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Measuring the CKM γ angle with $B^0 \rightarrow DK^{*0}$ decay at LHCb

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LHC France
Annecy

Alexandra MARTÍN SÁNCHEZ (LAL, Orsay)

The γ angle of the CKM theory

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- Quark mixing:

mass eigenstates \neq interaction eigenstates

→ Cabibbo-Kobayashi-Maskawa matrix (CKM)

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

CKM matrix

- 3 x 3 matrix → can be parametrised by three real parameters and a complex phase

Usually: Wolfenstein parametrisation

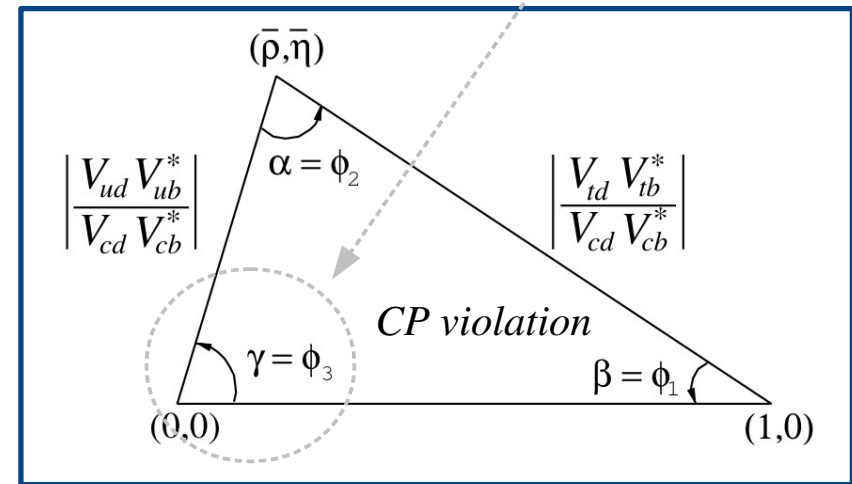
$$V = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

- Rotation matrix → unitarity

$$V V^* = I$$

$$\underbrace{V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^*}_{=0} = 0$$

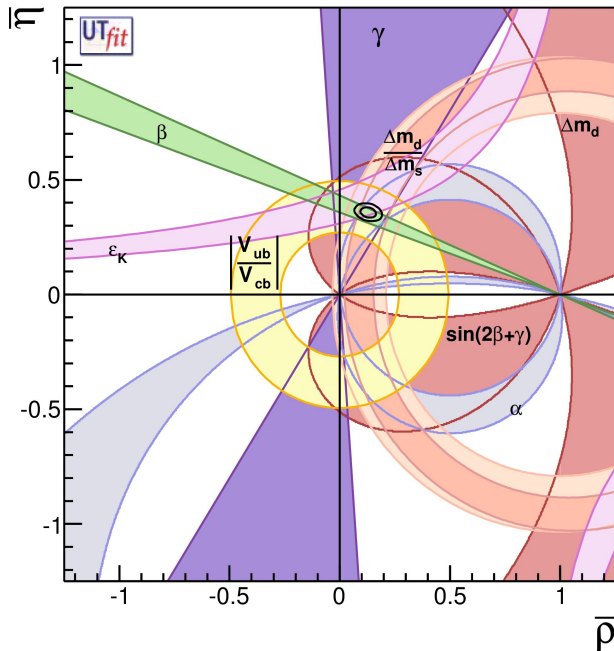
The γ angle



CKM Unitary Triangle

State of the art

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UTfit:

$$\alpha = (88.7 \pm 3.1)^\circ$$

$$\beta = (21.95 \pm 0.87)^\circ$$

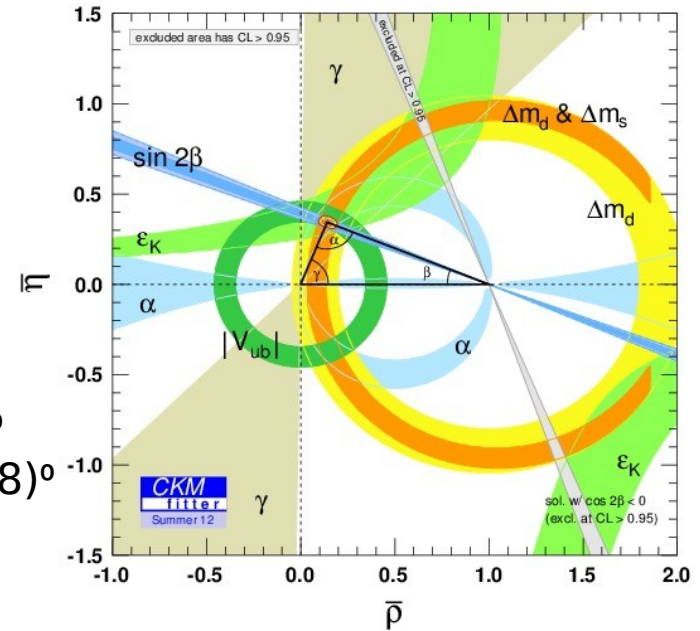
$$\gamma = (69.2 \pm 3.2)^\circ$$

CKM fitter:

$$\alpha = (90.5 \pm 4.3)^\circ$$

$$\beta = (21.73 \pm 0.78)^\circ$$

$$\gamma = (67.7 \pm 4.3)^\circ$$



- Unitary Triangle well constrained from B factories, Tevatron and LHC results.
- Global fits combine all results in order to determine the different CKM parameters.
 - γ is the one known with the **largest uncertainty**.

$$\gamma^{\text{BaBar}} = (69 \pm 17)^\circ$$

$$\gamma^{\text{Belle}} = (68 \pm 15)^\circ$$

$$\gamma^{\text{LHCb}} = (71.1 \pm 16.7)^\circ$$

Large uncertainties in the γ **direct measurements compared with the global fits**. Need to measure γ precisely to check the Unitary Triangle consistency.

