Composite scalar dark matter

Michele Frigerio Laboratoire Charles Coulomb, CNRS & UM2, Montpellier

MF, Alex Pomarol, Francesco Riva, Alfredo Urbano, JHEP 1207 (2012) 015 MF, Sylvain Lacroix, Alfredo Urbano, in preparation

New Perspectives in Dark Matter



 pseudo Nambu-Goldstone bosons (pNGBs) related to the electroweak scale: appealing candidates for dark matter (DM)

- pseudo Nambu-Goldstone bosons (pNGBs) related to the electroweak scale: appealing candidates for dark matter (DM)
- a strongly-coupled sector at the multi-TeV scale and the Higgs as a composite pNGB

- pseudo Nambu-Goldstone bosons (pNGBs) related to the electroweak scale: appealing candidates for dark matter (DM)
- a strongly-coupled sector at the multi-TeV scale and the Higgs as a composite pNGB
- DM as a composite pNGB coupled to the composite Higgs: the interactions are determined by global symmetries

- pseudo Nambu-Goldstone bosons (pNGBs) related to the electroweak scale: appealing candidates for dark matter (DM)
- a strongly-coupled sector at the multi-TeV scale and the Higgs as a composite pNGB
- DM as a composite pNGB coupled to the composite Higgs: the interactions are determined by global symmetries
- phenomenology: the effect of compositeness on the DM relic density, the Higgs searches & the DM searches

 spontaneously symmetry breaking (SB) of a global symmetry: massless spin-0 field with only derivative interactions, an exact Nambu-Goldstone boson (NGB)

- spontaneously symmetry breaking (SB) of a global symmetry: massless spin-0 field with only derivative interactions, an exact Nambu-Goldstone boson (NGB)
- explicitly SB (by a coupling or an anomaly): the pseudo-NGB acquires a mass and non-derivative interactions

- spontaneously symmetry breaking (SB) of a global symmetry: massless spin-0 field with only derivative interactions, an exact Nambu-Goldstone boson (NGB)
- explicitly SB (by a coupling or an anomaly): the pseudo-NGB acquires a mass and non-derivative interactions
- approximate symmetry: the scale of spontaneous SB is larger than the scale of explicit SB / the source of explicit SB are weak couplings

• The pNGB mass scale is not chosen ad-hoc: it is induced by a physical scale, e.g. Λ_{QCD} or Λ_{EW} , and it is radiatively stable

- The pNGB mass scale is not chosen ad-hoc: it is induced by a physical scale, e.g. Λ_{QCD} or Λ_{EW} , and it is radiatively stable
- Explicit SB parameters induce both the pNGB mass & its couplings to the SM, that control its relic density: compelling correspondence between mDM and Ω_{DM}

- The pNGB mass scale is not chosen ad-hoc: it is induced by a physical scale, e.g. Λ_{QCD} or Λ_{EW} , and it is radiatively stable
- Explicit SB parameters induce both the pNGB mass & its couplings to the SM, that control its relic density: compelling correspondence between mDM and Ω_{DM}
- Rationale for DM stability: either SB preserves a remnant global symmetry that forbids DM decays, or DM is sufficiently longlived because the spontaneous SM scale f is very large, TDM ~ f²

A oversimplified set-up

- Before coming to compositeness, a light pNGB just means that the effective theory to be studied amounts to the SM plus a gauge singlet real scalar η
- Assuming a parity $\eta \rightarrow -\eta$, the only renormalizable coupling to the SM is the Higgs portal: $\lambda H^{\dagger} H \eta \eta$
- A warm-up exercise: let us compute the η relic density in this minimal case

Minimal renormalizable model extensively studied: Silveira Zee '85, McDonald '94, Burgess Pospelov ter Veldhuis '01,

...

