



# Precision Measurement of the W Boson Mass at CDF

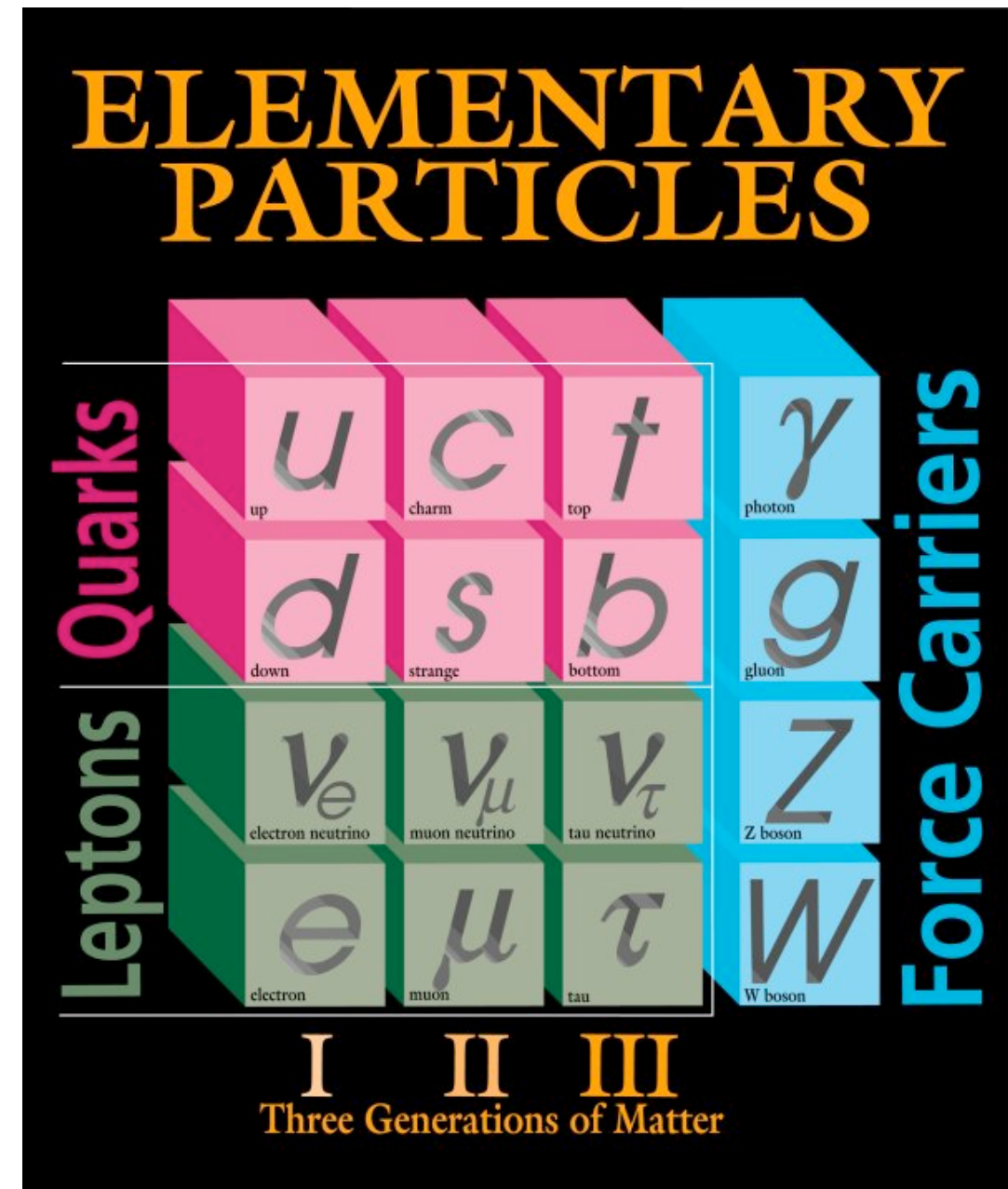
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*Duke University*

Séminaire de physique expérimentale  
LAPP Annecy

5 October 2012

# Motivation: a picture to start with

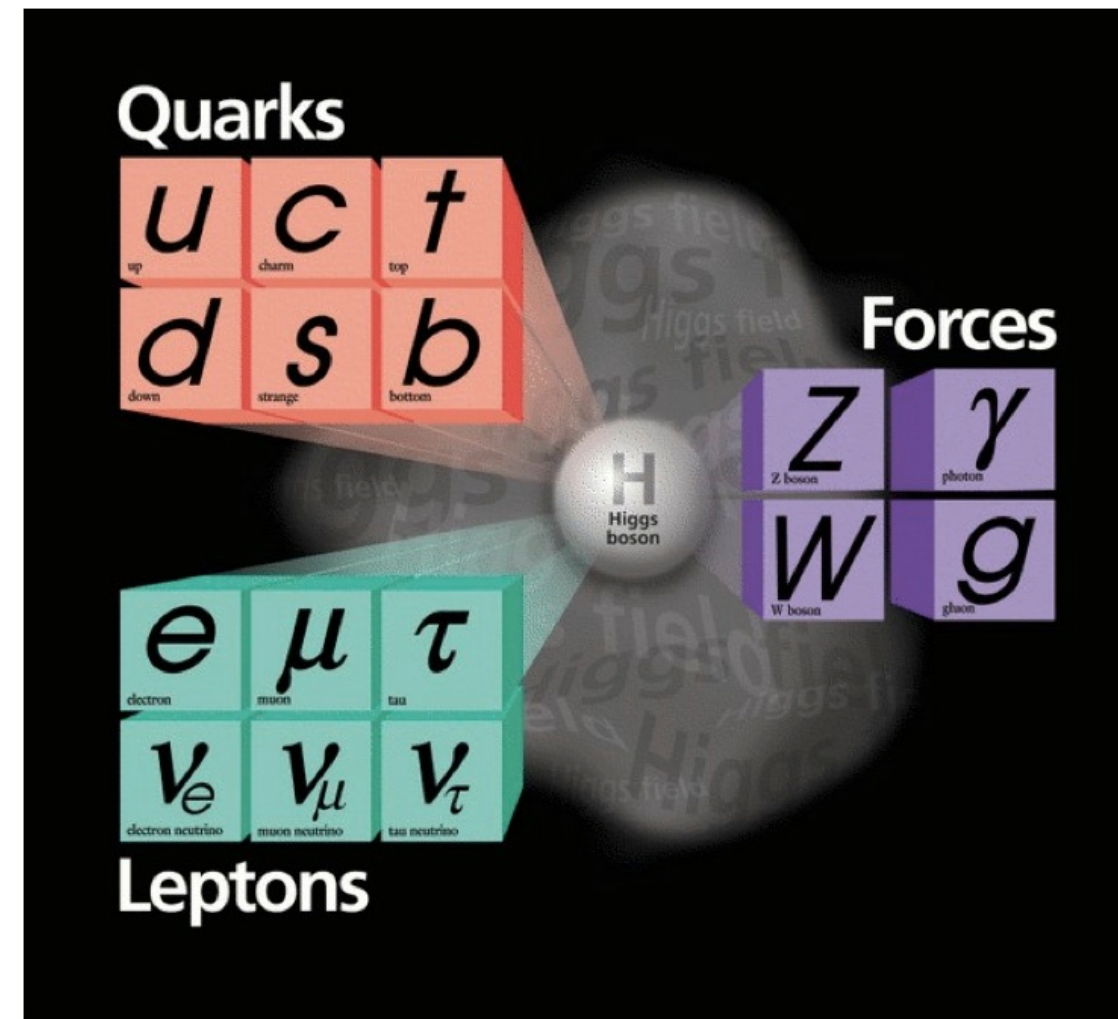
- The standard model
  - Describes known particles and interactions
  - Does not (verifiably) describe
    - Spontaneous symmetry breaking of  $U(1) \times SU(2)$
    - Fermion masses



Fermilab 95-759

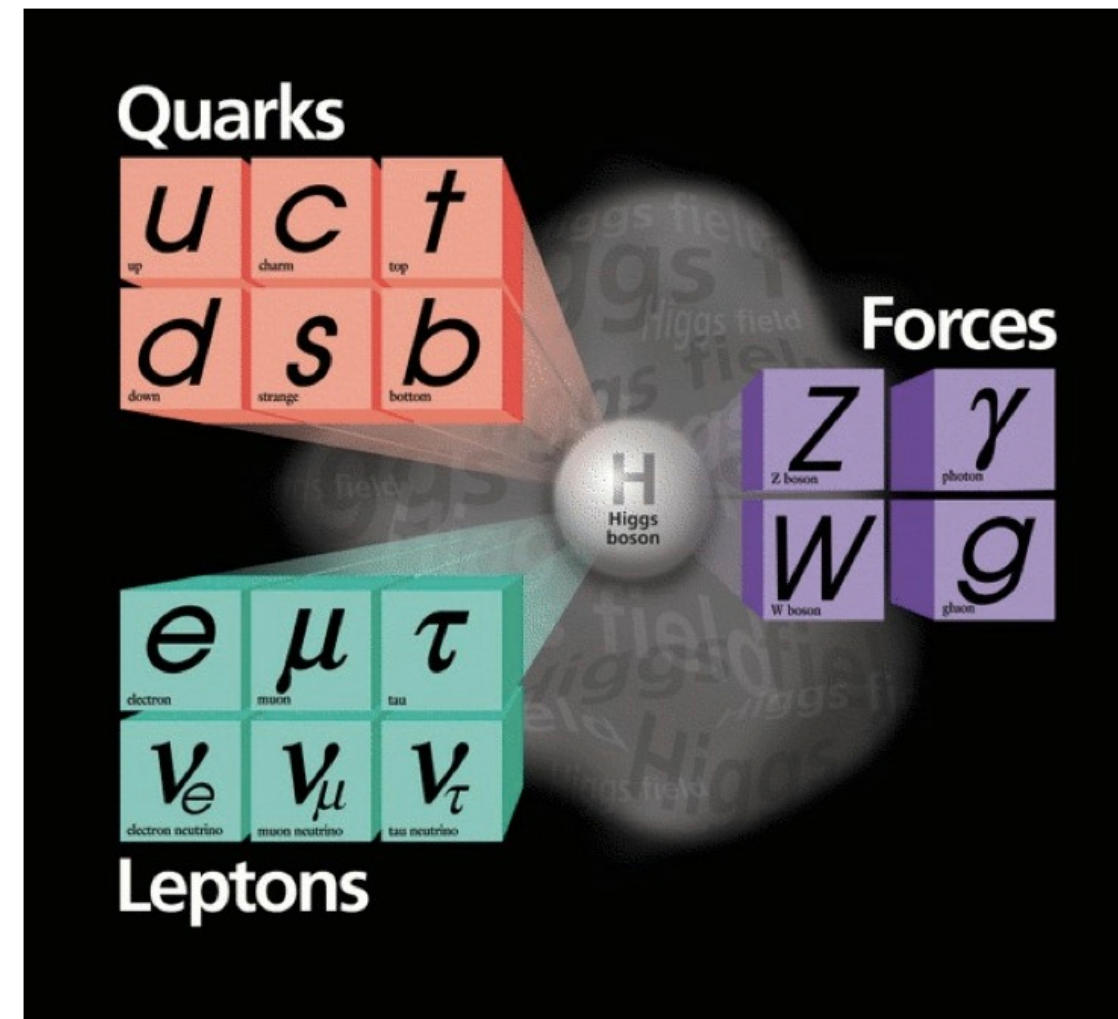
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    - Fermion masses
- Simple explanation: **Higgs mechanism**
  - Explains EWSB and fermion masses
  - Physical manifestation of Higgs boson



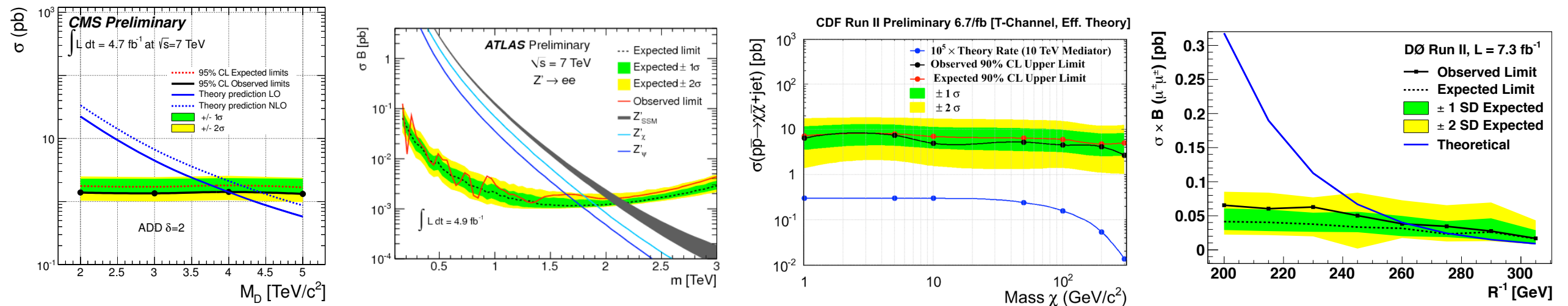
# Motivation: a picture to start with

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- Alternatively: ????

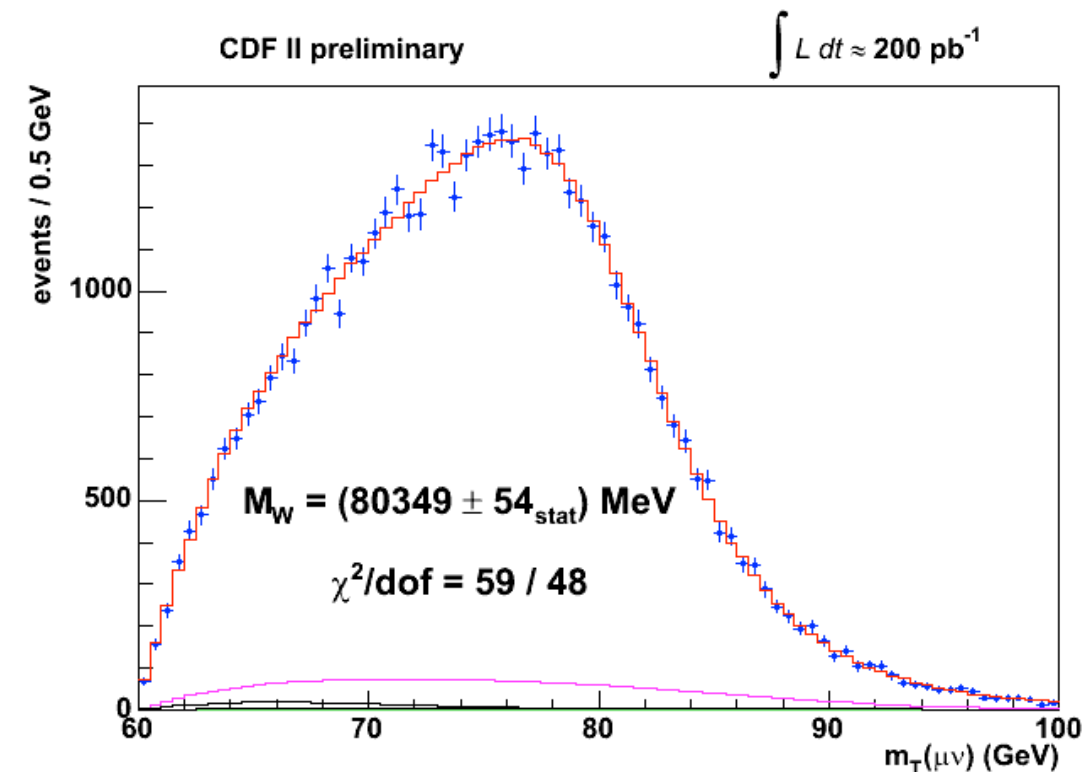
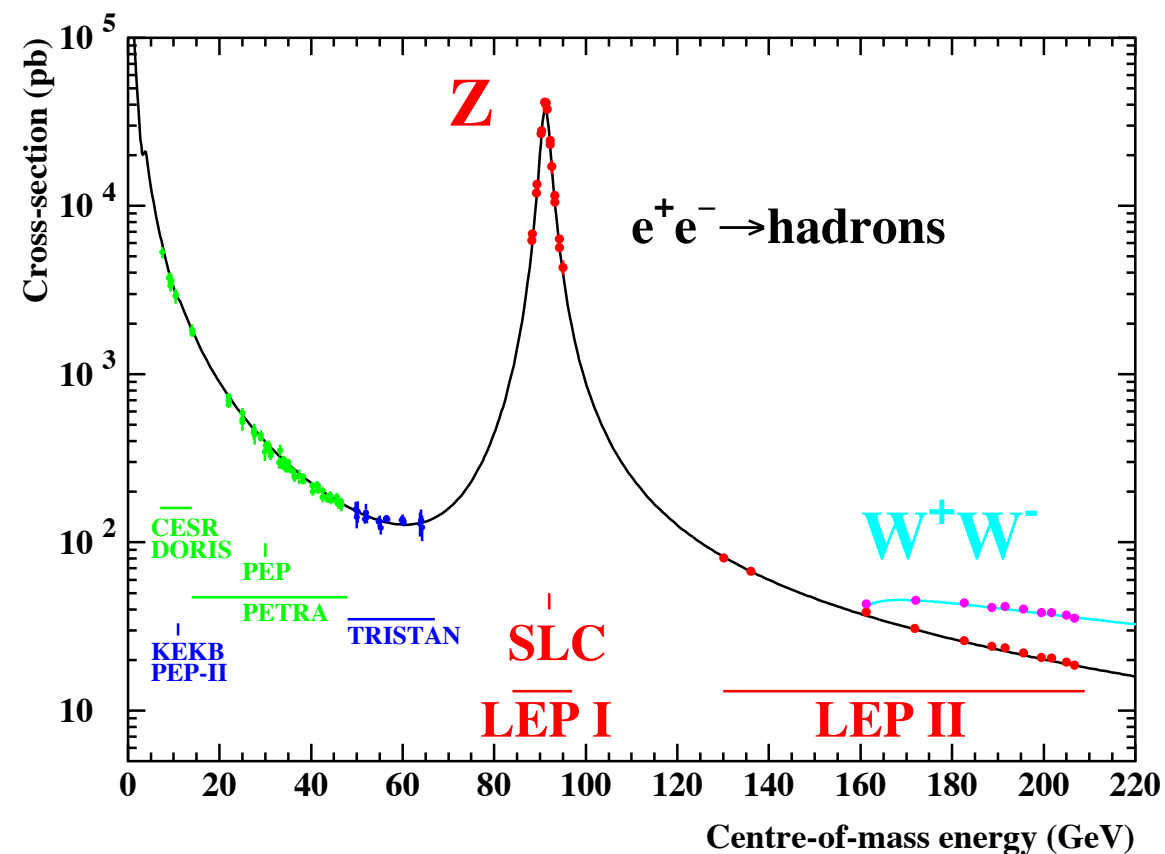


# Cracking/checking the picture with colliders

## 1. Direct searches. e.g.:



## 2. Precision measurements



# What the W mass tells us

- Electroweak sector of the standard model (SM) is constrained by

$$G_F = 1.16637(1) \times 10^{-5} \text{ GeV}^{-2} \quad \alpha_{EM}(Q^2 = M_Z^2) = 1/127.918(18)$$

$$m_Z = 91.1876(21) \text{ GeV}/c^2$$

- These inputs give a prediction of  $m_W$

$$m_W^2 = \frac{\pi \alpha_{em}}{\sqrt{2} G_F \sin^2 \theta_W (1 - \Delta r)} \quad \sin^2 \theta_W = 1 - \frac{m_W^2}{m_Z^2}$$

- Radiative corrections  $\Delta r$  dominated by top and Higgs loops

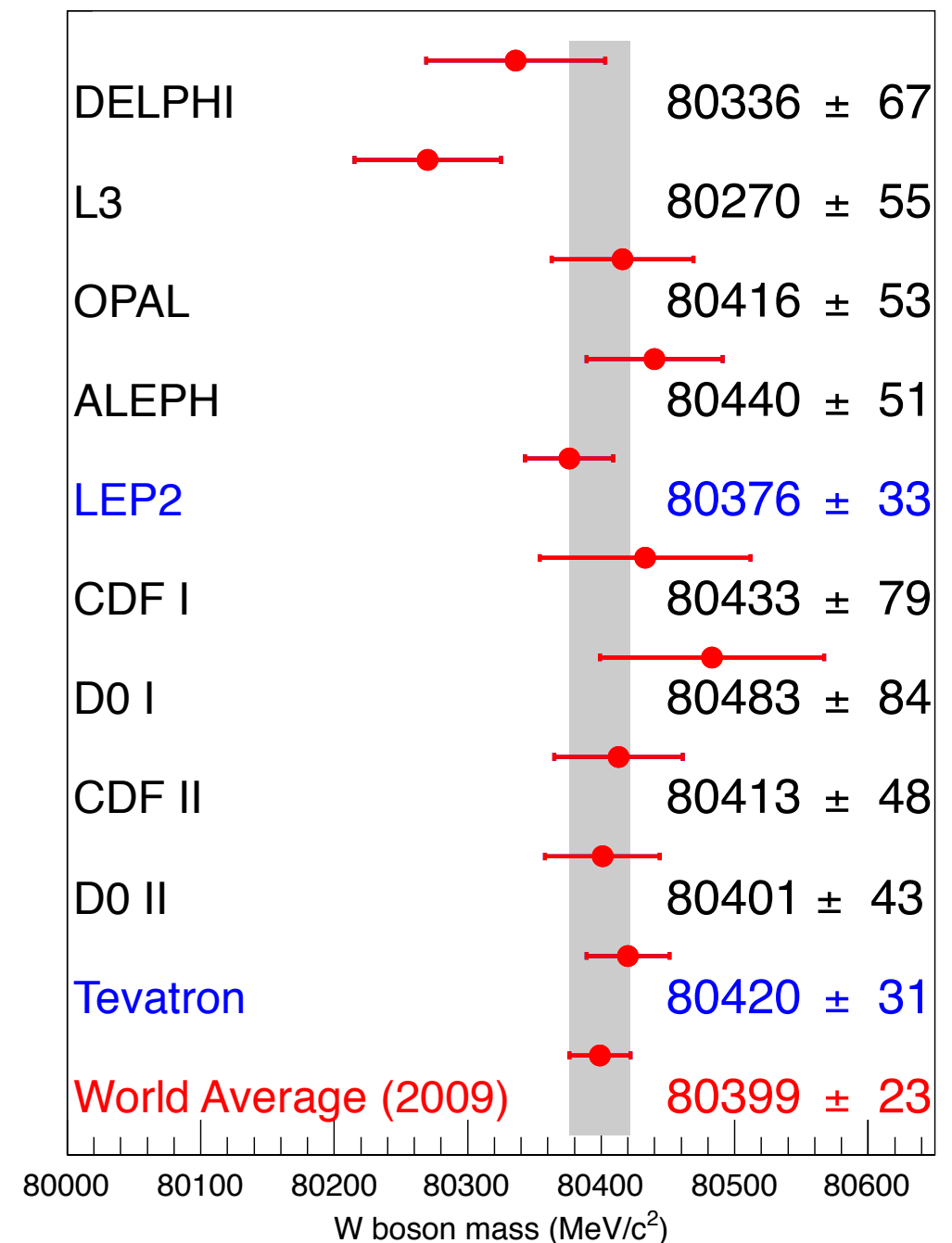


- Precision measurements of  $m_W$  and  $m_{top}$  constrain SM Higgs mass

*Where should the Higgs be?*

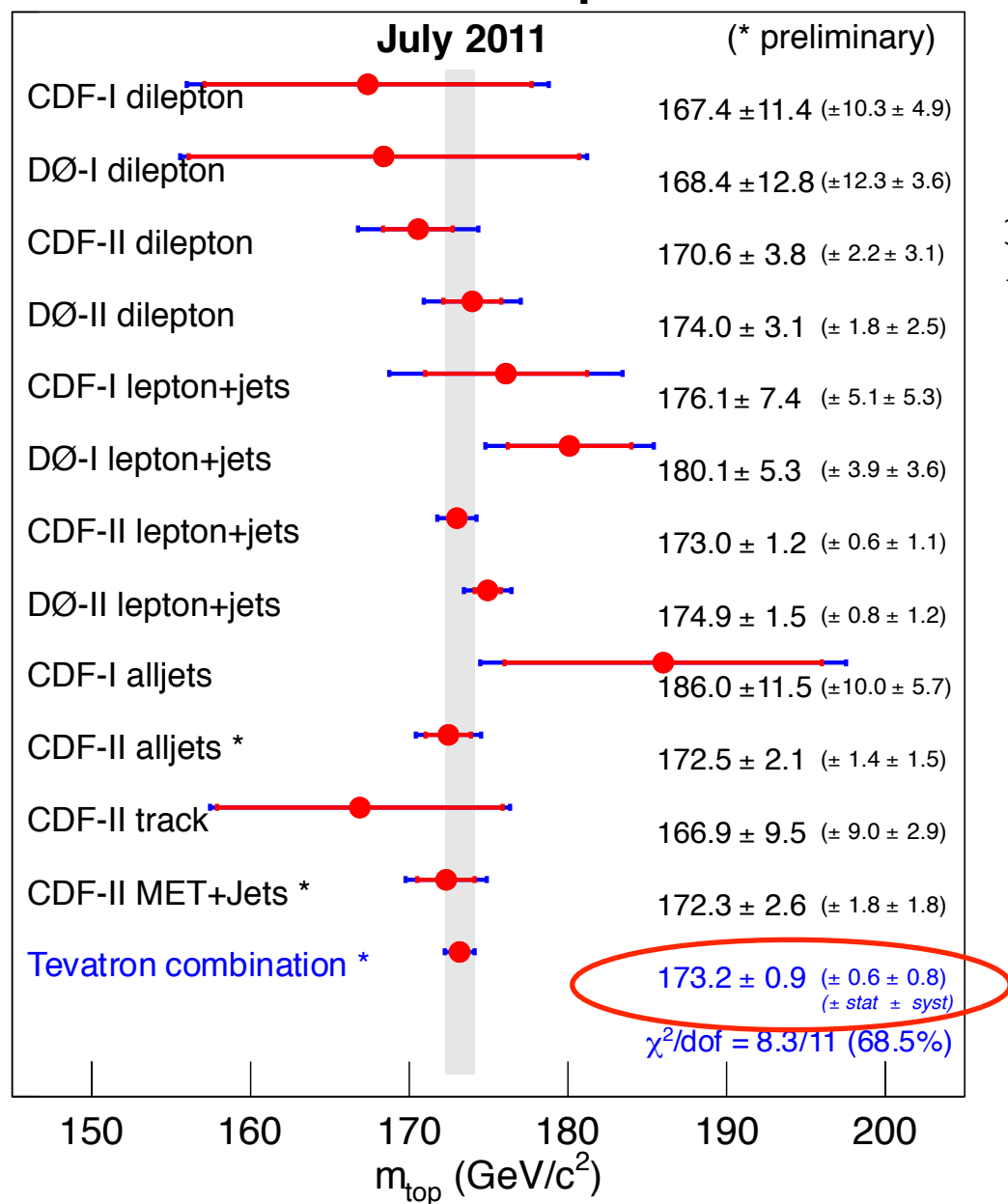
# Measurements of $M_W$

- State-of-the-art (Jan 2012)
  - DØ  $M_W=80401\pm43$  MeV [ $1\text{ fb}^{-1}$ , e]  
*PRL* **103**:141801 (2009)
  - CDF  $M_W=80413\pm48$  MeV [ $200\text{ pb}^{-1}$ ,  $e+\mu$ ]  
*PRL* **99**:151801 (2007)  
*PRD* **77**:112001 (2008)
  - Combining with LEP  $\Delta M_W = 23$  MeV
- *Achieved*: exceed precision of  $e^+e^-$  machine measurements with hadron collider
- *Goal*: match precision of all previous measurements with single CDF measurement

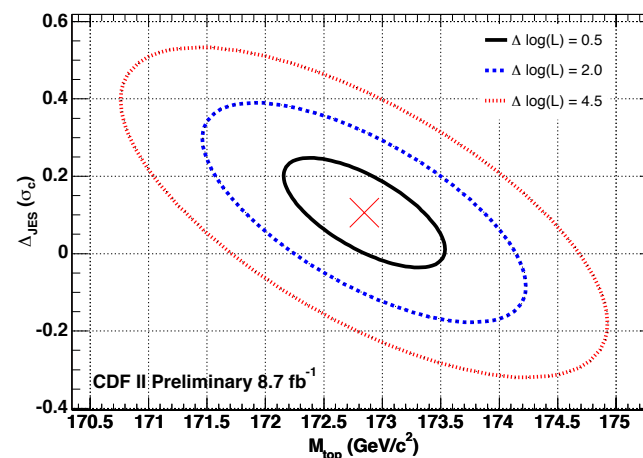


# The top quark mass

## Mass of the Top Quark

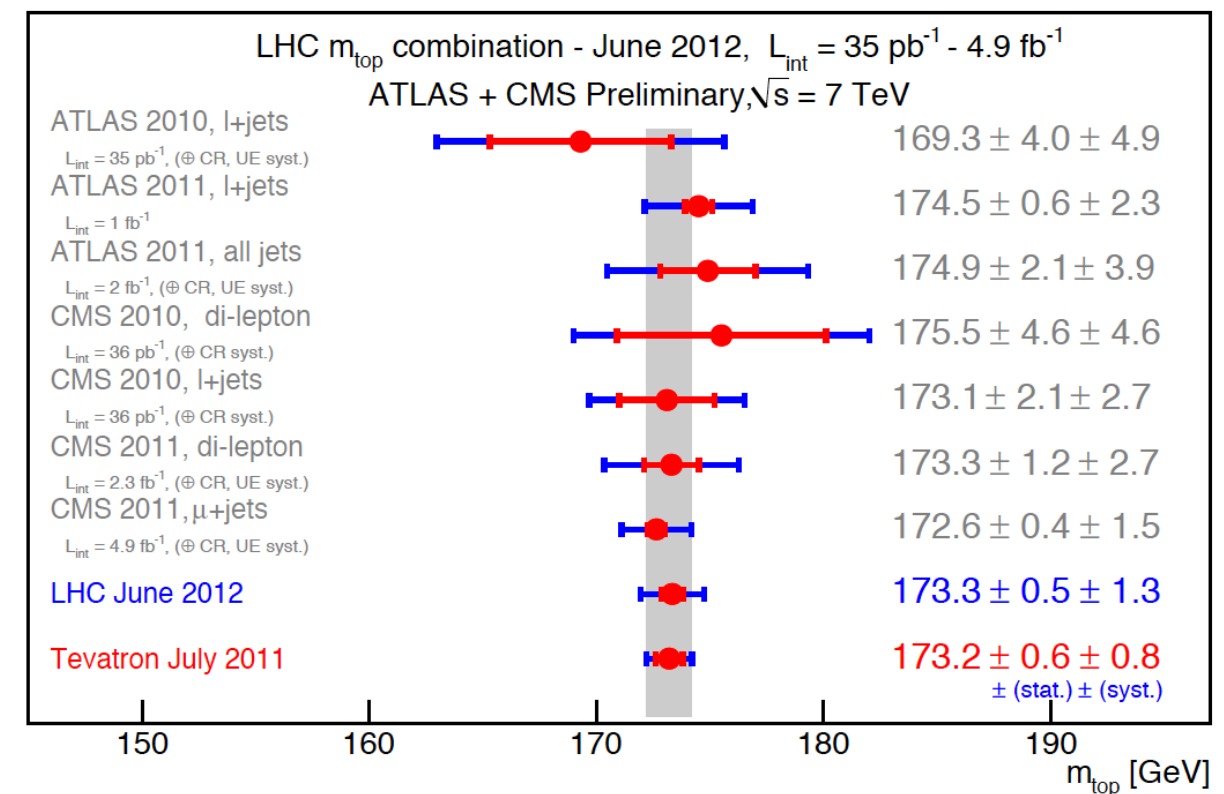


Combination **does not (yet) include**



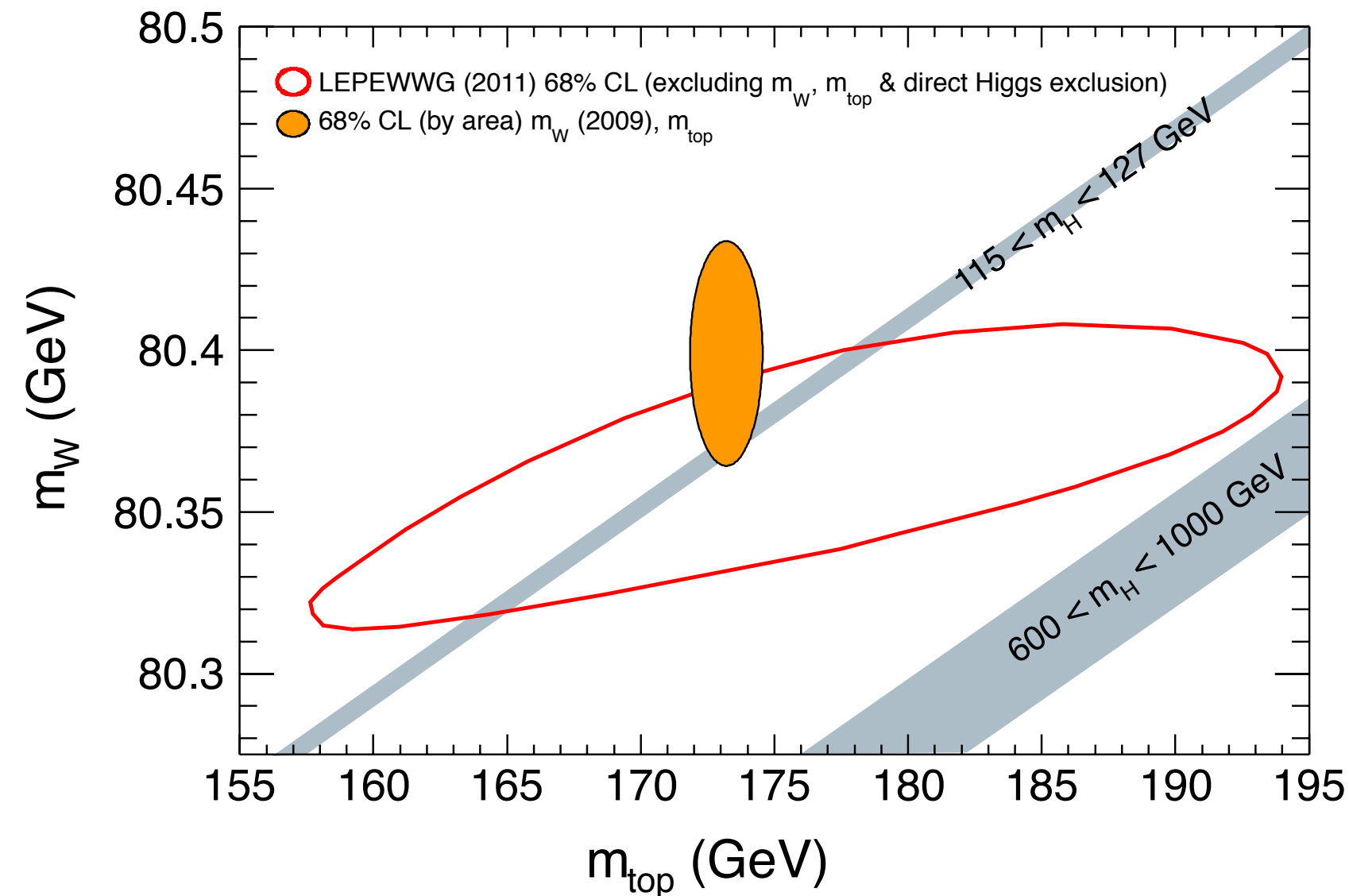
Single best measurement  
 $m_{\text{top}} = 172.8 \pm 1.1$  GeV [CDF]

## Impressive results from LHC



- $m_{\text{top}} = 173.2 \pm 0.9$  GeV
  - Equivalent to  $\Delta m_W = 6$  MeV on  $m_H$  fit
  - $m_W$  is limiting factor on  $m_H$  prediction!

