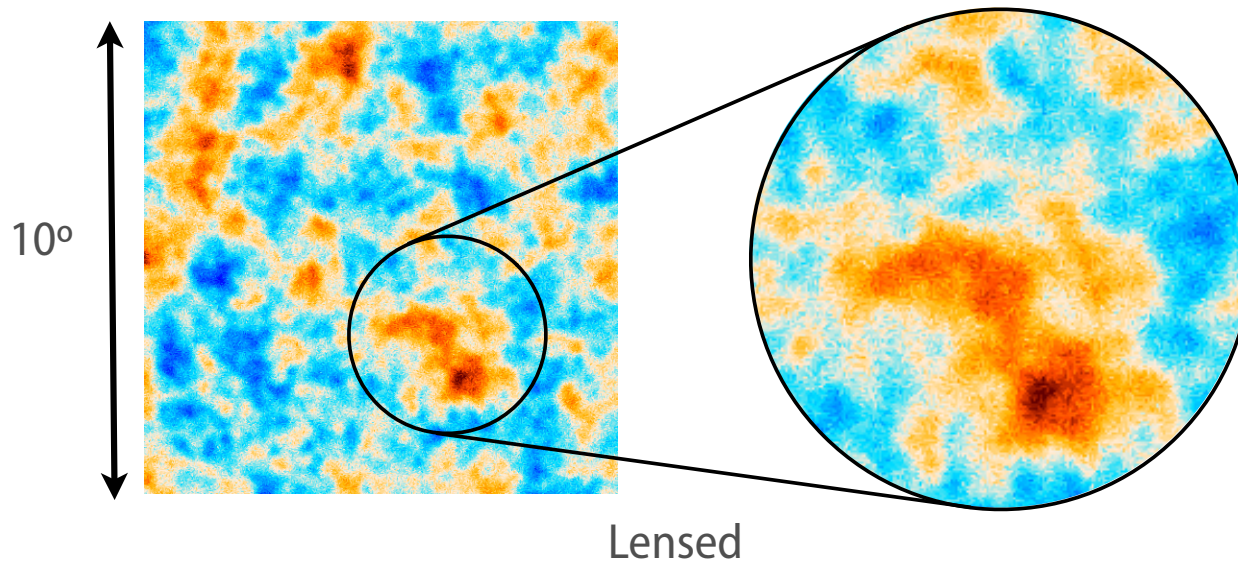
CMB lensing reconstruction



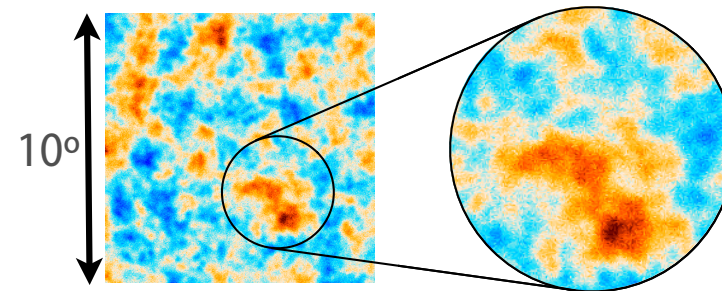
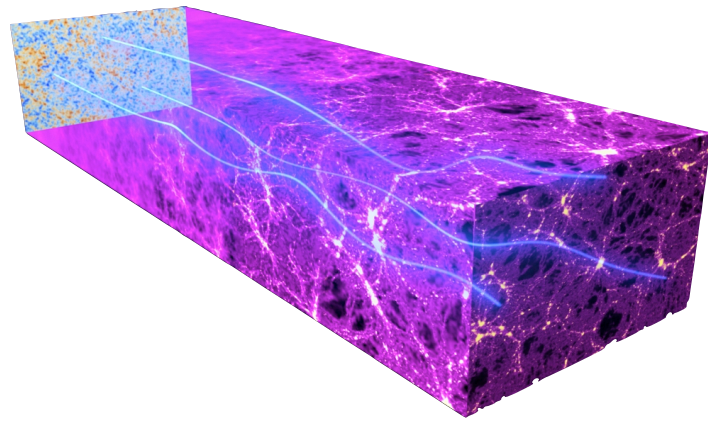
CMB lensing reconstruction



Displacement is 0.3 arcmin scale.
HFI beam is 5 arcmin at best



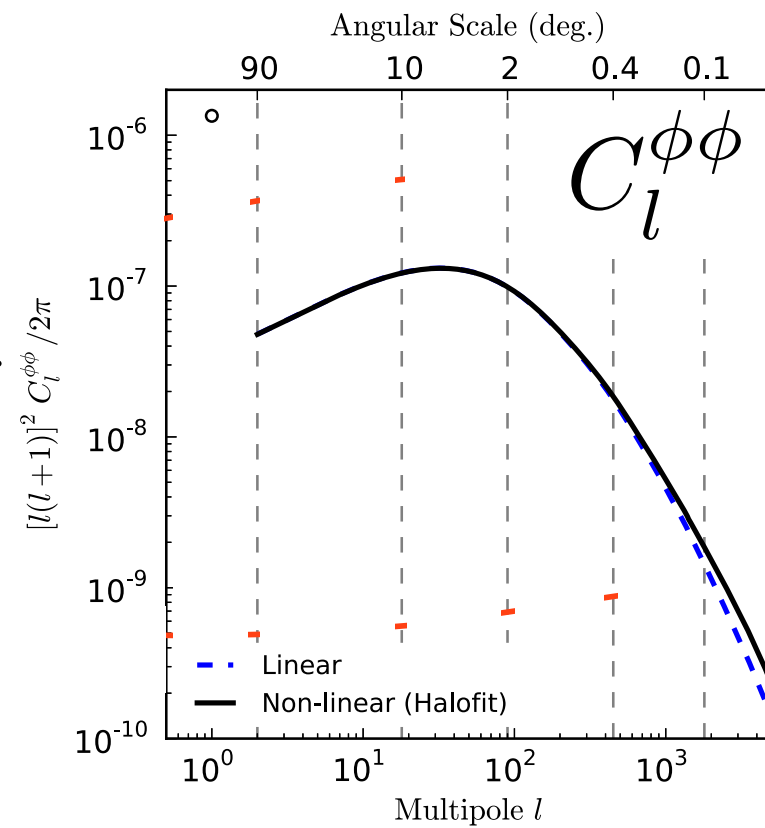
CMB lensing reconstruction



Lensing on CMB is small BUT

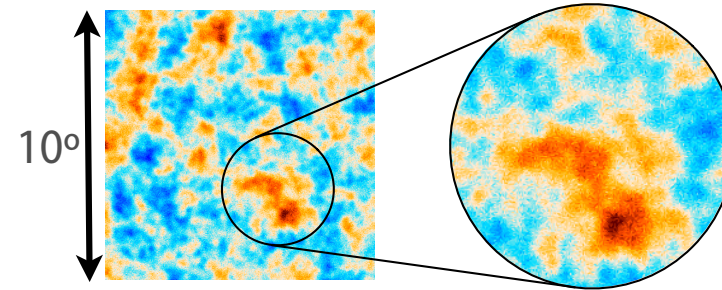
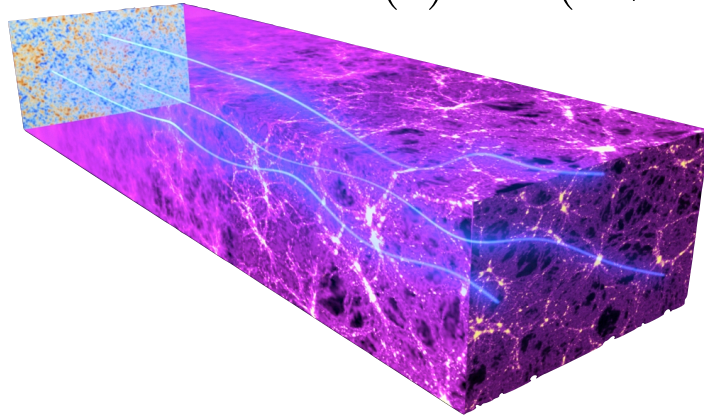
$$\hat{T}(\vec{\theta}) = T(\vec{\theta} + \vec{\nabla}\phi) \approx T(\vec{\theta}) + \vec{\nabla}\phi \cdot \vec{\nabla}T(\vec{\theta}) + \dots$$

It couples the Temperature anisotropies field with its gradient. And it's coherent on degree scales



CMB lensing reconstruction

$$\hat{T}(\vec{\theta}) = T(\vec{\theta} + \vec{\nabla}\phi) \approx T(\vec{\theta}) + \vec{\nabla}\phi \cdot \vec{\nabla}T(\vec{\theta}) + \dots$$



A quadratic estimator to measure the specific NG signature.

$$\Delta\langle T_{\ell_1 m_1} T_{\ell_2 m_2} \rangle = \sum_{LM} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^\phi \phi_{LM},$$

$$W_{\ell_1 \ell_2 L}^\phi = -\sqrt{\frac{(2\ell_1 + 1)(2\ell_2 + 1)(2L + 1)}{4\pi}} \sqrt{L(L + 1)\ell_1(\ell_1 + 1)}$$

$$\times C_{\ell_1}^{TT} \left(\frac{1 + (-1)^{\ell_1 + \ell_2 + L}}{2} \right) \begin{pmatrix} \ell_1 & \ell_2 & L \\ 1 & 0 & -1 \end{pmatrix} + (\ell_1 \leftrightarrow \ell_2). \quad (6)$$

$$\hat{\phi}_{LM}^x = \frac{1}{\mathcal{R}_L^{x\phi}} \left(\bar{x}_{LM} - \bar{x}_{LM}^{MF} \right).$$

$$\mathcal{R}_L^{x\phi, (1)(2)} = \frac{1}{(2L + 1)} \sum_{\ell_1 \ell_2} \frac{1}{2} W_{\ell_1 \ell_2 L}^x W_{\ell_1 \ell_2 L}^\phi F_{\ell_1}^{(1)} F_{\ell_2}^{(2)}.$$

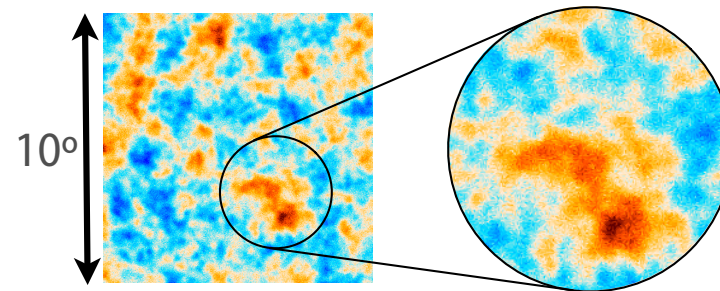
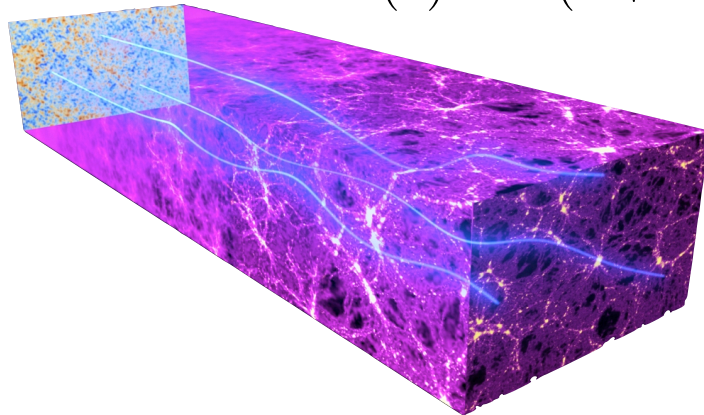
$$\bar{x}_{LM} = \frac{1}{2} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^x \bar{T}_{\ell_1 m_1}^{(1)} \bar{T}_{\ell_2 m_2}^{(2)}.$$

$$\bar{x}_{LM}^{MF} = \frac{1}{2} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^x \langle \bar{T}_{\ell_1 m_1}^{(1)} \bar{T}_{\ell_2 m_2}^{(2)} \rangle.$$

$$\bar{T}_{\ell m} = [S + N]^{-1} T_{\ell m} \approx [C_\ell^{TT} + C_\ell^{NN}]^{-1} T_{\ell m} = F_\ell T_{\ell m}$$

CMB lensing reconstruction

$$\hat{T}(\vec{\theta}) = T(\vec{\theta} + \vec{\nabla}\phi) \approx T(\vec{\theta}) + \vec{\nabla}\phi \cdot \vec{\nabla}T(\vec{\theta}) + \dots$$



A quadratic estimator to measure the specific NG signature.

$$\Delta\langle T_{\ell_1 m_1} T_{\ell_2 m_2} \rangle = \sum_{LM} \sum_{\ell_1 m_1, \ell_2 m_2} \bar{\phi} \equiv \Delta^{-1} \vec{\nabla} \cdot [C^{-1} T \vec{\nabla} (C_\ell \otimes C^{-1} T)] \quad (6)$$

$$W_{\ell_1 \ell_2 L}^\phi = -\sqrt{\frac{(2\ell_1 + 1)(2\ell_2 + 1)(2L + 1)}{4\pi}} \sqrt{L(L + 1)\ell_1(\ell_1 + 1)}$$

$$W^\phi(l_1, l_2) = C_{|l_1|}^{TT} l_1 \cdot L + C_{|l_2|}^{TT} l_2 \cdot L.$$

- Take two temperature maps and inverse variance filter them.

