



Expected Uncertainties on the Jet Cross Section Measurement in ATLAS

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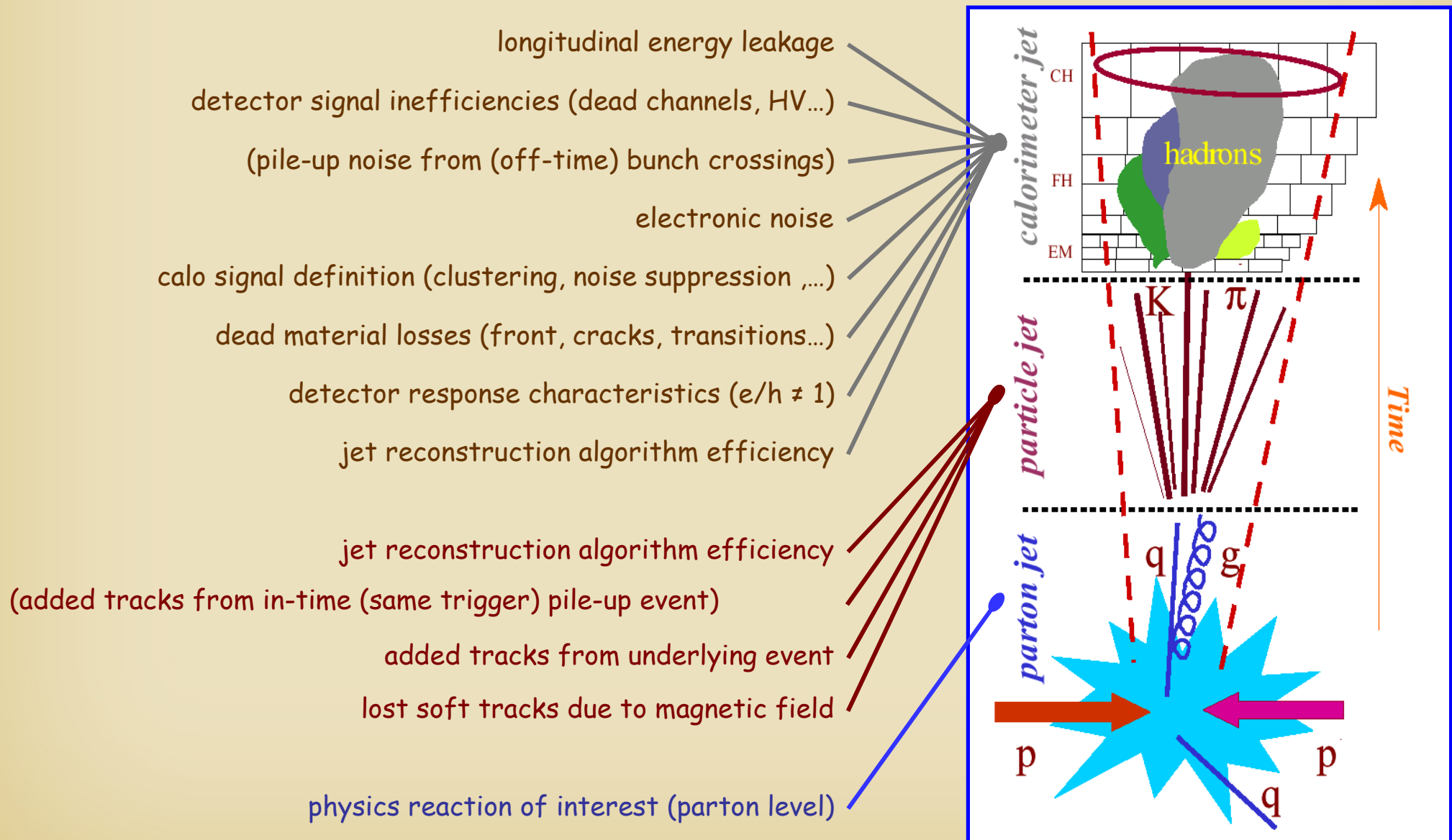
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Jet Measurements – Truth Definition

- Typically the aim is to **test parton level predictions** (measure the partons originating the jets)
- The parton level result is “masked” at **different levels**:
 - theoretical level (everything which leads to the final state particles: ISR/FSR, hadronization, multiple parton-parton interactions, multiple proton-proton interactions)
 - experimental level (detector inefficiencies, non-linearities, resolution)
- The measurement goes through **two different steps**:
 - **Remove the effect of the detector**, i.e., measure at best the final state particles: this is a common step of all the possible analysis done with jets
 - Correct the final state objects to get back the parton level
 - The **truth jets** (particle jets) are those obtained running the **same reconstruction algorithm** used in the detector on the **final state MC particles**.

What enters where

- While discussing about Jet Energy Scale we should keep in mind this picture

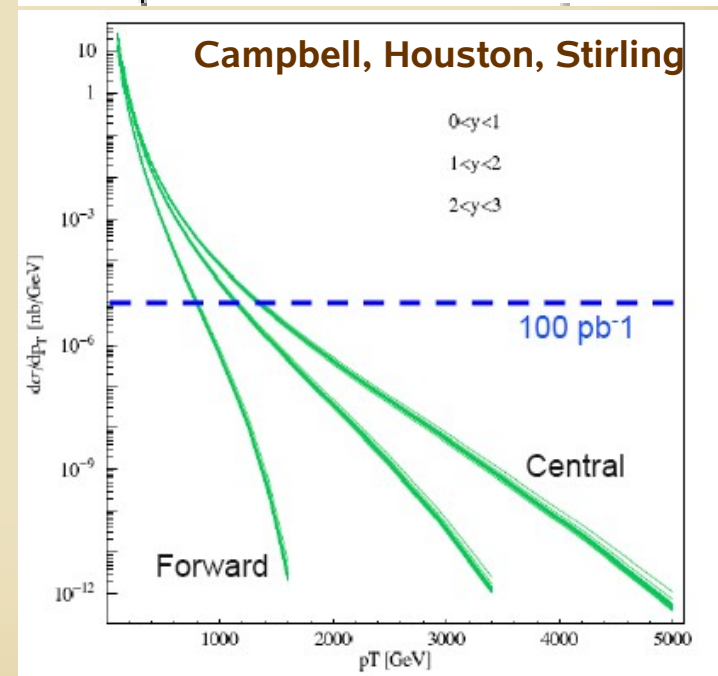
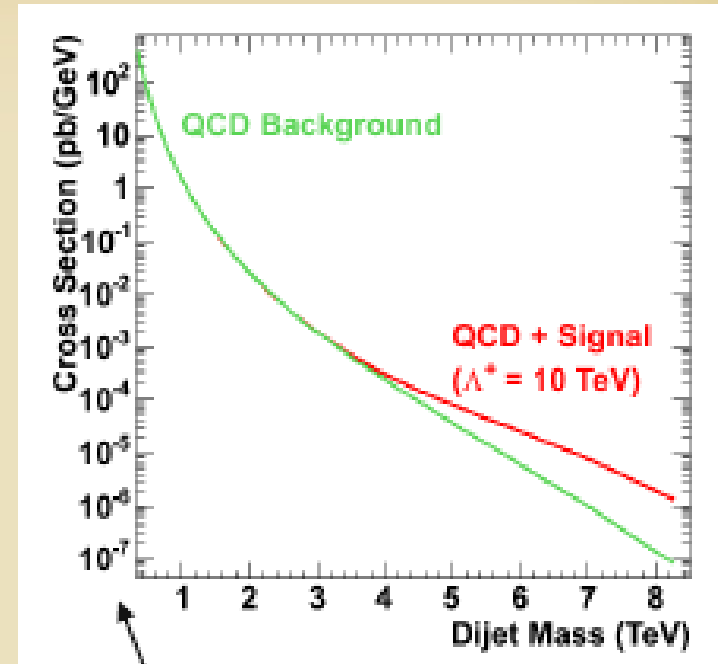


Introduction - Disclaimer

- Most of the material I am showing is “work in progress”:
 - Documented in ATLAS-COM-PHYS-2008-62 – P.Francavilla, C.Roda
 - Documented in ATLAS-COM-PHYS-2007-014 – T. LeCompte
 - Documented in [an ATLAS TWiki page](#) (public)
- Part of the material is (or will become soon) public in the ATLAS CSC notes.
- Long list people contributing

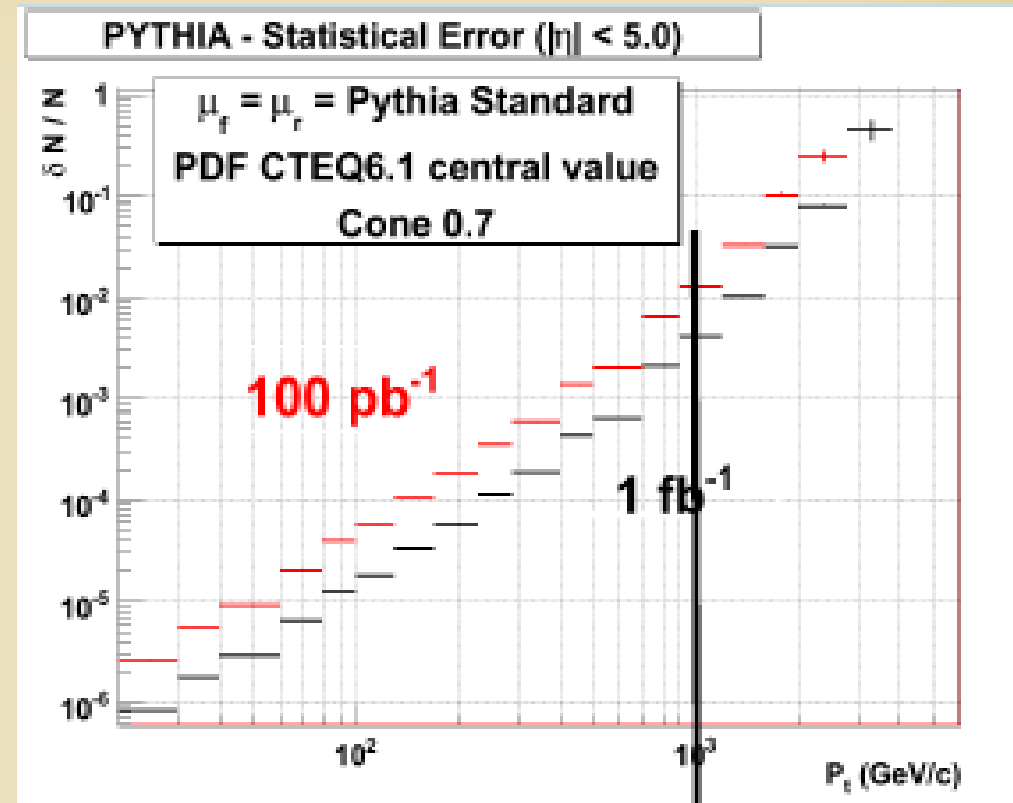
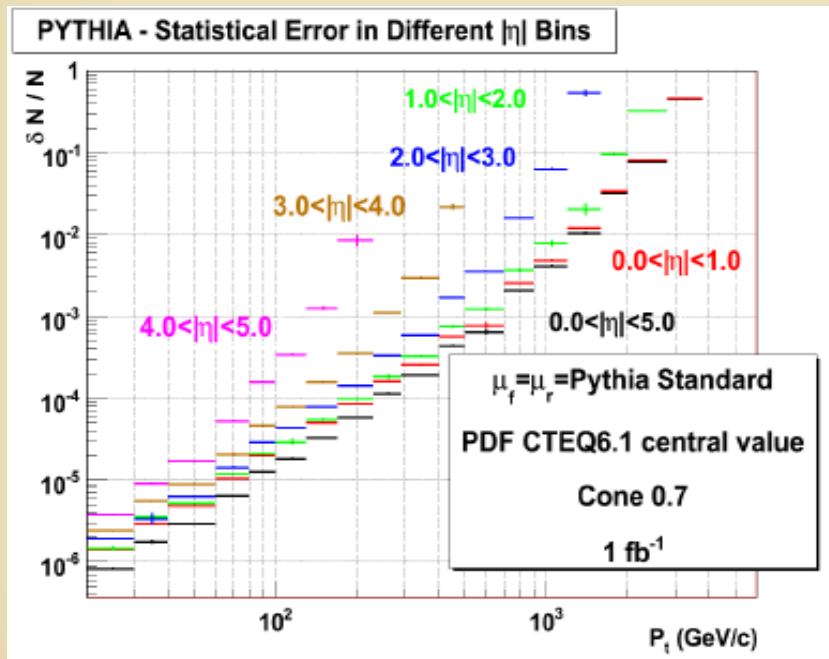
Inclusive Jet Cross Section

- Physics motivations:
 - interesting per-se
 - Background for all the physics channels
 - Possible signals from physics BSM
- Uncertainties in the theoretical prediction:
 - Renormalization and factorization scale
 - PDF
- Experimental issues:
 - Understanding of the **X axis**:
 - *Jet Scale and resolution*
 - *Underlying event – pileup*
 - Understanding the **Y axis** (jet counting):
 - *Jet reconstruction efficiencies*
 - *Jet trigger efficiencies*
 - *Luminosity*



Inclusive Jet Cross Section (2)

- Up to what scale can we probe with the first data?
 - The statistical error at 1 TeV is 1.2% with 100 pb^{-1} , 0.4% with 1 fb^{-1}
 - This is much lower than other errors



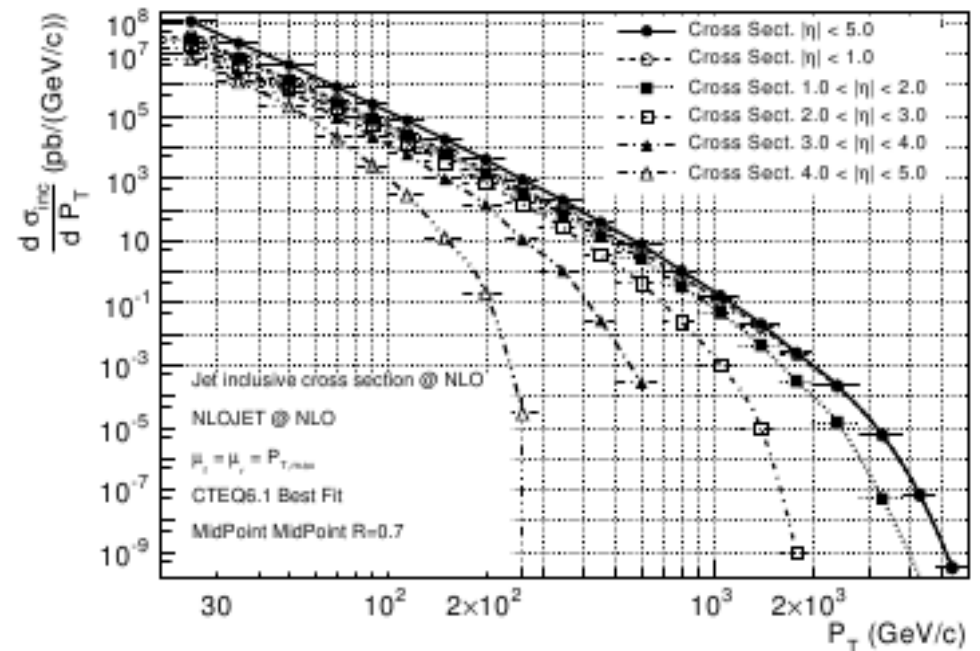
ATLAS MC preliminary

With 1 fb^{-1} we can measure up to **$\sim 2.5 \text{ TeV}$** (statistical error \sim theoretical error)

Theoretical Uncertainties

- Two main theoretical uncertainties considered so far:
 - Neglected higher orders (renormalization and factorization scales)
 - PDF uncertainties
- Cross sections evaluated using NLOJET++ (Nucl. Phys. B269 (1986) 445-484) and Pythia:
 - NLOJET can provide the LO and NLO estimate:
 - *With consistent choices, Pythia and NLOJET give the same result at LO*
 - *NLOJET allows only parton level studies*
 - NLO cross section with CTEQ6.1, $\mu_f = \mu_r = P_{tmax}$ has been chosen as reference

ATLAS MC preliminary



Theoretical Uncertainties (2)

- Sensitivity of the cross section to the choice of μ_f and μ_r .

