

Colour Dynamics and Hadronization.

FRAGMENTATION

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Journée des Jets
LPNHE
June 20, 2008

- Hard interactions and Jets
- Hadroproduction and Colour
- Gluons in and beyond(?) PT QCD
- Gluons
 - Gluons and Feynman plateau in hard and soft processes
 - Gluons and colour blanching
- LPHD and QCD Radiophysics
 - inside jets
 - in-between jets
- Things we learned and things we haven't yet
- α_s in and beyond(?) PT QCD
- How to demystify the Kogut–Susskind hadronization picture?

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Hit hard to see what is it there *inside* (a childish but productive idea)

Hit hard to see what is it there *inside*

Heat the *Vacuum*

- e^+e^- annihilation into hadrons : $e^+e^- \rightarrow q\bar{q} \rightarrow \text{hadrons}$.

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Hit the *proton* (with an electromagnetic/electroweak probe)

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production of a quark/gluon = “jet” of hadrons

Existence of Jets was envisaged from “parton models” in the late 1960’s.

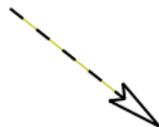
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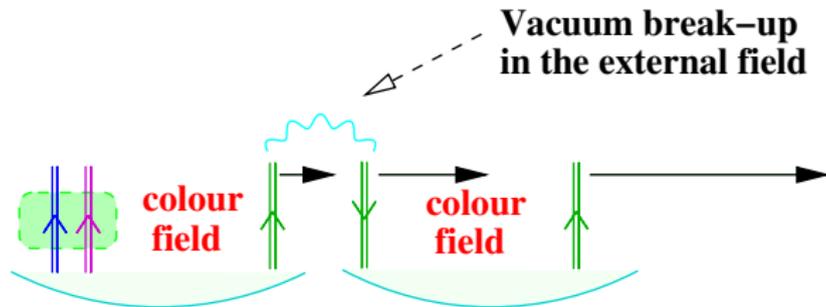
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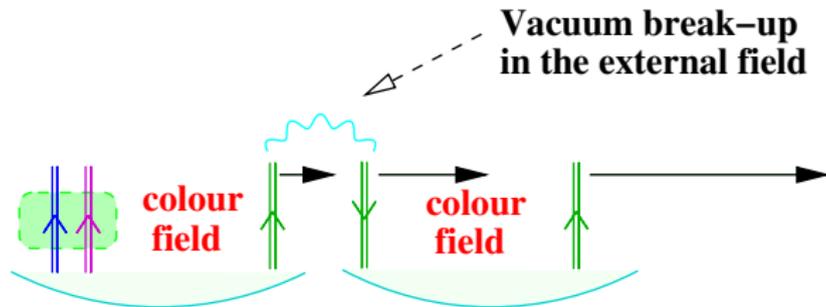
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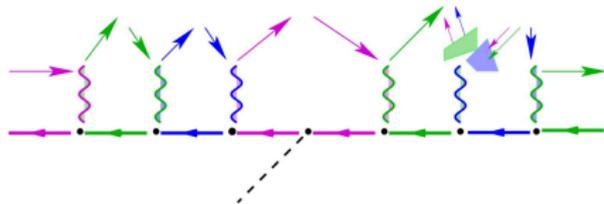
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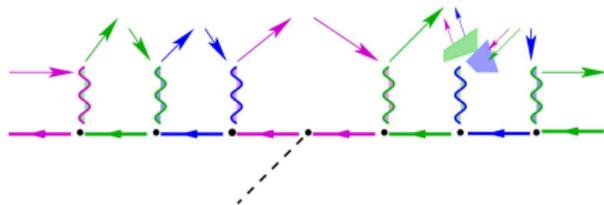
Repeating, one gets the “Feynman Plateau” :

“One” hadron per $\frac{\Delta\omega}{\omega}$; Hadron multiplicity $\propto \ln Q$.

Phenomenological realization of the Kogut–Susskind scenario



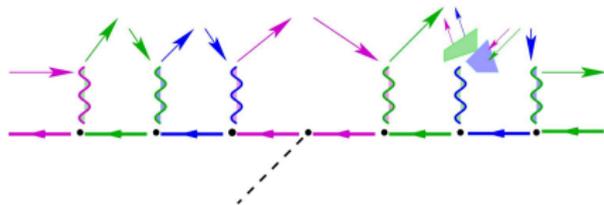
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The base of the Lund Model

The key features of the Lund hadronization model:

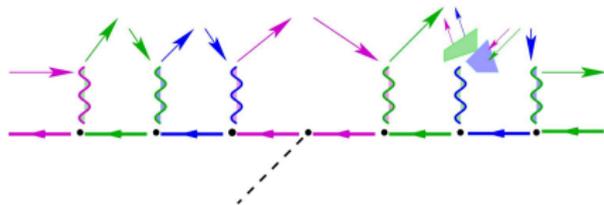
- Uniformity in *rapidity*: $dN_h = \text{const} \times \frac{d\omega_h}{\omega_h}$

- Limited k_{\perp} of hadrons

- Quark combinatorics at work:

$$\left\{ \begin{array}{l} \text{green arrow } u, d \text{ vs. } s \\ \text{green arrow } \textit{mesons} \text{ vs. } \textit{baryons} \end{array} \right.$$

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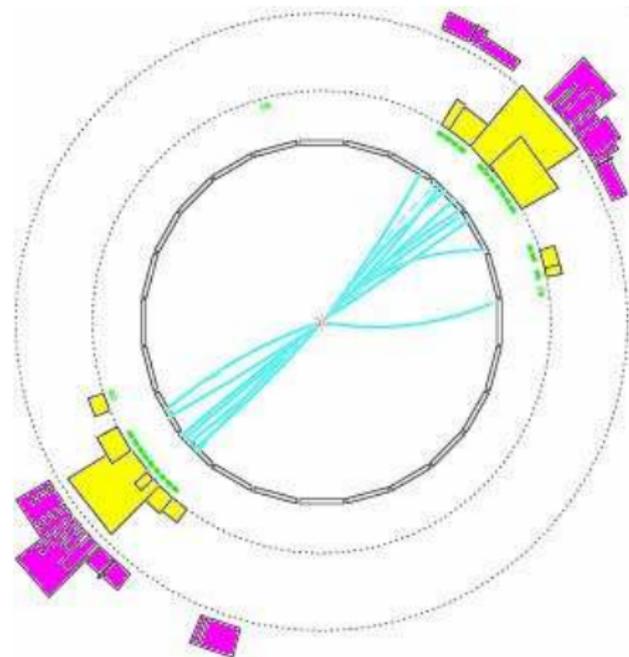
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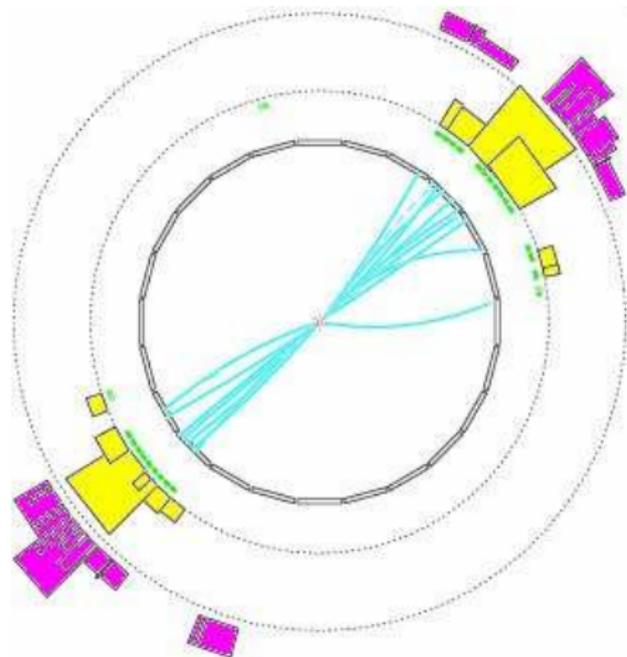
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The crucial step: Stress on the *rôle of colour* in multiple hadroproduction



Near 'perfect' 2-jet event

2 well-collimated jets of particles.



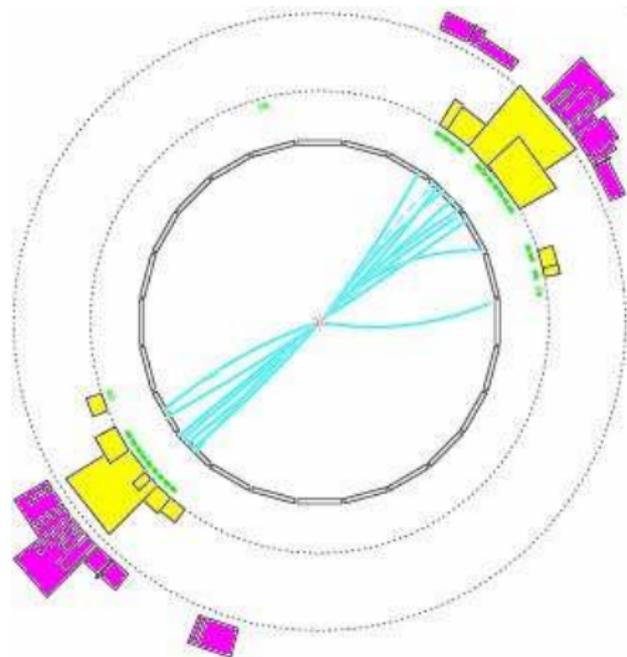
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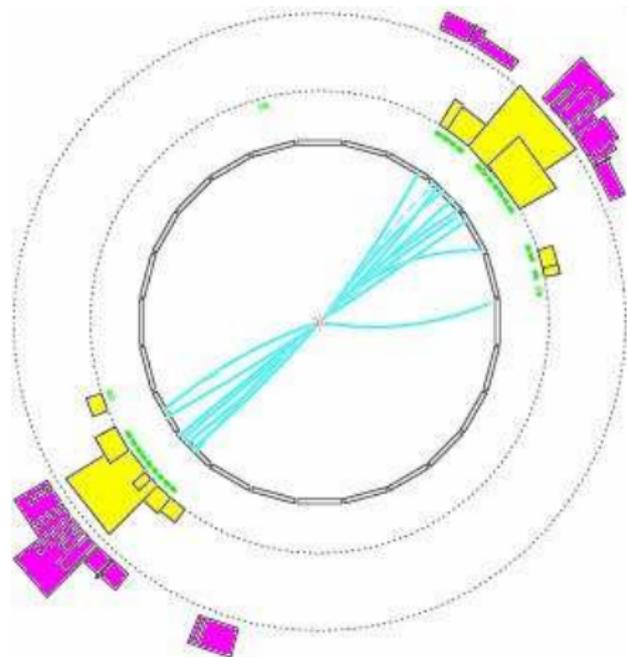
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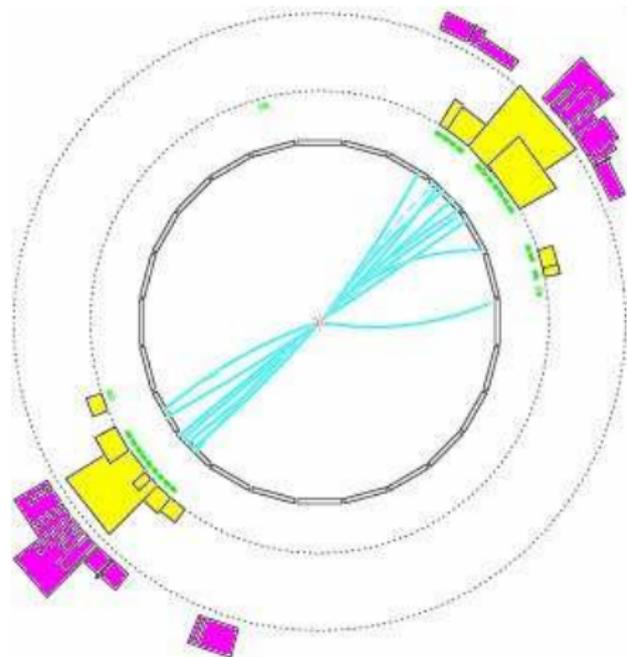
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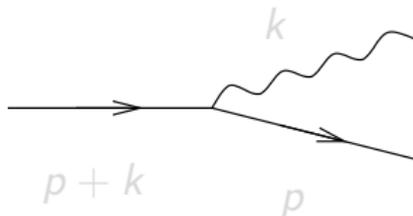
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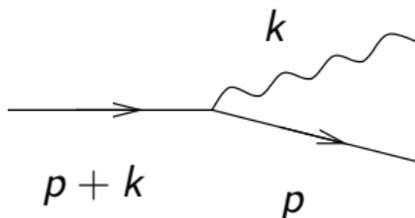


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In all cases $k_{\perp}^2 \ll Q^2$ — the domain of the MC cascade generation (scientific name: **collinear factorization**)

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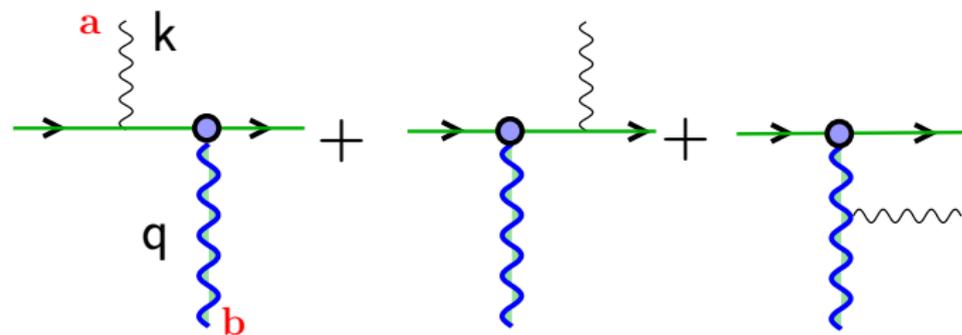
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Hadron plateau in “**minimum bias**” hadron–hadron collisions.

