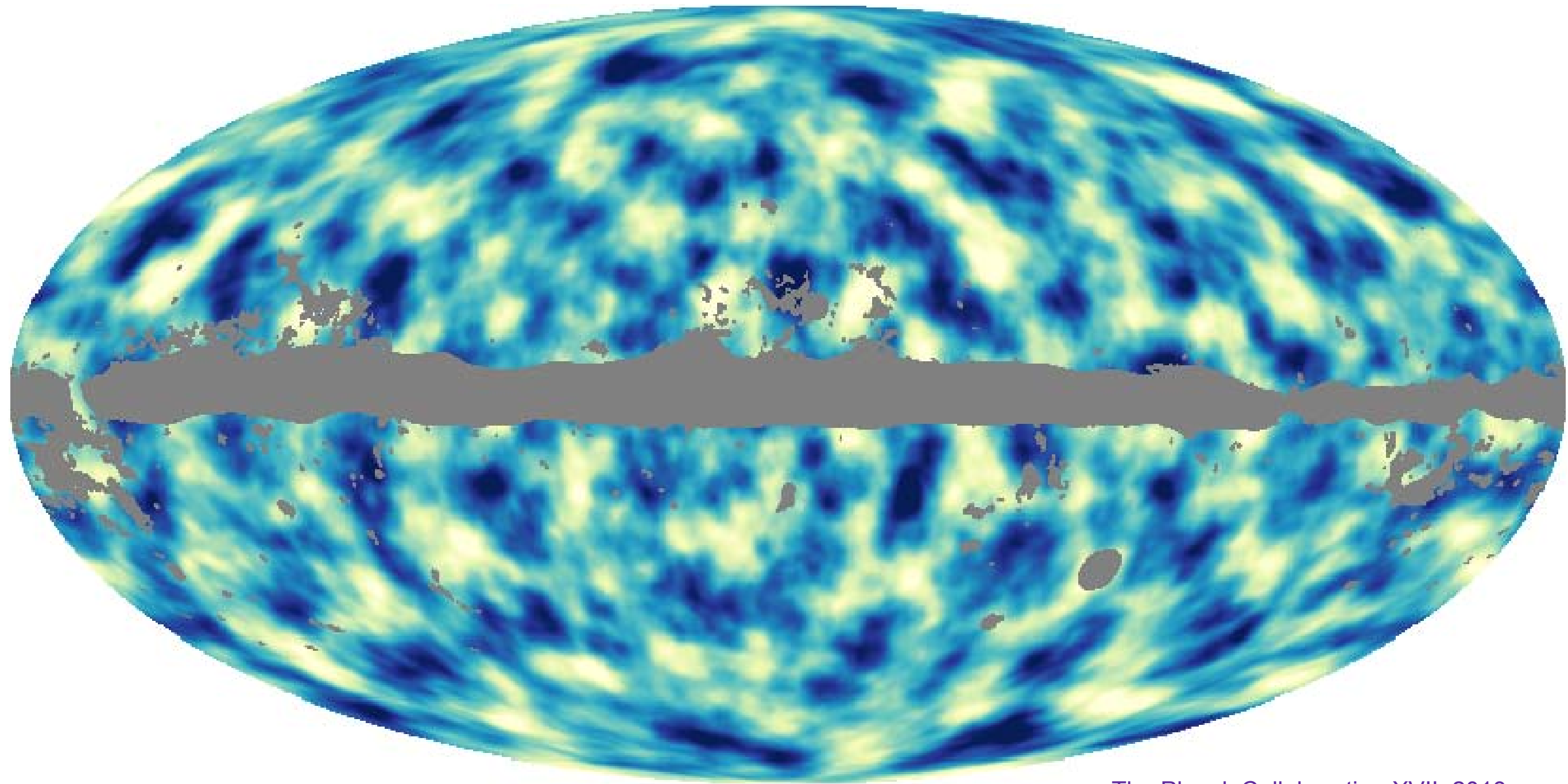

The large-scale structure of the Universe as seen by Planck

Results from Planck 2013 Results. XVII

Aurélien Benoit-Lévy
University College London

The matter in the Universe as seen by Planck

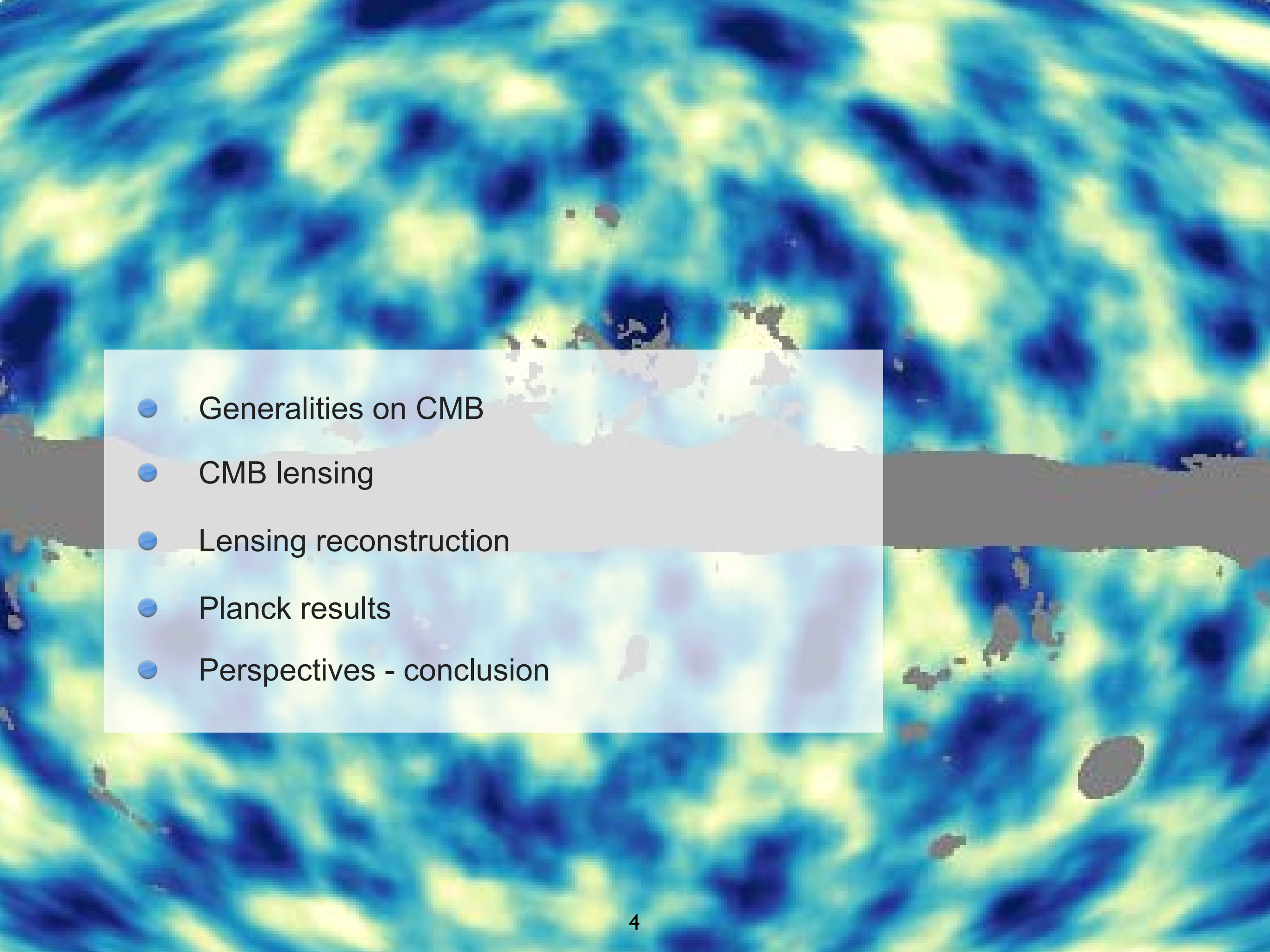


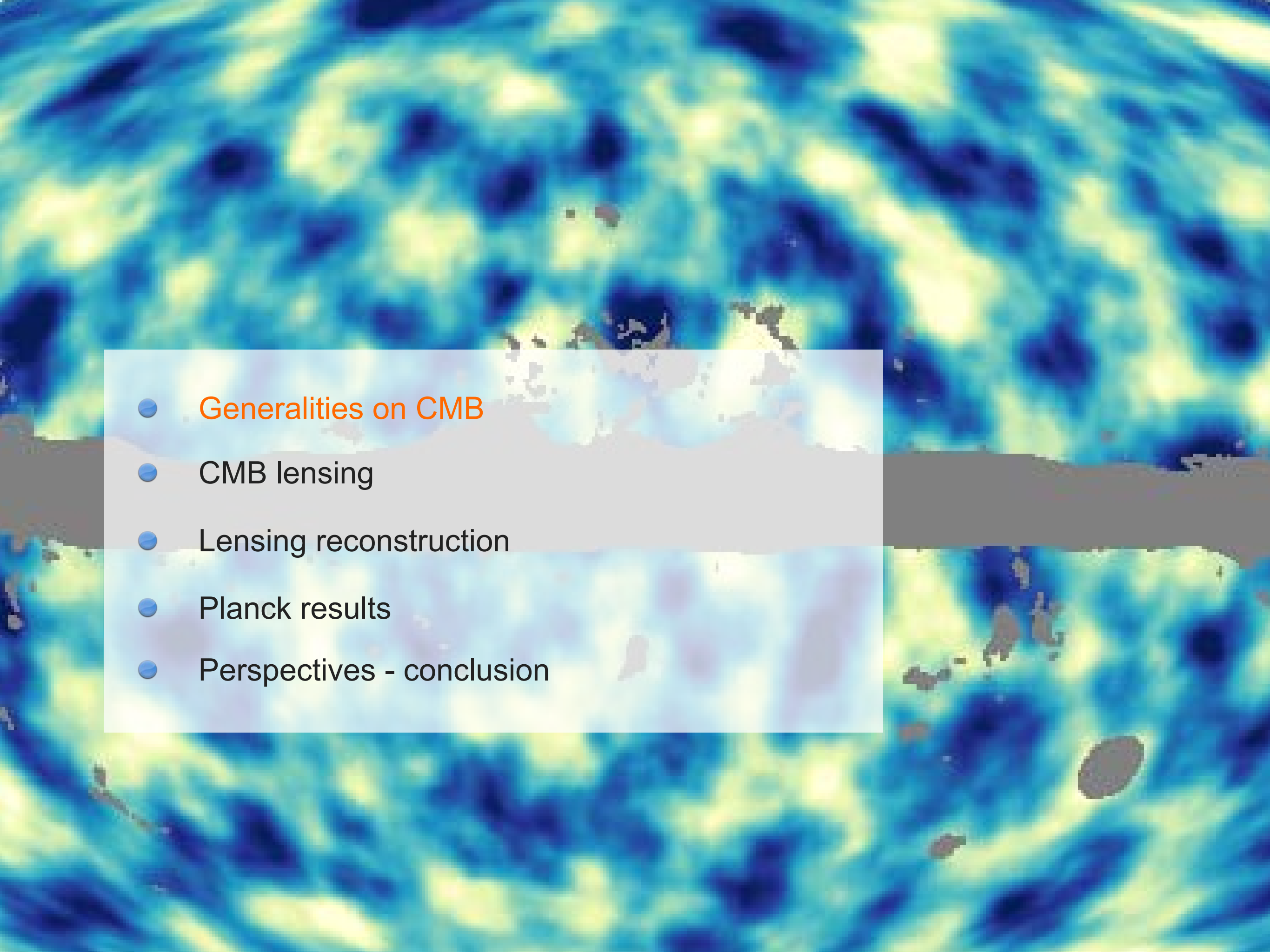
The Planck Collaboration XVII, 2013

The scientific results that we present today are a product of the Planck Collaboration, including individuals from more than 100 scientific institutes in Europe, the USA and Canada

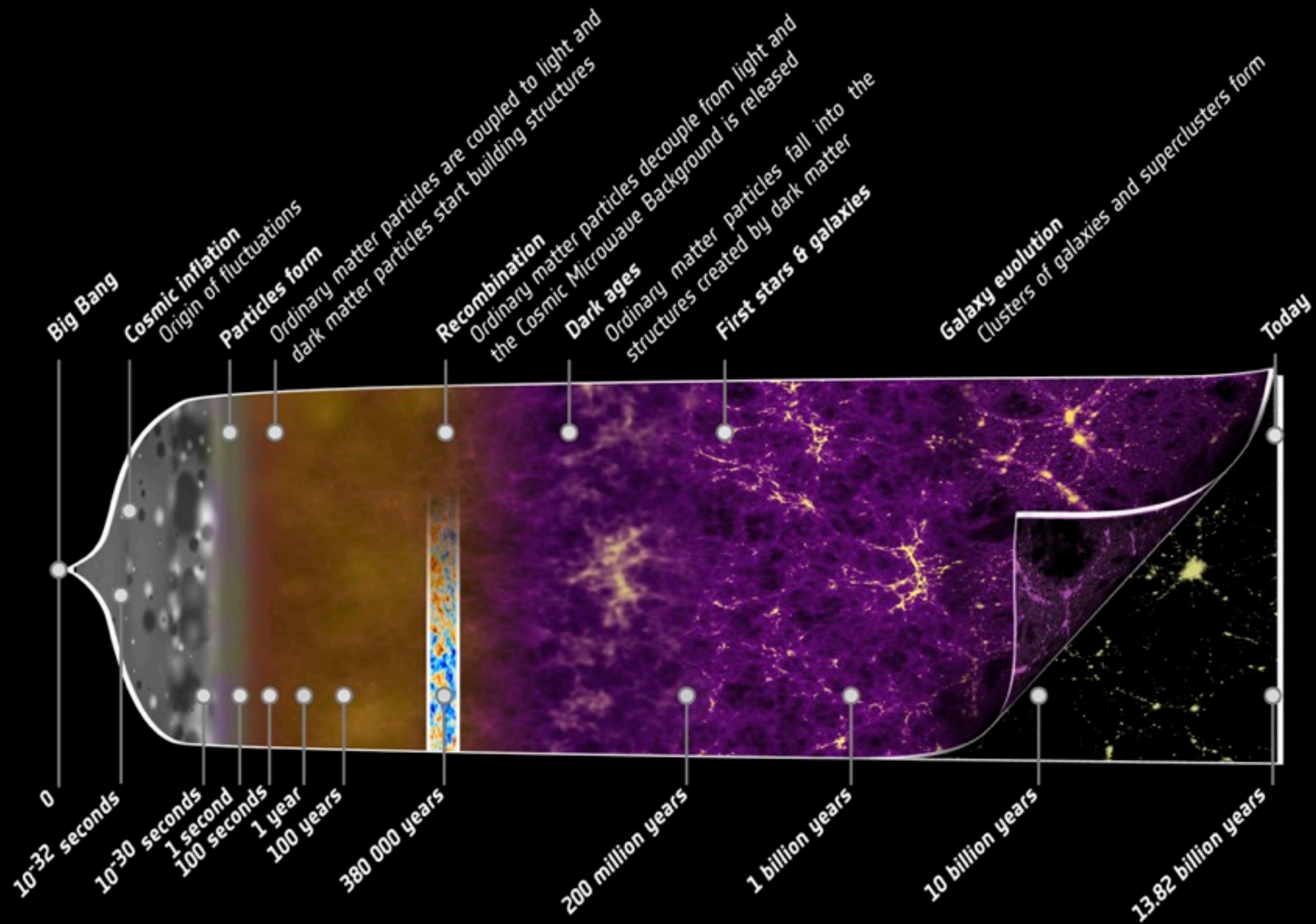


Planck is a project of the European Space Agency, with instruments provided by two scientific Consortia funded by ESA member states (in particular the lead countries: France and Italy) with contributions from NASA (USA), and telescope reflectors provided in a collaboration between ESA and a scientific Consortium led and funded by Denmark.

- 
- The background of the slide is a full-page image of a Cosmic Microwave Background (CMB) fluctuation map. It shows a complex pattern of temperature variations across the sky, with colors ranging from dark blue (cooler) to yellow and white (warmer). The pattern consists of a dense network of filaments and voids, representing the large-scale structure of the universe as it was in the early stages.
- Generalities on CMB
 - CMB lensing
 - Lensing reconstruction
 - Planck results
 - Perspectives - conclusion

- 
- The background of the slide is a full-frame image of the Cosmic Microwave Background (CMB) fluctuation map. It displays a complex pattern of temperature variations across the sky, with colors ranging from deep blue (cooler) to bright yellow and white (warmer). The pattern shows large-scale structures and smaller-scale fluctuations, characteristic of the early universe's density distribution.
- Generalities on CMB
 - CMB lensing
 - Lensing reconstruction
 - Planck results
 - Perspectives - conclusion

A (very) schematic history of our Universe



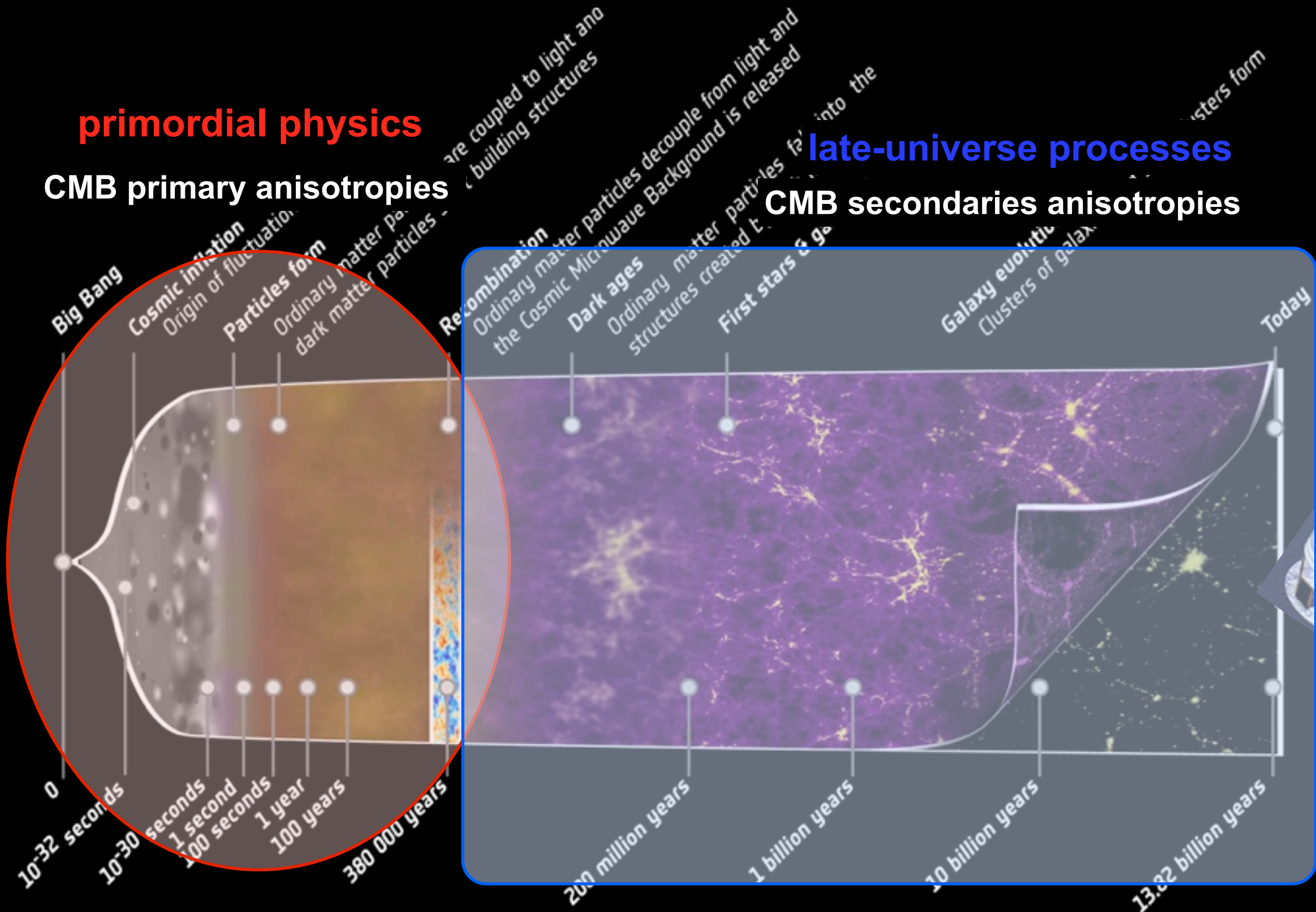
CMB: central observation in cosmology

primordial physics

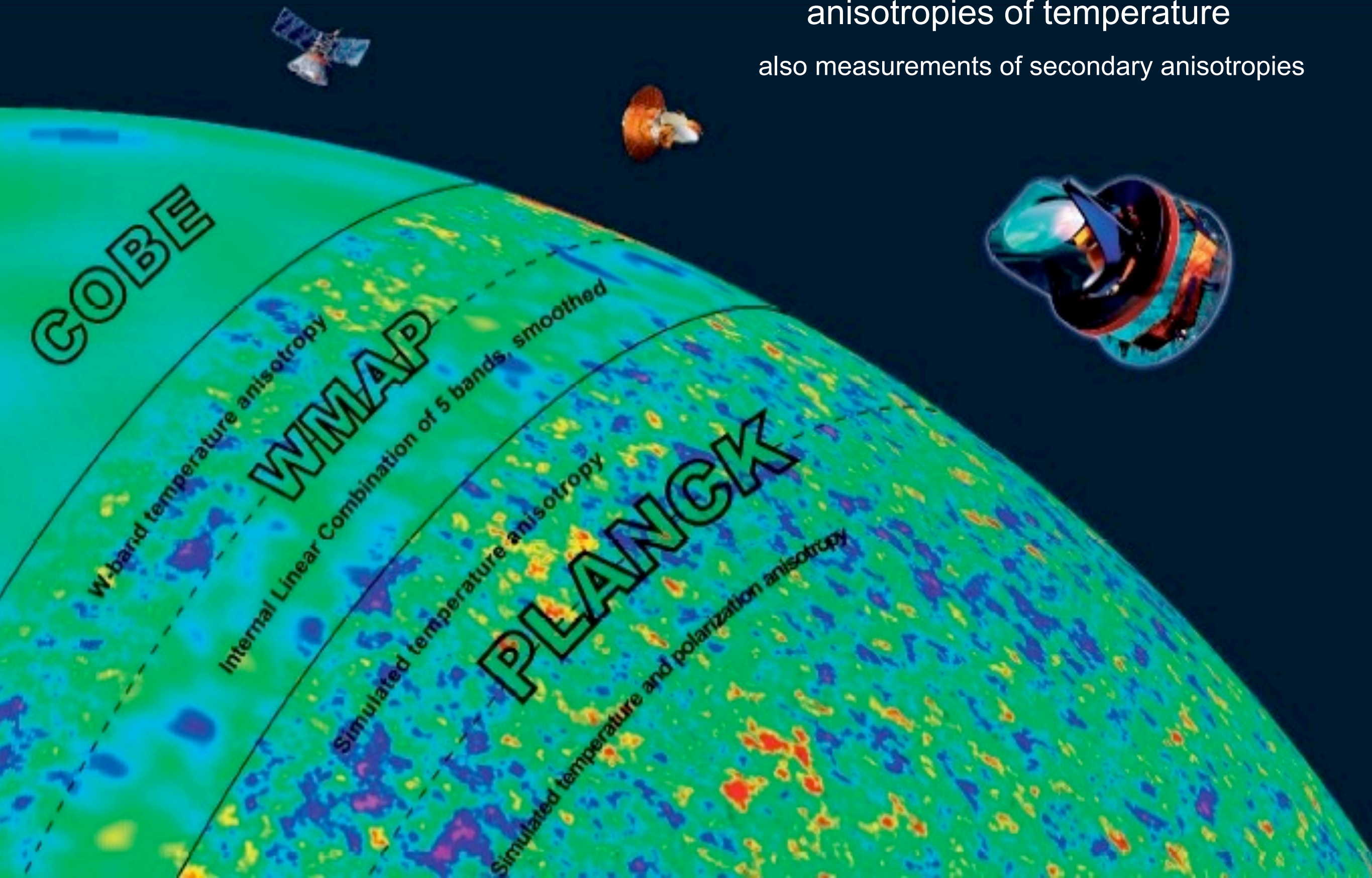
CMB primary anisotropies

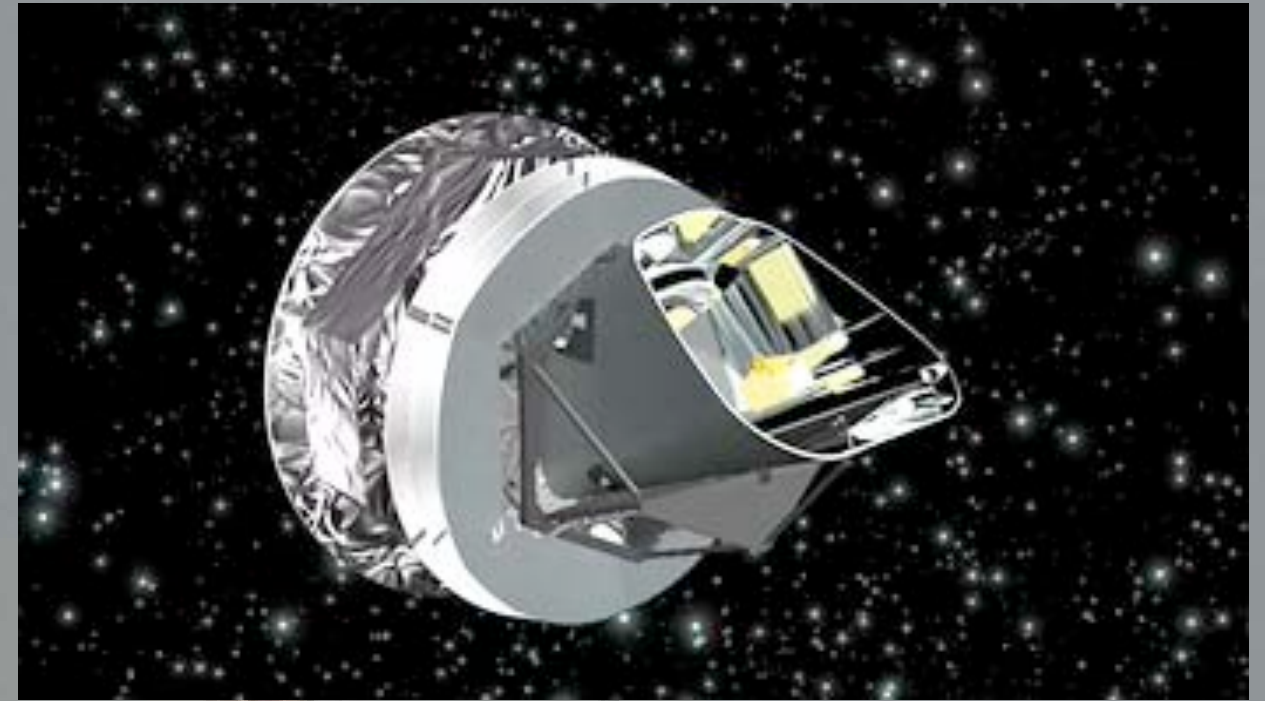
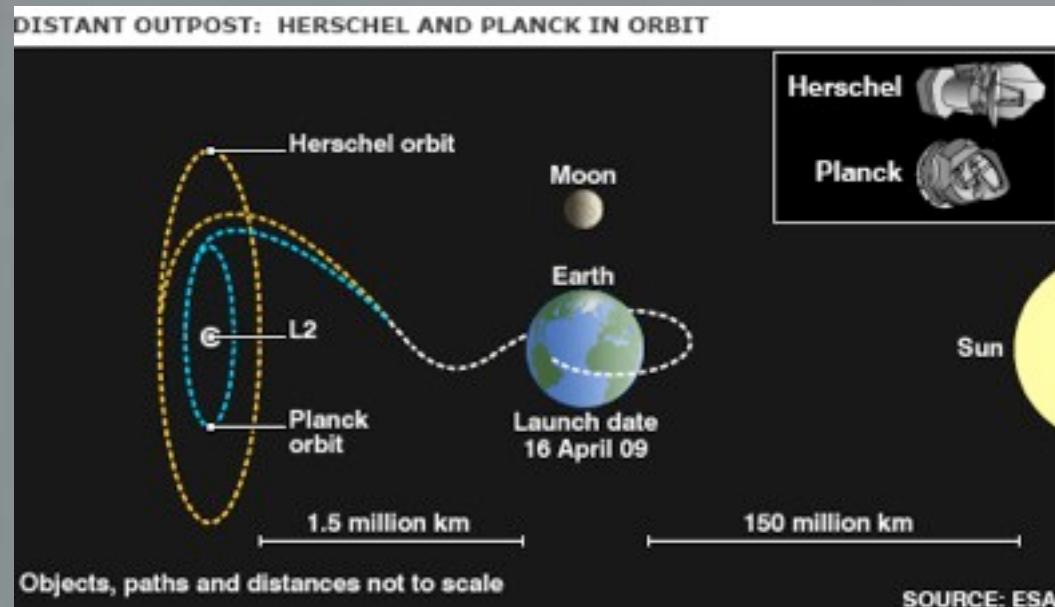
late-universe processes

CMB secondaries anisotropies



ultimate measurements of primary
anisotropies of temperature
also measurements of secondary anisotropies





- Launched in May 14th 2009
- First complete coverage of sky in June 2010
- Nominal mission completed in November 2010
- End of light January 14th 2012. 32 months after launch

First cosmology release 21st March 2013

- Full release in 2014

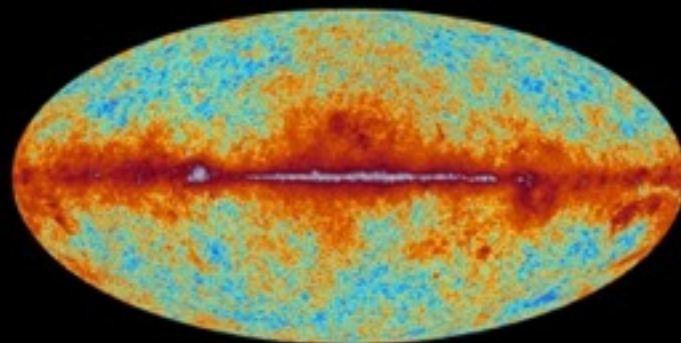
Ariane 5 ECA Launch • HERSCHEL – PLANCK - May 14, 2009

