

SDA\_02:

Electroweak Radiative Corrections  
for Higgs Studies  
at LHC and ILC ( $e^-e^-$  option)

Y. Kurihara  
(KEK)

TYL/FKPPL Joint Workshop  
04/June/2013 @ Seoul



# Introduction

- Member List

## FJPPL (TYL) application 2013-2014


*Fiscal year april 1<sup>st</sup> 2013 – March 31<sup>st</sup> 2014*

<b>ID<sup>1</sup>:</b>	<b>Title:Electroweak Radiative Corrections for Higgs studies in LHC and future <math>e^- e^-</math> collider</b>					
<b>Leader</b>	<b>French Group</b>			<b>Japanese Group</b>		
	<b>Name</b>	<b>Title</b>	<b>Lab./Organis.<sup>2</sup></b>	<b>Name</b>	<b>Title</b>	<b>Lab/Organis.<sup>3</sup></b>
<b>Members</b>	Denis Perret-Gallix	Dr.	LAPP/IN2P3	Yoshimasa Kurihara	Dr.	KEK
				Junpei Fujimoto	Dr.	KEK
				P. H. Khiem	Mr.	KEK/Sokendai
				Kiyoshi Kato	Prof.	Kogakuin Univ.

Introduction  
Electron-  
electron Collision  
in ILC

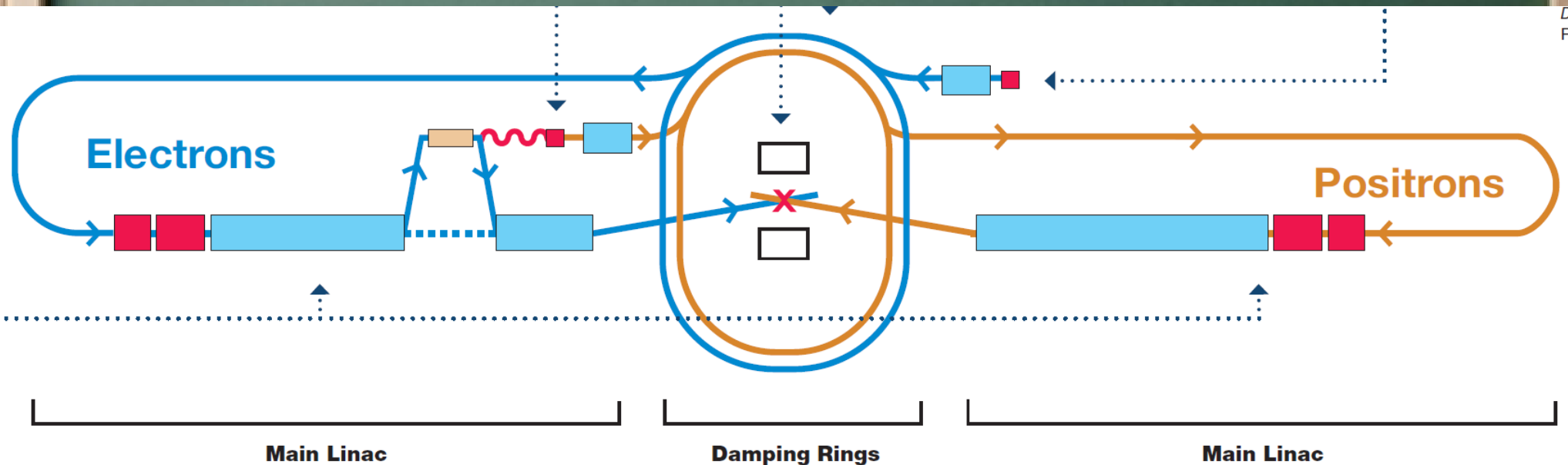


# Introduction

- An  $e^-e^-$  option in ILC?
    - Higgs Studies are possible by the  $e^-e^-$  ILC.
    - Positron source is more **difficult** and more **expensive** than the electron source.
    - At a commissioning period of ILC, do we have to wait a  $e^+$  beam??
    - An  $e^-e^-$  option must be considered **seriously**.
- 