Rapidity plateau in hh interaction

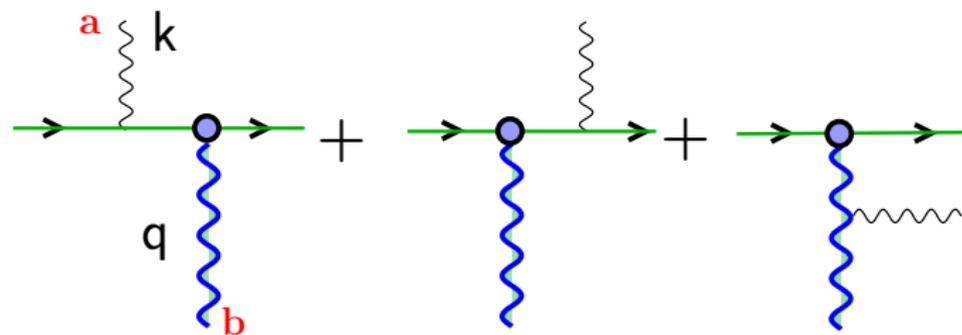
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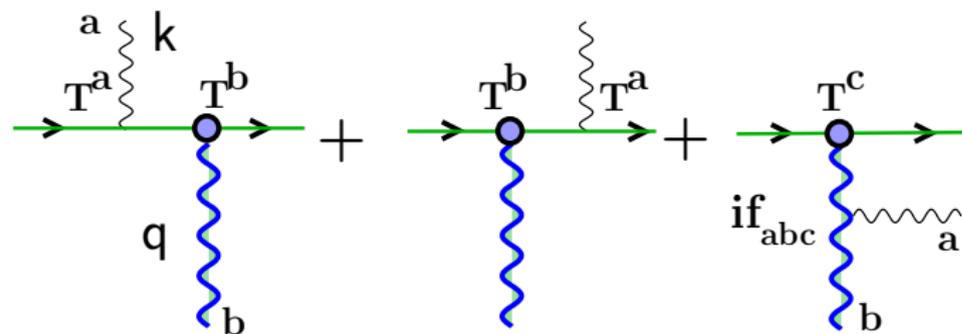
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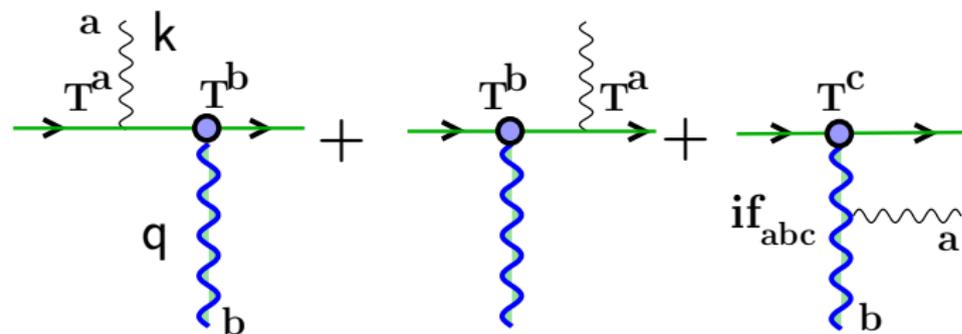
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Hadron plateau in “minimum bias” hadron–hadron collisions.

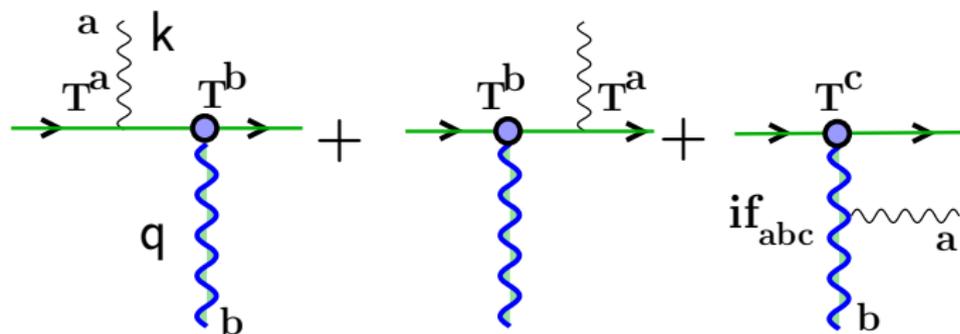
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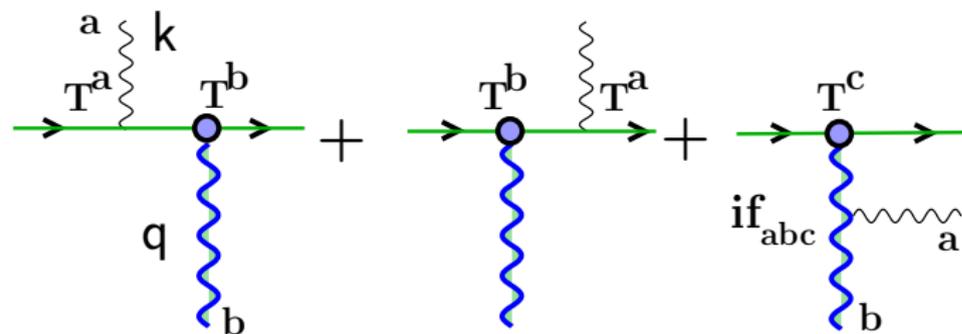
• Accompanying gluon radiation spectrum :

✓ $d\omega/\omega \implies$ rapidity plateau ;

✓ $k_{\perp} < q_{\perp} \implies$ finite transverse momenta.

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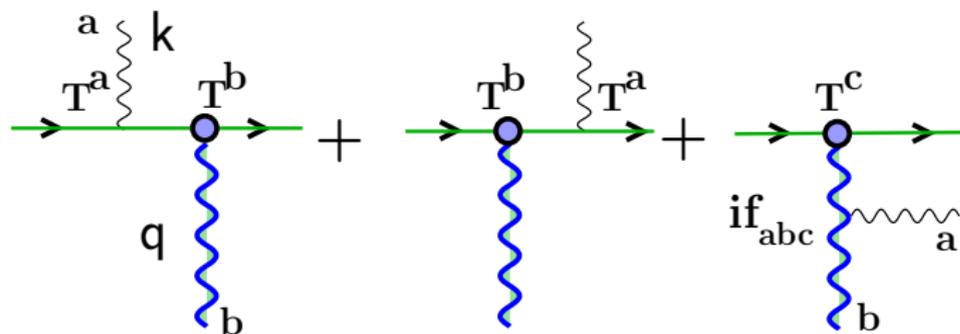


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\Rightarrow scattering cross section of the projectile

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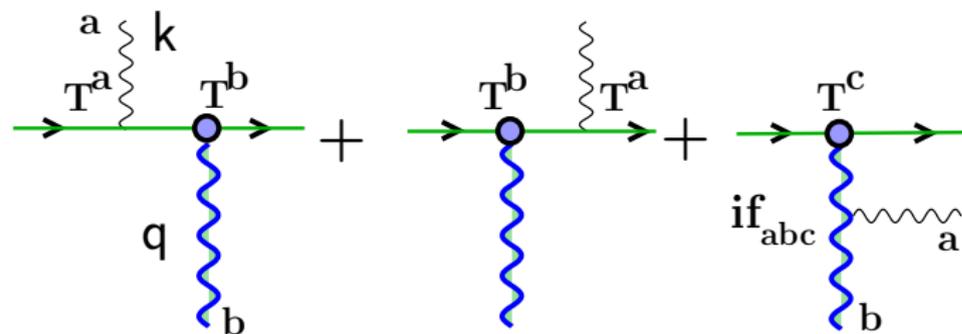


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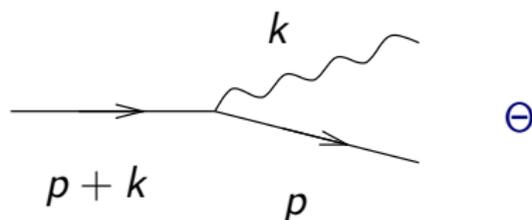
- Multiple scattering of a quark (meson)



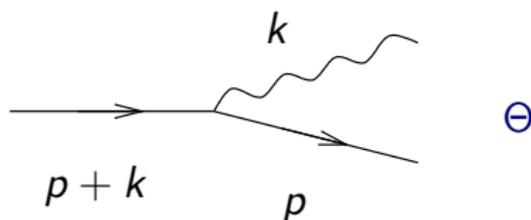
N Participant scaling



How will an additional PT gluon contribute to the hadron yield?

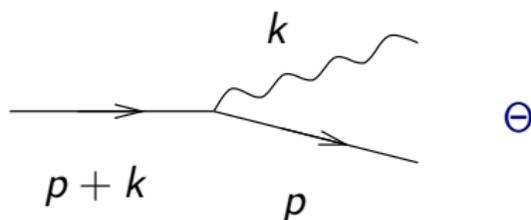


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Look at the time when the secondary gluon (with emission angle $\Theta \simeq k_{\perp}/k$) and its parent will separate in the transverse plane at a critical confinement distance: $t^{\text{separ}} \cdot c\Theta \simeq \Delta\rho_{\perp} \sim R$.

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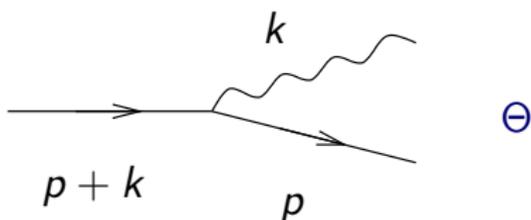


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We expect strong interaction to enter the stage at this moment:

- vacuum break-up,
- production of a hadron (or a few),
- colour blanching of separating objects a'la Kogut–Susskind

How will an additional PT gluon contribute to the hadron yield?



t^{separ} falls right in-between the formation and hadronization times:

$$t^{\text{form}} \approx k/k_{\perp}^2,$$

$$t^{\text{separ}} \approx R/\Theta = t^{\text{form}} * (k_{\perp} R),$$

$$t^{\text{hadr}} \approx kR^2 = t^{\text{form}} * (k_{\perp} R)^2.$$

At this very time a *gluer* is formed with $k_{\text{gluer}} \sim (R\Theta)^{-1}$:

$$\left(t^{\text{form}} \sim t^{\text{separ}} \sim t^{\text{hadr}} \right)_{\text{gluer}} \approx R/\Theta = (t^{\text{separ}})_{qg},$$

which ensures separation of partons as globally blanched sub-jets.

1. The first (the softest) hadron that appears in the system due to the gluon radiation is *quite energetic*: $\omega_h \sim k_{\text{gluer}} \sim (R\Theta)^{-1} \gg R^{-1}$.

This is the effect of the “Lorentz boost” of the *qg* system, *provided* it is the development of the colour field that is responsible indeed for the hadron production!