Planck sky maps

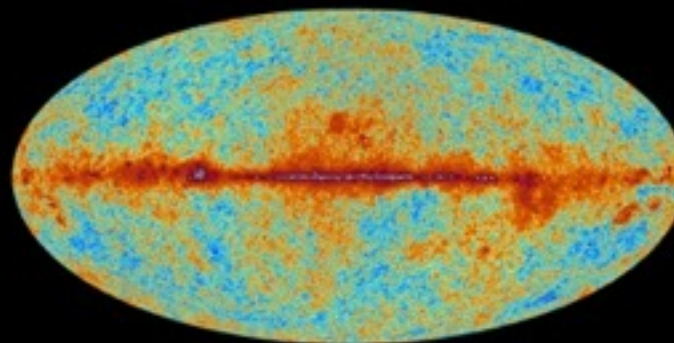


planck

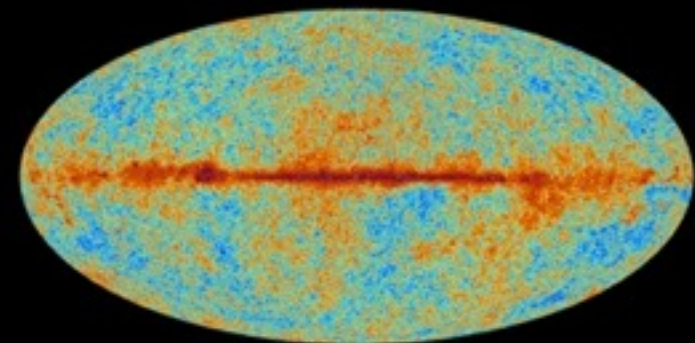
The sky as seen by Planck



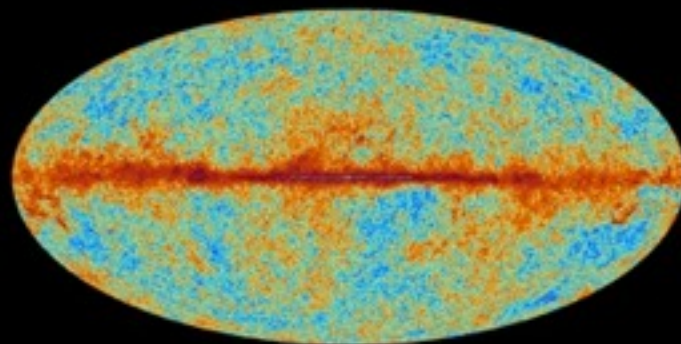
30 GHz



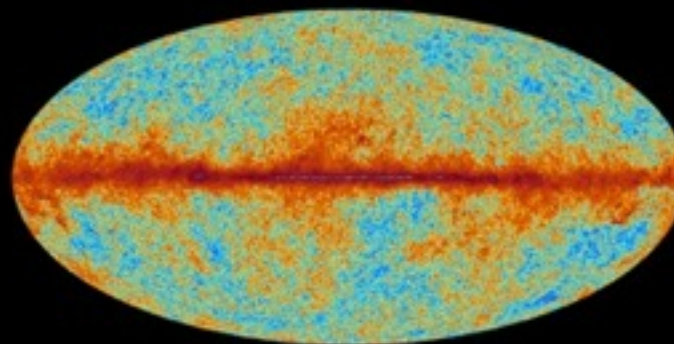
44 GHz



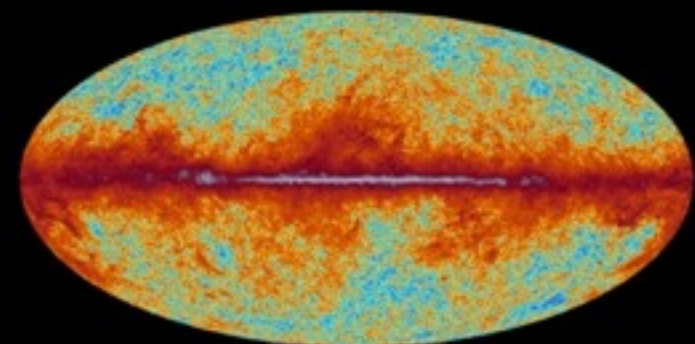
70 GHz



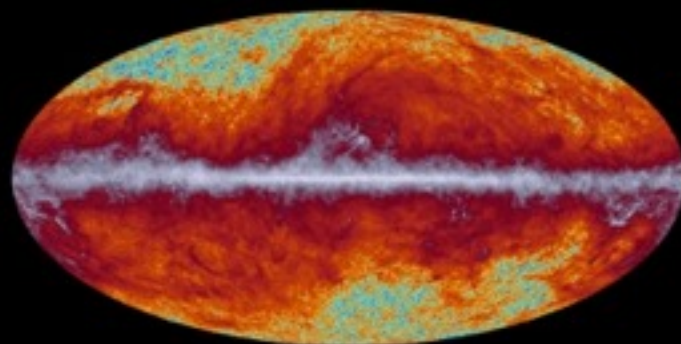
100 GHz



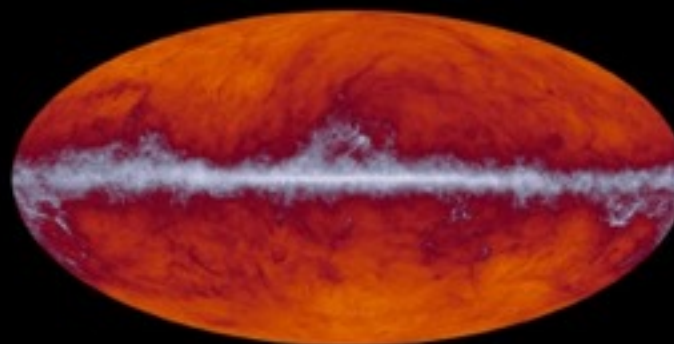
143 GHz



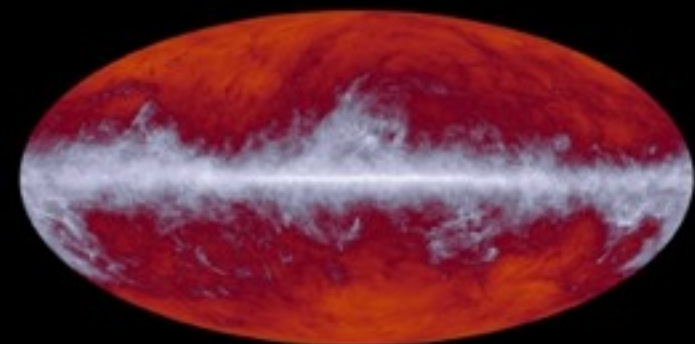
217 GHz



353 GHz

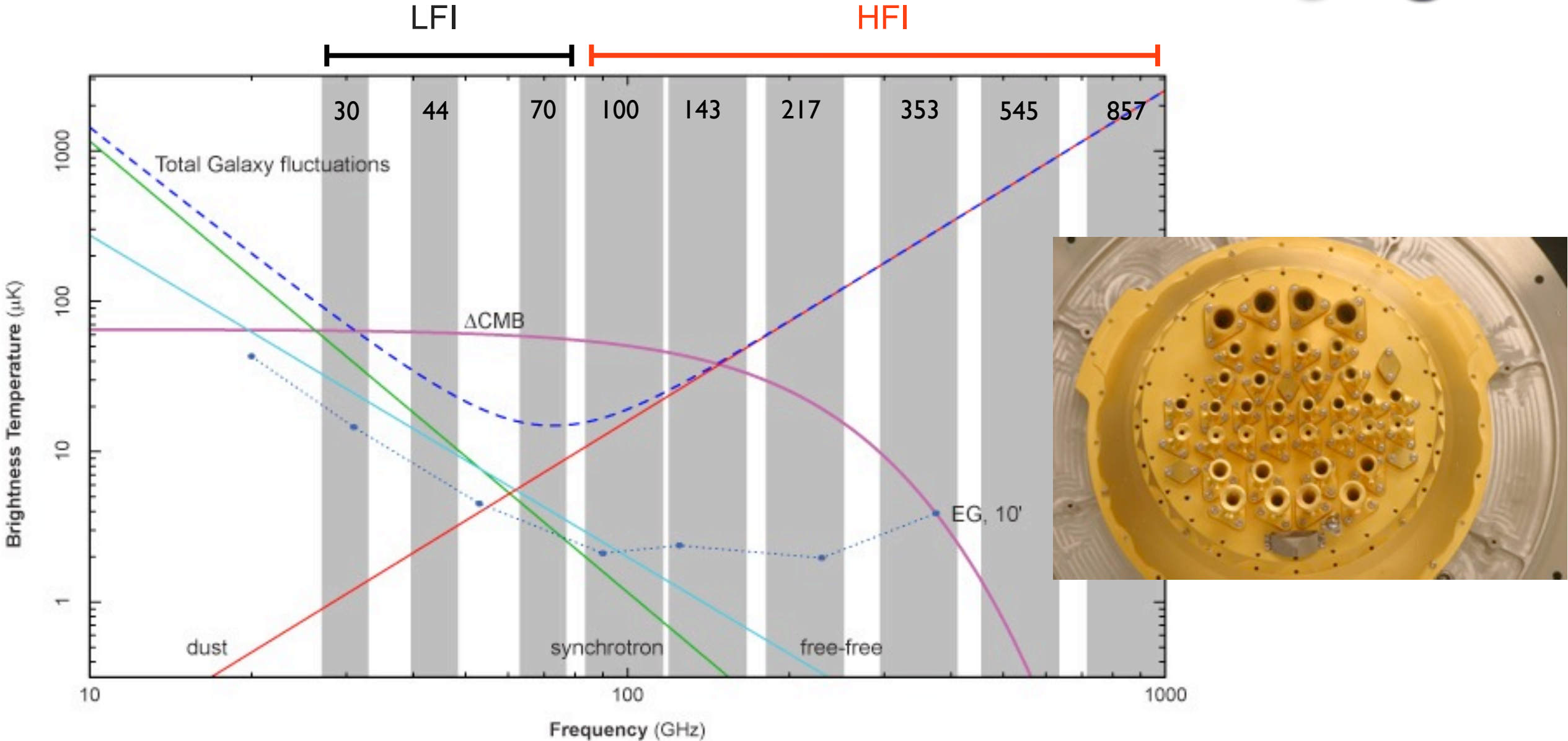


545 GHz



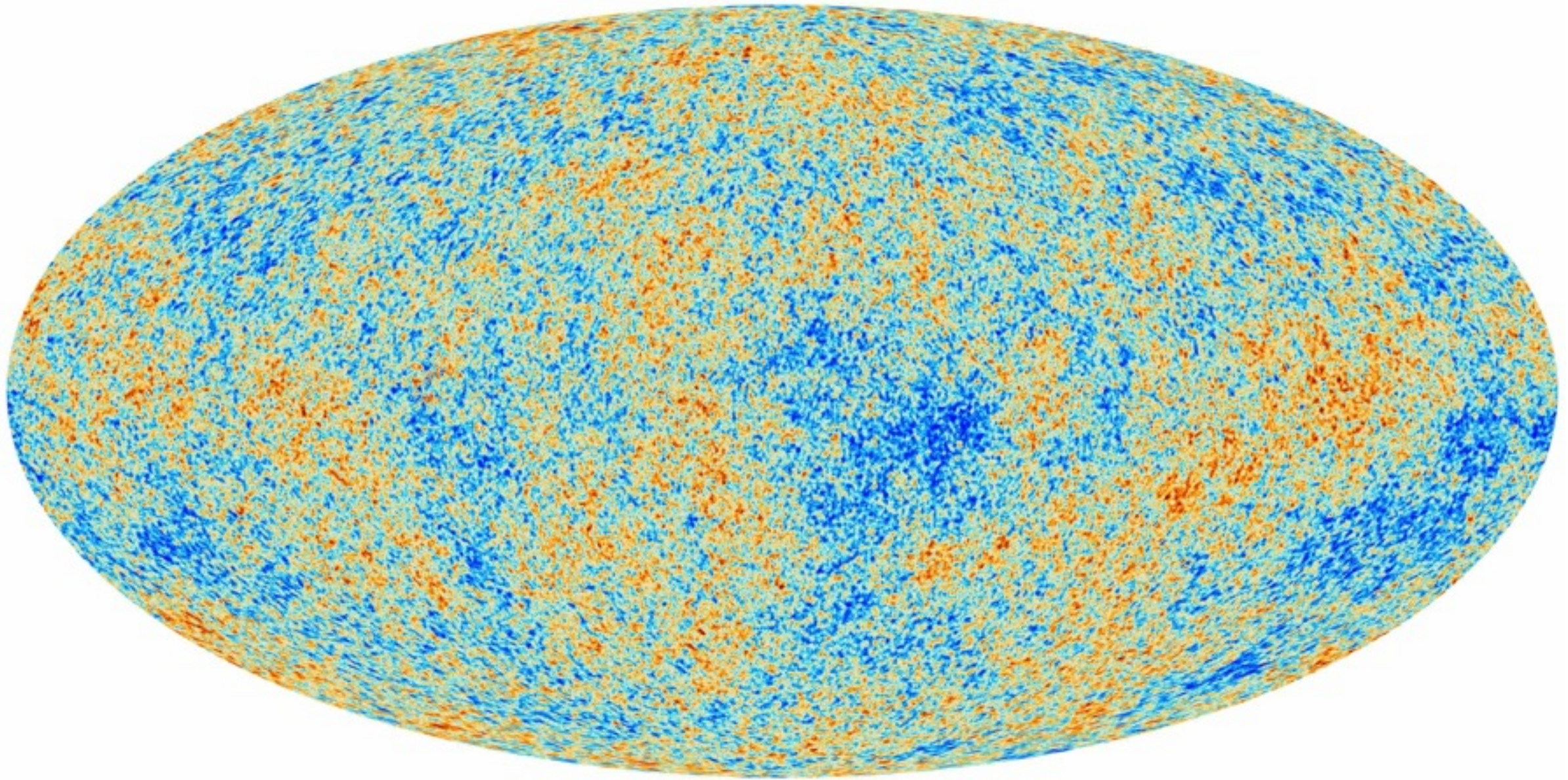
857 GHz

Planck concept



PLANCK	LFI			HFI					
Center Freq (GHz)	30	44	70	100	143	217	353	545	857
Angular resolution (FWHM arcmin)	33	24	14	10	7.1	5.0	5.0	5	5
Sensitivity in I [$\mu\text{K.deg}$] [$\sigma_{\text{pix}} \Omega_{\text{pix}}^{1/2}$]	3.0	3.0	3.0	1.1	0,7	1.1	3.3	33	3.0

Planck full-sky CMB map



- 3% sky fraction filled with Gaussian constrained realisations

Cosmic Microwave background



- Decompose the temperature on the sphere

$$T(\hat{\mathbf{n}}) \longrightarrow T_{\ell m}$$

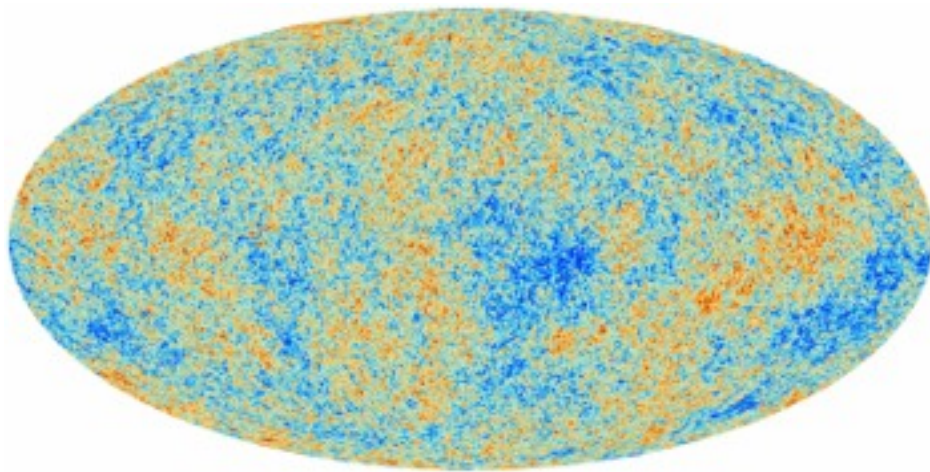
Cosmic Microwave background



- Decompose the temperature on the sphere

$$T(\hat{\mathbf{n}}) \longrightarrow T_{\ell m}$$

$$T(\hat{\mathbf{n}})$$



$$T_{\ell m}$$

```
-1.36393664e-06 +1.78900125e-07j,  
3.48160018e-07 +5.48607128e-07j,  
8.64414116e-07 +1.58062970e-06j,  
2.32962756e-07 +1.72990879e-07j,  
2.07366735e-07 -1.48637056e-06j,  
1.33636760e-06 +1.44430207e-06j,  
-1.33047477e-06 +1.49222938e-06j,  
2.01588688e-07 +1.39367943e-08j,  
1.20185303e-06 -1.04105033e-06j,  
-1.88960308e-06 -2.69868746e-07j,  
1.06239463e-06 +4.31127048e-07j,  
3.98739296e-07 +1.19163879e-07j,  
-1.24503110e-06 -1.93401840e-06j,  
5.68052758e-07 +6.49802586e-08j,  
5.05386856e-07 -2.28955226e-07j,  
-2.60272490e-07 +2.21246718e-06j,  
-1.11889361e-06 +1.87312956e-06j,  
9.72080476e-07 -6.89214224e-07j,  
3.26351028e-07 +1.08530943e-06j,  
2.14977119e-06 -9.44341599e-07j,
```

Cosmic Microwave background



- Decompose the temperature on the sphere

$$T(\hat{\mathbf{n}}) \longrightarrow T_{\ell m}$$

- CMB is (almost) Gaussian: all the information is in the variance

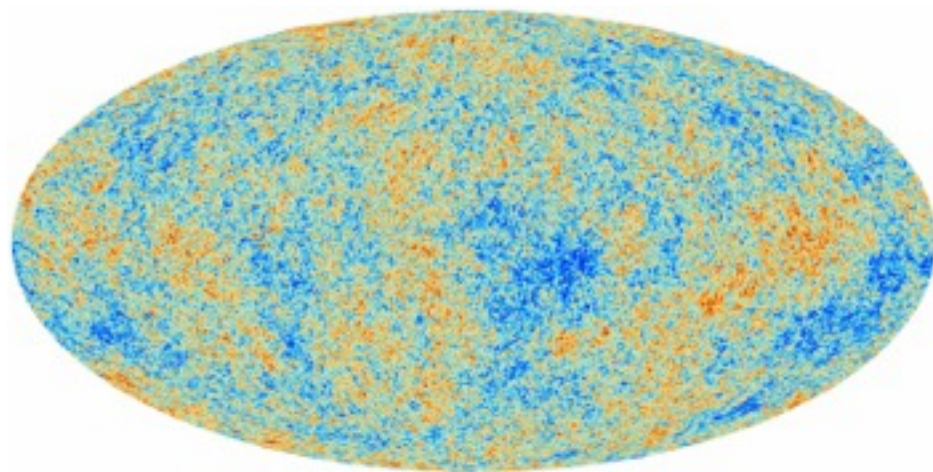
$$\langle t_{\ell m} t_{\ell' m'}^* \rangle = C_{\ell}$$

Power spectrum can be computed: e.g. CAMB

Can be measured from observations: e.g. pseudo-Cl's

$$\hat{C}_{\ell} = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} |T_{\ell m}|^2$$

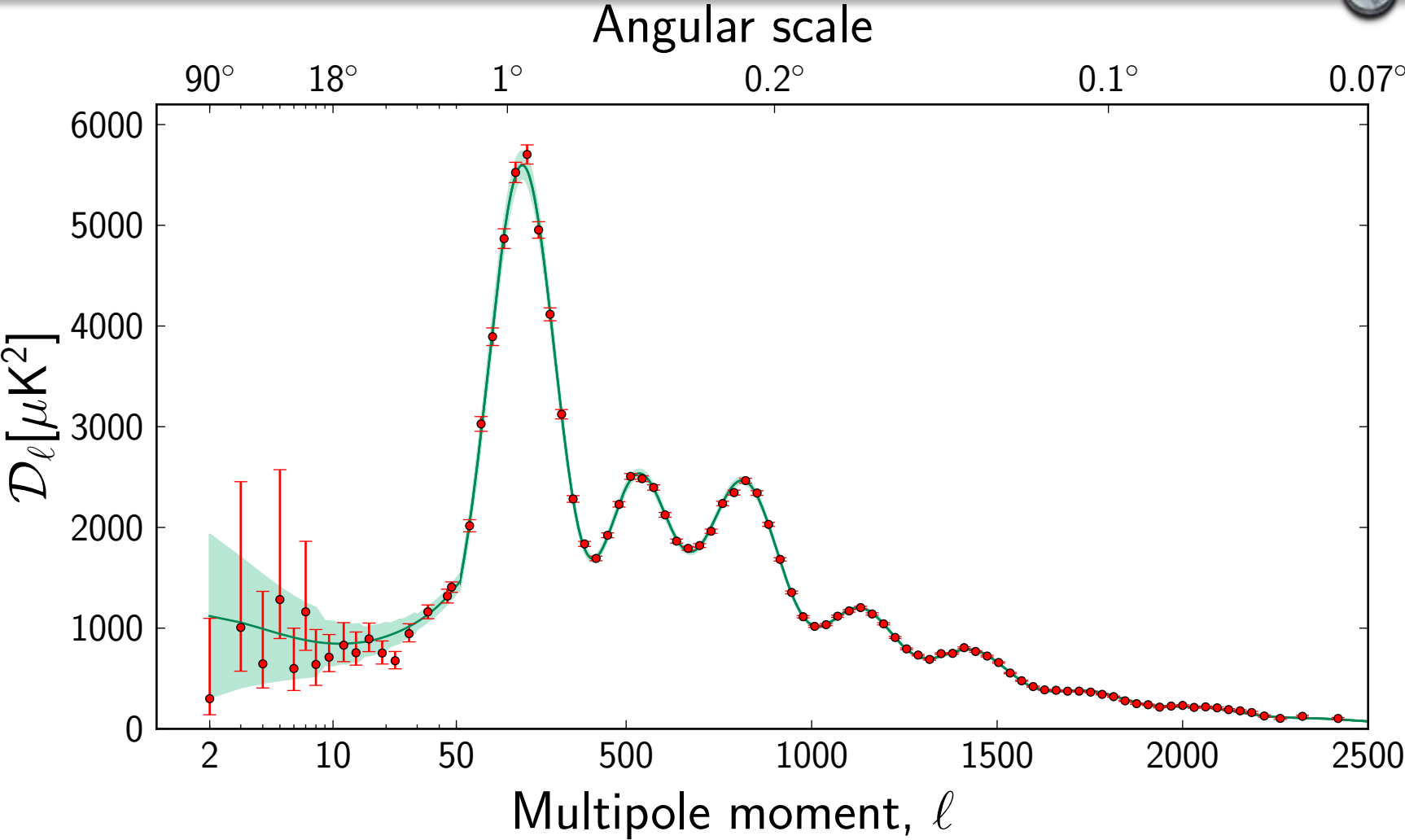
$$T(\hat{\mathbf{n}})$$



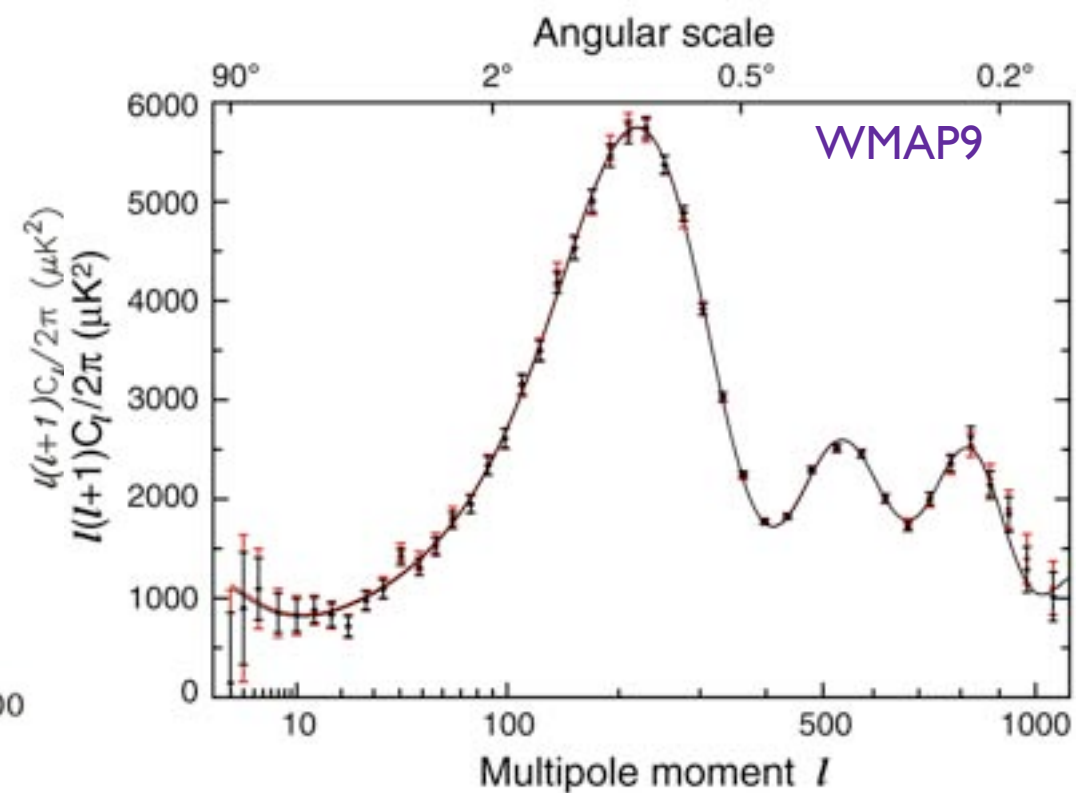
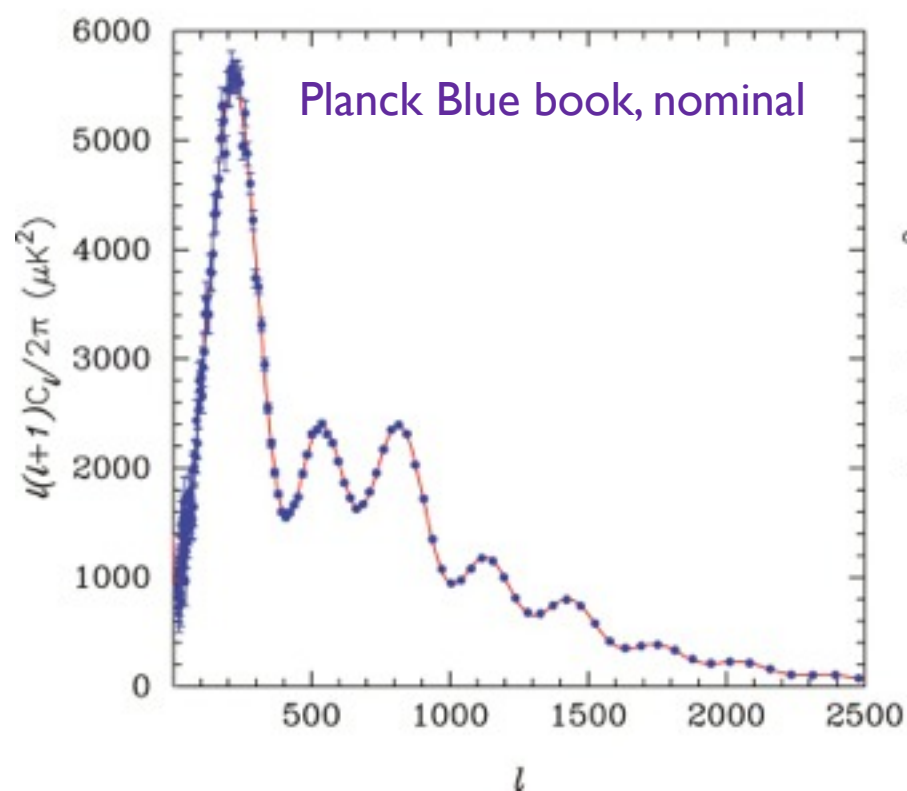
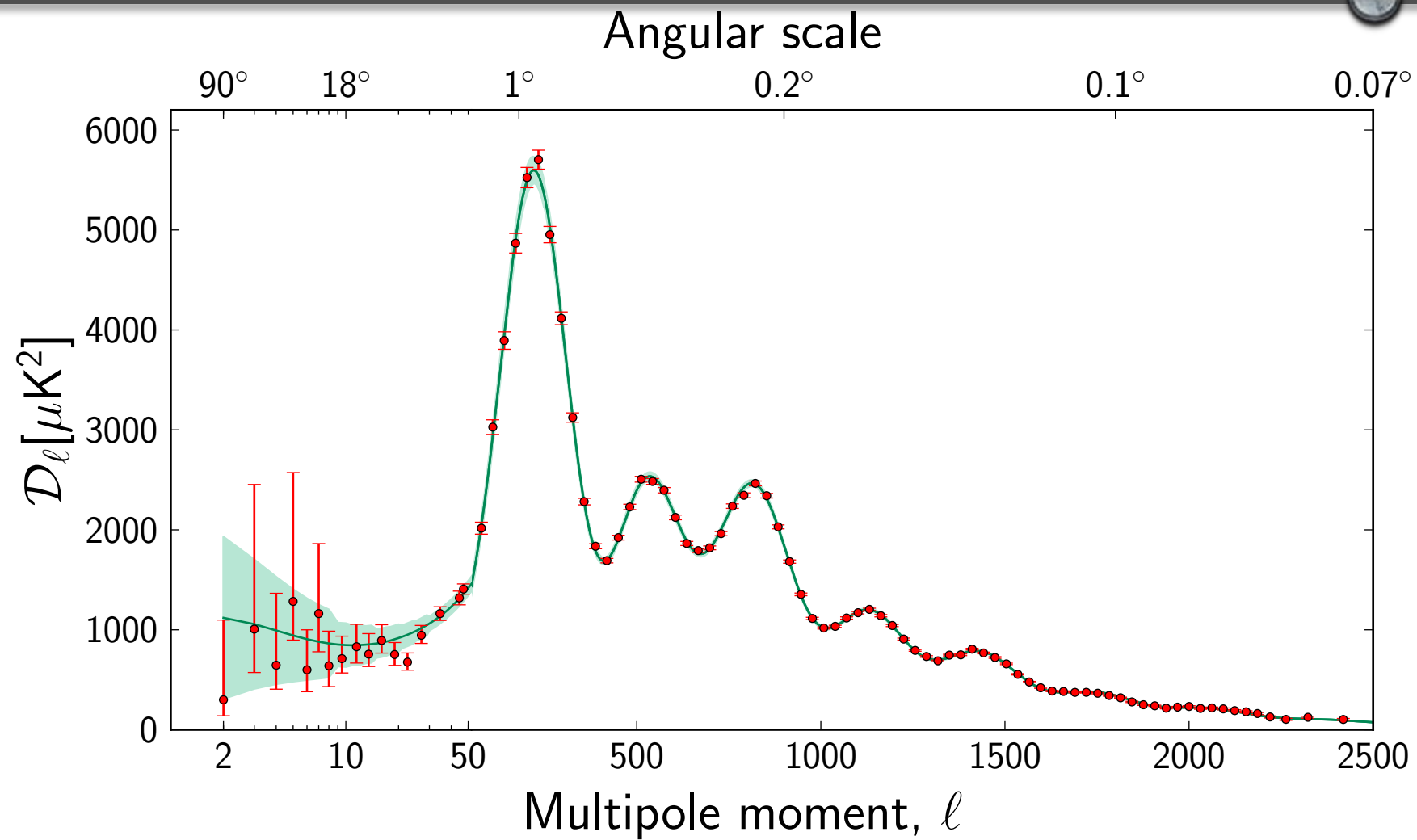
$$T_{\ell m}$$

```
-1.36393664e-06 +1.78900125e-07j,
3.48160018e-07 +5.48607128e-07j,
8.64414116e-07 +1.58062970e-06j,
2.32962756e-07 +1.72990879e-07j,
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1.33636760e-06 +1.44430207e-06j,
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2.01588688e-07 +1.39367943e-08j,
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9.72080476e-07 -6.89214224e-07j,
3.26351028e-07 +1.08530943e-06j,
2.14977119e-06 -9.44341599e-07j,
```

Cosmic Microwave background



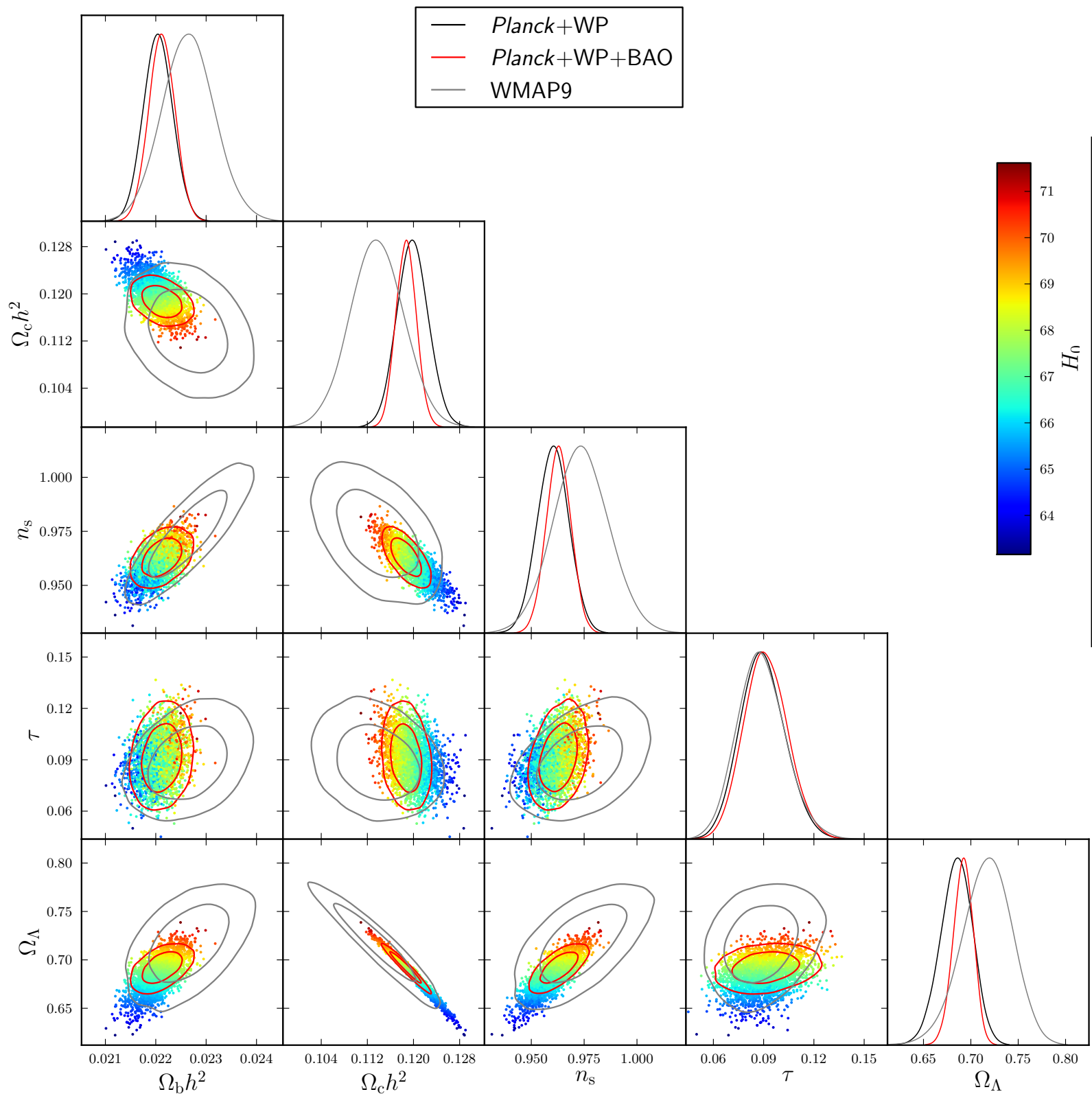
Cosmic Microwave background



Planck cosmological parameters

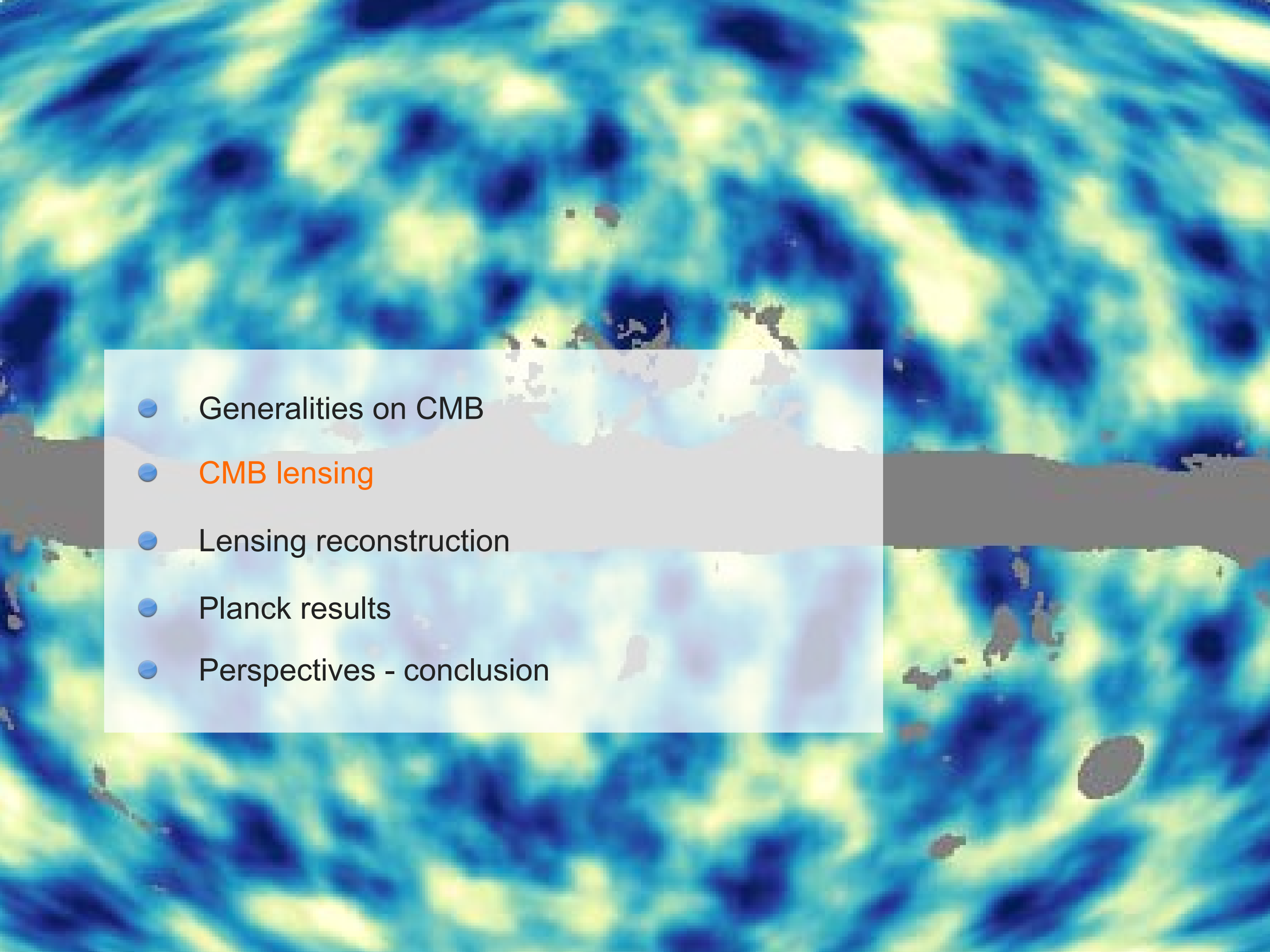


A model described by only 6 parameters



Planck + WP

- Peak scale 0.060%
- Baryon density 1.3%
- CDM density 2.3%
- Primordial amplitude 2.5%
- Primordial spectral index 0.76%
- Reionization optical depth 0.13%

- 
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- Generalities on CMB
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Cosmic Microwave background



- Decompose the temperature on the sphere $T(\hat{\mathbf{n}}) \longrightarrow T_{\ell m}$
- CMB is (almost) Gaussian: all the information is in the variance $\langle t_{\ell m} t_{\ell' m'}^* \rangle = C_\ell$

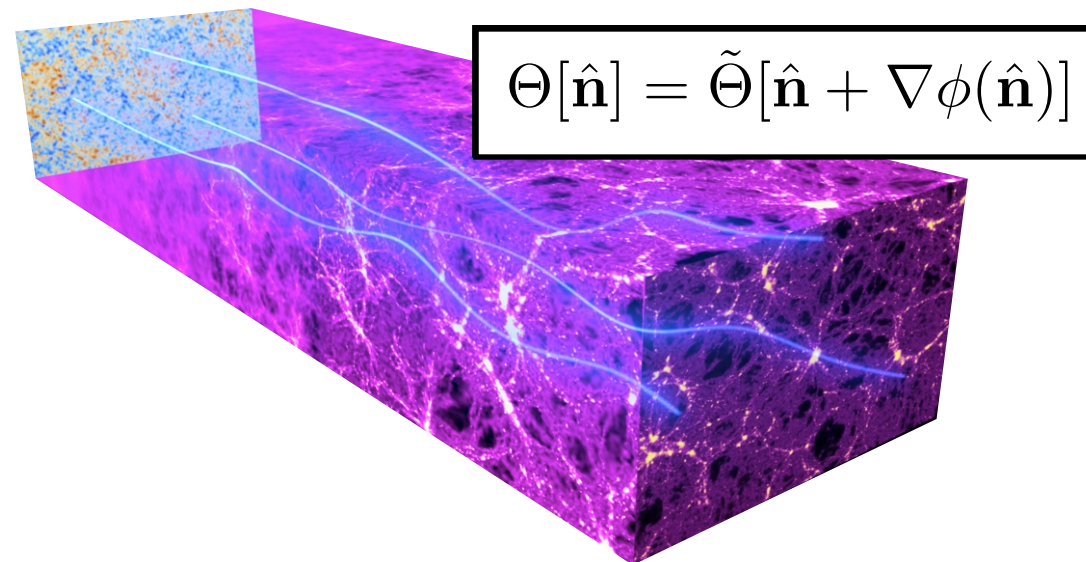
Cosmic Microwave background



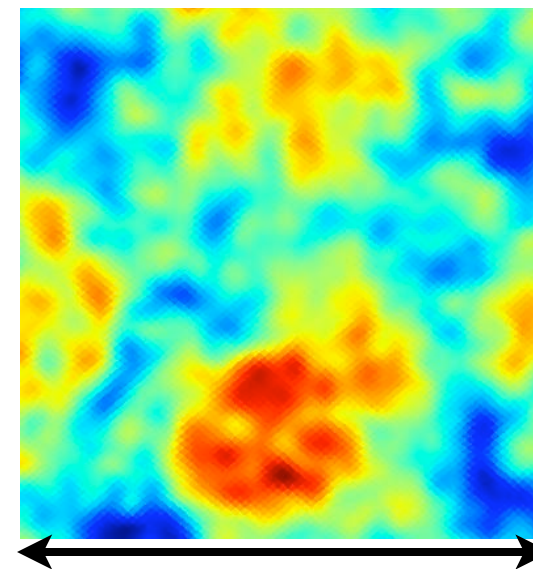
- Decompose the temperature on the sphere $T(\hat{\mathbf{n}}) \longrightarrow T_{\ell m}$
- CMB is (almost) Gaussian: all the information is in the variance $\langle t_{\ell m} t_{\ell' m'}^* \rangle = C_\ell$
 - ★ Primordial non-Gaussianities, e.g f_{nl}
 - ★ Gravitational lensing of the CMB
 - ★ ...



