

Deeply virtual Compton Scattering cross section measured with CLAS

Baptiste GUEGAN

PHOTON 2013, Paris, 22/05/13

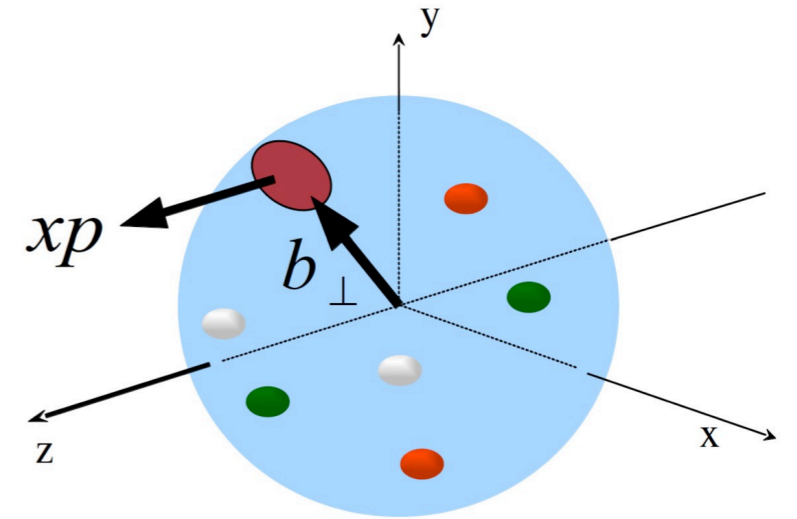


Deeply Virtual Compton Scattering



Generalized Parton Distributions (GPD):

→ correlation between x and t



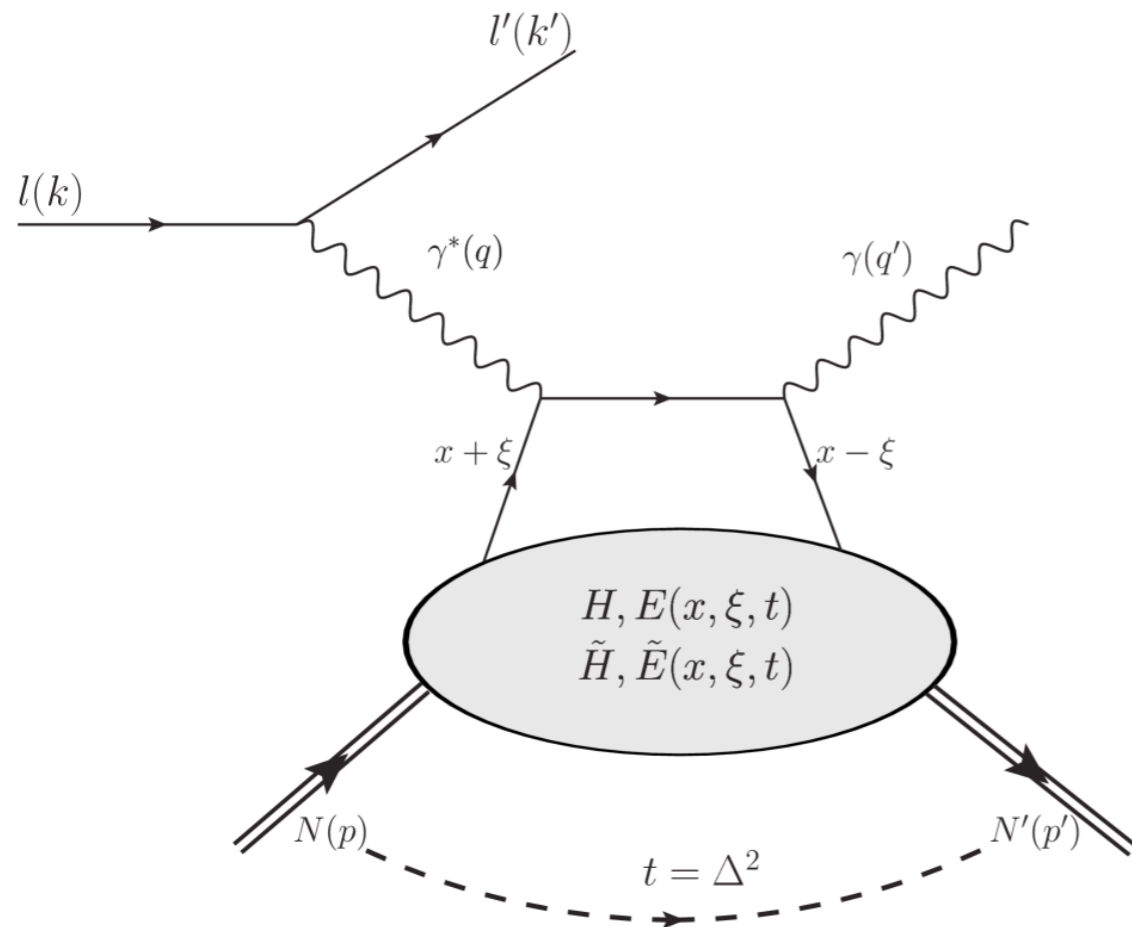
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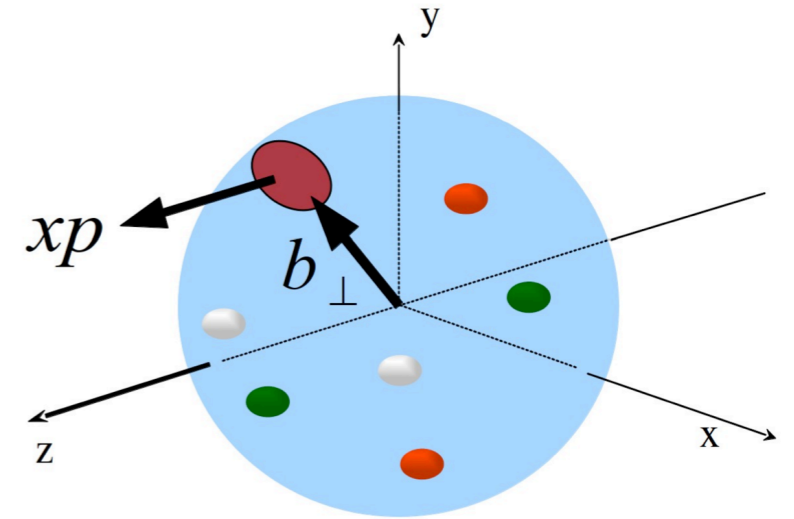
→ correlation between x and t

Accessible via Deeply Virtual Compton Scattering:



$(x + \xi)$ | longitudinal momentum fractions of quark
 $(x - \xi)$ |

$t = \Delta^2 = (p' - p)^2$: squared momentum transfer



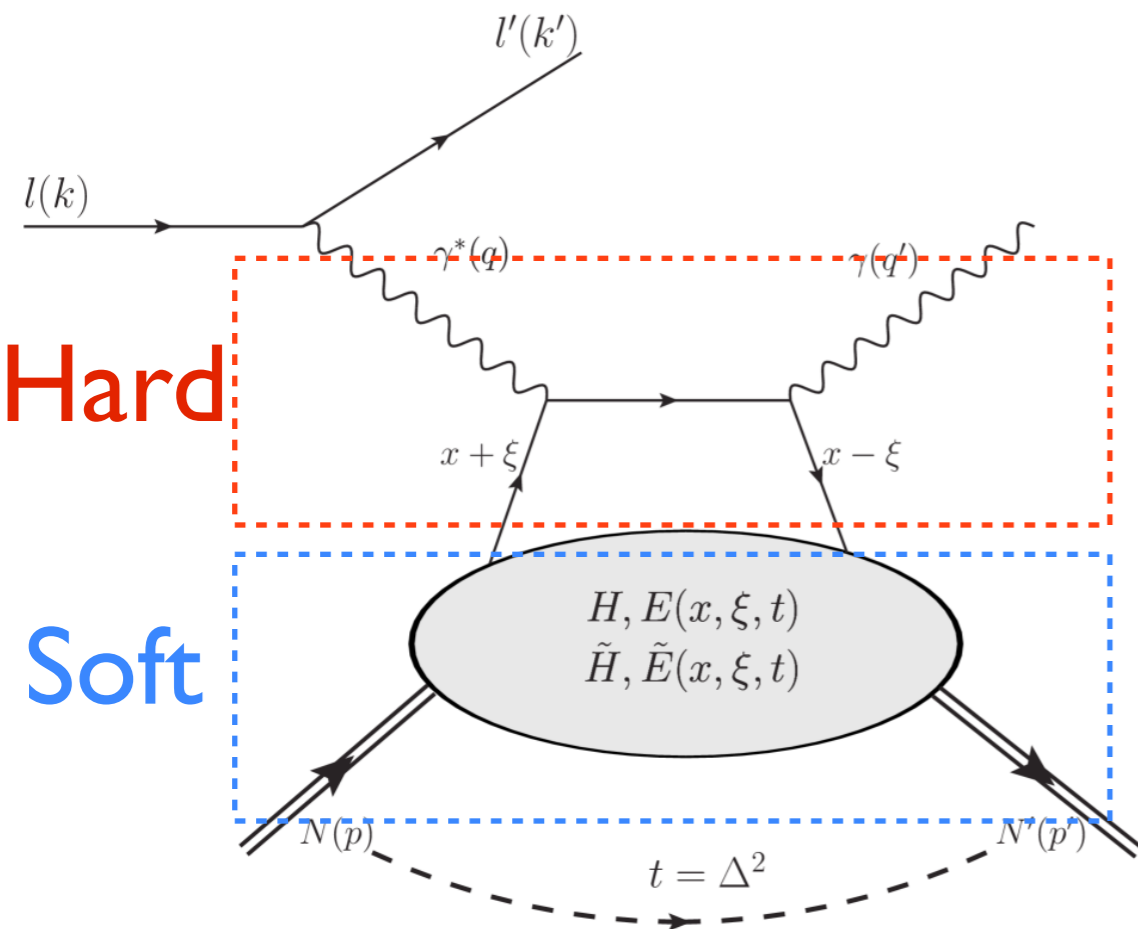
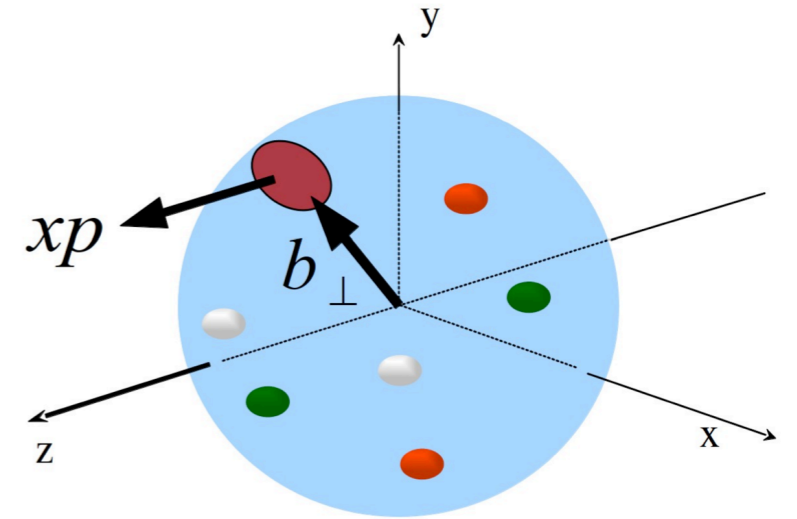
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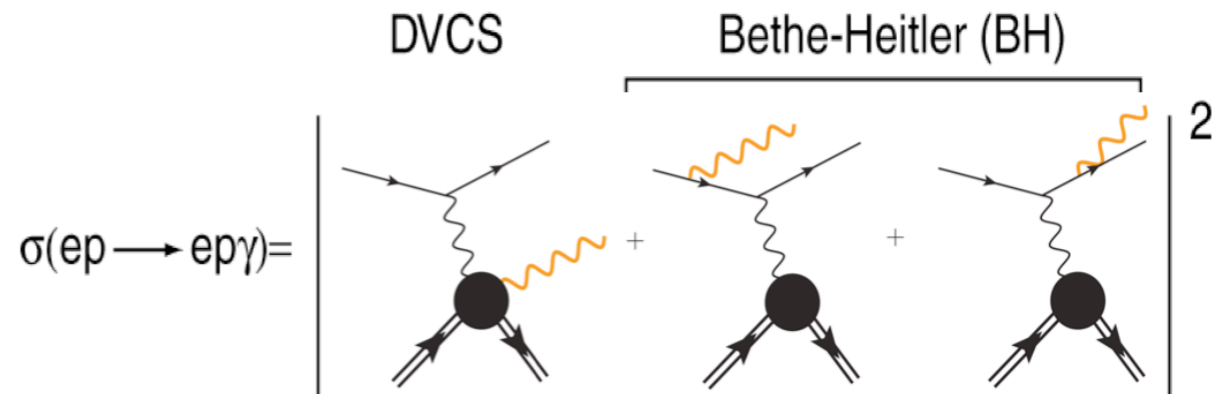
$$x_B = \frac{Q^2}{2p \cdot q} \quad \xi \approx \frac{x_B}{2 - x_B}$$

At large Q^2 , small t and fixed x_B , the process can be factorized and described by 4 Generalized Parton Distributions

Exclusive electroproduction of a photon

Contribution from both DVCS and Bethe-Heitler (undistinguishable experimentally):

$$\sigma_{(ep \rightarrow ep\gamma)} \propto |T^{DVCS} + T^{BH}|^2$$



● T^{BH} : At low t , the nucleon FFs (Dirac, Pauli) are well known so that T^{BH} is precisely calculable

● $T^{DVCS} \propto \int_{-1}^1 dx \frac{GPD(x, \xi, t)}{x \pm \xi \mp i\epsilon} = \mathcal{P} \int_{-1}^1 dx \frac{GPD(x, \xi, t)}{x \pm \xi} \pm i\pi GPD(x = \mp \xi, \xi, t)$

