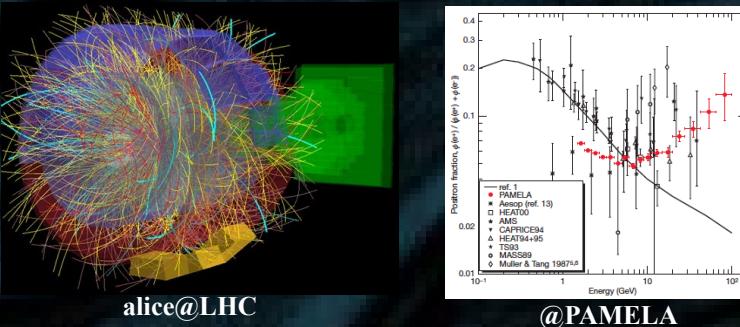


Impact of cross-section uncertainties on the GCR electron/positron fluxes



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Secondary GCR $e^{+/-}$ production

$$\mathcal{Q}_{\text{sec}}(T, \vec{x}) = 4\pi \sum_{i,j} \int dT_i \frac{d\phi_i(T_i, \vec{x})}{dT_i} \frac{d\sigma_{ij \rightarrow \text{sec}}(T_i \rightarrow T)}{dT} n_j(\vec{x})$$

Low energy ($T < 3$ GeV)

$$p + p \longrightarrow p + \Delta^+ \longrightarrow \begin{cases} p + n + \pi^+ & (73\%) \\ p + p + \pi^0 & (27\%) \end{cases}$$

$$\pi^\pm \longrightarrow \mu^\pm + \nu_\mu \longrightarrow e^\pm + 2\nu_\mu + \nu_e$$

$$K^\pm \longrightarrow \begin{cases} \mu^\pm + \nu_\mu & (63.5\%) \\ \pi^\pm + \pi^0 & (21.2\%) \\ \pi^\pm + \pi^\pm + \pi^\mp & (5.6\%) \end{cases}$$

Higher energy ($T > 3$ GeV)

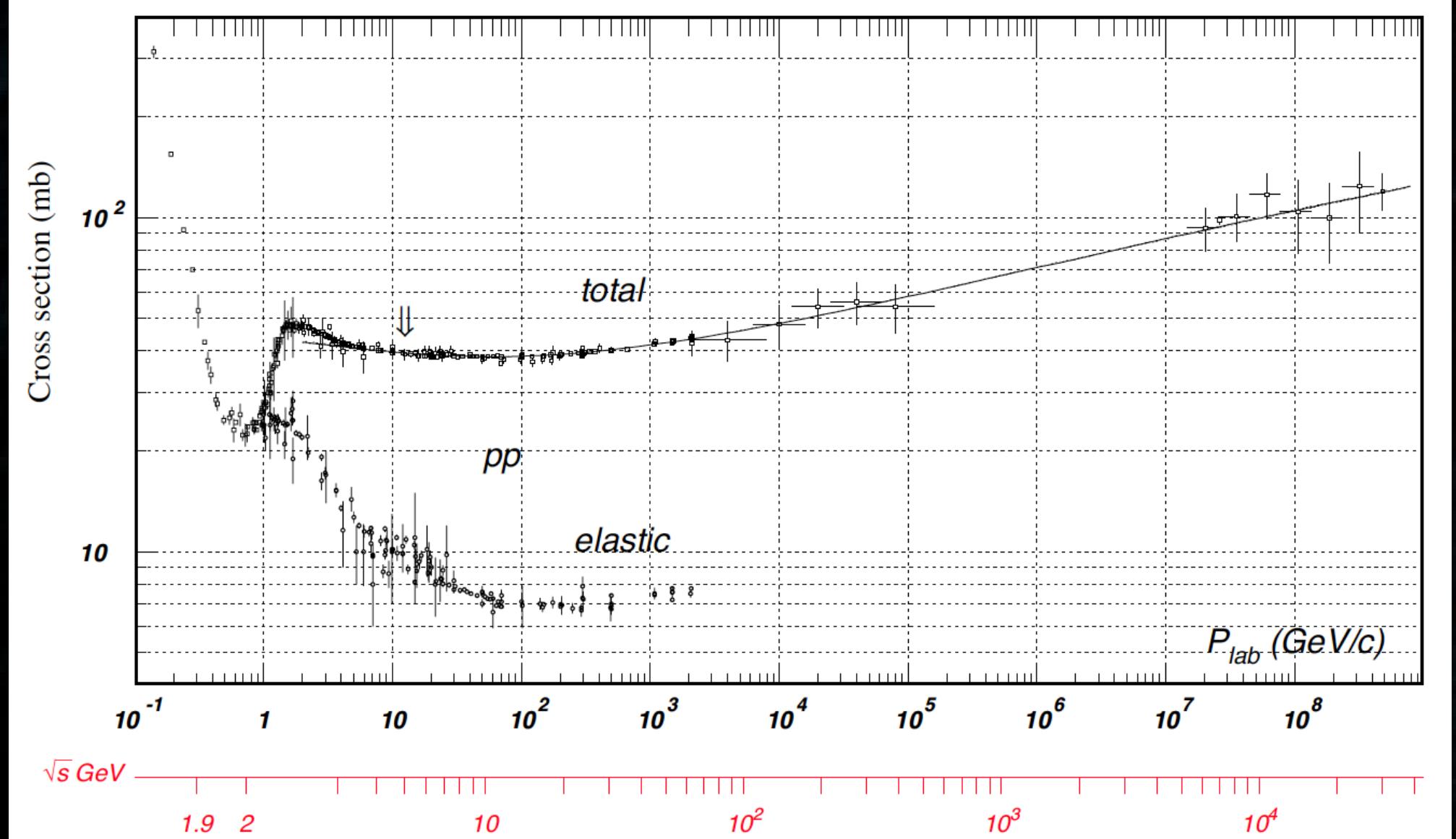
$$p + p \longrightarrow \begin{cases} \pi^\pm + X \\ K^\pm + Y \end{cases}$$