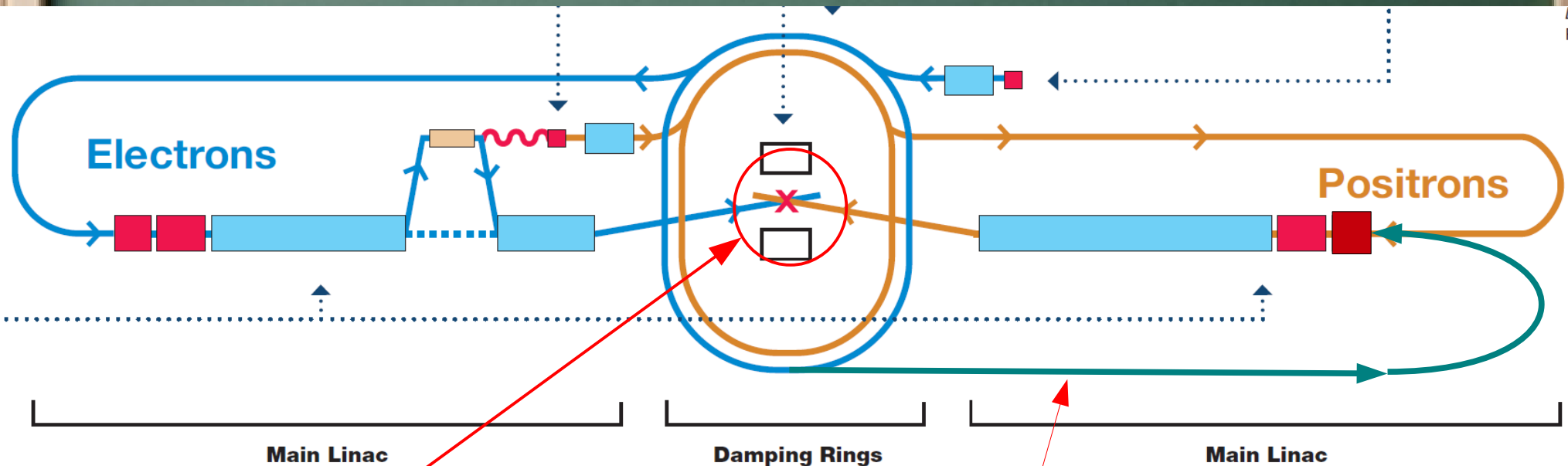
# Introduction

- An  $e^-e^-$  option in ILC



# Introduction

- An  $e^-e^-$  option in ILC

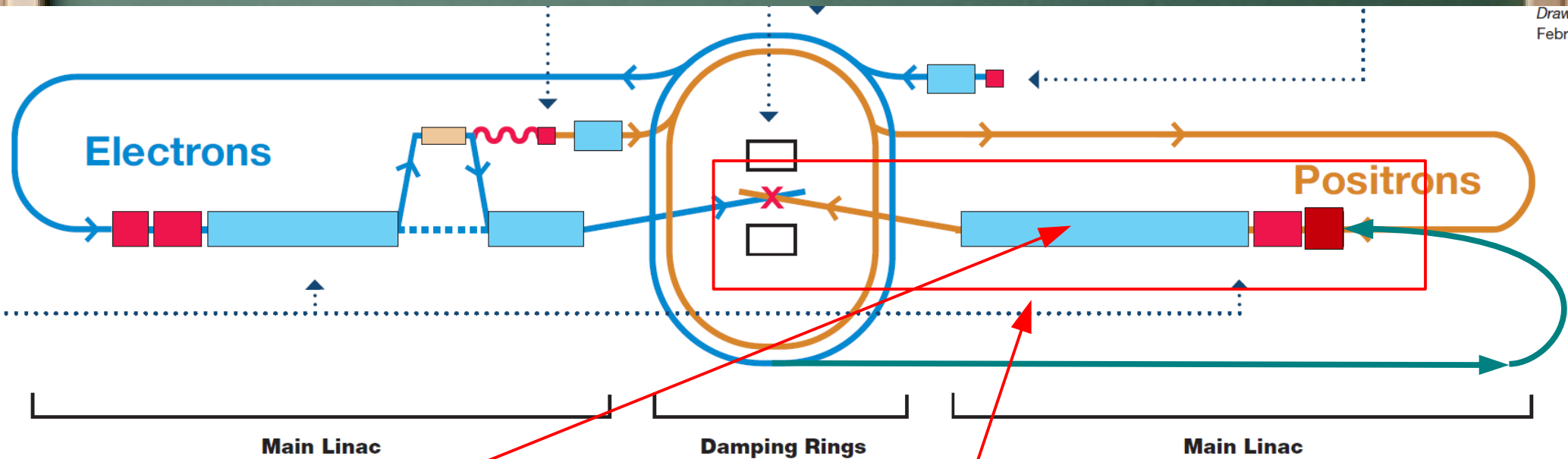


Special Extraction Line

Final focus system (crossing angle) is the same as the  $e^+e^-$  collider  
Detector can be common to the  $e^+e^-$  collider

# Introduction

- An  $e^-e^-$  option in ILC

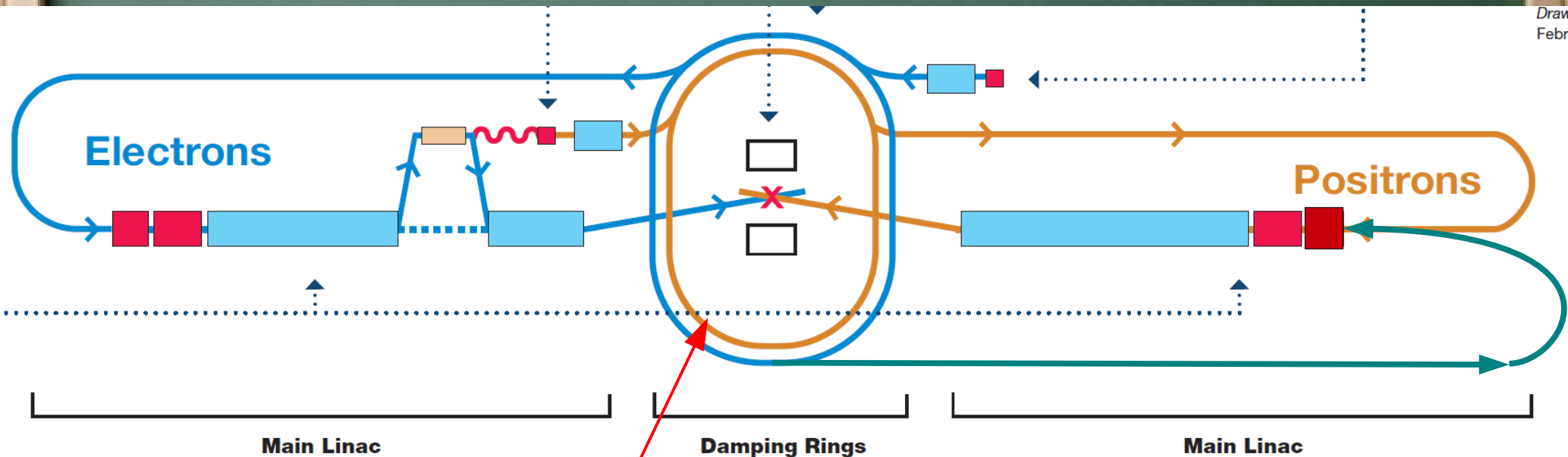


Acceleration Phase Change

Magnet Polarity Change

# Introduction

- An  $e^-e^-$  option in ILC



Expensive positron dumping ring is not necessary

Earlier start of experiment may be possible!



Electron-  
electron Physics  
in ILC



# e<sup>-</sup>e<sup>-</sup> Physics

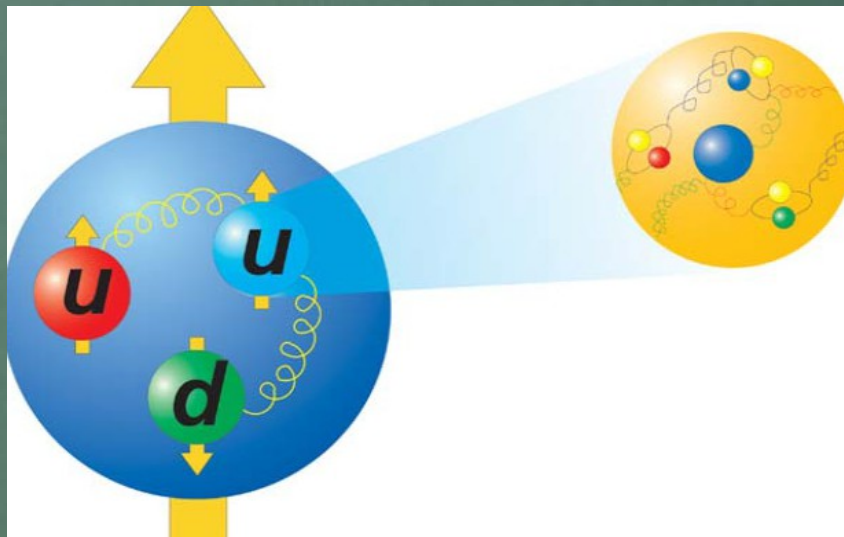
- What kinds of physics can be performed?
  - No e<sup>-</sup>e<sup>-</sup> annihilation of course.



