



# Constraints on New Phenomena via Higgs Coupling Measurements with the ATLAS Detector

David Delgove

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# Introduction

- **The Higgs boson**, the last missing piece of Standard Model, **has been discovered at a mass around 125.5 GeV** and is compatible with  $0^{++}$
- **Nevertheless, questions remains** : Hierarchy problem, dark matter, new interactions or particles → Imply deviations with respect to Standard Model
- In the Higgs couplings combination :
  - Measure **deviation of the number of signal events** with respect to the expected one :
$$n = s + b = \mu\sigma_{SM}BR_{SM}\mathcal{L}\mathcal{A}\epsilon + b$$
  - **Assume perfect understanding of experimental conditions and analysis** (Luminosity, efficiency background...)
  - Interpret results as a **deviation with respect to Standard Model** ( cross section, branching ratio, couplings ... )
  - No informations on the origins of the deviations
- In ATLAS-CONF-2014-010, **deviations are used to constrain BSM theories**, results are not final and will be updated
- Results use the  $h \rightarrow 4l$ ,  $h \rightarrow 2l2\nu$ ,  $h \rightarrow bb$ ,  $h \rightarrow \gamma\gamma$ ,  $h \rightarrow \tau\tau$  analysis at 7 TeV with up to 4.6-4.8  $\text{fb}^{-1}$  and 8 TeV with 20.3  $\text{fb}^{-1}$

# Deviation coupling modifiers

- Define the deviation coupling modifiers  $\kappa$  :
  - ratio of the Higgs boson coupling over the Standard Model coupling
  - $\kappa = 1$  corresponds to Standard Model

- Determination is based on the maximization of an unbinned likelihood function

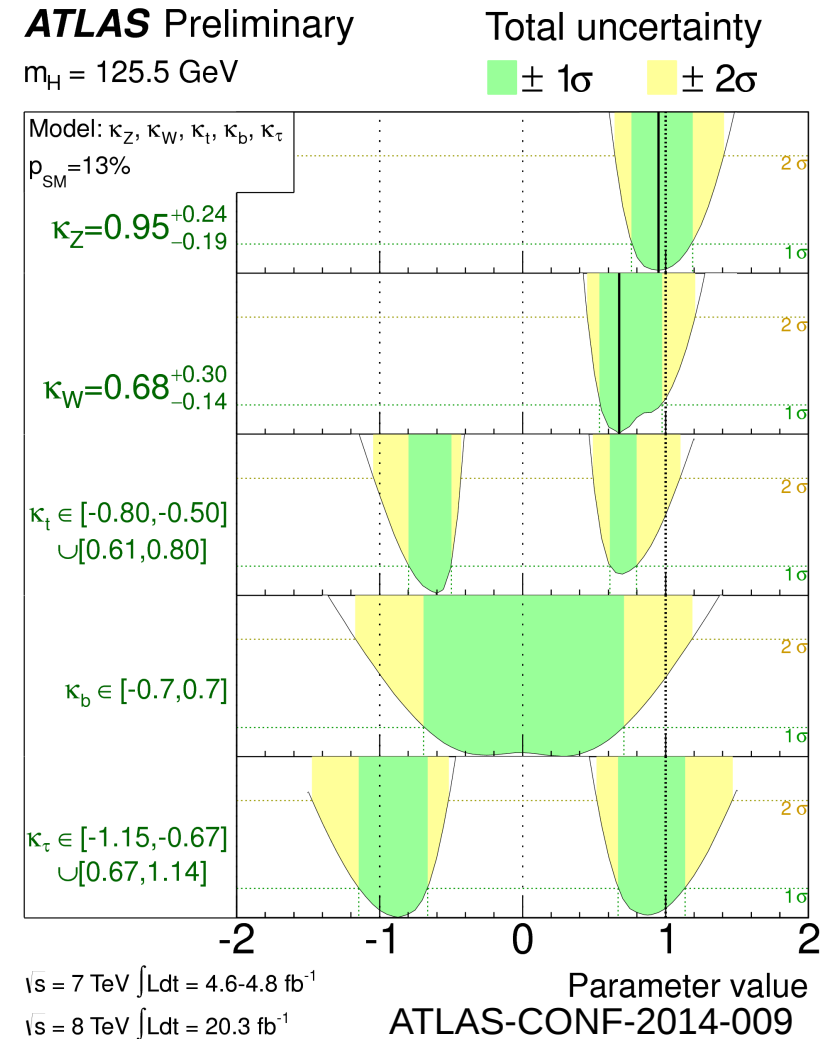
- Use **Narrow width approximation** :
  - Decouple production and decay
  - Example for  $qq \rightarrow Zh \rightarrow b\bar{b}$  :

$$s \propto \kappa_Z^2 \frac{\kappa_b^2}{\kappa_h^2}$$

$$\rightarrow \text{With : } \kappa_h^2 = \frac{\Gamma_h}{\Gamma_{h,SM}}$$

- If assume Standard Model decays only :

$$\kappa_h^2 = \sum_i \kappa_i^2 BR_{i,SM}$$



# Additional comments

- **Photons and gluons are not massive but interact with the Higgs boson via a loop**
- **Two treatments are possible :**
  - **Keep the modifiers** and consider an effective coupling : **sensitive to new particles in the loops** (charged for the photons, colored for the gluons)
  - Resolved couplings : **Express as a function of the modifiers of the massive particle**, assume standard model content in the loop
- Determination of the confidence interval uses the profiled likelihood ratio :

$$\Lambda(\alpha) = \frac{\mathcal{L}(\alpha, \hat{\theta}(\alpha))}{\mathcal{L}(\hat{\alpha}, \hat{\theta})} \quad \begin{array}{l} \alpha : \text{parameters of interest} \\ \theta : \text{nuisance parameters} \end{array}$$

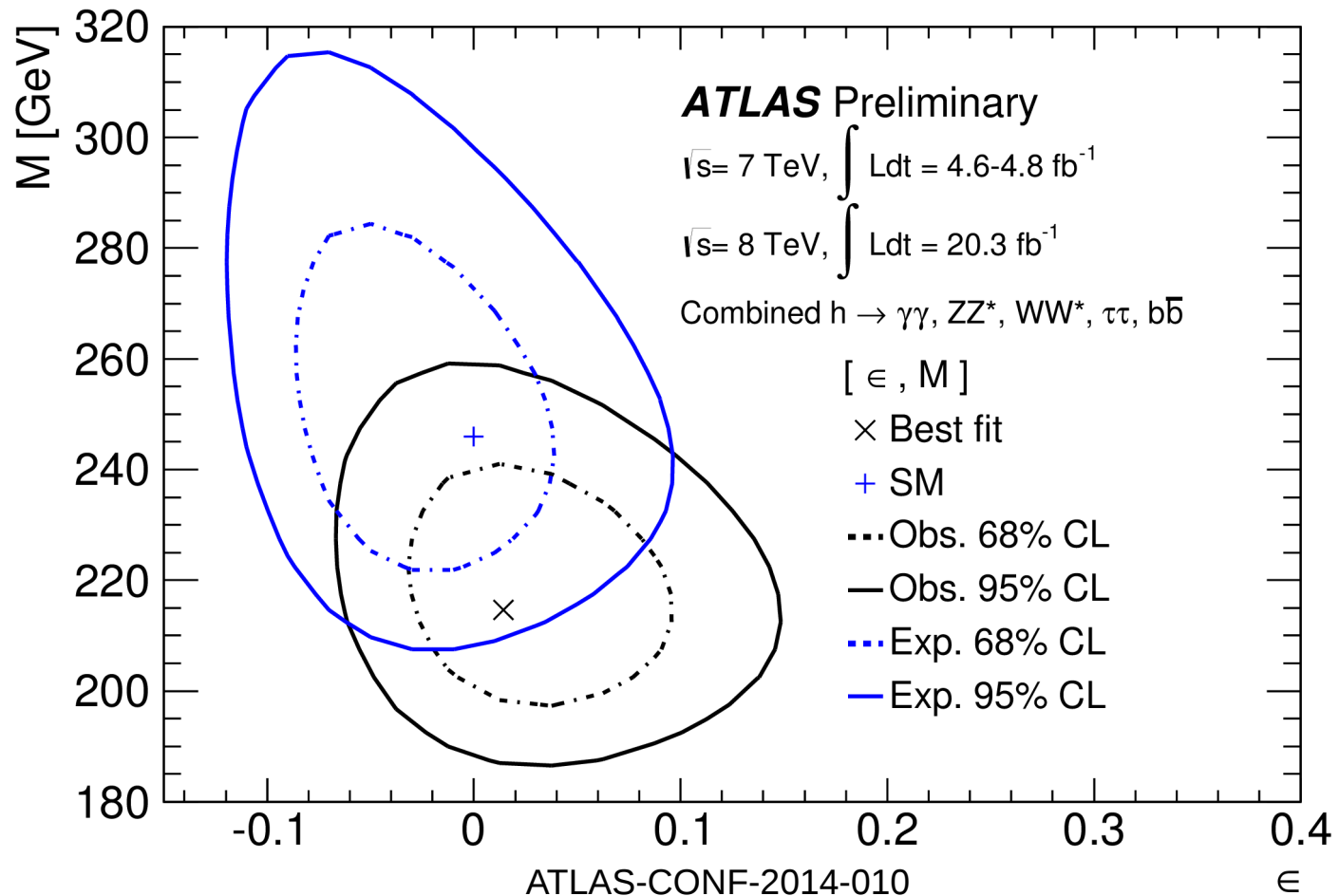
- **If the studied parameter has a physical boundary** (for instance  $\text{BR}_{\text{inv}} > 0$ ), an **alternative test statistic is defined** (similar to the Feldmans and Cousins procedure)
- Assume asymptotic distributions for the two tests