- Differentiate one and filter it by the temperature power spectrum

$$\hat{\phi}_{LM}^x = \frac{1}{\mathcal{R}_L^{x\phi}} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^{m_1} \binom{\ell_1}{m_1} \binom{\ell_2}{m_2} W_{\ell_1 \ell_2 L}^x \bar{T}_{\ell_1 m_1}^{(1)} \bar{T}_{\ell_2 m_2}^{(2)}$$

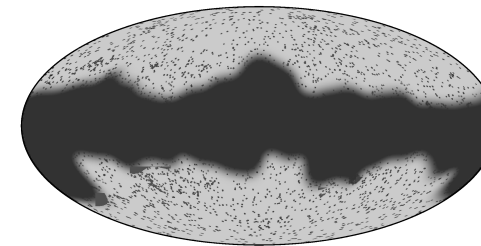
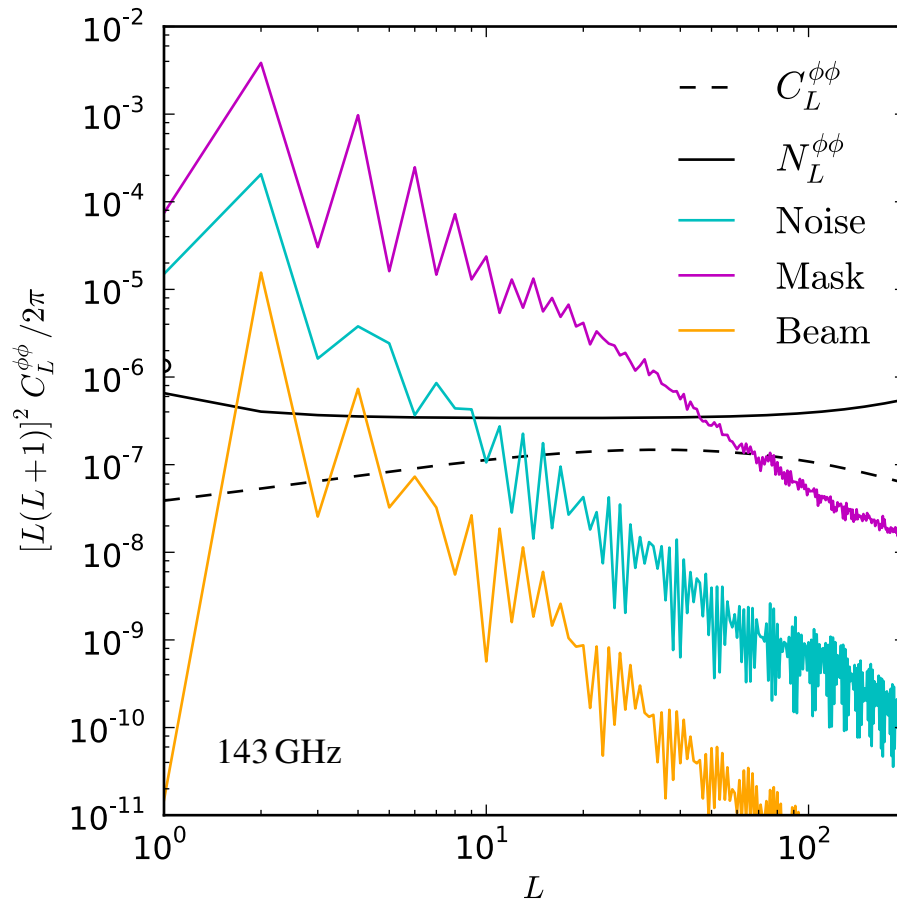
- Multiply with the other inverse variance filtered map

- Normalize to get unbiased estimator

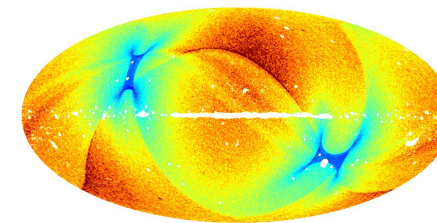
$$\mathcal{R}_L^{x\phi, (1)(2)} = \frac{1}{(2L + 1)} \sum_{\ell_1 \ell_2} \frac{1}{2} W_{\ell_1 \ell_2 L}^x W_{\ell_1 \ell_2 L}^\phi F_{\ell_1}^{(1)} F_{\ell_2}^{(2)}$$

$$\bar{T}_{\ell m} = [S + N]^{-1} T_{\ell m} \approx [C_\ell^{TT} + C_\ell^{NN}]^{-1} T_{\ell m} = F_\ell T_{\ell m}$$

Biases at the map level

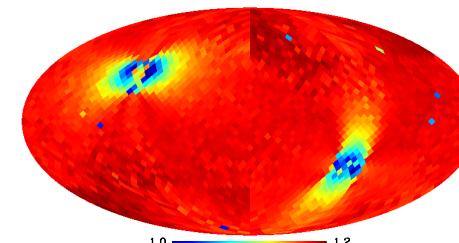


Mask



noise RMS

Ellipticity - 100 GHz

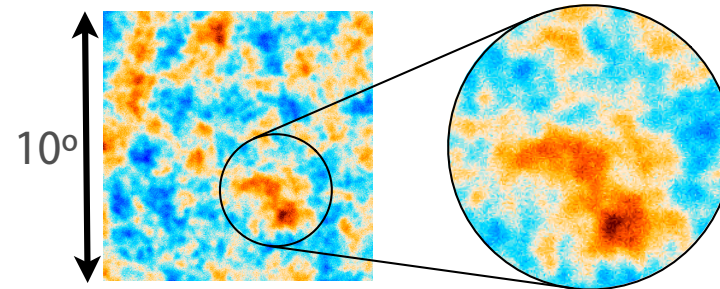
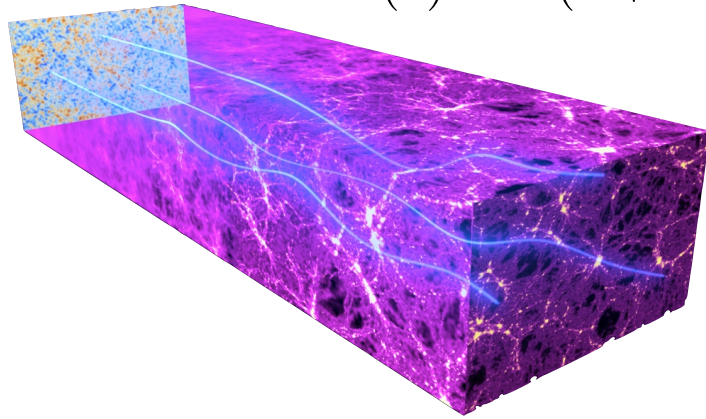


Beam ellipticity

Due to the response of the quadratic estimator to sources of statistical anisotropies in the data.
 Dominates the largest scales.
 Can be removed on average by estimating a «mean-field» contribution from Monte Carlo.

CMB lensing reconstruction

$$\hat{T}(\vec{\theta}) = T(\vec{\theta} + \vec{\nabla}\phi) \approx T(\vec{\theta}) + \vec{\nabla}\phi \cdot \vec{\nabla}T(\vec{\theta}) + \dots$$



A quadratic estimator to measure the specific NG signature.

$$\Delta \langle T_{\ell_1 m_1} T_{\ell_2 m_2} \rangle = \sum_{LM} \sum_{\ell_1 m_1, \ell_2 m_2} \bar{\phi} = \Delta^{-1} \vec{\nabla} \cdot [C^{-1} T \times \vec{\nabla} (C^{-1} T)]_{\ell_1 \ell_2 L} + (\ell_1 \leftrightarrow \ell_2). \quad (6)$$

- Take two temperature maps and inverse variance filter them.

- Differentiate one and filter it by the temperature power spectrum

- Multiply with the other inverse variance filtered map

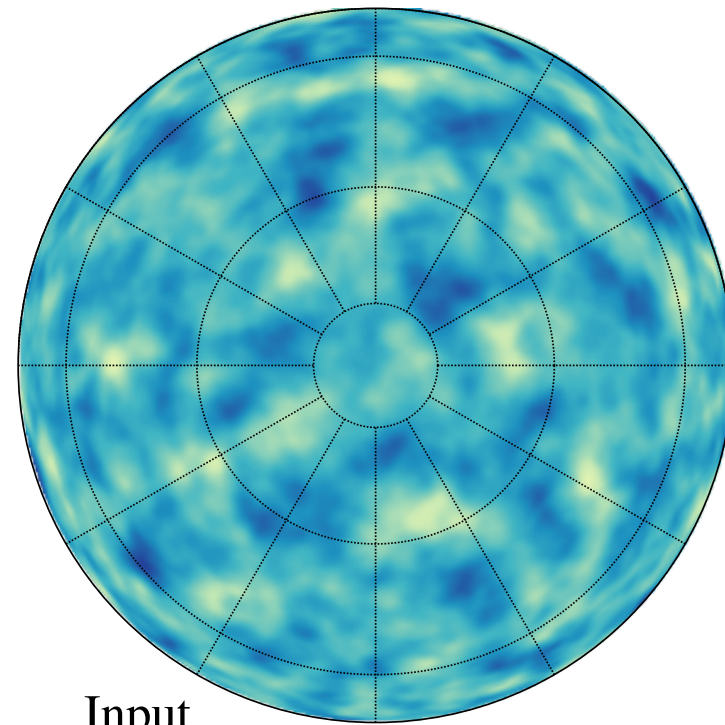
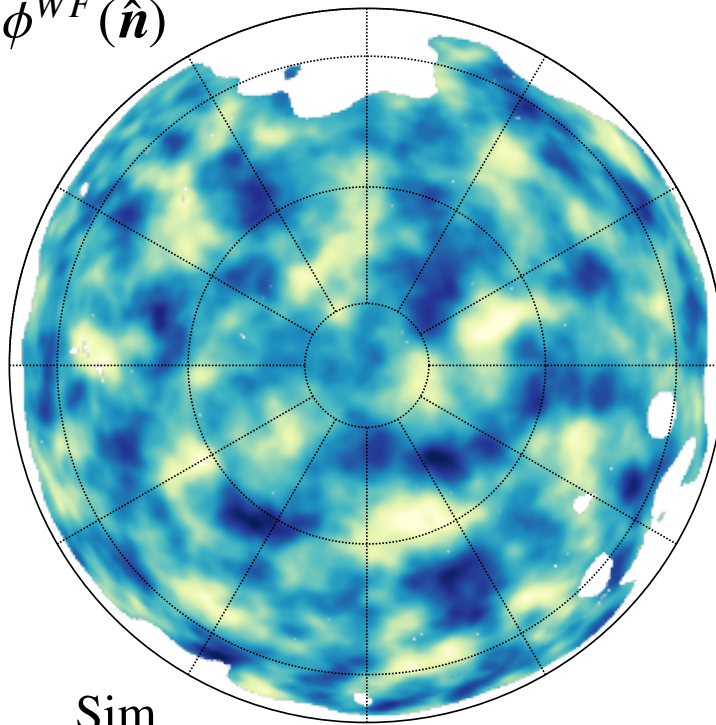
- Do the same with a set of CMB simulations containing your source of statistical anisotropies (mask, noise, beams)

- Take the difference and normalize

$$\mathcal{R}_L^{x\phi, (1)(2)} = \frac{1}{(2L+1)} \sum_{\ell_1 \ell_2} \frac{1}{2} W_{\ell_1 \ell_2 L}^x W_{\ell_1 \ell_2 L}^\phi$$

