

# SFitter and the NMSSM

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# Outline

## 1. Results for mSUGRA

Latest Paper: Constraining Supersymmetry using the relic density and the Higgs boson [4]

Phys. Rev. D 89, 055017 (2014), Sophie Henrot-Versillé et al.

## 2. SFitter - Software Update

## 3. First results for the constrained NMSSM starting from mSUGRA best fit points

# SFitter

- We can constrain SUSY models via SM measurements (Higgs, B-Physics, ...), Dark Matter, ...
- SFitter: Tool to determine the fundamental supersymmetric parameters from experimental measurements
- Monte Carlo Markov Chains
- Creates likelihood maps reducible to lower-dimensional profile likelihoods or Bayesian probability maps

## Tools for MSSM

- SuSpect2, mass spectrum calculation
  - Susy-Hit, SUspect-SdecaY-Hdecay-InTerface
  - Higgsprod, Higgs couplings
  - SusyPope, EW precision data
  - MicrOMEGAs, relic density
- 
- SuSpect2 → SuSpect3 c++ interface

# Constraints from Data

- $m_h = (126.0 \pm 0.4_{st} \pm 0.4_{sy} \pm 3.0_{th}) \text{ GeV}$  (ATLAS/CMS)
- $\Omega h^2 = 0.1187 \pm 0.0017_{st} \pm 0.0120_{th}$  (Planck)
- $a_\mu = (287 \pm 63_{st} \pm 49_{sy} \pm 20_{th}) \cdot 10^{-11}$
- B Physics:
  - $BR(B \rightarrow X_s \gamma) = (3.55 \pm 0.24_{st} \pm 0.09_{sy}) \cdot 10^{-4}$
  - $BR(B_s^0 \rightarrow \mu^+ \mu^-) = (3.2 \pm 1.4_{st} \pm 0.5_{sy} \pm 0.2_{th}) \cdot 10^{-9}$
  - $BR(B \rightarrow \tau \nu) = (1.41 \pm 0.43_{st}) \cdot 10^{-4}$
  - $\Delta m_{B^0} = (0.510 \pm 0.004_{st} \pm 0.003_{sy} \pm 0.400_{th}) \cdot 10^{12} \text{ fs}^{-1}$
  - $\Delta m_{B_s^0} = (17.69 \pm 0.08_{st} \pm 7.00_{th}) \cdot 10^{12} \text{ fs}^{-1}$
- EW:
  - $\Gamma_{Z \rightarrow Inv} = (1.9 \pm 1.5_{st} \pm 0.2_{th}) \text{ MeV}$
  - $\Gamma_{Z \rightarrow Higgs} = (6.5 \pm 2.3_{st} \pm 1.0_{th}) \text{ MeV}$
- Higgs couplings