# Probing the mass dependence (1/2)

- **Check the mass dependence of the Higgs boson couplings with respect to the Standard Model** (linear for the fermions, quadratic for the W, Z bosons)
- Introduce a **phenomenological parametrization** of couplings, or equivalently, of the coupling constant modifiers (arXiv:1303.3879) :
  - For the couplings :  $g_f = \sqrt{2} \frac{m_f^{1+\epsilon}}{M^{1+\epsilon}}$  and  $g_V = 2 \frac{m_V^{2(1+\epsilon)}}{M^{1+2\epsilon}}$
  - For the modifiers :  $\kappa_f = v \frac{m_f^\epsilon}{M^{1+\epsilon}}$  and  $\kappa_V = v \frac{m_V^{2\epsilon}}{M^{1+2\epsilon}}$
- Mass scaling :  $\epsilon$  and "vacuum expectation value" : M
- **Standard Model** is found for ( $\epsilon \rightarrow 0$ ,  $M \rightarrow v \approx 246$  GeV )
- Consider only Standard Model particles
- Except  $\epsilon = 0$  (Standard Model), others values have no interpretation

# Probing the mass dependence (2/2)

- Plot the 2D contours in the plan (  $\epsilon$ , M ) which correspond to :
  - $-2\ln(\Lambda(\epsilon, M)) = 2.3$  corresponds to 68 % confidence level
  - $-2\ln(\Lambda(\epsilon, M)) = 6$  corresponds to 95 % confidence level
- **Standard Model is compatible with data within  $1.5 \sigma$**



# Higgs Compositeness (1/2)

- **Possible solution of the hierarchy problem : Higgs boson is a composite particle**
- Introduce a **compositeness scale f** :  $f \rightarrow \infty$  corresponds to Standard Model
- The Higgs coupling are modified, two models have been tested :

$$\rightarrow \text{MCHM 4 : } \kappa = \kappa_V = \kappa_F = \sqrt{1 - \xi} \quad (1)$$

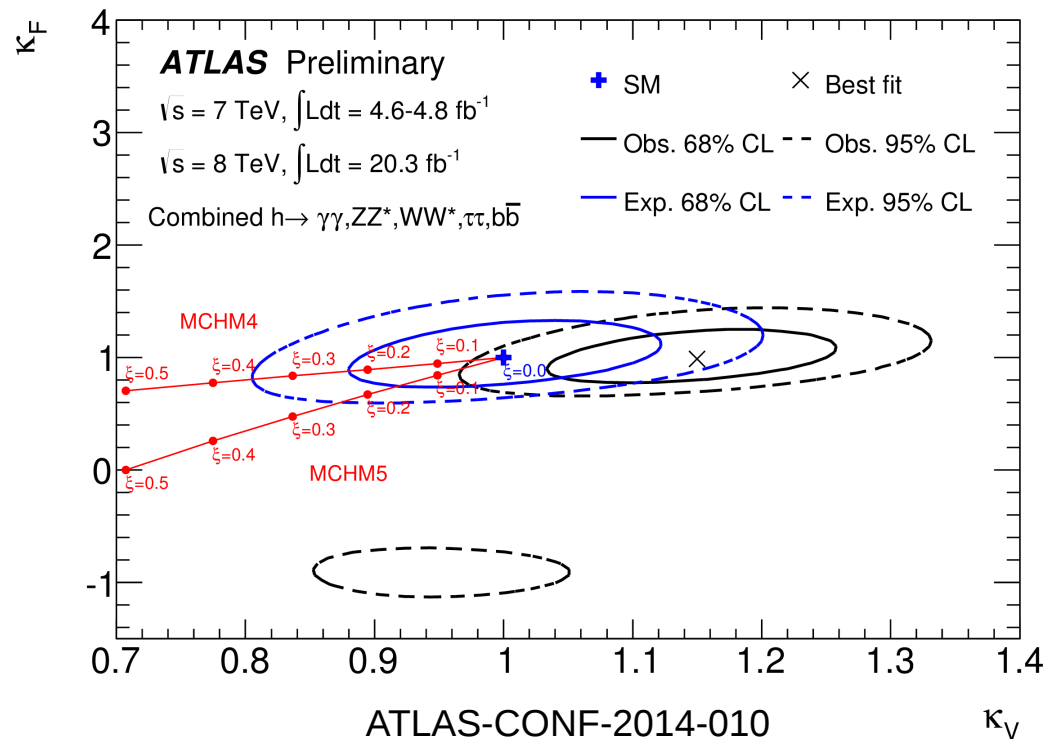
$$\rightarrow \text{MCHM 5 : } \kappa_V = \sqrt{1 - \xi} \text{ and } \kappa_F = \frac{1 - 2\xi}{\sqrt{1 - \xi}} \quad (2)$$

where  $\xi = v^2/f^2$  and  $\xi \rightarrow 0$  is the **Standard Model case**

- Assume **decays and particle content for the loops of standard model**
- Limits on  $\xi$  can be deduced and convert into a limit on f  
→ **Physical boundary at  $\xi = 0$**

# Higgs Compositeness : Results (2/3)

- (1) and (2) define a parametric equation in the plan ( $\kappa_V$ ,  $\kappa_F$ )

