

$e^+e^- \rightarrow N\bar{N}$  at BESIII

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on behalf of the BESIII Collaboration

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## Electromagnetic structure of hadrons: annihilation and scattering processes

GDR 3034 - Chromodynamique Quantique  
et Physique des Hadrons

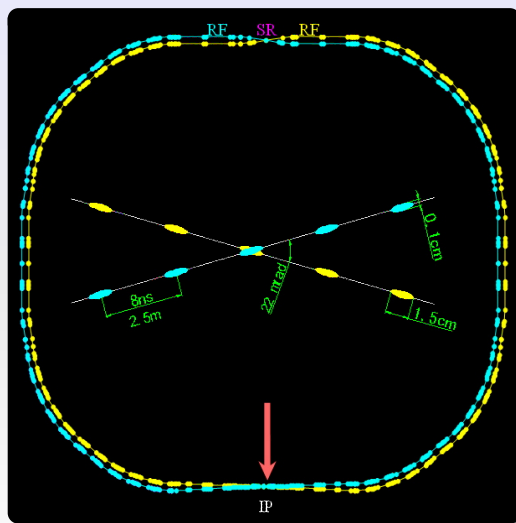
GDR-PH-QCD, Meeting Groupe 2

 IPN Orsay, October 3<sup>rd</sup> - 5<sup>th</sup>, 2012

The background of the slide is a complex grid of hand-drawn lines and circles in black ink. The lines are mostly straight but some are curved, and they intersect to form various geometric shapes. There are also several small circles and larger, more irregular shapes scattered across the grid. The overall appearance is that of a technical drawing or a set of diagrams related to particle physics.

# BESIII/BEPCII

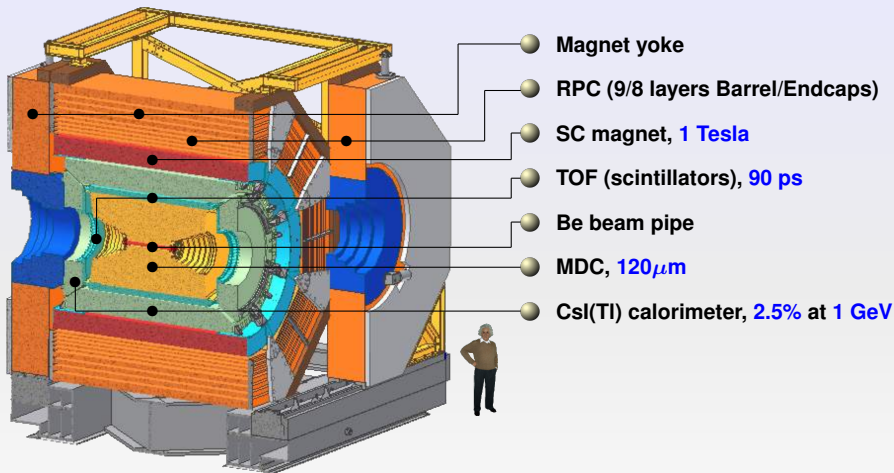
# BEPCII: $e^+e^-$ double ring collider



## Design Features

- Beam energy: 1.0 - 2.3 GeV
- Crossing angle: 22 mrad  
(DAΦNE 50 mrad)
- **Luminosity:  $10^{33} \text{ cm}^{-2}\text{s}^{-1}$**
- **Optimum energy: 1.89 GeV**
- Energy spread:  $5.16 \times 10^{-4}$
- Number of bunches: 93
- Bunch length: 1.5 cm
- Total current: 0.91 A

# The BESIII detector

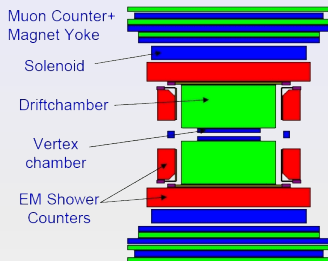


A significant improvement with respect to BESII

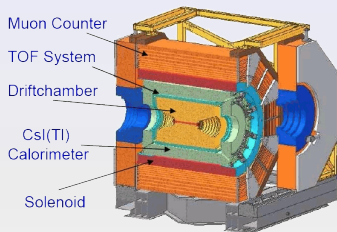


# The BESII and BESIII detectors

## BESII @ BEPC



## BESIII @ BEPCII



Device	Performance
MDC	$\sigma_p/p = 1.7\% \sqrt{1 + p^2}$ , $dE/dx = 8\%$
TOF	180 ps (bhabha)
EMC	$\sigma_E/E < 22\%/\sqrt{E}$
MUC	3 layers
Magnet	0.4 T Solenoidal

Device	Performance
MDC	$\sigma_p/p = 0.5\%$ , $dE/dx < 6\%$
TOF	80 ps barrel (bhabha), 100 ps endcap
EMC	$\sigma_E/E < 2.5\%/\sqrt{E}$
MUC	9 barrel + 8 endcap layers
Magnet	1 T Solenoidal

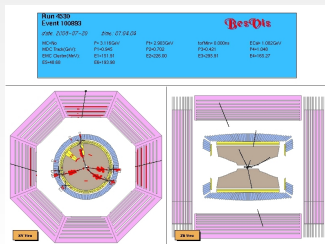
- $R_{\text{had}}$  and precision test of Standard Model
- Light hadron spectroscopy ( $\phi f_0(980)$ ,  $\phi\pi^0$ , ...)
- Charm and charmonium physics
- $\tau$  physics
- Precision measurements of CKM matrix elements
- Search for new physics / new particles

Physics Channels	Energy (GeV)	Luminosity ( $10^{33} \text{ cm}^{-2} \text{ s}^{-1}$ )	Events/year
$J/\psi$	3.10	0.6	$1.0 \times 10^{10}$
$\tau$	3.67	1.0	$1.2 \times 10^7$
$\psi(2S)$	3.69	1.0	$3.0 \times 10^9$
$D^*$	3.77	1.0	$2.5 \times 10^7$
$D_s$	4.03	0.6	$1.0 \times 10^6$
$D_s$	4.14	0.6	$2.0 \times 10^6$



# BEPCII / BESIII milestones

- **Mar. 2008:** Collisions at  $500 \text{ mA} \times 500 \text{ mA}$ ,  
Luminosity:  $1 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
- **Apr. 30, 2008:** Move BESIII to IP
- **July 18, 2008:** First  $e^+e^-$  collision event in BESIII
- **Apr. 14, 2009:**  $\sim 106 \text{ M } \Psi(2S)$  events ( $150 \text{ pb}^{-1}$ )  $\sim 4 \times \text{CLEO-c}$   
( $\sim 42 \text{ pb}^{-1}$  at 3.65 GeV)
- **July 28, 2009:**  $\sim 225 \text{ M } J/\Psi$  events ( $65 \text{ pb}^{-1}$ )  $\sim 4 \times \text{BESII}$
- **2010-2011:**  $\sim 2.9 \text{ fb}^{-1}$  at  $\psi(3770)$   $\sim 11 \times \text{CLEO-c}$   
( $\sim 70 \text{ pb}^{-1}$  scanning in the  $\psi(3770)$  energy region)
- **May, 2011:**  $\sim 0.5 \text{ fb}^{-1}$  at 4.01 GeV (Ds and XYZ spectroscopy)
- **2012:**  $\sim 0.4 \text{ B } \Psi(2S)$  events  $\sim 16 \times \text{CLEO-c}$   
 $\sim 1 \text{ B } J/\Psi$  events  $\sim 18 \times \text{BESII}$



Record Luminosity

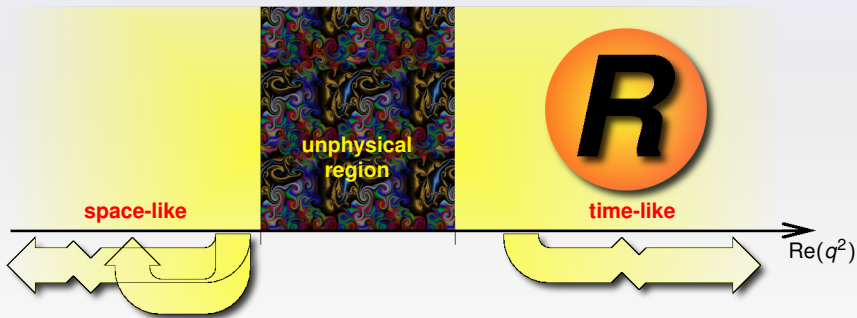
$$6.5 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$$

or

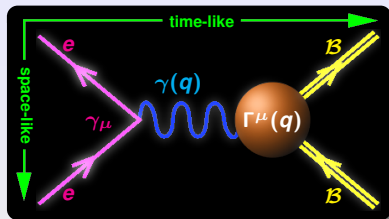
$8 \times \text{CESRc}$

$45 \times \text{BEPC}$

The ratio  $R = \mu_p \frac{G_E^p}{G_M^p}$



# Nucleon form factors and cross sections



**Nucleon current operator (Dirac & Pauli)**

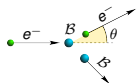
$$\Gamma^\mu(q) = \gamma^\mu F_1(q^2) + \frac{i}{2M_B} \sigma^{\mu\nu} q_\nu F_2(q^2)$$

**Electric and Magnetic Form Factors**

$$G_E(q^2) = F_1(q^2) + \tau F_2(q^2) \quad \tau = \frac{q^2}{4M_B^2}$$

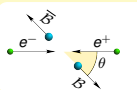
$$G_M(q^2) = F_1(q^2) + F_2(q^2)$$

**Elastic scattering** (Rosenbluth)



$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 E_e' \cos^2 \frac{\theta}{2}}{4E_e^3 \sin^4 \frac{\theta}{2}} \left[ G_E^2 - \tau \left( 1 + 2(1-\tau) \tan^2 \frac{\theta}{2} \right) G_M^2 \right] \frac{1}{1-\tau}$$