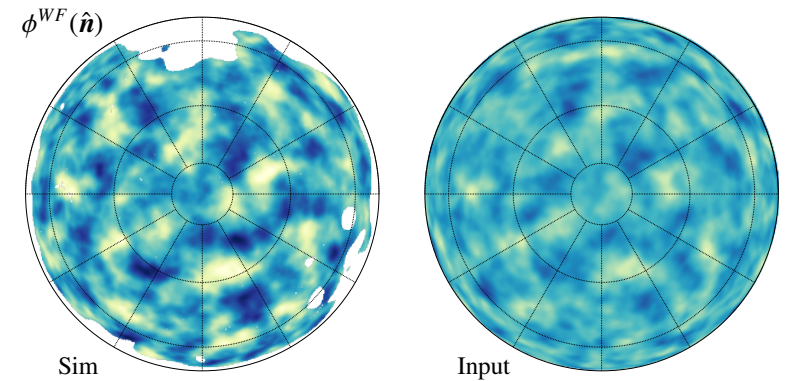
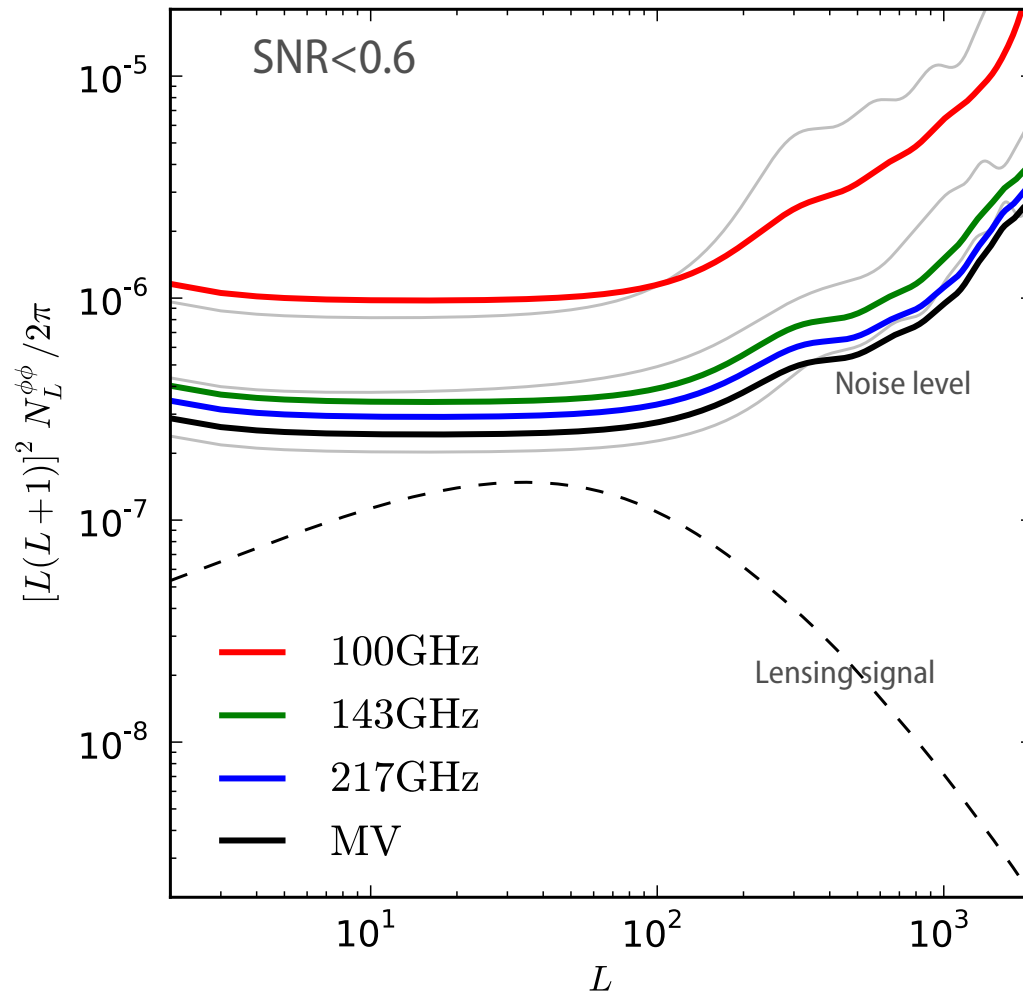
On simulation

$$\phi^{WF}(\hat{n})$$

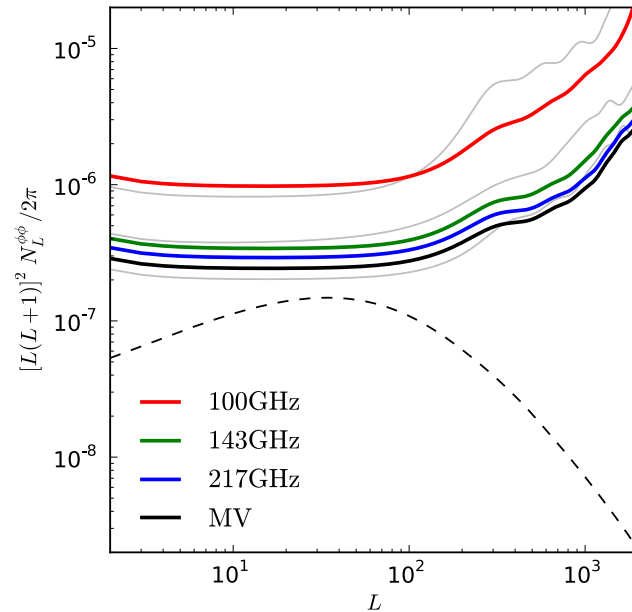


Reconstruction on a realistic Planck simulation.

Map noise - spectrum biases

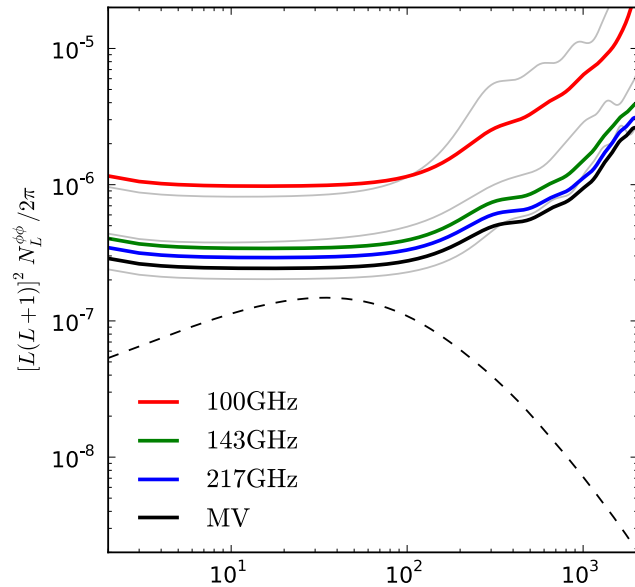


Power spectrum biases



$$\hat{C}_{L,x}^{\phi\phi} = \frac{f_{\text{sky},2}^{-1}}{2L+1} \sum_M |\tilde{\phi}_{LM}^x|^2 - \Delta C_L^{\phi\phi} |_{N0} - \Delta C_L^{\phi\phi} |_{N1} - \Delta C_L^{\phi\phi} |_{PS} - \Delta C_L^{\phi\phi} |_{MC},$$

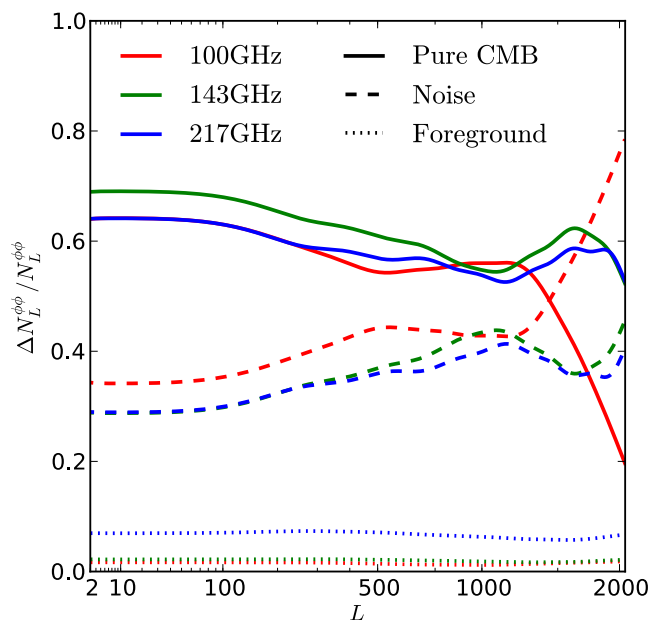
Power spectrum biases



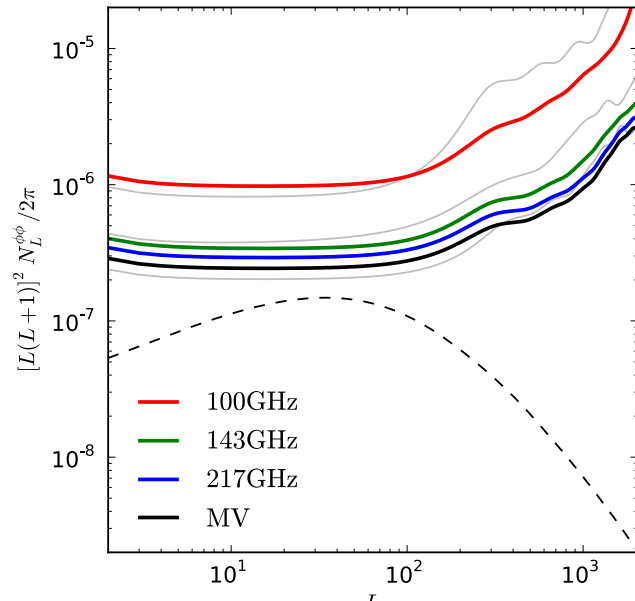
$$\hat{C}_{L,x}^{\phi\phi} = \frac{f_{\text{sky},2}^{-1}}{2L+1} \sum_M |\tilde{\phi}_{LM}^x|^2 - \Delta C_L^{\phi\phi} |_{N0} - \Delta C_L^{\phi\phi} |_{N1} - \Delta C_L^{\phi\phi} |_{PS} - \Delta C_L^{\phi\phi} |_{MC},$$

Gaussian bias. Dealt with by MC. Close to the analytical value.

Dominates the final error budget.



Power spectrum biases

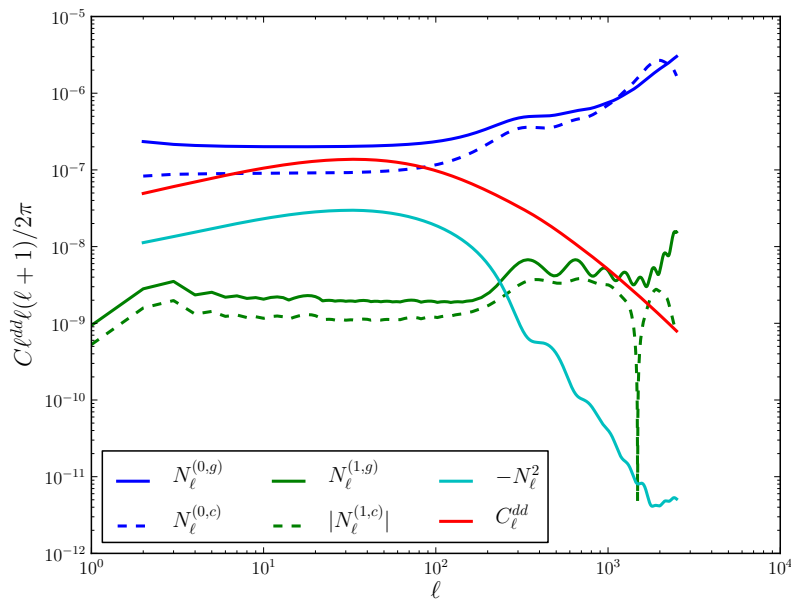


$$\hat{C}_{L,x}^{\phi\phi} = \frac{f_{\text{sky},2}^{-1}}{2L+1} \sum_M |\tilde{\phi}_{LM}^x|^2 - \Delta C_L^{\phi\phi} \Big|_{N0} - \Delta C_L^{\phi\phi} \Big|_{N1} - \Delta C_L^{\phi\phi} \Big|_{PS} - \Delta C_L^{\phi\phi} \Big|_{MC},$$

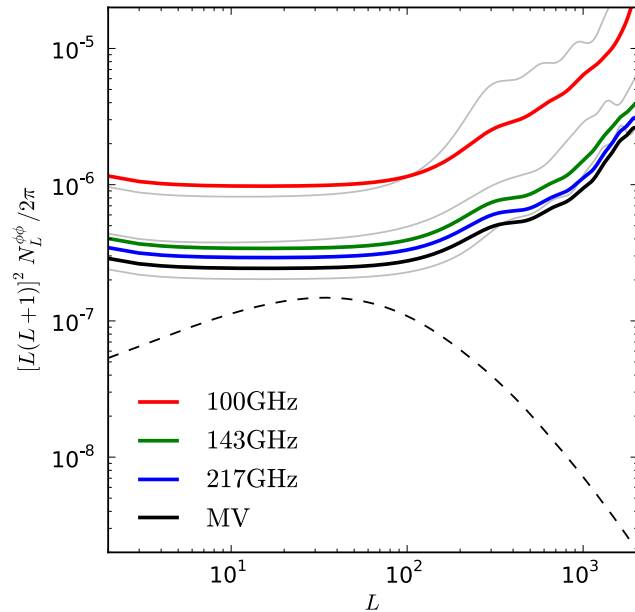
Gaussian bias. Dealt with by MC. Close to the analytical value.