# mSUGRA

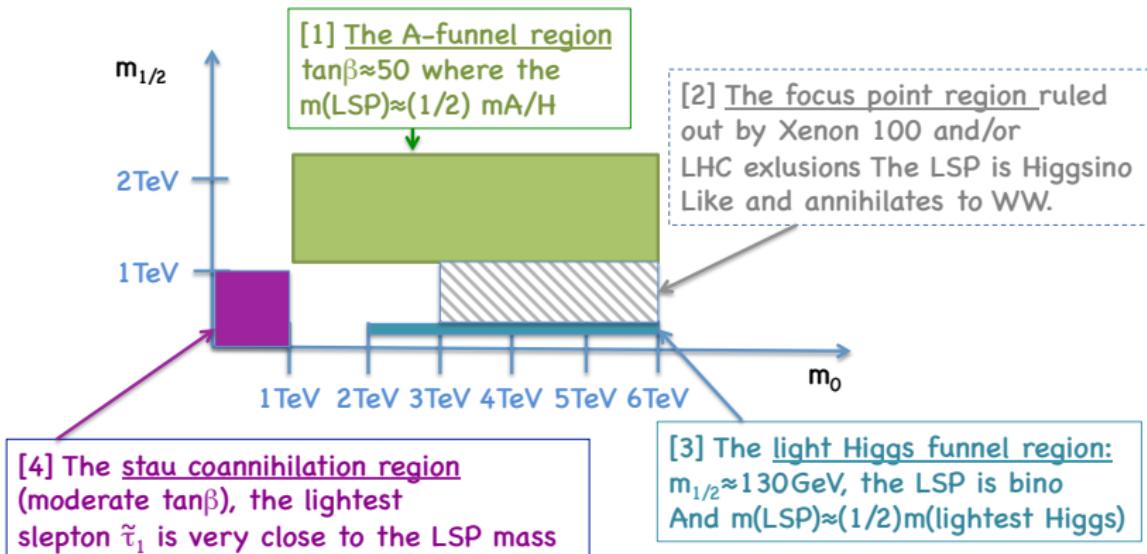
minimal SUper GRAvity

Unification of masses and couplings at GUT scale

## Input parameters set at mGUT

- |                           |  |
|---------------------------|--|
| $m_0 < 5 \text{ TeV}$     | common scalar mass parameter                                     |
| $m_{1/2} < 5 \text{ TeV}$ | common gaugino mass parameter                                    |
| $ A_0  < 4 \text{ TeV}$   | common trilinear coupling  |
| $\tan \beta \leq 60$      | ratio of the vacuum expectation values of the two Higgs doublets |
| $\text{sgn}(\mu) = +1$    | sign of Higgsino mass parameter                                  |
| $(m_t)$                   |  |

# Annihilation channels: Illustration with mSUGRA

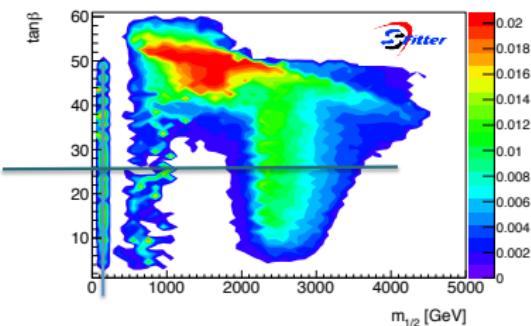
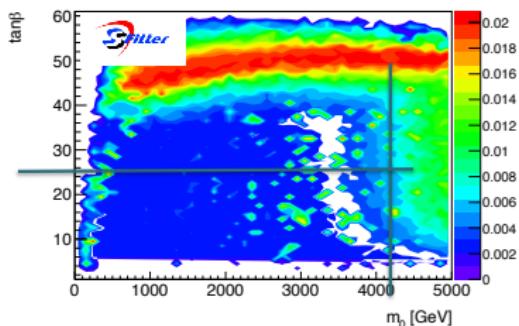
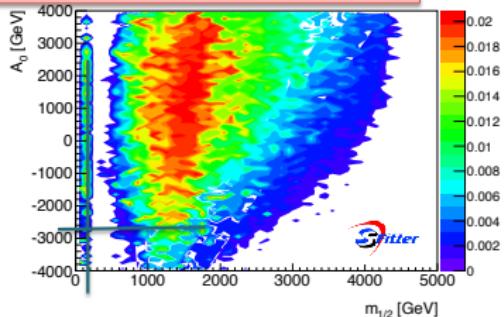
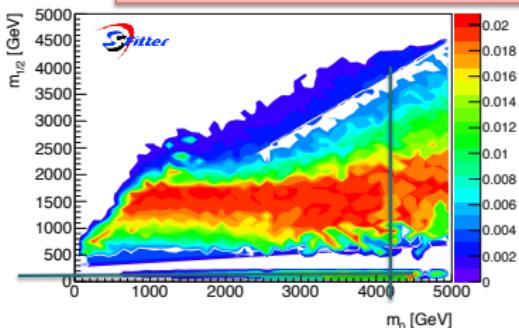


# mSUGRA

**h funnel**

- ⇒ the LSP is mostly bino
- ⇒  $M_{top}(\text{fitted value}) = 174.2 \text{ GeV}$
- ⇒  $M(\tilde{\chi}_1^0) = 59 \text{ GeV}$ ,  $M(\tilde{g}) = 476 \text{ GeV}$