# e<sup>-</sup>e<sup>-</sup> Physics

- What kinds of physics can be performed?
  - No e<sup>-</sup>e<sup>-</sup> annihilation of course.

LHC: Proton-Proton Collider  
Proton beam = {quark, anti-quark, gluon}-beams



<http://www.interactions.org>

# $e^-e^-$ Physics

- What kinds of physics can be performed?
  - No  $e^-e^-$  annihilation of course.

ILC:  $e^-e^-$  collider option

Electron beam = {electron, photon,  $Z$ -boson}-beams

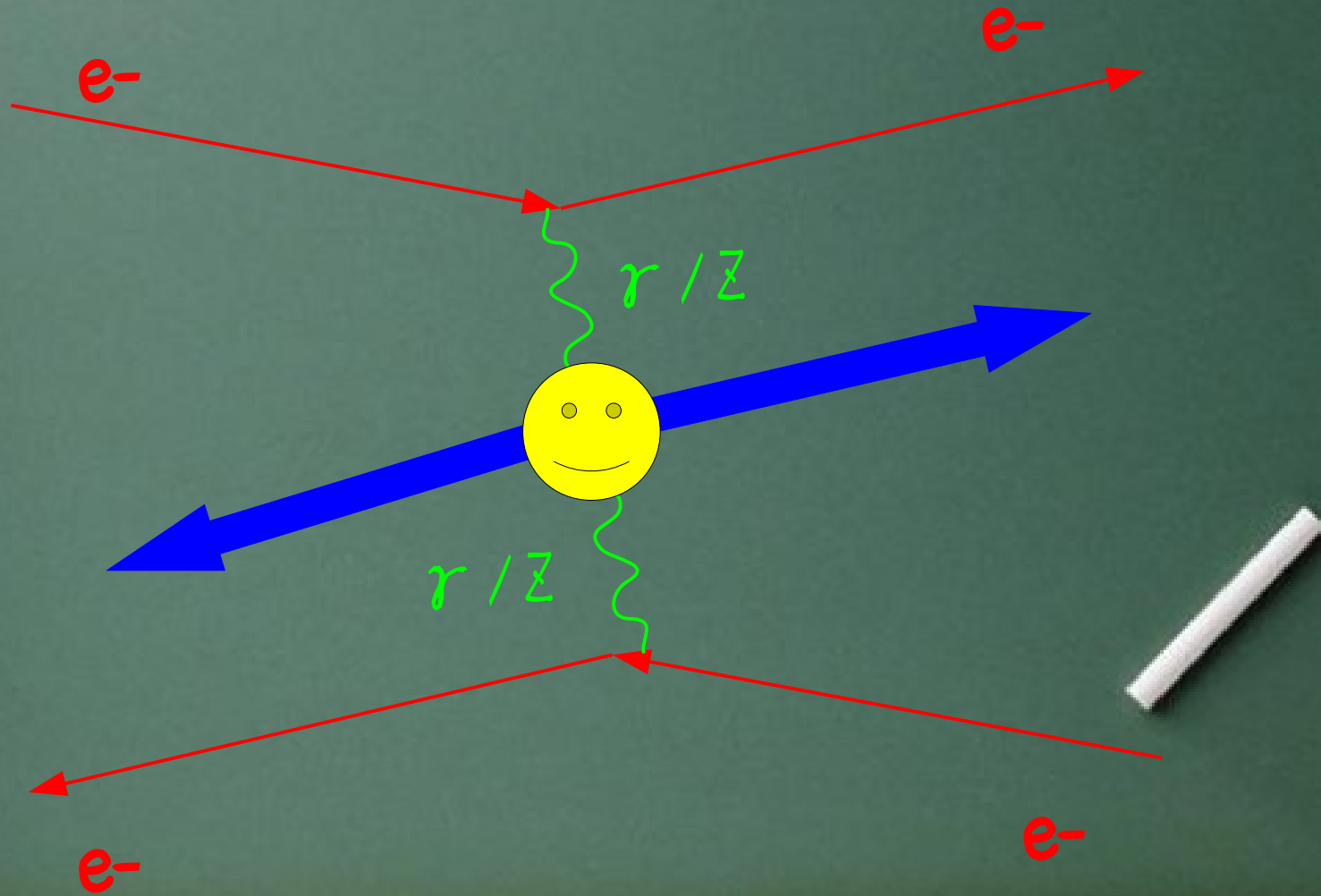
$e^-e^-$  Collider  $\rightarrow e^-$ -photon,  $e^-$ - $Z$ , photon-photon  
 $Z$ - $Z$ , ..., colliders