Dominates the final error budget.

Higher order bias. We further include cosmological uncertainty.



Power spectrum biases



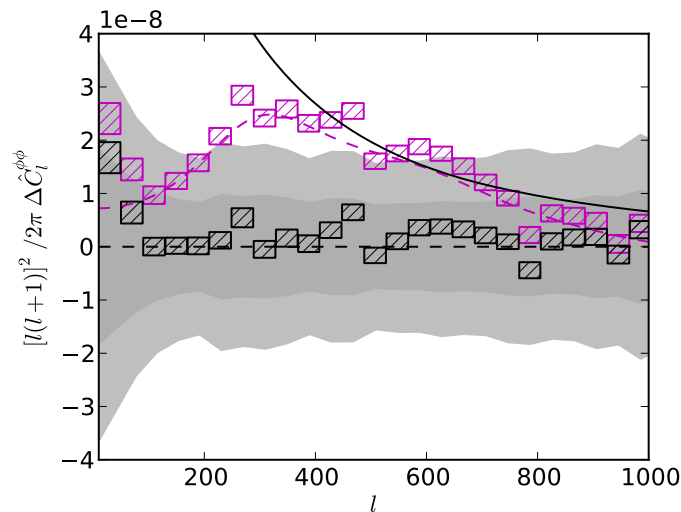
$$\hat{C}_{L,x}^{\phi\phi} = \frac{f_{\text{sky},2}^{-1}}{2L+1} \sum_M |\tilde{\phi}_{LM}^x|^2 - \Delta C_L^{\phi\phi}|_{N0} - \Delta C_L^{\phi\phi}|_{N1} - \Delta C_L^{\phi\phi}|_{PS} - \Delta C_L^{\phi\phi}|_{MC},$$

Gaussian bias. Dealt with by MC. Close to the analytical value.

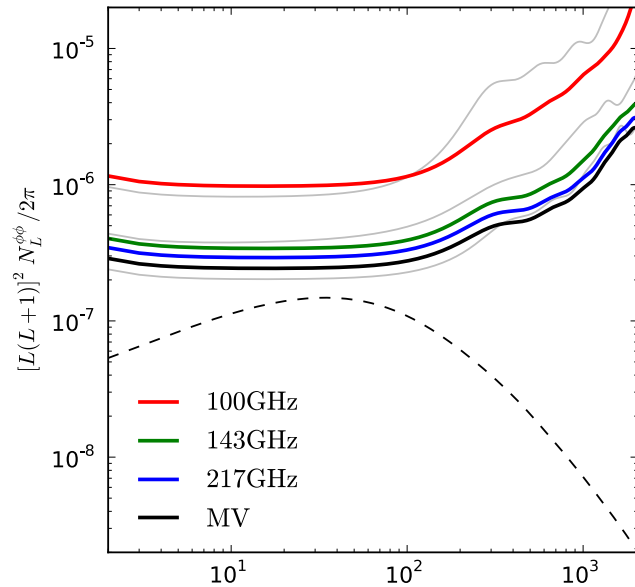
Dominates the final error budget.

Higher order bias. We further include cosmological uncertainty.

Point source trispectrum contribution. Measured on data



Power spectrum biases



$$\hat{C}_{L,x}^{\phi\phi} = \frac{f_{\text{sky},2}^{-1}}{2L+1} \sum_M |\tilde{\phi}_{LM}^x|^2 - \Delta C_L^{\phi\phi}|_{N0} - \Delta C_L^{\phi\phi}|_{N1} - \Delta C_L^{\phi\phi}|_{PS} - \Delta C_L^{\phi\phi}|_{MC}$$

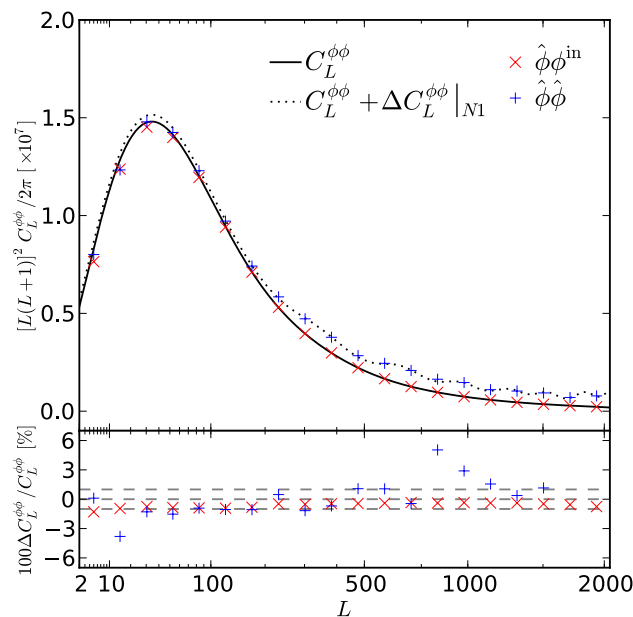
Gaussian bias. Dealt with by MC. Close to the analytical value.

Dominates the final error budget.

Higher order bias. We further include cosmological uncertainty.

Point source trispectrum contribution. Measured on data

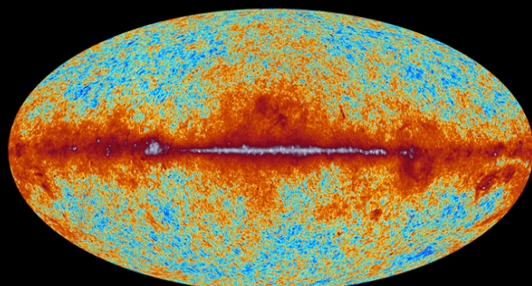
Residual bias. Also account for small multiplicative bias. Dealt with lensed MC.