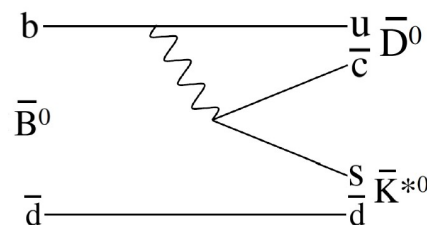
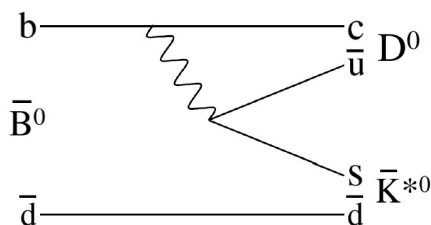
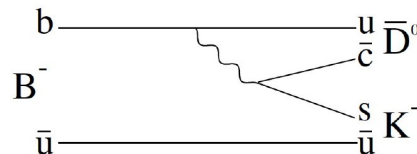
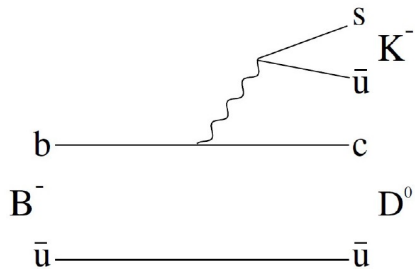
Measuring γ at the tree level

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- From the Unitary Triangle:

$$\gamma = \arg \left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right)$$

- With **tree diagrams**, γ is measured from decays involving the **interference** of a $b \rightarrow u$ (V_{ub}) transition and a $b \rightarrow c$ (V_{cb}) transition.
 - No physics beyond the Standard Model contributions (no loops).
 - Typically decays of the type $B^{\pm,0} \rightarrow DK^{\pm,*0}$.

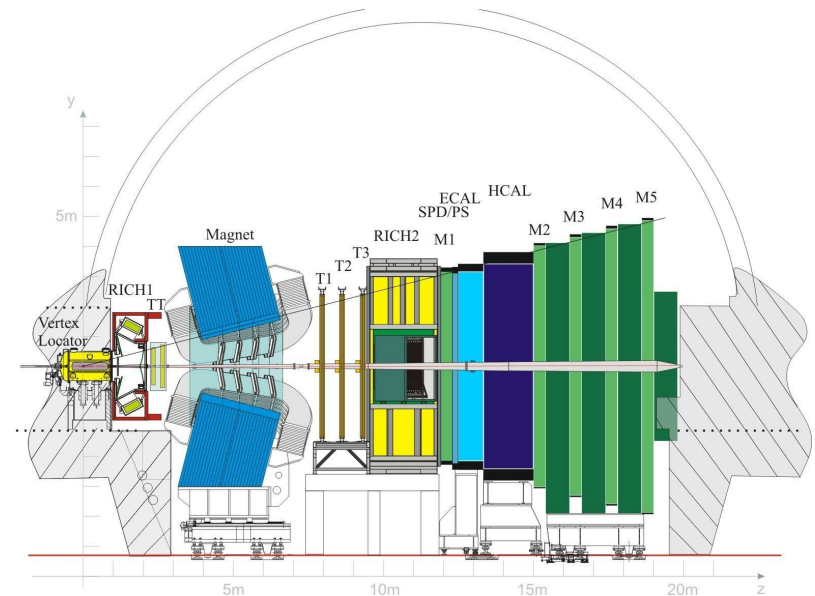


- When the **same final state** is accessible for both D^0 and \bar{D}^0 , the interference can be studied.
 - Access to γ from the **measurement of CP observables** (asymmetries between $B^{0,+}$ and $\bar{B}^{0,-}$ signal yields).

$B \rightarrow DK$ decays at LHCb

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- LHCb detector well suited for the study of heavy flavoured hadronic decays, thanks to:
 - Geometry, $2 < \eta < 5$.
 - Vertex locator:
 - Precise reconstruction of primary and secondary vertices (resolution = 45 fs for $B_s \rightarrow J/\psi \varphi$ and for $B_s \rightarrow D_s \pi$).
 - RICHs particle identification detectors:
 - Excellent $K - \pi$ separation (K identification efficiency = 95 % with 5 % of π misidentification).
 - LHC collision energy:
 - All type of B hadrons produced (B^\pm , B^0 , B_s^0 , b -baryons, B_c^\pm).
 - Big boost, long-lived particles fly over long distances.
 - Easy secondary vertex separation.
 - Hadronic trigger (HCAL+ECAL):
 - Able to select B decays to open charm purely hadronic final states.



More information in
S. T'jampens talk of yesterday

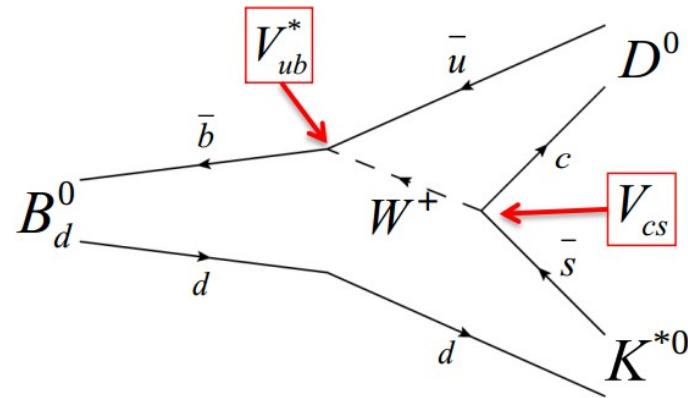
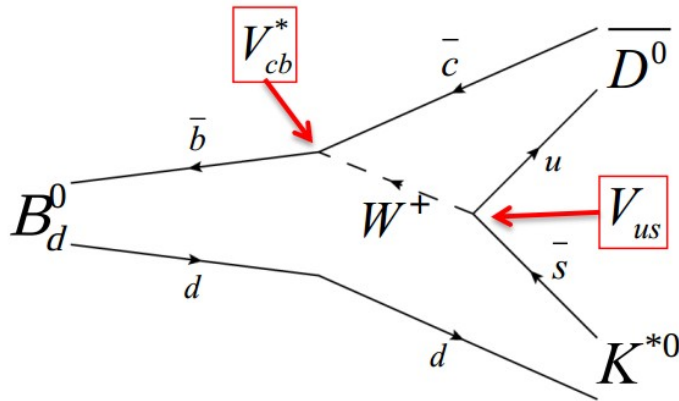
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$B^0 \rightarrow D K^{*0}$ analysis at LHCb