Photons/ $Z$ s

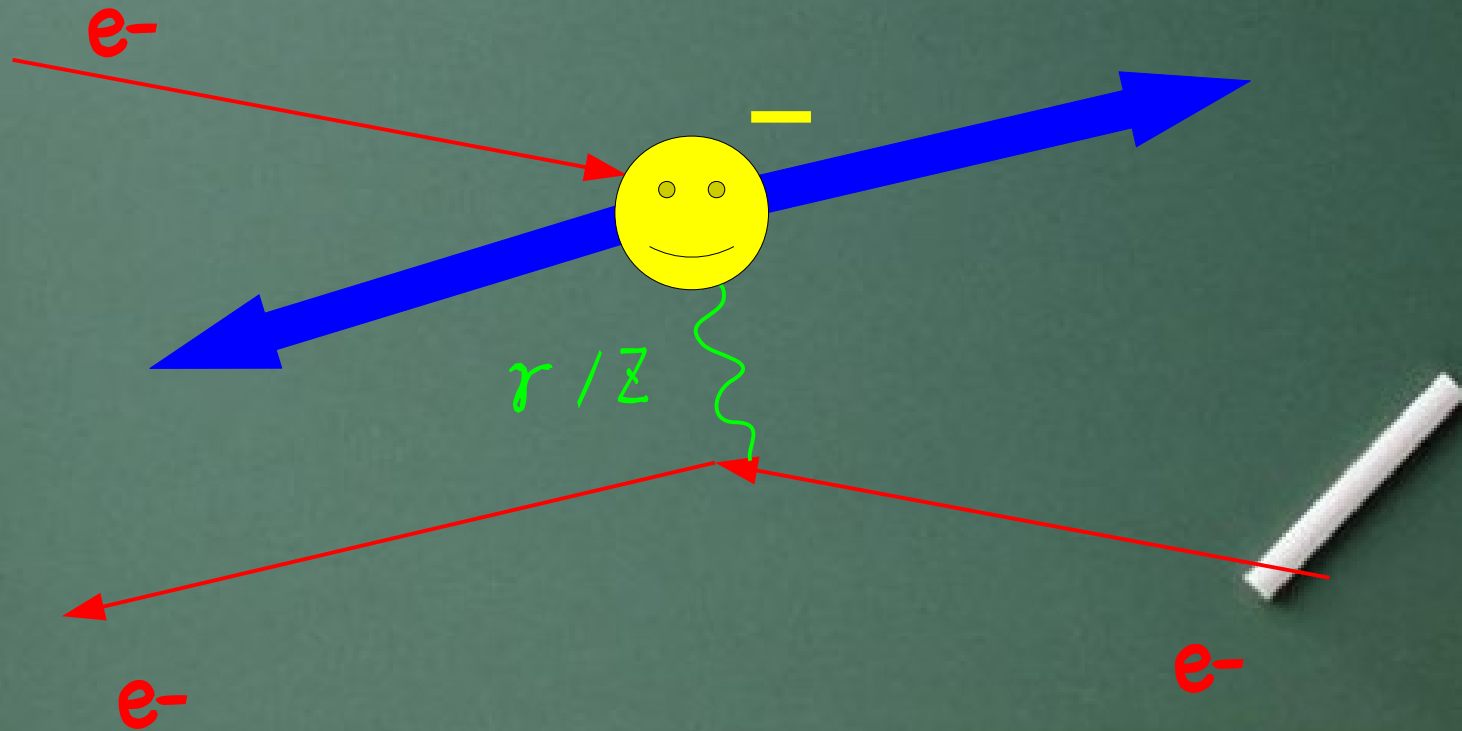
# e<sup>-</sup>e<sup>-</sup> Physics

- What kinds of physics can be performed?



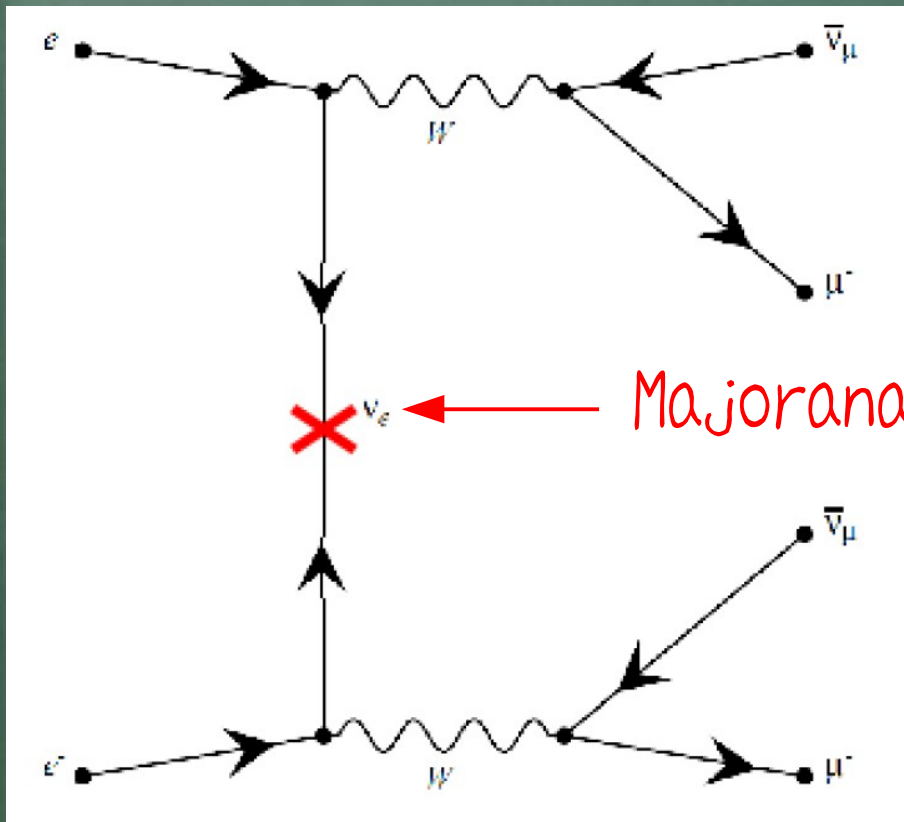
# Introduction

- What kinds of physics can be performed?