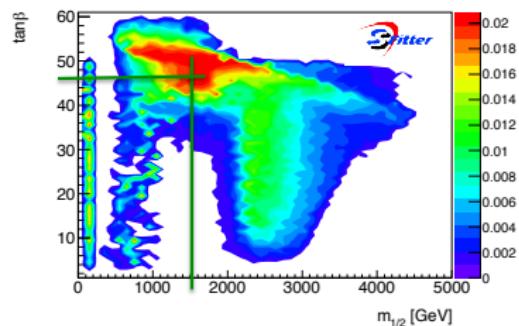
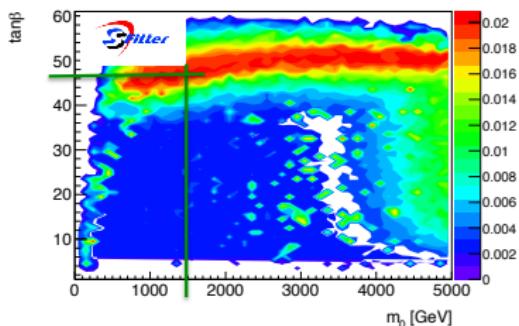
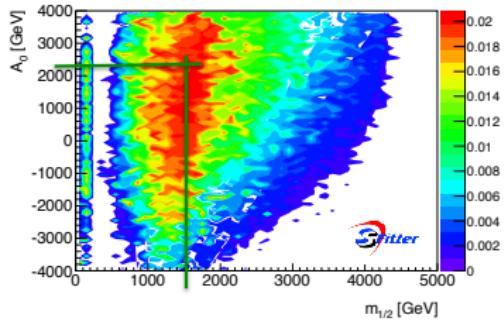
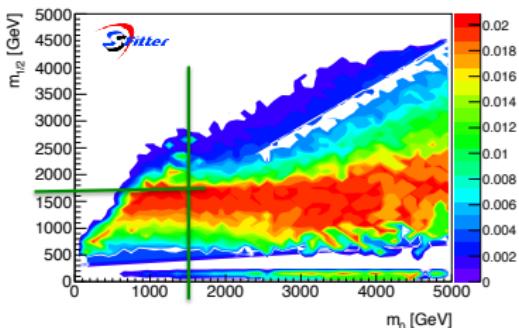
Excluded by ATLAS/CMS Inclusive squark and gluinos searches



# mSUGRA

A funnel

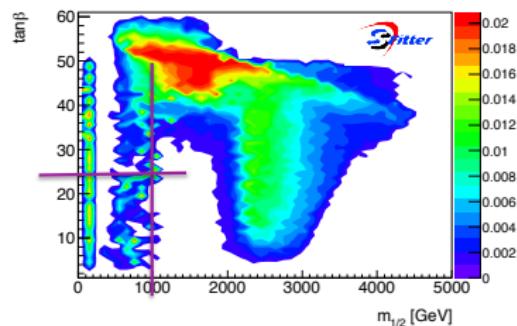
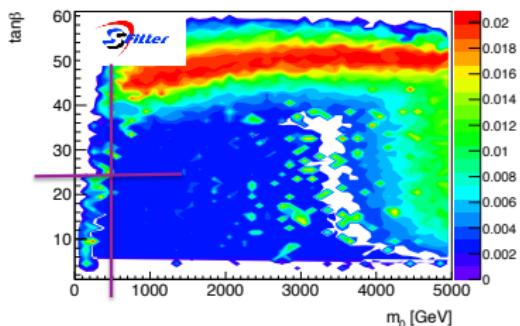
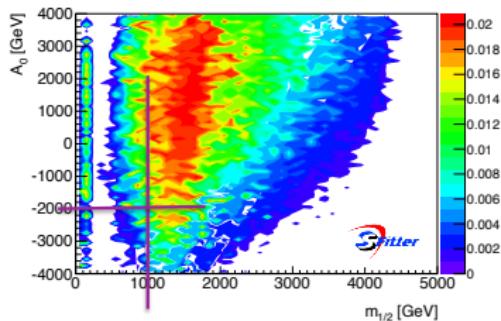
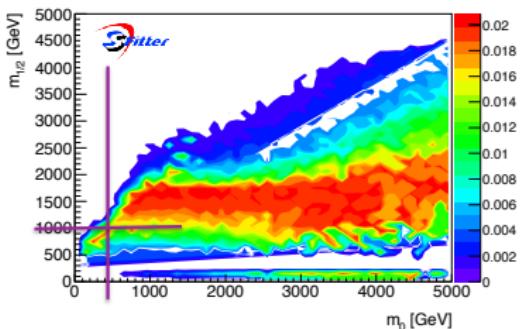
- ⇒ the LSP is mostly bino
- ⇒  $M_{top}(\text{fitted value}) = 173.9 \text{ GeV}$
- ⇒  $M(\tilde{\chi}_1^0) = 745 \text{ GeV}$ ,  $M(\tilde{q}) \approx 3.4 \text{ TeV}$ ,  $M(\tilde{g}) \approx 3.6 \text{ TeV}$