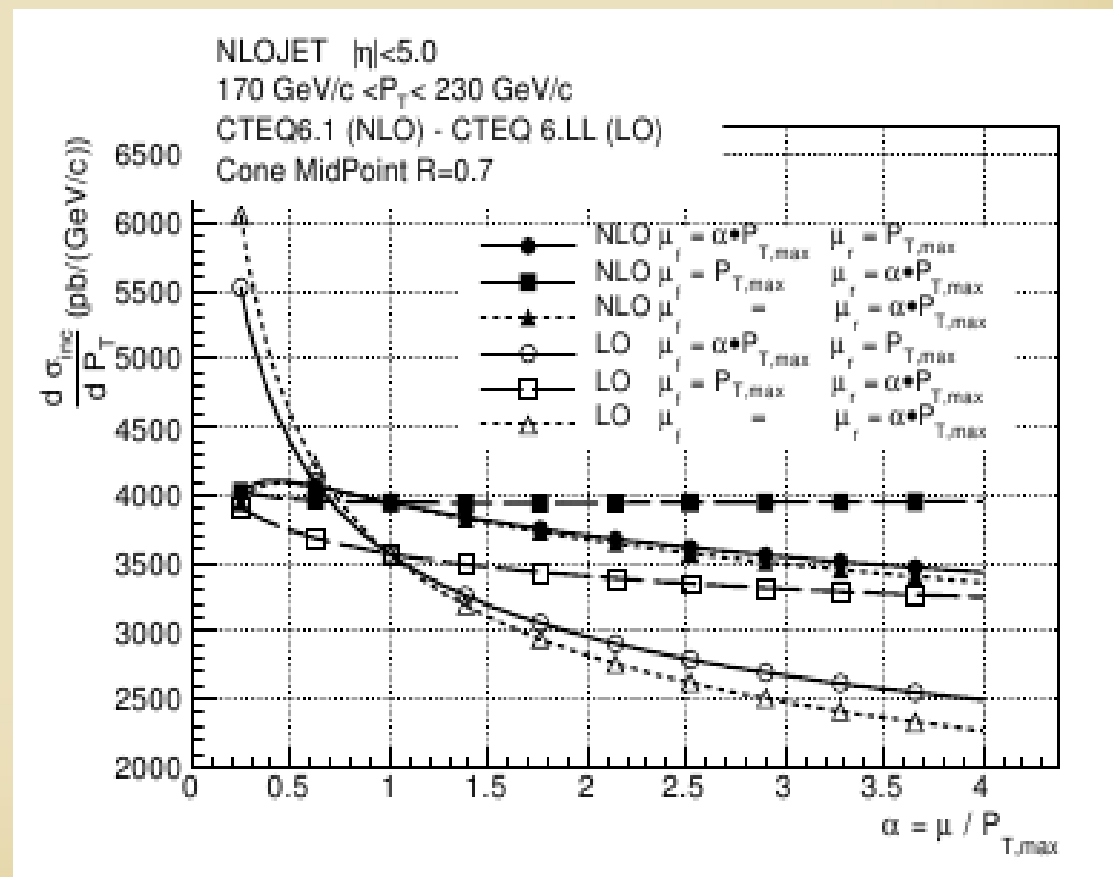
- Define $\mu_f, \mu_r = \alpha P_{Tmax}$, with $0.25 < \alpha < 4$.

- Let μ_f, μ_r vary separately and together

- Compute the ratio $\sigma(\mu_f, \mu_r) / \sigma(\mu_f = P_{Tmax}, \mu_r = P_{Tmax})$

ATLAS MC preliminary

- Only jets with $170 \text{ GeV} < P_T < 230 \text{ GeV}$ are considered in this plot
- The LO is sensitive in particular to μ_r . $\sigma(\mu_r = 0.25 P_{Tmax}) \sim 2 \sigma(\mu_r = 4 P_{Tmax})$
- Limited sensitivity of the NLO

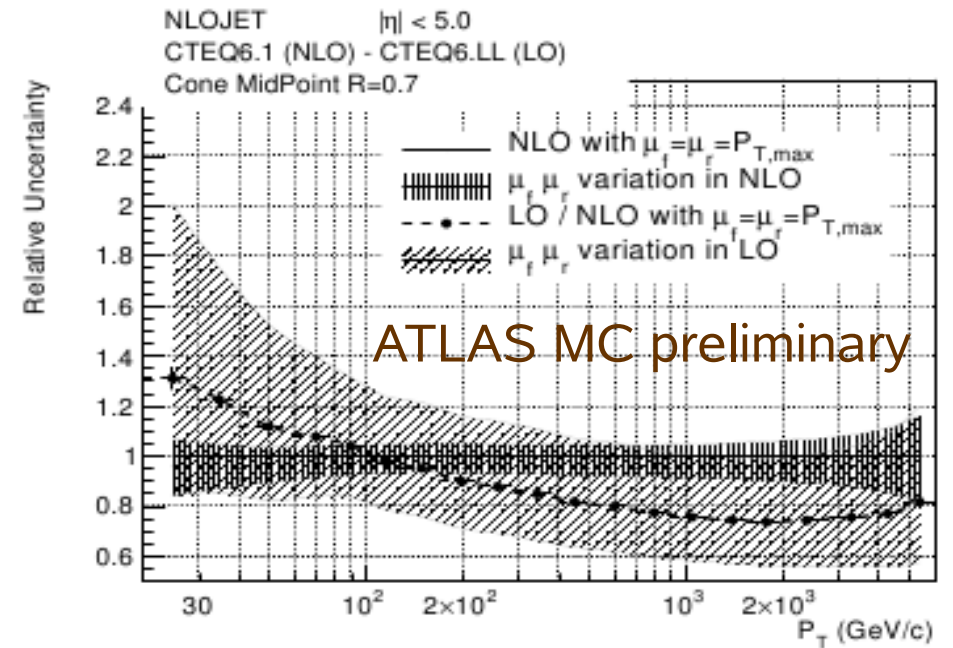
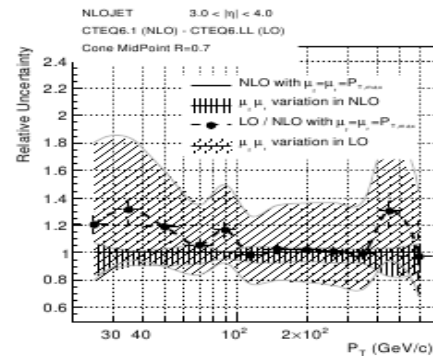
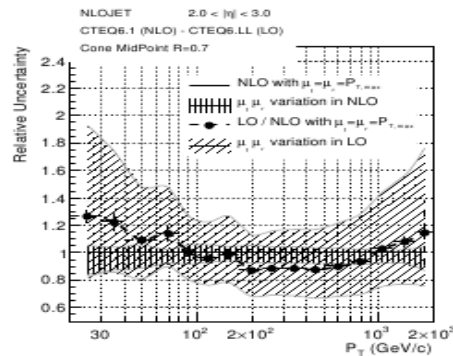
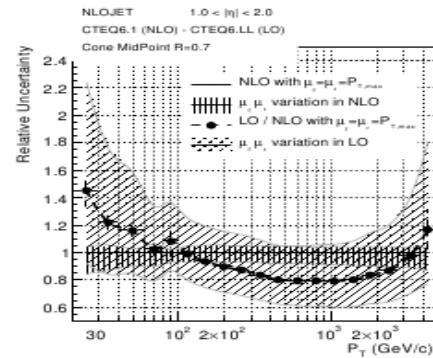
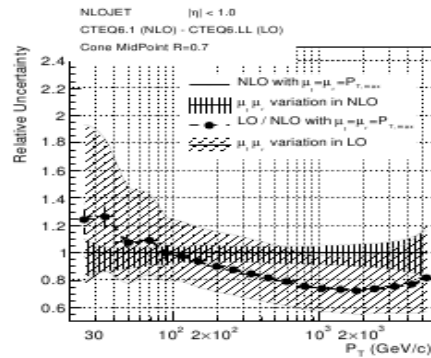


Theoretical Uncertainties (3)

- Bands obtained as max and min of the ratio

$$\frac{\sigma(\mu_r = x P_{Tmax}, \mu_f = y P_{Tmax})}{\sigma(\mu_r = P_{Tmax}, \mu_f = P_{Tmax})}$$

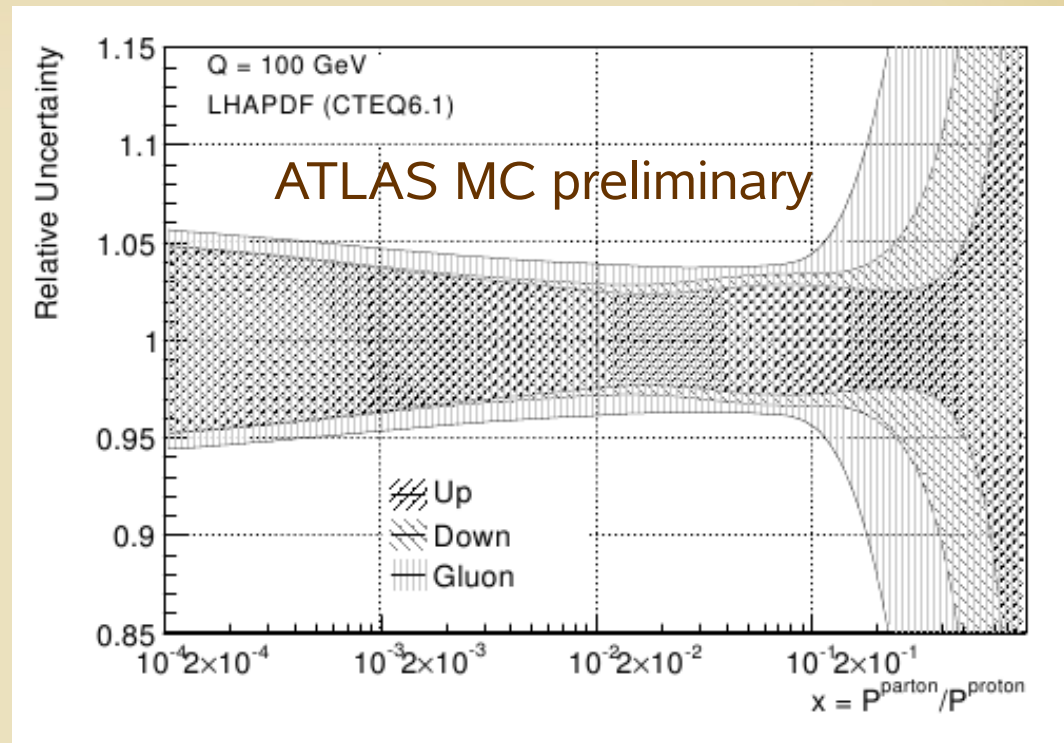
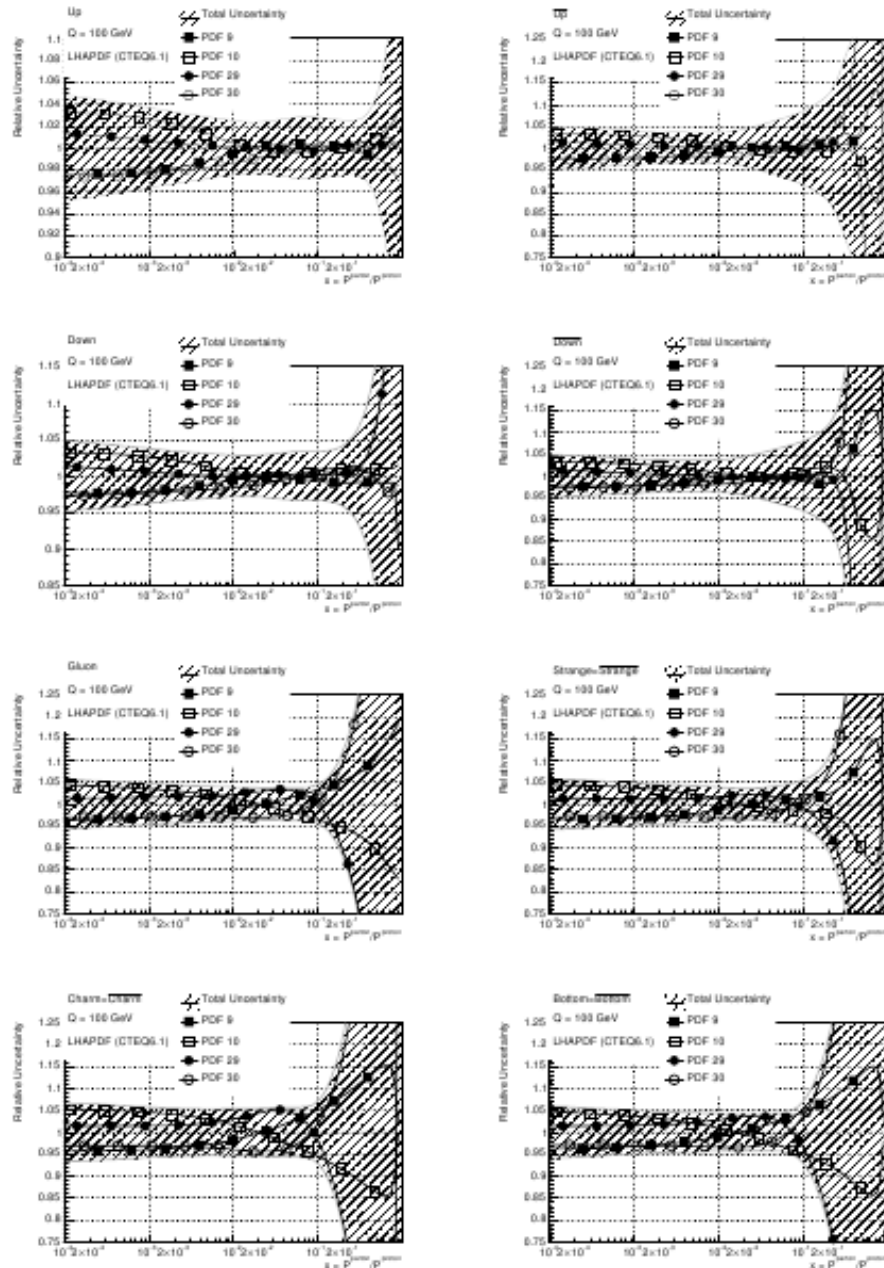
$$x, y = 0.5, 1, 2$$



- The uncertainty is almost independent of P_T above 200 GeV. The numbers are:
 - 7% for the NLO
 - 22% for the LO

Theoretical Uncertainties (4)

