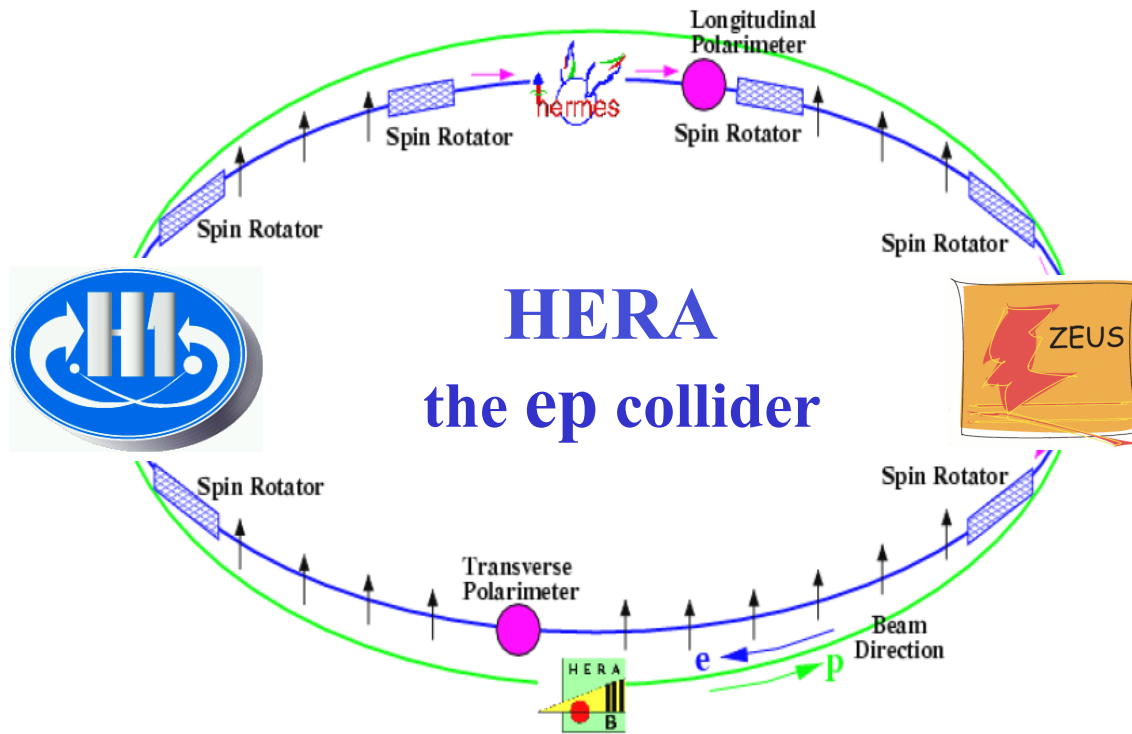


Proton Structure and PDFs at HERA

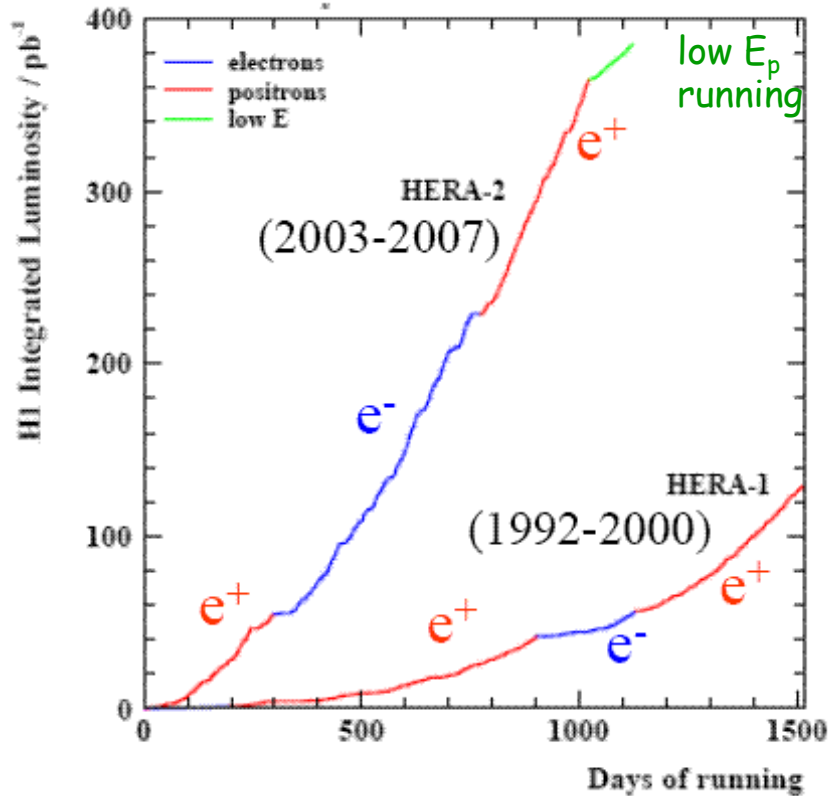
Vladimir Chekelian (MPI for Physics, Munich)

on behalf of the H1 and ZEUS Collaborations

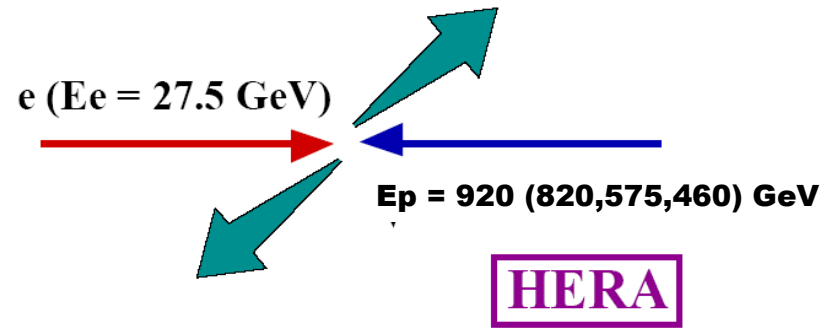


- HERA / DIS / NC / CC
- Inclusive ep Cross Sections
- Proton Structure Functions
- HERAPDF
- Charm Production
- HERAFitter
- Summary

The ep collider HERA (1992–2007)



HERA I	1992-2000	~120 pb ⁻¹
HERA II	2003-2007	~380 pb ⁻¹



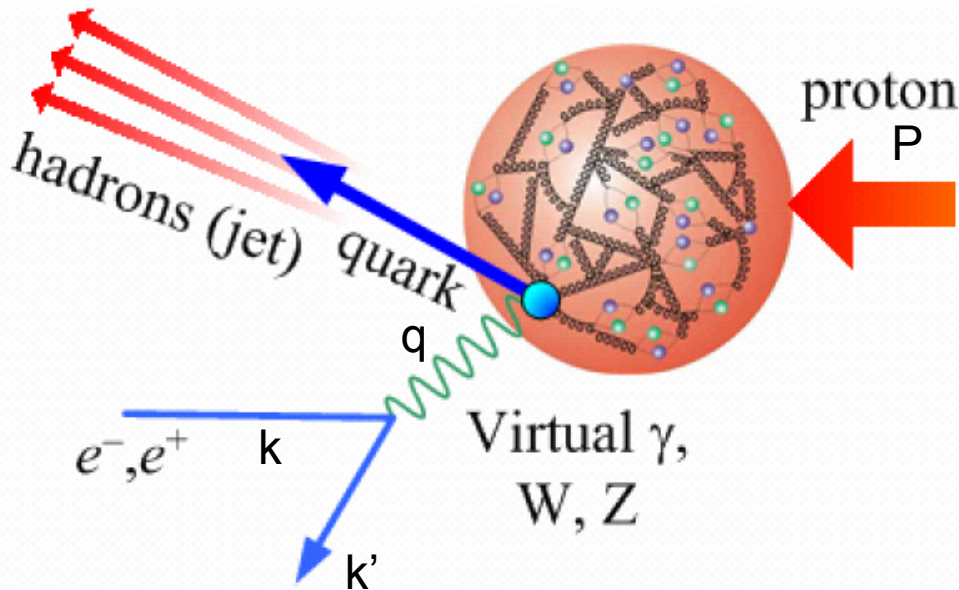
located at DESY, Hamburg
 peak luminosity $5 \cdot 10^{31} \text{ cm}^{-2} \text{ sec}^{-1}$
 $Q^2_{\text{max}} = 10^5 \text{ GeV}^2$
 $\lambda_{\text{min}} \sim 1/1000 r_{\text{proton}}$
 longitudinal polarisation of e-beam

H1+ZEUS in total $2 \times 0.5 \text{ fb}^{-1}$
about equally shared between

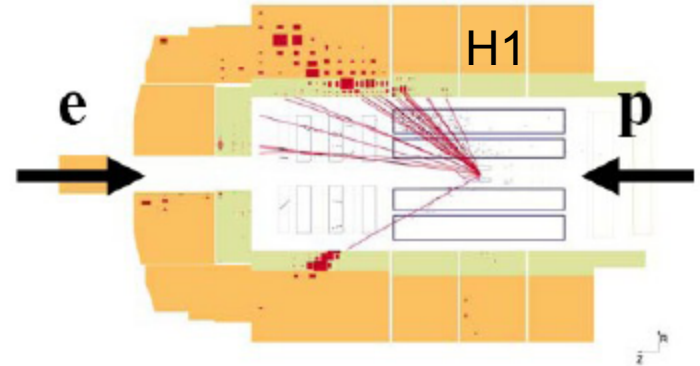
- e^+ and e^- ,
- positive and negative P_e

low proton energy running for F_L

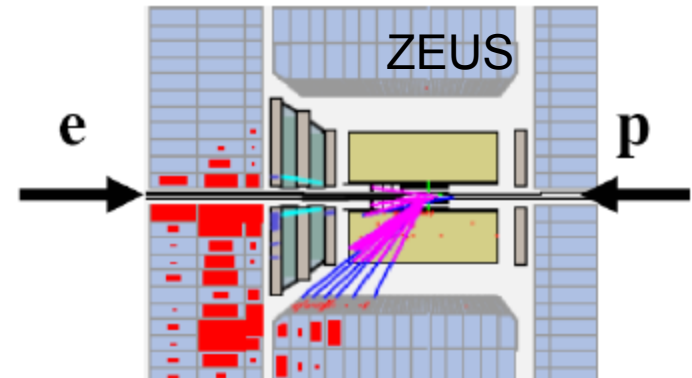
Deep Inelastic Scattering (DIS)