**Annihilation** Coulomb correction



$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta C}{4q^2} \left[ (1 + \cos^2 \theta) |G_M|^2 + \frac{1}{\tau} \sin^2 \theta |G_E|^2 \right]$$

$$\beta = \sqrt{1 - \frac{1}{\tau}}$$

**Pointlike fermions**  
e.g.  $e^+e^- \rightarrow \mu^+\mu^-$

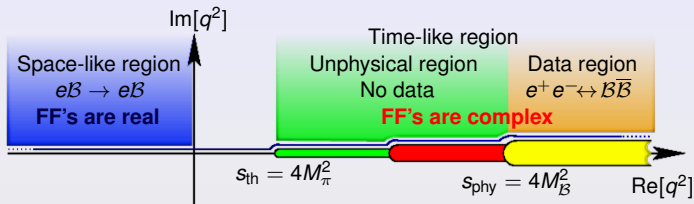
$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta_\mu C}{4q^2} (2 - \beta_\mu^2 \sin^2 \theta)$$



$$|G_E| = |G_M| \equiv 1$$

# Analyticity of baryon form factors

## $q^2$ -complex plane



Crossing: tot. helicity =  $\begin{cases} 1 \Rightarrow G_E \\ 0 \Rightarrow G_M \end{cases}$

$$G_E(4M_B^2) = G_M(4M_B^2)$$

## QCD counting rule constrains the asymptotic behaviour

Matveev, Muradyan, Tevkheldize, Brodsky, Farrar

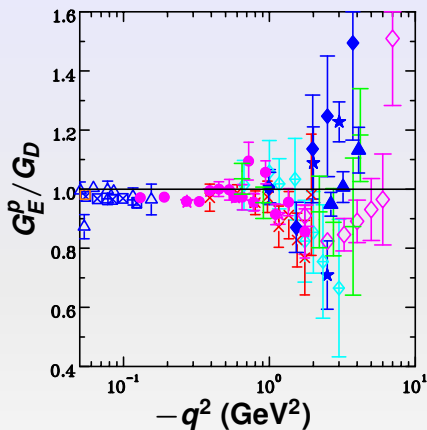
**Counting rule:**  $q^2 \rightarrow -\infty$   
 $i = 1$  Dirac,  $i = 2$  Pauli FF

$$F_i(q^2) \propto (-q^2)^{-(i+1)} \Rightarrow G_{E,M} \propto (-q^2)^{-2}$$

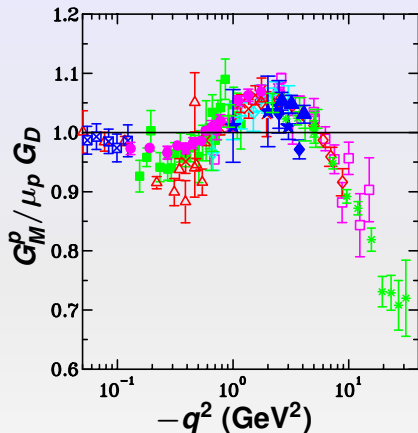
**Analyticity:**  $q^2 \rightarrow \pm\infty$   
 (Phragmén Lindelöf)

$$G_{E,M}(-\infty) = G_{E,M}(+\infty)$$

# $G_E^p$ and $G_M^p$ with Rosenbluth separation

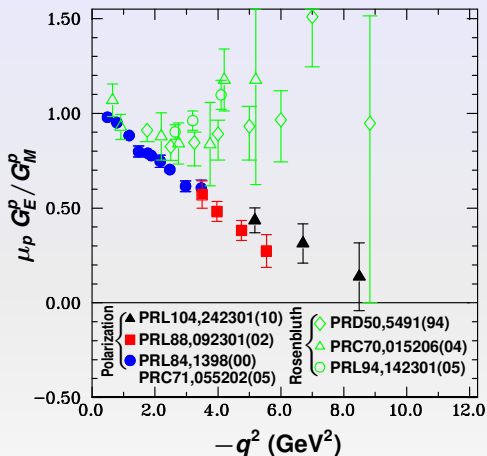


- |                 |                    |
|-----------------|--------------------|
| △ RMP35,335(63) | ⊠ NPB93,461(75)    |
| ◆ PLB31,40(70)  | □ NPA333,381(80)   |
| ● PRD4,45(71)   | ◇ PRD50,5491(94)   |
| × PLB35,87(71)  | ★ PRD49,5671(94)   |
| ◊ NPB58,429(73) | + PRC70,015206(04) |
| ☆ PRD8,753(73)  | ▲ PRL94,142301(05) |



- |                 |                    |
|-----------------|--------------------|
| △ RMP35,335(63) | ◊ NPB58,429(73)    |
| ■ PR142,922(66) | ⊠ NPB93,461(75)    |
| □ PRL20,292(68) | * PRD48,29(93)     |
| ◆ PLB31,40(70)  | ◇ PRD50,5491(94)   |
| ● PRD4,45(71)   | ★ PRD49,5671(94)   |
| × PLB35,87(71)  | + PRC70,015206(04) |
| ☆ PRD8,753(73)  | ▲ PRL94,142301(05) |

# $G_E^p/G_M^p$ in polarization transfer experiments



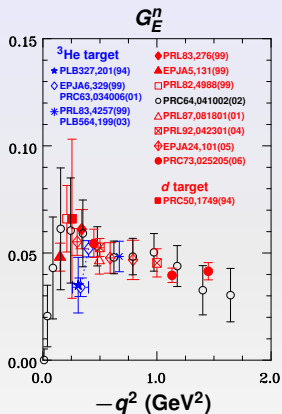
Polarization data do not agree with old Rosenbluth data (◊)



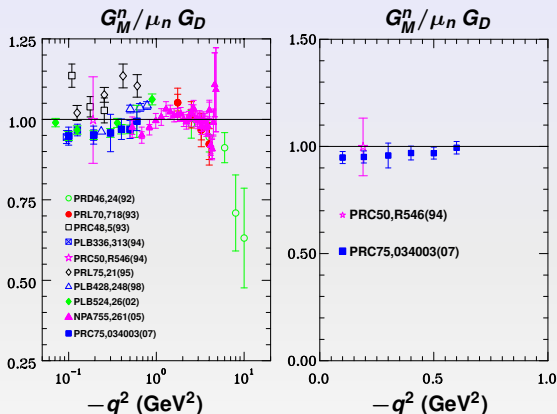
New Rosenbluth separation data from JLab still do not agree with polarization data



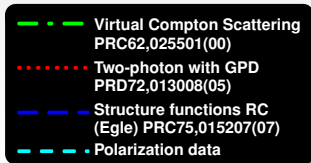
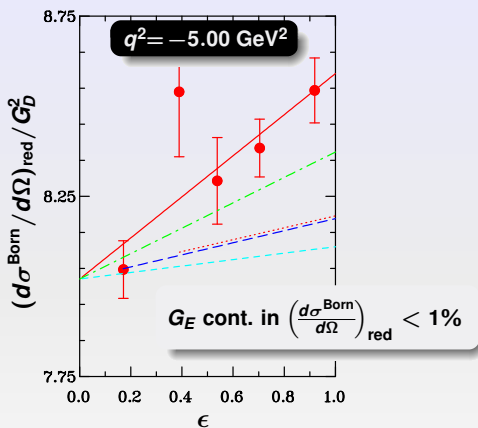
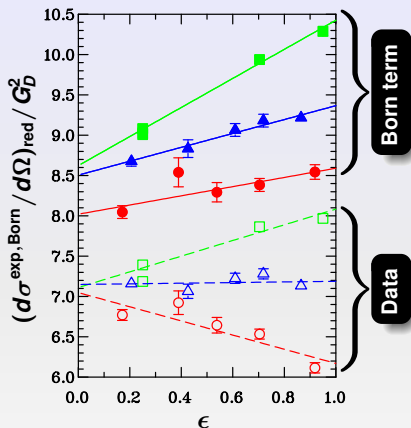
# $G_E^n$ and $G_M^n$ with different techniques



- Elastic  $e$ - $d$  cross section
- Polarization observables in electron scattering with  $^2\text{H}$  and  $^3\text{He}$  targets

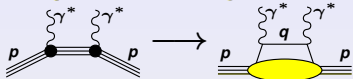


- Quasi-elastic  $e$ - $d$  / elastic  $e$ - $p$  cross sections
- Polarization observables in electron scattering on a polarized  $^3\text{He}$  target



# Rosenbluth $\rightarrow$ Polarization

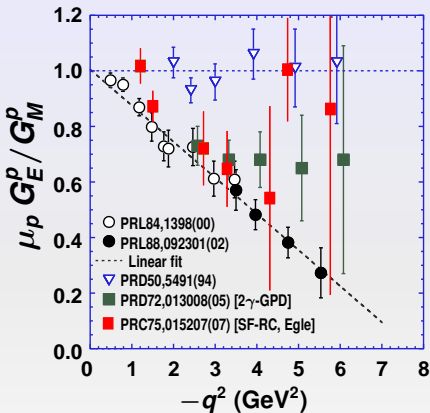
## Two-photon exchange (2 $\gamma$ -GPD)



- Two-photon exchange: contributions from intermediate far off-shell states
- Two hard photons
- Structure of nucleon: partonic "handbag" and GPD's

## Structure function radiative corrections (SF-RC)

- Hard bremsstrahlung from electron lines
- No co-linearity approximation
- Two-photon exchange contribution  $\sim 1\%$

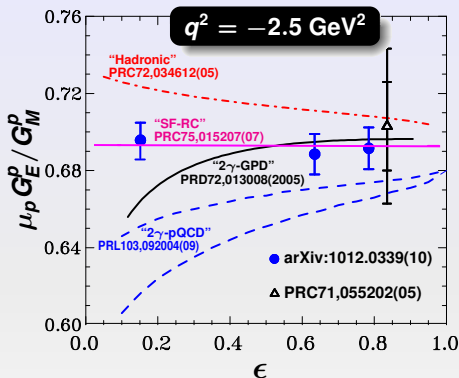


2 $\gamma$ -GPD and SF-RC change the slope in Rosenbluth plots

2 $\gamma$ -GPD and SF-RC have negligible contribution to the polarized cross section ratio

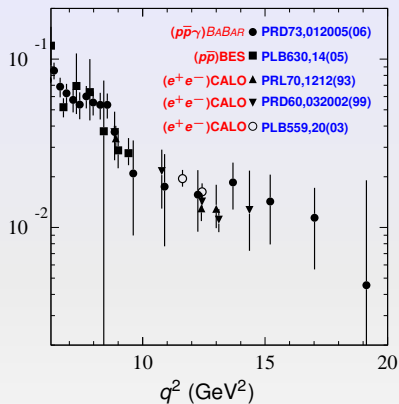
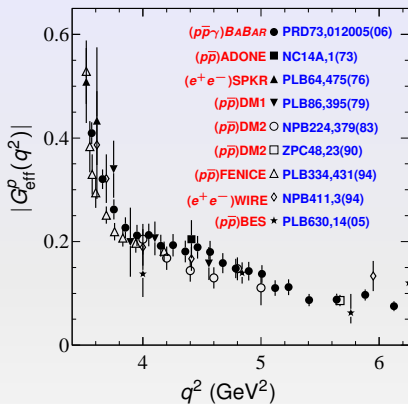
The  $1\gamma$ - $2\gamma$  interference terms have opposite signs in  $e^+p$  and  $e^-p$  elastic scattering cross sections  $\sigma_{\pm}$

A large (some %)  $2\gamma$  contribution produces deviations from unity as a function of  $\epsilon$  for the ratio  $\sigma_+/\sigma_-$