ATLAS MC preliminary

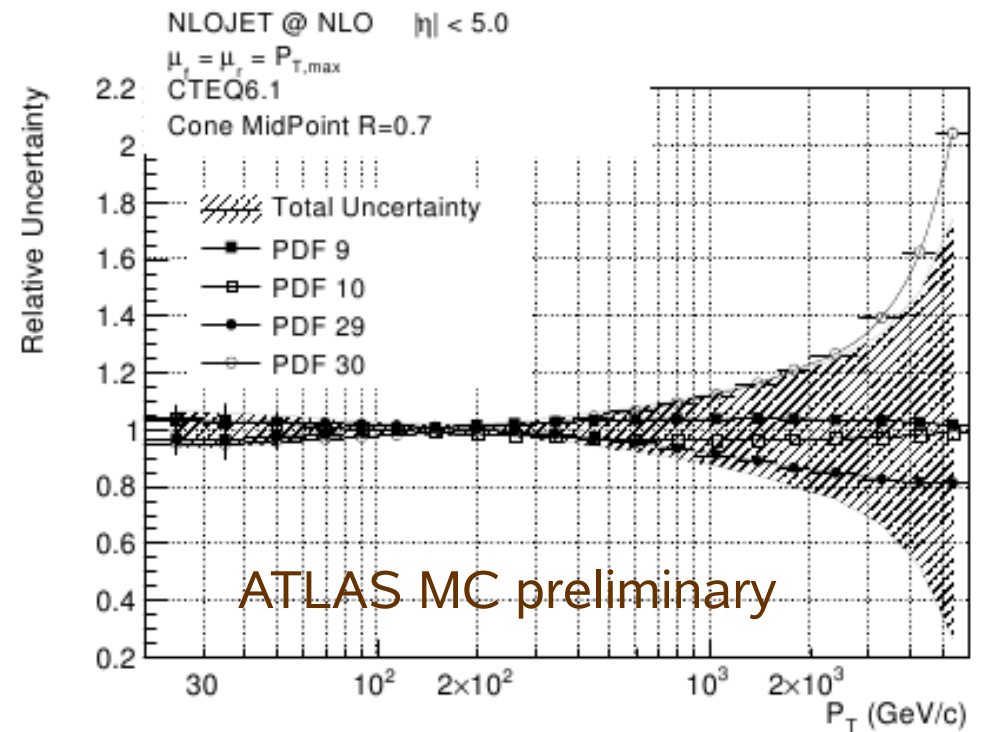
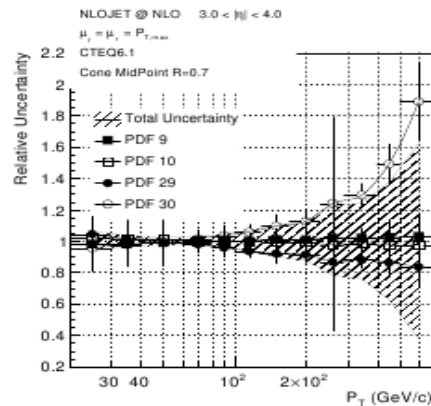
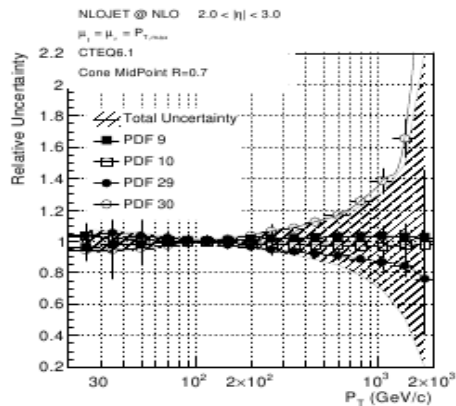
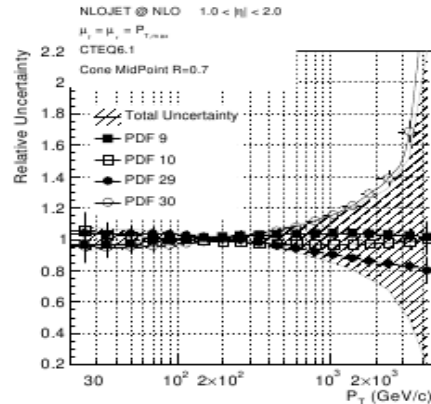
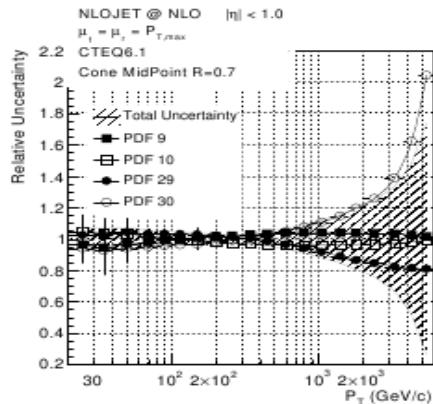


- Uncertainty due to the PDF (LHAPDF CTEQ6.1 used):
 - Uncertainty is dominated by the gluon PDF.
 - Low $x \rightarrow$ PDF sets 9 and 10
 - High $x \rightarrow$ PDF sets 29 and 30

Theoretical Uncertainties (5)

- The uncertainty of the PDFs propagates in an uncertainty of the cross section

$$\Delta\sigma = \frac{1}{2} \sqrt{\sum_i (\sigma(f_i^{\max}) - \sigma(f_i^{\min}))^2}$$



- The error is 2% at 200 GeV and 1 TeV at 13%

ATLAS MC preliminary

Experimental uncertainties

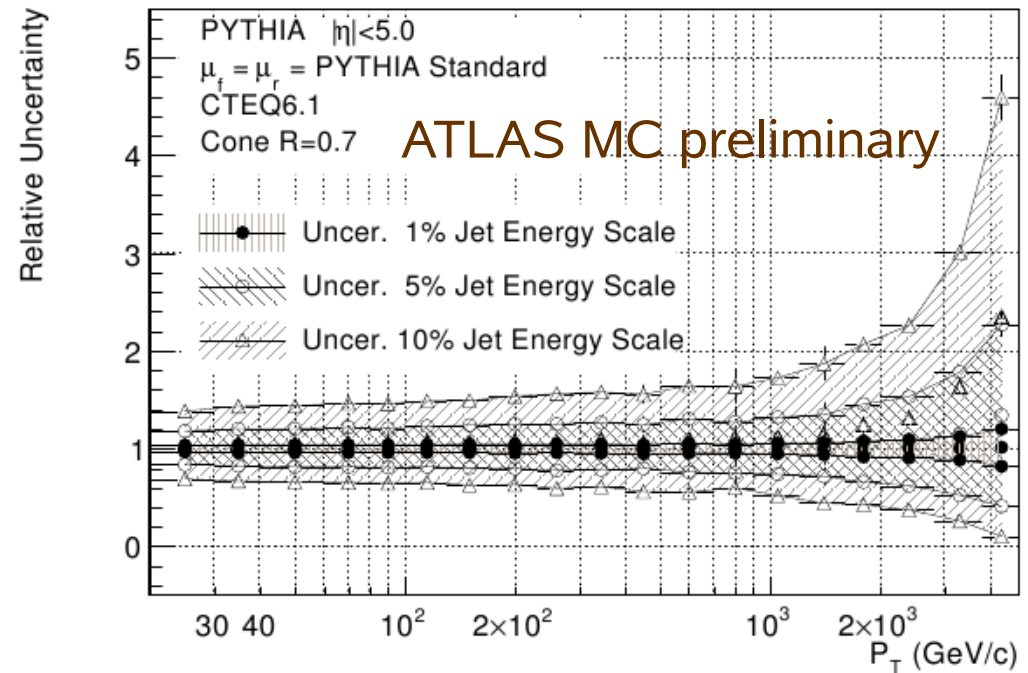
- Several different ingredients enter in the jet cross section measurement at particle level
- Discussed in the following:
 - Jet energy scale and jet resolution
 - Jet trigger efficiencies
 - Jet reconstruction efficiencies
- Not discussed:
 - Luminosity
 - Corrections to apply to the particle level measurement
- The general approach: try to get an estimate of the uncertainties associated with the early data:
 - As much as possible data drive approach to the measurement

Inclusive Jet Cross Section

- Study on the role of the jet scale uncertainty:

- The ATLAS fast simulation has been used to estimate the error on the cross section due to the jet scale.
- The response of the ATLAS fast simulation jets is manually shifted by

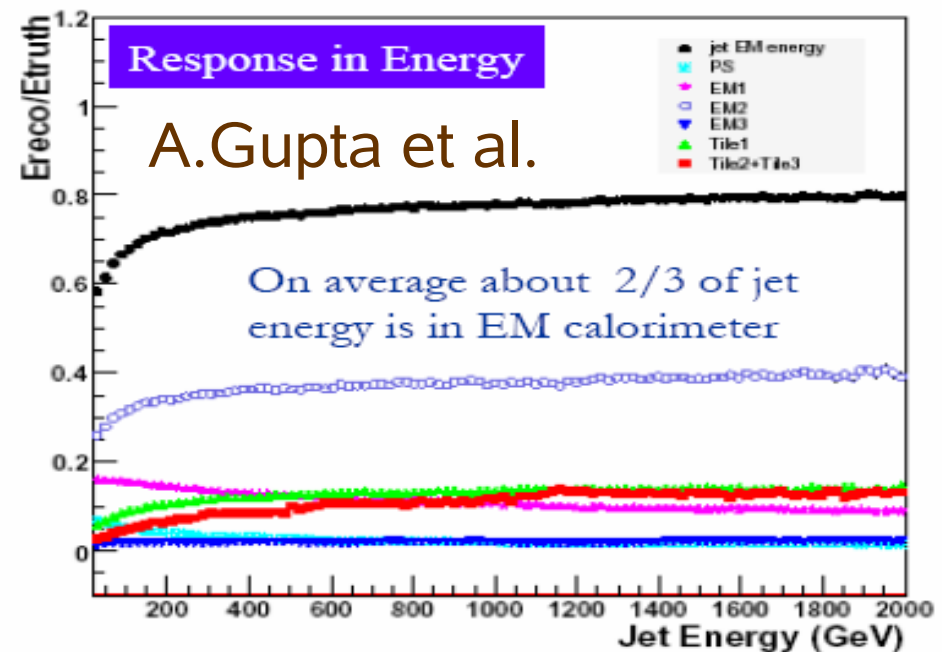
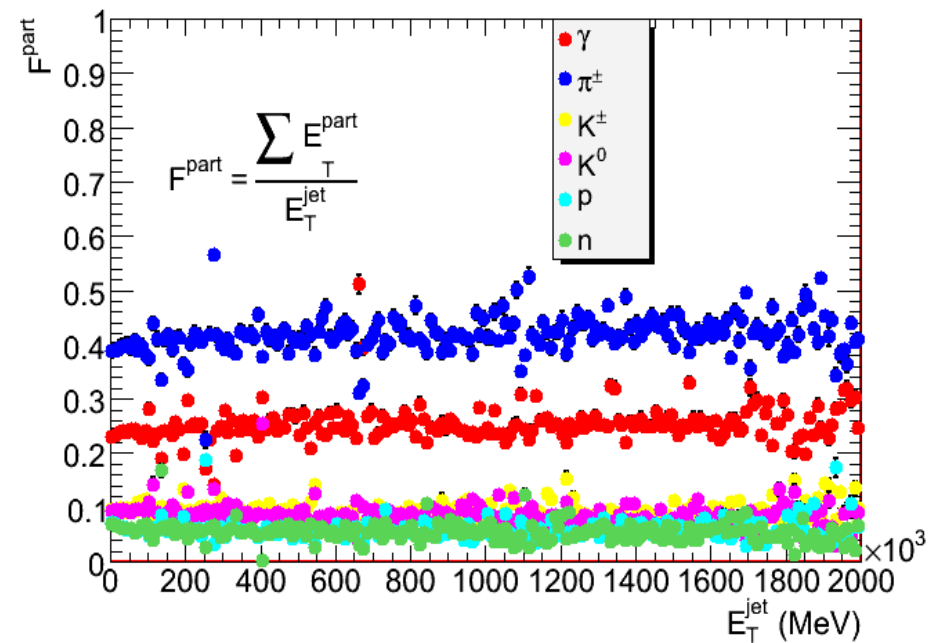
- 1% (*ATLAS TDR claim*)
- 5% (*Optimistic initial ATLAS jet scale*)
- 10% (*Pessimistic initial ATLAS jet scale*)



- 10% error on the jet scale \rightarrow 60% error on the cross section @ 1 TeV
- 5% error on the jet scale \rightarrow 30% error on the jet scale @ 1 TeV

Jet Energy Measurement

- 25% of the jet energy is carried by **photons**
- 75% of the energy is **hadronic** – energy dependent EM fraction in the shower
- The ATLAS calorimeters are **non-compensating**:
 - The response to EM and HAD energy is different
 - The measured jet energy is non-linear with the true jet energy
- The detector has holes and dead material:
 - ~10% of the energy is lost



Jet Energy Measurement (2)

- An event by event correction for the dead material energy loss and fluctuations in the em fraction of the hadronic shower gives an improved jet resolution
- In ATLAS we studied the possibility to correct using:
 - Longitudinal shower development (weights associated to the longitudinal calorimeter samplings)
 - Energy density in the cells (cell level weights depending on the energy density)
 - Cluster level corrections using both the above (local hadron calibration)
- All these quantities are sensitive to the electromagnetic/hadronic fraction of a shower.
- The corrections are usually MC based.

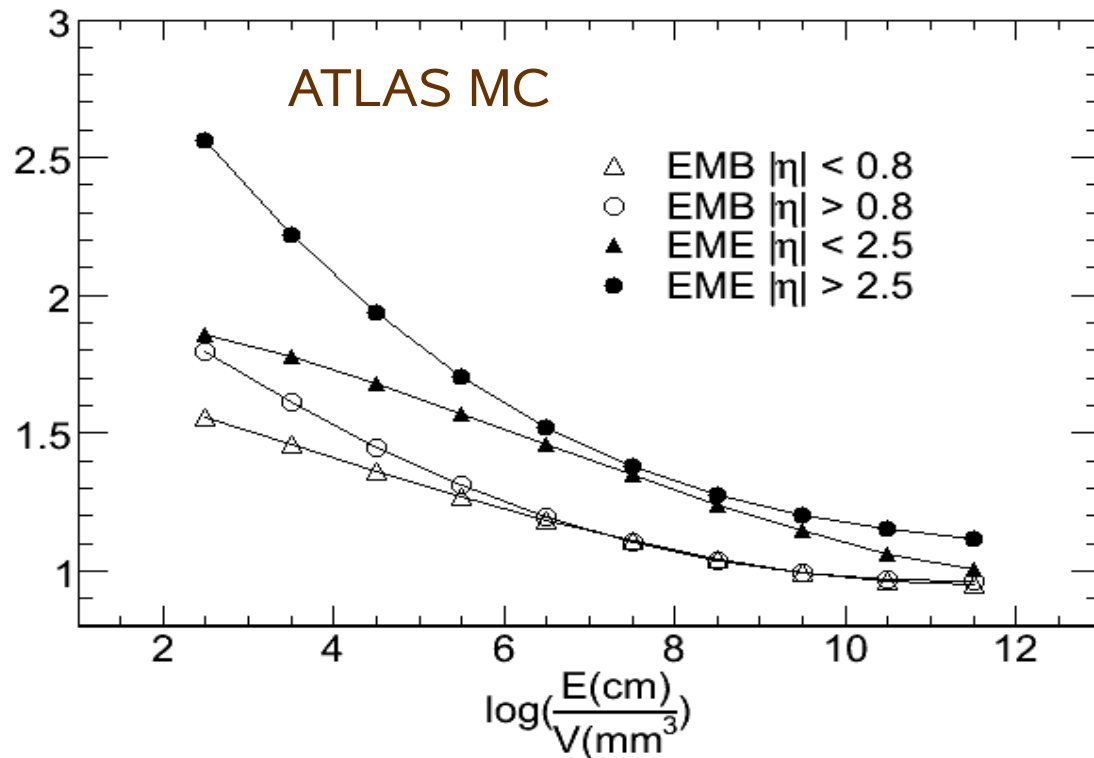
H1 jet corrections

- The total energy is computed as follows: $E_{rec}^{jet} = \sum_{i=cells} w_i \left(\frac{E_i}{V_i} \right) E_i$
- The weights depend on the **cell energy density** (and pseudorapidity, through a rough binning)