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The idea of a **mathematical similarity between calculable parton and observable hadron distributions** was formulated in

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Ya.I.Azimov et.al, Z.Phys. **C27** (1985) 65

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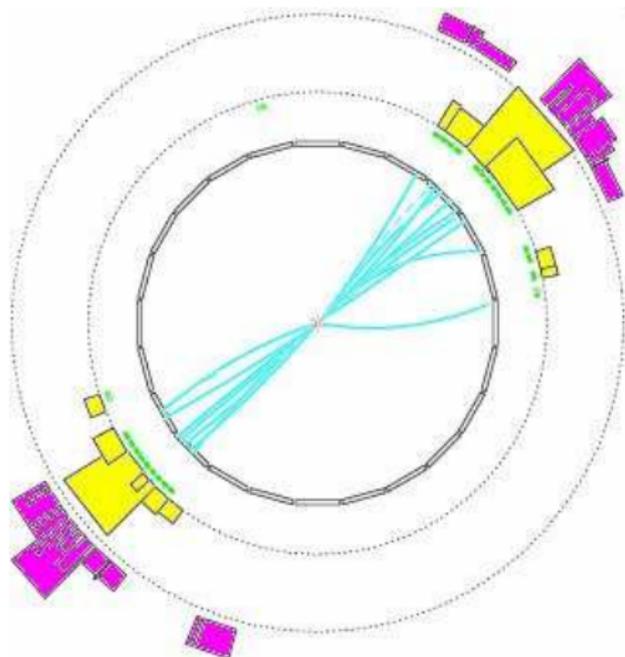
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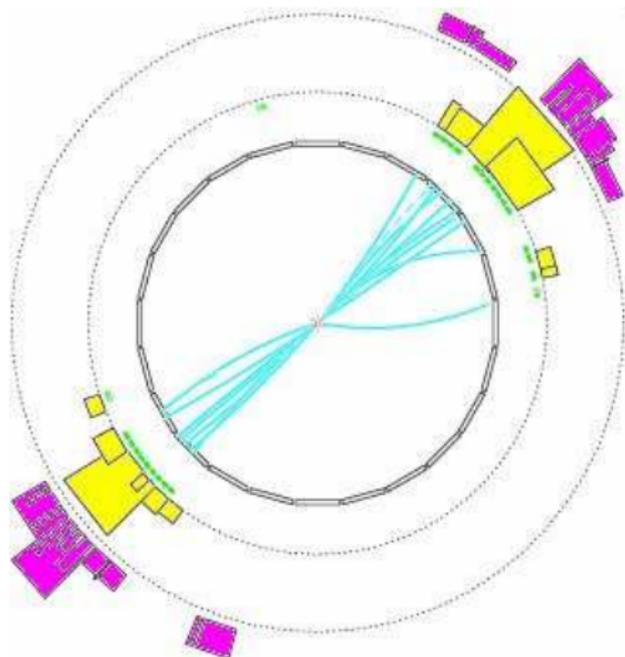
In fact, both Fragmentation Models (that survived) — the **Lund string** (Andersson, Gustafson et.al) and the **HERWIG cluster** (Marchesini, Webber) — do respect the locality:

- **Lund** by construction (universal fragmentation of the colour tube)
- **HERWIG** by virtue of finiteness of $\langle M^2 \rangle$ of neighbouring PT-partons.



Near 'perfect' 2-jet event

2 well-collimated jets of particles.

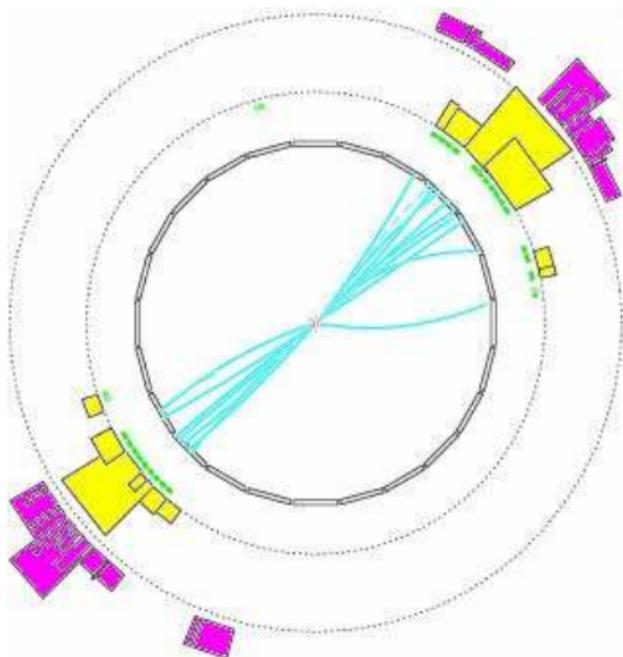


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Jets become "**fatter**" in k_{\perp}
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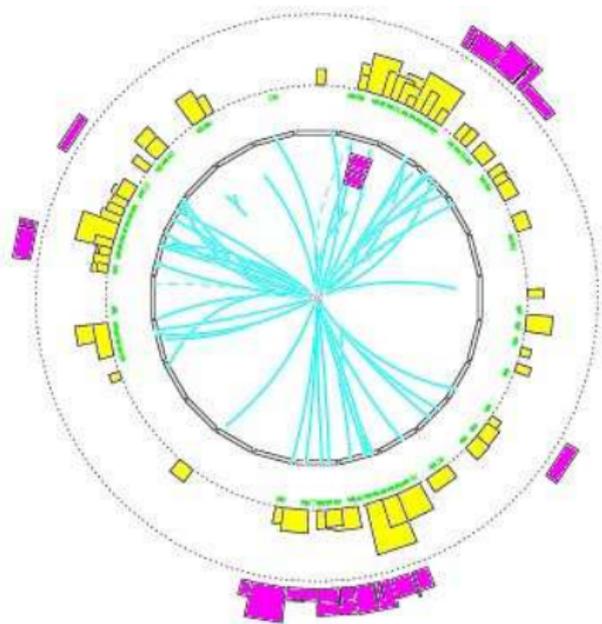
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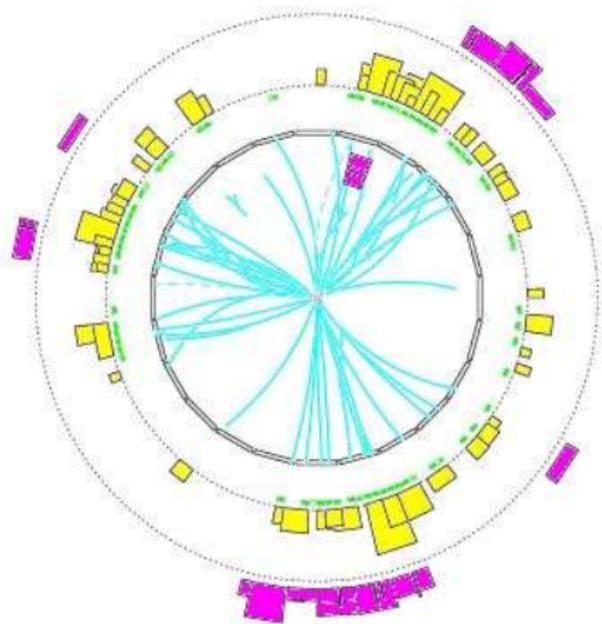
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Moreover,

In 10% of e^+e^- annihilation
events
— striking fluctuations !



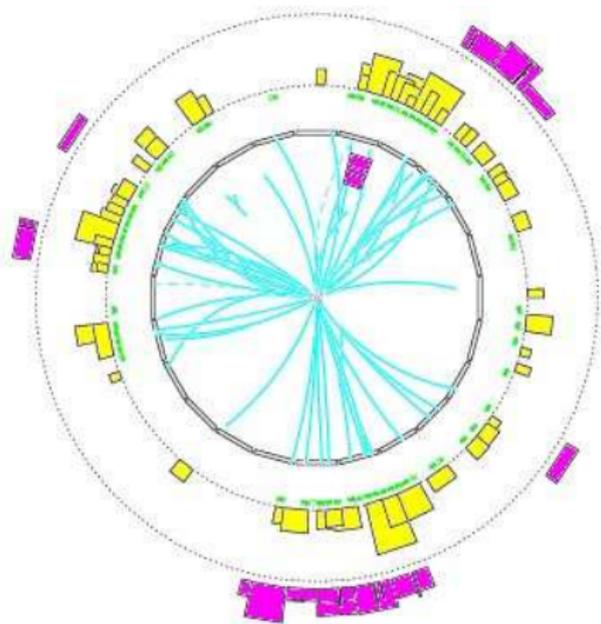
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No surprise : (Kogut & Susskind, 1974)

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The first QCD analysis was done by J.Ellis, M.Gaillard & G.Ross (1976)

- Planar events with large k_{\perp} ;
- How to measure gluon spin ;
- Gluon jet – softer, more populated.

QCD possesses $N_c^2 - 1$ gauge fields — vector gluons g .

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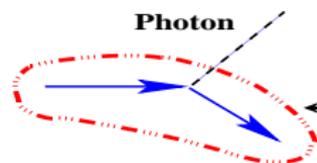
B.Andersson, G.Gustafson & C.Peterson, Lund Univ., Sweden (1977)

Gluon \simeq quark-antiquark pair:

$$3 \otimes \bar{3} = N_c^2 = 9 \simeq 8 = N_c^2 - 1.$$

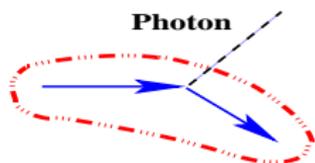
Relative mismatch : $\mathcal{O}(1/N_c^2) \ll 1$ (the large- N_c limit)

Look at hadrons produced in a $q\bar{q} + \text{photon}$
 e^+e^- annihilation event.



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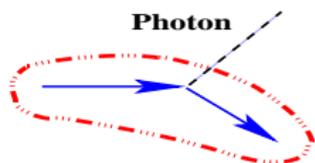
The hot-dog of hadrons that was “*cylindric*” in
the cms, is now *lopsided* [boosted string]



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Now substitute a **gluon** for the photon in the same kinematics.

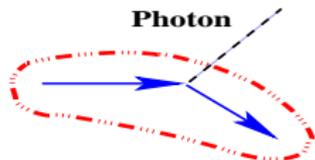




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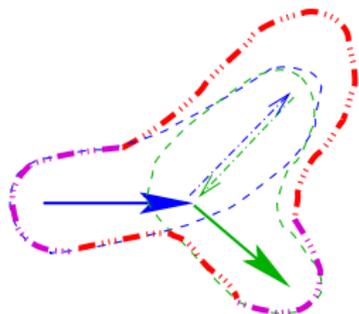
The gluon carries "double" colour charge;
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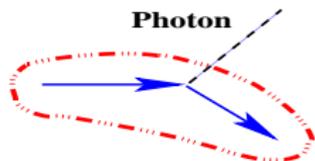
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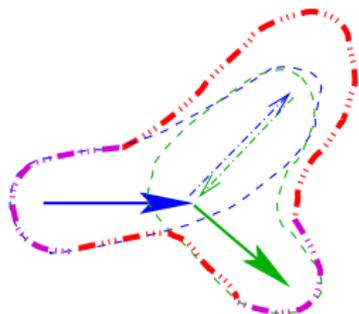


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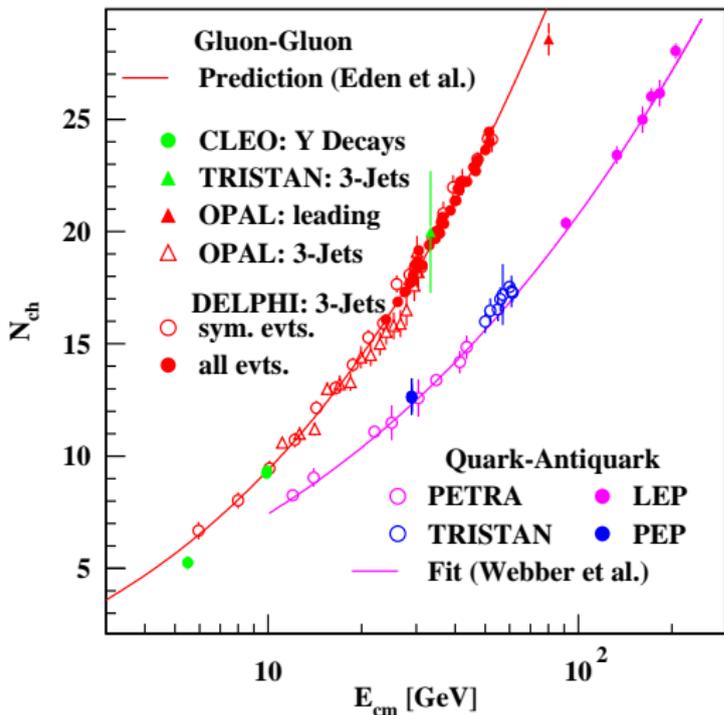
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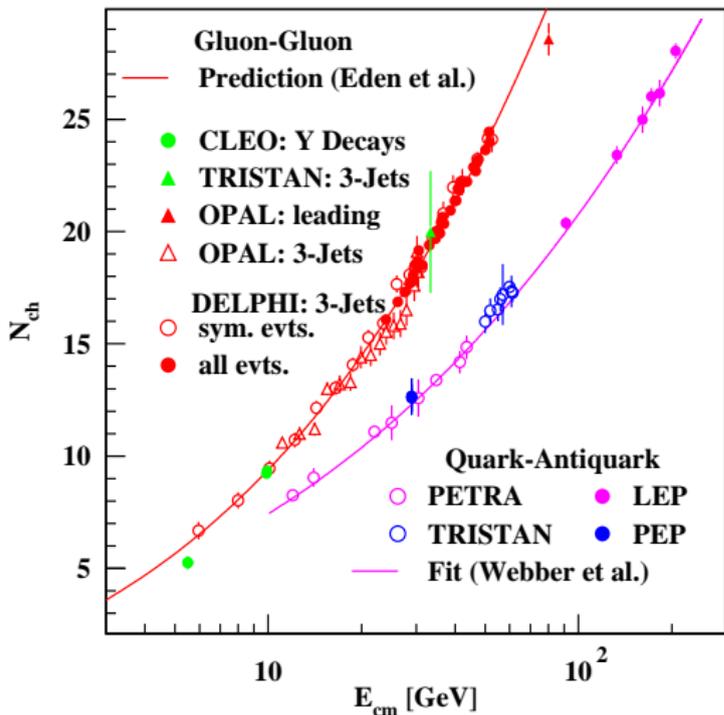