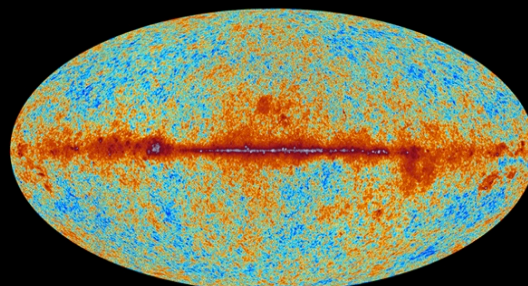


planck

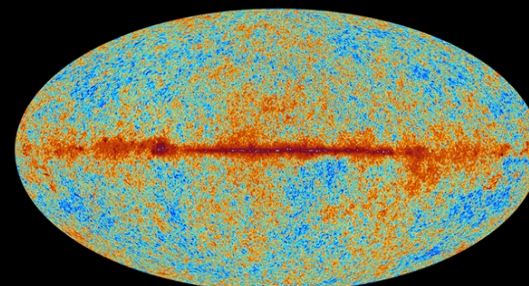
The sky as seen by Planck



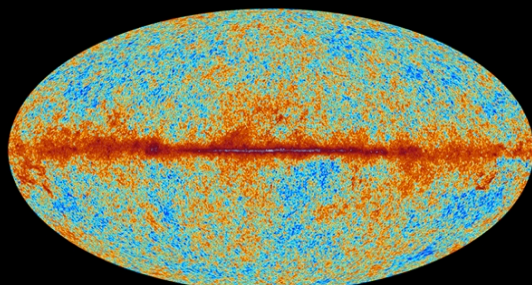
30 GHz



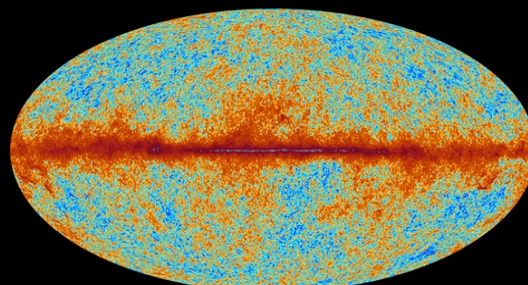
44 GHz



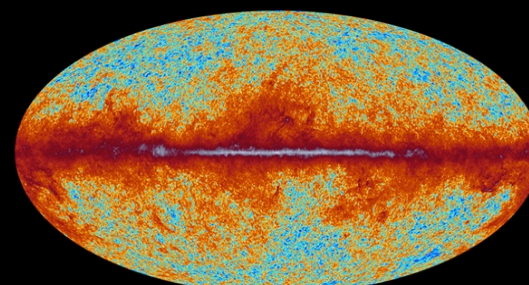
70 GHz



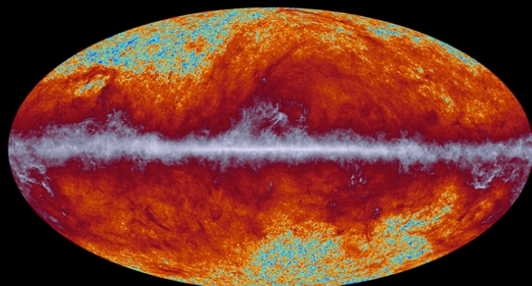
100 GHz



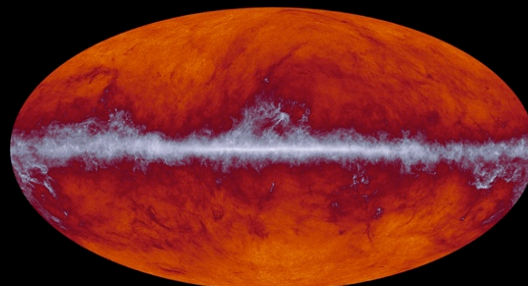
143 GHz



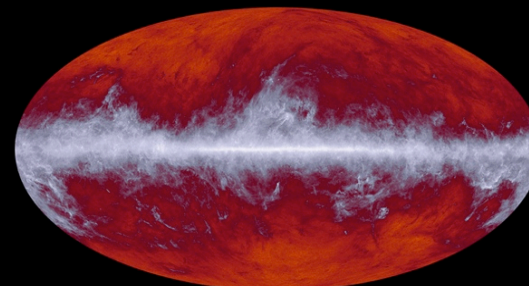
217 GHz



353 GHz



545 GHz

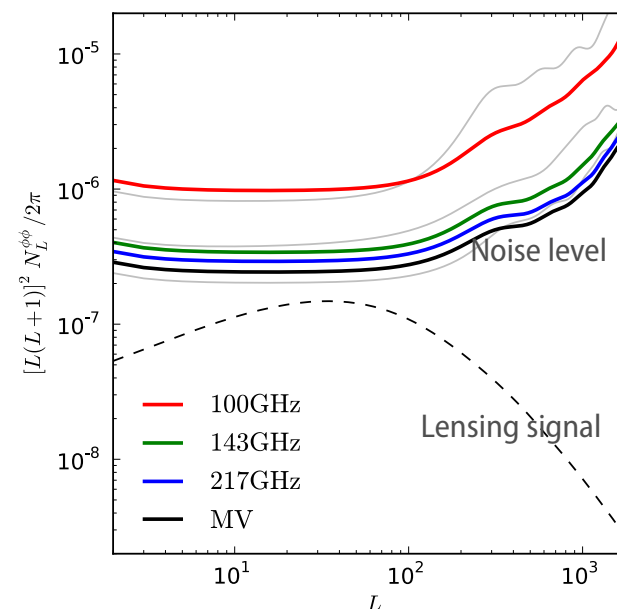


857 GHz

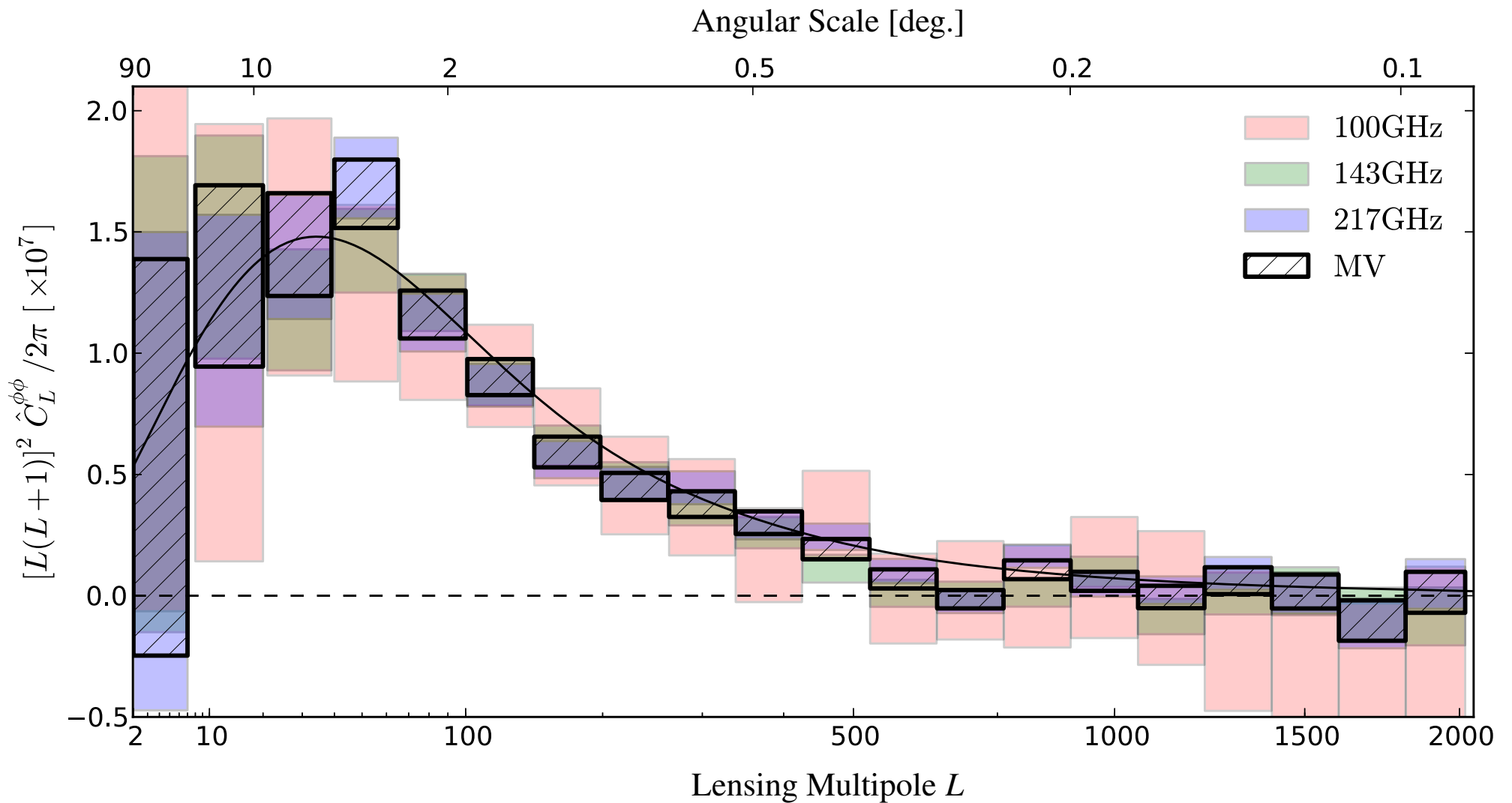
Best reconstruction



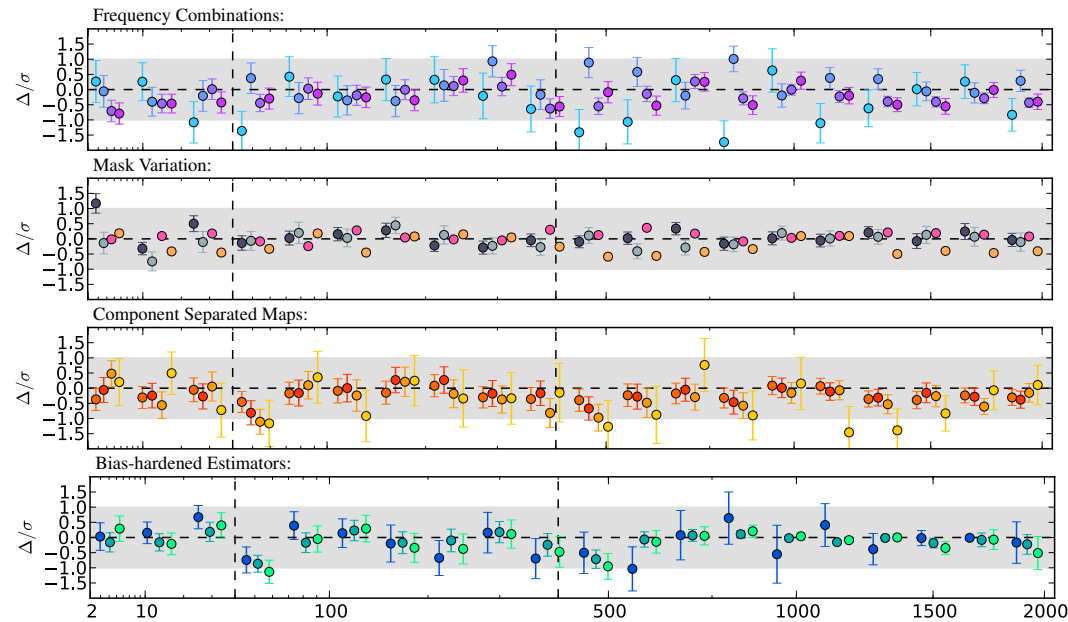
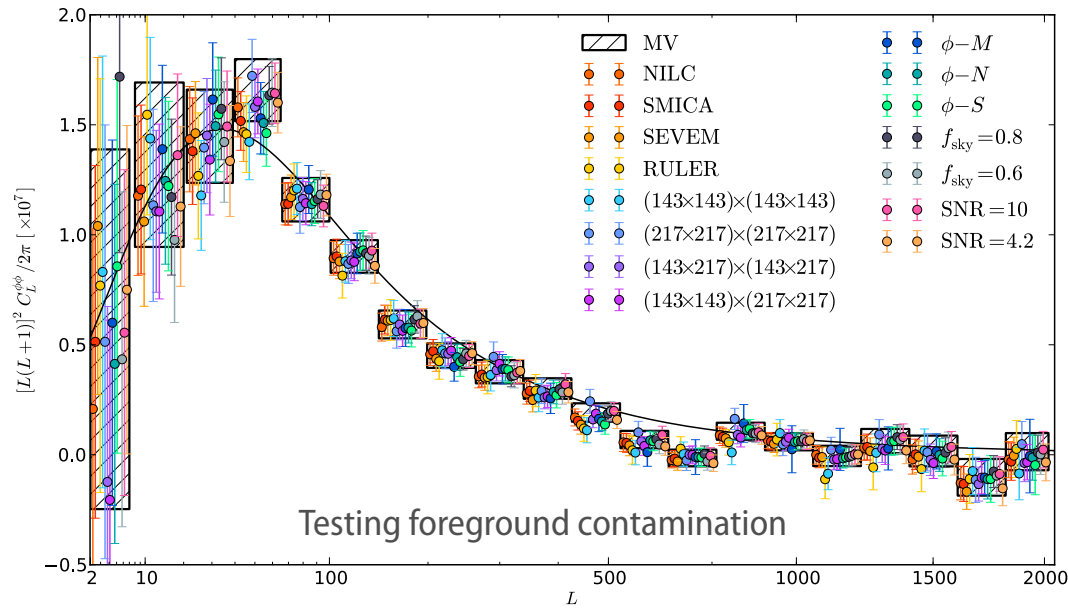
- MV combination between the 143GHz & 217GHz
- 857GHz used as a template for dust cleaning
- 30% Galactic mask + CO mask + point sources SNR5
- 5° apodization (for power spectrum estimation)
- fsky = 0.67