# Putting it together

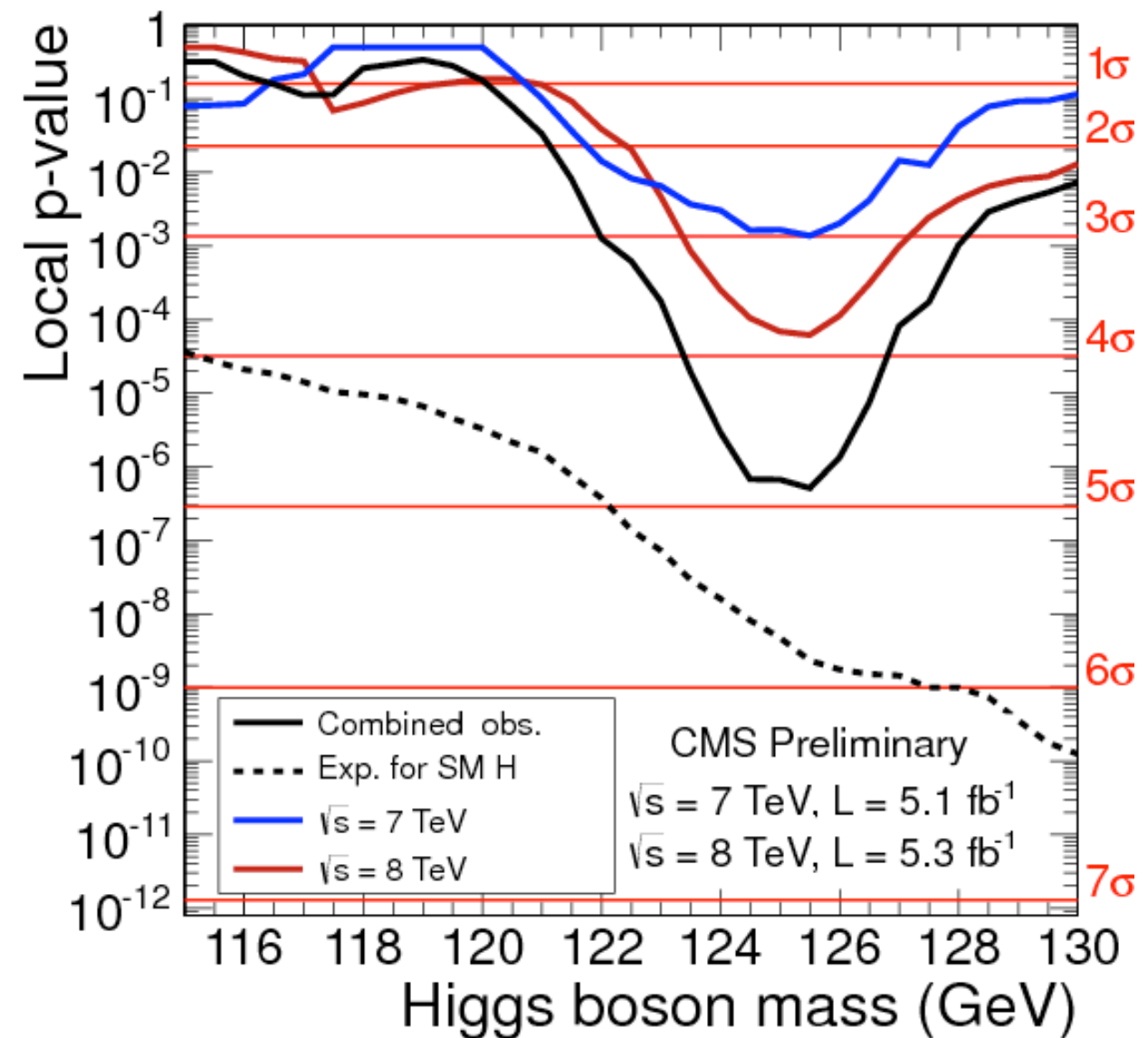
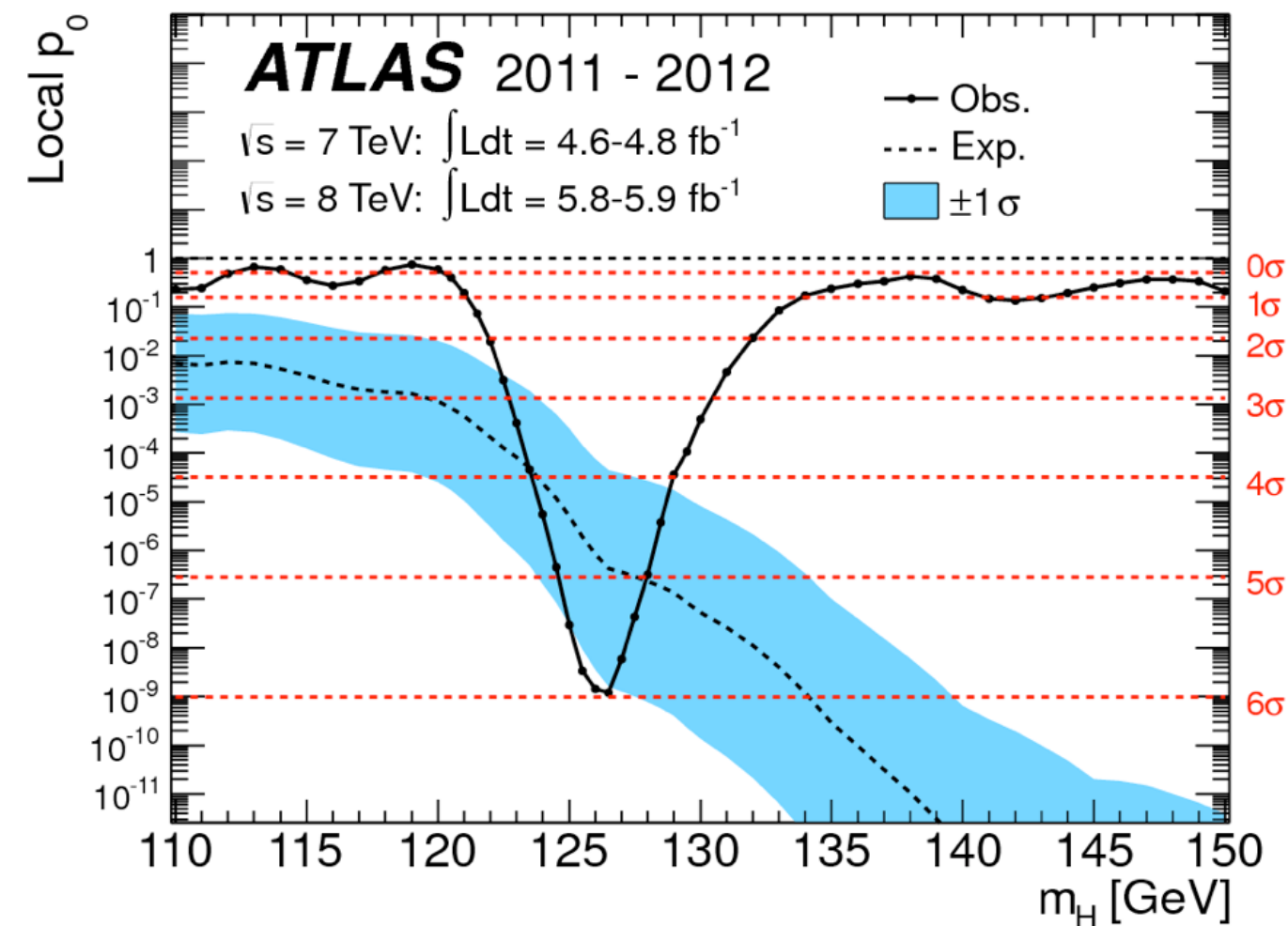


As of July 2011:

$$m_H = 92^{+34}_{-26} \text{ GeV}$$

$$m_H < 161 \text{ GeV @95\% CL}$$

# Since then...

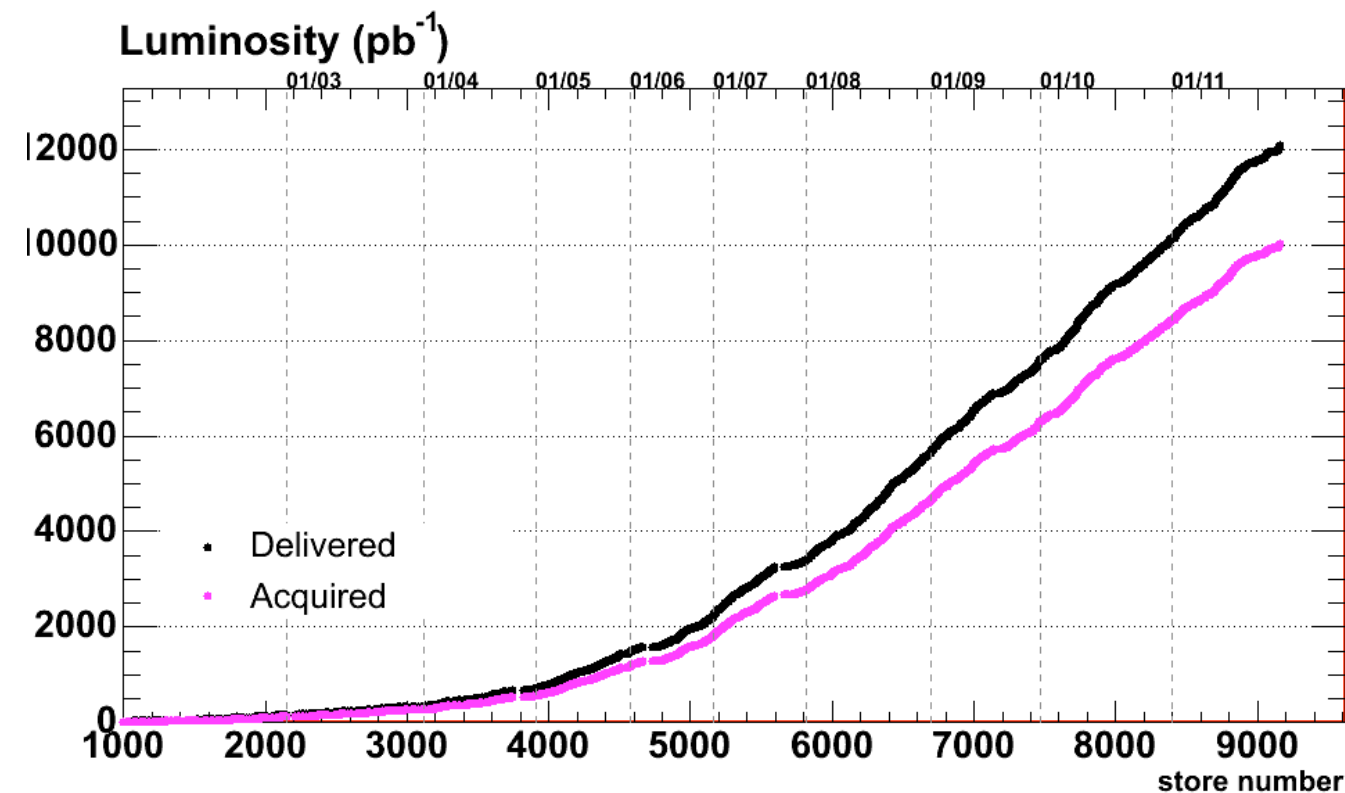


- ATLAS and CMS observe a boson with mass  **$\sim 125-126 \text{ GeV}$** 
  - CDF and DØ see evidence of a boson decaying to  $b\bar{b}$
- *Do precision measurements indicate a Higgs boson with this mass?*

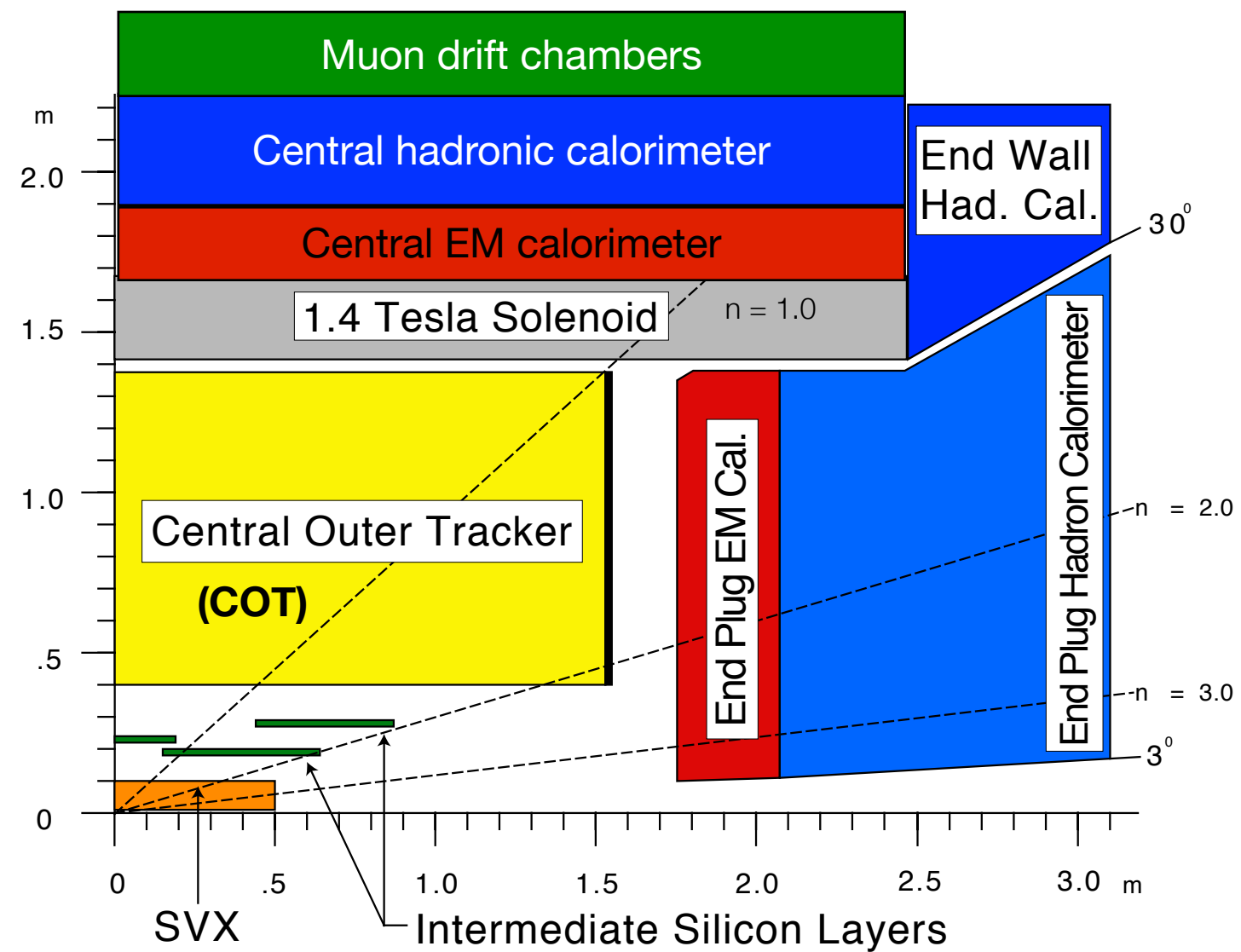
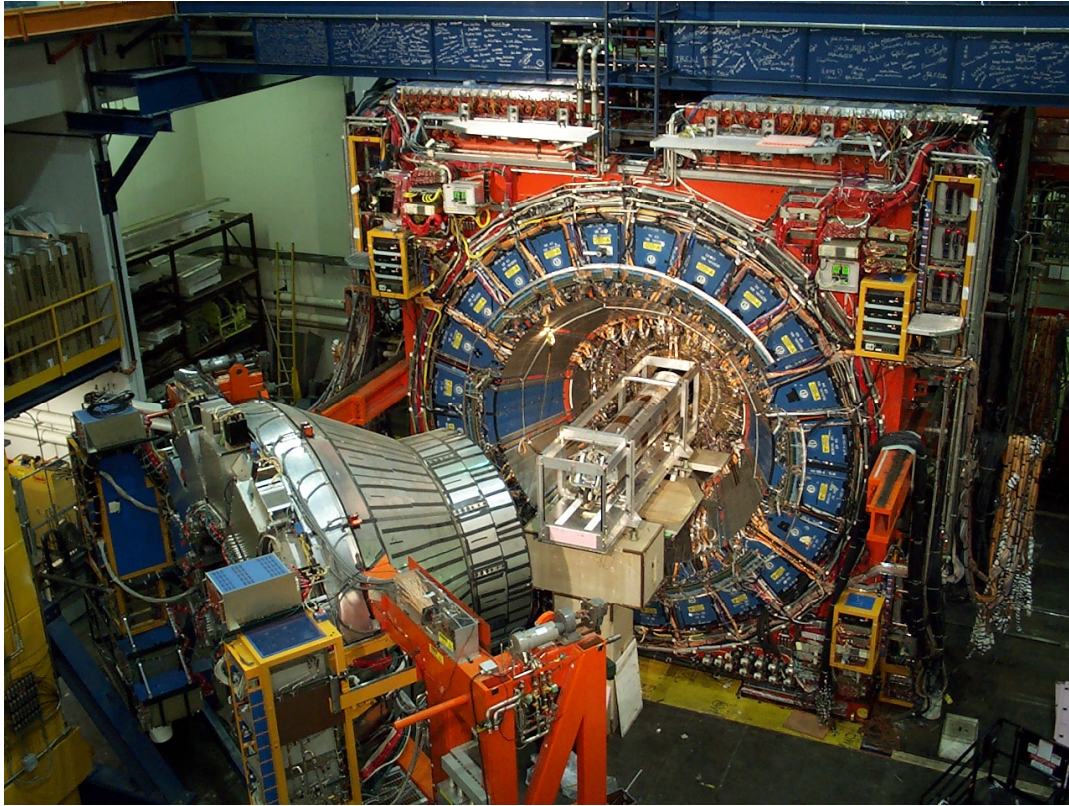
Analysis strategy

# The Tevatron at Fermilab

- 1.96 TeV pp $\bar{p}$  collider
  - Highest energy collider in the world
  - Typical inst. lumi.:  $3 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$ 
    - 2011 LHC:  $\sim 3 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$
  - Bunch spacing: 396 ns
    - 2011 LHC: 50 ns
- Ceased operations Sep 30, 2011
  - $\sim 12 \text{ fb}^{-1}$  delivered to CDF and DØ
- Analysis presented utilizes  $2.2 \text{ fb}^{-1}$

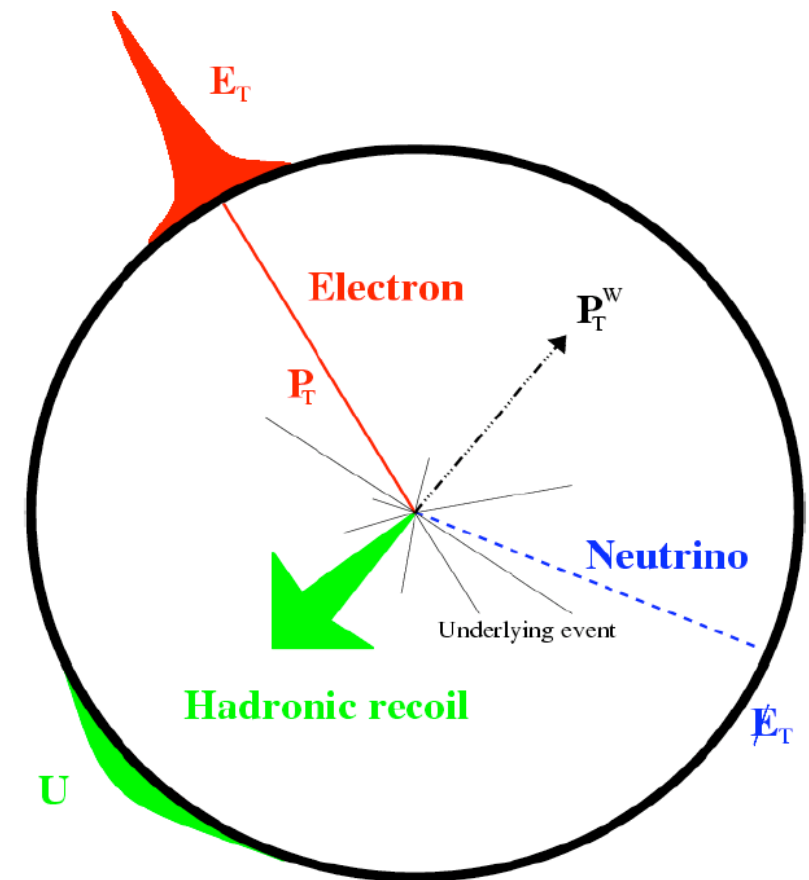


# CDF II (2001-2011)



# Precision?

- Start with **clean, low-background** events
  - *i.e.*, no taus, no hadronic decays
- **Lepton  $p_T$**  carries most information
  - Precision achieved:  $0.01\%$
- **Hadronic recoil** affects inference of **neutrino energy**
  - Calibrate to  $\sim 0.5\%$
  - Reduce impact by requiring  $p_T(W) \ll M_W$
- Need:
  - Accurate **theoretical model**
    - Including boson  $p_T$  model and QED radiation
  - Tunable **fast simulation**
    - Parameterized detector description for study of systematic effects
  - Large data samples of well-measured states
    - Various dimuon resonances
    - $Z$  boson



# Measurement strategy (broadly speaking)

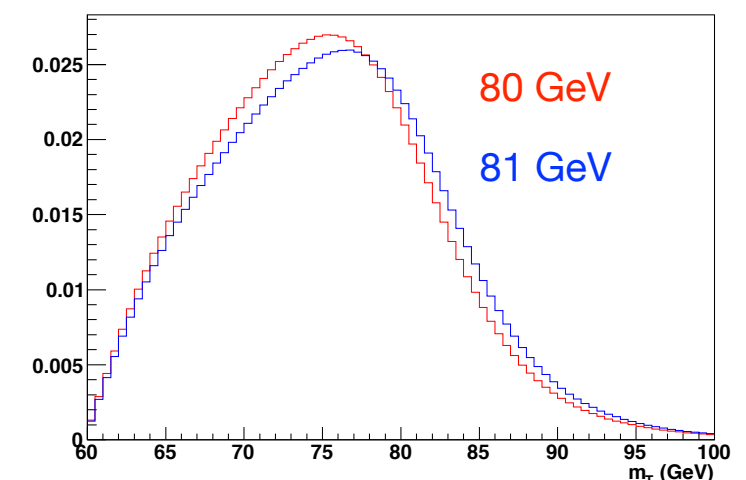
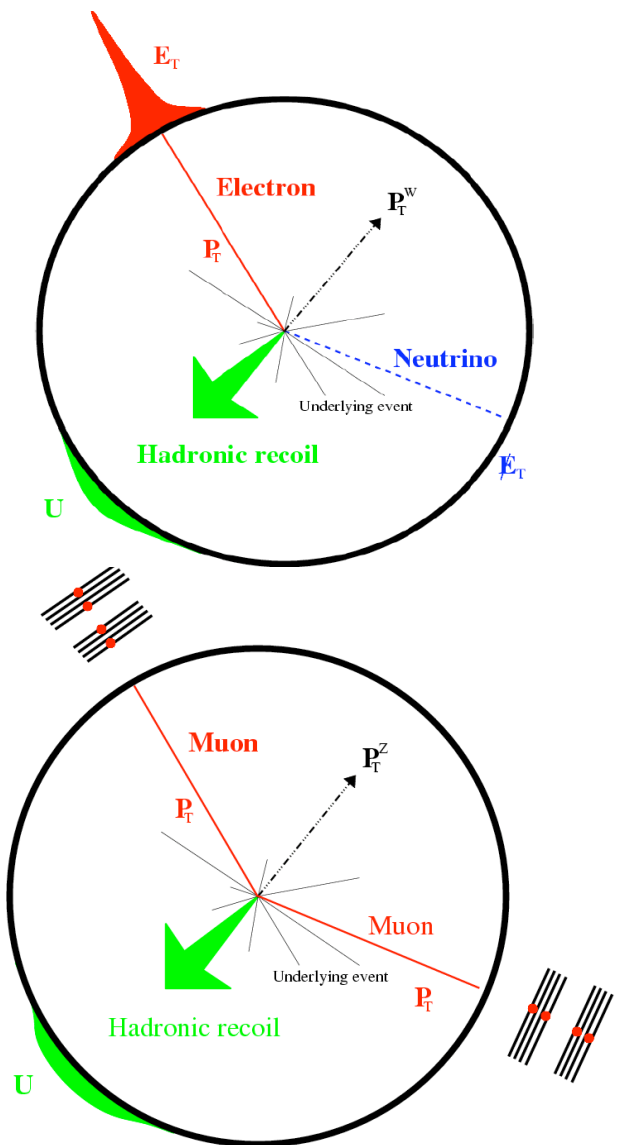
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- Maximize internal constraints and cross-checks
- Why?
  1. **Robustness:** Constrain the same parameter multiple ways
  2. **Precision:** After demonstrating 1), combine independent measurements

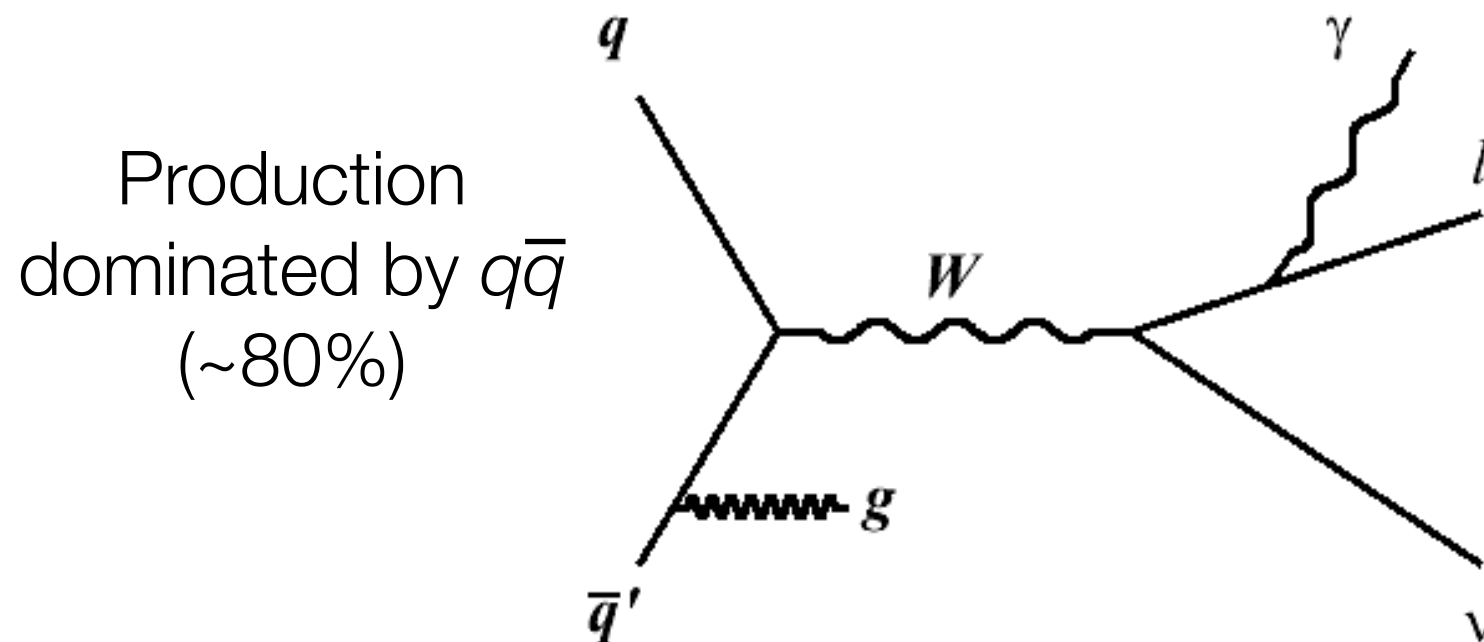
# Measurement strategy (more specifically)

- Perform COT alignment with cosmic ray data
- Calibrate **track momentum scale** using dimuon resonances ( $J/\psi$ ,  $\Upsilon$ ).
  - **Cross-check** with  $Z$  mass measurement and add as further calibration point
- Calibrate **calorimeter energy** using  $E/p$  of  $W$  and  $Z$  decays
  - **Cross-check** with  $Z$  mass measurement
- Calibrate **hadronic recoil** with  $Z$  decays to  $\mu$ ,  $e$ 
  - **Cross-check** with  $W$  recoil distributions
- Perform fits to  $e/\mu$   $p_T$ ,  $\nu$   $p_T$ , and **transverse mass**

$$m_T = \sqrt{2p_T^\ell p_T^\nu (1 - \cos \Delta\theta_{\ell\nu})}$$
  - Binned maximum likelihood fit to templates from tuned simulation
- Combine all **six** fits to yield final answer



# Selecting $W$ (and $Z$ ) bosons at CDF



Select  $e\nu$  and  $\mu\nu$  decays with high- $p_T$  lepton trigger

Lepton candidates:  
Electron  $E_T > 30$  GeV  
(track  $p_T > 18$  GeV)  
or Muon  $p_T > 30$  GeV

$W$  boson candidates:  
1 lepton passing cuts  
 $|\mathbf{u}| < 15$  GeV  
 $p_T^\nu > 30$  GeV  
 $60 < m_T < 100$  GeV

$Z$  boson candidates:  
2 lepton passing cuts  
 $66 < m_{ll} < 116$  GeV

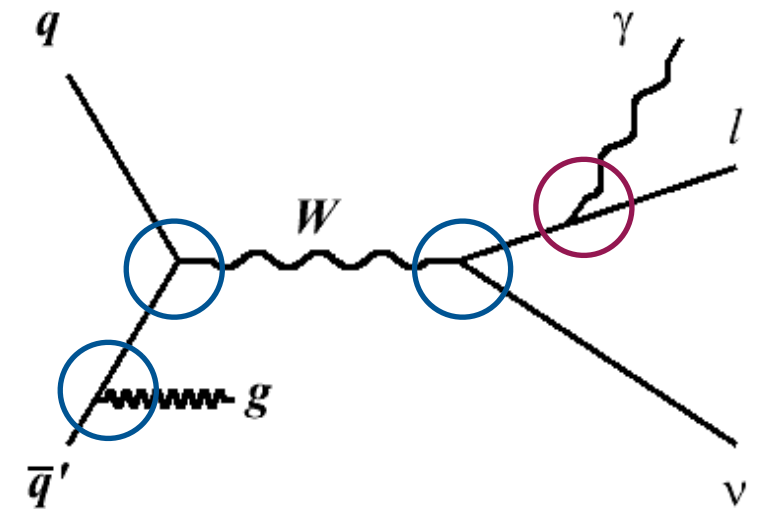
Analysis dataset: **2.2 fb<sup>-1</sup>**

**Candidate events:**  
 $W$ : 470126 (e), 624708 ( $\mu$ )  
 $Z$ : 16134 (e), 59738 ( $\mu$ )

Theoretical model

# Event generation and boson $p_T$

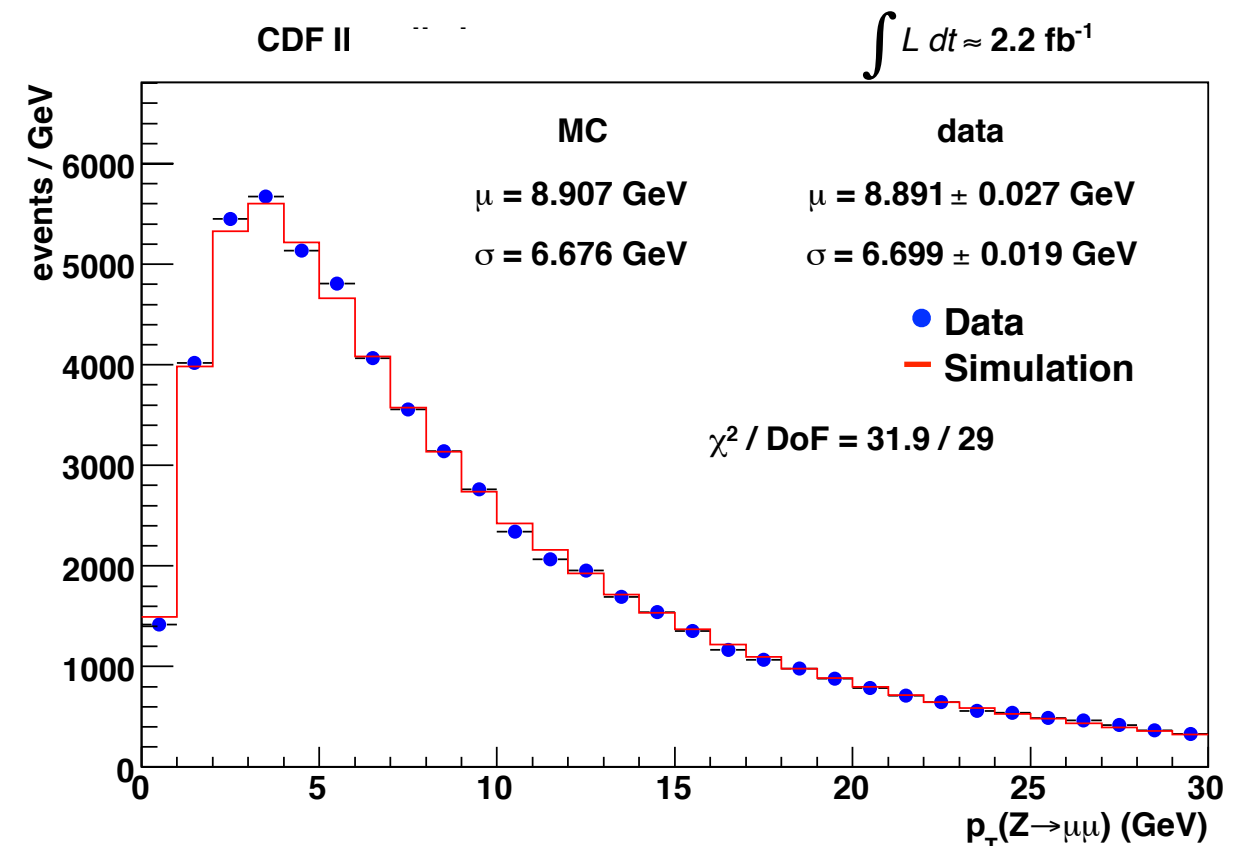
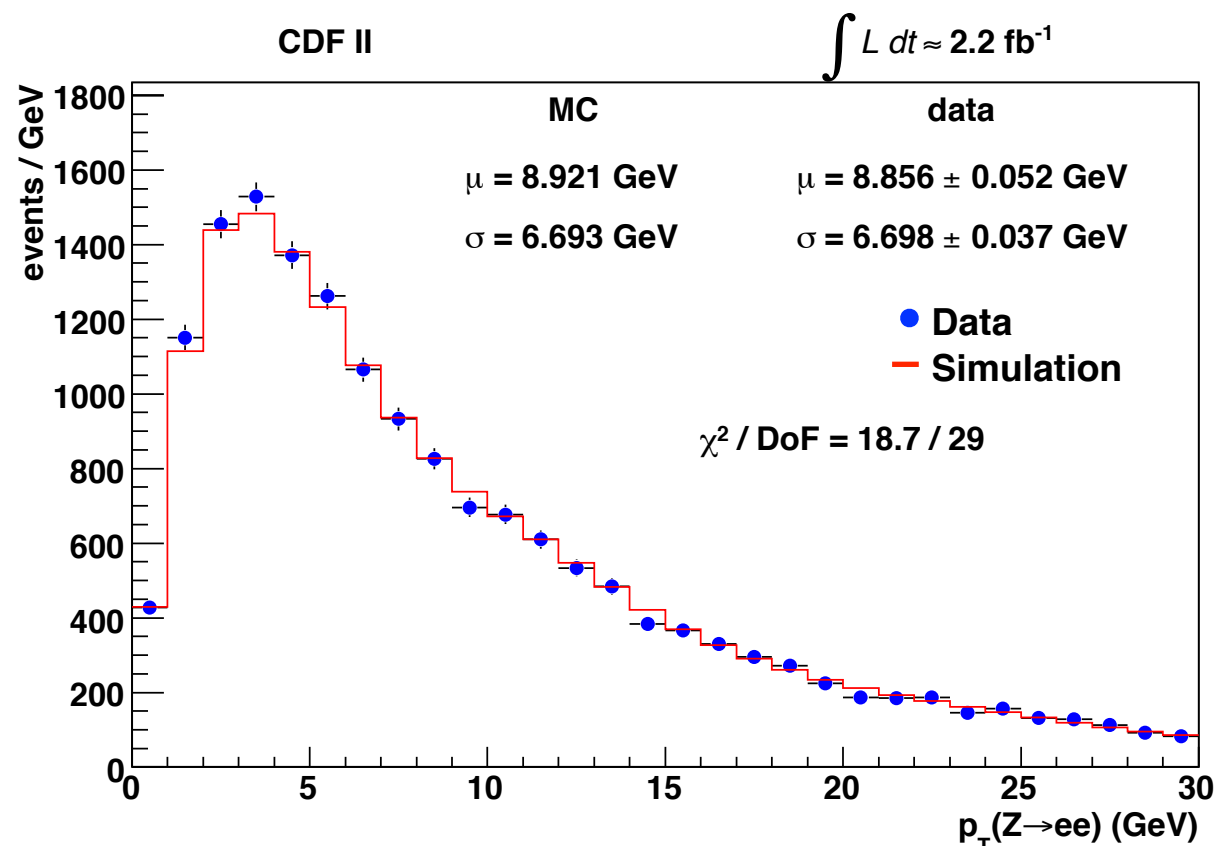
- Generator level simulation from **RESBOS**<sup>1</sup>
  - QCD effects, tunable parameters for non-perturbative regime (low- $p_T$ )
- QED radiation simulated by **PHOTOS**<sup>2</sup>
  - FSR multiphoton simulation
- Fit parameters in boson  $p_T$  shape
  - Low  $p_T$  sensitive to  $g_2$
  - Intermediate-high  $p_T$  sensitive to  $\alpha_s$
- Tuning with  $Z$  data applied to  $W$ s



<sup>1</sup>C Balazs and C-P Yuan, *PRD* **55**, 5558 (1997)