Neutral Current (NC): $e^\pm p \rightarrow e^\pm X$



Charged Current (CC): $e^\pm p \rightarrow \nu X$



$$Q^2 = -q^2 = -(k-k')^2 \quad \text{virtuality of } \gamma^*, Z^0, W$$

$$x = Q^2/2(Pq) \quad \text{Bjorken } x$$

$$y = (Pq)/(Pk) \quad \text{inelasticity}$$

$$Q^2 = sxy \quad s=(k+P)^2$$

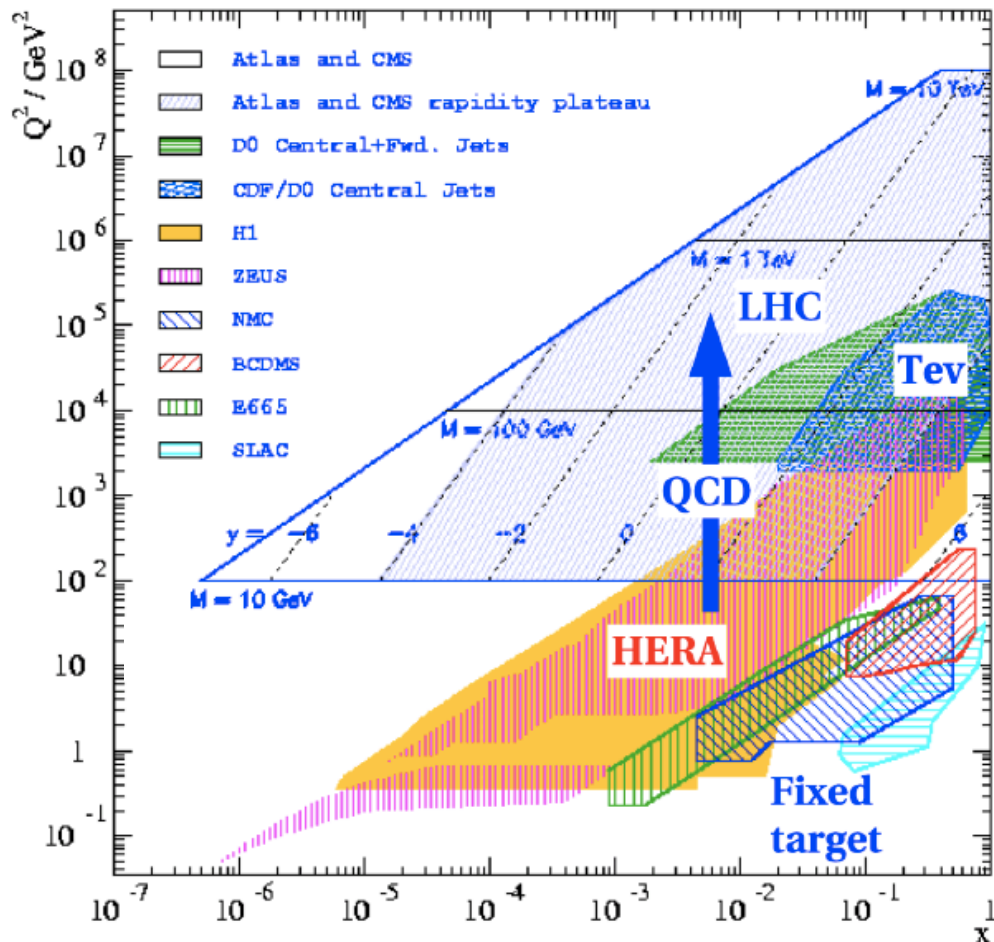
Factorisation: $\sigma_{DIS} : \hat{\sigma} \otimes pdf(x)$

$\hat{\sigma}$ - perturbative QCD cross section

pdf - universal parton distribution functions

Q^2 -x plane at HERA

HERA: span 5 orders of magnitude in x and Q^2



Inclusive data sets from H1 and ZEUS cover different parts of the phase space are obtained in different periods using different detector components, different beam energies and polarisation.

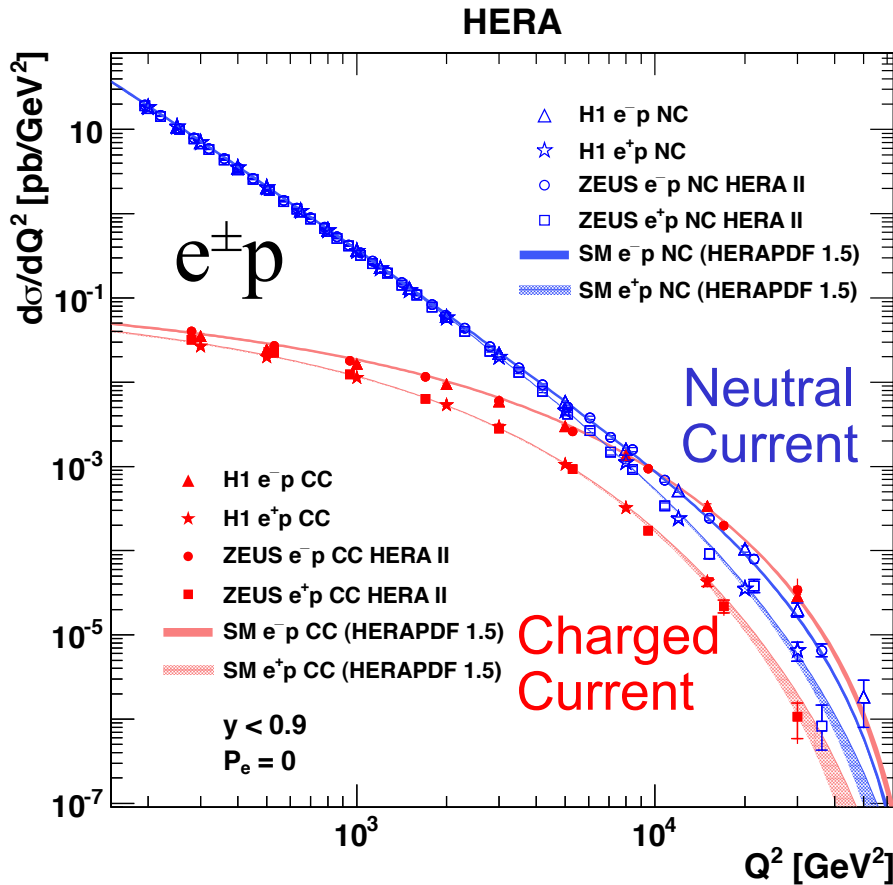
HERA I (1994-2000) inclusive NC & CC analyses are completed, published both by H1 and ZEUS and combined.

HERA II (2003-2007) NC & CC analyses with longitudinally polarised lepton beams are completed in 2012 and published both by H1 and ZEUS

Full HERA x range is important for the LHC

→ HERA inclusive data are an indispensable input to modern QCD PDF fits

Inclusive NC & CC at HERA



$$\sigma_{NC} \approx \sigma_{CC} \text{ at } Q^2 \approx M_Z^2, M_W^2$$

→ remaining differences are due to u/d flavor asymmetry and helicity factors

$$\tilde{\sigma}_{NC}^\pm \equiv \frac{d^2\sigma_{NC}^{e^\pm p}}{dx dQ^2} \frac{xQ^4}{2\pi\alpha^2} \frac{1}{Y_\pm} \equiv \tilde{F}_2 - \frac{y^2}{Y_+} \tilde{F}_L \mp \frac{Y_-}{Y_+} x\tilde{F}_3$$

$$F_2(x, Q^2) = x \sum A_i(q_i + \bar{q}_i) \quad xF_3(x, Q^2) = x \sum B_i(q_i - \bar{q}_i)$$

$$F_L = F_2 - 2xF_1 = 0 \quad (\text{QPM}) \quad Y_\pm = 1 \pm (1-y)^2$$

→ all three SF are measured at HERA

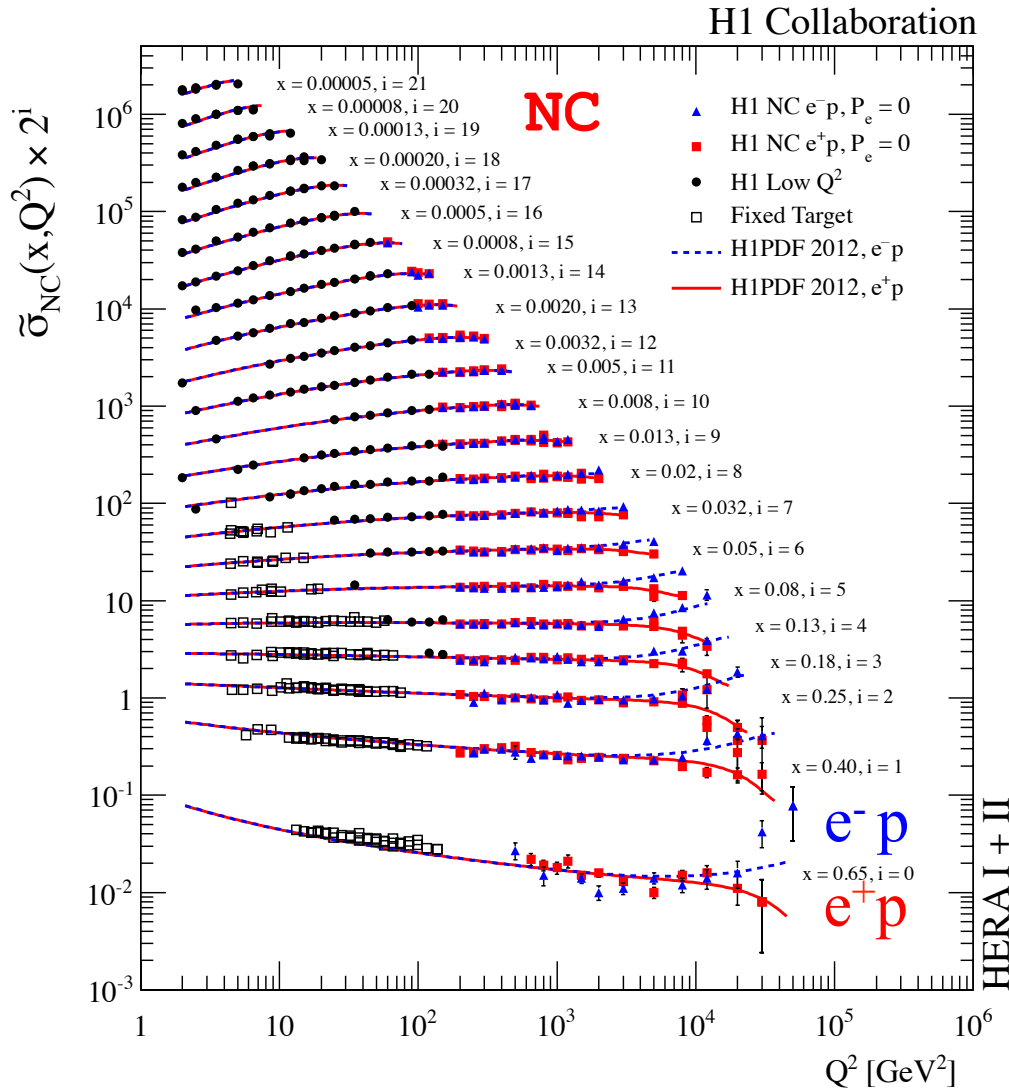
$$\tilde{\sigma}_{CC} = \frac{2\pi x}{G_F^2} \left[\frac{M_W^2 + Q^2}{M_W^2} \right]^2 \frac{d^2\sigma_{CC}}{dx dQ^2}$$