The Higgs portal to dark matter $\mathcal{L}_{eff} = \mathcal{L}_{SM} - \frac{\lambda}{2} H^{\dagger} H \eta \eta \qquad m_{\eta}^2 = \lambda v^2$

(i) explicit SB induces a quartic coupling between H and a pNGB η (ii) a parity $\eta \rightarrow -\eta$ is preserved, as a residual global symmetry

(iii) a direct mass term η^2 is suppressed, that can be the case in some models

The Higgs portal to dark matter

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} - \frac{\lambda}{2} H^{\dagger} H \eta \eta \qquad m_{\eta}^2 = \lambda v^2$$

(i) explicit SB induces a quartic coupling between H and a pNGB η (ii) a parity $\eta \rightarrow -\eta$ is preserved, as a residual global symmetry

(iii) a direct mass term η^2 is suppressed, that can be the case in some models

At temperatures $T \sim m_h$ the interaction λ may or may not thermalize η

$$\Gamma(h \to \eta \eta) = \frac{1}{16\pi} \lambda^2 \frac{v^2}{m_h} \sqrt{1 - \frac{4m_\eta^2}{m_h^2}} \quad \text{versus} \quad \mathcal{H}(T = m_h) \simeq 17 \frac{m_h^2}{M_{Planck}}$$

Thermalization for: $\lambda \gtrsim 6 \times 10^{-8} \left(\frac{m_h}{125 \text{ GeV}}\right)^{3/2}$ or $m_\eta \gtrsim 42 \text{ MeV}$



Freeze-out: n thermalizes and later decouples, at $T \leq m_{\eta}$. To obtain the correct Ω_{DM} one needs $m_{\eta} \approx 50$ GeV.

e.g. Farina, Pappadopulo, Strumia, 2010

• Freeze-out: η thermalizes and later decouples, at $T \leq m_{\eta}$. To obtain the correct Ω_{DM} one needs $m_{\eta} \approx 50$ GeV.

e.g. Farina, Pappadopulo, Strumia, 2010

Y = n/s



 $z_{f.o.} = m_{\eta}/T$

arrows indicate increasing values of λ

• Freeze-out: η thermalizes and later decouples, at $T \leq m_{\eta}$. To obtain the correct Ω_{DM} one needs $m_{\eta} \approx 50$ GeV.

e.g. Farina, Pappadopulo, Strumia, 2010



from Hall, Jedamzik, March-Russell, West, 2009



arrows indicate increasing values of λ

• Freeze-out: η thermalizes and later decouples, at $T \leq m_{\eta}$. To obtain the correct Ω_{DM} one needs $m_{\eta} \approx 50$ GeV.

e.g. Farina, Pappadopulo, Strumia, 2010

Freeze-in: a less-than-thermal population of η 's is produced by the annihilation/decay of heavier particles, X = h, W, Z. The η number density reaches a plateau at T \approx m_X. We found that Ω_{DM} is reproduced for $m_{\eta} \approx 3$ MeV ($\lambda \approx 10^{-10}$).

Frigerio, Hambye, Masso 2011

$$Y = n/s$$

from Hall, Jedamzik, March-Russell, West, 2009



 $\frac{z_{f.o.}}{z_{f.i.}} = \frac{m_{\eta}}{T}$

arrows indicate increasing values of λ

Composite pNGBs



















The composite sector (I)



SM + a new sector strongly coupled & approximately conformal from M_{Pl} down to $\Lambda_{EW} \sim \text{TeV}$, where strong dynamics breaks conformal & global symmetries: $G \rightarrow K$

The composite sector (I)



SM + a new sector strongly coupled & approximately conformal from M_{Pl} down to $\Lambda_{EW} \sim \text{TeV}$, where strong dynamics breaks conformal & global symmetries: $G \rightarrow K$

$$\begin{array}{lcl} G &=& O(6) \times U(1) \\ K &=& O(5) \times U(1) \supset SU(2)_L \times U(1)_Y \mbox{ with custodial} \\ \rho &= \frac{m_W^2}{m_Z^2 \cos \theta_W^2} = 1 \ , & \mbox{ without custodial } \Delta \rho \simeq \frac{v^2}{f^2} \lesssim 10^{-3} \end{array}$$

The composite sector (II)

The couplings of elementary fields with composite operators break explicitly (weakly) G, while preserving G_{SM}

$$\mathcal{L}_{mixing} = g_i A_i^{\mu} \mathcal{J}_{\mu} + \lambda_{\psi} \overline{\psi} \mathcal{O}_{\psi}$$