→ GPDs appear in the real part through an integral over x

→ GPDs appear in the **imaginary part** at the lines $x = \pm \xi$

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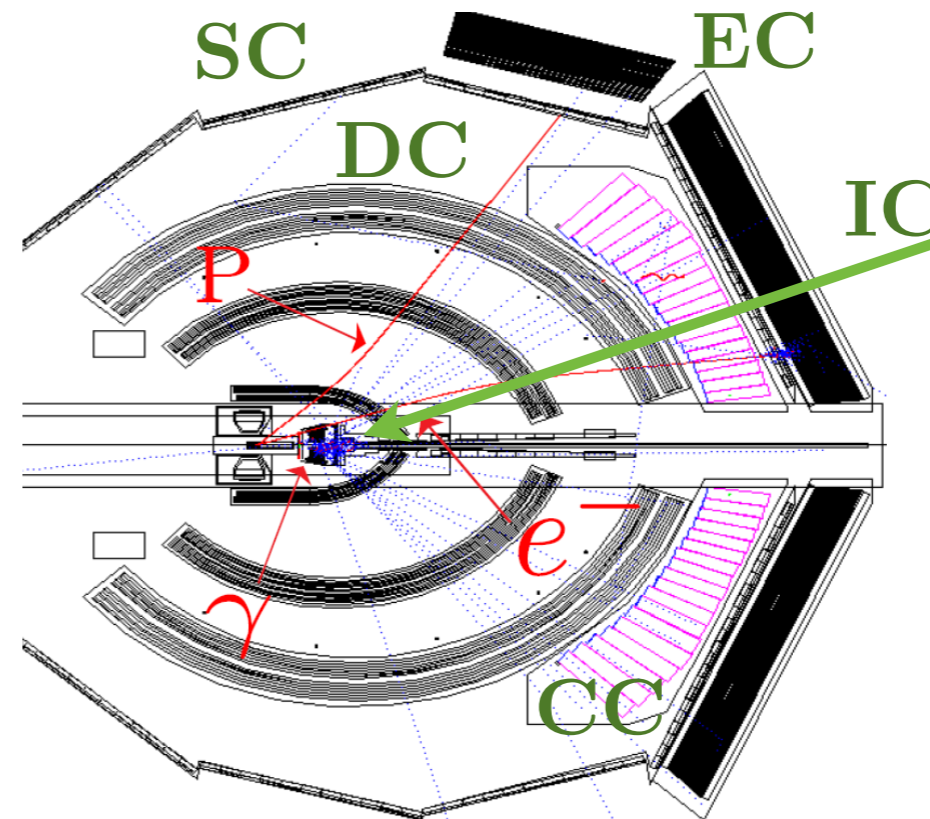
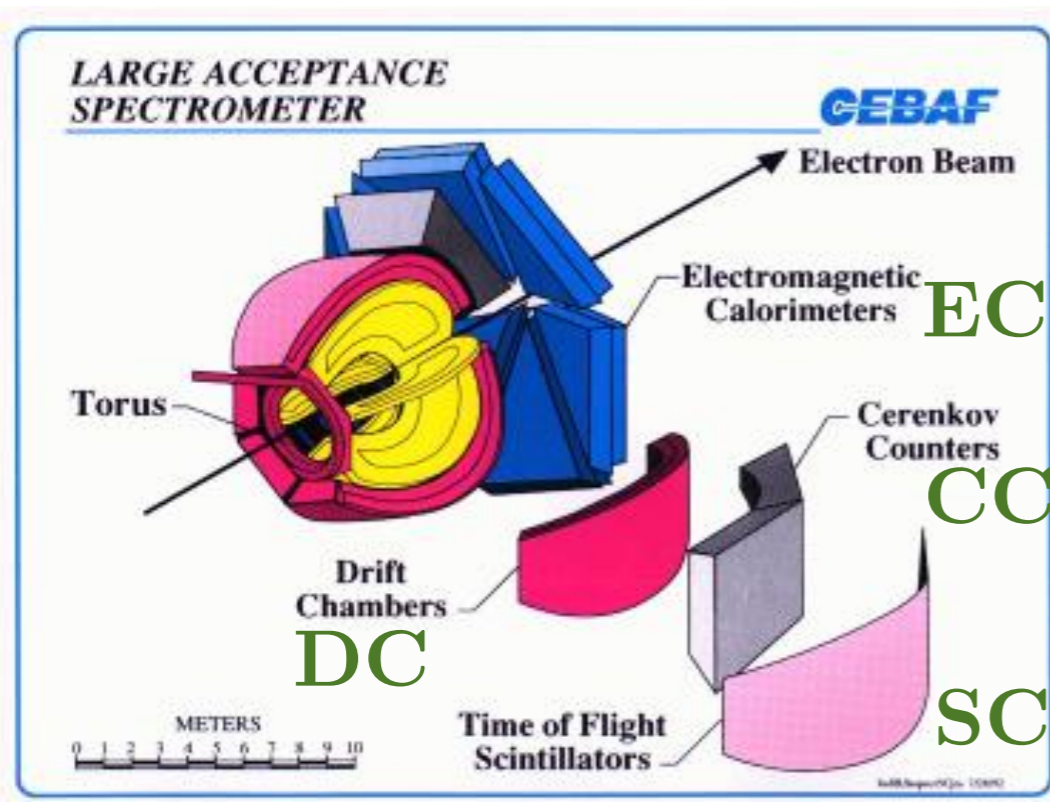
With a polarized beam and an unpolarized target, one can measure 2 observables:

● $\frac{d^4\sigma}{dtdQ^2 dx_B d\phi} \propto |T^{BH}|^2 + 2T^{BH} \text{Re}(T^{DVCS}) + |T^{DVCS}|^2$

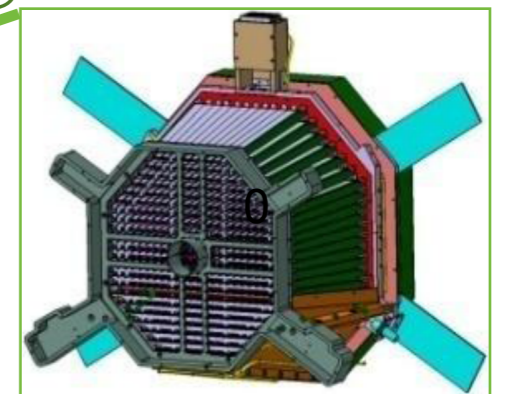
● $\frac{d^4\vec{\sigma} - d^4\overleftarrow{\sigma}}{dtdQ^2 dx_B d\phi} \propto 2T^{BH} \text{Im}(T^{DVCS}) + \left[|T^{D\vec{V}CS}|^2 - |T^{D\overleftarrow{V}CS}|^2 \right]$

DVCS experiment

- One experiment with two data set: e1-dvcs1 (2005) H-S.Jo, and e1-dvcs2 (2008)
- CLAS + dedicated equipment (IC electromagnetic calorimeter + solenoid)



lead tungstate
crystals
+ APD readout



DVCS photons are
mostly emitted
at forward angles

Beam energy: 5.88 GeV

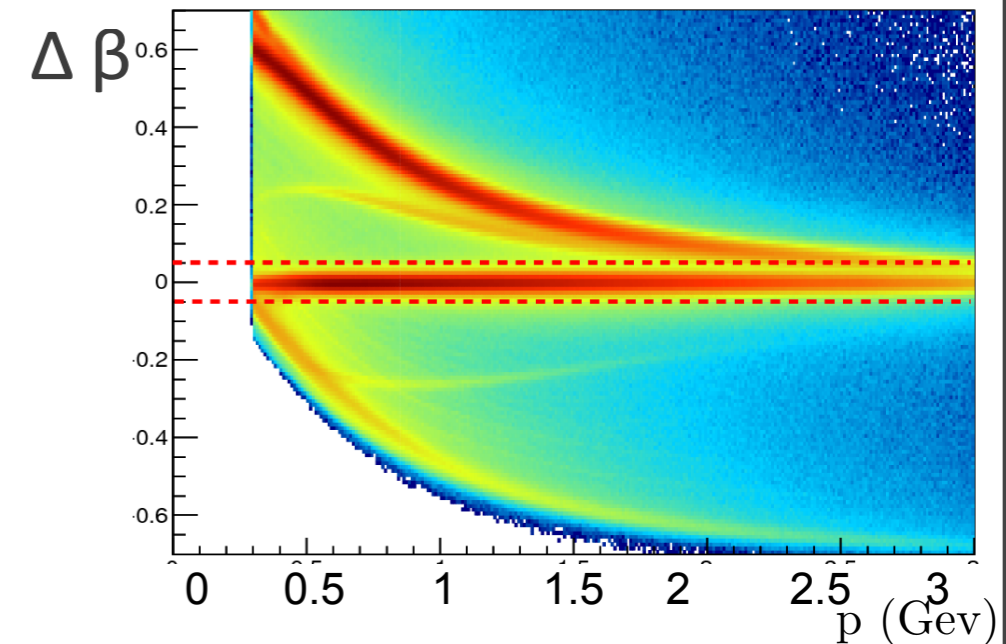
Beam polarization: 82-87%

Beam current: 20nA

DVCS analysis steps

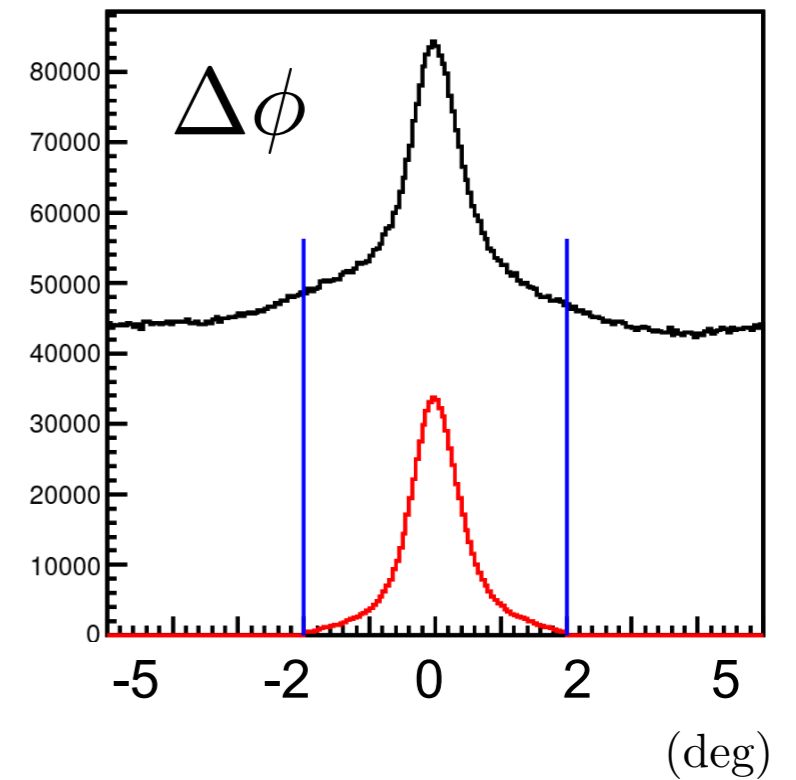
- Identification of the final-state particles: e, p, γ

$$\Delta\beta = \beta_{\text{measured}}^{SC} - \beta_{\text{calculated}}^{DC}(M_p) = \frac{d}{ct} - \frac{p}{\sqrt{p^2 + M_p^2}}$$



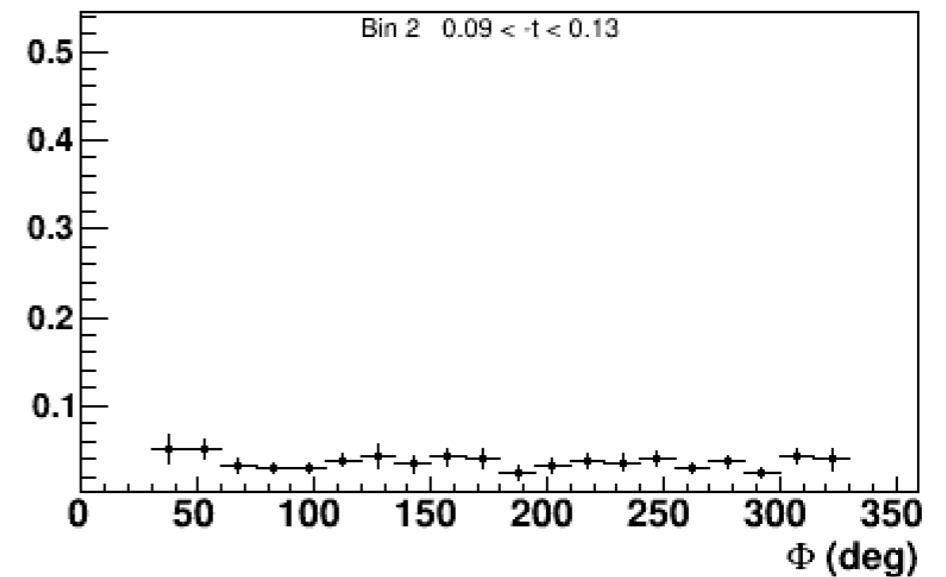
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DVCS analysis steps

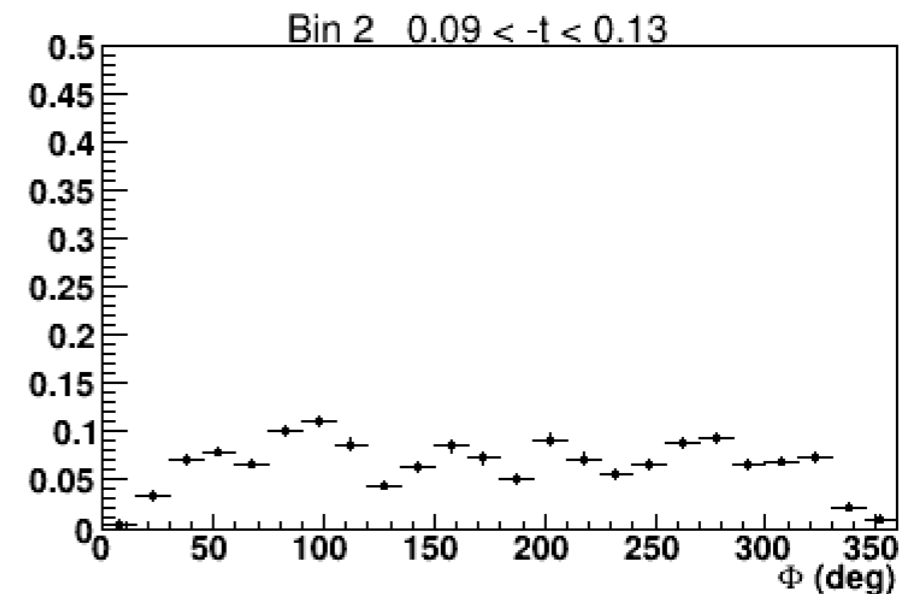
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- Evaluation of the contamination of the DVCS channel by the π^0 when one of the two photons is undetected: $ep \rightarrow ep\pi^0 \rightarrow ep\gamma(\gamma)$