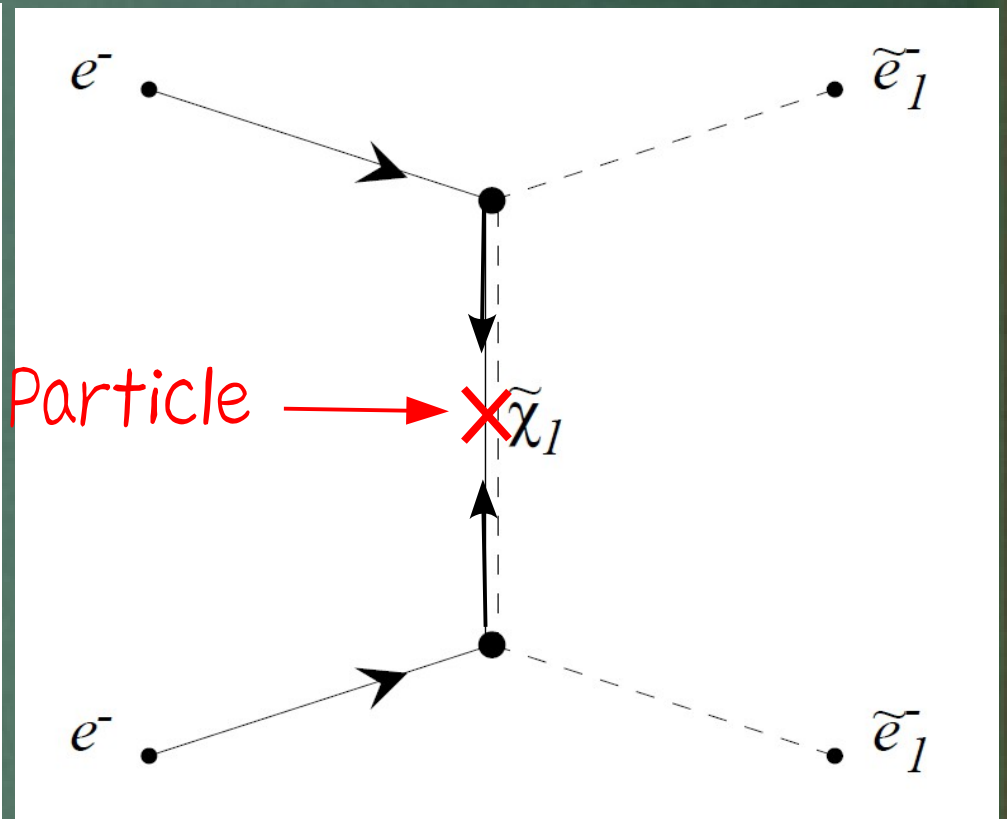


# e-e-Physics

- What kinds of physics can be performed?



Majorana Neutrino Search



s-electron Search

Majorana Particle

# Higgs Physics: New Window to BSM





# BSM Signal Search in Higgs couplings

## Higgs boson signal in the effective model with the full set of dim-6 operators

E. Boos<sup>1,2</sup>, V. Bunichev<sup>2</sup>, M. Dubinin<sup>1,2</sup>, Y. Kurihara<sup>2</sup>

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Japan*

# BSM Signal Search in Higgs couplings

- *scalar-gauge boson sector*

$$O_{\Phi G} = \frac{1}{2}(\Phi^\dagger\Phi - \frac{v^2}{2})G_{\mu\nu}^a G^{a\mu\nu}$$

$$O_{\Phi B} = \frac{1}{2}(\Phi^\dagger\Phi - \frac{v^2}{2})B_{\mu\nu} B^{\mu\nu}$$

$$O_{\Phi W} = \frac{1}{2}(\Phi^\dagger\Phi - \frac{v^2}{2})W_{\mu\nu}^i W^{i\mu\nu}$$

$$O_{\Phi}^{(1)} = (\Phi^\dagger\Phi - \frac{v^2}{2})D_\mu\Phi^\dagger D^\mu\Phi$$

$$O_{\Phi G} = \frac{1}{2}(\Phi^\dagger\Phi - \frac{v^2}{2})G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

$$O_{\Phi B} = \frac{1}{2}(\Phi^\dagger\Phi - \frac{v^2}{2})B_{\mu\nu} \tilde{B}^{\mu\nu}$$

$$O_{\Phi W} = \frac{1}{2}(\Phi^\dagger\Phi - \frac{v^2}{2})W_{\mu\nu}^i \tilde{W}^{i\mu\nu}$$

- *scalar-fermion sector*

$$O_{t\Phi} = (\Phi^\dagger\Phi - \frac{v^2}{2})(\bar{Q}_L\Phi^c t_R)$$

$$O_{b\Phi} = (\Phi^\dagger\Phi - \frac{v^2}{2})(\bar{Q}_L\Phi b_R)$$

$$O_{\tau\Phi} = (\Phi^\dagger\Phi - \frac{v^2}{2})(\bar{L}_L\Phi\tau_R)$$

# BSM Signal Search in Higgs couplings

Effective operators	Triple vertices	Feynman rules
$O_{t\Phi} = (\Phi^\dagger\Phi - \frac{v^2}{2})(-\lambda_t)(\bar{Q}_L\Phi^c t_R)$	$\bar{t} \quad t \quad H$	$-M_t \cdot \frac{v}{\Lambda^2} \cdot C_{t\Phi}$
$O_{b\Phi} = (\Phi^\dagger\Phi - \frac{v^2}{2})(-\lambda_b)(\bar{Q}_L\Phi b_R)$	$\bar{b} \quad b \quad H$	$-M_b \cdot \frac{v}{\Lambda^2} \cdot C_{b\Phi}$
$O_{\tau\Phi} = (\Phi^\dagger\Phi - \frac{v^2}{2})(-\lambda_\tau)(\bar{L}_L\Phi\tau_R)$	$\bar{\tau} \quad \tau \quad H$	$-M_\tau \cdot \frac{v}{\Lambda^2} \cdot C_{\tau\Phi}$
$O_{\Phi G} = \frac{1}{2}(\Phi^\dagger\Phi - \frac{v^2}{2})G_{\mu\nu}^a G^{a\mu\nu}$	$G_\mu \quad G_\nu \quad H$	$-2 \cdot \frac{v}{\Lambda^2} \cdot C_{\Phi G} \cdot (g^{\mu\nu} p_1 p_2 - p_1^\nu p_2^\mu)$
$O_{\Phi B} = \frac{1}{2}(\Phi^\dagger\Phi - \frac{v^2}{2})B_{\mu\nu} B^{\mu\nu}$	$A_\mu \quad A_\nu \quad H$ $A_\mu \quad Z_\nu \quad H$ $Z_\mu \quad Z_\nu \quad H$	$-2 \cdot c_W^2 \cdot \frac{v}{\Lambda^2} \cdot C_{\Phi B} \cdot (g^{\mu\nu} p_1 p_2 - p_1^\nu p_2^\mu)$ $+2 \cdot c_W \cdot s_W \cdot \frac{v}{\Lambda^2} \cdot C_{\Phi B} \cdot (g^{\mu\nu} p_1 p_2 - p_1^\nu p_2^\mu)$ $-2 \cdot s_W^2 \cdot \frac{v}{\Lambda^2} \cdot C_{\Phi B} \cdot (g^{\mu\nu} p_1 p_2 - p_1^\nu p_2^\mu)$
$O_{\Phi W} = \frac{1}{2}(\Phi^\dagger\Phi - \frac{v^2}{2})W_{\mu\nu}^i W^{i\mu\nu}$	$A_\mu \quad A_\nu \quad H$ $A_\mu \quad Z_\nu \quad H$ $Z_\mu \quad Z_\nu \quad H$ $W_\mu^+ \quad W_\nu^- \quad H$	$-2 \cdot s_W^2 \cdot \frac{v}{\Lambda^2} \cdot C_{\Phi W} \cdot (g^{\mu\nu} p_1 p_2 - p_1^\nu p_2^\mu)$ $-2 \cdot c_W \cdot s_W \cdot \frac{v}{\Lambda^2} \cdot C_{\Phi W} \cdot (g^{\mu\nu} p_1 p_2 - p_1^\nu p_2^\mu)$ $-2 \cdot c_W^2 \cdot \frac{v}{\Lambda^2} \cdot C_{\Phi W} \cdot (g^{\mu\nu} p_1 p_2 - p_1^\nu p_2^\mu)$ $-2 \cdot \frac{v}{\Lambda^2} \cdot C_{\Phi W} \cdot (g^{\mu\nu} p_1 p_2 - p_1^\nu p_2^\mu)$
$O_\Phi^{(1)} = (\Phi^\dagger\Phi - \frac{v^2}{2})D_\mu\Phi^\dagger D^\mu\Phi$	$W_\mu^+ \quad W_\nu^- \quad H$ $Z_\mu \quad Z_\nu \quad H$	$M_W^2 \cdot \frac{v}{\Lambda^2} \cdot C_\Phi^{(1)} \cdot g^{\mu\nu}$ $M_Z^2 \cdot \frac{v}{\Lambda^2} \cdot C_\Phi^{(1)} \cdot g^{\mu\nu}$