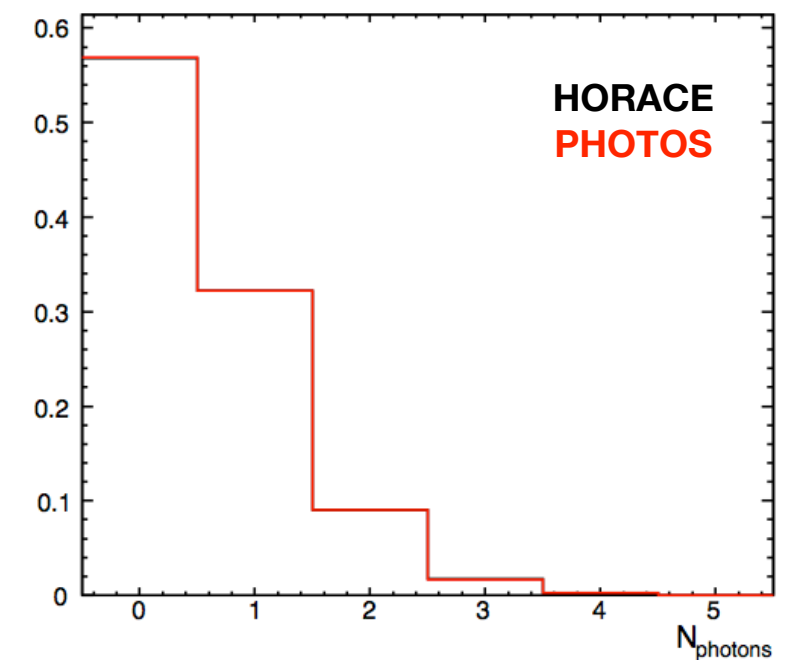
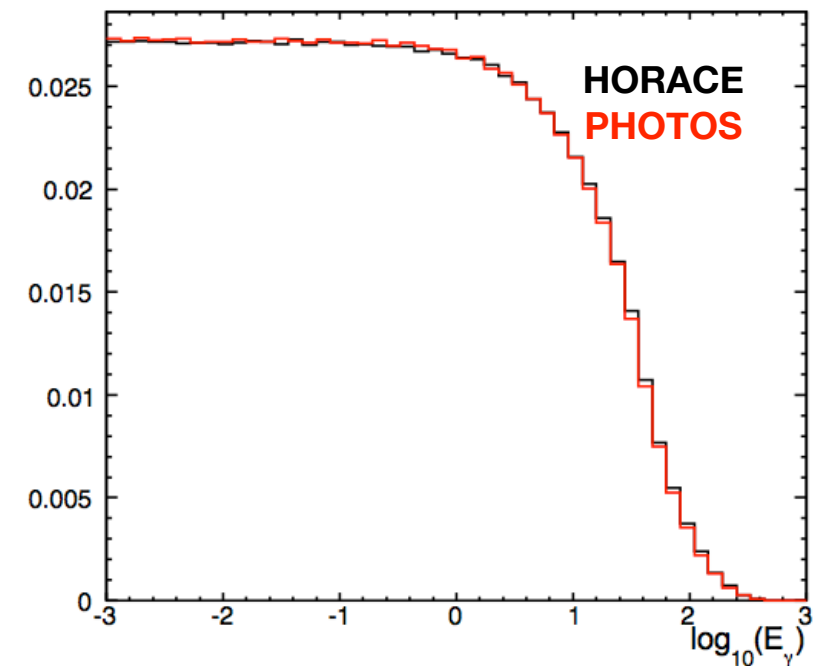
<sup>2</sup>P. Golonka and Z. Was, *Eur. J. Phys. C* **45**, 97 (2006)

$\Delta M_W = 5 \text{ MeV}$



# QED Radiation

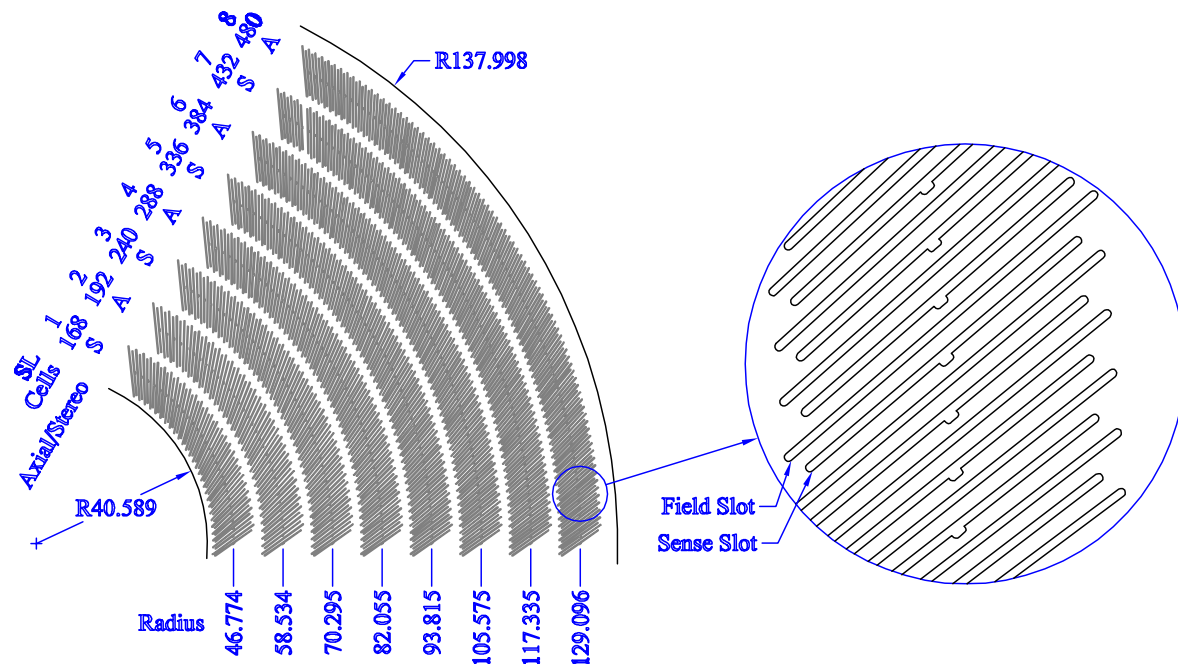
- Extensive studies of QED effects using **HORACE**<sup>1</sup>
  - Leading log approximation vs. exact single photon calculation
  - Multi-photon calculations
  - Higher-order soft/virtual corrections
  - $e^+e^-$  pair creation
  - ISR/FSR interference
  - Dependence on electroweak parameters/scheme
- Detailed comparison of HORACE and PHOTOS
  - Use PHOTOS in final model
- Total systematic uncertainty due to QED  $\Delta M_W = 4 \text{ MeV}$ 
  - *c.f.*  $\Delta M_W = 11 \text{ MeV}$  in 200/pb measurement (uncertainty dominated by subleading photons)



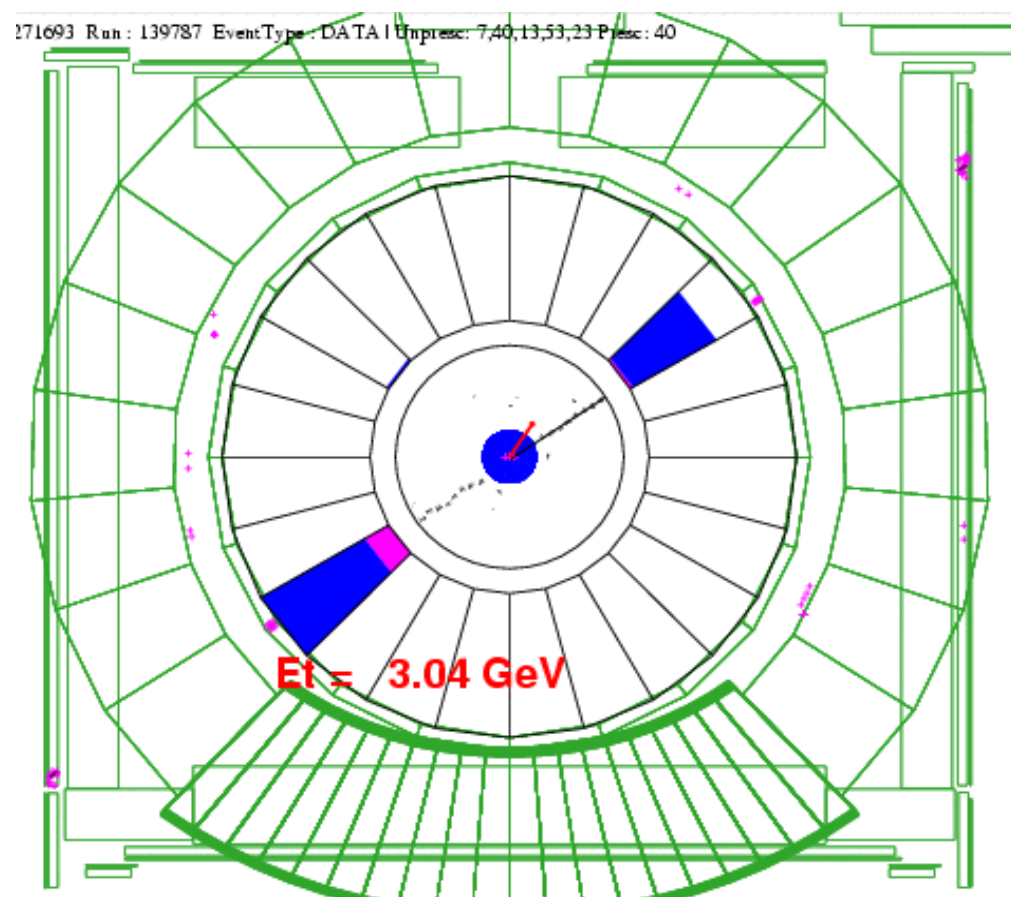
<sup>1</sup>C.M. Carloni Calame, G. Montagna, O. Nicrosini and A. Vicini, JHEP **0710**:109 (2007)

Tracker alignment

# COT alignment with cosmic rays

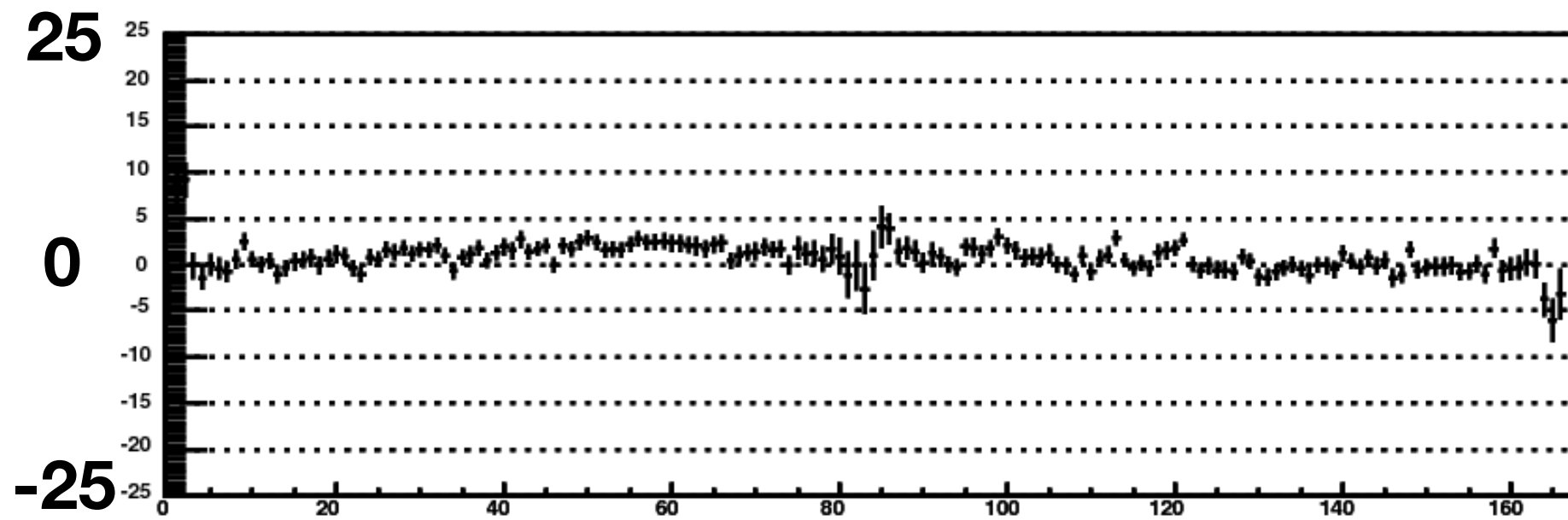
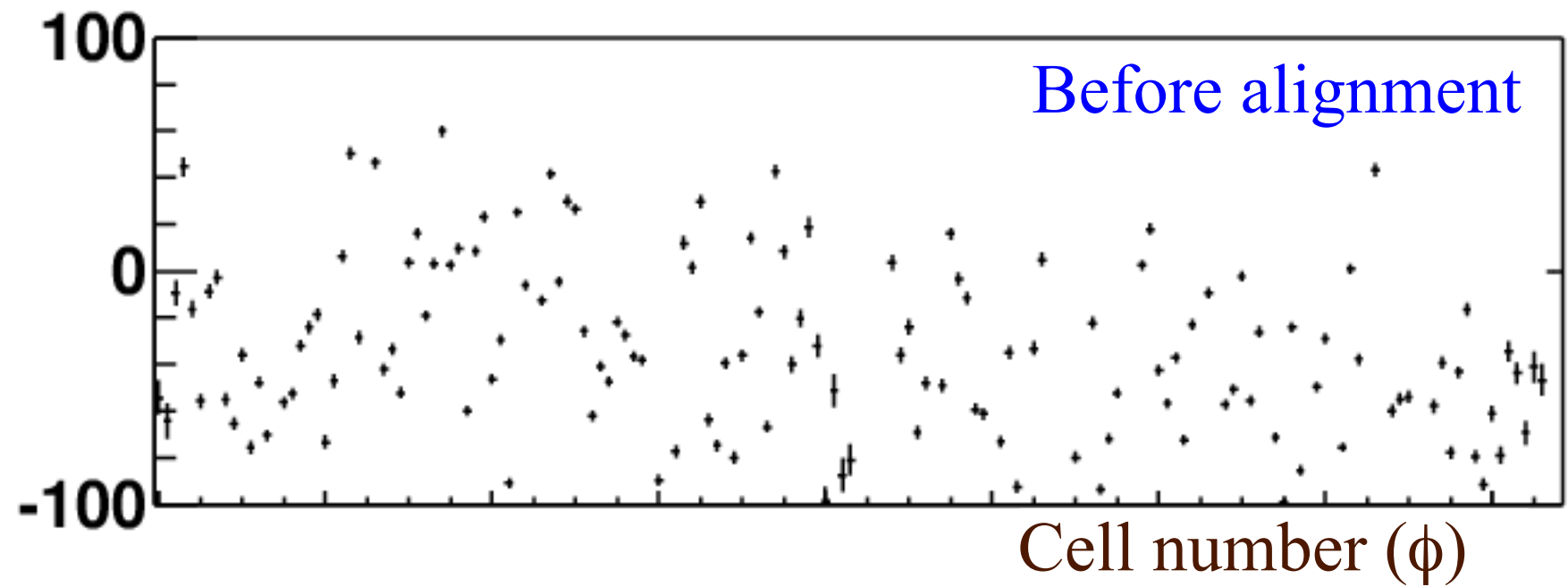


- COT consists of ~30k wires organized into ~2400 “cells”
- Accurate measure of wire positions crucial for precision track  $p_T$
- Use *in-situ* cosmic ray data for alignment
  - Fit of COT hits on either side of vertex to single helix
  - A. Kotwal, H. Gerberich, C. Hays, NIM A **506**, 110 (2003)



# Tracker alignment

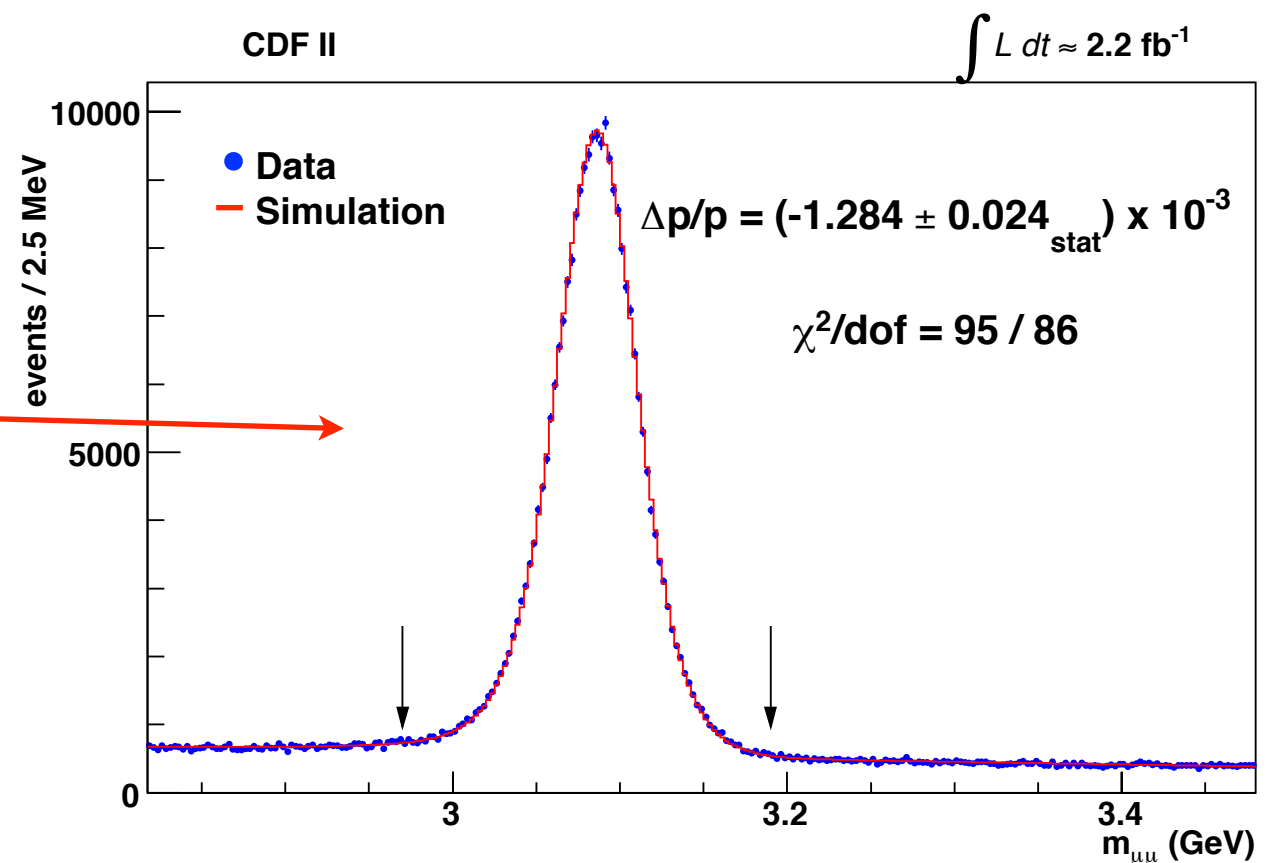
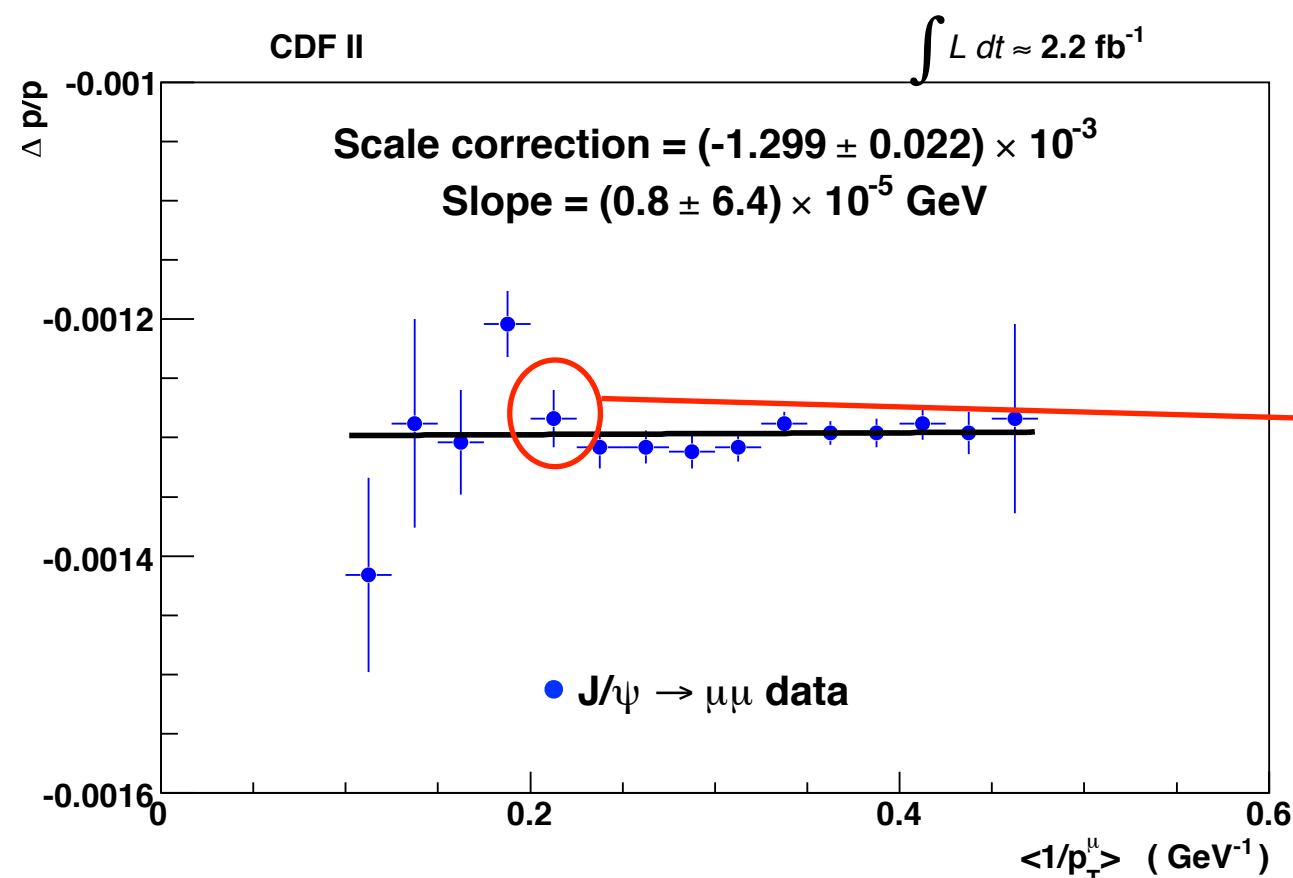
- Improve relative alignment precision from  $\sim 50\mu\text{m}$  to  $\sim 2\mu\text{m}$



Track momentum scale

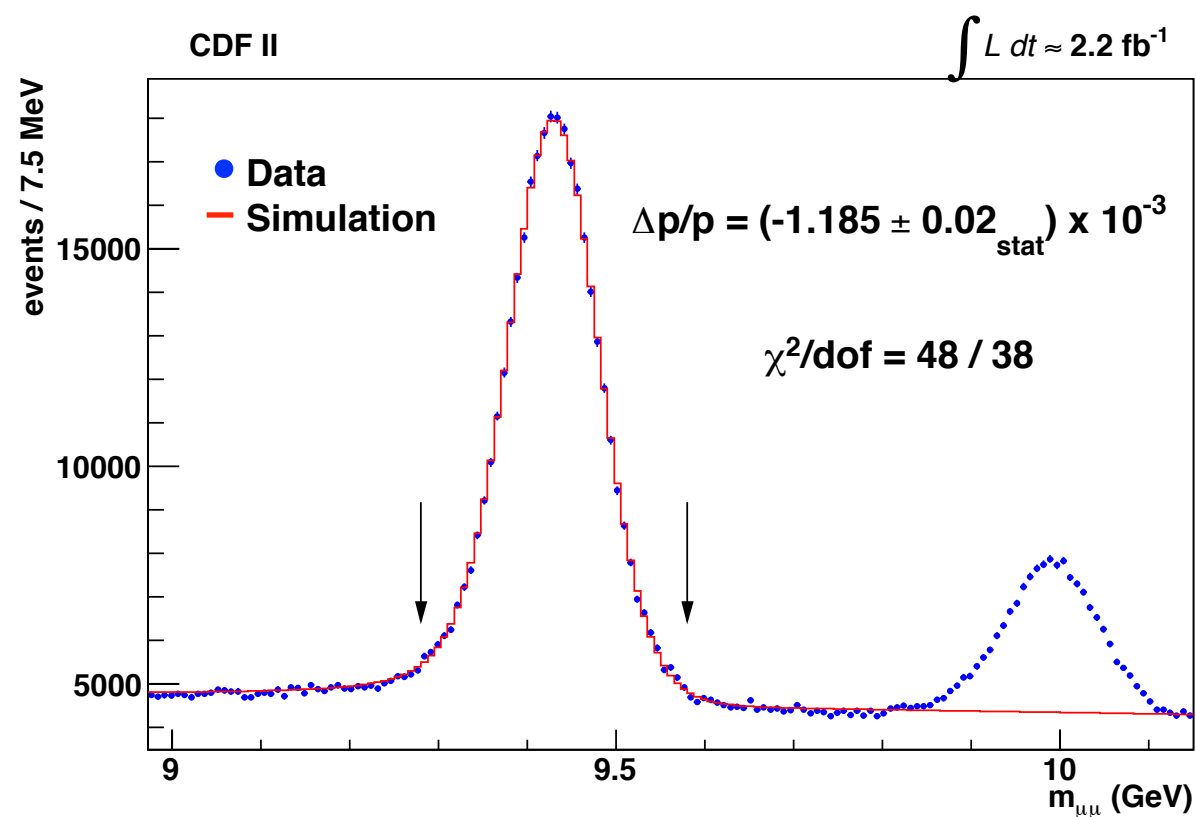
# Track momentum scale: $J/\psi$

- Utilize large samples of  $\mu\mu$  resonances ( $J/\psi$ ,  $\Upsilon$ ,  $Z$ ) to set overall scale
- Size of  $J/\psi$  sample allows subsample fits
  - Fit  $J/\psi$  mass in bins of  $\langle 1/p_T(\mu) \rangle$  and apply material scale calibration (4%) to remove dependence
- Apply calibration from  $J/\psi$  to  $\Upsilon$

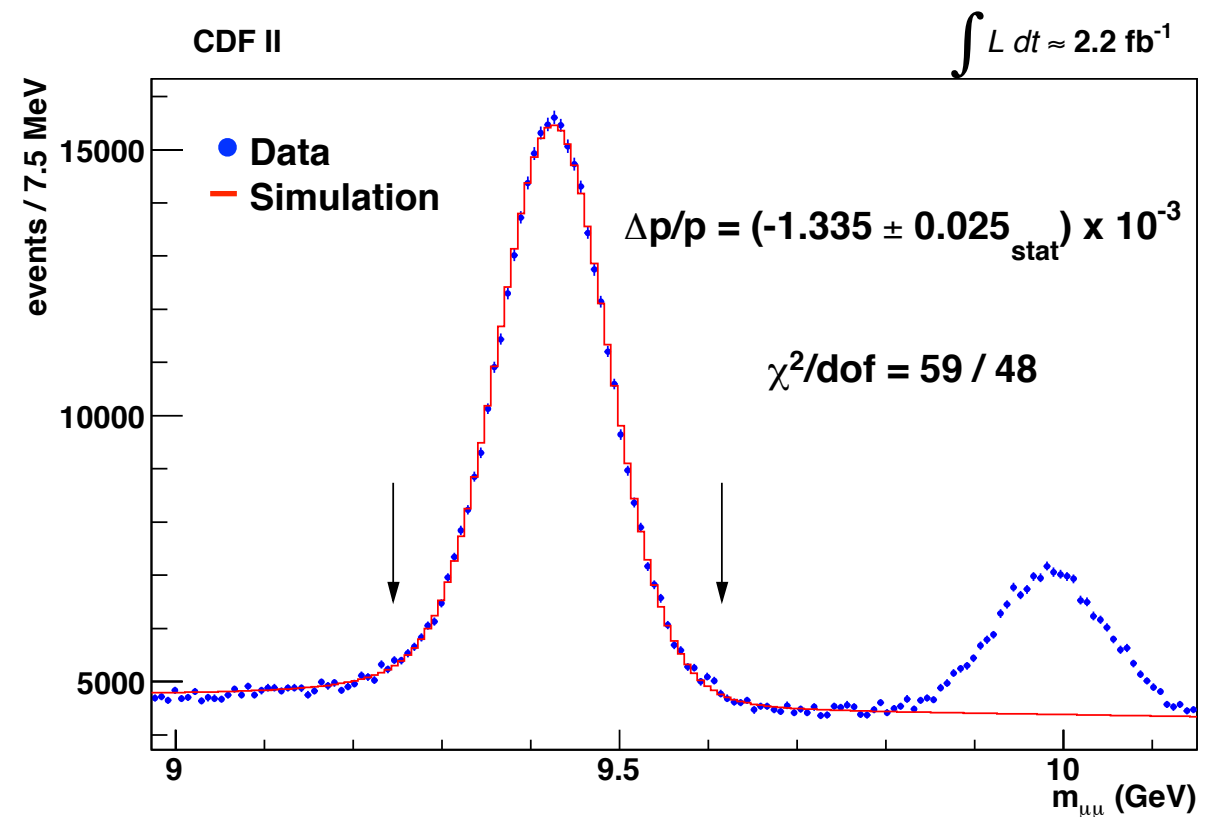


# Track momentum scale: $\Upsilon$

- $\Upsilon$  sample provides higher- $p_T$  sample
- $\Upsilon$ s produced promptly: validation of beam-constraining (BC) procedure
  - Perform fit with BC and non-BC tracks
  - Take average of two fits, assign systematic
- Combine  $J/\psi$  and  $\Upsilon$  scales and apply to  $Z$ s



Beam constrained tracks



Non-beam constrained tracks

# Track momentum scale: systematic uncertainties

| Source                 | $J/\psi$ ( $\cdot 10^{-3}$ ) | NBC- $\Upsilon$ ( $\cdot 10^{-3}$ ) | common ( $\cdot 10^{-3}$ ) |
|------------------------|------------------------------|-------------------------------------|----------------------------|
| QED                    | 0.080                        | 0.045                               | 0.045                      |
| B field non-uniformity | 0.032                        | 0.034                               | 0.032                      |
| Ionizing material      | 0.022                        | 0.014                               | 0.014                      |
| Resolution             | 0.010                        | 0.005                               | 0.005                      |
| Backgrounds            | 0.011                        | 0.005                               | 0.005                      |
| Misalignment           | 0.009                        | 0.018                               | 0.009                      |
| Trigger efficiency     | 0.004                        | 0.005                               | 0.004                      |
| Fitting window         | 0.004                        | 0.005                               | 0.004                      |
| $\Delta p/p$ step size | 0.002                        | 0.003                               | 0                          |
| World-average          | 0.004                        | 0.027                               | 0                          |
| Total systematic       | 0.092                        | 0.068                               | 0.058                      |
| Statistical            | 0.004                        | 0.025                               | 0                          |
| Total                  | 0.092                        | 0.072                               | 0.058                      |

- Dominated by QED and B-field non-uniformity
  - BC vs NBC comparison contributes additional  $0.036 \times 10^{-3}$

# Track momentum scale: systematic uncertainties

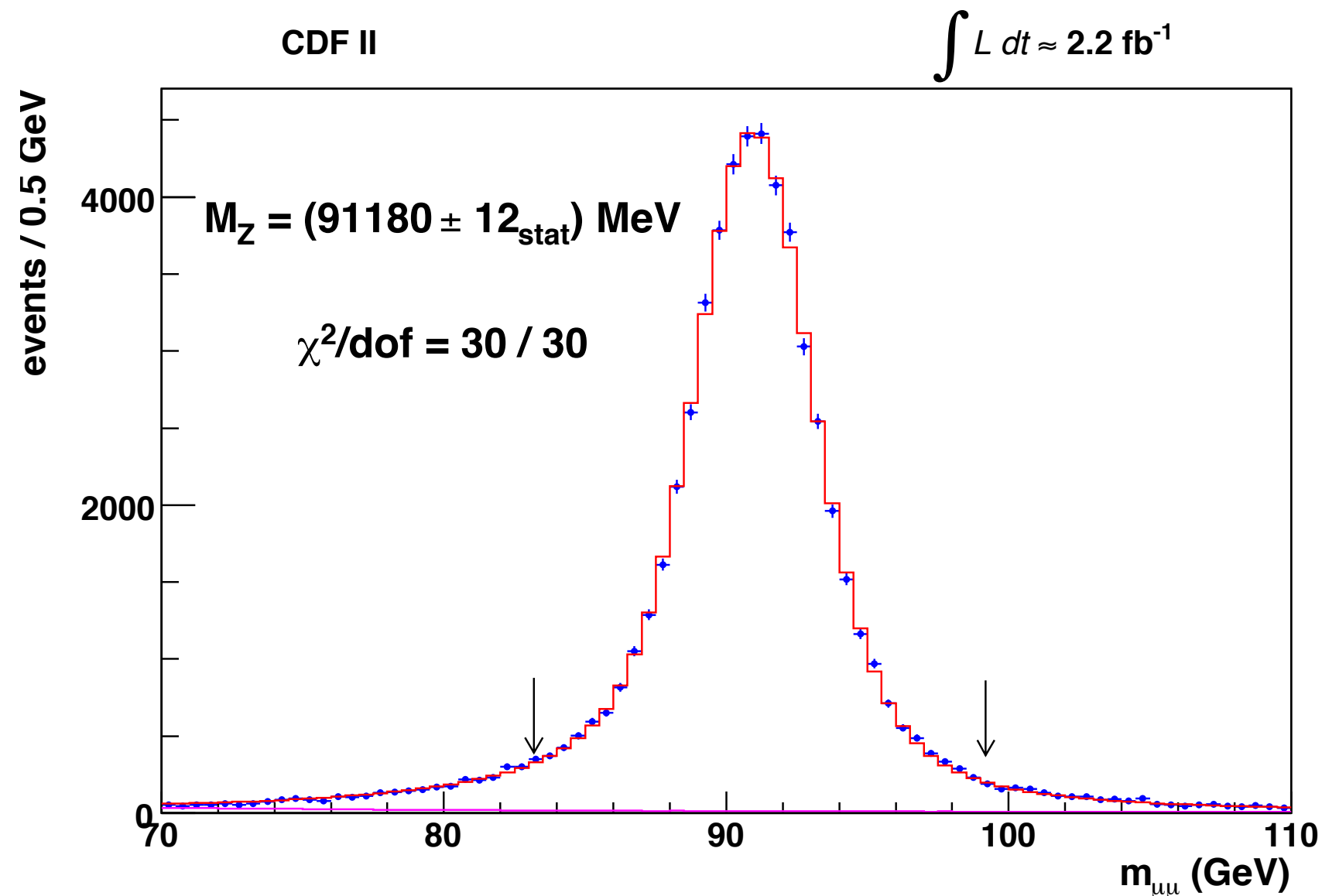
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$$\Delta M_W \sim 6 \text{ MeV}$$

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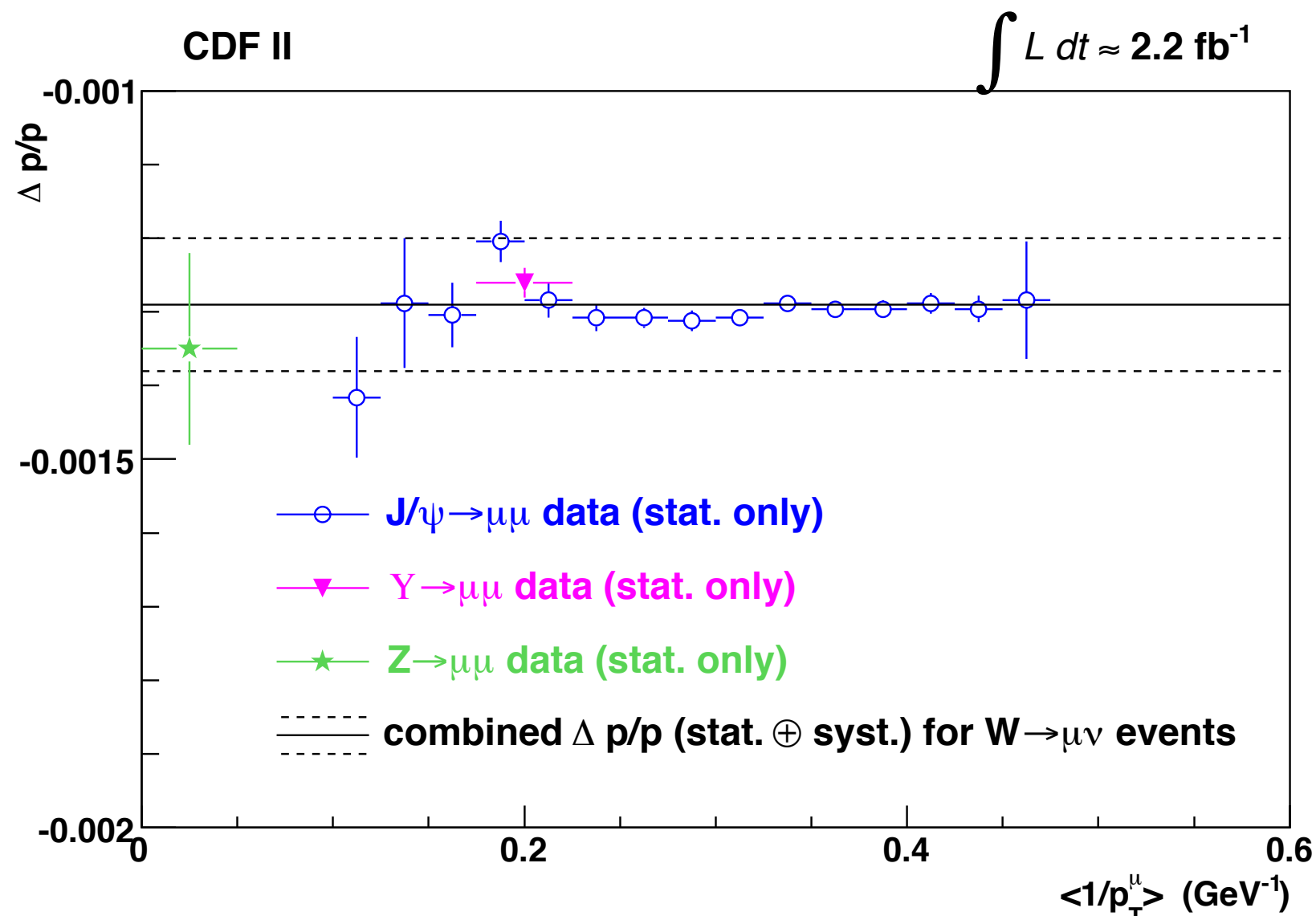
# Muon $Z$ mass measurement