$$w_i \left(\frac{E_i}{V_i} \right) = \sum_{j=0}^3 a_j \log \frac{E_i}{V_i}$$

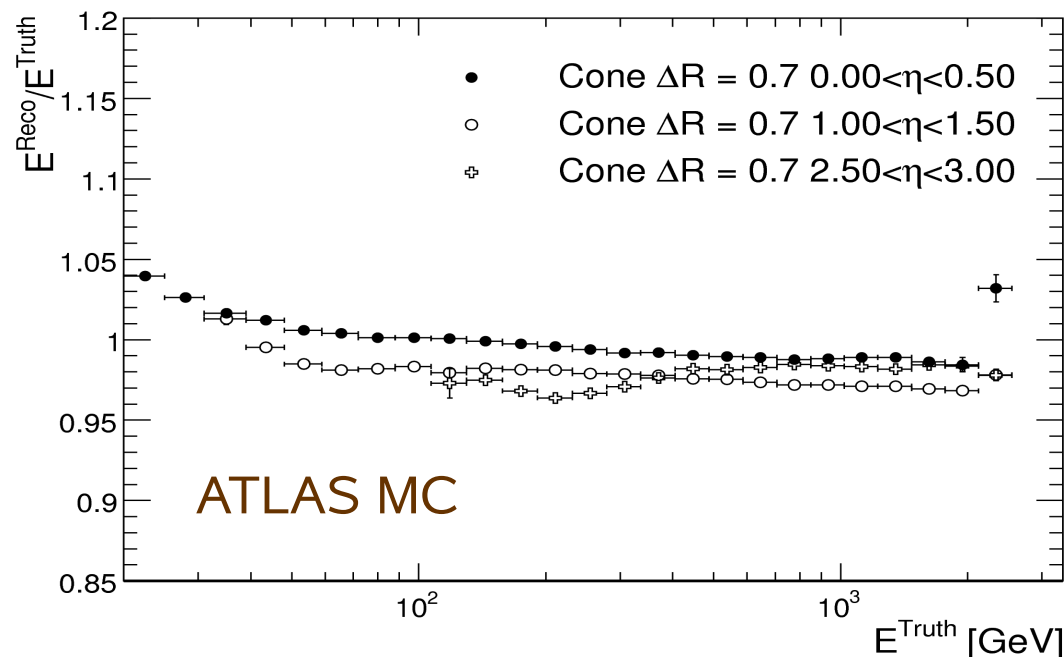
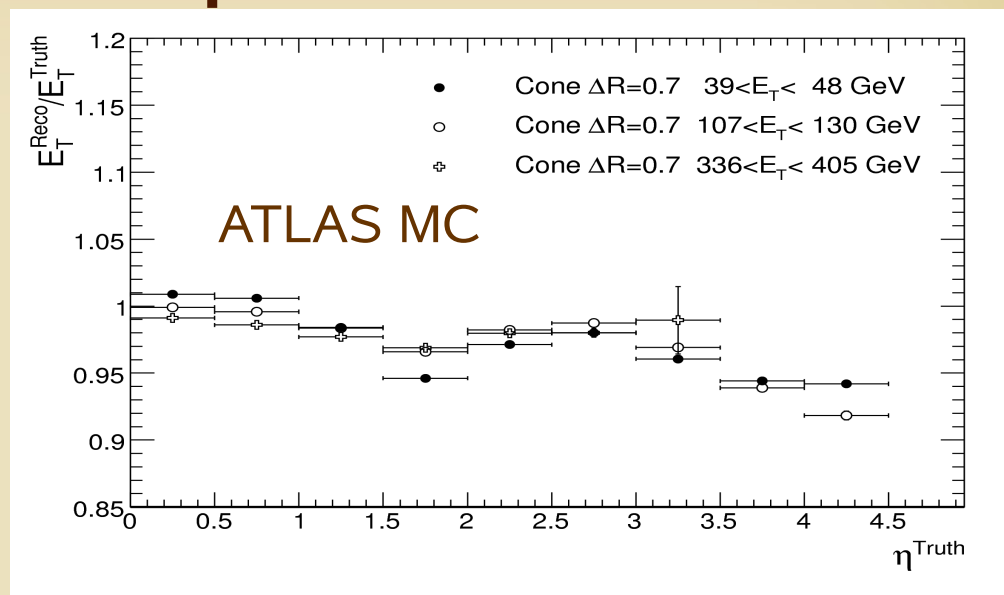
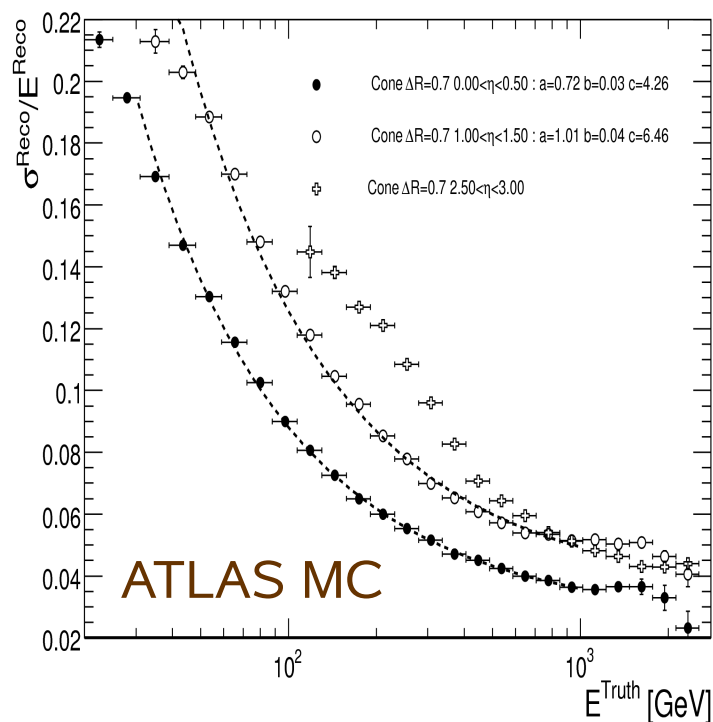
The weights enhance the response of low energy density cells (Had energy).

High density is associated with EM deposits: the weights go to 1

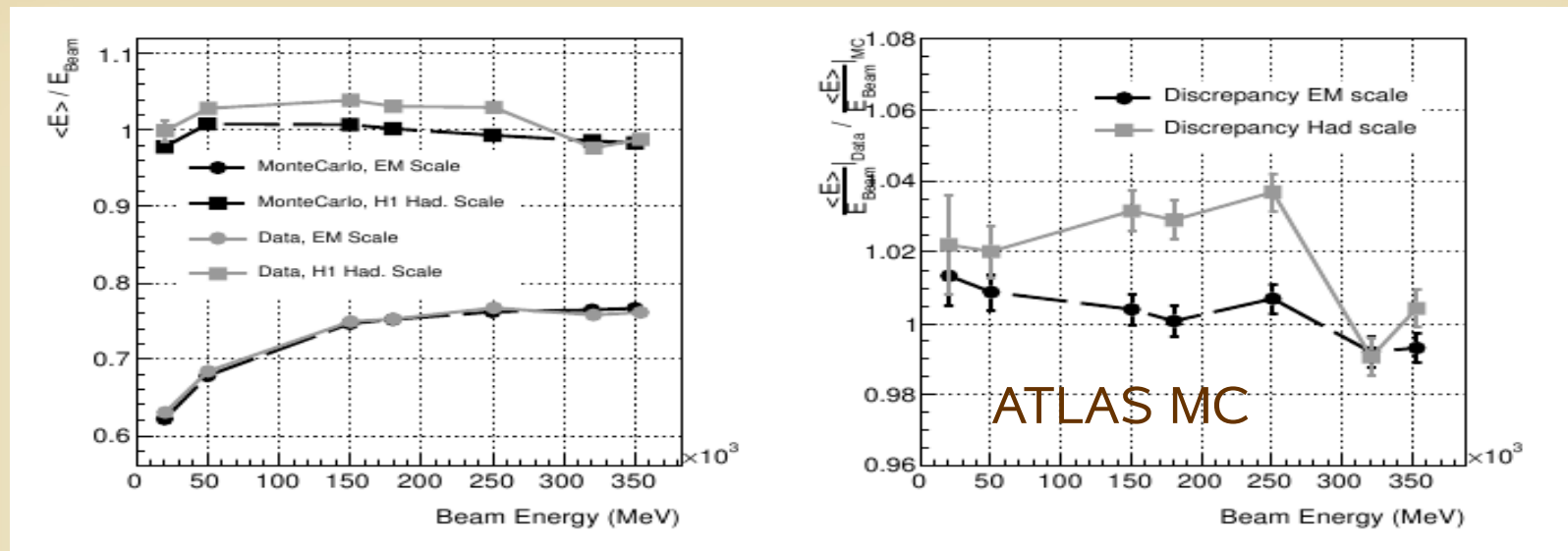


Some examples

- SU3 sample plots
- SU3 is very different from what has been used to find the calibration constants



Combined Test Beam data



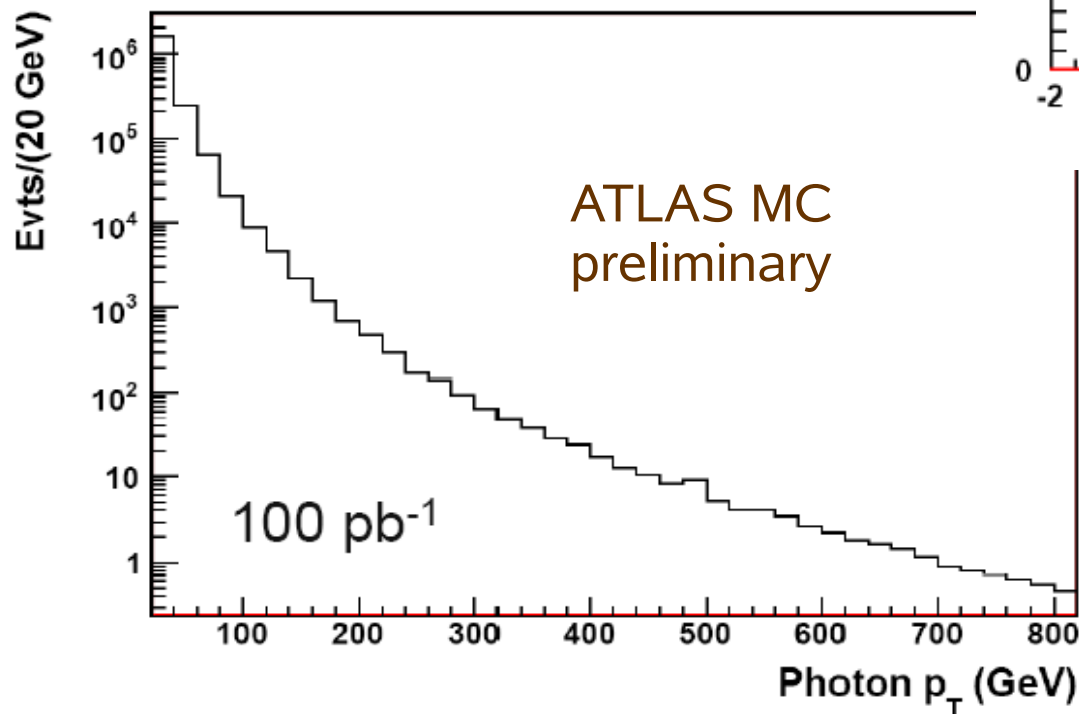
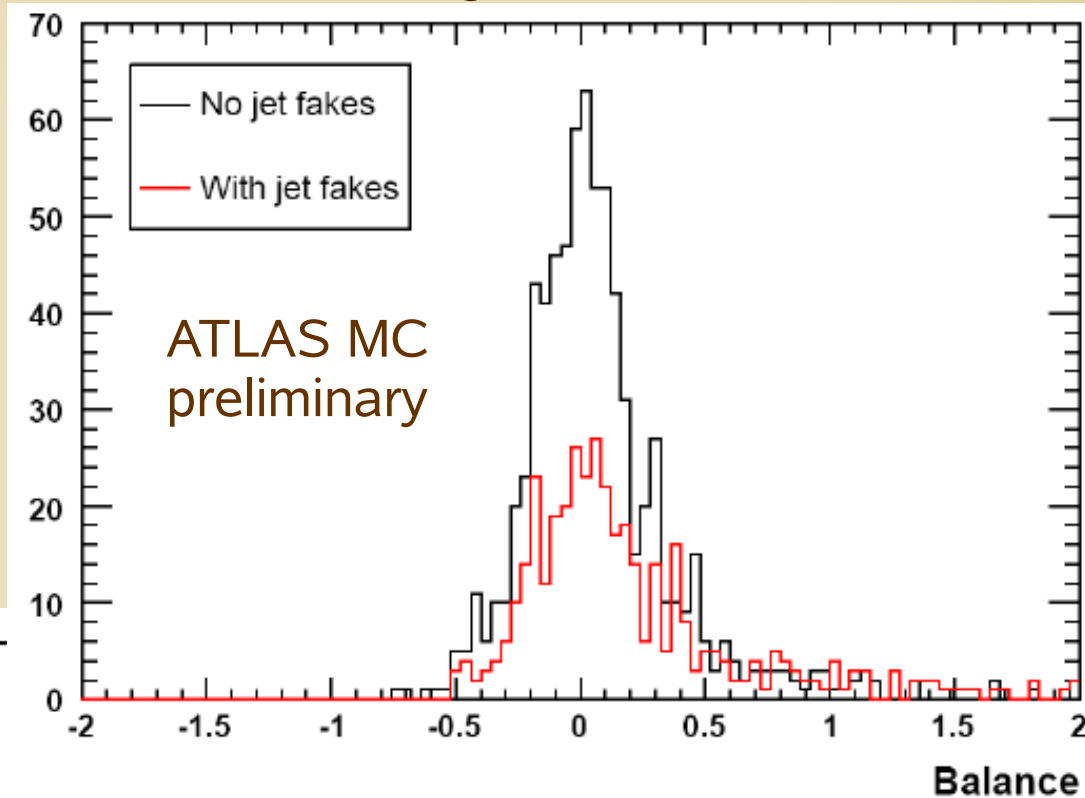
- Estimate the scale bias at day 1 directly from the test beam data:
 - Make use of CTB2004 pion
 - Apply the jet corrections (computed for jets in the ATLAS setup) to the real pions
 - Agreement MC/DATA (before corrections) good:
 - *Maximum disagreement ~1-2%*
 - After the corrections:
 - *Maximum disagreement ~4%*

Comments on the Jet Scale

- Corrections to fix the jet scale are in place:
 - Performance tested in a variety of different geometries, physics channels, jet fragmentation, showering model, Combined Test Beam data. .
 - Each of the above introduces uncertainties of the order of few percent (rarely larger than 5%)
 - It looks plausible to achieve $\sim 5\%$ jet scale using the best G4 physics list (QGSP_BERT) with accurate as-built geometry.

