

The background of the slide features a photograph of a small, blue wooden boat resting on a grassy bank. The boat is oriented diagonally, pointing towards the top right. The water behind it is calm, with the warm, golden light of a sunset or sunrise reflected in the ripples, creating a peaceful atmosphere.

## **Seminar at LPNHE Paris**

# **CP violation with heavy mesons**

Malcolm John  
10 May 2012

# Three subjects

Observation of direct  $CP$  violation in  $B^+$  decays

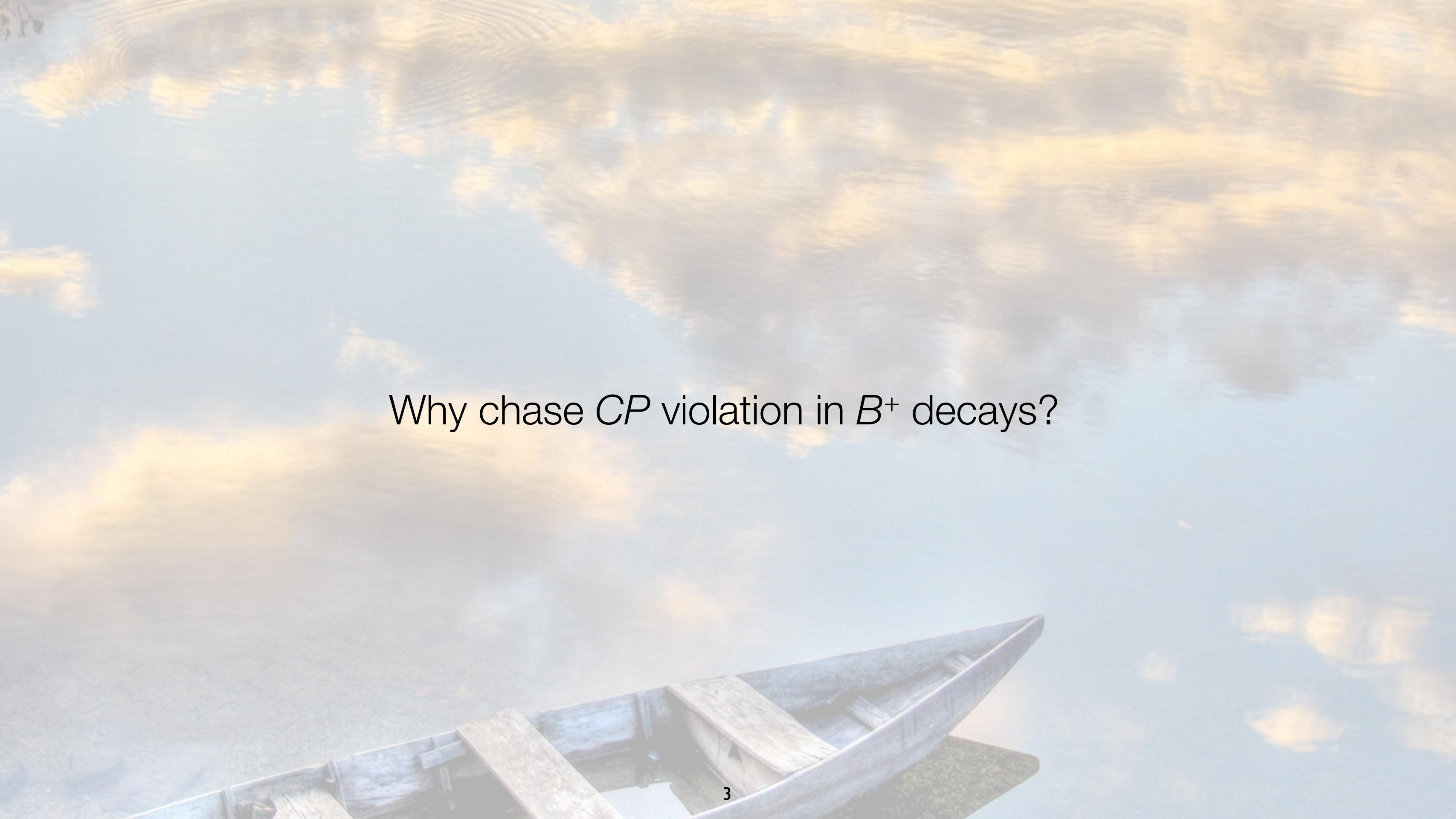
$1\text{fb}^{-1}$  arXiv:1203.3662

Searches for time-dependent  $CP$ -violation in  
the mixing and decay of  $B_s$  mesons

$1\text{fb}^{-1}$  LHCb-CONF-2012-002

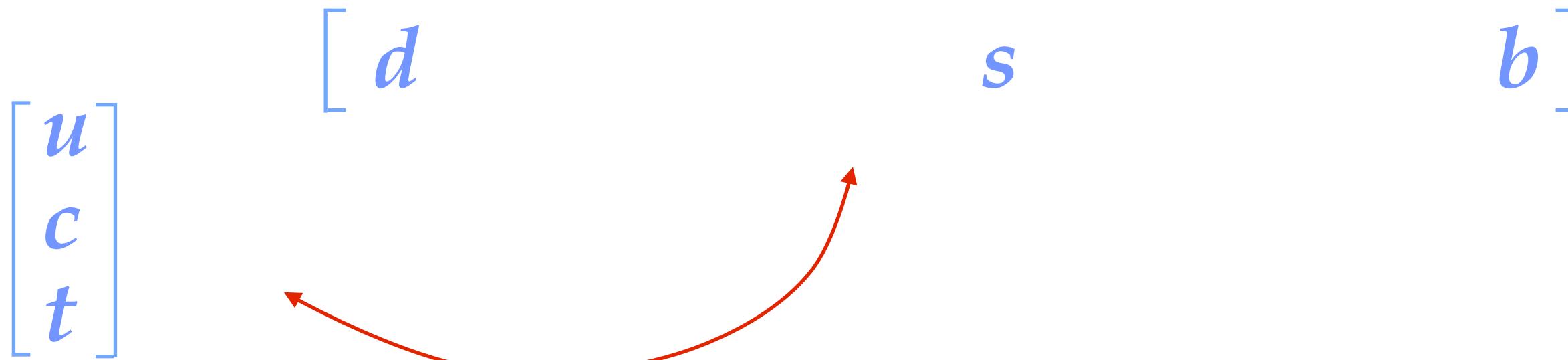
Evidence for direct  $CP$  violation in  $D^0$  decays

$0.6\text{fb}^{-1}$  arXiv:1112.0938

A photograph of a small, traditional wooden boat with a pointed bow, resting on a body of water. The sky is filled with soft, orange and yellow clouds at sunset. The boat is positioned in the lower third of the frame, facing towards the right.

Why chase  $CP$  violation in  $B^+$  decays?

$CP$  violation known only to occur in the weak interaction of quarks



by emission or absorption of a  
 $W^\pm$  boson, quarks change flavour



CKM model: 3 quark generations  $\Rightarrow$  3 mixing angles, 1 phase

---

$$V_{CKM} = \begin{pmatrix} d & s & b \\ u & c & t \\ \bar{c} & \bar{s} & \bar{b} \end{pmatrix} \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda + \frac{1}{2}A^2\lambda^5(1 - 2(\rho + i\eta)) & 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}(1 + 4A^2)\lambda^4 & A\lambda^2 \\ A\lambda^3(1 - (1 - \frac{1}{2}\lambda^2)(\rho - i\eta)) & -A\lambda^2 + \frac{1}{2}A\lambda^4(1 - 2(\rho - i\eta)) & 1 - \frac{1}{2}A^2\lambda^4 \end{pmatrix} + \mathcal{O}(\lambda^7)$$

Wolfenstein expansion in powers of the Cabibbo angle,  $\lambda$ , up to  $\lambda^6$

This single phase give rise to all CP violation phenomena

$$V_{CKM} = \begin{pmatrix} u & d \\ c & s \\ t & b \end{pmatrix} \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 \\ -\lambda + \frac{1}{2}A^2\lambda^5(1 - 2(\rho + i\eta)) \\ A\lambda^3(1 - (1 - \frac{1}{2}\lambda^2)(\rho - i\eta)) \end{pmatrix}$$

$$= \begin{pmatrix} \lambda \\ 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}(1 + 4A^2)\lambda^4 \\ -A\lambda^2 + \frac{1}{2}A\lambda^4(1 - 2(\rho - i\eta)) \end{pmatrix} + \mathcal{O}(\lambda^7)$$

Wolfenstein expansion in powers of the Cabibbo angle,  $\lambda$ , up to  $\lambda^6$

$$0 = 1 + \frac{V_{tb}^* V_{td}}{V_{cb}^* V_{cd}} + \frac{V_{ub}^* V_{ud}}{V_{cb}^* V_{cd}}$$

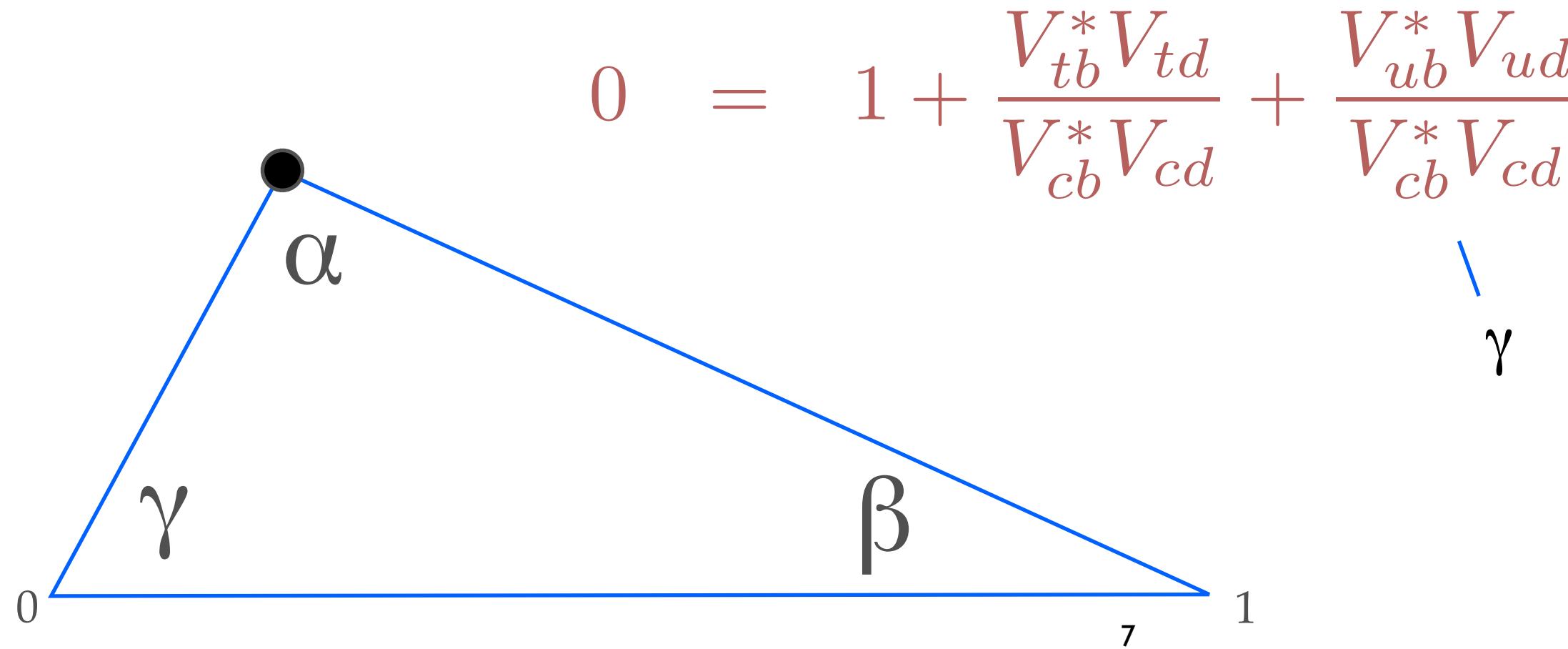
Testing the unitarity of this matrix is a huge part of flavour physics

$$V_{CKM} = \begin{pmatrix} u & d \\ c & s \\ t & b \end{pmatrix} \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 \\ -\lambda + \frac{1}{2}A^2\lambda^5(1 - 2(\rho + i\eta)) \\ A\lambda^3(1 - (1 - \frac{1}{2}\lambda^2)(\rho - i\eta)) \end{pmatrix}$$

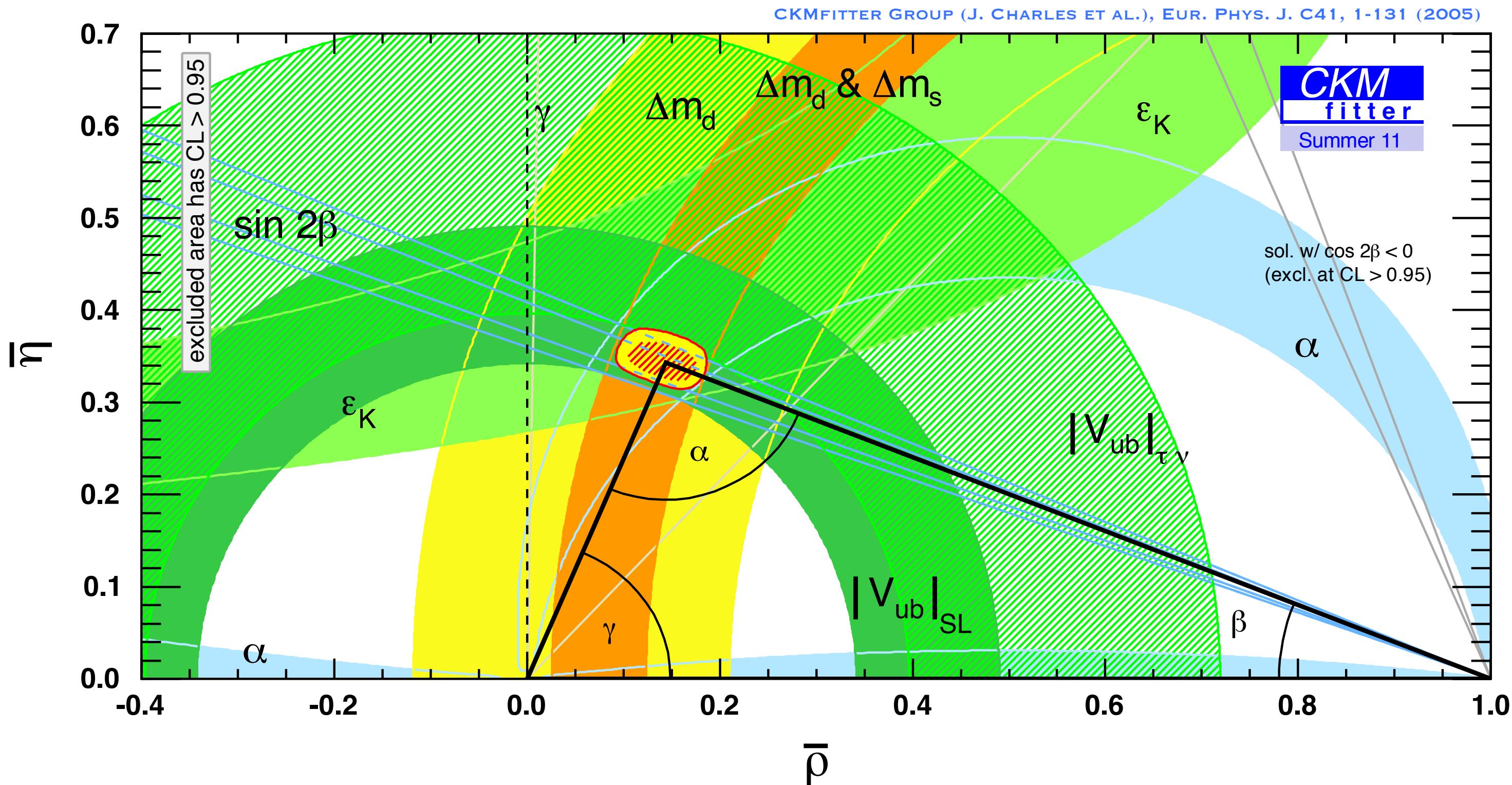
$$\begin{pmatrix} \lambda \\ 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}(1 + 4A^2)\lambda^4 \\ -A\lambda^2 + \frac{1}{2}A\lambda^4(1 - 2(\rho - i\eta)) \end{pmatrix}$$

$$\begin{pmatrix} A\lambda^3(\rho - i\eta) \\ A\lambda^2 \\ 1 - \frac{1}{2}A^2\lambda^4 \end{pmatrix} + \mathcal{O}(\lambda^7)$$

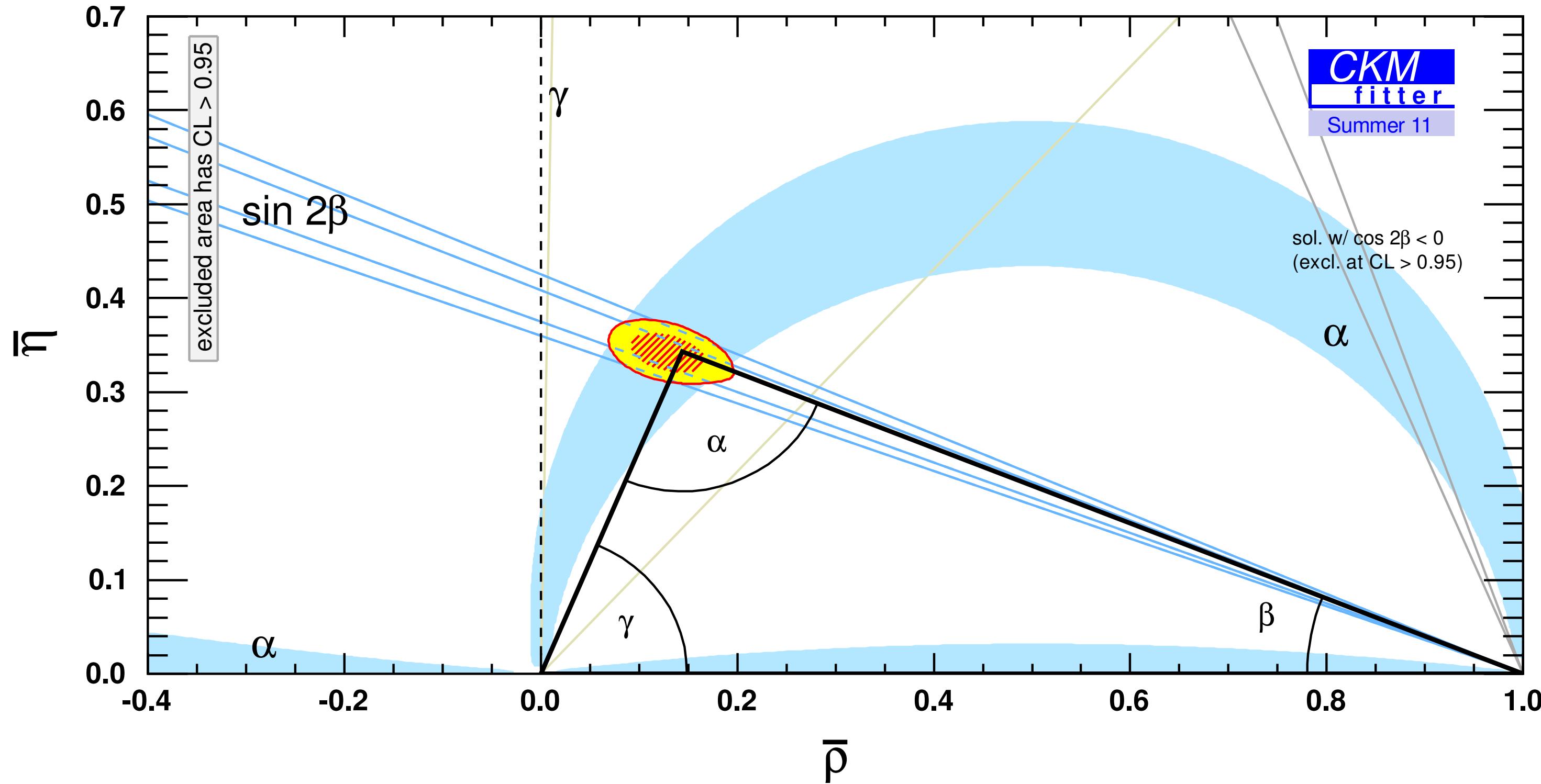
Wolfenstein expansion in powers of the Cabibbo angle,  $\lambda$ , up to  $\lambda^6$



We know the Standard Model describes Nature well.



But  $\gamma$  is poorly determined by direct methods; “direct” == “tree process”

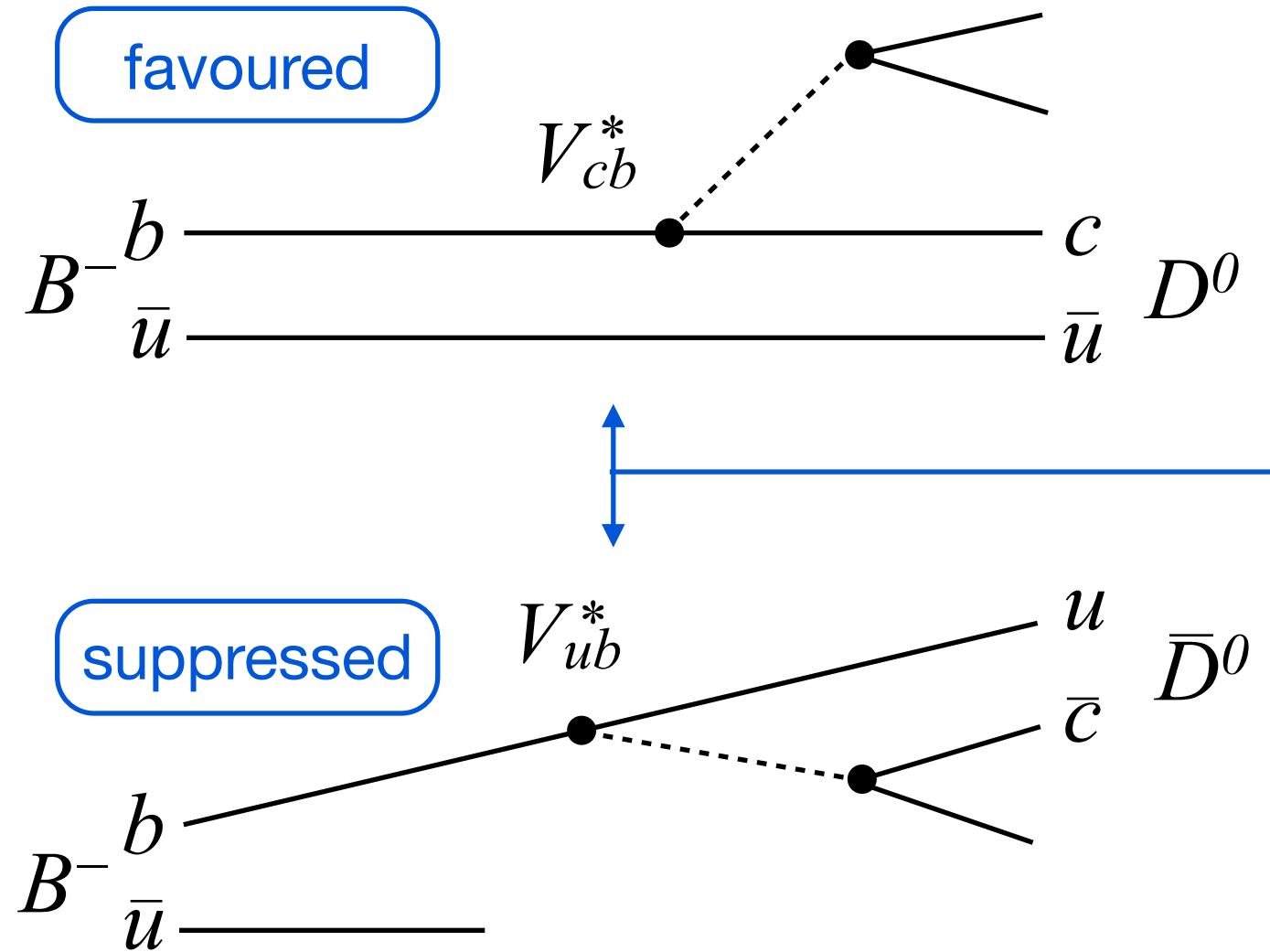


A photograph of a traditional wooden boat, possibly a dugout canoe, resting on a body of water. The boat is dark wood with a white stripe along the hull. The background is a vast, calm lake under a sky filled with wispy clouds colored in shades of orange, yellow, and blue from a setting sun.

Simple ways to measure  $\gamma$  with trees

# How could we measure $\gamma$ ?

- Need a  $b \rightarrow c$  and  $b \rightarrow u$  transition

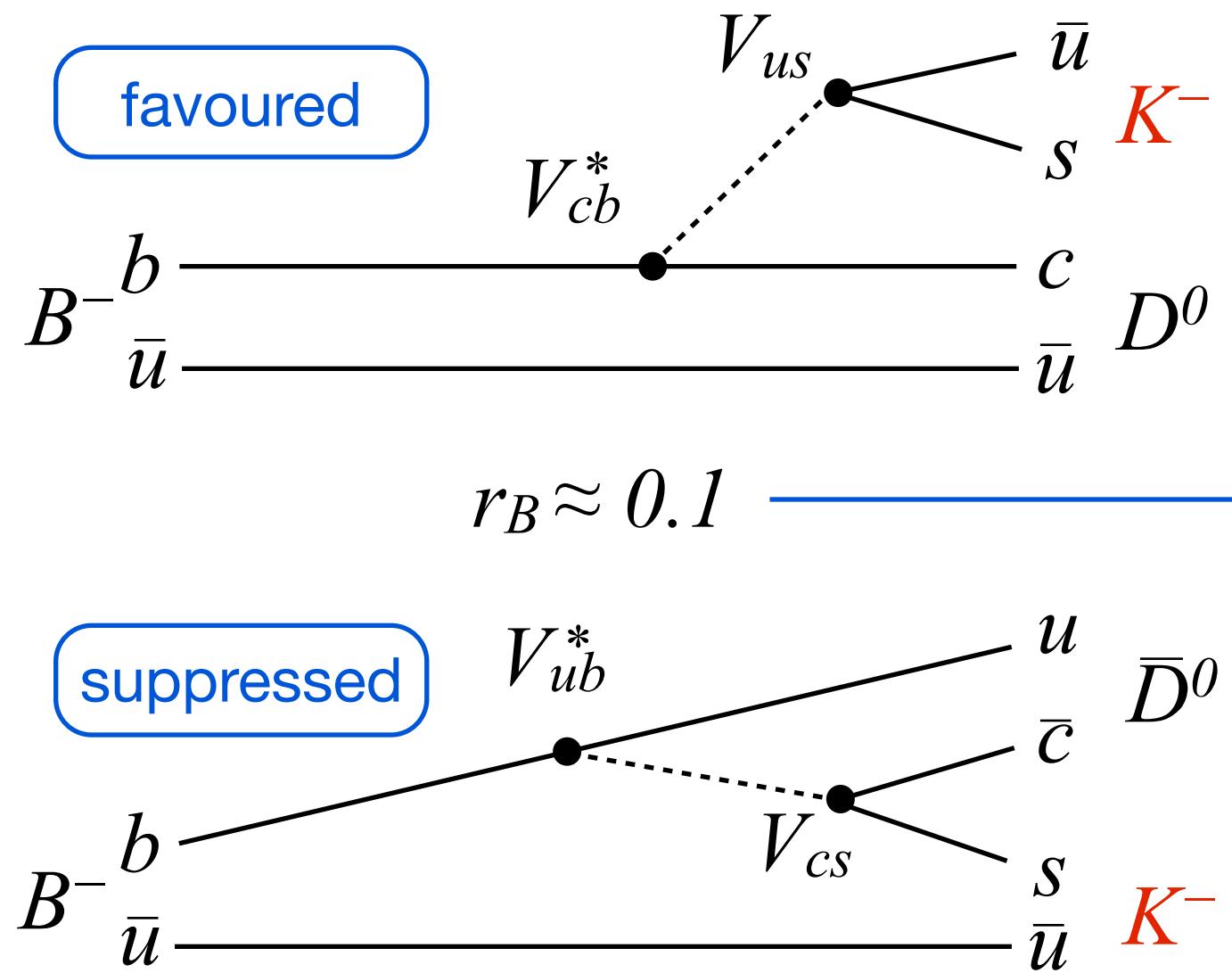


weak phase difference:

$$\begin{aligned} &= \arg \left( -\frac{V_{ub}^*}{V_{cb}^*} \right) \\ &= \gamma \end{aligned}$$

# How could we measure $\gamma$ ?

- Need a  $b \rightarrow c$  and  $b \rightarrow u$  transition of similar probability



relative amplitude:

$$\left| \frac{V_{cs} V_{ub}^*}{V_{us} V_{cb}^*} \right| f_{col} = r_B$$

relative strong phase:

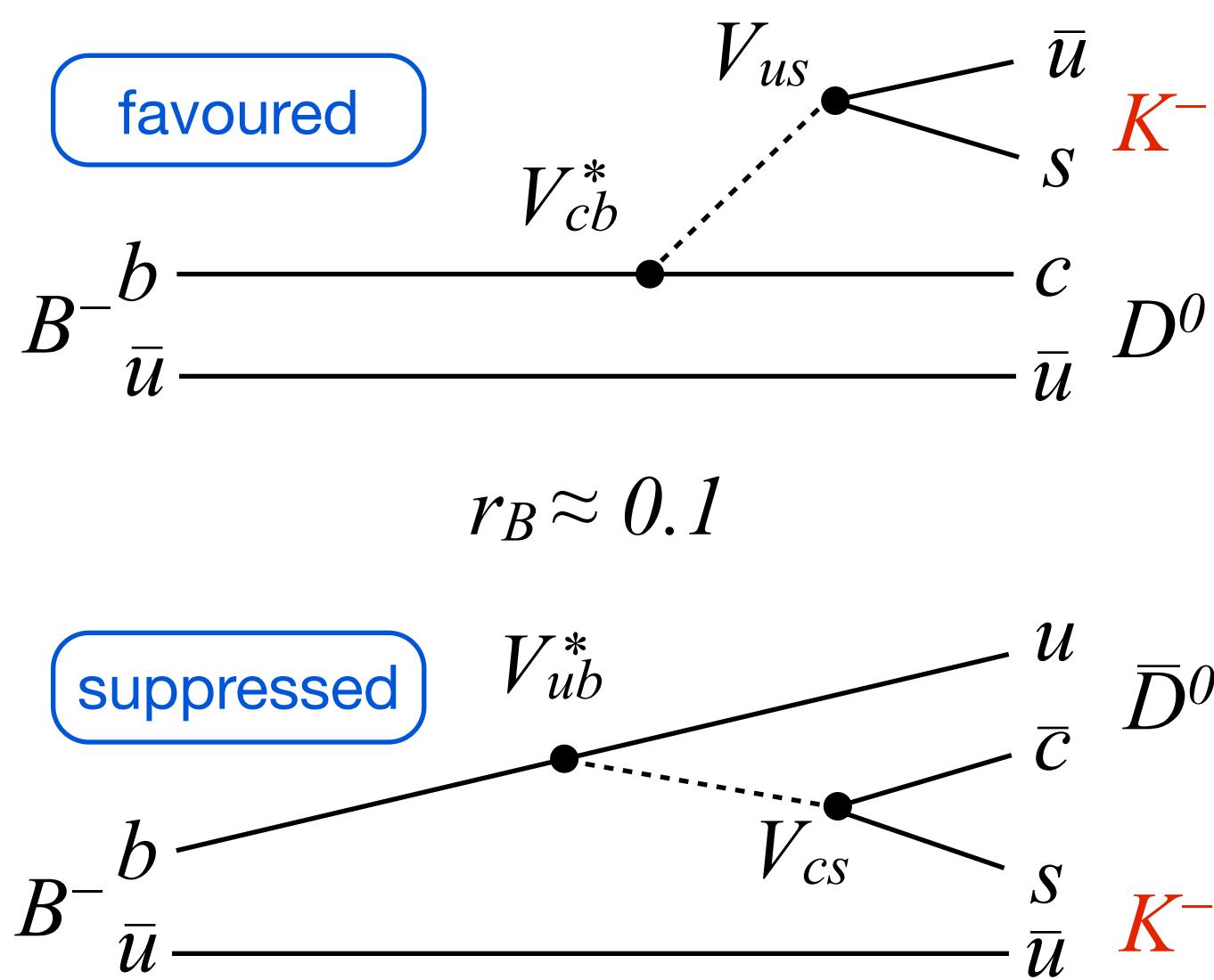
$$= \delta_B$$

weak phase difference:

$$\arg \left( \frac{V_{cs} V_{ub}^*}{V_{us} V_{cb}^*} \right) = \arg \left( -\frac{V_{ub}^*}{V_{cb}^*} \right) = \gamma$$

# How could we measure $\gamma$ ?

- Need a  $b \rightarrow c$  and  $b \rightarrow u$  transition of similar probability and a common final state



$$D^0/\bar{D}^0 \rightarrow \begin{array}{l} K^+ K^- \\ \pi^+ \pi^- \end{array}$$

relative amplitude:      weak phase difference:

$$\left| \frac{V_{cs} V_{ub}^*}{V_{us} V_{cb}^*} \right| f_{col} = r_B$$

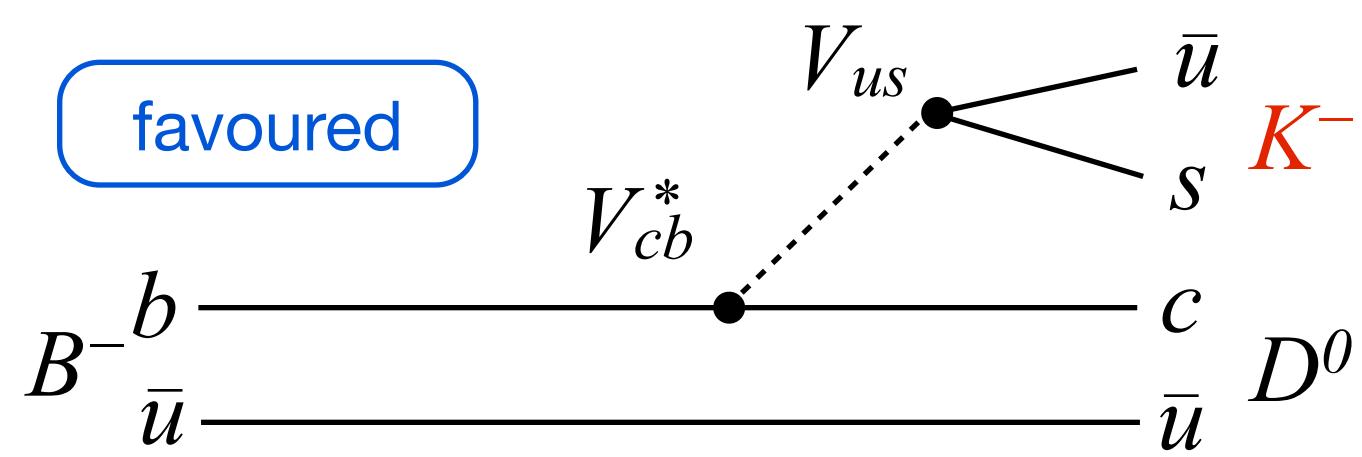
$$\arg \left( \frac{V_{cs} V_{ub}^*}{V_{us} V_{cb}^*} \right)$$

relative strong phase:

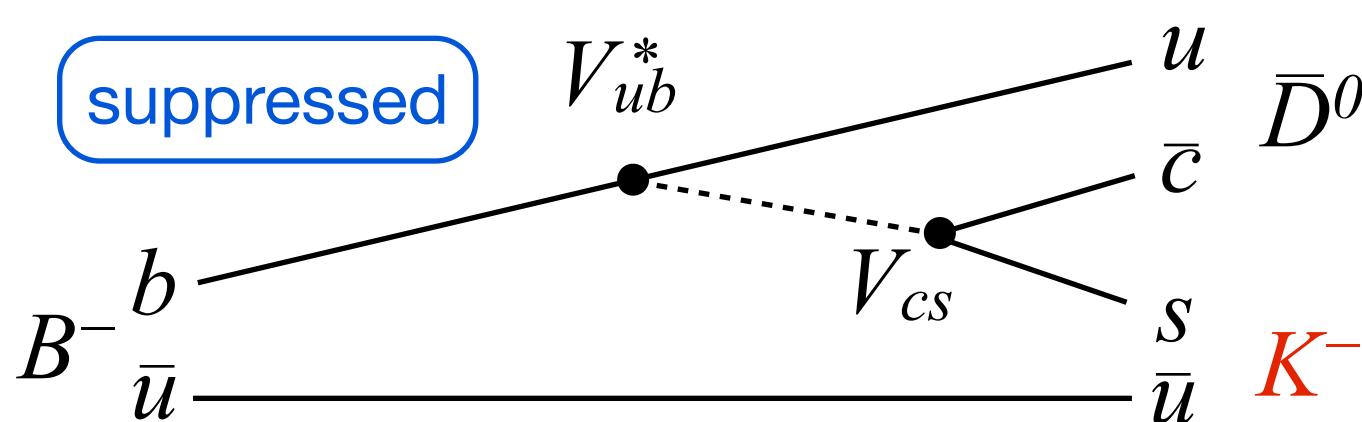
$$= \delta_B \qquad \qquad \qquad = \gamma$$

# How could we measure $\gamma$ ?

- Need a  $b \rightarrow c$  and  $b \rightarrow u$  transition of similar probability and a common final state



$$r_B \approx 0.1$$



$$\begin{aligned} D^0/\bar{D}^0 &\rightarrow K^+K^- \\ &\rightarrow \pi^+\pi^- \end{aligned}$$

A blue box labeled "CP eigenstates" is associated with these decay channels.

Nota bene:

$D \rightarrow K^+K^- , \pi^+\pi^-$  are  $CP+$  eigenstates

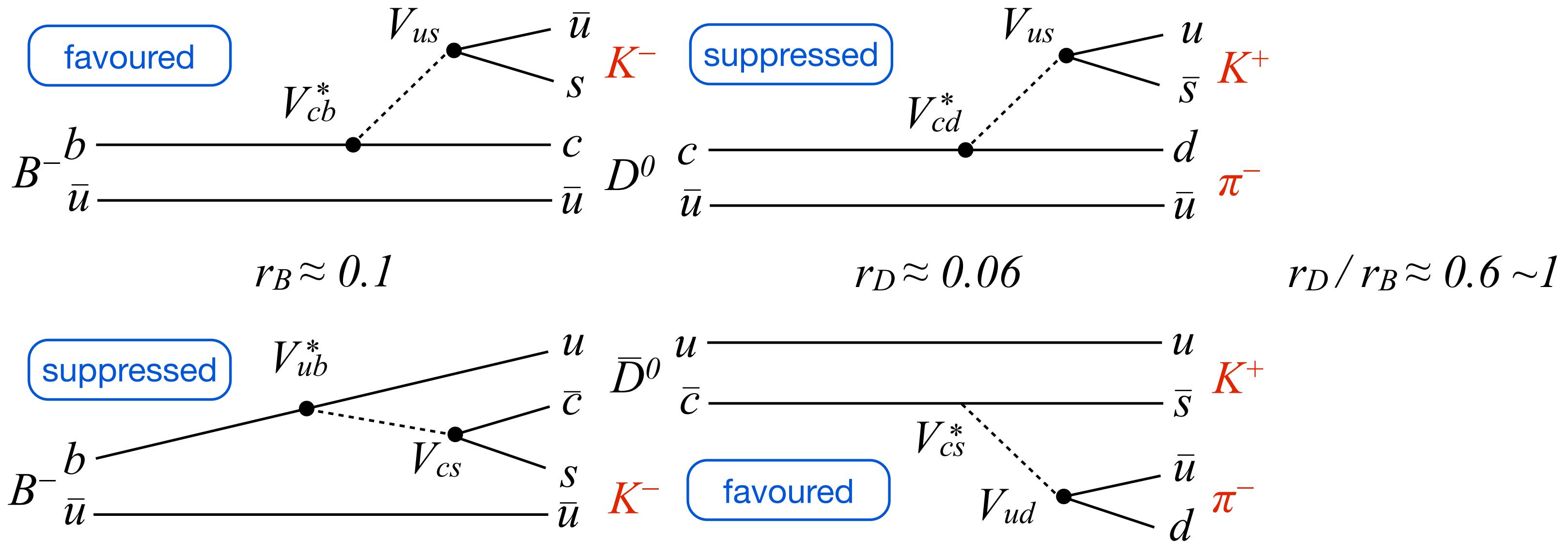
$D \rightarrow K^0\pi^0 , K^0\omega\dots$  are  $CP-$  eigenstates

However:

modes with  $K^0 + \pi^0$  are difficult to trigger and reconstruct at LHCb so are not considered [yet].