Different approaches:

- in the past, **semi-empirical** models for inclusive pion/kaon production cross section (Delta resonance + non-diffractive processes treated in scaling models)
- more recently, **Monte-Carlo based** methods including non-perturbative QCD (scaling violation) + diffractive processes

p-p cross section from RPP2012

PDG: Beringer et al (2012), data available at
<http://pdg.lbl.gov/2012/hadronic-xsections/>



Some reference works for pion/kaon production models applied to HE astrophysics

Semi-empirical approaches:

Stecker (1970) – neutral pions: Delta (1232 MeV) for $T < 2.2$ GeV; “fireball” process for $T > 2.2$ GeV

Badhwar et al (1977) – charged pions: scaling model

Stephens & Badhwar (1981) – neutral pions: scaling model

Tan & Ng (1983) – charged pions: scaling model

Dermer (1986) – charged and neutral pions: isobaric (à la Stecker) for $T < 3$ GeV, then scaling à la Badhwar et al.

***** Moskalenko & Strong (1998)**: à la Dermer – reference work for secondary positron predictions (before 2008)

→ no diffractive interactions + no Feynman scaling violation in the non-diffractive inelastic interaction

→ constant inelastic p-p cross section assumed for $T >> 10$ GeV (not supported by more recent data)

Monte-Carlo based approaches:

Mori (1997) – neutral pions: Pythia-like (perturbative QCD – Lund model, beyond scaling model, nondiffractive processes only)

Kelner et al (2006): Based on SIBYLL (Fletcher et al, 1994) and QGSJET (Kalmykov et al, 1997)

Kamae et al (2006):