$$\tilde{\sigma}_{CC}^+ \sim (x\bar{u} + x\bar{c}) + (1-y)^2 (xd + xs)$$

$$\tilde{\sigma}_{CC}^- \sim (xu + xc) + (1-y)^2 (x\bar{d} + x\bar{s})$$

→ CC data allow flavor separation in QCD fits

NC and CC Cross Sections $\sigma_{\text{NC,CC}}(x, Q^2)$

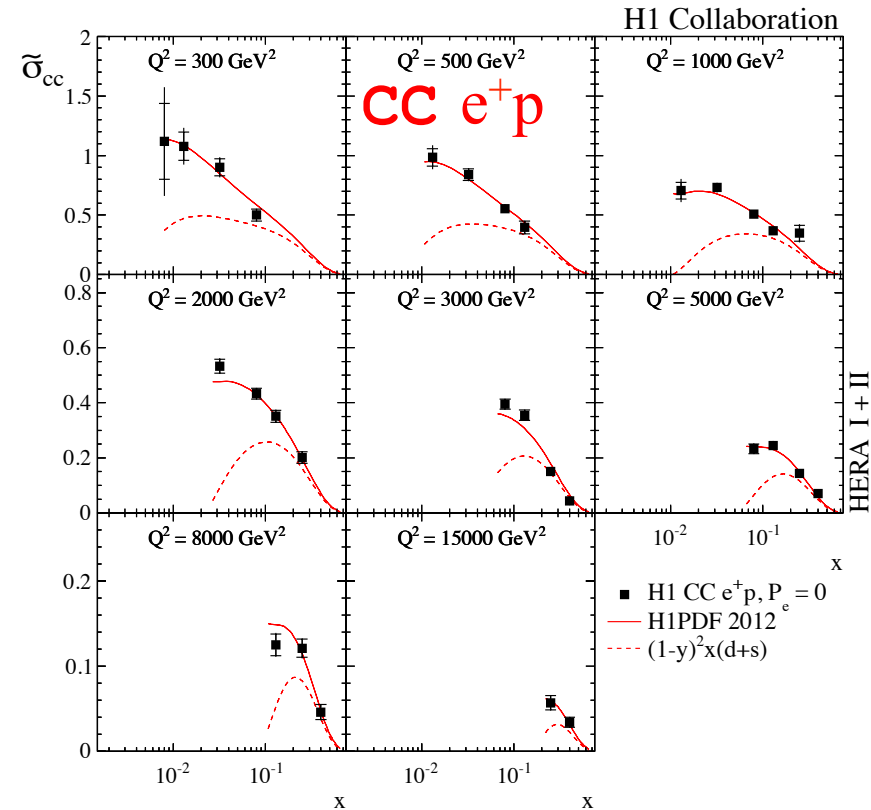


H1 and ZEUS completed
the HERA II NC&CC measurements:

H1: JHEP 09 (2012) 061

ZEUS: PRD 87 (2013) 052014 EPJ C61 (2009) 223

EPJ C62 (2009) 625 EPJ C70 (2010) 945

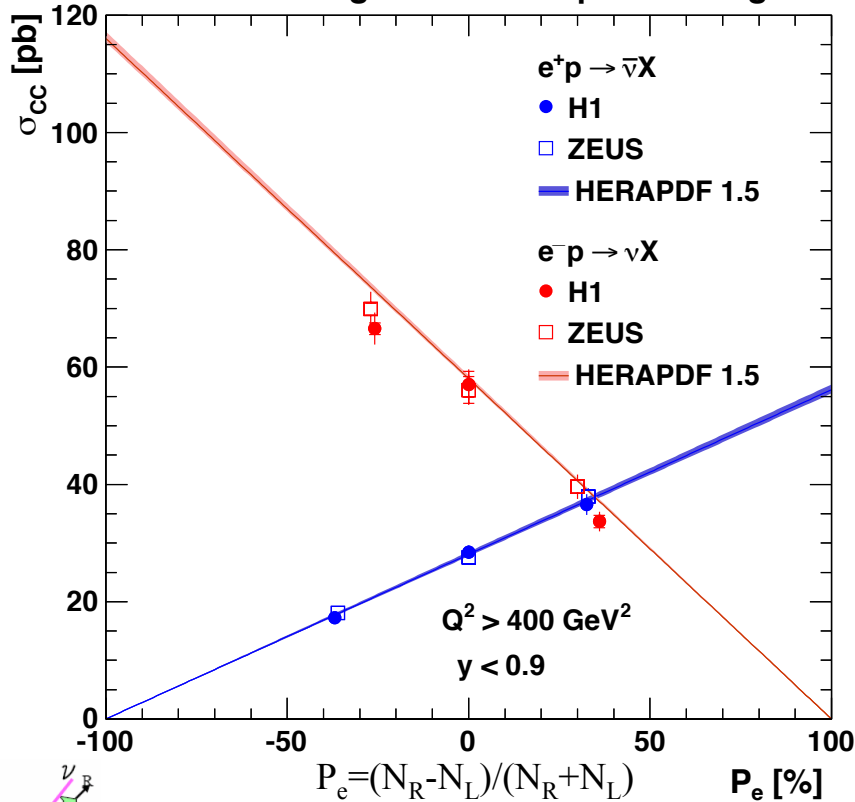


Polarisation effects in CC and NC

Polarisation dependence of the total CC cross section

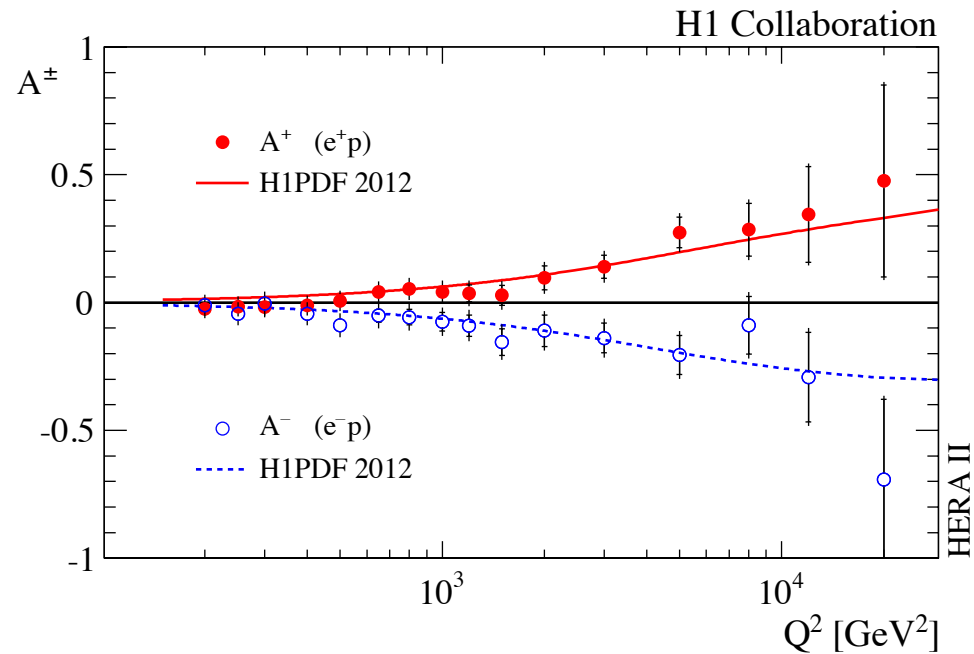
$$\sigma_{CC}^{e^\pm p} = (1 \pm P_e) \sigma_{CC}^{e^\pm p} (P_e = 0)$$

HERA Charged Current $e^\pm p$ Scattering



Polarisation asymmetry in NC:

$$A^\pm = \frac{2}{P_L^\pm - P_R^\pm} \cdot \frac{\sigma^\pm(P_L^\pm) - \sigma^\pm(P_R^\pm)}{\sigma^\pm(P_L^\pm) + \sigma^\pm(P_R^\pm)}$$