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- Acceptance computation:
$$\frac{N_{ep\gamma}^{REC} MC}{N_{ep\gamma}^{GEN} MC}$$



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- The integrated luminosity for the whole DVCS2 data set

DVCS analysis steps

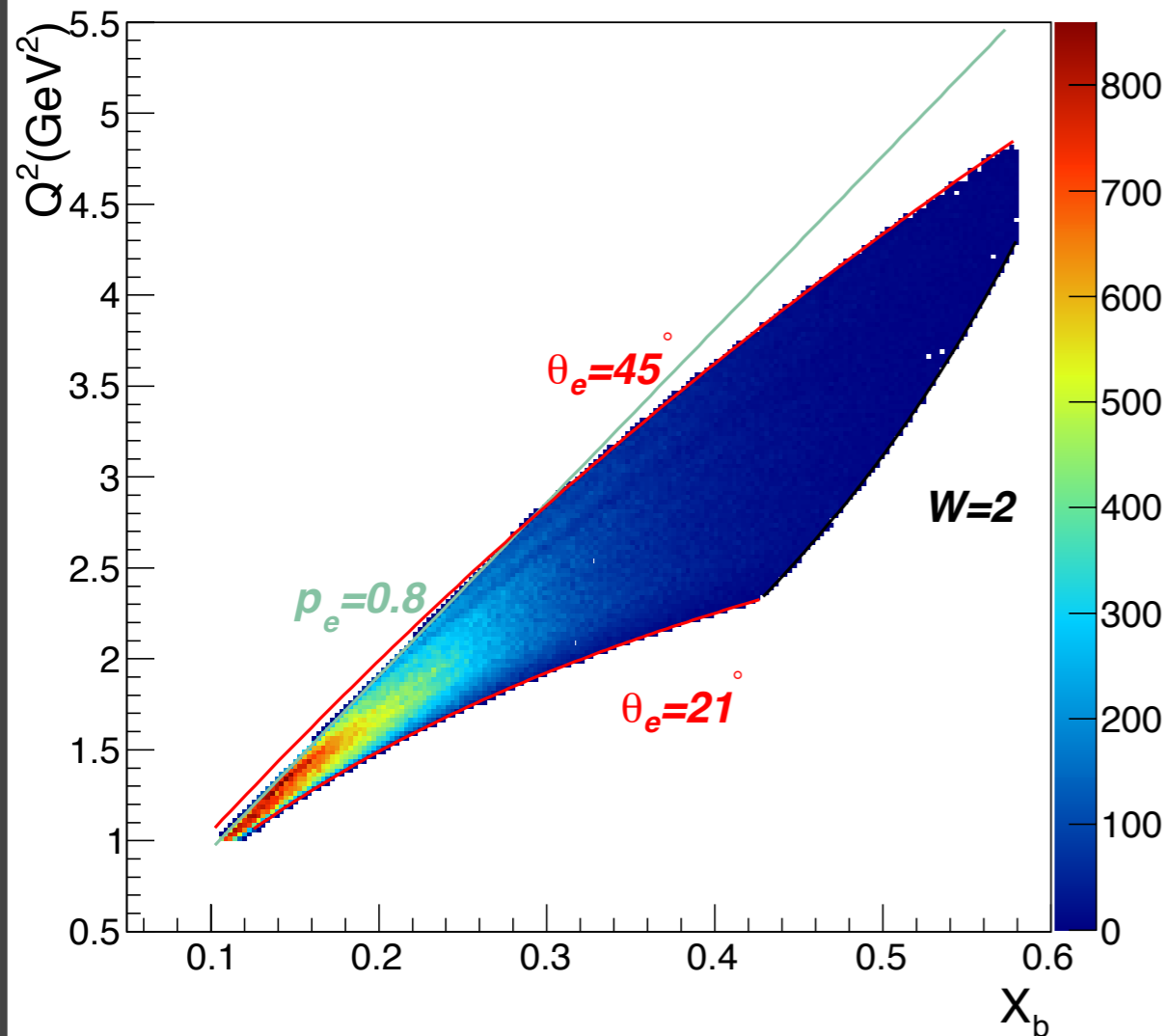
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- The radiative corrections calculated in each bin in order to compute the cross section at the Born term: $\sim 20\%$ in the BH approximation

Kinematic coverage of the e1-DVCS data and binning

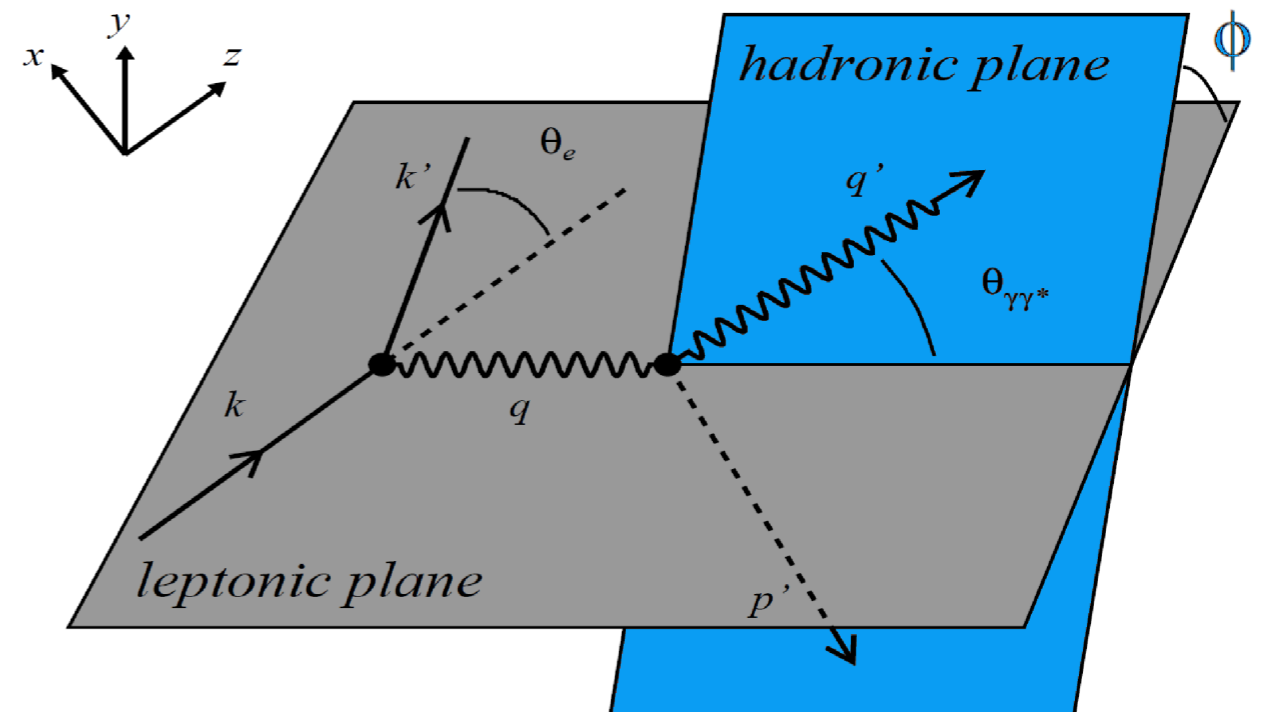
$$Q^2 > 1 \text{ GeV}^2, W > 2 \text{ GeV}, 21^\circ < \theta_e < 45^\circ, p_e > 0.8 \text{ GeV}$$



The kinematics of the DVCS reaction is defined by 4 independent variables :