- Photons from last scattering surface deflected by gravitational potential of large-scale structure

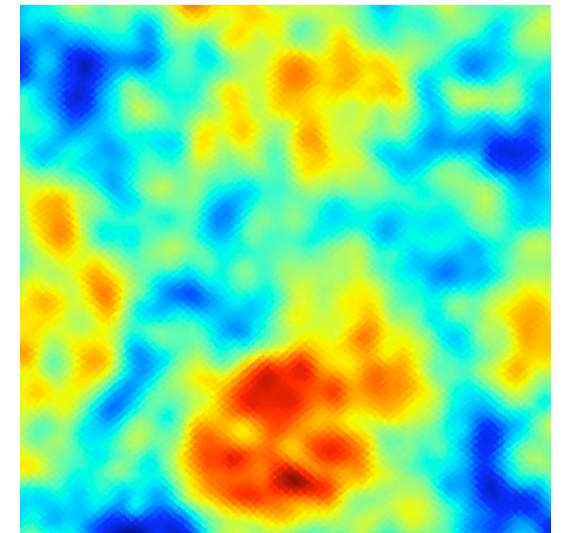


Unlensed



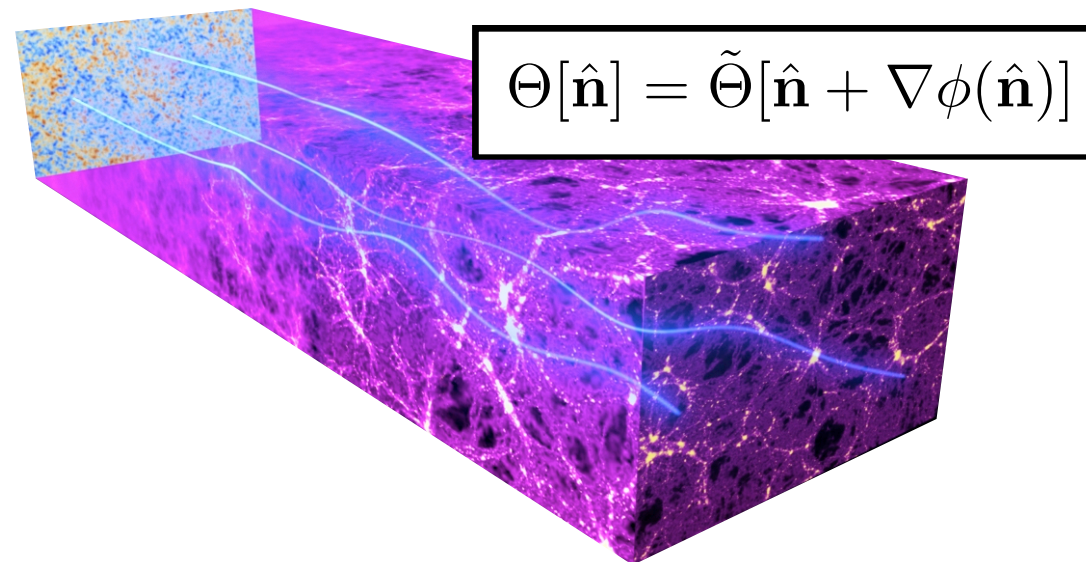
2.5°

Lensed

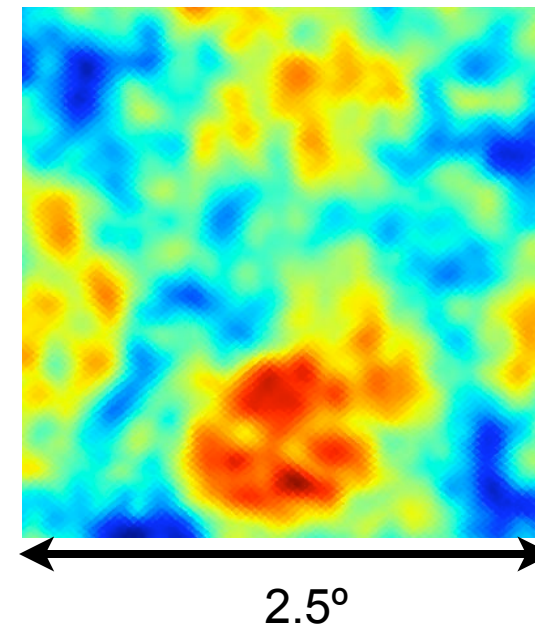




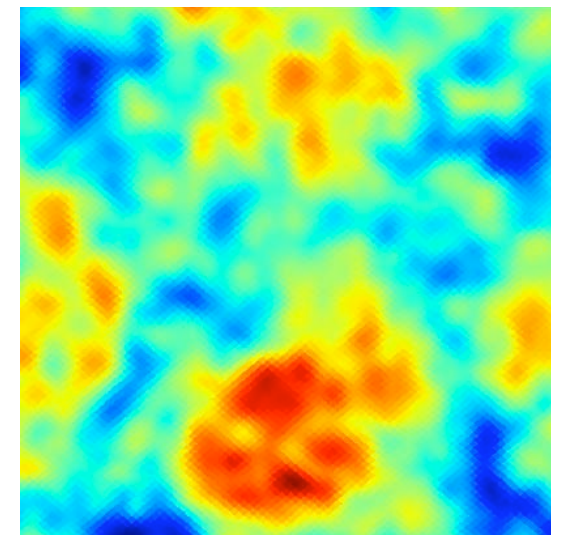
- Photons from last scattering surface deflected by gravitational potential of large-scale structure



Lensed

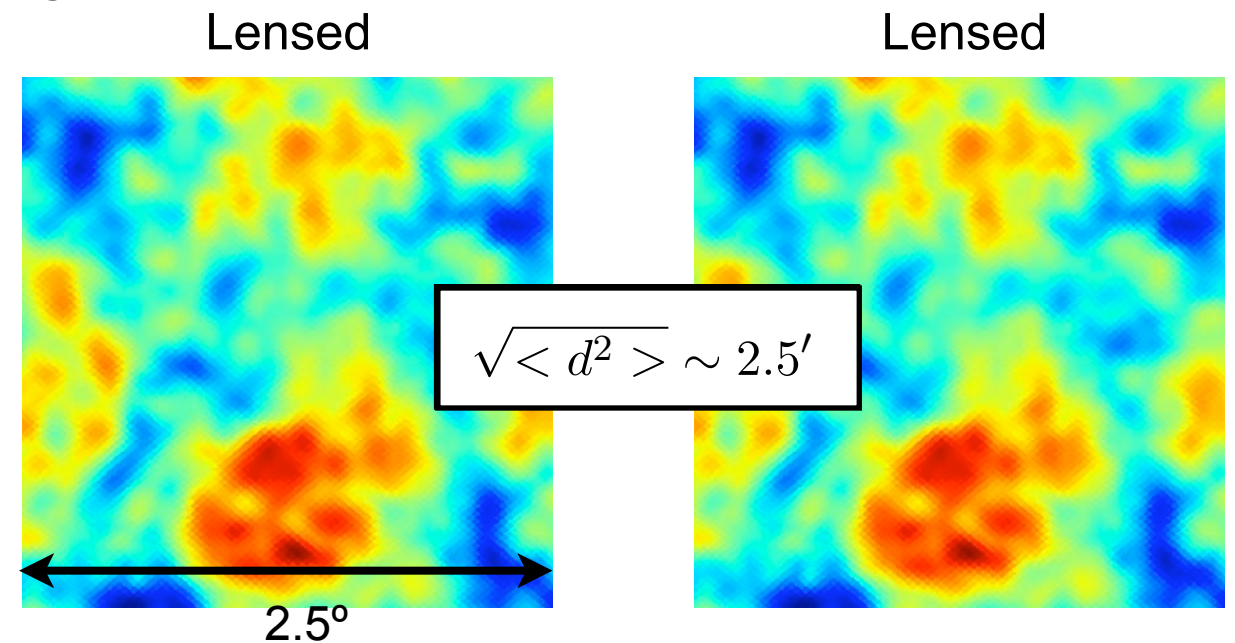
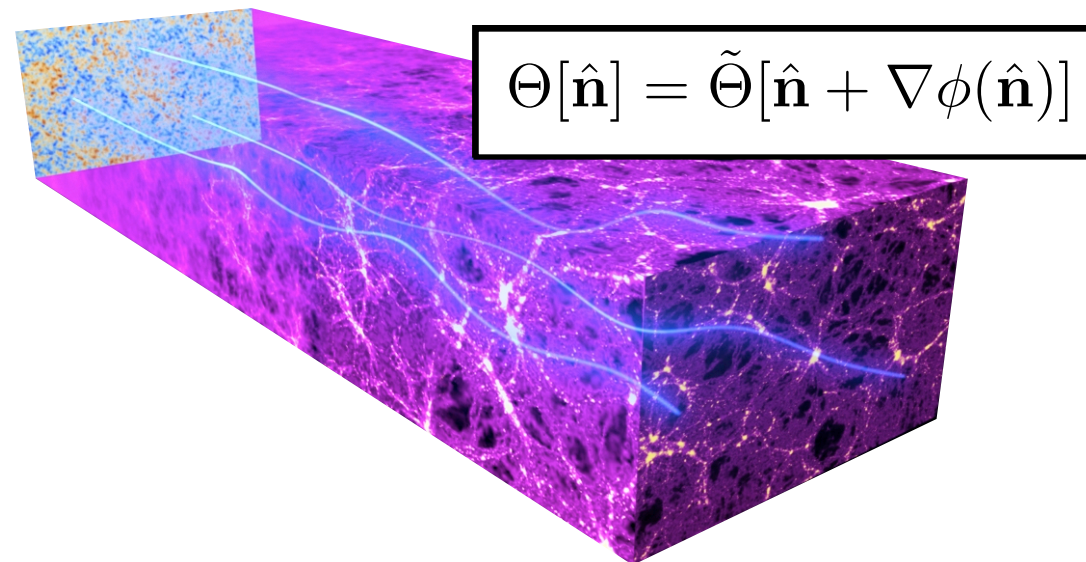


Lensed





- Photons from last scattering surface deflected by gravitational potential of large-scale structure



$$\phi(\hat{\mathbf{n}}) = -2 \int d\eta \frac{\chi(\eta - \eta_{\text{rec}})}{\chi(\eta_{\text{rec}})\chi(\eta)} \Psi(\chi\hat{\mathbf{n}}, \eta)$$

- Typical deflections: ~ 2.5 arcmin
- Coherent on the degree scale
- Sources temperature-gradient correlation

Lensing potential reconstruction

Impact of CMB lensing



$$\Theta[\hat{\mathbf{n}}] = \tilde{\Theta}[\hat{\mathbf{n}} + \nabla\phi(\hat{\mathbf{n}})] \longrightarrow \Theta(\hat{\mathbf{n}}) = \tilde{\Theta}(\hat{\mathbf{n}}) + \nabla_i\phi(\hat{\mathbf{n}})\nabla^i\tilde{\Theta}(\hat{\mathbf{n}}) + \dots$$

Temperature and gradient become correlated

$$\langle t_{\ell m} t_{\ell' m'}^* \rangle_{\text{CMB}} = C_{\ell} + \sum_{\lambda\mu} F_{mm'\mu}^{\ell\ell'\lambda} \phi_{\lambda\mu}$$

Impact of CMB lensing



$$\Theta[\hat{\mathbf{n}}] = \tilde{\Theta}[\hat{\mathbf{n}} + \nabla\phi(\hat{\mathbf{n}})] \longrightarrow \Theta(\hat{\mathbf{n}}) = \tilde{\Theta}(\hat{\mathbf{n}}) + \nabla_i\phi(\hat{\mathbf{n}})\nabla^i\tilde{\Theta}(\hat{\mathbf{n}}) + \dots$$

Temperature and gradient become correlated

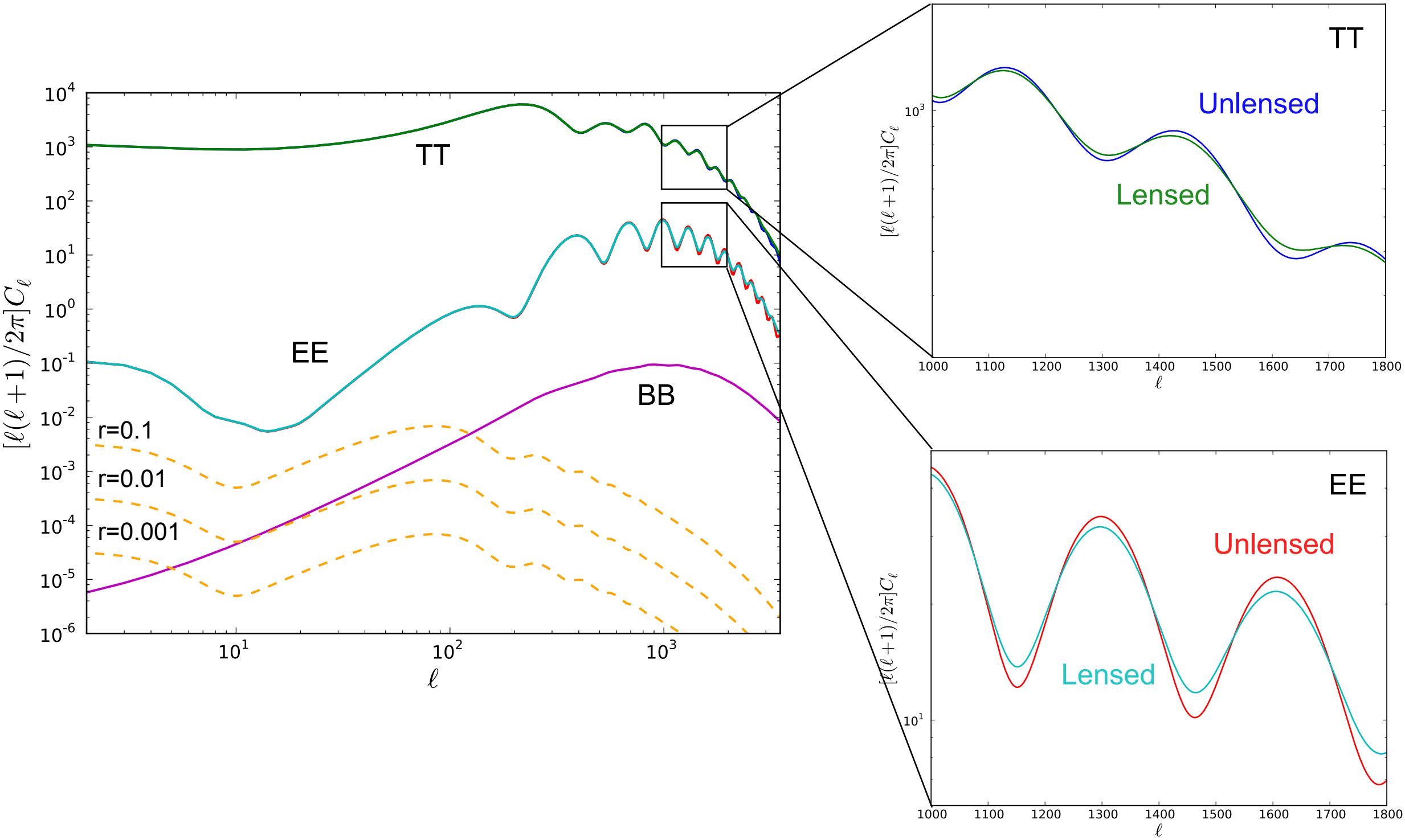
$$\langle t_{\ell m} t_{\ell' m'}^* \rangle_{\text{CMB}} = C_\ell + \sum_{\lambda\mu} F_{mm'\mu}^{\ell\ell'\lambda} \phi_{\lambda\mu}$$

CMB lensing induces mode coupling

$$C_\ell \sim (1 - \alpha_\ell) \tilde{C}_\ell + \sum_{\ell_1 \ell_2} C_{\ell_1}^{\phi\phi} \tilde{C}_{\ell_2} F_{\ell\ell_1\ell_2}$$

- Modifies the shape of observed power spectra

Effect on power spectra



Impact of CMB lensing



$$\Theta[\hat{\mathbf{n}}] = \tilde{\Theta}[\hat{\mathbf{n}} + \nabla\phi(\hat{\mathbf{n}})] \longrightarrow \Theta(\hat{\mathbf{n}}) = \tilde{\Theta}(\hat{\mathbf{n}}) + \nabla_i\phi(\hat{\mathbf{n}})\nabla^i\tilde{\Theta}(\hat{\mathbf{n}}) + \dots$$

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- Modifies the shape of observed power spectra
 - Creates non-Gaussian terms in the spectra covariance
- ABL, Smith & Hu (*PRD*, 2012)

Lensing information is encoded
in anisotropies spectra

Effect on power spectra covariance



- Unlensed CMB is Gaussian: modes are independent

$$\text{cov}(C_{\ell_1}^{XY}, C_{\ell_2}^{WZ}) = \text{cov}^G(C_{\ell_1}^{XY}, C_{\ell_2}^{WZ})$$

$$\text{Cov}_{\ell_1 \ell_2}^{XY, WZ} = \frac{1}{2\ell_1 + 1} [C_{\ell_1}^{XW} C_{\ell_1}^{YZ} + C_{\ell_1}^{XZ} C_{\ell_1}^{YW}] \delta_{\ell_1, \ell_2}$$

$$\text{Cov}_{\ell_1 \ell_2}^{BB, BB} = \frac{2}{2\ell_1 + 1} (C_{\ell_1}^{BB})^2 \delta_{\ell_1, \ell_2}$$

Effect on power spectra covariance



- Covariance induced by CMB lensing

$$\text{cov}(C_{\ell_1}^{XY}, C_{\ell_2}^{WZ}) = \text{cov}^G(C_{\ell_1}^{XY}, C_{\ell_2}^{WZ}) + \text{cov}^{\text{NG}}(C_{\ell_1}^{XY}, C_{\ell_2}^{WZ})$$

$$\begin{aligned} \text{Cov}_{\ell_1 \ell_2}^{XY, WZ} &= \frac{1}{2\ell_1 + 1} [C_{\ell_1}^{XW} C_{\ell_1}^{YZ} + C_{\ell_1}^{XZ} C_{\ell_1}^{YW}] \delta_{\ell_1, \ell_2} \\ &\quad + \sum_{\ell} \left[\frac{\partial C_{\ell_1}^{XY}}{\partial C_{\ell}^{\phi\phi}} \text{Cov}_{\ell\ell}^{\phi\phi, \phi\phi} \frac{\partial C_{\ell_2}^{WZ}}{\partial C_{\ell}^{\phi\phi}} \right] \end{aligned}$$

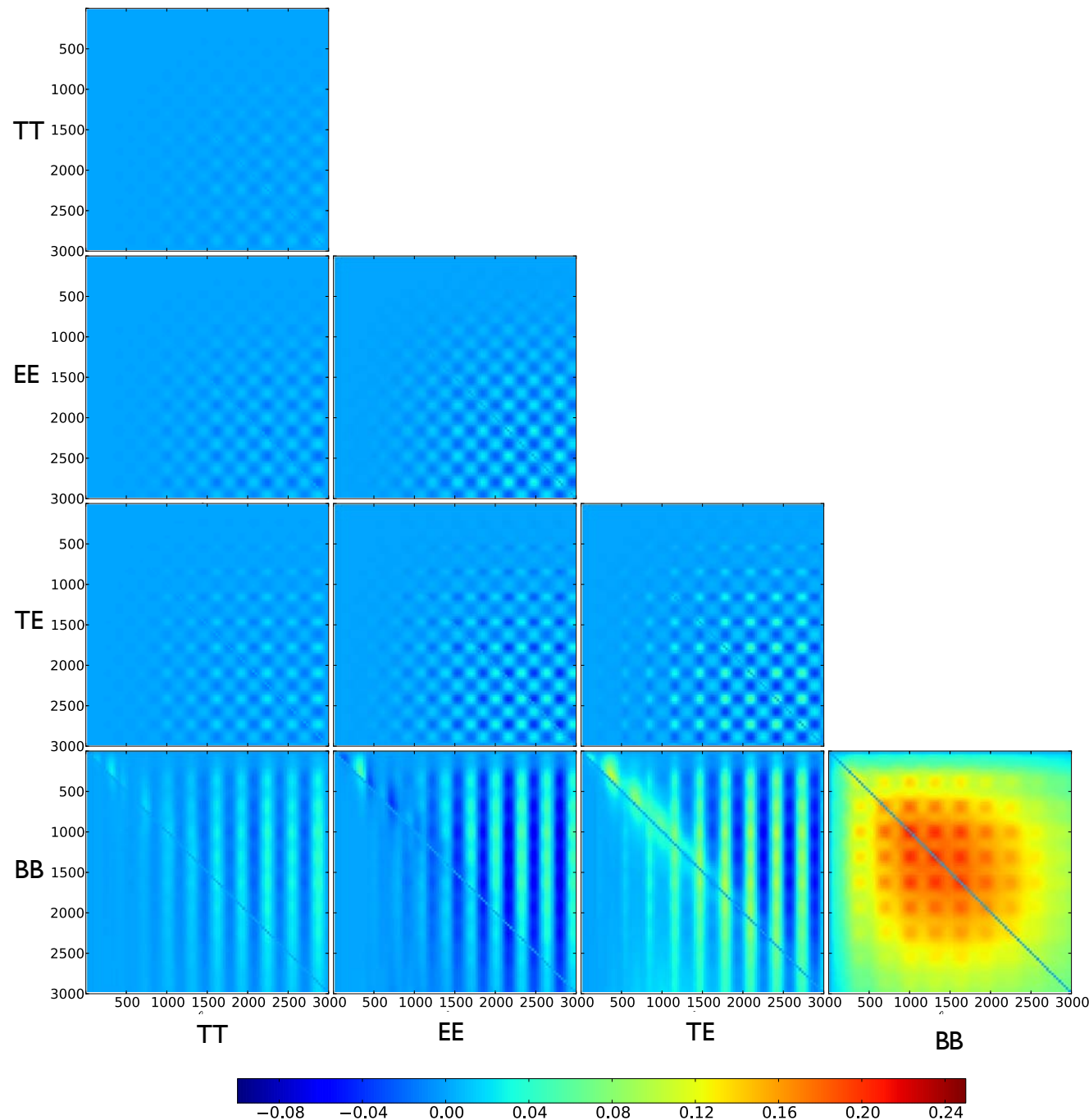
$$\begin{aligned} \text{Cov}_{\ell_1 \ell_2}^{BB, BB} &= \frac{2}{2\ell_1 + 1} (C_{\ell_1}^{BB})^2 \delta_{\ell_1, \ell_2} \\ &\quad + \sum_{\ell} \left(\frac{\partial C_{\ell_1}^{BB}}{\partial C_{\ell}^{\tilde{E}\tilde{E}}} \text{Cov}_{\ell\ell}^{\tilde{E}\tilde{E}, \tilde{E}\tilde{E}} \frac{\partial C_{\ell_2}^{BB}}{\partial C_{\ell}^{\tilde{E}\tilde{E}}} \right) \\ &\quad + \sum_{\ell} \left(\frac{\partial C_{\ell_1}^{BB}}{\partial C_{\ell}^{\phi\phi}} \text{Cov}_{\ell\ell}^{\phi\phi, \phi\phi} \frac{\partial C_{\ell_2}^{BB}}{\partial C_{\ell}^{\phi\phi}} \right) \end{aligned}$$

ABL, Smith & Hu (*PRD*, 2012)

Effect on power spectra covariance

- Covariance induced by CMB lensing

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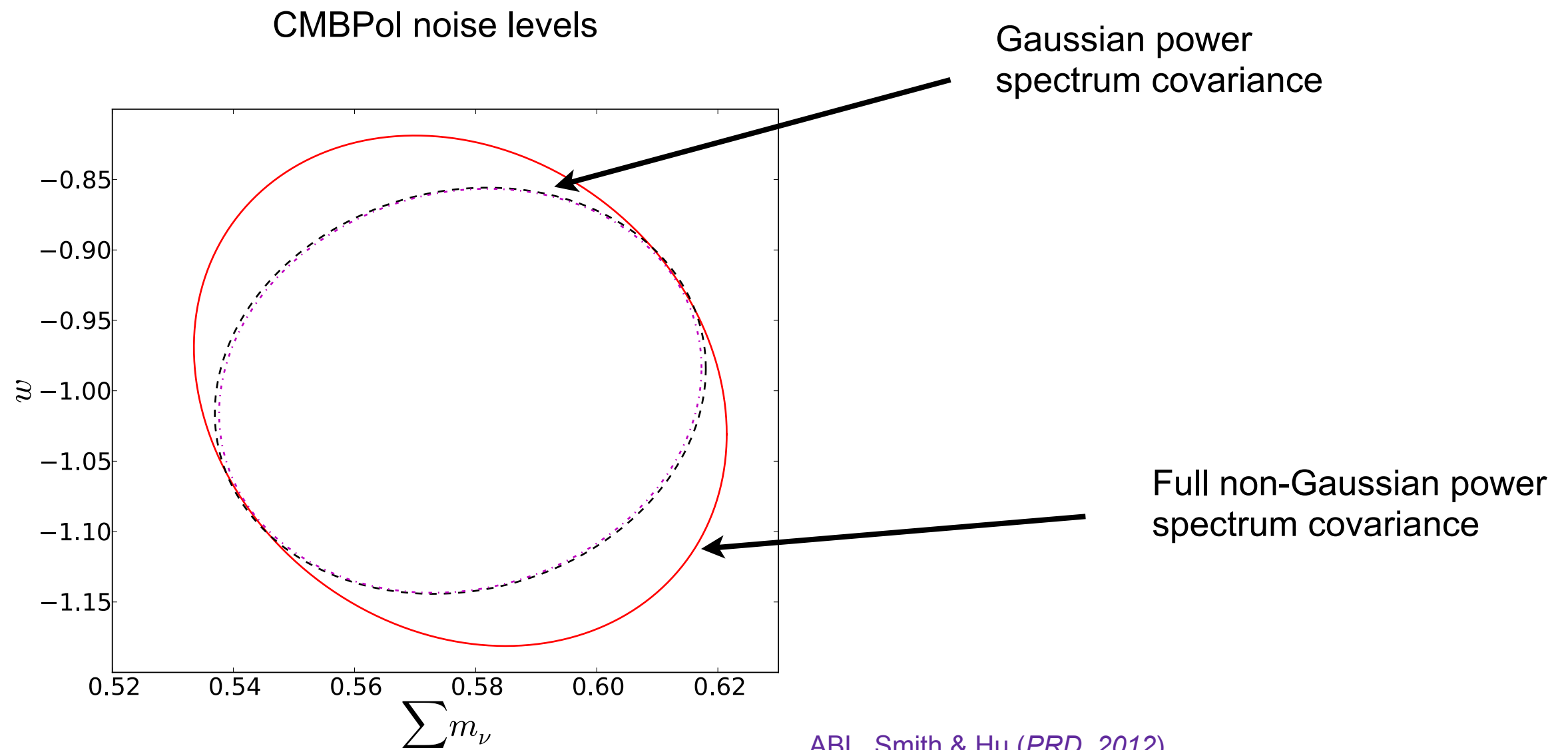


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$$\text{Cov}_{\ell_1 \ell_2}^{BB, BB} = \frac{2}{2\ell_1 + 1} (C_{\ell_1}^{BB})^2 \delta_{\ell_1, \ell_2} + \sum_{\ell} \left(\frac{\partial C_{\ell_1}^{BB}}{\partial C_{\ell}^{\tilde{E}\tilde{E}}} \text{Cov}_{\ell\ell}^{\tilde{E}\tilde{E}, \tilde{E}\tilde{E}} \frac{\partial C_{\ell_2}^{BB}}{\partial C_{\ell}^{\tilde{E}\tilde{E}}} \right) + \sum_{\ell} \left(\frac{\partial C_{\ell_1}^{BB}}{\partial C_{\ell}^{\phi\phi}} \text{Cov}_{\ell\ell}^{\phi\phi, \phi\phi} \frac{\partial C_{\ell_2}^{BB}}{\partial C_{\ell}^{\phi\phi}} \right)$$

ABL, Smith & Hu (*PRD*, 2012)

Effect on power spectra covariance



Significant effect for a post-Planck experiment

Impact of CMB lensing



$$\Theta[\hat{\mathbf{n}}] = \tilde{\Theta}[\hat{\mathbf{n}} + \nabla\phi(\hat{\mathbf{n}})] \longrightarrow \Theta(\hat{\mathbf{n}}) = \tilde{\Theta}(\hat{\mathbf{n}}) + \nabla_i\phi(\hat{\mathbf{n}})\nabla^i\tilde{\Theta}(\hat{\mathbf{n}}) + \dots$$

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ABL, Smith & Hu (*PRD*, 2012)

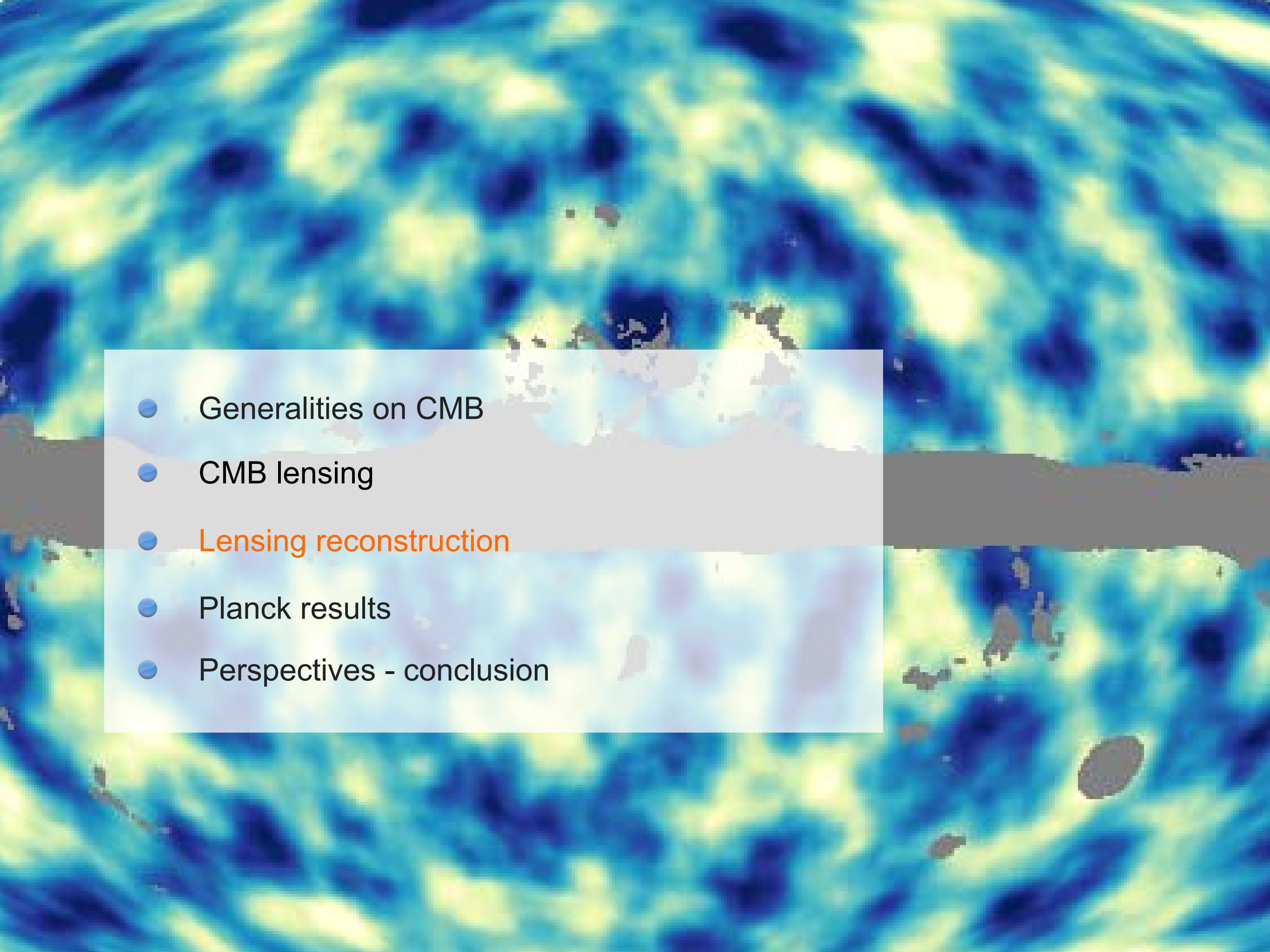
«Statistical inversion»

$$\langle \Theta \nabla \Theta \rangle \Rightarrow \phi$$

- Allows the reconstruction of the lensing potential and its power spectrum

Lensing information is encoded in anisotropies spectra

Reconstruction provides direct measurement of the lensing potential

- 
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Lensing reconstruction



● Optimal quadratic estimator Okamoto & Hu (2003)

$$\hat{\phi}_L^M \propto A_L \sum_{l_1 m_1} \sum_{l_2 m_2} (-1)^M \begin{pmatrix} l_1 & l_2 & L \\ m_1 & m_2 & -M \end{pmatrix} \frac{(\tilde{C}_{l_2} F_{l_1 L l_2} + \tilde{C}_{l_1} F_{l_2 L l_1})^2}{2C_{l_1}^{\text{tot}} C_{l_2}^{\text{tot}}} \Theta_{m_1}^{l_1} \Theta_{m_2}^{l_2} \quad \text{Harmonic space}$$

$$\hat{\phi}_L^M \propto A_L \int d\hat{\mathbf{n}} Y_L^{M*} \left(\sum_{l_1 m_1} \frac{1}{C_{l_1}^{\text{tot}}} \Theta_{l_1}^{m_1} Y_{l_1}^{m_1} \right) \nabla \left(\sum_{l_2 m_2} \frac{\tilde{C}_{l_2}}{C_{l_2}^{\text{tot}}} \Theta_{l_2}^{m_2} Y_{l_2}^{m_2} \right) \quad \text{Real space}$$

Lensing reconstruction



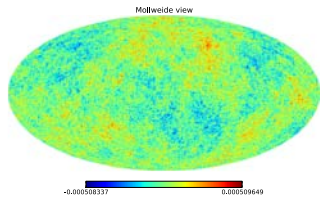
Optimal quadratic estimator Okamoto & Hu (2003)

$$\hat{\phi}_L^M \propto A_L \sum_{l_1 m_1} \sum_{l_2 m_2} (-1)^M \begin{pmatrix} l_1 & l_2 & L \\ m_1 & m_2 & -M \end{pmatrix} \frac{(\tilde{C}_{l_2} F_{l_1 L l_2} + \tilde{C}_{l_1} F_{l_2 L l_1})^2}{2C_{l_1}^{\text{tot}} C_{l_2}^{\text{tot}}} \Theta_{m_1}^{l_1} \Theta_{m_2}^{l_2}$$

Harmonic space

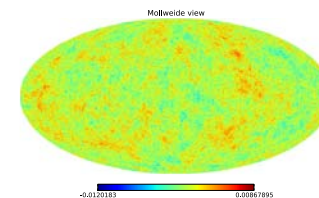
$$\hat{\phi}_L^M \propto A_L \int d\hat{\mathbf{n}} Y_L^{M*} \left(\sum_{l_1 m_1} \frac{1}{C_{l_1}^{\text{tot}}} \Theta_{l_1}^{m_1} Y_{l_1}^{m_1} \right) \nabla \left(\sum_{l_2 m_2} \frac{\tilde{C}_{l_2}}{C_{l_2}^{\text{tot}}} \Theta_{l_2}^{m_2} Y_{l_2}^{m_2} \right)$$

Real space



- Consider the observed map
- Two different filters
- Take the gradient of the second filtered map
- Multiply the two
- Extract the gradient component

Here is the lensing field !