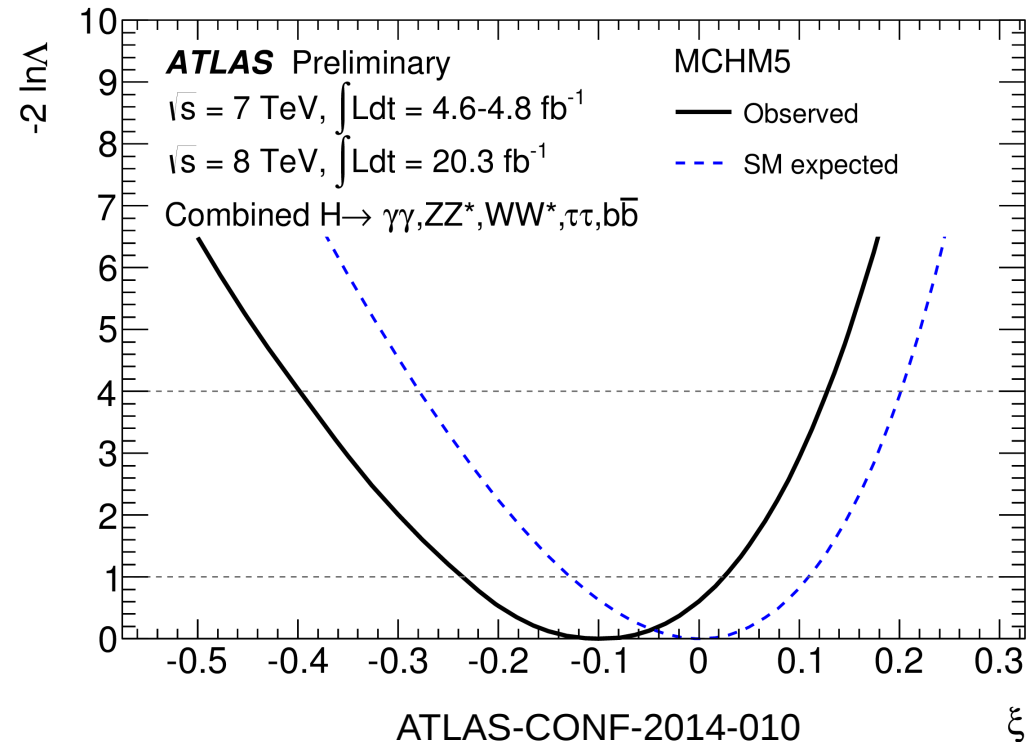
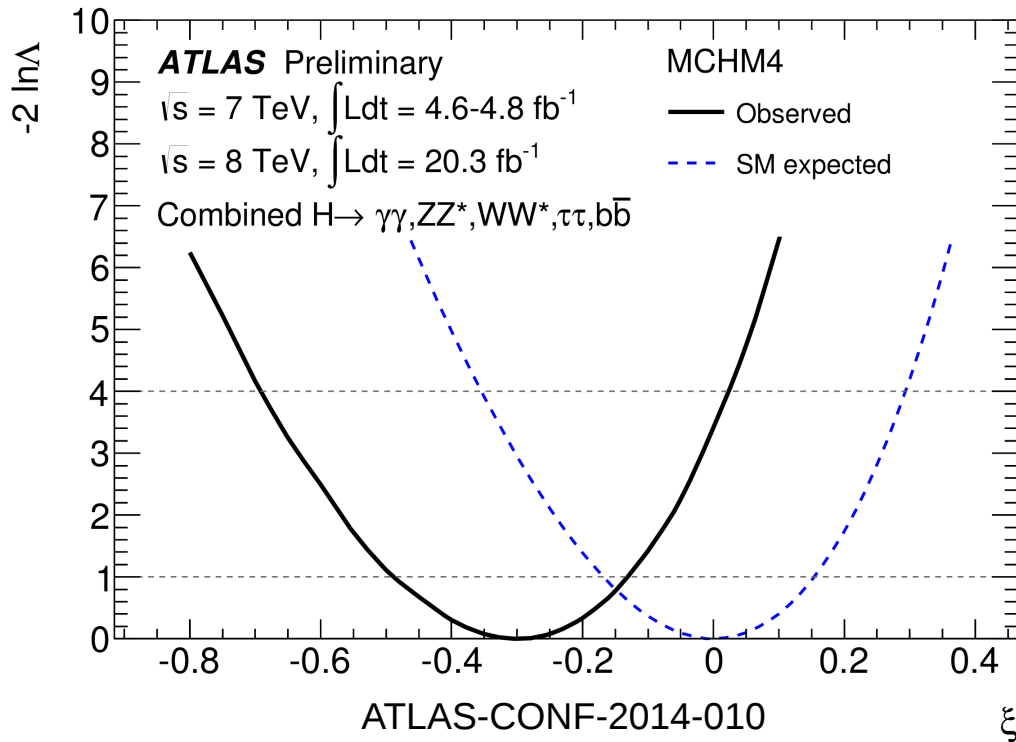


- Easy visualization of the probed region in the plan ( $\kappa_V$ ,  $\kappa_F$ )  
 → Composite models are disfavoured



# Higgs Compositeness : Results (3/3)

- Profiled likelihood for the two models :



- **Current Limits at 95 % CL (Alternative procedure) :**
  - **MCHM 4 :  $f > 710$  GeV (exp. :  $f > 460$  GeV)**
  - **MCHM 5 :  $f > 640$  GeV (exp. :  $f > 550$  GeV)**

# Additional Electroweak singlet (1/3)

- **Simplest extension of the Standard Model Higgs Sector :**
  - Additional Electroweak Singlet
  - Possible solution to dark matter problem
  - **Two Higgs Boson h (Standard Model) and H**
- **Coupling of h/H are the standard model prediction for the mass of the considered Higgs Boson decreased by a factor  $\kappa/\kappa'$  such that :**

$$\kappa^2 + \kappa'^2 = 1 \quad (\text{unitarity constraint})$$

- For the lightest Higgs boson, consider only Standard Model particles :

$$\sigma_h = \kappa^2 \sigma_{h,SM}, \Gamma_h = \kappa^2 \Gamma_{h,SM}, BR_{h,i} = BR_{h,SM,i}$$

- Consider the **possibility for the heaviest Higgs boson to decay into new particles with no charge and no color** (resolved couplings for photons and gluons) :
  - For instance, if allowed,  $H \rightarrow hh$
  - Introduce a branching ratio :  $BR_{H,\text{new}}$

# Additional Electroweak singlet (2/3)

- For the heaviest Higgs boson :

$$\sigma_H = \kappa'^2 \sigma_{H,SM}, \quad \Gamma_H = \frac{\kappa'^2}{1 - BR_{H,new}} \Gamma_{H,SM}, \quad BR_{H,i} = \frac{\kappa'^2}{1 - BR_{H,new}} BR_{H,i,SM}$$

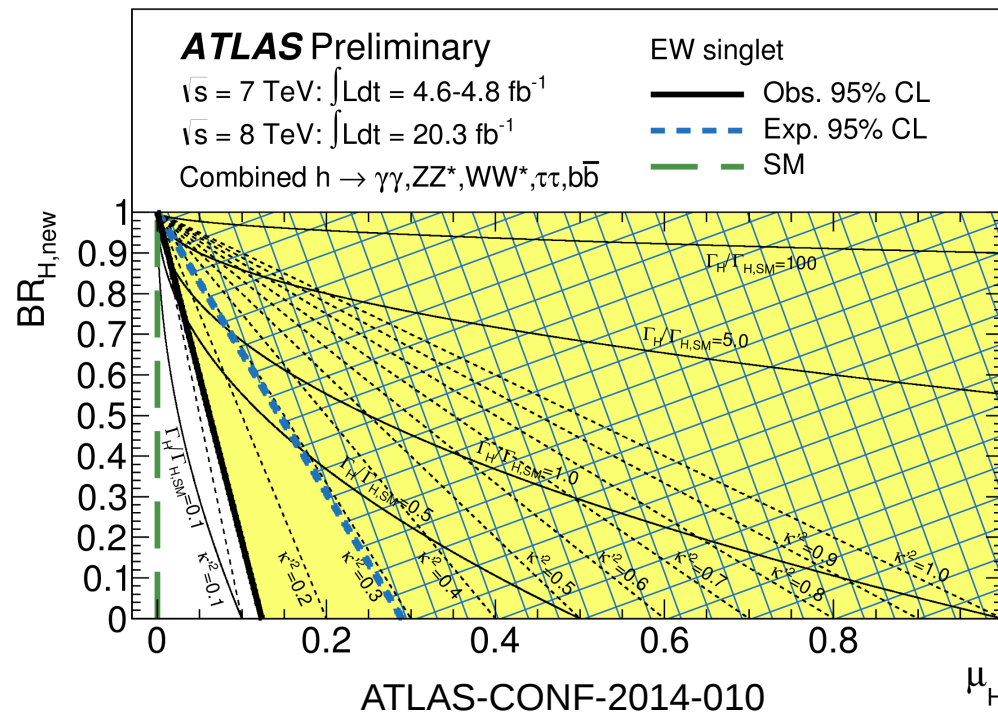
- Using the unitarity constraint, the likelihood (initially a function of  $\kappa$ ) can be expressed as a function of  $\kappa'$  :
  - Possible to deduce a limit on  $\kappa'$
  - Observed :  $\kappa'^2 = -0.30^{+0.17}_{-0.18}$
  - Expected :  $\kappa'^2 = -0.00^{+0.15}_{-0.17}$
- **Applying alternative Procedure at 95 % CL :**
  - **the limit is  $\kappa'^2 < 0.12$  (0.29 for exp.)**

# Additional Electroweak singlet (3/3)

- Define the signal strength factor :

$$\mu_H = \frac{\sigma_H BR_H}{(\sigma_H BR_H)_{SM}} = \kappa'^2 (1 - BR_{H,new})$$