In situ verification of the jet scale

- Check the energy scale with γ +jet
- The balance looks good, but:
 - Large background from DiJet



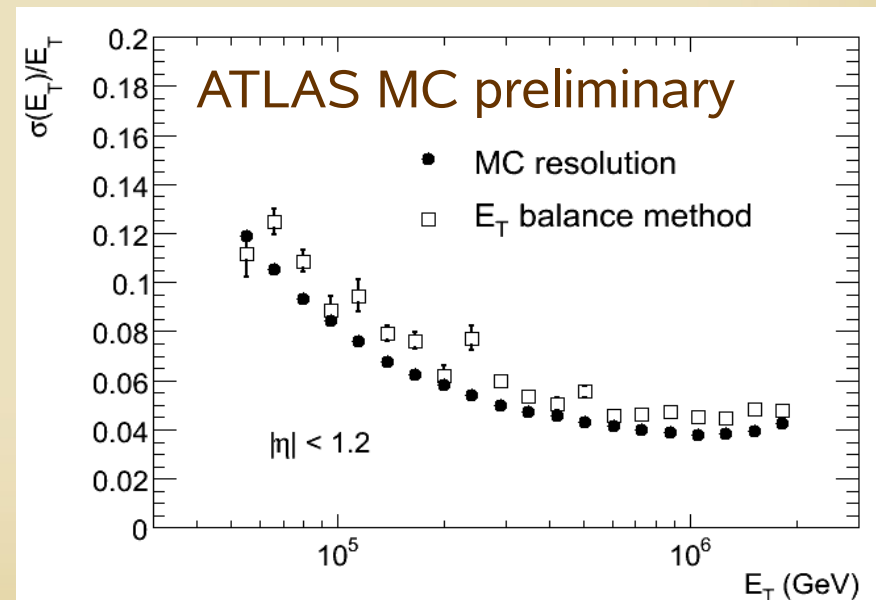
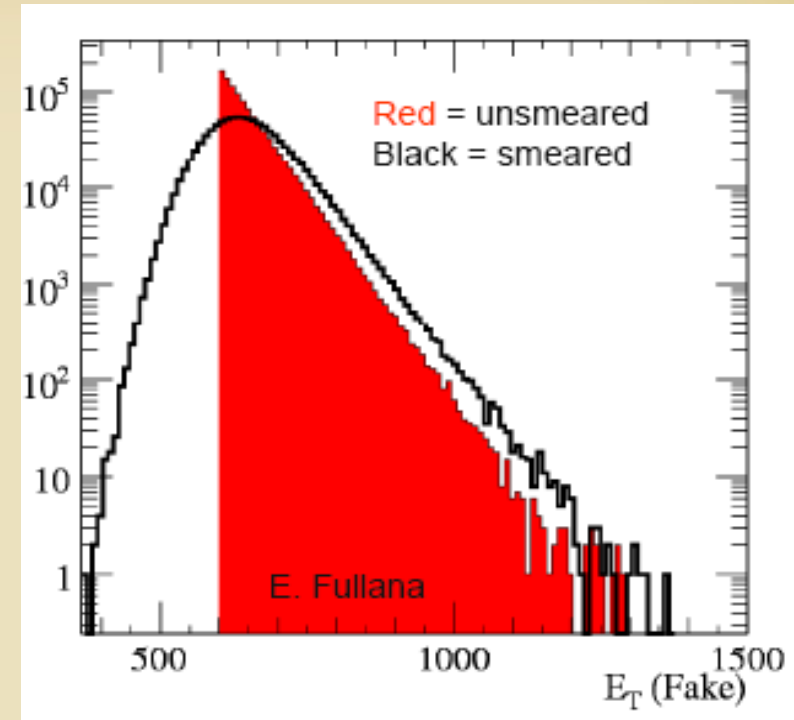
- 100 pb⁻¹: γ +jet can probe up to few hundreds GeV:
 - We need a way to get up to the TeV scale

Jet Resolution

- Experimental resolution + a steeply falling P_T spectrum \rightarrow bias in the energy measurement
- Correcting for this requires the knowledge of the jet resolution.
- The di-jet balance method :
 - Define the unbalance in the transverse plane between the leading jets as

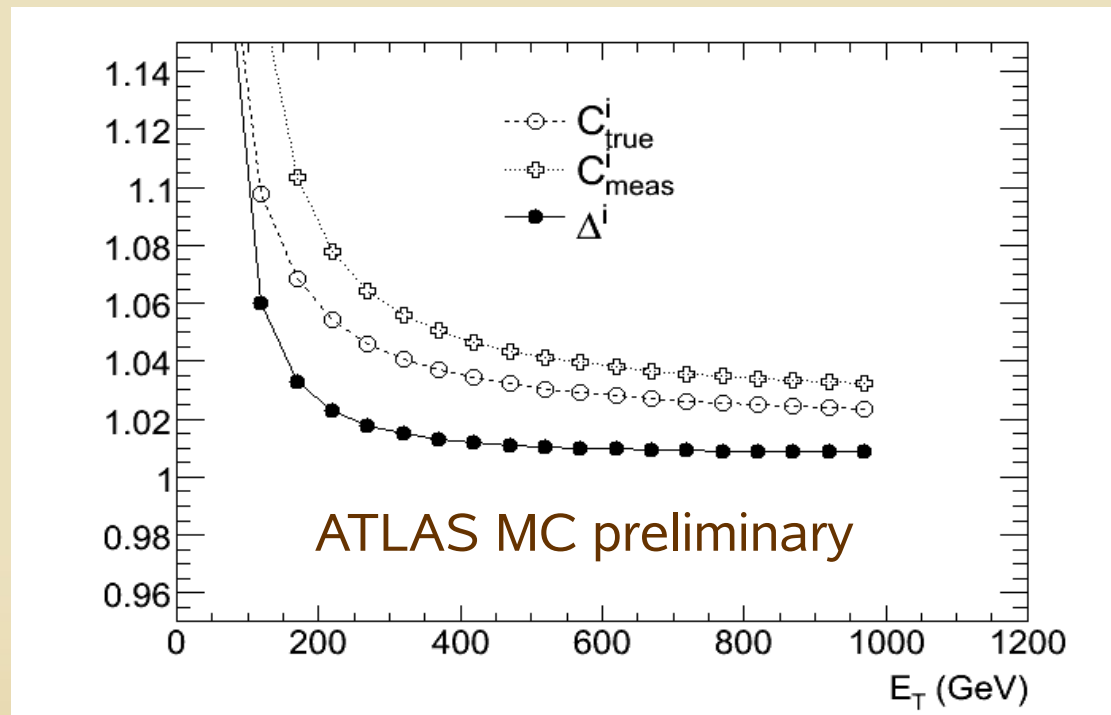
$$A = \frac{(E_{T1} - E_{T2})}{(E_{T1} + E_{T2})}$$

It can be shown that $\sigma(E_T)/E_T = \sqrt{2} \sigma_A$ if $\langle E_{T1} \rangle = \langle E_{T2} \rangle$ and $\sigma(E_{T1}) = \sigma(E_{T2})$, which means balanced jets with uniform resolution



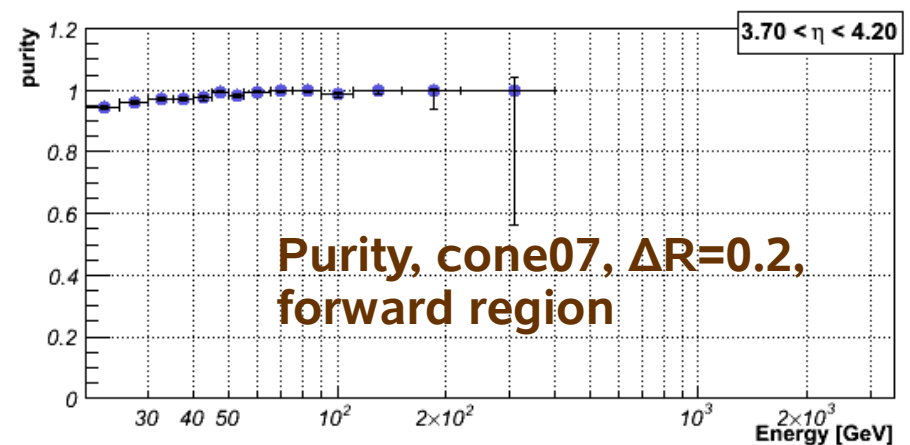
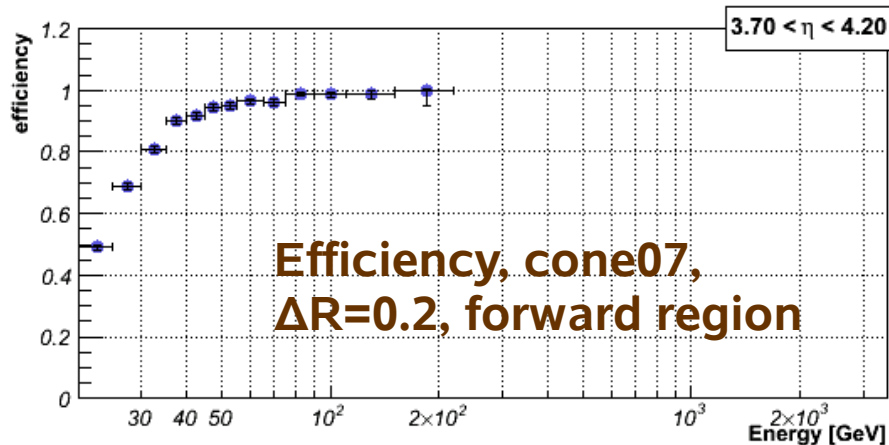
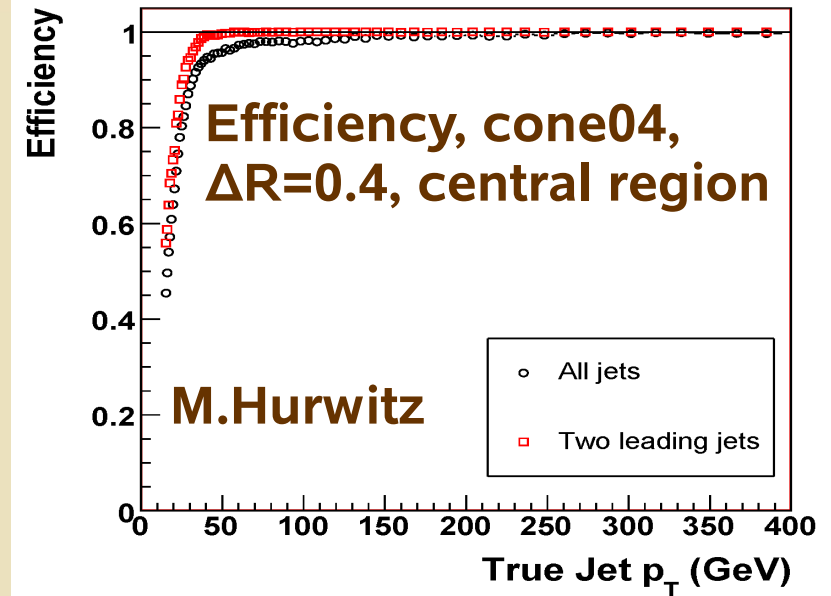
Jet Resolution (2)

- The “true” corrections to the cross section are of the order of 5% at 200 GeV, 3% at 1 TeV
- The “measured” corrections are $\sim 8\%$ at 200 GeV, 4% at 1 TeV
- The introduced bias is $\sim 5\%$ at 100 GeV, $\sim 2\%$ at 200 GeV and it decreases with E_T



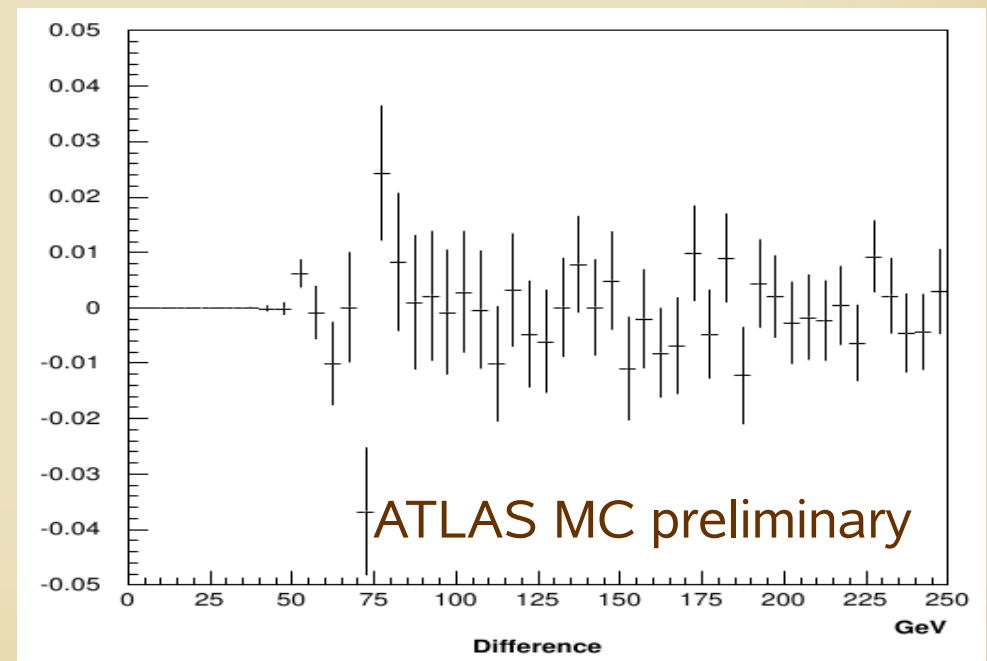
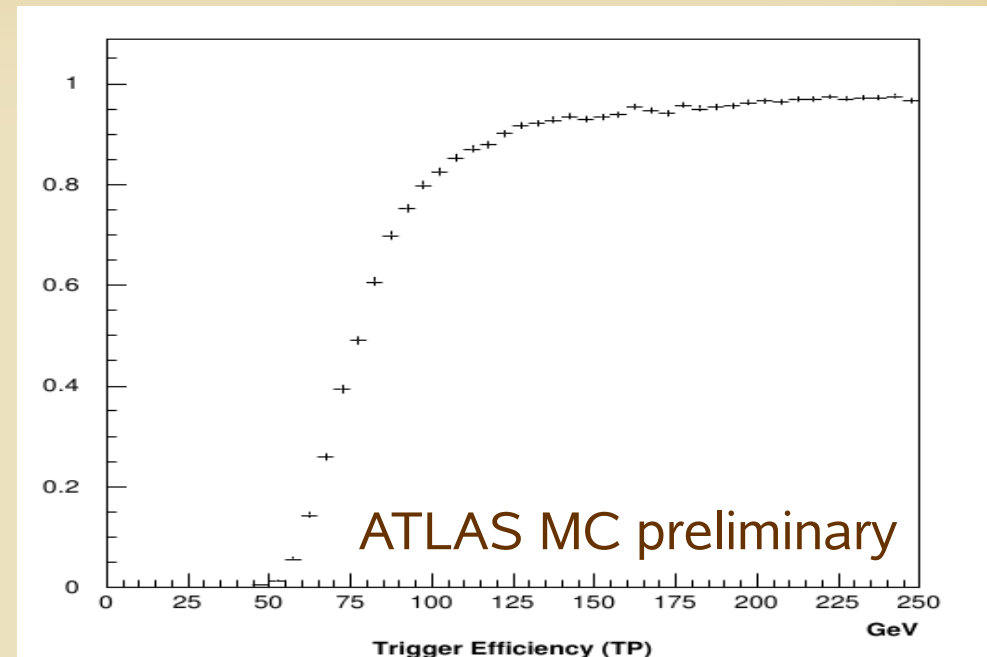
Jet Reconstruction Efficiencies

- Reconstruction efficiency:
 - Define a ΔR_{match} (choice based on the angular resolution)
 - Match reconstructed jets with truth jets if $\Delta R < \Delta R_{\text{match}}$
 - The efficiency is the number of matched reco jets/number of truth jets
 - The purity is the number of matched reco jets/number of reco jets
- Both numbers depend on ΔR_{match}



Trigger efficiencies

- Data drive approach to understand trigger efficiencies.
- Two possible approaches:
 - Start with MB trigger and understand the efficiency of the lowest jet trigger. Iterate
 - Tag and probe:
 - *The jet that triggered is the tag*
 - *The other jets in the event are the probe*
 - *Efficiency curves obtained matching the probes to the ROIs*



Summarizing....