# mSUGRA

Coannihilation

$\Rightarrow M_{top}(\text{fitted value})=174.$  GeV  
 $\Rightarrow M(\tilde{\chi}_1^0)=429\text{GeV}, M(\tilde{q})\approx 2\text{TeV}, M(\tilde{g})\approx 2\text{TeV}$



We found three allowed regions:

### h-funnel

- $m_{LSP} = 1/2m_h \rightarrow m_{1/2} \approx 130 \text{ GeV}$

### A-funnel

- $m_{LSP} = 1/2m_A \rightarrow m_{1/2} \approx 1.7 \text{ TeV}$

### co-annihilation

- $m_{LSP} \approx m_{\tilde{\tau}}$
- $m_{1/2} < 1 \text{ TeV}, m_0 < 500 \text{ GeV}$

Expand to NMSSM, using these regions as starting points.

What is the influence of additional parameters?

→ new SFitter code

# Software Update

- Include NMSSMTools (U. Ellwanger, C. Hugonie):
  - NMSPEC computes mass spectrum [3]
    - +  $g_\mu$
    - + B Physics observables ( $\Delta m_{B^0}$ ,  $\Delta m_{B_s^0}$ ,  $BR(B \rightarrow X_s \gamma)$ , ...)
  - NMHDECAY computes Higgs masses, coupling and decay widths [1], [2]
- Update interfaces for other tools:
  - HiggsProd → free to specify which Higgs ( $h_1, h_2, h_3$ ) is the Standard Model like
  - Micromegas → switch to dynamic libraries
- NMSSMTools provides a wide range of models.
- SFitter needs specific model
- First model: semi constrained NMSSM

## Model

- From MSSM to NMSSM:

$$W_{NMSSM} = W_{MSSM} + \lambda S H_u H_d + \frac{1}{3} \kappa S^3$$

→ additional singlet  $S$

- Semi constrained version of the NMSSM,  
comparable to MSUGRA
- Unification of squark, slepton and gaugino masses, gauge  
couplings
- Additional soft SUSY breaking parameters appear:

$$-\mathcal{L}_{soft} \supset \lambda A_\lambda H_u H_d S + \frac{1}{3} \kappa A_\kappa S^3$$

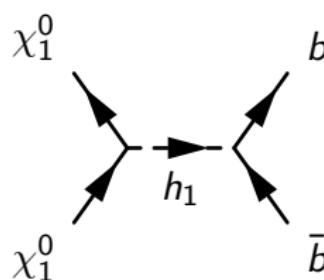
Complete set of input parameters

$m_0, m_{1/2}, A_0, \tan\beta, \mu_{eff}(, m_t)$   
 $\lambda, \kappa, A_\lambda, A_\kappa$

# h-funnel in mSUGRA

Best fit input parameters:

$m_0$	4232 GeV
$m_{1/2}$	135 GeV
$\tan \beta$	26.6
$A_0$	-2925 GeV
$\text{sgn}(\mu)$	+1
$m_t$	174.2 GeV
$\mu_{\text{eff}}$	484.44 GeV



Predictions:

$\Omega h^2$	0.1105
$m_h$	123.84 GeV
$m_H$	3626 GeV
$m_A$	3626 GeV
$m_{H^+}$	3627 GeV
$m_{\chi_1^0}$	59.48 GeV
$m_{\chi_2^0}$	119 GeV
$m_{\tilde{q}_L}$	4175 GeV
$m_{\tilde{t}_1}$	2376 GeV
$m_g$	477 GeV