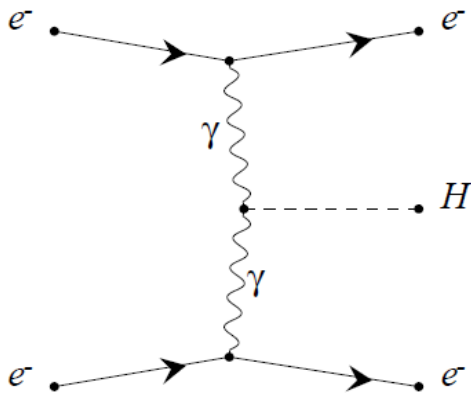
# BSM Signal Search in Higgs couplings

Triple vertices	Feynman rules
$\bar{t} \quad t \quad H$	$-\frac{M_t}{v} \cdot c$
$\bar{b} \quad b \quad H$	$-\frac{M_b}{v} \cdot c$
$\bar{\tau} \quad \tau \quad H$	$-\frac{M_\tau}{v} \cdot c$
$G_\mu \quad G_\nu \quad H$	$-\frac{2}{v} \cdot \frac{\alpha_s}{6\pi} \cdot c_G \cdot (g^{\mu\nu} p_1 p_2 - p_1^\nu p_2^\mu)$
$A_\mu \quad A_\nu \quad H$	$-\frac{2}{v} \cdot \frac{4\alpha}{9\pi} \cdot c_\gamma \cdot (g^{\mu\nu} p_1 p_2 - p_1^\nu p_2^\mu)$
$A_\mu \quad Z_\nu \quad H$	$+2 \cdot c_W \cdot s_W \cdot (C_{\Phi B} - C_{\Phi W}) \cdot \frac{v}{\Lambda^2} (g^{\mu\nu} p_1 p_2 - p_1^\nu p_2^\mu)$
$Z_\mu \quad Z_\nu \quad H$	$+\frac{2}{v} \cdot [M_Z^2 \cdot a \cdot g^{\mu\nu} - a_Z \cdot (g^{\mu\nu} p_1 p_2 - p_1^\nu p_2^\mu)]$
$W_\mu^+ \quad W_\nu^- \quad H$	$+\frac{2}{v} \cdot [M_W^2 \cdot a \cdot g^{\mu\nu} - a_W \cdot (g^{\mu\nu} p_1 p_2 - p_1^\nu p_2^\mu)]$