- The dominant error is by far the one on JES:
 - should not be true anymore if the nominal 1% is reached
- Largest theoretical error comes from the PDF uncertainty
- Statistical error, jet resolution, small compared to the JES

Error	200 GeV/c	1 TeV/c
Jet Energy Scale (10%)	43%	57%
Jet Energy Scale(5%)	21%	29%
Neglected higher orders (LO)	22%	21%
Parton distribution functions	2%	13%
Neglected higher orders (NLO)	6%	7%
Jet Energy Scale(1%)	5%	5%
Jet Energy Resolution (20%)	6%	4%
Jet Energy Resolution (10%)	3%	2%
Statistical error (100 pb ⁻¹)	0.018%	1.2%

What is missing

- The analysis aims to measure the jet cross section at particle level:
 - particle/parton level corrections not studied much:
 - *UE correction from MC after its tuning? Event by event subtraction using the energy density? Early subtraction a la D0*
 - *Hadronization corrections not in place*
- At “experimental” level:
 - Uncertainty on the luminosity not estimated
 - Assuming a working detector. Dead cells not in the game (current status ~0.1% dead cells in Lar EM, ~0.8% in Tile (HAD))
 - Statistics available in 2008 basically an unknown (small) number
 - No studies done at 10 TeV

Conclusions

- Jet performance well understood (on simulated events):
 - Good performance in terms of reconstruction efficiencies, jet linearity and resolution
 - Strategies are in place to estimate them from the data
- Inclusive jet cross section measurement:
 - We hope to measure up to $E_T \sim 1 \text{ TeV}$ with the first 100 pb^{-1}
 - The most relevant experimental uncertainty comes from the jet energy scale:
 - *It will be controlled with γ +jets up to $\sim 300 \text{ GeV}$ (with 100 pb^{-1})*
 - *Scale variations changing material, shower model, physics sample are maximum 5%*
 - *A direct estimation with real CTB data gives 5% error*
- Waiting for the data

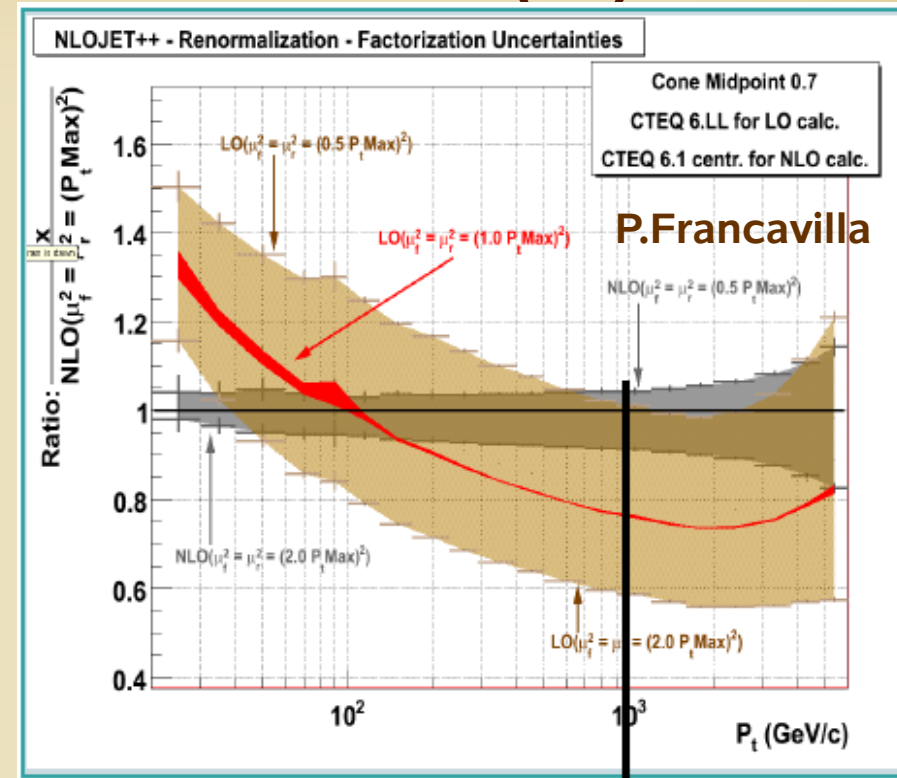
BACKUP

Jet Measurements – Truth Definition (2)

- The aim: the reconstructed final state is close to that reconstructed from the final state particles (truth):
 - The **truth jets** (particle jets) are those obtained running the **same reconstruction algorithm** used in the detector on the **final state MC particles**.
- Two issues play a role:
 - **Jet reconstruction algorithms** (how one does cluster particles/calorimeter clusters to get jets)
 - **Jet calibration**
- What ATLAS uses for the jet reconstruction:
 - **Cone algorithm** with and without midpoints – about to import the SIS cone algorithm from the FastJet (G.Salam et al.)
 - **K_T** different ΔR parameters

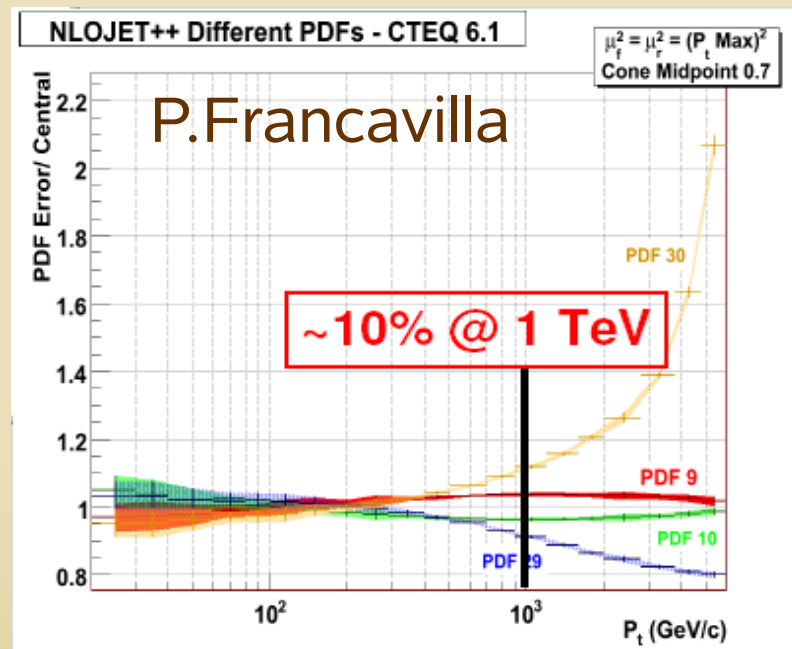
Inclusive Jet Cross Section (2)

- There are quite large uncertainties in the theoretical prediction. The main sources are:
 - Renormalization and factorization scales
 - PDF uncertainties (evaluated using the LHAPDF)
 - *At high energy the high x gluon PDF gives the largest uncertainty*



1 TeV uncertainty:

- 30% LO
- 7 % NLO



Ren/Fact
PDF

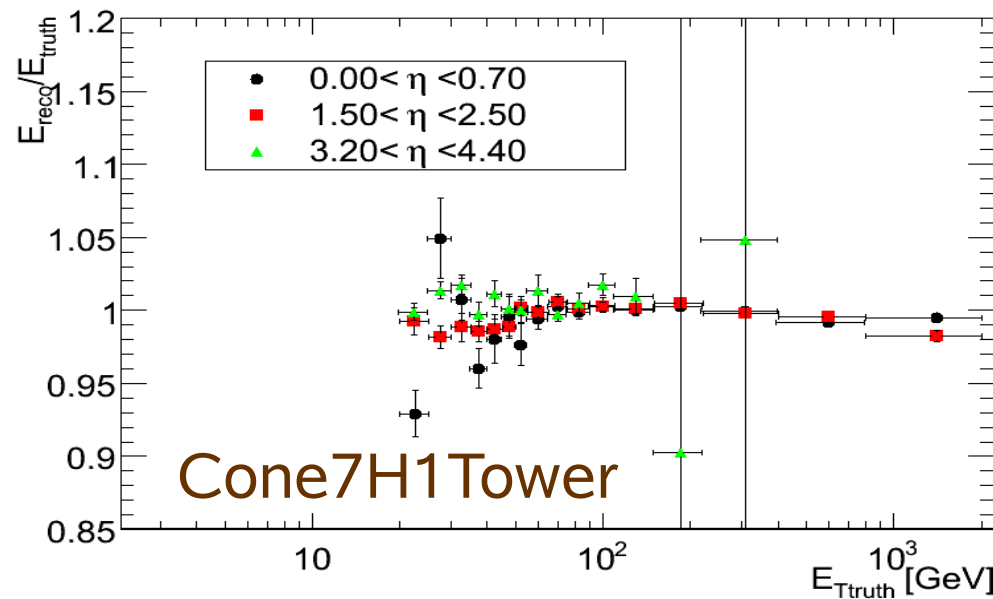
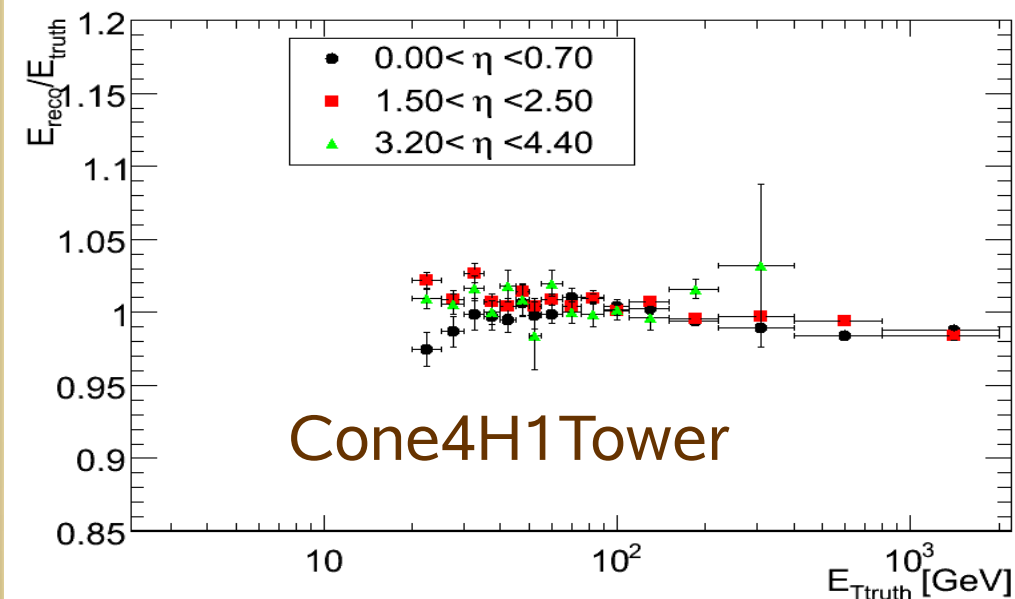
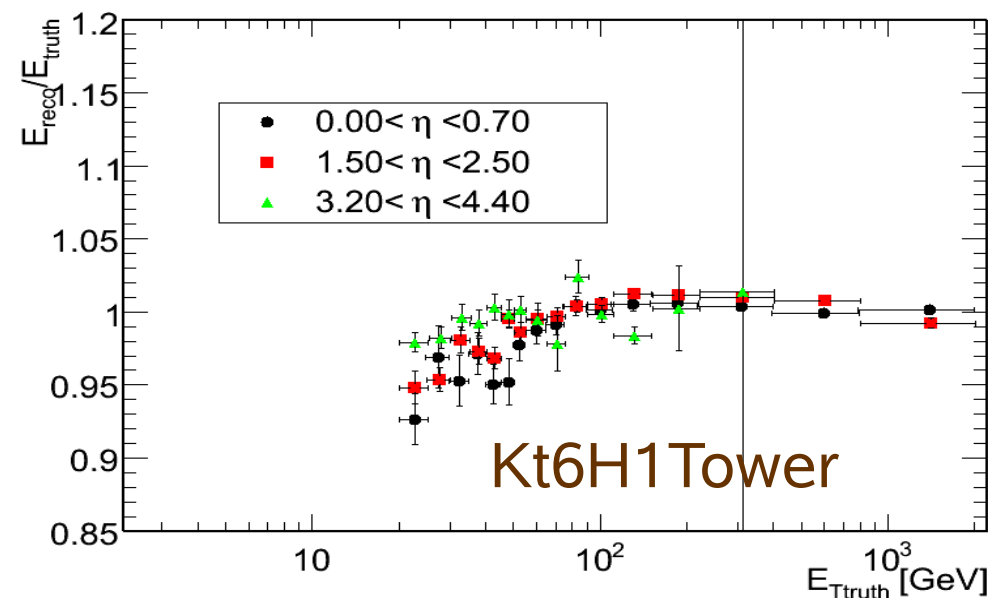
	1 TeV	200 GeV
Ren/Fact	7%	5%
PDF	10%	<5%

H1 jet corrections

- The weights w_i are **the same for all the reco algos**, all inputs.
 - They are the same still hard coded for EtMiss reconstruction
- Crack and Gap regions not taken into account in the weight computing. For each reco algo and input clusters, a **scale factor** is computed:
 - Intended to correct for non-linearities **caused by the gap and the crack**
 - It corrects also for **residual reconstruction algorithm dependent effects**