The first immediate consequence :

Double Multiplicity of hadrons in fragmentation of the *gluon*

Look at experimental findings

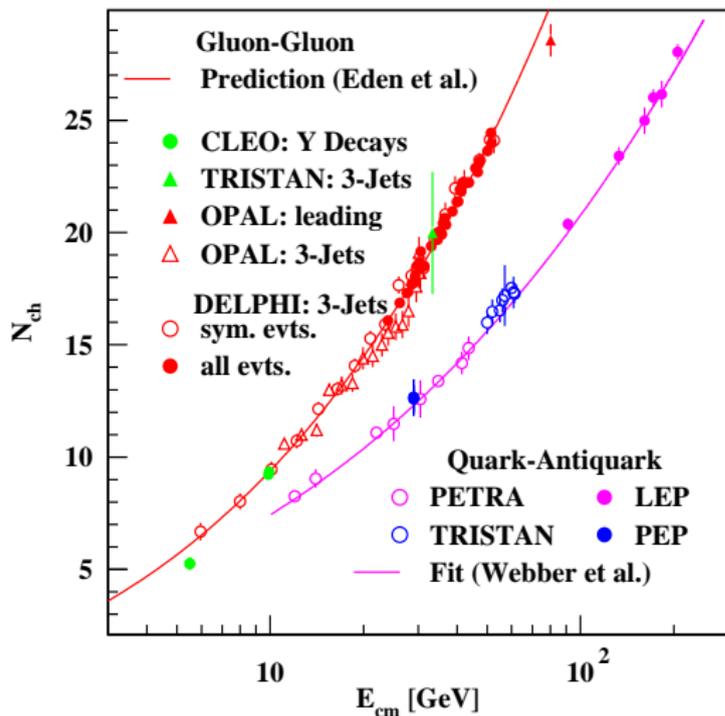




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- N increases *faster* than $\ln E$
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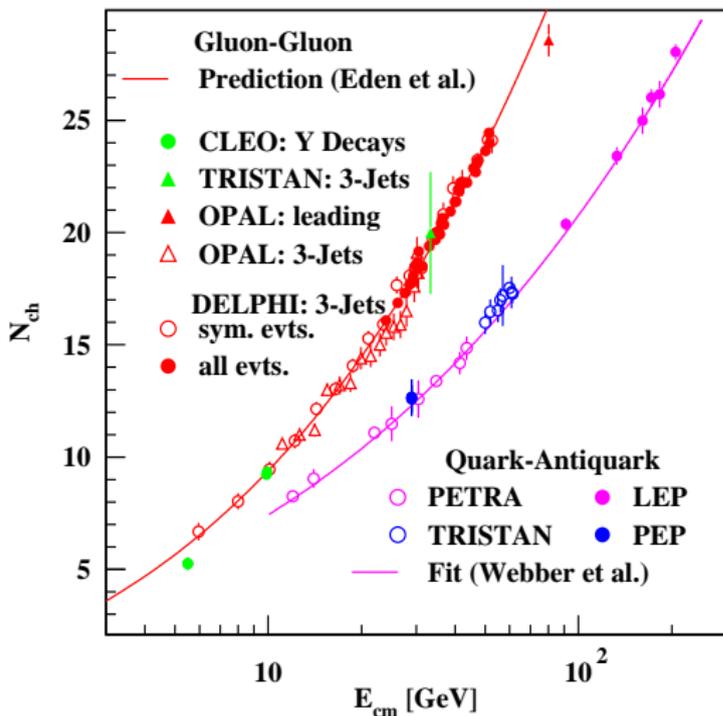


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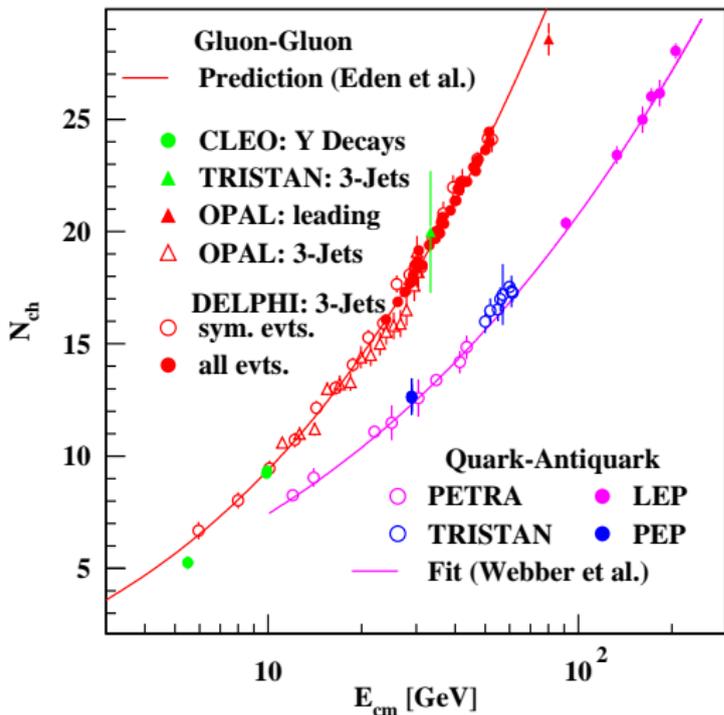


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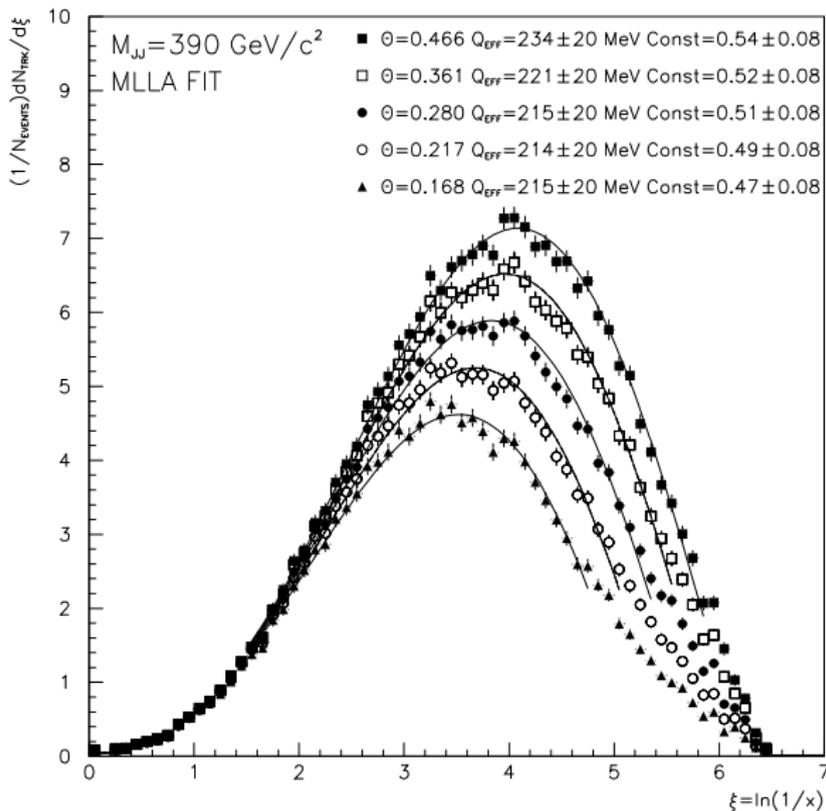
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Which are the particles that multiply most efficiently inside the jet?

CDF PRELIMINARY



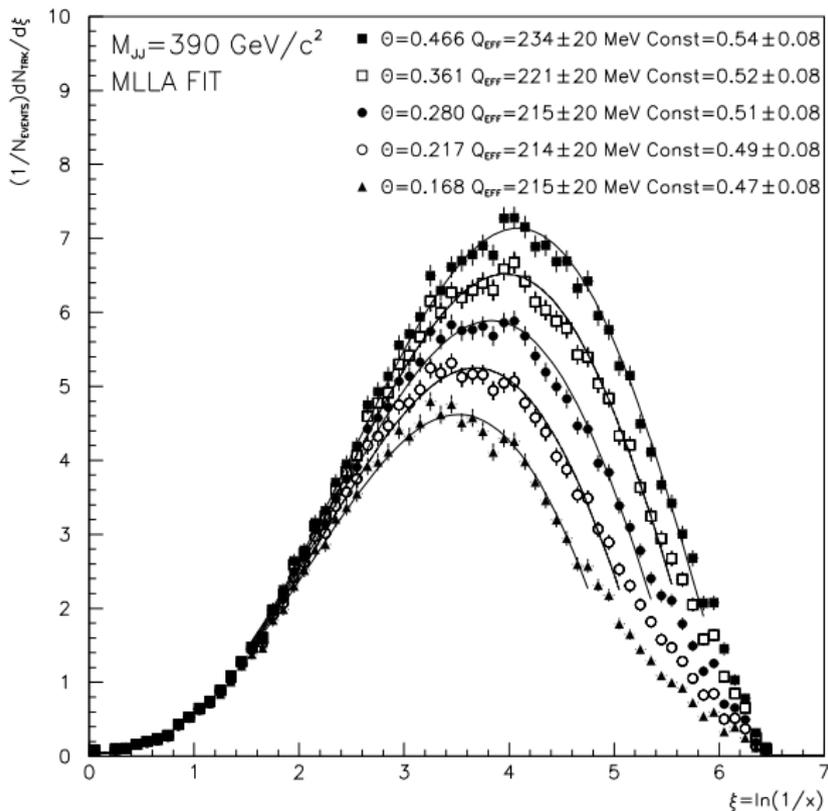
First confronted with theory in $e^+e^- \rightarrow h+X$.

CDF (Tevatron)

$pp \rightarrow 2 \text{ jets}$

Charged hadron yield as a function of $\ln(1/x)$ for different values of jet hardness, versus (MLLA) QCD prediction.