→ Delta(1232 MeV) resonance + 1600 MeV effective resonance

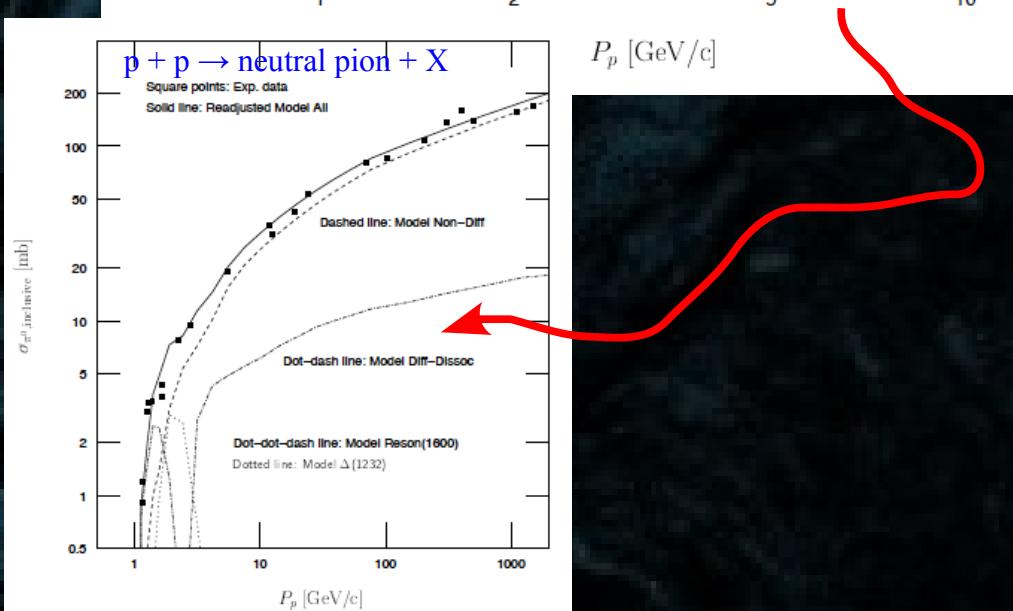
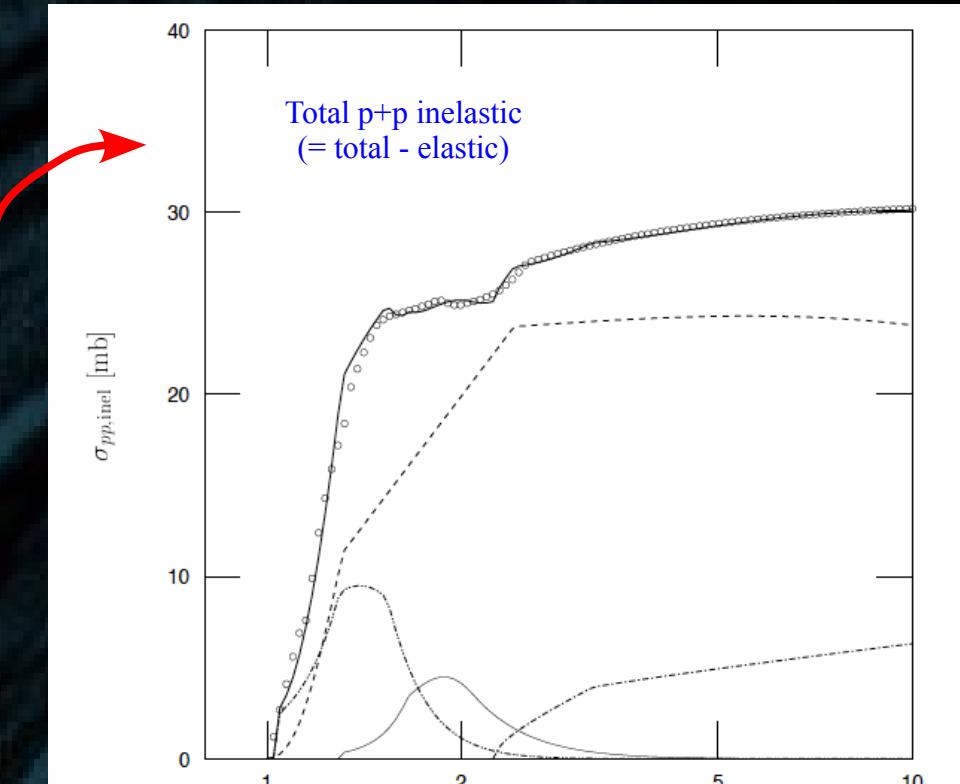
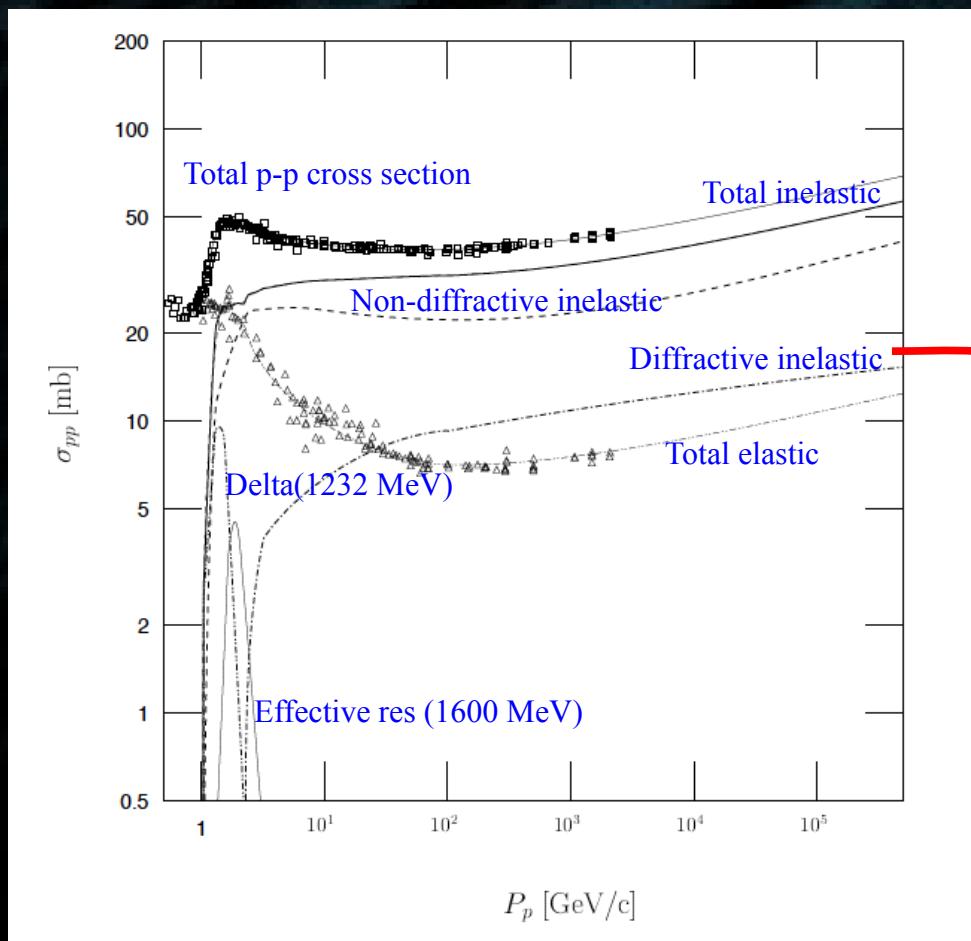
→ low energy ($T < 50$ GeV): diffractive by Kamae (Pythia also works), non-diffractive from Blattnig et al (2000)

→ high energy ($T > 50$ GeV) non-diffractive: Pythia 6.2 (Sjöstrand et al, 2001)