- Perform **independent** measurement of  $Z$  mass using tuned momentum scale
  - Fit central value kept blind during scale calibration
  - $M_Z = 91180 \pm 12_{\text{stat}} \pm 9_{\text{p-scale}} \pm 5_{\text{QED}} \pm 2_{\text{alignment}} = \mathbf{91180 \pm 16 \text{ MeV}}$
  - Excellent agreement with world average ( $91188 \pm 2 \text{ MeV}$ )



# Final momentum scale

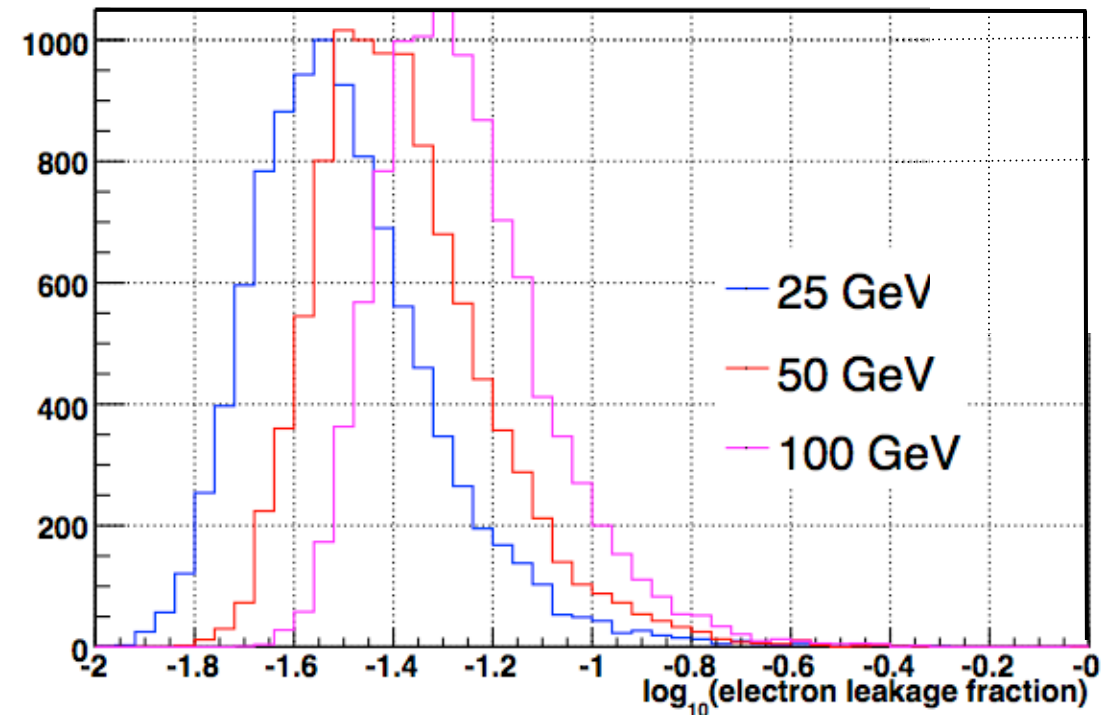
- Add Z data as final calibration point for momentum scale
  - $\Delta p/p_{\text{final}} = (-1.29 \pm 0.07_{\text{stat}} \pm 0.05_{\text{QED}} \pm 0.02_{\text{align}}) \times 10^{-3}$
  - Apply scale to  $W$  muons and  $E/p$  calibration
  - Systematic uncertainty  $\Delta M_W = 7 \text{ MeV}$



EM calorimeter scale

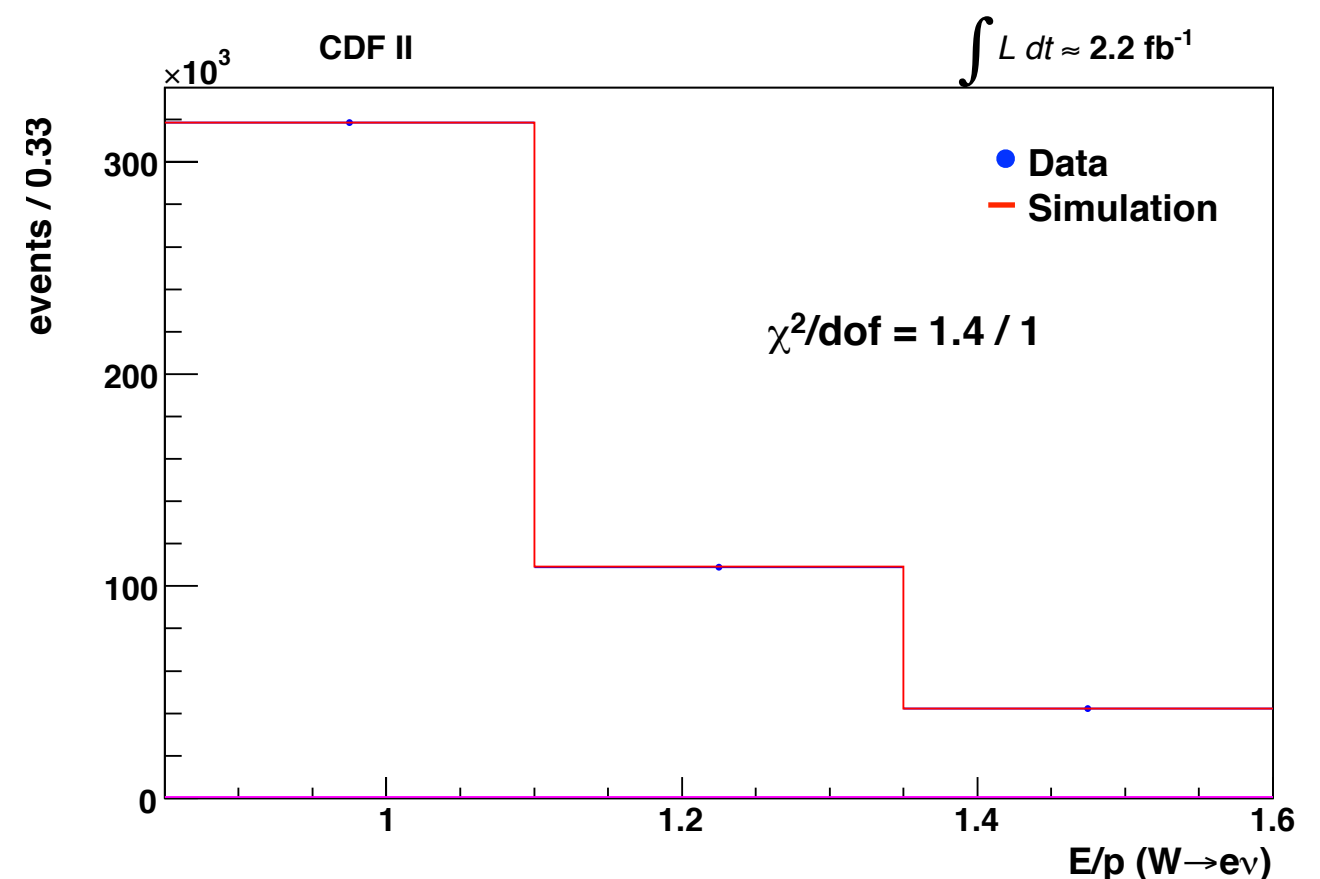
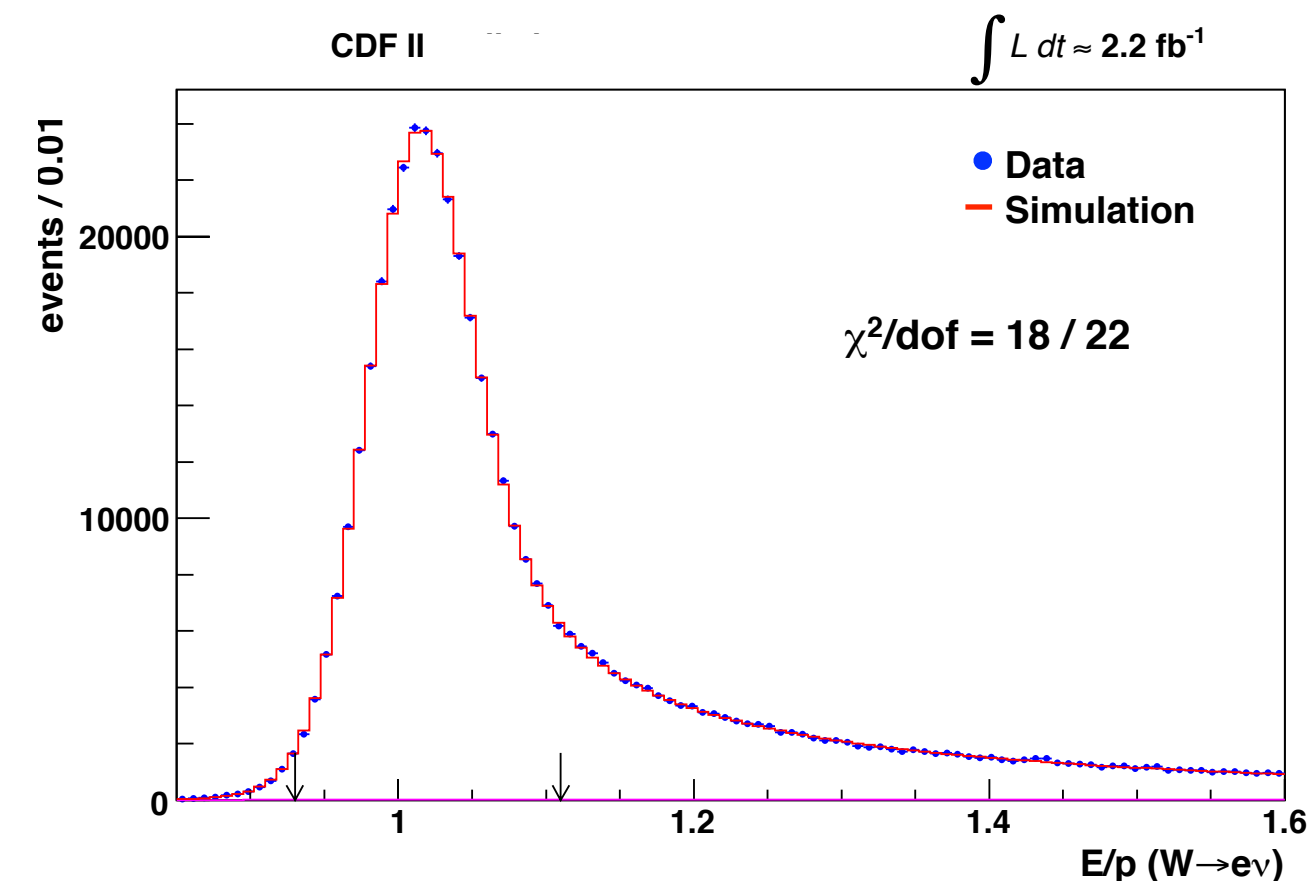
# Simulation for electrons and photons

- EM energy loss studied using detailed GEANT4-based simulation
  - Leakage into hadronic calorimeter
  - Absorption into coil
  - Dependence on incident angle and  $E_T$
- Improved model of Landau-Pomeranchuk-Migdal (LPM) suppression of bremsstrahlung
  - Sophisticated material map for tracker region of detector



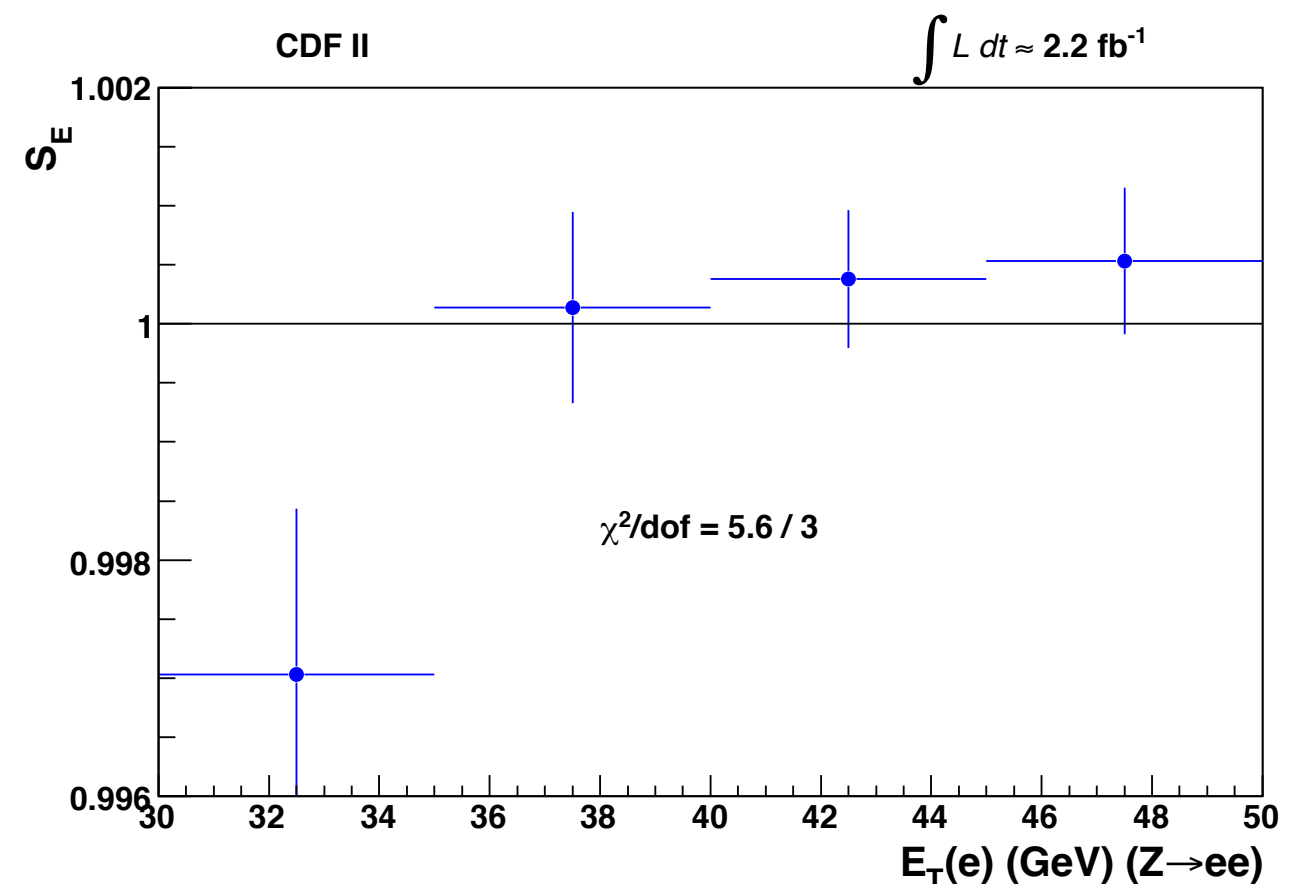
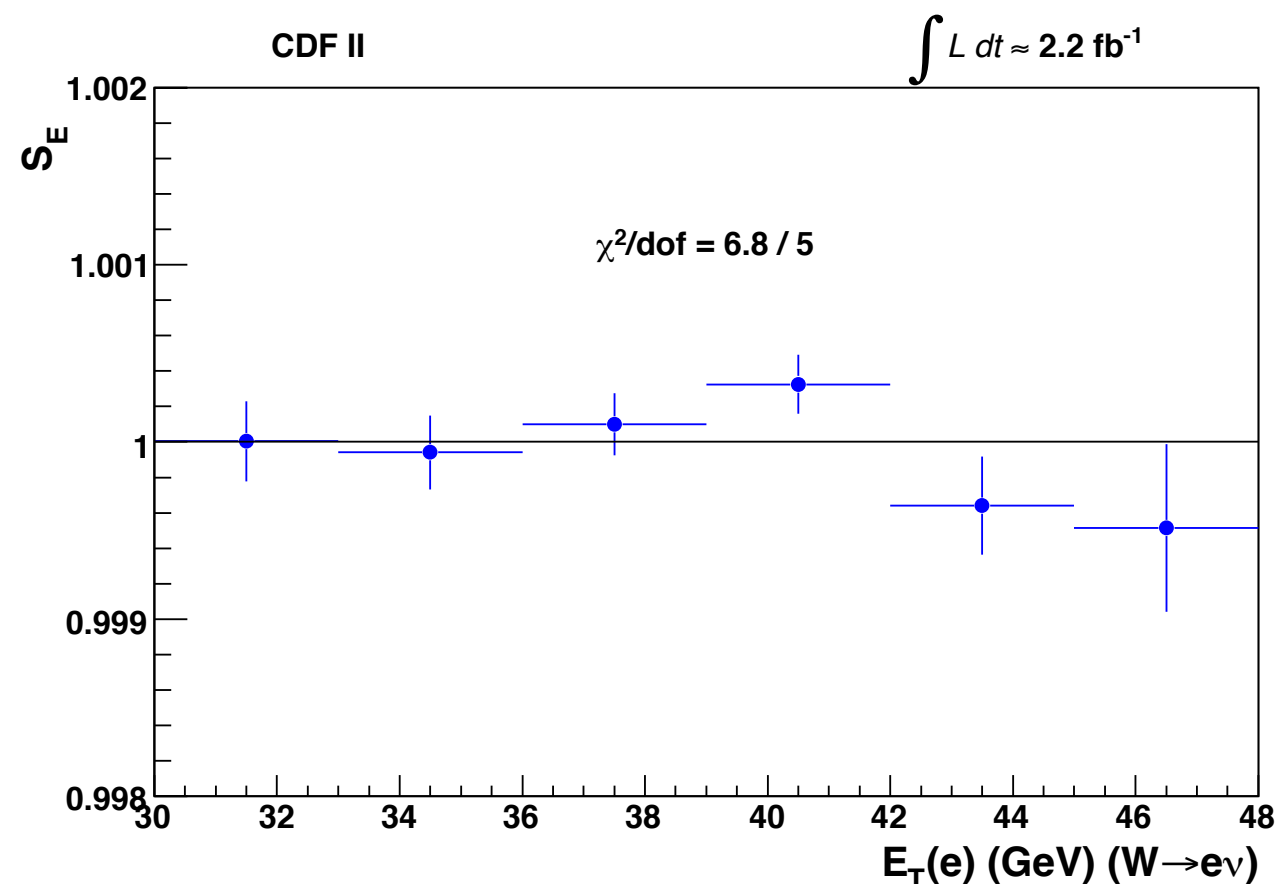
# Energy scale calibration

- Calibrate EM calorimeter response using  $W$  and  $Z$   $E/p$  distributions
  - Fit to peak to obtain scale (central value of 1 by construction)
    - $\Delta S_E = (9_{\text{stat}} \pm 5_{\text{non-linearity}} \pm 5_{\text{mat}} \pm 9_{\text{p-scale}}) \times 10^{-5}$
  - Fit to tail to tune amount of radiative material
    - Apply scale factor to material model  $S_{X0} = 1.026 \pm 0.003_{\text{stat}} \pm 0.002_{\text{bkg}}$
- Systematic uncertainty  $\Delta M_W = 13 \text{ MeV}$



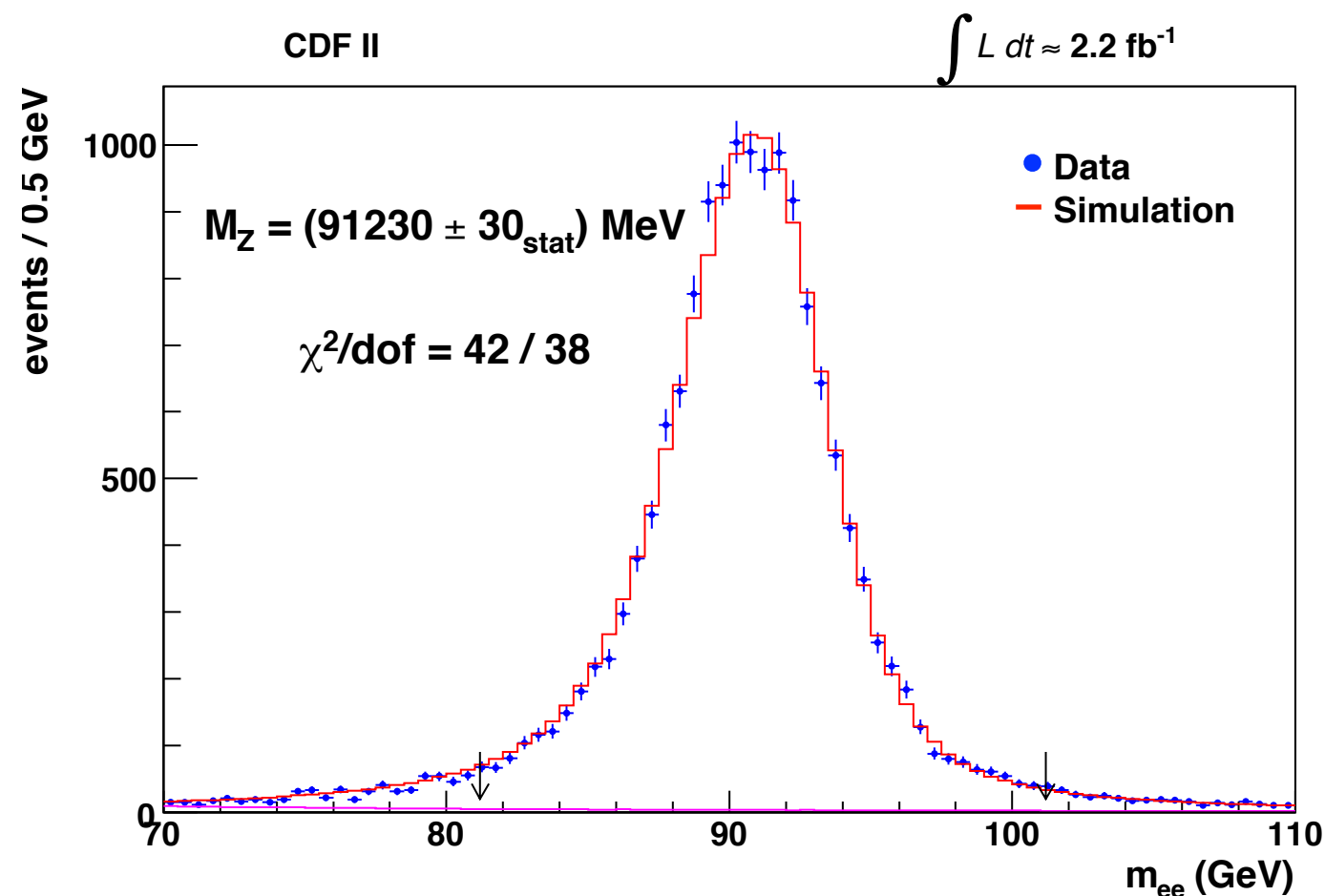
# EM scale non-linearity

- Fit  $E/p$  in bins of electron  $E_T$ 
  - Parameterize non-linearity as  $S_E = 1 + \beta \log(E_T/39 \text{ GeV})$
- Tune using W and Z data and obtain  $\beta = (5.2 \pm 0.7_{\text{stat}}) \times 10^{-3}$ 
  - $\Delta M_W = 4 \text{ MeV}$
- Obtain flat response in  $E_T$  after tuning



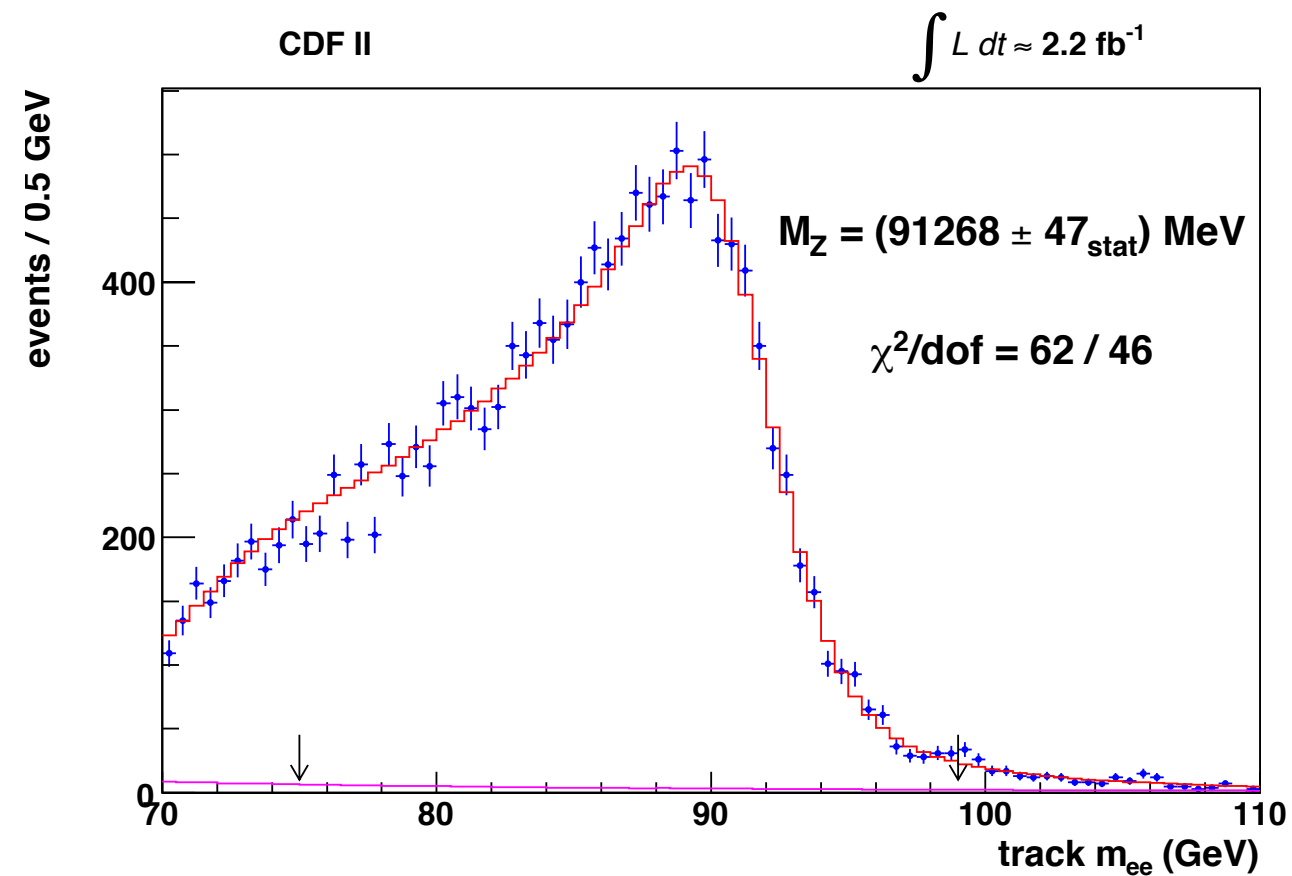
# Electron $Z$ mass and final EM energy scale

- Perform **independent** measurement of  $Z$  mass using calibrated EM scale
  - $M_Z = 91230 \pm 30_{\text{stat}} \pm 10_{E/p} \pm 8_{p\text{-scale}} \pm 5_{\text{QED}} \pm 2_{\text{alignment}} = \mathbf{91230 \pm 33 \text{ MeV}}$
  - Excellent agreement with world average  $M_Z = 91188 \pm 2 \text{ MeV}$
- Combine  $E/p$  calibration with  $M_Z$  to obtain final EM calibration
  - Systematic uncertainty  $\Delta M_W = \mathbf{10 \text{ MeV}}$



# Z mass with electron tracks

- Measurement made with only track momenta of Z electrons
- Validates material model and application of momentum scale to high- $p_T$  electron tracks



# Lepton resolution

---

- Muons
  - Track resolution determined by uncertainty on beamspot size ( $35 \pm 1 \text{ } \mu\text{m}$ ) and track hit resolution ( $150 \pm 1 \text{ } \mu\text{m}$ )
  - Tuned using widths of Z and Y peaks
- Electrons
  - EM calorimeter resolution defined by sampling term and constant term
$$\sigma = 12.6\% \sqrt{E_T / \text{GeV}} \oplus \kappa$$
  - Constant term tuned using E/p distribution  $\kappa = (0.58 \pm 0.05)\%$
  - Apply secondary constant term for radiative electrons ( $E/p > 1.1$ )
    - $\kappa_Y = (7.4 \pm 1.8)\%$
- Resolution terms total  $\Delta M_W = 4 \text{ MeV}$

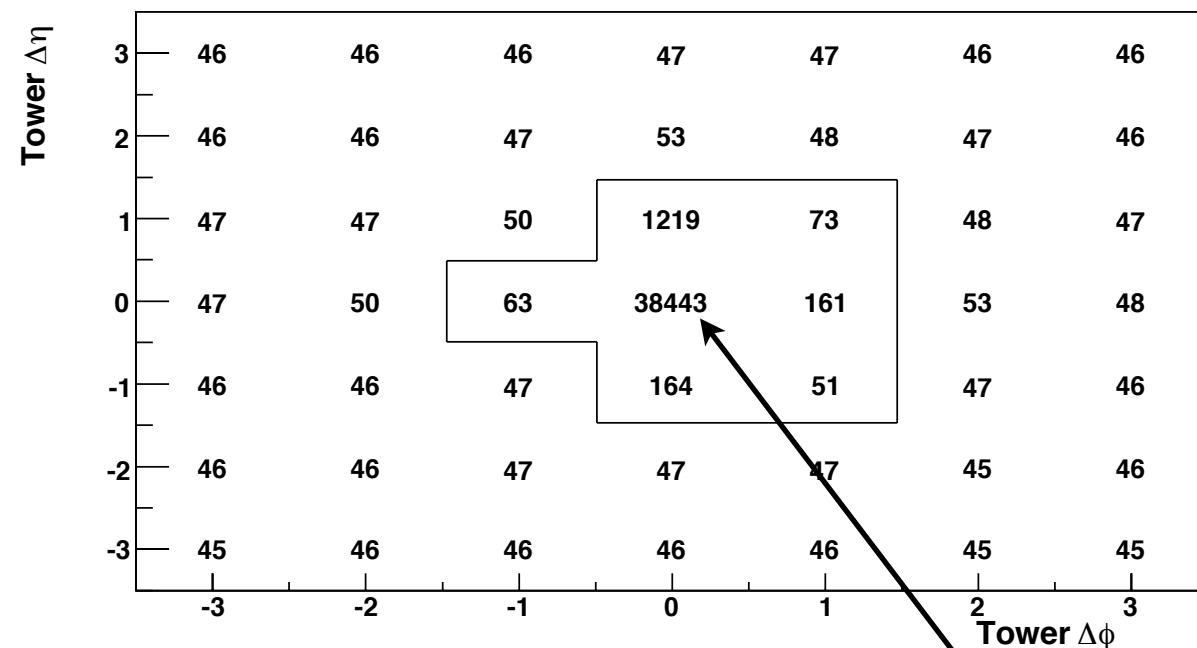
Hadronic recoil

# Hadronic recoil: lepton removal

- Hadronic recoil  $\mathbf{u}$  is vector sum of all calorimeter towers minus towers containing lepton energy
- Some underlying event energy removed with “lepton towers”
  - Estimate using rotated lepton removal windows
  - Systematic uncertainty  $\Delta M_W = 2 \text{ MeV}$

## Electron channel W data:

Mean EM calorimeter deposition (MeV)

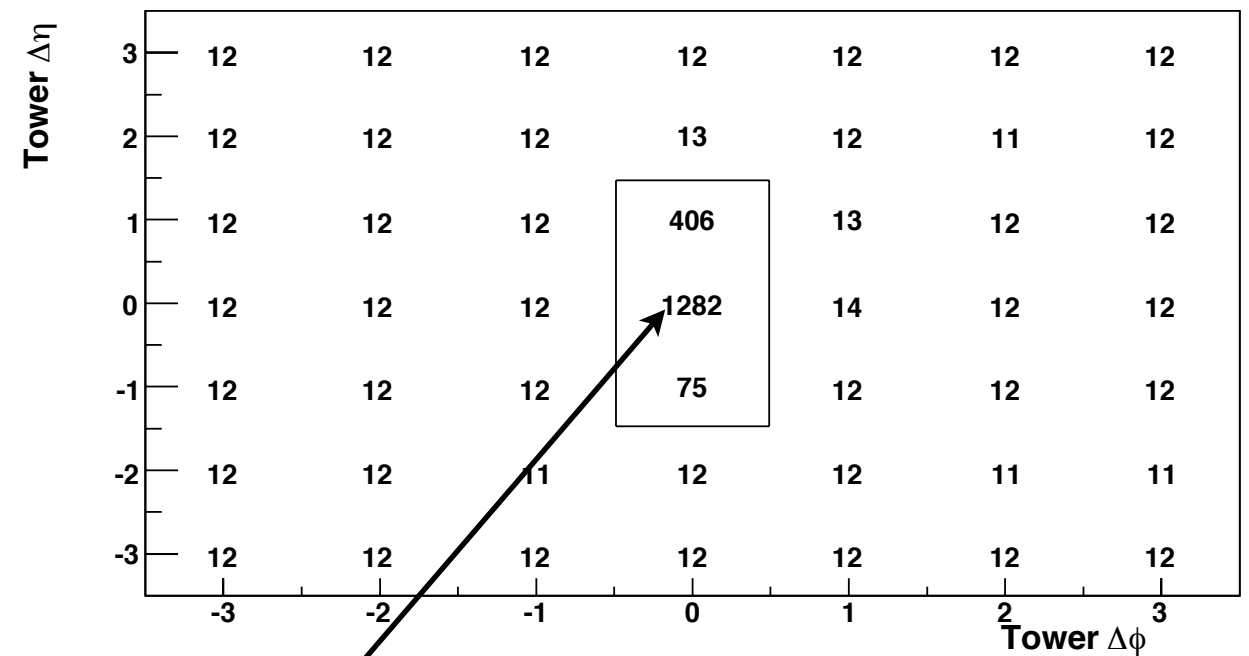


□ Default towers removed

Central lepton tower

## Muon channel W data:

Mean hadronic calorimeter deposition (MeV)