$B^0 \rightarrow D K^{*0}$ introduction

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- Sensitivity to the CKM weak phase γ :



- Both decays are colour suppressed \rightarrow larger ratio of amplitudes between the two diagrams, **enhanced interference** (compared to $B^\pm \rightarrow DK^\pm$, which is the “usual” mode for measuring γ).
- Small branching fractions.
- $K^{*0} \rightarrow K^+ \pi^- \rightarrow$ **self-tagged decay**, the flavour of the B known from the sign of the K from the K^{*0} in the final state.
- Different methods to extract γ depending on the D decay mode:
 - **GLW** (Gronau, London, Wyler): $D \rightarrow K^+ K^-$ (CP eigenstates).
 - **ADS** (Atwood, Dunietz, Soni): **suppressed** $D \rightarrow K^- \pi^+$ (flavour specific final state).
 - **GGSZ** (Giri, Grossman, Soffer, Zupan): $D \rightarrow$ **multi-body decay**.

Analysis overview

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- $B^0 \rightarrow D K^{*0}$, $D \rightarrow K^+ K^-$ (signal channel), $D \rightarrow K^+ \pi^-$ (favoured, normalisation channel)
- GLW analysis, sensitive to the γ angle.
- Cut-based analysis using 1 fb^{-1} of 2011 data.
- Measurement of *CP* asymmetries and ratios built from the partial widths of $B^0 \rightarrow D K^{*0}$, and its conjugate $\bar{B}^0 \rightarrow D \bar{K}^{*0}$ decay.
 - Which depend on γ .
 - Together with
 - the ratios of amplitudes $r_{B^0, D}$,
 - strong phases $\delta_{B^0, D}$ and the
 - K^{*0} coherence factor κ .

$$\begin{aligned}
 \mathcal{A}_d^{KK} &= \frac{\Gamma(\bar{B}^0 \rightarrow [K^+ K^-]_D \bar{K}^{*0}) - \Gamma(B^0 \rightarrow [K^+ K^-]_D K^{*0})}{\Gamma(\bar{B}^0 \rightarrow [K^+ K^-]_D \bar{K}^{*0}) + \Gamma(B^0 \rightarrow [K^+ K^-]_D K^{*0})} \\
 &= \frac{\pm 2\kappa r_{B^0} \sin \delta_{B^0} \sin \gamma}{1 + r_{B^0}^2 \pm 2\kappa r_{B^0} \cos \delta_{B^0} \cos \gamma}, \\
 \mathcal{R}_d^{KK} &= \frac{\Gamma(\bar{B}^0 \rightarrow [K^+ K^-]_D \bar{K}^{*0}) + \Gamma(B^0 \rightarrow [K^+ K^-]_D K^{*0})}{\Gamma(\bar{B}^0 \rightarrow [K^- \pi^+]_D \bar{K}^{*0}) + \Gamma(B^0 \rightarrow [K^+ \pi^-]_D K^{*0})} \\
 &= \frac{1 + r_{B^0} \pm 2\kappa r_{B^0} \cos \delta_{B^0} \cos \gamma}{1 + r_{B^0}^2 r_D^2 \pm 2\kappa r_{B^0} r_D \cos(\delta_{B^0} + \delta_D) \cos \gamma}, \\
 \mathcal{A}_s^{KK} &= \frac{\Gamma(B_s^0 \rightarrow [K^+ K^-]_D \bar{K}^{*0}) - \Gamma(\bar{B}_s^0 \rightarrow [K^+ K^-]_D K^{*0})}{\Gamma(B_s^0 \rightarrow [K^+ K^-]_D \bar{K}^{*0}) + \Gamma(\bar{B}_s^0 \rightarrow [K^+ K^-]_D K^{*0})}, \\
 \mathcal{A}^{\text{fav}} &= \frac{\Gamma(\bar{B}^0 \rightarrow [K^- \pi^+]_D \bar{K}^{*0}) - \Gamma(B^0 \rightarrow [K^+ \pi^-]_D K^{*0})}{\Gamma(\bar{B}^0 \rightarrow [K^- \pi^+]_D \bar{K}^{*0}) + \Gamma(B^0 \rightarrow [K^+ \pi^-]_D K^{*0})}.
 \end{aligned}$$

Selection

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Meson	Variable	Cut value
D^0	$p_T(K^\pm, \pi^\pm)$	$> 400 \text{ MeV}/c$
	$\text{DLL}_{K\pi}(K^\pm)$	> 0
	$\text{DLL}_{K\pi}(\pi^\pm)$	< 4
	Vertex χ^2/ndf	< 5
	Min IP χ^2	> 4
	Flight distance significance	> 2.5
	$ M(K\pi) - M(D^0) $	$< 20 \text{ MeV}/c^2$
K^{*0}	$p_T(K^\pm, \pi^\pm)$	$> 300 \text{ MeV}/c$
	$\text{DLL}_{K\pi}(K^\pm)$	> 3
	$\text{DLL}_{K\pi}(\pi^\pm)$	< 3
	$\text{DLL}_{pK}(K^\pm)$	< 10
	Min IP χ^2	> 25
	$ M(K\pi) - M(K^{*0}) $	$< 50 \text{ MeV}/c^2$
B	Vertex χ^2/ndf	< 4
	Min IP χ^2	< 9
	$\cos(\theta_{\text{dira}})$	> 0.99995
	$\sum_{\text{tracks}} \sqrt{\text{IP}\chi^2}$	> 32
	$ \cos \theta^* $	> 0.4
	$ M(K\pi\pi) - M(D^+) $	$> 15 \text{ MeV}/c^2$
	$ M(KK\pi) - M(D_s^+) $	$> 15 \text{ MeV}/c^2$

- **Topology:**
 - ▢ B vertex.
 - ▢ Displaced D vertex.
 - ▢ K and π from K^{*0} coming from the B vertex (wide resonance).
- **Cut-based** selection: kinematics, vertex quality, particle identification ($\text{DLL}_{K-\pi}$).
- Background from charmless decays (such as $B^0 \rightarrow K^+ K^- K^{*0}$, etc.) removed by D meson flight distance significance cut.
- $B^0 \rightarrow D_{(s)}^{+/-} h^{-/+}$ (same particles in the final state) and $\Lambda_b^0 \rightarrow \bar{D}^0 p h^-$ (proton mis-id) contributions vetoed ($h = K, \pi$).