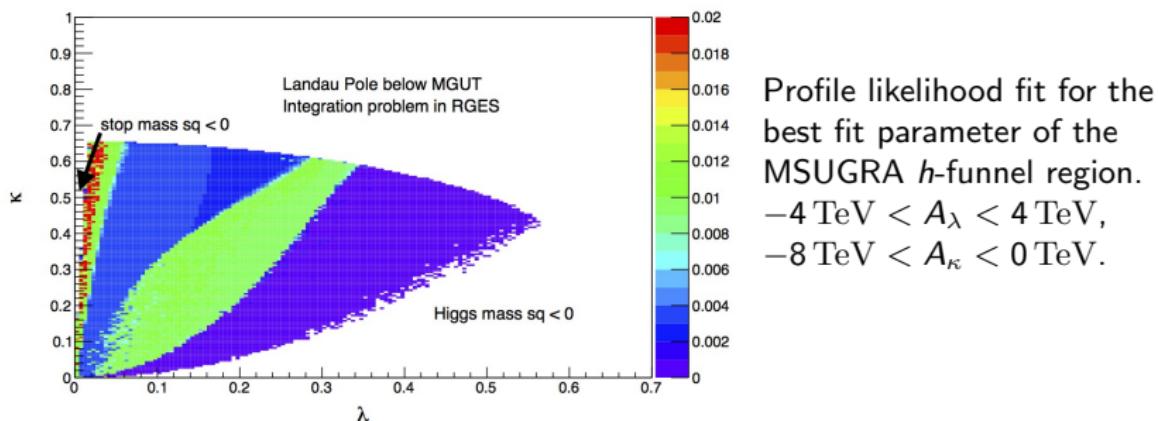
# mSUGRA as starting point for the NMSSM

- mSUGRA input:  
 $m_0 = 4232 \text{ GeV}$ ,  $m_{1/2} = 135 \text{ GeV}$ ,  $\tan \beta = 26.6$ ,  $A_0 = -2925 \text{ GeV}$
- $\lambda \ll 1$ ,  $\kappa$  and  $\mu_{\text{eff}}$  calculated by unification of  $m_{H_u}^2$  and  $m_{H_d}^2$

Model	mSUGRA	CNMSSM	
$\lambda$		1E-16	1E-16
$m_t \text{ [GeV]}$	174.2	174.2	175.4
$\kappa$		1.408E-15	5.775E-16
$\mu_{\text{eff}} \text{ [GeV]}$	484.4	259.4	482.5
$m_{h1} \text{ [GeV]}$	123.84	121.9	122.2
$m_{h2} \text{ [GeV]}$	3626	3613	3633
$m_{\chi_1^0} \text{ [GeV]}$	59.48	57.86	59.68
$m_{\tilde{t}_1} \text{ [GeV]}$	2376	2429	2406
$\Omega h^2$	0.1105	0.0209	0.0804

- $\mu_{\text{eff}}$  depends through  $M_{H_u}^2$  strongly on the Yukawa coupling  $h_t^2$ , results of extrapolation differ → adjust the mass of top quark (Many thanks to U. Ellwanger!)

# Likelihood Fit over $\lambda, \kappa, A_\lambda$ and $A_\kappa$



$$\lambda < 0.6, \kappa < 0.7$$

Input parameters are given @SUSY scale

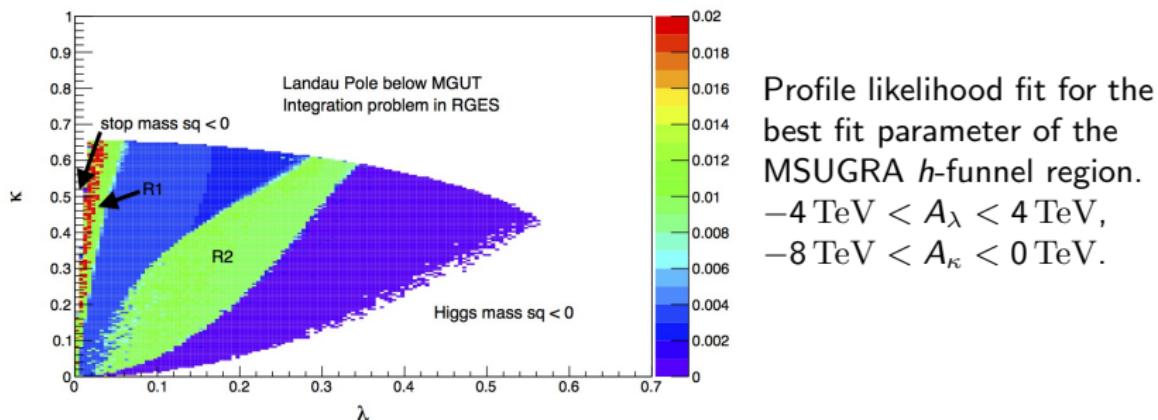
→ RGEs:

$$16\pi^2 \frac{d\lambda^2}{d \ln Q^2} = 4\lambda^4 + 2\lambda^2\kappa^2 + \dots$$

$$16\pi^2 \frac{d\kappa^2}{d \ln Q^2} = 6\kappa^4 + 6\kappa^2\lambda^2 + \dots$$

$\lambda, \kappa$  increase with  $Q \rightarrow$  upper limit on  $\lambda, \kappa$  to keep  $\lambda, \kappa < 1$  up to GUT scale.