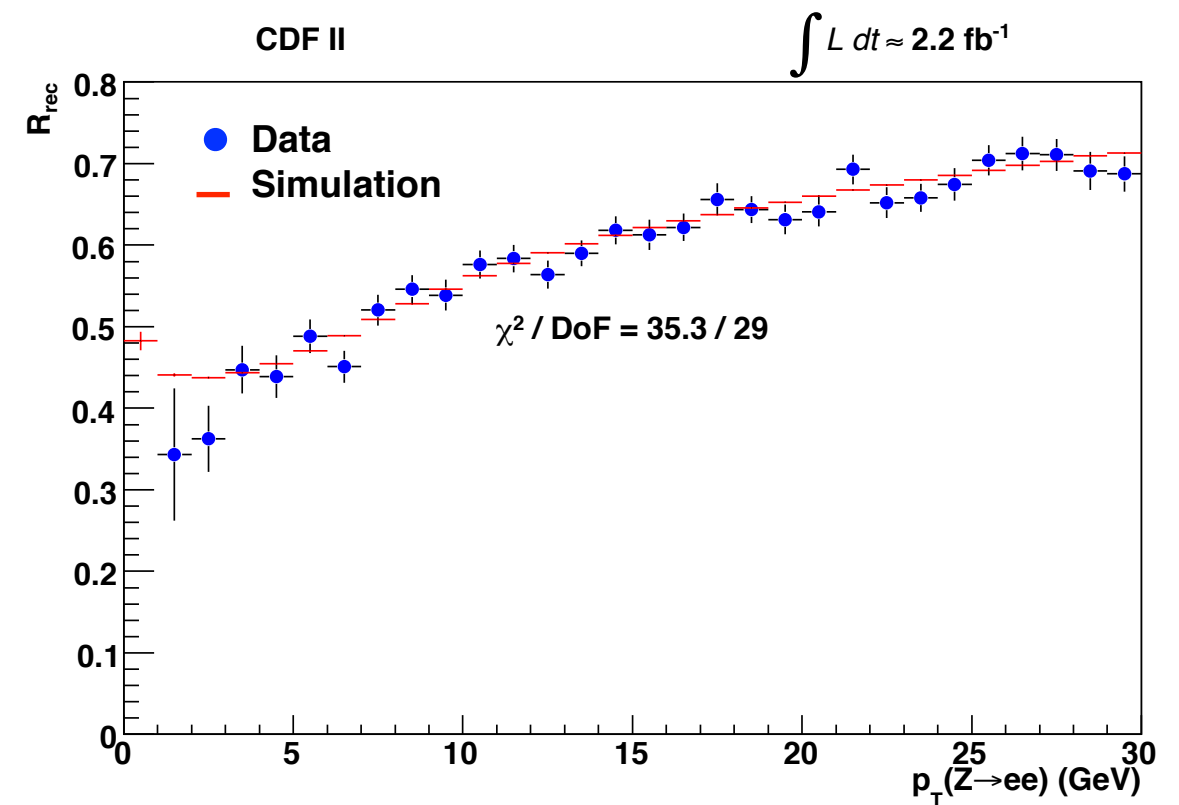
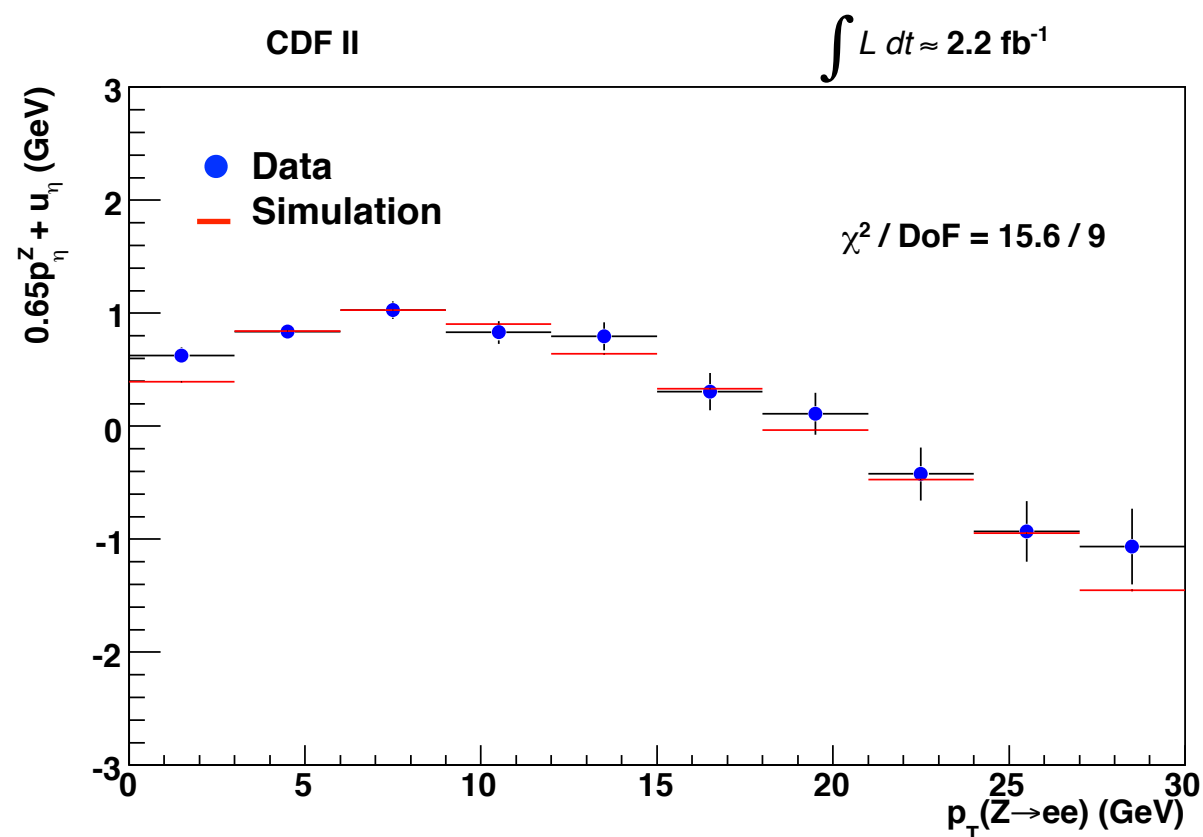
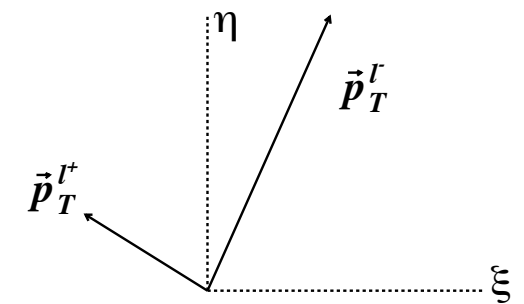
# Recoil model

---

- Parametrize recoil model and tune using data
- Two components
  1. Soft “spectator interaction” component
    - Randomly oriented ( $\sim 2$  additional interactions per event)
    - Model using minimum-bias data
  2. Hard “jet” component
    - Boson  $p_T$  dependent response and resolution
    - Tune by balancing boson  $p_T$  and recoil

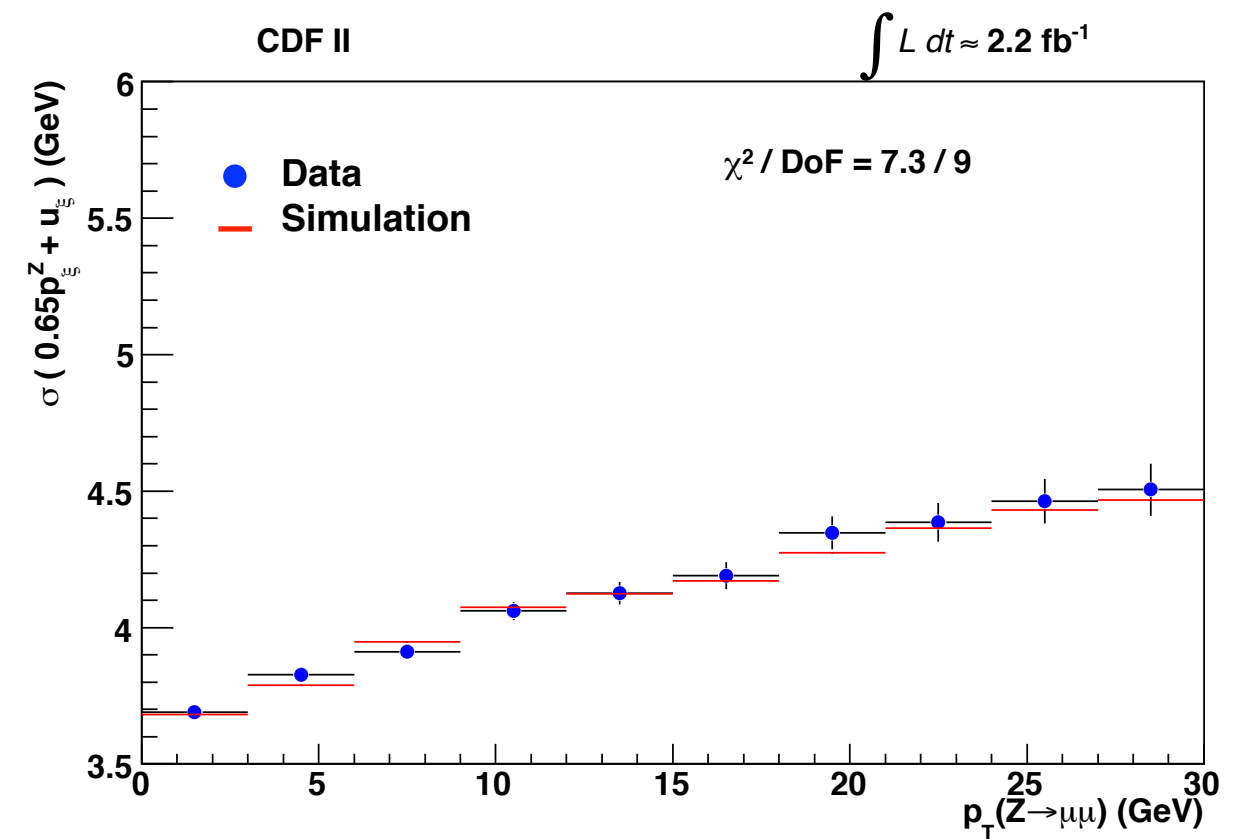
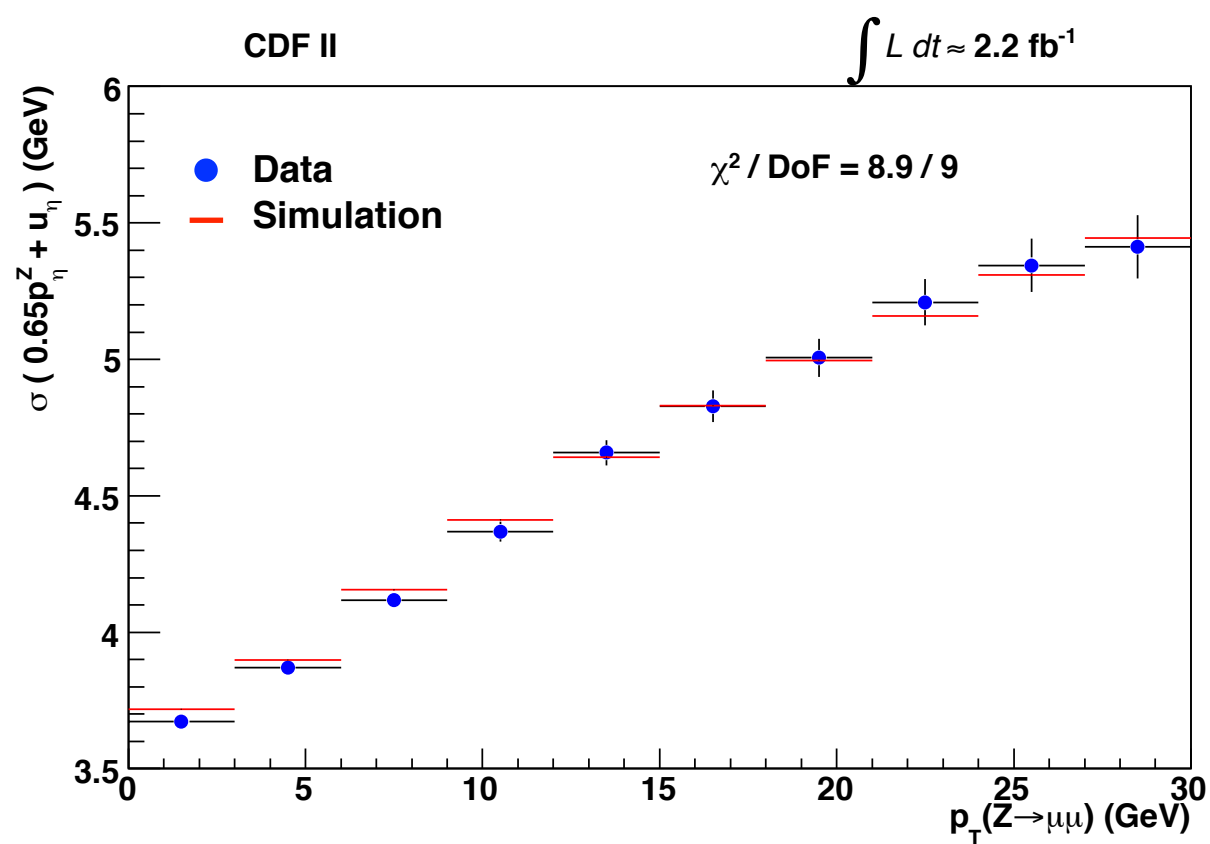
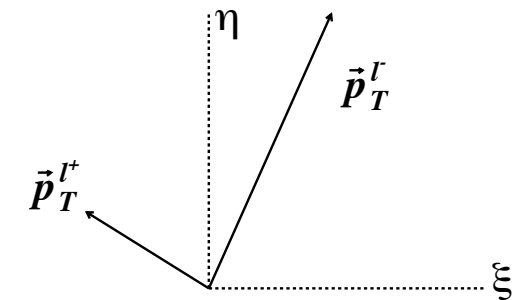
# Calibrating recoil response

- Recoil scale  $R = u_{\text{meas}} / u_{\text{true}}$ 
  - Calibrate by balancing  $Z$   $p_T$  against  $p_T + u$  along eta axis  $\Delta M_W = 4 \text{ MeV}$



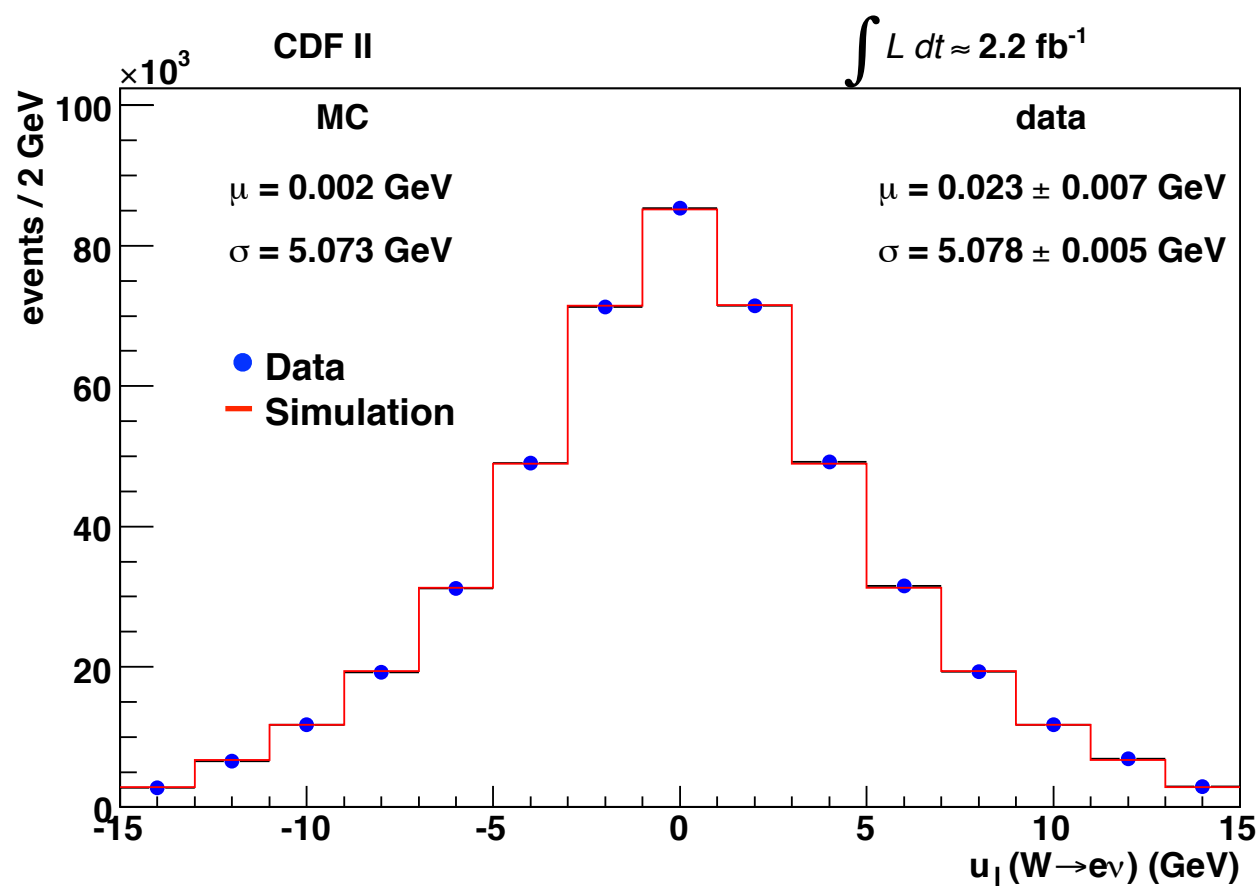
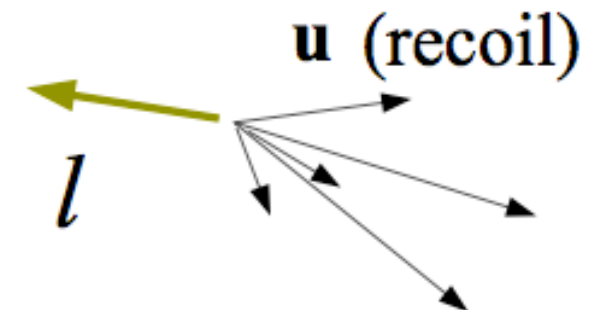
# Calibrating recoil resolution

- Recoil resolution
  - Calibrate balancing  $Z$   $p_T$  against  $\text{rms}(p_T+u)$  along both axes  $\Delta M_W = 4 \text{ MeV}$

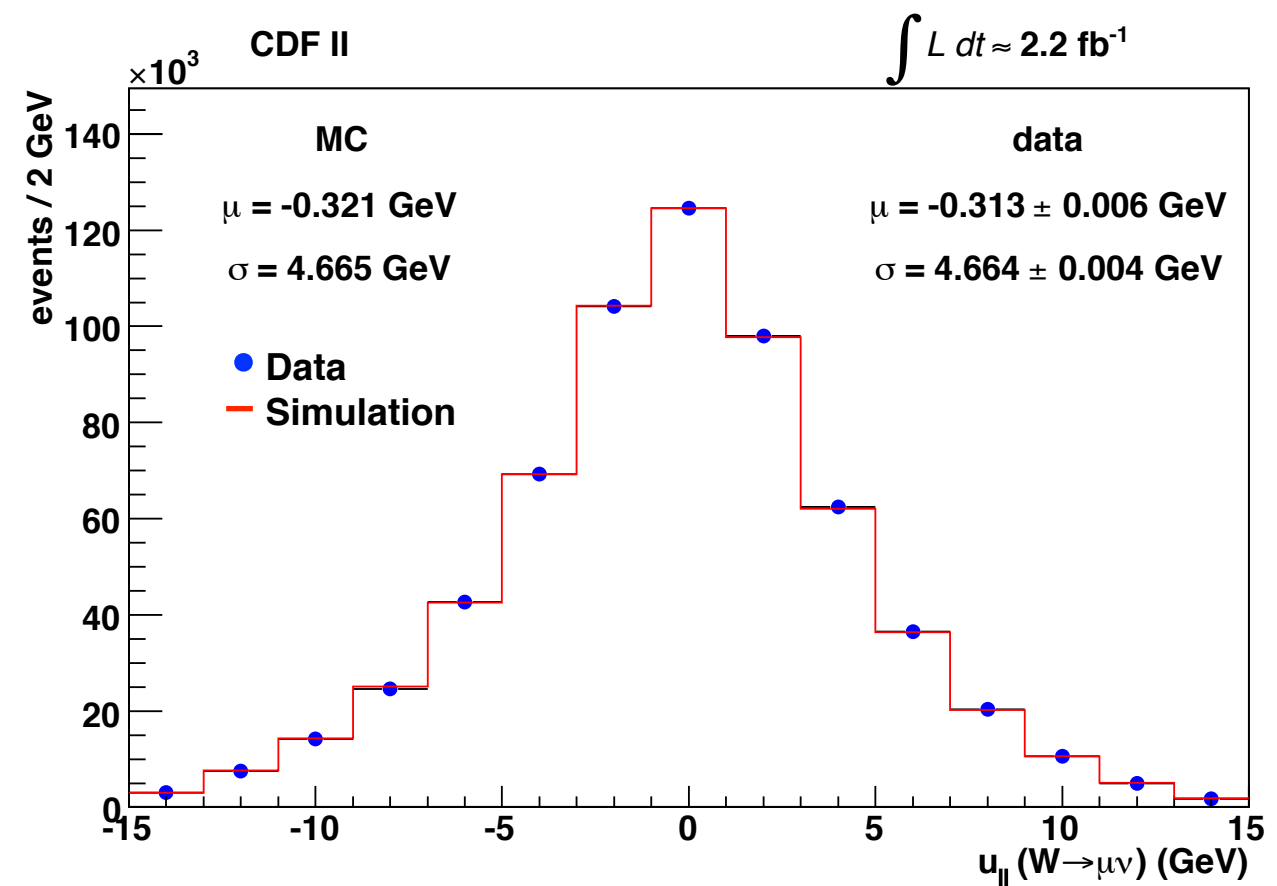


# Recoil validation

- Test recoil model with W events
  - Compare measured recoil in data to model tuned with Z



Recoil projection perpendicular to lepton  
(electrons)



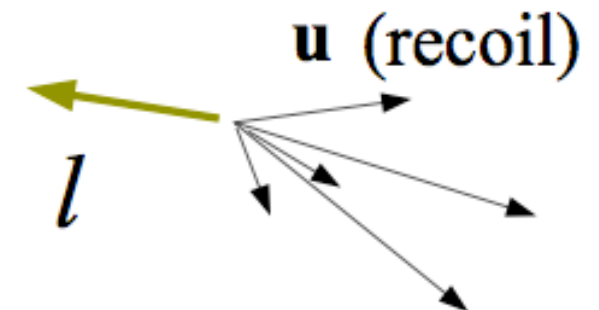
Recoil projection in direction of lepton  
(muons)

for  $u \ll p_T^l$  :

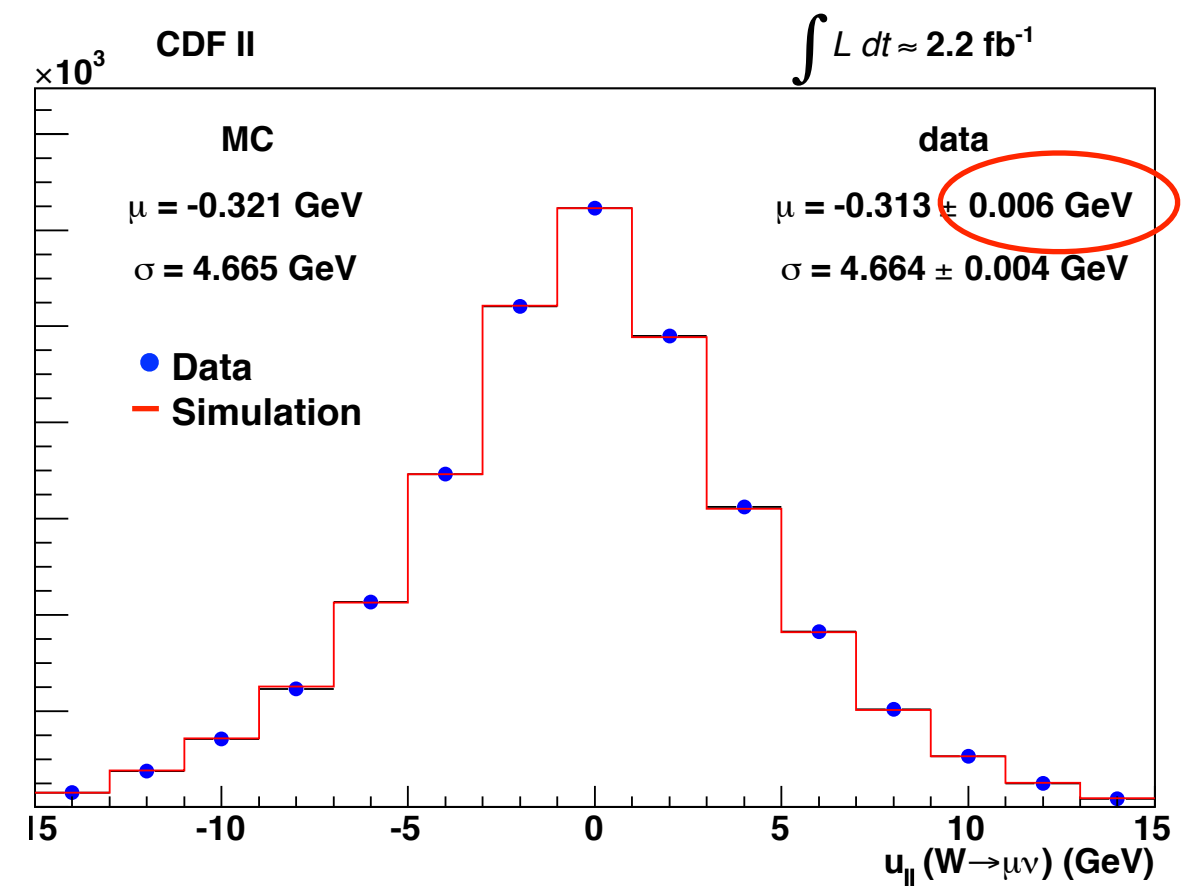
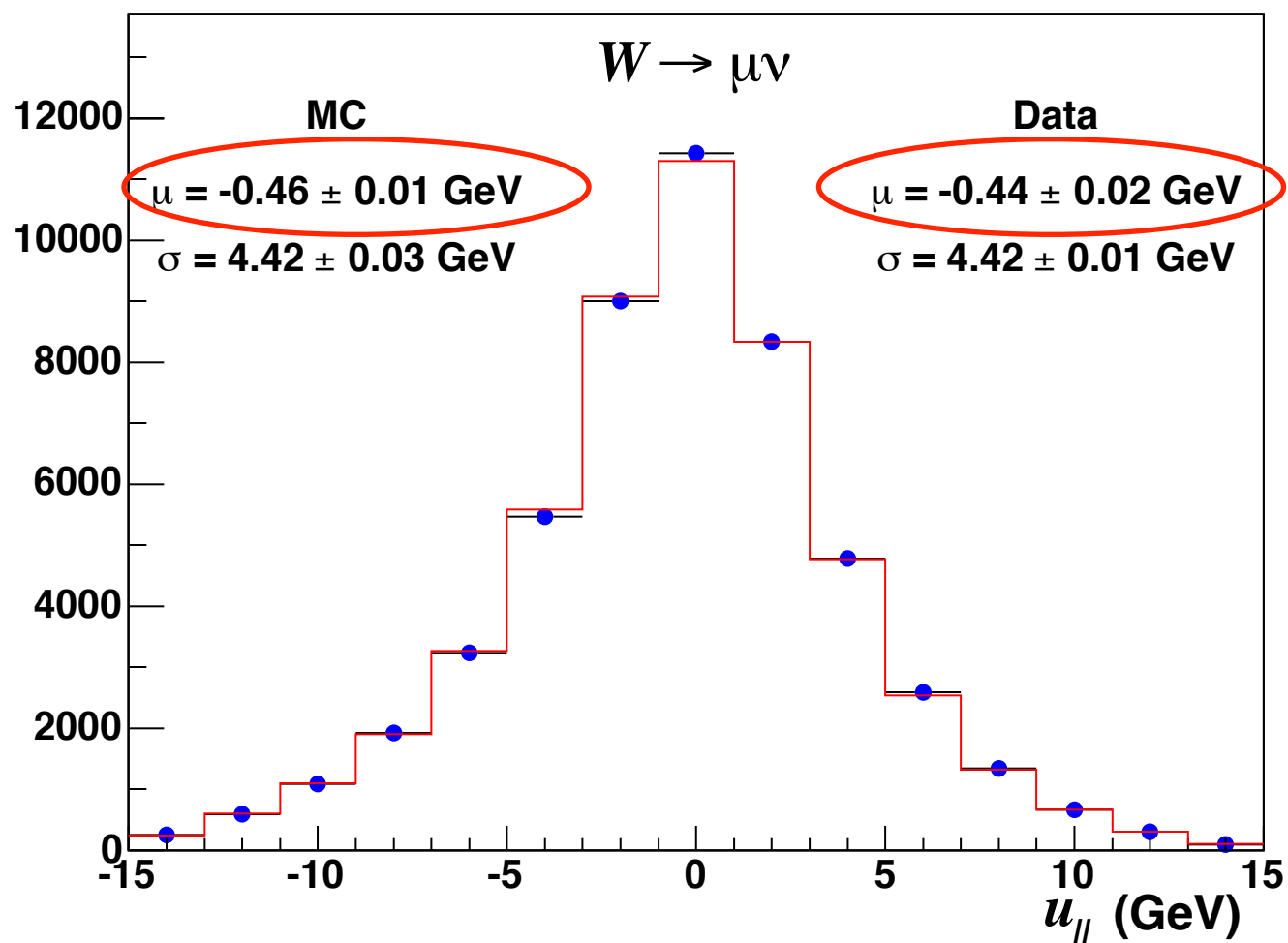
$$m_T \approx 2p_T^l + u_{\parallel}, \quad p_T^{\nu} \approx 2p_T^l + 2u_{\parallel}$$

# Recoil validation

- Test recoil model with W events
  - Compare measured recoil in data to model tuned with Z



$200 \text{ pb}^{-1}$  [PRD77:112001,2008]



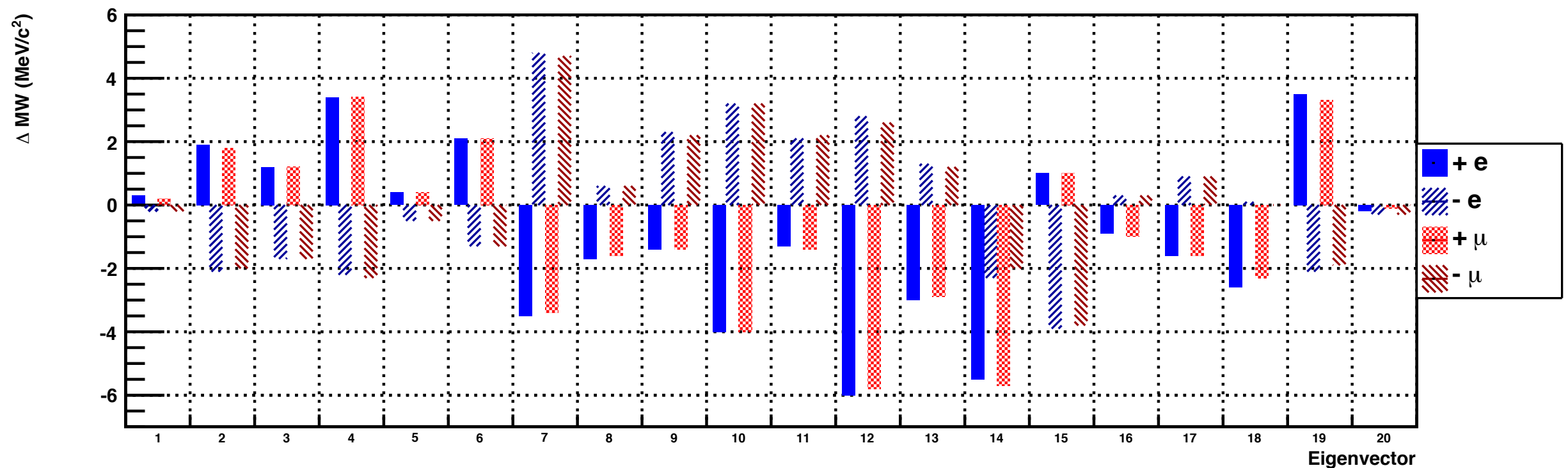
Recoil projection in direction of lepton (muons)

for  $u \ll p_T^l$ :

$$m_T \approx 2p_T^l + u_{||}, \quad p_T^v \approx 2p_T^l + 2u_{||}$$

# Parton distribution functions

- Utilize CTEQ6.6 PDF as default
- Evaluate 90% CL uncertainty eigenvectors for MSTW2008 and CTEQ6.6 (consistent)
- Use 68% CL MSTW2008 to determine systematic  $\Delta M_W = 10 \text{ MeV}$



# Backgrounds

- Electroweak backgrounds ( $Z \rightarrow \ell\ell$ ,  $W \rightarrow \tau\nu$ )
  - Model using standard CDF detector simulated MC
  - Tune recoil model and lepton response
- QCD backgrounds (hadronic jets, meson decay-in-flight)
  - Model using control regions in data
- Except  $Z \rightarrow \mu\mu$  (lost forward muon), backgrounds are small
- Include all estimated background shapes in final templates

| Background               | Fraction of W data (%) | $m_T$       | $\Delta m_W$ (MeV) |   |         |   |           |   |
|--------------------------|------------------------|-------------|--------------------|---|---------|---|-----------|---|
|                          |                        |             | $p_T^l$            |   | $p_T^j$ |   | $p_T^\nu$ |   |
| $Z \rightarrow \ell\ell$ | 7.35±0.09              | 0.139±0.014 | 2                  | 1 | 4       | 2 | 5         | 1 |
| $W \rightarrow \tau\nu$  | 0.880±0.004            | 0.93±0.01   | 0                  | 1 | 0       | 1 | 0         | 1 |
| QCD                      | 0.035±0.025            | 0.39±0.14   | 1                  | 4 | 1       | 2 | 1         | 4 |
| Decay-in-flight          | 0.24±0.02              |             | 1                  |   | 3       |   | 1         |   |
| Cosmic Rays              | 0.02±0.02              |             | 1                  |   | 1       |   | 1         |   |
| <i>Total</i>             |                        |             | 3                  | 4 | 5       | 3 | 6         | 4 |

|           |
|-----------|
| muons     |
| electrons |

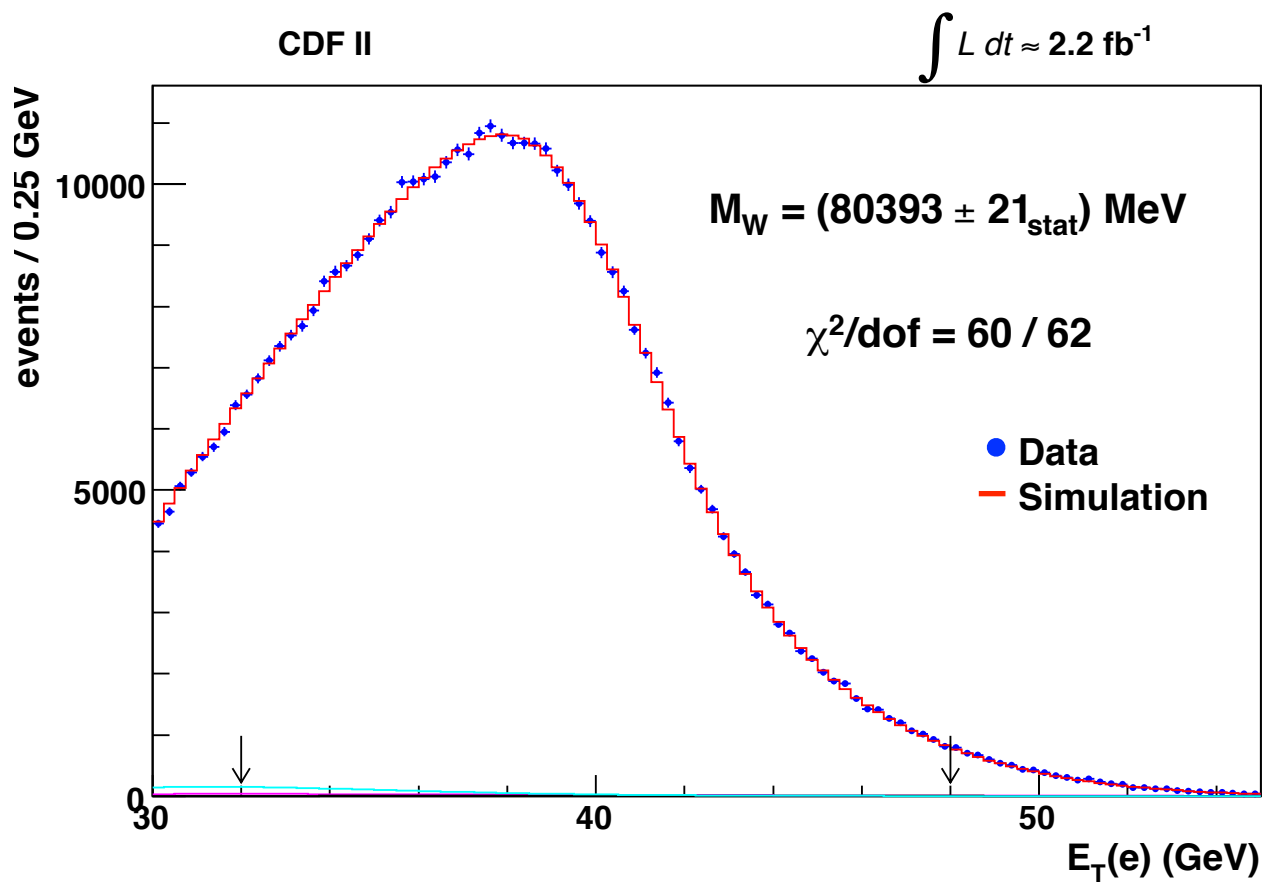
# Results

# A word on blinding

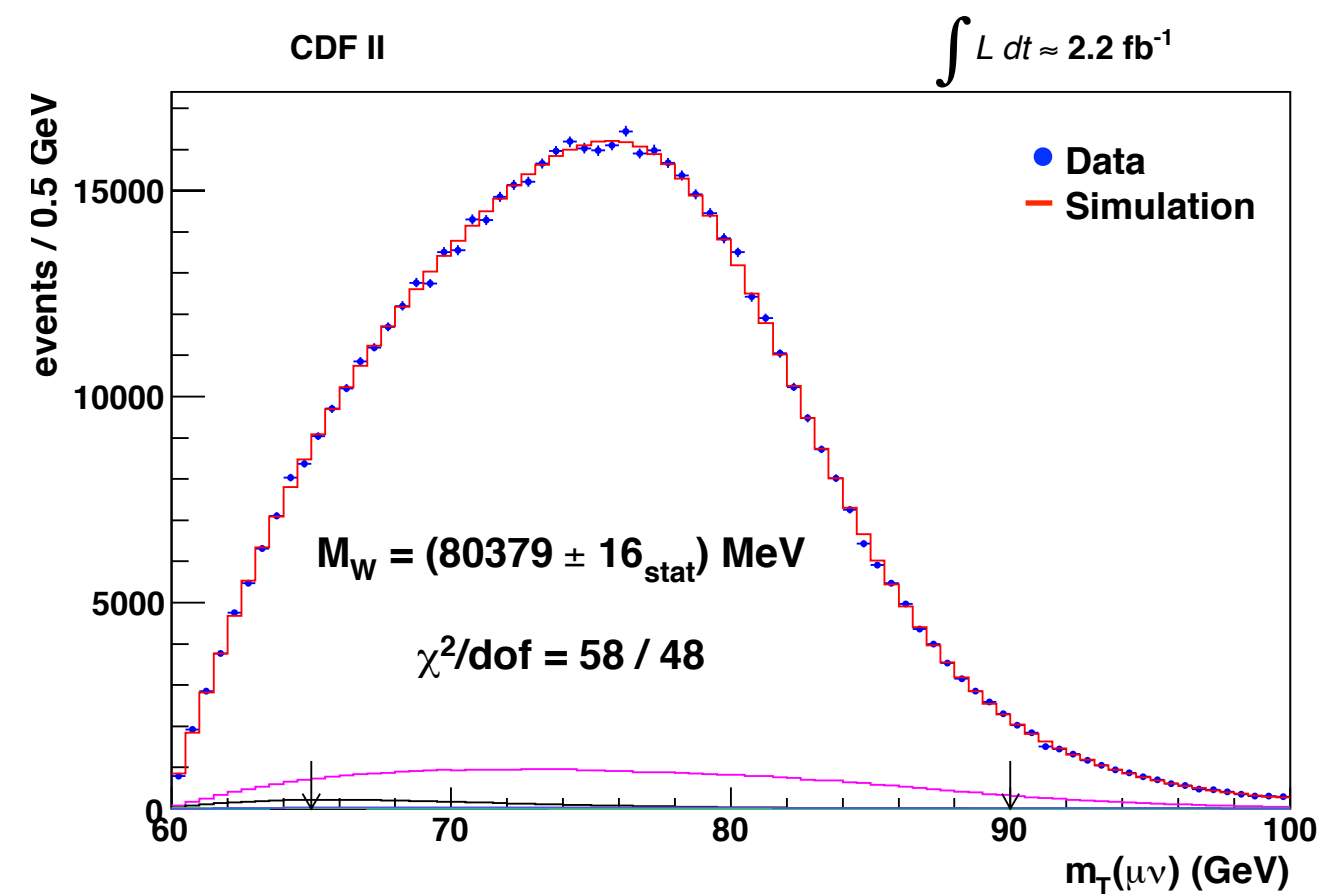
---

- During development of analysis, all fits **blinded** with random offset from  $[-75, 75]$  MeV
  - Common offset applied to all six mass fits
    - Allows for comparison and cross-check
  - During calibration of energy scales, separate offset applied to Z mass fits
- Blinding offset removed only after analysis frozen
  - No changes made since removal