But the larger the interference, the greater the sensitivity to  $\gamma$

- Need a  $b \rightarrow c$  and  $b \rightarrow u$  transition of similar probability and a common final state



$$B^- \rightarrow D\bar{K}^- \quad D_s \rightarrow K^+K^-, \pi^+\pi^-$$

favoured  
⊕  
suppressed

⊗ CP eigenstates

$$B^- \rightarrow D\bar{K}^- \quad D \rightarrow \pi^-\bar{K}^+$$

favoured  
⊕  
suppressed

suppressed  
⊕  
favoured

$$B^- \rightarrow D\bar{K}^- \quad D \rightarrow K^-\pi^+$$

favoured  
⊕  
suppressed

favoured  
⊕  
suppressed

## “CP” or “GLW” modes

M. Gronau and D. London, *How to determine all the angles of the unitarity triangle from  $B_d^0 \rightarrow D\bar{K}_s^0$  and  $B_s^0 \rightarrow D\phi$* , Phys. Lett. **B253** (1991) 483; M. Gronau and D. Wyler, *On determining a weak phase from CP asymmetries in charged B decays*, Phys. Lett. **B265** (1991)

## “ADS” mode

D. Atwood, I. Dunietz, and A. Soni, *Enhanced CP violation with  $B \rightarrow K D^0(\bar{D}^0)$  modes and extraction of the CKM angle  $\gamma$* , Phys. Rev. Lett. **78** (1997) 3257, arXiv:hep-ph/9612433;

## “Favoured” mode

- Logic is equally applicable to  $B^- \rightarrow D\pi^-$  though  $r_B$ , and hence the interference is smaller  $r_{B(\pi)} \sim 0.01$  compared to  $r_{B(K)} \sim 0.1$
- The “physics” observables are ratios of branching fractions and CP asymmetries
- All mode has dependence on  $\gamma$  though this is essentially negligible in the favoured mode

# The “physics” observables

$$\frac{\langle \Gamma(B^\pm \rightarrow [\pi\pi]_D K^\pm), \Gamma(B^\pm \rightarrow [KK]_D K^\pm) \rangle}{\Gamma(B^\pm \rightarrow [K\pi]_D K^\pm)}$$

*CP modes*  
*favoured mode*

$$R_{CP+} = 1 + r_B^2 + 2r_B \cos \delta_B \cos \gamma$$

$$\frac{\Gamma(B^\pm \rightarrow [\pi K]_D K^\pm)}{\Gamma(B^\pm \rightarrow [K\pi]_D K^\pm)}$$

*ADS mode*  
*favoured mode*

**effective  
BF~10<sup>-7</sup>**

$$R^{ADS} = \frac{r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos \gamma}{1 + (r_B r_D)^2 + 2r_B r_D \cos(\delta_B - \delta_D) \cos \gamma}$$

$$\frac{\text{average of } KK \text{ and } \pi\pi \text{ modes}}{\Gamma(B^- \rightarrow D_{CP} K^-) - \Gamma(B^+ \rightarrow D_{CP} K^+)}$$

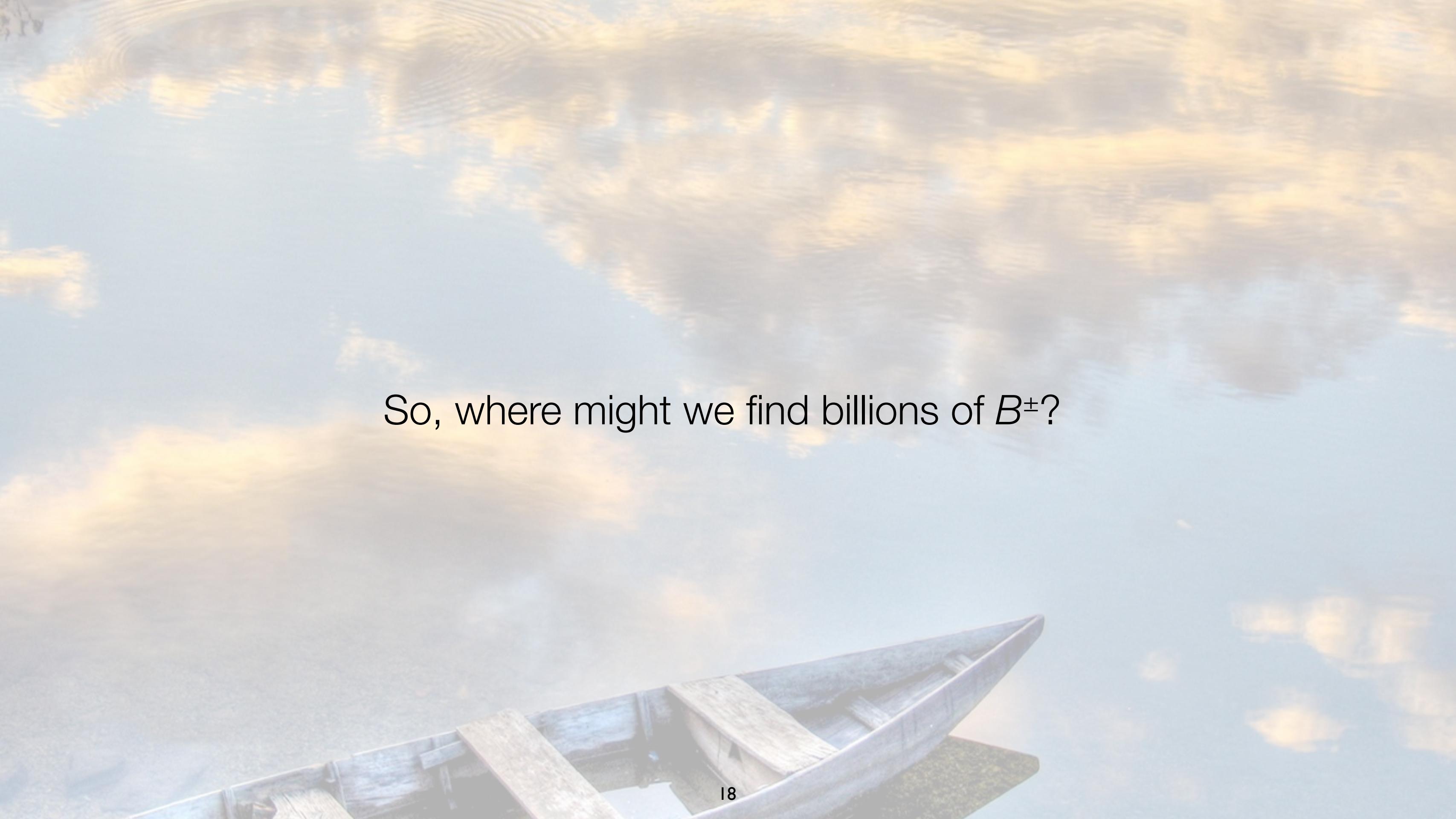
$$\quad \quad \quad /$$

$$\Gamma(B^- \rightarrow D_{CP} K^-) + \Gamma(B^+ \rightarrow D_{CP} K^+)$$

$$A_{CP+} = \frac{2r_B \sin \delta_B \sin \gamma}{1 + r_B^2 + 2r_B \cos \delta_B \cos \gamma}$$

$$\frac{\Gamma(B^- \rightarrow D_{ADS} K^-) - \Gamma(B^+ \rightarrow D_{ADS} K^+)}{\Gamma(B^- \rightarrow D_{ADS} K^-) + \Gamma(B^+ \rightarrow D_{ADS} K^+)}$$

$$A^{ADS} = \frac{2r_B r_D \sin(\delta_B + \delta_D) \sin \gamma}{r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos \gamma}$$

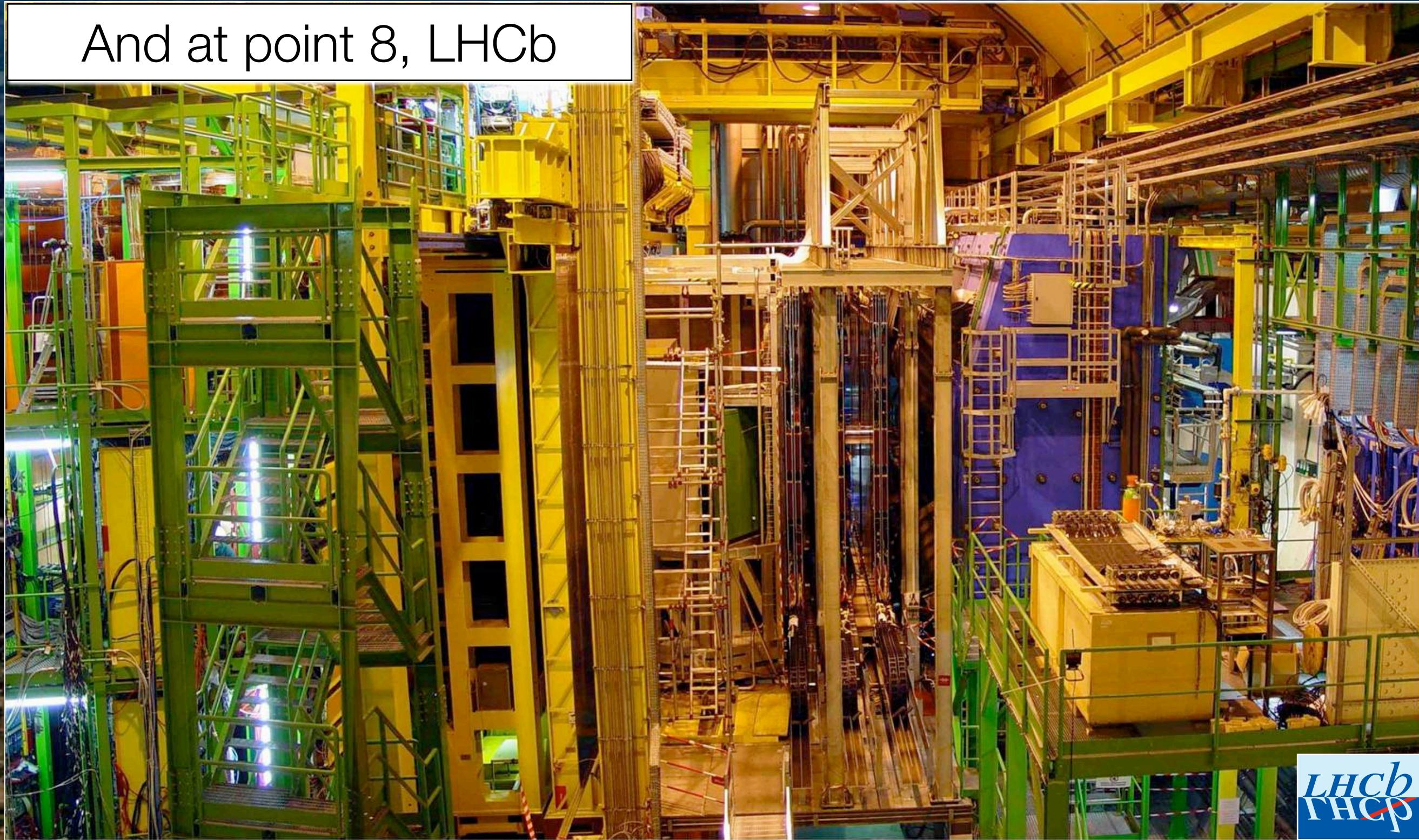
A photograph of a traditional wooden boat, possibly a dugout canoe, resting on a body of water. The boat is dark wood with a white stripe along its side. The background is a vast, calm lake under a sky filled with wispy clouds colored in shades of orange, yellow, and blue from a setting or rising sun.

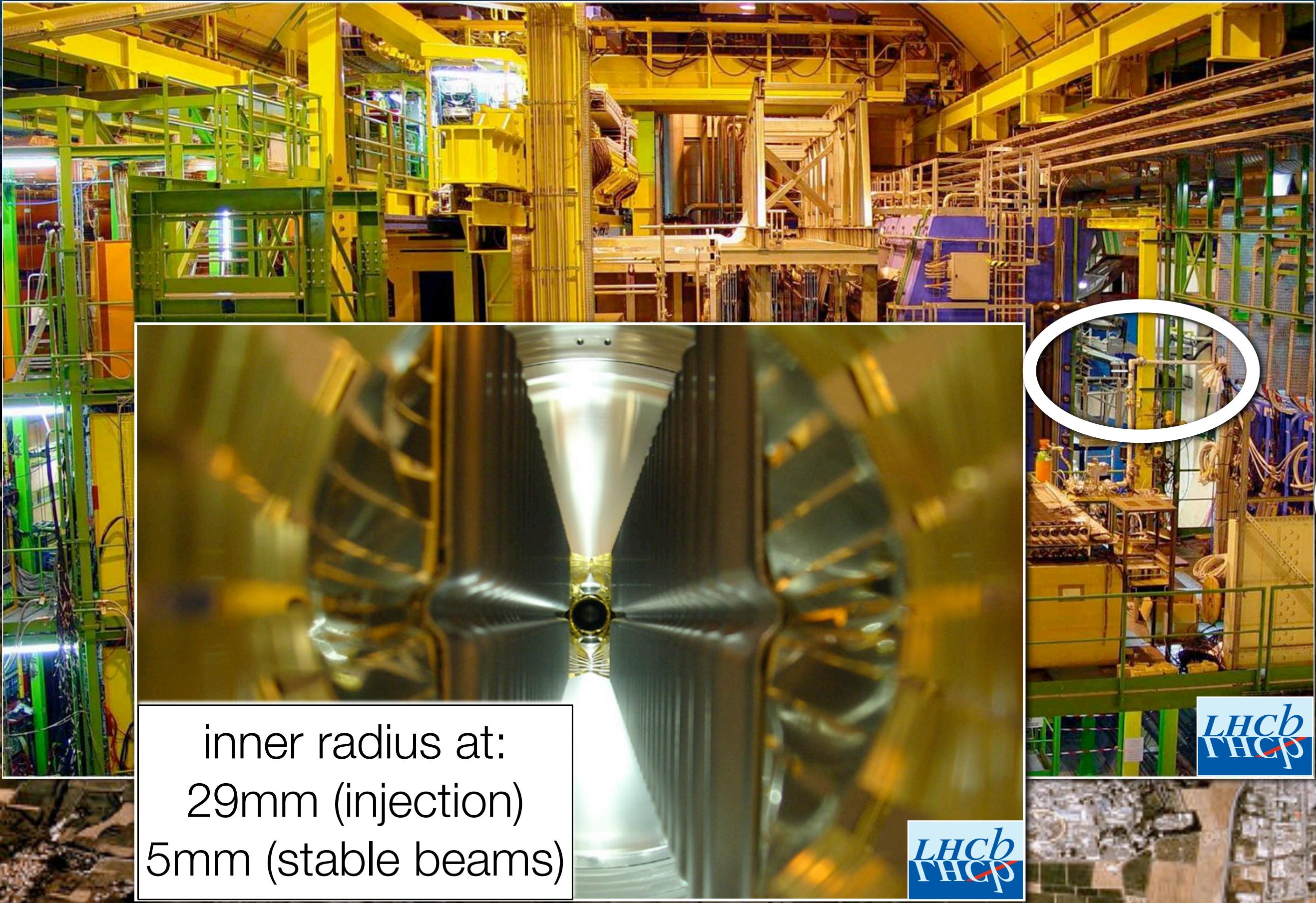
So, where might we find billions of  $B^\pm$ ?

You will recognise this...



And at point 8, LHCb

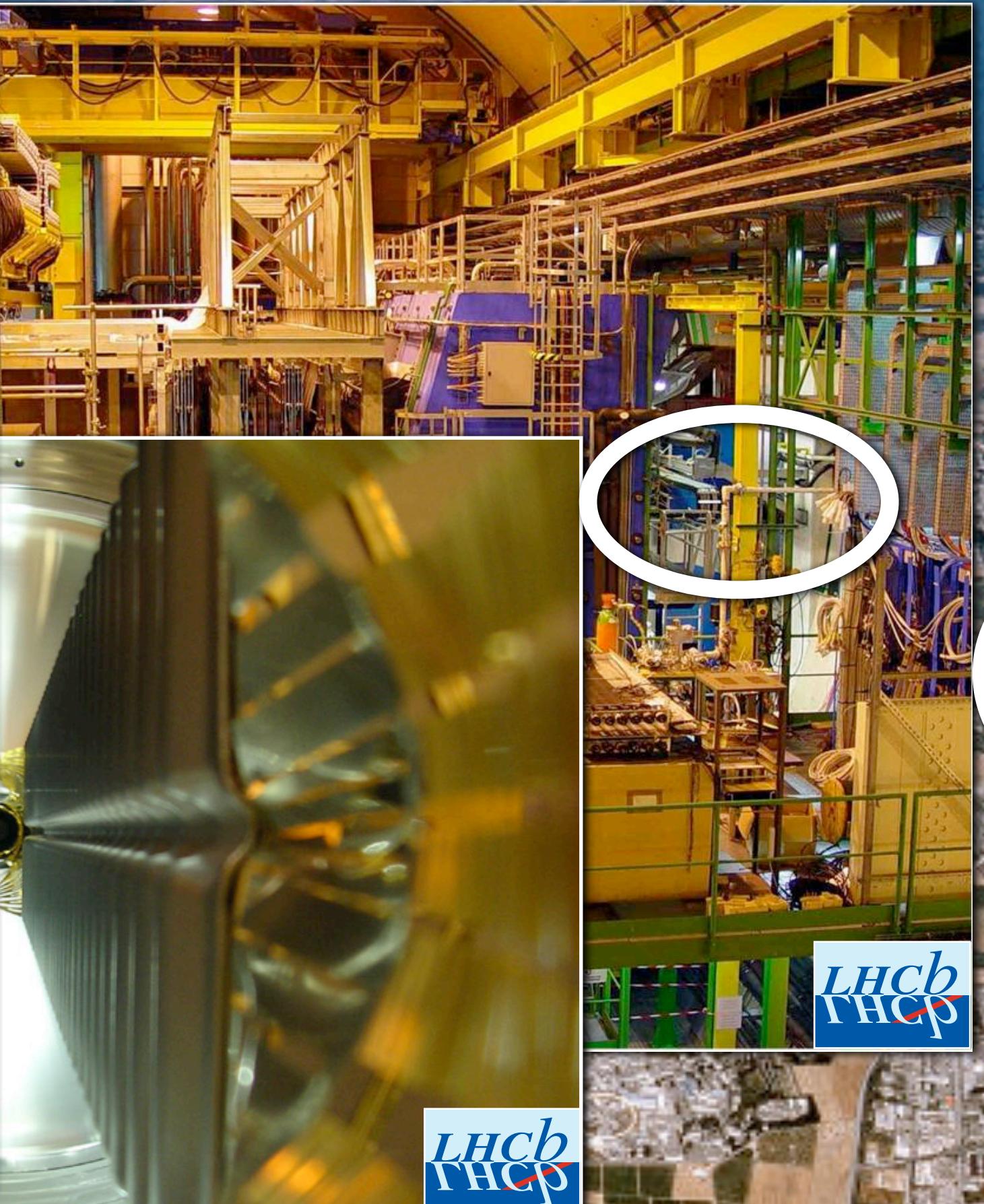




Silicon strip vertex detector.  
 $>40\mu\text{m}$  pitch at 8.2mm radius



LHCb  
FHCP



LHCb  
FHCP

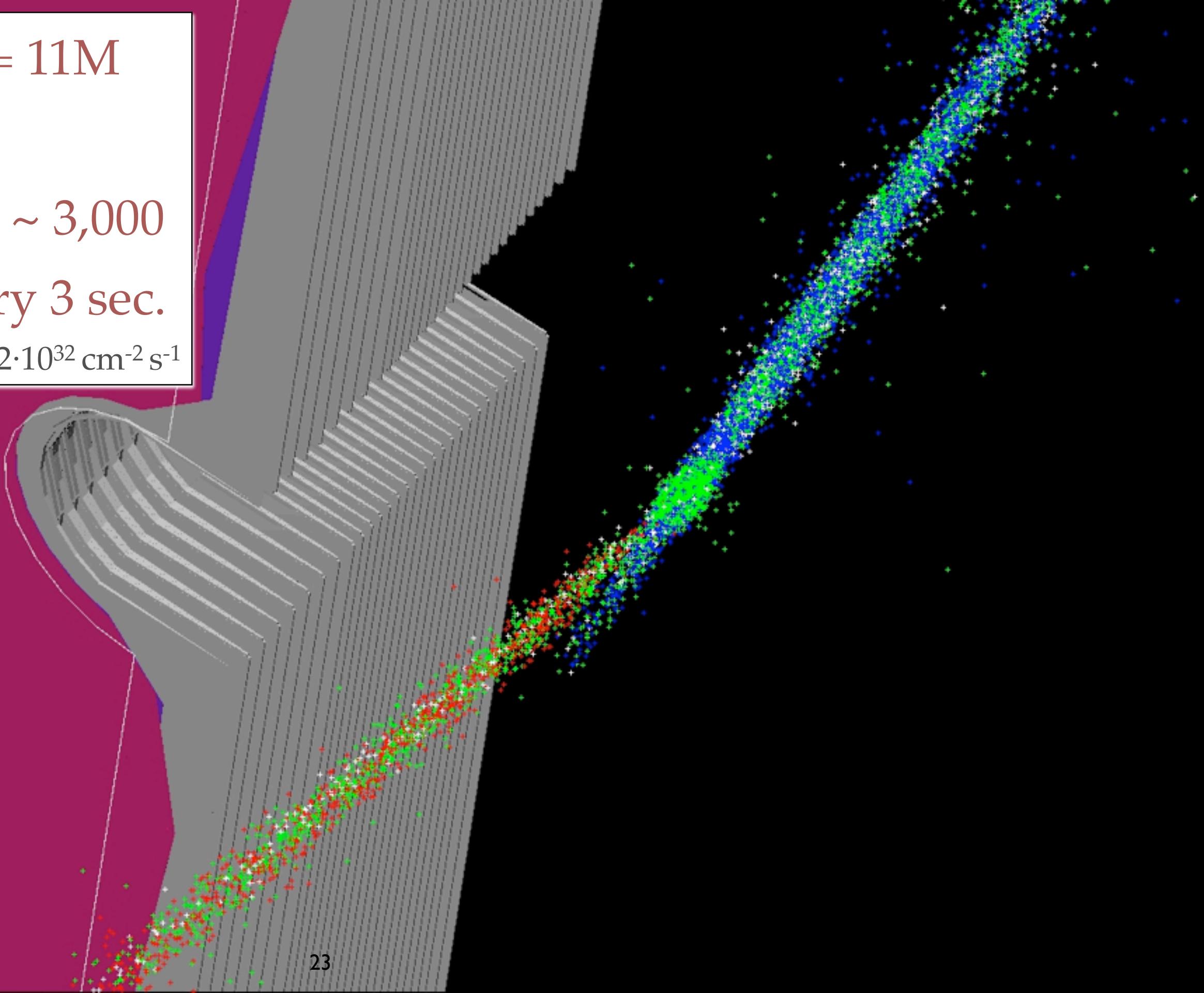


LHCb  
FHCP



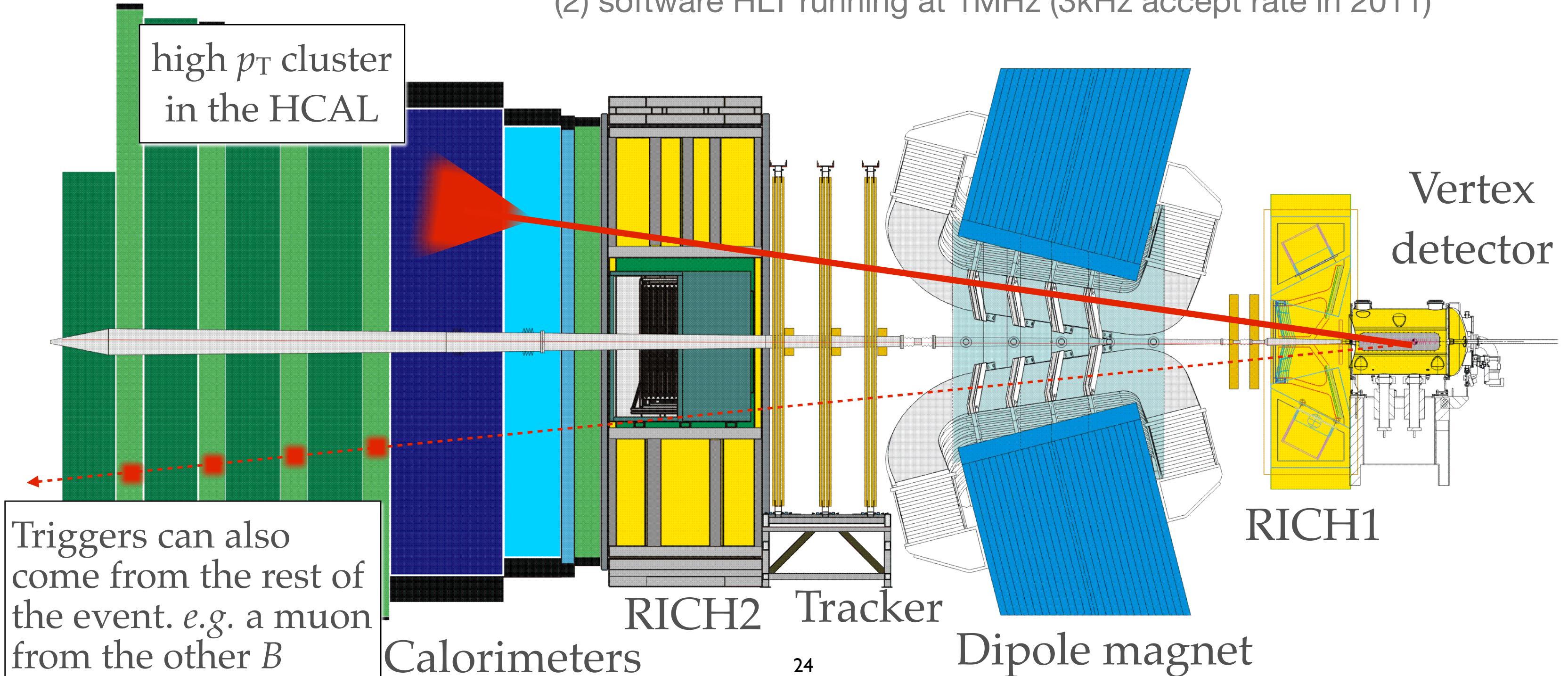
- $N(pp \text{ collisions})/\text{sec} = 11M$
- $N_{4\pi}(b\bar{b})/\text{sec} = 70,000^{(*)}$
- $N(\text{events stored})/\text{sec} \sim 3,000$
- $N(B \rightarrow [hh]_{Dh}) \sim 1 \text{ every 3 sec.}$

(\*)  $\mathcal{L} \approx 2 \cdot 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$



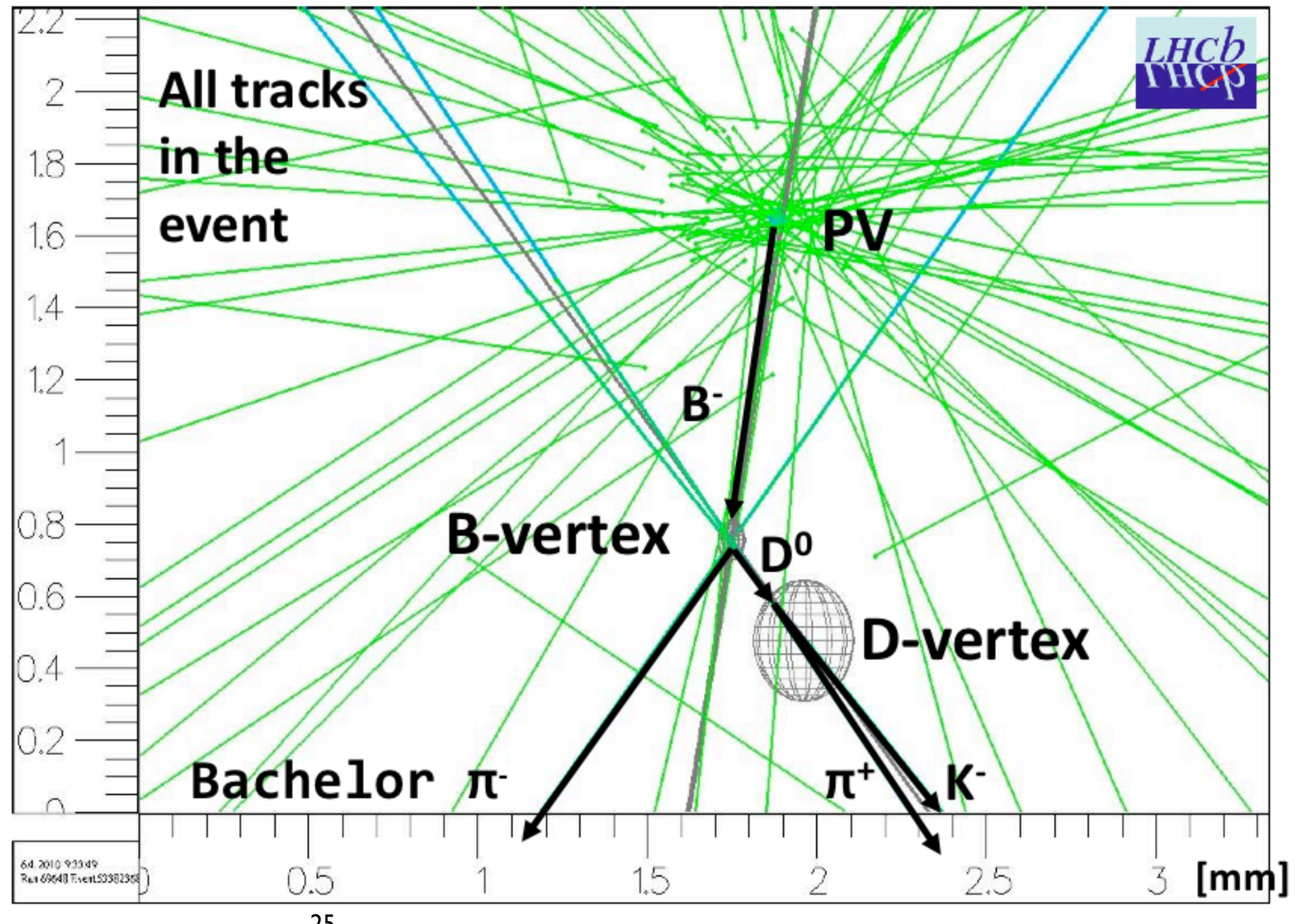
# Triggering of the exclusive hadronic final state: $B^\pm \rightarrow [h^+ h^-]_D h^\pm$

- LHCb has a two-stage trigger.
  - (1) hardware “L0” trigger running at 40MHz (decisions at 11MHz)
  - (2) software HLT running at 1MHz (3kHz accept rate in 2011)



# The high level trigger for $B^\pm \rightarrow [h^+ h^-]_D h^\pm$

- Find a high quality, high  $p_T$ , high impact parameter track (this is often the ‘bachelor’  $\pi$  or  $K$  from the  $B$  decay)
- If this successful, then require it to be part of a good quality displaced vertex, consistent with the  $B$  mass.
  - In 2011, a decision tree algorithm has been successfully used.

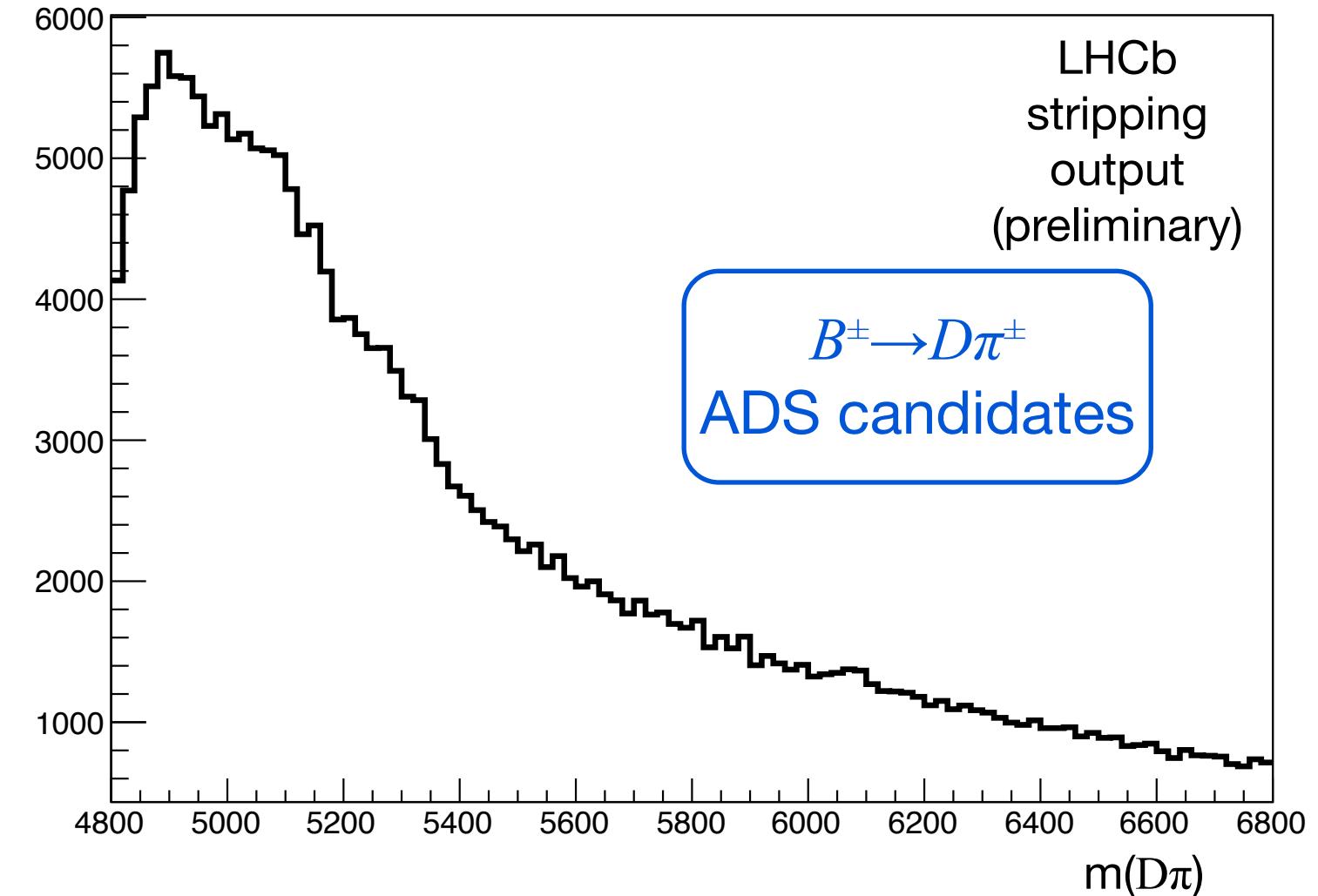
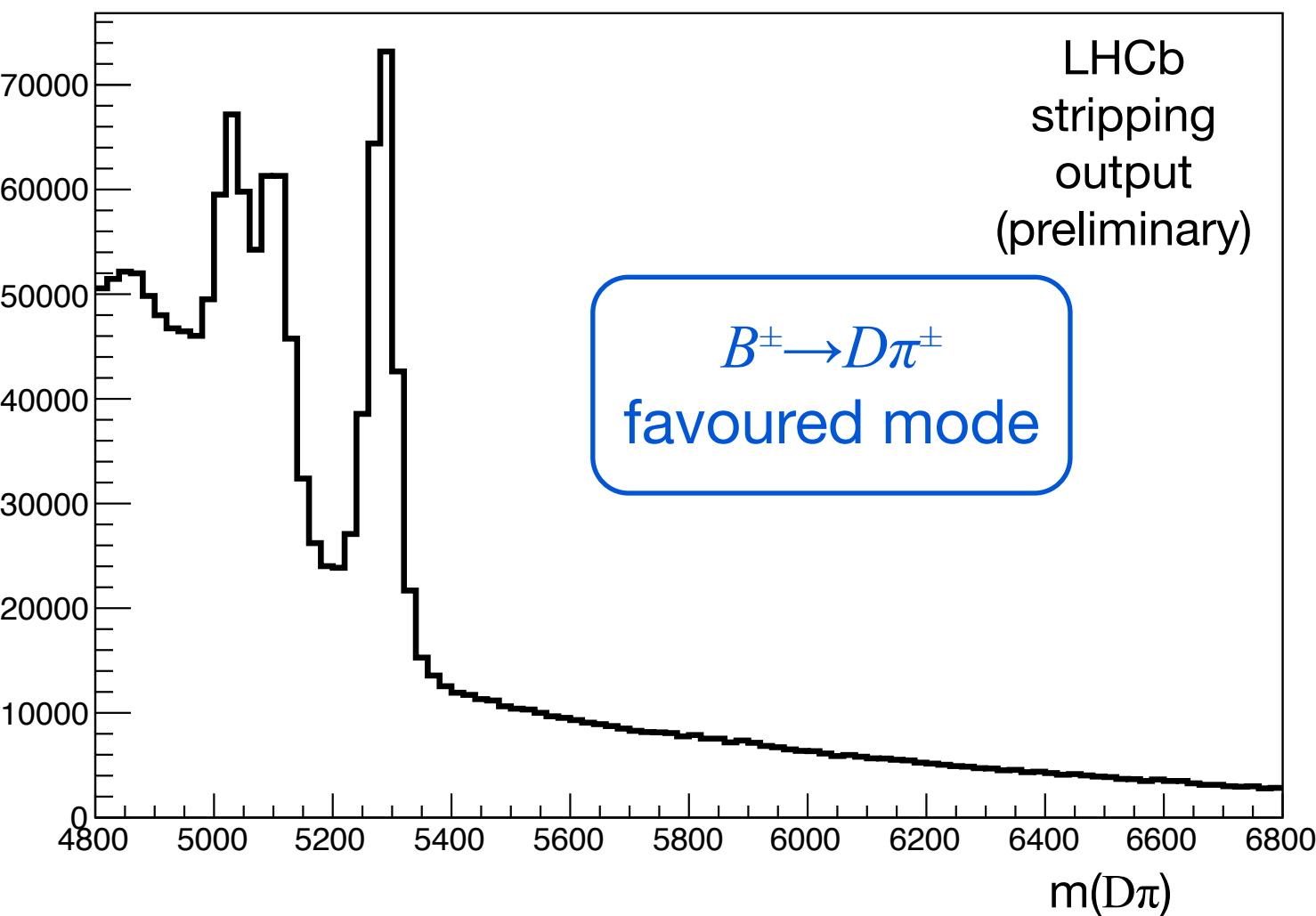


A photograph of a traditional wooden boat, possibly a dugout canoe, resting on a body of water. The boat is dark wood with a light-colored interior. The background is a vast, calm lake under a sky filled with soft, orange and yellow clouds at sunset or sunrise. The overall atmosphere is peaceful and somewhat melancholic.