→ $0.488 \text{ GeV} < T < 512 \text{ TeV}$

Kachelriess & Ostapchenko (2012): QGSJET-II + Kamae et al (2006)

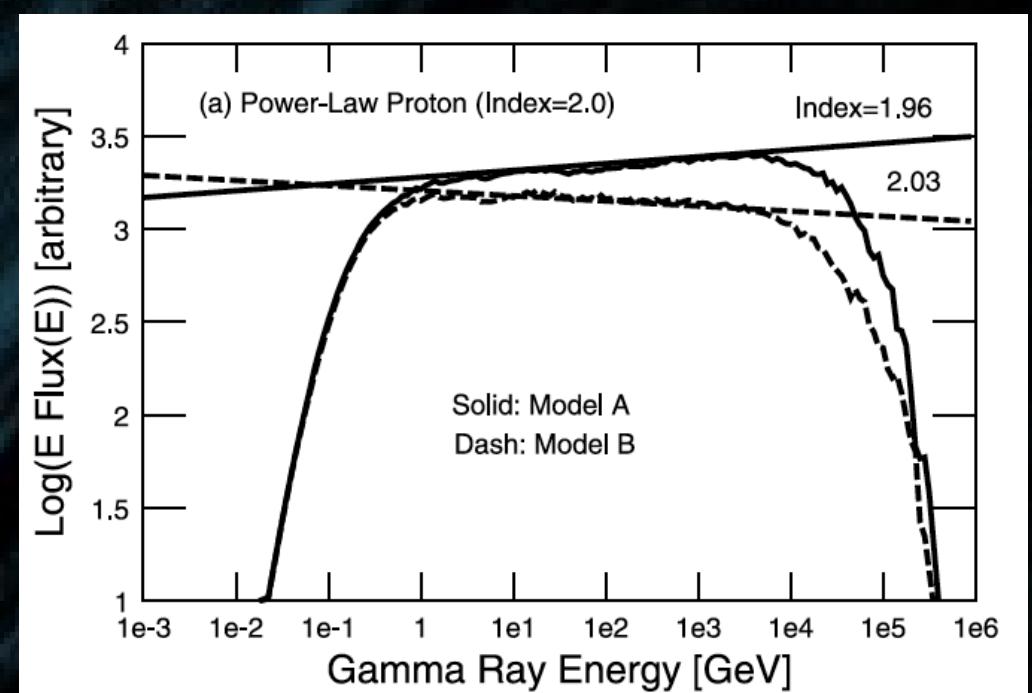
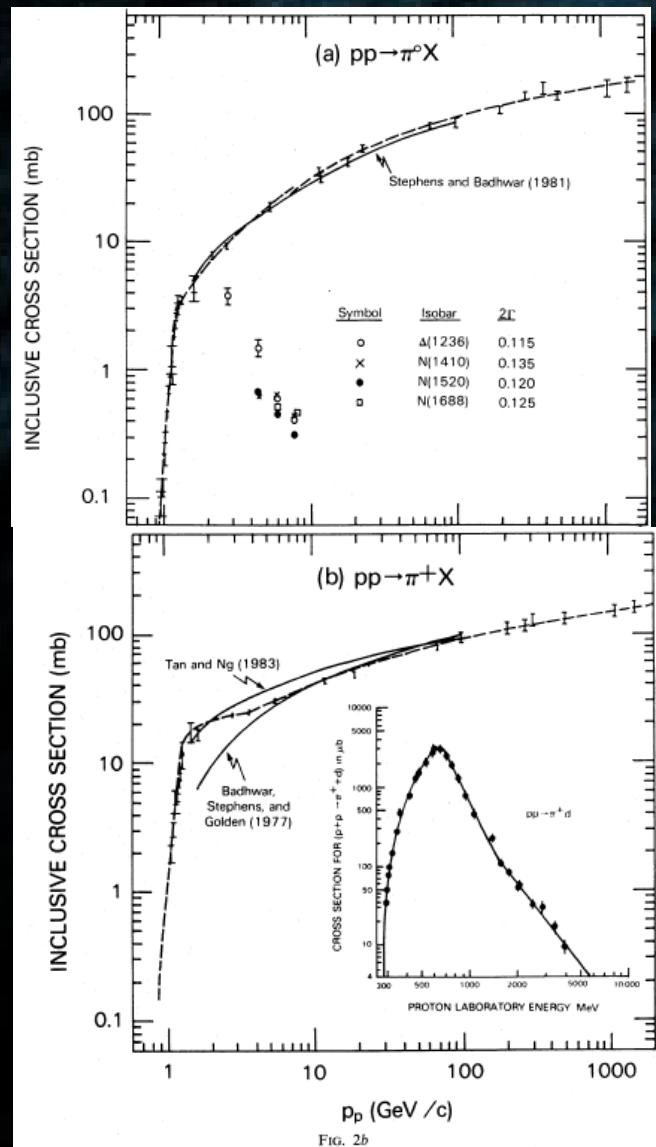
Parameterization of Kamae et al (2006)