→ a direct measure of parity violation in NC

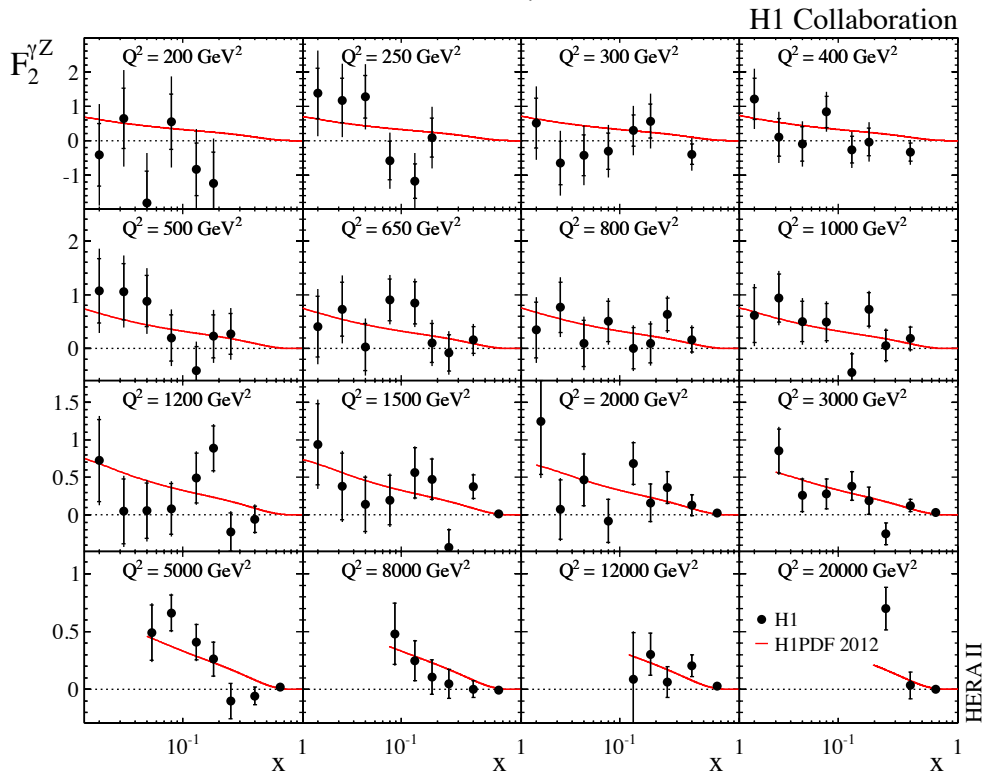
→ absence of right-handed weak current

The First Measurement of Parity Violating SF $F_2^{\gamma Z}(x, Q^2)$

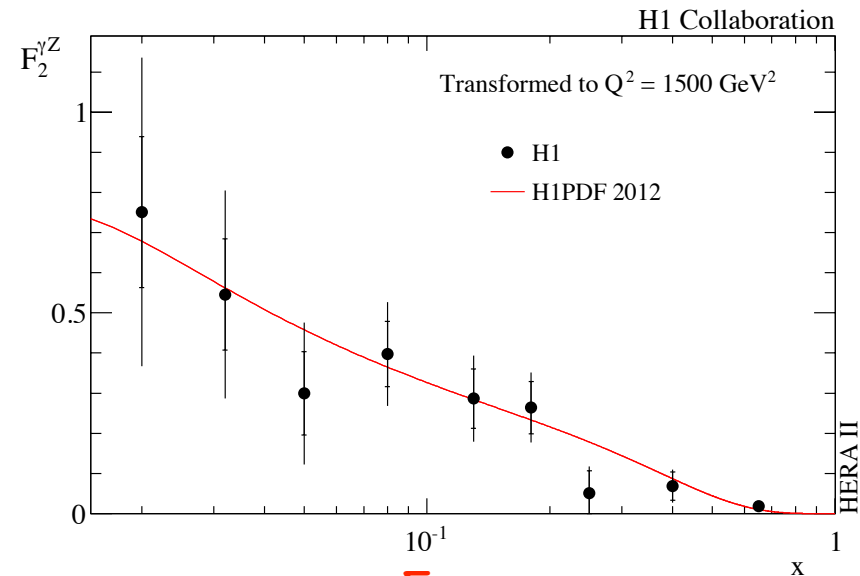
$$\frac{\sigma^\pm(P_L^\pm) - \sigma^\pm(P_R^\pm)}{P_L^\pm - P_R^\pm} = \frac{\kappa Q^2}{Q^2 + M_Z^2} \left[\mp a_e F_2^{\gamma Z} + \frac{Y_-}{Y_+} v_e x F_3^{\gamma Z} - \frac{Y_-}{Y_+} \frac{\kappa Q^2}{Q^2 + M_Z^2} (v_e^2 + a_e^2) x F_3^Z \right]$$

taking the difference for e^+p and e^-p , the terms with $x F_3^{\gamma Z}$ and $x F_3^Z$ cancel and $F_2^{\gamma Z}$ can be directly extracted from measured polarised cross sections

$$\kappa^{-1} = 4 \frac{M_W^2}{M_Z^2} \left(1 - \frac{M_W^2}{M_Z^2} \right)$$



transform the $F_2^{\gamma Z}(x, Q^2)$ measurements to $Q^2 = 1500 \text{ GeV}^2$ and average them to get $F_2^{\gamma Z}(x)$ at $Q^2 = 1500 \text{ GeV}^2$



$$\rightarrow F_2^{\gamma Z} = x \sum [2e_q v_q (q + \bar{q})]$$

Structure Function $x\tilde{F}_3(x, Q^2)$

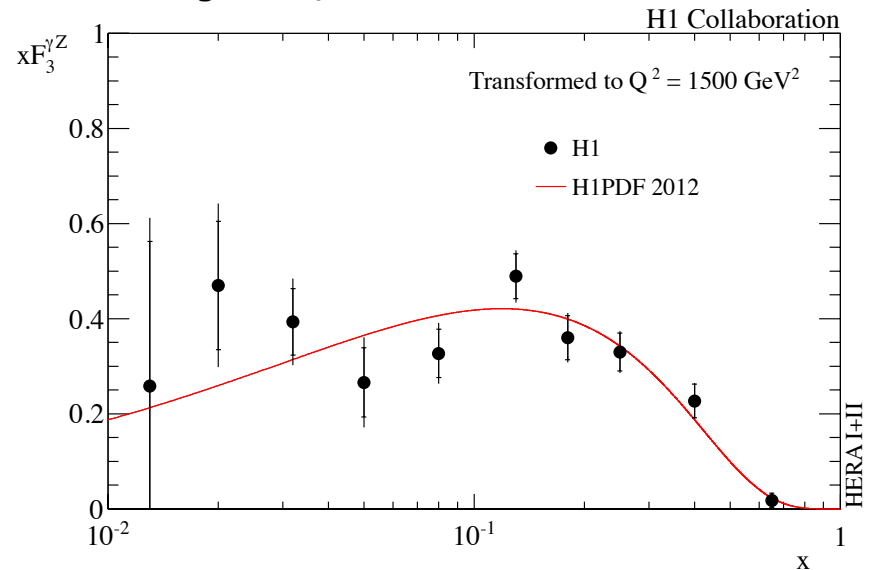
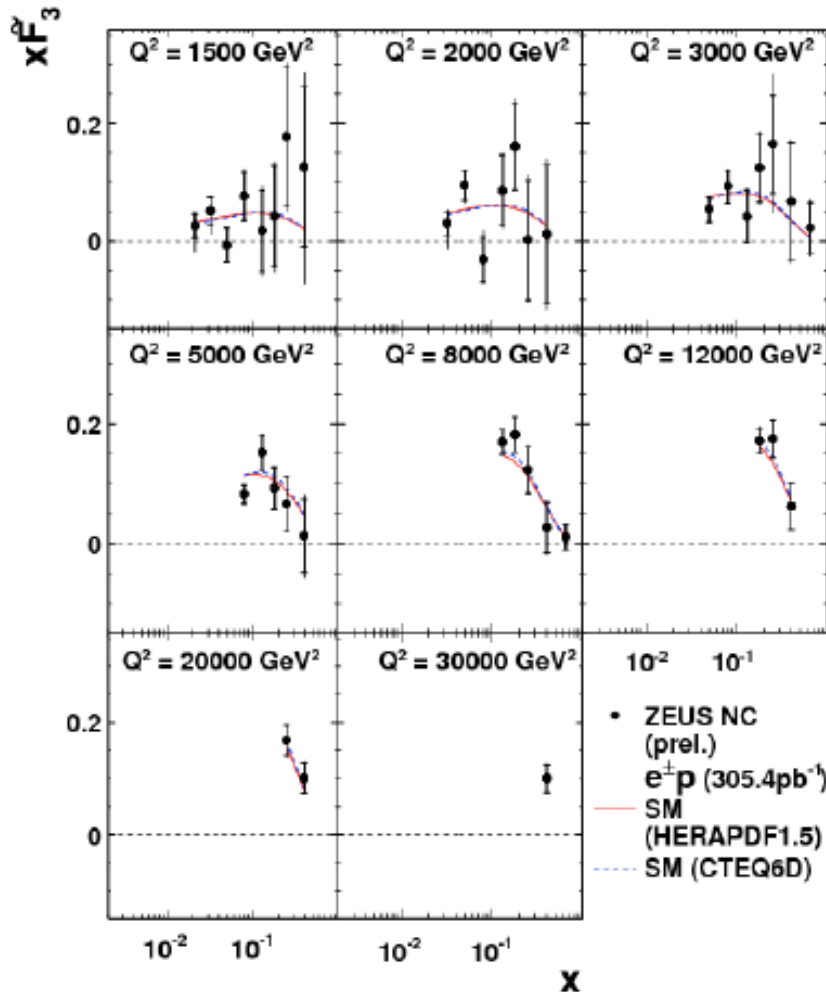
$$x\tilde{F}_3 = \frac{Y_+}{2Y_-} (\tilde{\sigma}_{NC}^- - \tilde{\sigma}_{NC}^+) \quad \text{ZEUS}$$

- charge asymmetry of unpolarised $e^\pm p$ NC cross sections

→ mostly due to γZ interference

$$xF_3^{\gamma Z} = -x\tilde{F}_3 \cdot (Q^2 + M_Z^2) / (a_e \kappa Q^2)$$

transform the $xF_3^{\gamma Z}(x, Q^2)$ measurements to $Q^2 = 1500 \text{ GeV}^2$ and average them to get $xF_3^{\gamma Z}(x)$ at $Q^2 = 1500 \text{ GeV}^2$