# Signal selection and extraction

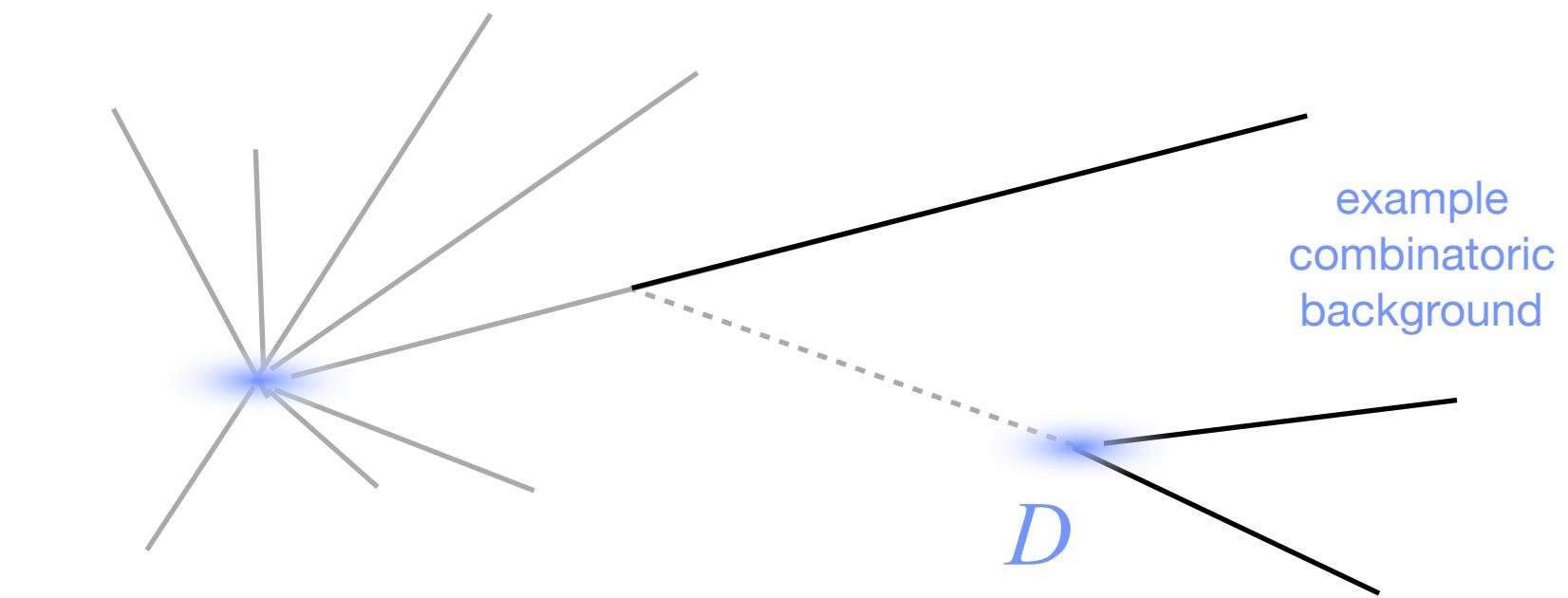
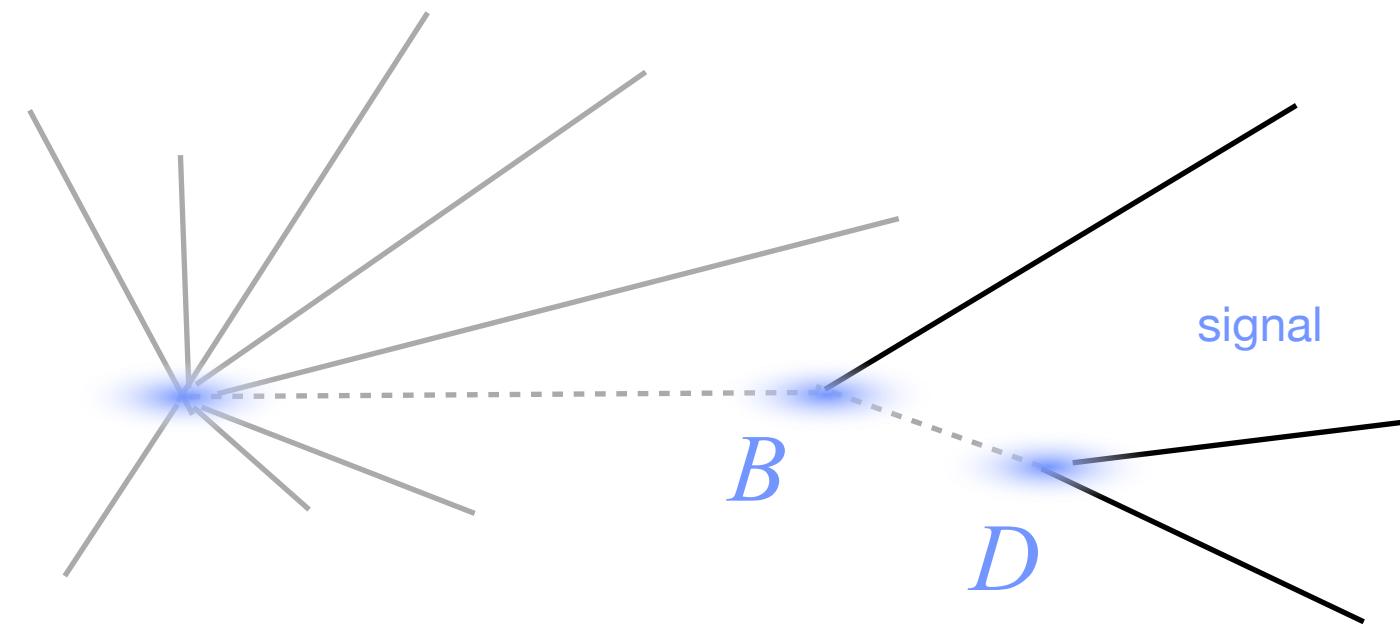
# Analysis of $B^\pm \rightarrow [h^+ h^-]_D h^\pm$

- The full 2011 dataset is used in this analysis, approximately  $1 \text{ fb}^{-1}$
- $B$  candidates are refitted, constraining vertices to points and the  $D$ -candidate mass to  $m(D^0)_{\text{PDG}}$
- The data are “stripped” down to a manageable size with a loose selection.
  - At this point  $B$  peaks are clearly visible in the most abundant modes

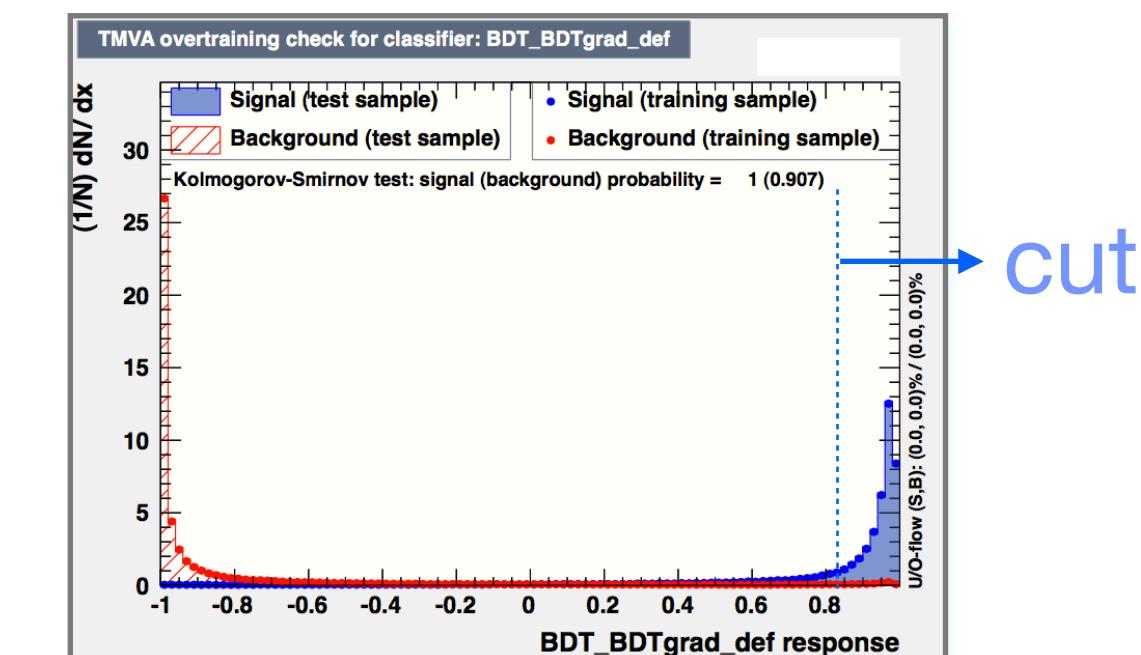


# Minimising combinatoric background

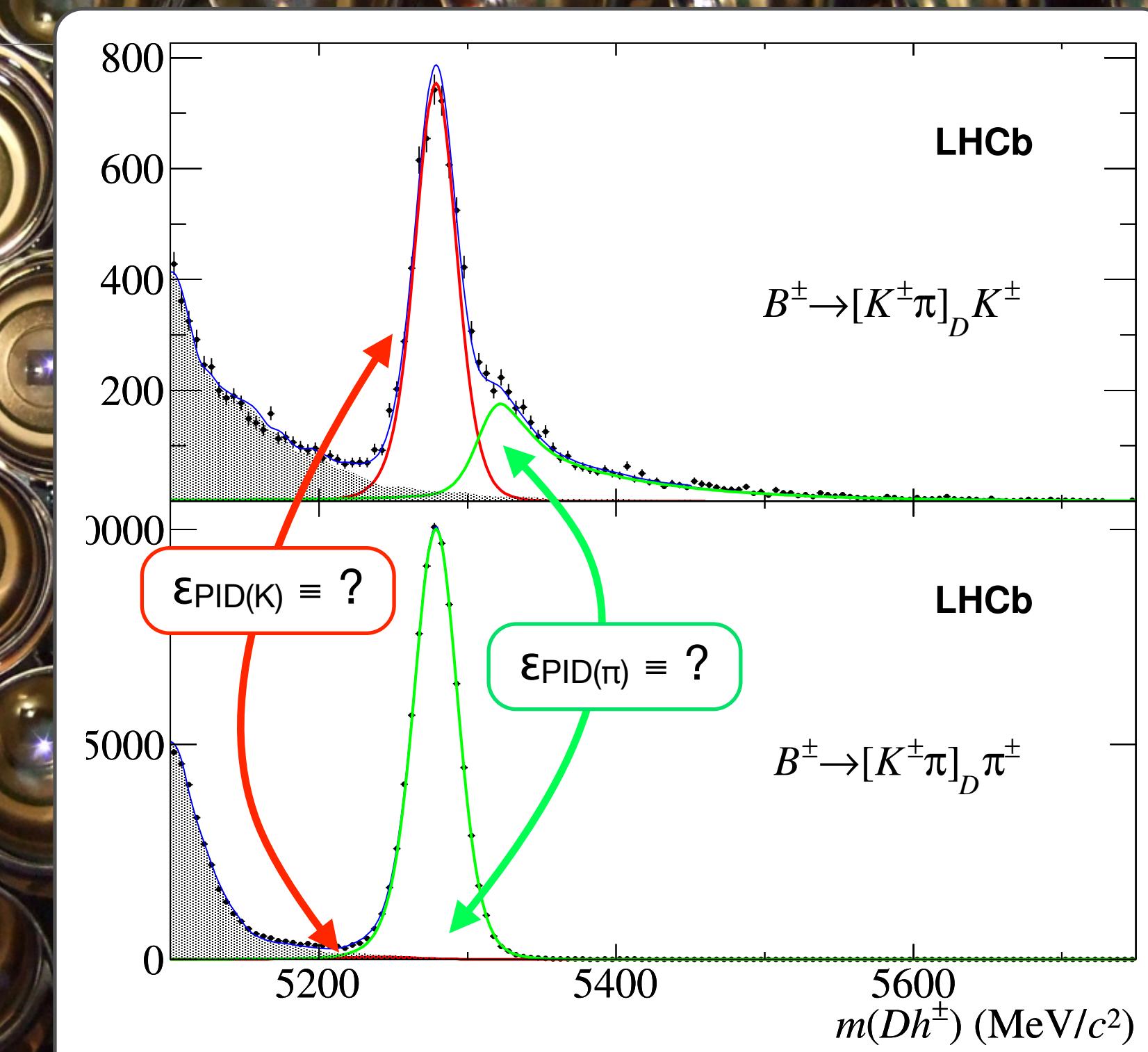
- Use the TMVA Boosted Decision Tree with 20 variables.
- Train on a simulated  $B^\pm \rightarrow [K\pi]_D K^\pm$  sample vs. the data sidebands from the **2010 dataset** ( $35 \text{ pb}^{-1}$ )



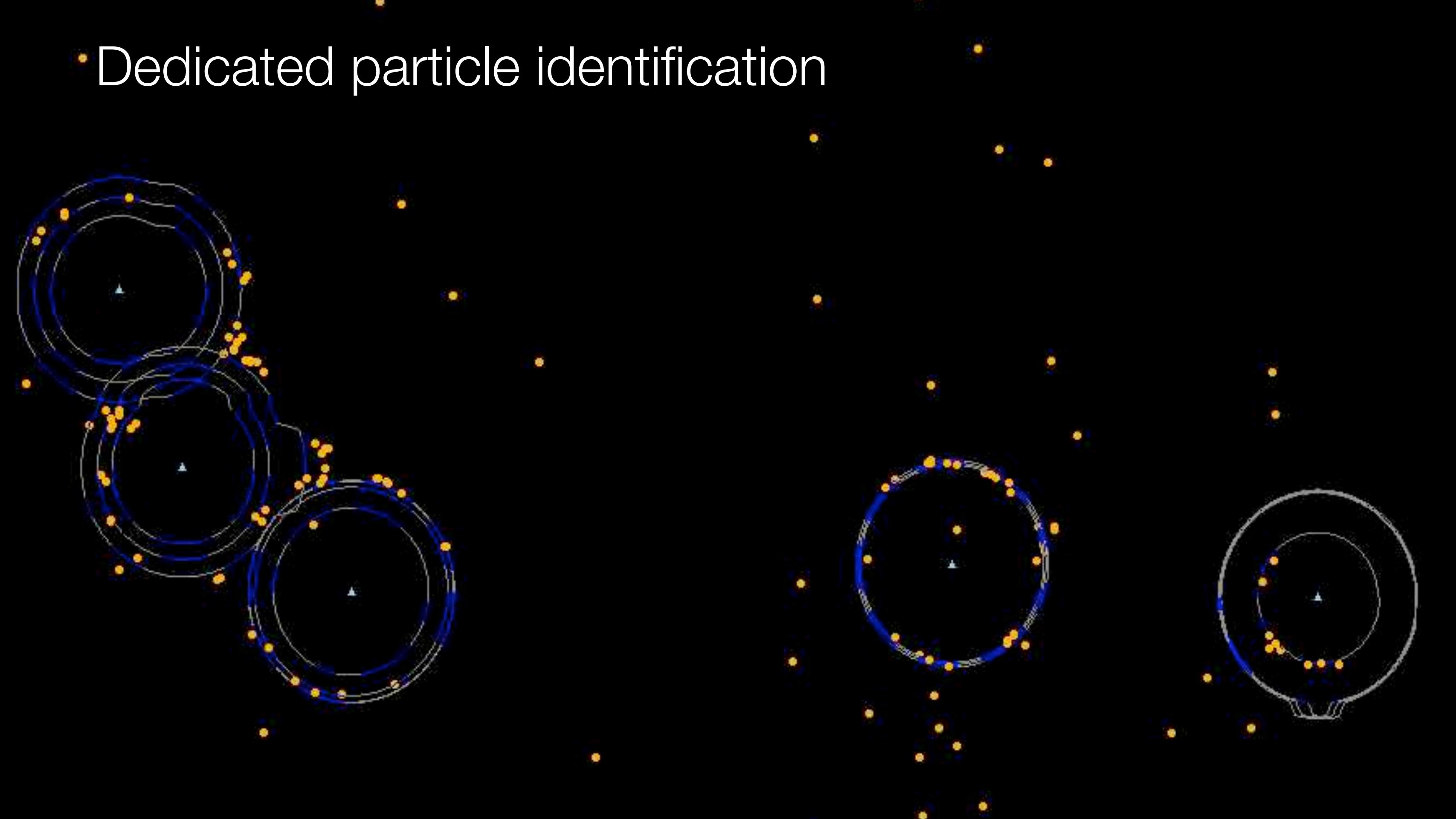
- Useful quantities to distinguish the signal:
  - Transverse momenta
  - Impact parameters
  - Flight distances
  - Quality of vertices
  - Distances of closest approach
  - Comparison of momentum and spatial vectors
  - And some pT information from the rest of the event



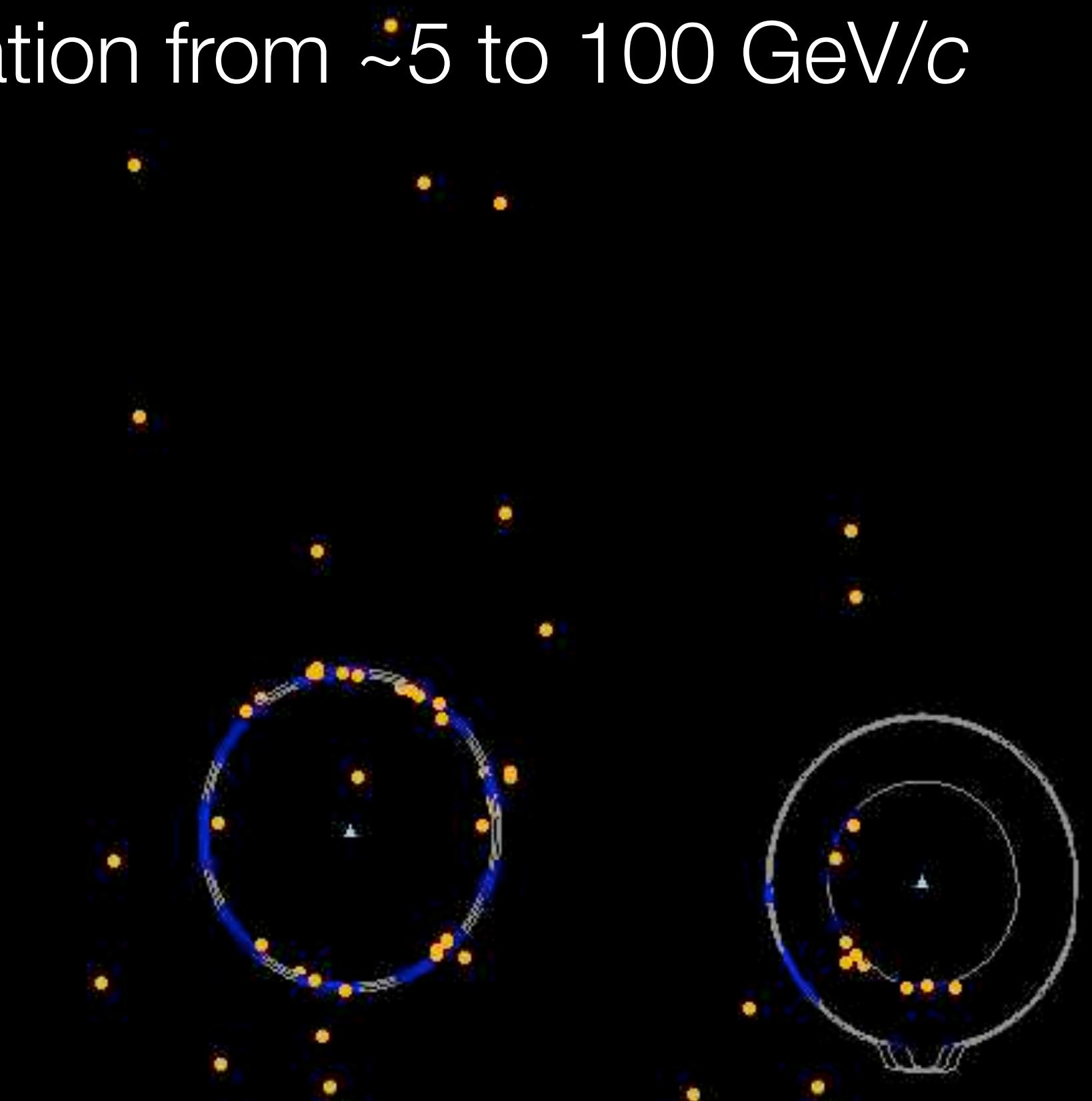
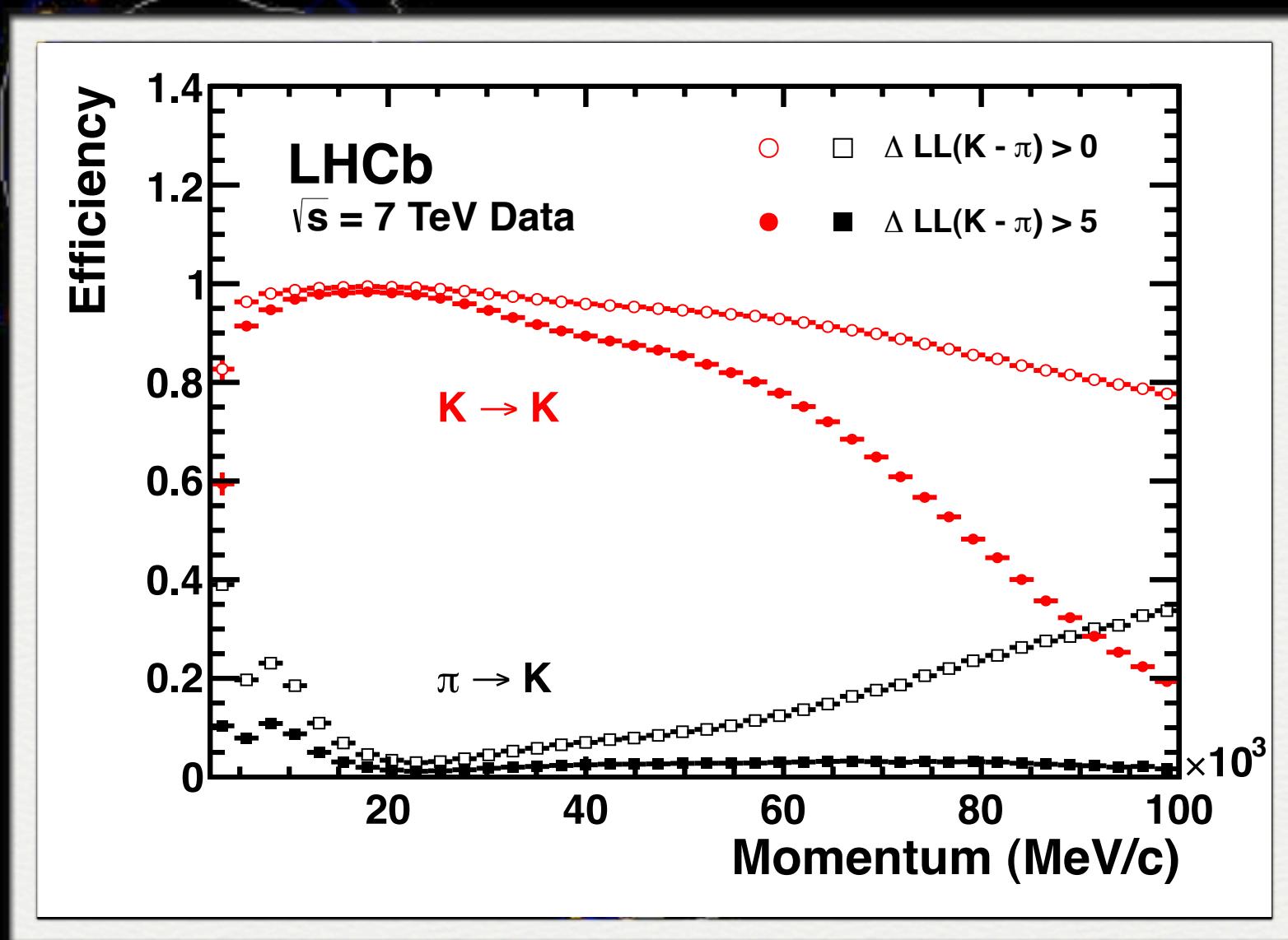
# Dedicated particle identification



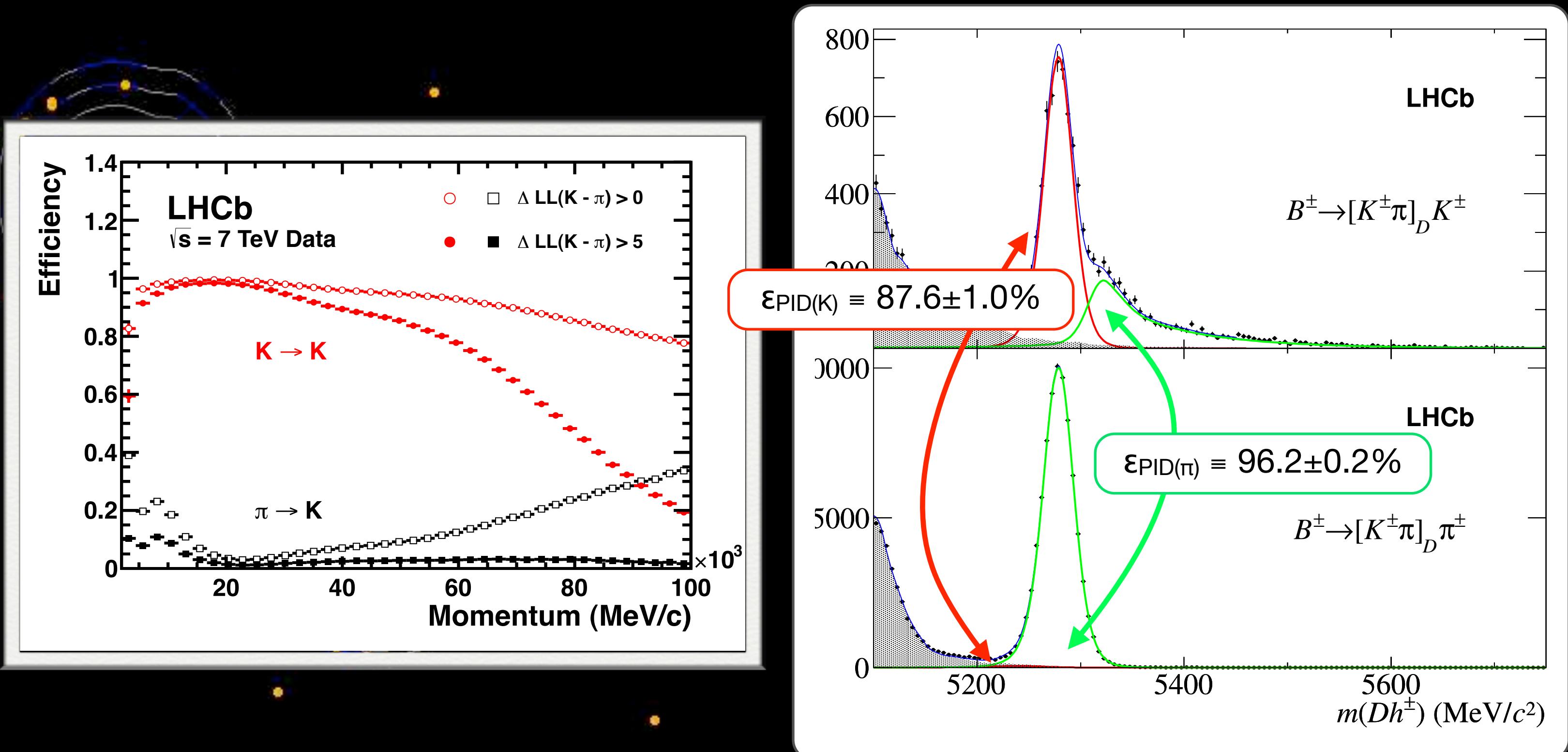
- Dedicated particle identification



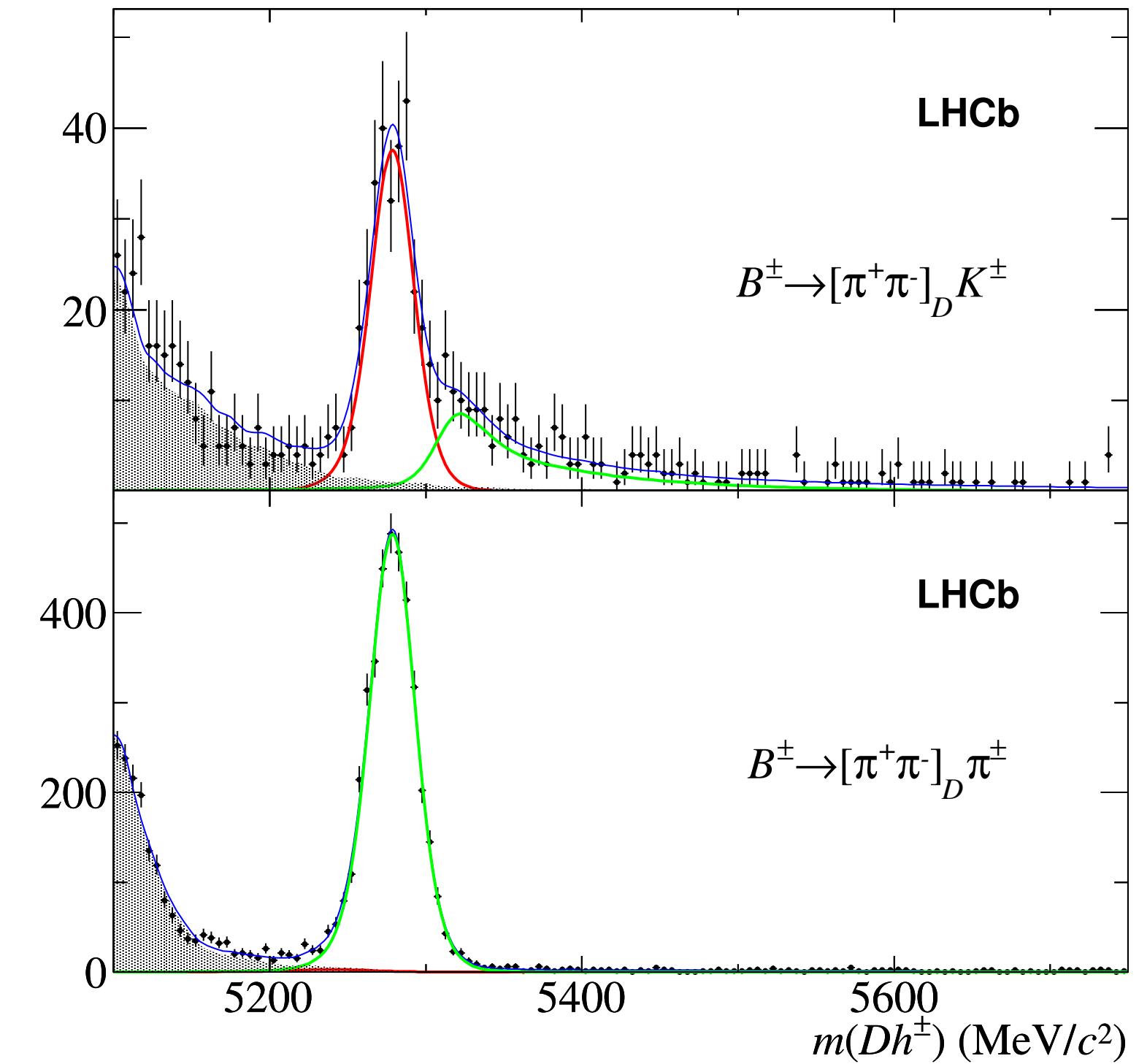
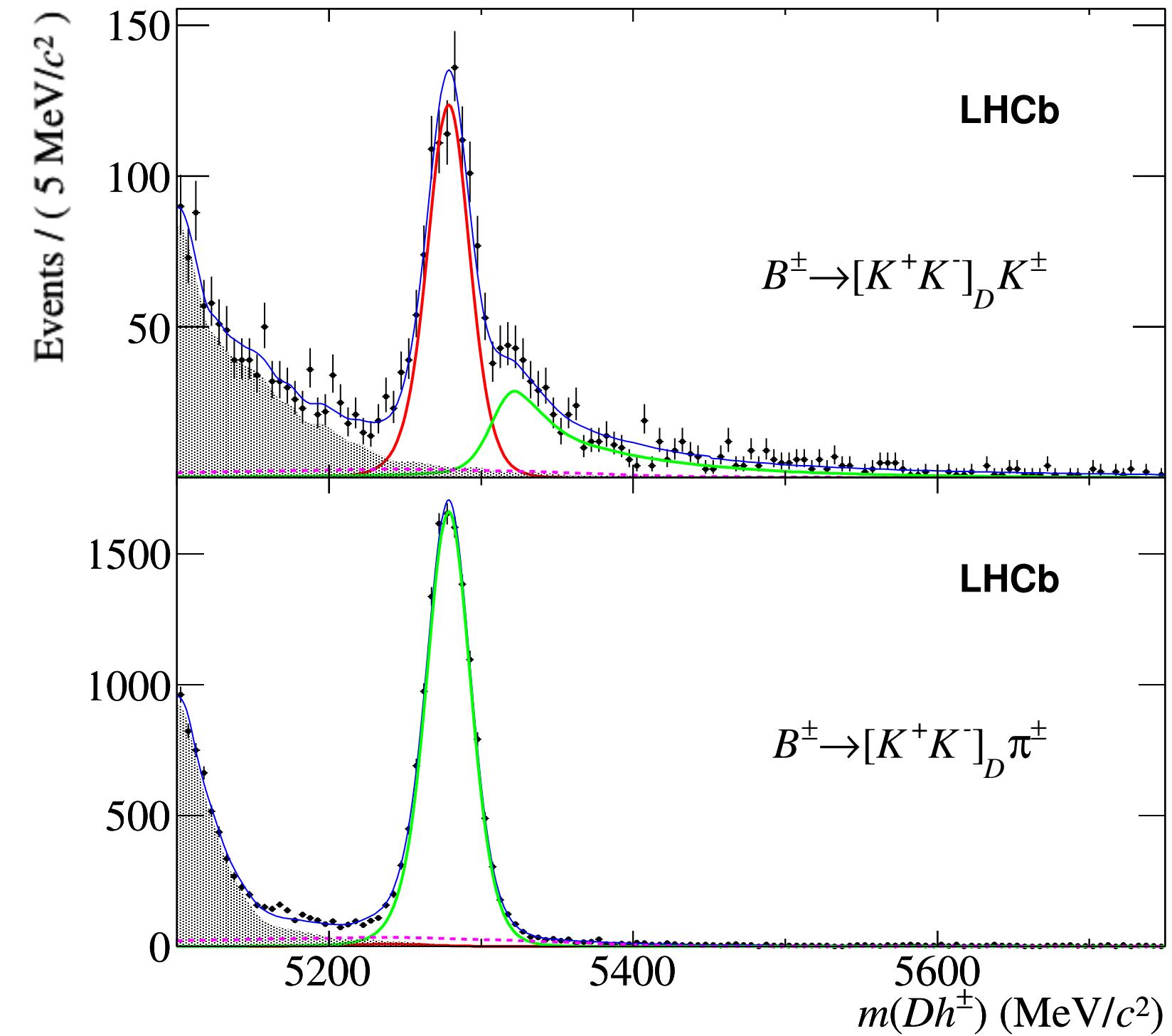
Achieves pion-kaon separation from  $\sim 5$  to  $100 \text{ GeV}/c$



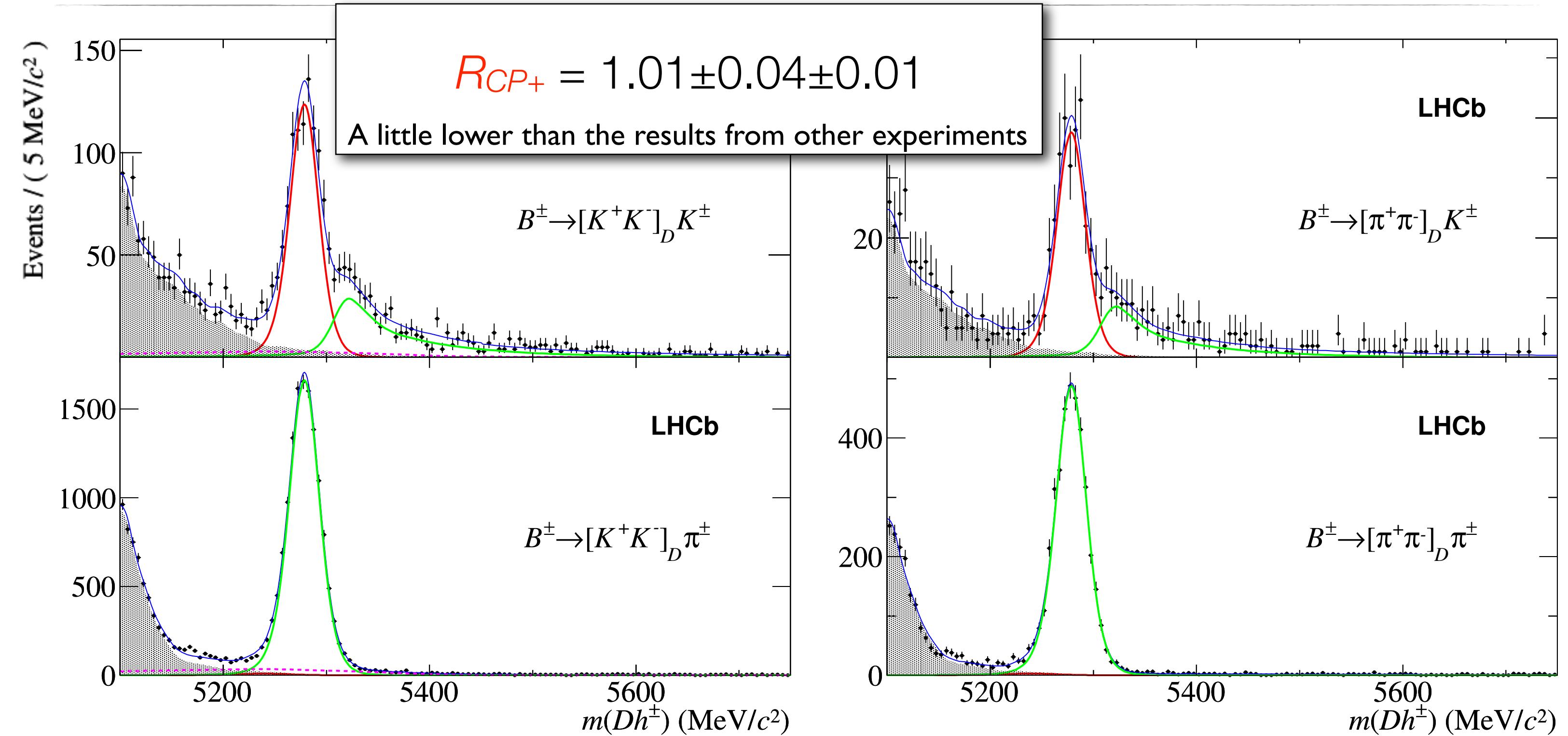
- The result is applicable to all modes considered