Above couplings are implemented in GRACE

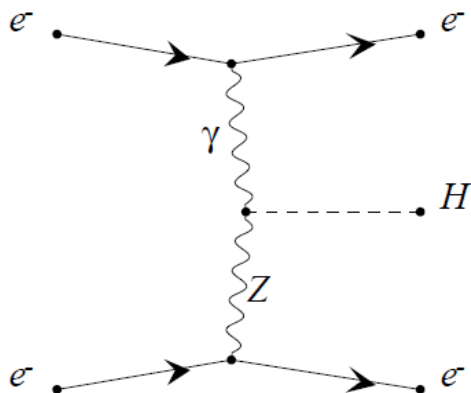
# BSM Signal Search in Higgs couplings

Graph 16

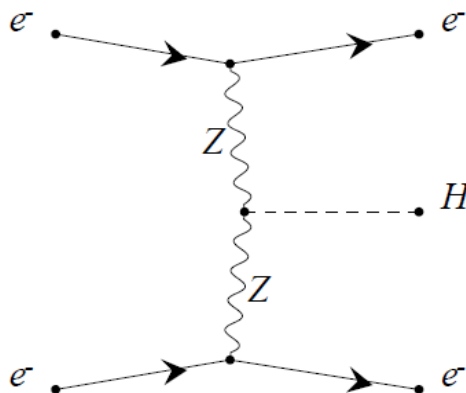


Generated by GRACE

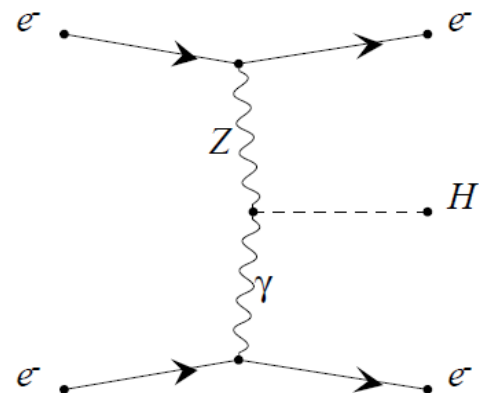
Graph 17



Graph 18



Graph 19



# BSM Signal Search in Higgs couplings

LHC Experiment  
analysis

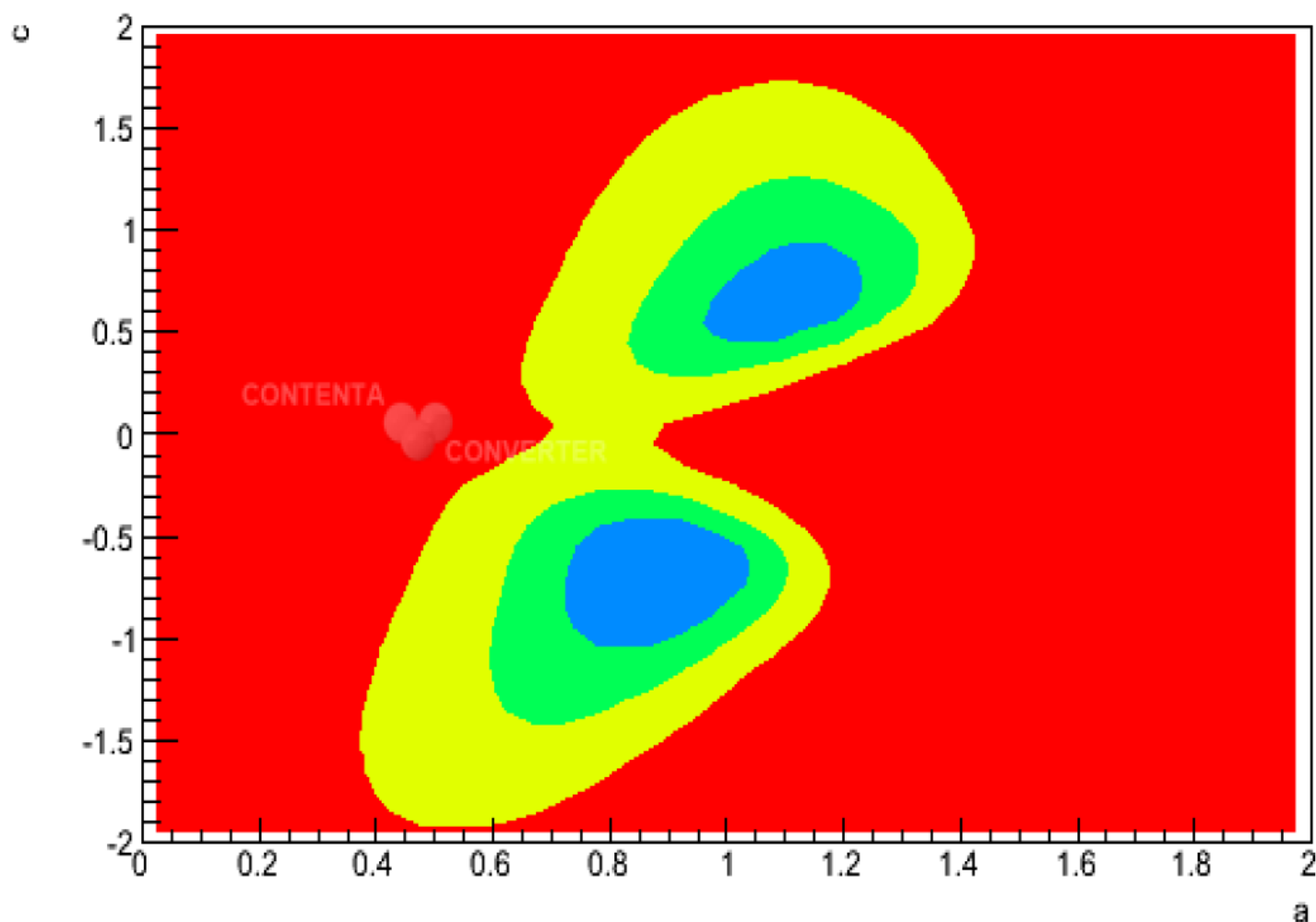
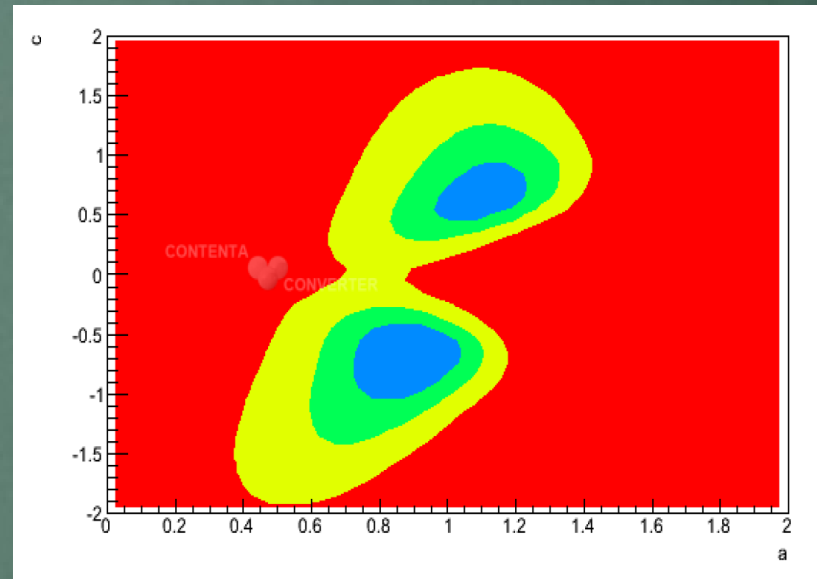


Figure 3: (a) - global  $\chi^2$  fit in the  $(a, c)$  plane calculated with Higgs boson width for all two-particle,  $WW^*$  and  $ZZ^*$  decay channels within the production  $\times$  decay approximation, (b) - global  $\chi^2$  fit in the  $(a, c)$  plane from [9]

# BSM Signal Search in Higgs couplings



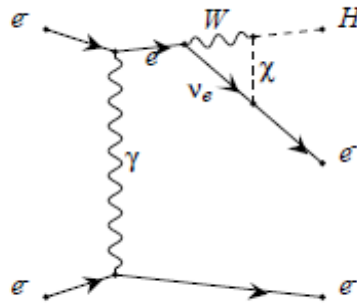
LHC Experiment  
analysis

???  
in ILC ( $e^+e^-e^-e^-$ )