## Likelihood Fit over $\lambda$ , $\kappa$ , $A_\lambda$ and $A_\kappa$



Two regions are observed:

$R_1$  :  $10 \lesssim \kappa/\lambda \lesssim 30$ : for  $\kappa < 0.1$  and fixed values of  $A_\lambda$  and  $A_\kappa$  the relic density depends only on the ratio  $\kappa/\lambda$

$R_2$  :  $\lambda_{min} = 0.02$ ,  $\kappa/\lambda \approx 2.2$

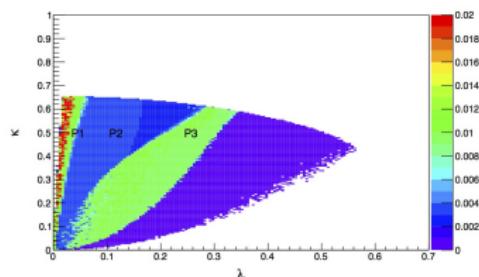
The regions are limited by  $\Omega h^2$ .

DM annihilation by  $h$ -funnel (87% :  $\chi_1^0 + \chi_1^0 \rightarrow b + \bar{b}$ )

## Dependence of $\Omega h^2$ on $\lambda$

$\Omega h^2$  depends on  $m_{h_1}$  which depends through  $m_{\tilde{t}_R}$  and  $A_\lambda$  on  $\lambda$ .

	$P_1$	$P_2$	$P_3$
$\lambda$	0.05	0.15	0.2
$\kappa$	0.5	0.5	0.5
$m_{h_1}$ [GeV]	120.66	120.83	120.47
$m_{\chi_1^0}$ [GeV]	60.043	59.981	59.959
$\Omega h^2$	0.1065	0.0854	0.1075



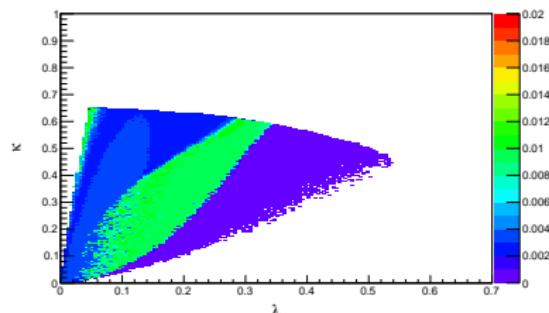
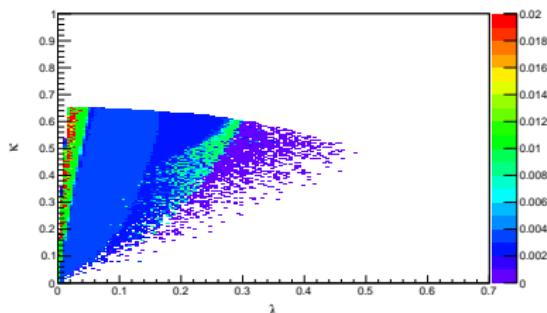
$P_1 \rightarrow P_2$   $m_{h_1}$  increases,  $m_{\chi_1^0}$  decreases  $\rightarrow$  closer to onshell condition  
 $\rightarrow \sigma$  increases  $\rightarrow \Omega h^2$  decreases

$P_2 \rightarrow P_3$   $m_{h_1}$  decreases by  $\approx 300$  MeV  
 $\rightarrow \Omega h^2$  increases

Investigate influence of mixing in Higgs sector:

1. Decouple the singlet part:  
require the heaviest Higgs Boson to be mainly singlet  
 $\rightarrow$  Higgs mixing matrix  $N_{H\text{MIX},33} > 0.99$
2. Compare to a singlet like second Higgs Boson  
 $N_{H\text{MIX},23} > 0.99$

# Singletlike Higgs ( $h_2$ & $h_3$ )



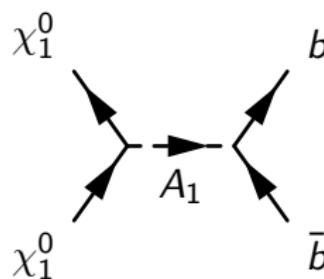
- $N_{HMIX,33} > 99\%$
- $R_1$  restricted to  $13 \lesssim \kappa/\lambda \lesssim 30$
- $R_2$  strongly reduced