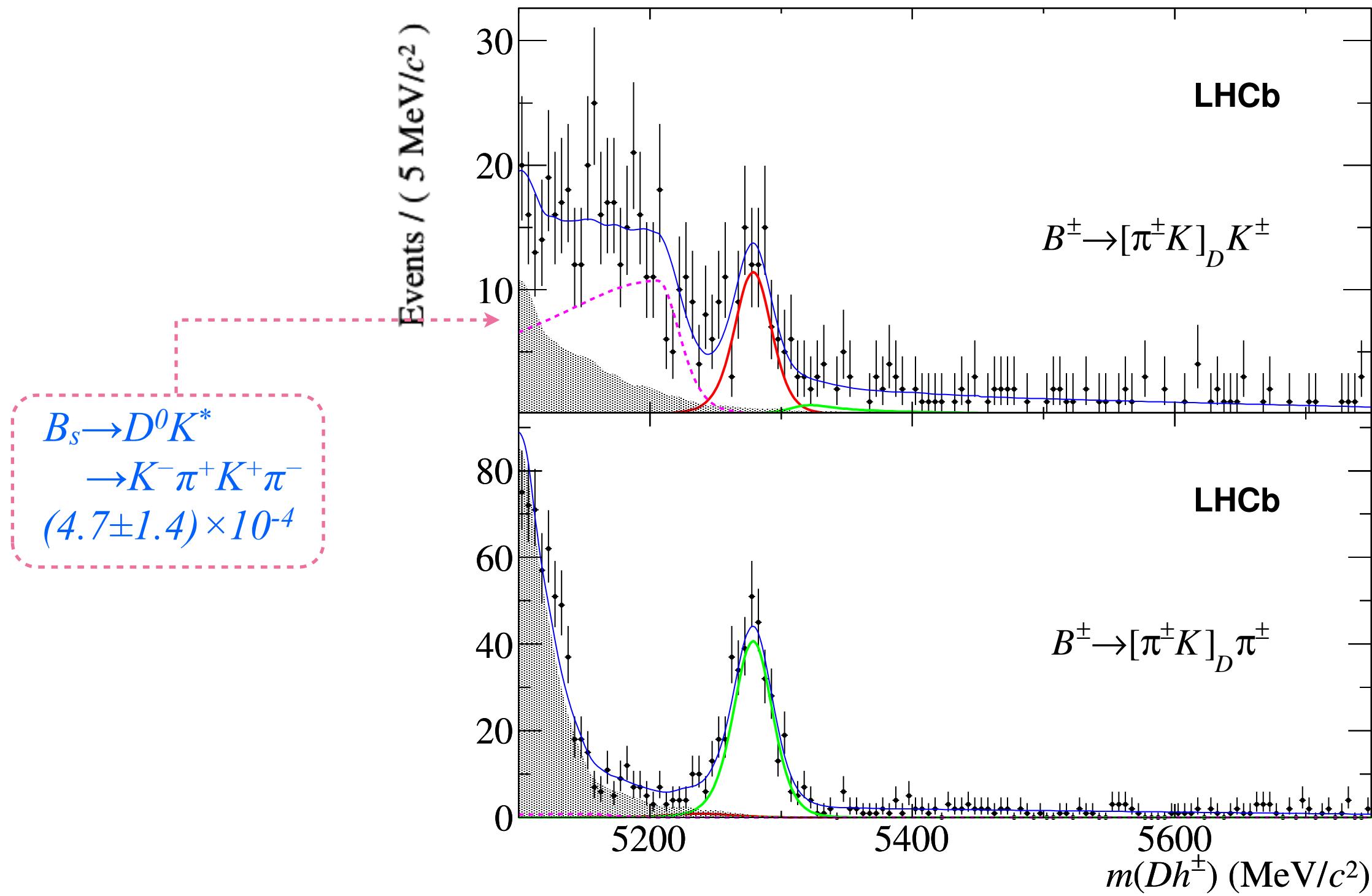
# The $CP$ eigenstate modes



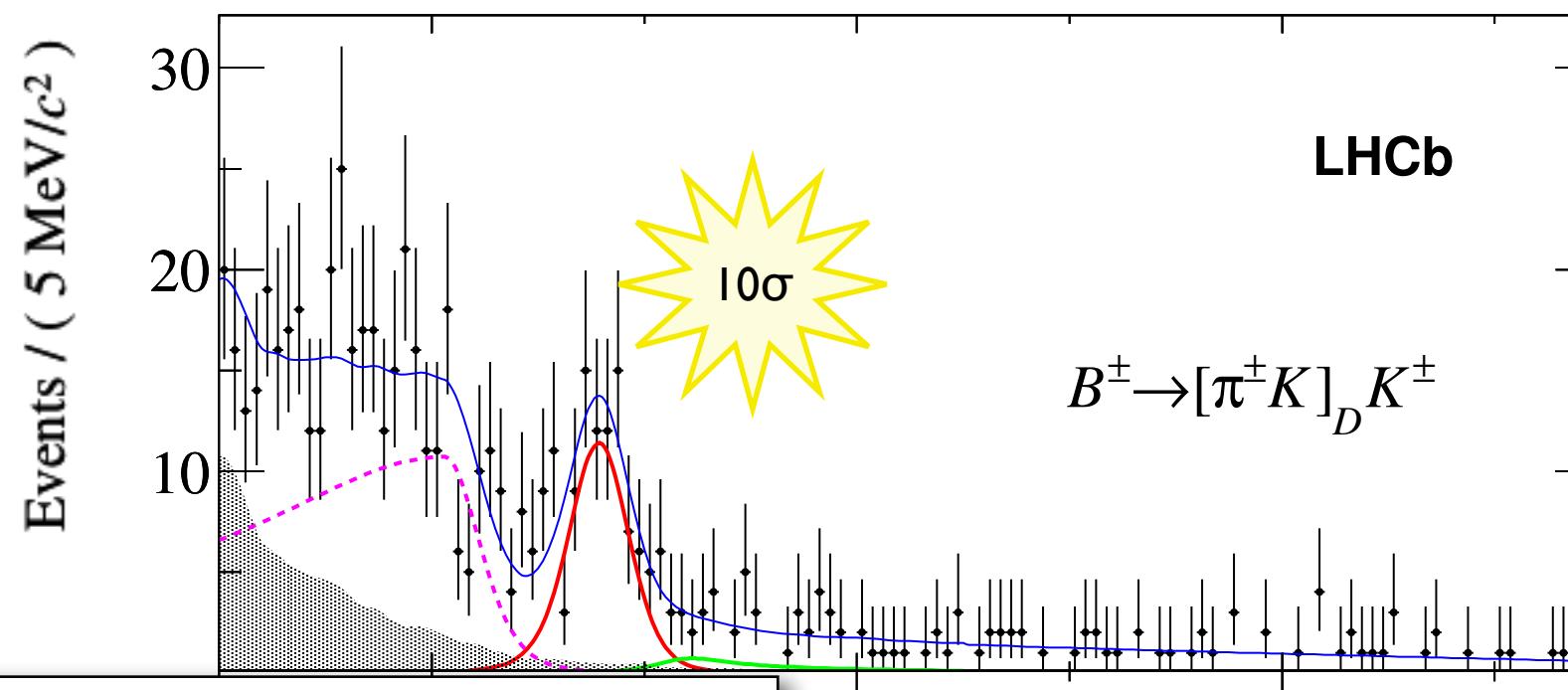
# The $CP$ eigenstate modes



# First observation of the $DK^\pm$ , ADS mode

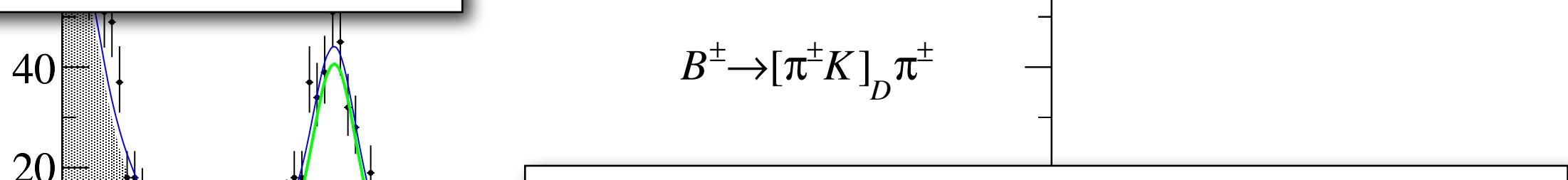


# First observation of the $D\bar{K}^\pm$ , ADS mode



$$\mathcal{B}(B^\pm \rightarrow [\pi^\pm K]_D K^\pm) \approx (2.2 \pm 0.3) \times 10^{-7}$$

$R_{ADS} = (1.52 \pm 0.20 \pm 0.04)\%$   
Compatible with previous measurements

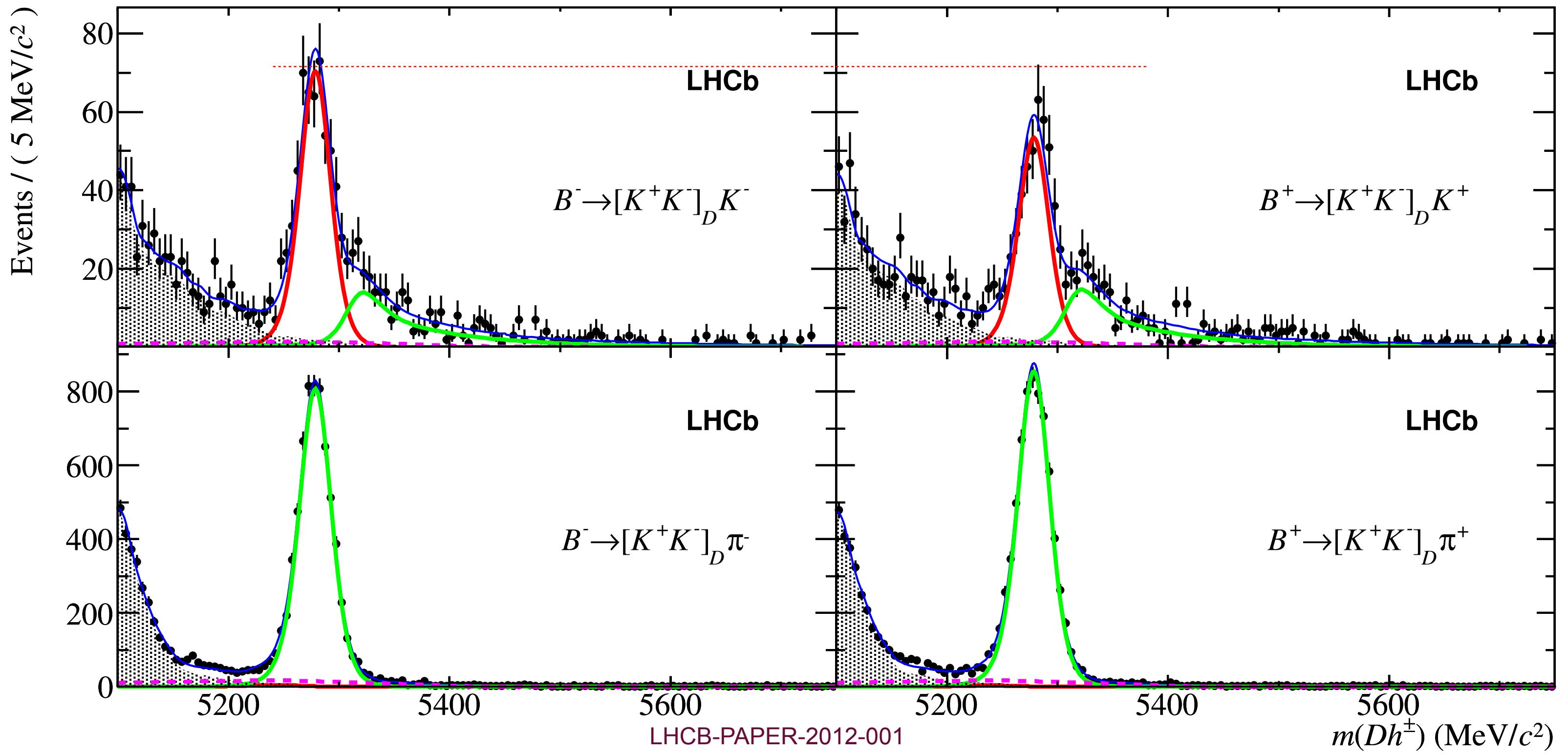


$R_{ADS(\pi)} = (0.410 \pm 0.025 \pm 0.005)\%$   
~ $2\sigma$  higher than previous measurements

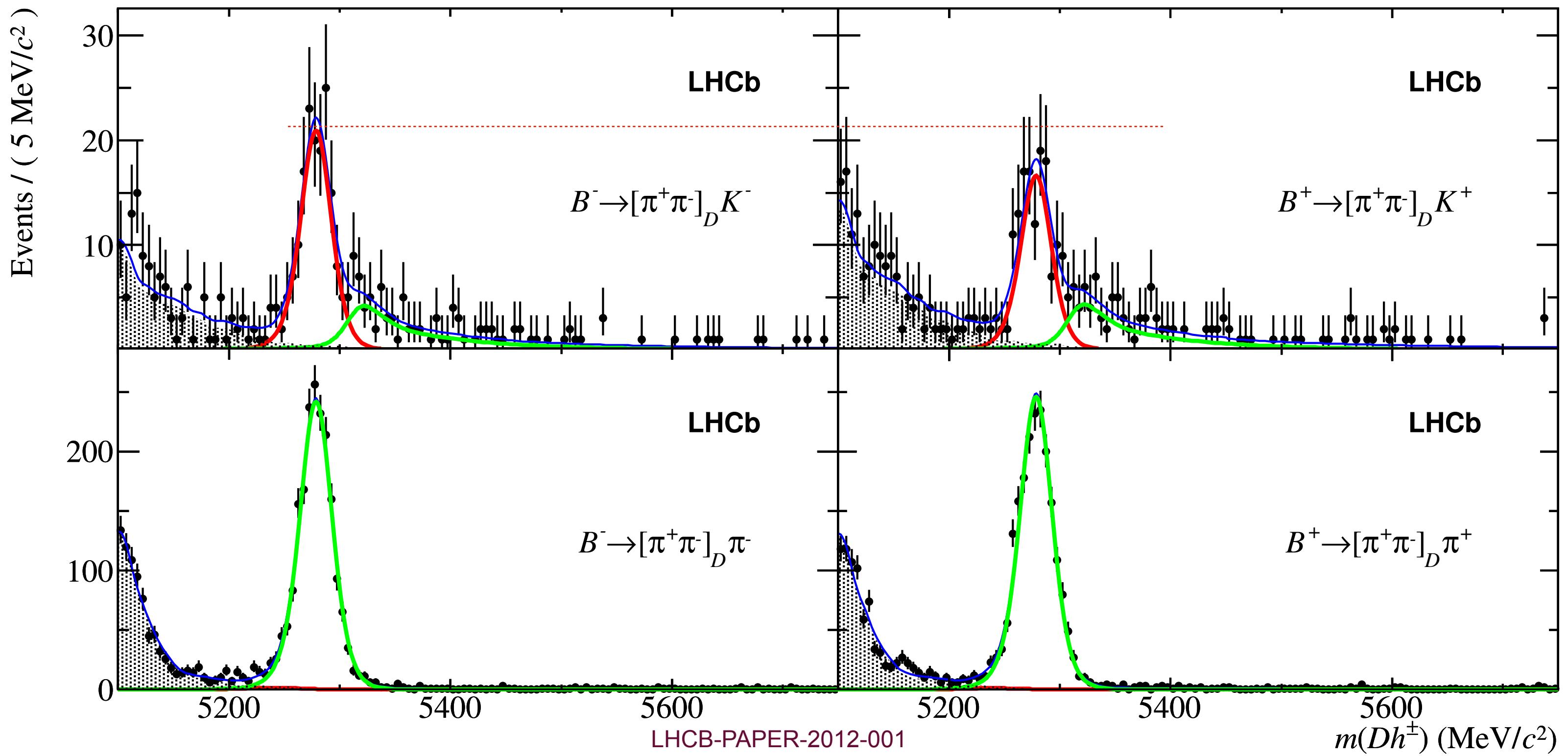
A photograph of a traditional wooden boat with a pointed bow, resting on a body of water. The sky is filled with soft, orange and yellow clouds at sunset. The boat's hull is a light wood color, and it has a dark, possibly black, interior visible through the open stern.

What about  $CP$  violation?

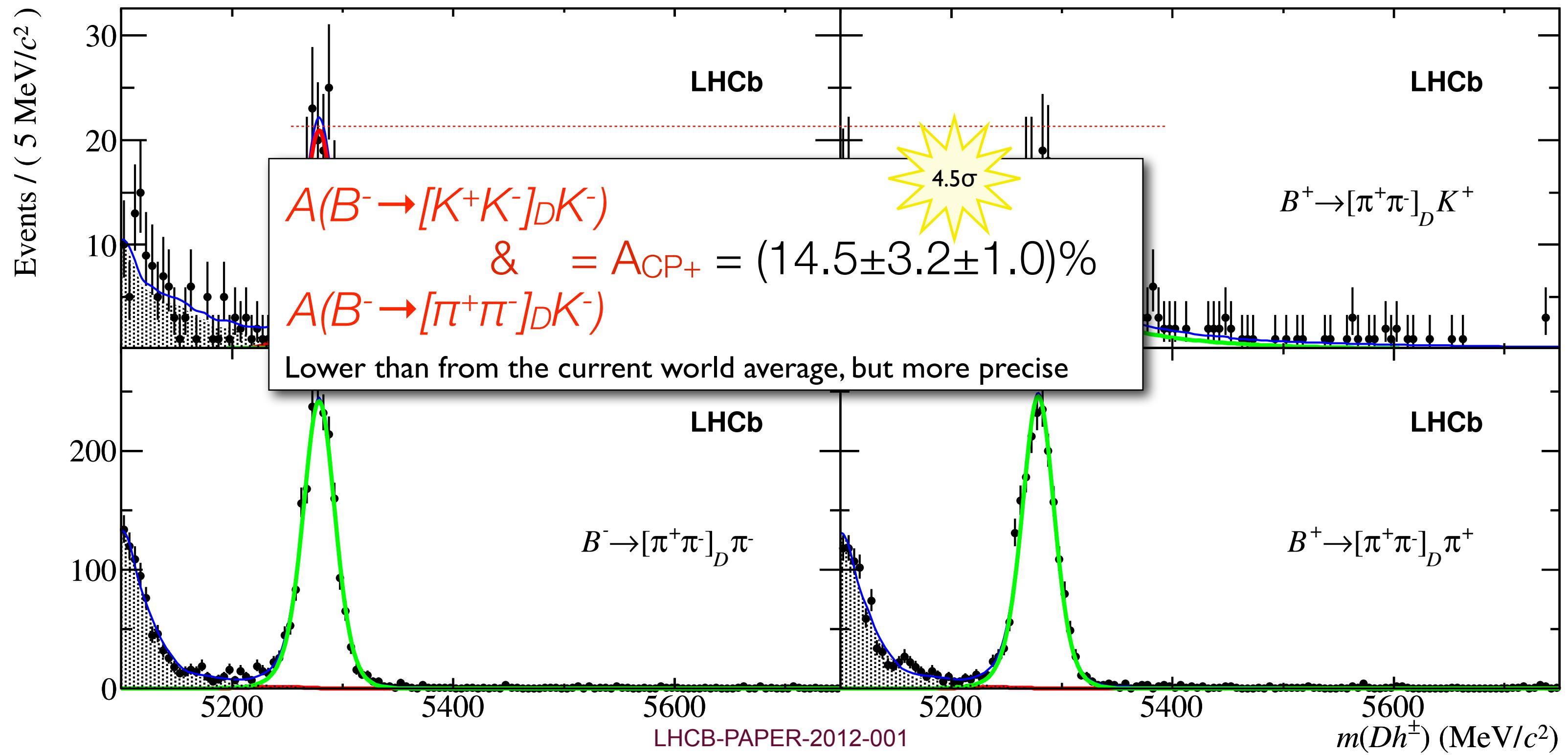
# $KK$ mode, split by the charge of the $B$



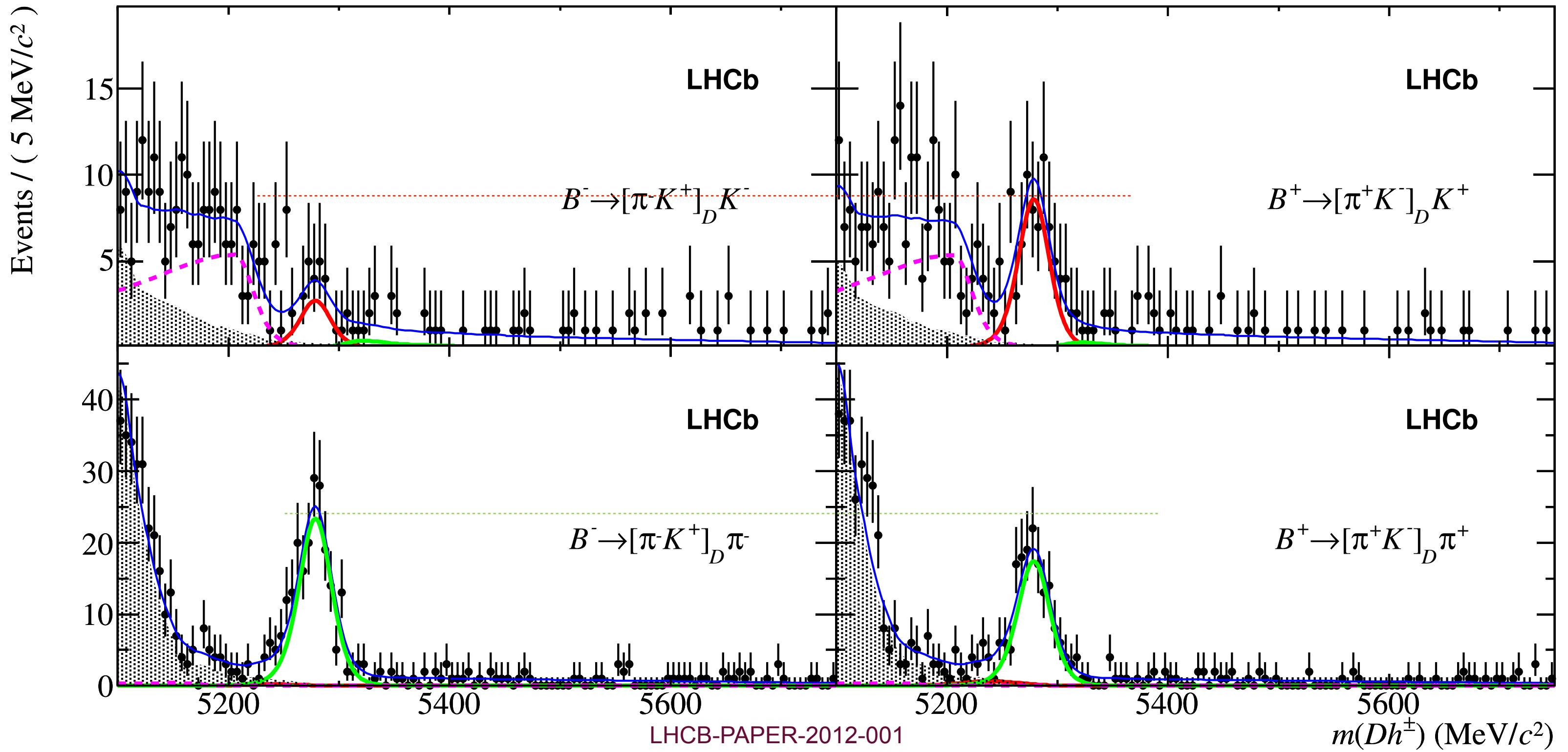
# $\pi\pi$ mode, split by the charge of the $B$



# $\pi\pi$ mode, split by the charge of the $B$



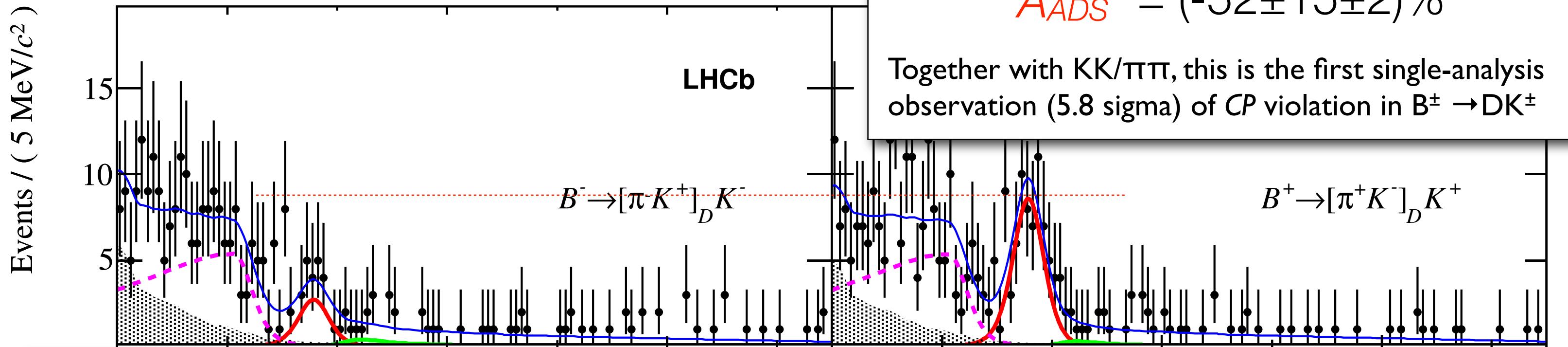
# ADS mode, split by the charge of the $B$



# ADS mode, split by the charge of the $B$

4.0 $\sigma$

Events / ( 5 MeV/ $c^2$ )



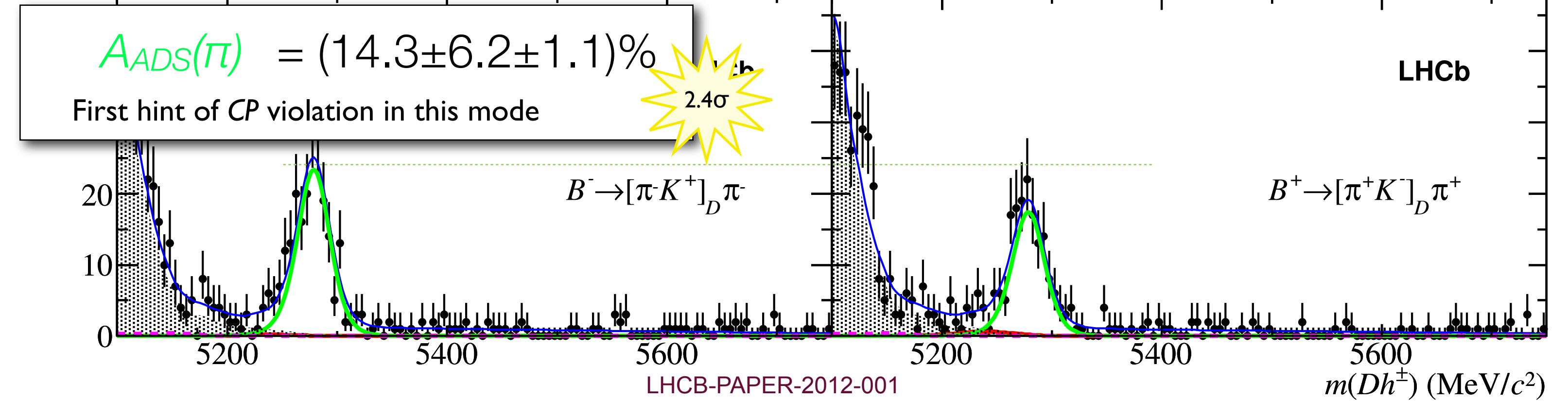
$$A_{ADS} = (-52 \pm 15 \pm 2)\%$$

Together with KK/ $\pi\pi$ , this is the first single-analysis observation (5.8 sigma) of  $CP$  violation in  $B^\pm \rightarrow D K^\pm$

$$A_{ADS}(\pi) = (14.3 \pm 6.2 \pm 1.1)\%$$

First hint of  $CP$  violation in this mode

LHCb  
2.4 $\sigma$



A photograph of a traditional wooden boat, possibly a dugout canoe, resting on calm water. The sky is filled with soft, warm-colored clouds, transitioning from blue to orange and yellow, suggesting either sunrise or sunset. The boat's hull is dark wood, and its interior is visible, showing some debris or equipment.

Interpretation and [near] future

# But how does this tie-in with $\gamma$ ?

- All of the physics observables may be written in terms of the “fundamental” parameters:  $r_B$ ,  $\gamma$ ,  $\delta_B$
- A full multi-mode treatment, leading to an LHCb measurement of  $r_B$ ,  $\gamma$ ,  $\delta_B$  is in preparation.
- However, in the short-term, we can get an idea by using the standard equations (below);
  - take the strong phase  $\delta_D$  is well known. (neglecting a  $\pm 12^\circ$  uncertainty)

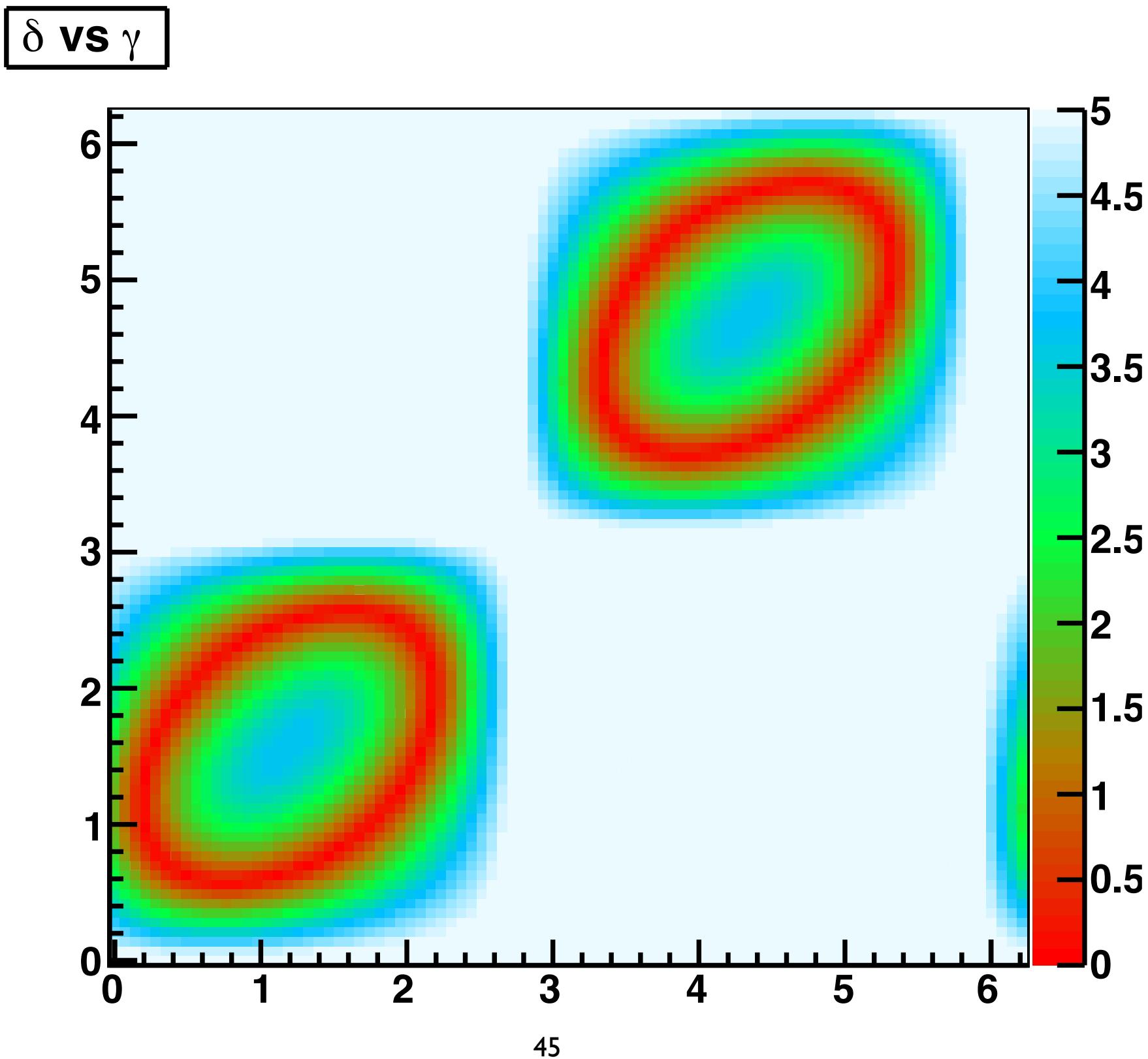
$$R_{CP+} = 1 + r_B^2 + 2r_B \cos \delta_B \cos \gamma$$

$$A_{CP+} = \frac{2r_B \sin \delta_B \sin \gamma}{1 + r_B^2 + 2r_B \cos \delta_B \cos \gamma}$$

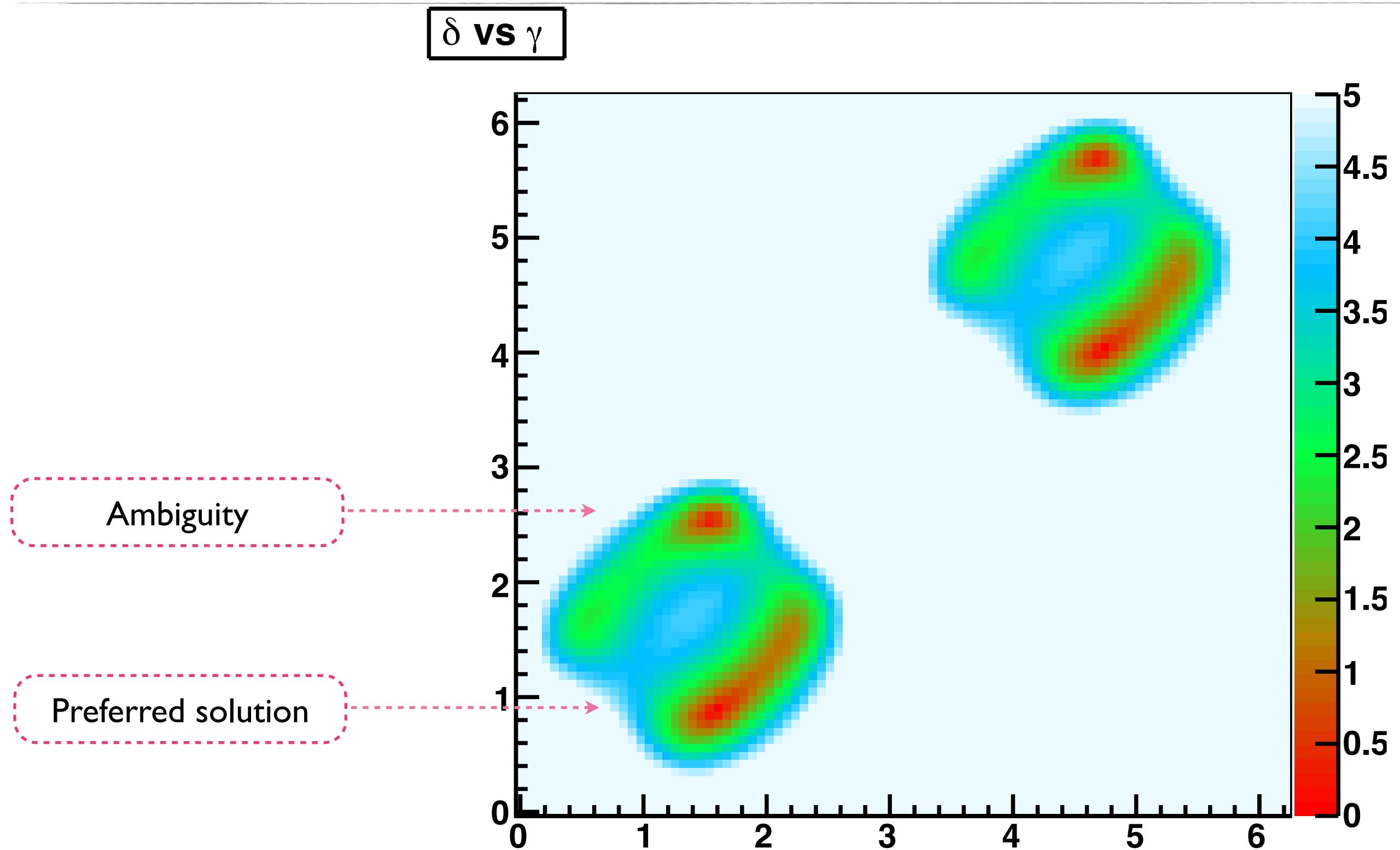
$$R^{ADS} = \frac{r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos \gamma}{1 + (r_B r_D)^2 + 2r_B r_D \cos(\delta_B - \delta_D) \cos \gamma}$$

$$A^{ADS} = \frac{2r_B r_D \sin(\delta_B + \delta_D) \sin \gamma}{r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos \gamma}$$

Using:  $R_{ADS(K)}$  and  $A_{ADS(K)}$



Using:  $R_{ADS(K)}$  and  $A_{ADS(K)}$  and  $R_{CP+}$  and  $A_{CP+}$



# This is just the first step for LHCb!

Many direct CPV analyses coming to maturity:

$$B^- \rightarrow D \ K^-$$

$$D \rightarrow K^+ \pi^-$$

$$D \rightarrow K^- K^+$$

$$D \rightarrow \pi^- \pi^+$$

$$D \rightarrow K_S^0 \pi^+ \pi^-$$

$$D \rightarrow K_S^0 K^+ K^-$$

$$D \rightarrow K^+ \pi^- \pi^+ \pi^-$$

$$D \rightarrow K^+ \pi^- \pi^0$$

$$\bar{B}^0 \rightarrow D \ K^{*0}$$

$$D \rightarrow K^+ \pi^-$$

$$D \rightarrow K^- K^+$$

$$D \rightarrow \pi^- \pi^+$$

$$B^- \rightarrow D \ K^- \pi^+ \pi^-$$

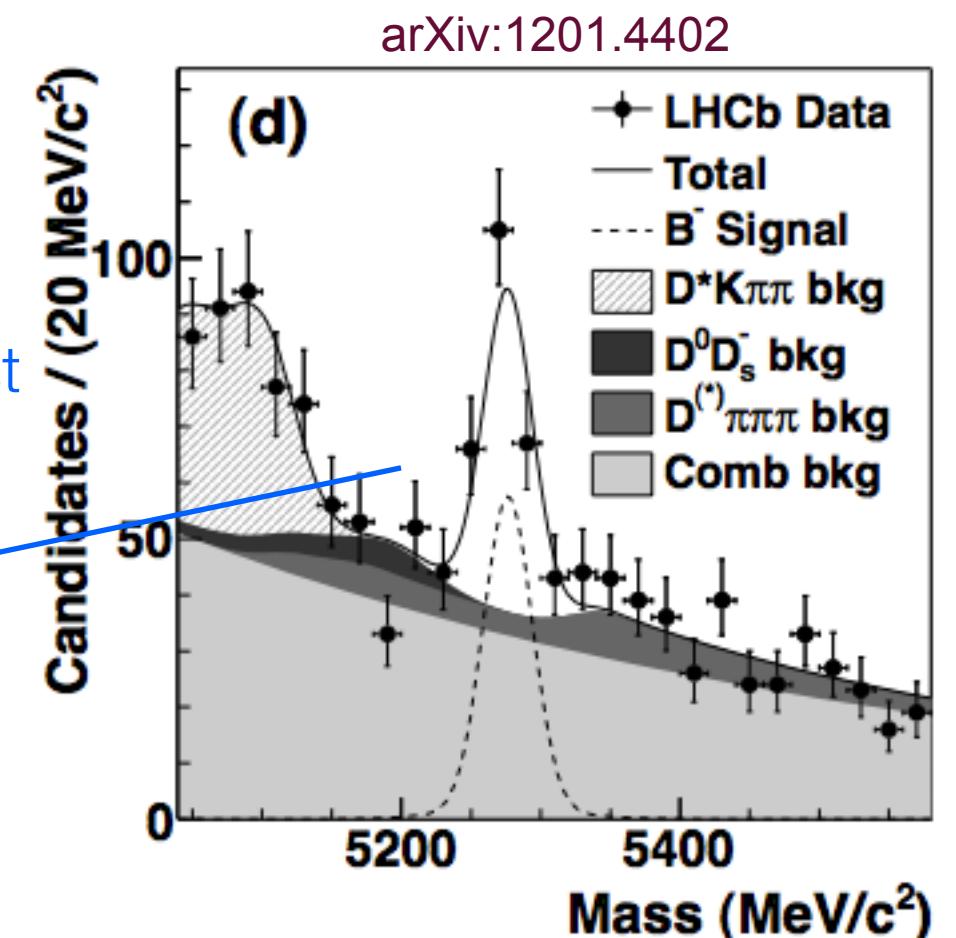
$$D \rightarrow K^+ \pi^-$$

$$D \rightarrow K^- K^+$$

$$D \rightarrow \pi^- \pi^+$$

presented  
today.