# Example mass fits



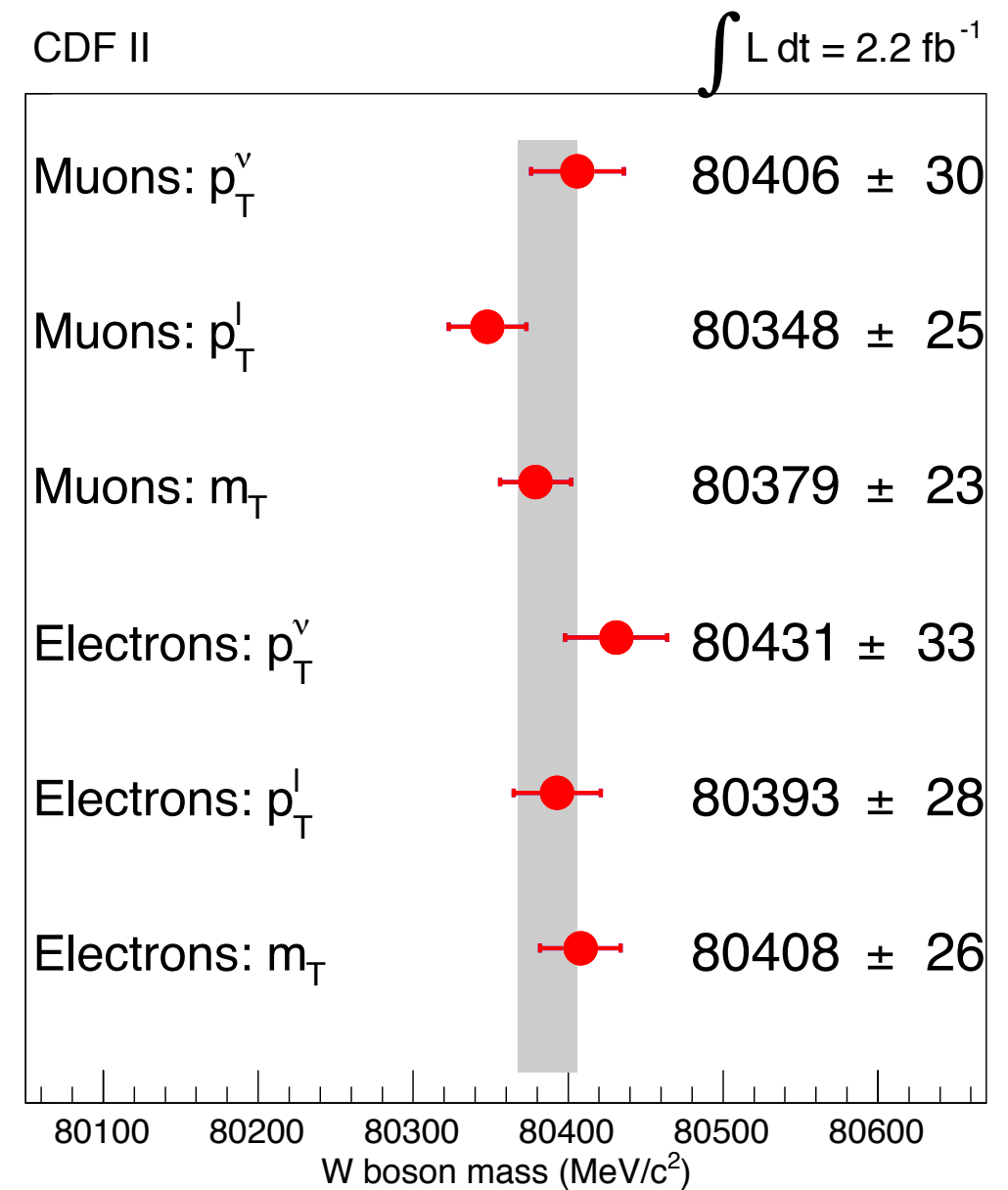
$p_T^l$ : electrons



$m_T$ : muons

# All fits

| Fit                                  | Fit result (MeV)                                  | $\chi^2/\text{dof}$ |
|--------------------------------------|---------------------------------------------------|---------------------|
| $W \rightarrow e\nu$ ( $m_T$ )       | $80408 \pm 19_{\text{stat}} \pm 18_{\text{syst}}$ | 52/48               |
| $W \rightarrow e\nu$ ( $p_T^l$ )     | $80393 \pm 21_{\text{stat}} \pm 19_{\text{syst}}$ | 60/62               |
| $W \rightarrow e\nu$ ( $p_T^\nu$ )   | $80431 \pm 25_{\text{stat}} \pm 22_{\text{syst}}$ | 71/62               |
| $W \rightarrow \mu\nu$ ( $m_T$ )     | $80379 \pm 16_{\text{stat}} \pm 16_{\text{syst}}$ | 58/48               |
| $W \rightarrow \mu\nu$ ( $p_T^l$ )   | $80348 \pm 18_{\text{stat}} \pm 18_{\text{syst}}$ | 54/62               |
| $W \rightarrow \mu\nu$ ( $p_T^\nu$ ) | $80406 \pm 22_{\text{stat}} \pm 20_{\text{syst}}$ | 79/62               |



# Combined results

---

Combine using *BLUE*  
L. Lyons, D. Gibaut, and P. Clifford,  
NIM A **270**, 110 (1988).

# Combined results

---

- All electron fits combined

$$M_W = 80406 \pm 25 \text{ MeV}, \chi^2/\text{dof} = 1.4/2 \text{ (49\%)}$$

Combine using *BLUE*  
L. Lyons, D. Gibaut, and P. Clifford,  
NIM A **270**, 110 (1988).

# Combined results

---

- All electron fits combined

$$M_W = 80406 \pm 25 \text{ MeV}, \chi^2/\text{dof} = 1.4/2 \text{ (49\%)}$$

- All muon fits combined

$$M_W = 80374 \pm 22 \text{ MeV}, \chi^2/\text{dof} = 4/2 \text{ (12\%)}$$

Combine using *BLUE*  
L. Lyons, D. Gibaut, and P. Clifford,  
NIM A **270**, 110 (1988).

# Combined results

---

- All electron fits combined

$$M_W = 80406 \pm 25 \text{ MeV}, \chi^2/\text{dof} = 1.4/2 (49\%)$$

- All muon fits combined

$$M_W = 80374 \pm 22 \text{ MeV}, \chi^2/\text{dof} = 4/2 (12\%)$$

- All fits combined

$$M_W = 80387 \pm 19 \text{ MeV}, \chi^2/\text{dof} = 6.6/5 (25\%)$$

Combine using *BLUE*  
L. Lyons, D. Gibaut, and P. Clifford,  
NIM A **270**, 110 (1988).

# Combined uncertainties

---

| Source                   | Uncertainty<br>2.2 fb <sup>-1</sup> (MeV) |
|--------------------------|-------------------------------------------|
| Lepton energy scale      | 7                                         |
| Lepton energy resolution | 2                                         |
| Recoil energy scale      | 4                                         |
| Recoil energy resolution | 4                                         |
| Lepton removal           | 2                                         |
| Backgrounds              | 3                                         |
| p <sub>T</sub> (W) model | 5                                         |
| PDFs                     | 10                                        |
| QED radiation            | 4                                         |
| <i>Total systematics</i> | <i>15</i>                                 |
| W statistics             | 12                                        |
| <b>Total</b>             | <b>19</b>                                 |

$$M_W = 80387 \pm 12_{\text{stat}} \pm 15_{\text{syst}} \text{ MeV}/c^2$$

# Combined uncertainties

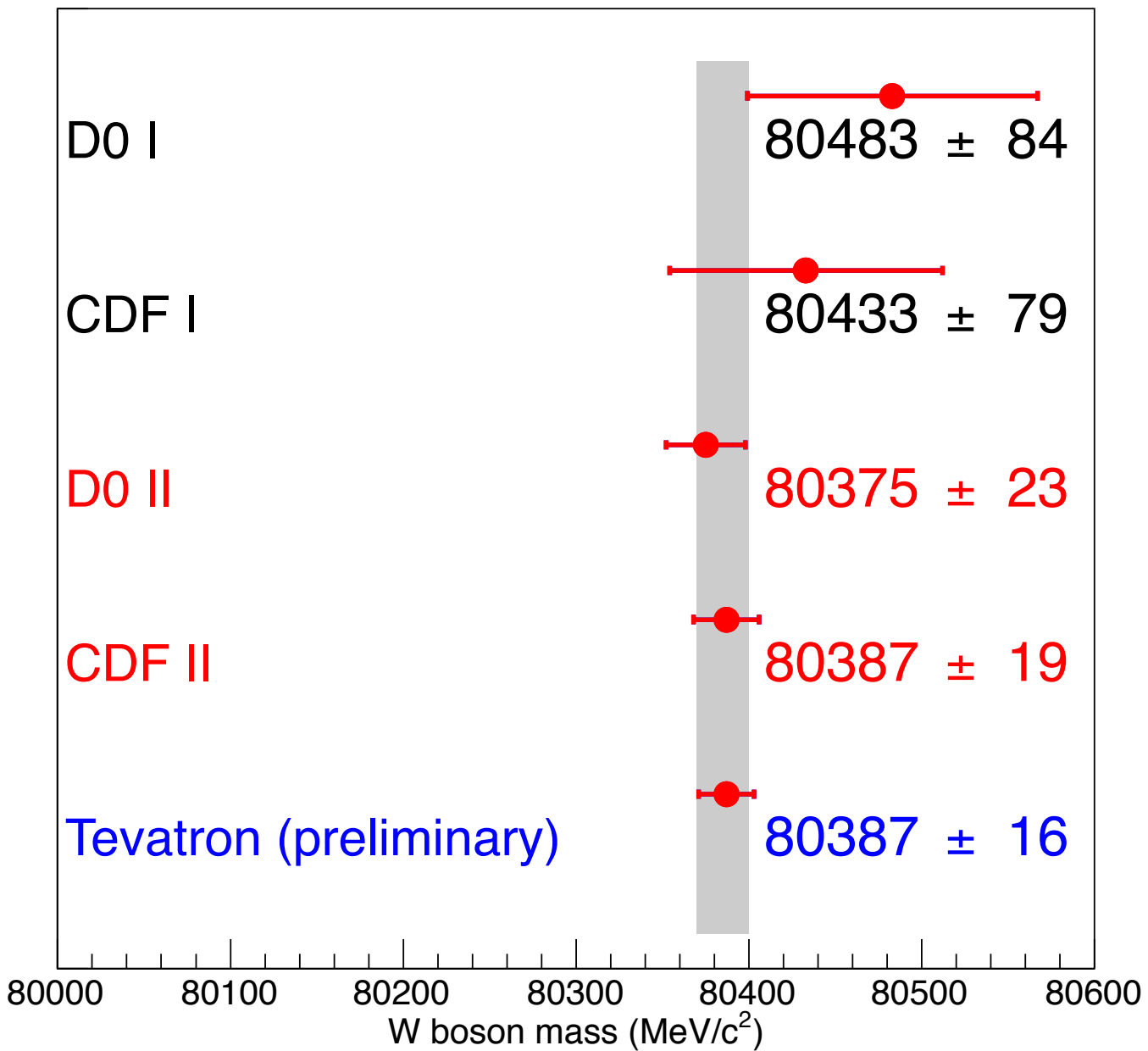
Statistics limited by  
control data

Theory based  
(external inputs)

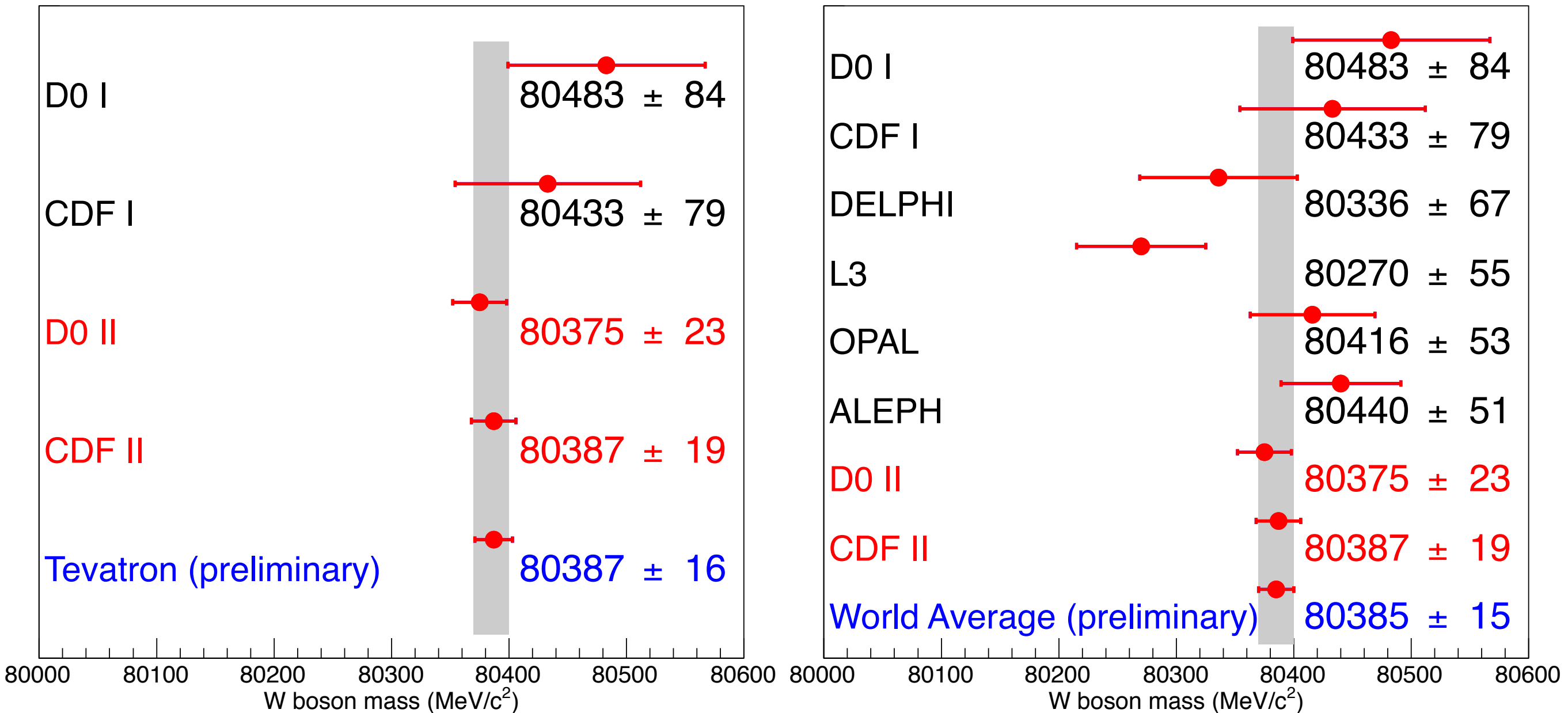
| Source                   | Uncertainty<br>2.2 fb <sup>-1</sup> (MeV) | Uncertainty<br>0.2 fb <sup>-1</sup> (MeV) |
|--------------------------|-------------------------------------------|-------------------------------------------|
| Lepton energy scale      | 7                                         | 23                                        |
| Lepton energy resolution | 2                                         | 4                                         |
| Recoil energy scale      | 4                                         | 8                                         |
| Recoil energy resolution | 4                                         | 10                                        |
| Lepton removal           | 2                                         | 6                                         |
| Backgrounds              | 3                                         | 6                                         |
| p <sub>T</sub> (W) model | 5                                         | 4                                         |
| PDFs                     | 10                                        | 11                                        |
| QED radiation            | 4                                         | 10                                        |
| <i>Total systematics</i> | <i>15</i>                                 | <i>34</i>                                 |
| W statistics             | 12                                        | 34                                        |
| <b>Total</b>             | <b>19</b>                                 | <b>48</b>                                 |

$$M_W = 80387 \pm 12_{\text{stat}} \pm 15_{\text{syst}} \text{ MeV}/c^2$$

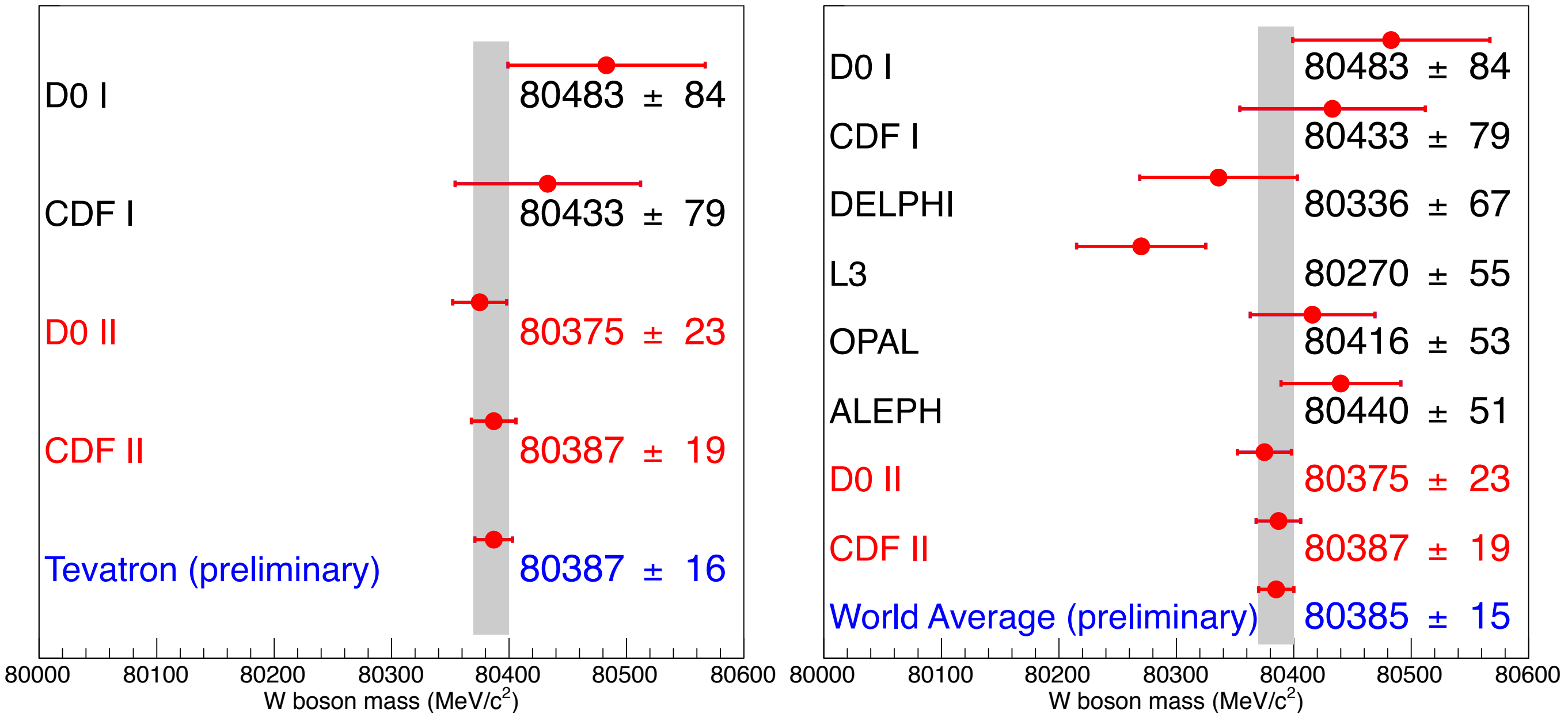
# Tevatron and world combinations



# Tevatron and world combinations



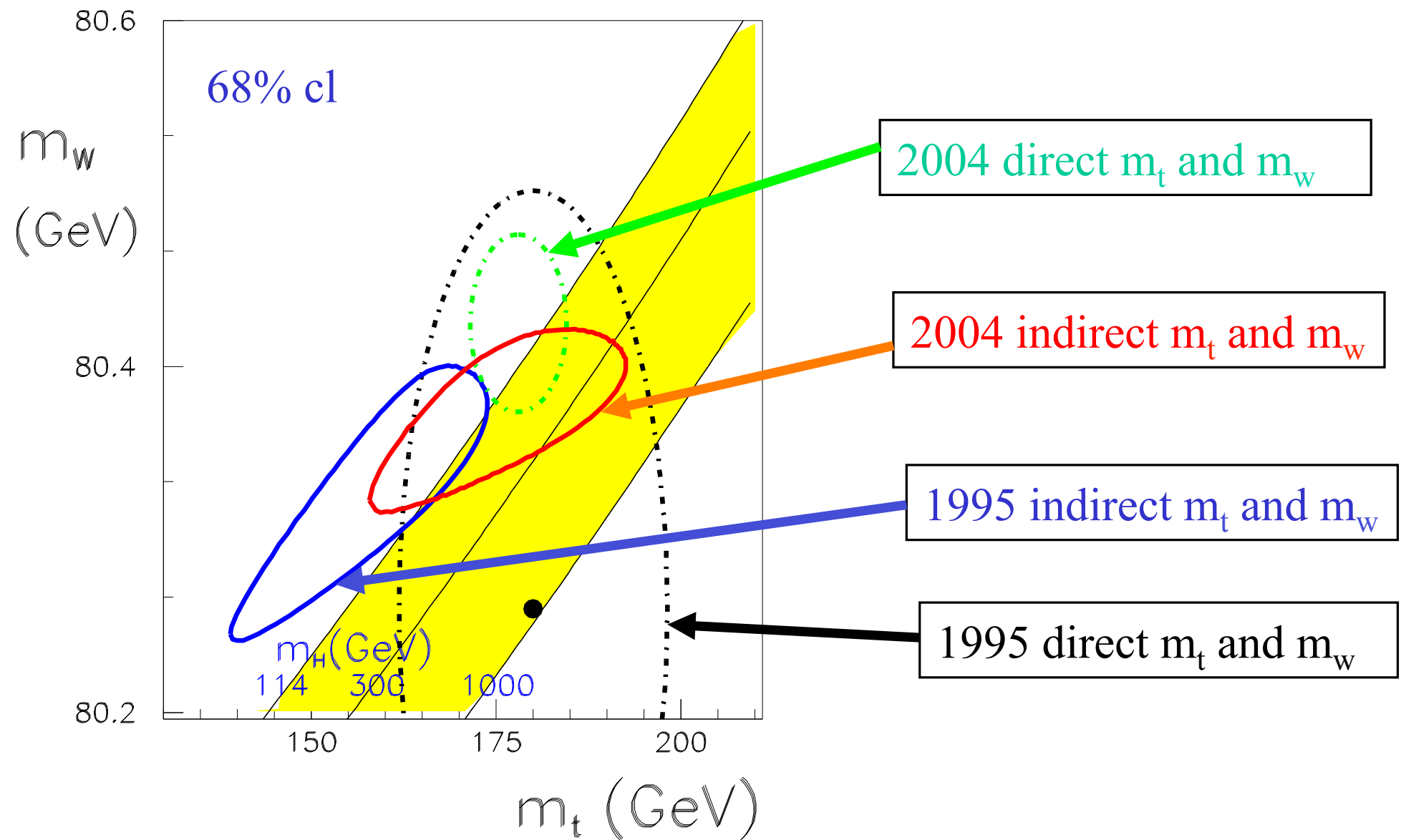
# Tevatron and world combinations



*nb:* 2009 world average  
 $M_W = 80399 \pm 23 \text{ MeV}$

*New CDF measurement  
 significantly exceeds  
 precision of all previous  
 measurements of  $M_W$   
 combined!*