- Delta(1232 MeV) resonance + 1600 MeV effective resonance
- low energy ($T < 50$ GeV):
 - * diffractive by Kamae (Goulianos, 1983) – Pythia includes it now
 - * non-diffractive from Blattnig et al (2000)
- high energy ($T > 50$ GeV) non-diffractive: Pythia 6.2 (Sjöstrand et al, 2001)
- validity: 0.488 GeV $< T <$ 512 TeV

Results wrt other parameterizations

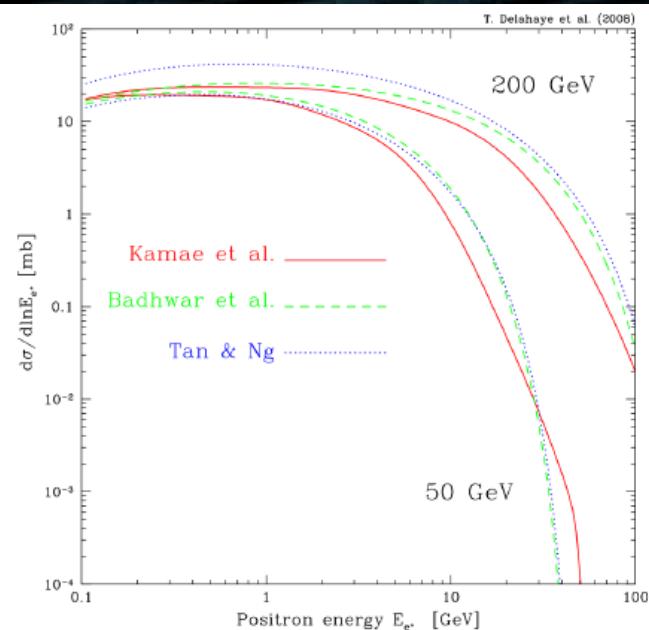
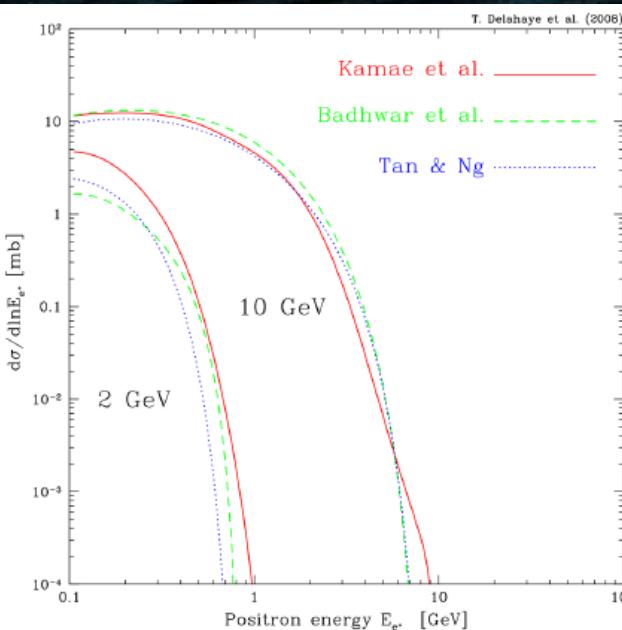
Compilation of pion data in e.g. Blattnig et al (2000)
and Dermer (1986)



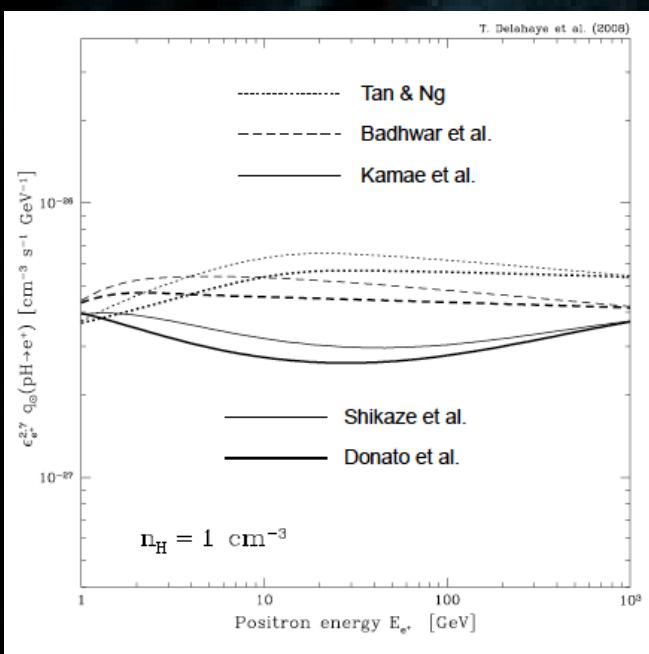
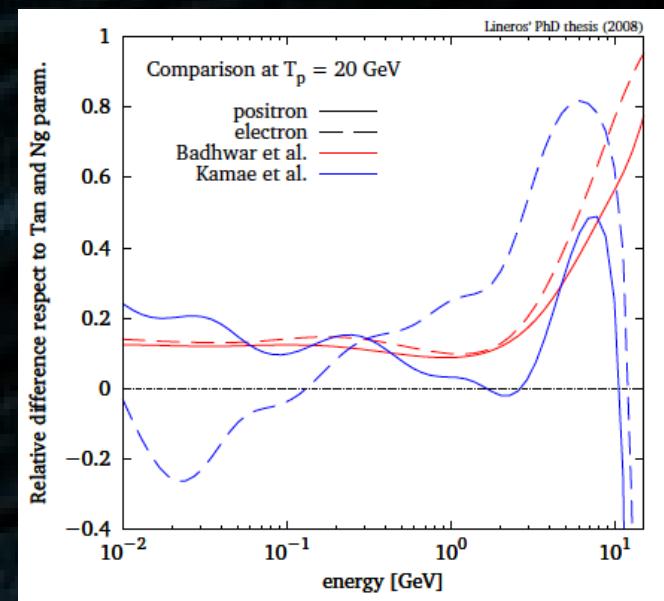
=> Spectral index is found harder, + 0.4
(valid for all pions, neutral and charged)