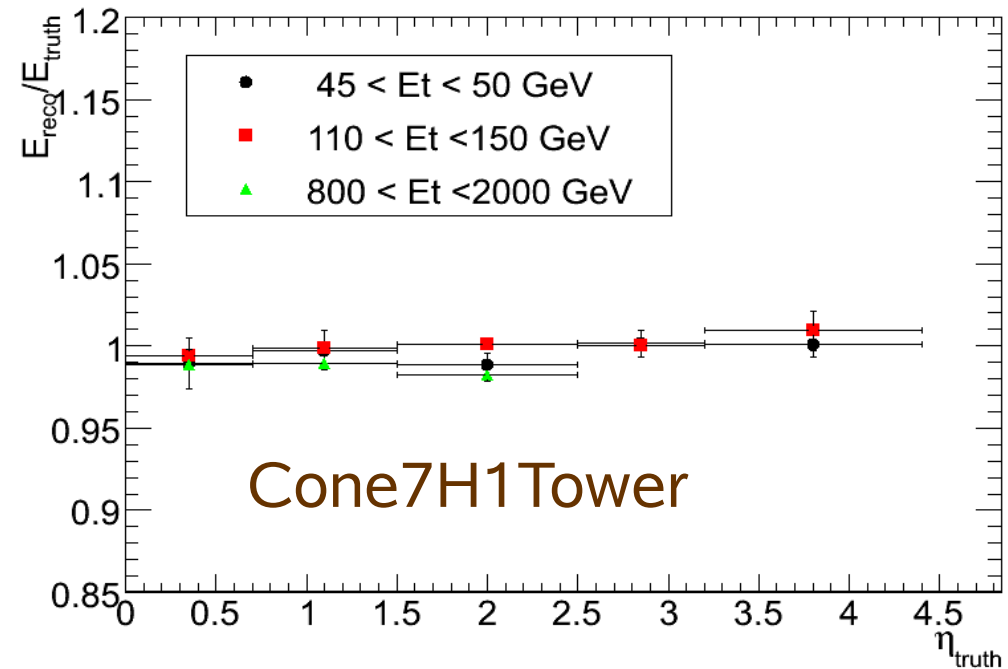
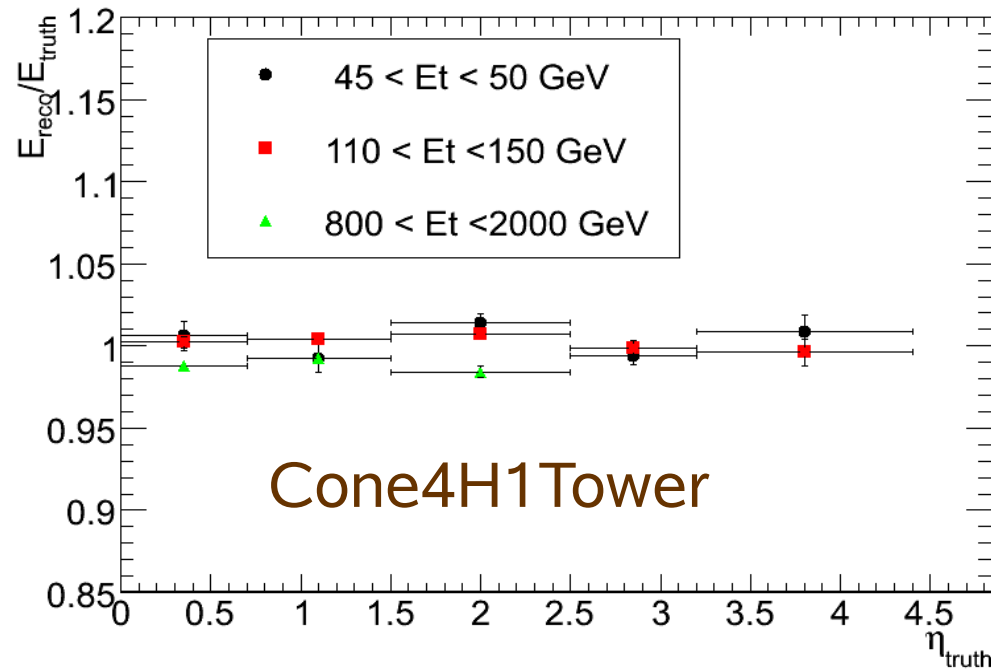
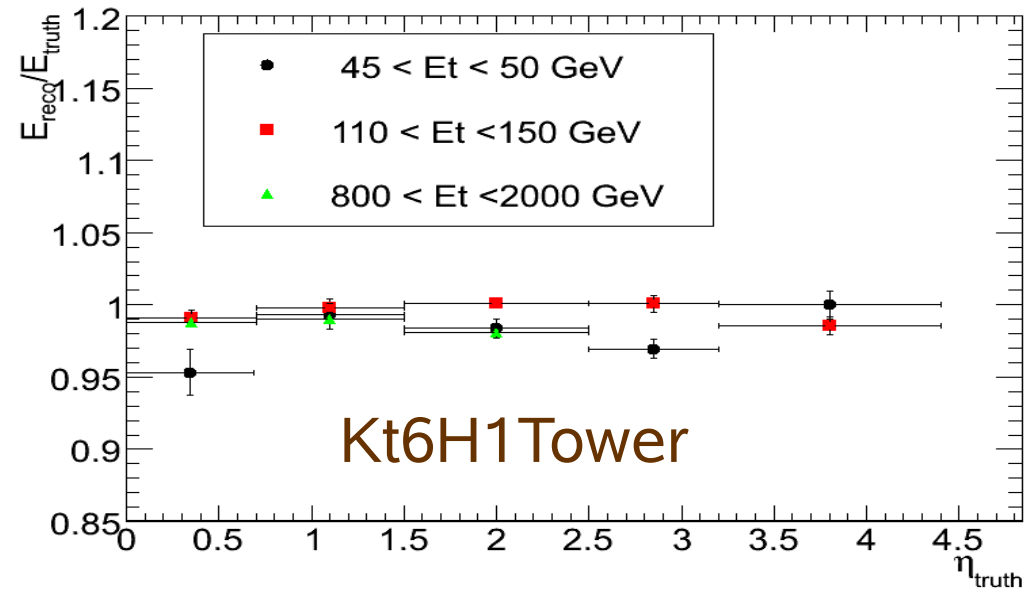
Jet Linearity in FastCaloSim

- Linearity **close to 1** in a large range of jet E_T , in different pseudorapidity regions
- Some **5% deviation** observed for Kt6 at low E_T
- Kt4 and TopoJets not done yet



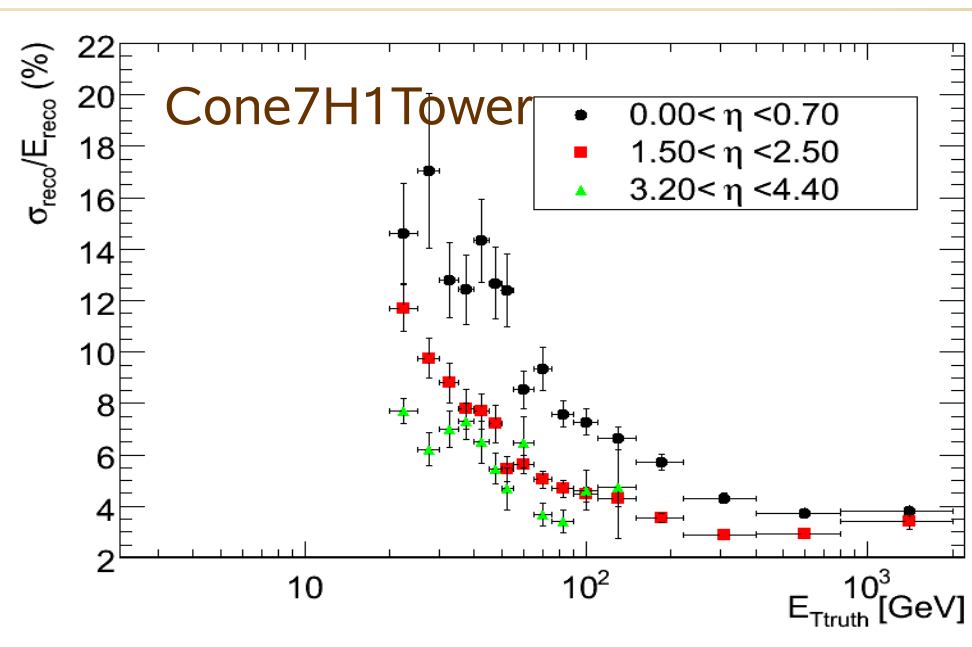
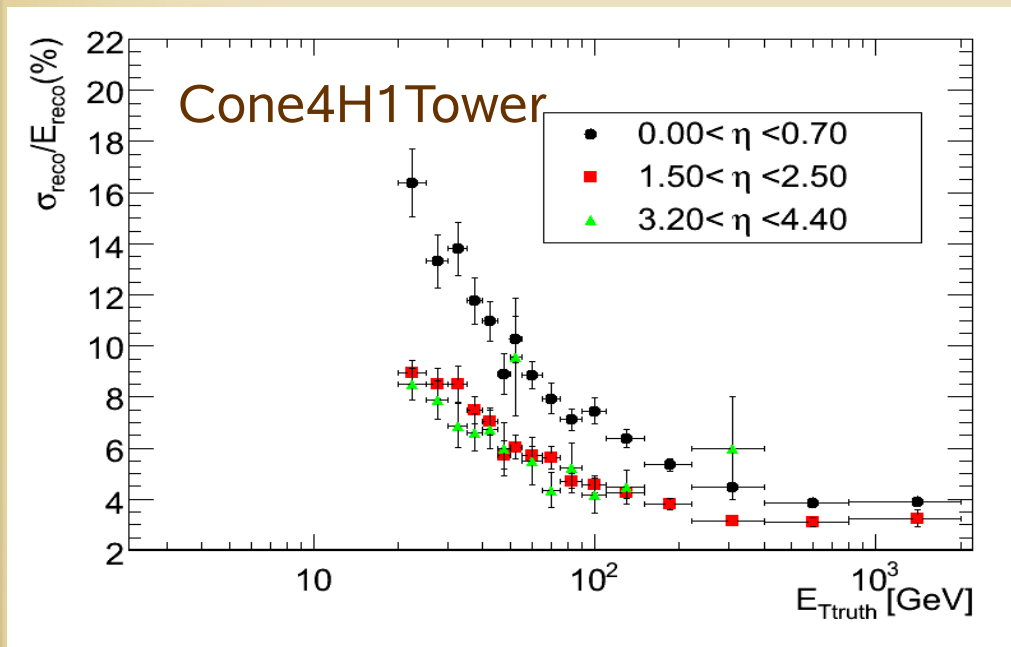
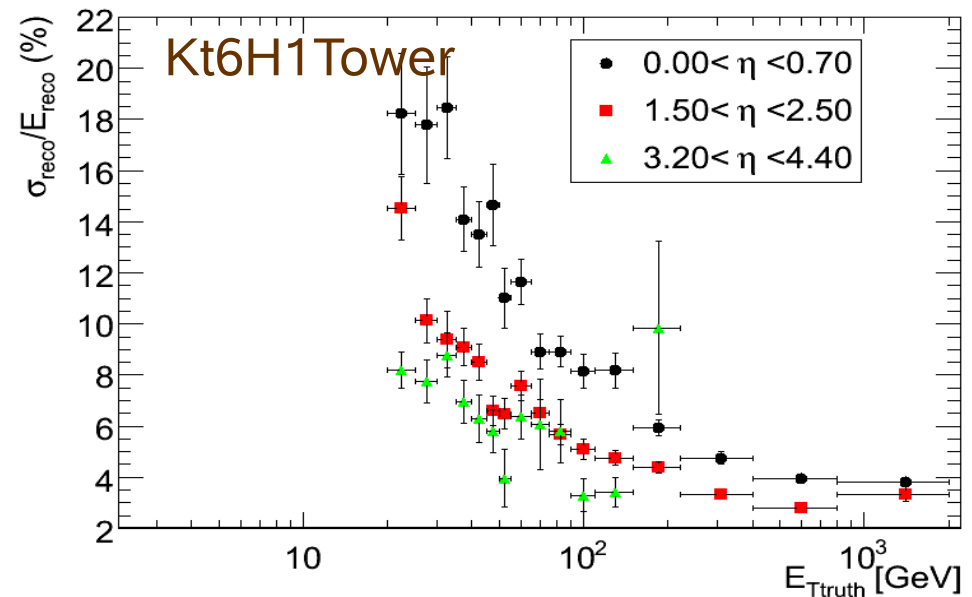
Uniformity over Pseudorapidity

- Uniformity also **very good** on all the pseudorapidity range
- Again some 5% deviation for Kt6 at low energy in the central region

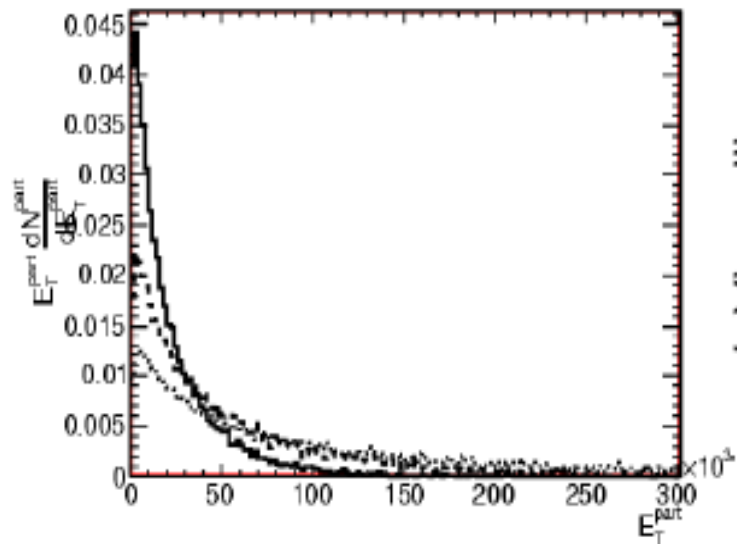
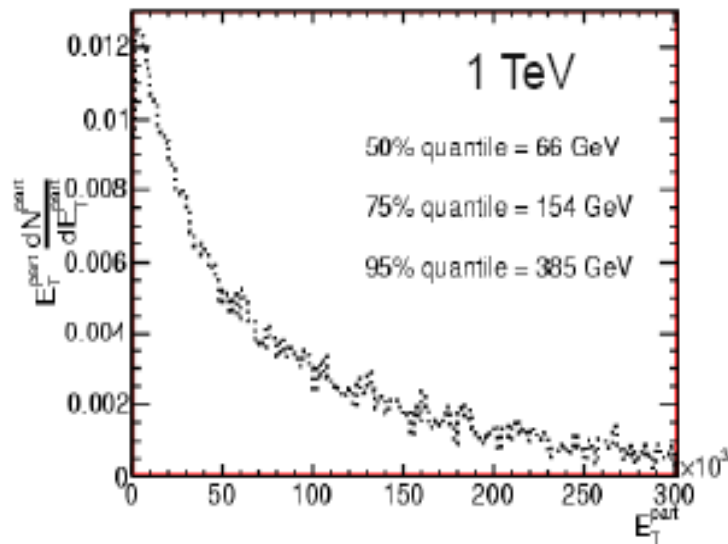
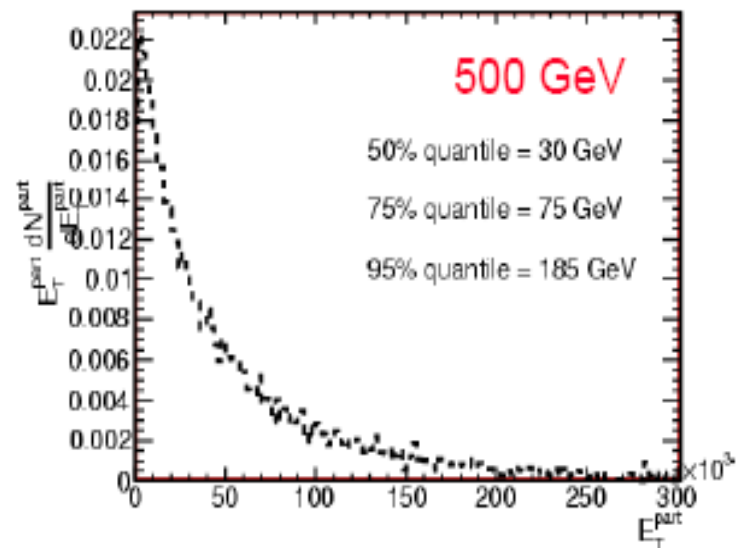
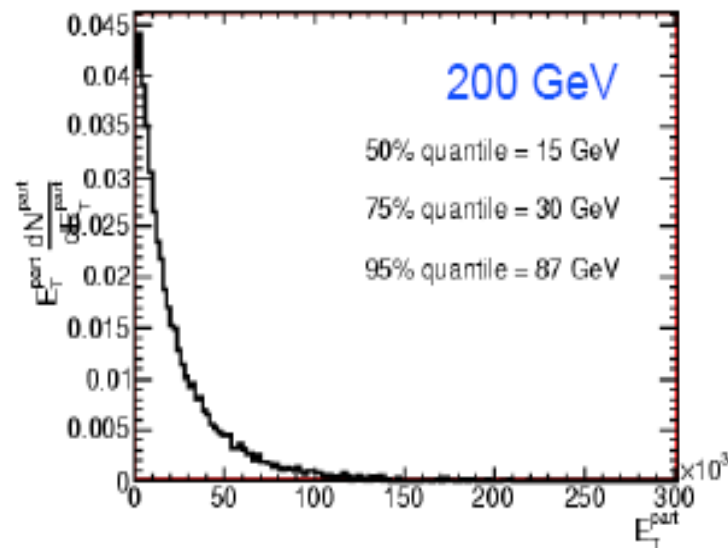


Resolution

- The plot is $\sigma(E_{\text{rec}})/E_{\text{rec}}$ Vs E_T (need to be fixed in JetPerformance)
- Resolution is a little bit worse in K_T (known)