- From the limit on  $\kappa'$  : deduce excluded region in the plan  $(\mu_H, BR_{H,new})$



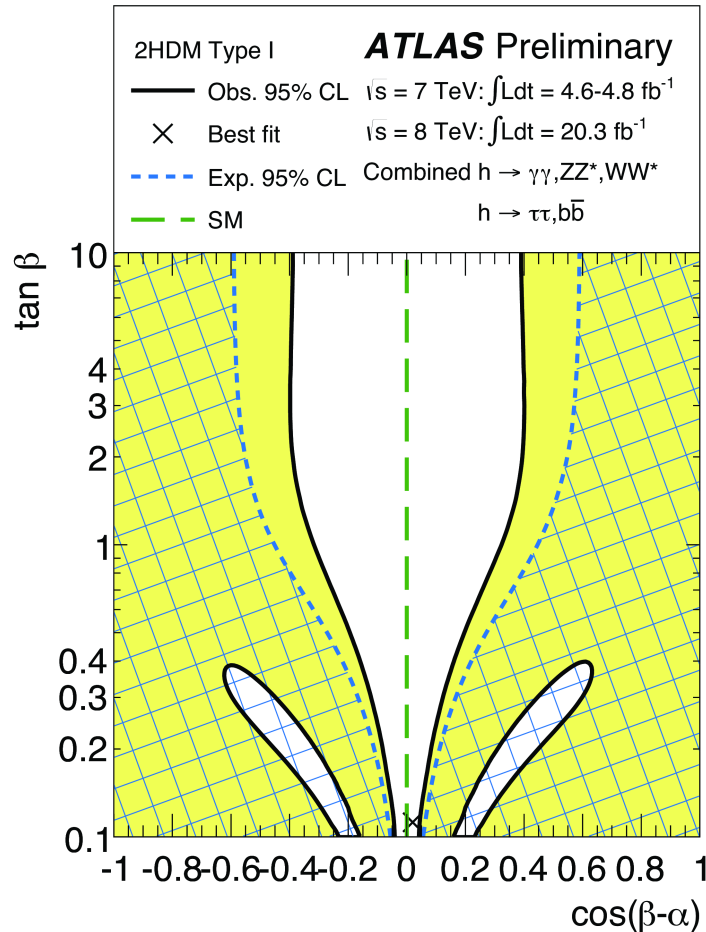
# Two Higgs doublet models (1/3)

- Other extension of the Standard Model Higgs Sector :
  - Additional Higgs doublet such as MSSM ( 5 Higgs Bosons)
  - Motivated by hierarchy problem and dark matter
- **Couplings described by two parameters :**
  - **$\tan \beta$  : the ratio of the vev's of the two Higgs doublets**
  - **$\alpha$  : the mixing angle between the two CP-even Higgs states**
- Assume the discovered Higgs boson is the lightest CP-even states
  - Standard model particles content for the loops and decays
- In the models, **b-quark coupling** to the light Higgs boson can **become important** :
  - Need to **take in account the  $bbH$  production mode**
  - Done for all the two Higgs doublet models
  - **Rescale the fusion gluon cross section with the prediction of SUSHI and 2HDMC**
  - **Corrections below 10 % for the region compatible at 95 % confidence level**

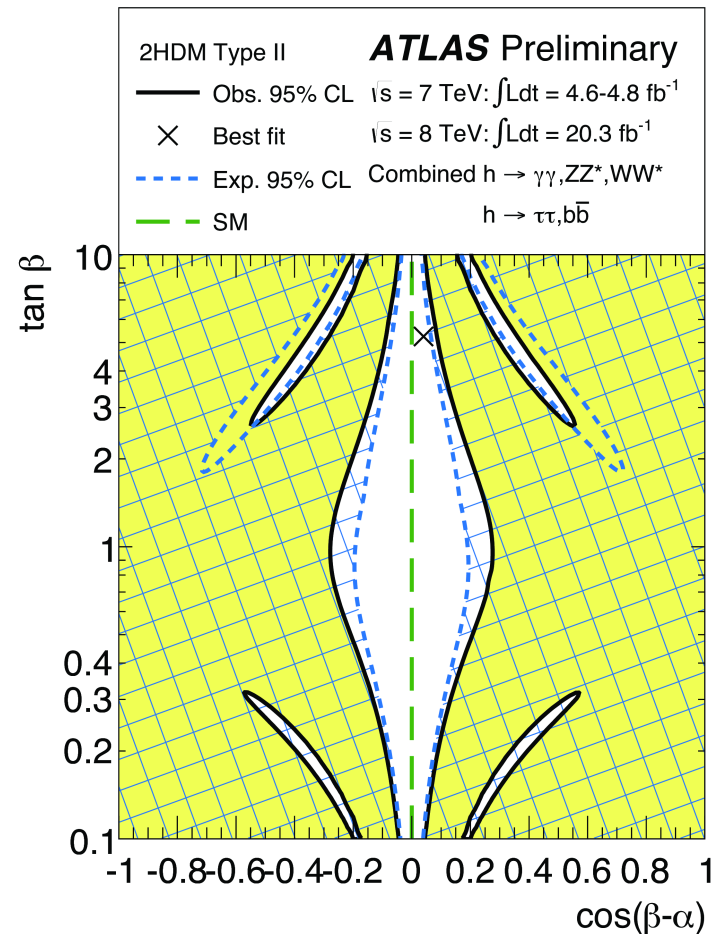
# Two Higgs doublet models : Type I and II (2/3)

	$K_V$	$K_u$	$K_d$	$K_l$
Type 1	$\sin(\beta-\alpha)$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$
Type 2	$\sin(\beta-\alpha)$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$	$-\sin \alpha / \cos \beta$

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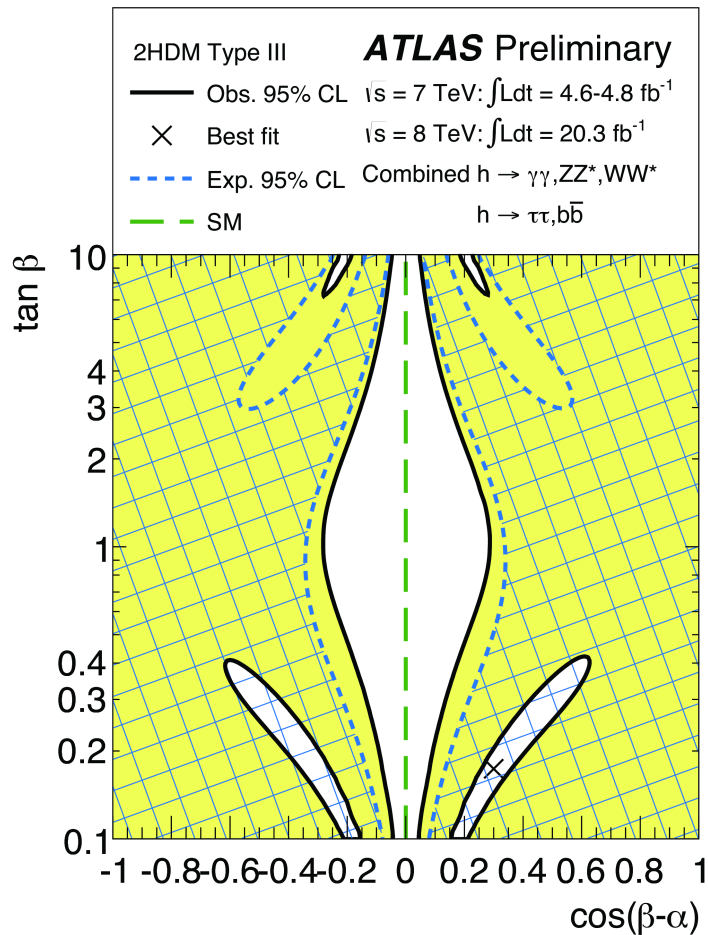
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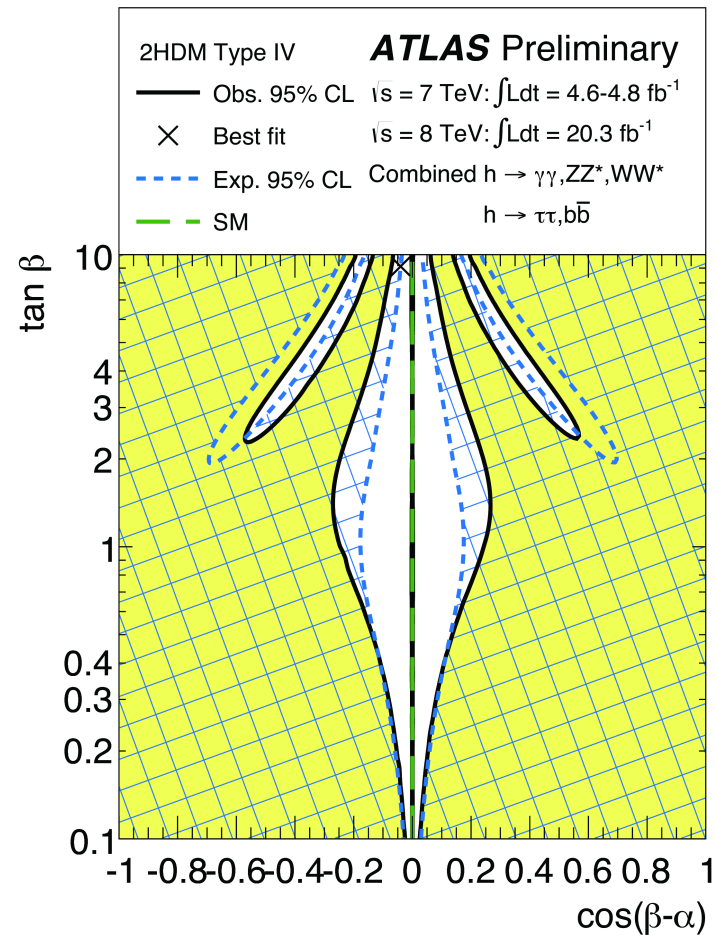
# Two Higgs doublet models Type III and IV (3/3)