Mass fit philosophy

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□ B^0 and \bar{B}_s^0 signals.

- Double gaussians.
- Shape fixed from simulation samples, resolution free.
- Same resolutions for the B^0 and \bar{B}_s^0 peak,
 $M(B_s^0) - M(B^0)$ fixed to PDG value.

□ Cross-feed from $B^0 \rightarrow D \rho^0(\pi^+\pi^-)$.

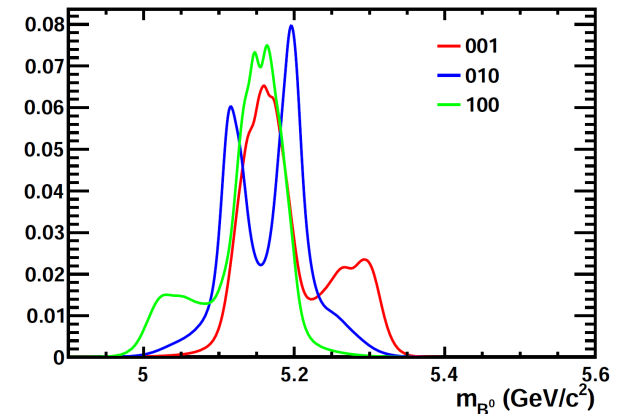
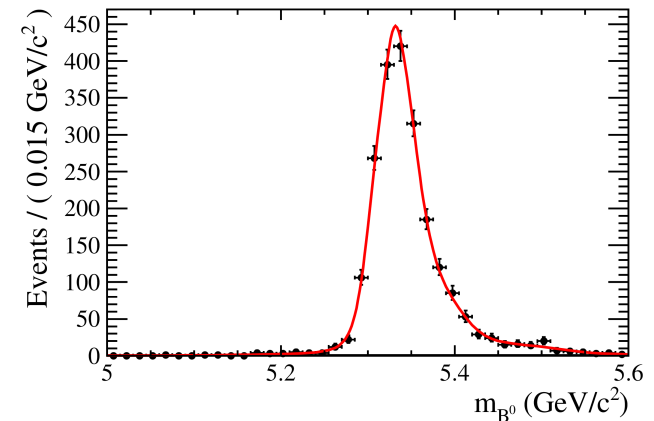
- One of the π from the ρ^0 is misidentified for a K .
- Shape extracted from simulation.

□ Low mass background from partially reconstructed $B_{(s)}^0 \rightarrow D^* K^{*0}$.

- $D^{*0} \rightarrow D^0 \pi^0/\gamma$, if π^0/γ not reconstructed.
- Three possible helicity amplitudes.
- Shapes reproduced from simulation.

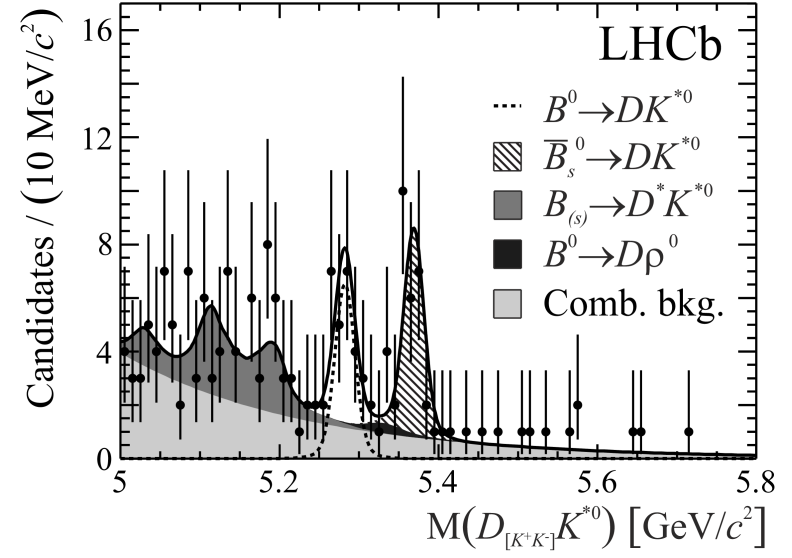
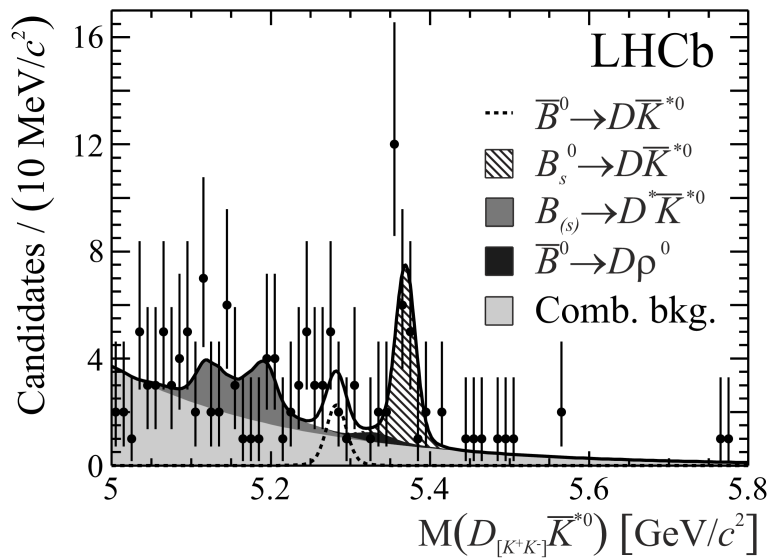
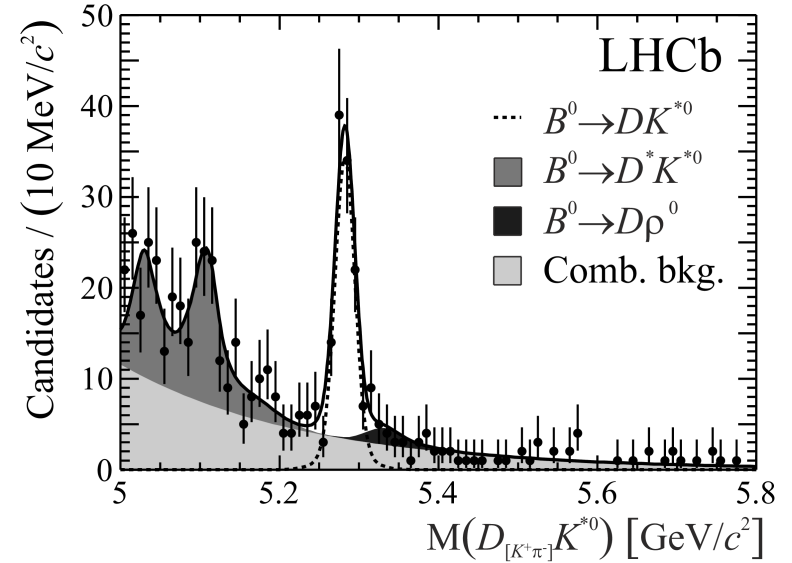
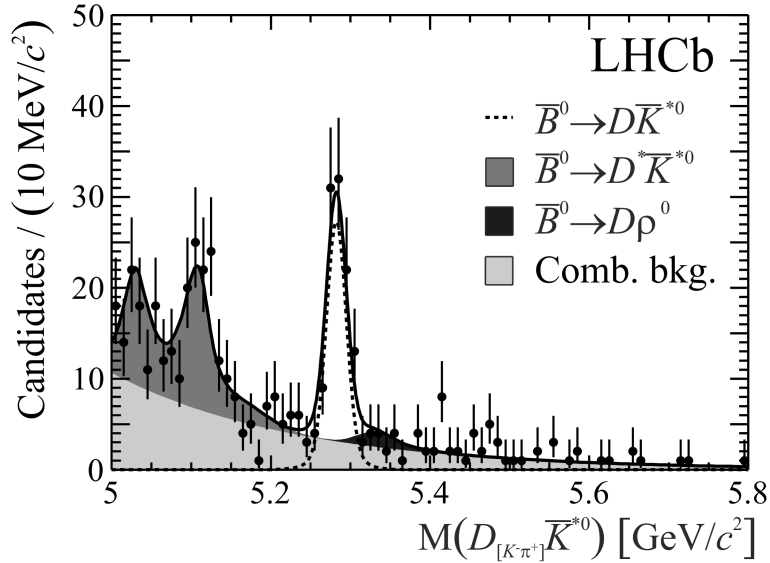
□ Combinatorial background.