Results on secondary positron production

Delahaye et al (2008)



Lineros' PhD thesis, Delahaye's PhD thesis



Badhwar et al / Tan & Ng / Kamae et al

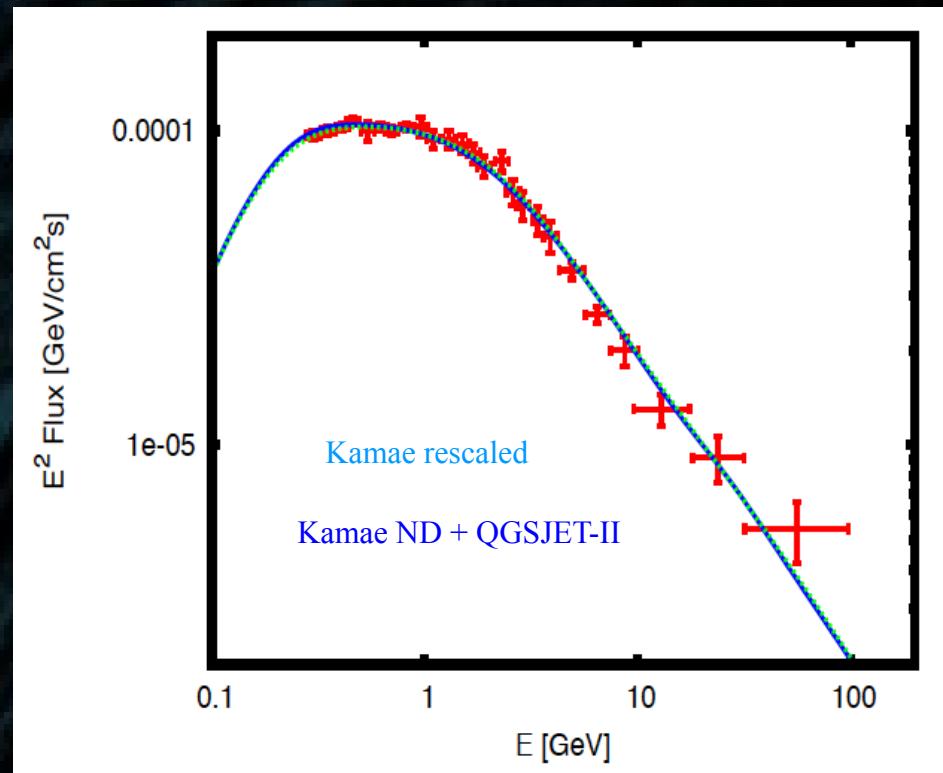
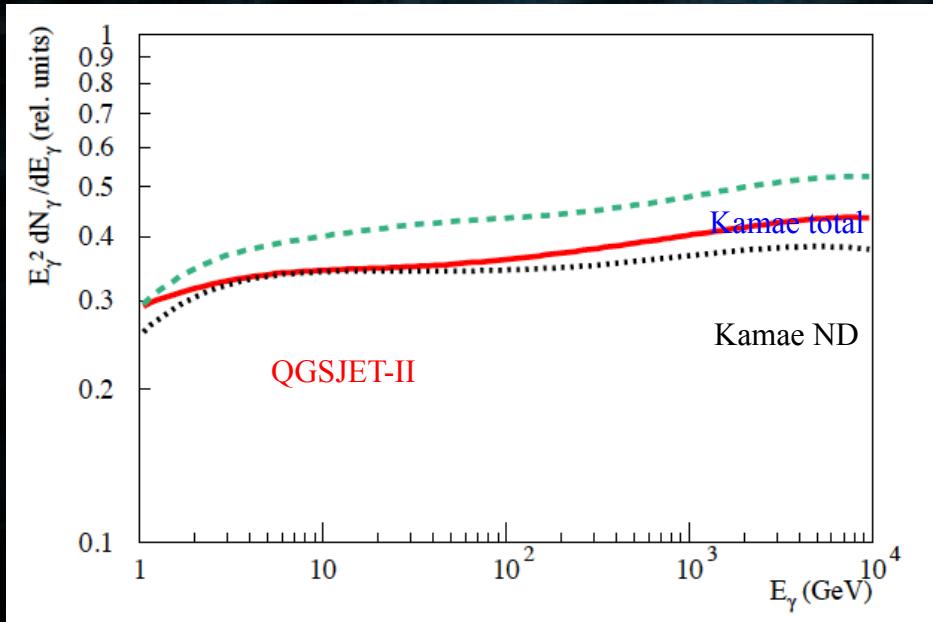
- * Factor of 2 difference in amplitude
- * Differences in spectral shape
- * Most recent model gives lowest flux

*** Badhwar et al (1977) and Tan & Ng (1983) models are somehow outdated

=> Confidence in Kamae et al (2006) ?