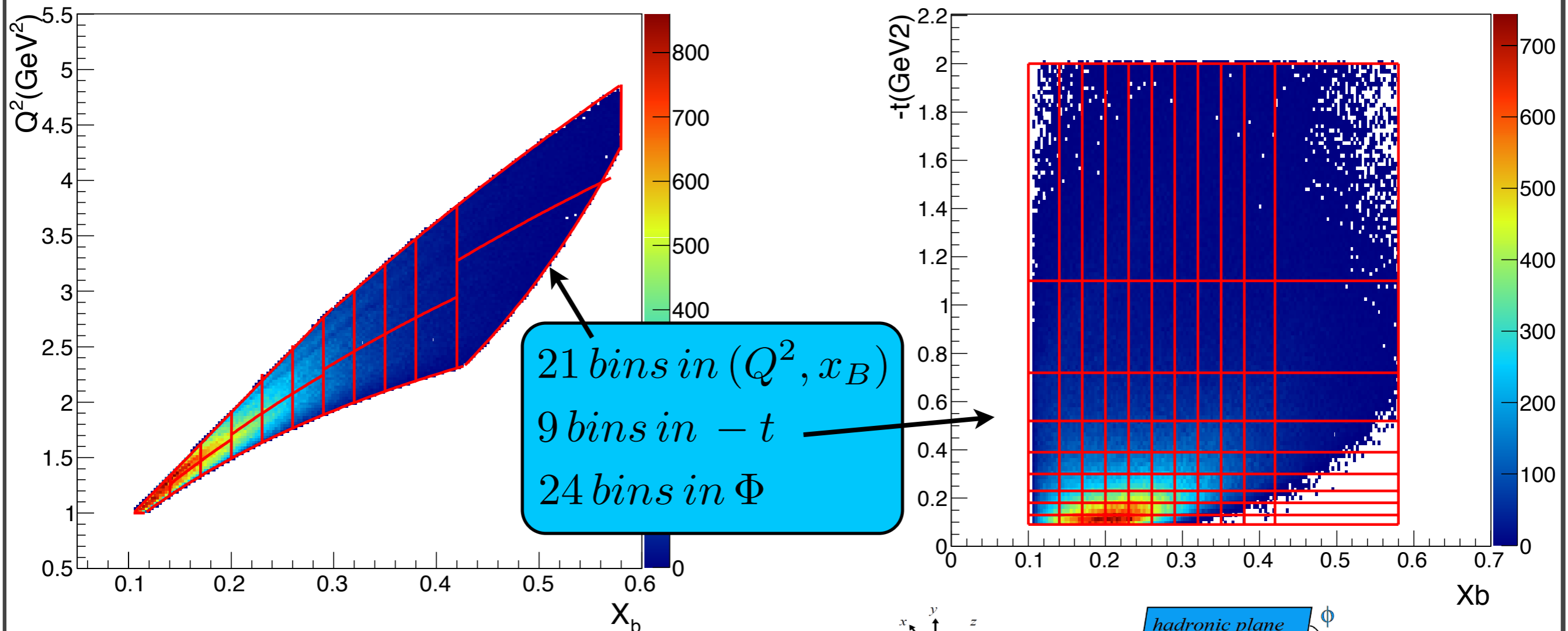
$$Q^2, x_B, -t, \Phi$$

→ 4-dimensional binning



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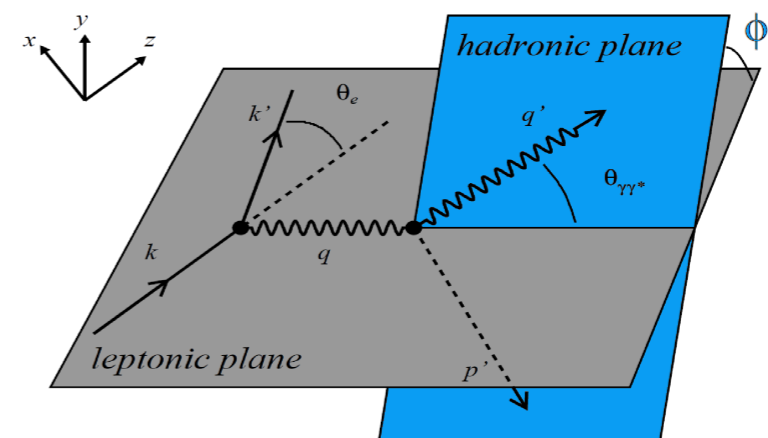
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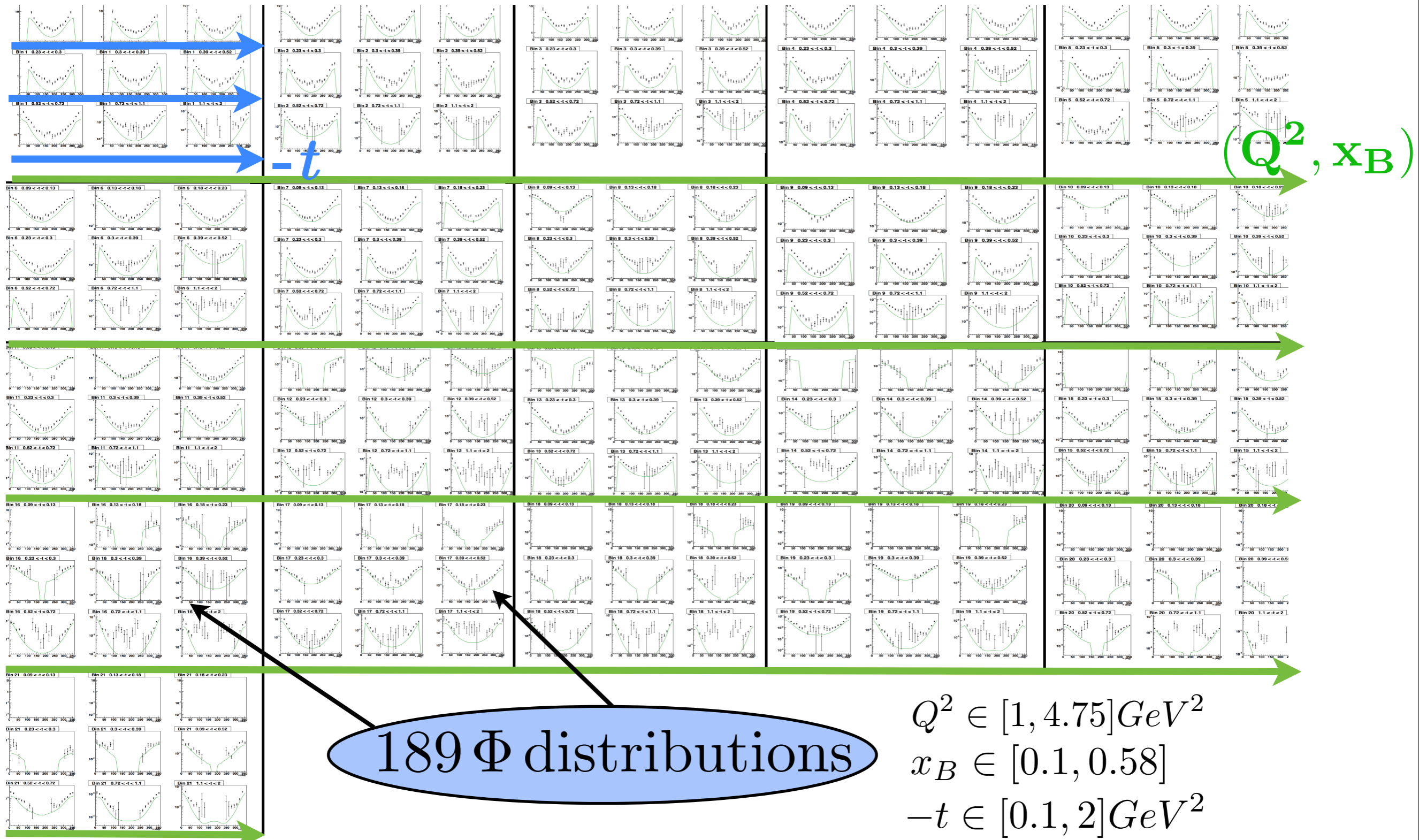
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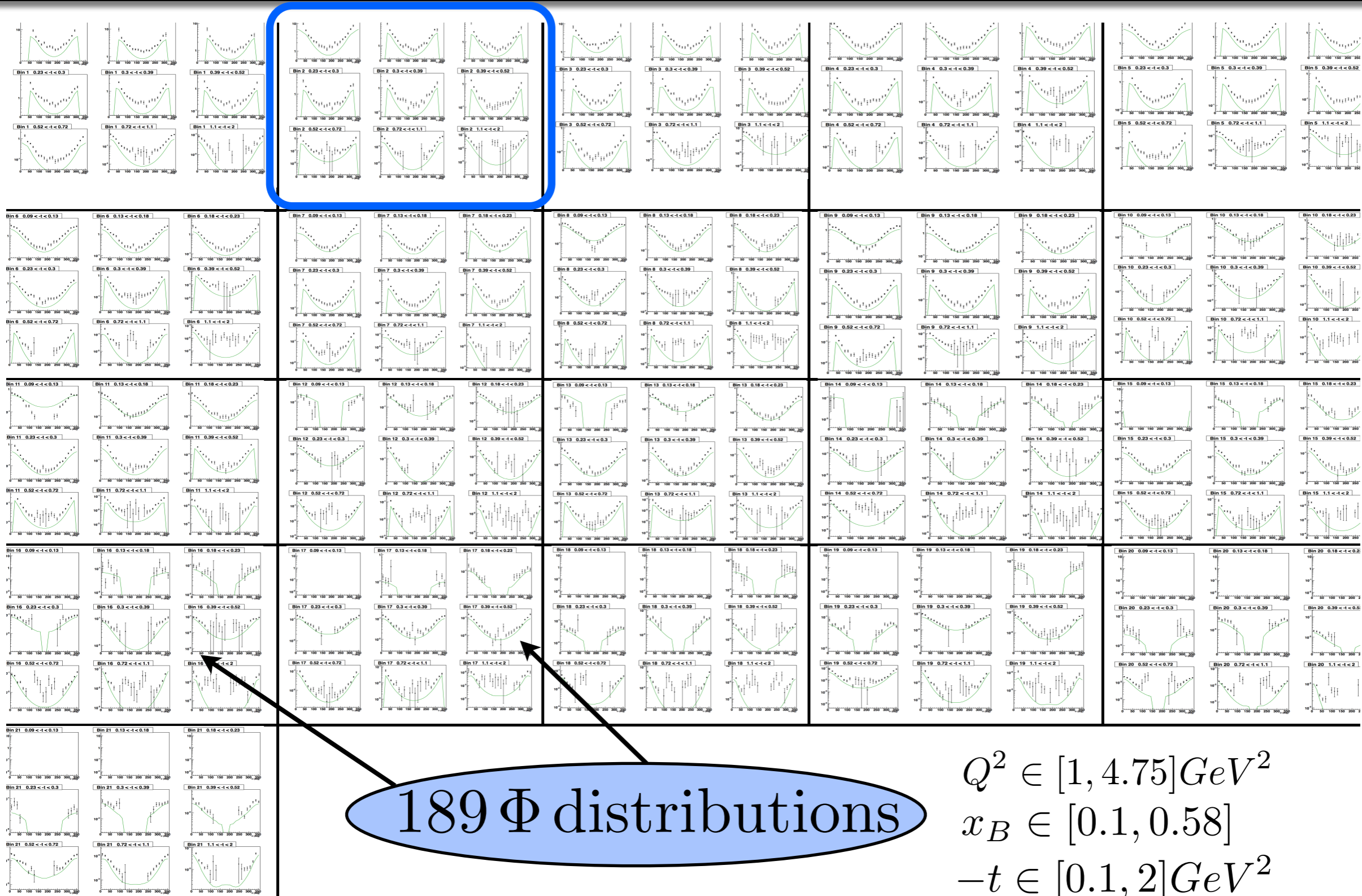
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DVCS differential cross section



DVCS differential cross section



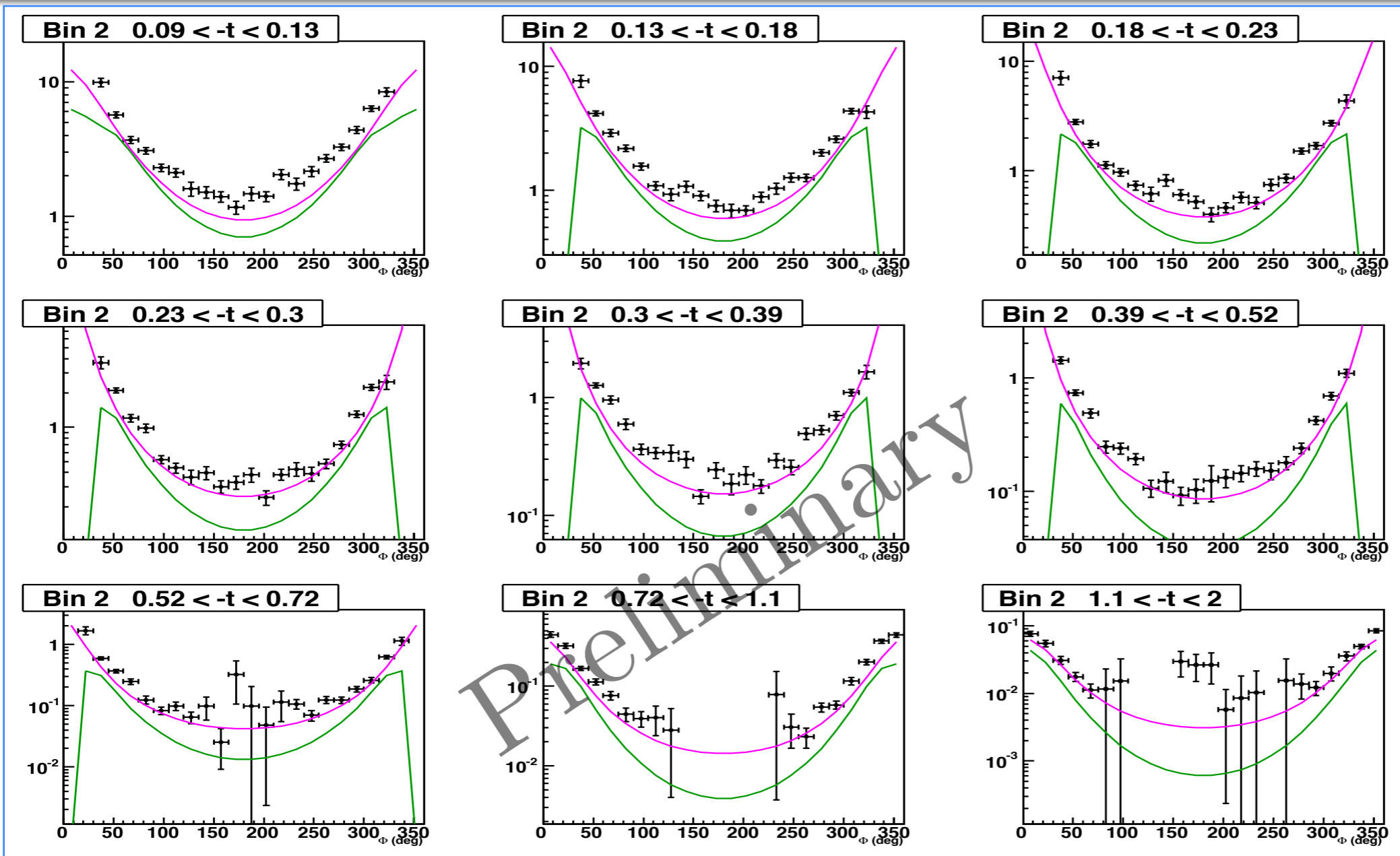
189 Φ distributions

$$Q^2 \in [1, 4.75] GeV^2$$

$$x_B \in [0.1, 0.58]$$

$$-t \in [0.1, 2] GeV^2$$

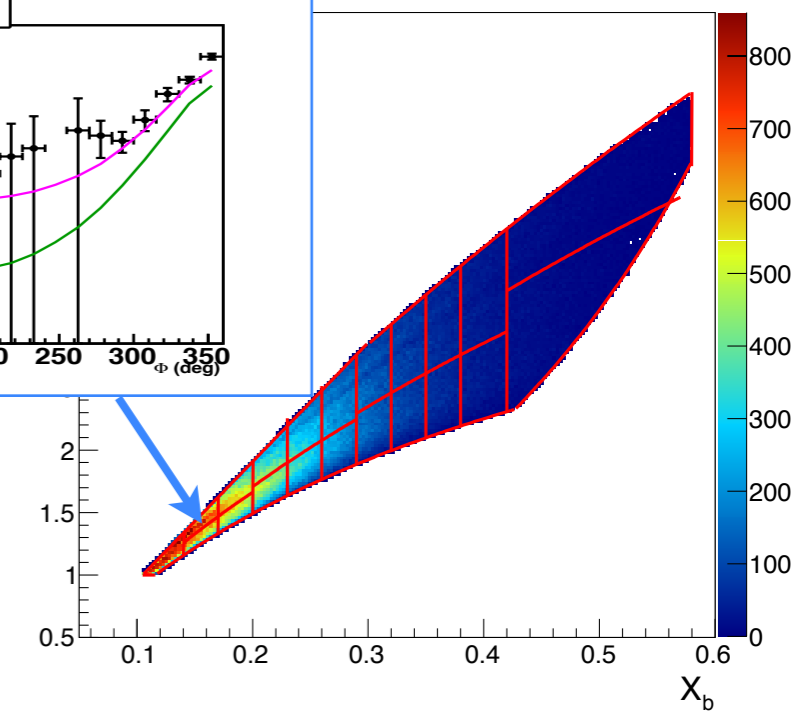
Unpolarized cross section



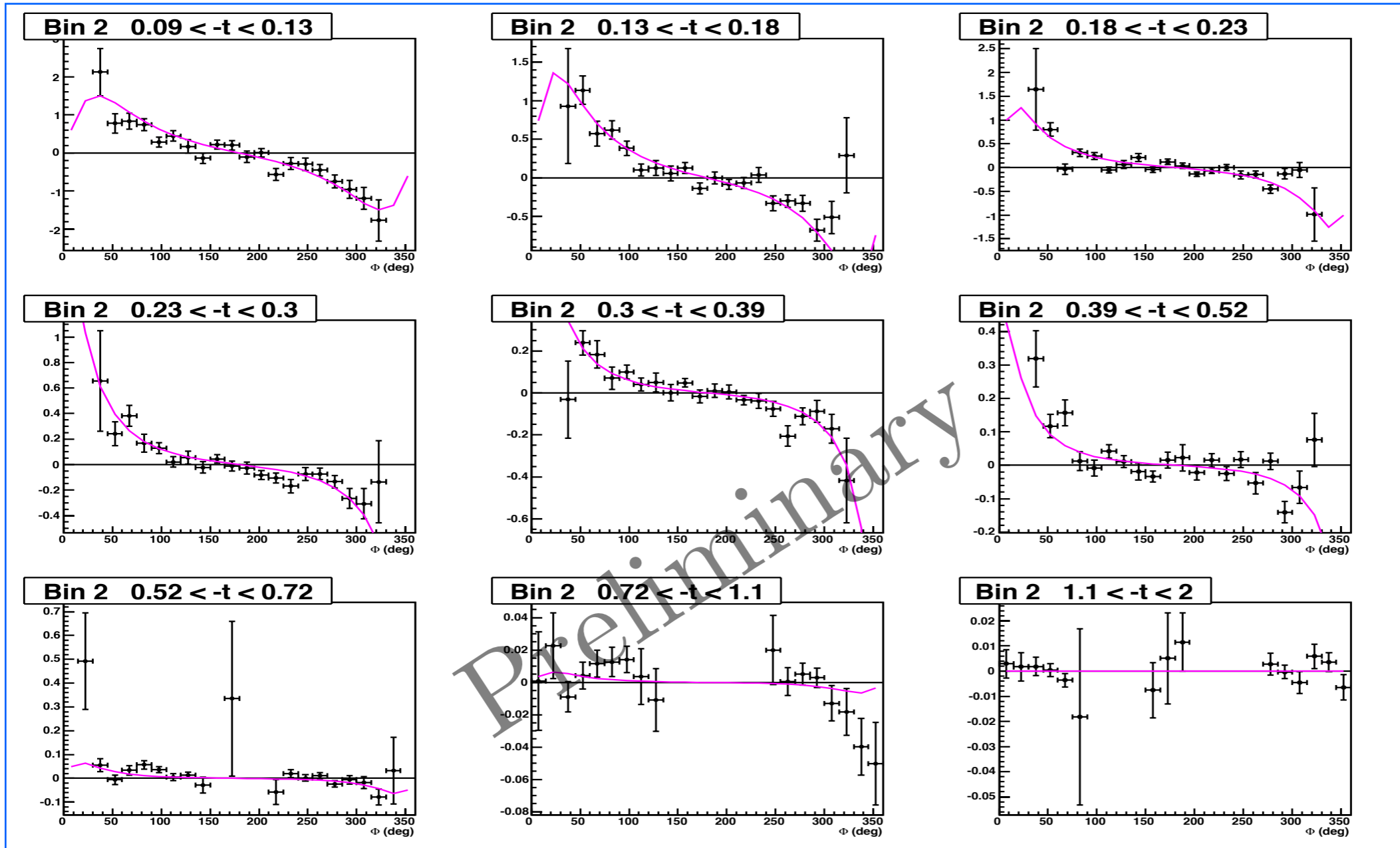
● $\frac{d^4 \sigma_{ep \rightarrow ep \gamma}}{dQ^2 dx_B dt d\Phi}$ (nb/GeV⁴)