→ sensitive to valence quark: $F_3^{\gamma Z} \approx (2u_v + d_v)/3$

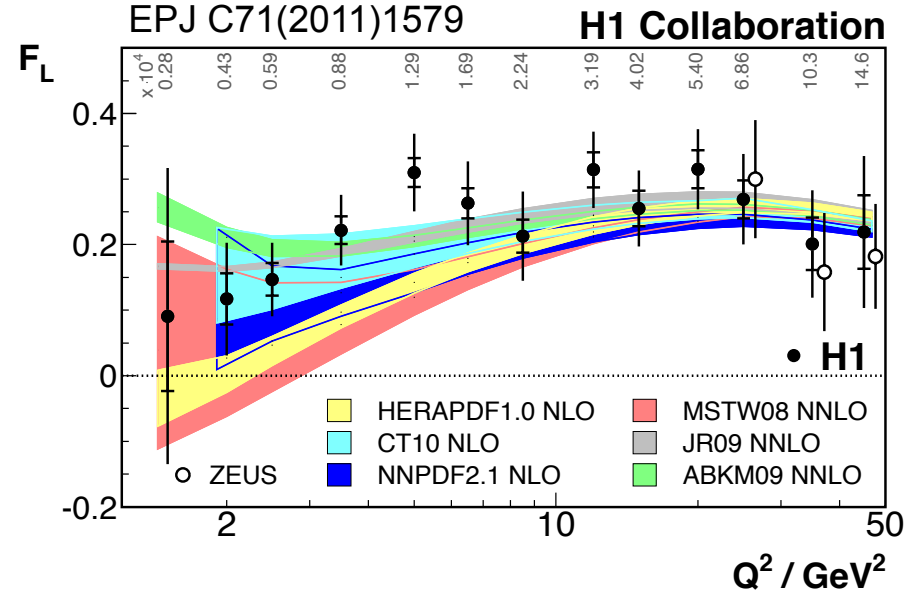
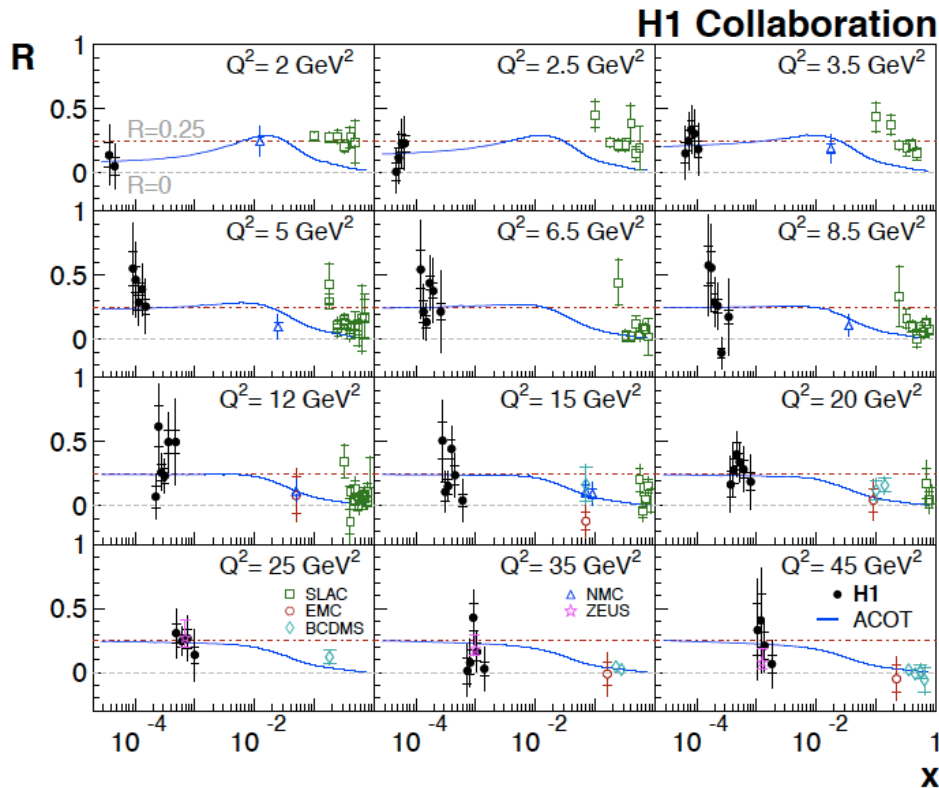
$$\int_{0.016}^{0.725} dx F_3^{\gamma Z}(x, Q^2 = 1500 \text{ GeV}^2) = 1.22 \pm 0.09(\text{stat}) \pm 0.07(\text{syst})$$

(H1PDF2012: $1.16 + 0.02 - 0.03$)

The longitudinal structure function $F_L(x, Q^2)$

- F_L is a pure QCD effect sensitive to gluon density $F_L(x, Q^2) = \frac{\alpha_s}{4\pi} x^2 \int_x^1 \frac{dz}{z^3} \left[\frac{16}{3} F_2 + 8 \sum_q e_q^2 \left(1 - \frac{x}{z}\right) \cdot xg \right]$
- F_L is measured at HERA using cross sections at the same x, Q^2 and different y (different proton beam energies $E_p = 460, 575, 920 \text{ GeV}$)

$$\sigma_{NC}(x, Q^2, y) = F_2(x, Q^2) - f(y) F_L(x, Q^2), \quad f(y) = y^2 / (1 + (1-y)^2)$$



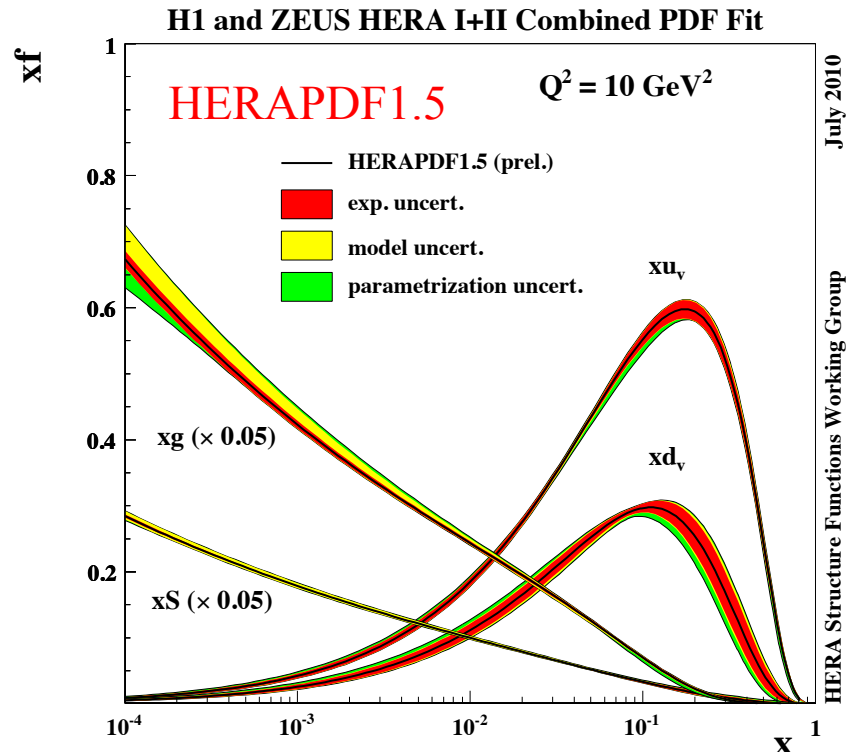
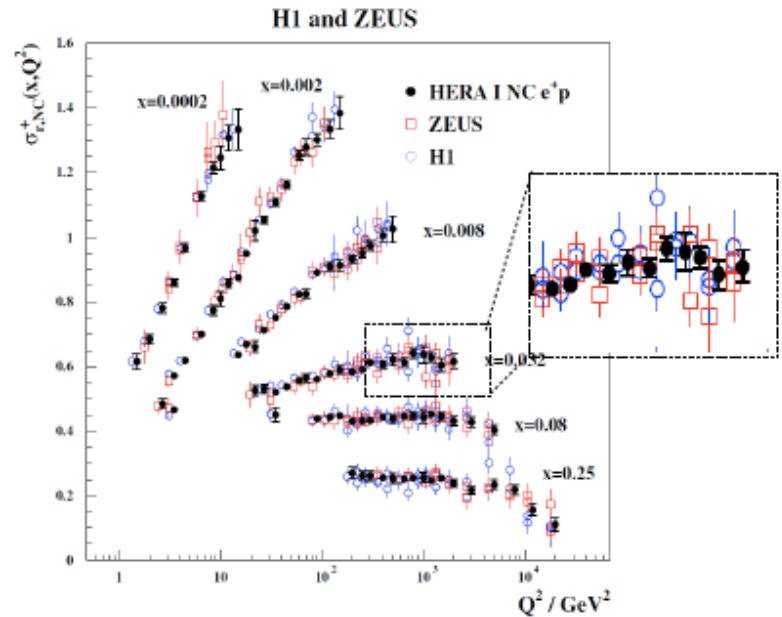
→ HERA F_L data are consistent with constant value of $R = F_L / (F_2 - F_L) = 0.26 \pm 0.05$

HERAPDF: QCD Fits using HERA data only

Input: **combined H1 & ZEUS incl. NC and CC data**
 which include expert knowledge in the treatment
 of the correlations between many individual data sets.

- precise, complete and easy in use
- significant reduction of systematic uncertainties

1. HERA I data: JHEP 1001:109,2010 HERAPDF 1.0
2. HERA I and preliminary HERA II data HERAPDF 1.5



HERAPDF

- no nuclear corrections
- no heavy target correction
- $\Delta\chi^2 = 1$ criterion for exp. errors
- parametrise $xg(x), xU_v, xd_v, xU_{bar}, D_{bar}$ at starting scale Q_0^2
- apply quark number and momentum sum rules
- NLO/NNLO DGLAP evolution
- different schemes for heavy flavor treatment
- uncertainty bands:
 - experimental
 - model (variations of Q^2_{min}, f_s, m_c, m_b)
 - parameterisation (variation of param. assumptions)

Combination of charm data at HERA



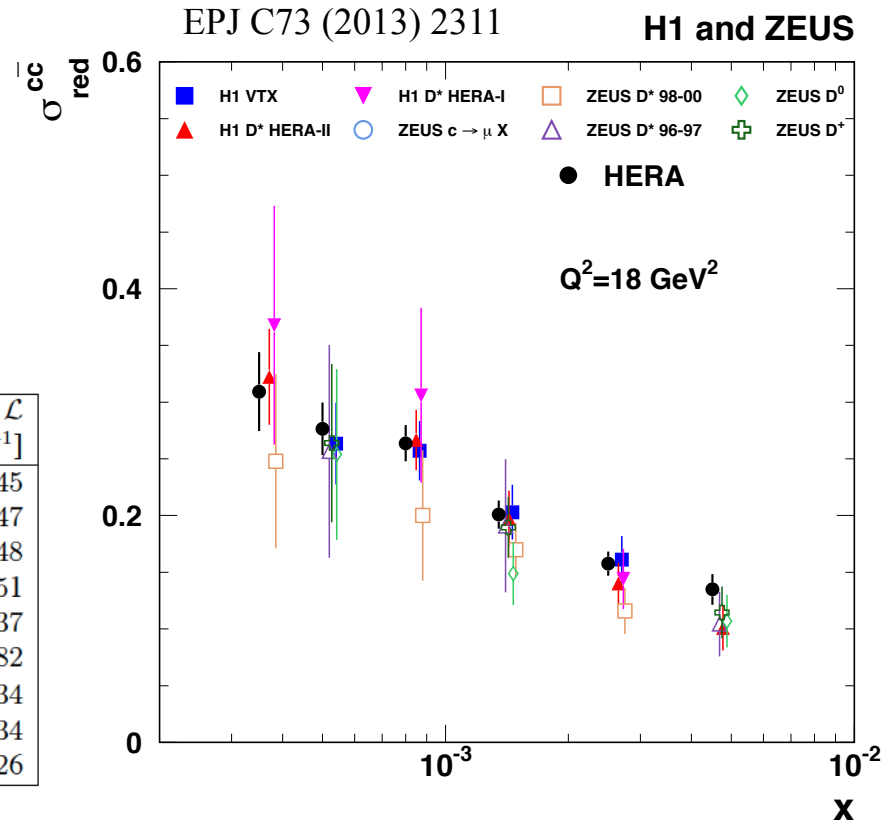
Combine different H1 and ZEUS measurements

- reconstruction of D^* and D decays
- inclusive analysis of tracks lifetime information
- muons from charm semi-leptonic decays