Lensing reconstruction



$$\mathbf{d} = \nabla \phi + \nabla \times \psi$$

Gradient of the
lensing potential

Curl component
null for lensing

Mean of the estimator

$$\langle \hat{\phi}_{lm}^g \rangle|_{\text{lens}} = A_l \phi_{lm} + \delta_{l0} X$$

$$\langle \hat{\phi}_{lm}^c \rangle|_{\text{lens}} = 0$$

Covariance of the estimator

$$\langle \hat{\phi}_{lm} \hat{\phi}_{lm}^* \rangle = A_l^2 \sum_{\ell_i m_i} \begin{pmatrix} \ell_1 & \ell_2 & l \\ m_1 & m_2 & -m \end{pmatrix} \begin{pmatrix} \ell_3 & \ell_4 & l \\ m_3 & m_4 & -m \end{pmatrix} g_{\ell_1 \ell_2}(l) g_{\ell_3 \ell_4}(l) \langle \Theta_{\ell_1}^{m_1} \Theta_{\ell_2}^{m_2} \Theta_{\ell_3}^{m_3} \Theta_{\ell_4}^{m_4} \rangle$$

Summation of the trispectrum (4-points correlation function)

$$\langle \hat{\phi}_L^M \hat{\phi}_L^{M*} \rangle^G = C_L^{\phi\phi} + N_L^{(0,G)} + N_L^{(1,G)} + N_L^{(2,G)} + \dots$$

Gaussian noise

high order biases

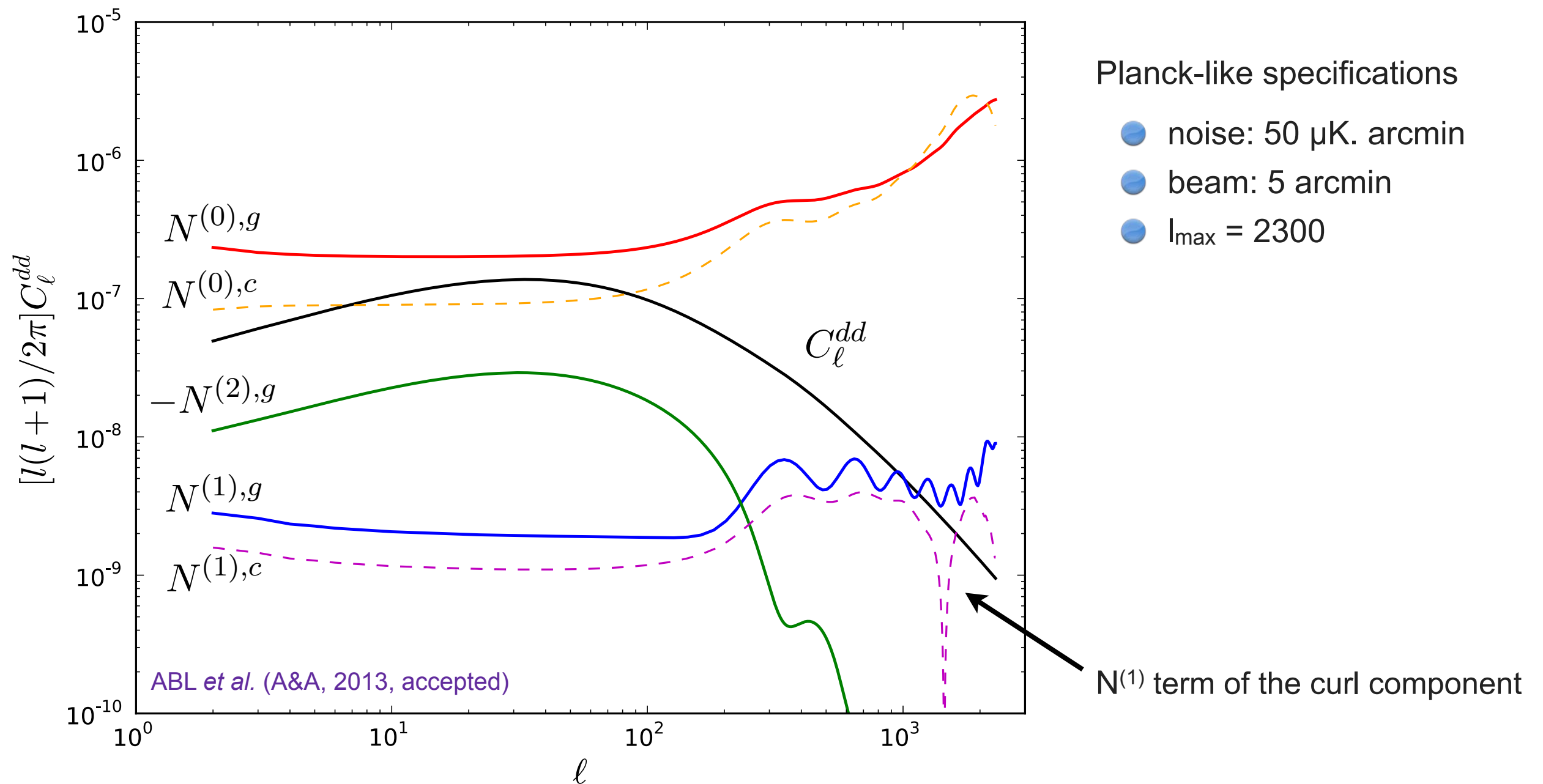
$$\langle \hat{\phi}_L^M \hat{\phi}_L^{M*} \rangle^C = N_L^{(0,C)} + N_L^{(1,C)} + \dots$$

Kesden et al. (2003), Hanson et al. (2011),
ABL et al. (A&A, 2013, accepted)

Lensing potential and biases



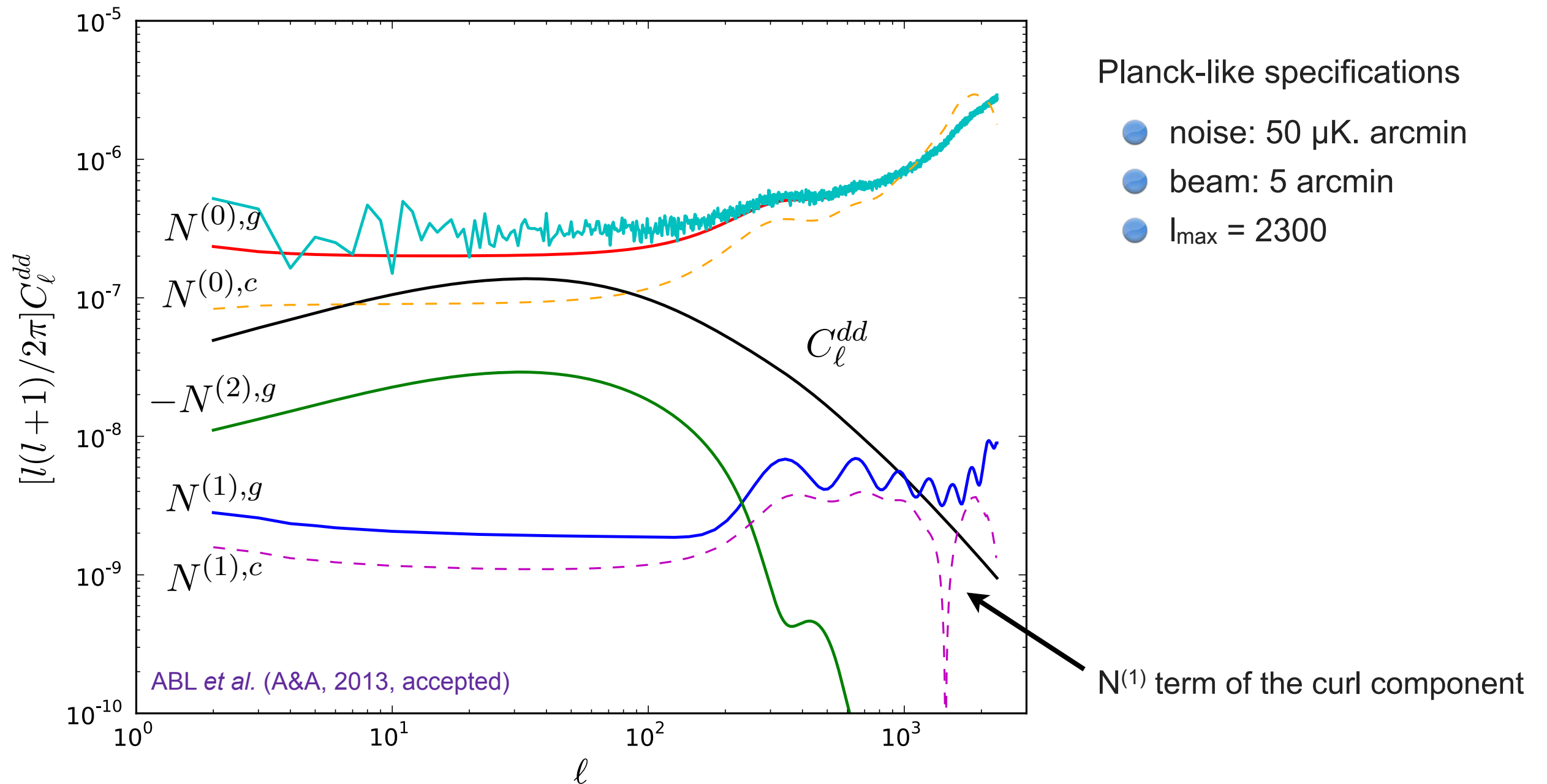
$$\langle \hat{\phi}_L^M \hat{\phi}_L^{M*} \rangle^G = C_L^{\phi\phi} + N_L^{(0,G)} + N_L^{(1,G)} + N_L^{(2,G)} + \dots$$



Lensing potential and biases



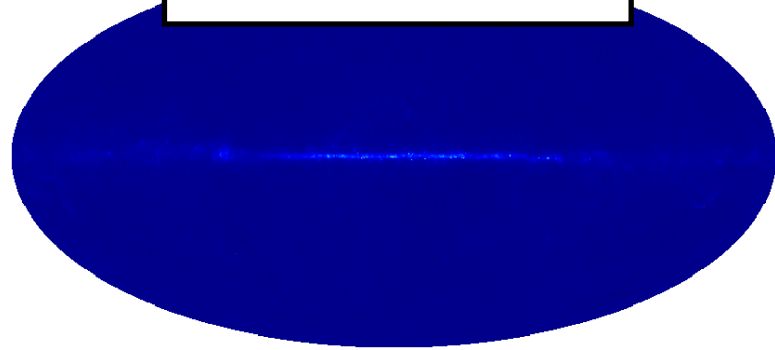
$$\langle \hat{\phi}_L^M \hat{\phi}_L^{M*} \rangle^G = C_L^{\phi\phi} + N_L^{(0,G)} + N_L^{(1,G)} + N_L^{(2,G)} + \dots$$