	$K_V$	$K_u$	$K_d$	$K_l$
Type 3	$\sin(\beta-\alpha)$	$\cos \alpha / \sin \beta$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$
Type 4	$\sin(\beta-\alpha)$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$	$\cos \alpha / \sin \beta$

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# Simplified MSSM (1/2)

- MSSM provides a possible solution to the hierarchy problem and dark matter
- Simplification of MSSM (arxiv:1307.5205) :
  - **Radiative corrections involving top quark and stops are fixed by the mass of the standard model Higgs boson**
  - **Loops corrections from stops in ggF and diphoton decays are neglected** (expected less than 5%)
  - **Corrections which break universality of down type fermions ( $\kappa_b \neq \kappa_\tau$ ) are neglected**
  - **Deviation coupling modifiers for boson ( $\kappa_V$ ), up type-fermion ( $\kappa_u$ ), down type-fermion ( $\kappa_d$ ) depend only on  $\tan \beta$  and  $m_A$  the mass of the pseudo scalar Higgs boson**
- **Take in account the bbh production** mode by modifying the deviation coupling modifier of gluons only in the case of gluons fusion production :

$$1.06\kappa_t^2 - 0.07\kappa_b\kappa_t + 0.01\kappa_b^2 + 0.011\kappa_b^2$$

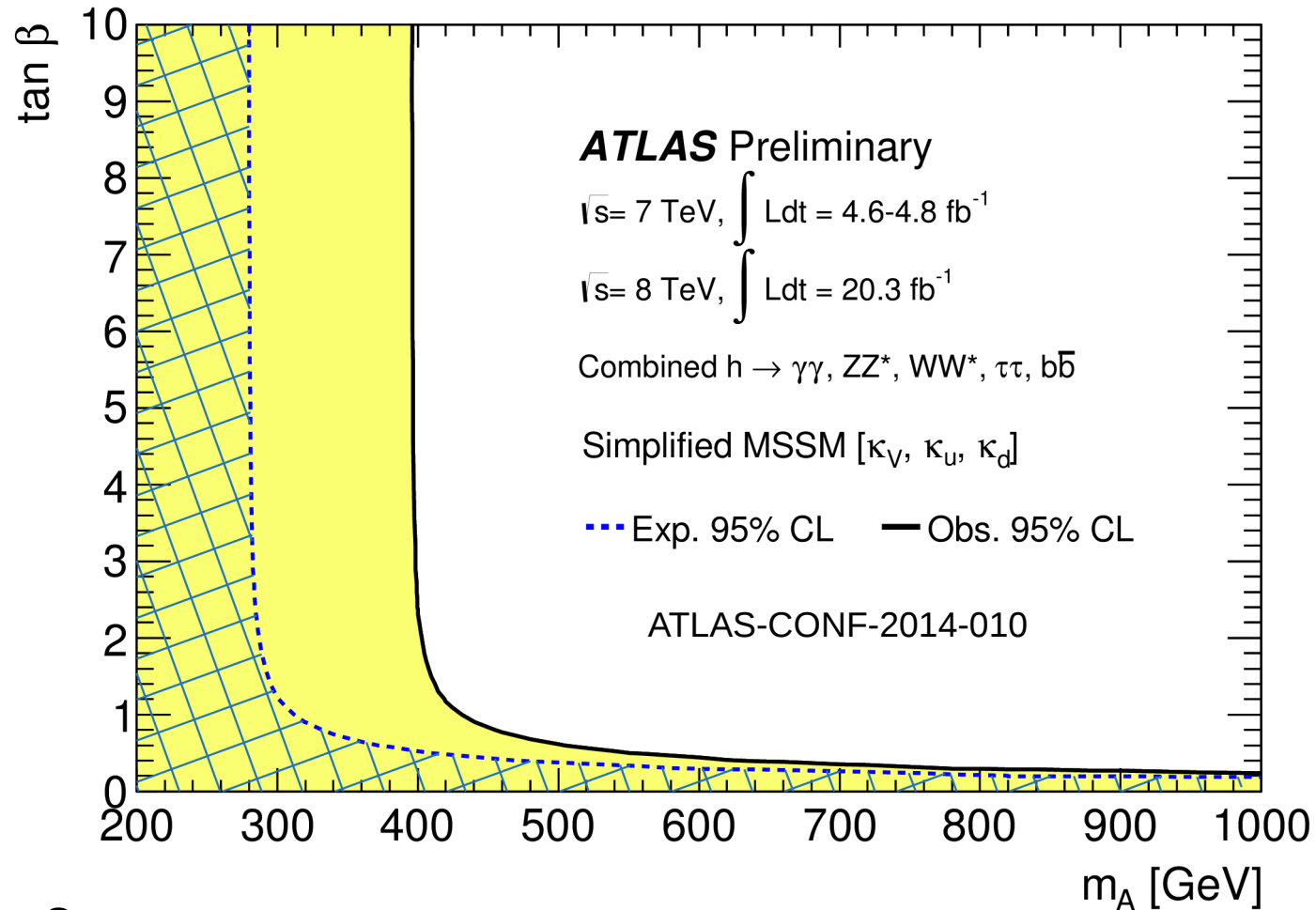
- Standard Model corresponds to  $m_A \rightarrow \infty$

Contribution of bbh



# Simplified MSSM (2/2)

- 2D contours in the plan ( $m_A$ ,  $\tan \beta$ ) :



- For  $\tan \beta > 2$  :
  - $m_A > 400 \text{ GeV @ 95\% CL (obs.)}$
  - $m_A > 290 \text{ GeV @ 95\% CL (exp.)}$