- Exponential shape.
- Slope free, same value for both D modes.
- B^0 and \bar{B}^0 yields forced to be the same in each mode.

simulation $B^0 \rightarrow D \rho^0(\pi^+\pi^-)$ simulation $\bar{B}_s^0 \rightarrow D^* K^{*0}$
($D^* \rightarrow D \gamma$) + ($D^* \rightarrow D \pi^0$)

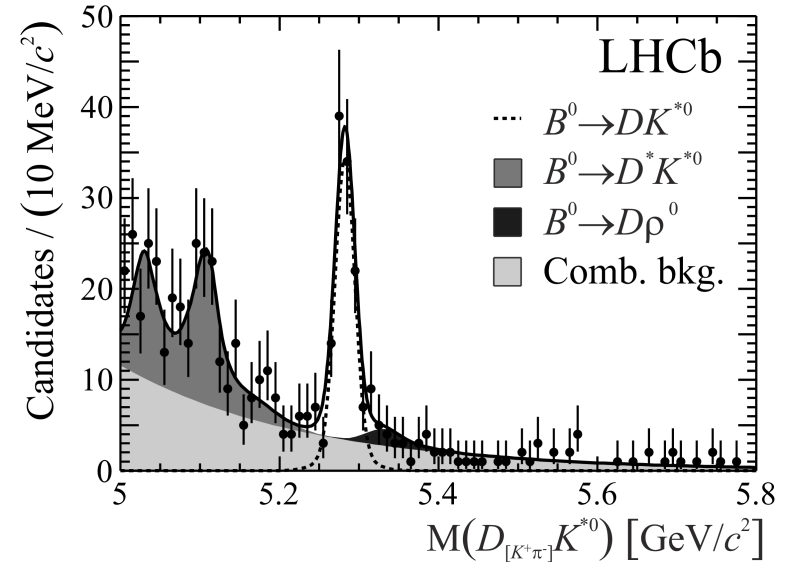
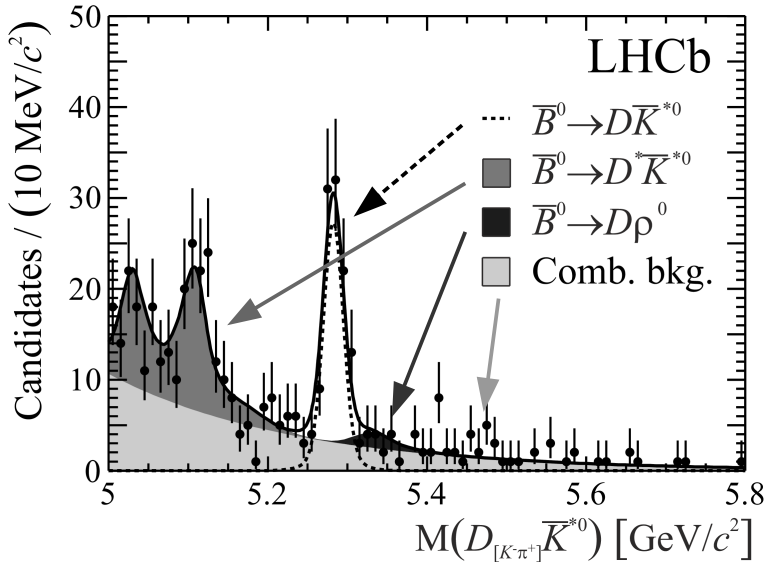
Results