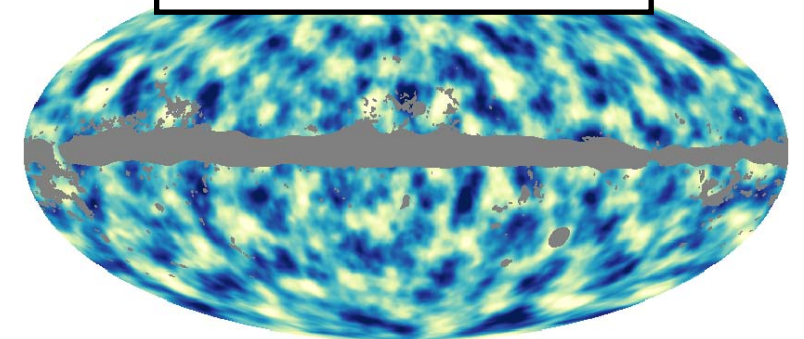
CMB lensing reconstruction with masks



Temperature



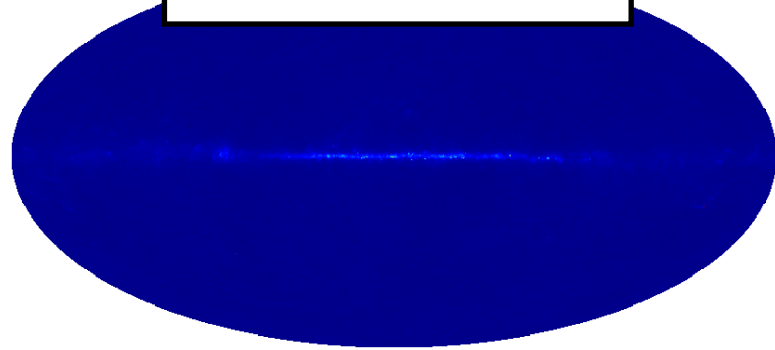
Lensing potential



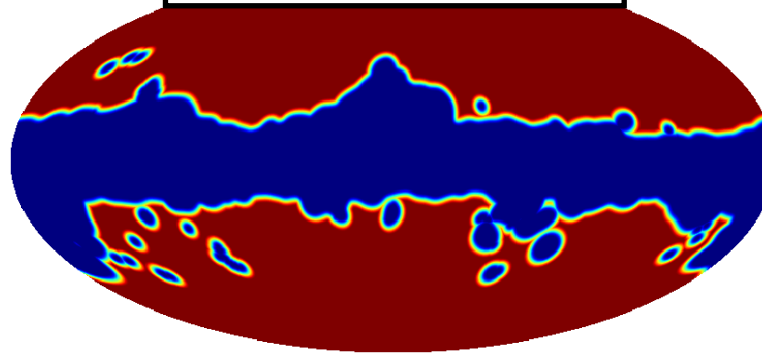
CMB lensing reconstruction



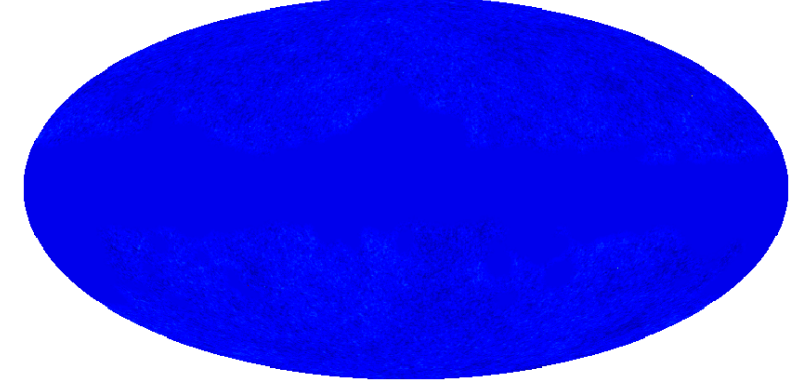
Temperature



Apodized Galactic mask



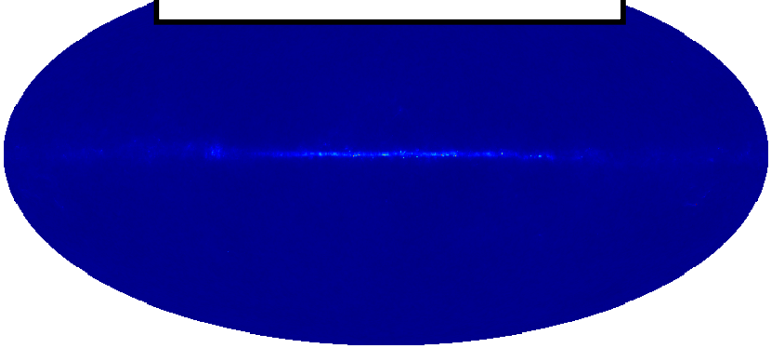
Mollweide view



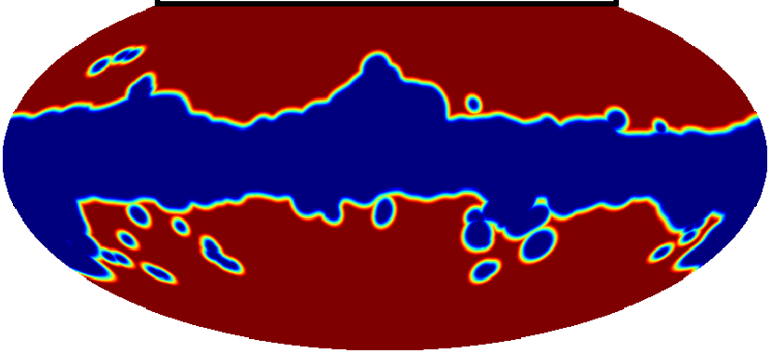
CMB lensing reconstruction



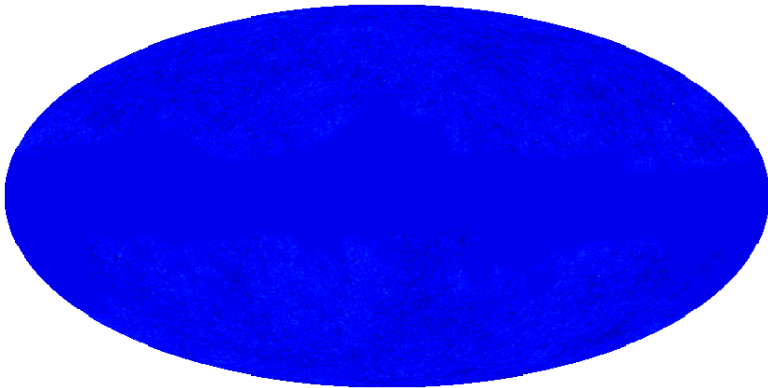
Temperature



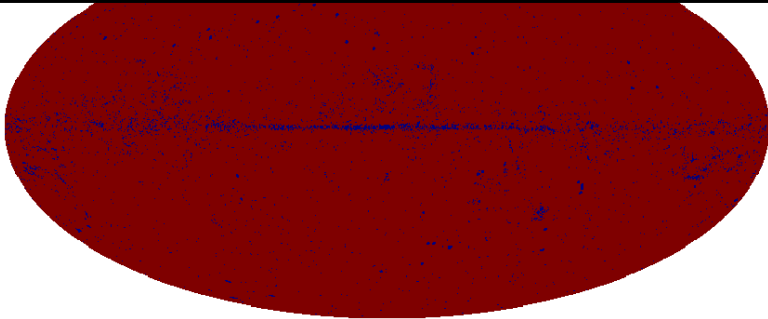
Apodized Galactic mask



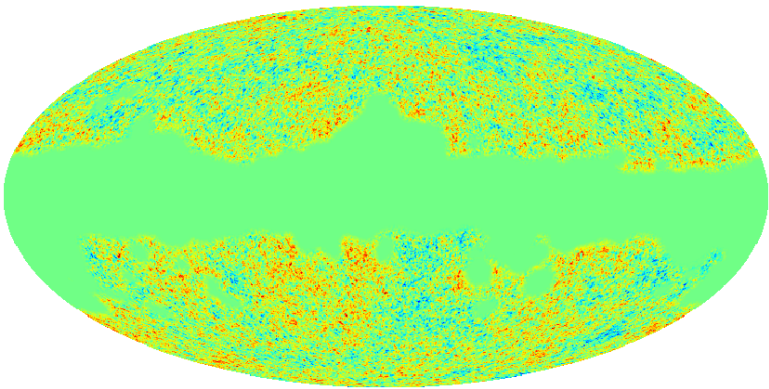
Mollweide view



Point sources mask + Gaussian constrained realizations



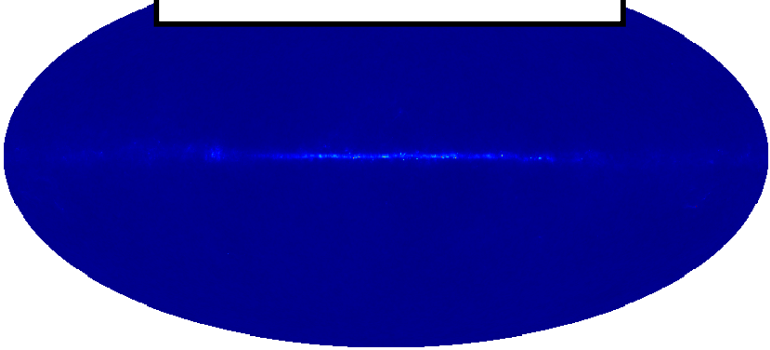
Mollweide view



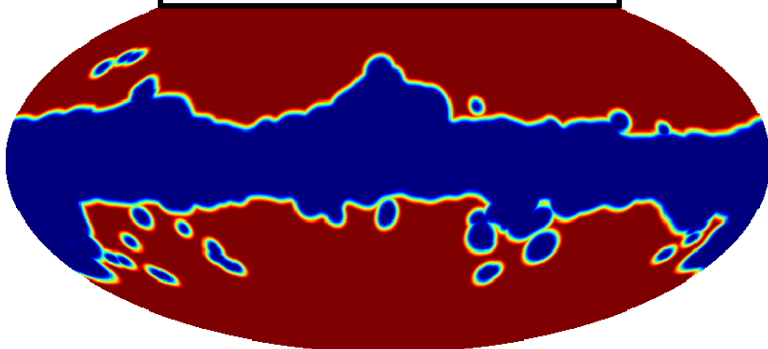
CMB lensing reconstruction



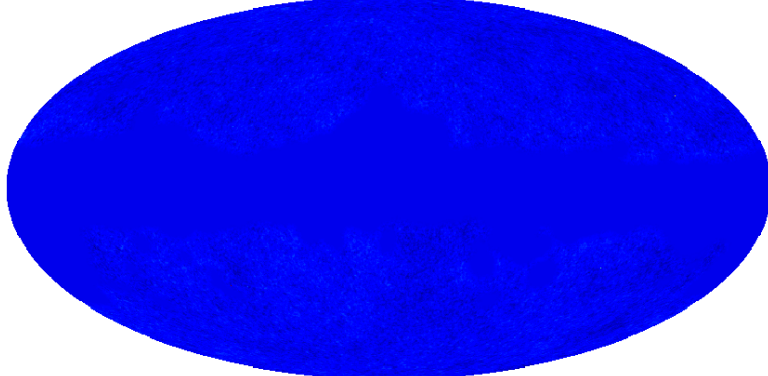
Temperature



Apodized Galactic mask

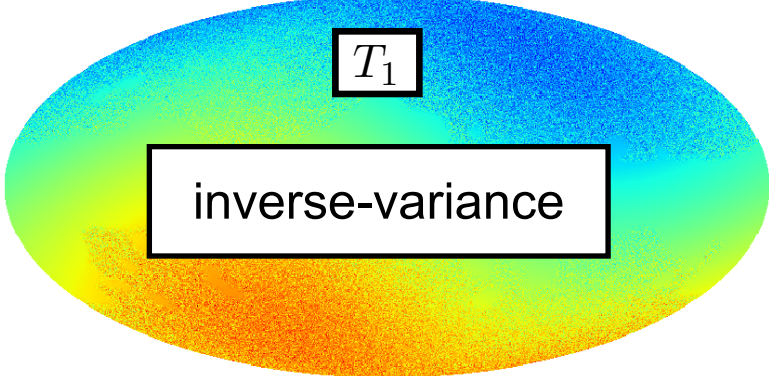


Mollweide view



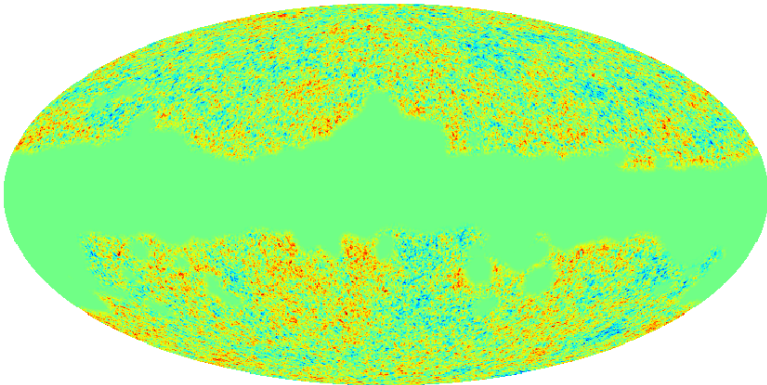
Filtering

Mollweide view

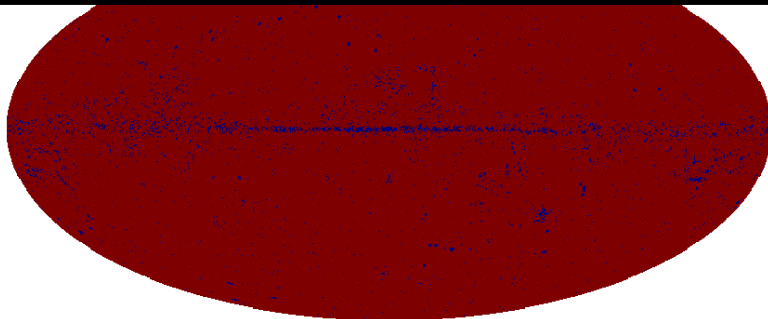


inverse-variance

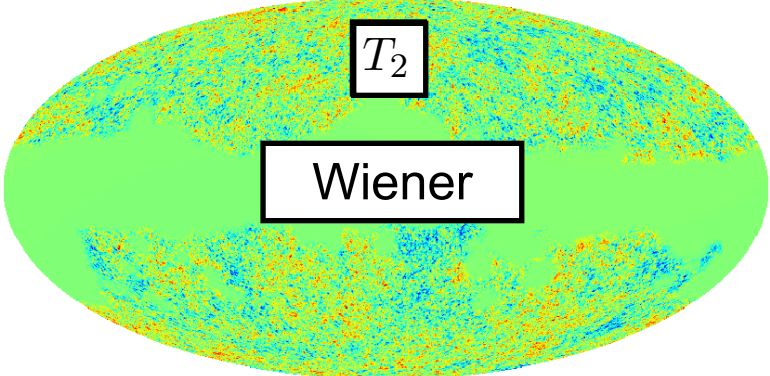
Mollweide view



Point sources mask + Gaussian constrained realizations



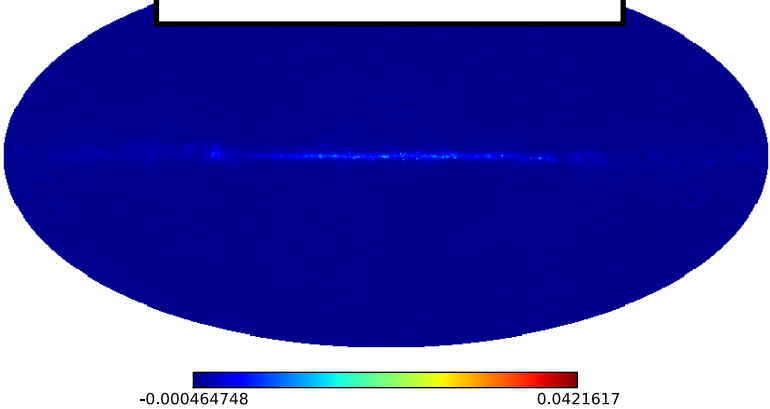
Mollweide view



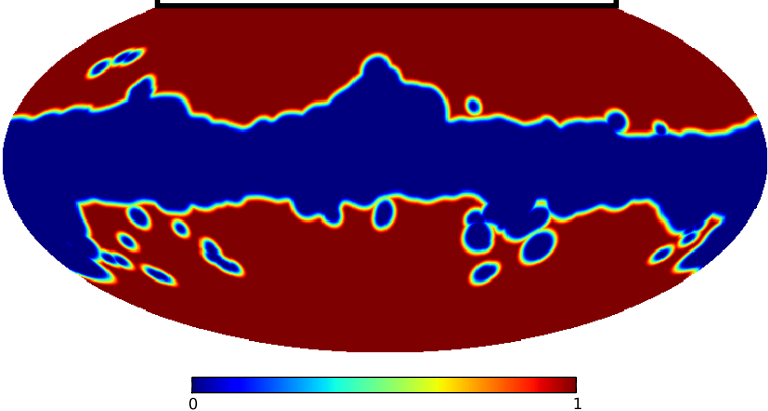
CMB lensing reconstruction



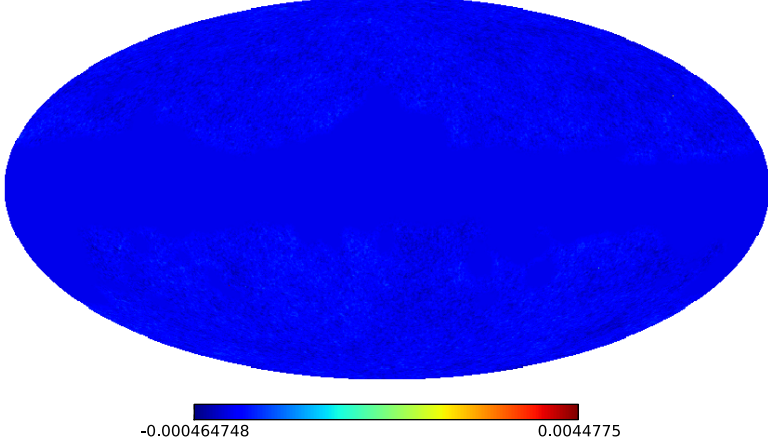
Temperature



Apodized Galactic mask

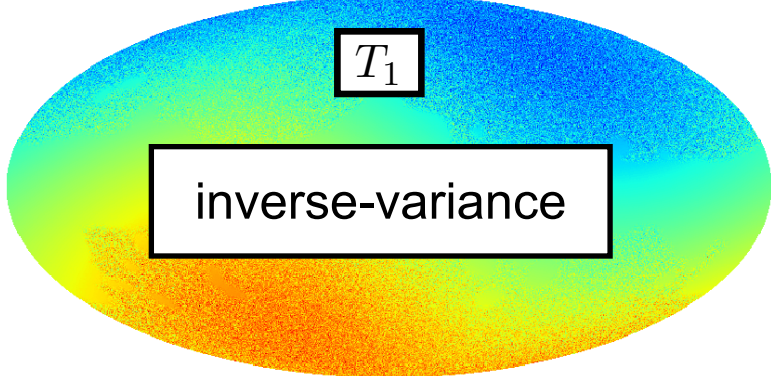


Mollweide view

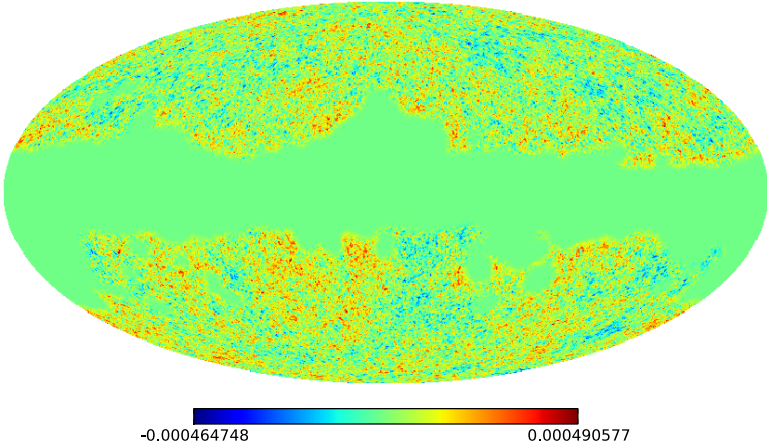


Filtering

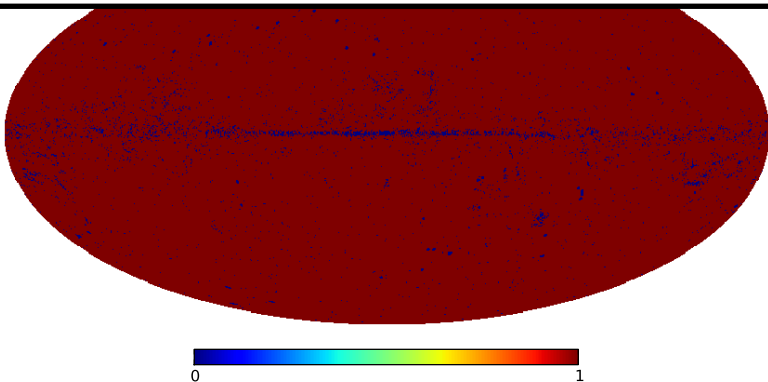
Mollweide view



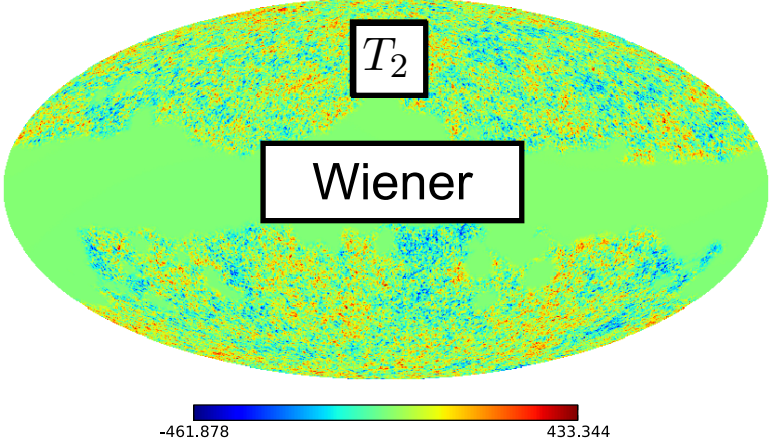
Mollweide view



Point sources mask + Gaussian constrained realizations



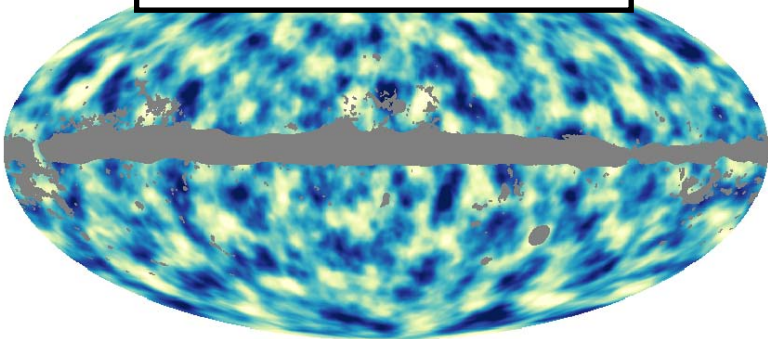
Mollweide view



Estimation

$$\hat{\phi} \propto \nabla \cdot (T_1 \nabla T_2)$$

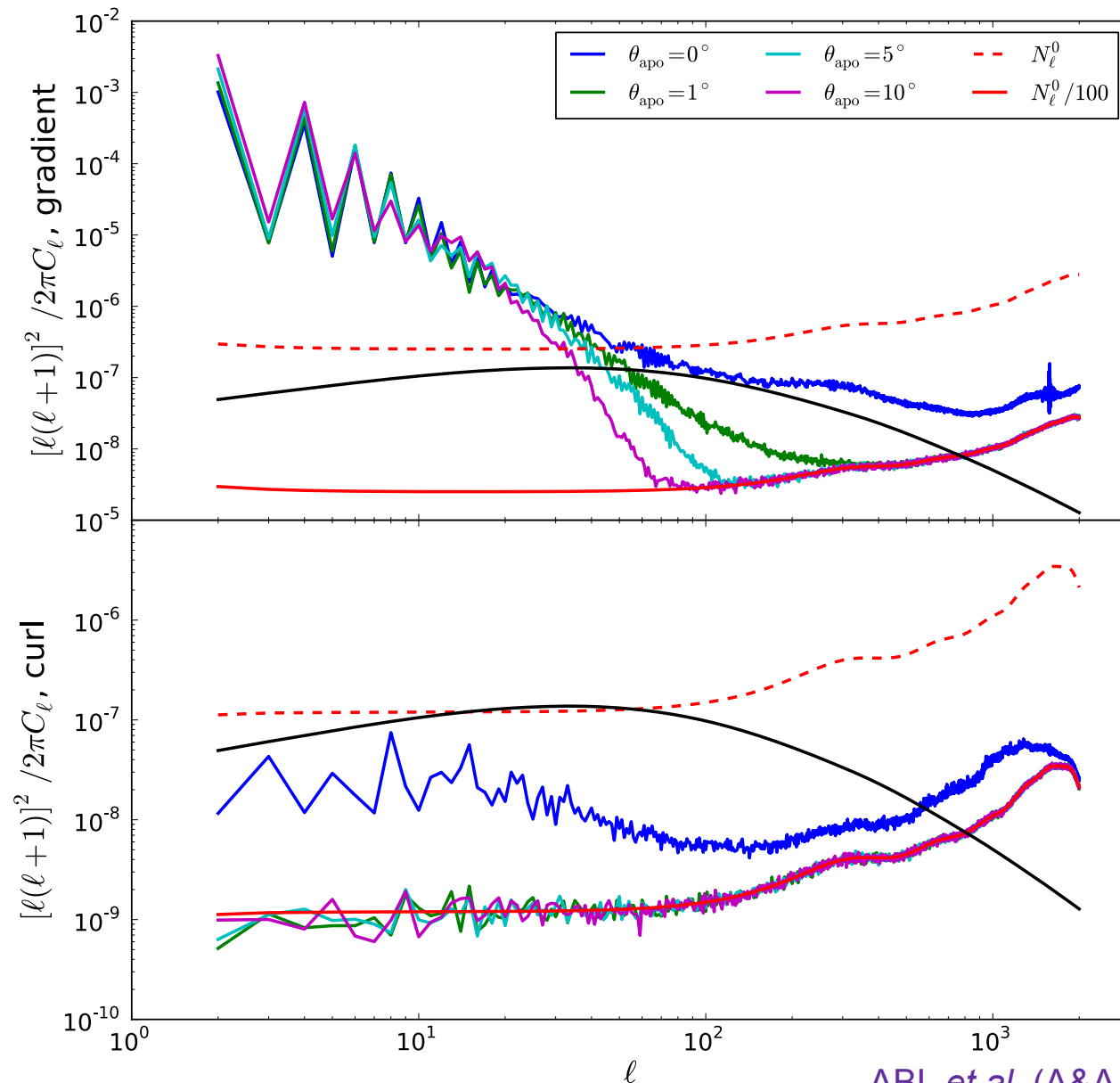
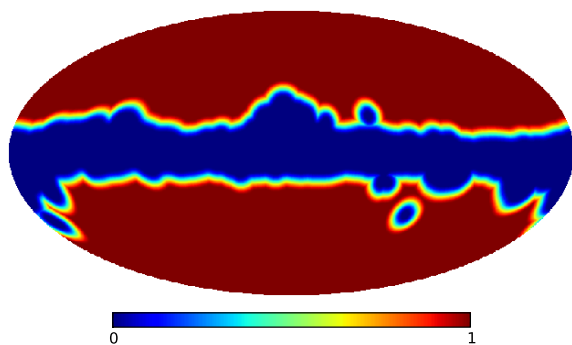
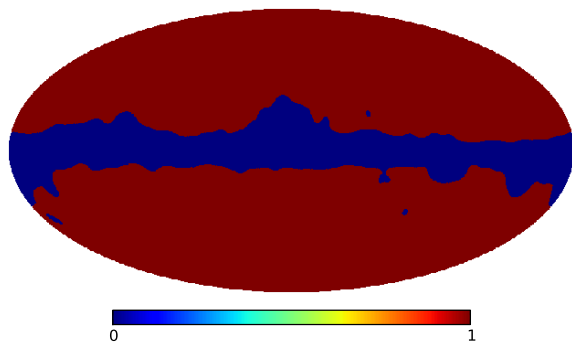
Lensing potential



Treatment of masks

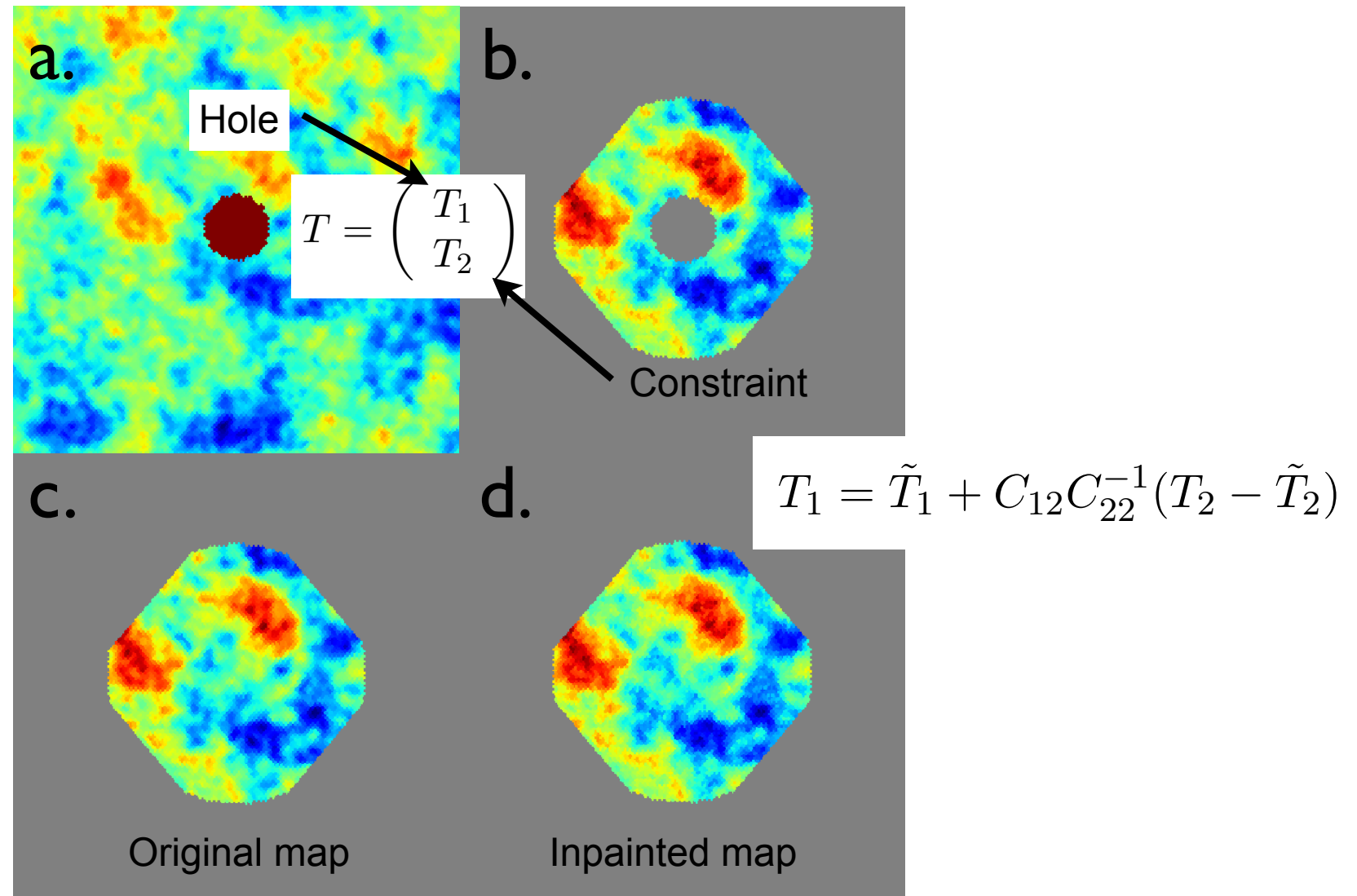
Galaxy

- Mask creates a bias in the estimator: mask mean field
- Apodized mask
- Apodization reduces mode couplings
- Mean-field can be efficiently subtracted





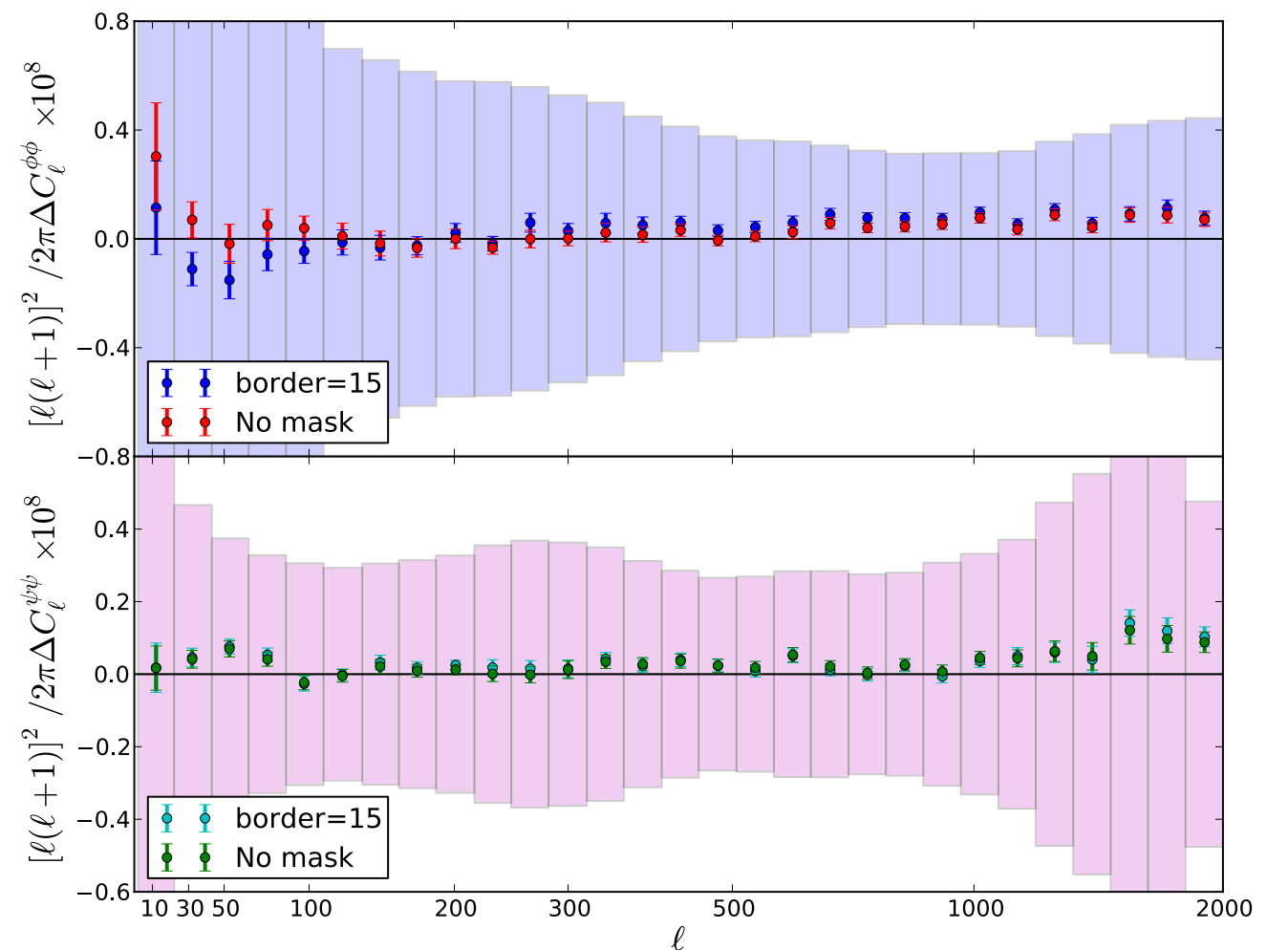
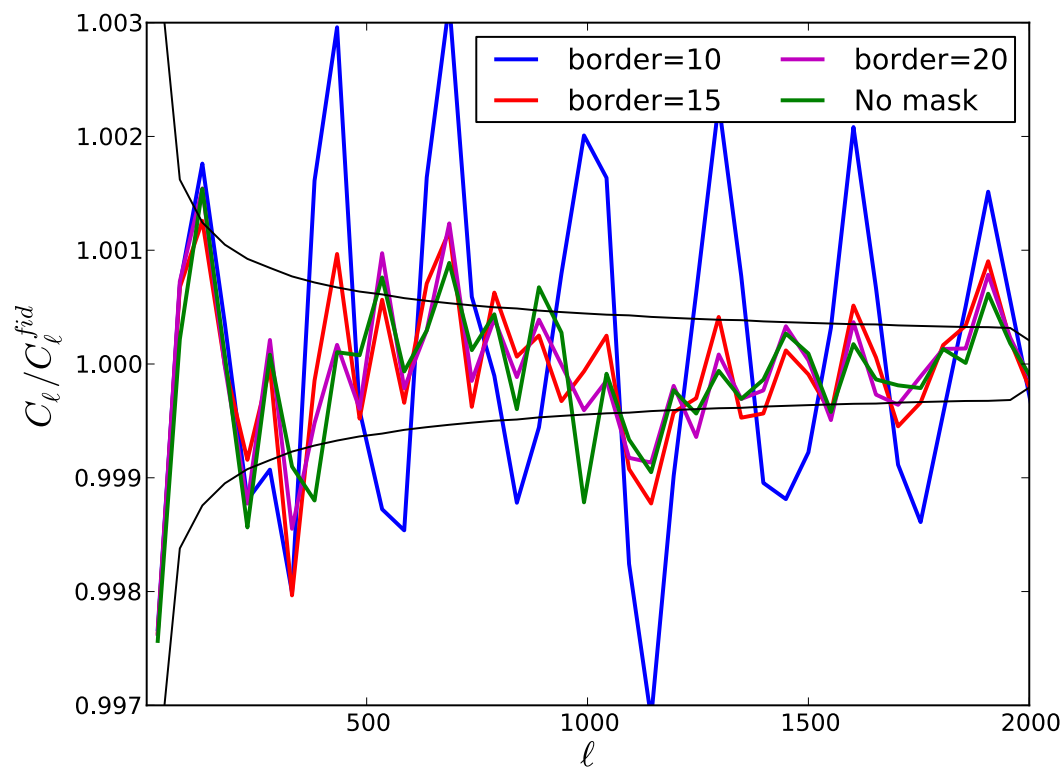
Point source inpainting

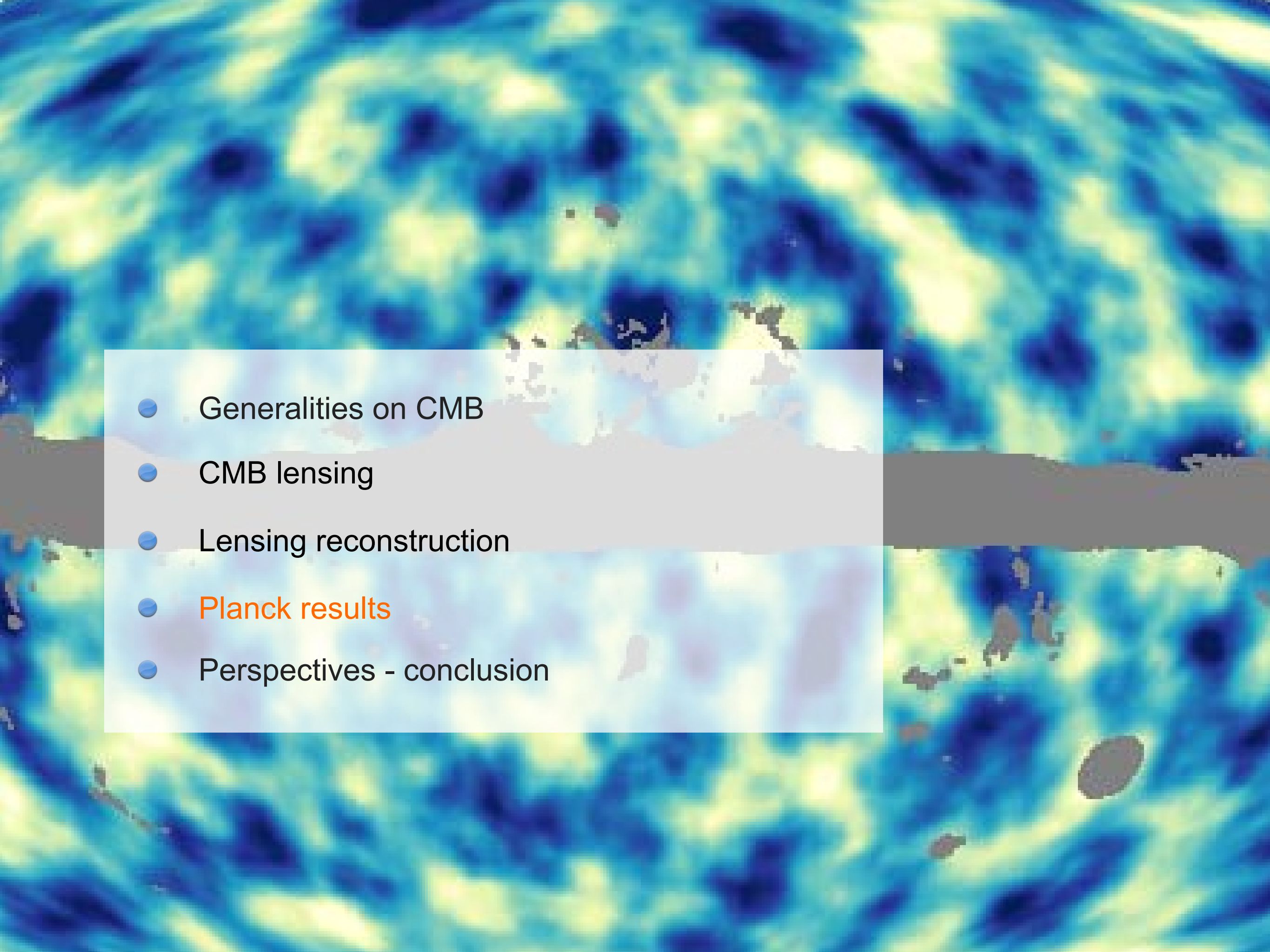


Treatment of masks

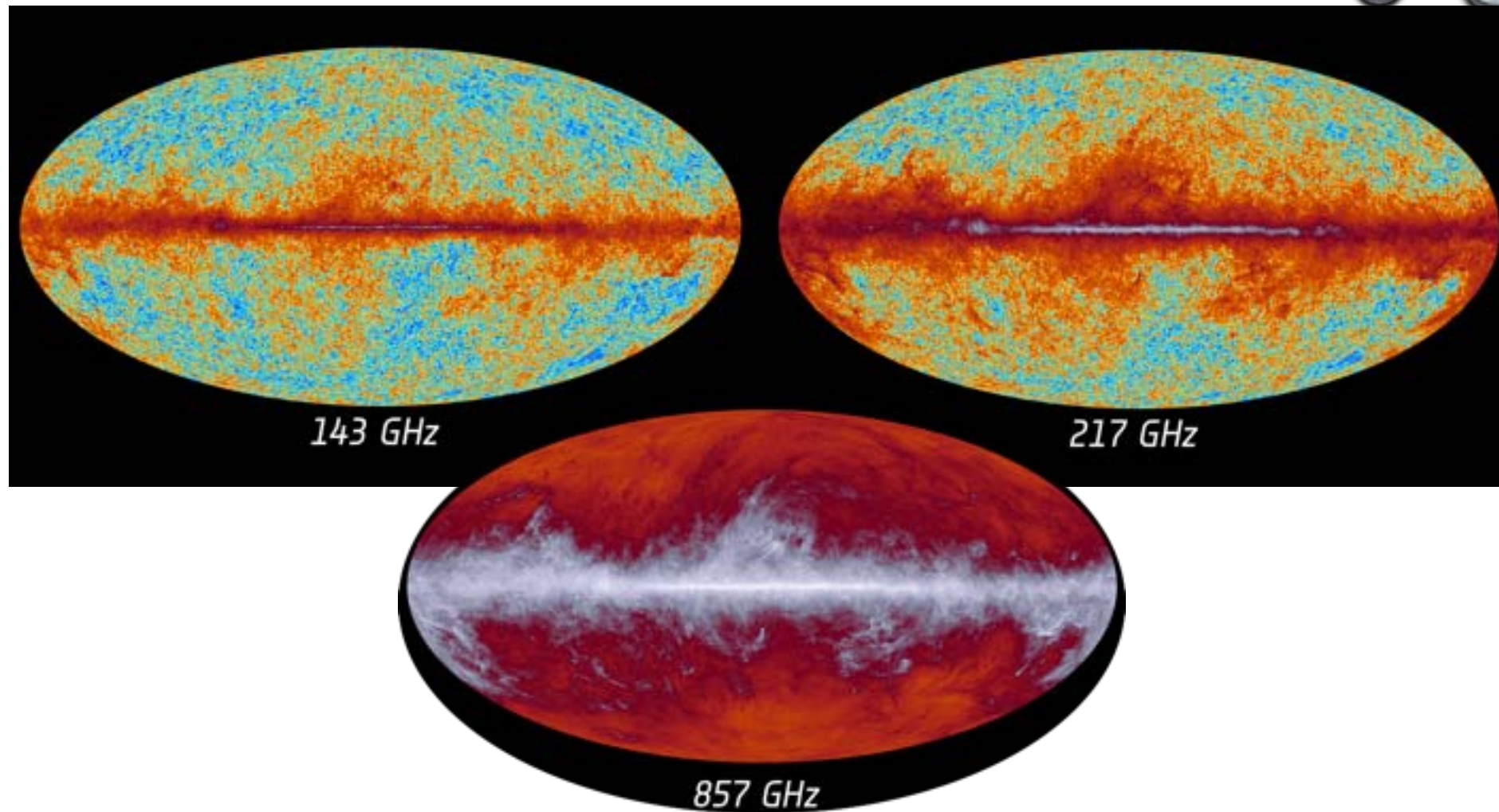
Point sources

- Fill in missing data with realistic simulated data
- Neighboring pixels used to generate constrained Gaussian realizations
- Two-point statistic is restored (i.e. power spectrum)
- Creates no bias in lensing estimator



- 
- The background of the slide is a full-frame image of the Cosmic Microwave Background (CMB) temperature fluctuations. It shows a complex, grainy pattern of blue and yellow colors, representing the distribution of matter and energy in the early universe. The pattern is isotropic and homogeneous, with small-scale fluctuations visible throughout.
- Generalities on CMB
 - CMB lensing
 - Lensing reconstruction
 - **Planck results**
 - Perspectives - conclusion

Fiducial data map



- Minimum-variance combination of 143GHz & 217GHz
- 857 GHz map used a template for dust cleaning
- 30% Galactic mask + CO + point sources
- 5° apodization (for lensing power spectrum estimation)

Some technical details

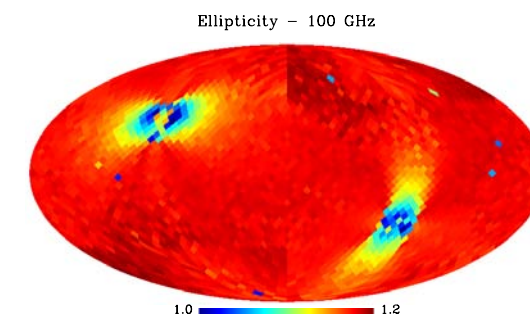
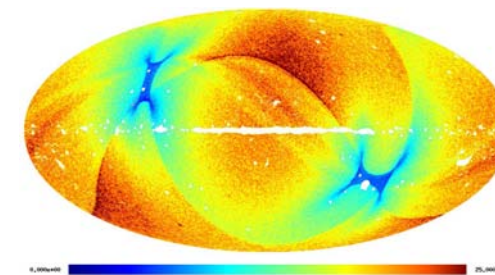
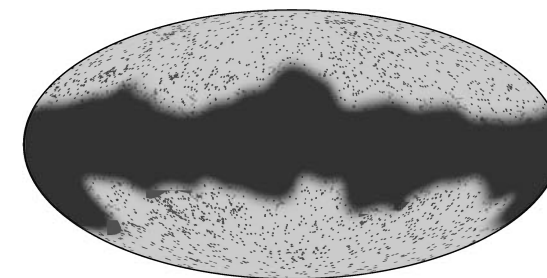
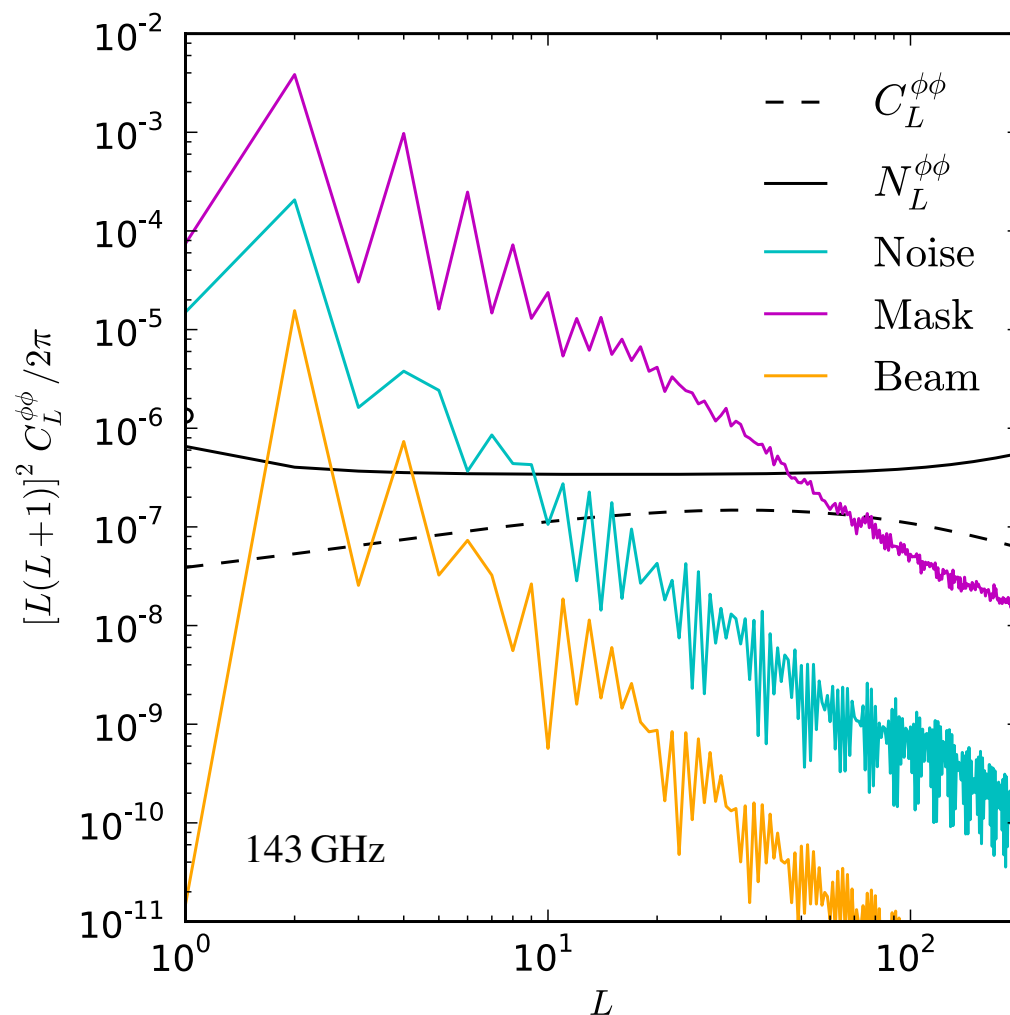
$$\hat{\phi}_{LM}^x = \frac{1}{\mathcal{R}_L^{x\phi}} \left(\bar{x}_{LM} - \bar{x}_{LM}^{MF} \right).$$

$$\mathcal{R}_L^{x\phi,(1)(2)} = \frac{1}{(2L+1)} \sum_{\ell_1 \ell_2} \frac{1}{2} W_{\ell_1 \ell_2 L}^x W_{\ell_1 \ell_2 L}^\phi F_{\ell_1}^{(1)} F_{\ell_2}^{(2)}.$$

$$\bar{x}_{LM} = \frac{1}{2} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^x \bar{T}_{\ell_1 m_1}^{(1)} \bar{T}_{\ell_2 m_2}^{(2)}.$$

$$\bar{x}_{LM}^{MF} = \frac{1}{2} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^x \langle \bar{T}_{\ell_1 m_1}^{(1)} \bar{T}_{\ell_2 m_2}^{(2)} \rangle.$$

$$\bar{T}_{\ell m} = [S + N]^{-1} T_{\ell m} \approx [C_\ell^{TT} + C_\ell^{NN}]^{-1} T_{\ell m} = F_\ell T_{\ell m}$$