Favoured  
mode first  
observed  
in 2010



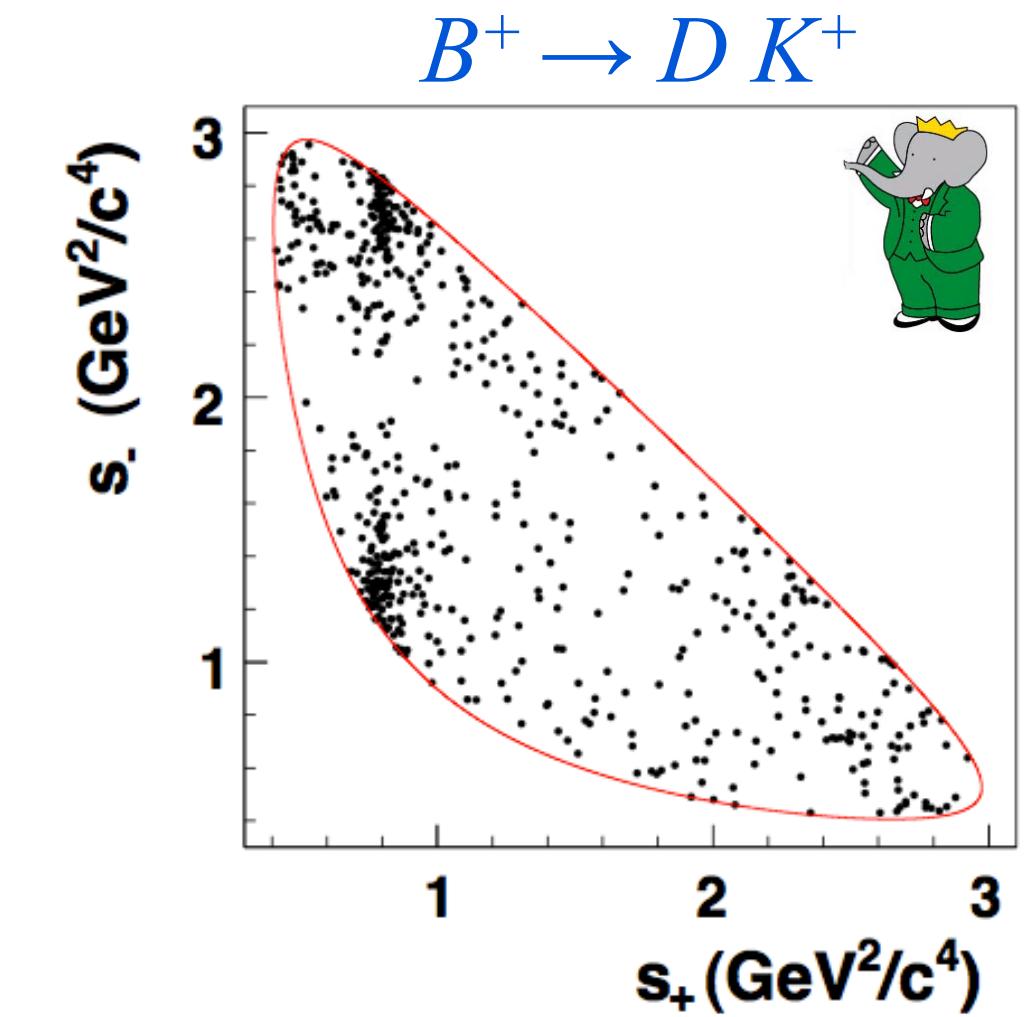
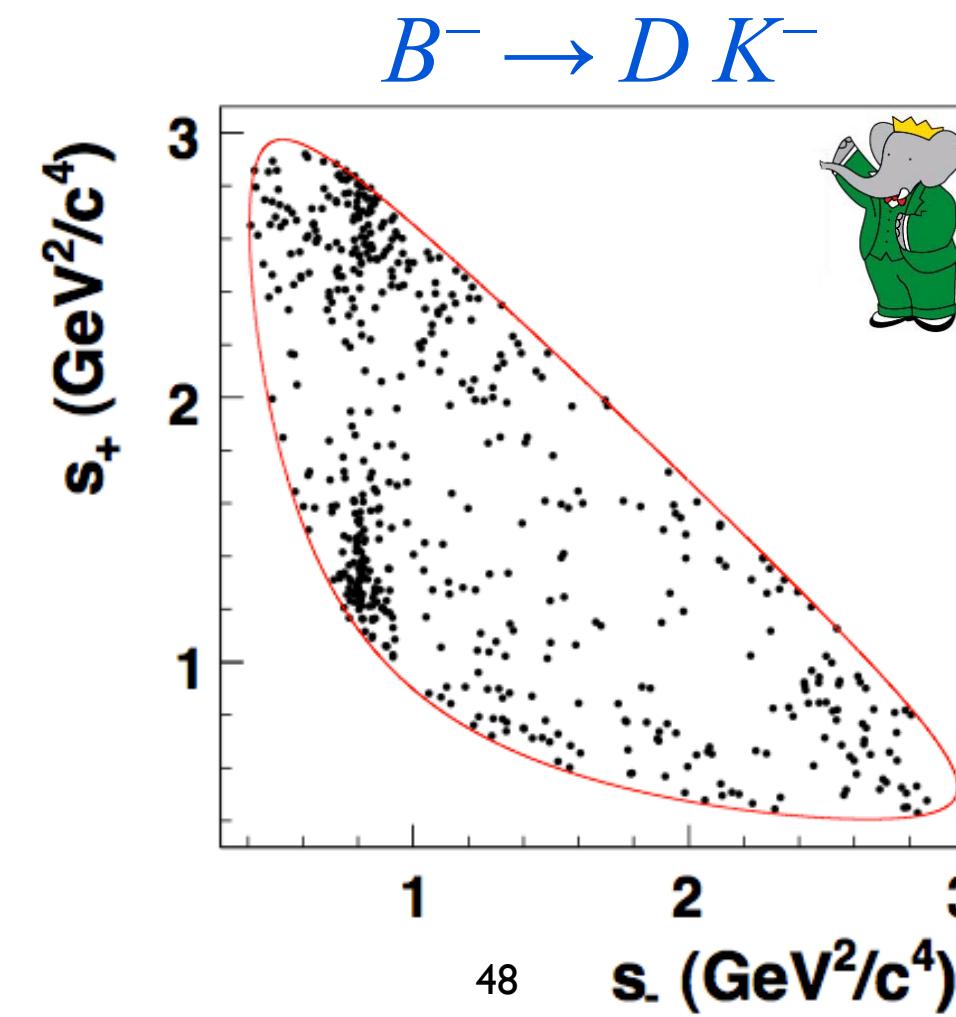
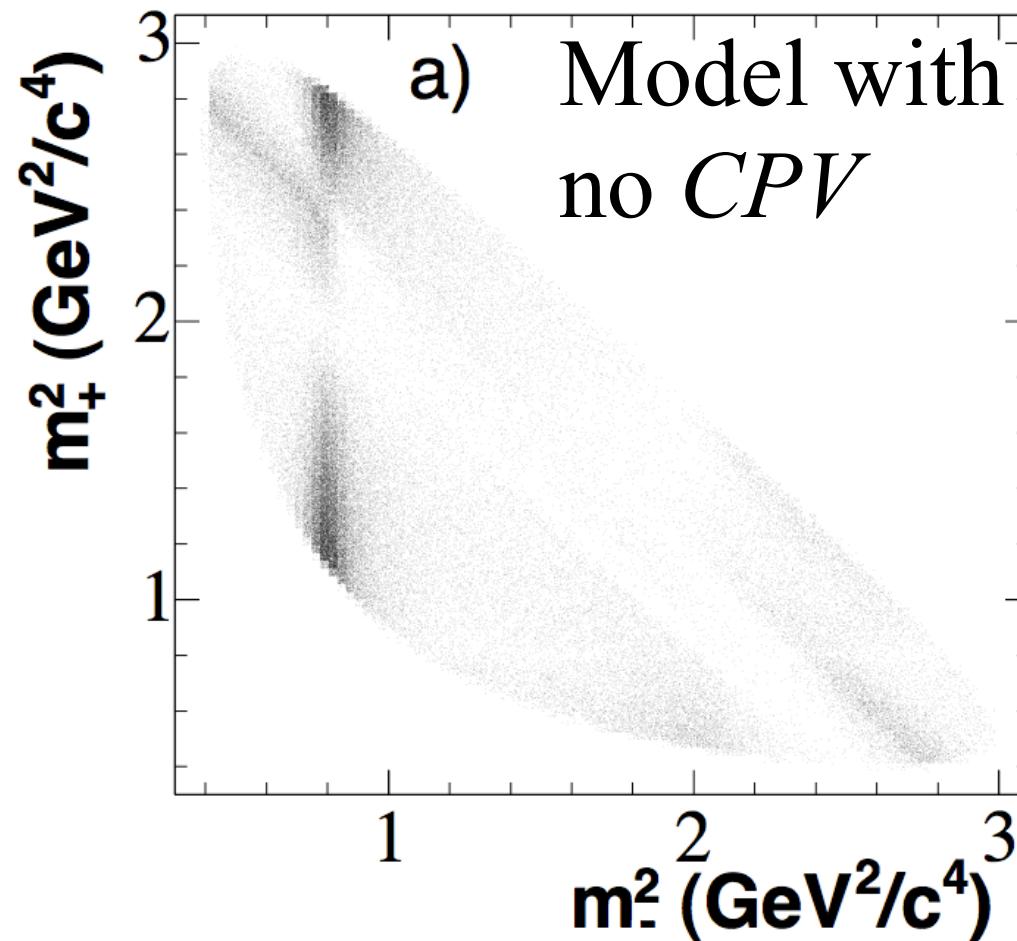
# Summer 2012: important contribution from the “GGSZ” method

- Exactly the same idea: interference between  $b \rightarrow u$  and  $b \rightarrow c$  transitions but this time, use a three-body common final state

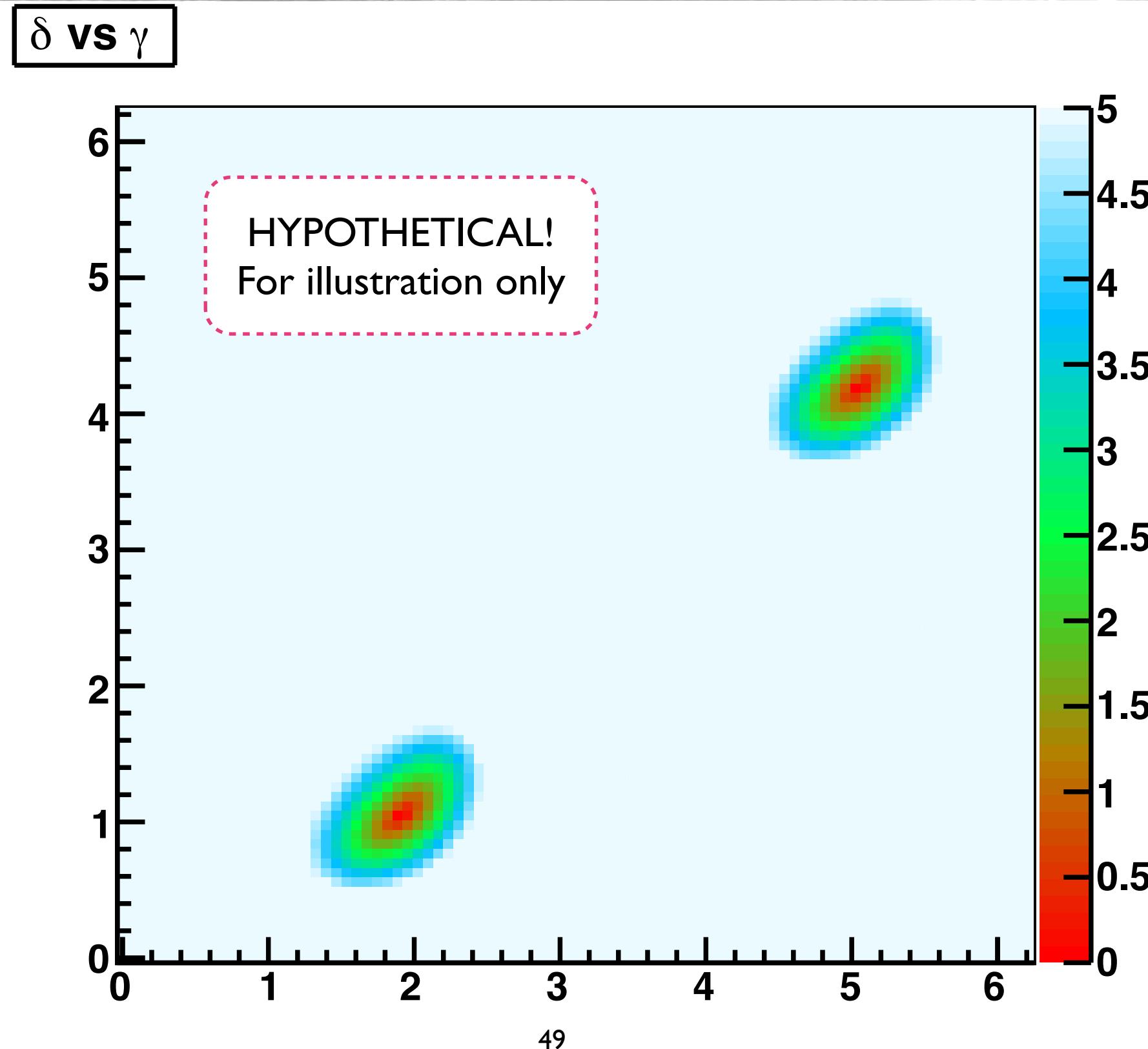
$$B^- \rightarrow D \textcolor{red}{K}^-$$

$$D \rightarrow \textcolor{red}{K}_S^0 \pi^+ \pi^-$$

- This method is particularly useful for combatting the trigonometric ambiguities present in the determination of  $\gamma$  from the ADS & CP methods



Using:  $R_{ADS(K)}$  and  $A_{ADS(K)}$  and  $R_{CP+}$  and  $A_{CP+}$  and the GGSZ modes



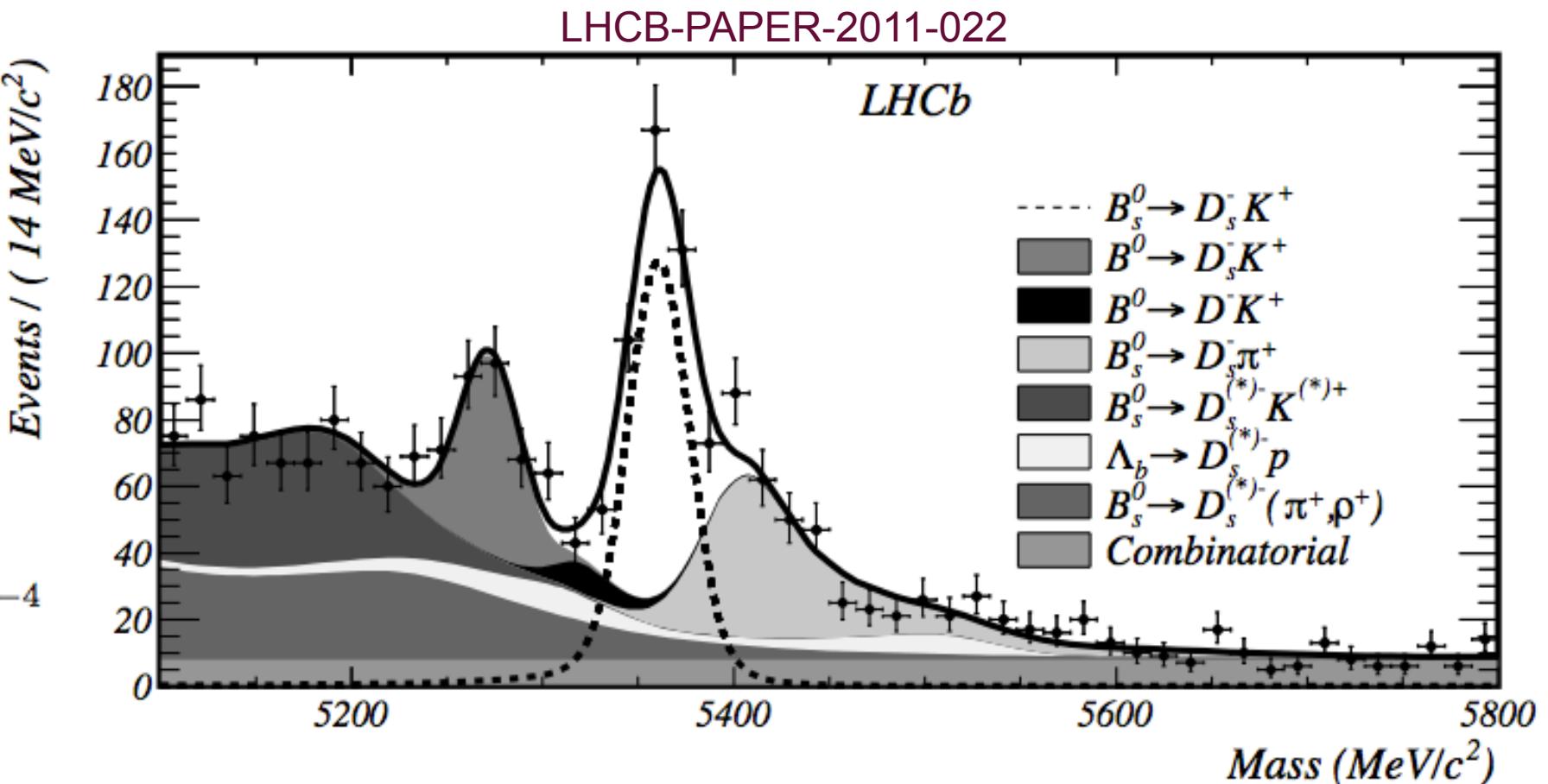
# And unique to LHCb: $\gamma$ from $B_s$ tree decays

Precise measurement of

$$B_s^0 \rightarrow D_s^- K^+$$

branching now made. Time-dependent measurement of  $\gamma$  on-going.

$$\mathcal{B}(B_s^0 \rightarrow D_s^- K^+) = (1.90 \pm 0.12 \pm 0.13)^{+0.12}_{-0.14} \times 10^{-4}$$



LHCb is on-track to make a combined measurement of  $\gamma$  using  $B^\pm, B^0, B_s$  tree decays, to an accuracy of 5~8° with the 2011+2012 dataset.

# Neutral meson formalism

The time evolution of a two-state mixing system is well known

$$i \frac{d}{dt} \begin{pmatrix} |B_q(t)\rangle \\ |\bar{B}_q(t)\rangle \end{pmatrix} = \left( \hat{M}^q - \frac{i}{2} \hat{\Gamma}^q \right) \begin{pmatrix} |B_q(t)\rangle \\ |\bar{B}_q(t)\rangle \end{pmatrix}$$

Trivial case. Applies to  $B^\pm$  decays

$$\begin{pmatrix} M_{11} & 0 \\ 0 & M_{22} \end{pmatrix} \quad \begin{pmatrix} \Gamma_{11} & 0 \\ 0 & \Gamma_{22} \end{pmatrix}$$

Mixing can occur with  $B^0$  and  $B_s$

$$\begin{pmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{pmatrix} \quad \begin{pmatrix} \Gamma_{11} & \Gamma_{12} \\ \Gamma_{21} & \Gamma_{22} \end{pmatrix}$$

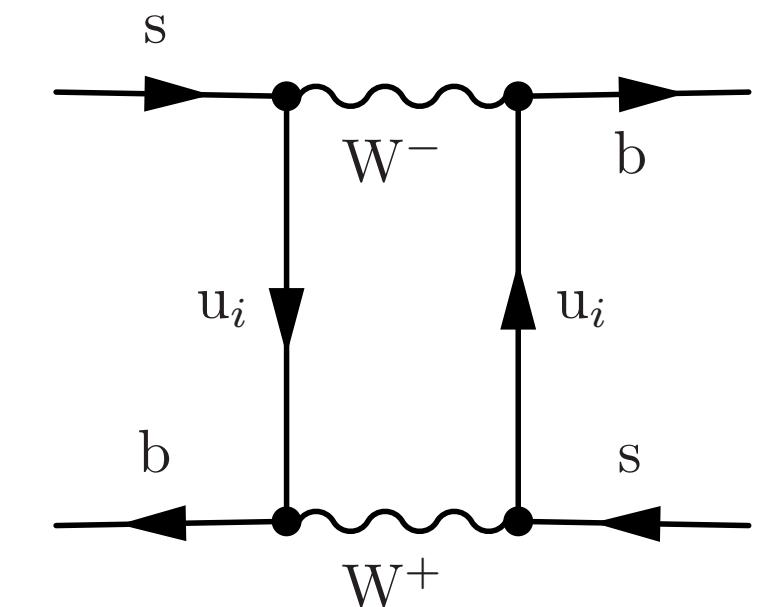
And CP violation in mixing occurs if

$$\phi_q = \arg(-M_{12}^q/\Gamma_{12}^q) \text{ is non-zero.}$$

Diagonalising the matrix obtains the two [observable] mass eigenstates.  
Referred to the Heavy and Light states.

$$\begin{aligned} B_{q,H} &:= p B_q + q \bar{B}_q \\ B_{q,L} &:= p B_q - q \bar{B}_q \end{aligned}$$

$B_s^0$



# Properties

If there is no  $CP$  violation,  $p=q=\sqrt{2}$ ,  
 **$B_H$  is pure  $CP+$**  and  **$B_L$  is pure  $CP-$**

$$B_{q,H} := p B_q + q \bar{B}_q \quad |p|^2 + |q|^2 = 1$$
$$B_{q,L} := p B_q - q \bar{B}_q$$

In addition to the  $CP$  violating phase, two other observables can be measured:

The mass difference

$$\Delta M_q := M_H^q - M_L^q = 2|M_{12}^q| \left( 1 - \frac{1}{8} \frac{|\Gamma_{12}^q|^2}{|M_{12}^q|^2} \sin^2 \phi_q + \dots \right)$$

$B^0$  :  $\Delta m_d = 0.507 \pm 0.004 \text{ ps}^{-1}$  ( SM:  $0.54 \pm 0.09 \text{ ps}^{-1}$  )

$B_s$  :  $\Delta m_s = 17.69 \pm 0.08 \text{ ps}^{-1}$  ( SM:  $17.3 \pm 2.6 \text{ ps}^{-1}$  )

The lifetime difference

$$\Delta \Gamma_q := \Gamma_L^q - \Gamma_H^q = 2|\Gamma_{12}^q| \cos \phi_q \left( 1 + \frac{1}{8} \frac{|\Gamma_{12}^q|^2}{|M_{12}^q|^2} \sin^2 \phi_q + \dots \right)$$

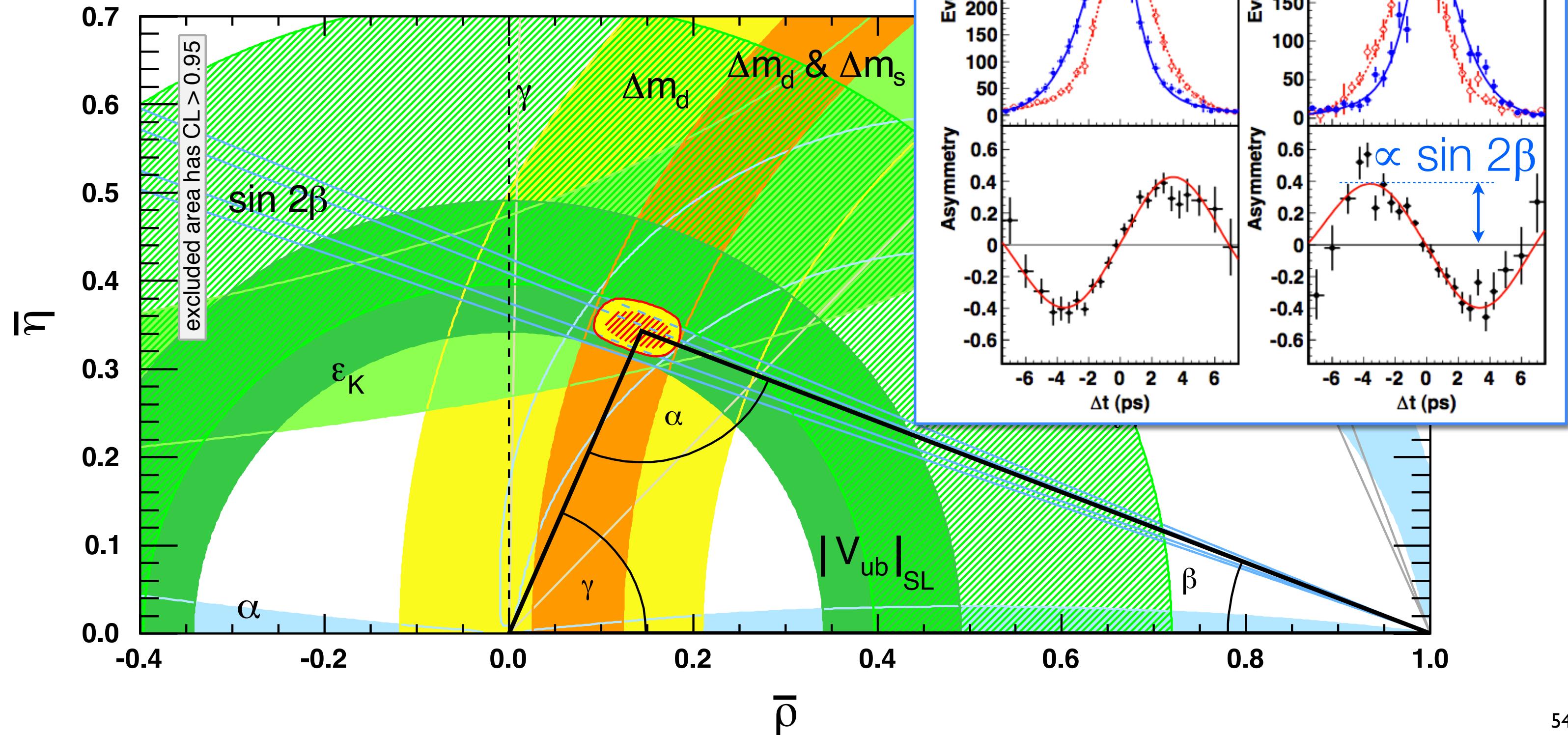
$B^0$  :  $\Delta \Gamma_d = \text{small}$  ( SM:  $\sim 0$  )

$B_s$  :  $\Delta \Gamma_s = \underline{0.100 \pm 0.013 \text{ ps}^{-1}}$  ( SM:  $0.087 \pm 0.021 \text{ ps}^{-1}$  )

Update in a moment

# Reminder of the $B^0$ system measurement

Latest sin  $2\beta$  measurement from Belle. arXiv:1201.4643v1



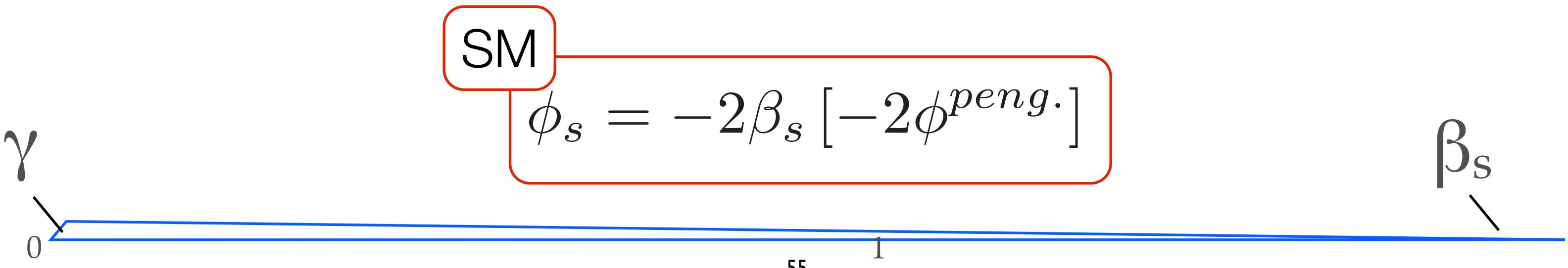
The CKM triangle relevant to the  $B_s$  system has a rather different shape

$$V_{CKM} = \begin{matrix} u \\ c \\ t \end{matrix} \begin{pmatrix} d & s & b \end{pmatrix}$$

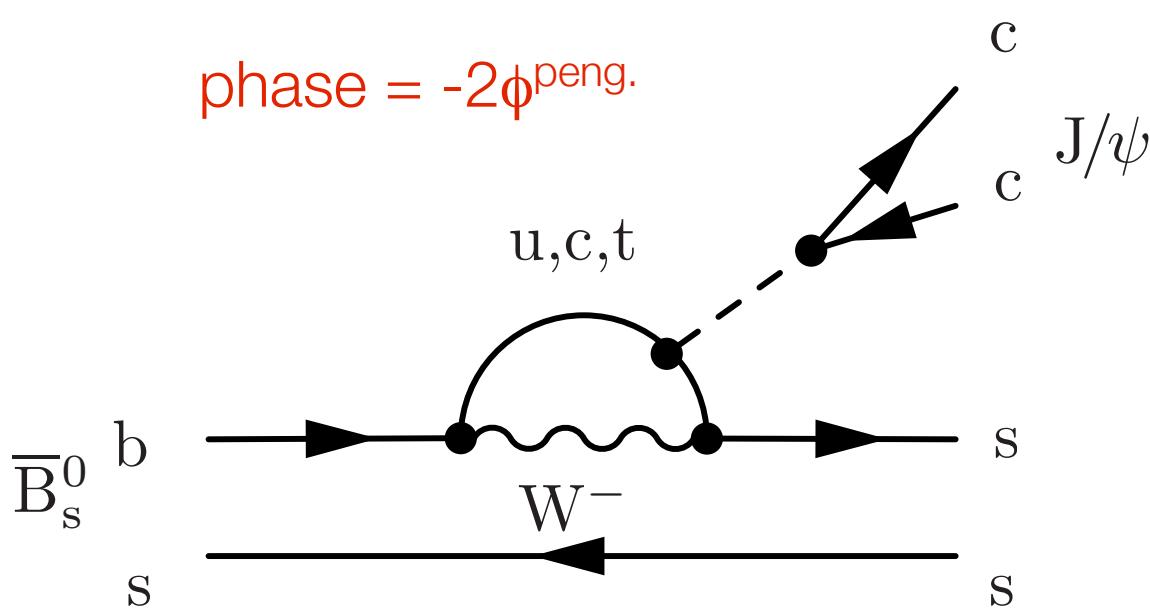
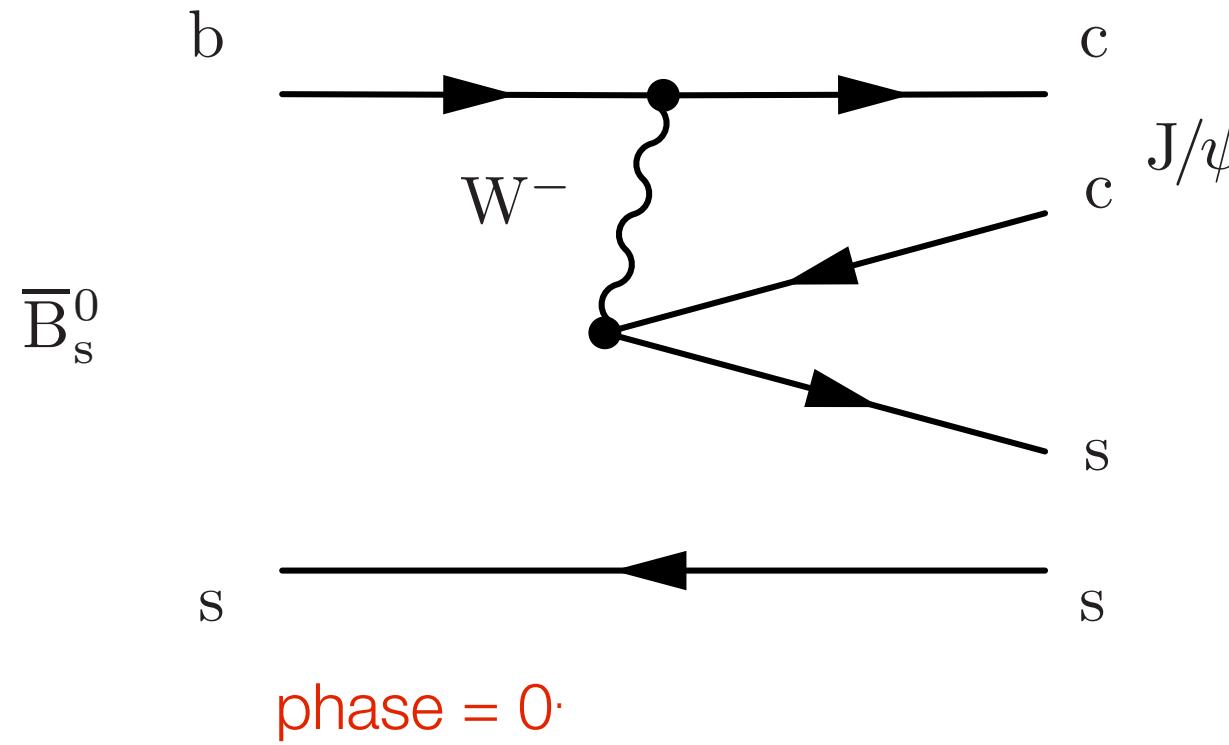
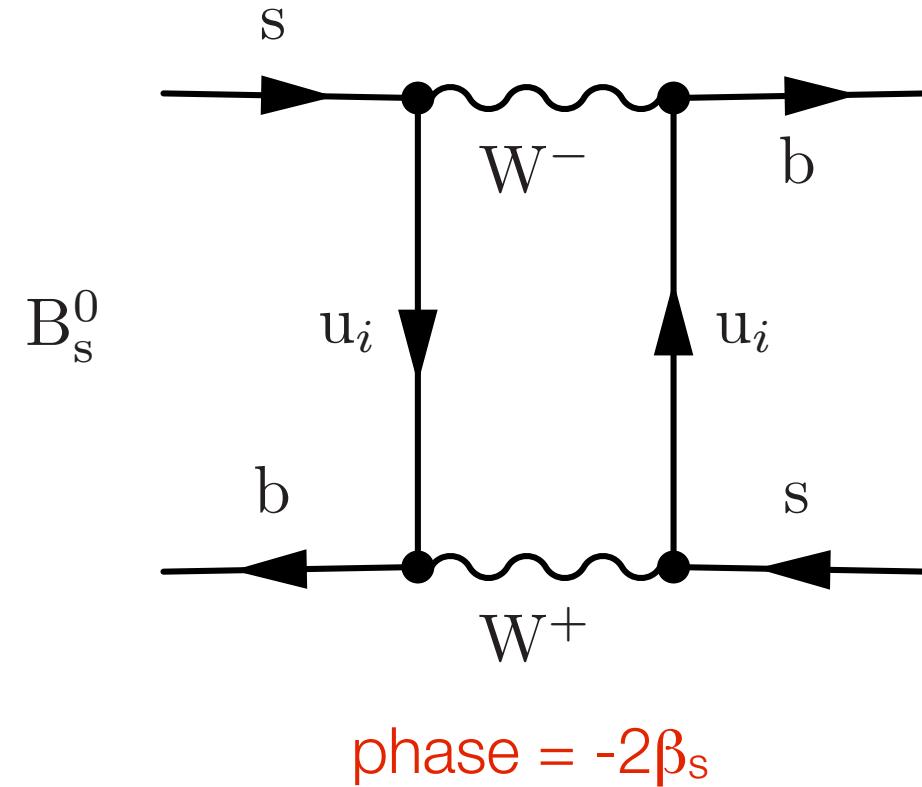
$$= \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 \\ -\lambda + \frac{1}{2}A^2\lambda^5(1 - 2(\rho + i\eta)) \\ A\lambda^3(1 - (1 - \frac{1}{2}\lambda^2)(\rho - i\eta)) \end{pmatrix} \begin{pmatrix} \lambda \\ 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}(1 + 4A^2)\lambda^4 \\ -A\lambda^2 + \frac{1}{2}A\lambda^4(1 - 2(\rho - i\eta)) \end{pmatrix} \begin{pmatrix} A\lambda^3(\rho - i\eta) \\ A\lambda^2 \\ 1 - \frac{1}{2}A^2\lambda^4 \end{pmatrix} + \mathcal{O}(\lambda^7)$$

Wolfenstein expansion in powers of the Cabibbo angle,  $\lambda$ , up to  $\lambda^6$

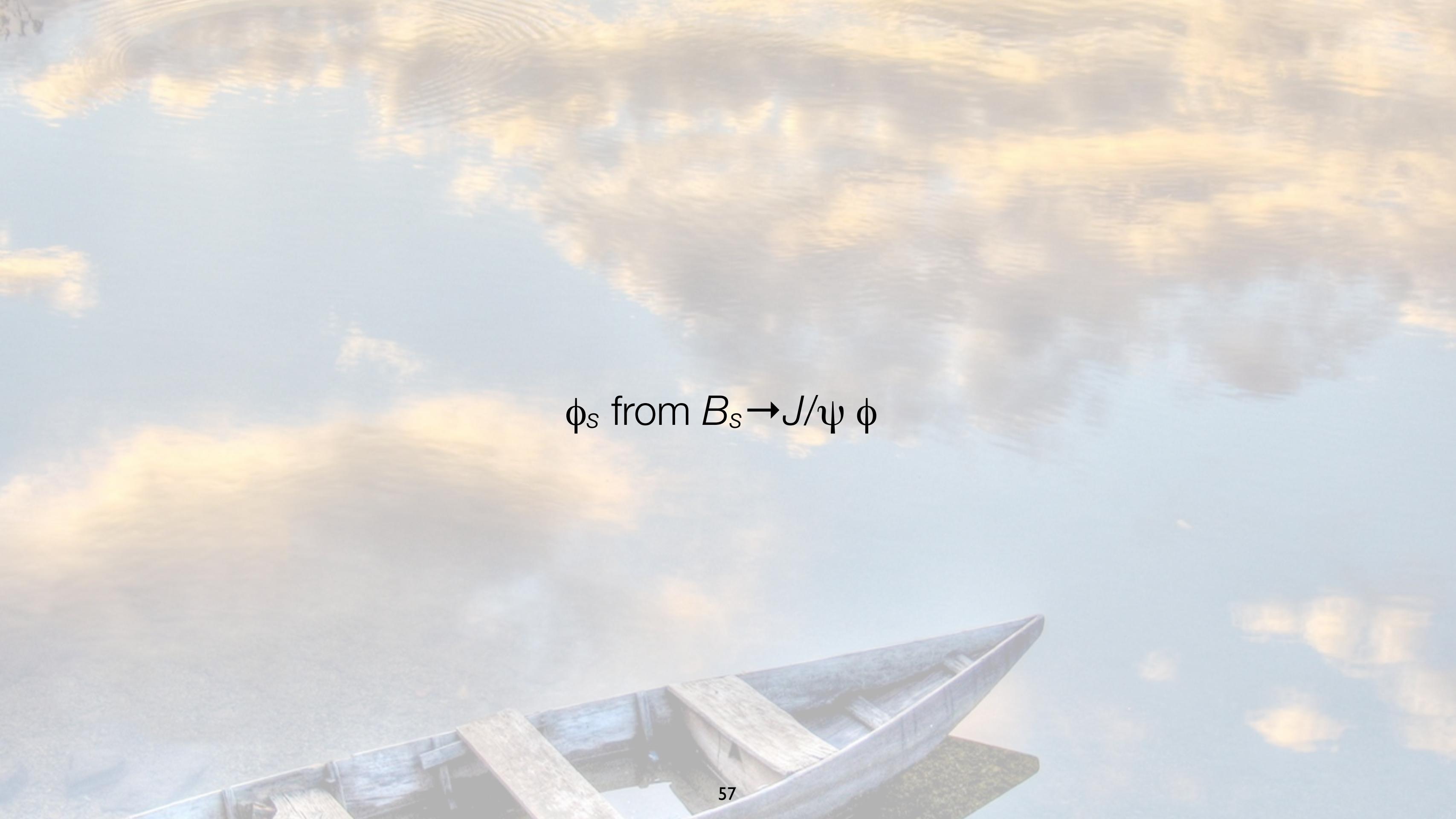
$$0 = 1 + \frac{V_{tb}^* V_{ts}}{V_{cb}^* V_{cs}} + \frac{V_{ub}^* V_{us}}{V_{cb}^* V_{cs}}$$



# Possible penguin pollution

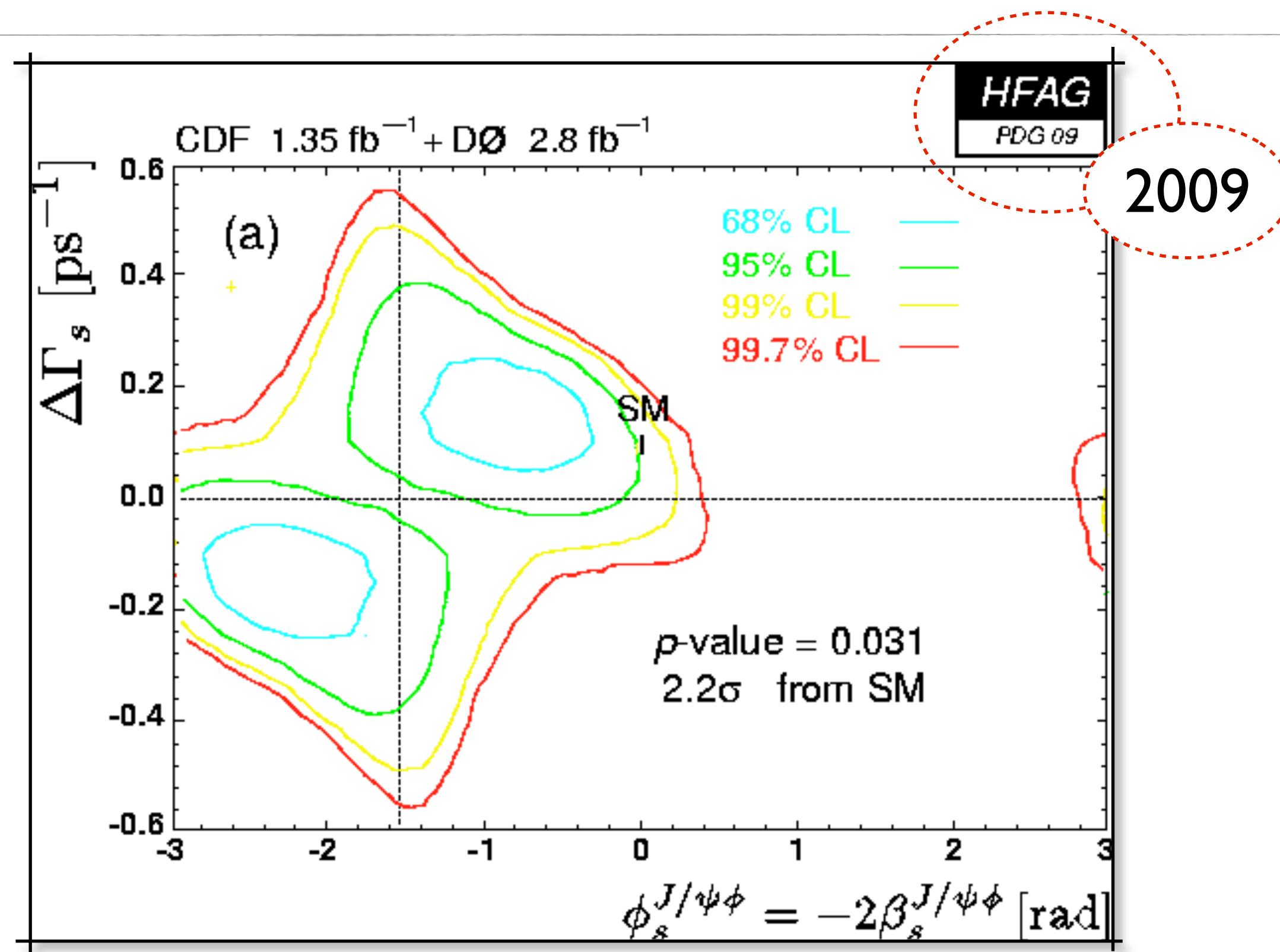


penguin phase and amplitude is unknown though expected small

A photograph of a small, traditional wooden boat with a pointed bow, resting on a body of water. The sky is filled with soft, orange and yellow clouds at sunset. The boat's hull is a light wood color, and it has a dark, possibly black, interior. The water is calm, reflecting the warm colors of the sky.