— Bethe-Heitler

— VGG M. Vanderhaeghen
P.A.M. Guichon,
M. Guidal



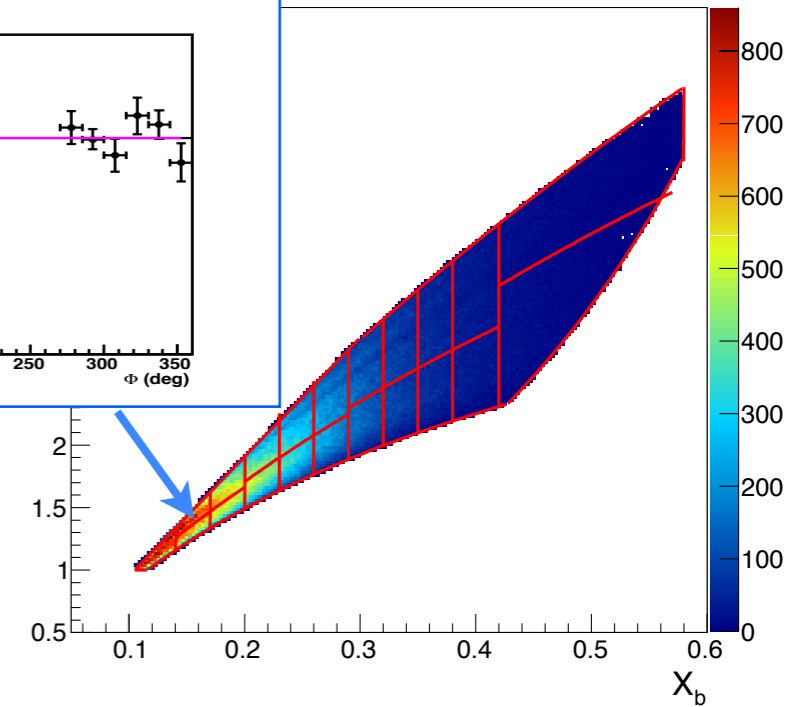
Difference of polarized cross sections



$$\bullet \frac{1}{2} \left(\frac{d^4 \sigma_{ep \rightarrow ep \gamma}^{\rightarrow}}{dQ^2 dx_B dt d\Phi} - \frac{d^4 \sigma_{ep \rightarrow ep \gamma}^{\leftarrow}}{dQ^2 dx_B dt d\Phi} \right) \text{ (nb/GeV}^4\text{)}$$

$$= \sin(\Phi) \Gamma_{\Phi} \Im m \left[F_1 \mathcal{H} + \xi (F_1 + F_2) \tilde{\mathcal{H}} - \frac{t}{4M^2} F_2 \mathcal{E} \right]$$

— VGG



Extraction of Compton Form Factors (CFFs)

Quasi-model-independent fitting procedure (M. Guidal, Eur. Phys. J. A 37, 319 (2008)):

→ One does not extract the GPDs, but associated quantities called Compton Form Factors

$$\mathcal{T}^{DVCS} \propto \int_{-1}^1 dx \frac{GPD(x, \xi, t)}{x \pm \xi \mp i\epsilon} = \mathcal{P} \int_{-1}^1 dx \frac{GPD(x, \xi, t)}{x \pm \xi} \pm i\pi GPD(x = \mp \xi, \xi, t)$$

Real part Imaginary part

→ One has two CFFs for each GPD $H, \tilde{H}, E, \tilde{E} \rightarrow 8$ CFFs

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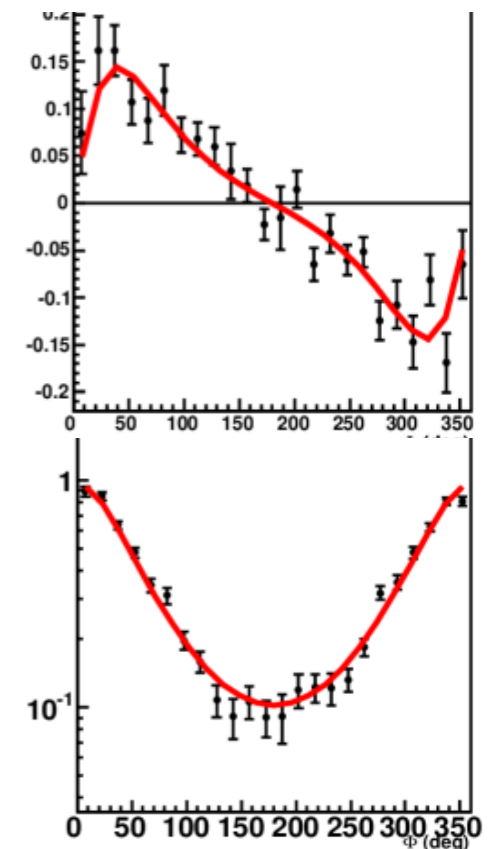
→ 2 independent observables, 8 unknowns (the CFFs):



→ Non-linear problem, strong correlations

→ Bounding the domain of variation of the CFFs (5xVGG)

→ At fixed $(Q^2, x_B, -t)$, extraction of the CFFs from the unpolarized and polarized cross sections (x189 bins) with MINUIT + MINOS.



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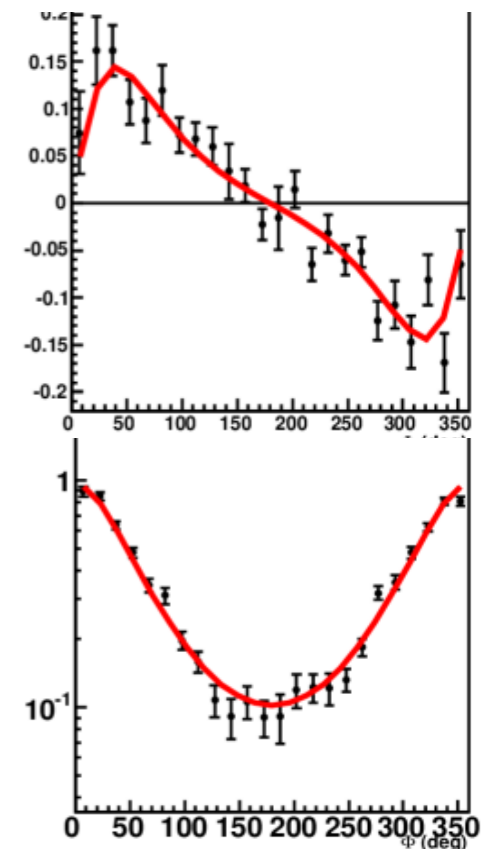
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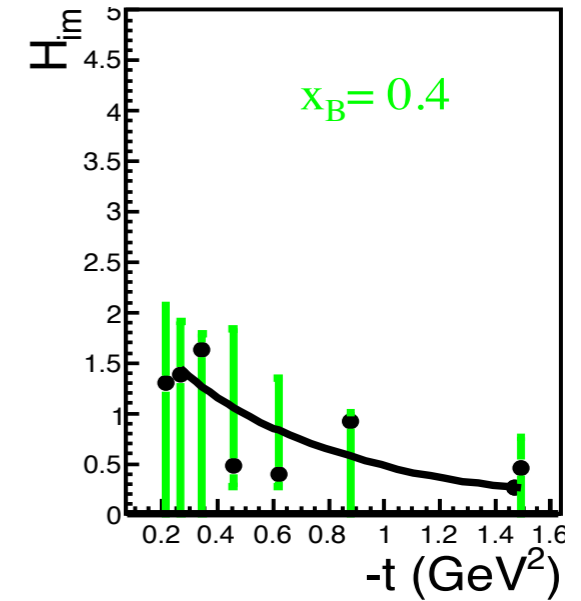
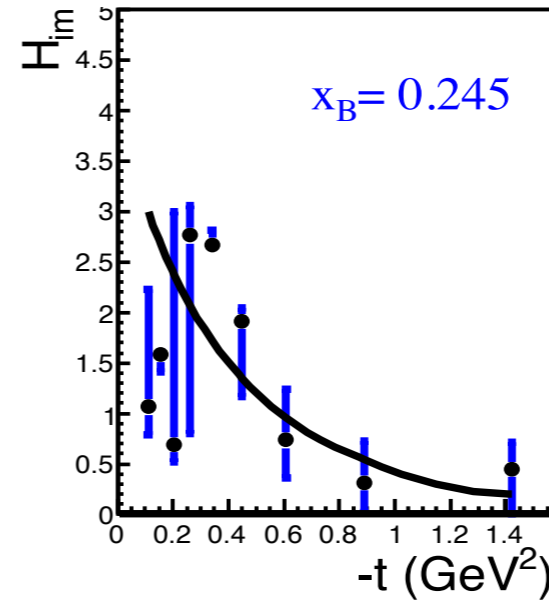
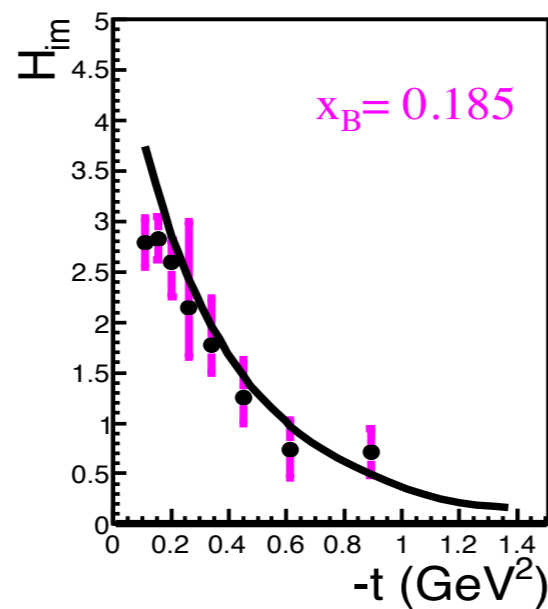
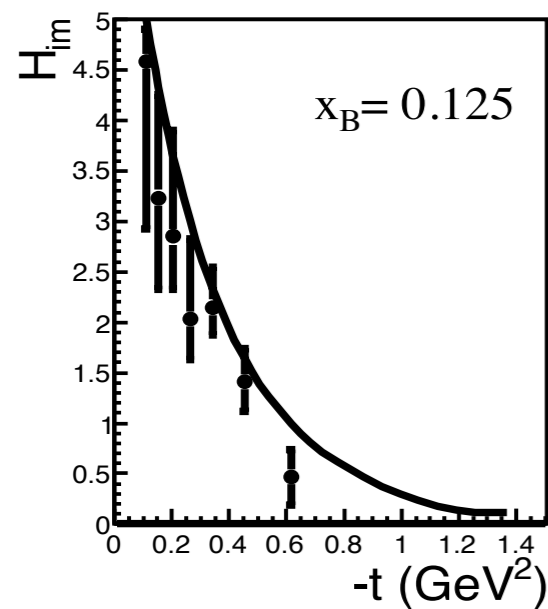


→ Extraction of the real part and the imaginary part of the GPD H

→ $\mathcal{H}_{Im} \mathcal{H}_{Re}$

Extraction of Compton Form Factors (CFFs)

Imaginary part of the CFF H for four values of x :