**No evidence of two-photon effects**

# Time-like magnetic proton form factor

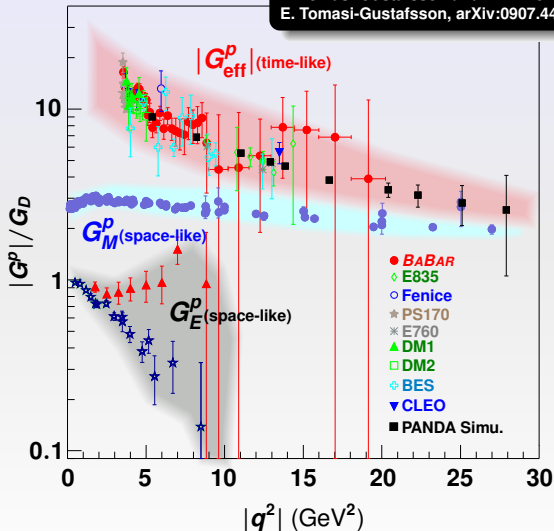


Data obtained assuming  $|G_M^p| = |G_E^p| \equiv |G_{\text{eff}}^p|$  (true only at threshold)

$$|G_{\text{eff}}^p|^2 = \frac{\sigma_{p\bar{p}}(q^2)}{\frac{16\pi\alpha^2 C_e}{3} \frac{\sqrt{1-1/\tau}}{4q^2} \left(1 + \frac{1}{2\tau}\right)}$$

# Asymptotic behavior

E. Tomasi-Gustafsson and M. P. Rekalo, PLB504,291  
E. Tomasi-Gustafsson, arXiv:0907.4442



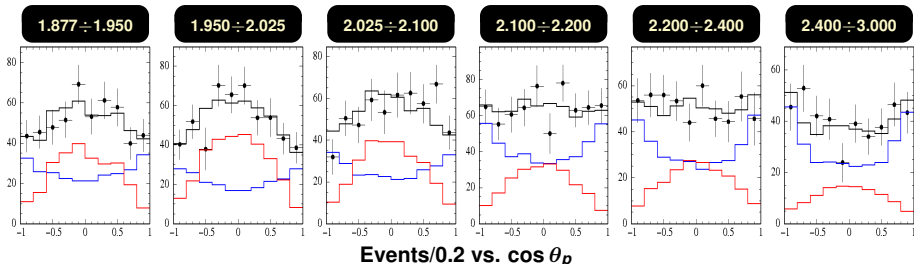
pQCD

$$G_{\text{eff}}^p(q^2) \underset{q^2 \rightarrow \infty}{\sim} G_M^p(q^2)$$

Phragmén Lindelöf

$$\lim_{q^2 \rightarrow \infty} \frac{G_{\text{eff}}^p(q^2)}{G_M^p(-q^2)} = 1$$

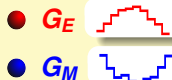
$\cos \theta_p$  distributions from threshold up to 3 GeV [intervals in  $E_{CM} \equiv q$  (GeV)]



$$\frac{d\sigma}{d\cos\theta_p} = A \left[ H_E(\cos\theta_p, q^2) \left| \frac{G_E^p(q^2)}{G_M^p(q^2)} \right|^2 + H_M(\cos\theta_p, q^2) \right]$$

$H_E$  and  $H_M$  from MC

Histograms show contributions from



At low  $q$

$$\sin^2 \theta_p > 1 + \cos^2 \theta_p \Rightarrow$$

First observation!

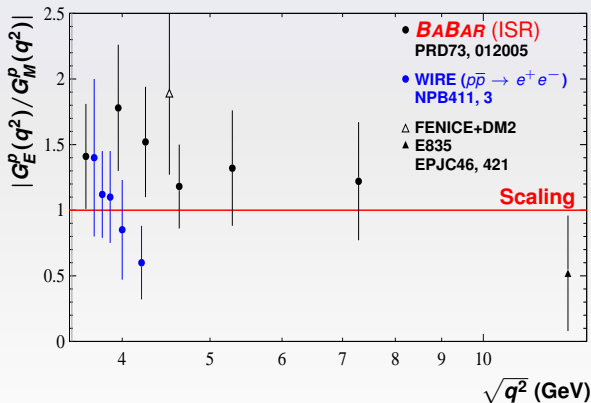
$$|G_E^p| > |G_M^p|$$

At higher  $q$ ,  $|G_E^p| \rightarrow |G_M^p|$

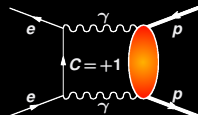
# Time-like $|G_E^p/G_M^p|$ measurements

$$\frac{d\sigma}{d\cos\theta} = \frac{\pi\alpha^2\beta C}{2q^2} |G_M^p|^2 \left[ (1 + \cos^2\theta) + \frac{4M_p^2}{q^2\mu_p^2} \sin^2\theta |R|^2 \right]$$

$$R(q^2) = \mu_p \frac{G_E^p(q^2)}{G_M^p(q^2)}$$



$\gamma\gamma$  exchange



$\gamma\gamma$  exchange interferes with the Born term



Asymmetry in angular distributions  
 [E. Tomasi-Gustafsson,

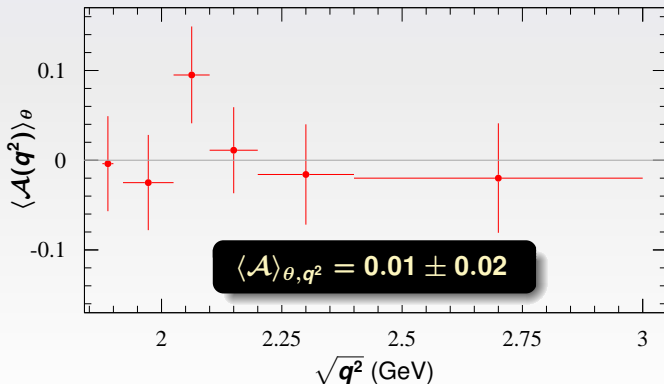
M.P. Rekalo, PLB504,291(01)]

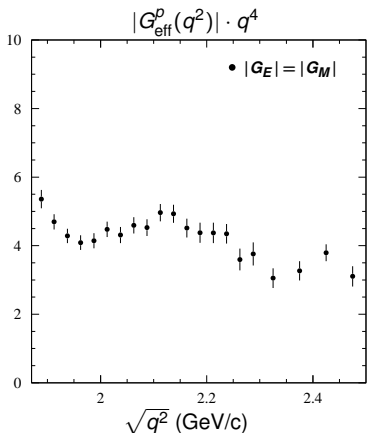


# $\gamma\gamma$ exchange from $e^+e^- \rightarrow p\bar{p}\gamma$ *BABAR* data

E. Tomasi-Gustafsson,  
E.A. Kuraev, S. Bakmaev, SP  
PLB659,197(08)

$$\mathcal{A}(\theta, q^2) = \frac{\frac{d\sigma}{d\Omega}(\theta, q^2) - \frac{d\sigma}{d\Omega}(\pi - \theta, q^2)}{\frac{d\sigma}{d\Omega}(\theta, q^2) + \frac{d\sigma}{d\Omega}(\pi - \theta, q^2)} = \frac{\frac{d\sigma}{d\Omega}(\theta, q^2) - \frac{d\sigma}{d\Omega}(\pi - \theta, q^2)}{2 \frac{d\sigma^{\text{Born}}}{d\Omega}(\theta, q^2)}$$

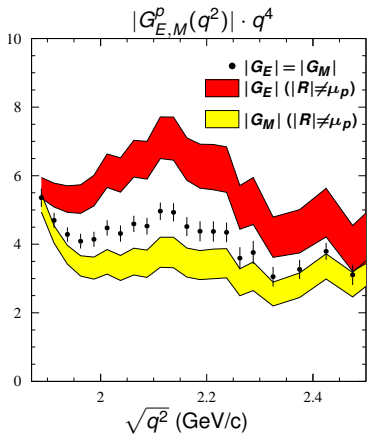




$$|G_{\text{eff}}^p(q^2)|^2 = \frac{\sigma_{p\bar{p}}(q^2)}{\frac{4\pi\alpha^2\beta C}{3s}} \left(1 + \frac{1}{2\tau}\right)^{-1}$$

- Usually what is extracted from the cross section  $\sigma(e^+e^- \rightarrow p\bar{p})$  is the effective time-like form factor  $|G_{\text{eff}}^p|$  obtained assuming  $|G_E^p| = |G_M^p|$  i.e.  $|R| = \mu_p$
- Using DR's to parameterize  $R$  and the *BABAR* data on  $\sigma(e^+e^- \leftrightarrow p\bar{p})$ ,  $|G_E^p|$  and  $|G_M^p|$  may be disentangled
- BESIII can measure separately  $|G_E^p|$  and  $|G_M^p|$

Cfr. talk by Simone Pacetti

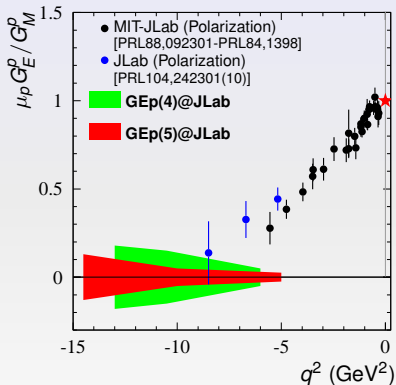


$$|G_M(q^2)|^2 = \frac{\sigma_{p\bar{p}}(q^2)}{\frac{4\pi\alpha^2\beta C}{3s}} \left(1 + \frac{|R(q^2)|}{2\mu_p\tau}\right)^{-1}$$

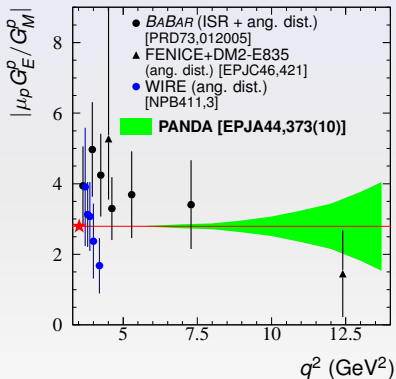
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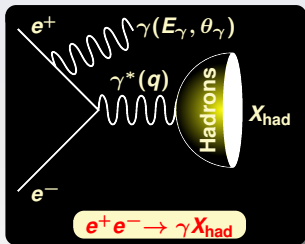
## Space-like region



## Time-like region



# ISR



- Existing results, obtained by **BABAR** (ISR), show interesting and unexpected behaviors, mainly at thresholds, for

$$e^+e^- \rightarrow p\bar{p}$$

and

$$e^+e^- \rightarrow \Lambda\bar{\Lambda}$$

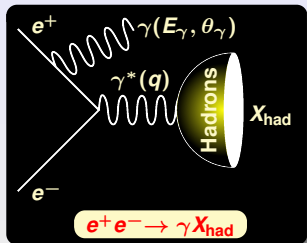
- Only one measurement (**FENICE** with energy scan) for

$$e^+e^- \rightarrow n\bar{n}$$

There are physical limits in reaching the threshold of many of these channels via energy scan (stable hadrons produced at rest can not be detected)