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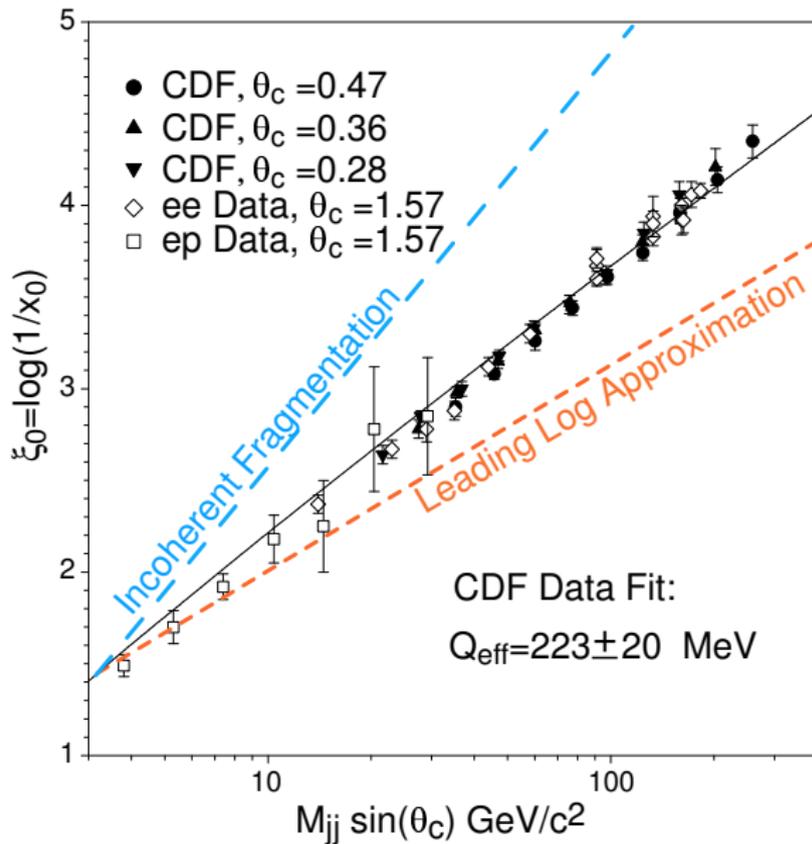
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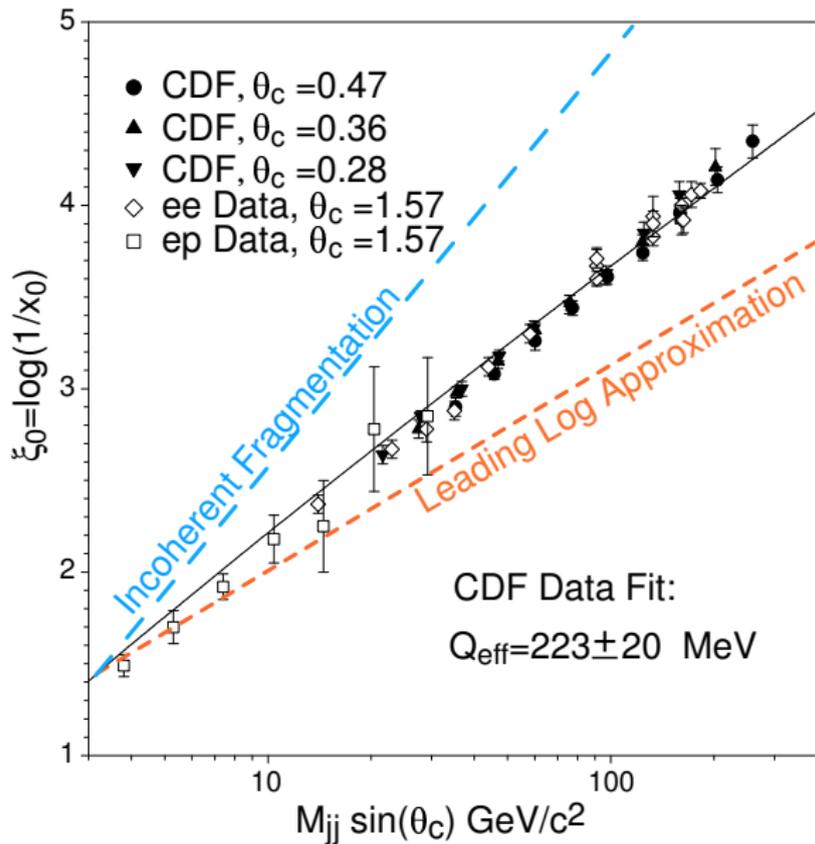
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One free parameter – overall normalization (the number of final π 's per extra gluon)



Position of the Hump as
 a function of
 $Q = M_{jj} \sin \Theta_c$
 (hardness of the jet)

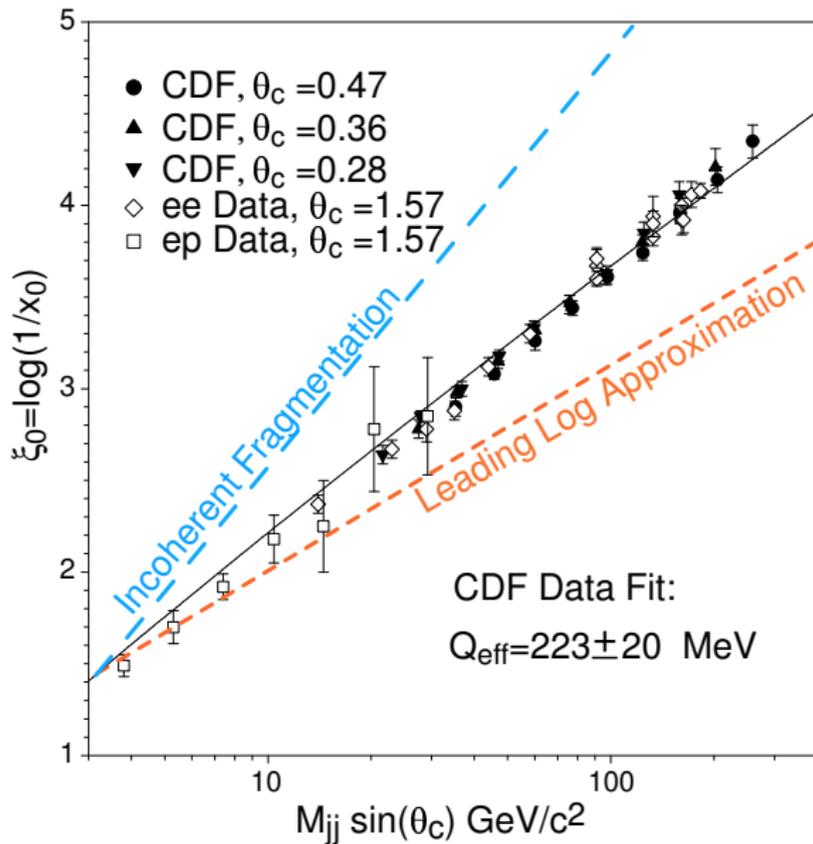


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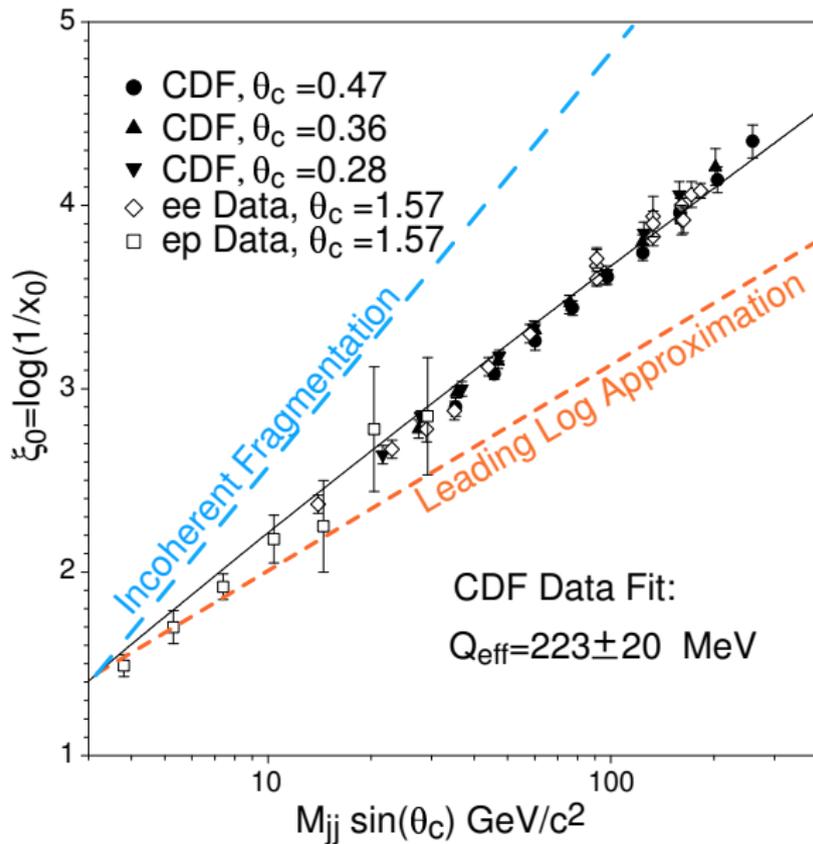
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Mark **Universality**:
 same behaviour seen in e^+e^- , DIS (ep), hadron–hadron coll.

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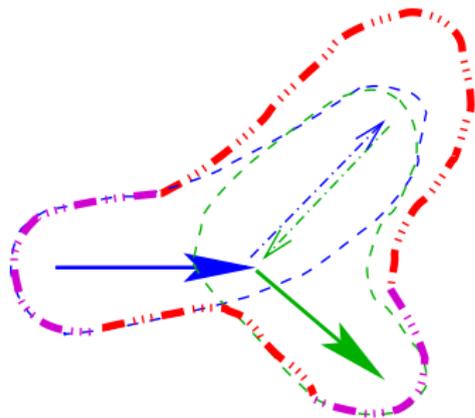
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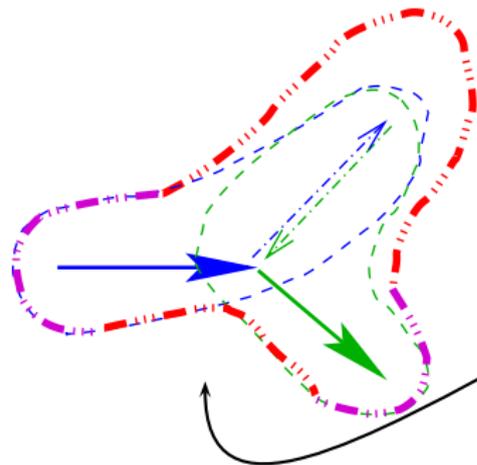
Convergence:

“*The string effect and QCD coherence*”, Phys.Lett. **165B** (1985) 147



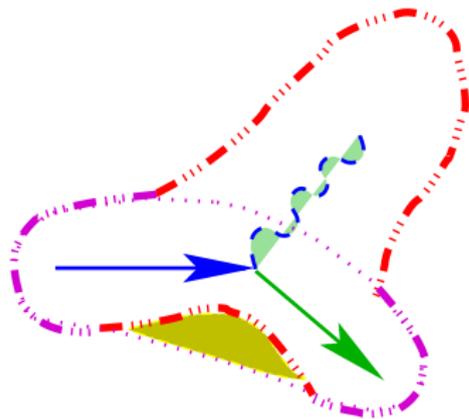
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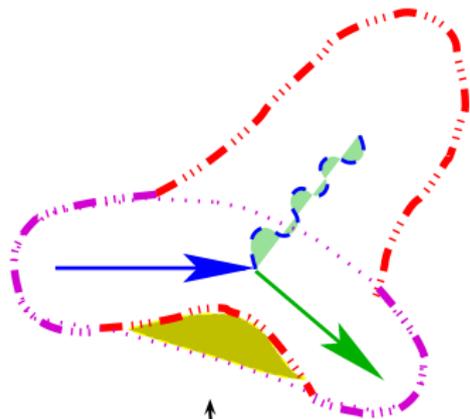


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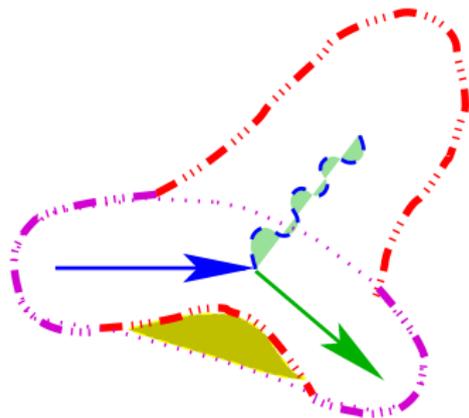


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Destructive interference from the QCD point of view



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QCD prediction :

$$\frac{dN_{q\bar{q}\gamma}}{dN_{q\bar{q}g}} \simeq \frac{2(N_c^2 - 1)}{N_c^2 - 2} = \frac{16}{7}$$

(experiment: 2.3 ± 0.2)

Destructive interference
 from the QCD point of view

Ratios of hadron flows between jets in various multi-jet processes — example of non-trivial CIS (collinear-and-infrared-safe) QCD observable

Recall the equation:

Inclusive spectrum of gluers = Feynman hadron plateau

$$dN = \left[\int_{k_{\perp} \sim R^{-1}} \frac{dk_{\perp}^2}{k_{\perp}^2} 4C_F \frac{\alpha_s(k_{\perp}^2)}{4\pi} \right] \frac{dk}{k} = \text{const} \cdot \frac{dk}{k}.$$

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A first timid step in this direction was made in the 1990's.

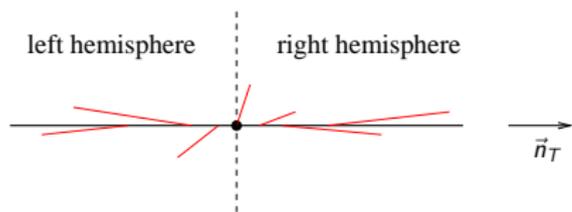
There is a specific (though not too narrow a) class of QCD observables that taught us couple of things about **genuine non-perturbative effects** in multiple production of hadrons in hard processes. Among them — the so called ***event shapes*** which measure global properties of final states (jet profiles) in an inclusive manner.