● Results of model-independent fit

— VGG model prediction

From CFFs to spatial densities

- \mathcal{H}_{Im} is a combination of GPDs at the line: $x = \pm\xi$

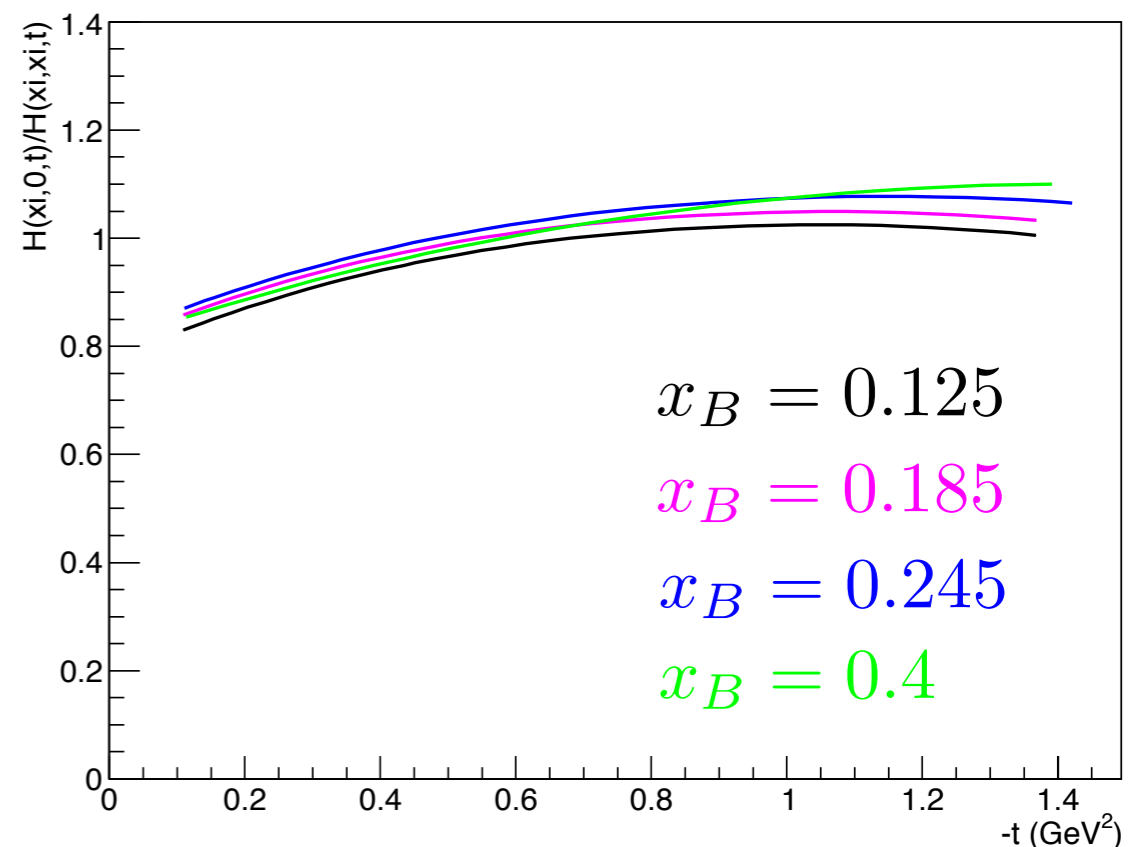
Neglecting the antiquark contribution $\rightarrow H_{Im}(\xi, t) = H(\xi, \xi, t)$

Density distribution: $\rho(x = \xi, b) = \int_0^\infty \frac{dt}{4\pi} J_0(b\sqrt{-t}) H(x = \xi, 0, t)$ M. Burkardt
Phys.Rev. D 62, 071503 (2000)

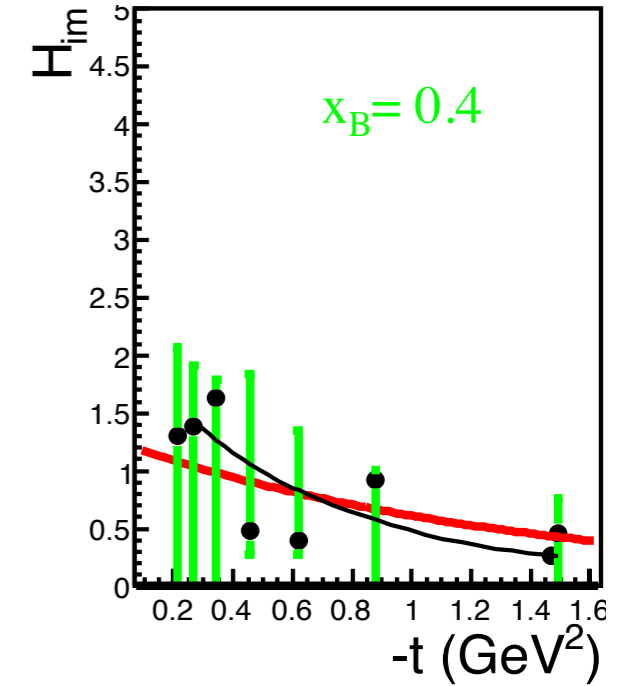
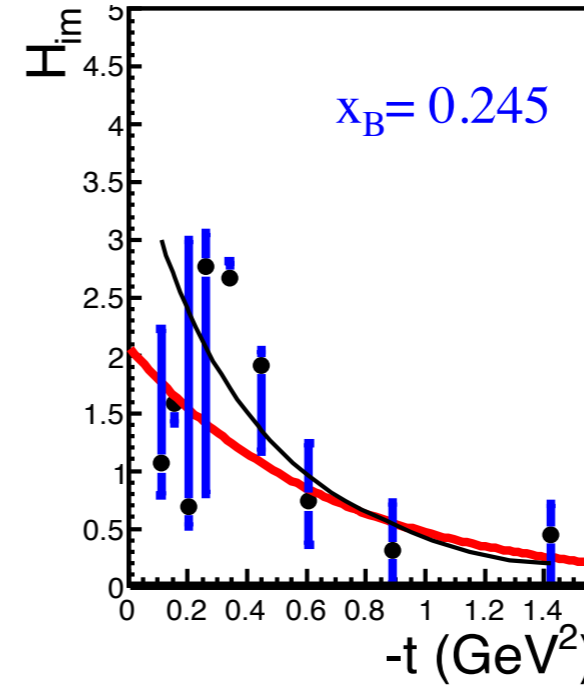
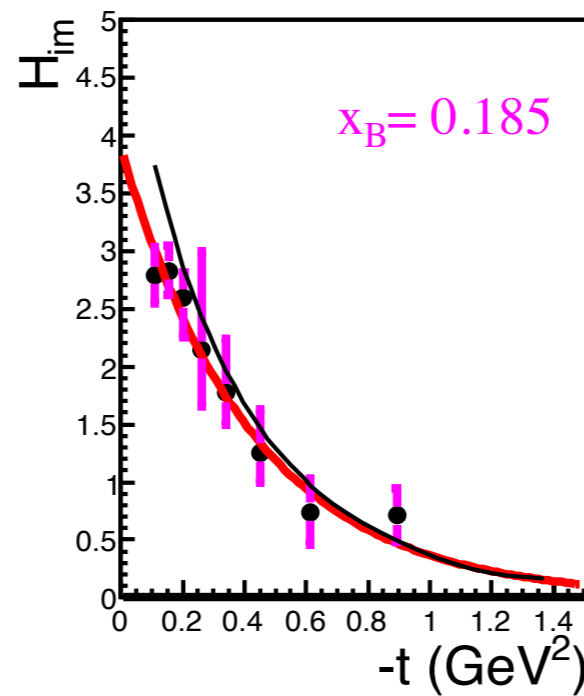
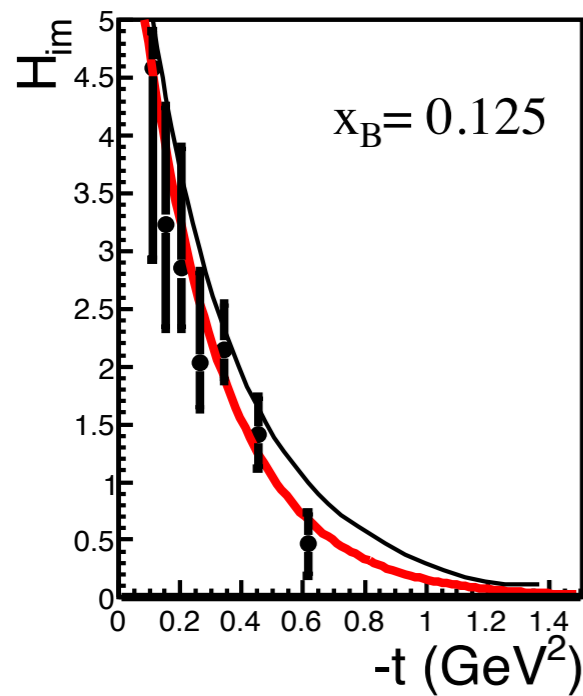
BUT: $H(\xi, 0, t) \neq H(\xi, \xi, t)$

Model dependent correction factors (VGG):

$$\rightarrow \frac{H(\xi, 0, t)}{H(\xi, \xi, t)} \quad \text{Effect is } < 20\%$$

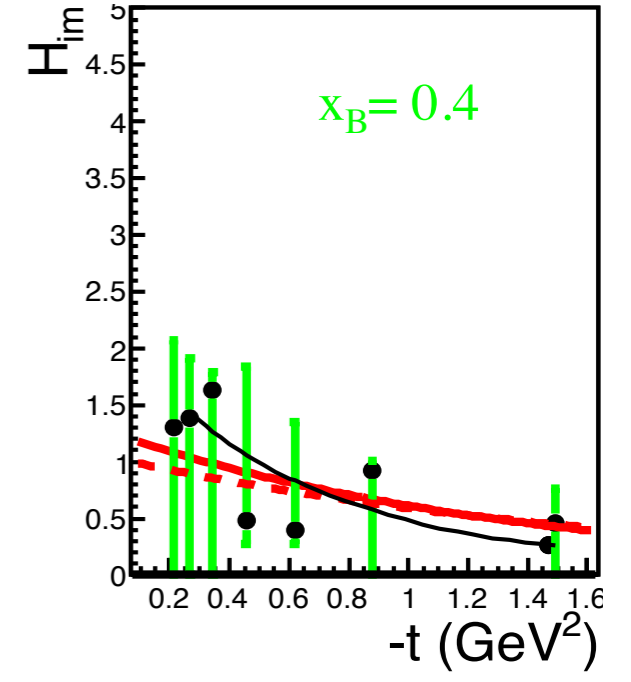
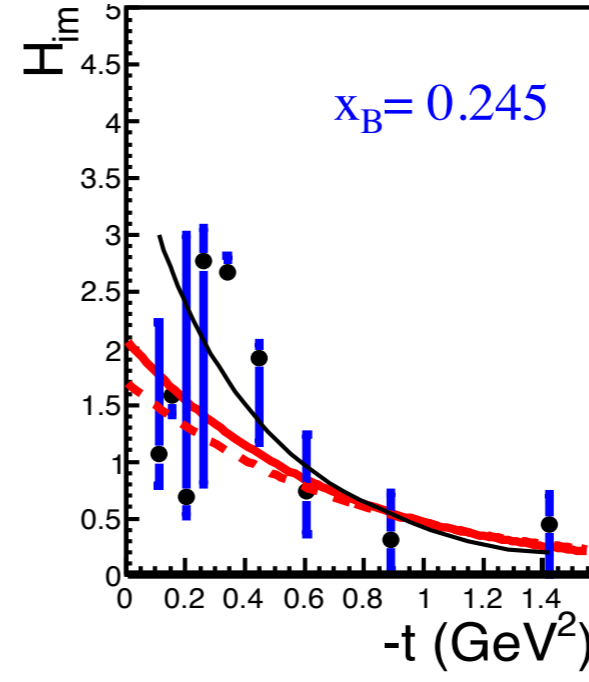
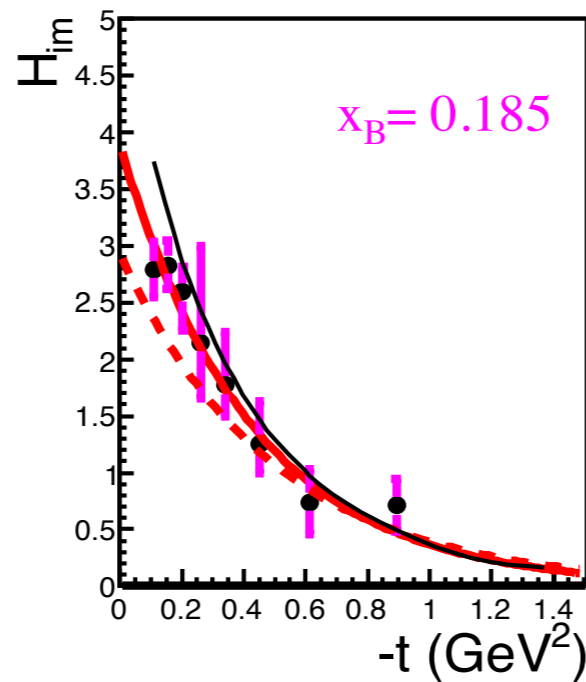
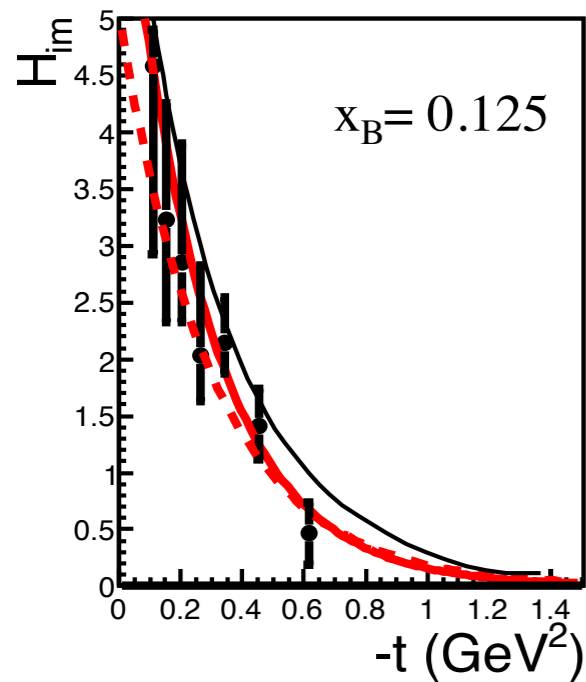