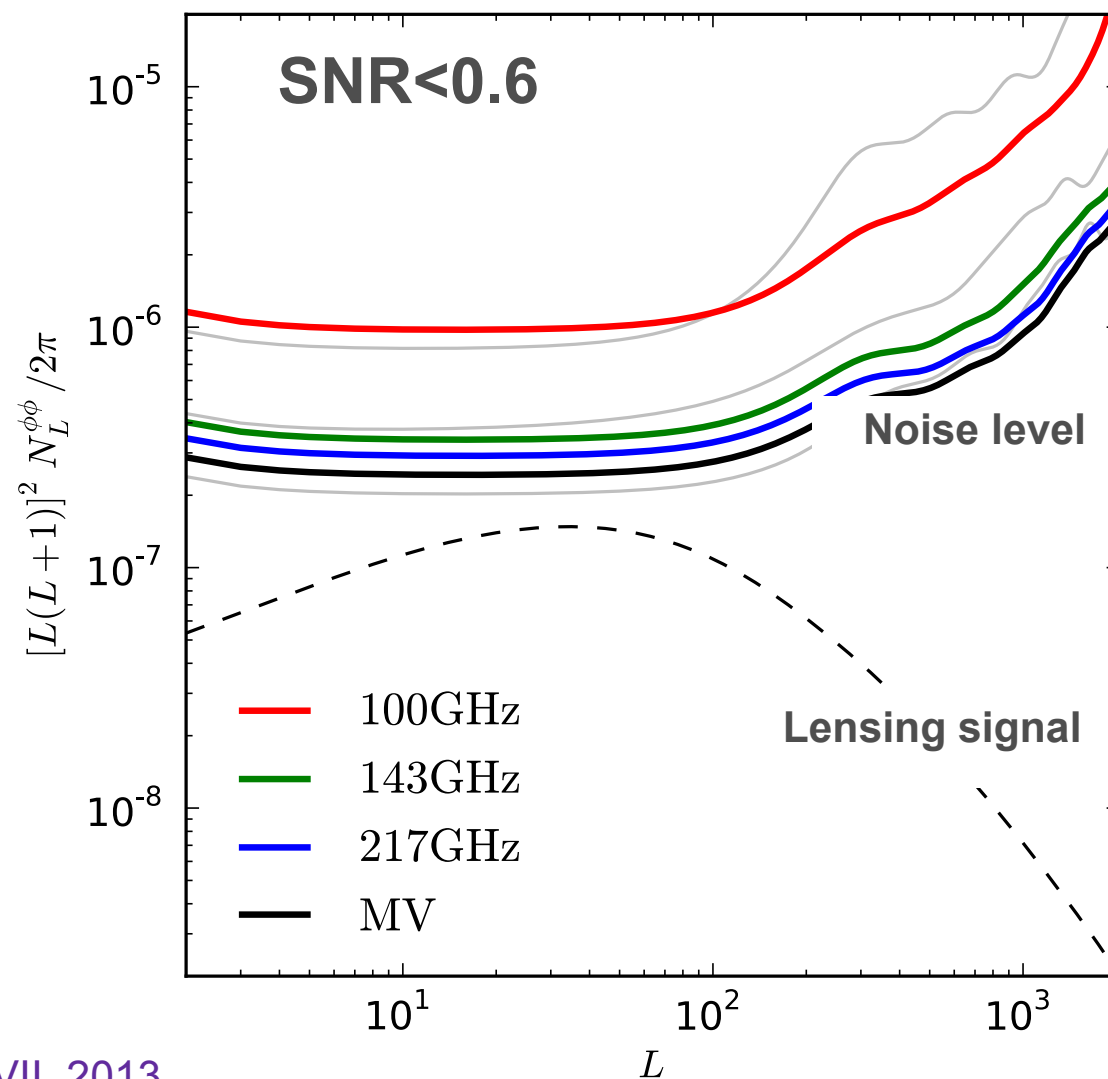
$$\hat{\phi}_{LM}^x = \frac{1}{\mathcal{R}_L^{x\phi}} (\bar{x}_{LM} - \bar{x}_{LM}^{MF}).$$

$$\mathcal{R}_L^{x\phi,(1)(2)} = \frac{1}{(2L+1)} \sum_{\ell_1 \ell_2} \frac{1}{2} W_{\ell_1 \ell_2 L}^x W_{\ell_1 \ell_2 L}^\phi F_{\ell_1}^{(1)} F_{\ell_2}^{(2)}.$$

$$\bar{x}_{LM} = \frac{1}{2} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^x \bar{T}_{\ell_1 m_1}^{(1)} \bar{T}_{\ell_2 m_2}^{(2)}.$$

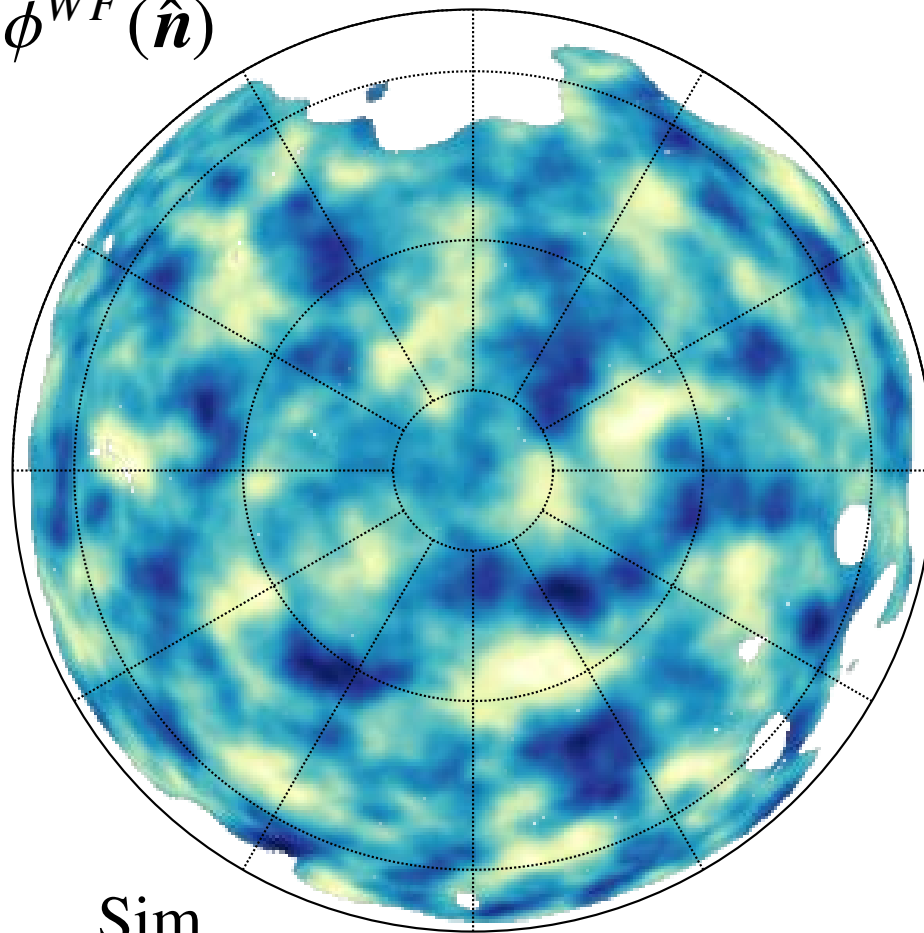
$$\bar{x}_{LM}^{MF} = \frac{1}{2} \sum_{\ell_1 m_1, \ell_2 m_2} (-1)^M \begin{pmatrix} \ell_1 & \ell_2 & L \\ m_1 & m_2 & -M \end{pmatrix} W_{\ell_1 \ell_2 L}^x \langle \bar{T}_{\ell_1 m_1}^{(1)} \bar{T}_{\ell_2 m_2}^{(2)} \rangle.$$

$$\bar{T}_{\ell m} = [S + N]^{-1} T_{\ell m} \approx [C_\ell^{TT} + C_\ell^{NN}]^{-1} T_{\ell m} = F_\ell T_{\ell m}$$

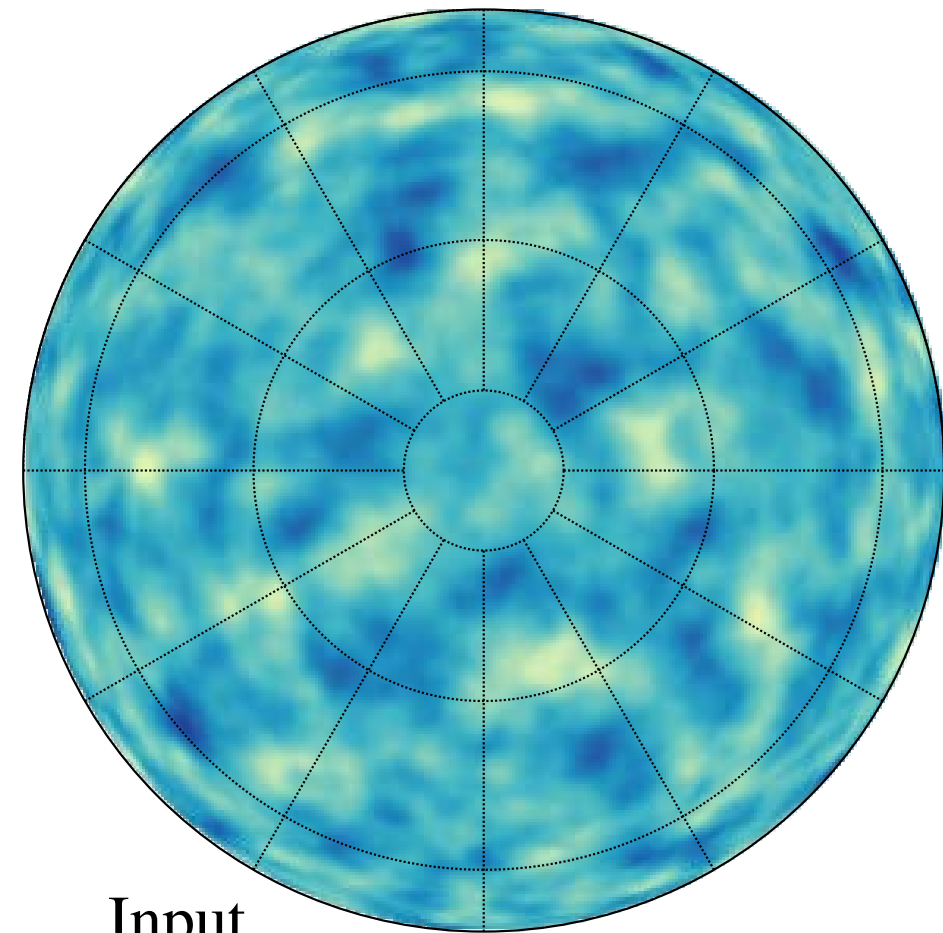




$$\phi^{WF}(\hat{n})$$



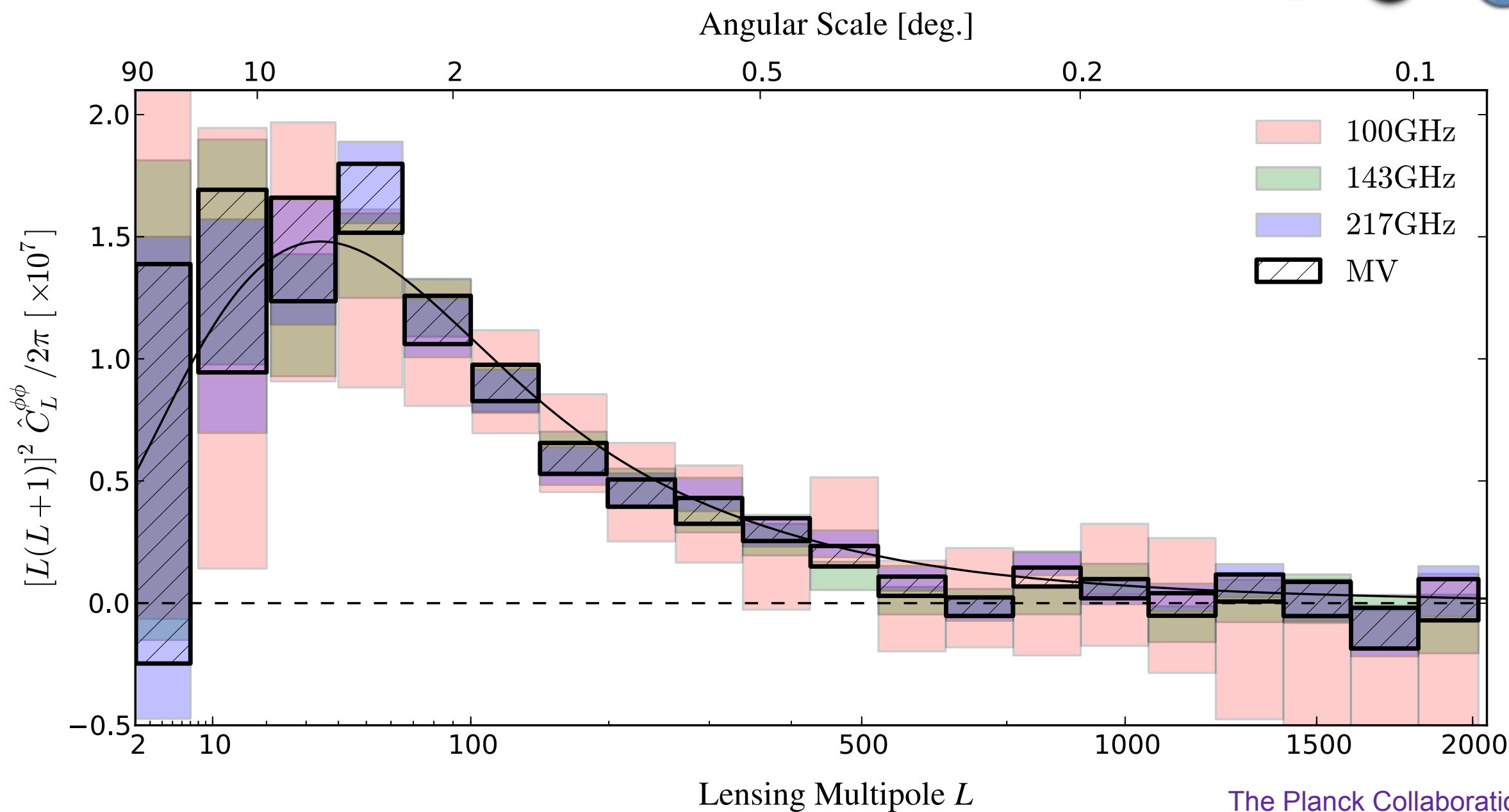
Sim



Input

Reconstruction on a realistic Planck simulation

Cosmological constraints

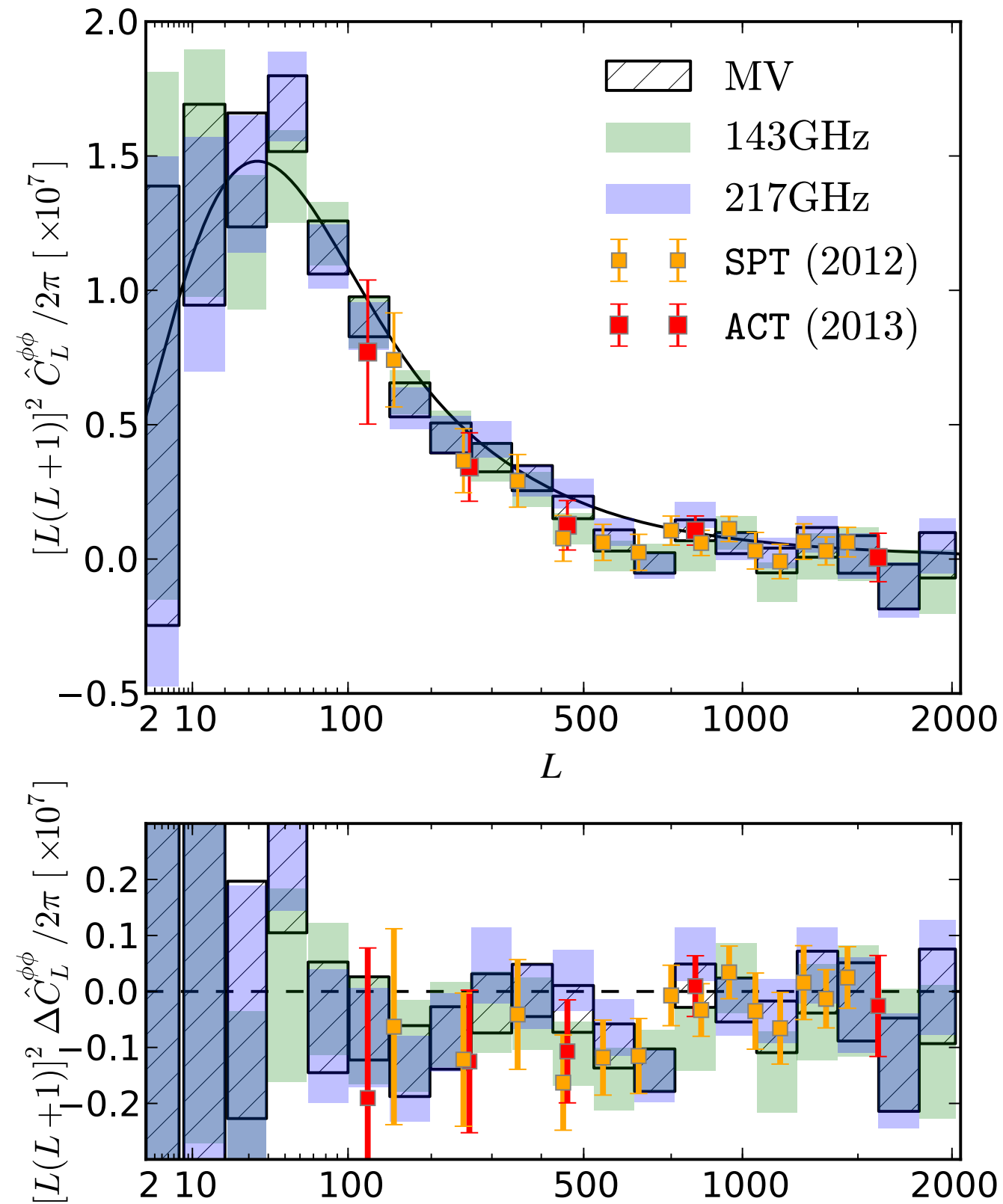


The Planck Collaboration XVII, 2013

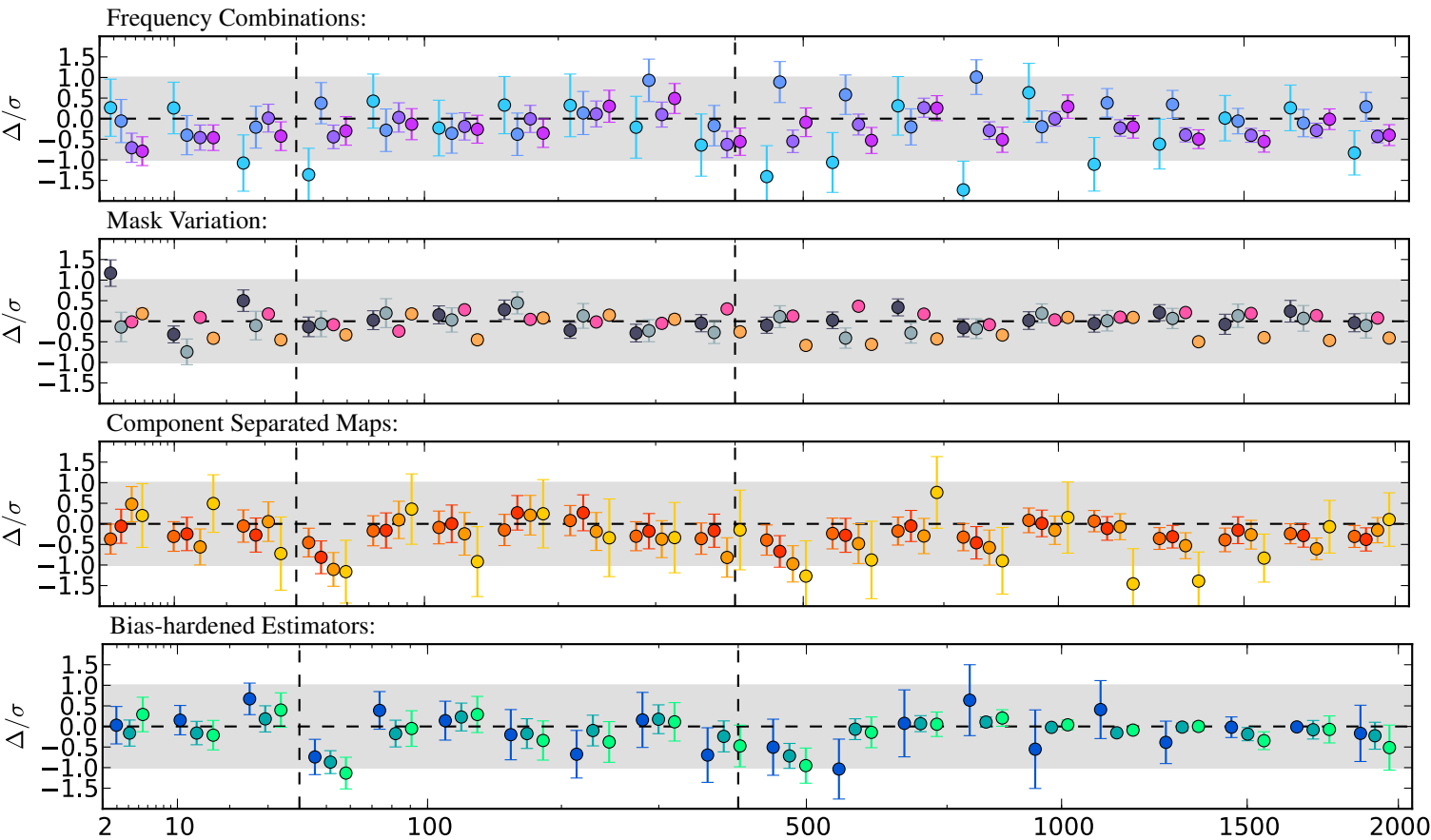
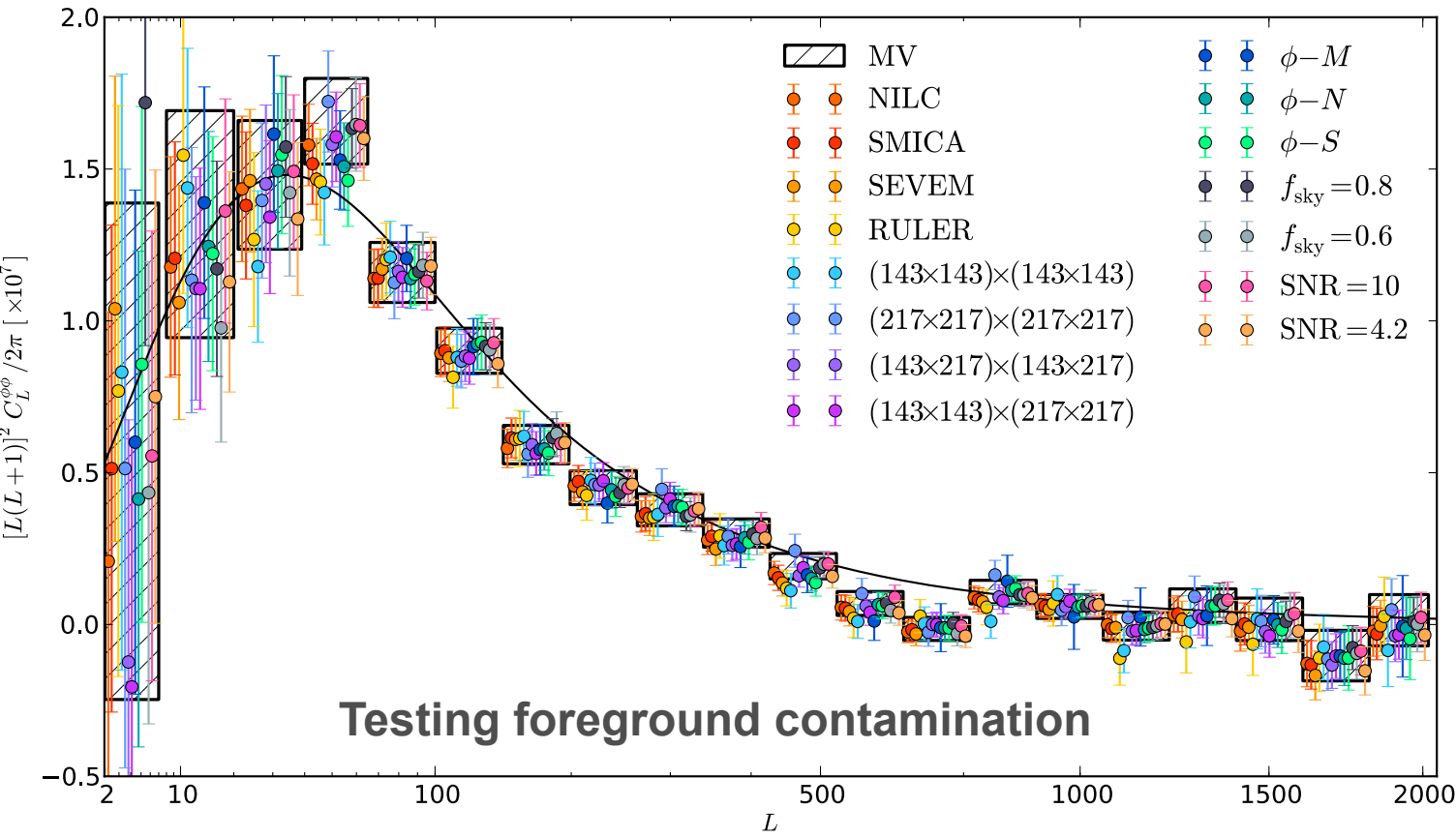
- Agreement between 3 frequencies
- Agreement with the prediction
- New cosmological constraints