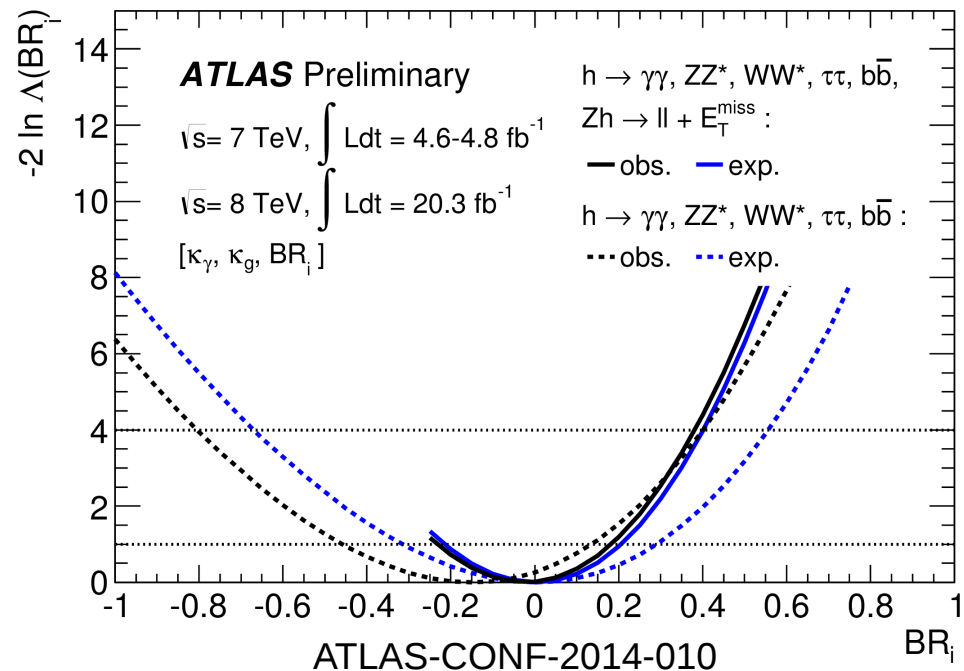
# Higgs invisible branching ratio (1/2)

- Models introduce weakly interacting particles (Wimps) to solve the dark matter problem
- **Interact weakly with all the standard model particles except the Higgs Boson**, if the mass of the particle is lower than  $m_h/2$  :
  - Higgs Boson could decay in these particles ( $BR_{inv}$ )
- Possibility to probe this model with the visible searches using the following **model** ( $\kappa_{gluon}$ ,  $\kappa_\gamma$ ,  $BR_{inv}$ ) :
  - **Sensitive to new particles in loops and decays**
  - Formula of  $\kappa_h$  is modified :
$$\kappa_H^2 = \frac{0.085\kappa_{gluon}^2 + 0.0023\kappa_\gamma^2 + 0.91}{1 - BR_{inv}}$$
  - **Others :  $\kappa_b$ ,  $\kappa_t$ ,  $\kappa_W$ ,  $\kappa_Z$ ,  $\kappa_\tau$  are fixed to 1**
  - **Assume  $BR_{und} = 0$**
- For this model only : **Combine the  $Zh \rightarrow ll + E_{miss}$  (arxiv :1402.3244) with the 5 visible searches (referred as 6 channels)**

# Higgs invisible branching ratio (2/2)

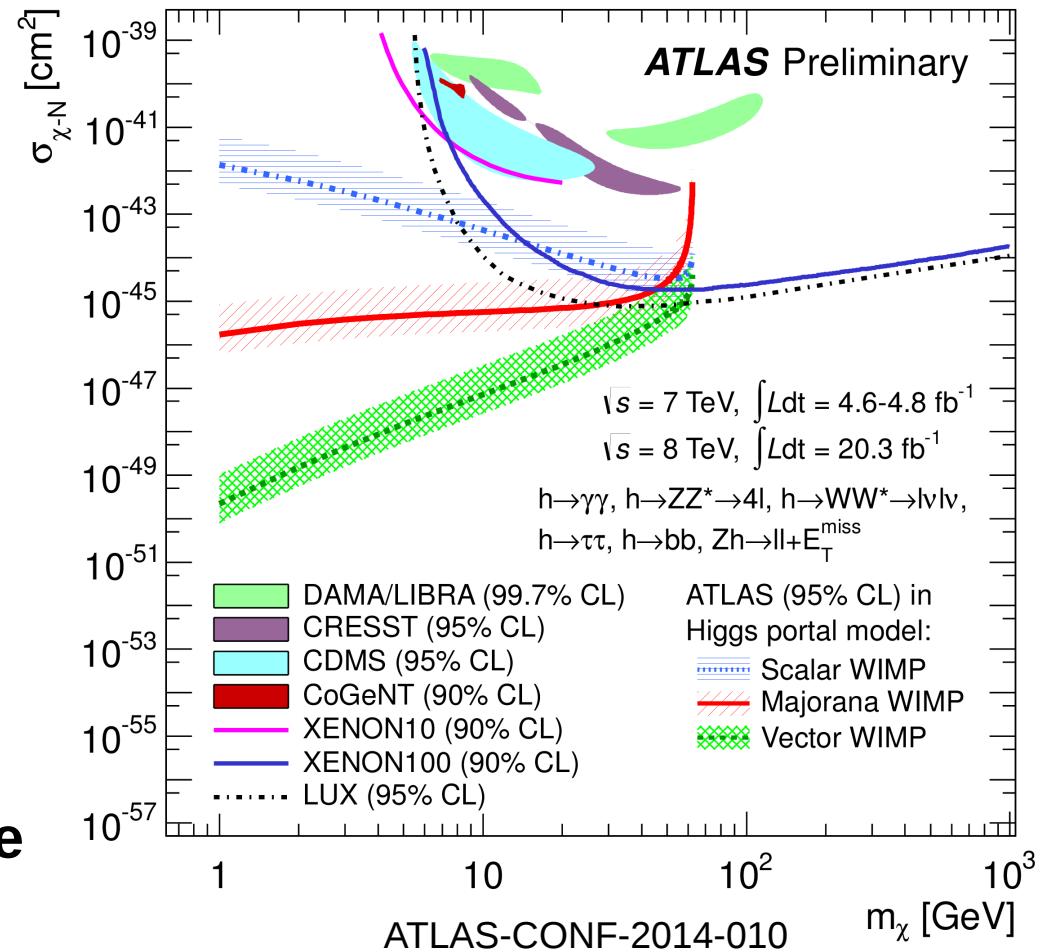
- **6-channels** : Ignoring physical boundary → alternative procedure :
  - Obs. :  $BR_{inv} = -0.02 \pm 0.20 \rightarrow \mathbf{BR_{inv} < 0.37 @ 95 \% CL}$
  - Exp. :  $BR_{inv} = 0.00 \pm 0.21 \rightarrow \mathbf{BR_{inv} < 0.39 @ 95 \% CL}$
- **5-channels results** : Ignoring physical boundary → alternative procedure :
  - Obs. :  $BR_{inv} = -0.16^{+0.28}_{-0.30} \rightarrow \mathbf{BR_{inv} < 0.41 @ 95 \% CL}$
  - Exp. :  $BR_{inv} = 0.00^{+0.29}_{-0.32} \rightarrow \mathbf{BR_{inv} < 0.55 @ 95 \% CL}$

- Continuous curves stop at -0.3 due to negative pdfs



# Higgs portal to Dark matter

- Possible to convert the invisible branching ratio into scattering cross section of dark matter on a nuclei
- Depends on the nature (scalar, fermionic, vector) of dark matter
- Allow **comparison with direct searches** ( e.g XENON)
- Assume the invisible branching ratio of the Higgs boson only comes from the wimps
- Assume VH production rate of Standard Model
- **Limits from ATLAS in Higgs Portal model at low mass significantly better than those from direct detection limits**



# Conclusion

- All results compatible with Standard Model
- Higgs Imposter : consistent with mass scaling and vev within  $1.5\sigma$
- Higgs compositeness :
  - MCHM 4 :  $f > 710$  GeV (exp. :  $f > 460$  GeV)
  - MCHM 5 :  $f > 640$  GeV (exp. :  $f > 550$  GeV)
- Electroweak Singlet :  $\kappa'^2 < 0.12$  (0.29) observed (expected)
- 2HDM : consistent with SM alignment limit within 1-2 $\sigma$
- Simplified MSSM model :
  - for  $\tan \beta > 2$ ,  $m_A > 400$  (290) GeV obs. (exp.) @ 95% CL
- Higgs Portal to dark matter :
  - $BR_{inv} < 0.37$  (0.39) observed (expected) @ 95 % CL

Thanks

Questions ?