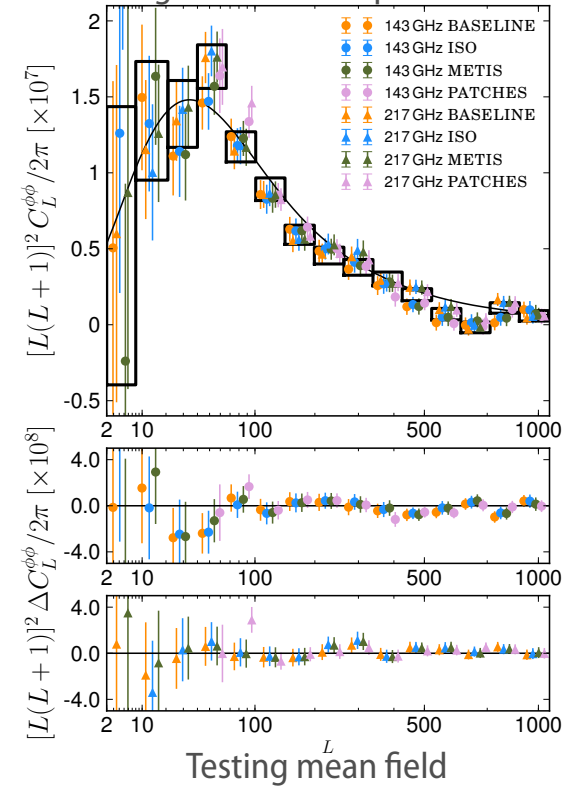
CMB lensing reconstruction



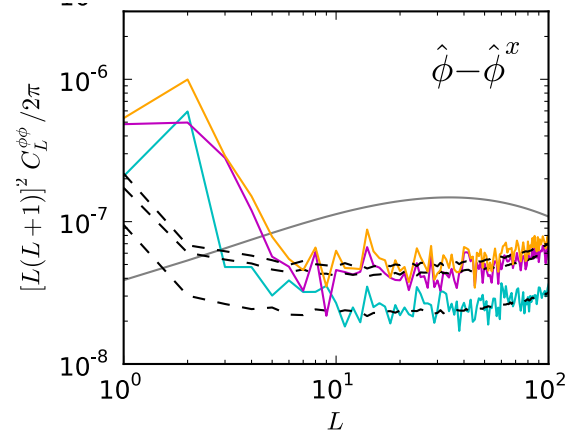
Robustness



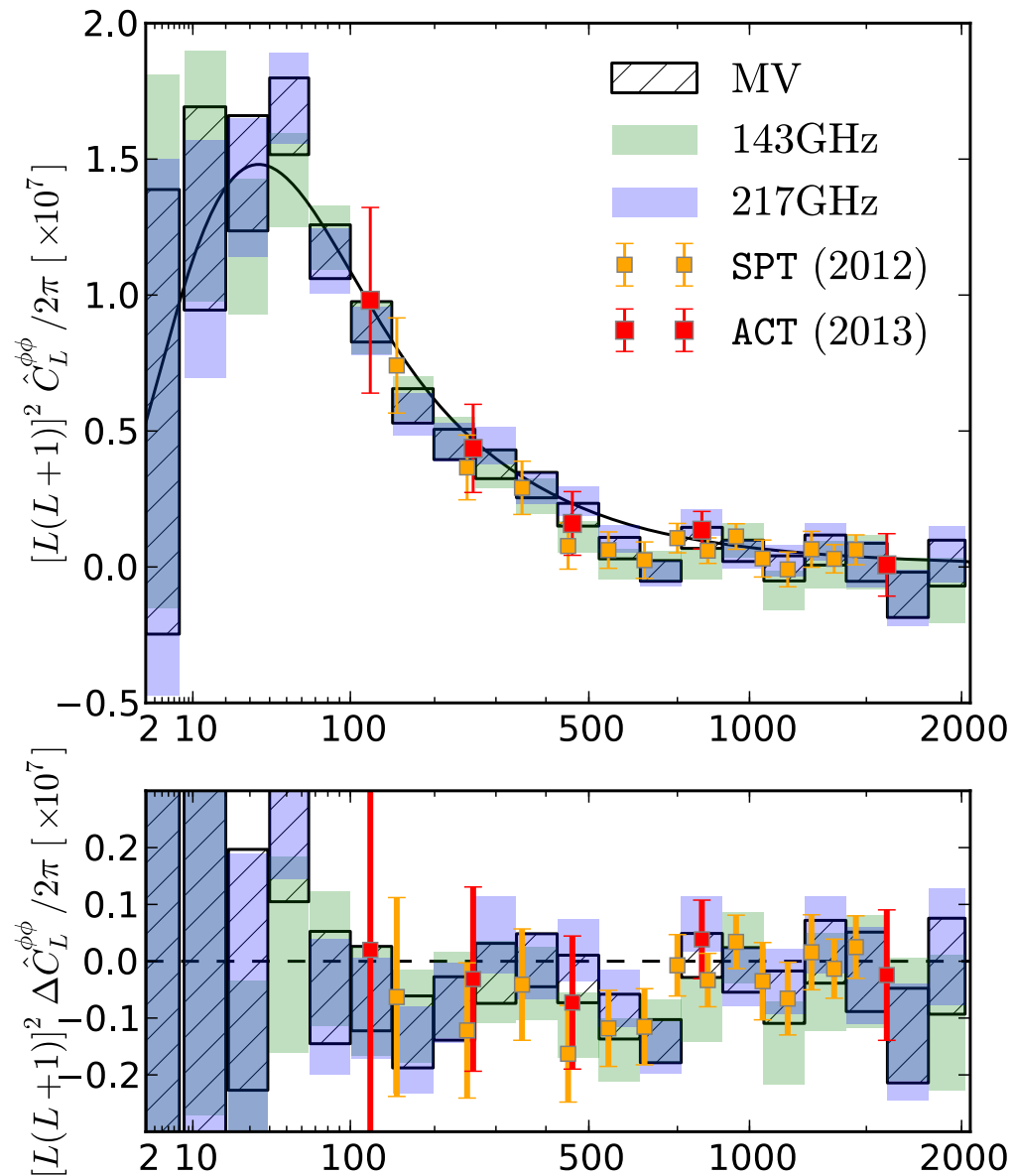
Testing the filter & implementation



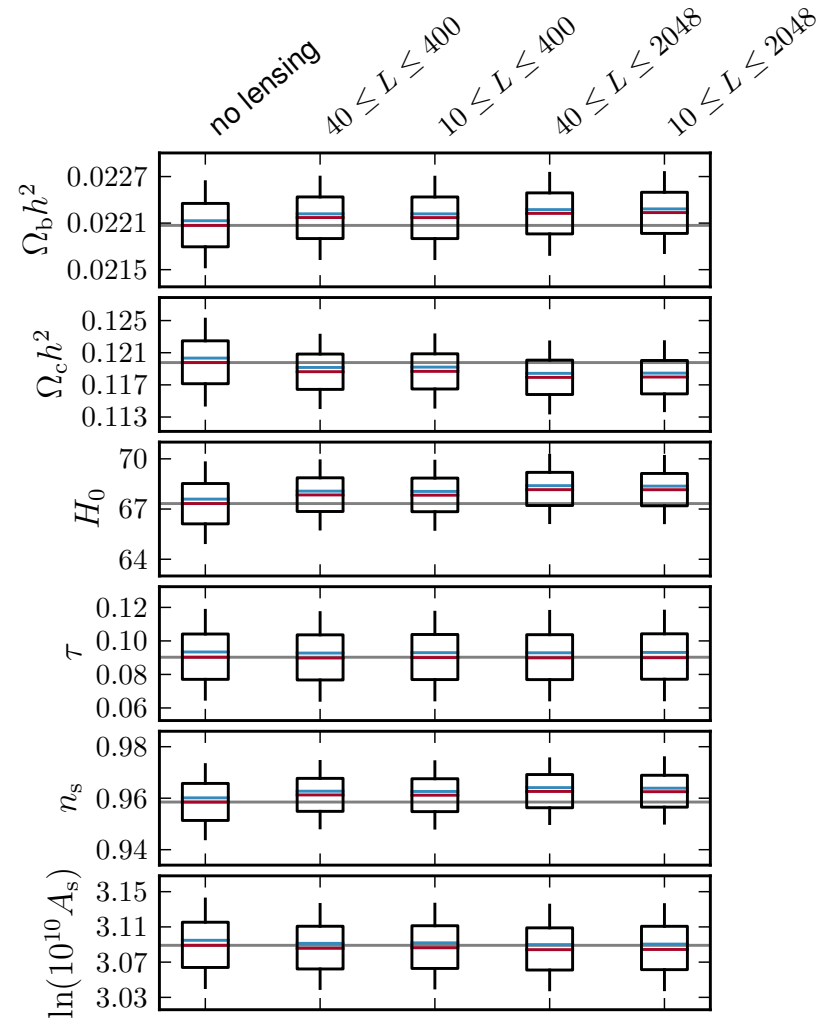
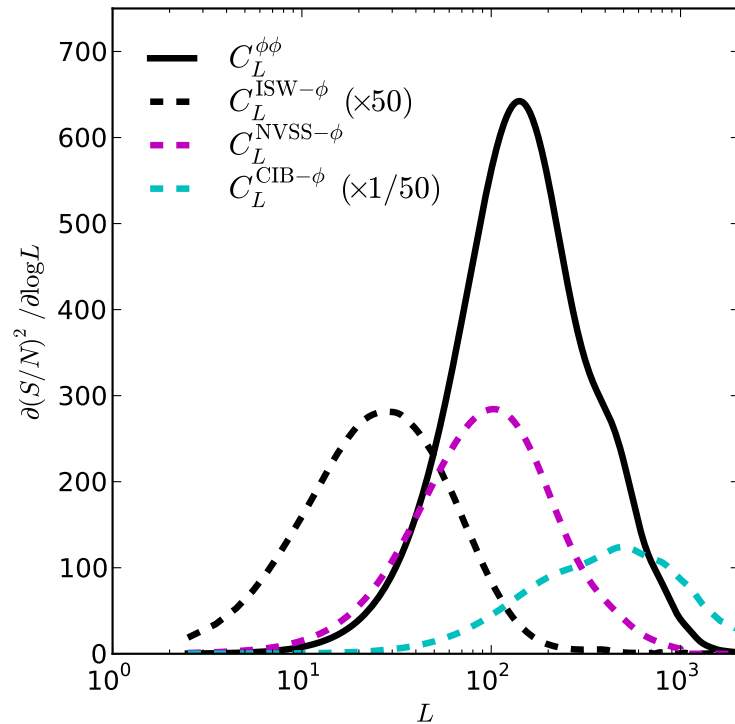
Testing mean field



Comparison to other surveys



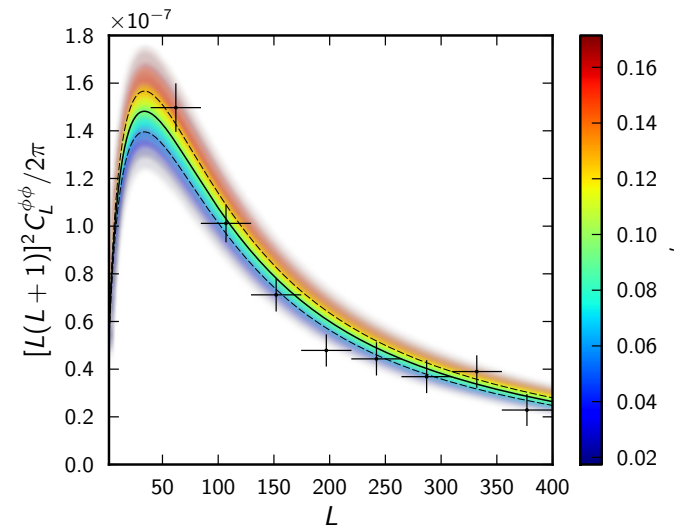
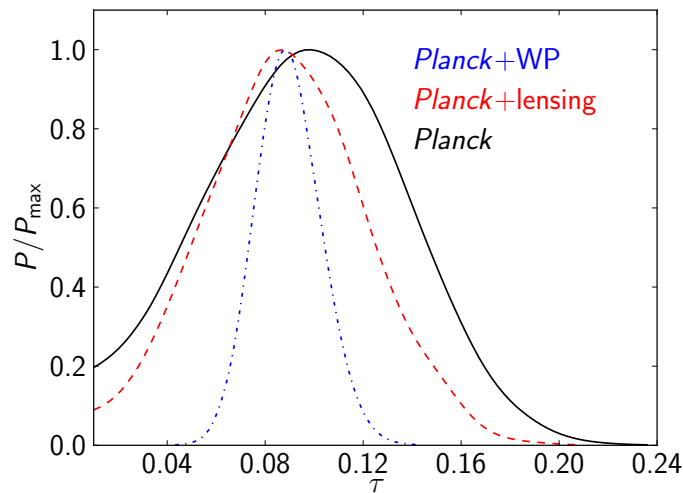
Cosmology



We are using the most significant (and cleanest) part of the data $L=40-400$. Lensing brings a 20%ish improvement on some of the vanilla LCDM parameters.

Cosmology - I

Constraining the reionization from Planck alone
strengthen the Polarization result



$$\tau = 0.097 \pm 0.038 \quad (68\%; \text{Planck})$$

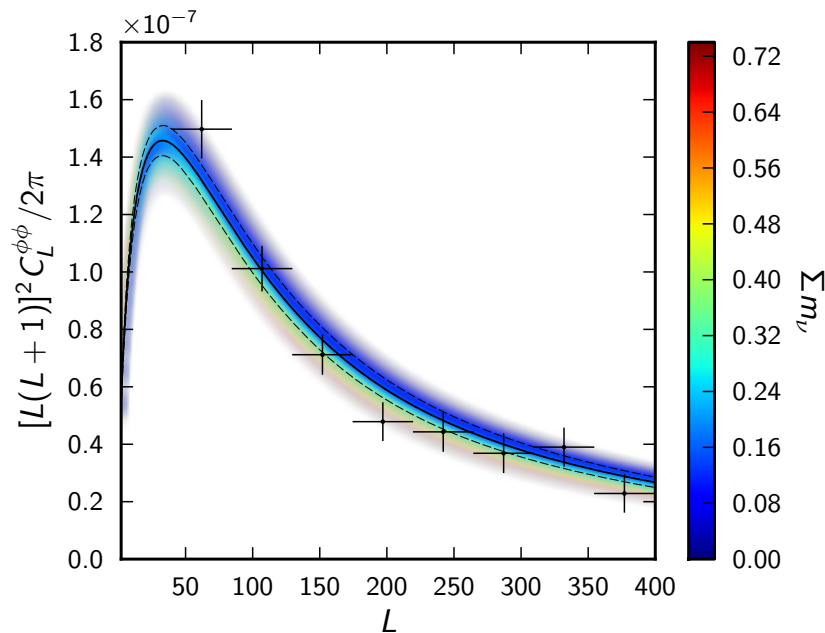
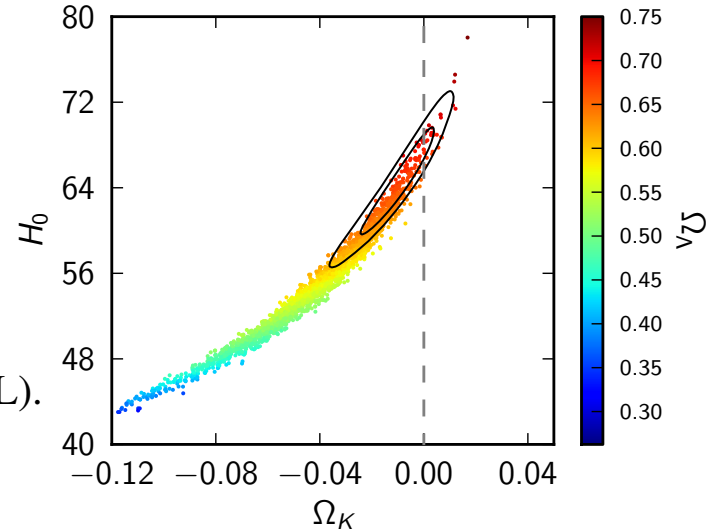
$$\tau = 0.089 \pm 0.032 \quad (68\%; \text{Planck+lensing}).$$