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$B^0 \rightarrow D K^{*0}, D^0 \rightarrow K^+ \pi^-$ (normalisation mode)

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$$\begin{aligned} N(\bar{B}^0) &= 94 \pm 11 \\ N(B^0) &= 108^{+12}_{-11} \end{aligned}$$

Favoured, control mode
No CP asymmetry expected

$$\mathcal{A}_d^{\text{fav}} = -0.08 \pm 0.08 \text{ (stat)} \pm 0.01 \text{ (syst)}$$

$B^0 \rightarrow D K^{*0}, D^0 \rightarrow K^+ K^-$ (signal mode)

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$$\mathcal{A}_d^{KK} = -0.45 \pm 0.23 \text{ (stat)} \pm 0.02 \text{ (syst)}$$

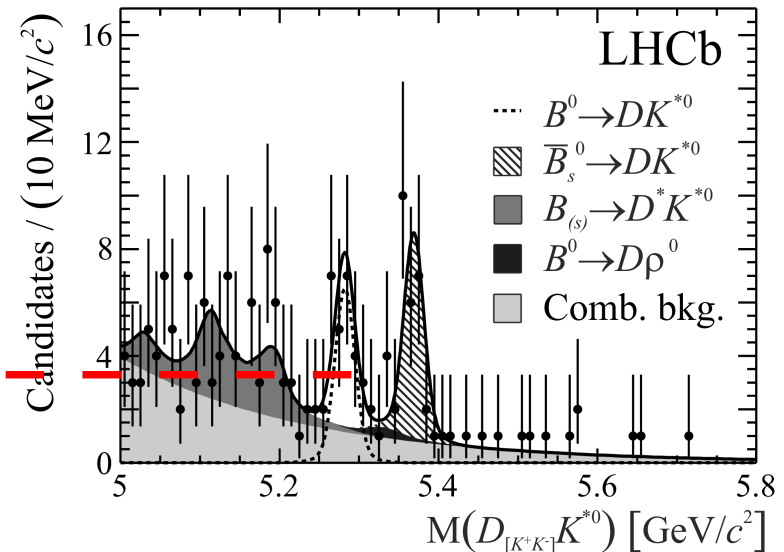
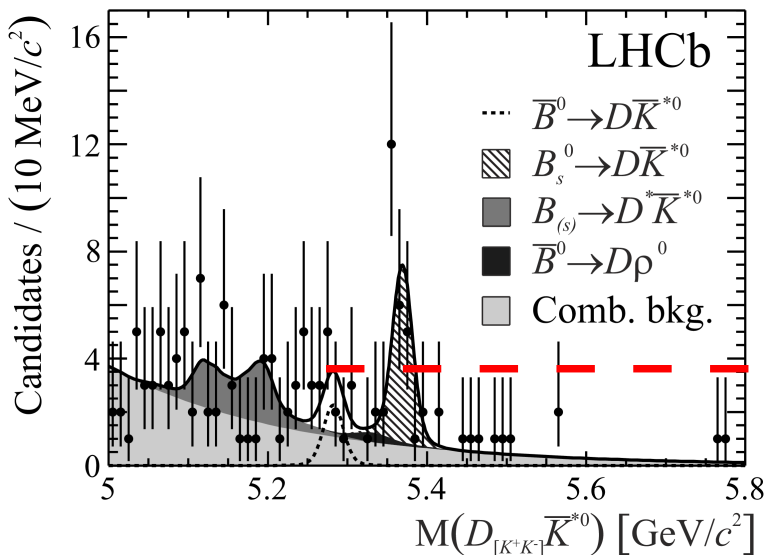
$$\mathcal{A}_s^{KK} = 0.04 \pm 0.16 \text{ (stat)} \pm 0.01 \text{ (syst)}$$

$$\mathcal{R}_d^{KK} = 1.36 \pm_{-0.32}^{+0.37} \text{ (stat)} \pm 0.07 \text{ (syst)}$$

5.1 σ B^0
signal
($B^0 + \bar{B}^0$)

$$\begin{aligned} N(\bar{B}^0) &= 8 \pm 4 \\ N(B^0) &= 24 \pm_{-5}^{+6} \\ N(B_s^0) &= 23 \pm_{-5}^{+6} \\ N(\bar{B}_s^0) &= 24 \pm_{-5}^{+6} \end{aligned}$$

*1st measurement
in the $B^0 \rightarrow [K^+ K^-] K^{*0}$
system*



Conclusion

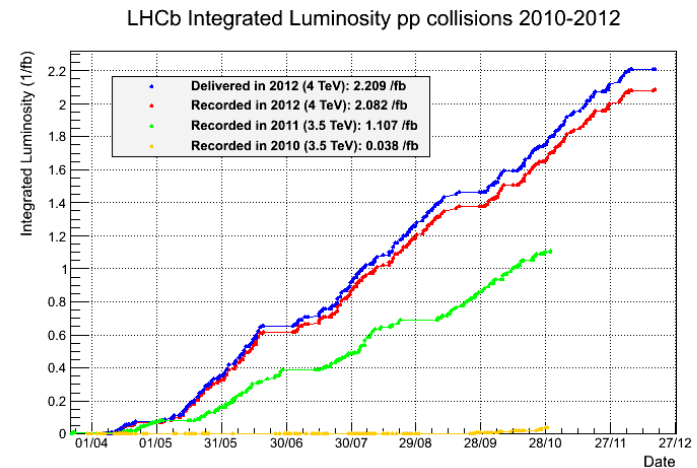
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- LHCb well suited for the study of heavy flavoured hadronic decays.
- Measuring γ precisely is one of the main goals of its physics program.
- Result published on the CP asymmetries of the $B^0 \rightarrow D K^{*0}$ decay mode:

LHCb collaboration, R. Aaij et al., *Measurement of CP observables in $B^0 \rightarrow D K^{*0}$ with $D \rightarrow K^+ K^-$* , JHEP **1303** (2013) 067, arXiv:1212.5205.

- Total dataset is 3 fb^{-1} .
 - 2 fb^{-1} of data collected by LHCb in 2012.
 - Plans:
 - Update this analysis with the complete data set.
 - Add new modes sensitive to γ .
 - GLW $D \rightarrow \pi^+ \pi^-$.
 - ADS suppressed $D \rightarrow K \pi^+$.