**BACKUP**



# Input Channels : 7 TeV

Higgs Boson Decay	Subsequent Decay	Sub-Channels	$\int L dt$ [fb <sup>-1</sup> ]
2011 $\sqrt{s} = 7$ TeV			
$H \rightarrow \gamma\gamma$	–	10 categories $\{p_{Tl} \otimes \eta_\gamma \otimes \text{conversion}\} \oplus \{2\text{-jet VBF}\}$	4.8
$H \rightarrow ZZ^{(*)}$	4l	$\{4e, 2e2\mu, 2\mu2e, 4\mu, 2\text{-jet VBF}, \ell\text{-tag}\}$	4.6
$H \rightarrow WW^{(*)}$	$l\nu l\nu$	$\{ee, e\mu, \mu e, \mu\mu\} \otimes \{0\text{-jet}, 1\text{-jet}, 2\text{-jet VBF}\}$	4.6
$VH \rightarrow Vbb$	$Z \rightarrow \nu\nu$	$E_T^{\text{miss}} \in \{120 - 160, 160 - 200, \geq 200 \text{ GeV}\} \otimes \{2\text{-jet}, 3\text{-jet}\}$	4.6
	$W \rightarrow l\nu$	$p_T^W \in \{< 50, 50 - 100, 100 - 150, 150 - 200, \geq 200 \text{ GeV}\}$	4.7
	$Z \rightarrow ll$	$p_T^Z \in \{< 50, 50 - 100, 100 - 150, 150 - 200, \geq 200 \text{ GeV}\}$	4.7

- For the invisible Higgs combination (and Higgs portal to dark matter), use also the  $Zh \rightarrow ll + E_t^{\text{miss}}$ :  
 → arxiv:1402.3244

# Input Channels : 8 TeV

Higgs Boson Decay	Subsequent Decay	Sub-Channels	$\int L dt$ [fb <sup>-1</sup> ]
2012 $\sqrt{s} = 8$ TeV			
$H \rightarrow \gamma\gamma$	–	14 categories: $\{p_{Tt} \otimes \eta_\gamma \otimes \text{conversion}\} \oplus$ $\{\text{loose, tight 2-jet VBF}\} \oplus \{\ell\text{-tag, } E_T^{\text{miss}}\text{-tag, 2-jet VH}\}$	20.3
$H \rightarrow ZZ^{(*)}$	$4\ell$	$\{4e, 2e2\mu, 2\mu2e, 4\mu, 2\text{-jet VBF}, \ell\text{-tag}\}$	20.3
$H \rightarrow WW^{(*)}$	$\ell\nu\ell\nu$	$\{ee, e\mu, \mu e, \mu\mu\} \otimes \{0\text{-jet, 1-jet, 2-jet VBF}\}$	20.3
$VH \rightarrow Vbb$	$Z \rightarrow \nu\nu$	$E_T^{\text{miss}} \in \{120 - 160, 160 - 200, \geq 200 \text{ GeV}\} \otimes \{2\text{-jet, 3-jet}\}$	20.3
	$W \rightarrow \ell\nu$	$p_T^W \in \{<90, 90\text{-}120, 120\text{-}160, 160\text{-}200, \geq 200 \text{ GeV}\} \otimes \{2\text{-jet, 3-jet}\}$	20.3
	$Z \rightarrow \ell\ell$	$p_T^Z \in \{<90, 90\text{-}120, 120\text{-}160, 160\text{-}200, \geq 200 \text{ GeV}\} \otimes \{2\text{-jet, 3-jet}\}$	20.3
$H \rightarrow \tau\tau$	$\tau_{\text{lep}}\tau_{\text{lep}}$	$\{ee, e\mu, \mu\mu\} \otimes \{\text{boosted, 2-jet VBF}\}$	20.3
	$\tau_{\text{lep}}\tau_{\text{had}}$	$\{e, \mu\} \otimes \{\text{boosted, 2-jet VBF}\}$	20.3
	$\tau_{\text{had}}\tau_{\text{had}}$	$\{\text{boosted, 2-jet VBF}\}$	20.3

- For the invisible Higgs combination (and Higgs portal to dark matter), use also the  $Zh \rightarrow \ell\ell + E_t^{\text{miss}}$ :

→ arxiv:1402.3244

# Alternative procedure : Test Statistic

- Determination of the confidence interval uses the profiled likelihood ratio :

$$\Lambda(\alpha) = \frac{\mathcal{L}(\alpha, \hat{\hat{\theta}}(\alpha))}{\mathcal{L}(\hat{\alpha}, \hat{\theta})} \quad \begin{array}{l} \alpha : \text{parameters of interest} \\ \theta : \text{nuisance parameters} \end{array}$$

- **If the studied parameter has a physical boundary** (for instance  $BR_{inv} > 0$ ), an **alternative test statistic is defined** (similar to the Feldmans and Cousins procedure)
- Alternative test statistic for a boundary at zero:

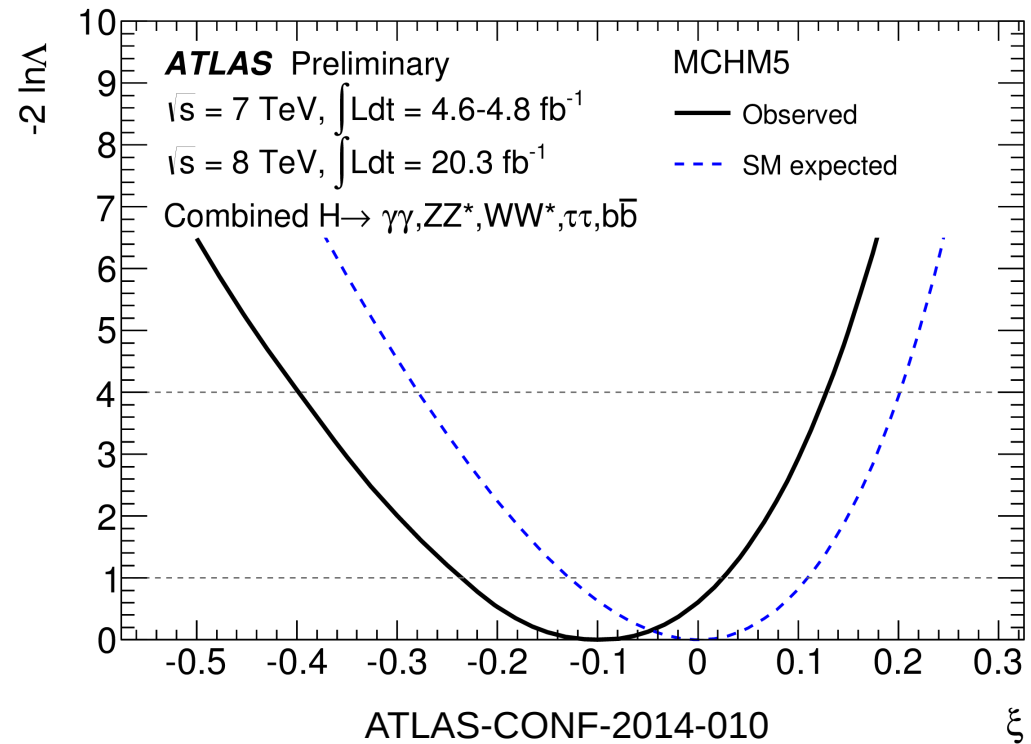
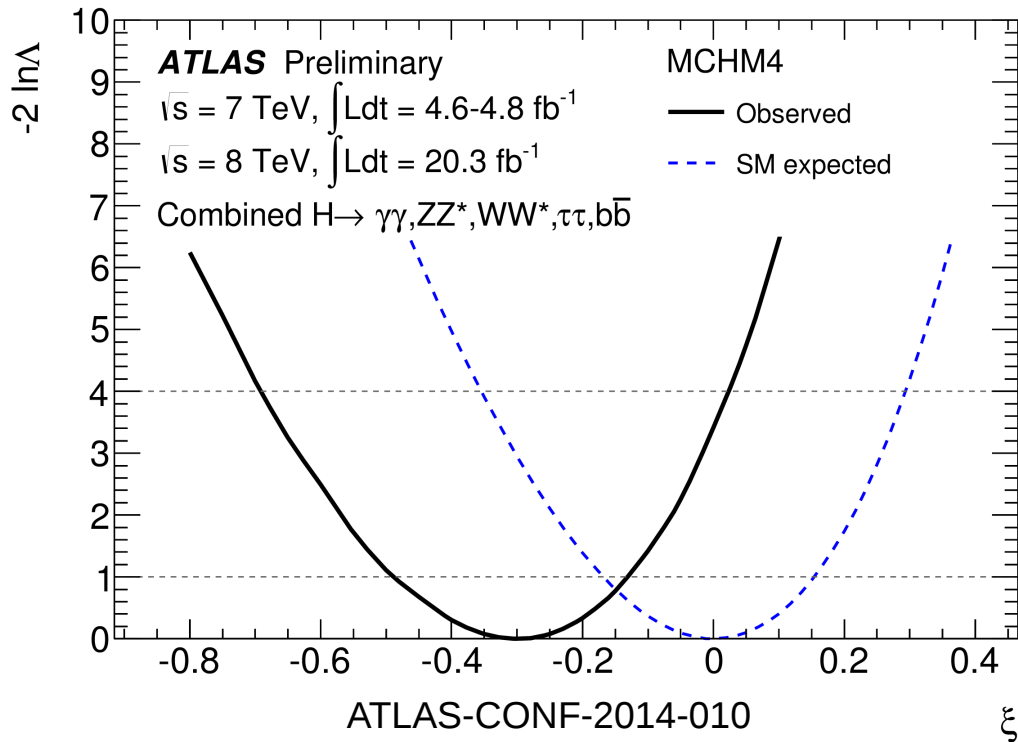
$$\tilde{t}_{\mu} = \begin{cases} \frac{\mathcal{L}(\alpha, \hat{\hat{\theta}}(\alpha))}{\mathcal{L}(0, \hat{\hat{\theta}}(0))} & \hat{\mu} < 0 \\ \frac{\mathcal{L}(\alpha, \hat{\hat{\theta}}(\alpha))}{\mathcal{L}(\hat{\alpha}, \hat{\theta})} & \hat{\mu} > 0 \end{cases}$$