The composite sector (II)

The couplings of elementary fields with composite operators break explicitly (weakly) G, while preserving G_{SM}

$$\mathcal{L}_{mixing} = g_i A_i^{\mu} \mathcal{J}_{\mu} + \lambda_{\psi} \overline{\psi} \mathcal{O}_{\psi}$$

Giudice-Grojean-Pomarol-Rattazzi '07

The DM global symmetries

At $\Lambda_{EW} \sim 3-4$ TeV, the strong dynamics breaks spontaneously $O(6) \rightarrow O(5)$

The coset of this non-linear σ -model:

$$\Sigma = \exp\left(i\frac{\sqrt{2}\pi^{a}T^{a}}{f}\right)\Sigma_{0} = \frac{1}{f}\left(h_{1}, h_{2}, h_{3}, h_{4}, \eta, \sqrt{f^{2} - h^{2} - \eta^{2}}\right)^{T}$$

The DM global symmetries

At $\Lambda_{EW} \sim 3-4$ TeV, the strong dynamics breaks spontaneously $O(6) \rightarrow O(5)$

The coset of this non-linear σ -model:

$$\Sigma = \exp\left(i\frac{\sqrt{2}\pi^{a}T^{a}}{f}\right)\Sigma_{0} = \frac{1}{f}\left(h_{1}, h_{2}, h_{3}, h_{4}, \eta, \sqrt{f^{2} - h^{2} - \eta^{2}}\right)^{T}$$

A parity $\eta \rightarrow -\eta$ guarantees the DM stability: $O(6) = P_{\eta} \times SO(6)$ $P_{\eta} = diag(1, 1, 1, 1, -1, 1)$

The DM global symmetries

At $\Lambda_{EW} \sim 3-4$ TeV, the strong dynamics breaks spontaneously $O(6) \rightarrow O(5)$

The coset of this non-linear σ -model:

$$\Sigma = \exp\left(i\frac{\sqrt{2}\pi^{a}T^{a}}{f}\right)\Sigma_{0} = \frac{1}{f}\left(h_{1}, h_{2}, h_{3}, h_{4}, \eta, \sqrt{f^{2} - h^{2} - \eta^{2}}\right)^{T}$$

A parity
$$\eta \rightarrow -\eta$$
 guarantees the DM stability:
 $O(6) = P_{\eta} \times SO(6)$ $P_{\eta} = diag(1, 1, 1, 1, -1, 1)$

The DM mass is protected by a shift symmetry $\eta \rightarrow \eta + \alpha$ $SO(6) \supset SO(4) \times SO(2)_{\eta} = SU(2)_L \times SU(2)_R \times U(1)_{\eta}$

Below the strong-coupling scale $\Lambda_{\rm EW}$ ~ 3-4 TeV, the Lagrangian for h and η can be expanded in 1/f, with f the pNGB decay constant $f\gtrsim 500\,{
m GeV}$

Below the strong-coupling scale $\Lambda_{\rm EW}$ ~ 3-4 TeV, the Lagrangian for h and η can be expanded in 1/f, with f the pNGB decay constant $f\gtrsim 500\,{
m GeV}$

Derivative interactions fixed by the O(6)/O(5) symmetry

$$\mathcal{L}_{kin}^{\eta} = \frac{1}{2} (\partial_{\mu} \eta)^2 + \frac{1}{2f^2} \partial_{\mu} |H|^2 \partial^{\mu} \eta^2 + \dots$$

DM-Higgs interaction growing with momentum

Below the strong-coupling scale $\Lambda_{\rm EW}$ ~ 3-4 TeV, the Lagrangian for h and η can be expanded in 1/f, with f the pNGB decay constant $f\gtrsim 500\,{
m GeV}$

Derivative interactions fixed by the O(6)/O(5) symmetry

$$\mathcal{L}^{\eta}_{kin} = \frac{1}{2} (\partial_{\mu} \eta)^2 + \frac{1}{2f^2} \partial_{\mu} |H|^2 \partial^{\mu} \eta^2 + \dots \qquad \begin{array}{l} \mathsf{DM-Higgs interaction} \\ \text{growing with momentum} \end{array}$$