- $B^0 \rightarrow D K^{*0}$ does not bring constraints to γ yet, but with the new LHCb data it becomes a promising channel.

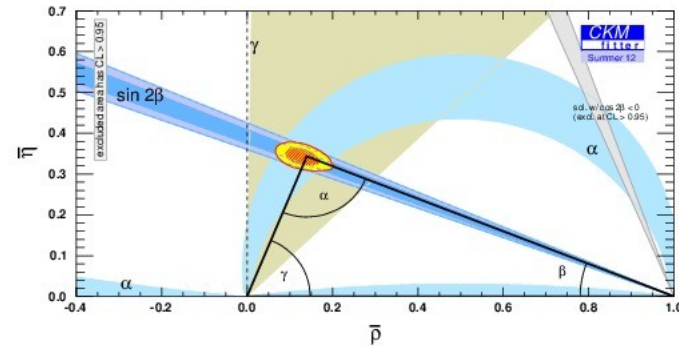
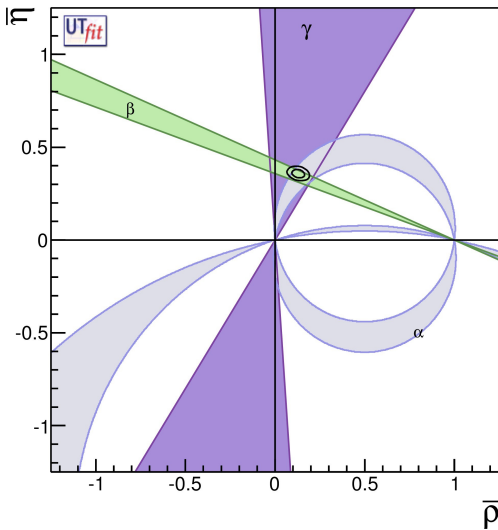


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Back up

The γ angle status

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Global fits

$$\gamma^{\text{UTfit}} = (69.2 \pm 3.2)^\circ$$

$$\gamma^{\text{CKMfitter}} = (67.7 \pm 4.3)^\circ$$

□ Focusing on the **angles**:

□ γ is the one known with the **largest uncertainty**.

$$\gamma^{\text{BaBar}} = (69 \pm 17)^\circ$$

$$\gamma^{\text{Belle}} = (68 \pm 15)^\circ$$

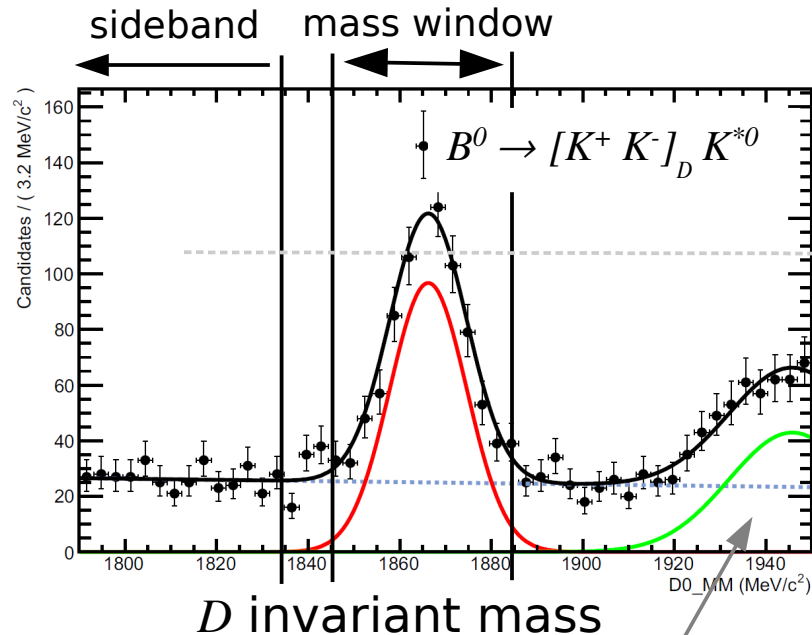
$$\gamma^{\text{LHCb}} = (71.1 \pm 16.7)^\circ$$

Large uncertainties in the **direct measurements** compared with the **global fits**. Need to measure γ precisely to check the Unitary Triangle consistency.

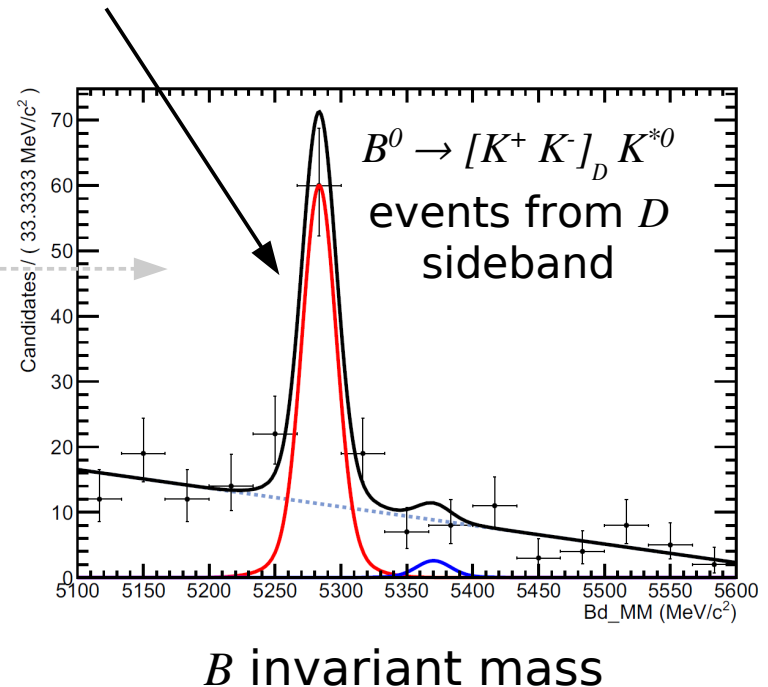
Charmless background: a closer look

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- From $B^0 \rightarrow K^+ K^- K^{*0}(K^+ \pi^-)$ decays.
- The case when the four final state particles come from the B vertex.
 - Instead of having a D displaced vertex.
- Estimate it from the D mass distributions sidebands.
 - Look for peaks at the B invariant mass coming from these events.