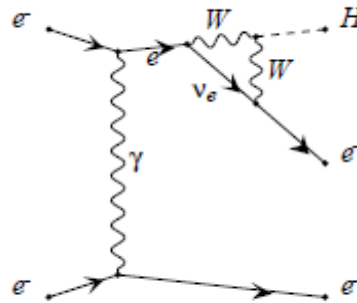


# SM Higher Corrections

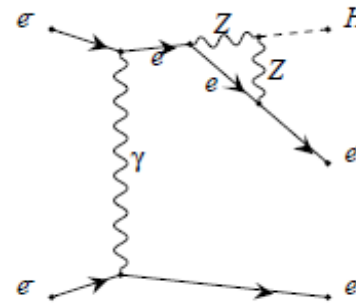
Graph 447



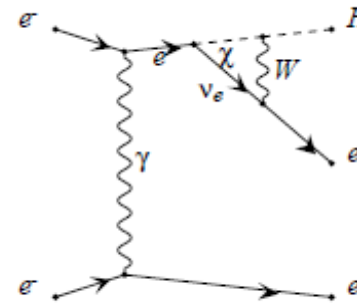
Graph 448



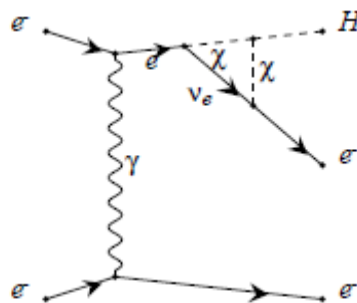
Graph 449



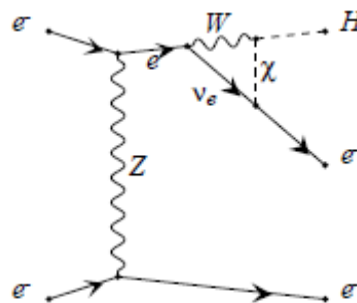
Graph 450



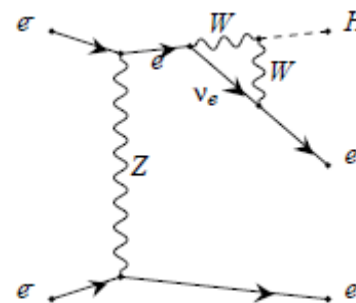
Graph 451



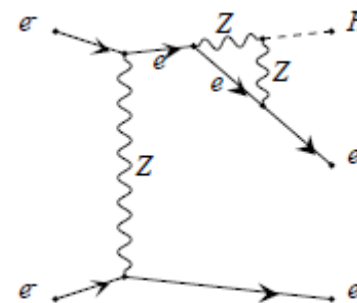
Graph 452



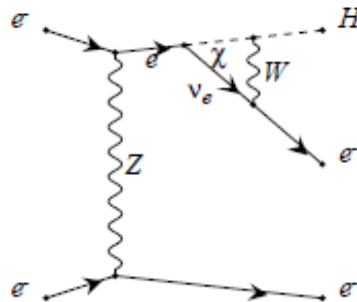
Graph 453



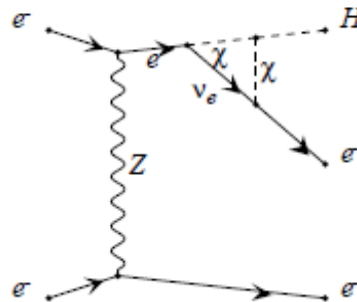
Graph 454



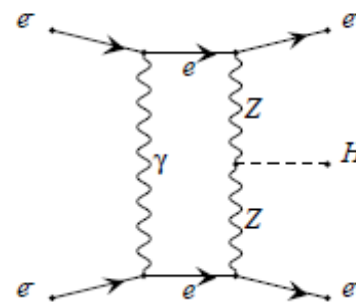
Graph 455



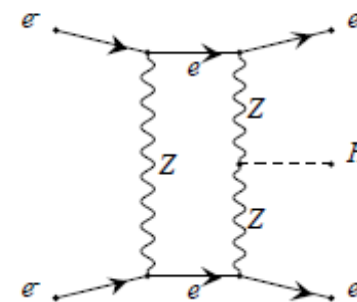
Graph 456



Graph 457



Graph 458





# SM Higher Corrections

## GRACE-Loop system

**GRACE-Loop is a generic automated program for calculating High Energy Physics process <sup>3</sup>.**

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- *All Feynman diagrams for a given process at fixing order of perturbation theory.*
- *A FORM or REDUCE code.*
- *A Fortran code generated for amplitude calculations.*
- *Kinematic library.*
- *The multi-dimensional integration by BASES.*
- *Event generation by SPRING.*

**P.H. Kiem**

SOKENDAI Univ. and KEK.

*JPS meeting Mar. 2013 @ Hiroshima*

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<sup>3</sup>Phys. Rept. 430 (2006) 117

# SM Higher Corrections

- Internal Consistency Check

	$2\text{Re}(T*L)$
$C_{uv} = \text{NLG} = 0, M_{\text{photon}} = 10^{-19}$	$-8.48001506245497E-003$
$C_{uv} = 1000$	$-8.48001506533981E-003$
$\text{NLG} = (10, 2030, 40, 50)$	$-8.48001504415896E-003$
$\text{IR} = 10^{-17}$	$-8.48001506378560E-003$

# SM Higher Corrections

- Result of full  $O(\alpha)$  Correction

	Cross Section(pb)
Tree	7.659E-4
Soft	4.823E-3
Loop	-6.353E-3
Tree+Loop+soft	-7.639E-4
Hard	1.680E-3
Total	9.158E-4
1-Tree/Total	16%

Photon mass  
 $= 10^{-19}$  GeV

$\sqrt{s}=250$  GeV,  $M_H=126$  GeV, No Cut.

Summary



# Summary

- Higgs Physics @ LHC and  $e^-e^-$  ILC
    - General dim-6 operators in Higgs sector.
    - Effective vertices in GRACE System.
    - What can be achieved in LHC and ILC??
  - Precise prediction with full electroweak  $O(\alpha)$  correction
    - New Physics = |Measurements - SM predictions|
    - GRACE/Loop system
    - Precise study is necessary!
  - An  $e^-e^-$  option of ILC is interesting!!
- 