# Higgs Compositeness : Results

- Best fit values and errors (Ignoring physical boundary  $\xi > 0$ ) :

→ MCHM 4 :  $\xi = -0.30^{+0.17}_{-0.18}$  (obs.) and  $\xi = 0.00^{+0.15}_{-0.17}$  (exp.)

→ MCHM 5 :  $\xi = -0.08^{+0.11}_{-0.16}$  (obs.) and  $\xi = 0.00^{+0.11}_{-0.13}$  (exp.)



# Simplified MSSM : Mass Matrix

- Mass matrix given by :

$$M_S^2 = \begin{pmatrix} m_Z^2 \cos^2 \beta + m_A^2 \sin^2 \beta & -(m_Z^2 + m_A^2) \cos \beta \sin \beta \\ -(m_Z^2 + m_A^2) \cos \beta \sin \beta & m_Z^2 \sin^2 \beta + m_A^2 \cos^2 \beta \end{pmatrix} + \begin{pmatrix} \Delta M_{11}^2 & \Delta M_{12}^2 \\ \Delta M_{12}^2 & \Delta M_{22}^2 \end{pmatrix}$$

- It is possible to show that :

$$\Delta M_{22}^2 = \frac{\delta}{\sin^2 \beta} \gg \Delta M_{11}^2, \Delta M_{12}^2$$

- And finally :  $M_h^2 = M_Z^2 \cos^2(2\beta) + \delta$

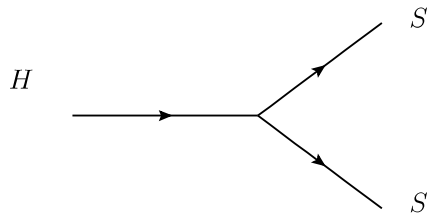
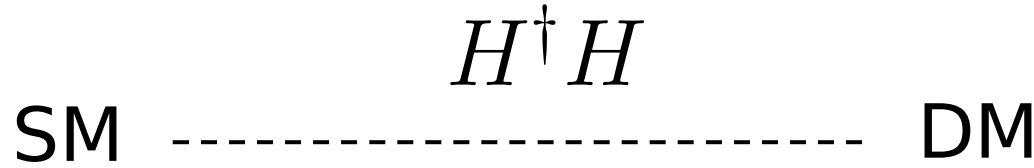
- The expressions of deviation coupling modifiers are :

$$\kappa_{down} = \frac{\sqrt{1 + \tan^2 \beta}}{\sqrt{1 + \left( \frac{m_h^2 - M_Z^2 \cos^2 \beta - M_A^2 \sin^2 \beta}{-(M_Z^2 + M_A^2) \cos \beta \sin \beta} \right)^2}} \quad \kappa_{up} = \frac{\frac{\sqrt{1 + \tan^2 \beta}}{\tan \beta} \frac{m_h^2 - M_Z^2 \cos^2 \beta - M_A^2 \sin^2 \beta}{-(M_Z^2 + M_A^2) \cos \beta \sin \beta}}{\sqrt{1 + \left( \frac{m_h^2 - M_Z^2 \cos^2 \beta - M_A^2 \sin^2 \beta}{-(M_Z^2 + M_A^2) \cos \beta \sin \beta} \right)^2}}$$

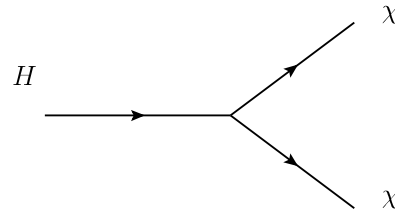
$$\kappa_V = \frac{\frac{1}{\sqrt{1 + \tan^2 \beta}}}{\sqrt{1 + \left( \frac{m_h^2 - M_Z^2 \cos^2 \beta - M_A^2 \sin^2 \beta}{-(M_Z^2 + M_A^2) \cos \beta \sin \beta} \right)^2}} + \frac{\frac{\tan \beta}{\sqrt{1 + \tan^2 \beta}} \frac{m_h^2 - M_Z^2 \cos^2 \beta - M_A^2 \sin^2 \beta}{-(M_Z^2 + M_A^2) \cos \beta \sin \beta}}{\sqrt{1 + \left( \frac{m_h^2 - M_Z^2 \cos^2 \beta - M_A^2 \sin^2 \beta}{-(M_Z^2 + M_A^2) \cos \beta \sin \beta} \right)^2}}$$

# Interpretation in Higgs Portal to DM

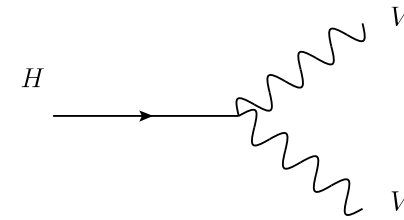
Djouadi, Falkowski, Mambrini, Quevillon



$$\mathcal{L}_S \supset -\frac{1}{2}m_S S^2 - \frac{1}{4}\lambda_S S^4 - \frac{1}{4}\lambda_{hSS} H^\dagger H S^2$$



$$\mathcal{L} \supset -\frac{1}{2}m_f \bar{\chi}\chi - \frac{1}{4}\frac{\lambda_{hff}}{\Lambda} H^\dagger H \bar{\chi}\chi$$



$$\mathcal{L} \supset \frac{1}{2}m_V^2 V_\mu V^\mu + \frac{1}{4}\lambda_V (V_\mu V^\mu)^2 + \frac{1}{4}\lambda_{hVV} H^\dagger H V_\mu V^\mu$$

Spin Independent (SI) DM-nucleon elastic cross section

$$\sigma_{S-N}^{SI} = \frac{\lambda_{hSS}^2}{16\pi m_h^4} \frac{m_N^4 f_N^2}{(M_S + m_N)^2},$$

$$\sigma_{V-N}^{SI} = \frac{\lambda_{hVV}^2}{16\pi m_h^4} \frac{m_N^4 f_N^2}{(M_V + m_N)^2},$$

$$\sigma_{f-N}^{SI} = \frac{\lambda_{hff}^2}{4\pi \Lambda^2 m_h^4} \frac{m_N^4 M_f^2 f_N^2}{(M_f + m_N)^2}$$

$$\Gamma_{h \rightarrow SS}^{\text{inv}} = \frac{\lambda_{hSS}^2 v^2 \beta_S}{64\pi m_h},$$

$$\Gamma_{h \rightarrow VV}^{\text{inv}} = \frac{\lambda_{hVV}^2 v^2 m_h^3 \beta_V}{256\pi M_V^4} \left( 1 - 4\frac{M_V^2}{m_h^2} + 12\frac{M_V^4}{m_h^4} \right),$$

$$\Gamma_{h \rightarrow \chi\chi}^{\text{inv}} = \frac{\lambda_{hff}^2 v^2 m_h \beta_f^3}{32\pi \Lambda^2},$$

$$\beta_X = \sqrt{1 - 4M_X^2/m_h^2}$$