**The Initial State Radiation technique provides a unique tool to access threshold regions working at higher resonances**

# Initial State Radiation



$$\bullet \frac{d^2\sigma}{dE_\gamma d\theta_\gamma} = W(E_\gamma, \theta_\gamma) \cdot \sigma_{e^+e^- \rightarrow X_{\text{had}}}(s)$$

$$\bullet W(E_\gamma, \theta_\gamma) = \frac{\alpha}{\pi x} \left( \frac{2 - 2x + x^2}{\sin^2 \theta_\gamma} \right)$$

- $s = q^2$ ,  $q$  .....  $X_{\text{had}}$  momentum
- $E_\gamma, \theta_\gamma$  ... CM  $\gamma$  energy, scatt. ang.
- $E_{\text{CM}}$  ..... CM  $e^+e^-$  energy
- $x = E_\gamma/2E_{\text{CM}}$

## Advantages

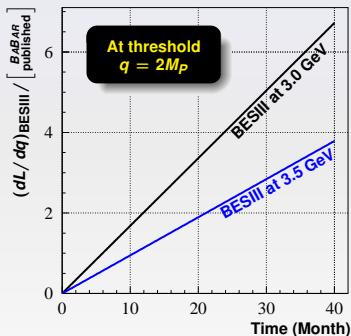
- All energies ( $q^2$ ) at the same time  
 $\Downarrow$   
 Better control on systematics  
 (e.g. greatly reduced point to point)
- Detected ISR  $\Rightarrow$  full  $X_{\text{had}}$  angular coverage
- CM boost  $\Rightarrow$   $\left\{ \begin{array}{l} \text{at threshold } \epsilon \neq 0 \\ \text{energy resolution } \sim 1 \text{ MeV} \end{array} \right.$

# ISR: BESIII vs BABAR

## ISR Luminosity

$$\frac{dL}{dq} = \frac{2q}{E_{\text{cm}}^2} L_{ee} \int_{\cos \theta_{\gamma}^{\min}}^{\cos \theta_{\gamma}^{\max}} W(E_{\gamma}, \theta_{\gamma}) d \cos \theta_{\gamma}$$

$L_{ee}$  ..... total luminosity  
 $\theta_{\gamma}^{\min, \max}$  ..... geom. accept.



**BESIII**

lower CM energy



lower background



ISR  $\gamma$  detection +  $0^\circ$   
and  
No ISR  $\gamma$  detection



×2.5 and ×5  
in statistics

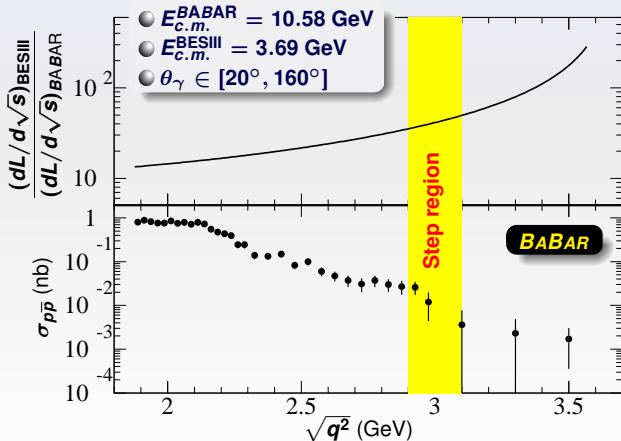


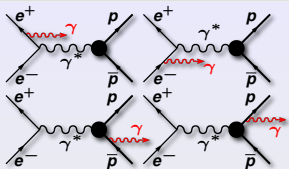
# ISR: BESIII vs *BABAR*

$$\frac{d^2L}{d \cos \theta_\gamma d\sqrt{s}} = \frac{2\sqrt{s} L_{e^+e^-}}{E_{c.m.}^2} \frac{\alpha}{\pi x} \left( \frac{2-2x+x^2}{\sin^2 \theta_\gamma} - \frac{x^2}{2} \right)$$

$L_{e^+e^-}$  = luminosity

$$x = \frac{2E_\gamma}{E_{c.m.}} = 1 - \frac{s}{E_{c.m.}^2}$$



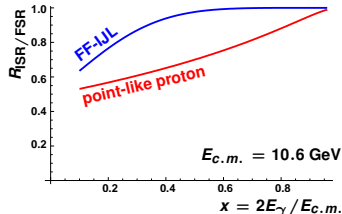
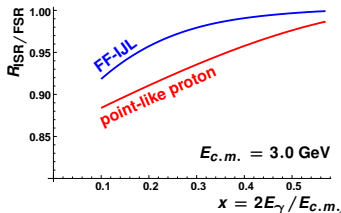


$$\frac{d^2\sigma_{\text{ISR}}}{dE_\gamma d\theta_\gamma} = \frac{\alpha^3 E_\gamma}{3E_{\text{c.m.}}^2 s} \left( |G_M^p(s)|^2 + \frac{|G_E^p(s)|^2}{2\tau} \right) \mathcal{W}(E_\gamma, \theta_\gamma)$$

$$\frac{d^2\sigma_{\text{FSR}}}{dE_\gamma d\theta_\gamma} = \frac{\alpha^3 E_\gamma}{3E_{\text{c.m.}}^4} \mathcal{F} \left[ E_\gamma, \theta_\gamma, G_E^p(E_{\text{c.m.}}^2), G_M^p(E_{\text{c.m.}}^2) \right]$$

**No ISR-FSR interference after  $d\Phi(p\bar{p})$  integration**

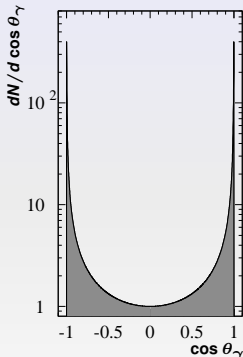
$$R_{\text{ISR/FSR}} = \frac{d\sigma_{\text{ISR}}/dE_\gamma}{d\sigma_{\text{ISR}}/dE_\gamma + d\sigma_{\text{FSR}}/dE_\gamma} [20^\circ \leq \theta_\gamma \leq 160^\circ]$$



**For large values of  $x$  or at small angle  $\theta_\gamma$  of photon emission the final state radiation is strongly suppressed**

# ISR angular distribution and zero-degree tagging

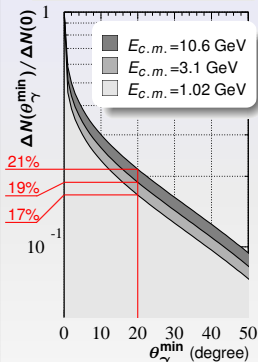
ISR angular distribution peaked at low angles



$$\frac{dN}{d \cos \theta_\gamma} = \frac{1 - \cos^2 \theta_\gamma}{(1 - \beta_e^2 \cos^2 \theta_\gamma)^2}$$

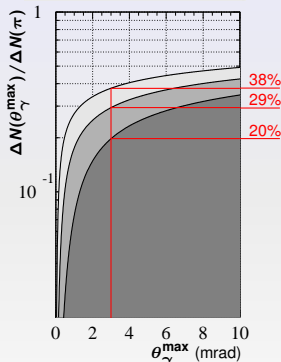
$$\beta_e = \sqrt{1 - 4m_e^2/E_{c.m.}^2}$$

$$\Delta N(\theta_\gamma^{\min}) \propto \int_{\theta_\gamma^{\min}}^{90^\circ} d\theta_\gamma \frac{dN}{d\theta_\gamma}$$



With a typical  $\theta_\gamma^{\min} = 20^\circ$   
 $\sim 80\%$  of events is lost!

$$\Delta N(\theta_\gamma^{\max}) \propto \int_0^{\theta_\gamma^{\max}} d\theta_\gamma \frac{dN}{d\theta_\gamma}$$



With  $\theta_\gamma^{\max} = 3$  mrad more statistics than at wide angle!

# BESIII Zero-Degree Detector

- $J/\psi$ ,  $\psi(2S)$ ,  $\psi(3770)$  resonances decay with high BR's to final states with  $\pi^0$  and  $\gamma_{FS}$  (final state)
- At BESIII these decay channels represent severe backgrounds for typical ISR final states with  $\gamma_{IS}$  detected at wide angle

●  $\pi^0$  and final  $\gamma$  angular distributions are isotropic

● ISR angular distribution is peaked at small angles



A zero-degree radiative photon tagger will suppress most of these backgrounds

A new zero-degree detector (**ZDD**),  
has been installed on summer 2011 at BESIII  
to tag ISR photons  
as well as to measure the luminosity

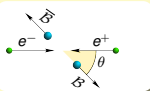
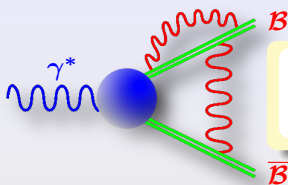


# Pointlike Baryons?

# The Coulomb Factor

## $p\bar{p}$ Coulomb interaction as FSI

[Sommerfeld, Sakharov, Schwinger, Fadin, Khoze]



Annihilation

Coulomb correction

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta C}{4q^2} \left[ (1 + \cos^2 \theta) |G_M|^2 + \frac{1}{\tau} \sin^2 \theta |G_E|^2 \right]$$

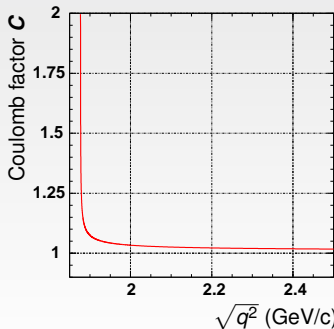
### Distorted wave approximation

$$C = |\Psi_{\text{Coul}}(0)|^2$$

S-wave:  $C = \frac{\frac{\pi\alpha}{\beta}}{1 - \exp\left(-\frac{\pi\alpha}{\beta}\right)} \xrightarrow{\beta \rightarrow 0} \frac{\pi\alpha}{\beta}$

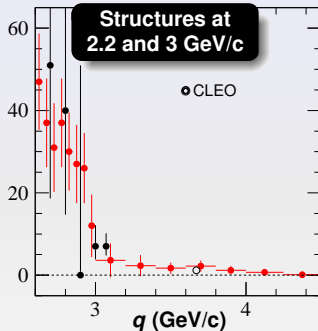
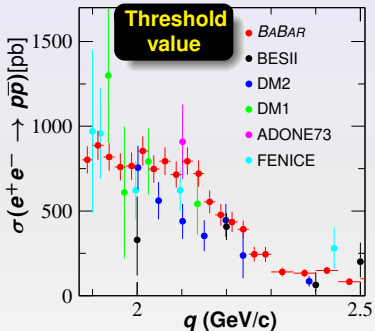
D-wave:  $C = 1$