$$\hat{A}_{40 \rightarrow 400} = 0.94 \pm 0.04$$

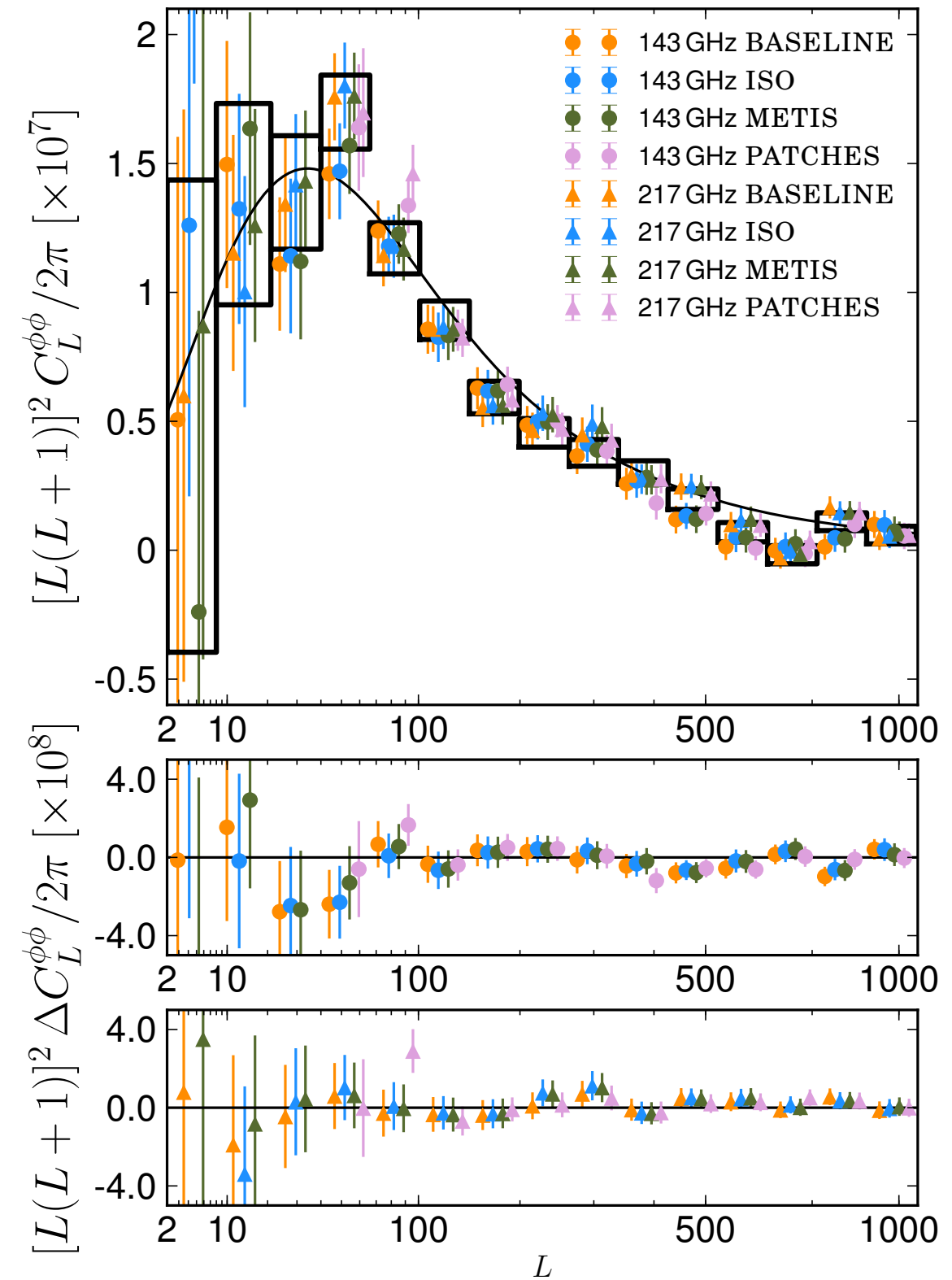
Comparison to ACT and SPT



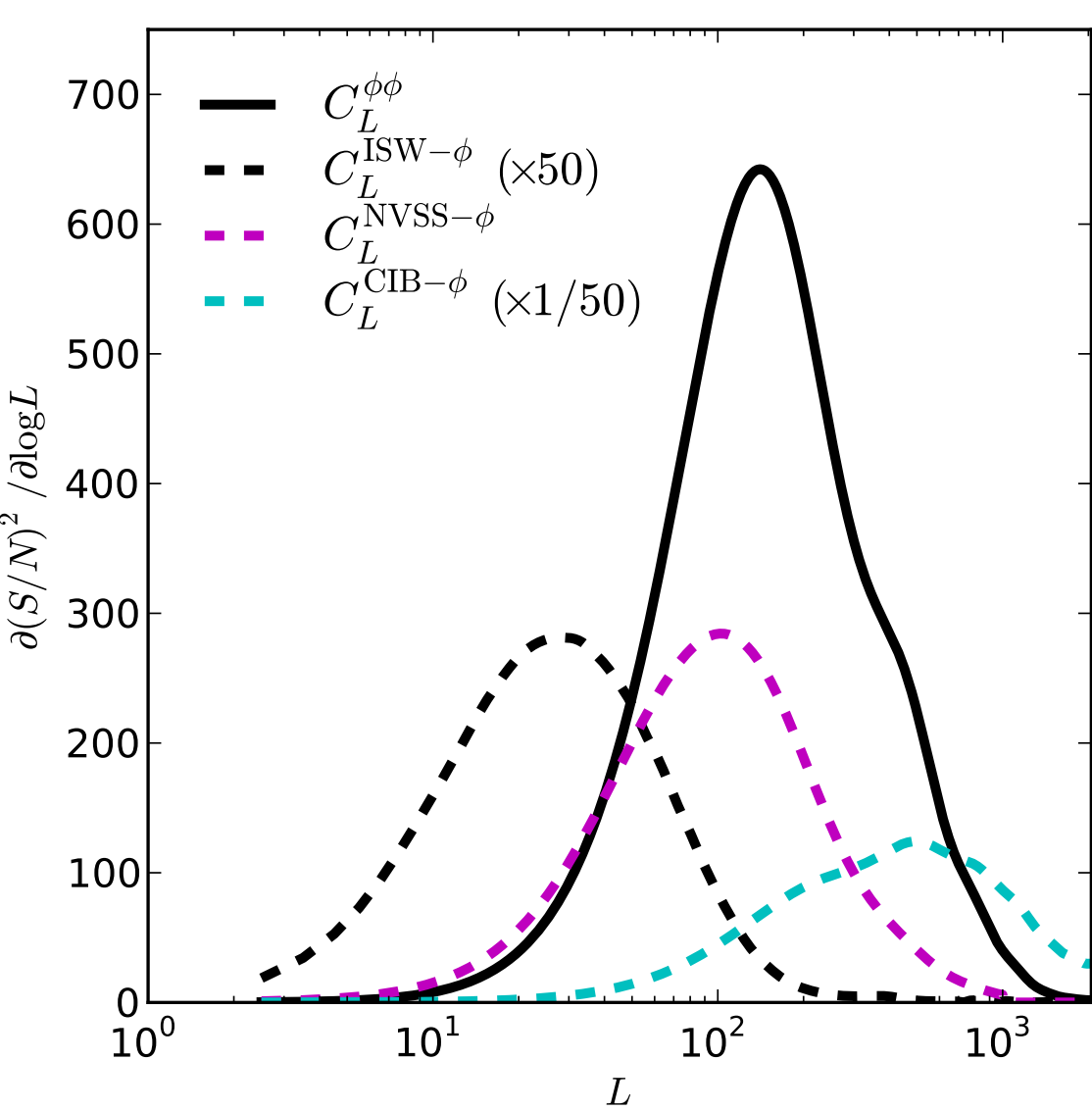
Robustness



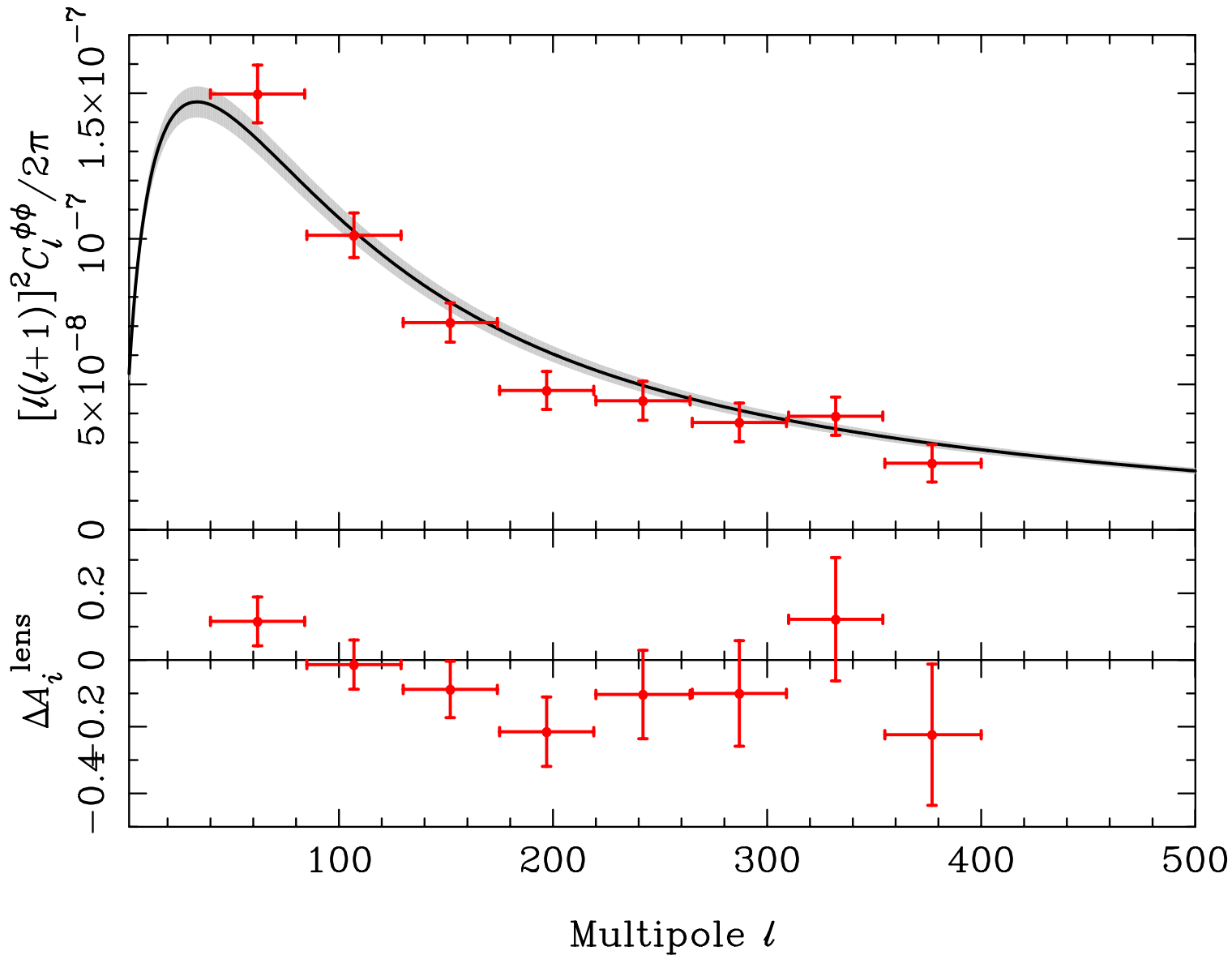
Testing the filter & implementation



Lensing likelihood



The Planck Collaboration XVII, 2013

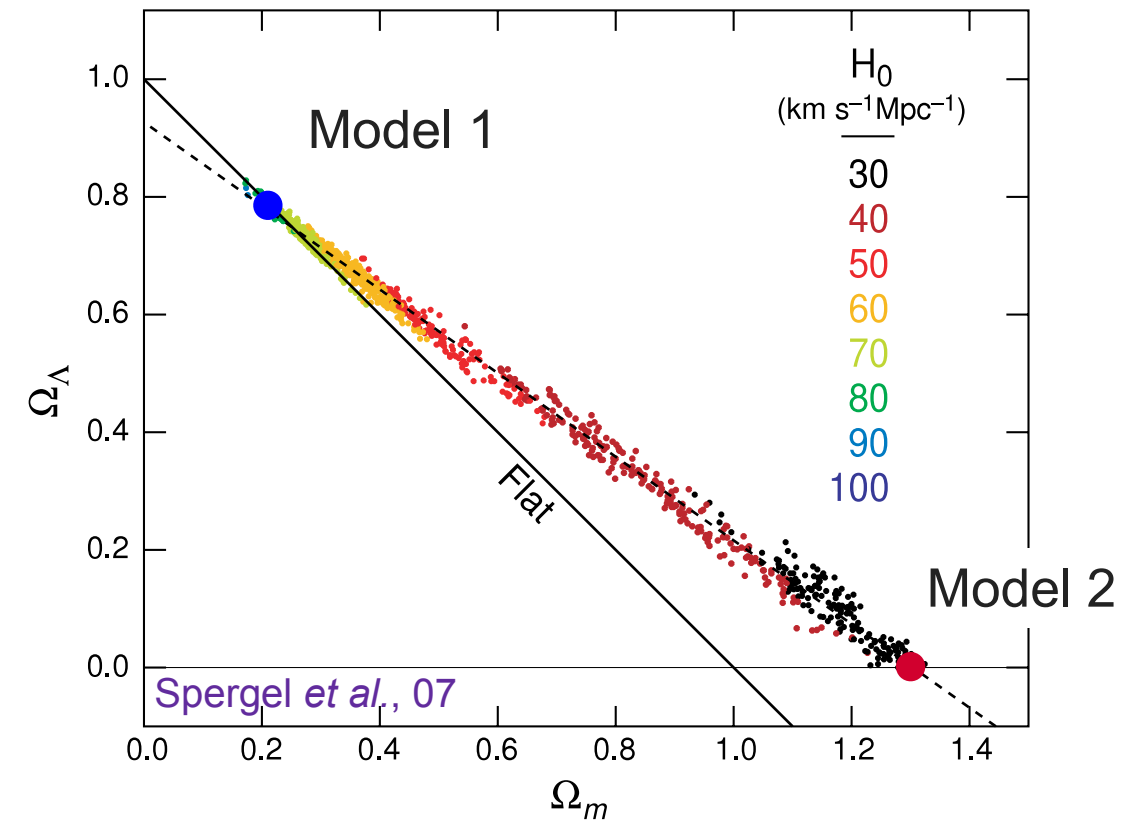
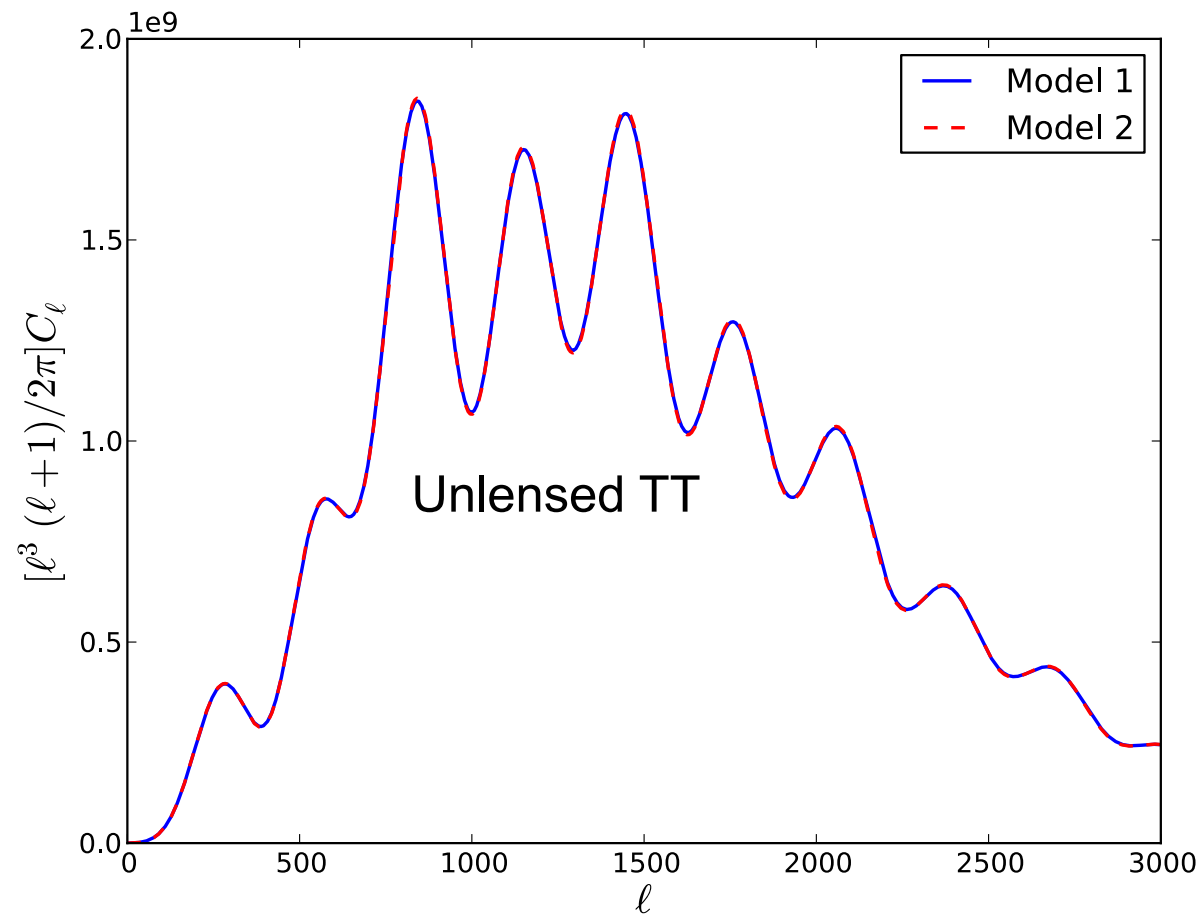


The Planck Collaboration XVI, 2013

Cosmological information from CMB lensing



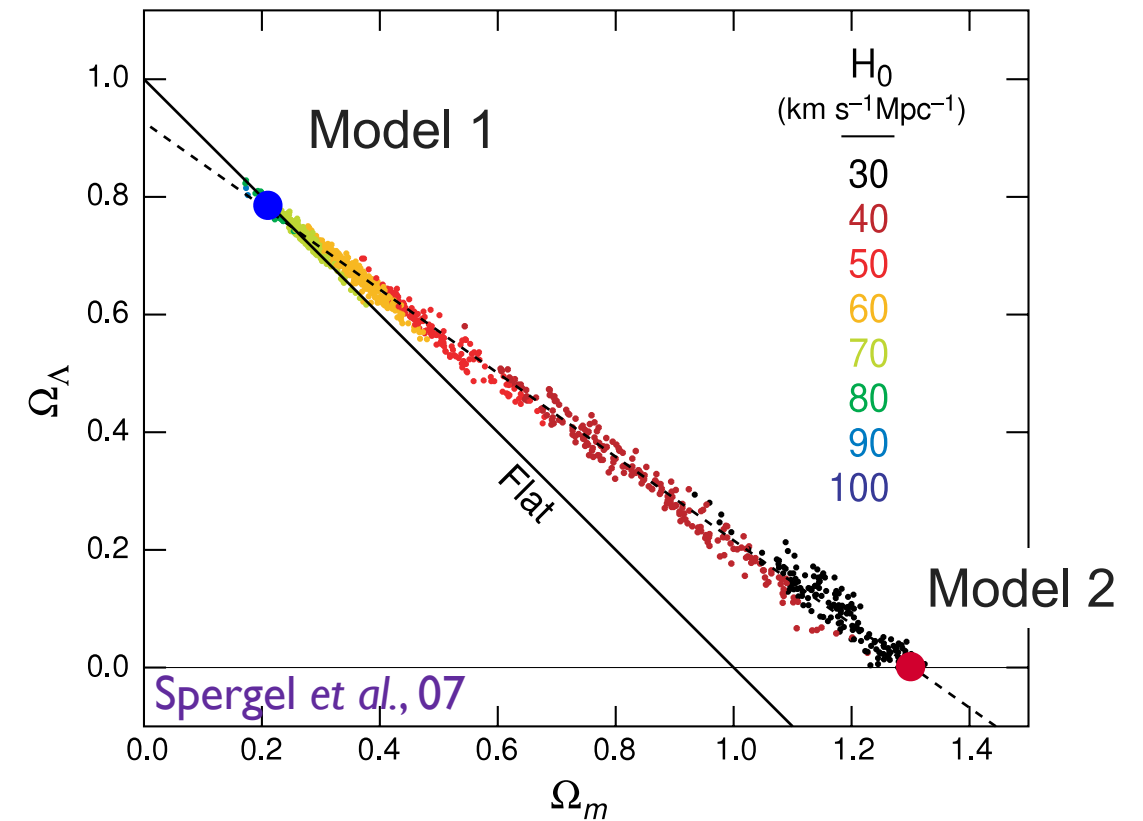
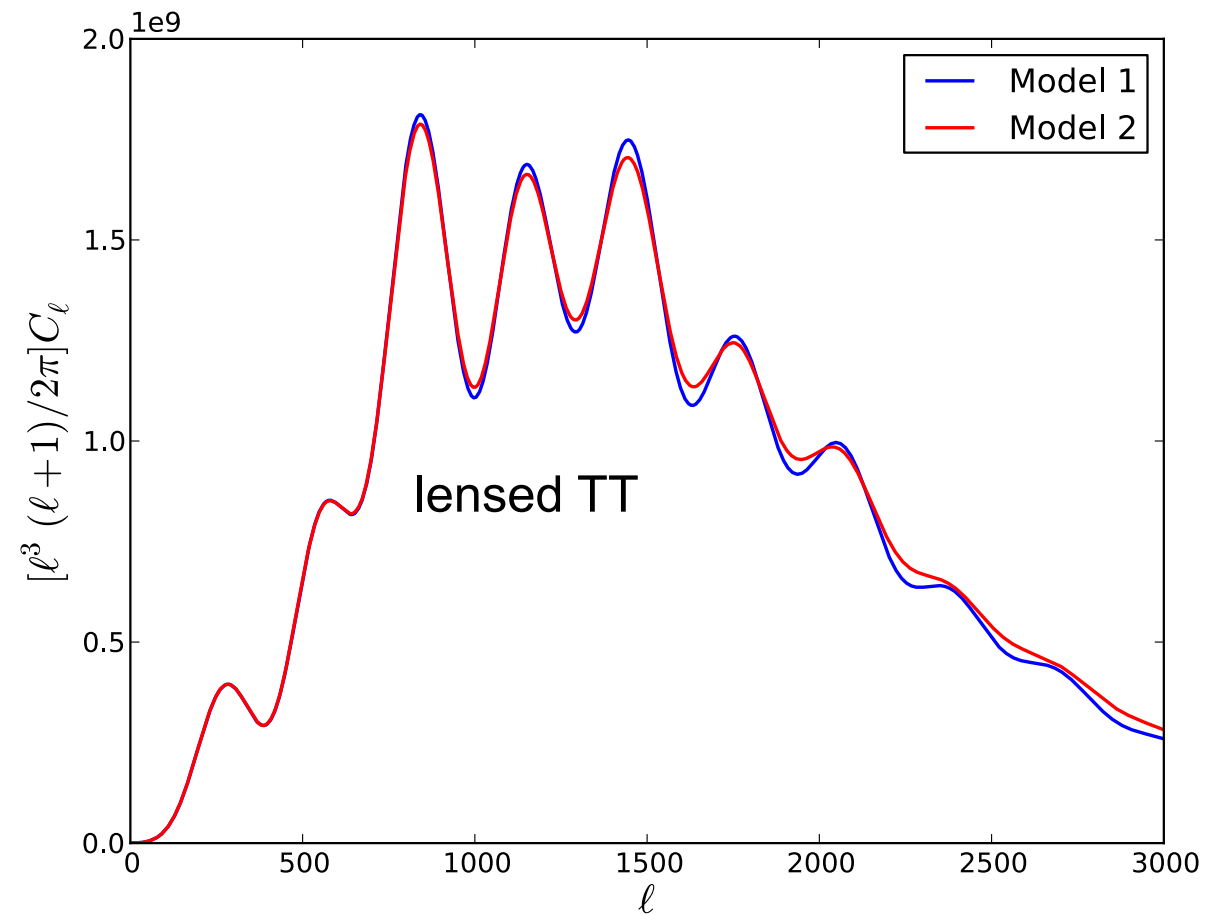
«Lensing breaks diameter degeneracy»



Cosmological information from CMB lensing



«Lensing breaks diameter degeneracy»

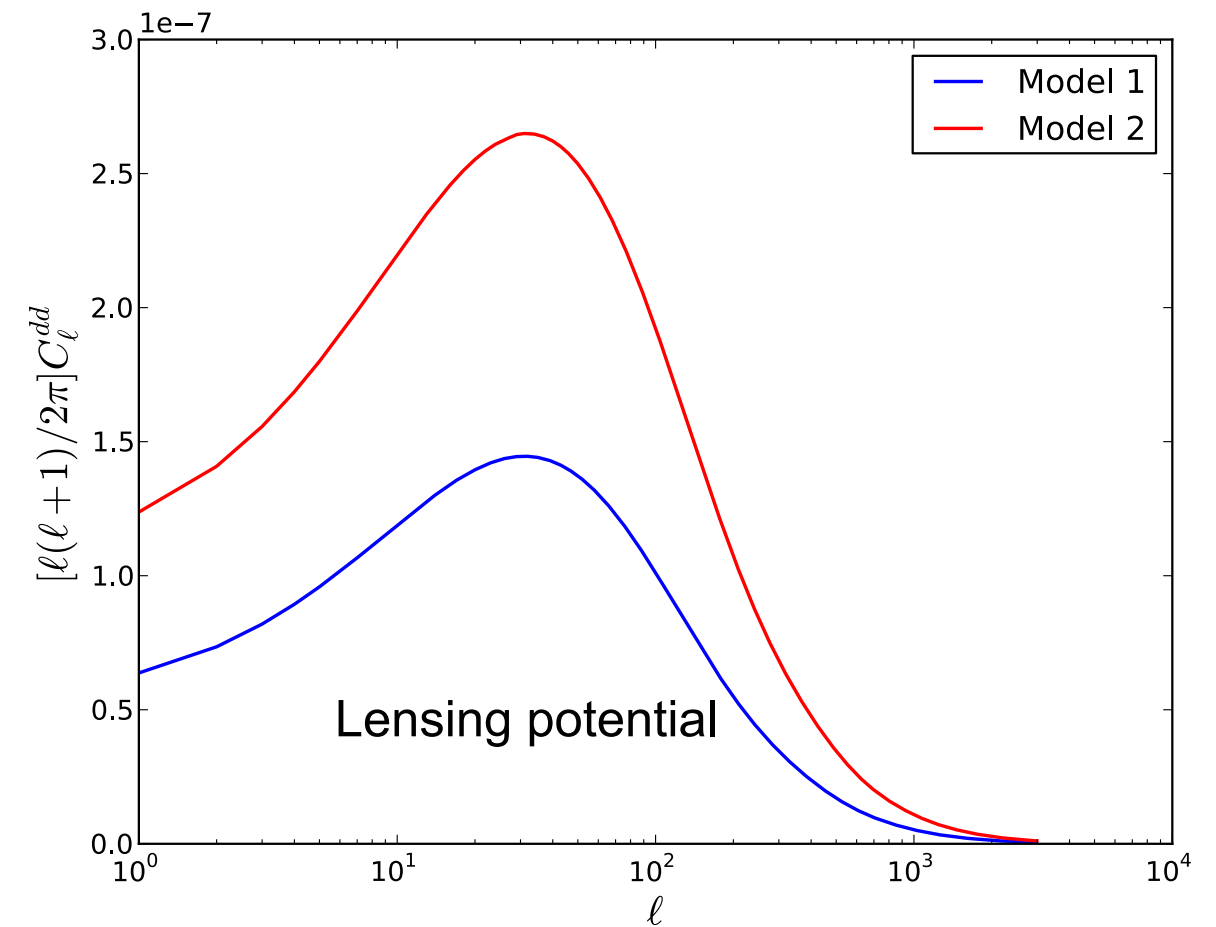
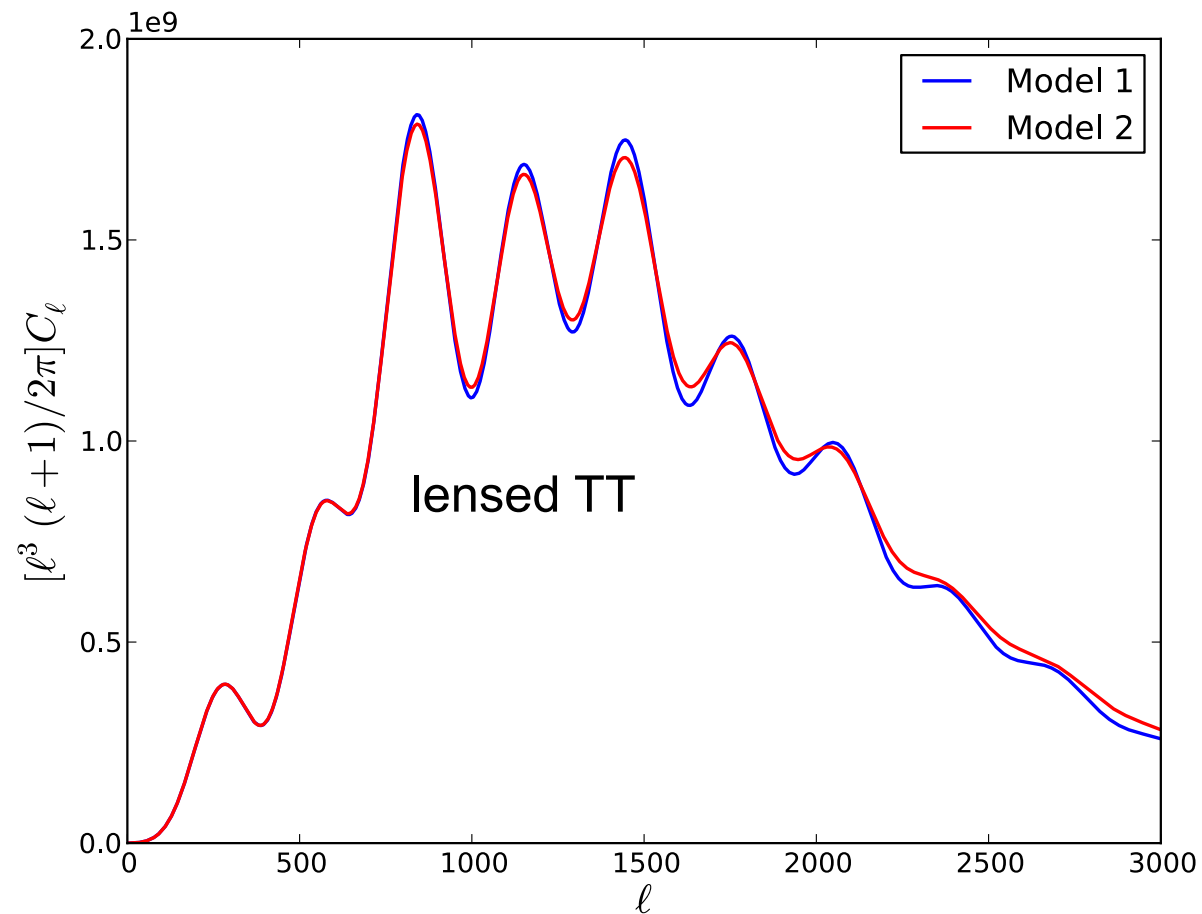


If lensed power spectra are different, that's because of lensing potential

Cosmological information from CMB lensing



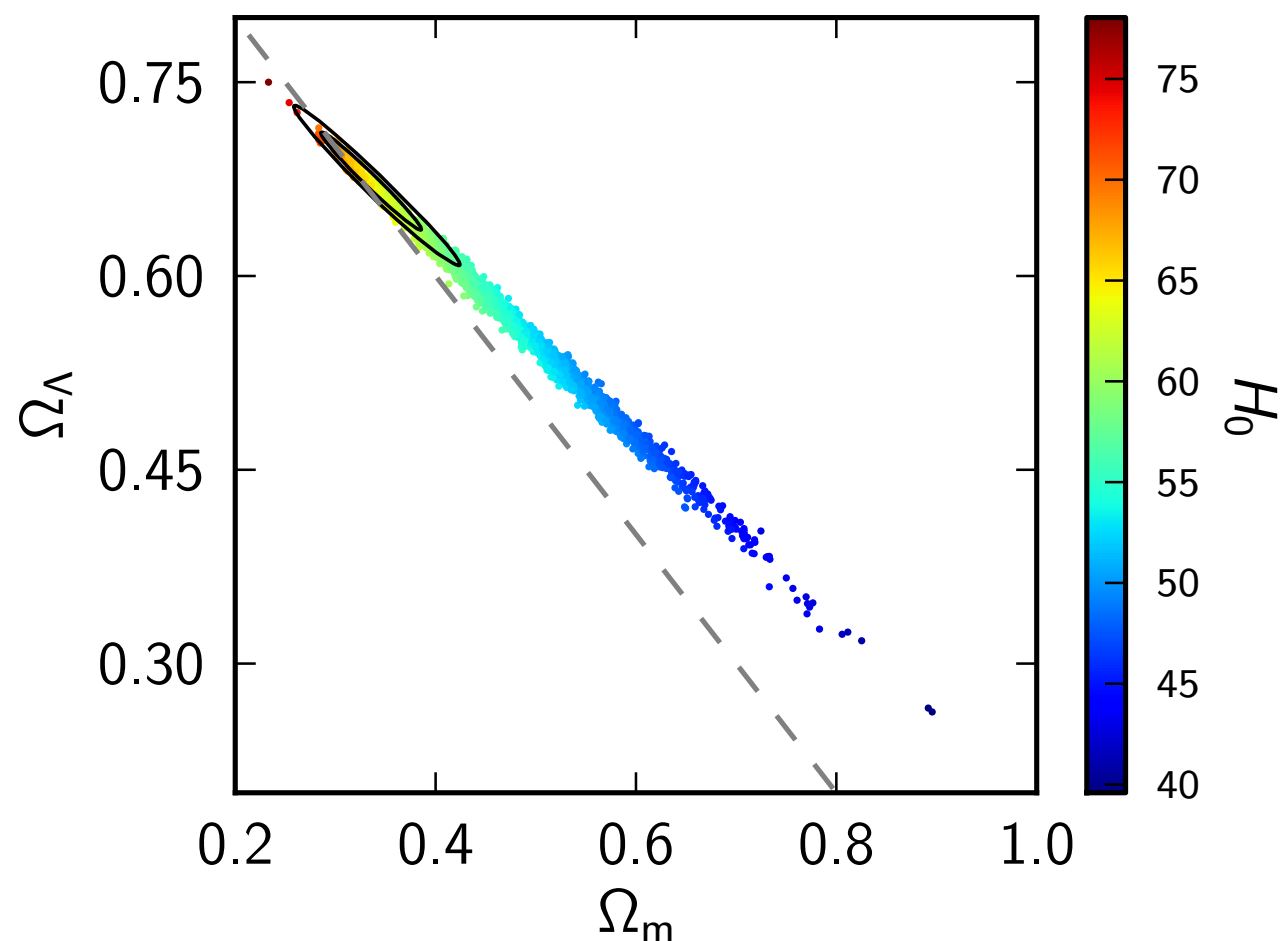
«Lensing breaks diameter degeneracies»



Cosmological information from CMB lensing

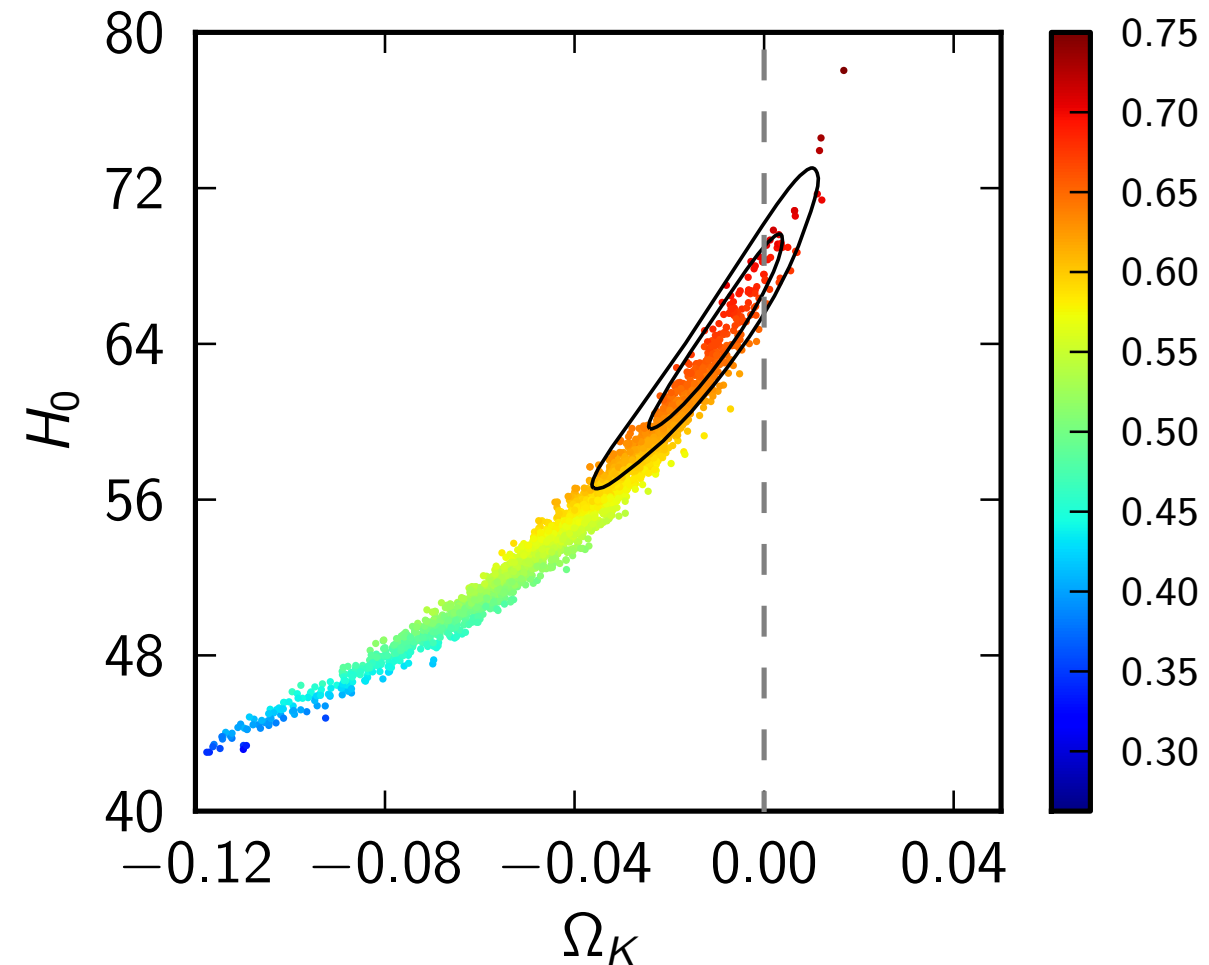


«Lensing breaks diameter degeneracies»



$$\Omega_\Lambda = 0.57^{+0.073}_{-0.055} \quad (68\%; \textit{Planck}+\textit{WP}+\textit{highL})$$

$$\Omega_\Lambda = 0.67^{+0.027}_{-0.023} \quad (68\%; \textit{Planck}+\textit{lensing}+\textit{WP}+\textit{highL}).$$



The Planck Collaboration XVI, 2013

$$100\Omega_K = -4.2^{+4.3}_{-4.8} \quad (95\%; \textit{Planck}+\textit{WP}+\textit{highL});$$

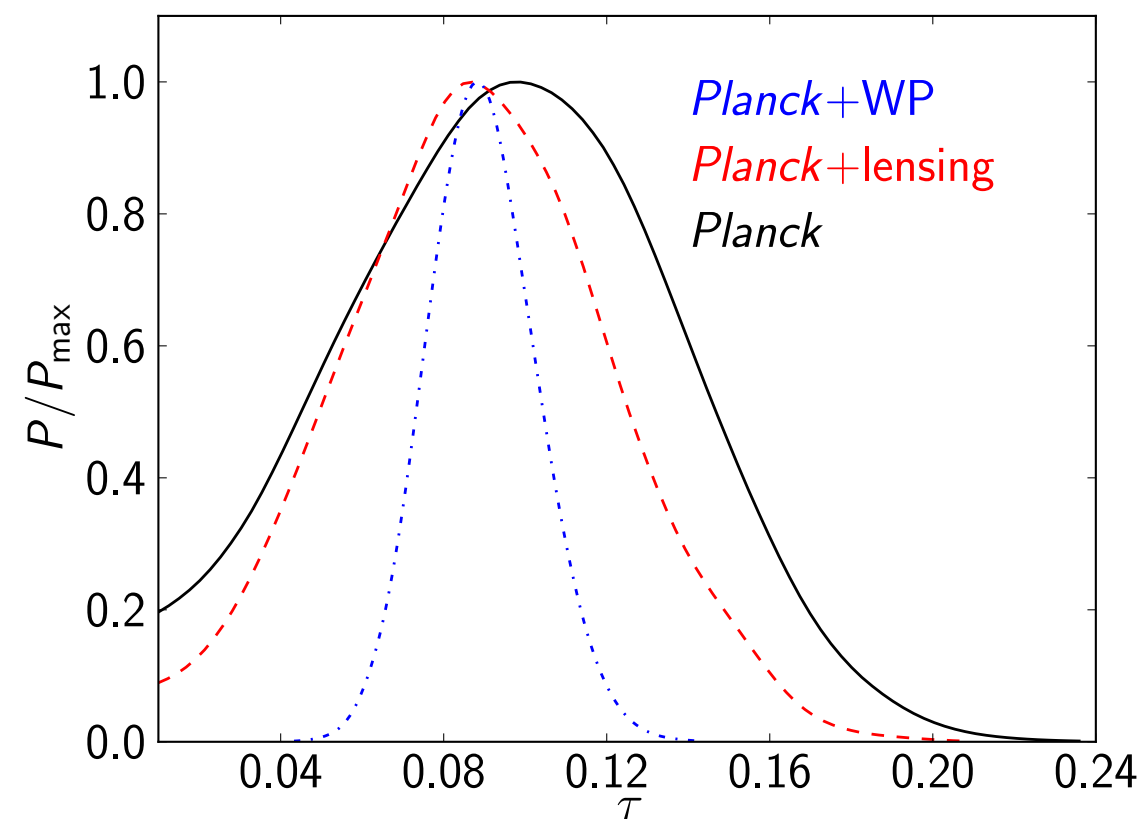
$$100\Omega_K = -1.0^{+1.8}_{-1.9} \quad (95\%; \textit{Planck}+\textit{lensing} + \textit{WP}+\textit{highL}).$$

Cosmological information from CMB lensing



Reionization

- Lensing provides «Planck only» constraint
- Cross-check of polarization



$$\tau = 0.097 \pm 0.038 \quad (68\%; \textit{Planck})$$

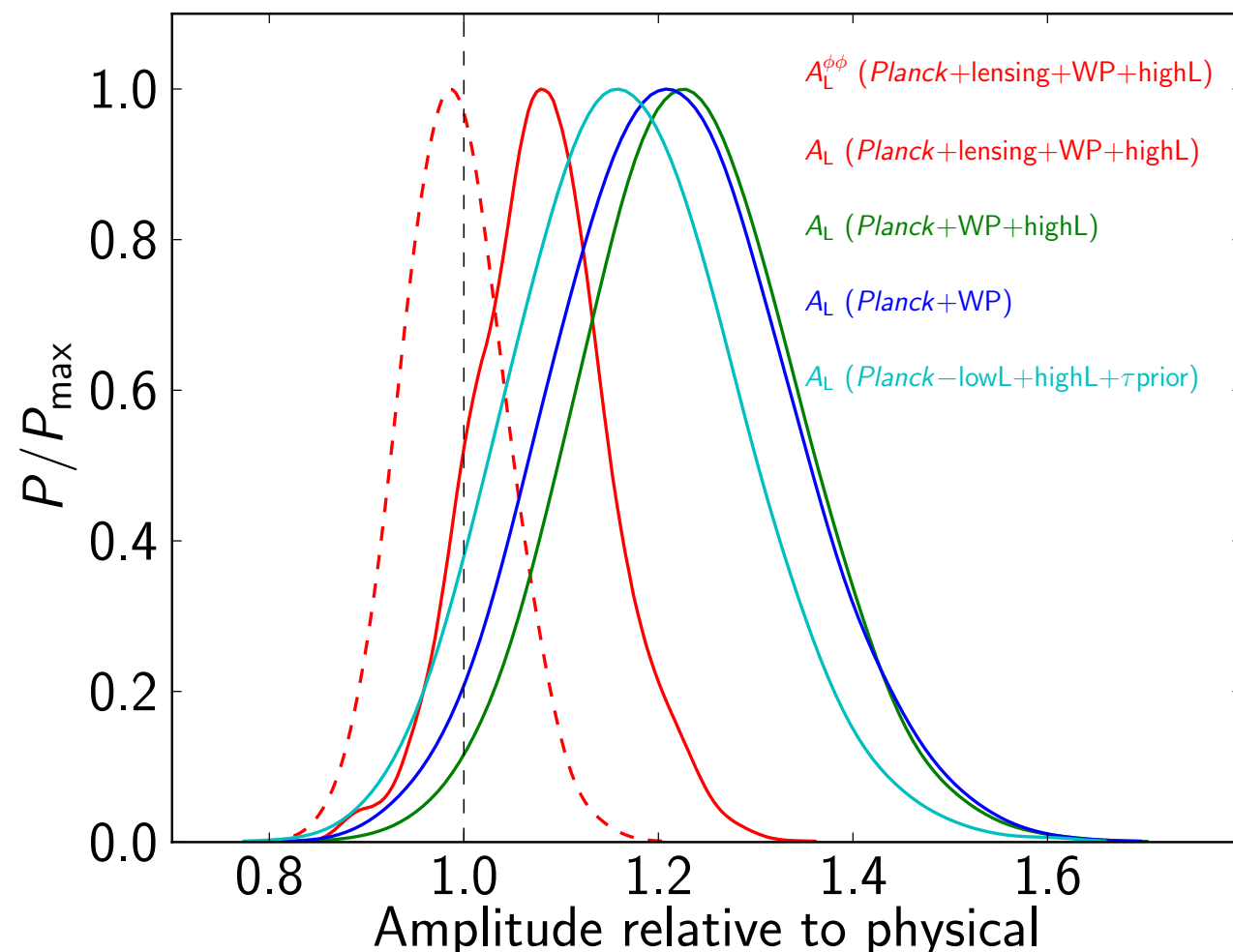
$$\tau = 0.089 \pm 0.032 \quad (68\%; \textit{Planck+lensing}).$$