Interactions with the elementary fermions proportional to Yukawas $\mathcal{L}_{fermions}^{\eta} = \frac{\eta^2}{f^2} \left(c_t y_t \ \overline{q_L} \tilde{H} t_R + c_b y_b \ \overline{q_L} H b_R + h.c. \right) + \dots$

If the top couplings break (preserve) the η -shift symmetry, then c_t is of order one (vanishes); analogously for the other fermions

Below the strong-coupling scale $\Lambda_{\rm EW}$ ~ 3-4 TeV, the Lagrangian for h and η can be expanded in 1/f, with f the pNGB decay constant $f\gtrsim 500\,{
m GeV}$

Derivative interactions fixed by the O(6)/O(5) symmetry

$$\mathcal{L}_{kin}^{\eta} = \frac{1}{2} (\partial_{\mu} \eta)^2 + \frac{1}{2f^2} \partial_{\mu} |H|^2 \partial^{\mu} \eta^2 + \dots \qquad \begin{array}{l} \mathsf{DM-Higgs interaction} \\ \text{growing with momentum} \end{array}$$

Interactions with the elementary fermions proportional to Yukawas $\mathcal{L}_{fermions}^{\eta} = \frac{\eta^2}{f^2} \left(c_t y_t \ \overline{q_L} \tilde{H} t_R + c_b y_b \ \overline{q_L} H b_R + h.c. \right) + \dots$

If the top couplings break (preserve) the η -shift symmetry, then c_t is of order one (vanishes); analogously for the other fermions

Effective potential generated by fermion loops

$$\mathcal{L}_{pot}^{\eta} = \frac{1}{2}\mu_{\eta}^2\eta^2 + \lambda|H|^2\eta^2 + \dots$$

 $m_{\eta} > O(100) \text{ GeV for } c_t = O(1)$ $m_{\eta} > O(10) \text{ GeV for } c_b = O(1)$



Couplings in the case SM + singlet with no compositeness



Couplings in the case SM + singlet with no compositeness

Three main effects of compositeness:



Couplings in the case SM + singlet with no compositeness

Three main effects of compositeness:

 new pNGB couplings proportional to p² / f²



Couplings in the case SM + singlet with no compositeness

Three main effects of compositeness:

 new pNGB couplings proportional to p² / f²

• new DM- ψ couplings of order m_{ψ}/f^2



The relic density of η



dashed line: no compositeness (SM + singlet) solid lines: compositeness with the bottom coupled to η (dotted lines: compositeness with also the top coupled to η)

Bounds from DM searches

Invisible Higgs decays into DM: $h \rightarrow \eta \eta$ (plus visible decays corrected at order ξ)

$$\Gamma_{inv} = \frac{v^2}{32\pi m_h} \sqrt{1 - \frac{4m_{\eta}^2}{m_h^2}} \left(\frac{m_h^2}{v^2} \frac{\xi}{\sqrt{1 - \xi}} - 2\lambda\sqrt{1 - \xi}\right)^2 \vartheta(m_h - 2m_{\eta})$$

ATLAS & CMS: $\Gamma_{inv} \lesssim \Gamma_{SM} / 4$ (95%C.L.)

Bounds from DM searches

Invisible Higgs decays into DM: $h \rightarrow \eta \eta$ (plus visible decays corrected at order ξ)

$$\Gamma_{inv} = \frac{v^2}{32\pi m_h} \sqrt{1 - \frac{4m_\eta^2}{m_h^2}} \left(\frac{m_h^2}{v^2} \frac{\xi}{\sqrt{1 - \xi}} - 2\lambda\sqrt{1 - \xi}\right)^2 \vartheta(m_h - 2m_\eta)$$

ATLAS & CMS: $\Gamma_{inv} \lesssim \Gamma_{SM} / 4$ (95%C.L.)