# Sidetrack down memory lane



**P. Renton, ICHEP 2004**

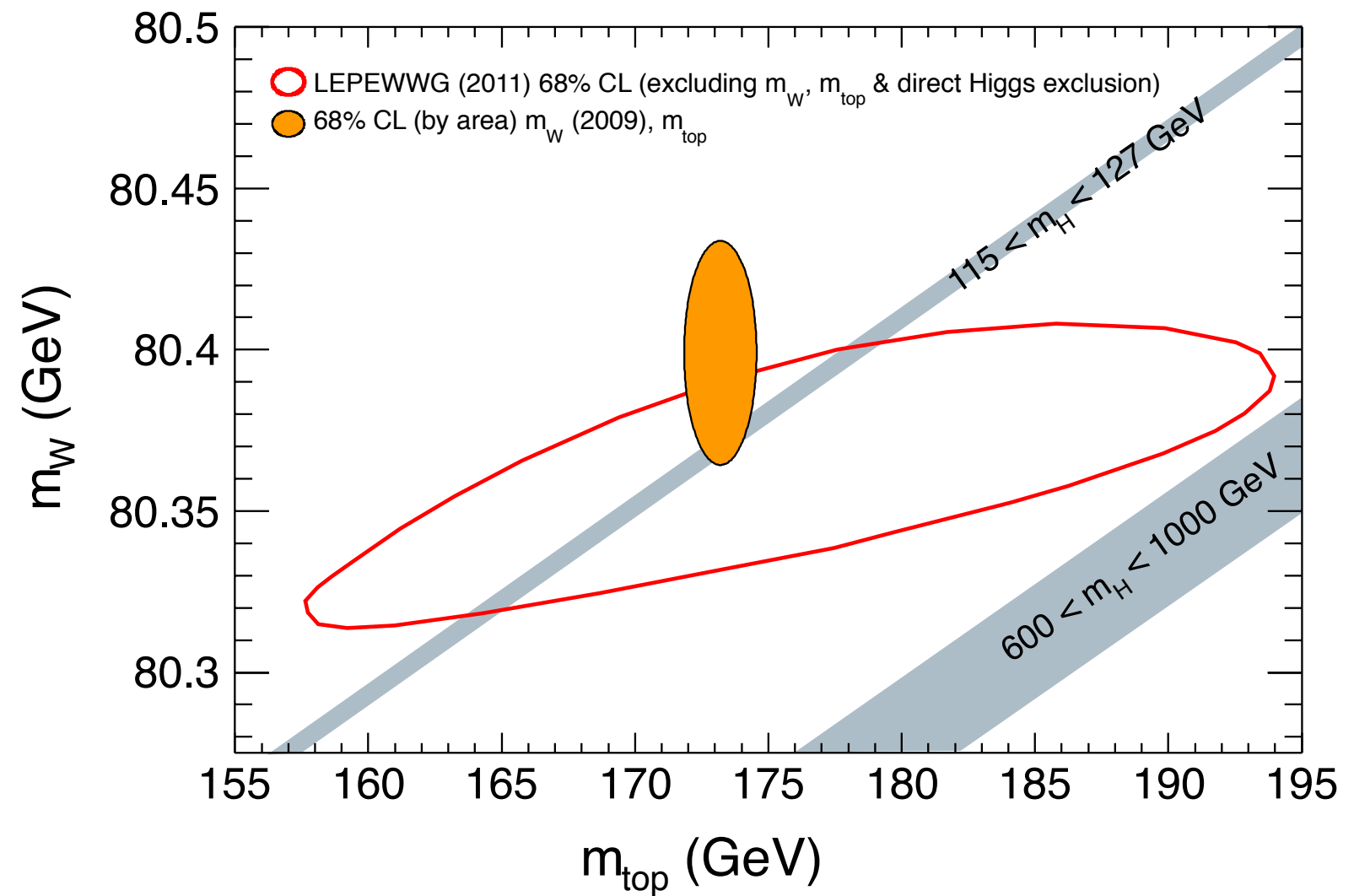
# Standard model fit

With  $M_W = 80399 \pm 23$  MeV

$M_H = 92^{+34}_{-26}$  GeV

$M_H < 161$  GeV @95% CL

*LEPEWWG/ZFitter*



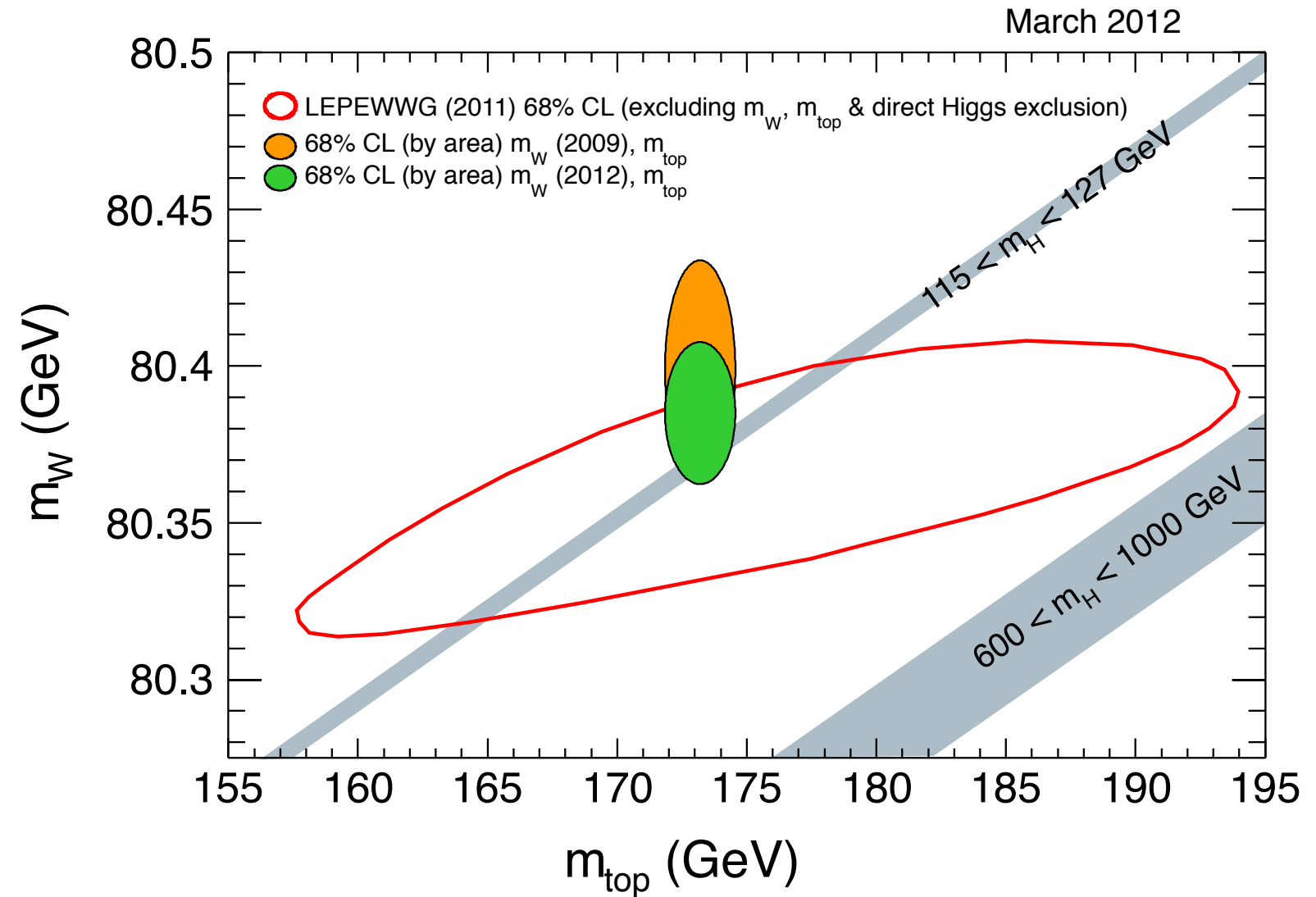
# Standard model fit

With  $M_W = 80385 \pm 15$  MeV

$M_H = 94^{+29}_{-24}$  GeV

$M_H < 152$  GeV @95% CL

*LEPEWWG/ZFitter*



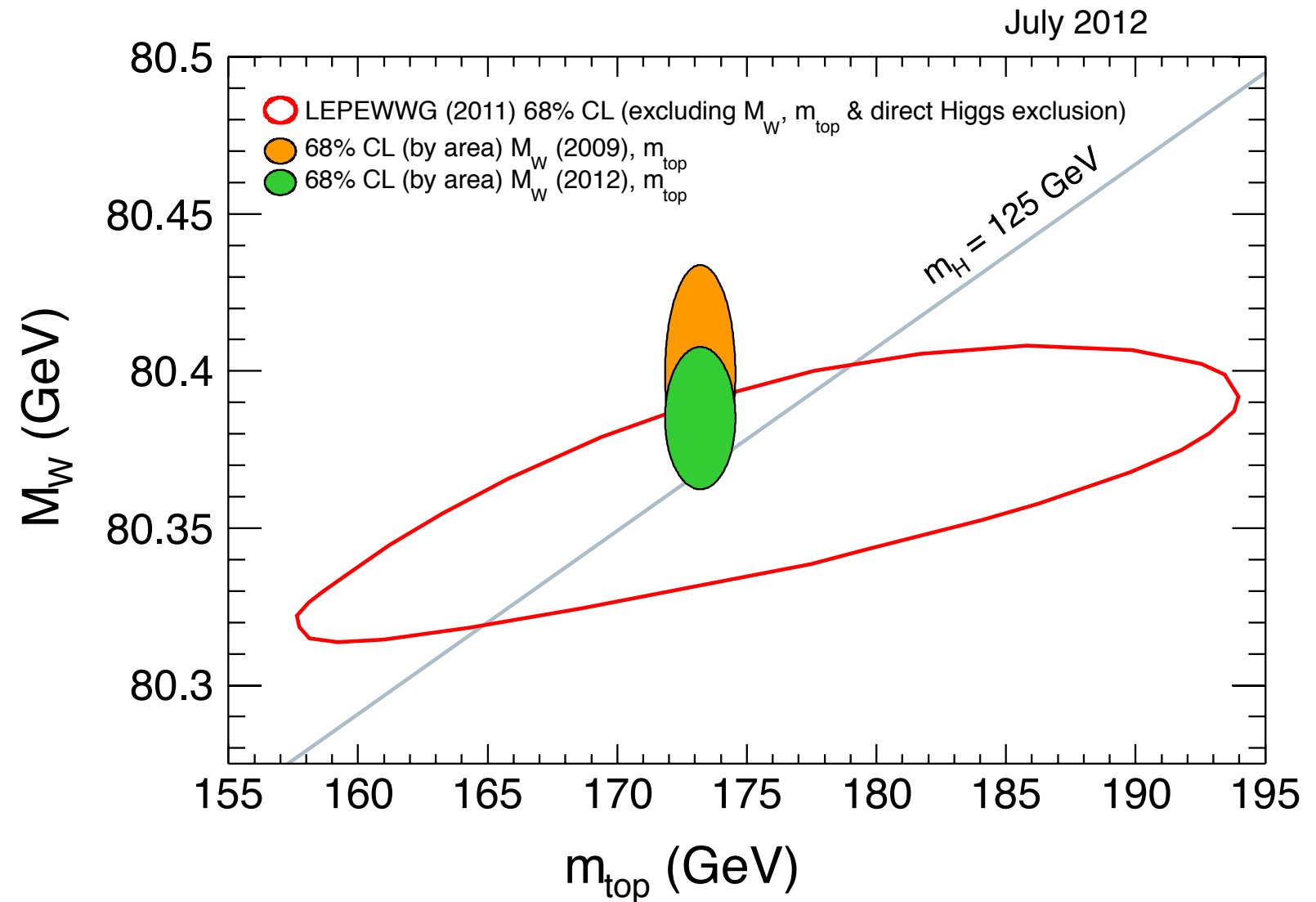
# Standard model fit

With  $M_W = 80385 \pm 15$  MeV

$M_H = 94^{+29}_{-24}$  GeV

$M_H < 152$  GeV @95% CL

*LEPEWWG/ZFitter*



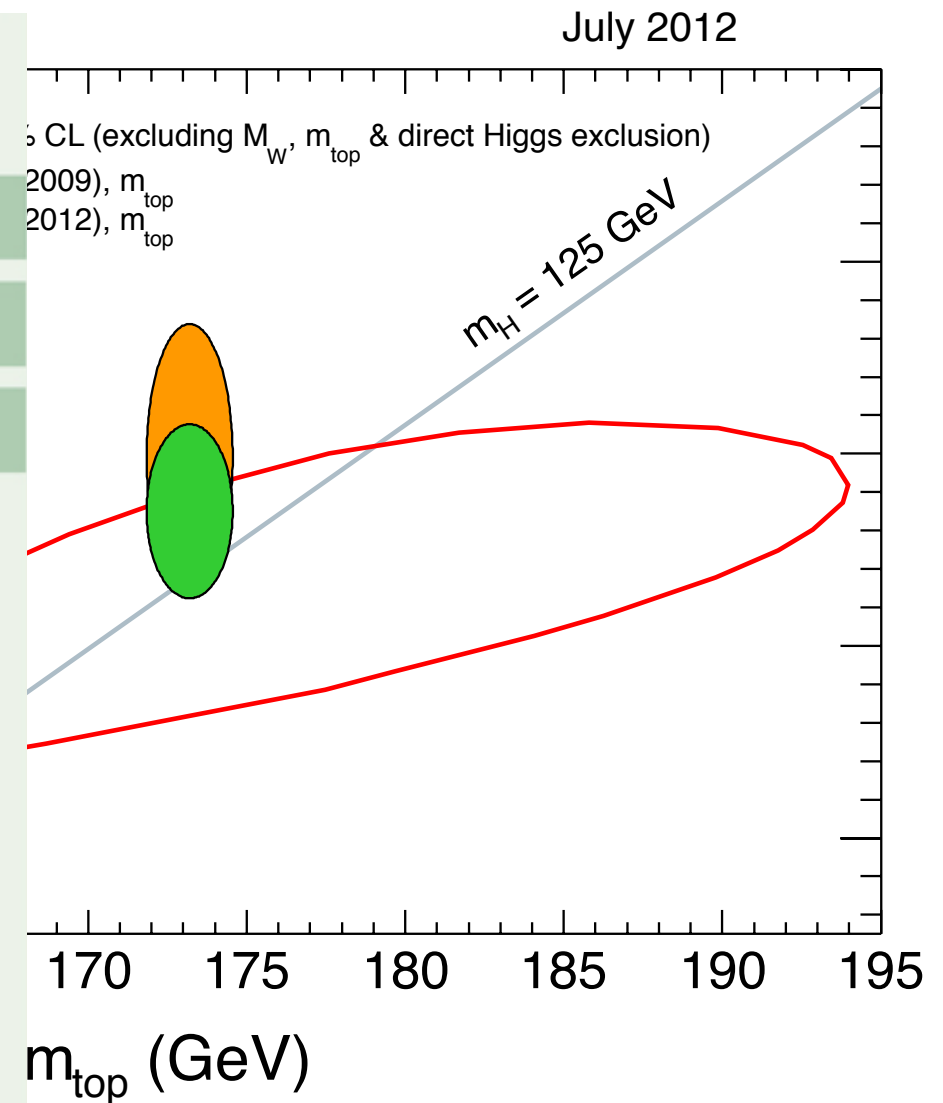
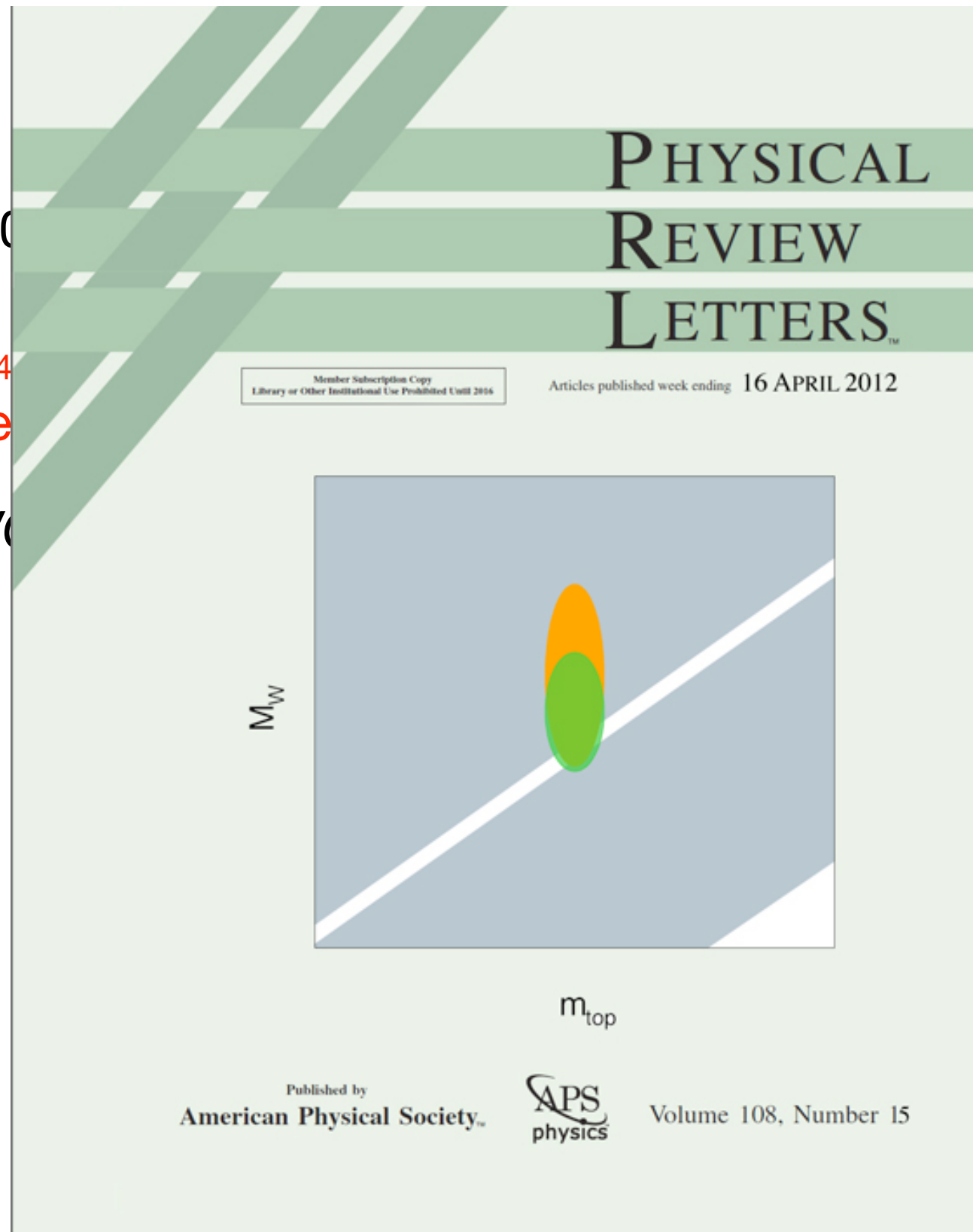
# Standard model fit

With  $M_W = 80.385 \pm 0.015$  GeV

$M_H = 94^{+29}_{-24}$  GeV

$M_H < 152$  GeV

LEPEWW

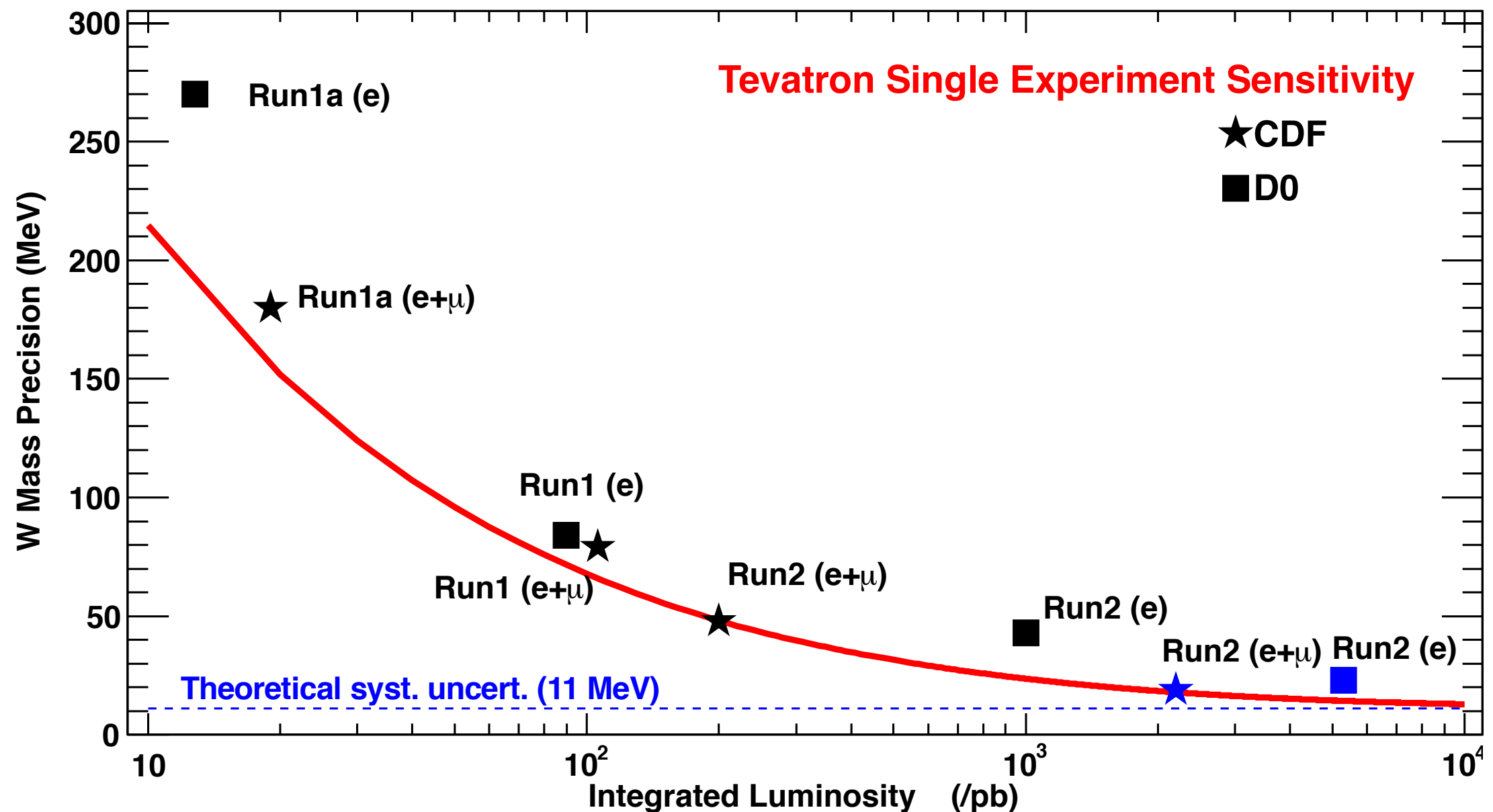


CDF: PRL **105**, 151803 (2012)

DØ: PRL **105**, 151804 (2012)

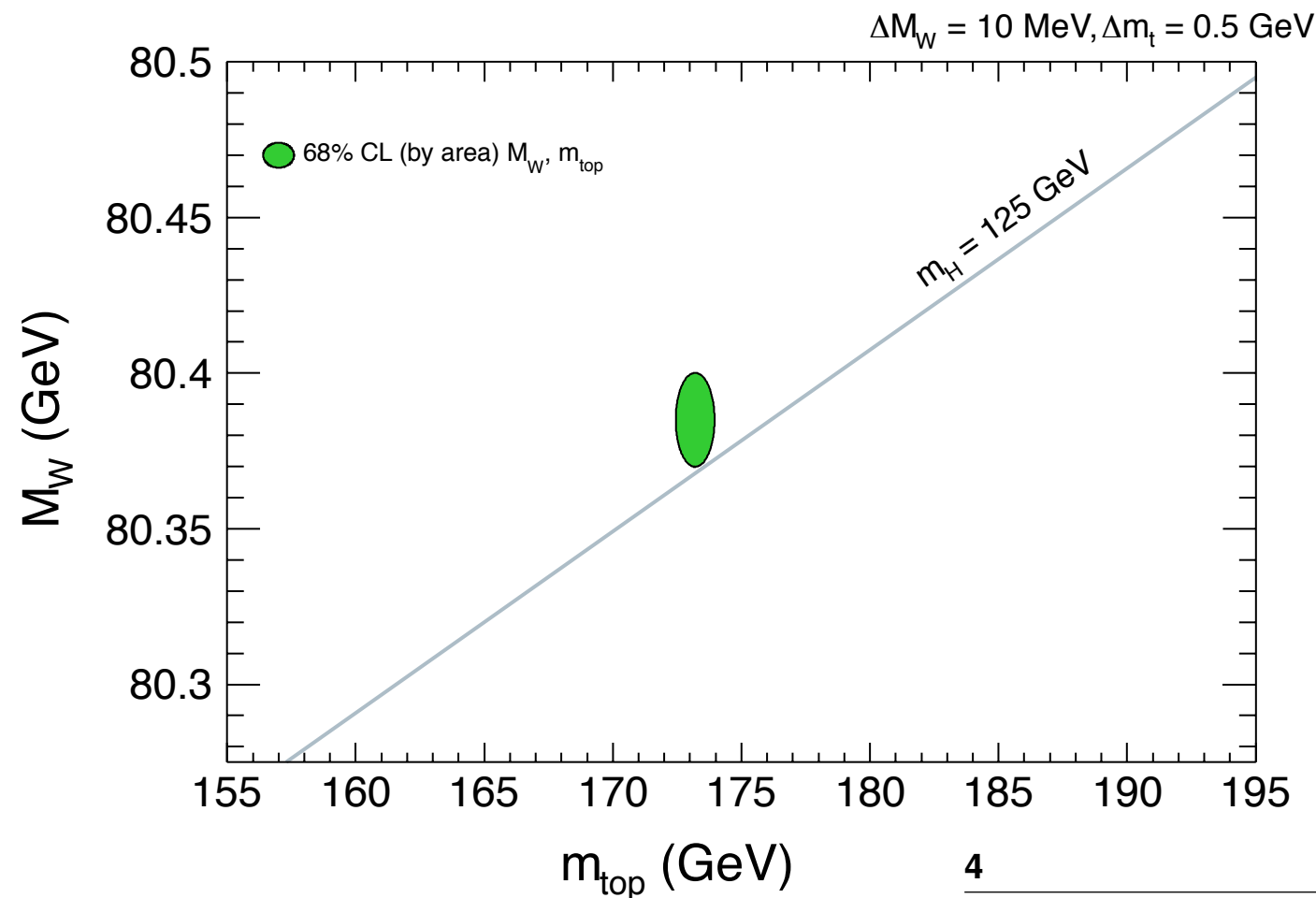
*PRL Editors' Suggestions*

# Uncertainty projections



- Projection assumes PDF+QED errors (11 MeV) fixed
  - Become limiting uncertainty for measurements with full Tevatron dataset

# Where could we be?



Future Tevatron  $m_W$  and  
Tevatron+LHC  $m_t$

or... back to  $e^+e^-$  ?

4

2 The LEP3 Physics case

From **CMS Note 2012/003**  
P. Azzi *et al.*

“Prospective Studies for LEP3  
with the CMS Detector”

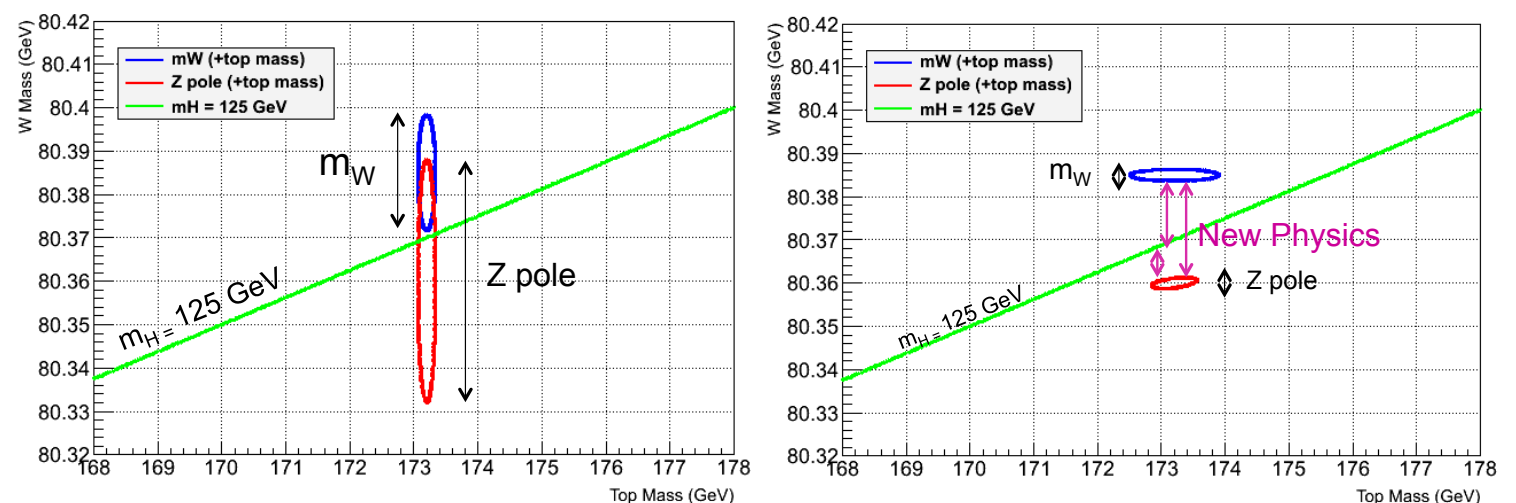


Figure 3: The effect of improving the precision of the top mass measurement by a factor 10 (left), or the precision of the Z pole and the W mass measurements by factors of 25 and 10, respectively (right), in the  $(m_W, m_{\text{top}})$  plane.

# Conclusion

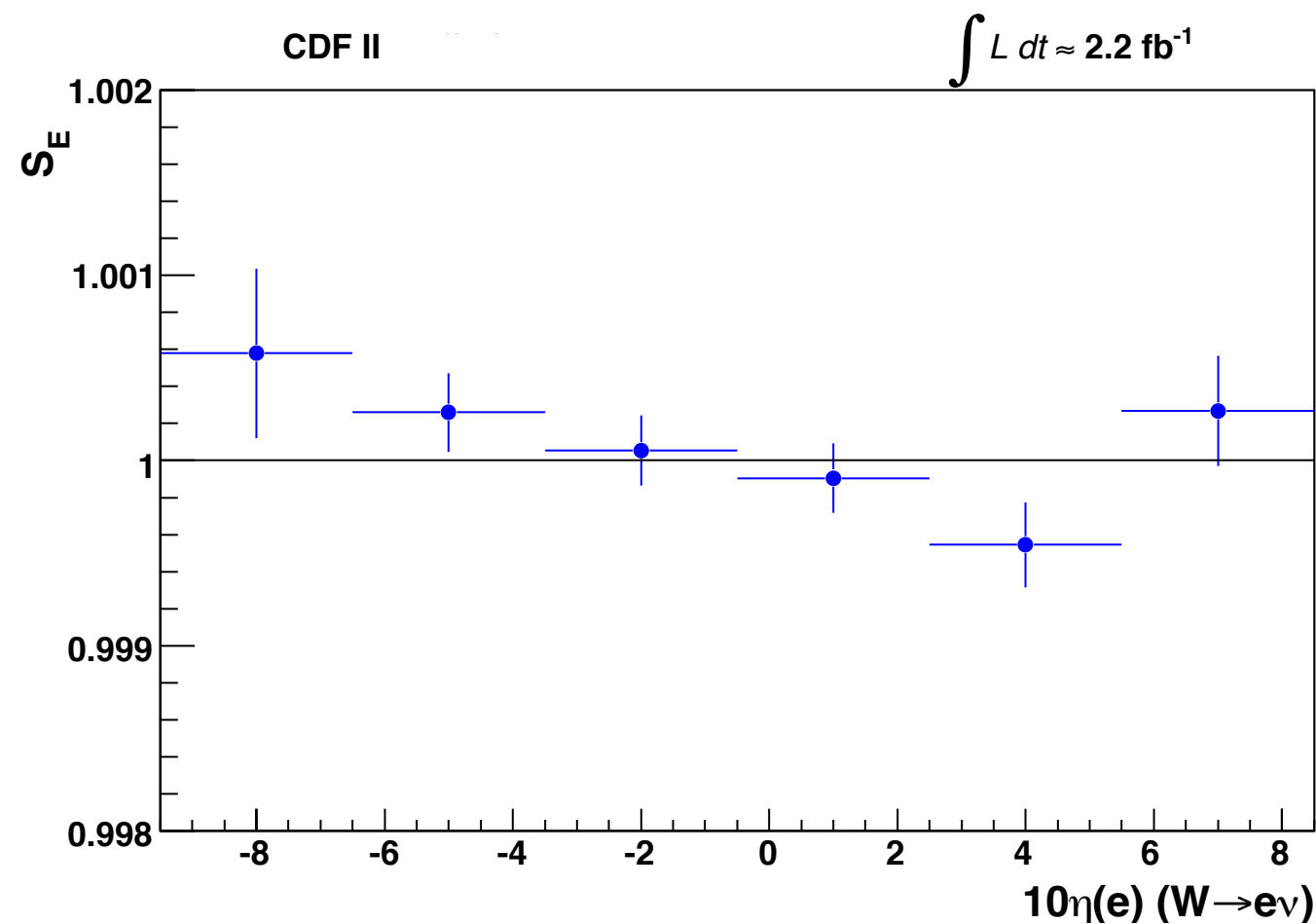
---

- CDF has performed the most precise measurement of the  $W$  boson mass
  - $M_W = 80387 \pm 19 \text{ MeV}$  [*Phys. Rev. Lett.* **105**, 158103]
  - More precise than all previous measurements combined
  - Improves world average uncertainty from 23 MeV to 16 MeV
- New combinations (including DØ [*Phys. Rev. Lett.* **105**, 158104])
  - **Tevatron:**  $M_W = 80387 \pm 16 \text{ MeV}$  (TeVWWG, preliminary)
  - **World:**  $M_W = 80385 \pm 15 \text{ MeV}$  (TeVWWG, preliminary)
- Results in SM fits of  $M_H < 152 \text{ GeV}$  @ 95% CL
  - Previously  $M_H < 161 \text{ GeV}$  @ 95% CL
  - $M_W$  still is the limiting factor in  $M_H$  prediction
- Full Tevatron dataset ( $\sim 10 \text{ fb}^{-1}$ ) on hand
  - $\Delta M_W < 15 \text{ MeV}$  per experiment achievable

Backup

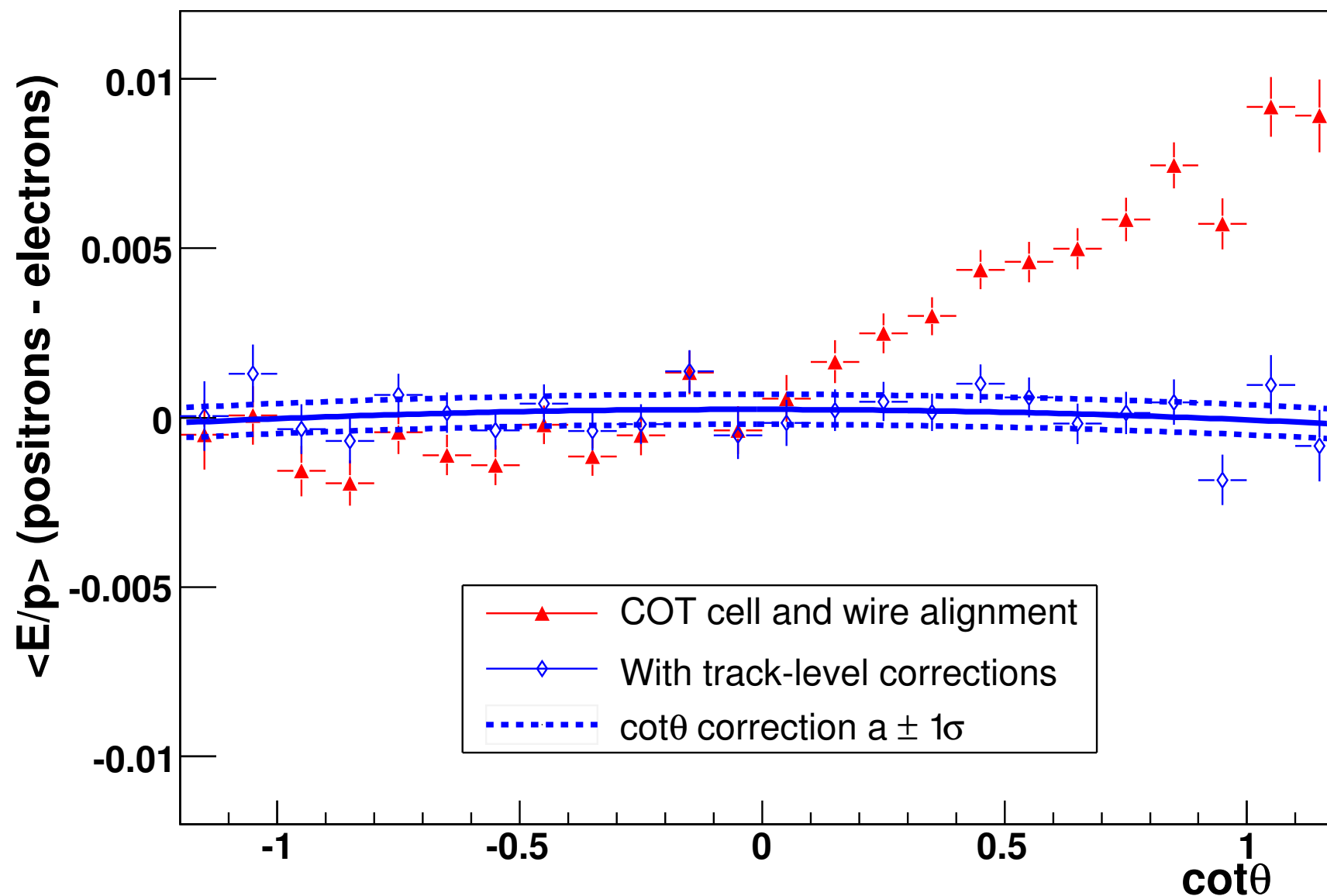
# EM calorimeter spatial uniformity

- Apply tower-by-tower correction to flatten response in eta
  - Response after tuning flat

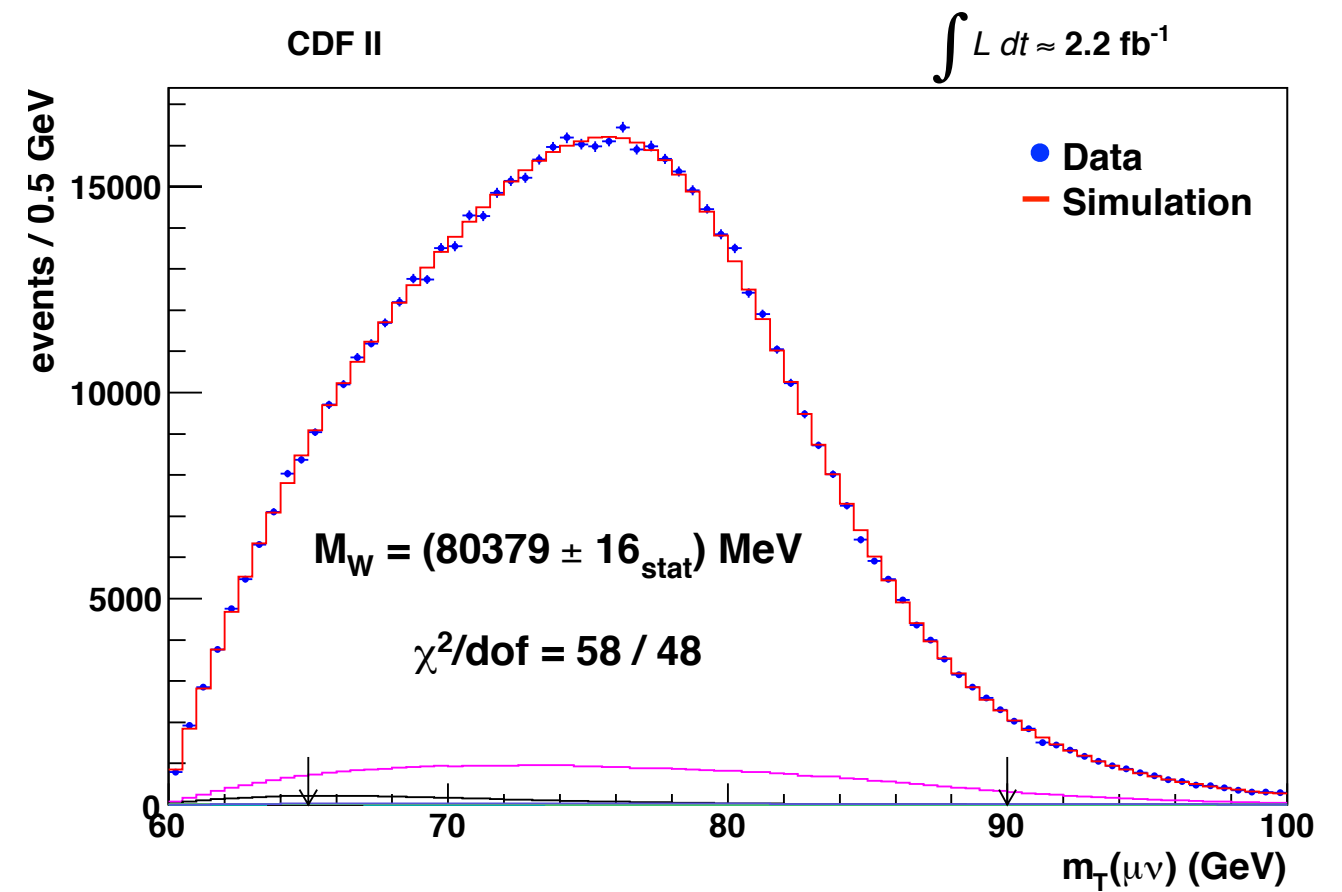
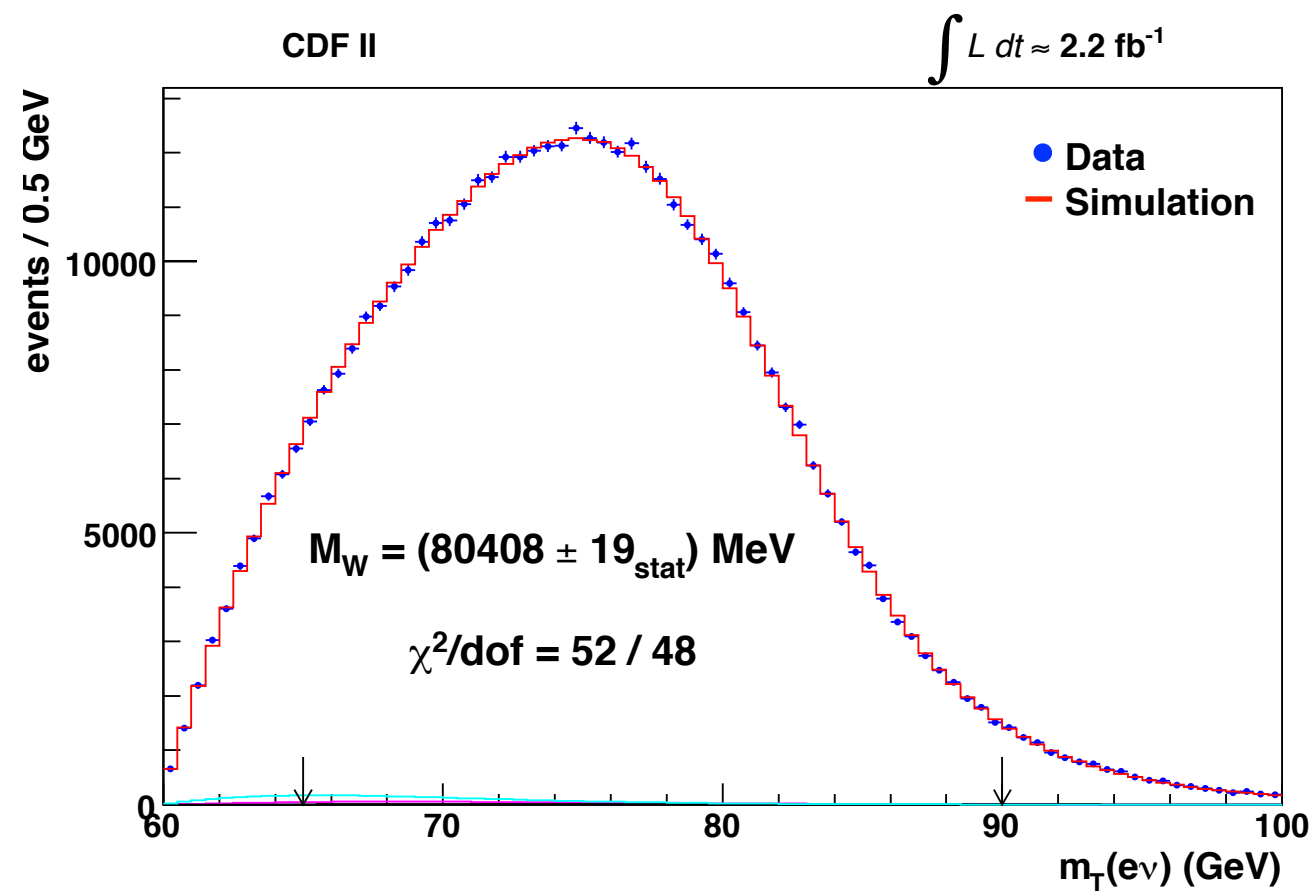


# Residual alignment corrections

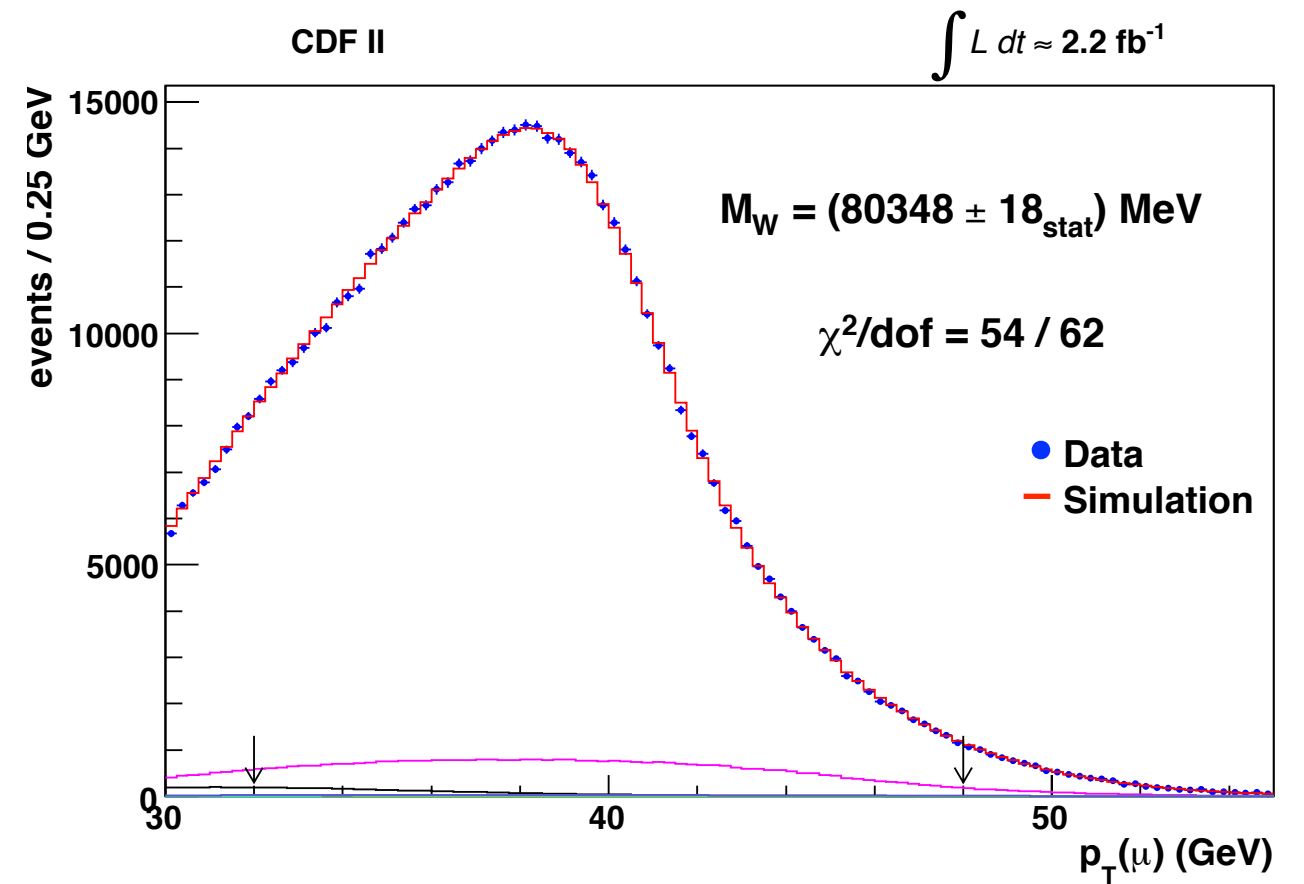
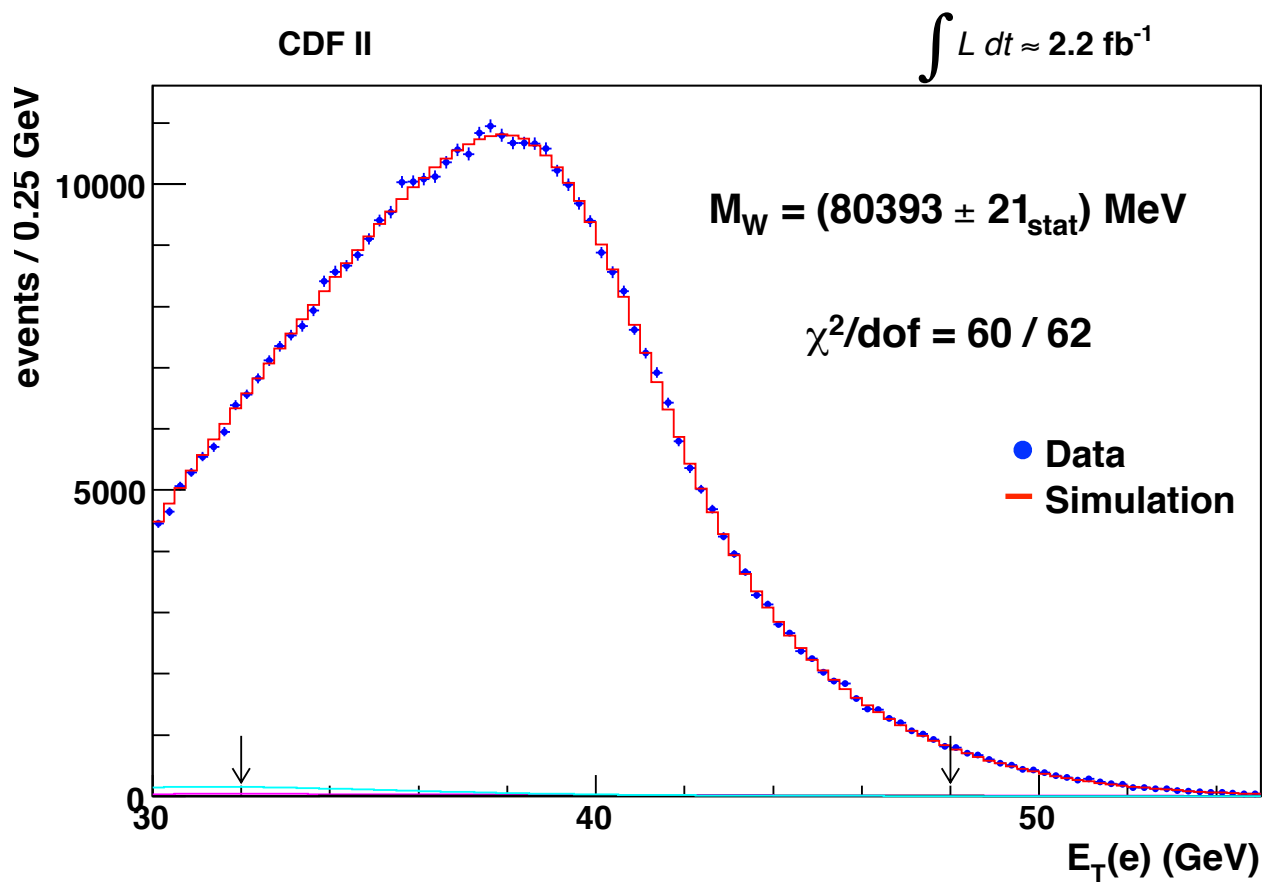
- Some “weakly constrained modes” not corrected by cosmic alignment
- Study these using difference in  $\langle E/p \rangle$  between  $e^+$  and  $e^-$  events
  - Apply correction to alignment based on this difference