Cosmological information from CMB lensing

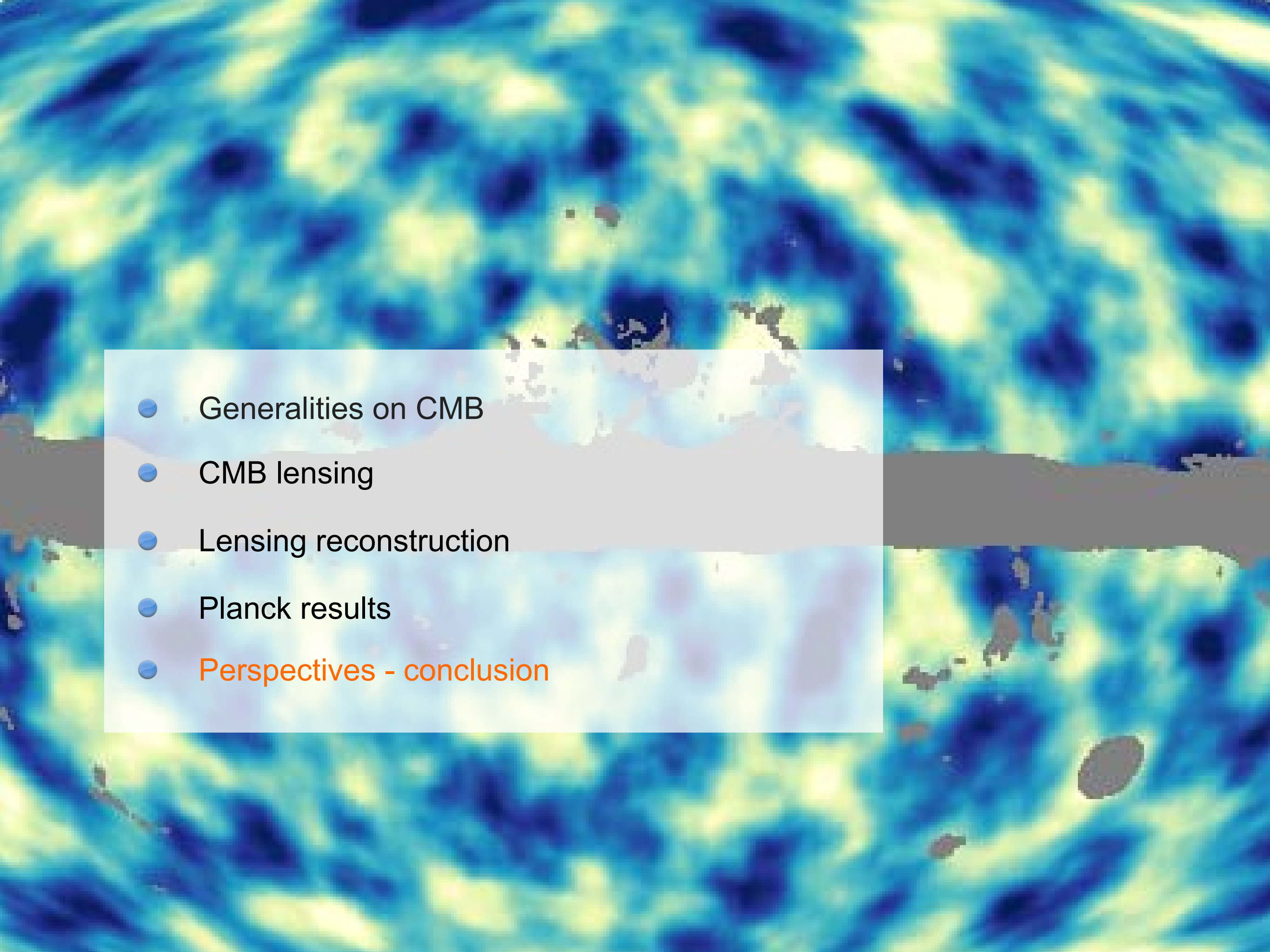


● Sum of neutrino masses

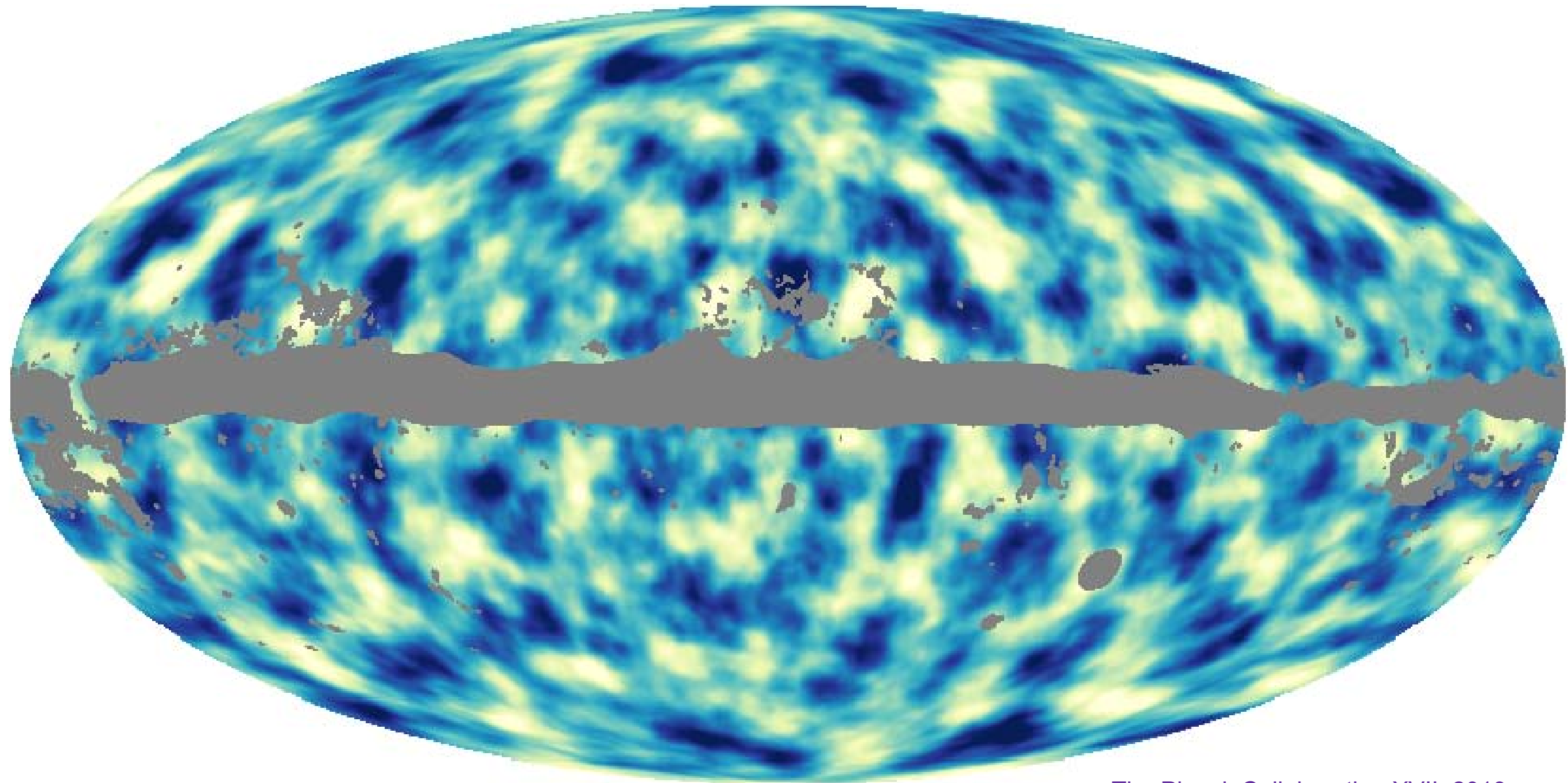
- Mild tension : constraint weaker than expected!
- Temperature power spectra: more lensing = smaller mass
- Reconstruction: less lensing = larger mass



$$\sum m_\nu < 0.66 \text{ eV}, \quad (95\%; \textit{Planck}+\textit{WP}+\textit{highL}),$$
$$\sum m_\nu < 0.85 \text{ eV}, \quad (95\%; \textit{Planck}+\textit{lensing}+\textit{WP}+\textit{highL}),$$

- 
- The background of the slide is a full-frame image of the Cosmic Microwave Background (CMB) fluctuation map. It displays a complex pattern of temperature variations across the sky, with colors ranging from dark blue (cooler) to yellow and white (warmer). The pattern shows large-scale structures and smaller-scale fluctuations, characteristic of the early universe's density distribution.
- Generalities on CMB
 - CMB lensing
 - Lensing reconstruction
 - Planck results
 - Perspectives - conclusion

The matter in the Universe as seen by Planck

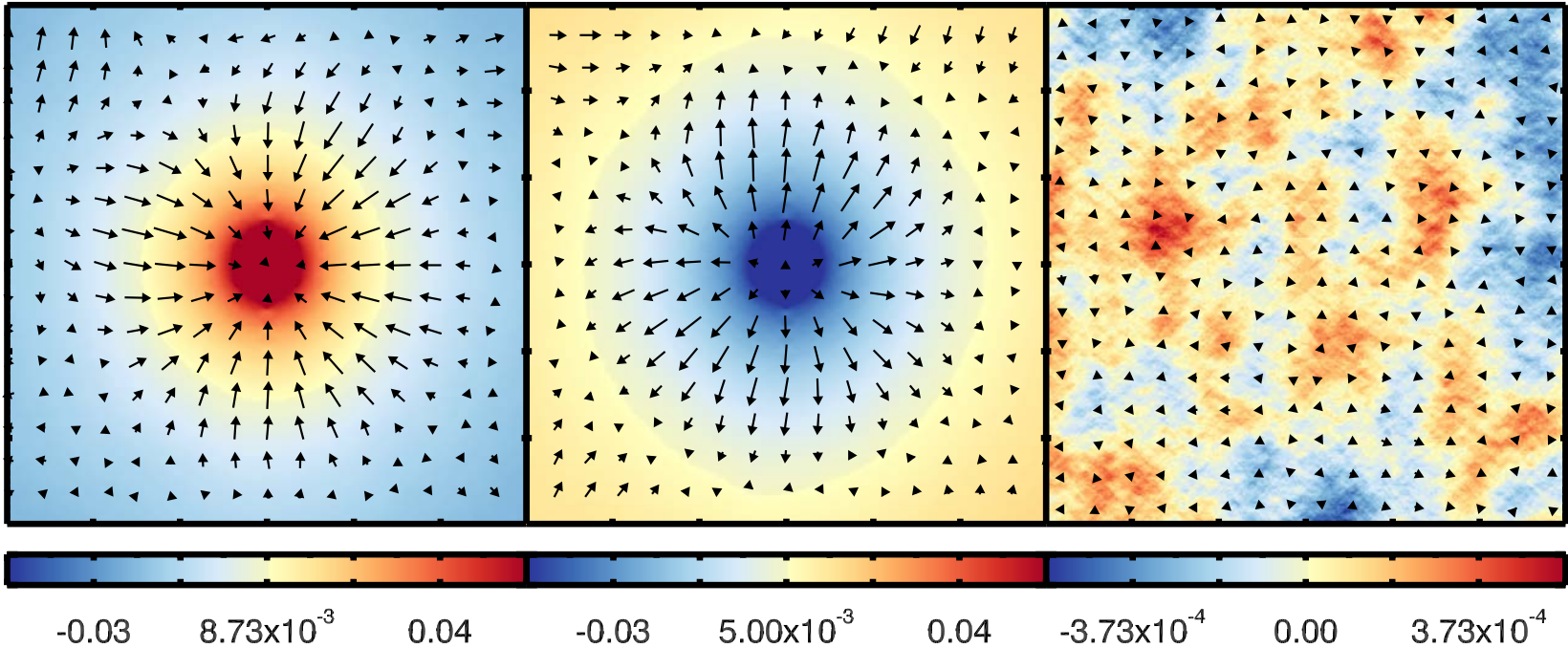


The Planck Collaboration XVII, 2013

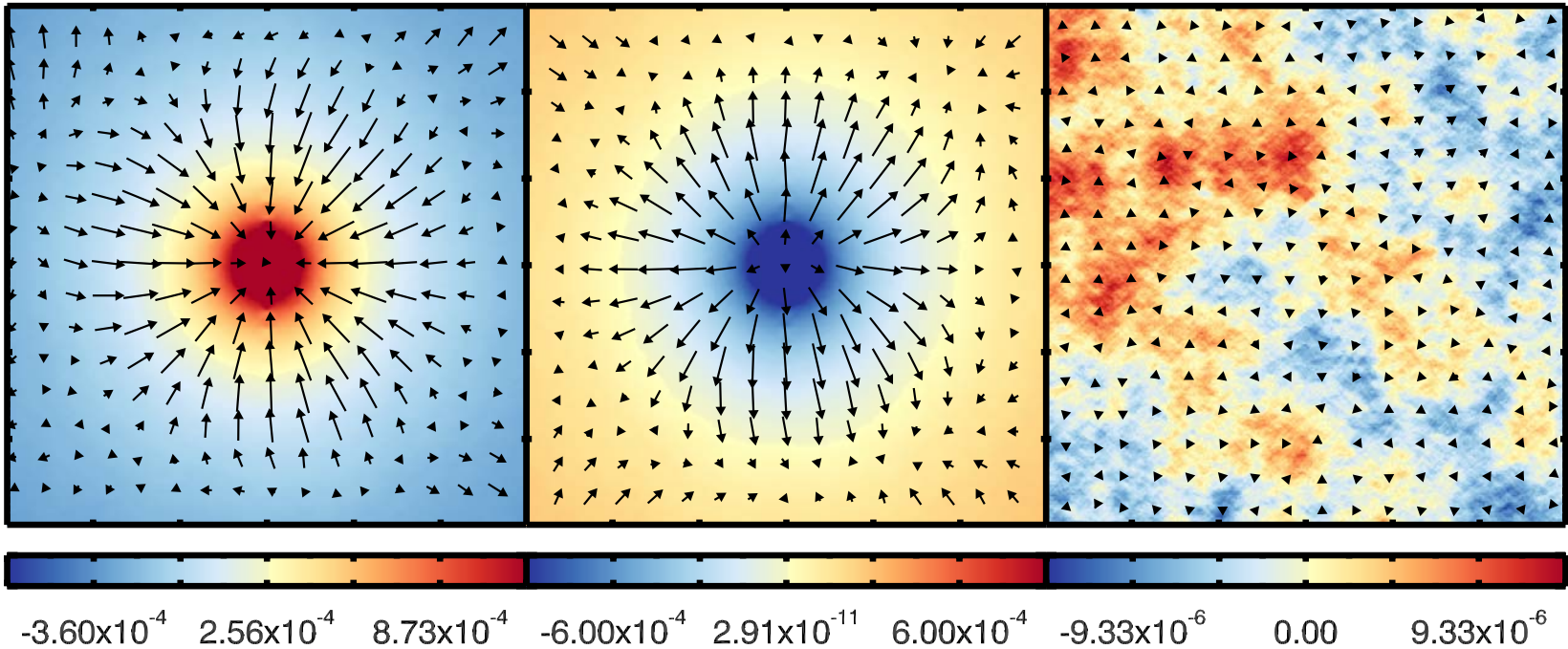
The lensing map traces the matter distribution up to the last scattering surface



857 GHz



545 GHz



Cross-correlations



$$C_{\ell}^{XY} \sim \int_0^{\chi_*} d\chi w^X(\chi) w^Y(\chi) P(\ell/\chi, \chi)$$

$$w^l(\chi) \propto \Omega_m H_0^2 \frac{\chi_* - \chi}{\chi_*} \frac{\chi}{a}$$

CMB lensing

Planck

$$w^g(\chi) \propto b \frac{dN}{d\chi}$$

Galaxy distribution

SDSS, NVSS

Cross-correlations



$$C_{\ell}^{XY} \sim \int_0^{\chi_*} d\chi w^X(\chi) w^Y(\chi) P(\ell/\chi, \chi)$$

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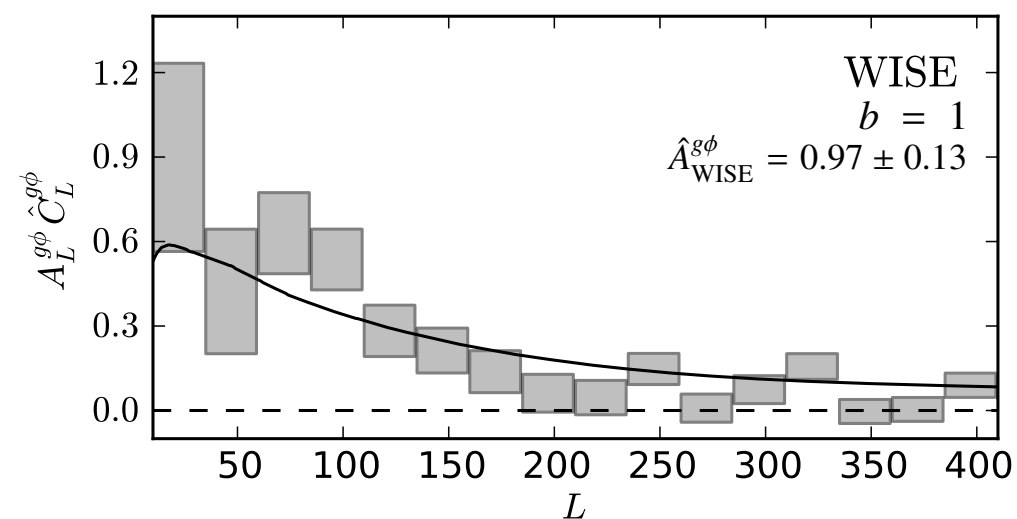
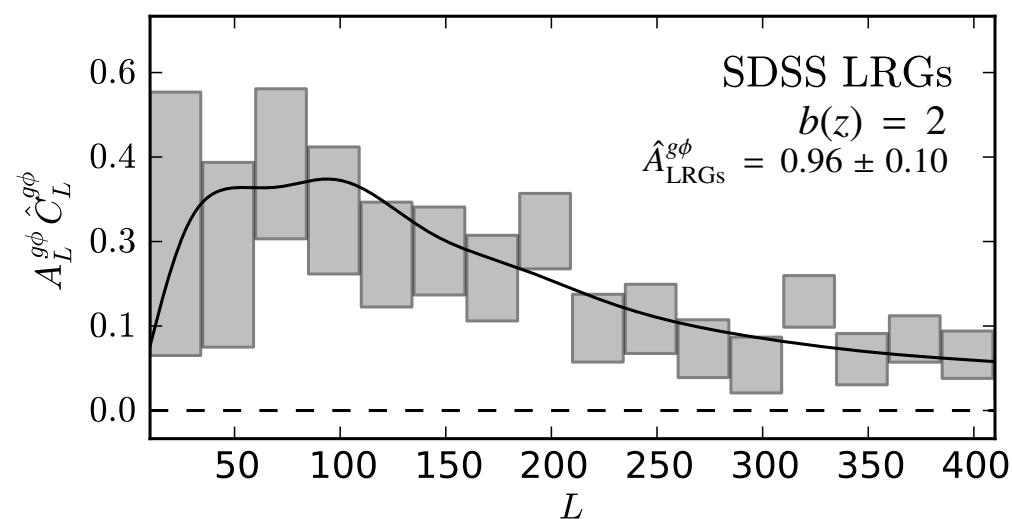
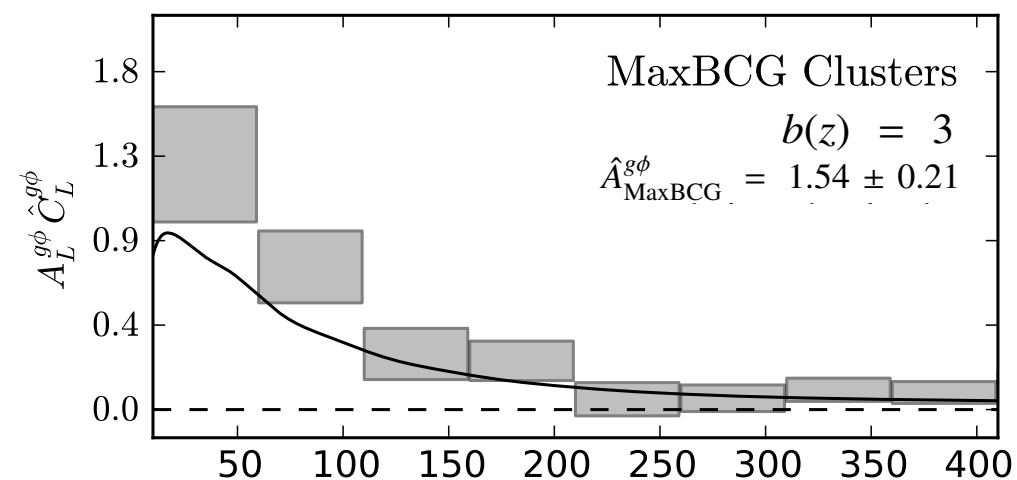
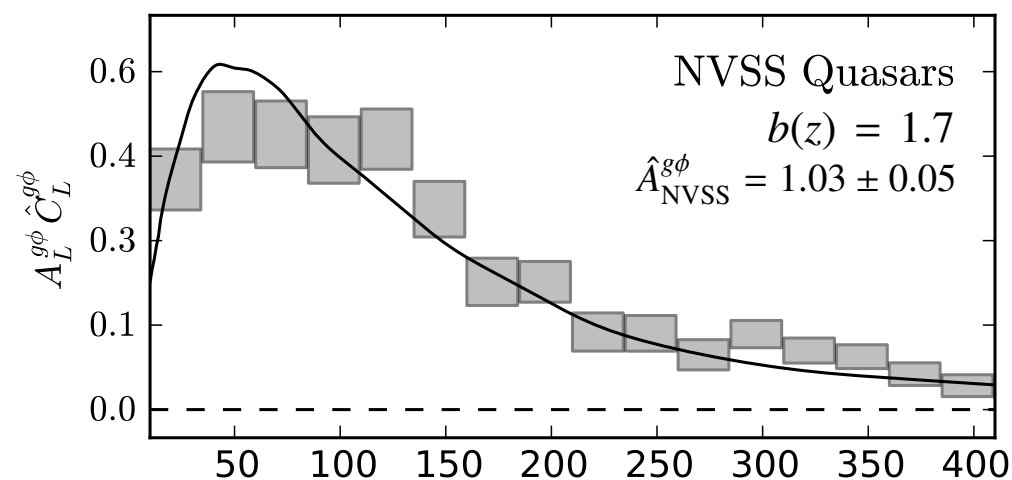
CMB lensing

$$w^g(\chi) \propto b \frac{dN}{d\chi}$$

Galaxy distribution

Planck

SDSS, NVSS



Planck mass will stay the reference on the full-sky for many years!



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$$w^l(\chi) \propto \Omega_m H_0^2 \frac{\chi_* - \chi}{\chi_*} \frac{\chi}{a}$$

CMB lensing

Planck

$$w^g(\chi) \propto b \frac{dN}{d\chi}$$

Galaxy distribution

SDSS, DES, Euclid, LSST

$$w^s(\chi) \propto H_0^2 \Omega_m \frac{\chi}{a} \int_{\chi}^{\chi_*} d\chi' \frac{dN}{d\chi'} \frac{\chi' - \chi}{\chi'}$$

Weak lensing on galaxies

DES, Euclid, LSST

- CMB lensing: non biased, purely geometric, source plane well-known



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Weak lensing on galaxies

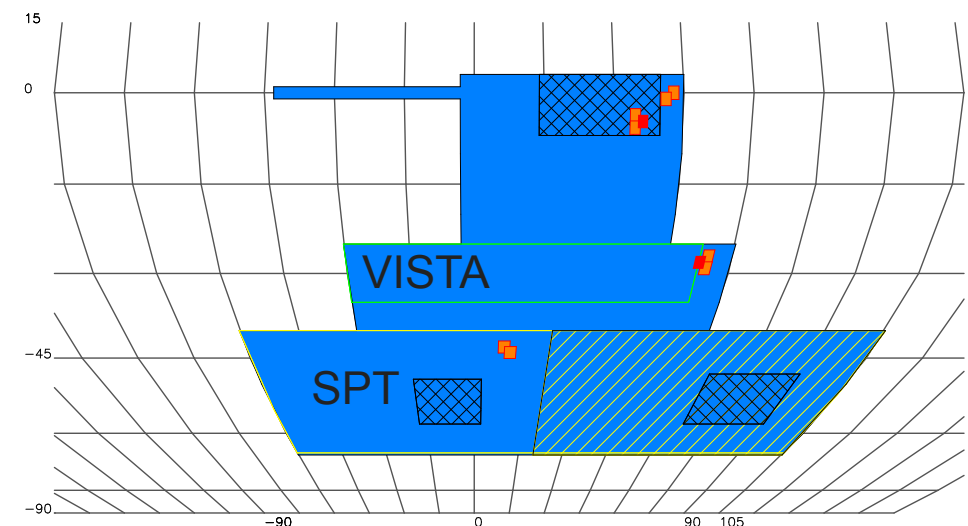
DES, Euclid, LSST

- CMB lensing: non biased, purely geometric, source plane well-known

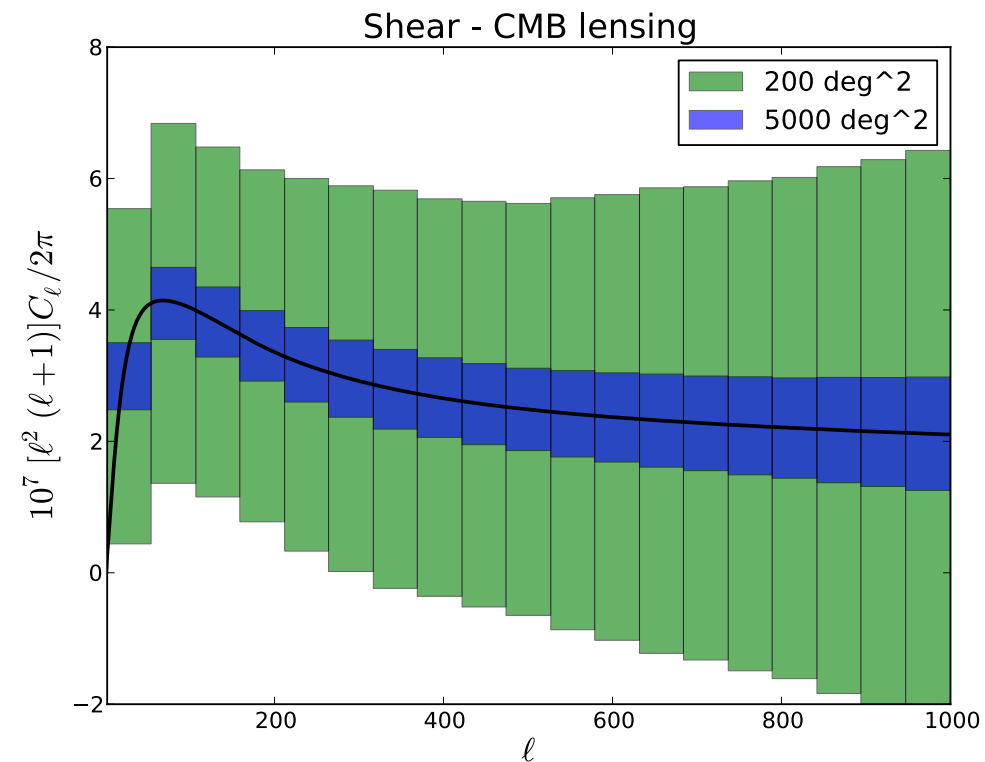
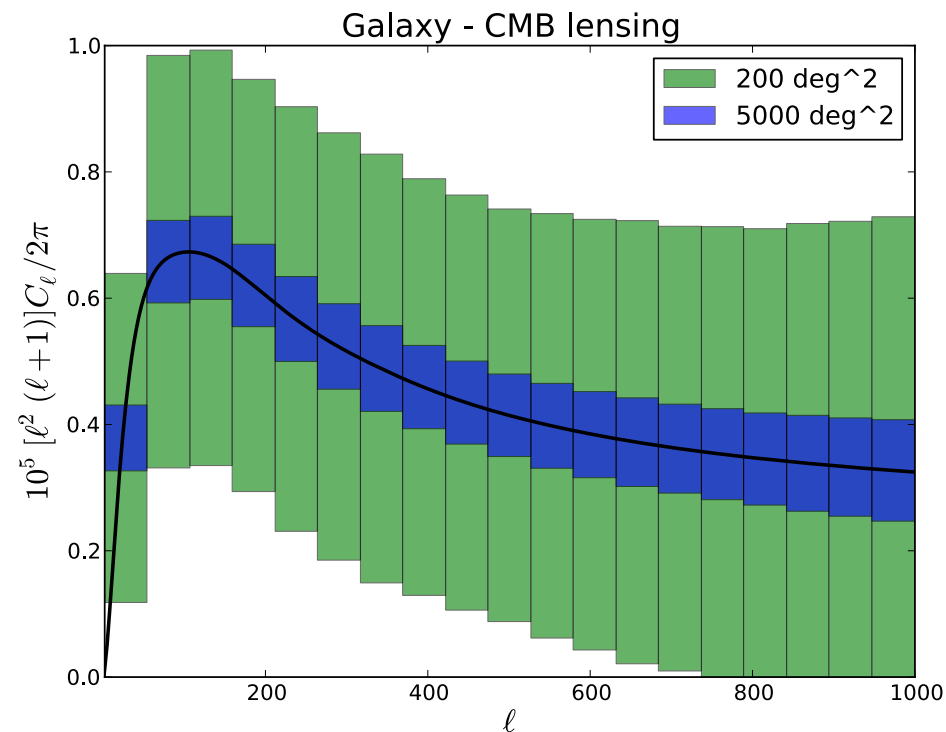
● The Dark Energy Survey

- 5000 deg² grizY to 24th mag
- 15 deg² for type Ia supernovae
- 5 years
- 300 millions photometric redshifts
- Cluster count
- Weak lensing
- Large Scale structure
- Type Ia supernovae

DES footprint



The Dark Energy Survey



Benoit-Lévy & Kirk, DES internal note



Open questions

- Simply new observable?
- Better control on systematic errors?
- Better constraints on bias?
- Would a post-Planck CMB lensing measurement help?

CMB lensing: central in observational cosmology

CMB

provides finer constraints on parameters
deep understanding required for
next-generation polarization analysis

large-scale structure

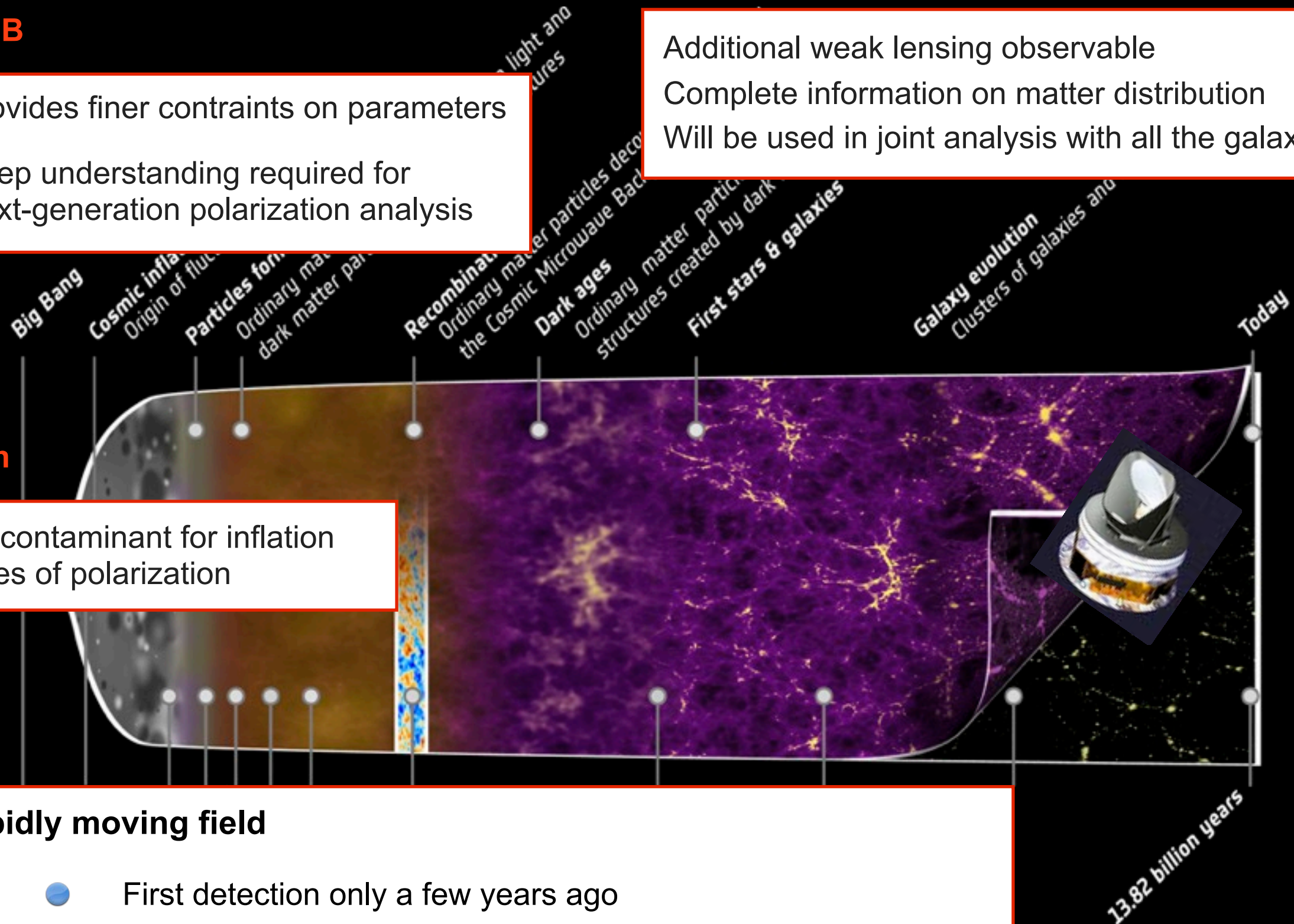
Additional weak lensing observable
Complete information on matter distribution
Will be used in joint analysis with all the galaxy surveys

Inflation

known contaminant for inflation
B-modes of polarization

Rapidly moving field

- First detection only a few years ago
- Planck full-sky lensing map available!



Large-scale structure needed