DM elastic scattering on nuclei: $\eta N \rightarrow \eta N$

$$\sigma_{\rm SI} \simeq 3.5 \cdot 10^{-40} {\rm cm}^2 \left(\frac{10 \,{\rm GeV}}{m_\eta}\right)^2 \left(\frac{125 \,{\rm GeV}}{m_h}\right)^4 \\ \times \left[\lambda \left(1 - \frac{2v^2}{f^2}\right) + \frac{m_h^2}{f^2} \,{\rm Re} \left(0.04 \,c_u + 0.11 \,c_d + 0.18 \,c_s + 0.22 \,\sum_{q=c,b,t} c_q\right)\right]^2$$

 $\begin{array}{l} \text{XENON 100:} \\ \sigma_{\text{SI}} \lesssim 10^{\text{-44}} \text{cm}^2 \text{ for} \\ m_\eta \sim (20\text{-}500) \text{ GeV} \end{array}$

Bounds from DM searches

Invisible Higgs decays into DM: $h \rightarrow \eta \eta$ (plus visible decays corrected at order ξ)

$$\Gamma_{inv} = \frac{v^2}{32\pi m_h} \sqrt{1 - \frac{4m_\eta^2}{m_h^2}} \left(\frac{m_h^2}{v^2} \frac{\xi}{\sqrt{1 - \xi}} - 2\lambda\sqrt{1 - \xi}\right)^2 \vartheta(m_h - 2m_\eta)$$

ATLAS & CMS: $\Gamma_{inv} \lesssim \Gamma_{SM} / 4$ (95%C.L.)

DM elastic scattering on nuclei: $\eta N \rightarrow \eta N$

$$\sigma_{\rm SI} \simeq 3.5 \cdot 10^{-40} {\rm cm}^2 \left(\frac{10 \,{\rm GeV}}{m_\eta}\right)^2 \left(\frac{125 \,{\rm GeV}}{m_h}\right)^4 \\ \times \left[\lambda \left(1 - \frac{2v^2}{f^2}\right) + \frac{m_h^2}{f^2} \,{\rm Re} \left(0.04 \,c_u + 0.11 \,c_d + 0.18 \,c_s + 0.22 \,\sum_{q=c,b,t} c_q\right)\right]^2$$

 $\begin{array}{l} \text{XENON 100:} \\ \sigma_{\text{SI}} \lesssim 10^{\text{-44}} \text{cm}^2 \text{ for} \\ m_\eta \sim (20\text{-}500) \text{ GeV} \end{array}$

DM annihilations today: $\eta \eta \rightarrow b b$ -bar, WW, $\gamma\gamma$, ... (work in progress)

The signal is enhanced close to the Higgs resonance, where $\langle\sigma v_{rel}\rangle$ differs significantly from the freeze-out one. Constraints from FERMI-LAT, AMS, ...

non-composite case: Cline-Kainulainen-Scott-Weniger '13



dashed: elementary DM

solid: composite DM with f = I TeV



dashed: elementary DM

solid: composite DM with f = I TeV

Purple: relic density contours with $\Omega_{\eta} = \Omega_{DM}$



dashed: elementary DM

solid: composite DM with f = I TeV

Purple: relic density contours with $\Omega_{\eta} = \Omega_{DM}$

Red: disfavoured by LHC Higgs searches



dashed: elementary DM

solid: composite DM with f = I TeV

Purple: relic density contours with $\Omega_{\eta} = \Omega_{DM}$

Red: disfavoured by LHC Higgs searches

Green: disfavoured by DM direct searches



dashed: elementary DM

solid: composite DM with f = I TeV

Purple: relic density contours with $\Omega_{\eta} = \Omega_{DM}$

Red: disfavoured by LHC Higgs searches

Green: disfavoured by DM direct searches

below the yellow line: theoretically favoured ($\lambda \le m_{\eta}^2 / f^2$)



dashed: elementary DM

solid: composite DM with f = I TeV

Purple: relic density contours with $\Omega_{\eta} = \Omega_{DM}$

Red: disfavoured by LHC Higgs searches

Green: disfavoured by DM direct searches

below the yellow line: theoretically favoured ($\lambda \le m_{\eta}^2 / f^2$)