Caution with Kamae et al (2006)

New analysis by Kachelriess & Ostapchenko (2012) for neutral pion production (QGSJET-II + HERA and LHCdata)



- * QGSJET-II valid from $T > 10$ GeV
- * Kamae non-diffractive agrees well with data below 10 GeV
- * Kamae diffractive over-simplistic (uniform distribution of energy among produced pions)
=> 20% over-estimate

** Kamae total still OK for the spectral shape, only amplitude in excess

=> Compromise: Kamae ND for $T < 10$ GeV + QGSJET-II for $T > 10$ GeV

**** Are diffractive processes included in QGSJET-II?

=> Beware of MC-based statements: all claim to reach 10% precision

Nucleus-nucleus \rightarrow pions ???

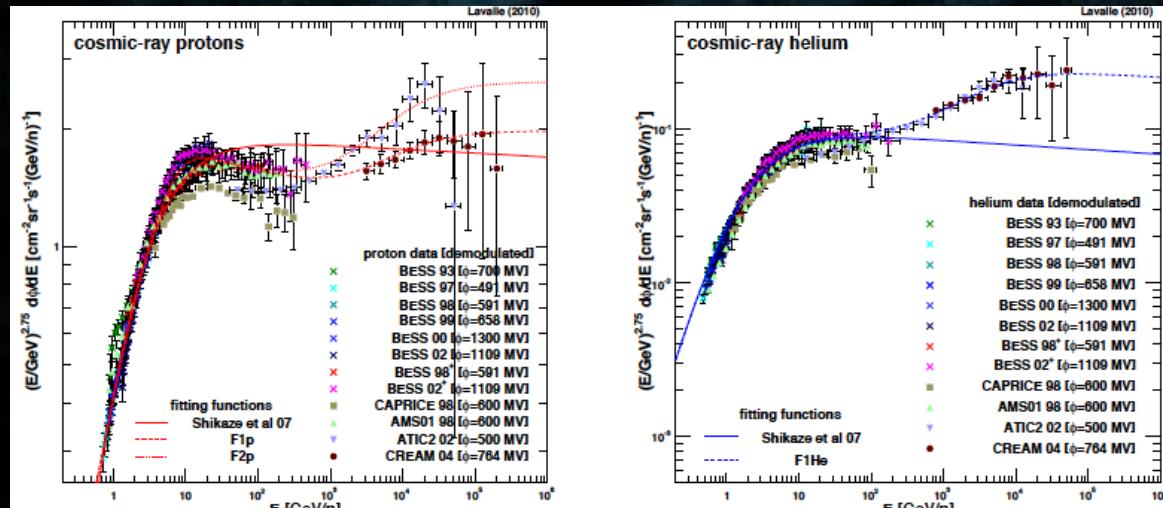
Orth & Buffington (1976)

$$\sigma_{A_1 A_2} = (A_1^{3/8} + A_2^{3/8} - 1)^2 \sigma_{pp}$$

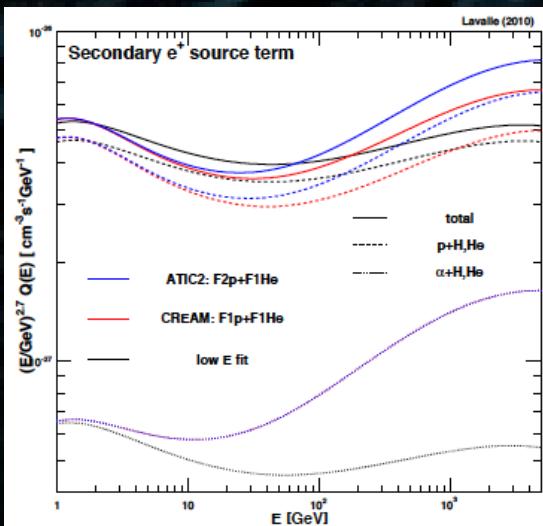
Norbury & Townsend (2007)

$$\text{Prob}(pp) = \frac{Z_P}{A_P} \frac{Z_T}{A_T}$$

$$\text{Prob}(nn) = \frac{A_P - Z_P}{A_P} \frac{A_T - Z_T}{A_T}$$



p+alpha fluxes
+++
H+Helium gas



$$\frac{\sigma_{AA \rightarrow \pi^+ X}}{\sigma_{AA \rightarrow \pi^- X}} = \left(\frac{Z_P}{A_P} \frac{Z_T}{A_T} \frac{\sigma_{pp \rightarrow \pi^+ X}}{\sigma_{pp \rightarrow \pi^- X}} \right) + \left(\frac{A_P - Z_P}{A_P} \frac{A_T - Z_T}{A_T} \frac{\sigma_{pp \rightarrow \pi^- X}}{\sigma_{pp \rightarrow \pi^+ X}} \right)$$