Cosmology - II

Breaking the geometrical degeneracy
 2+fold improvement on the errorbar
 3% precision determination of Dark Energy
 from CMB alone

$$\Omega_{\Lambda} = 0.57^{+0.073}_{-0.055} \quad (68\%; \text{Planck+WP+highL})$$

$$\Omega_{\Lambda} = 0.67^{+0.027}_{-0.023} \quad (68\%; \text{Planck+lensing+WP+highL}).$$



Mild tension with neutrino masses

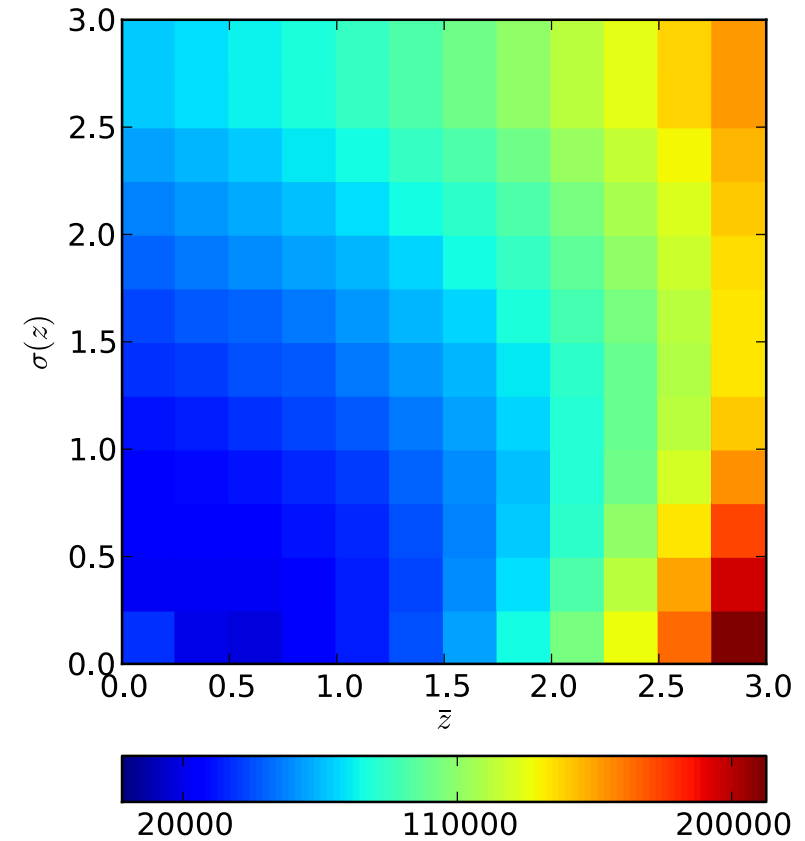
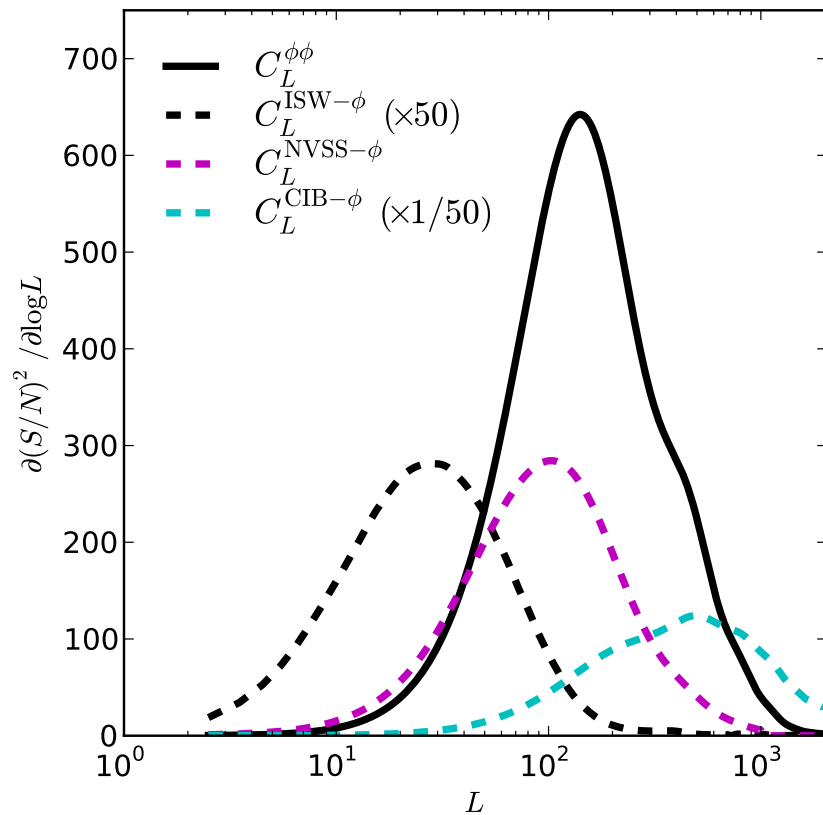
TT wants more lensing

TTTT wants less lensing

$$\sum m_{\nu} < 0.66 \text{ eV}, \quad (95\%; \text{Planck+WP+highL}),$$

$$\sum m_{\nu} < 0.85 \text{ eV}, \quad (95\%; \text{Planck+lensing+WP+highL}),$$

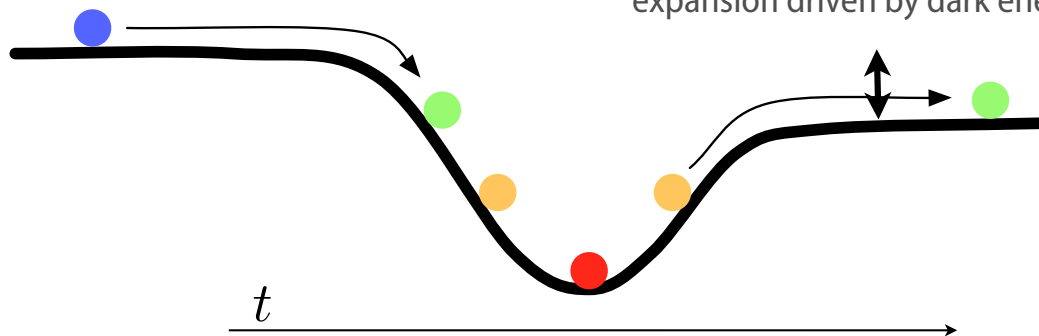
Cross correlation



Number of object needed for a 5sigma cross correlation with CMB lensing on 20% of the sky as a function of redshift and redshift dispersion

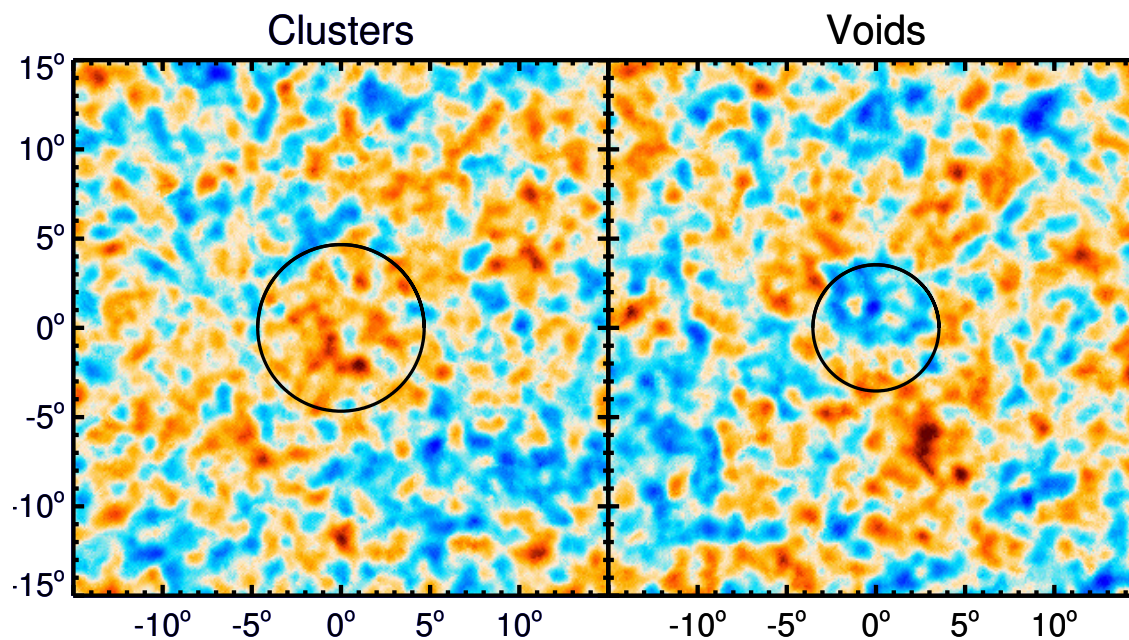
ISW

Shallowing of the potential due to expansion driven by dark energy



$$\frac{\Delta T}{T} = \frac{2}{c^3} \int_{\eta^*}^{\eta_0} d\eta \frac{\partial \Phi}{\partial \eta}$$

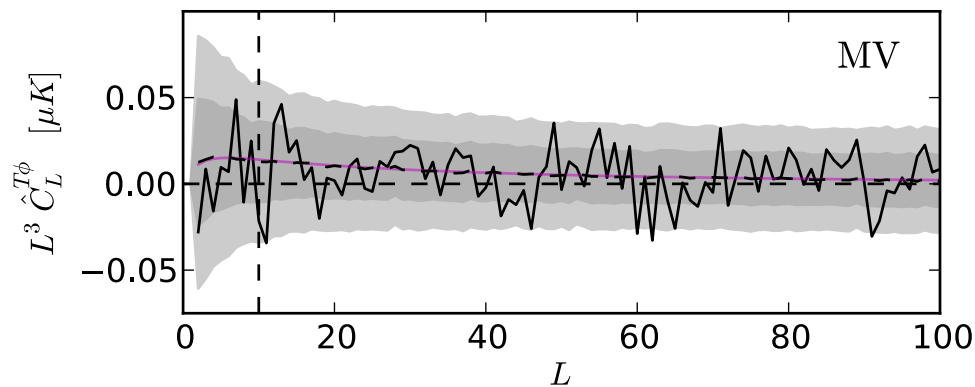
Stacking the *Planck* CMB at the location of clusters and voids



ISW - Lensing correlation



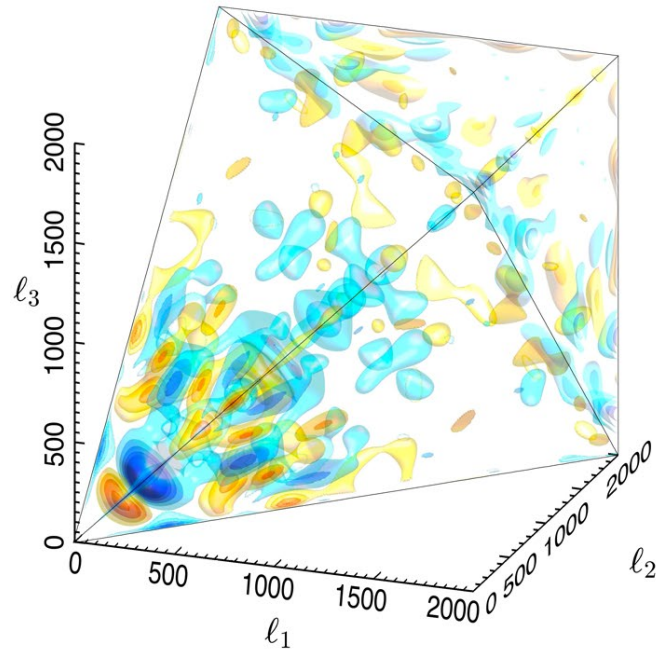
Estimator		C-R	σ	NILC	σ	SEVEM	σ	SMICA	σ	MV	
$T\phi$	$\ell \geq 10$	0.52 ± 0.33	1.5	0.72 ± 0.30	2.4	0.58 ± 0.31	1.9	0.68 ± 0.30	2.3	0.78 ± 0.32	2.4
	$\ell \geq 2$	0.52 ± 0.32	1.6	0.75 ± 0.28	2.7	0.62 ± 0.29	2.1	0.70 ± 0.28	2.5		
KSW		0.75 ± 0.32	2.3	0.85 ± 0.32	2.7	0.68 ± 0.32	2.1	0.81 ± 0.31	2.6		
binned		0.80 ± 0.40	2.0	1.03 ± 0.37	2.8	0.83 ± 0.39	2.1	0.91 ± 0.37	2.5		
modal		0.68 ± 0.39	1.7	0.93 ± 0.37	2.5	0.60 ± 0.37	1.6	0.77 ± 0.37	2.1		