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thrust $T = \max_{\vec{n}} \frac{\sum_i |\vec{p}_i \cdot \vec{n}|}{\sum_i |\vec{p}_i|},$

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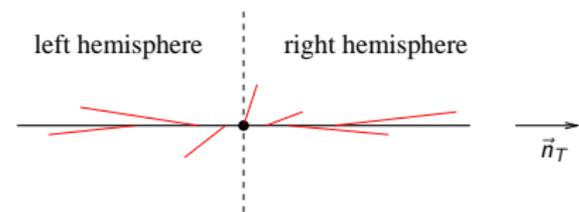
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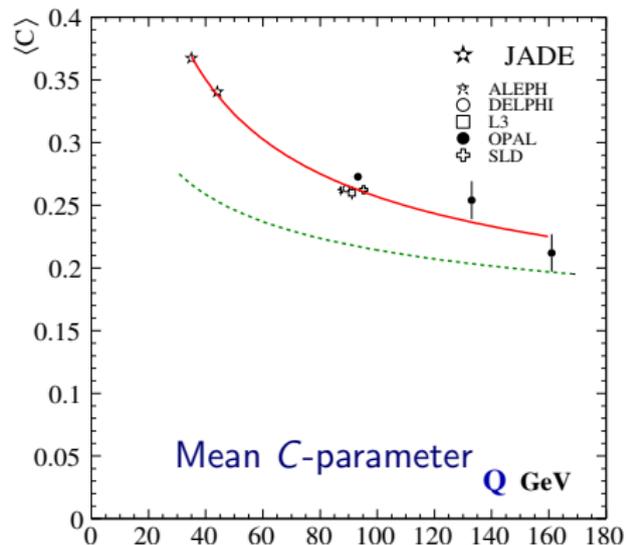
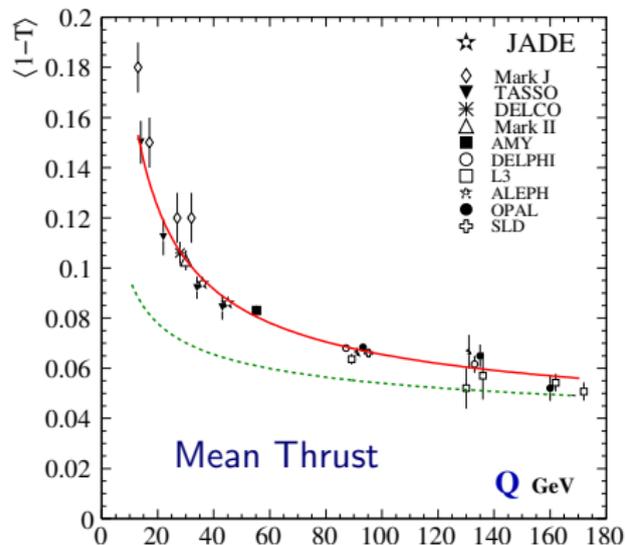
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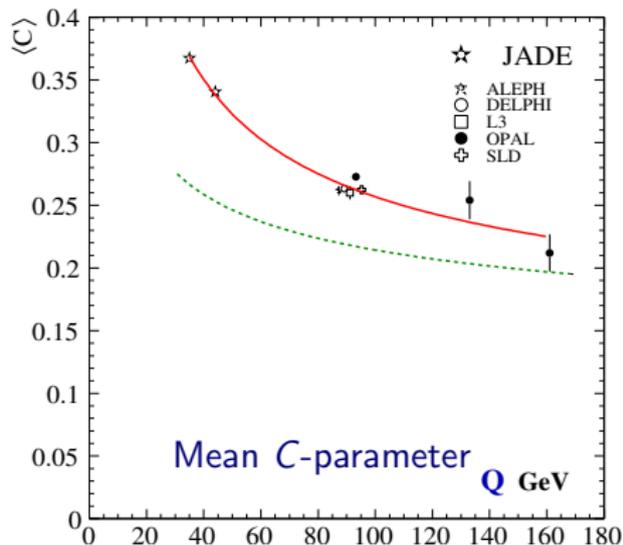
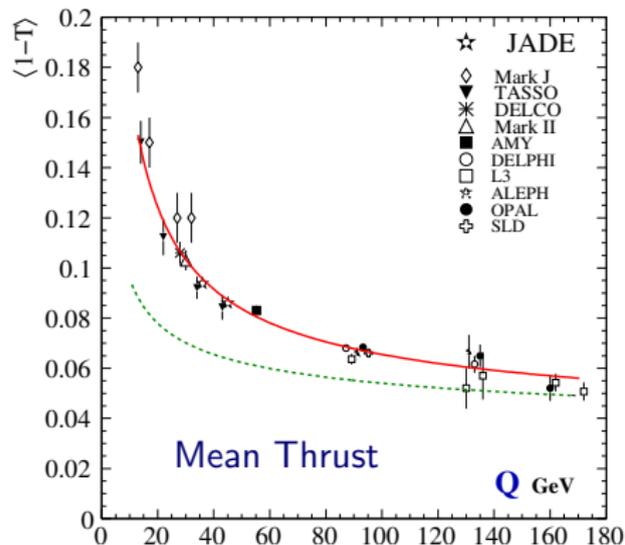
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They are formally calculable in pQCD (being collinear and infrared safe) but possess large non-perturbative $1/Q$ -suppressed corrections.

1/Q Confinement effects in mean shapes



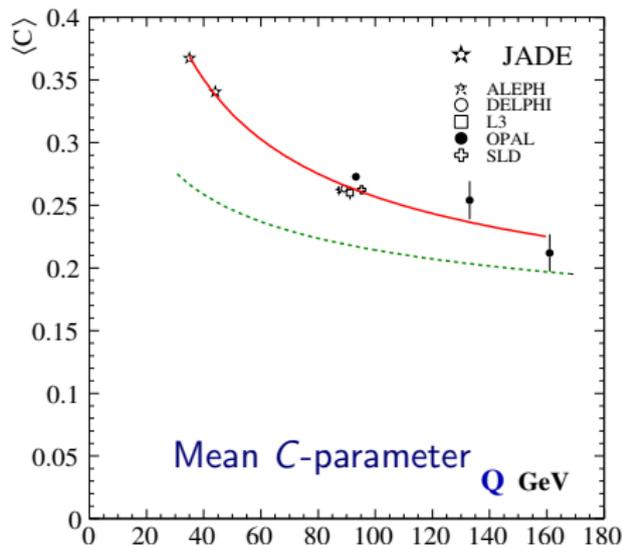
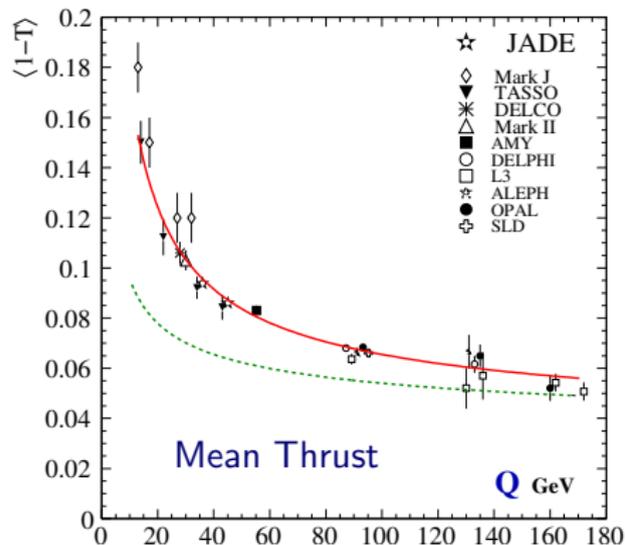
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“p” QCD
theory

12 years
old

and still
running

$$\left\{ \begin{array}{l} 4 \\ 1 \end{array} \right\} \Rightarrow \frac{3\pi}{2}$$

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Let's have a brief NP look at these

This “**industry-standard**” way of fitting event-shape power corrections exploits the idea that the power correction is driven by the NP modification of the **QCD coupling in the InfraRed**:

$$\delta\mathcal{V}_p = \frac{2C_F}{\pi} \int_0^{\mu_I} \frac{dm}{m} \cdot \left(\frac{m}{Q}\right)^p \cdot \left(\alpha_s(m^2) - \alpha_s^{\text{PT}}(m^2)\right) \cdot c_p$$

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This Universality Hypothesis is the key ingredient of the game: the new NP parameter α_0 must inherit the *universal nature* of the QCD coupling itself.

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- new (PT-obtainable) coefficients $c_{\mathcal{V}}$

This is as far as event shape *mean values* $\langle \mathcal{V} \rangle$ go, plus similar – and consistent – results from (theoretical and experimental) DIS jet studies.

The same technology is applicable to event shape *distributions*, $dN/d\mathcal{V}$. Here the genuine NP physics manifests itself, basically, in *shifting* the PT spectra, in \mathcal{V} variable, by an amount proportional to $1/Q$ (D & Webber 1997)

Distributions turned out to be an important addition to the menu.

- ➡ Firstly, functions are more informative and revealing than numbers.
- ➡ Secondly, it was the studies of *event shape distributions* that allowed theorists to better understand what the hell they've been doing, thanks to pedagogical lessons theorists were taught by *those impatient* colleagues experimenters (P. Movilla Fernandez, JADE 1998)