Data set	Tagging method	Q^2 range [GeV ²]	N	\mathcal{L} [pb ⁻¹]
1 H1 VTX [14]	Inclusive track lifetime	5 – 2000	29	245
2 H1 D^* HERA-I [10]	D^{*+}	2 – 100	17	47
3 H1 D^* HERA-II [18]	D^{*+}	5 – 100	25	348
4 H1 D^* HERA-II [15]	D^{*+}	100 – 1000	6	351
5 ZEUS D^* (96-97) [4]	D^{*+}	1 – 200	21	37
6 ZEUS D^* (98-00) [6]	D^{*+}	1.5 – 1000	31	82
7 ZEUS D^0 [12]	$D^{0, \text{no} D^{*+}}$	5 – 1000	9	134
8 ZEUS D^+ [12]	D^+	5 – 1000	9	134
9 ZEUS μ [13]	μ	20 – 10000	8	126

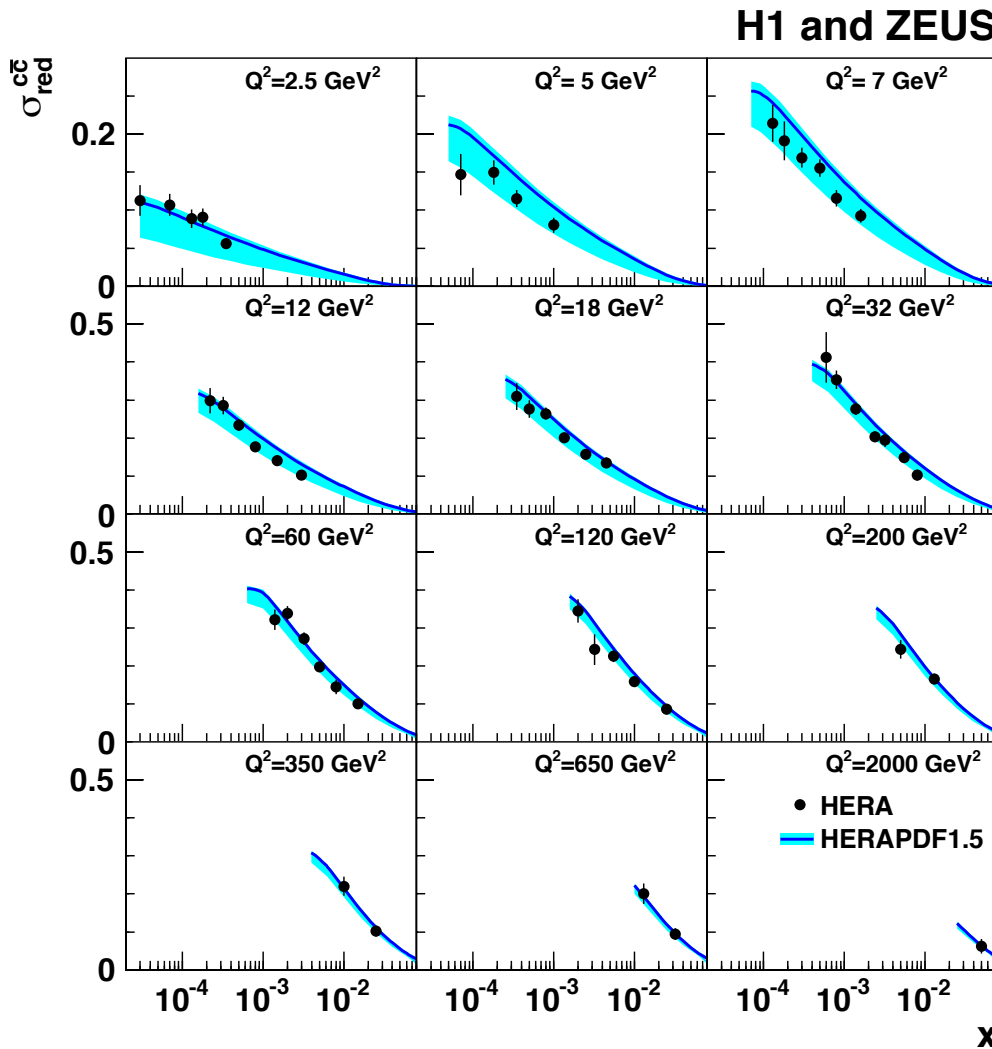
Extension of visible cross section (D^* , D , μ) to the full phase space at given x and Q^2 using HVQDIS and pdfs according to FFNS version of HERAPDF1.0 at NLO

Example of combination of charm data



→ Precision of the combined data is two times better than each of the most precise individual data sets in the combination

Charm contributions to proton str. functions $F_{2(L)}^{c\bar{c}}$



$$\begin{aligned}\sigma_{\text{red}}^{c\bar{c}} &= \frac{d^2\sigma^{c\bar{c}}}{dx dQ^2} \cdot \frac{xQ^4}{2\pi\alpha^2(Q^2)(1+(1-y)^2)} \\ &= F_2^{c\bar{c}} - \frac{y^2}{1+(1-y)^2} F_L^{c\bar{c}}\end{aligned}$$

FFNS: Fixed Flavour Number Scheme
three light quarks (u,d,s) and massive c,b (boson-gluon fusion)

Global fit ABM ($\overline{\text{MS}}$ running mass $m_c(m_c)$)

VFNS: Variable Flavour Number Scheme
from three to five active quarks (u,d,s,c,b)
c,b massive at low Q^2 , massless at high Q^2
→ different approximations (matching) in between

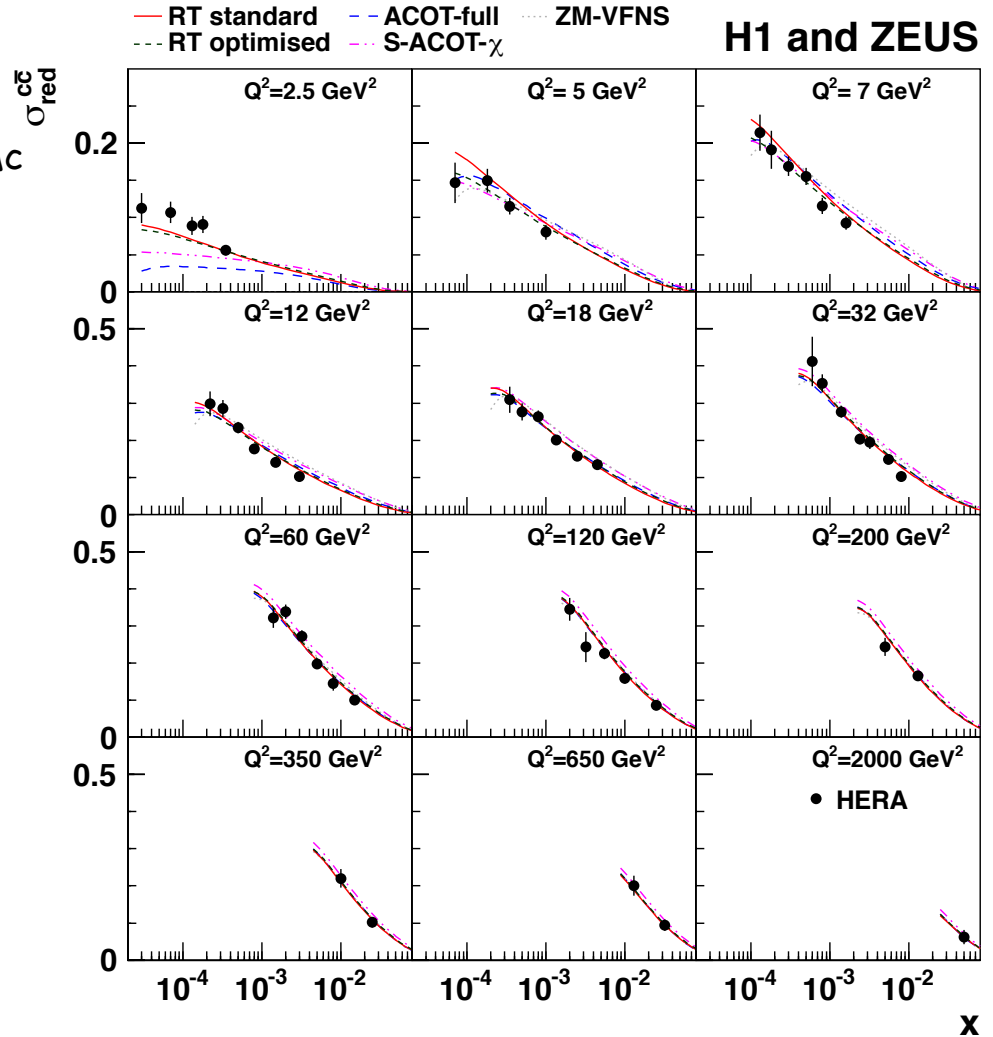
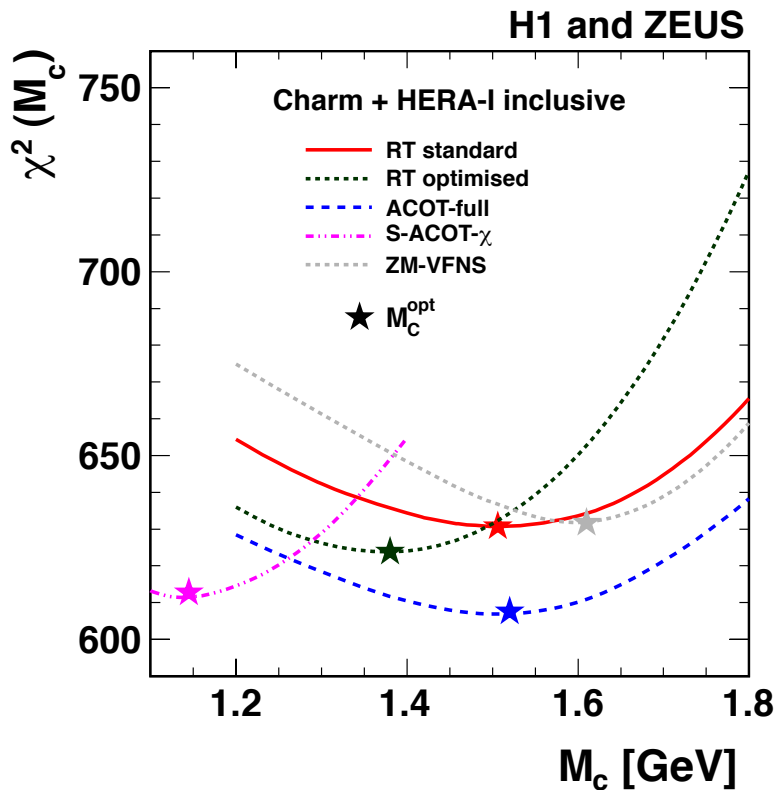
Global fits MSTW, CTEQ, NNPDF
pole mass (PDG : $m_c=1.67$)
 $m_c=1.4$ GeV recommended by RT