$\phi_s$  from  $B_s \rightarrow J/\psi \phi$

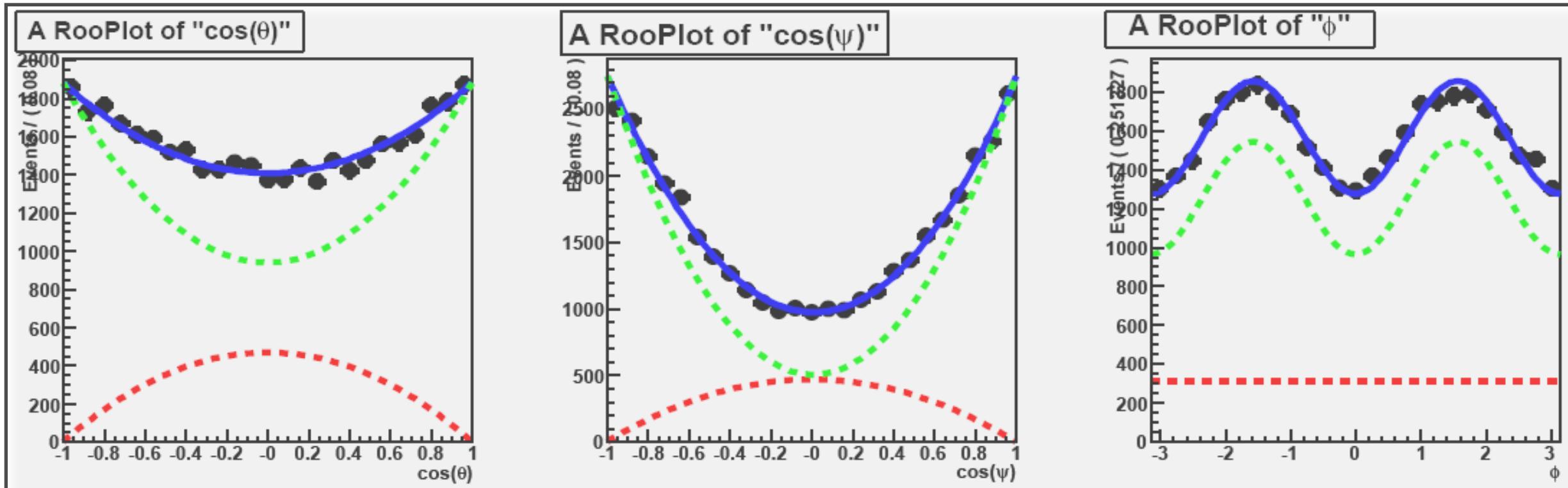
Three years ago...



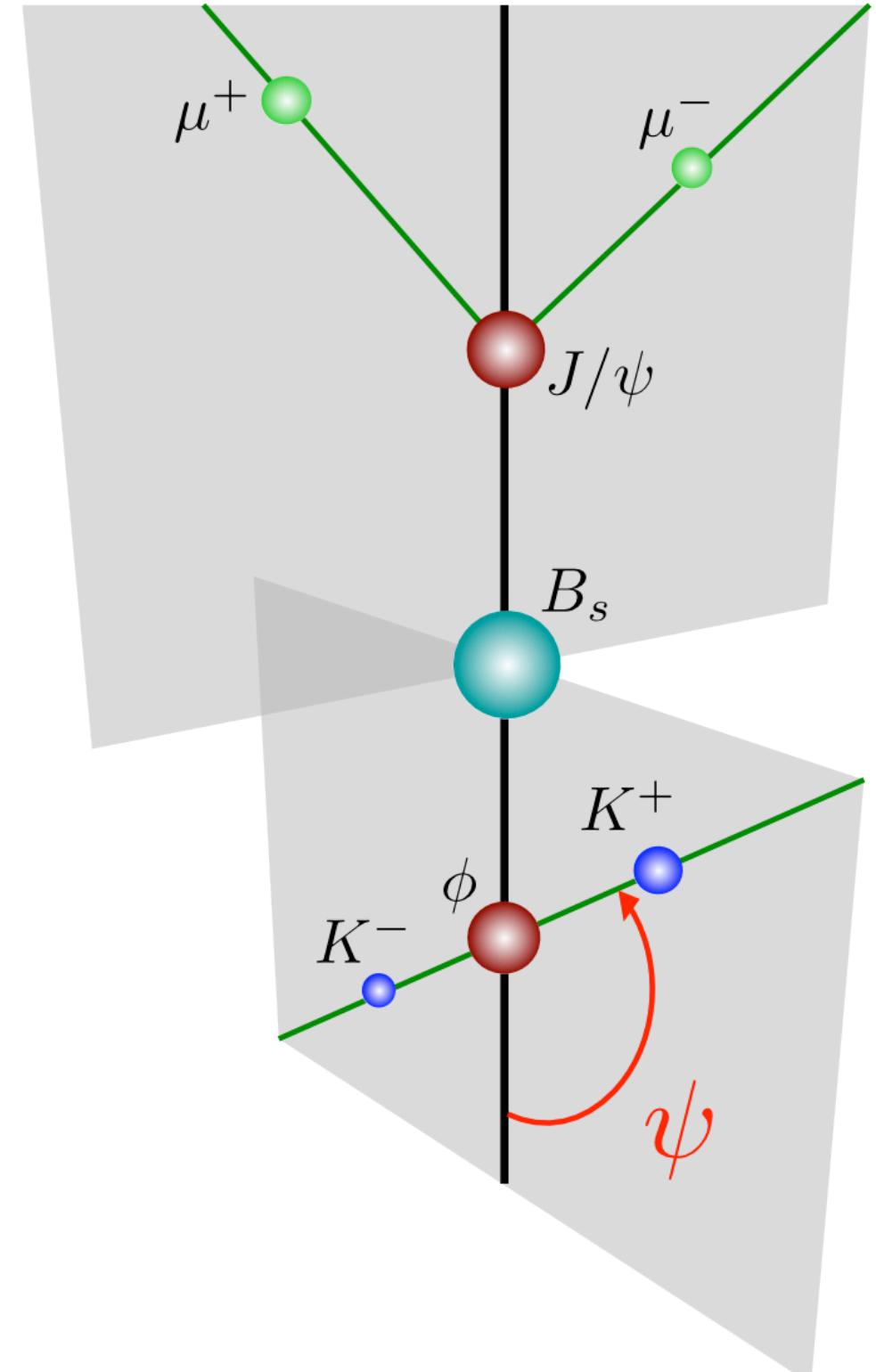
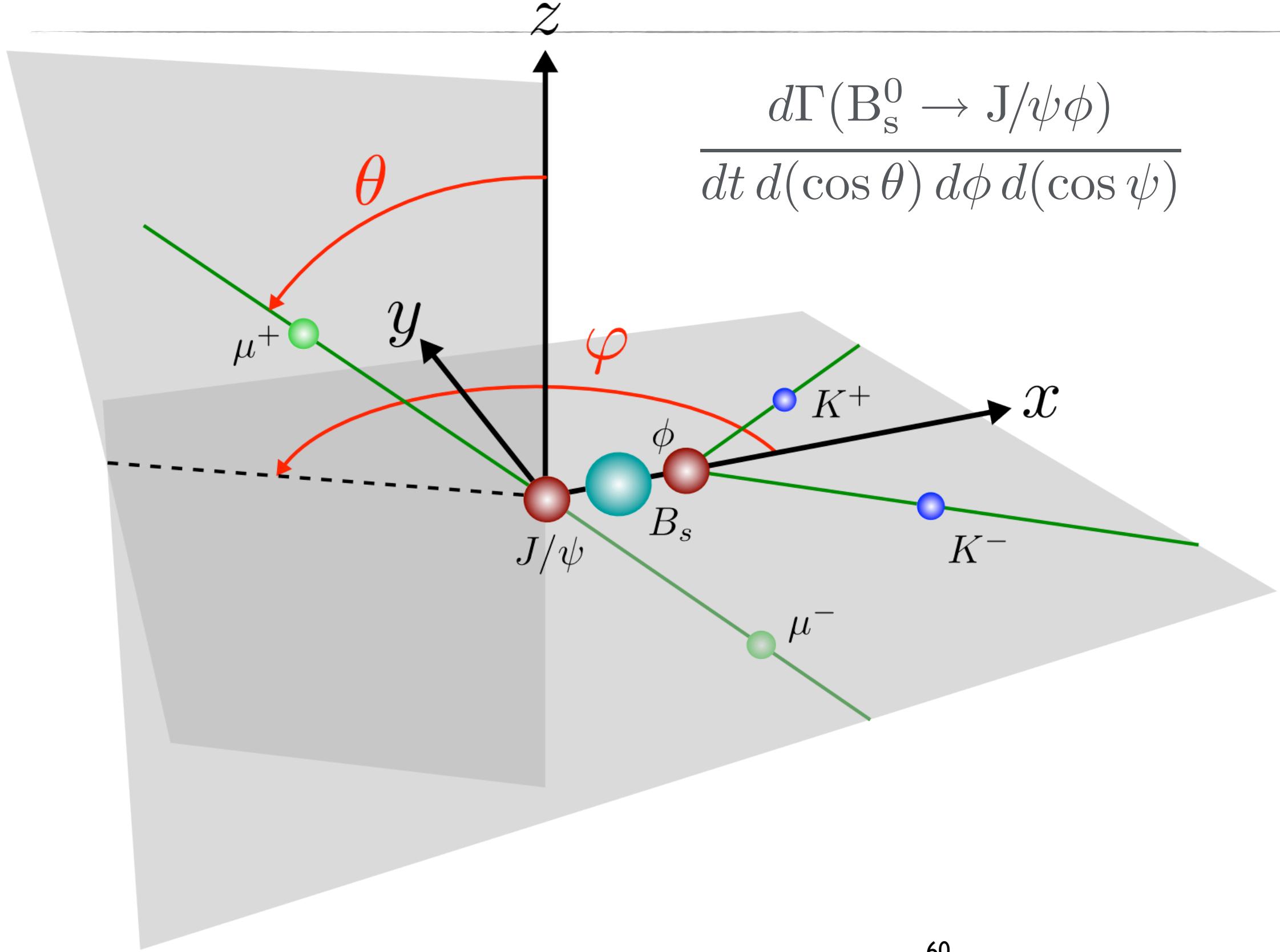
# Angular analysis is needed to separate the CP+ and CP- components

- In the  $B_s$  rest frame,  $\phi$  and  $J/\psi$  have relative orbital momentum  $\ell = 0, 1, 2$
- Since  $CP |f\rangle = (-1)^\ell |f\rangle$ , the final state is mixture of CP even ( $\ell = 0, 2$ ) and CP odd ( $\ell = 1$ )
- Three angles  $\theta, \varphi, \psi$  describe directions of final decay products  $J/\psi \rightarrow \mu\mu$  and  $\phi \rightarrow K^+K^-$  from which the CP+ and CP- components may be extracted

## SIMULATION



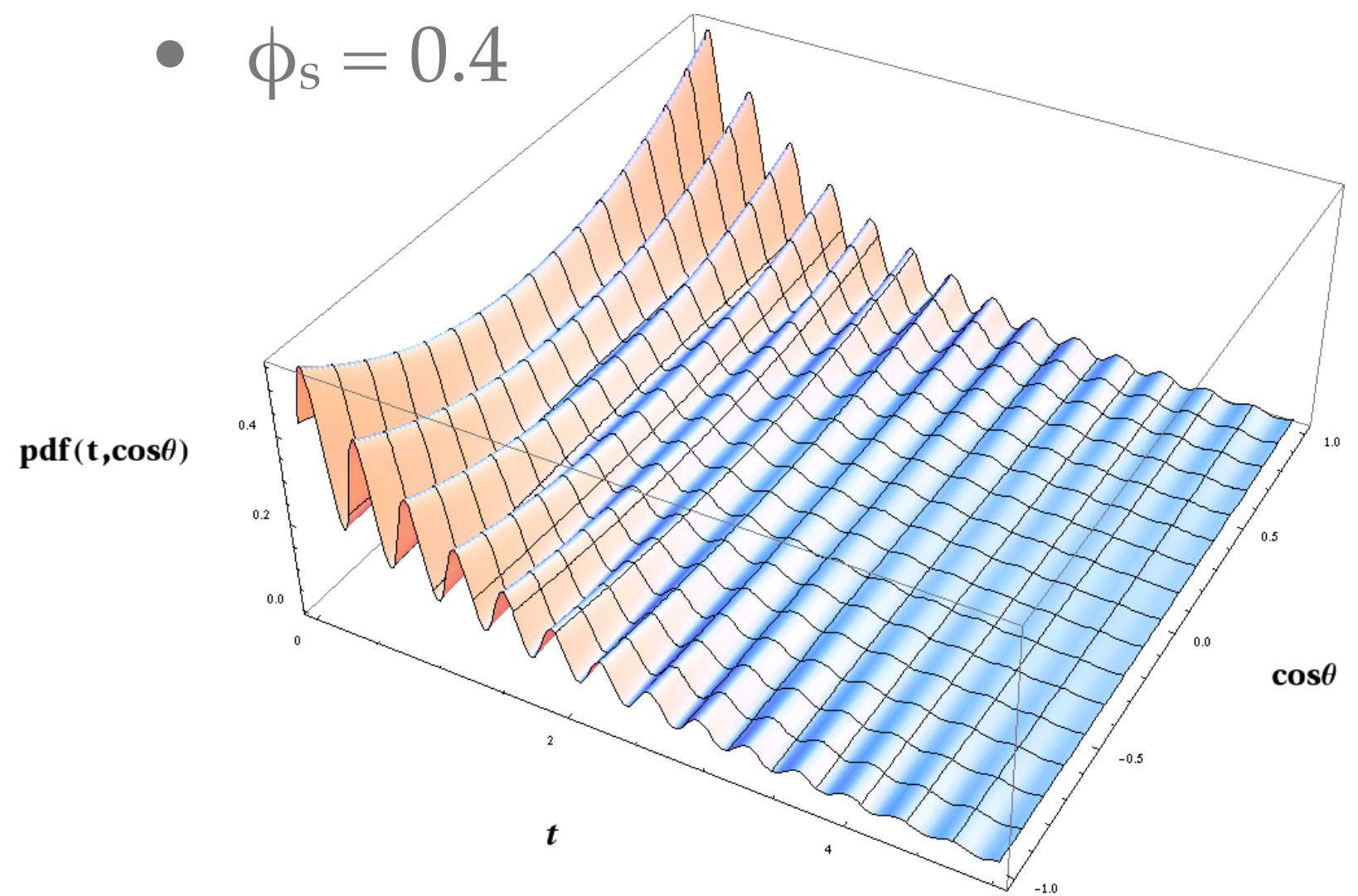
Angular analysis is needed to separate the CP+ and CP- components



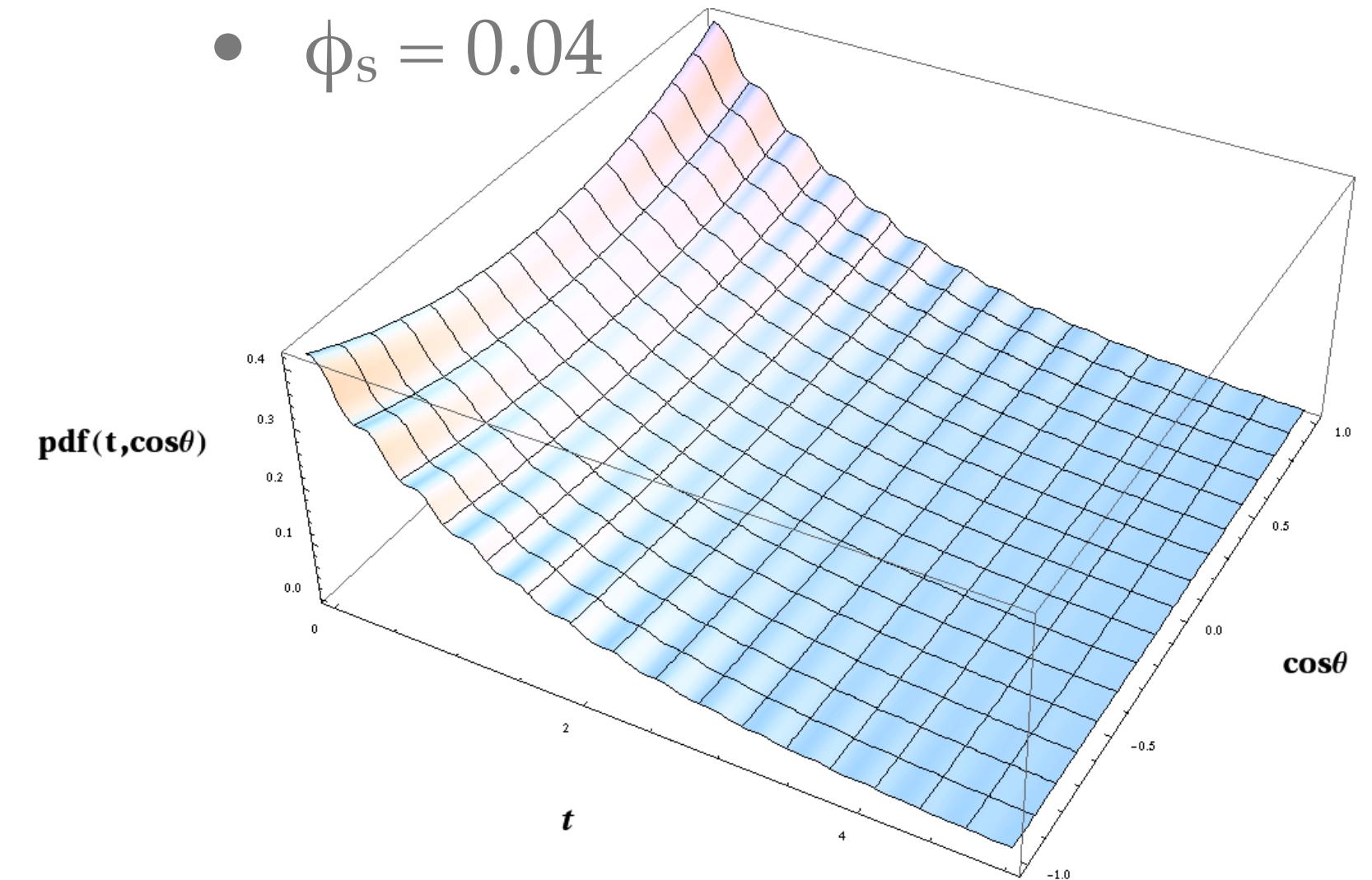
# Visualise the expected PDF after integrating over 2 of the 3 angles

- Amplitude of “wiggles”  $\propto \sin \phi_s$

- $\bullet \phi_s = 0.4$



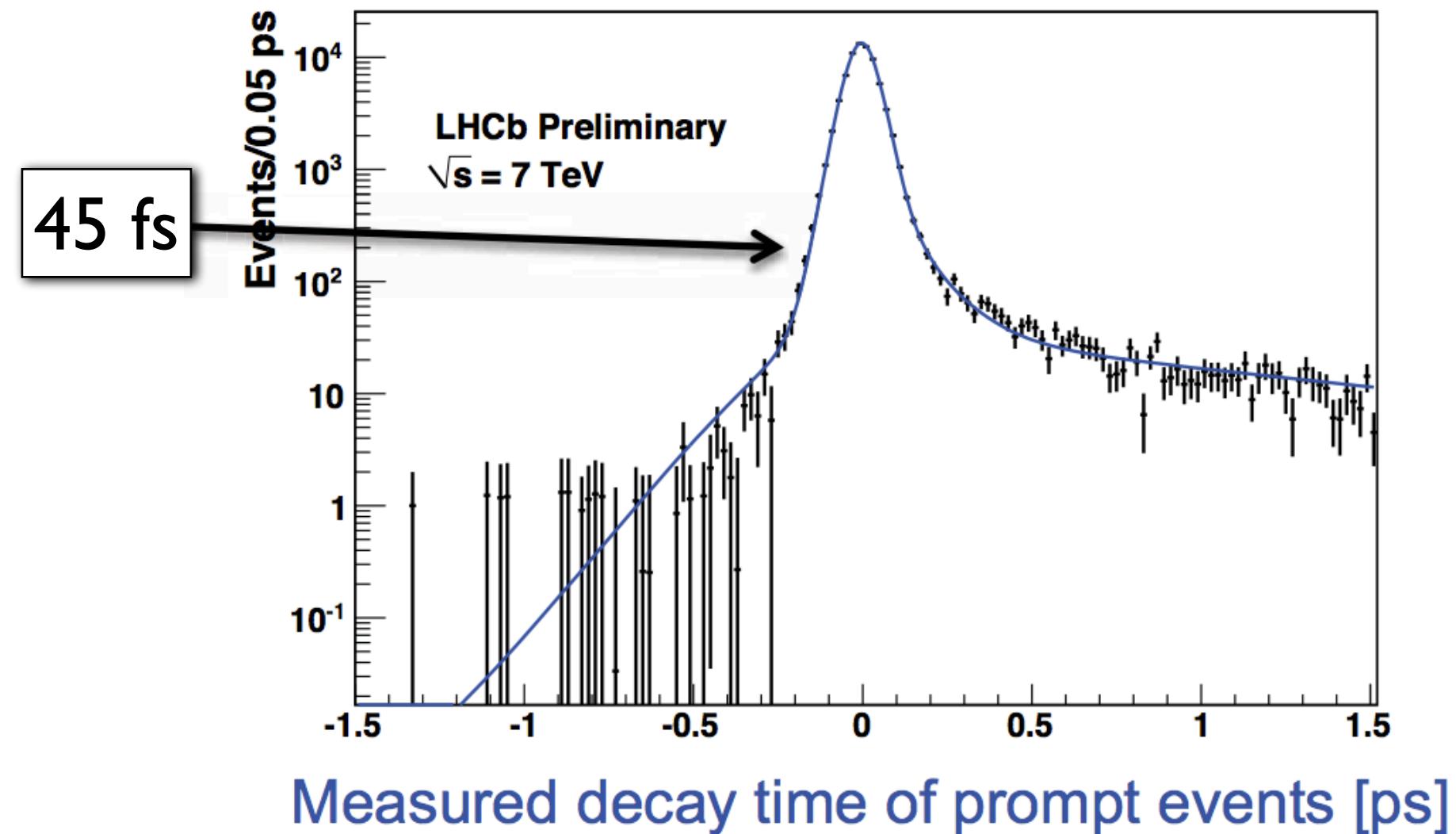
- $\bullet \phi_s = 0.04$



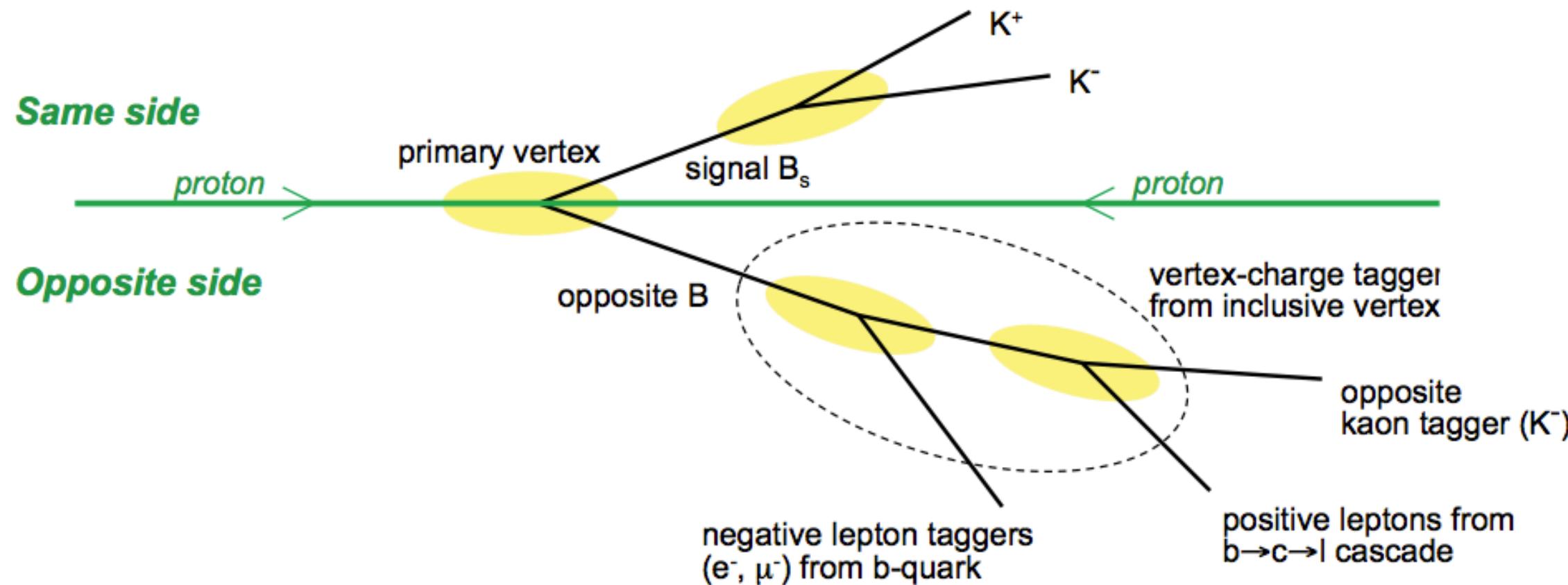
# Again, the vertex detector plays a vital role



- Need to have a good proper time resolution with respect to the meson oscillation period,  $\sim 350$  fs



And importantly, need to tag the flavour at production



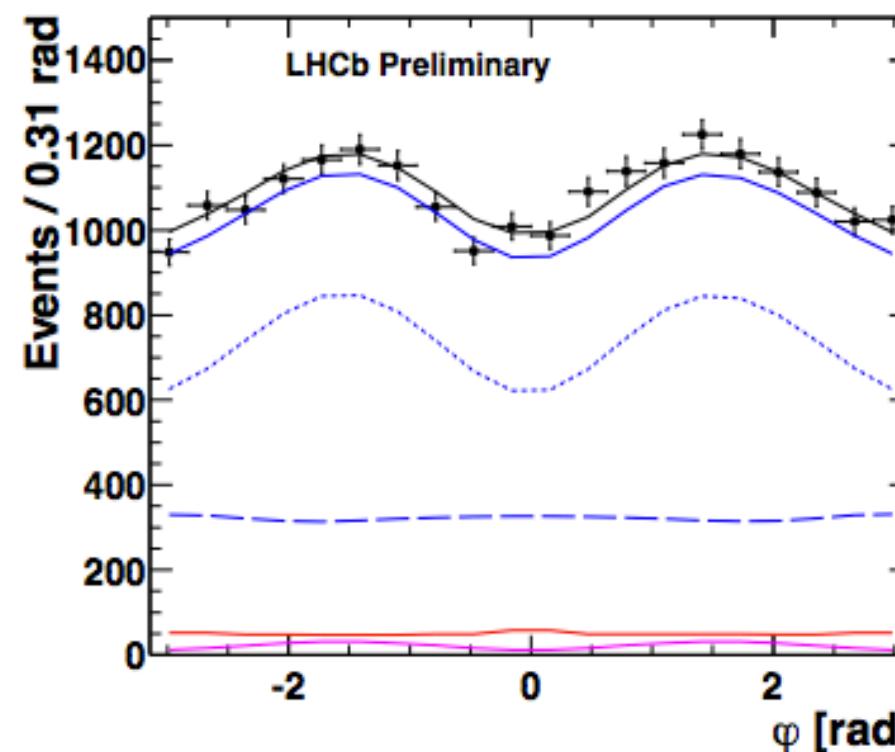
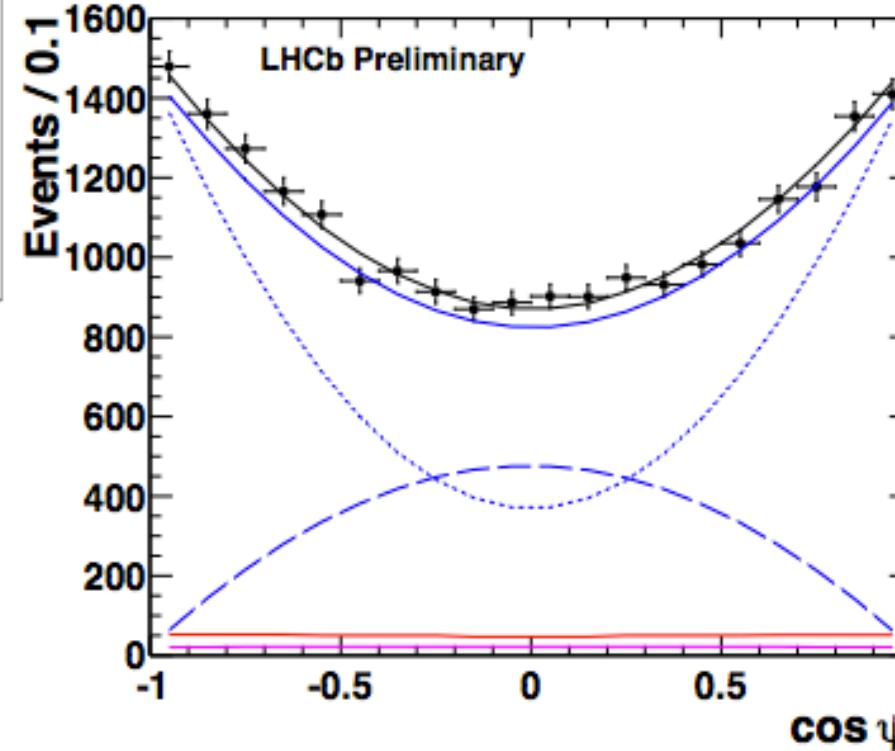
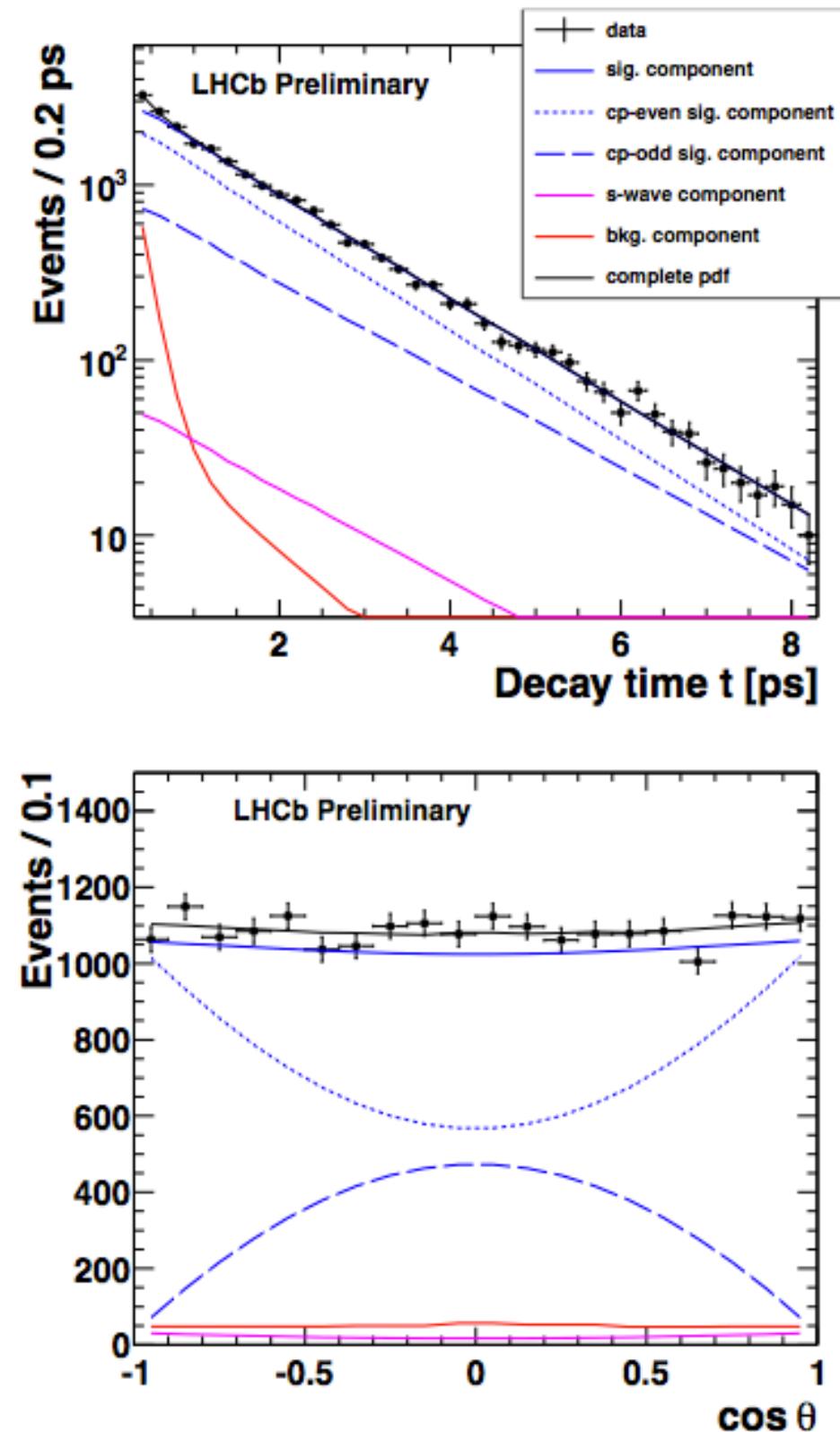
tagging efficiency  $\epsilon_{\text{tag}} \sim 33\%$

effective mistag  $\omega_{\text{tag}} \sim 36.8\%$

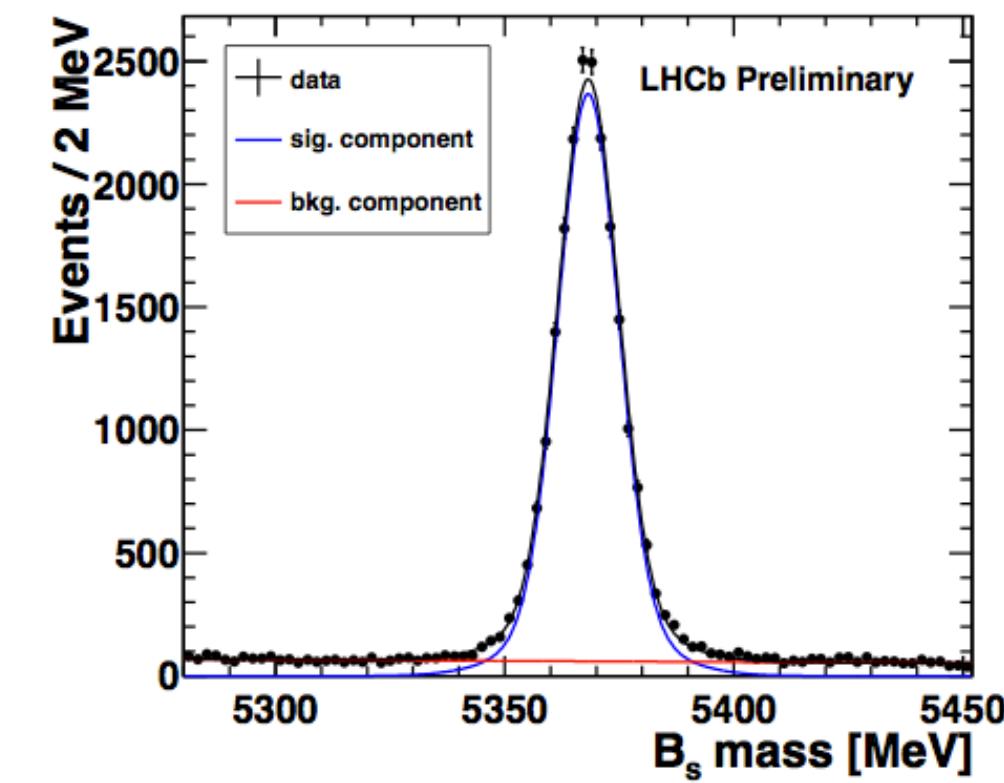
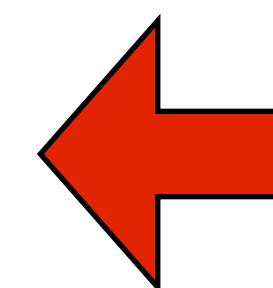
effective tagging power  $\epsilon_{\text{tag}}(1 - 2\omega_{\text{tag}})^2 \sim 2.3\%$