$$\sigma_{AA \rightarrow \pi^+ X} \approx (A_P A_T)^{2/3} \sigma_{pp \rightarrow \pi^+ X}$$

$$\sigma_{AA \rightarrow \pi^- X} = \frac{(A_P A_T)^{2/3} \sigma_{pp \rightarrow \pi^+ X}}{\left(\frac{Z_P}{A_P} \frac{Z_T}{A_T} \frac{\sigma_{pp \rightarrow \pi^+ X}}{\sigma_{pp \rightarrow \pi^- X}} \right) + \left(\frac{A_P - Z_P}{A_P} \frac{A_T - Z_T}{A_T} \frac{\sigma_{pp \rightarrow \pi^- X}}{\sigma_{pp \rightarrow \pi^+ X}} \right)}$$

2/3 \rightarrow 2.2/3 gives better fits

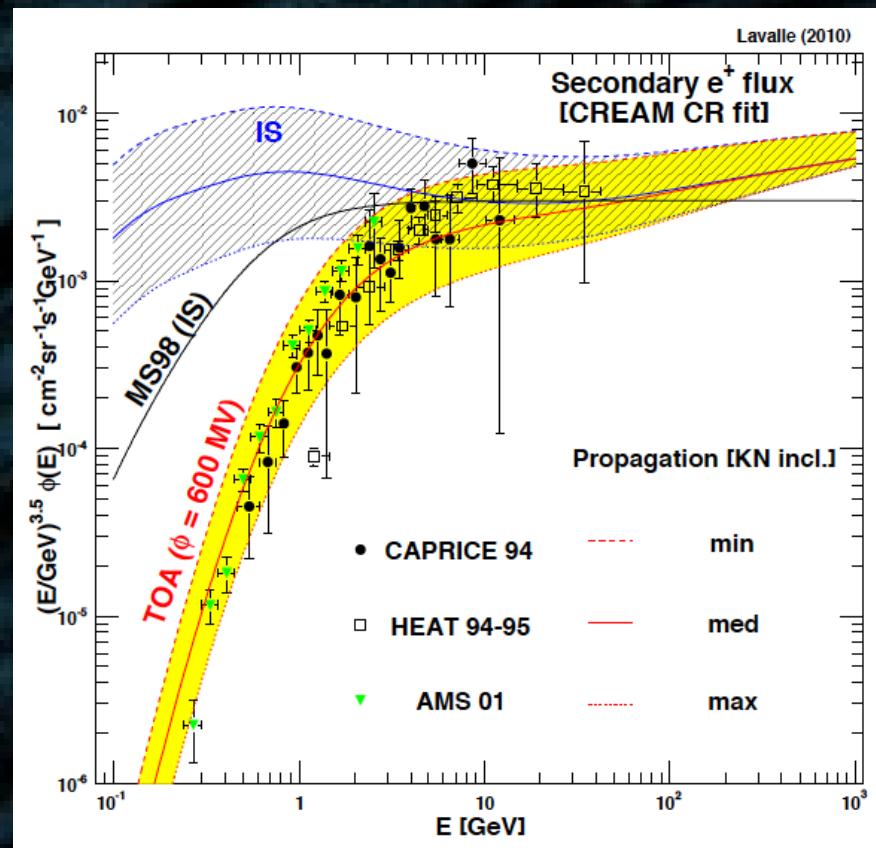
Ex. of proton+Helium:

$$\begin{aligned} O\&B &= 3^{(3/4)} &= 2.28 \\ N \& T &= 3^{(2.2/3)} &= 2.24 \end{aligned}$$

Including CR alpha's and He gas
 \Rightarrow 20% correction

Heavier species < 10% if scaling relation valid

Comparison with transport uncertainties



Conclusions:

- * Error on production cross section $\sim 20\%$
(amplitude more affected than spectrum)
- * Larger if scaling for nuclei fails $< 20\%$
- * to compare with error on ISM and GCR densities
- * Transport parameters \Rightarrow factor of 2 unc.

Pion/kaon production and decay to e+/- In Galprop

Manual of Galprop v54

<http://galprop.stanford.edu/code.php?option=manual>

2.1.6 Secondary positrons and electrons

Secondary positrons and electrons in cosmic rays are the final product of decay of charged pions and kaons which in turn created in collisions of cosmic-ray particles with gas. Pion production in pp -collisions is considered following a method developed by Dermer (1986a,b), which combines isobaric (Stecker, 1970) and scaling (Badhwar et al., 1977; Stephens & Badhwar, 1981) models of the reaction. Secondary positron and electron production is computed as described in Moskalenko & Strong (1998), that includes a critical reevaluation of the charged pion and kaon decay calculations. Primary electrons are computed in the same propagation model.

Nota: $n_{He}/nH = 0.11$ in Galprop

(We have also taken $n_{He}/nH = 0.11$, $nH=0.9/\text{cm}^3$, $n_{He}=0.1/\text{cm}^3$)

Alice @ LHC

arXiv:1101.4110