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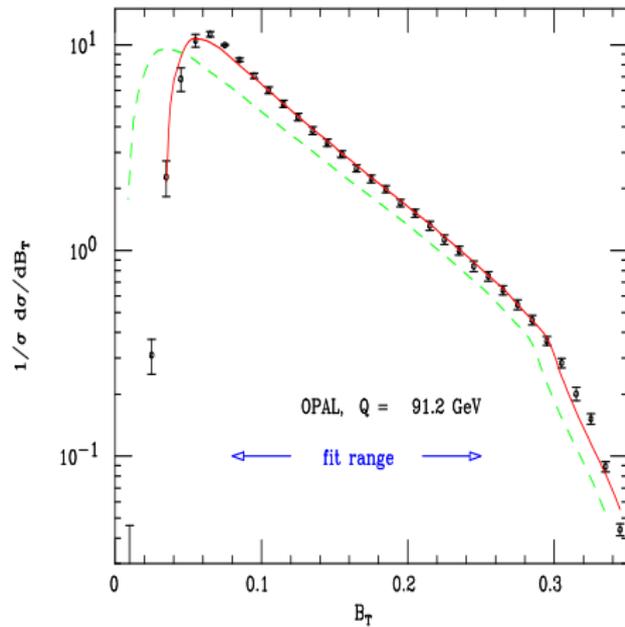
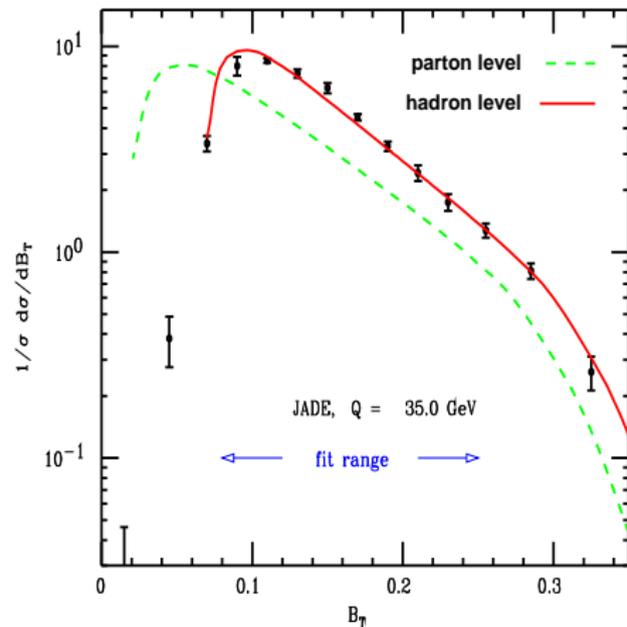
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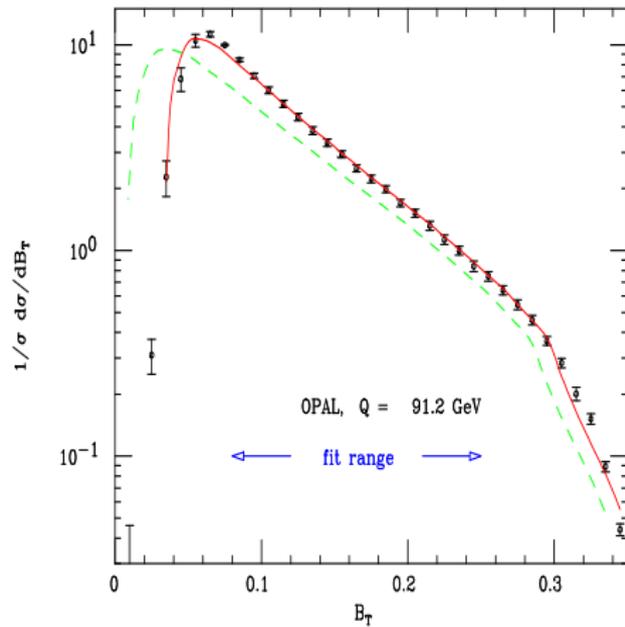
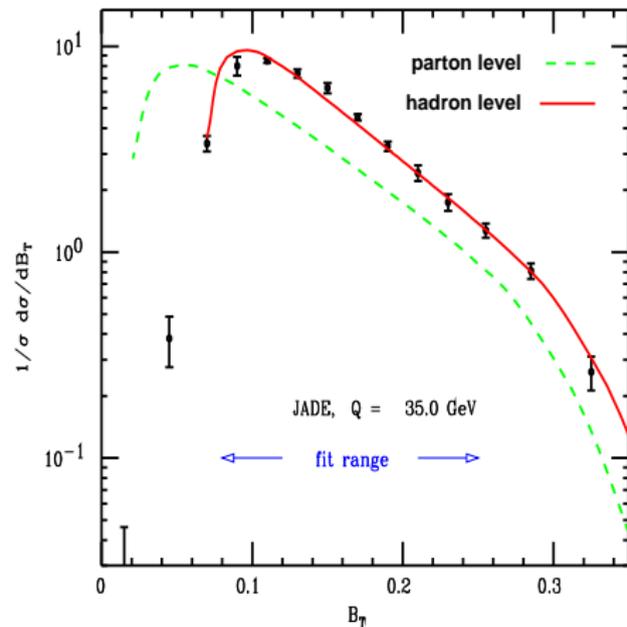
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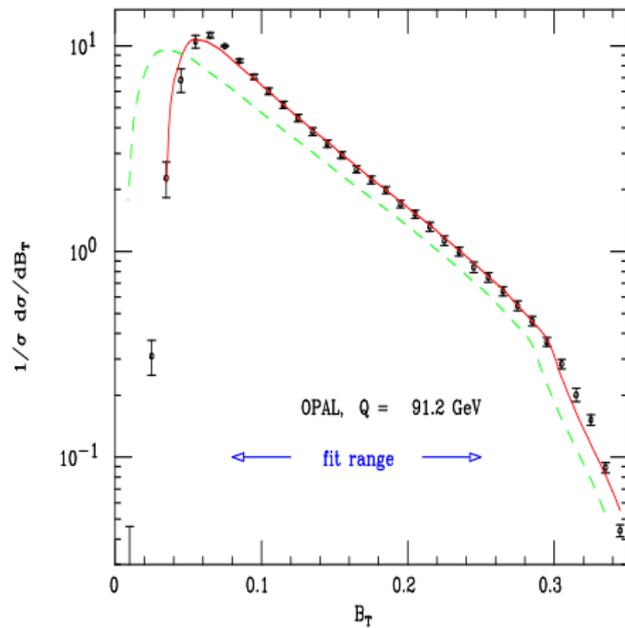
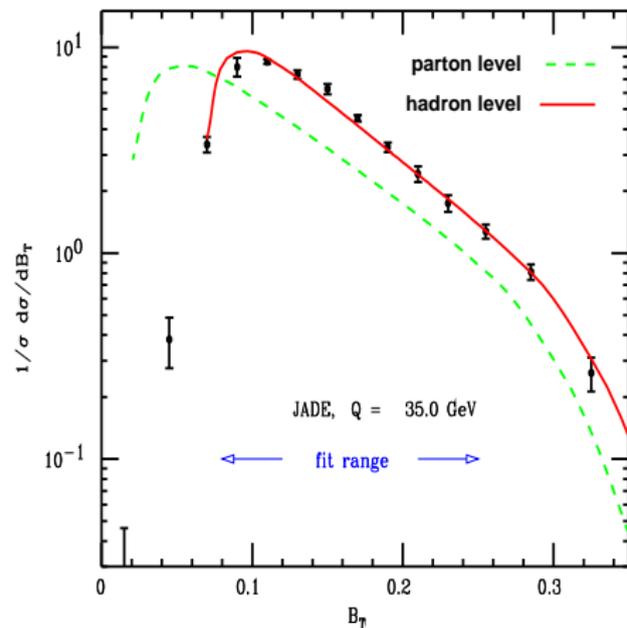
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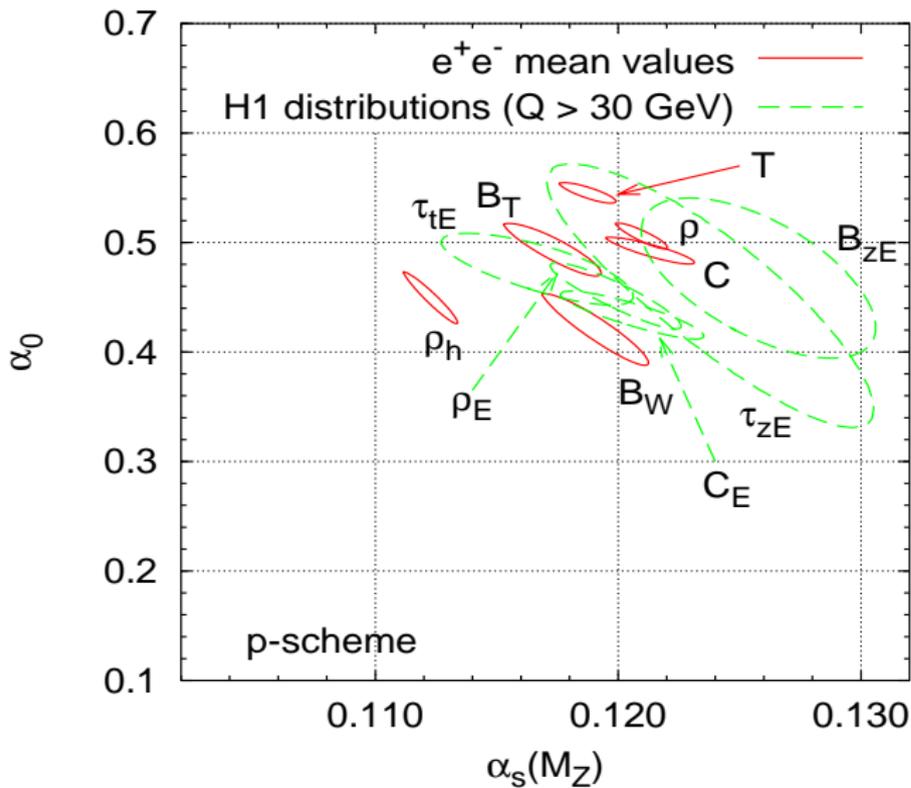


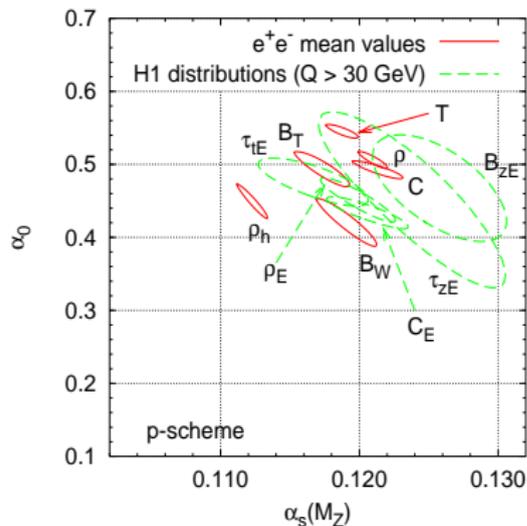
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E.g., **squeezing** at the hadron-level (!!), uncovered by the *JADE gang*



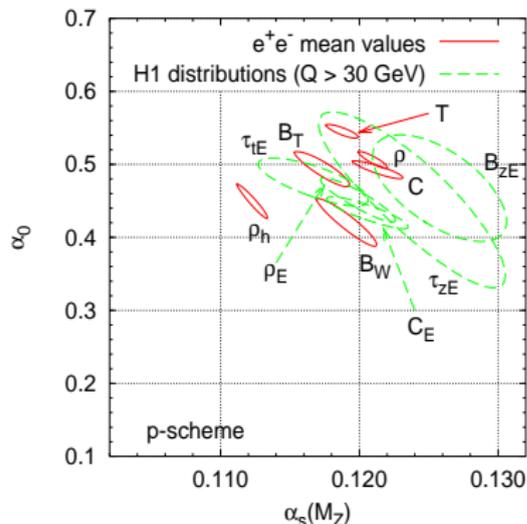


Theory + Phenomenology of $1/Q$ effects in event shape observables, both in e^+e^- annihilation and Deep Inelastic Scattering systematically points at the *average* value of the infrared coupling

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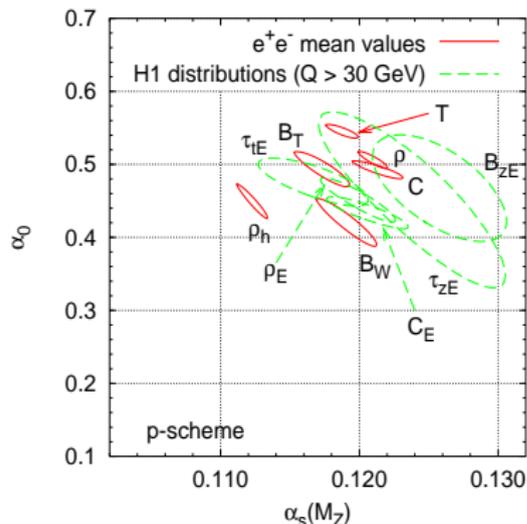


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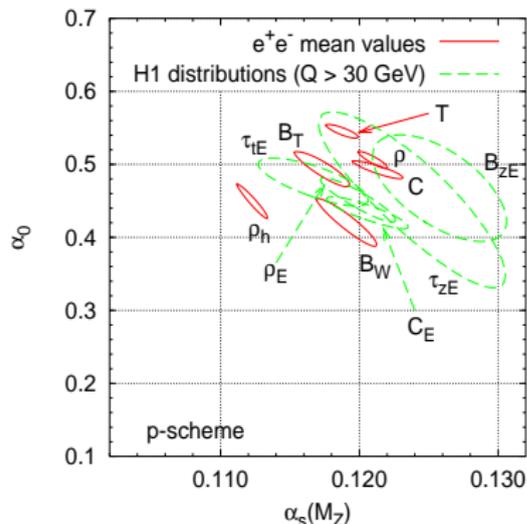


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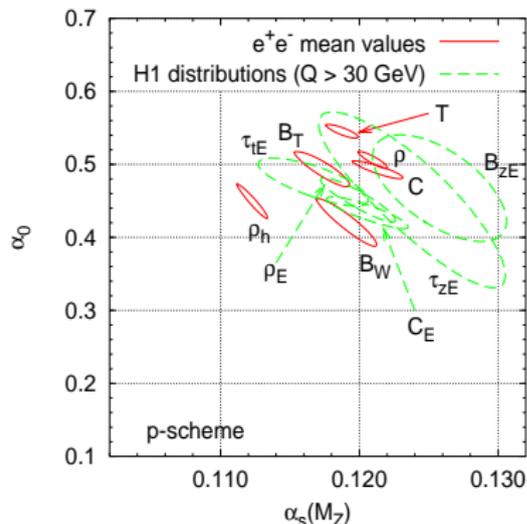
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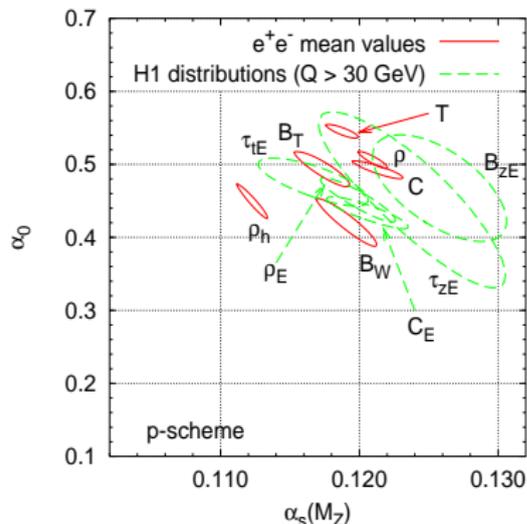


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Interestingly enough, the core of the potential solution of the problem of quantitative understanding of the physics of hadronization lies in a deeper penetration in the origin of the Asymptotic Freedom in non-Abelian QFT.