NB: tagging is much less precise, i.e. more diluted at LHCb than the B factories

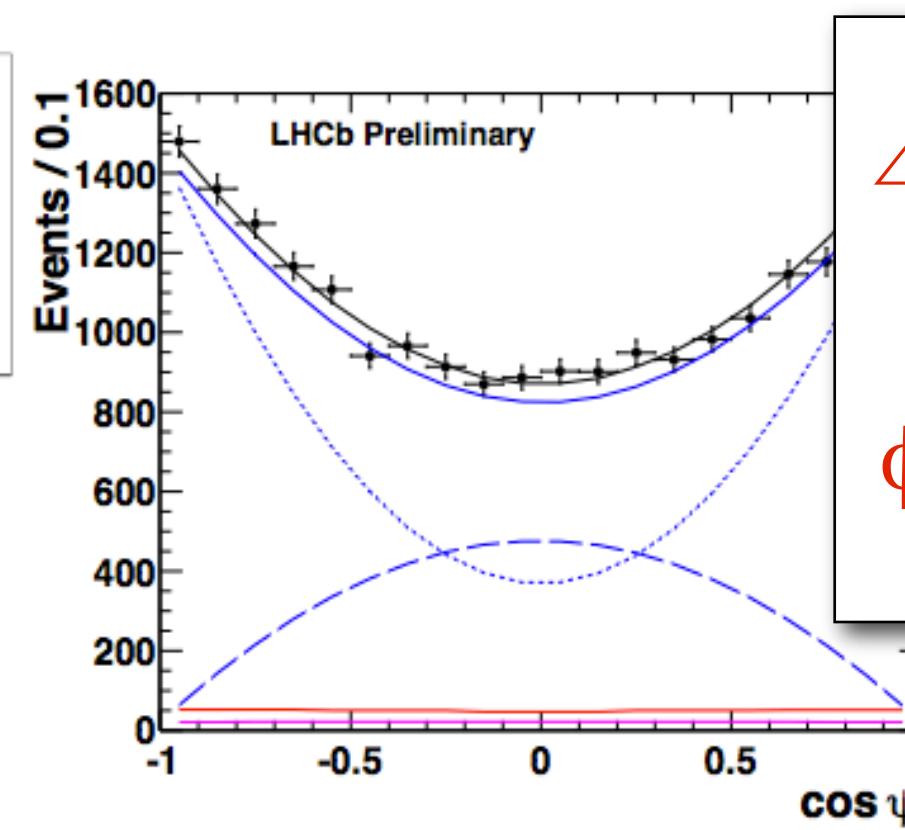
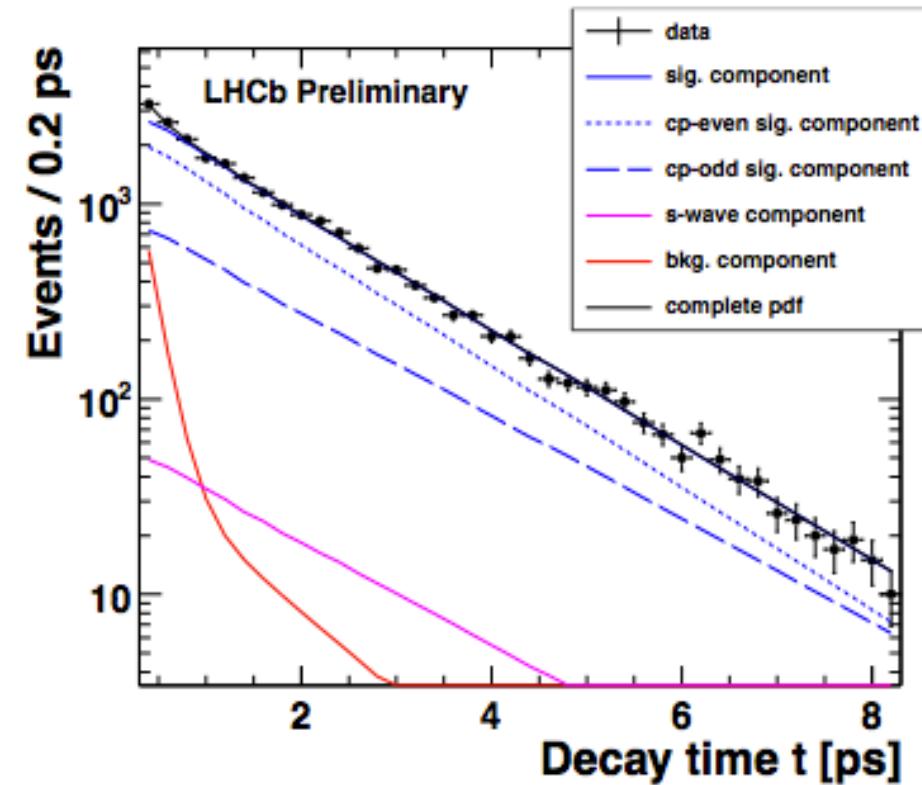
# Fit to data in four variables



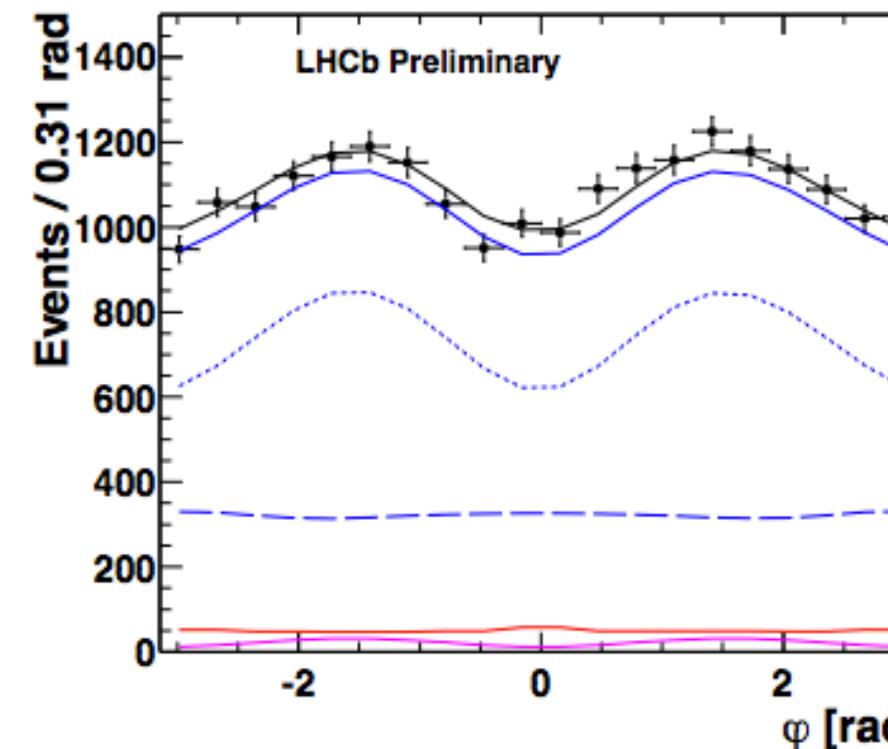
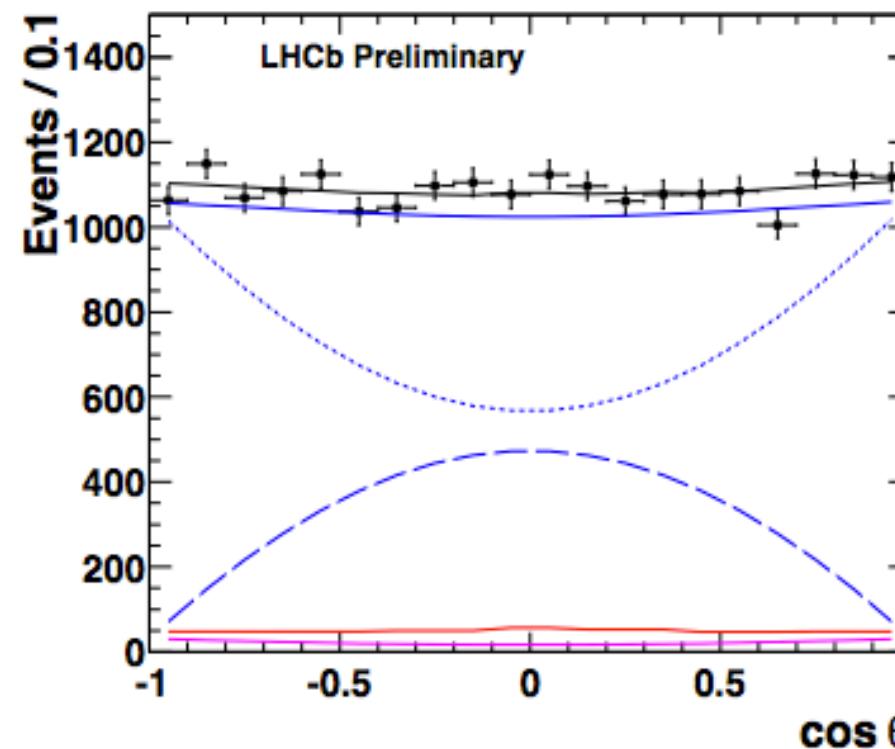
- As the full CP information is extracted, the lifetimes of the Heavy and Light mass eigenstates are fit for separately, i.e.  $\Delta\Gamma_s$



# Fit to data in four variables



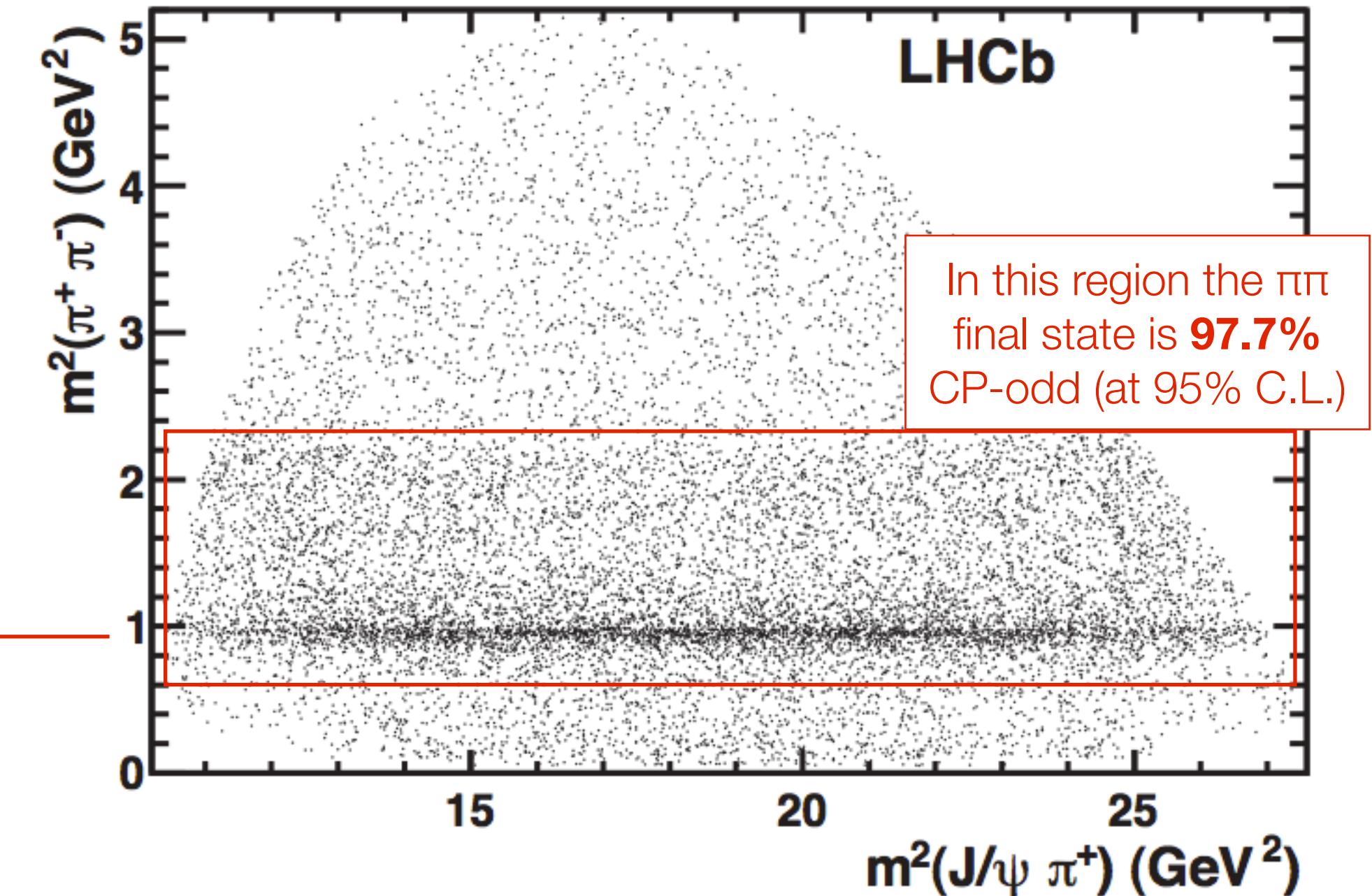
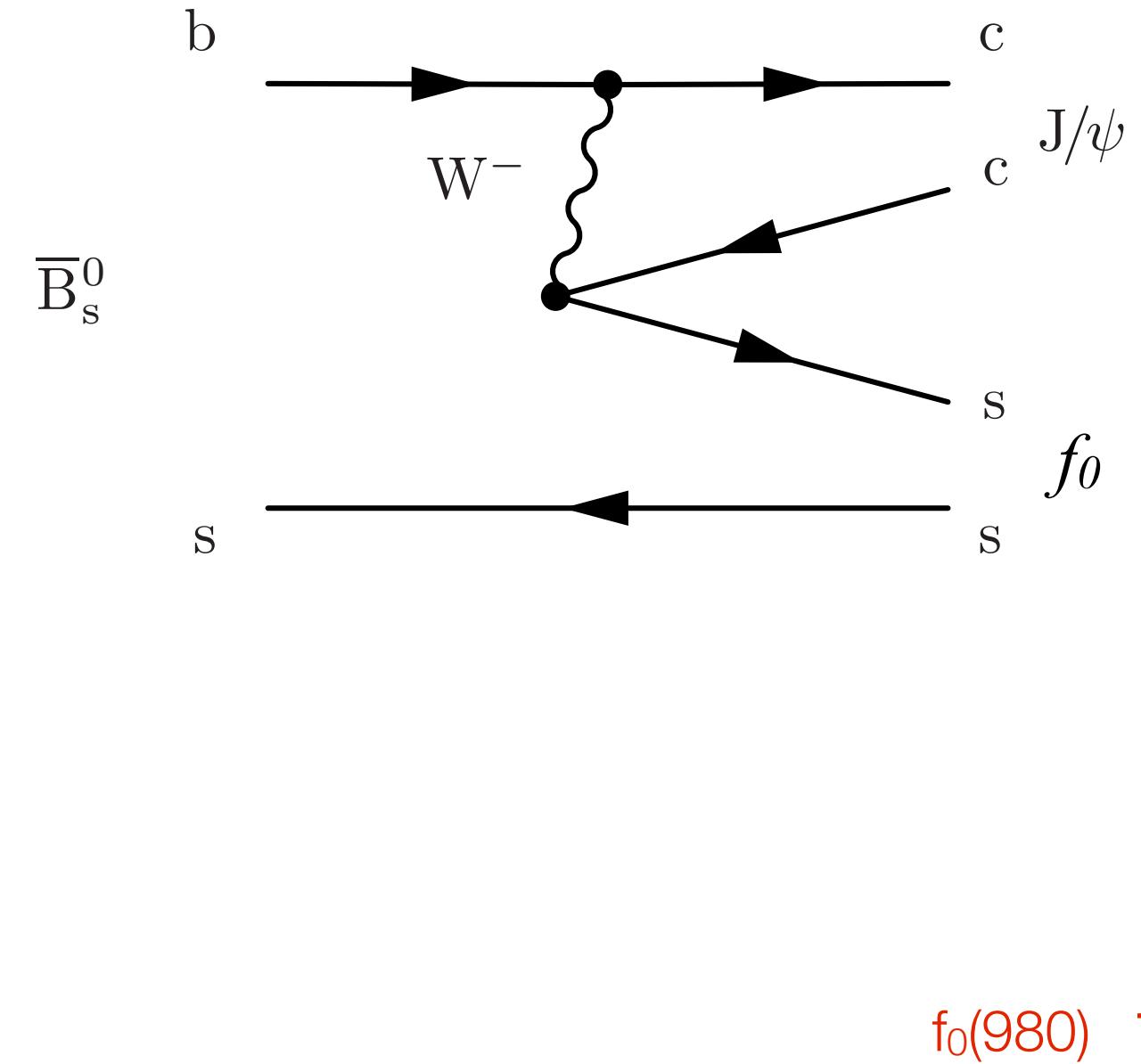
$$\Delta\Gamma_s = 0.116 \pm 0.018 \pm 0.006 \text{ ps}^{-1}$$

$$\phi_s = -0.001 \pm 0.101 \pm 0.027 \text{ rad.}$$


A photograph of a traditional wooden boat with a pointed bow, resting on a body of water. The sky is filled with warm, golden-yellow clouds at sunset. The boat's hull is a light wood color, and it has a dark, possibly black, interior visible through the open stern.

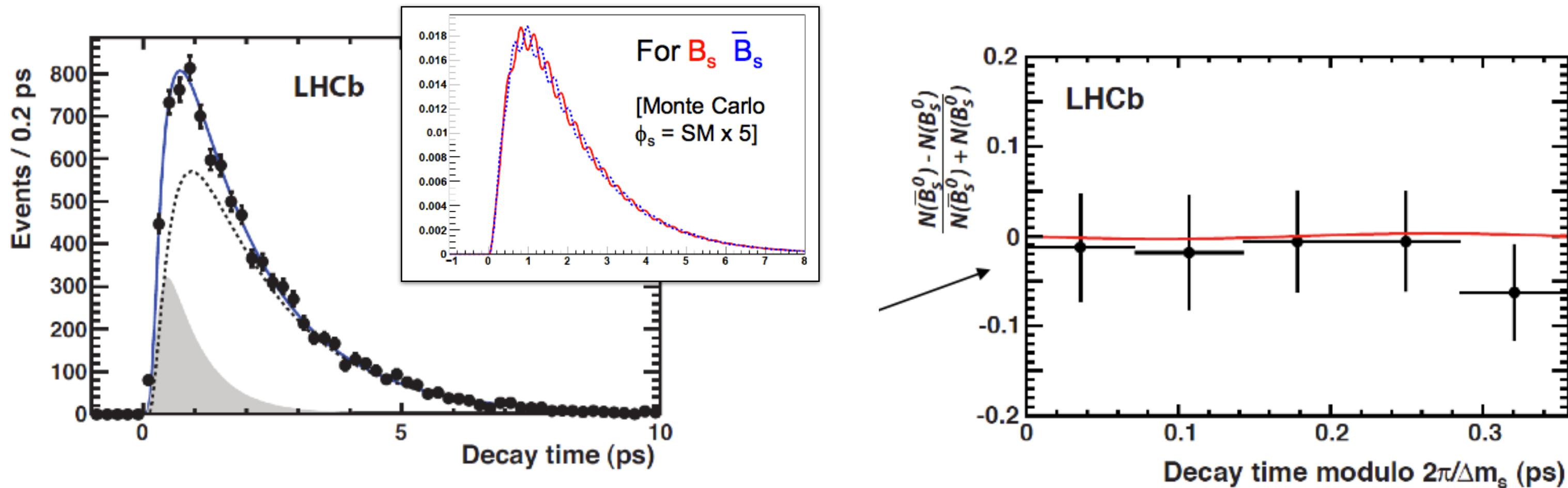
$\phi_s$  from  $B_s \rightarrow J/\psi \pi^+ \pi^-$

If just one CP eigenstate is present, the analysis is simpler



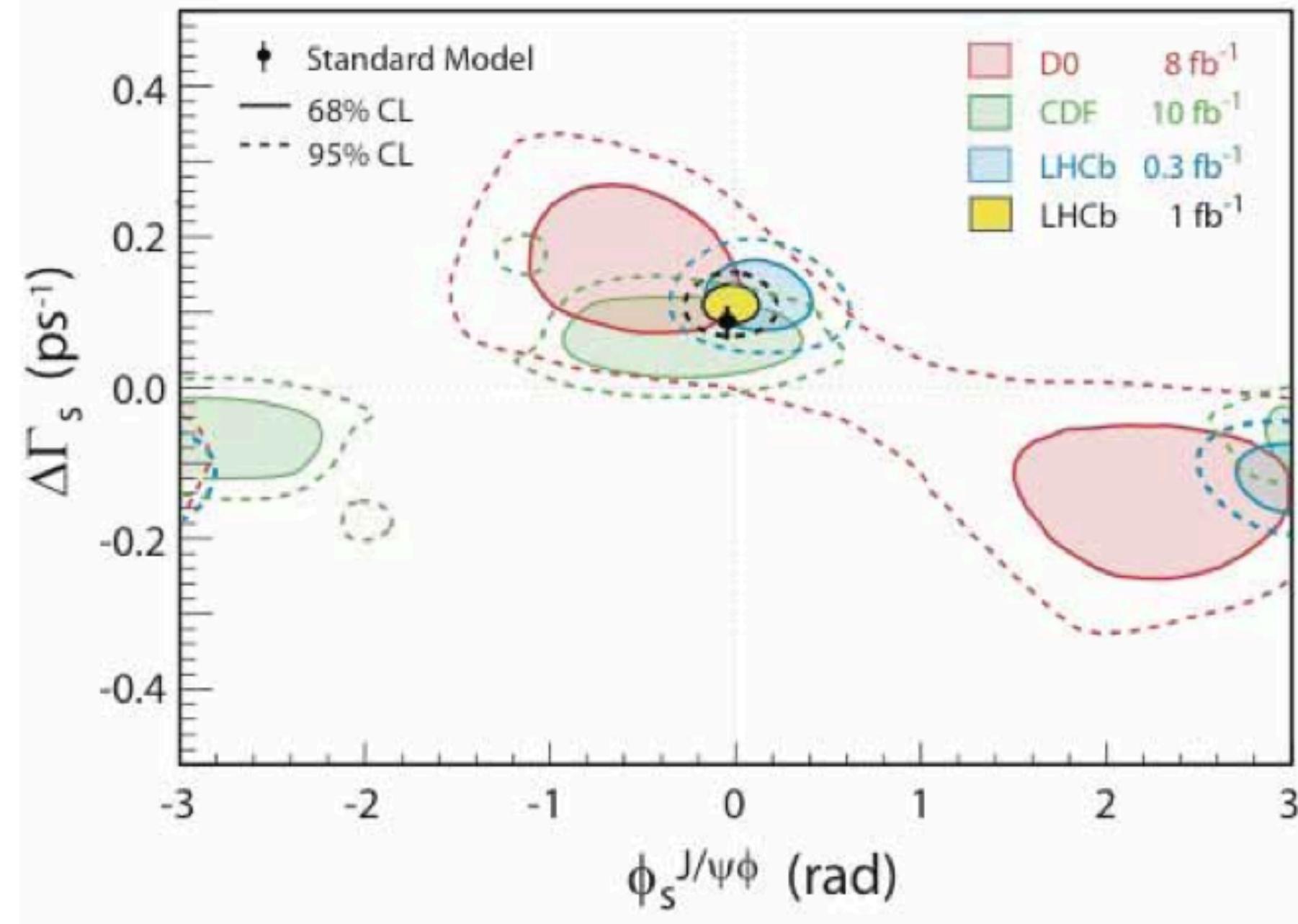
If just one CP eigenstate is present, the analysis is simpler

$$\Gamma \left( \bar{B}_s^0 \rightarrow f_- \right) = \frac{\mathcal{N}}{2} e^{-\Gamma_s t} \left\{ e^{\Delta \Gamma_s t / 2} (1 + \cos \phi_s) + e^{-\Delta \Gamma_s t / 2} (1 - \cos \phi_s) \pm \sin \phi_s \sin (\Delta m_s t) \right\}$$



$B_s \rightarrow J/\psi \pi^+ \pi^-$  result:  $\phi_s = -0.02 \pm 0.17 \pm 0.02$  rad

# Pictorial world summary and final LHCb result



$$\Delta\Gamma_s = 0.116 \pm 0.018 \pm 0.006 \text{ ps}^{-1}$$

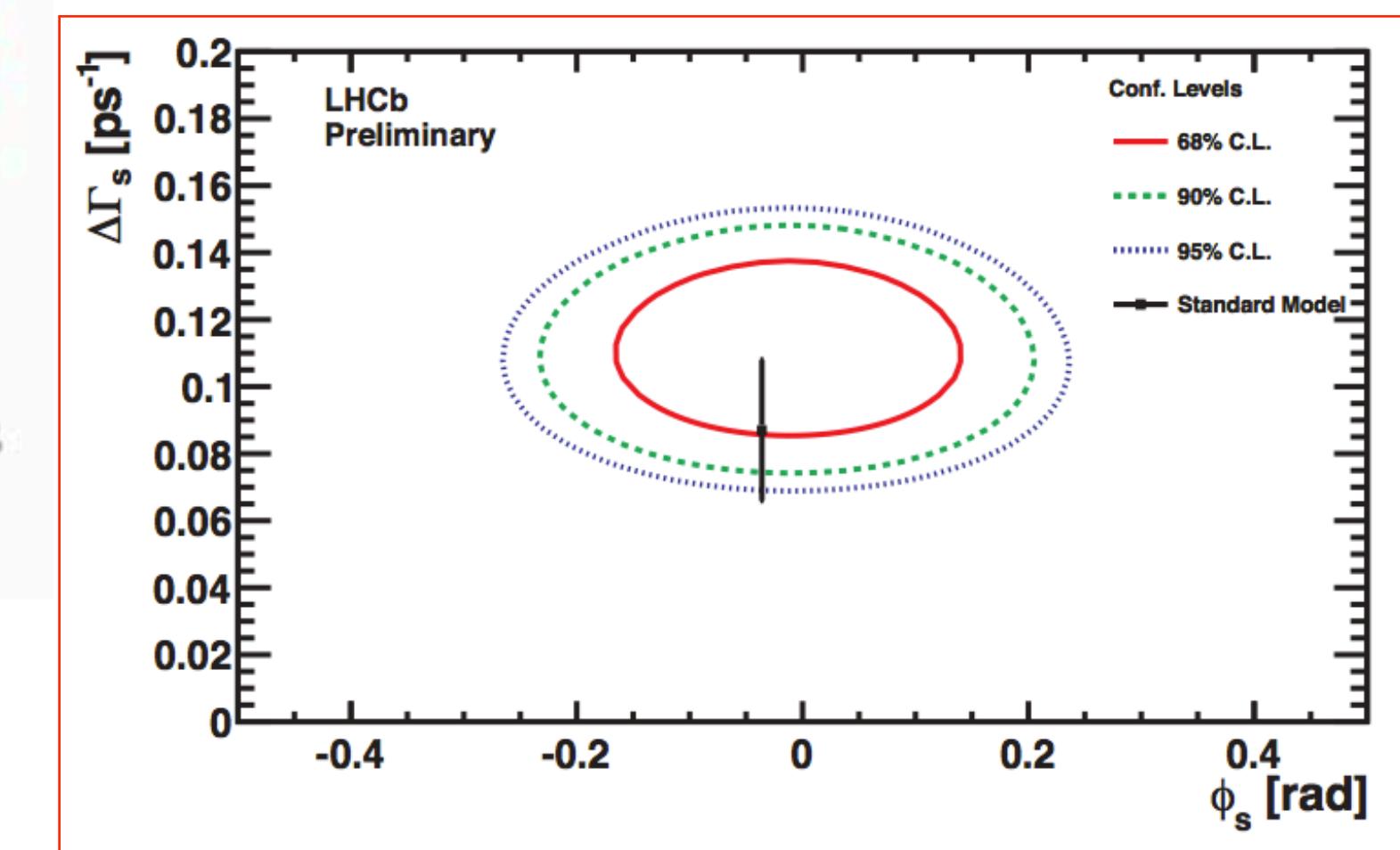
$J/\psi\phi$  only

$$(\text{SM: } 0.087 \pm 0.021 \text{ ps}^{-1})$$

$$\phi_s = -0.002 \pm 0.083 \pm 0.027 \text{ rad.}$$

$J/\psi\pi^+\pi^-$  and  $J/\psi\phi$

$$(\text{SM: } -0.036 \pm 0.002 \text{ rad.})$$





$\Delta A_{CP}$

# $CP$ violation in charm is suppressed in the SM

$$V_{CKM} = \begin{pmatrix} u & d & s & b \\ c & \left( \begin{array}{ccc} 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda + \frac{1}{2}A^2\lambda^5(1 - 2(\rho + i\eta)) & 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}(1 + 4A^2)\lambda^4 & A\lambda^2 \\ A\lambda^3(1 - (1 - \frac{1}{2}\lambda^2)(\rho - i\eta)) & -A\lambda^2 + \frac{1}{2}A\lambda^4(1 - 2(\rho - i\eta)) & 1 - \frac{1}{2}A^2\lambda^4 \end{array} \right) \\ t & \end{pmatrix} + \mathcal{O}(\lambda^7)$$

Wolfenstein expansion in powers of the Cabibbo angle,  $\lambda$ , up to  $\lambda^6$

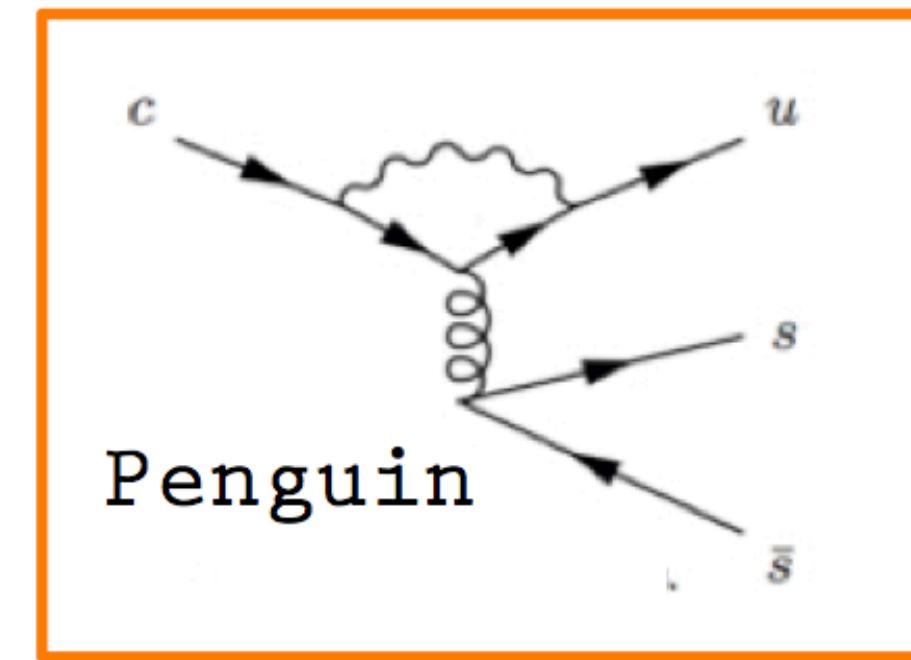
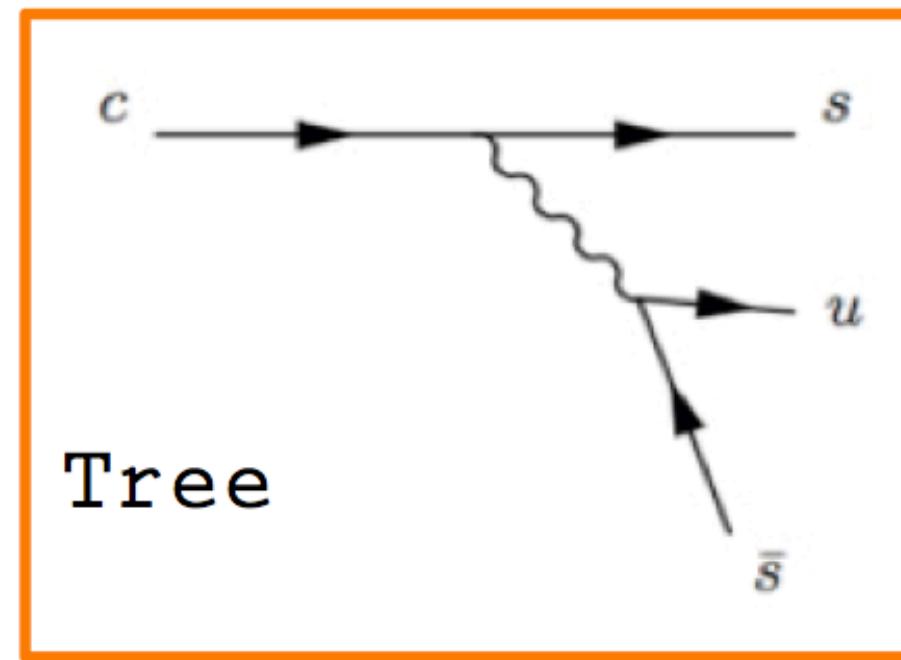
$$0 = V_{us}^* V_{cs} + V_{ub}^* V_{cb} + V_{ud}^* V_{cd}$$

$\searrow \propto \lambda$        $\searrow \propto \lambda^5$        $\searrow \propto \lambda$

*if the  $b$  contribution can be neglected then only two generations contribute, i.e. approximates to a real Cabibbo matrix, and no  $CP$  violating phases*

# Where to look for CP violation in charm

- A good bet is singly Cabibbo suppressed decays
- Interference between tree and penguin may generate *CP* asymmetries



- And look for it at LHCb where huge D-meson samples are appearing

$$\sigma_{b\bar{b}}(pp \rightarrow b\bar{b}X) = (284 \pm 20 \pm 49)\mu b$$

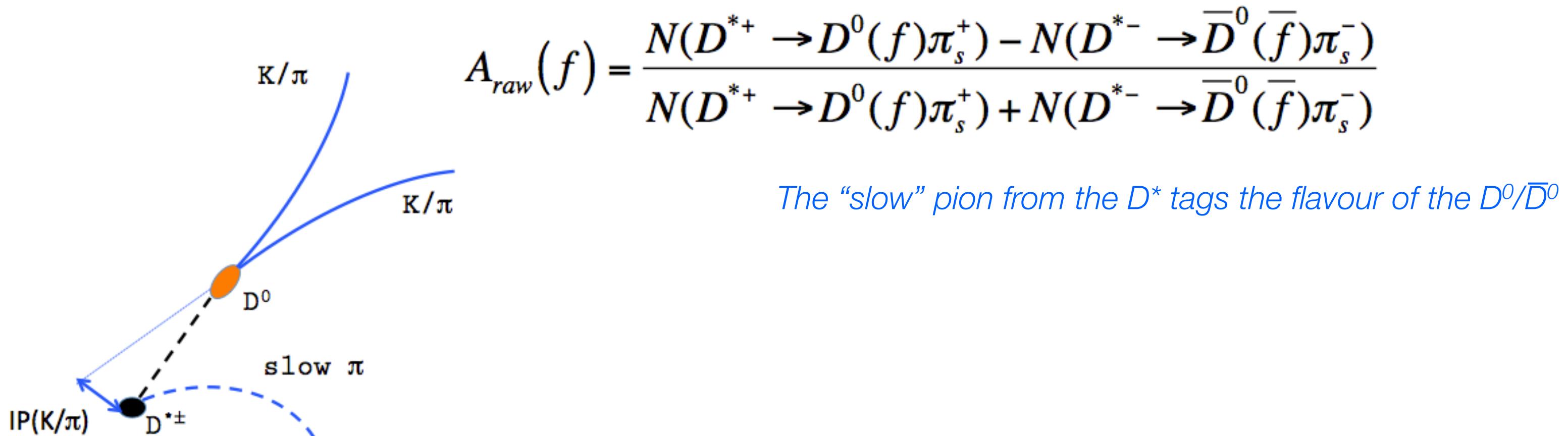
$$\sigma_{c\bar{c}}(pp \rightarrow c\bar{c}X) = (6.10 \pm 0.93)\text{mb}$$

# Time-integrated CP asymmetry

- We would like to measure (for  $f=CP$  eigenstate,  $KK$  or  $\pi\pi$ ):

$$A_{CP}(f) = \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow f)}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow f)}$$

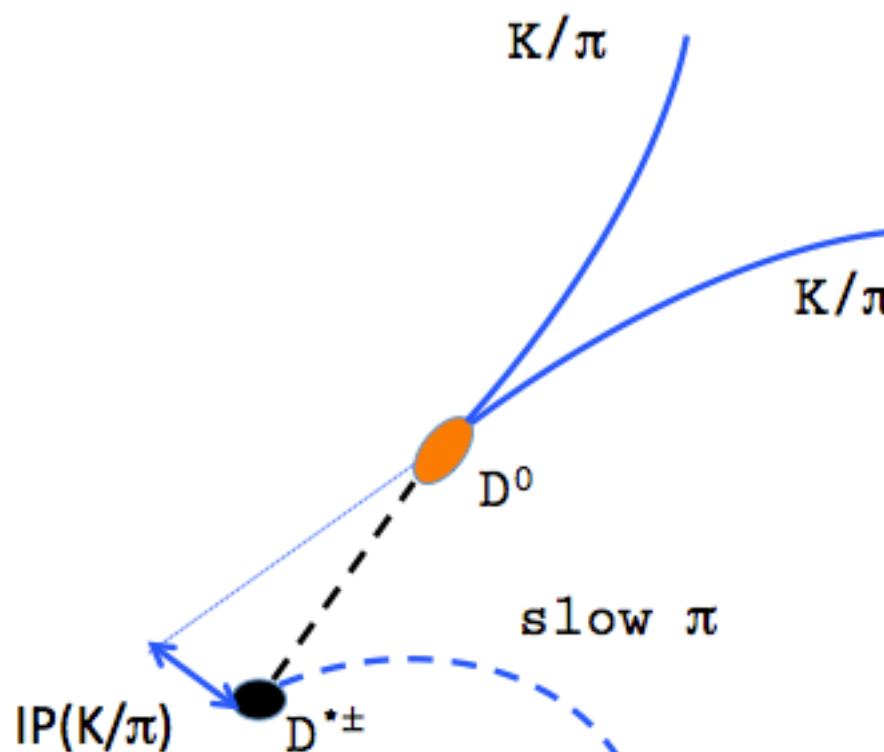
- What we can measure is:



# Detector effects are present in the raw asymmetry

$$A_{\text{raw}}(f) = A_{CP}(f) + A_D(f) + A_D(\pi_s) + A_P(D^{*+})$$

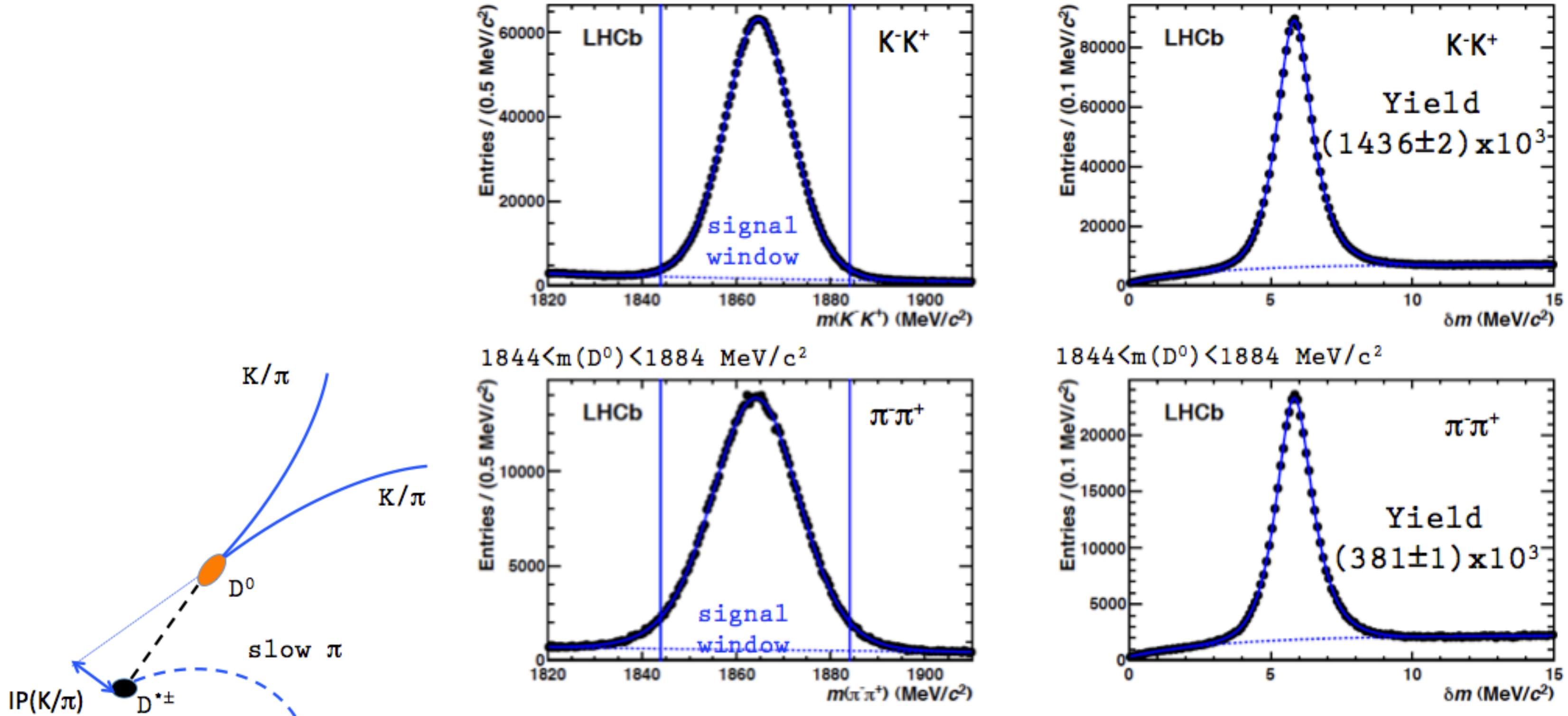
Physics CP asymmetry  
Production asymmetry  
Detection asymmetry of  $D^0$   
Detection asymmetry of "slow" pions