No Coulomb factor for boson pairs (P-wave)



$$\sigma(e^+e^- \rightarrow p\bar{p}) = \frac{4\pi\alpha^2\beta_p C}{3q^2} \left[ |G_M|^2 + \frac{2M_p^2}{q^2} |G_E|^2 \right]$$

$$C \underset{\beta \rightarrow 0}{\sim} \frac{\pi\alpha}{\beta}$$



$$\sigma(e^+e^- \rightarrow p\bar{p})(4M_p^2) = \frac{\pi^2\alpha^3}{2M_p^2} \frac{\beta_p}{\beta_p} |G^P(4M_p^2)|^2 = 0.85 |G^P(4M_p^2)|^2 \text{ nb}$$

$$|G^P(4M_p^2)| \equiv 1 \quad \text{as pointlike fermion pairs!}$$

Using the ISR technique with only few  $fb^{-1}$  of integrated luminosity BESIII can easily achieve the **BABAR** statistics

# Sommerfeld Enhancement and Resummation Factors

Coulomb Factor  $\mathcal{C}$  for S-wave only:

● Partial wave FF:  $G_S = \frac{2G_M \sqrt{q^2/4M^2} + G_E}{3}$       $G_D = \frac{G_M \sqrt{q^2/4M^2} - G_E}{3}$

● Cross section:  $\sigma(q^2) = 2\pi\alpha^2\beta \frac{4M^2}{(q^2)^2} [\mathcal{C} |G_S(q^2)|^2 + 2|G_D(q^2)|^2]$

$$\mathcal{C} = \mathcal{E} \times \mathcal{R}$$

● Enhancement factor:  $\mathcal{E} = \pi\alpha/\beta$

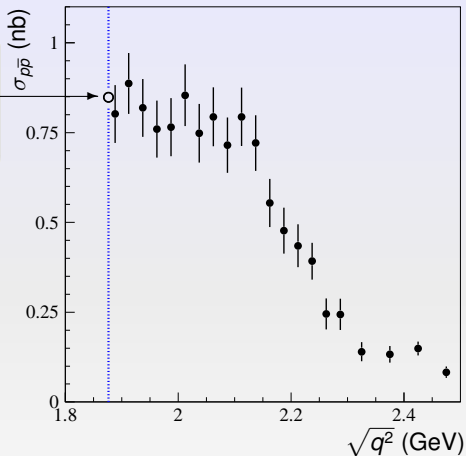
● Step at threshold:  $\sigma_{p\bar{p}}(4M_p^2) = \frac{\pi^2\alpha^3}{2M^2} \frac{\cancel{\beta}}{\cancel{\beta}} |G_S^p(4M_p^2)|^2 = 0.85 |G_S^p(4M_p^2)|^2 \text{ nb}$

● Resummation factor:  $\mathcal{R} = 1/[1 - \exp(-\pi\alpha/\beta)]$

● Few MeV above threshold:  $\mathcal{C} \simeq 1 \Rightarrow \sigma_{p\bar{p}}(q^2) \propto \beta |G_S^p(q^2)|^2$



Expected cross section with  $|G_S^p(4M_p^2)| = 1$



At the threshold

$$\sigma_{p\bar{p}}(4M_p^2) = \frac{\pi^2 \alpha^3}{2M_p^2} \frac{\beta_p}{\beta_p} |G_S^p(4M_p^2)|^2$$

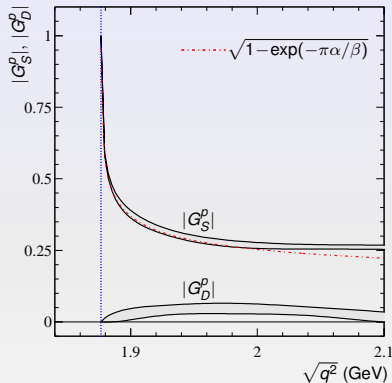
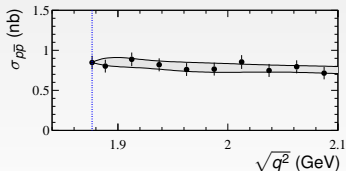
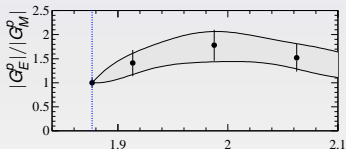
$$\sigma_{p\bar{p}}(4M_p^2) = 0.85 |G_S^p(4M_p^2)|^2 \text{ nb}$$



$|G_S^p(4M_p^2)| \equiv 1$   
as pointlike fermion pairs!

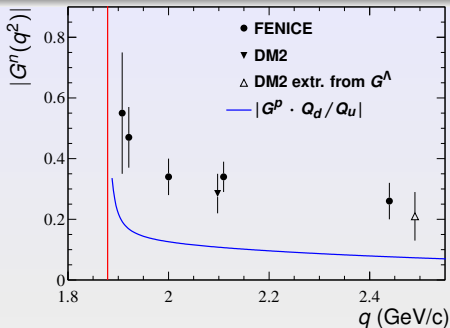
Extracting  $|G_S^p|$  and  $|G_D^p|$  using

- data on  $\sigma_{p\bar{p}}$
- data on  $|G_E^p|/|G_M^p|$
- $G_E^p/G_M^p$  phase  $\phi \simeq 0$



- $|G_S^p| \simeq \sqrt{1 - \exp(-\pi\alpha/\beta)}$
- **No need of resummation factor?**

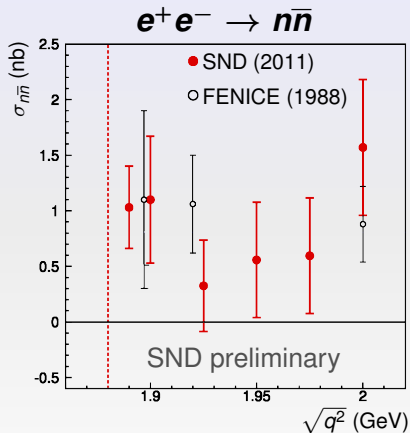
$$e^+ e^- \rightarrow n\bar{n}$$



- Measured only once by FENICE at ADONE
- $\int \mathcal{L} = 500 \text{ nb}^{-1}$  (15' at BESIII)
- $\sim 100$  candidates  $n\bar{n}$  events!
- $\sigma(n\bar{n}) > \sigma(p\bar{p})$ ?
- **Not zero at threshold?**

**BESIII has the unique possibility to measure this cross section**

- $J/\psi \rightarrow n\bar{n}$  (BR  $\simeq 2 \cdot 10^{-3}$ )  $\geq 10^4$  events
- $\psi(2S) \rightarrow n\bar{n}$  (BR  $\simeq 3 \cdot 10^{-4}$ )  $\geq 10^3$  events
- **At threshold by means of ISR (boost)**
- $n, \bar{n}$  detection efficiency and pattern by means of:  
 $J/\psi \rightarrow n(\bar{p}\pi^+)$  and  $J/\psi \rightarrow \bar{n}(p\pi^-)$  ( $\geq 10^5$  events)

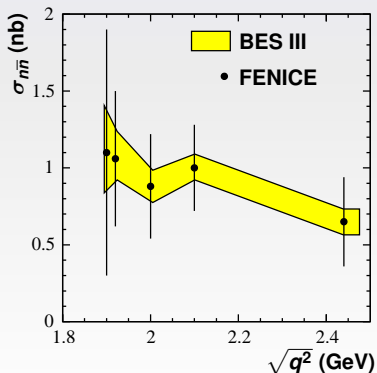


- Scan 2011
- Maximum energy: 2 GeV
- Efficiency  $\sim 30\%$
- Above  $n\bar{n}$  threshold:  
 $\sigma_{n\bar{n}} = 0.8 \pm 0.2$  nb

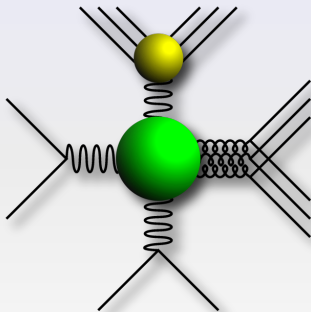
# $p\bar{p}$ and $n\bar{n}$ data from BESIII



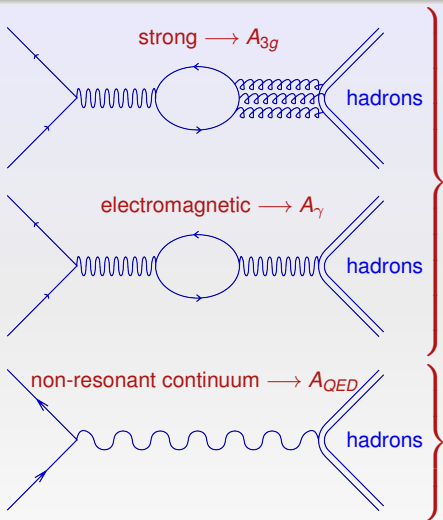
- One year of data taking:  $T = 1.5 \times 10^7$  s
- Average luminosity:  $\bar{\mathcal{L}} = 3 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1}$
- Center of mass energy:  $E_{c.m.} = 3.77 \text{ GeV}$
- Detection efficiencies:  $\epsilon_{n\bar{n}} = 0.4$      $\epsilon_{p\bar{p}} = 0.8$
- Number of events:  $N_{n\bar{n}} \simeq 1000$      $N_{p\bar{p}} \simeq 2000$



# $J/\psi$ strong and electromagnetic phase



# $J/\psi$ strong and electromagnetic decay amplitudes



## Resonant contributions

$$\Phi_p(G_p^M) \sim \Phi_\gamma \quad \Phi_{3g} = 0$$

$$\Phi_\gamma: \text{relative } A_{3g} - A_p$$

- $J/\psi \rightarrow N\bar{N}$   $\Phi_p = 89^\circ \pm 15^\circ$  [1]
- $J/\psi \rightarrow VP (1^-0^-)$   $\Phi_p = 106^\circ \pm 10^\circ$  [2]
- $J/\psi \rightarrow PP (0^-0^-)$   $\Phi_p = 89.6^\circ \pm 9.9^\circ$  [3]
- $J/\psi \rightarrow VV (1^-1^-)$   $\Phi_p = 138^\circ \pm 37^\circ$  [3]

**NO INTERFERENCE!**

## Non-resonant continuum

- affects the measured BR [4]
- affects  $\Phi_p$  [4]

**INTERFERENCE WITH  $A_{3g}$ !**

[1] R. Baldini, C. Bini, E. Luppi, Phys. Lett. B404, 362 (1997); R. Baldini et al., Phys. Lett. B444, 111 (1998).

[2] L. Kopke and N. Wermes, Phys. Rep. 174, 67 (1989); J. Jousset et al., Phys. Rev. D41,1389 (1990).

[3] M. Suzuki et al., Phys. Rev. D60, 051501 (1999).

[4] P. Wang, arXiv:hep-ph/0410028v2 and references therein.