Jet Constituents



I. Viverelli

Getting to TeV-scale jets

- Photon-jet balancing tests the JES to 200-250 GeV in early running.
- A 500 GeV jet has only ~20% of its energy in particles not probed by γ -jet balancing at 250 GeV. That number increases to ~50% at 1 TeV.
- We need a multi-stage process
 - Balance low multiplicity jets (a few high p_T particles) with inclusive jets of the same energy (200 GeV)
 - Balance γ 's against jets at 200 GeV.
 - Infer what the extrapolation uncertainty to 1 TeV is. (Looks to be around 15% or 20% of the energy is not directly verified to be calibrated)
 - We hope to test this process by looking at 100 GeV jets, and checking with 200 GeV jets (where we have data)

Reconstruction Algorithms

SEEDED CONE ALGORITHM

- Seed: $E_T > 1$ GeV in ATLAS
- Cone size \rightarrow ATLAS: $\Delta R = 0.7 - 0.4$
- Compute the centroid, iterate until a stable axis is found
- Split & Merge: 50% of the more energetic jets
- The resulting final jet has a (quite) precise geometrical shape

K_T ALGORITHM

For each cluster pair ij :

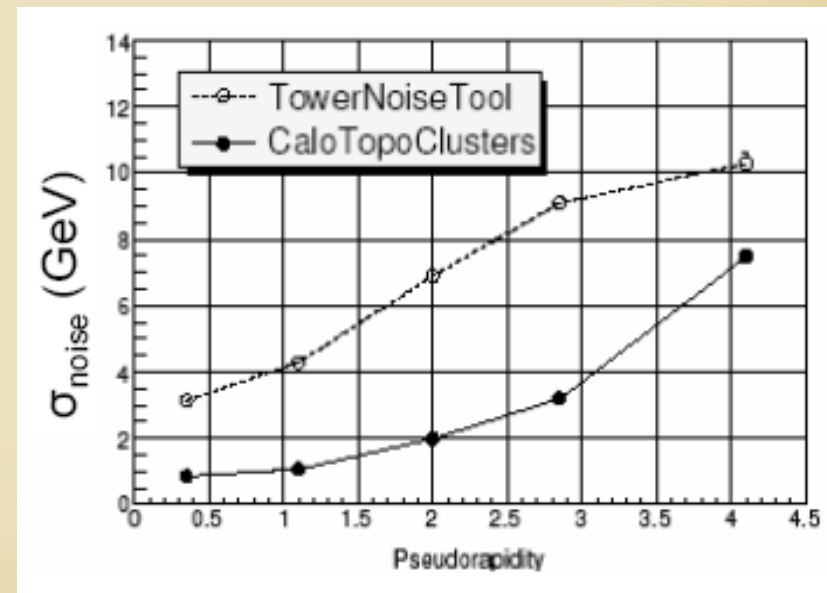
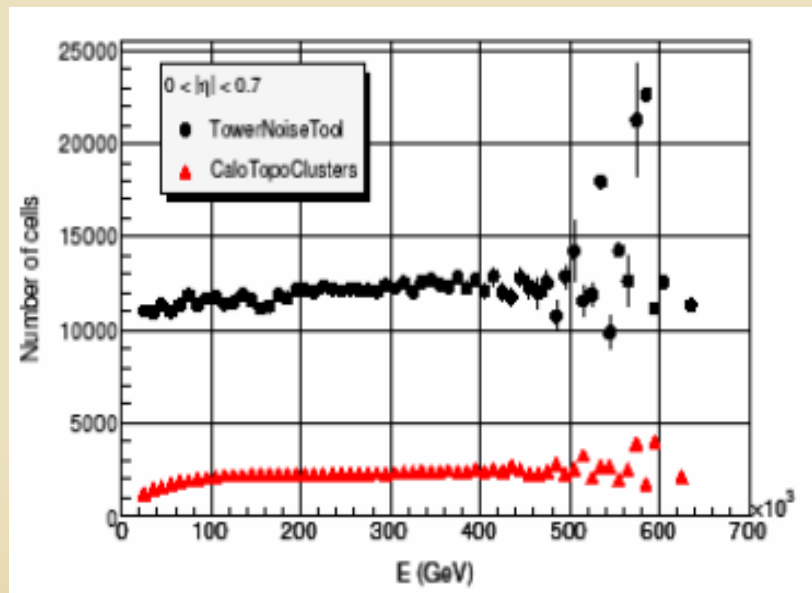
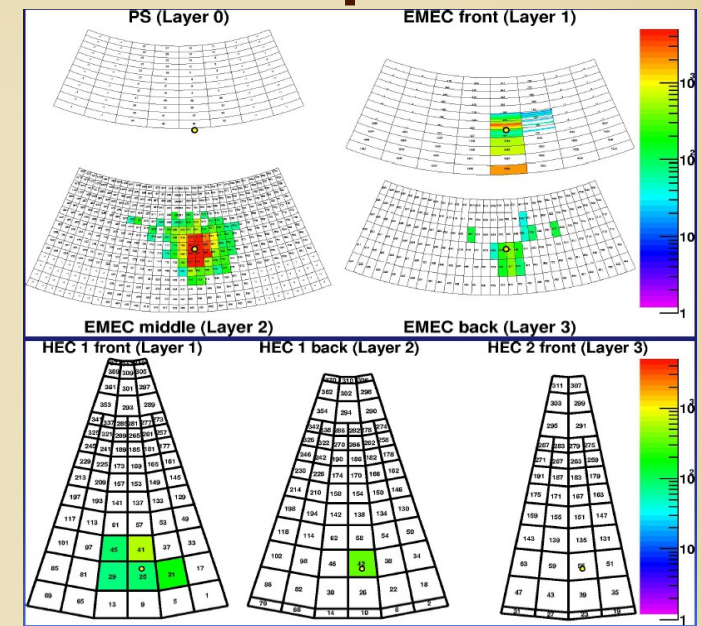
- compute $d = \begin{cases} d_{ij} = k_{T,i}^2 \\ d_{ij} = \min(k_{T,i}^2, k_{T,j}^2) \frac{\Delta R_{ij}^2}{D^2} \end{cases}$
- If $d_{\min} = d_{ij}$ the jet is found
- If $d_{\min} = d_{ij}$ then cluster i and j together
- Iterate
- The jet shape is not defined
- No split and merging applied

$D = 0.6, 0.4$

The most used reconstruction algorithm in ATLAS is the seeded cone with $\Delta R = 0.4$

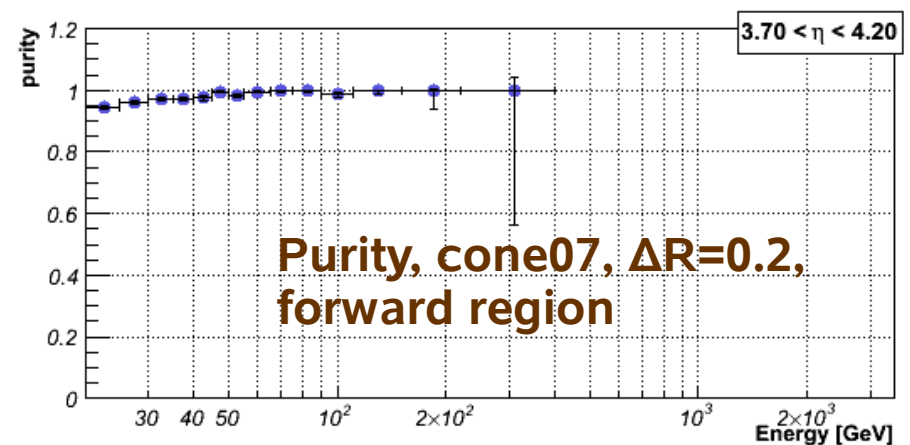
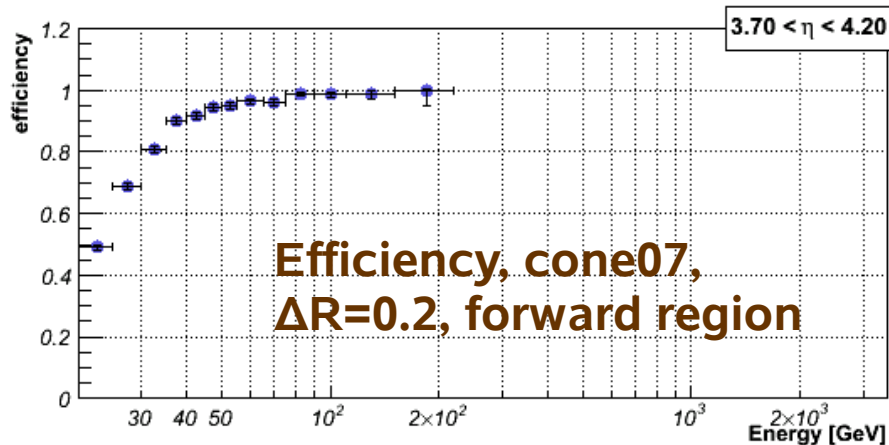
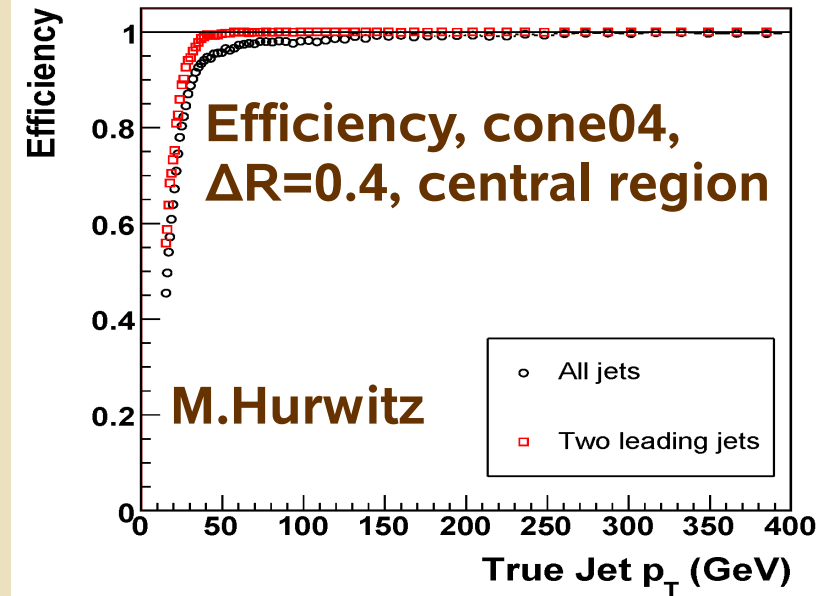
Reconstruction Algorithms Inputs

- Two preclustering algorithm:
 - **Calorimeter towers** ($\Delta\eta \times \Delta\phi = 0.1 \times 0.1$): no noise suppression (unbiased), finer granularity
 - **Topological clusters**: no fixed size, sophisticated noise treatment
- Higher noise level in tower jets (as a consequence of the higher number of cells)



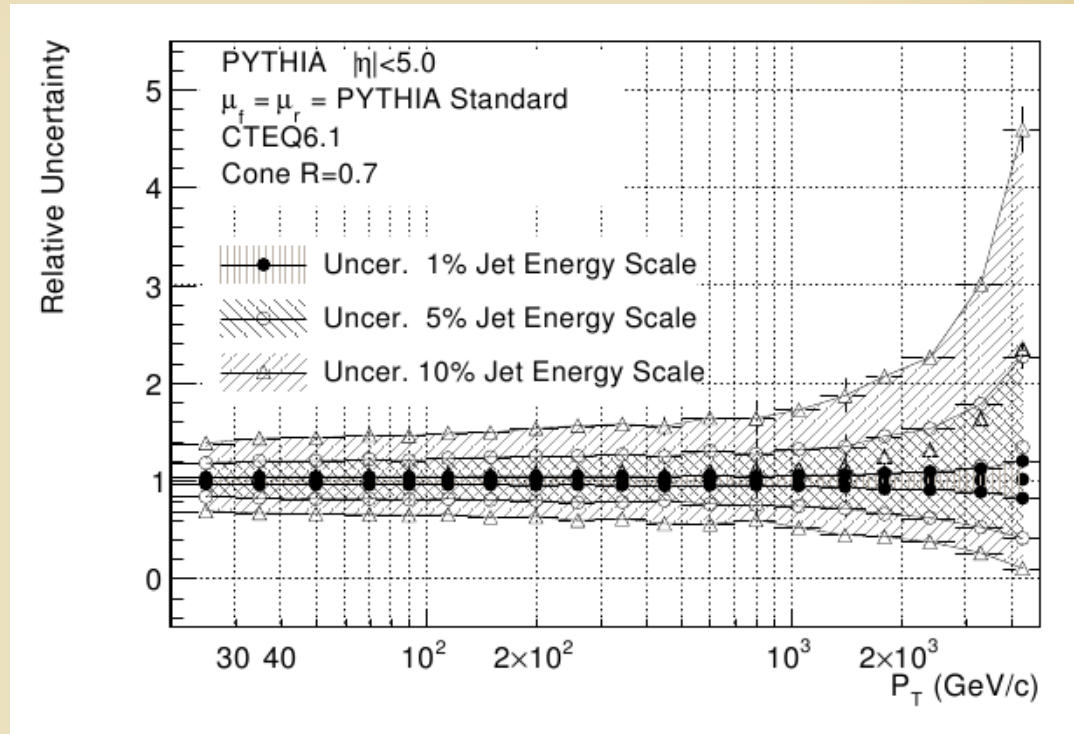
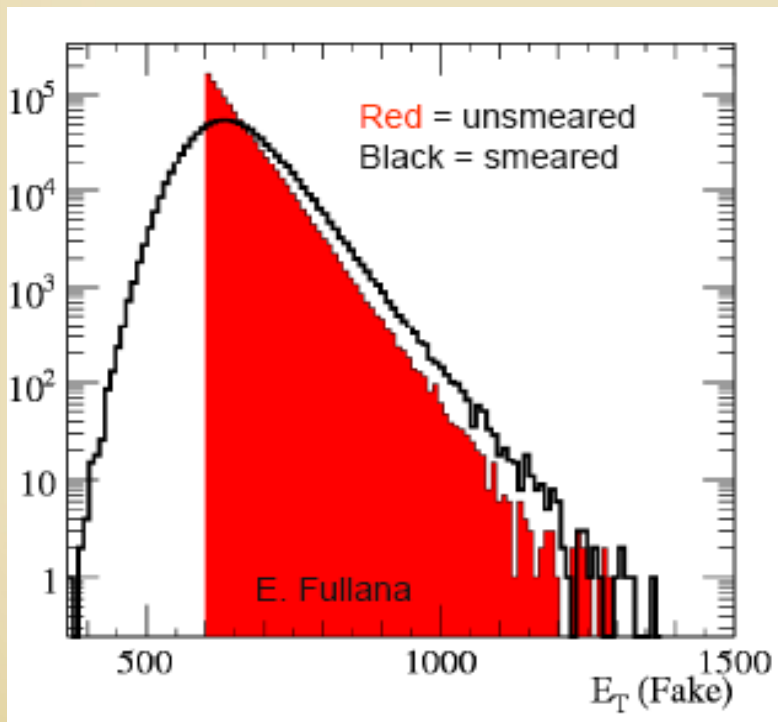
Jet Reconstruction Efficiencies

- Reconstruction efficiency:
 - Define a ΔR_{match} (choice based on the angular resolution)
 - Match reconstructed jets with truth jets if $\Delta R < \Delta R_{\text{match}}$
 - The efficiency is the number of matched reco jets/number of truth jets
 - The purity is the number of matched reco jets/number of reco jets
- Both numbers depend on ΔR_{match}



Inclusive Jet Cross Section (3)

- The uncertainty on the jet energy scale is the dominant experimental uncertainty:
 - 10% error on the energy at 1 TeV means 50% error on the cross section



- Experimental resolution + a steeply falling P_T spectrum \rightarrow bias in the energy measurement