(This is $D \rightarrow K\pi$ mis-id as $D \rightarrow KK$. Negligible inside D mass window cut ($\pm 20 \text{ MeV}/c^2$). OK)

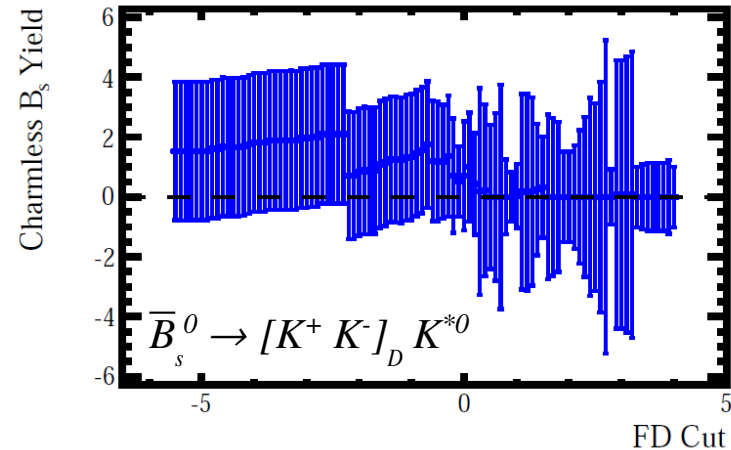
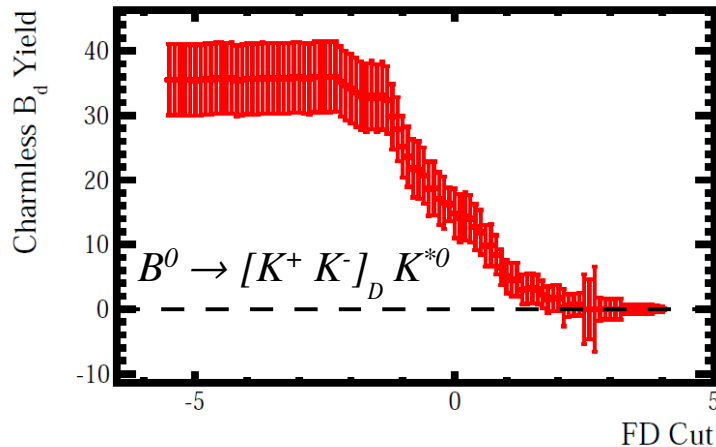


Charmless background: a closer look

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- Look for a D displaced vertex:
 - ▢ Apply a cut on the flight distance significance of the D meson.
 - And compute the number of events left from the D sidebands in the B mass distribution.

$$D_{FDsig} = \frac{z(D) - z(B)}{\sqrt{\sigma_{z(D)}^2 + \sigma_{z(B)}^2}}$$

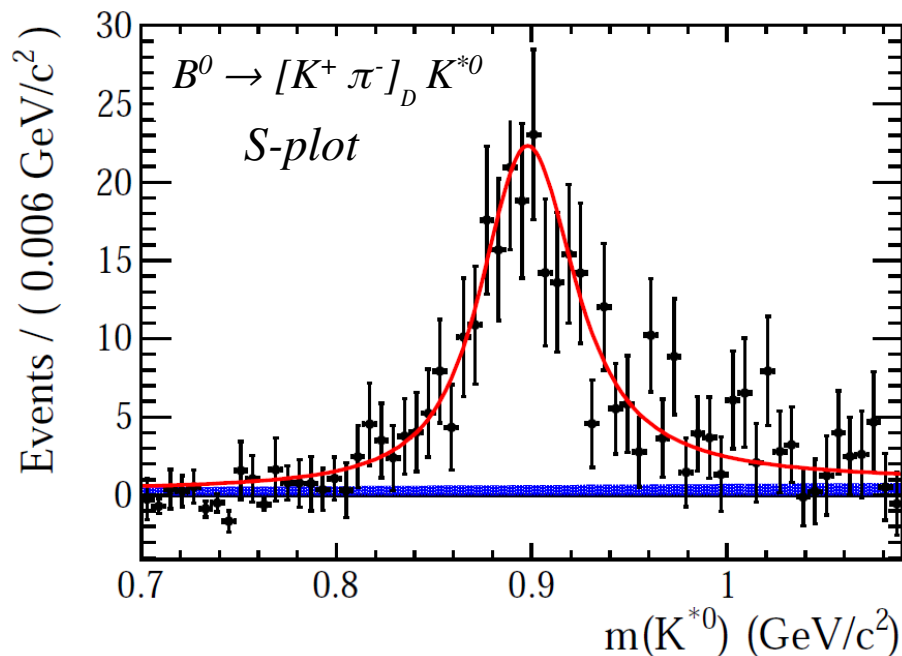


- A cut of $D_{FDsig} > 2.5$ removes this background.

Non-resonant K^{*0} background

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- From $B^0 \rightarrow D K^+ \pi^-$ decays.
- Important to control for the γ extraction from this mode.
- Addressed by computing the **background subtracted distribution (s-Plot) of the K^{*0} invariant mass**.
 - Signal in this plot is resonant, background is non-resonant.



Non-resonant
background
estimated to
(4.8 ± 3.4) % in K^{*0}
mass window.

Systematics

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Source	\mathcal{A}_d^{KK}	$\mathcal{A}_d^{\text{fav}}$	\mathcal{A}_s^{KK}	\mathcal{R}_d^{KK}
Production asymmetry	0.005	0.006	—	0.003
PID efficiency	0.004	0.008	0.005	0.014
Trigger efficiency	0.004	0.001	0.005	0.022
Selection efficiency	—	—	—	0.040
Bias correction	0.004	—	0.001	0.013
Low-mass background	0.017	0.001	0.004	0.042
$B^0 \rightarrow D\rho^0$ cross-feed	0.001	—	0.002	0.008
Signal description	0.001	0.001	0.001	0.005
D branching fractions	—	—	—	0.022
Total	0.019	0.010	0.008	0.069