First detection
 2.5sigma
 robust against foreground
 contamination and detection
 algorithm

Non-Gaussianity

Planck bispectrum

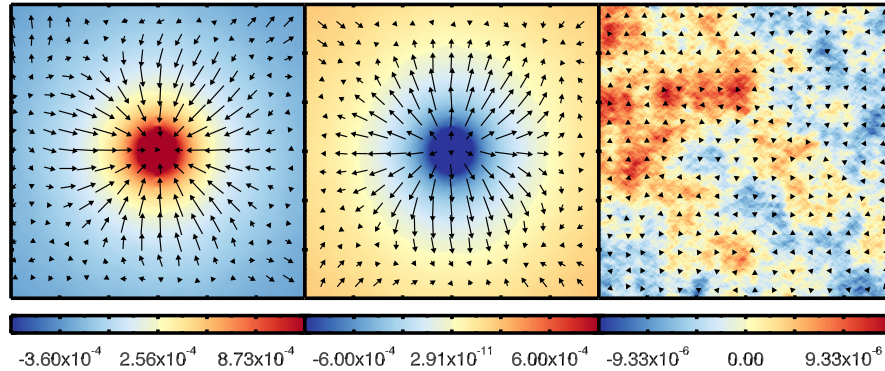


	Independent			ISW-lensing subtracted		
	KSW	Binned	Modal	KSW	Binned	Modal
SMICA						
Local	9.8 ± 5.8	9.2 ± 5.9	8.3 ± 5.9	2.7 ± 5.8	2.2 ± 5.9	1.6 ± 6.0
Equilateral	-37 ± 75	-20 ± 73	-20 ± 77	-42 ± 75	-25 ± 73	-20 ± 77
Orthogonal	-46 ± 39	-39 ± 41	-36 ± 41	-25 ± 39	-17 ± 41	-14 ± 42

No NG!

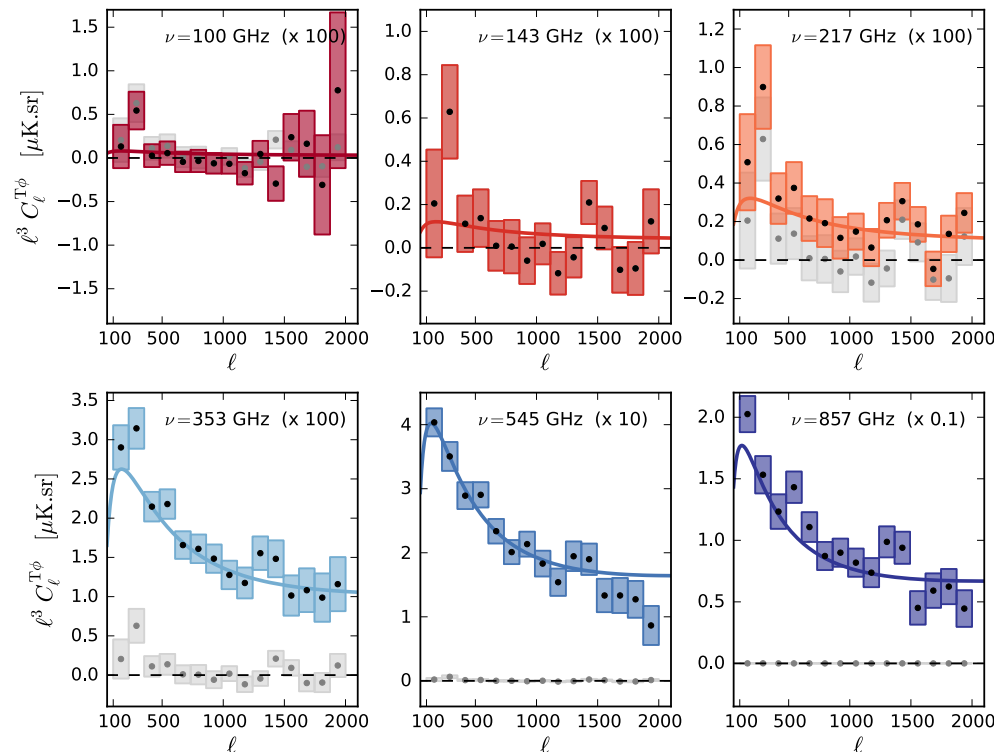
(WMAP9 constraint : local $f_{NL} = 37 \pm 20$)

Planck lensing X planck CIB



**Stacking of the extrema of the CIB field
(and at random locations)**

Impressive visual correlation on degree scale



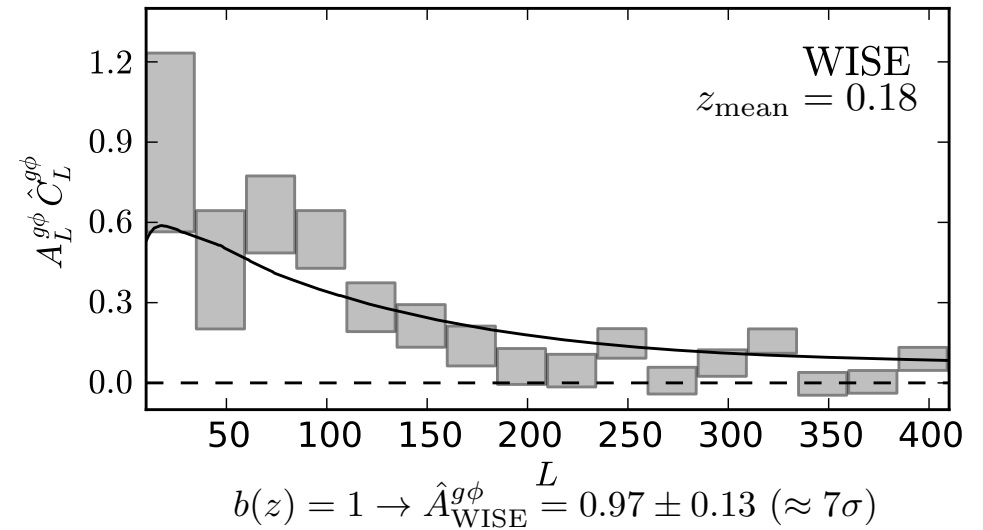
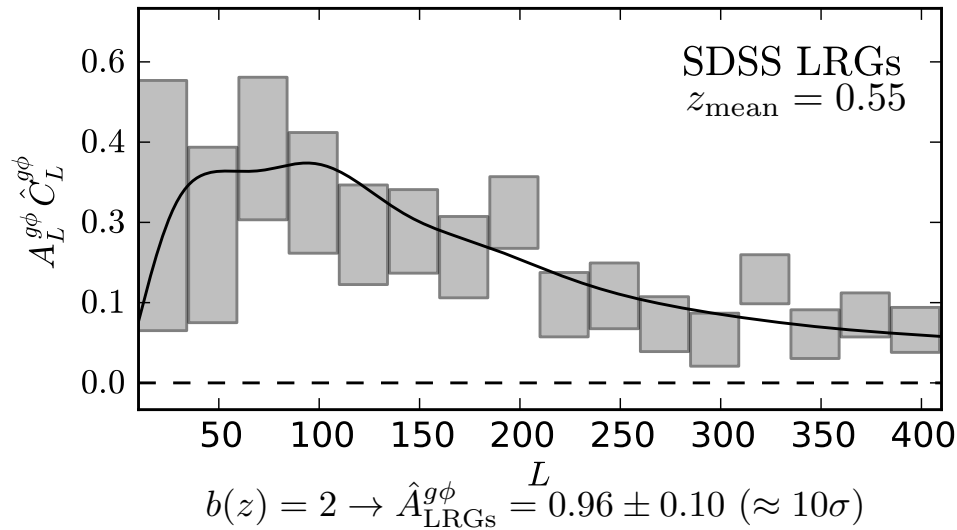
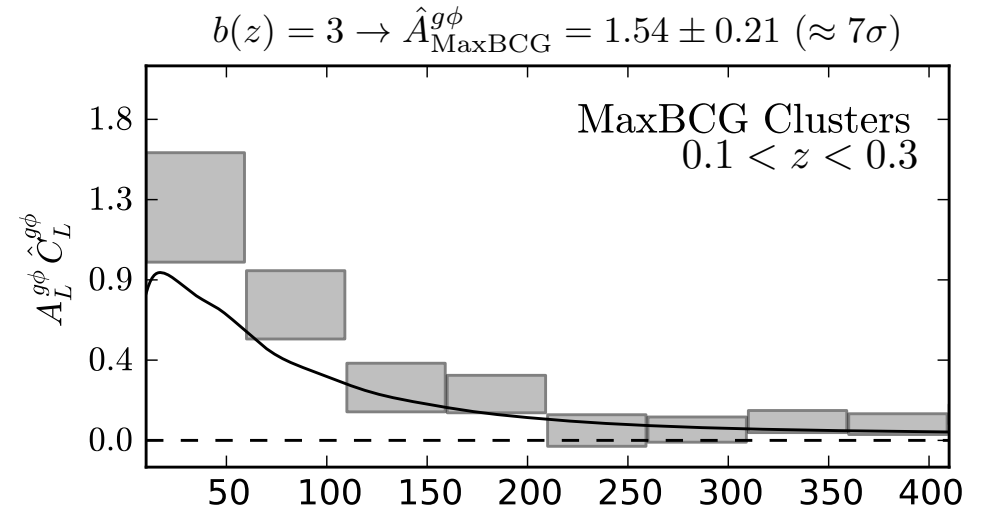
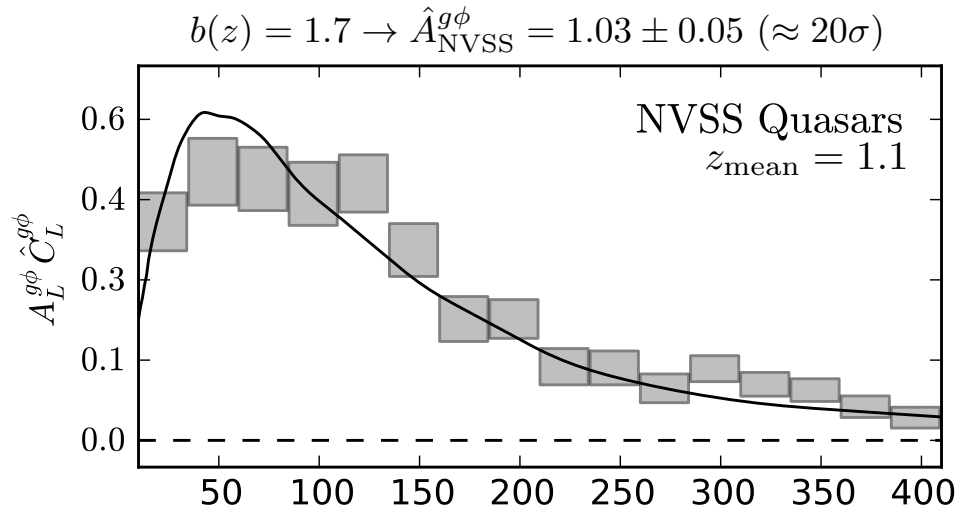
Cross correlation of the maps

Using the best 40% of the CIB & lensing from Planck

Boxes give statistical errors. Grey boxes are the 143-lensing X 143-cib correlation

Lines are the predictions from the Planck Early papers !

Lensing external tracers



No particular effort here to optimize the model for the external survey
There is an untapped astrophysical treasure in the Planck Lensing Map

Conclusion

- Planck trace late dark matter distribution
 - Lensing reconstruction on the whole sky
 - **Reconstruction of the full sky dark matter distribution**
 - First determination of the ISW-lensing correlation
 - Improvement of the cosmological parameters constraint
 - Tension for neutrino masses
 - **Great potential for cross-correlation with other surveys**
- Where do we go from here
 - SPT/ACT/others will greatly improve the small scales
 - PRISM ?