→ described well by HERAPDF1.5 fit to inclusive data (VFNS)
→ large error band due to $1.35 < M_c < 1.65$ GeV

consider M_c as an additional effective parameter →

Optimal charm mass parameter M_c

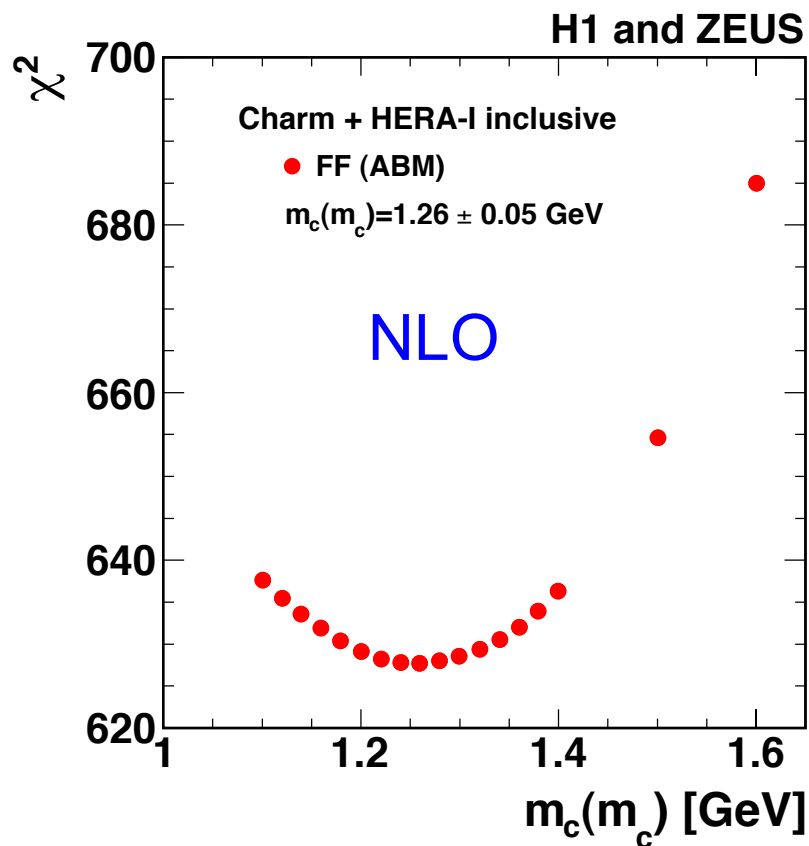
χ^2 scans of the QCD fits with different implementations of the VFNS to HERA I inclusive data and to combined charm data as function of the charm mass parameter M_c



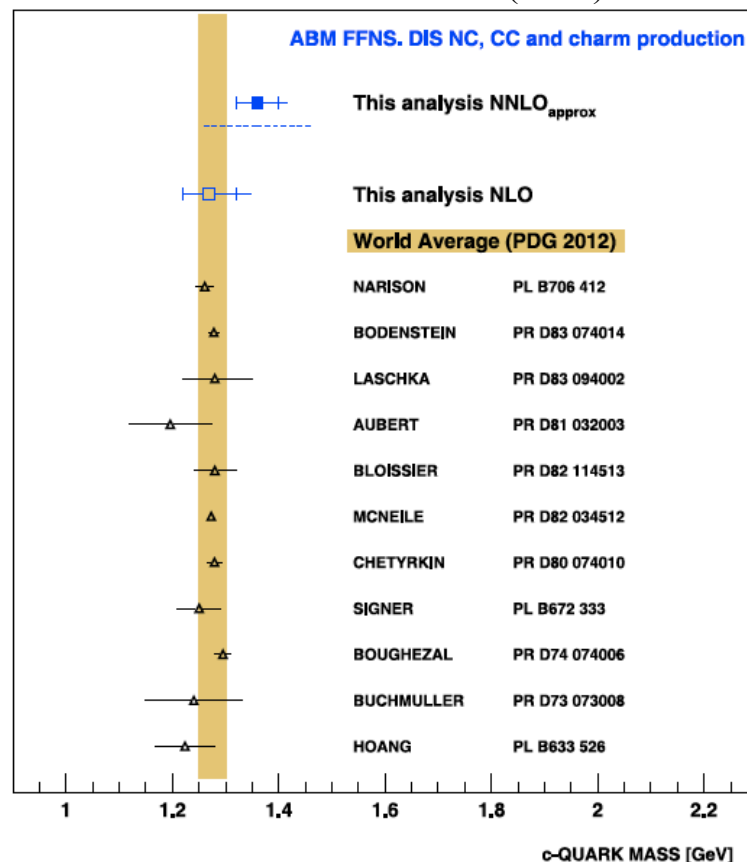
→ good description of the charm data at $Q^2 \geq 5 \text{ GeV}^2$ using optimal mass corresponding to min χ^2

Measurement of charm mass in DIS ($\overline{\text{MS}}$ scheme)

In FFNS, $\overline{\text{MS}}$ running mass $m_c(m_c)$ is a well defined physics concept with clear relation to the pole mass

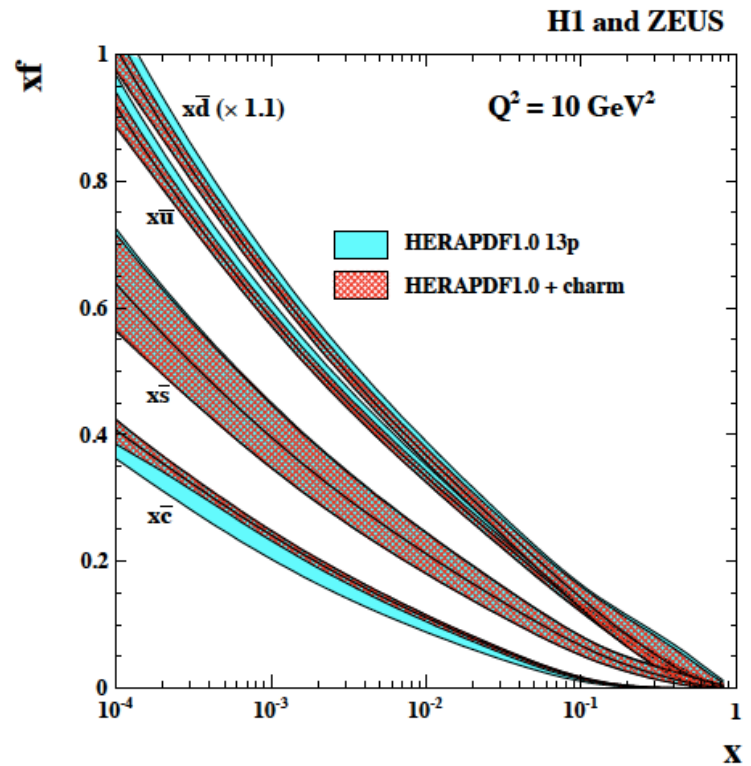
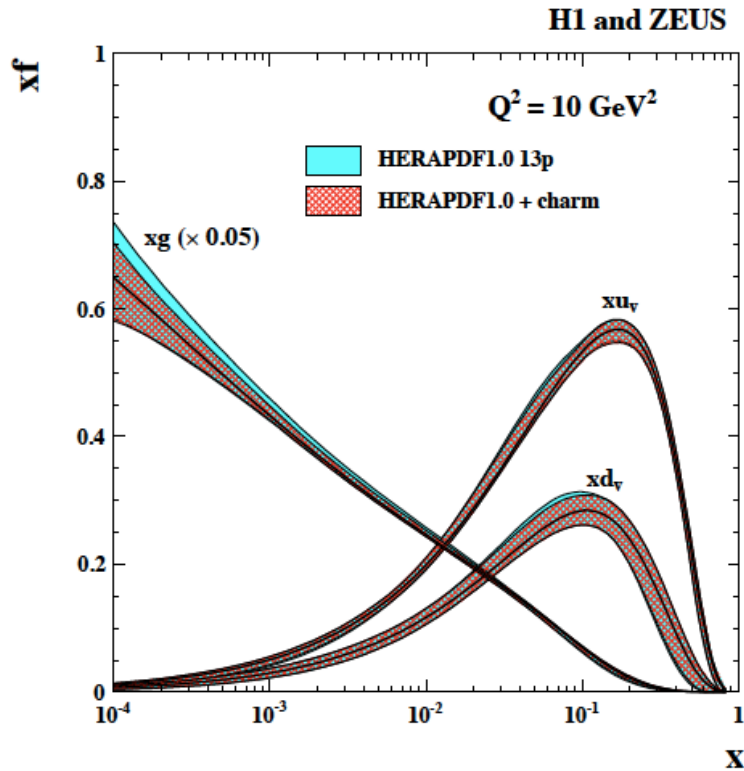


S.Alekhin et al. PLB 718 (2012) 550



- charm mass from DIS in the FFN scheme is in a good agreement with $e+e-$ and lattice
- comparable precision with world average.