From CFFs to spatial densities



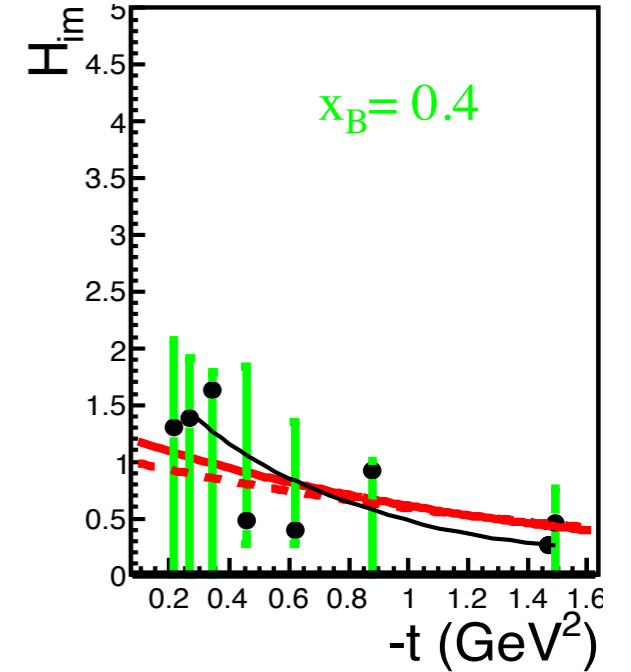
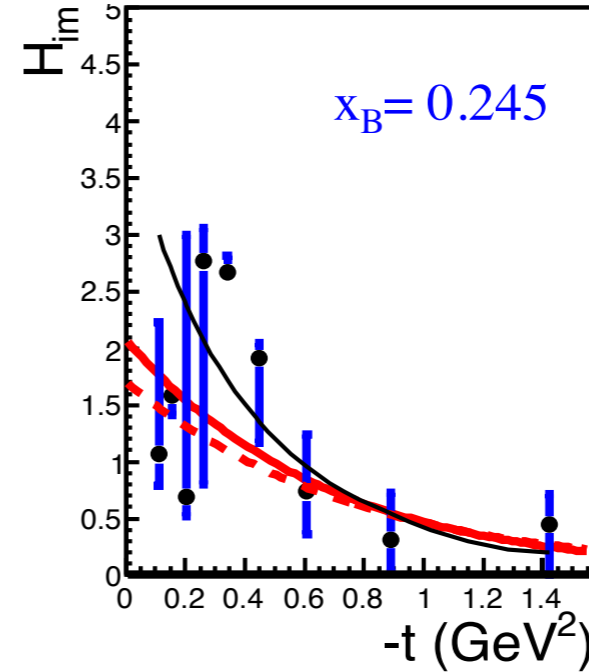
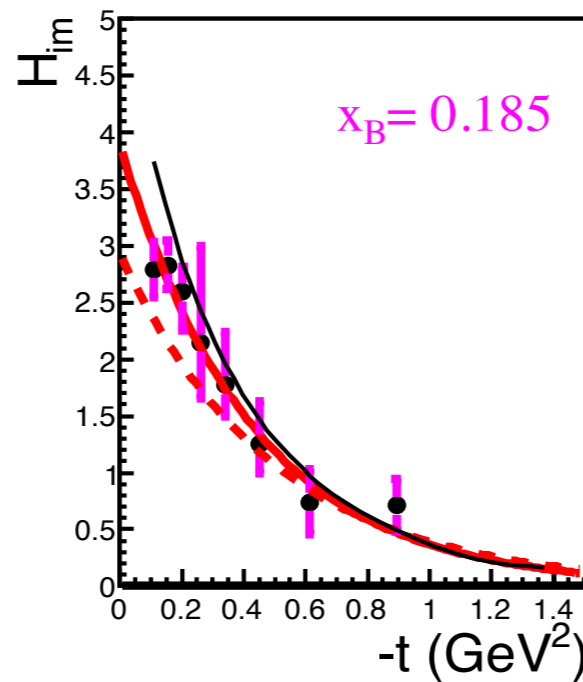
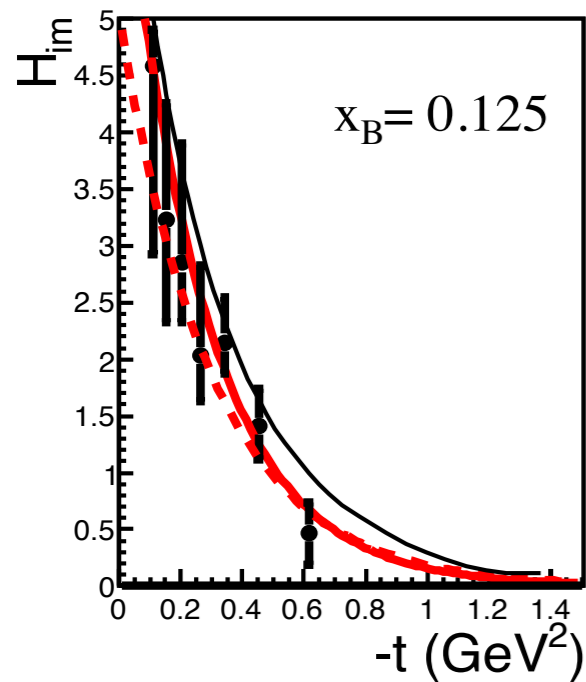
— Fit of the t -dependence of H_{Im} with: e^{a+bt} (uncorrected)

From CFFs to spatial densities

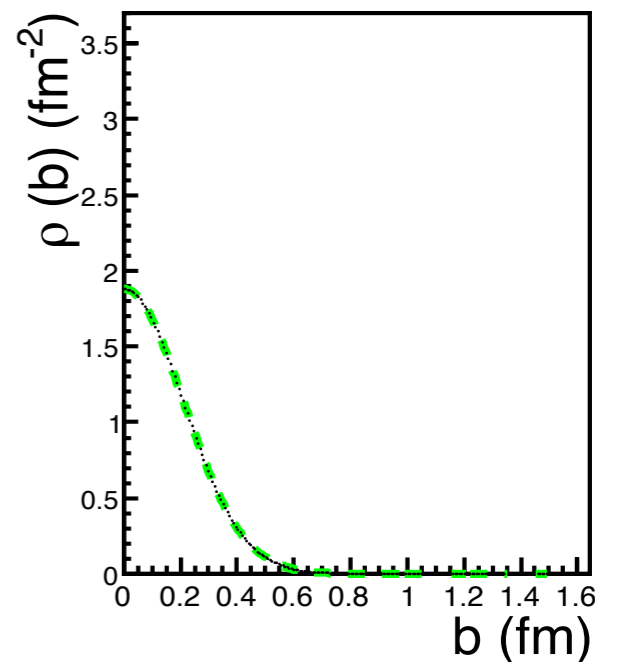
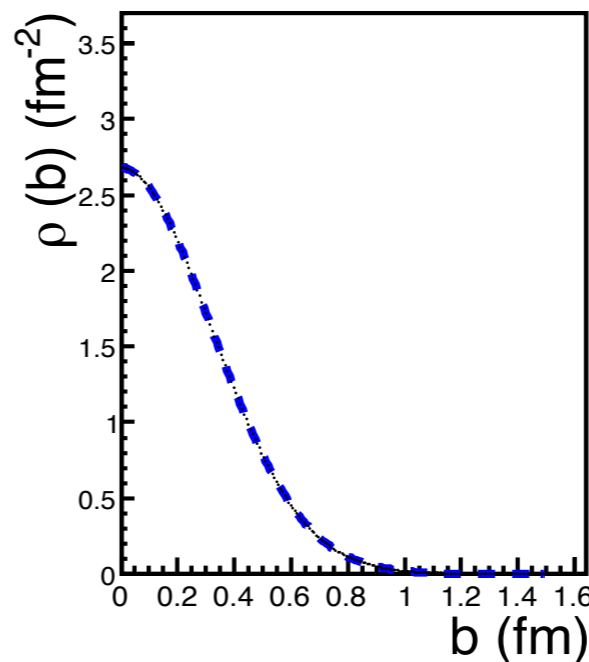
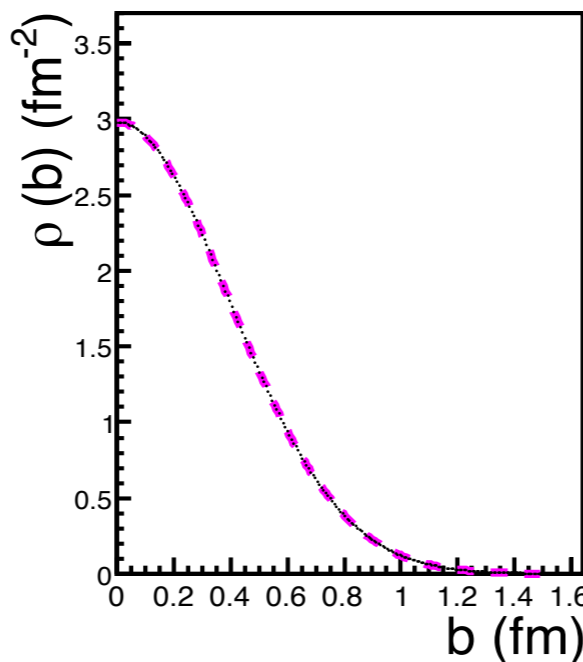
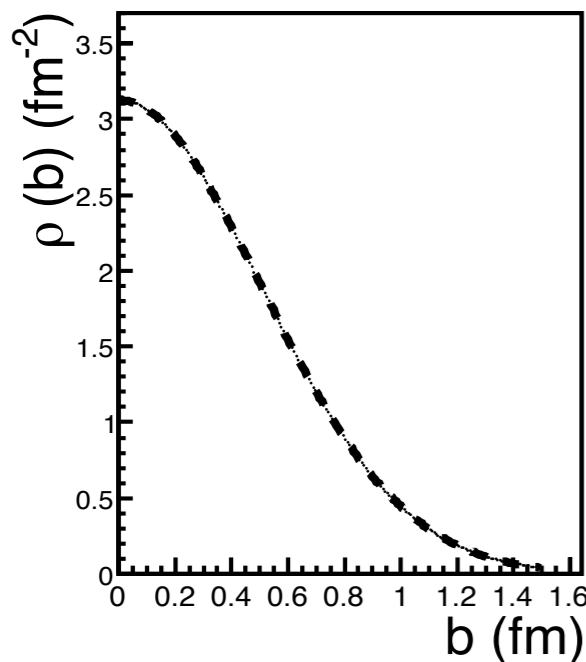


- Fit of the t -dependence of H_{Im} with: e^{a+bt} (uncorrected)
- - - Fit of the t -dependence of H_{Im} with: e^{a+bt} (corrected)

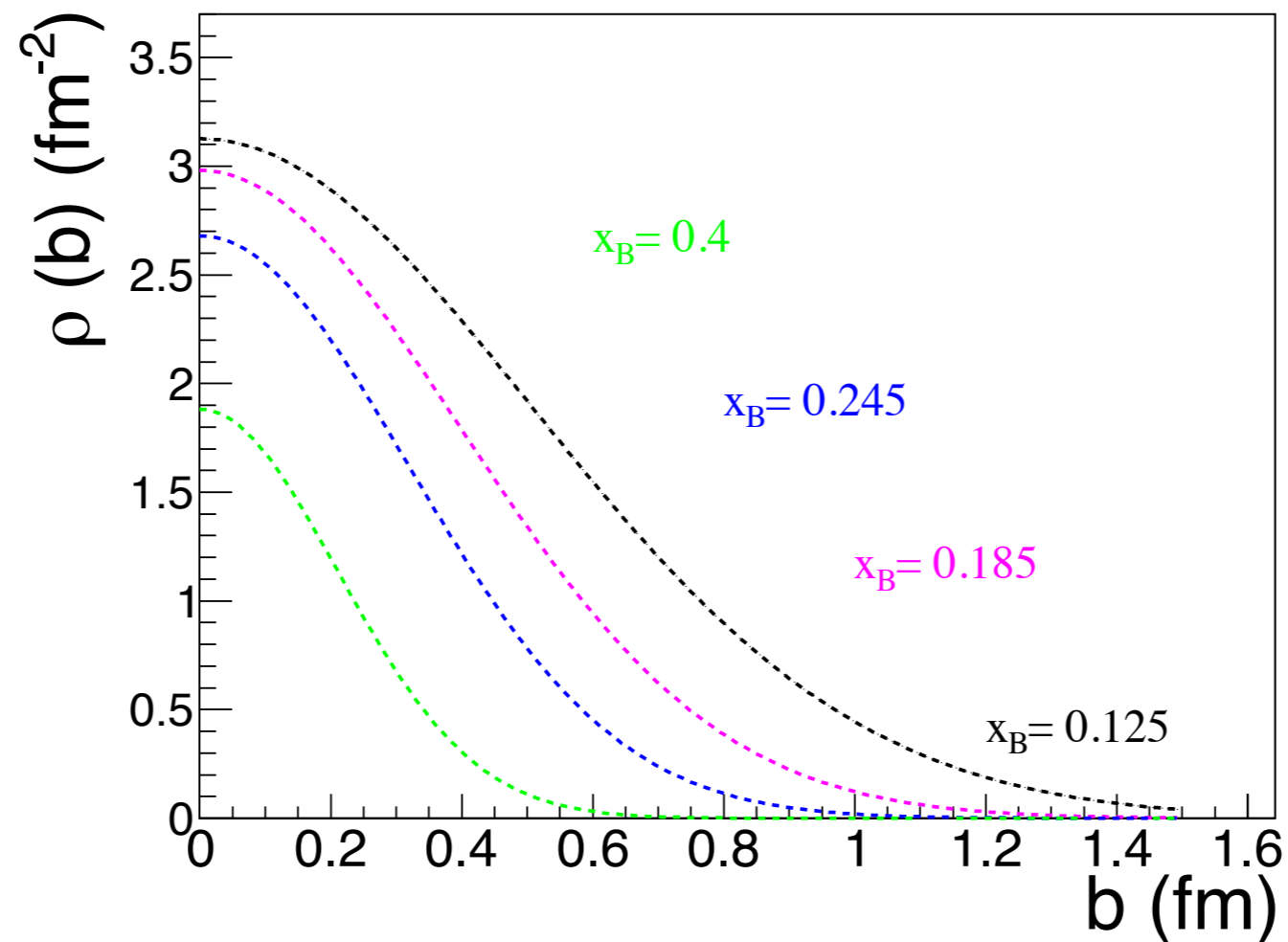
From CFFs to spatial densities



$$\rho(x = x_B, b) = \int_0^\infty \frac{dt}{4\pi} J_0(b\sqrt{t}) H(x = x_B, 0, t)$$