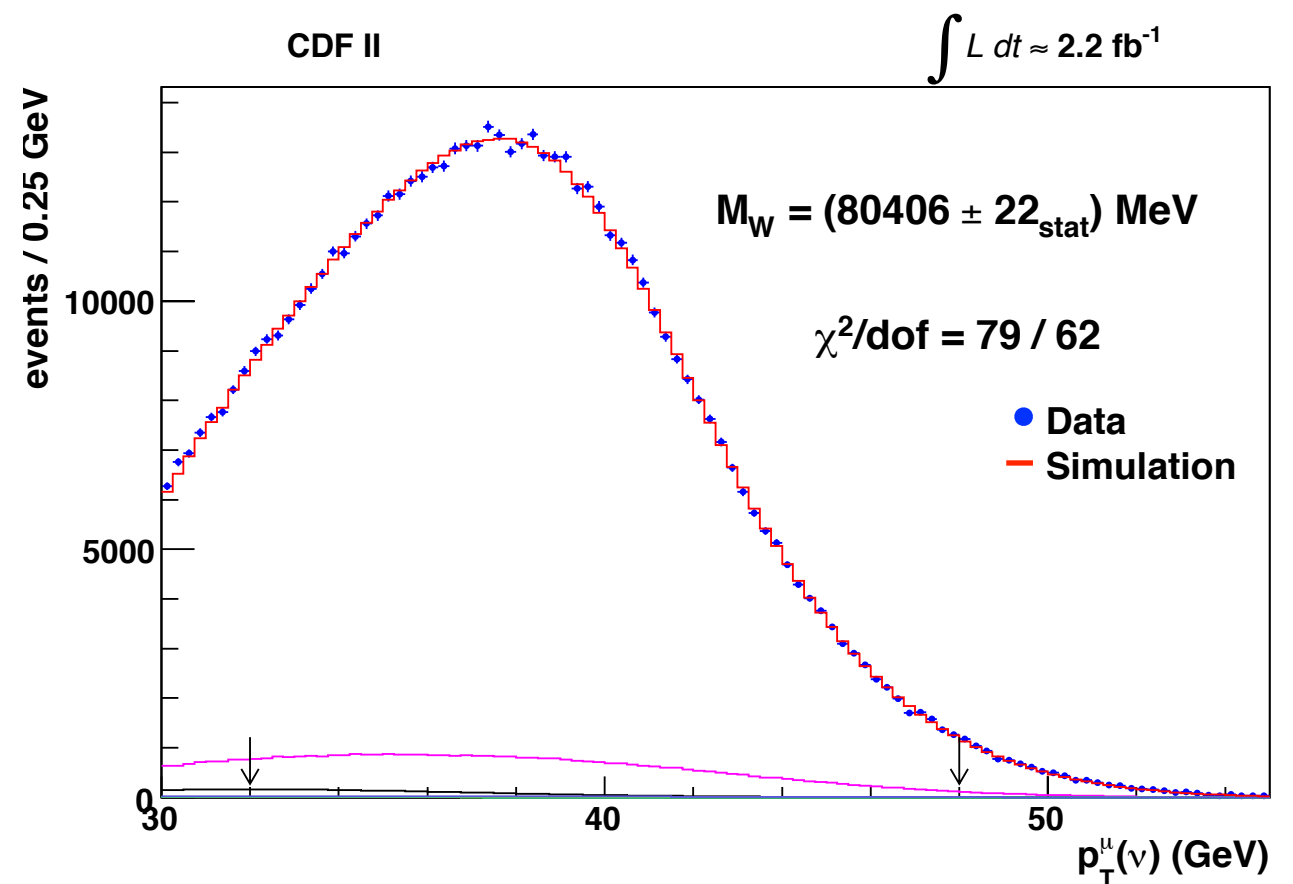
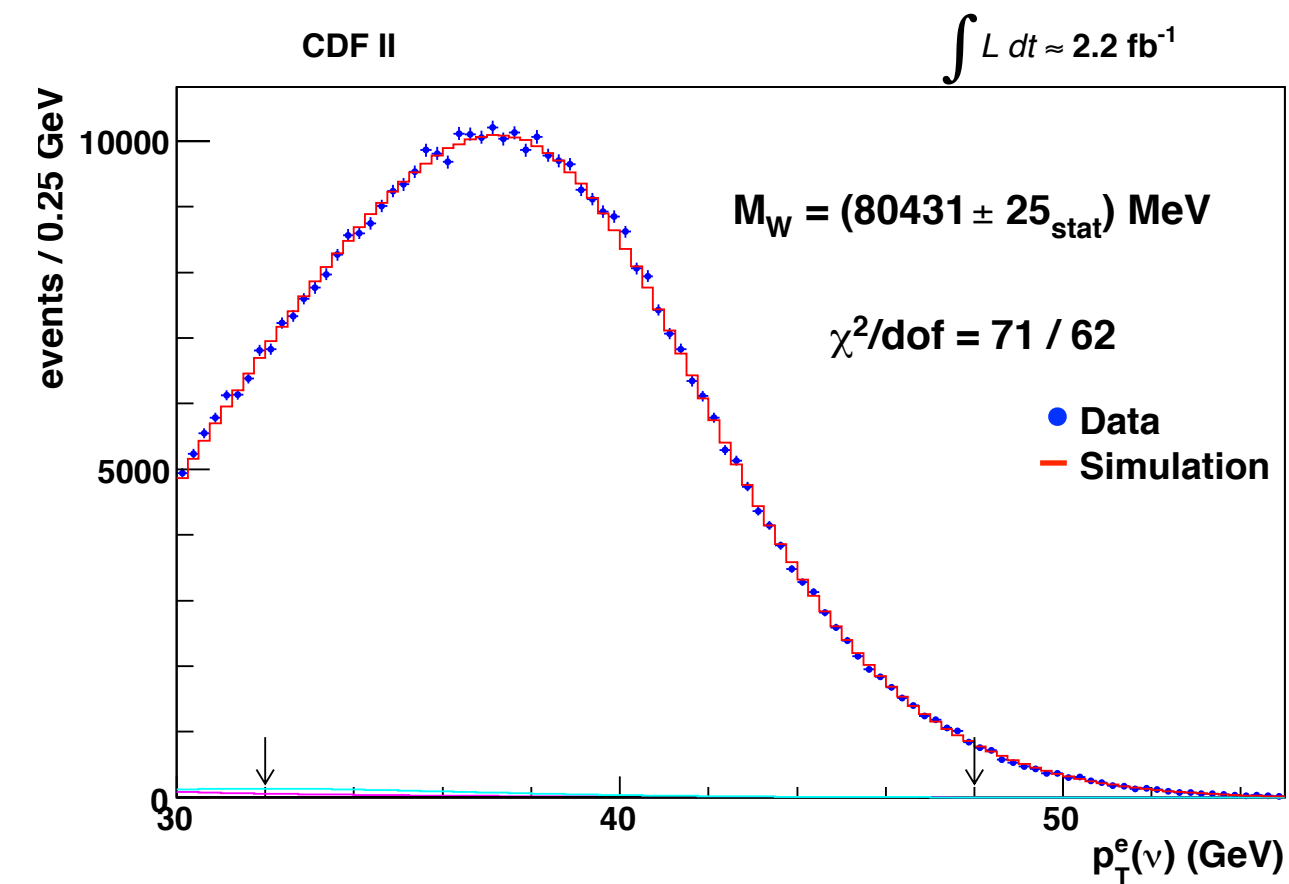
# W mass fits: $m_T$



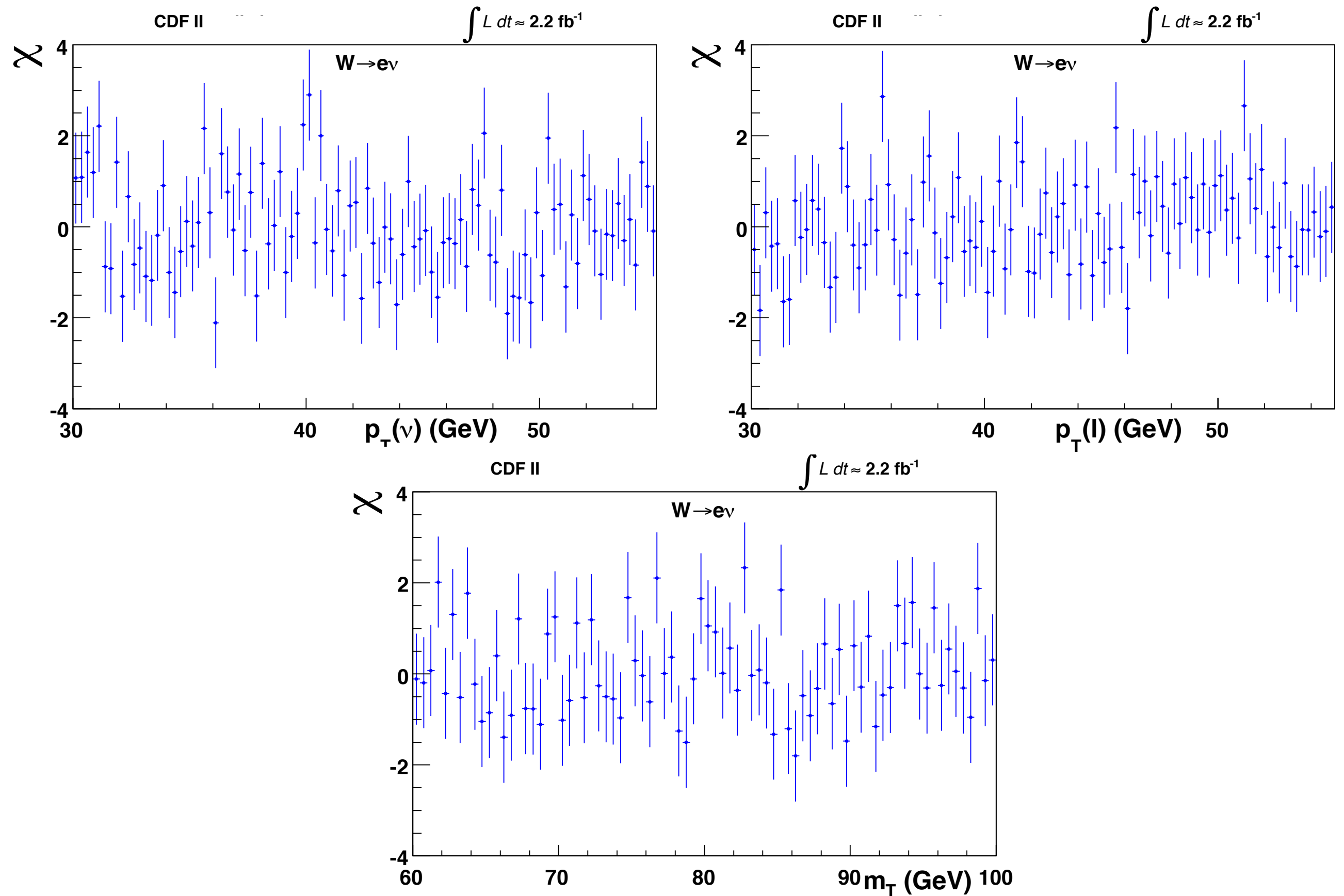
# W mass fits: lepton $p_T$



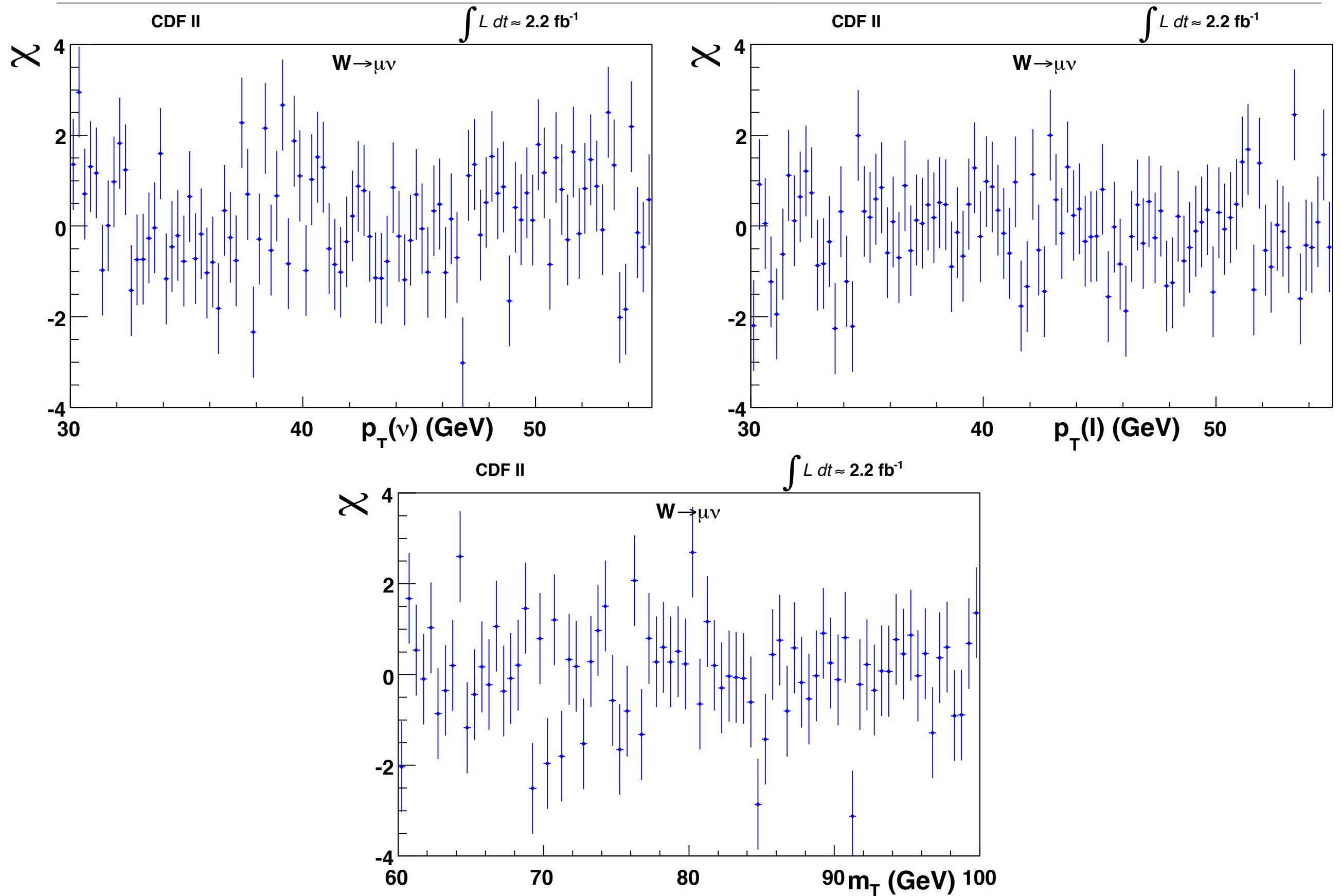
# W mass fits: neutrino $p_T$



# Electron fit residuals

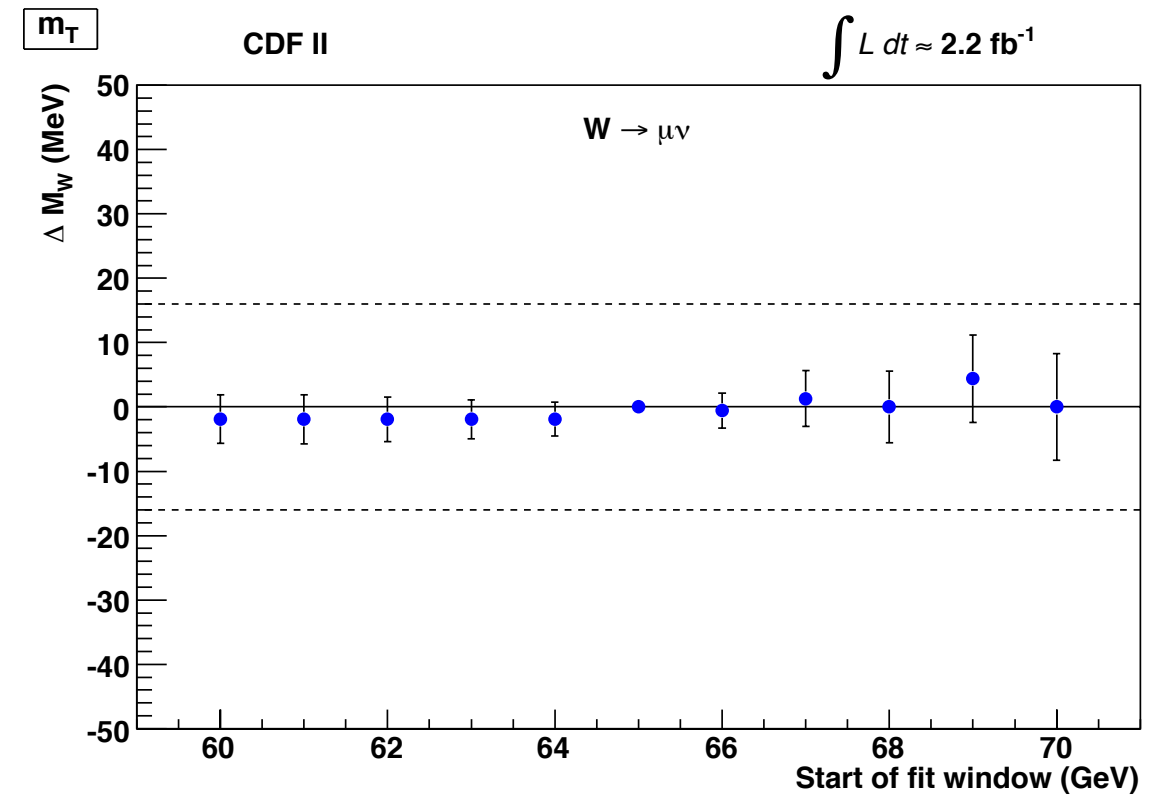
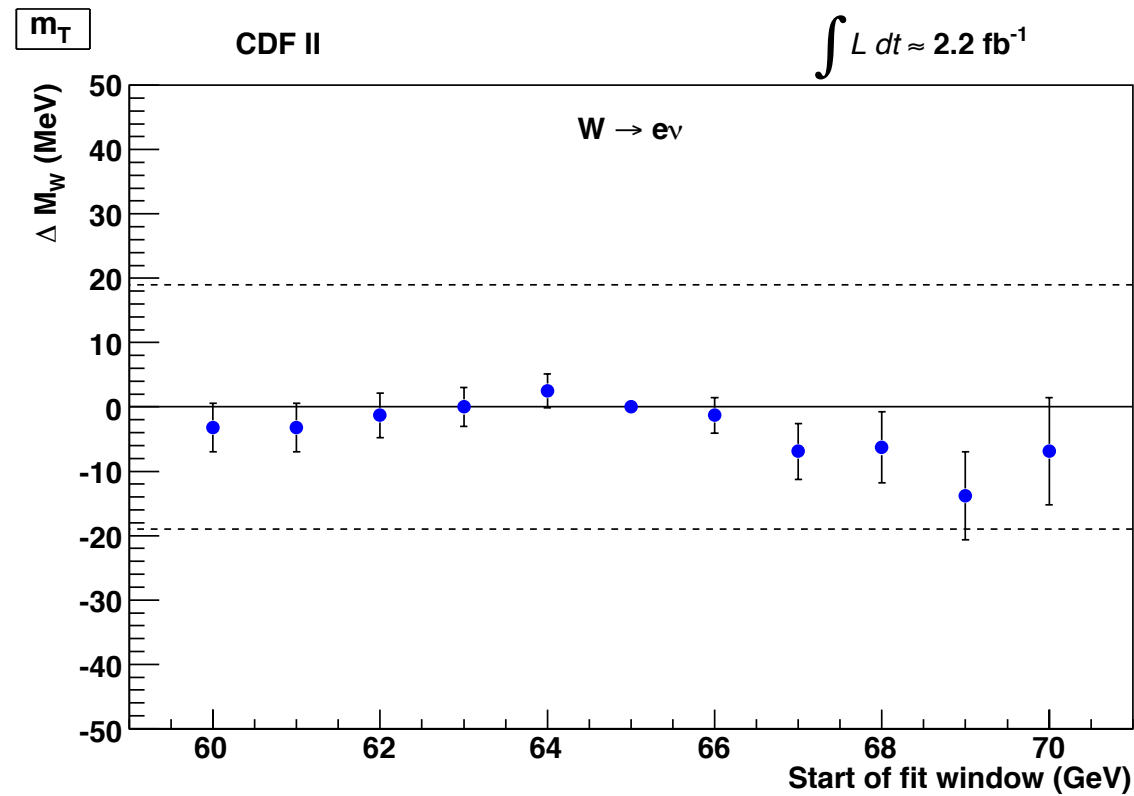


# Muon fit residuals

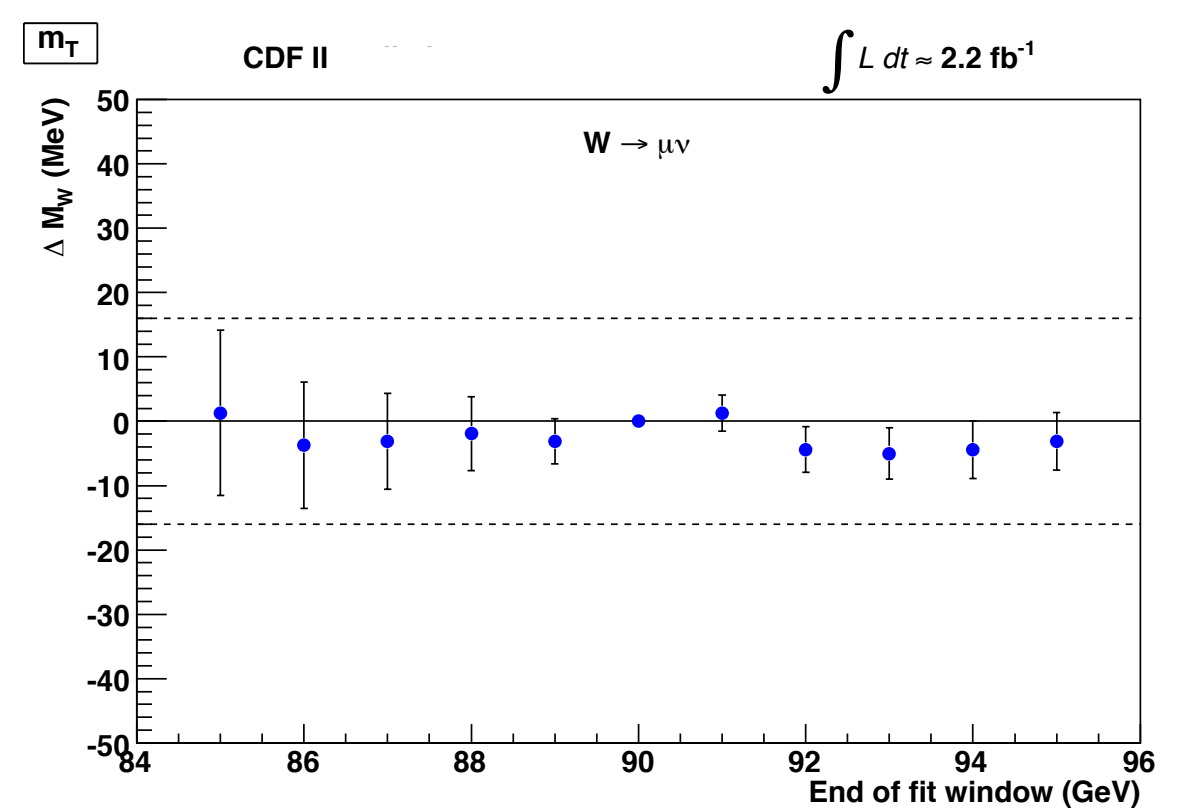
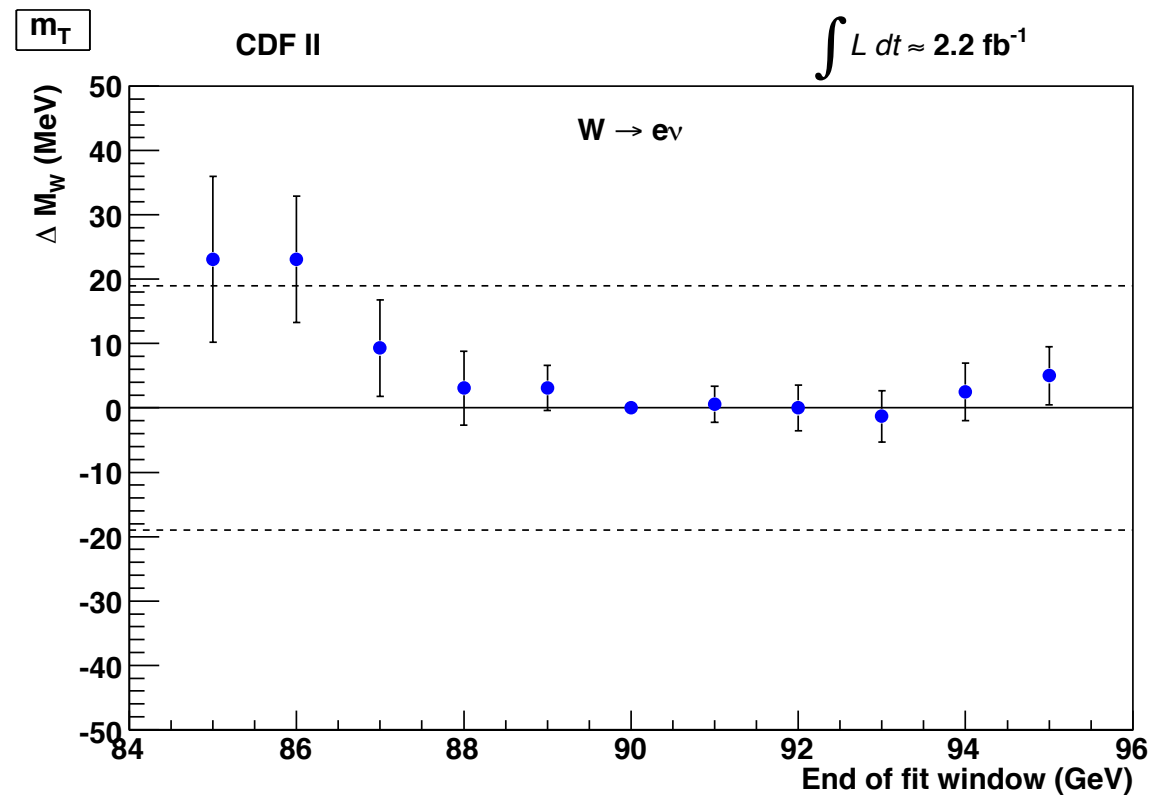


# Fit window variation: $m_T$

lower



upper



# Systematics: $m_T$

---

| Systematic (MeV)                        | Electrons | Muons | Common |
|-----------------------------------------|-----------|-------|--------|
| Lepton Energy Scale                     | 10        | 7     | 5      |
| Lepton Energy Resolution                | 4         | 1     | 0      |
| Recoil Energy Scale                     | 5         | 5     | 5      |
| Recoil Energy Resolution                | 7         | 7     | 7      |
| $u_{  }$ Efficiency                     | 0         | 0     | 0      |
| Lepton Removal                          | 3         | 2     | 2      |
| Backgrounds                             | 4         | 3     | 0      |
| $p_T(W)$ Model ( $g_2, g_3, \alpha_s$ ) | 3         | 3     | 3      |
| Parton Distributions                    | 10        | 10    | 10     |
| QED Radiation                           | 4         | 4     | 4      |
| Total                                   | 18        | 16    | 15     |

# Systematics: $p_T^l$

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| Systematic (MeV)                        | Electrons | Muons | Common |
|-----------------------------------------|-----------|-------|--------|
| Lepton Energy Scale                     | 10        | 7     | 5      |
| Lepton Energy Resolution                | 4         | 1     | 0      |
| Recoil Energy Scale                     | 6         | 6     | 6      |
| Recoil Energy Resolution                | 5         | 5     | 5      |
| $u_{  }$ efficiency                     | 2         | 1     | 0      |
| Lepton Removal                          | 0         | 0     | 0      |
| Backgrounds                             | 3         | 5     | 0      |
| $p_T(W)$ model ( $g_2, g_3, \alpha_s$ ) | 9         | 9     | 9      |
| Parton Distributions                    | 9         | 9     | 9      |
| QED radiation                           | 4         | 4     | 4      |
| Total                                   | 19        | 18    | 16     |

# Systematics: $p_T^\nu$

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| Systematic (MeV)                        | Electrons | Muons | Common |
|-----------------------------------------|-----------|-------|--------|
| Lepton Energy Scale                     | 10        | 7     | 5      |
| Lepton Energy Resolution                | 7         | 1     | 0      |
| Recoil Energy Scale                     | 2         | 2     | 2      |
| Recoil Energy Resolution                | 11        | 11    | 11     |
| $u_{  }$ efficiency                     | 3         | 2     | 0      |
| Lepton Removal                          | 6         | 4     | 4      |
| Backgrounds                             | 4         | 6     | 0      |
| $p_T(W)$ model ( $g_2, g_3, \alpha_s$ ) | 4         | 4     | 4      |
| Parton Distributions                    | 11        | 11    | 11     |
| QED radiation                           | 4         | 4     | 4      |
| Total                                   | 22        | 20    | 18     |

# Some cross-checks

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*Stat. uncertainty only.  $p_T^l$  fits only.*

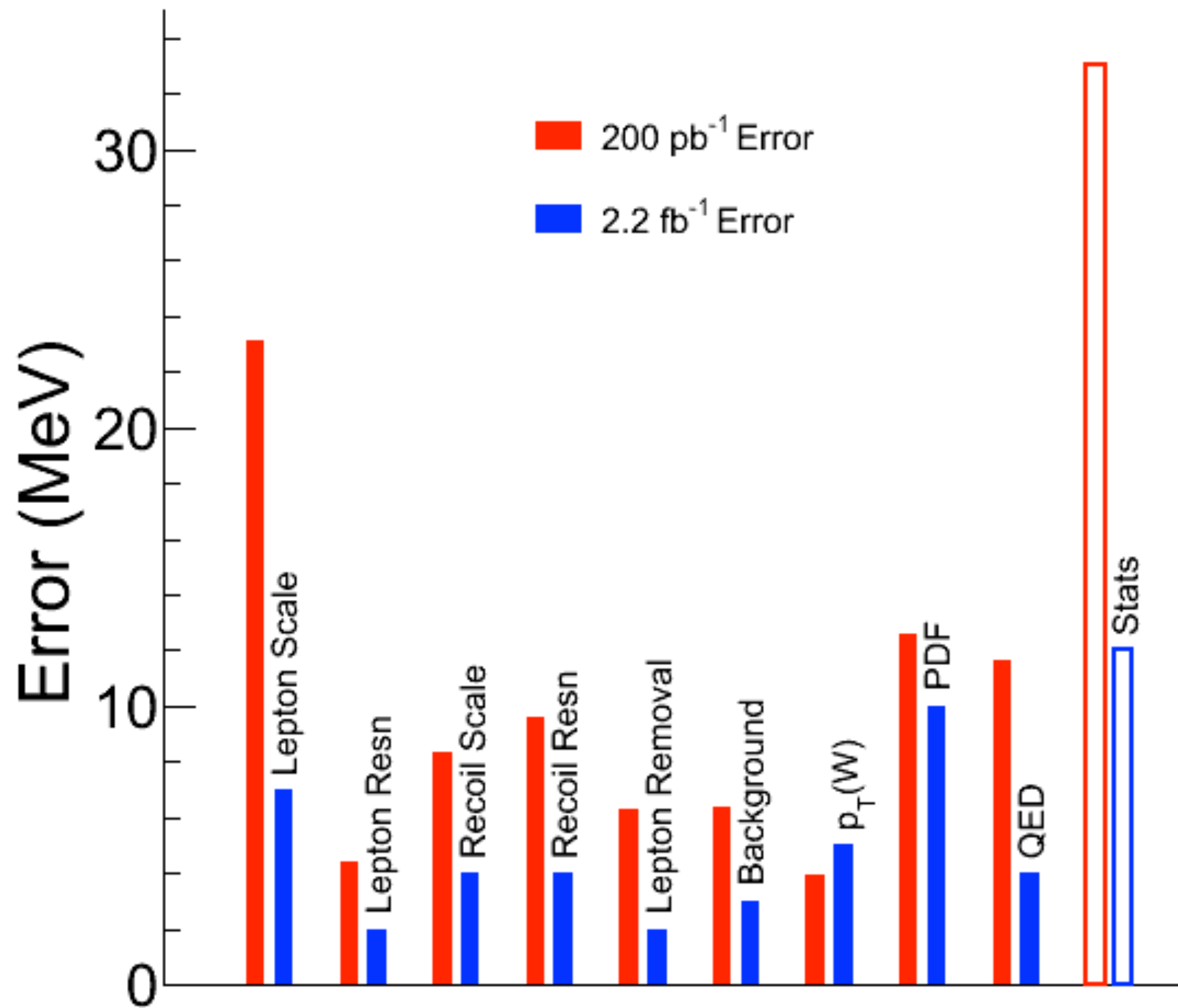
| Lepton   | Fit                             | Result (MeV) |
|----------|---------------------------------|--------------|
| Electron | $M_{W^+} - M_{W^-}$             | $-49 \pm 42$ |
| Electron | $M_W(\phi > 0) - M_W(\phi < 0)$ | $-58 \pm 45$ |
| Muon     | $M_{W^+} - M_{W^-}$             | $71 \pm 69$  |
| Muon     | $M_W(\phi > 0) - M_W(\phi < 0)$ | $-54 \pm 36$ |

# Mass fit combinations

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- Electron and muon  $m_T$  fits combined  
 **$m_W = 80390 \pm 20 \text{ MeV}$ ,  $\chi^2/\text{dof} = 1.2/1$  (28%)**
- Electron and muon  $p_T$  fits combined  
 **$m_W = 80366 \pm 22 \text{ MeV}$ ,  $\chi^2/\text{dof} = 2.3/1$  (13%)**
- Electron and muon MET fits combined  
 **$m_W = 80416 \pm 25 \text{ MeV}$ ,  $\chi^2/\text{dof} = 0.5/1$  (49%)**
- All electron fits combined  
 **$m_W = 80406 \pm 25 \text{ MeV}$ ,  $\chi^2/\text{dof} = 1.4/2$  (49%)**
- All muon fits combined  
 **$m_W = 80374 \pm 22 \text{ MeV}$ ,  $\chi^2/\text{dof} = 4/2$  (12%)**
- All fits combined  
 **$m_W = 80387 \pm 19 \text{ MeV}$ ,  $\chi^2/\text{dof} = 6.6/5$  (25%)**

# Uncertainty progress



# MSSM allowed region

*Heinemeyer, Hollik, Stockinger, Weiglein, Zeune*