Impact of the charm data on PDFs

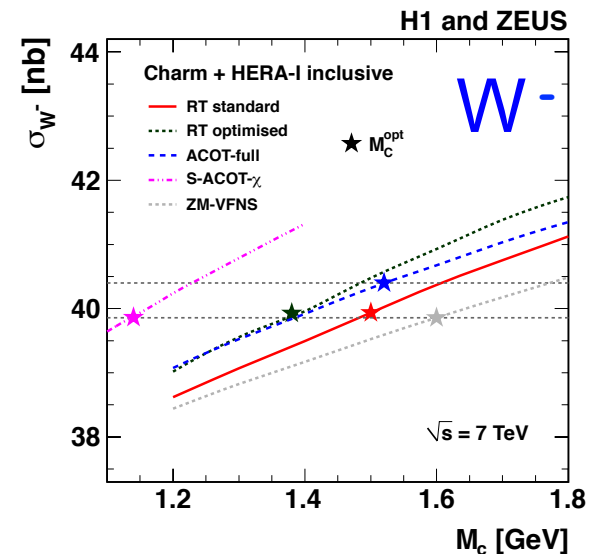
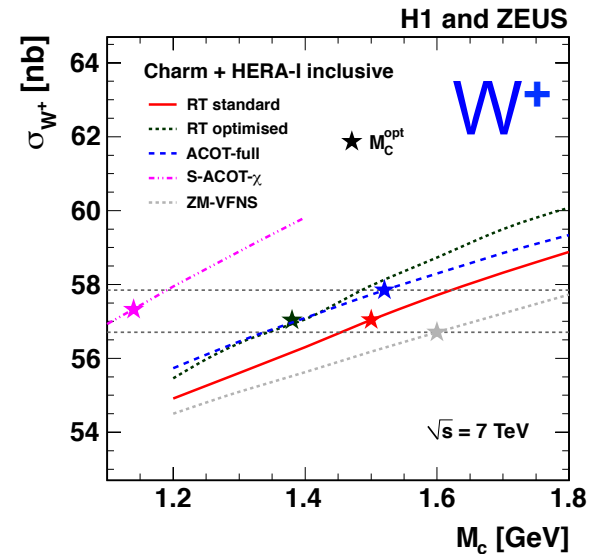
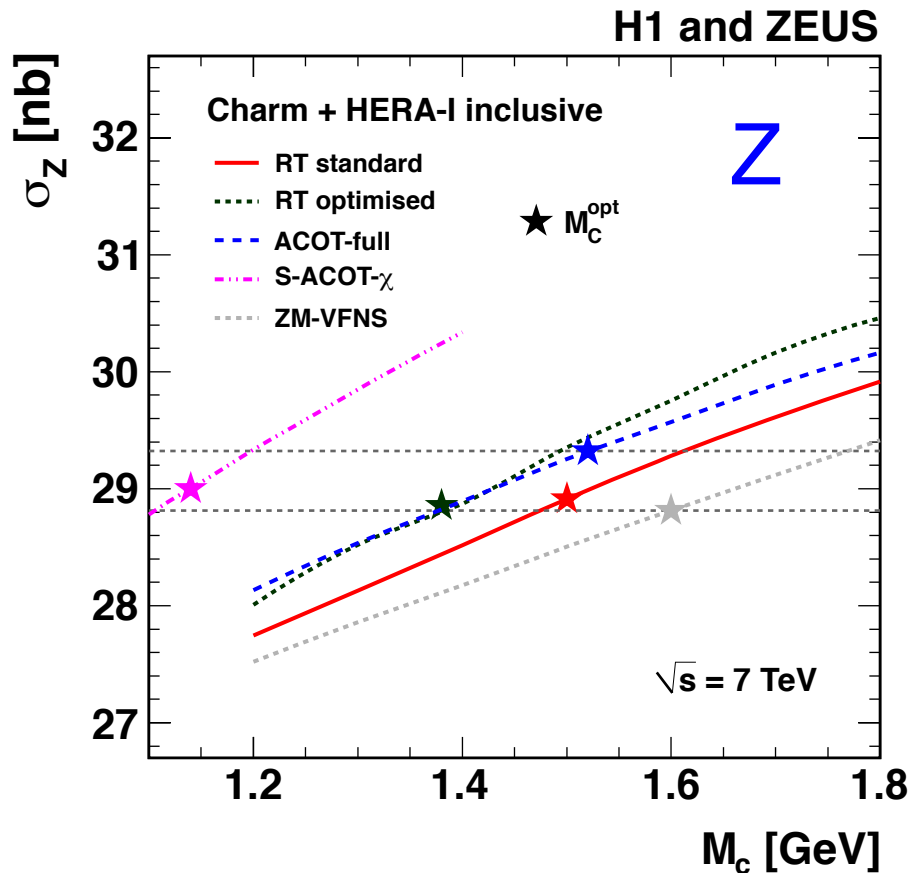


- charm distribution function uncertainty is drastically reduced
- impact on gluon (through $\gamma g \rightarrow cc$) and light sea

Z, W cross section predictions for LHC

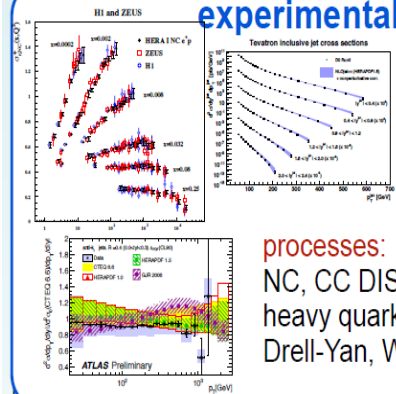
For different implementations of VFNS:
spread of 6% at fixed value of $M_c = 1.4 \text{ GeV}$

→ optimal M_c reduces uncertainty to below 2%



HERAFitter project is an open source QCD fit framework ready to extract PDFs and assess the impact of new data

experimental input



experiments:
HERA, Tevatron,
LHC, fixed target

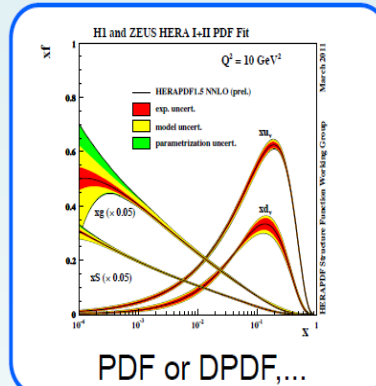
processes:
NC, CC DIS, jets, diffraction,
heavy quarks (c,b,t)
Drell-Yan, W production

theoretical calculations/tools

Heavy quark schemes:	MSTW, CTEQ, ABM
Jets, W, Z production:	fastNLO, Applgrid
Top production	NNLO (Hathor)
QCD Evolution	DGLAP (QCDNUM)
	k_T factorisation
Alternative tools	NNPDF reweighting
Other models	Dipole model

+ Different error treatment models
+ Tools for data combination (HERAaverager)

HERAFitter



$\alpha_S(M_Z), m_c, m_b, m_t, f_s, \dots$

Theory predictions

Benchmarking

Comparison of schemes

www.herafitter.org

H1 and ZEUS
(charm studies and HERA PDF)

[EPJ C73 \(2013\) 2311](#)

[JHEP 1209 \(2012\) 061](#)

ATLAS (s-quark density
determination, jets)

[PRL 109 \(2012\) 012001](#)

[ATLAS-CONF-2012-128](#)

few ongoing studies in CMS

LHeC studies

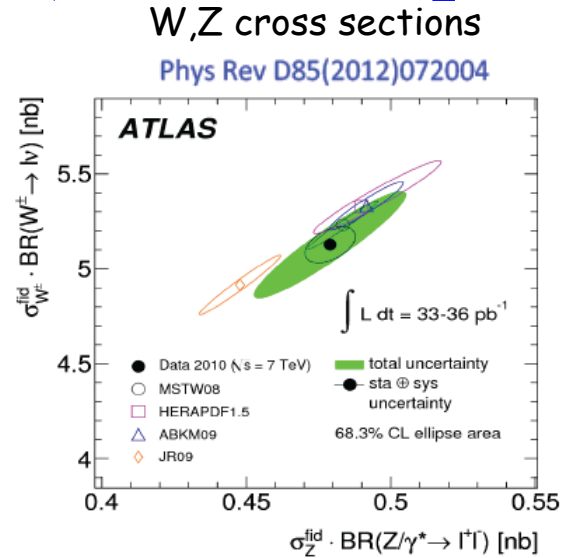
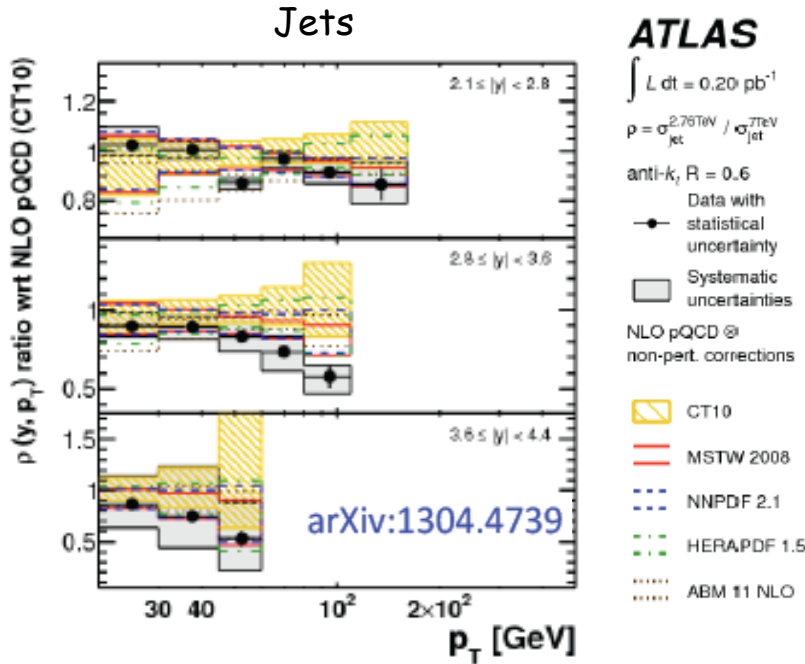
[J.Phys. G39 \(2012\) 075001](#)

→ well integrated into the high energy community (both, experiment and theory)

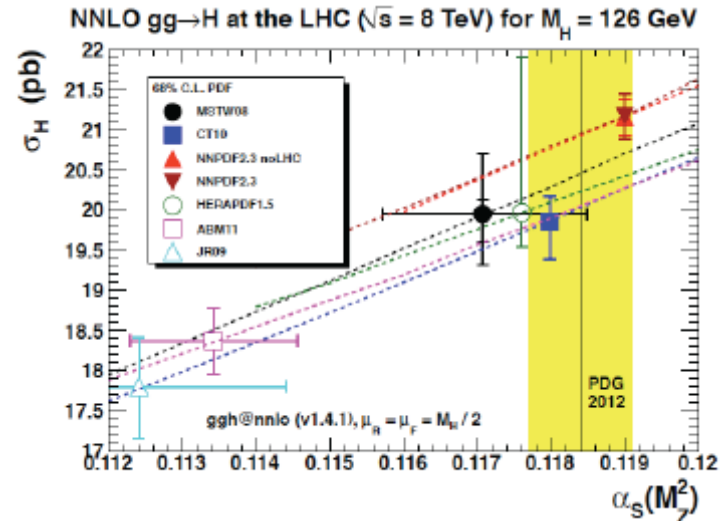
Summary

- HERA I and HERA II inclusive NC and CC cross section measurements are completed and published both by H1 and ZEUS
- Combination of the H1 and ZEUS inclusive NC and CC $e^\pm p$ data
 - all HERA I results are combined using a model independent approach leading to significant reduction of systematic uncertainties; combination is extended to include prelim. HERA II data
 - aiming for combination of the complete final HERA I+II H1&ZEUS data
- HERAPDF: QCD analyses of the HERA data only
 - HERAPDF 1.0 (HERA I); HERAPDF 1.5 (HERA I + prel. HERA II, recommended), ...
 - aiming for HERAPDF 2.0 using final combined inclusive data from HERA I+II
- Combined charm production cross sections in DIS at HERA
 - control of the heavy quark treatment in the QCD evolution
 - improve precision of PDFs, reduce uncertainties related to charm mass in predictions for LHC
 - measure charm mass in the \overline{MS} scheme
- HERAFitter
 - an open source QCD platform ready to extract PDFs using new (LHC) data

HERAPDF for LHC (few examples)



gg → H cross section



W charge asymmetry