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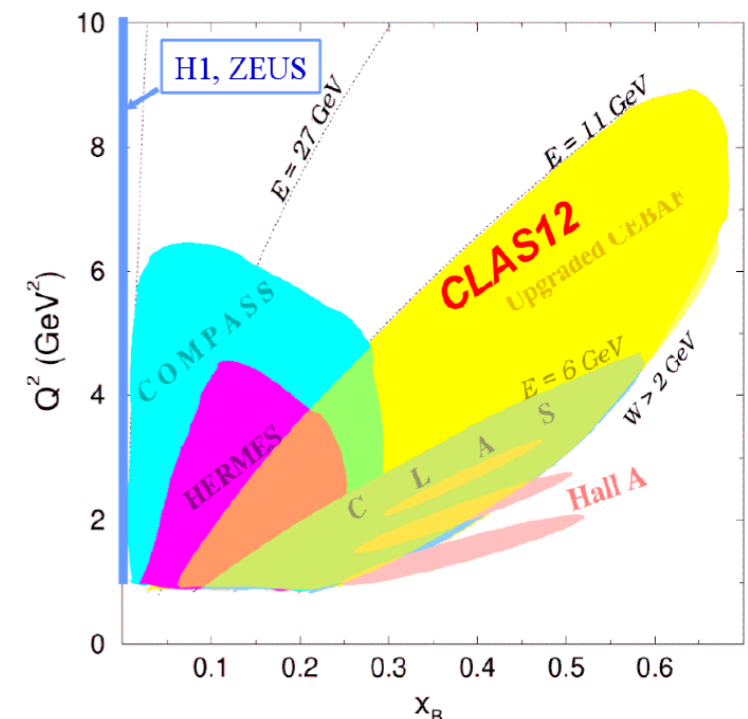


\mathcal{H}_{Im} : Correlation between transverse position and longitudinal momentum

- ➔ The sea quarks (low x) spread to the periphery of the nucleon
- ➔ The valence quarks (large x) remain in the center

Summary and outlook

- GPDs are a unique tool to explore the internal landscape of the nucleon:
→ 3D quark/gluon imaging of the nucleon
- Extraction of DVCS unpolarized and polarized cross sections in the largest kinematic domain ever explored in the valence region
- Extraction of the spatial densities as a function of x
- Analyses in the final stage to extract A_{UL} and $A_{LL}(H, \tilde{H})$ from CLAS data at 6 GeV with longitudinally-polarized target
- Dedicated GPD program at Jlab 12GeV:
Target spin asymmetry: A_{UT} , A_{LT}
Beam/Target spin asymmetries: A_{UL} , A_{LU}
DVMP: pseudoscalar/vector mesons



$$\mathcal{T}^{DVCS} \propto \int_{-1}^1 dx \frac{f(x, \xi, t)}{x \pm \xi \mp i\epsilon} = \mathcal{P} \int_{-1}^1 dx \frac{f(x, \xi, t)}{x \pm \xi} \pm i\pi f(x = \mp \xi, \xi, t)$$

Real part	Imaginary part
$\mathcal{H}_{Re}(\xi, t) = \mathcal{P} \int_0^1 dx [H(x, \xi, t) - H(-x, \xi, t)] C^+(x, \xi)$	$\mathcal{H}_{Im}(\xi, t) = H(\xi, \xi, t) - H(-\xi, \xi, t)$
$\mathcal{E}_{Re}(\xi, t) = \mathcal{P} \int_0^1 dx [E(x, \xi, t) - E(-x, \xi, t)] C^+(x, \xi)$	$\mathcal{E}_{Im}(\xi, t) = E(\xi, \xi, t) - E(-\xi, \xi, t)$
$\tilde{\mathcal{H}}_{Re}(\xi, t) = \mathcal{P} \int_0^1 dx [\tilde{H}(x, \xi, t) + \tilde{H}(-x, \xi, t)] C^-(x, \xi)$	$\tilde{\mathcal{H}}_{Im}(\xi, t) = \tilde{H}(\xi, \xi, t) + \tilde{H}(-\xi, \xi, t)$
$\tilde{\mathcal{E}}_{Re}(\xi, t) = \mathcal{P} \int_0^1 dx [\tilde{E}(x, \xi, t) + \tilde{E}(-x, \xi, t)] C^-(x, \xi)$	$\tilde{\mathcal{E}}_{Im}(\xi, t) = \tilde{E}(\xi, \xi, t) + \tilde{E}(-\xi, \xi, t)$

With: $C^\pm(x, \xi) = \frac{1}{x - \xi} \pm \frac{1}{x + \xi}$

	Sensitivity	Experiment
$\sigma_{unp} = \sigma^{\rightarrow} + \sigma^{\leftarrow}$	$\propto \mathcal{H}_{Re}$	H1 ((2001), (2005), (2008)) ZEUS ((2003) , (2009)) Hall-A (2006) Hall-B (E1-DVCS experiment: data under analysis)
$\sigma_{pol} = \sigma^{\rightarrow} - \sigma^{\leftarrow}$	$\propto \mathcal{H}_{Im}$	Hall-A (2006) Hall-B (E1-DVCS experiment: data under analysis)
\mathcal{A}_C	$\propto \mathcal{H}_{Re}$	HERMES ((2007) ; (2008) ; (2009))
\mathcal{A}_{LU}	$\propto \mathcal{H}_{Im}$	HERMES ((2001) ; (2009)) Hall-B ((2001) , (2008))
\mathcal{A}_{UL}	$\propto \mathcal{H}_{Im}, \tilde{\mathcal{H}}_{Im}$	Hall-B (2006) HERMES (2010) Hall-B (Eg1-DVCS experiment: data under analysis)
\mathcal{A}_{LL}	$\propto \mathcal{H}_{Re}, \tilde{\mathcal{H}}_{Re}$	HERMES (2010) Hall-B (Eg1-DVCS experiment: data under analysis)
\mathcal{A}_{UT}	$\propto \mathcal{E}_{Im}$	HERMES (2008) Hall-B proposal
\mathcal{A}_{LT}	$\propto \mathcal{H}_{Re}, \mathcal{E}_{Re}$	HERMES (2011) Hall-B proposal

- The second moment of (E+H) when $t \rightarrow 0$: total angular momentum

$$\int_{-1}^1 dx x [H^q(x, \xi, 0) + E^q(x, \xi, 0)] = 2 J_{quarks} \quad (\text{Ji sum rule})$$

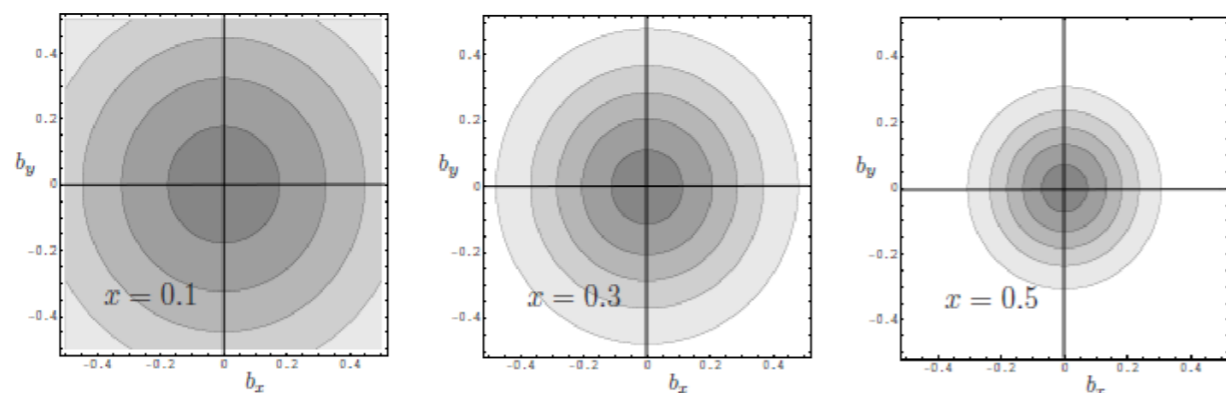
Nucleon spin decomposition: $\frac{1}{2} = J_{quarks} + J_{gluons} = S_{quarks} + L_{quarks} + S_{gluons} + L_{gluons}$

EMC: $\approx 30\%$

COMPASS, STAR, PHENIX: $\approx 0\%$

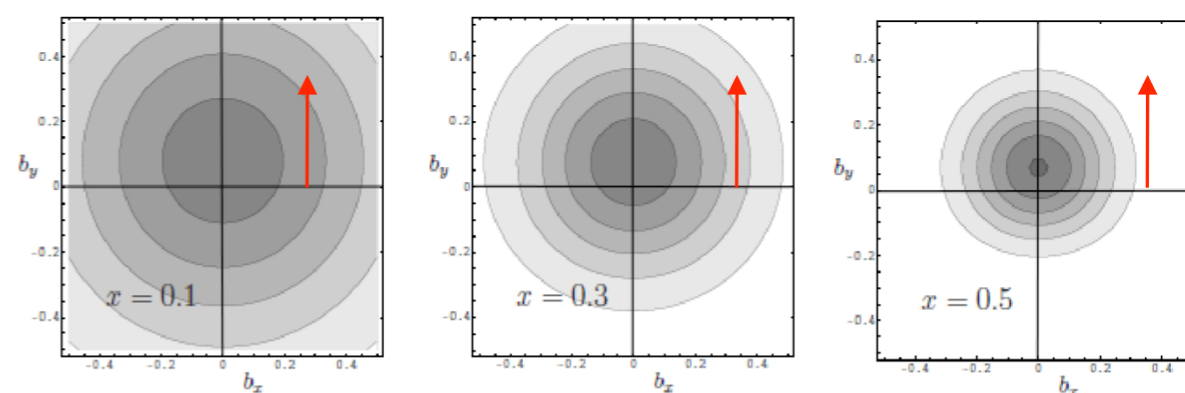
- At $\xi = 0$, a GPD is a x-decomposition of the form factor:

→ u-quark distribution in a unpolarized proton



$$q(x, 0, b_{\perp}) = \int \frac{d^2 \Delta_{\perp}}{(2\pi)^2} e^{i b_{\perp} \Delta_{\perp}} H^q(x, 0, -\Delta_{\perp}^2)$$

→ u-quark distribution in a polarized proton



$$q_{+X}(x, 0, b_{\perp}) = q(x, 0, b_{\perp}) - \frac{1}{2M} \frac{\partial}{\partial b_y} \int \frac{d^2 \Delta_{\perp}}{(2\pi)^2} e^{i b_{\perp} \Delta_{\perp}} E^q(x, 0, -\Delta_{\perp}^2)$$

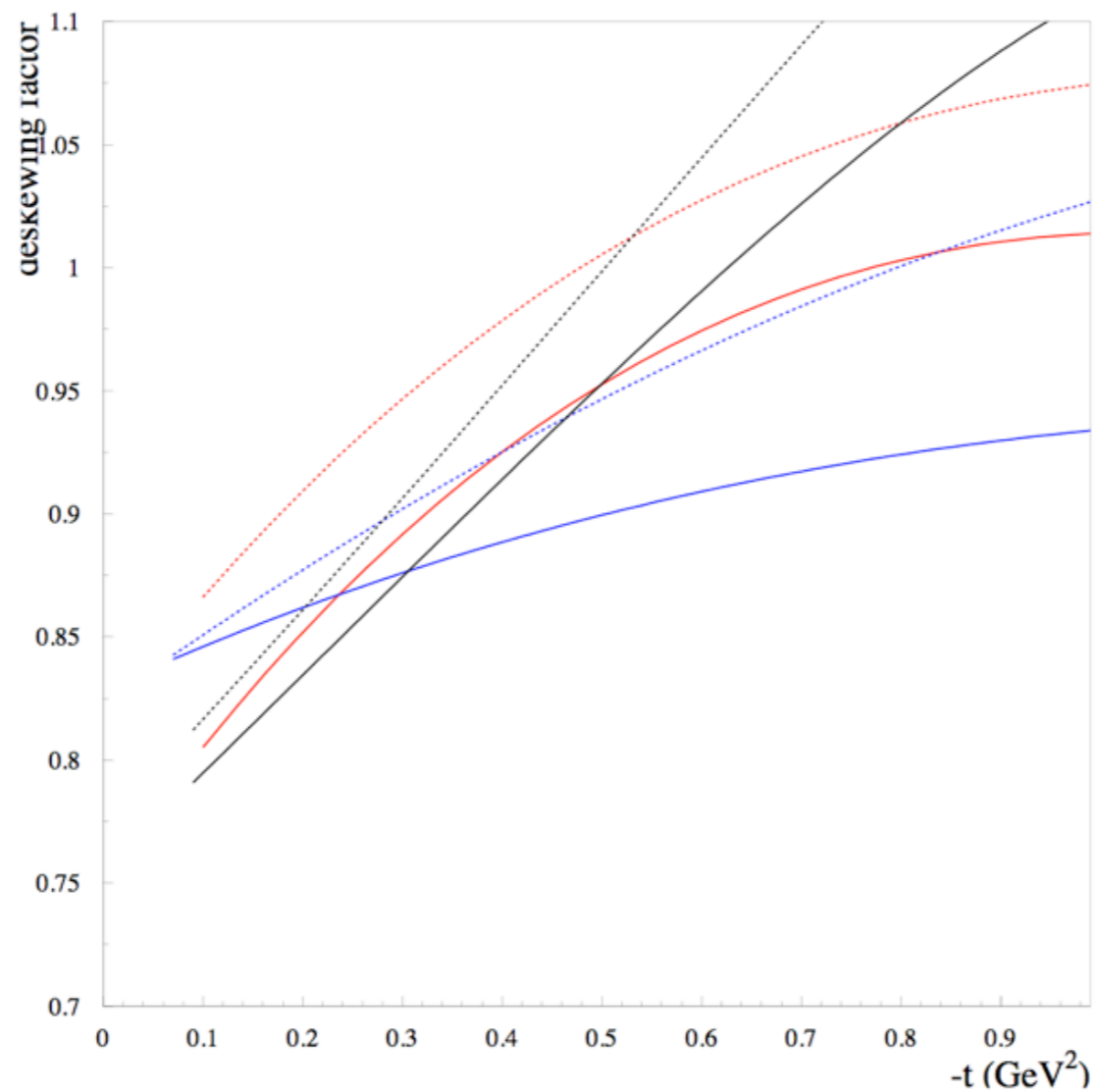


Figure 54. “Deskewing” factor $H(\xi, 0, t)/H(\xi, \xi, t)$ as a function of $-t$ for the VGG model (red curves), the GK model (blue curves) and the dual model (black curves). The solid curves correspond to $x_B=0.1$ (HERMES kinematics) and the dashed ones to $x_B=0.25$ (CLAS kinematics).