- $N_{HMIX,23} > 99\%$
- mainly congruent with unconstrained fit
- $R_1$  is reduced to  $10 < \kappa/\lambda < 13$

# A-funnel in MSUGRA

Best fit input parameters:

$m_0$	1500 GeV
$m_{1/2}$	1700 GeV
$\tan \beta$	46.5
$A_0$	2231 GeV
$\text{sgn}(\mu)$	+1
$m_t$	173.9 GeV
$\mu_{\text{eff}}$	1559.5 GeV

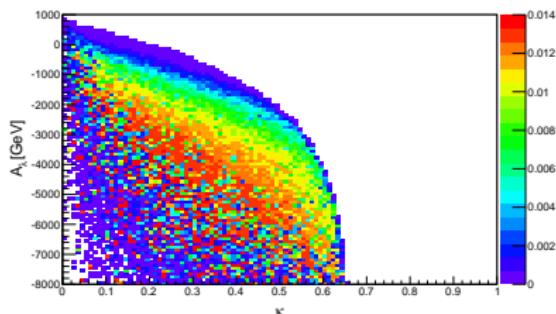
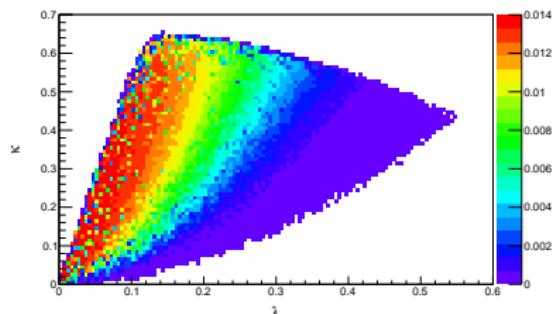


Predictions:

$\Omega h^2$	0.1127
$m_h$	123.03 GeV
$m_H$	1498 GeV
$m_A$	1498 GeV
$m_{H^+}$	1500 GeV
$m_{\chi_1^0}$	745 GeV
$m_{\chi_2^0}$	1379 GeV
$m_{\tilde{q}_L}$	3527 GeV
$m_{\tilde{t}_1}$	2771 GeV
$m_g$	3595 GeV

# Likelihood Fit over $\lambda$ , $\kappa$ , $A_\lambda$ and $A_\kappa$

First results:



- Linear correlation between  $\lambda$  and  $\kappa$
- Correlation between  $\kappa$  and  $A_\lambda$

# Summary

- NMSSMTools interfaced to SFitter
- started investigation of the NMSSM starting from mSUGRA analysis

Many thanks to

- Dirk Zerwas, Sophie Henrot-Versillé, Laurent Duflot for discussions and advise at all stages of the project
- Ulrich Ellwanger and Cyril Hugonie for support with all NMSSM related issues
- the SFitter team (Rémi Lafaye, Michael Rauch, Tilman Plehn, Dirk Zerwas)



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masses in the NMSSM with GUT scale boundary conditions*,  
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using the relic density and the Higgs boson*, Phys. Rev. D **89**  
(2014), no. 055017.

# Best fitting points for different mixing constraints in the Higgs sector

Model	MSUGRA	CNMSSM		
		without const.	$N_{H,33}$	$N_{H,23}$
$\lambda$		0.026	0.030	0.037
$\kappa$		0.589	0.554	0.505
$A_\lambda$ [GeV]		2540	3085	3852
$A_\kappa$ [GeV]		-1125	-7853	-6600
$\Omega h^2$	0.1105	0.1198	0.1108	0.1067
$m_{h1}$ [GeV]	123.84	125.3	124.9	120.4
$m_{h2}$ [GeV]	3626	14015	13944	12702
$m_{h3}$ [GeV]		22833	17794	12916
$m_{H^+}$ [GeV]	3627	14015	13944	12916
$m_{\chi_1^0}$ [GeV]	59.48	60.08	60.08	59.92
$m_{\chi_2^0}$ [GeV]	119	120.8	120.81	120.63
$m_{\tilde{q}_L}$ [GeV]	4175	4380	4380	4347
$m_{\tilde{t}_1}$ [GeV]	2376	212.3	215	1095
$m_{\tilde{g}}$ [GeV]	477	462	462	471