dashed: elementary DM

solid: composite DM with f = I TeV

Purple: relic density contours with $\Omega_{\eta} = \Omega_{DM}$

Red: disfavoured by LHC Higgs searches

Green: disfavoured by DM direct searches

below the yellow line: theoretically favoured $(\lambda \le m_{\eta}^2 / f^2)$



dashed: elementary DM

solid: composite DM with f = 500 GeV

Purple: relic density contours with $\Omega_{\eta} = \Omega_{DM}$

Red: disfavoured by LHC Higgs searches

Green: disfavoured by DM direct searches

below the yellow line: theoretically favoured $(\lambda \le m_{\eta}^2/f^2)$

• LHC is rapidly improving bounds on $pp \rightarrow 1jet + missing E_T$, that in this scenario mostly come from $gg \rightarrow gh^* \rightarrow g\eta \eta$

- LHC is rapidly improving bounds on $pp \rightarrow 1jet + missing E_T$, that in this scenario mostly come from $gg \rightarrow gh^* \rightarrow g\eta \eta$
- These searches may cover some allowed regions in the plane $m_{\eta} \lambda$, and be competitive in particular for $m_{\eta} > m_{h}/2$

- LHC is rapidly improving bounds on $pp \rightarrow 1jet + missing E_T$, that in this scenario mostly come from $gg \rightarrow gh^* \rightarrow g\eta \eta$
- These searches may cover some allowed regions in the plane $m_{\eta} \lambda$, and be competitive in particular for $m_{\eta} > m_{h}/2$
- We are studying how the jet p_T distribution depends on the relative size of λ and of the derivative coupling ...

- LHC is rapidly improving bounds on $pp \rightarrow 1jet + missing E_T$, that in this scenario mostly come from $gg \rightarrow gh^* \rightarrow g\eta\eta$
- These searches may cover some allowed regions in the plane $m_{\eta} \lambda$, and be competitive in particular for $m_{\eta} > m_{h}/2$
- We are studying how the jet p_T distribution depends on the relative size of λ and of the derivative coupling ...

$$\frac{\mathrm{d}^2\sigma}{\mathrm{d}p_T\mathrm{d}y} = \frac{\alpha_s^3 p_T}{1536\pi^4} \int_{x_{1,min}}^1 \mathrm{d}x_1 f_g(x_1) \int_{x_{2,min}(x_1)}^1 \mathrm{d}x_2 f_g(x_2) \frac{(\lambda - \frac{q^2}{2f^2})^2 \sqrt{1 - \frac{4m_\eta^2}{q^2}}}{(q^2 - m_h^2)^2 + \Gamma_h^2 m_h^2} \frac{q^8 + \hat{s}^4 + \hat{t}^4 + \hat{u}^4}{\hat{s}^2 \hat{t} \hat{u}}$$

- LHC is rapidly improving bounds on $pp \rightarrow 1jet + missing E_T$, that in this scenario mostly come from $gg \rightarrow gh^* \rightarrow g\eta \eta$
- These searches may cover some allowed regions in the plane $m_{\eta} \lambda$, and be competitive in particular for $m_{\eta} > m_{h}/2$
- We are studying how the jet p_T distribution depends on the relative size of λ and of the derivative coupling ...





 pNGBs could be the first (the lightest) piece of evidence for new physics associated to the electroweak scale

Conclusions

- pNGBs could be the first (the lightest) piece of evidence for new physics associated to the electroweak scale
- the set of pNGBs may include the Higgs h as well as a scalar DM candidate η

Conclusions

- pNGBs could be the first (the lightest) piece of evidence for new physics associated to the electroweak scale
- the set of pNGBs may include the Higgs h as well as a scalar DM candidate η
- compositeness solves the hierarchy problem of light scalars, and it modifies profoundly the couplings of h and η

Conclusions

- pNGBs could be the first (the lightest) piece of evidence for new physics associated to the electroweak scale
- the set of pNGBs may include the Higgs h as well as a scalar DM candidate η
- compositeness solves the hierarchy problem of light scalars, and it modifies profoundly the couplings of h and η
- composite scalar DM has mass in the range 60 to 500 GeV and can be probed very effectively in collider searches and DM searches