## IMAGINARY AMPLITUDES HARD TO BE EXPLAINED!

- $J/\psi \subset$  perturbative regime (  $\leftarrow \Gamma_{J/\psi} \sim 93\text{KeV}$  )
- pQCD  $\rightarrow$  real  $A_\gamma, A_{3g}$
- QCD does not provide sizeable imaginary amplitudes ( $\Phi_p$   $10^\circ$  at most [1])
- a  $J/\psi - V$  glueball mixing [2] may explain imaginary amplitudes; and  $\psi(2S)$ ?
- determination of phases  $\Phi_p$  rely on theoretical hypotheses

## EXPERIMENTAL DATA

- no interference term in the inclusive  $J/\psi$  and  $\psi(2S)$  production
- early evidence of an interf. term in  $e^+e^- \rightarrow J/\psi \rightarrow \mu^+\mu^-$  @ SLAC [3]
- no clear evidence of interf. or glueball in  $e^+e^- \rightarrow J/\psi \rightarrow \rho\pi$  @ BESII [4]

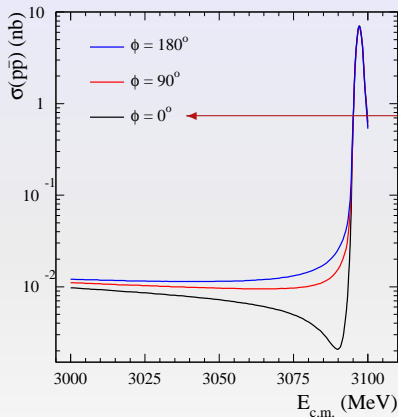
[1] J. Bolz and P. Kroll, WU B 95-35.

[2] S.J. Brodsky, G.P. Lepage, S.F. Tuan, Phys. Rev. Lett. 59, 621 (1987).

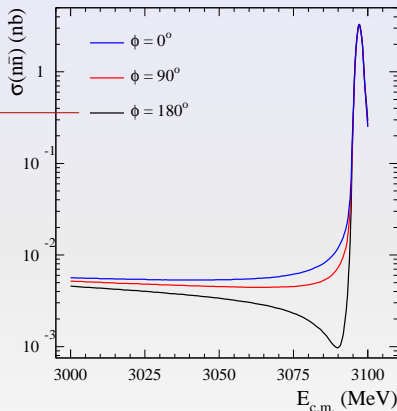


# Simulated $e^+e^- \rightarrow N\bar{N} @ s \sim M_{J/\psi}^2$

interference must have opposite sign as magnetic moments



continuum reference:  $\sigma(e^+e^- \rightarrow p\bar{p}) \sim 11 \text{ pb}$  [1]



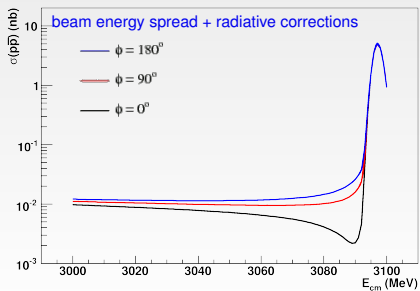
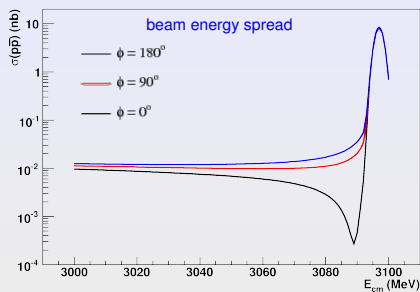
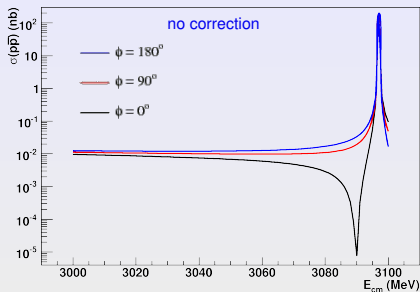
continuum reference:  $\sigma(e^+e^- \rightarrow n\bar{n}) \sim 5 \text{ pb}$  [1,2]

radiative corrections and beam energy spread (BESIII) included!

[1] B. Aubert et al. [BABAR Collaboration], Phys. Rev. D 73, 012005 (2006).

[2] R. Baldini, S. Pacetti, A. Zallo, arxiv:0812.3283 [hep-ph].

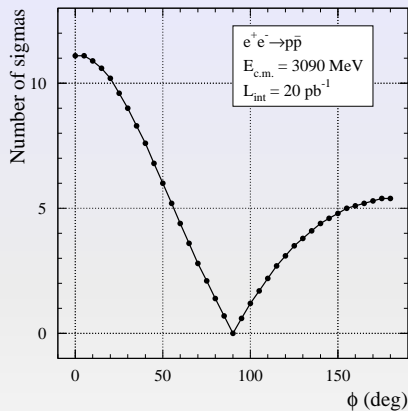
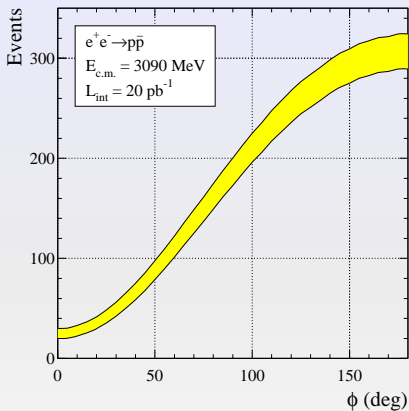
# Simulated $e^+e^- \rightarrow p\bar{p}$ @ $s \sim M_{J/\psi}^2$ - BESIII scenario



## CORRECTIONS NEEDED!

- small effects from beam energy spread
- significant suppression from radiative corrections

# Simulated $e^+e^- \rightarrow p\bar{p}$ @ $s \sim M_{J/\psi}^2$ ( $20 \text{ pb}^{-1}$ )

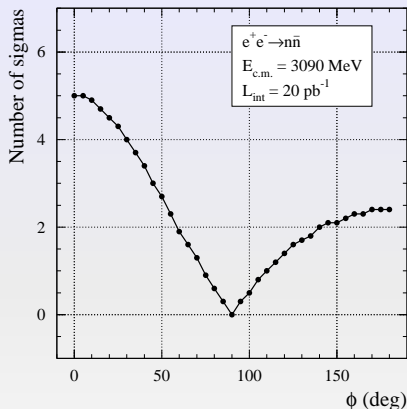
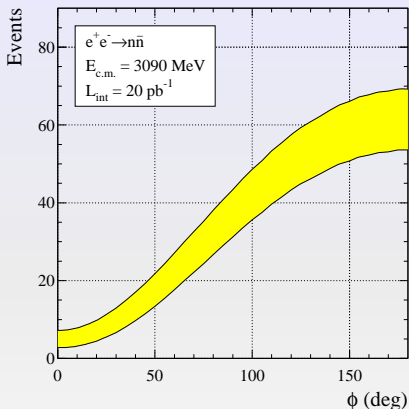


continuum reference:  $\sigma(e^+e^- \rightarrow p\bar{p}) \sim 11 \text{ pb}$  [1]

radiative corrections and beam energy spread (BESIII) included!

[1] B. Aubert et al. [BABAR Collaboration], Phys. Rev. D 73, 012005 (2006).

# Simulated $e^+e^- \rightarrow n\bar{n}$ @ $s \sim M_{J/\psi}^2$ ( $20 \text{ pb}^{-1}$ )



continuum reference:  $\sigma(e^+e^- \rightarrow n\bar{n}) \sim 5 \text{ pb}$  [1,2]

radiative corrections and beam energy spread (BESIII) included!

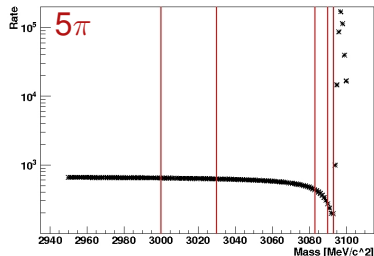
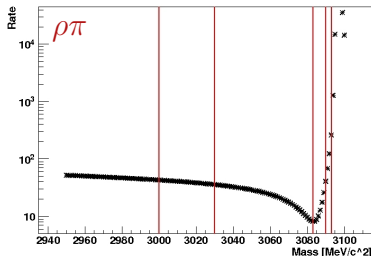
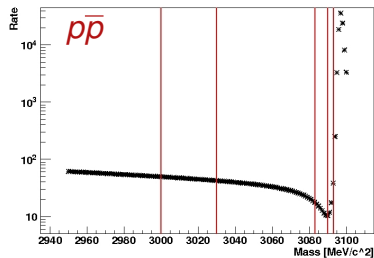
[1] B. Aubert et al. [BABAR Collaboration], Phys. Rev. D 73, 012005 (2006).

[2] R. Baldini, S. Pacetti, A. Zallo, hep-ph0812.328v2.

# 2012 $J/\psi$ line shape scan at BESIII

Energy selection depends on the process

- 2 points at low  $\sqrt{s}$ :
  - fix continuum
  - fix slope
- 2 points at the deep
- 1 point at resonance raise



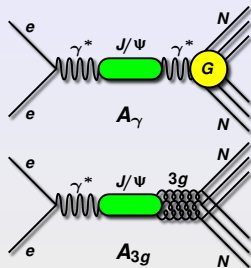
Energy requested [MeV]	Energy collected [MeV]	$L_{int}$ [ $pb^{-1}$ ]
3050	3046	14.0
3060	3056	14.0
3083	3086	16.5
3090	3085	14.0
3093	3088	14.0
3097	3097	79.6

**Analysis in progress!**

# Measurement of $J/\psi \rightarrow p\bar{p}, n\bar{n}$

- dominant strong amplitude:  $|A_{3g}^N| > |A_\gamma^N|$
- isospin symmetry  $\rightarrow |A_{3g}^p| = |A_{3g}^n|$
- $A_\gamma^p = -A_\gamma^n$  as magnetic moments
- assuming pQCD:  $\text{Im } A_{3g}^N \sim 0$

$$\frac{B(J/\psi \rightarrow n\bar{n})}{B(J/\psi \rightarrow p\bar{p})} = \left| \frac{A_{3g}^n + A_\gamma^n}{A_{3g}^p + A_\gamma^p} \right|^2 \sim 2$$

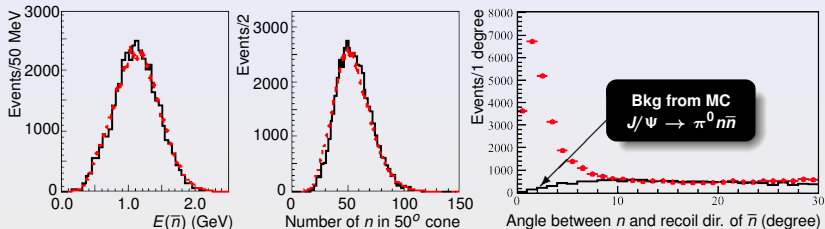


- BESII at BEPC [PLB591,42]:  $B(J/\psi \rightarrow p\bar{p}) = (2.26 \pm 0.01 \pm 0.14) \times 10^{-3}$
- FENICE at ADONE [PLB444,111]:  $B(J/\psi \rightarrow n\bar{n}) = (2.2 \pm 0.4) \times 10^{-3}$

$$B(J/\psi \rightarrow p\bar{p}) \simeq B(J/\psi \rightarrow n\bar{n})$$

$\Downarrow$   
 large  $A_{3g}^N - A_\gamma^N$  relative phase

## $n\bar{n}$ identification


**BESIII**

$$B(J/\psi \rightarrow n\bar{n}) = (2.07 \pm 0.01 \pm 0.17) \cdot 10^{-3}$$

$$B(J/\psi \rightarrow p\bar{p}) = (2.112 \pm 0.004 \pm 0.031) \cdot 10^{-3}$$

**PDG**

$$B(J/\psi \rightarrow n\bar{n}) = (2.2 \pm 0.4) \cdot 10^{-3}$$

$$B(J/\psi \rightarrow p\bar{p}) = (2.17 \pm 0.07) \cdot 10^{-3}$$

$$\Phi = (88.7 \pm 8.1)^\circ$$

large phase between strong and e.m. amplitudes!