- It seems natural to expect the effective interaction strength to *decrease* at large distances.
- Moreover, it was long thought to be *inevitable* as corresponding to the physics of 'screening'.
- The fact that the vacuum fluctuations have to screen the external charge in QFT follows from the first principles: unitarity and crossing symmetry (see Lecture 16 and 17 – QFT)

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So, *why* does this most general argument *fail in non-Abelian QFT* ?

Autopsy of Asymptotic Freedom

To address questions starting from *what* or *why* we better talk **physical degrees of freedom**; use the *Hamiltonian language*. Then, we have gluons of two sorts: 'physical' transverse gluons and the Coulomb gluon field — mediator of the instantaneous interaction between colour charges.

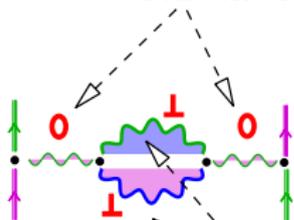
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Instantaneous Coulomb interaction



$$= -N_c * \frac{1}{3} - n_f * \frac{2}{3}$$

Transverse gluons (and quarks)



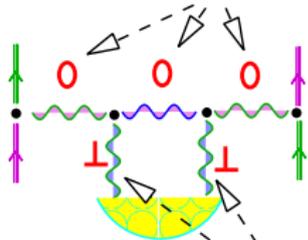
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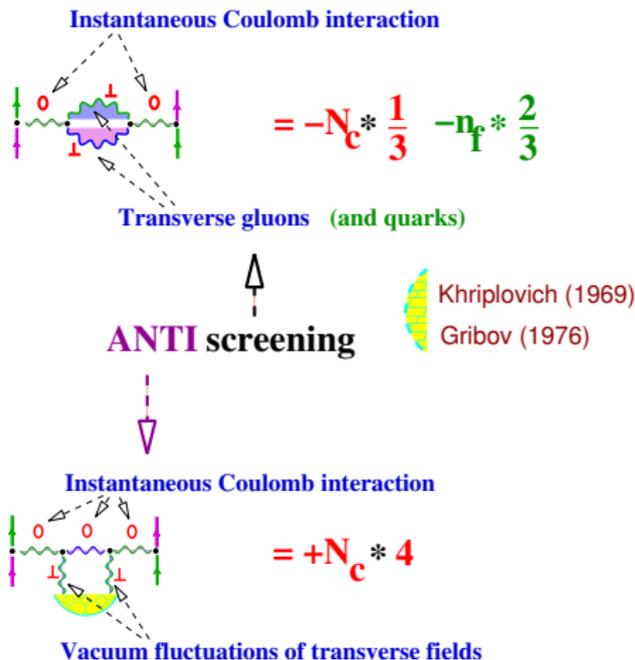
Instantaneous Coulomb interaction



$$= +N_c * 4$$

Vacuum fluctuations of transverse fields

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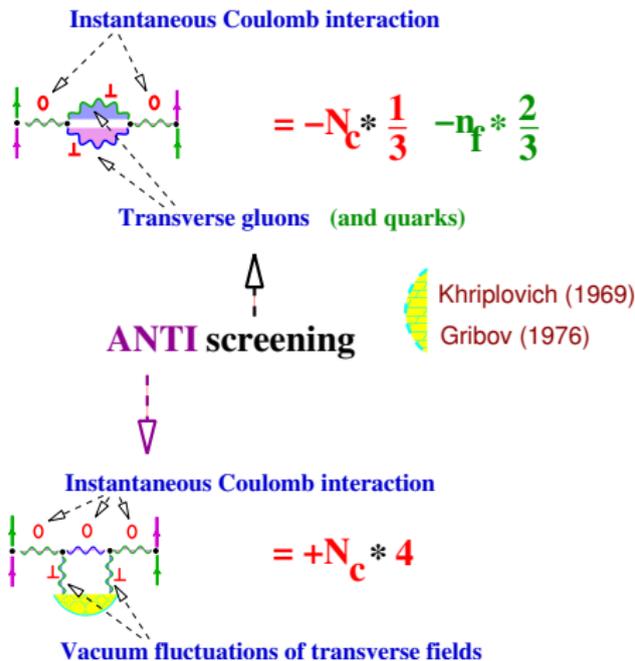


Combine into the QCD β -function:

$$\beta(\alpha_s) = \frac{d}{d \ln Q^2} 4\pi\alpha_s^{-1}(Q^2)$$

$$= \left[4 - \frac{1}{3} \right] * N_c - \frac{2}{3} * n_f$$

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The origin of *antiscreening* —
 deepening of the ground state under
 the 2nd order perturbation in NQM:

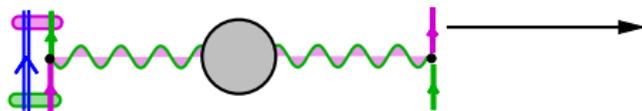
$$\Delta E_0 = \sum_n \frac{|\langle 0 | \delta V | n \rangle|^2}{E_0 - E_n} < 0.$$

Coulomb instability and Hadronization

What happens with the **Coulomb field** when the sources move apart?

Coulomb instability and Hadronization

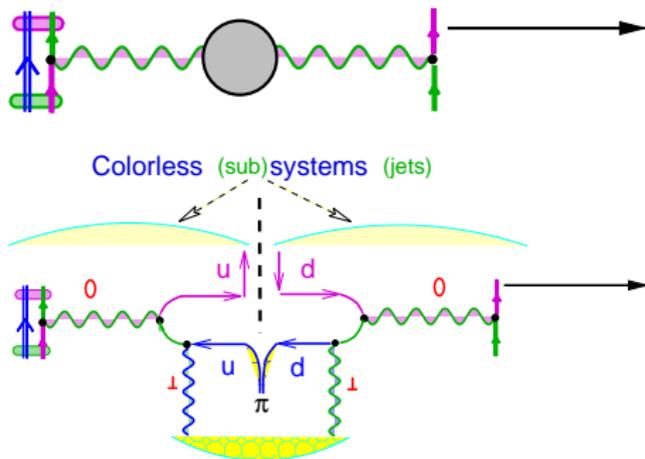
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Bearing in mind that **virtual quarks live in the background** of gluons (zero fluctuations of A_{\perp} gluon fields)

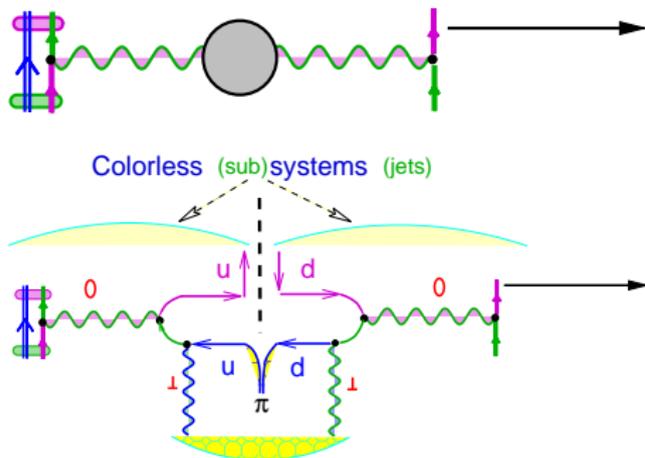
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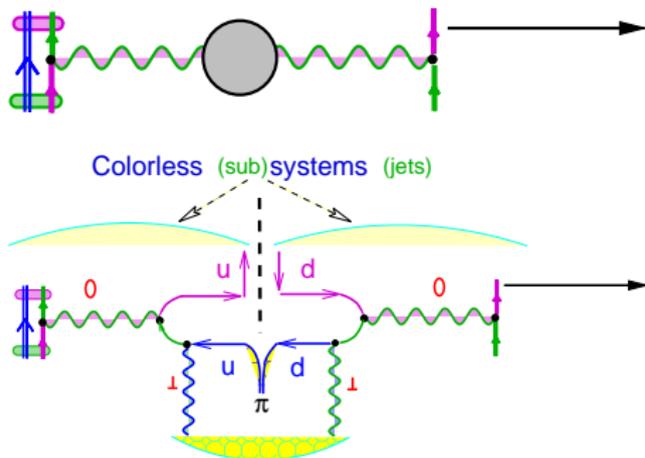
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$$\frac{\alpha}{\pi} > \frac{\alpha_{\text{crit}}}{\pi} = C_F^{-1} \left[1 - \sqrt{\frac{2}{3}} \right] \simeq 0.137$$

$$\left(C_F = \frac{N_c^2 - 1}{2N_c} = \frac{4}{3} \right)$$

Covariant derivative

$$\mathbf{D}[\mathbf{A}_\perp] \cdot = \nabla \cdot + ig_s [\mathbf{A}_\perp \cdot]$$

The Coulomb field “propagator”

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The Coulomb field “propagator” (*Abelian*)

$$G(\mathbf{x} - \mathbf{y}) = - \frac{1}{\nabla^2}$$

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average over transverse vacuum fields \mathbf{A}_\perp

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= the ghost rising from dead

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listen to Matteo Cacciari, attentively

EXTRAS

An amazing success of the relativistic theory of electron and photon fields — quantum electrodynamics (QED) — has produced a long-lasting **negative impact**: it taught the generations of physicists that came into the business in/after the 70's to “*not to worry*”.

Indeed, today one takes a lot of things for granted:

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- One takes the original concept of the “Dirac sea ” — the picture of the fermionic content of the vacuum — as an anachronistic model

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One was taught to look upon the problems that arise with field-theoretical description of point-like objects and their interactions at very small distances (ultraviolet divergences) as purely technical: *renormalize it and forget it.*

Gribov Confinement: setting up the Problem

- The question of interest is **The** confinement in the real world (with 2 very light u and d quarks), rather than **a** confinement.
- No mechanism for binding massless *bosons* (gluons) seems to exist in Quantum Field Theory (QFT), while the Pauli exclusion principle may provide means for binding together massless *fermions* (light quarks).
- The problem of ultraviolet regularization may be more than a technical trick in a QFT with apparently infrared-unstable dynamics: the **ultraviolet** and **infrared** regimes of the theory may be closely linked.
- The Feynman diagram technique has to be reconsidered in QCD if one goes beyond trivial perturbative correction effects.
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To understand and describe a physical process in a *confining theory*, it is necessary to take into consideration the response of the vacuum, which leads to essential modifications of the quark and gluon Green functions.

QED: physical objects — *electrons and photons* — are in one-to-one correspondence with the fundamental fields that one puts into the local Lagrangian of the theory.

QCD: the Vacuum changes the bare fields *beyond recognition*.

A known QFT example of such a violent response of the vacuum — screening of super-charged ions with $Z > 137$.

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Supercritical binding by over-charged nuclei

The expression for Dirac energy levels of an electron in an external static field created by the point-like electric charge Z contains

$$\epsilon \propto \sqrt{1 - (\alpha_{\text{e.m.}} Z)^2}.$$

For $Z > 137$ the energy becomes *complex*. This means *instability*.

- Classically, the electron “falls onto the centre”.
- Quantum-mechanically, it also “falls”, but into the Dirac sea.
- In QED, the instability develops when the energy ϵ of an upper Dirac level crosses the Dirac sea, which means $\epsilon < -m_e c^2$.
- As a result, electrons are pulled from the vacuum into the vacuum electron sea.
- This happens at the level of supercritically charged ions (see also the next slide).

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- In QFT the instability develops when the energy ϵ of an empty atomic electron level drops, with increase of Z , below $-m_e c^2$.

An e^+e^- pair pops up from the vacuum, with the vacuum electron occupying the level: the super-critically charged ion decays into an “atom” (the ion with the smaller positive charge, $Z - 1$) and a real positron:

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$$A_Z \implies A_{Z-1} + e^+, \quad \text{for } Z > Z_{\text{crit.}}$$

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Thus, the ion becomes *unstable* and gets rid of an excessive electric charge by emitting a positron (Pomeranchuk & Smorodinsky 1945)

In the **QCD** context, the increase of the running quark-gluon coupling at large distances replaces the large Z of the QED problem.

Gribov generalised the problem of supercritical binding in the field of an infinitely heavy source to the case of two massless fermions interacting via *Coulomb-like exchange*. He found that in this case the supercritical phenomenon develops much earlier.

Namely, a *pair of light fermions* develops supercritical behaviour if the coupling hits a definite critical value

$$\frac{\alpha}{\pi} > \frac{\alpha_{\text{crit}}}{\pi} = 1 - \sqrt{\frac{2}{3}}.$$

With account of the QCD colour Casimir operator, the value of the coupling above which restructuring of the perturbative vacuum leads to *chiral symmetry breaking* and, likely, to *confinement*, translates into

$$\frac{\alpha_{\text{crit}}}{\pi} = C_F^{-1} \left[1 - \sqrt{\frac{2}{3}} \right] \simeq 0.137$$

$$\left(C_F = \frac{N_c^2 - 1}{2N_c} \right) = \frac{4}{3}$$

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