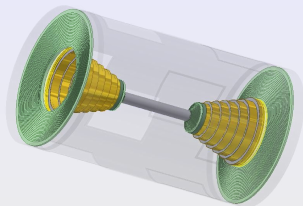
- Asymptotic behavior not well understood
  - Pointlike behavior not only at threshold
  - Sommerfeld resummation factor needed?
  - Neutral baryons puzzle
- 
- More precise data on  $\sigma_{p\bar{p}}$  above 3 GeV allow:
    - accurate study of the step around 3 GeV
    - precise measurement of the ratio  $|G_E^p|/|G_M^p|$
  - Unique possibility to measure the  $n\bar{n}$  cross section thanks to ISR and scan
  - Measurement of the relative phase between e.m. and strong amplitudes in  $J/\psi \rightarrow N\bar{N}$  decays
  - First BESIII results confirm a large phase scenario and considerably improve PDG data on  $J/\psi \rightarrow N\bar{N}$ .

# BACK-UP SLIDES

# BESIII main features

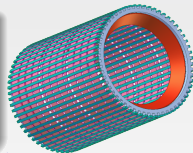
## Drift Chamber

- Low gas mixture (60% He, 40% Propane)
- Carbon filter cylinders:  $R_{in} = 6.3 \text{ cm}$ ,  $T_{in} = 1 \text{ mm}$ ,  
 $R_{out} = 81 \text{ cm}$   $T_{out} = 1 \text{ cm}$
- 6 Al stepped flanges:  $T = 1.8 \text{ cm}$
- 43 layers: 7000  $25 \mu\text{m}$  gold-plated sense wires,  
22000 Al field-shaping wires
- $\sigma_{x,y} \sim 130 \mu\text{m}$ ,  $\sigma(De/dx) \sim 6\%$



## Csl Calorimeter

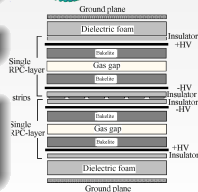
- 6240 Csl(Tl): 5280 Barrel, 960 Endcaps, 13000 photodiodes
- $28 \times 5.2^2 \text{ cm}^3$
- $\Delta E/E \sim 2.5\%$  at 1 GeV, noise  $\sim 220 \text{ keV}$

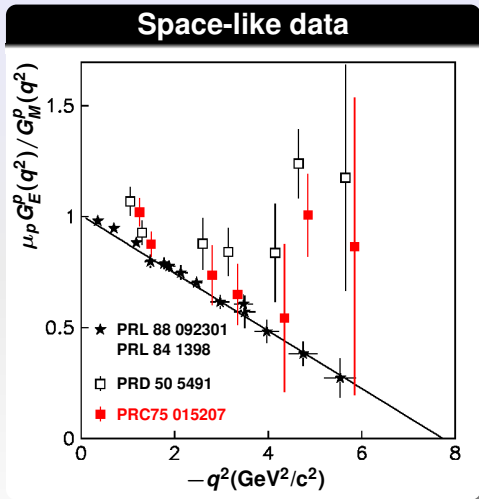


## Superconducting Magnet: 1 T

## RPC $\mu$ Chambers

9/8 layers Barrel/Endcaps, Strip  $x, y$  4cm  
Plastic foil instead linseed oil: noise  $\sim 0.1 \text{ Hz/cm}^2$ ,  $\epsilon \sim 95\%$





$$G_E^p = F_1^p + \frac{q^2}{4M_p^2} F_2^p$$

$$G_M^p = F_1^p + F_2^p$$

**Space-like**

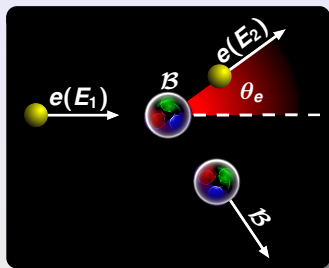
$F_1$  and  $\frac{q^2}{4M_p^2} F_2$  cancellation

$$\frac{G_E^p(q^2)}{G_M^p(q^2)} < 1$$

**Time-like**

$F_1$  and  $\frac{q^2}{4M_p^2} F_2$  enhancement

$$\left| \frac{G_E^p(q^2)}{G_M^p(q^2)} \right| > 1$$



## Rosenbluth formula

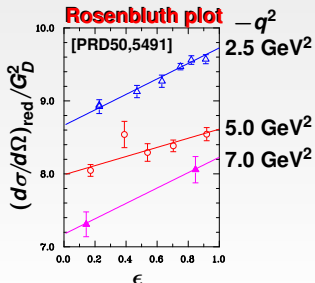
$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \frac{1}{1-\tau} \left[ G_E^2 - \frac{\tau}{\epsilon} G_M^2 \right] \quad \tau = \frac{q^2}{4M_N^2}$$

- Mott pointlike cross section

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} = \frac{4\alpha^2}{(-q^2)^2} \frac{E_2^3}{E_1} \cos^2(\theta_e/2)$$

- Photon polarization

$$\epsilon = \left[ 1 + 2(1 - \tau) \tan^2(\theta_e/2) \right]^{-1}$$



## Reduced cross section

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{red}} = \frac{\epsilon(1-\tau)}{\tau} \frac{(d\sigma/d\Omega)_{\text{exp}}}{(d\sigma/d\Omega)_{\text{Mott}}} = G_M^2 - \frac{\epsilon}{\tau} G_E^2$$

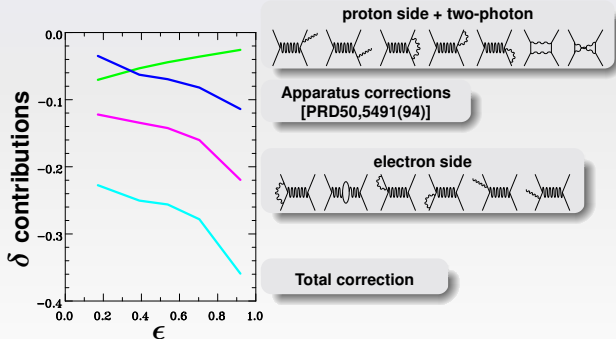
- $(d\sigma/d\Omega)_{\text{red}}(\epsilon)$  slope  $\rightarrow G_E$
- $(d\sigma/d\Omega)_{\text{red}}(\epsilon)$  intercept  $\rightarrow G_M$

# Radiative corrections in Rosenbluth separation

Sachs form factors  $G_E$  and  $G_M$  are extracted from Born cross sections (one- $\gamma$  exchange)

The Born term is obtained from experimental cross sections correcting for radiative effects

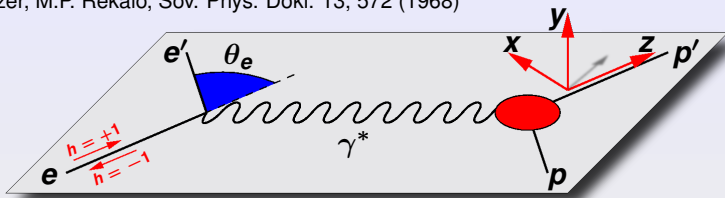
$$\frac{d\sigma^{\text{exp}}}{d\Omega} = (1 + \delta) \frac{d\sigma^{\text{Born}}}{d\Omega}$$



$\delta$  depends on  $\epsilon$   
↓  
It affects the slope in Rosenbluth plot

# Polarization observables

A.I. Akhiezer, M.P. Rekalov, Sov. Phys. Dokl. 13, 572 (1968)



- Elastic scattering of longitudinally polarized ( $h = \pm 1$ ) electrons on nucleon target
- Hadronic tensor:  $W_{\mu\nu} = \underbrace{W_{\mu\nu}(0)}_{\text{no pol.}} + \underbrace{W_{\mu\nu}(\vec{P}) + W_{\mu\nu}(\vec{P}')}_{\text{ini. or fin. pol. of } N} + \underbrace{W_{\mu\nu}(\vec{P}, \vec{P}')}_{\text{ini. and fin. pol. of } N}$
- In case of polarized ( $h = \pm 1$ ) electrons on unpolarized nucleon target:

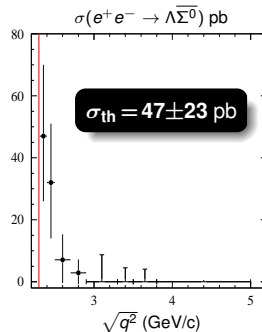
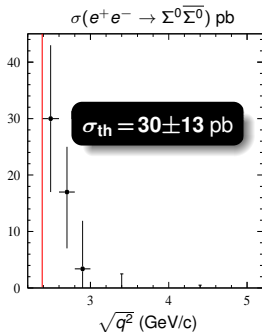
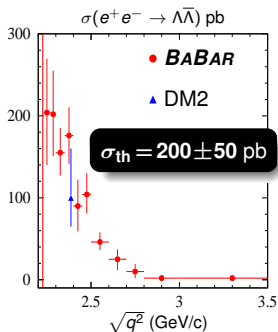
$$P'_x = -\frac{2\sqrt{\tau(\tau-1)}}{G_E^2 - \frac{\tau}{\epsilon} G_M^2} G_E G_M \tan\left(\frac{\theta_e}{2}\right)$$

$$P'_z = \frac{(E_e + E'_e)\sqrt{\tau(\tau-1)}}{M(G_E^2 - \frac{\tau}{\epsilon} G_M^2)} G_M^2 \tan^2\left(\frac{\theta_e}{2}\right)$$

$$\frac{P'_x}{P'_z} = -\frac{2M \cot(\theta_e/2)}{E_e + E'_e} \frac{G_E}{G_M}$$

$$\sigma(e^+e^- \rightarrow B^0\bar{B}^0) = \frac{4\pi\alpha^2\beta C_0}{3q^2} \left[ |G_M^{B^0}|^2 + \frac{2M_{B^0}^2}{q^2} |G_E^{B^0}|^2 \right] \xrightarrow{q \rightarrow 2M_{B^0}} \frac{\pi\alpha^2\beta}{2M_{B^0}^2} |G^{B^0}|^2 \rightarrow 0$$

**No Coulomb correction at hadron level:  $C_0 = 1$**



Remnant of  
Coulomb interactions  
at quark level?



$$C_0 \propto \beta^{-1}$$

as  $q \rightarrow 2M_{B^0}$



For any neutral baryon

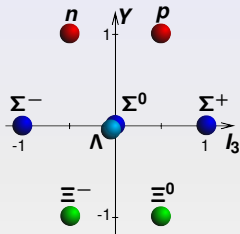
$$\sqrt{\sigma_{B^0\bar{B}^0}} \propto \frac{|G^{B^0}|}{M_{B^0}}$$



Coulomb correction  
at quark level

$$\sqrt{\sigma_{B^0 \bar{B}^0} (4M_{B^0}^2)} = K \cdot \frac{|G_{B^0}^{\Sigma^0}|}{M_{B^0}}$$

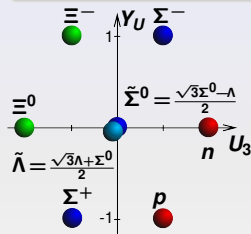
$K$  is unknown but equal  
for all neutral baryons  
with equal quark content



$$(Y, I_3) \rightarrow (Y_U, U_3)$$

$$U_3 = -\frac{1}{2} I_3 + \frac{3}{4} Y$$

$$Y_U = -Q$$



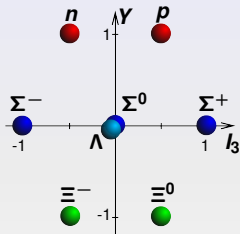
Indirect relation:  $G^{\Sigma^0} - G^\Lambda + \frac{2}{\sqrt{3}} G^{\Lambda\Sigma^0} = 0$

$$M_{\Sigma^0} \sqrt{\sigma_{\Sigma^0 \bar{\Sigma}^0}} - M_\Lambda \sqrt{\sigma_{\Lambda \bar{\Lambda}}} + \frac{2}{\sqrt{3}} M_{\Lambda\Sigma^0} \sqrt{\sigma_{\Lambda\Sigma^0}} = (-0.06 \pm 6.0) \times 10^{-4}$$

Coulomb correction  
at quark level

$$\sqrt{\sigma_{B^0 \bar{B}^0} (4M_{B^0}^2)} = K \cdot \frac{|G_{B^0}^{\Sigma^0}|}{M_{B^0}}$$

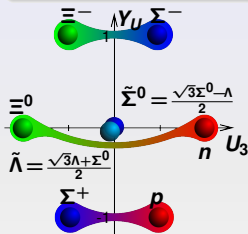
$K$  is unknown but equal  
for all neutral baryons  
with equal quark content



$$(Y, I_3) \rightarrow (Y_U, U_3)$$

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$$Y_U = -Q$$

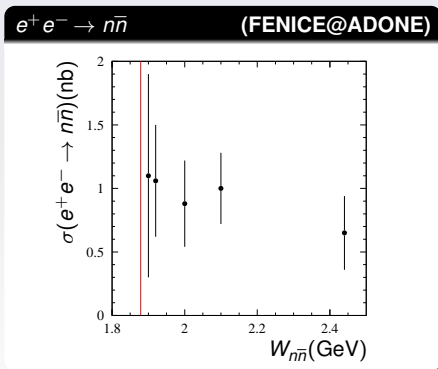


Indirect relation:  $G^{\Sigma^0} - G^{\Lambda} + \frac{2}{\sqrt{3}} G^{\Lambda\Sigma^0} = 0$

$$M_{\Sigma^0} \sqrt{\sigma_{\Sigma^0 \bar{\Sigma}^0}} - M_{\Lambda} \sqrt{\sigma_{\Lambda \bar{\Lambda}}} + \frac{2}{\sqrt{3}} M_{\Lambda\Sigma^0} \sqrt{\sigma_{\Lambda\Sigma^0}} = (-0.06 \pm 6.0) \times 10^{-4}$$

# Data and $U$ -spin predictions at threshold

- $M_{\Sigma^0} \sqrt{\sigma_{\Sigma^0 \Sigma^0}} - M_{\Lambda} \sqrt{\sigma_{\Lambda \bar{\Lambda}}} + \frac{2}{\sqrt{3}} M_{\Lambda \Sigma^0} \sqrt{\sigma_{\Lambda \Sigma^0}} = (-0.06 \pm 6.0) \times 10^{-4}$
- $\sigma(e^+ e^- \rightarrow n \bar{n}) = \frac{1}{4} (3 \sqrt{\sigma_{\Lambda \bar{\Lambda}}} M_{\Lambda} - \sqrt{\sigma_{\Sigma^0 \Sigma^0}} M_{\Sigma})^2 \frac{1}{M_n^2} = 0.5 \pm 0.2 \text{ nb}$

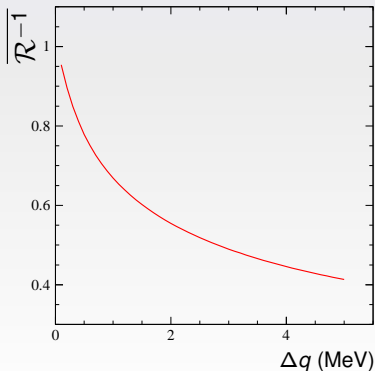
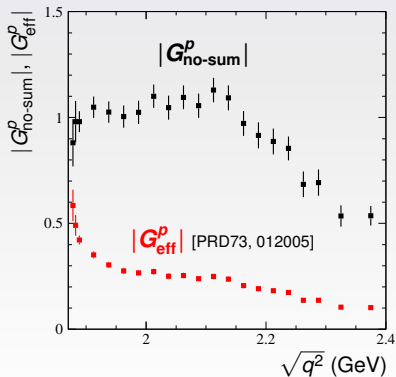


$$|G_{\text{eff}}^p|^2 = \frac{\sigma_{p\bar{p}}(q^2)}{\mathcal{C} \frac{16\pi\alpha^2}{3} \frac{\sqrt{1-1/\tau}}{4q^2} \left(1 + \frac{1}{2\tau}\right)}$$

$$|G_{\text{no-sum}}^p|^2 = \frac{\sigma_{p\bar{p}}(q^2)}{\mathcal{E} \frac{16\pi\alpha^2}{3} \frac{\sqrt{1-1/\tau}}{4q^2} \left(1 + \frac{1}{2\tau}\right)}$$

$$\overline{\mathcal{R}^{-1}} = \frac{1}{\Delta q} \int_0^{\Delta q} \left[1 - e^{-\frac{\pi\alpha}{\beta}}\right] d\sqrt{q^2}$$

$$\Delta q = \sqrt{q^2} - 2M_p$$



# $J/\psi$ strong and electromagnetic decay amplitudes



resonant



non resonant

$$x = \frac{M_{J/\psi} - \sqrt{s}}{\Gamma_{TOT}/2} \quad A_R = \alpha \left( \frac{x}{1+x^2} + i \frac{1}{1+x^2} \right)$$

$$\Phi_\alpha = \arctan \frac{|A_\gamma| \sin \Phi_p}{|A_{3g}| + |A_\gamma| \cos \Phi_p}$$

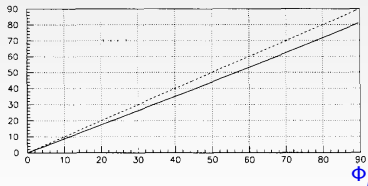
$$\Phi_{A_\gamma} \sim \Phi_p = \Phi_{G_p^M} \quad A_{NR} = -\beta e^{i\Phi_p}$$

$$\beta = \sqrt{\sigma(e^+e^- \leftrightarrow p\bar{p})}$$

$$G_p^M \text{ real @ } W \sim M_{J/\psi} \quad [1]$$

$$\Delta\Phi = \Phi_p - \Phi_\alpha \sim \Phi_p$$

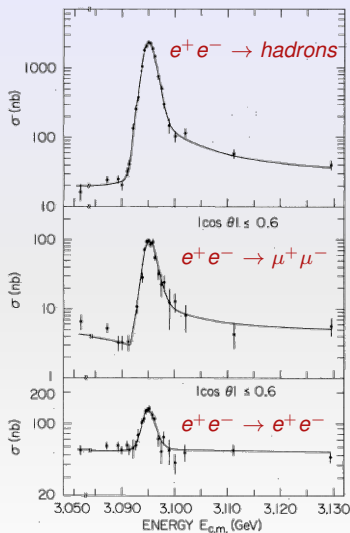
$\Delta\Phi$



$$\begin{aligned} I(x) &= |A_R + A_{NR}|^2 \\ &= \frac{\alpha^2}{1+x^2} + \beta^2 - \frac{2\beta\alpha}{1+x^2} (x \cos \Delta\Phi + \sin \Delta\Phi) \end{aligned}$$

[1] S.J. Brodsky, G.P. Lepage, S.F. Tuan, Phys. Rev. Lett. 59, 621 (1987).

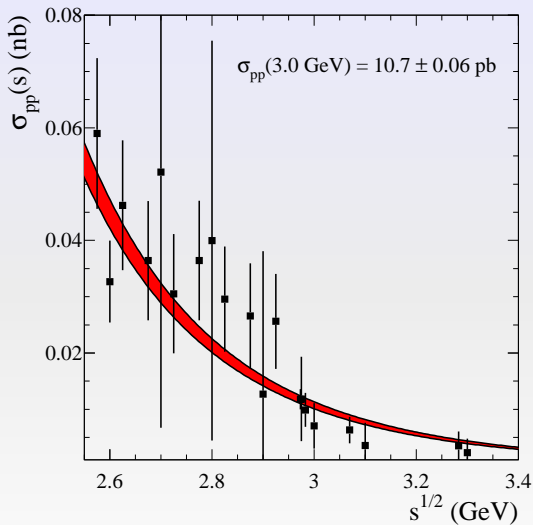
# Early evidence of interference in $e^+e^- \rightarrow \mu^+\mu^-$



$J/\psi$  production  
@ SPEAR (SLAC) [1]

[1] R. Baldini, C. Bini, E. Lippi, Phys. Lett. B404, 362 (1997).

# Simulated $e^+e^- \rightarrow p\bar{p} @ s \sim M_{J/\psi}^2$ ( $20 \text{ pb}^{-1}$ )



[1] B. Aubert et al. [BABAR Collaboration], Phys. Rev. D 73, 012005 (2006).