- But everything cancels, in principle, in the double difference

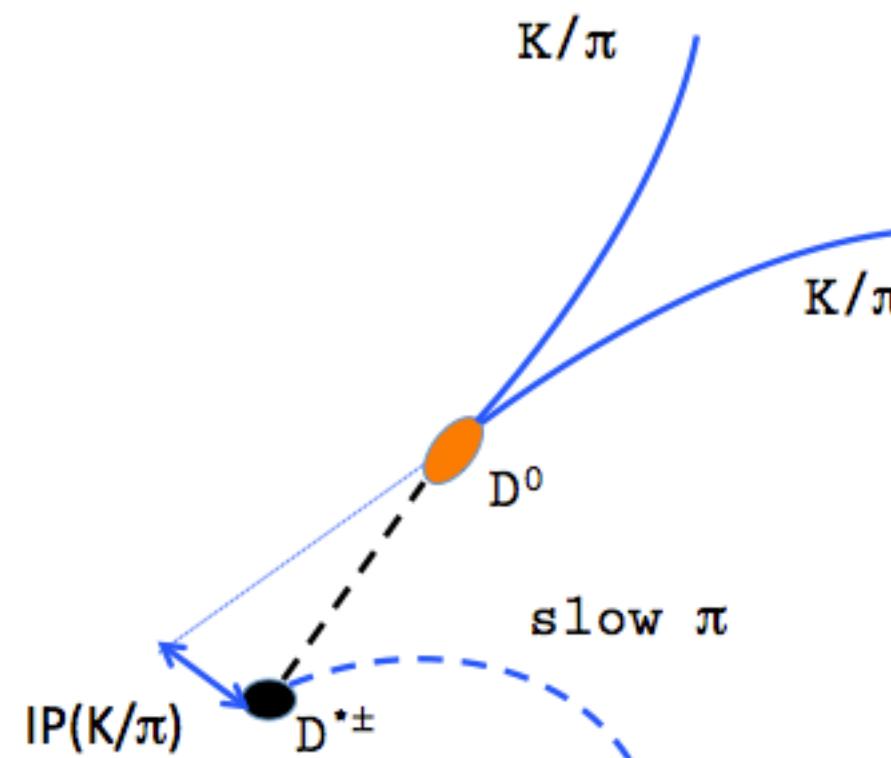
$$\Delta A_{CP} \equiv A_{\text{raw}}(KK) - A_{\text{raw}}(\pi\pi) = A_{CP}(KK) - A_{CP}(\pi\pi)$$

# Mass fits to the total, selected dataset

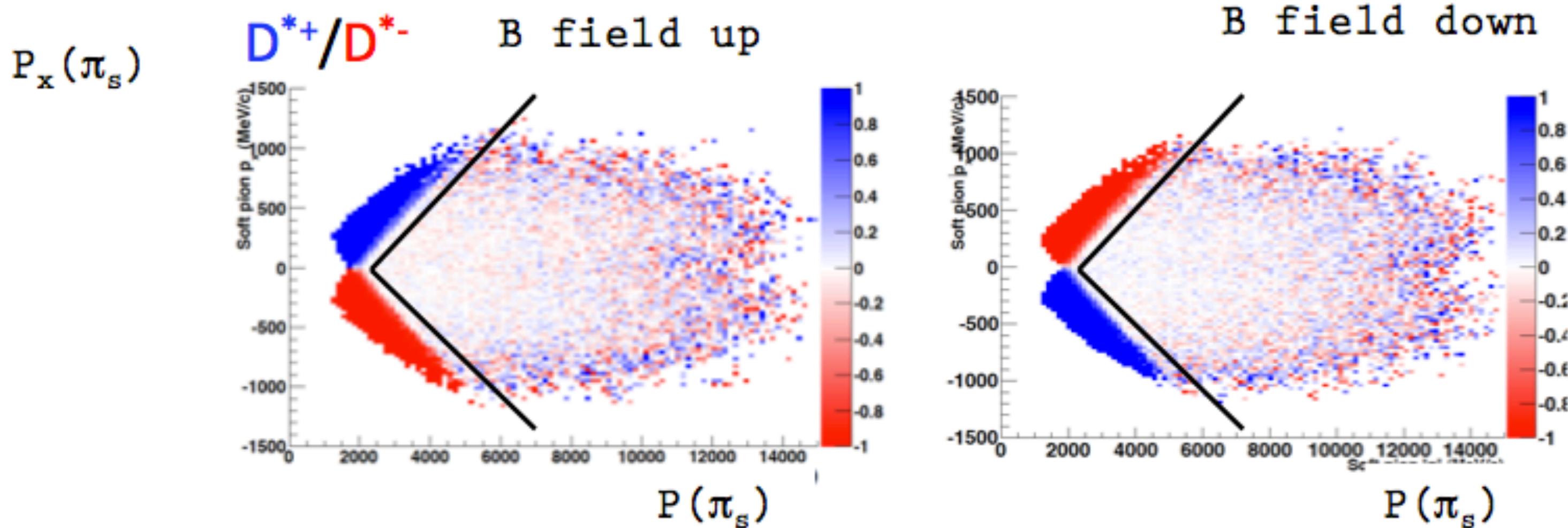


# Robustness against systematic effects

- The cancellation of the instrumentation asymmetries is unfortunately not exact. Second-order dependences on the  $KK/\pi\pi$  efficiency ratio could reintroduce small asymmetries
  - Solution: separate the dataset into several kinematic bins ( $p_T$  and pseudorapidity of the  $D^*$ , and momentum of the slow pion)
  - Similarly, analyse the dipole-up/down data separately, and the left and right hemisphere of LHCb separately.
  - In total 216 statistically independent measurements of  $\Delta A_{CP}$



Also minimise headaches by applying judicious fiducial cuts

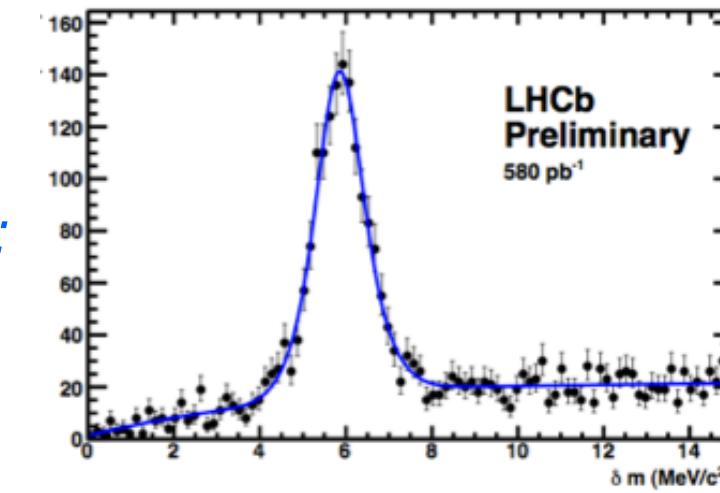


*Exclude regions of phase space where only  
one charge of the slow pion are seen.  
i.e. Don't rely on the UP and DOWN  
magnet samples to exactly cancel!*

## Final measurement fit

- Cut on  $D^0$  mass and fit the  $D^*-D^0$  mass difference only in 216 bins

*One example bin:*



$$\Delta A_{CP} = (-0.82 \pm 0.21 \pm 0.11)\%$$

*Largest systematics from:*  
*Alternative fit procedure (0.08%)*  
*Multiple candidate choice (0.06%)*  
*Hypothetical peaking bkgd (0.04%)*

Consistency:  $\chi^2/NDF = 211/215$ , prob = 56%

# Many, many cross-checks performed, some examples

- Tighter PID cuts using the RICH information

$$\Delta A_{CP} = (-0.88 \pm 0.26)\% \quad \text{tight....} \quad \Delta A_{CP} = (-1.03 \pm 0.31)\% \quad \text{tighter....}$$

- Examine different times, polarity and hemisphere of the detector

Subsample	$\Delta A_{CP}$	$\chi^2/\text{ndf}$
Pre-TS, field up, left	$(-1.22 \pm 0.59)\%$	13/26(98%)
Pre-TS, field up, right	$(-1.43 \pm 0.59)\%$	27/26(39%)
Pre-TS, field down, left	$(-0.59 \pm 0.52)\%$	19/26(84%)
Pre-TS, field down, right	$(-0.51 \pm 0.52)\%$	29/26(30%)
Post-TS, field up, left	$(-0.79 \pm 0.90)\%$	26/26(44%)
Post-TS, field up, right	$(+0.42 \pm 0.93)\%$	21/26(77%)
Post-TS, field down, left	$(-0.24 \pm 0.56)\%$	34/26(15%)
Post-TS, field down, right	$(-1.59 \pm 0.57)\%$	35/26(12%)
All data	$(-0.82 \pm 0.21)\%$	211/215(56%)

Consistency:  
 $\chi^2/\text{NDF} = 6.7/7$   
prob = 45%

# Initial euphoria has given way; the SM is probably not under threat

The screenshot shows a Mozilla Firefox browser window with the following details:

- Title Bar:** [1002.4794] How large can the SM contribution to CP violation in  $D^0-\bar{D}^0$  mixing be? - Mozilla Firefox
- Address Bar:** arxiv.org/abs/arXiv:1002.4794
- Toolbar:** Most Visited, Interactions.org, SPIEGEL ONLINE, Latest Headlines, CERN Hot News.
- Cornell University Library logo:** Cornell University Library
- Right Sidebar:**
  - Download:** PDF, PostScript, Other formats
  - Current browse context: hep-ph
  - < prev | next >
  - new | recent | 1002
  - Change to browse context: hep-ex
  - References & Citations
  - INSPIRE HEP (refers to | cited by)
  - NASA ADS
  - Bookmark (what is this)
  - Print, Copy, Share, Embed, etc.
- Main Content Area:**

## Theory statements about CPV in D before LHCb

### How large can the SM contribution to CP violation in $D^0-\bar{D}^0$ mixing be?

M. Bobrowski, A. Lenz, J. Riedl, J. Rohrwild  
(Submitted on 25 Feb 2010)

We investigate the maximum size of CP violating effects in  $D\bar{D}$ -mixing within the Standard Model (SM), using Heavy Quark Expansion (HQE) as theoretical working tool. For this purpose we determine the leading HQE contributions and also  $\alpha_s$  corrections as well as subleading  $1/m_c$  corrections to the absorptive part of the mixing amplitude of neutral  $D$  mesons. It turns out that these contributions to  $\Gamma_{12}$  do not vanish in the exact  $SU(3)\backslash\text{un}(\text{F})$  limit. Moreover, while the leading HQE terms give a result for  $\Gamma_{12}$  orders of magnitude lower than the current experimental value, we do find a sizeable phase. In the literature it was suggested that higher order terms in the HQE might be much less affected by the severe GIM cancellations of the leading terms; it is even not excluded that these higher order terms can reproduce the experimental value of  $\Gamma_{12}$ . If such an enhancement is realized in nature, the phase discovered in the leading HQE terms can have a sizeable effect. Therefore, we think that statements like: "if CP violating effects in  $D\bar{D}$ -mixing of the order of  $10^{-3}$  to  $10^{-2}$  are an unambiguous sign of new physics"--given our limited knowledge of the SM prediction--are premature. Finally, we give an example of a new physics model that can enhance the leading HQE terms to  $\Gamma_{12}$  by one to two orders of magnitude.

Comments: 14 pages, considerably extended version of 0904.3971 with completely new main aspect; text (except title and abstract) identical to the version accepted by JHEP.  
Subjects: High Energy Physics - Phenomenology (hep-ph); High Energy Physics - Experiment (hep-ex)  
Journal reference: JHEP 03(2010)008  
Report number: DO-TH 10/04, TTK-10-2  
Cite as: arXiv:1002.4794v1 [hep-ph]

#### Submission history

From: Alexander Lenz [view email]  
[v1] Thu, 25 Feb 2010 14:27:00 GMT (97kb)

Which authors of this paper are endorsers?

Link back to: arXiv, form interface, contact.

Alexander  
Lenz,  
Moriond  
2012

## Nevertheless, LHCb will continue to explore CPV in charm

---

- Considerable efforts to make the LHCb trigger more favourable to charm in 2012 will mean a quadrupling of the dataset, not x2.5.
- Instead of using the slow pion, an analysis using the muon from semi-leptonic B decays is underway. i.e.  $\Delta A_{CP}$  from  $B \rightarrow D^0 \mu^\pm \nu$
- Other singly Cabibbo suppressed decays under study, notably the Dalitz analysis of flavour-tagged  $D^0 \rightarrow K_S \pi \pi$

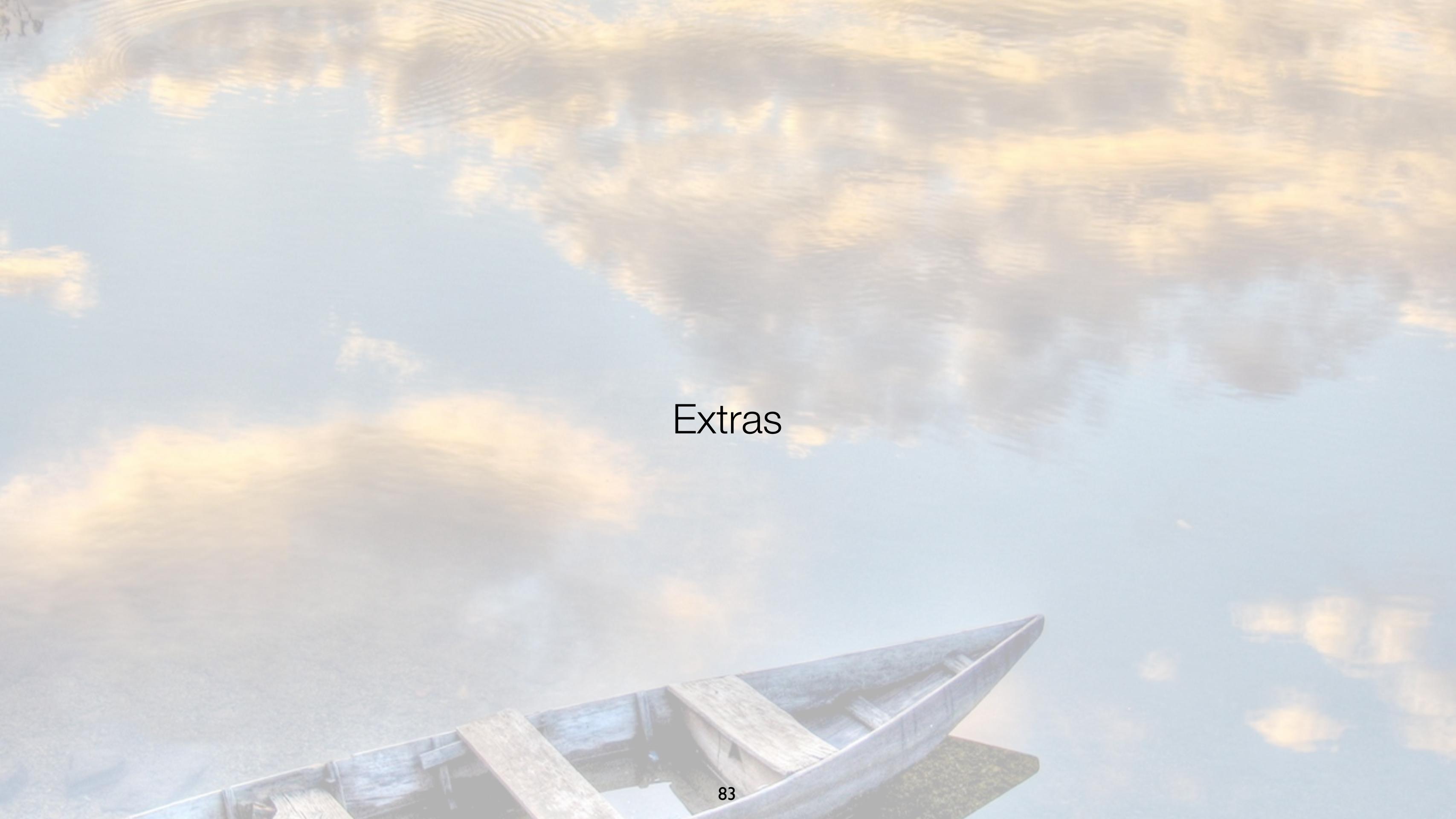
# Conclusion

Observation of direct  $CP$  violation in  $B^+$  decays  
Important step toward a measurement of  $\gamma$  with  $\sim 10\%$  precision in the  
next 12-15 months

Searches for time-dependent  $CP$ -violation in  
the mixing and decay of  $B_s$  mesons

Hints of unexpectedly large  $CP$  violation in the  $B_s$  system have been  
wiped away. Efforts continue, but quantifying the penguin contribution  
in both  $B^0$  and  $B_s$  systems needs the LHCb upgrade

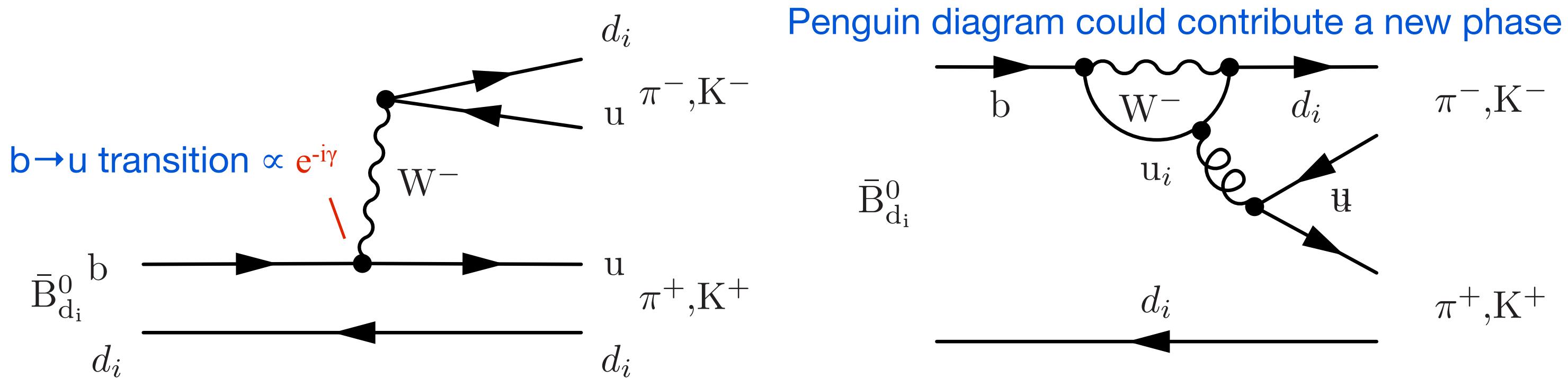
Evidence for direct  $CP$  violation in  $D^0$  decays  
Look to confirm this result in the next 18 months

A photograph of a traditional wooden boat on a body of water, likely a lake or river. The boat is dark wood with a white stripe along the side. The water is calm with some ripples. In the background, there are hills or mountains under a sky filled with clouds colored in shades of orange, yellow, and blue from a sunset. The overall atmosphere is peaceful and scenic.

Extras

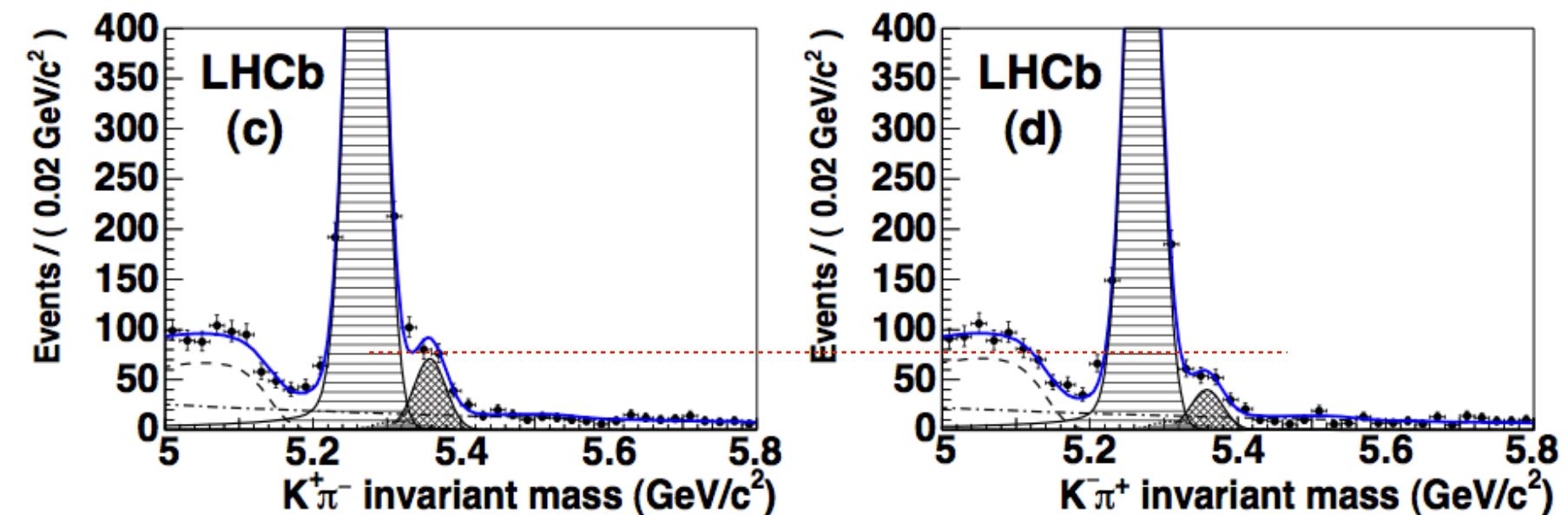
# Uses of $\gamma$ from trees: comparison with loop-mediated processes

- Charmless decays of  $B_d$  and  $B_s$  mesons can exhibit CP violation from tree-penguin interference



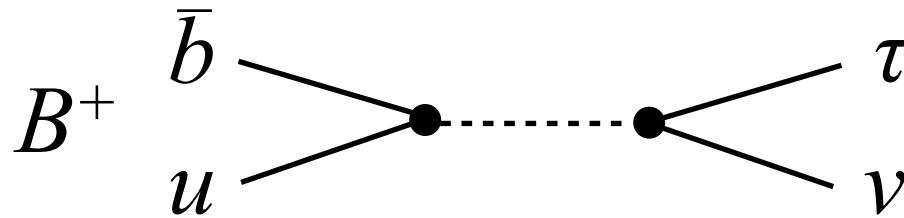
- Aside:
- First evidence of direct CP violation in charmless two-body decays of  $B_s^0$  mesons

LHCb. arXiv:1202.6251

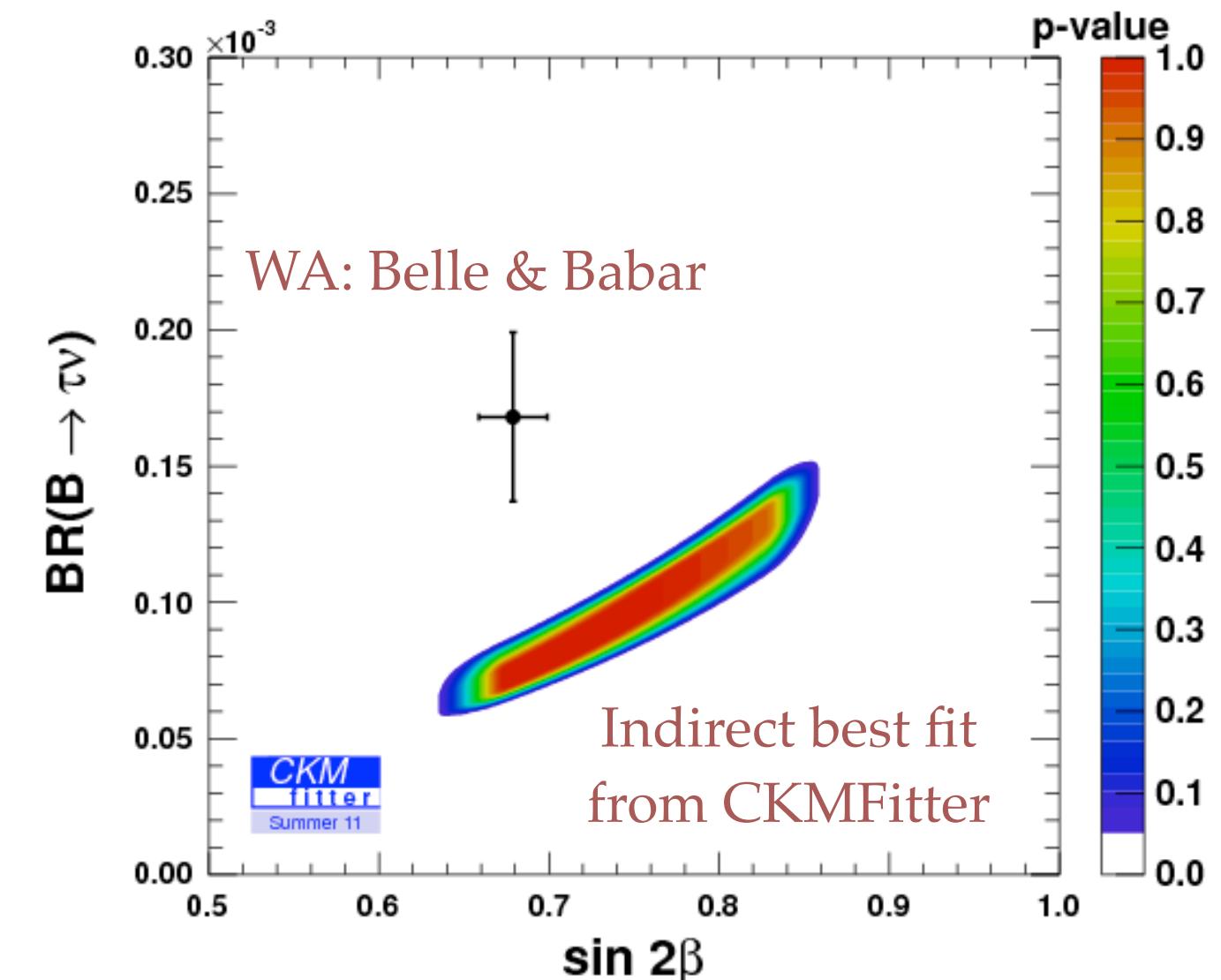


# Uses of $\gamma$ from trees: CKM triangle metrology

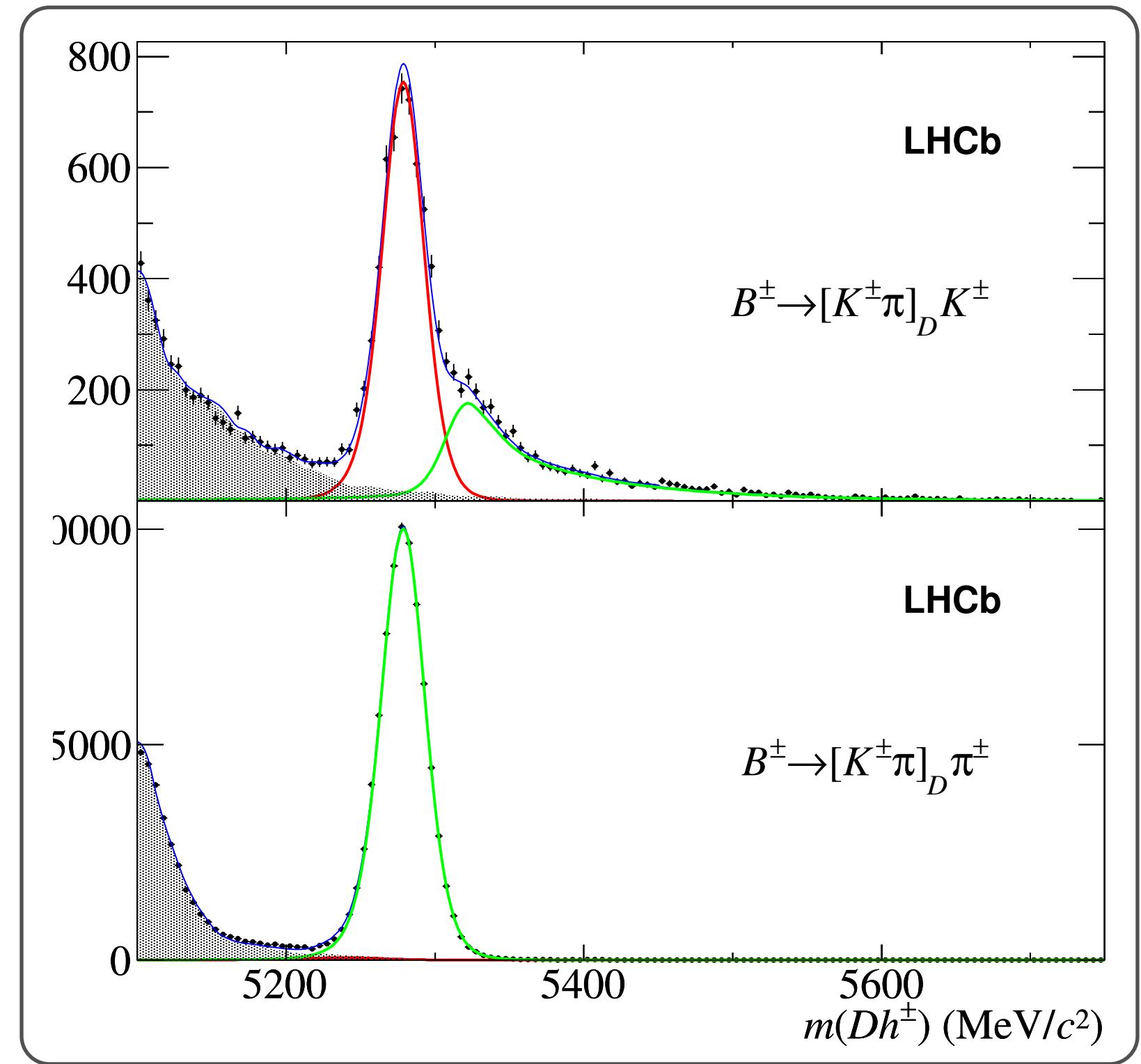
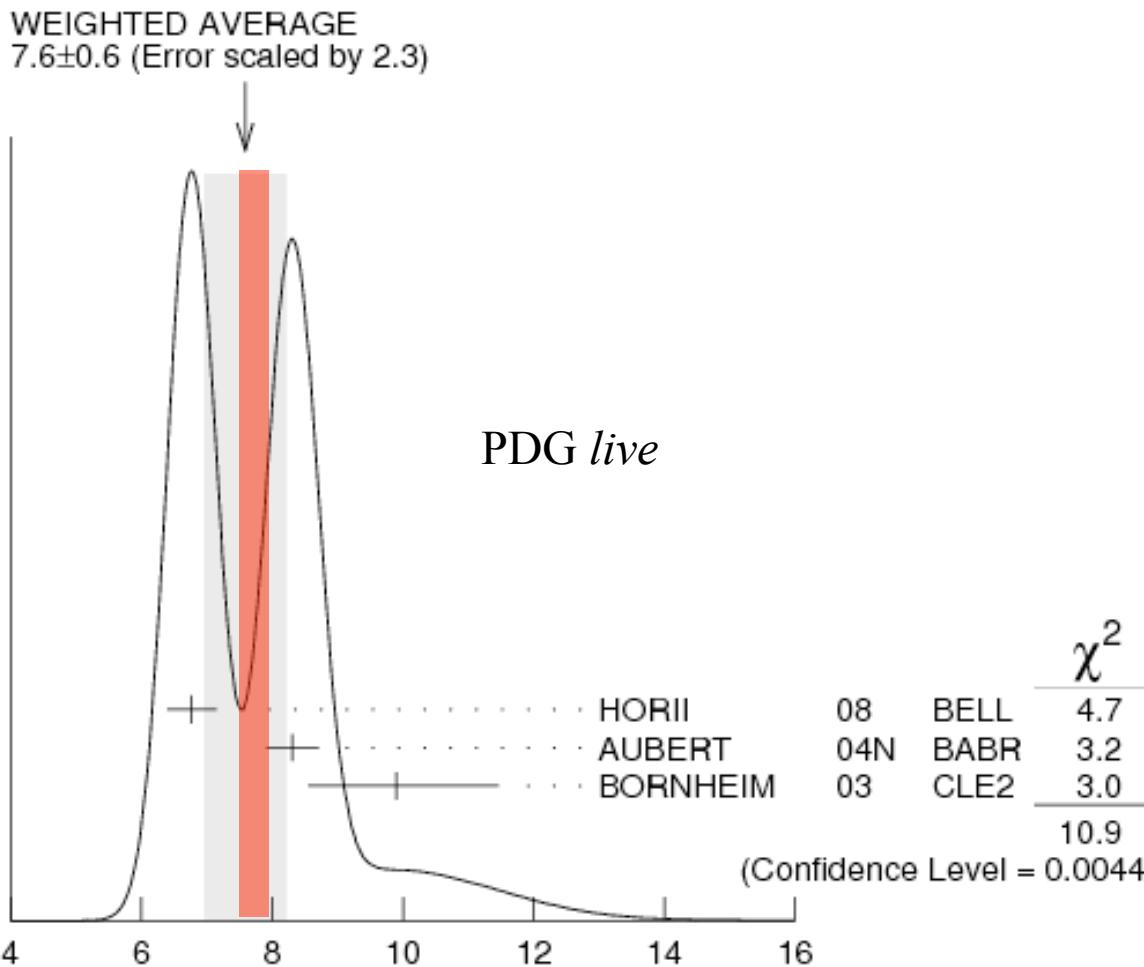
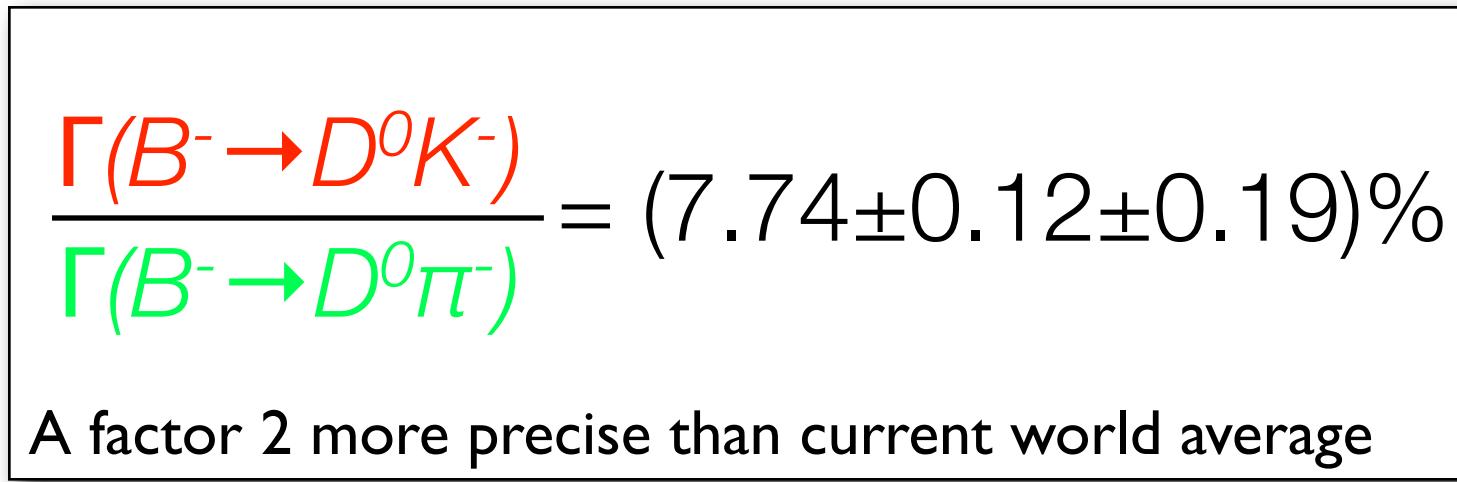
- $\sin 2\beta$  is the most precisely determined component of the unitarity triangle
  - the penguin contribution is usually neglected, but, this could be naive
- An example of tension in the unitarity triangle is with  $|V_{ub}|$  from  $B^+ \rightarrow \tau^+\nu$  and  $\sin 2\beta$ 
  - This is a simple tree decay (exchange diagram)
  - Small theoretical uncertainties.



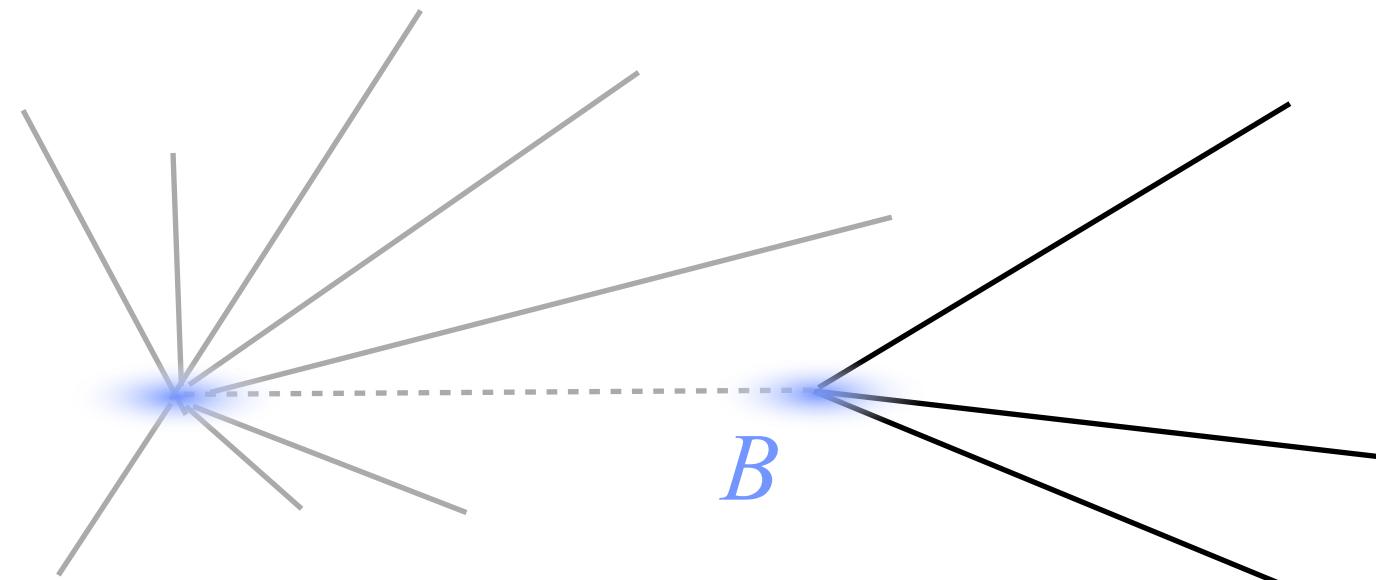
- As we seek to test the unitarity of the CKM model, it becomes increasingly important to distinguish tree measurements from those with sensitivity to loops.



# First result: the ratio of $B^- \rightarrow D^0 h^-$ branching fractions



# Non-true- $D$ peaking backgrounds in the CP and ADS modes



e.g.  $B^\pm \rightarrow [\pi\pi]K^\pm$  suffers from:

$$B^\pm \rightarrow K\pi\pi^\pm$$

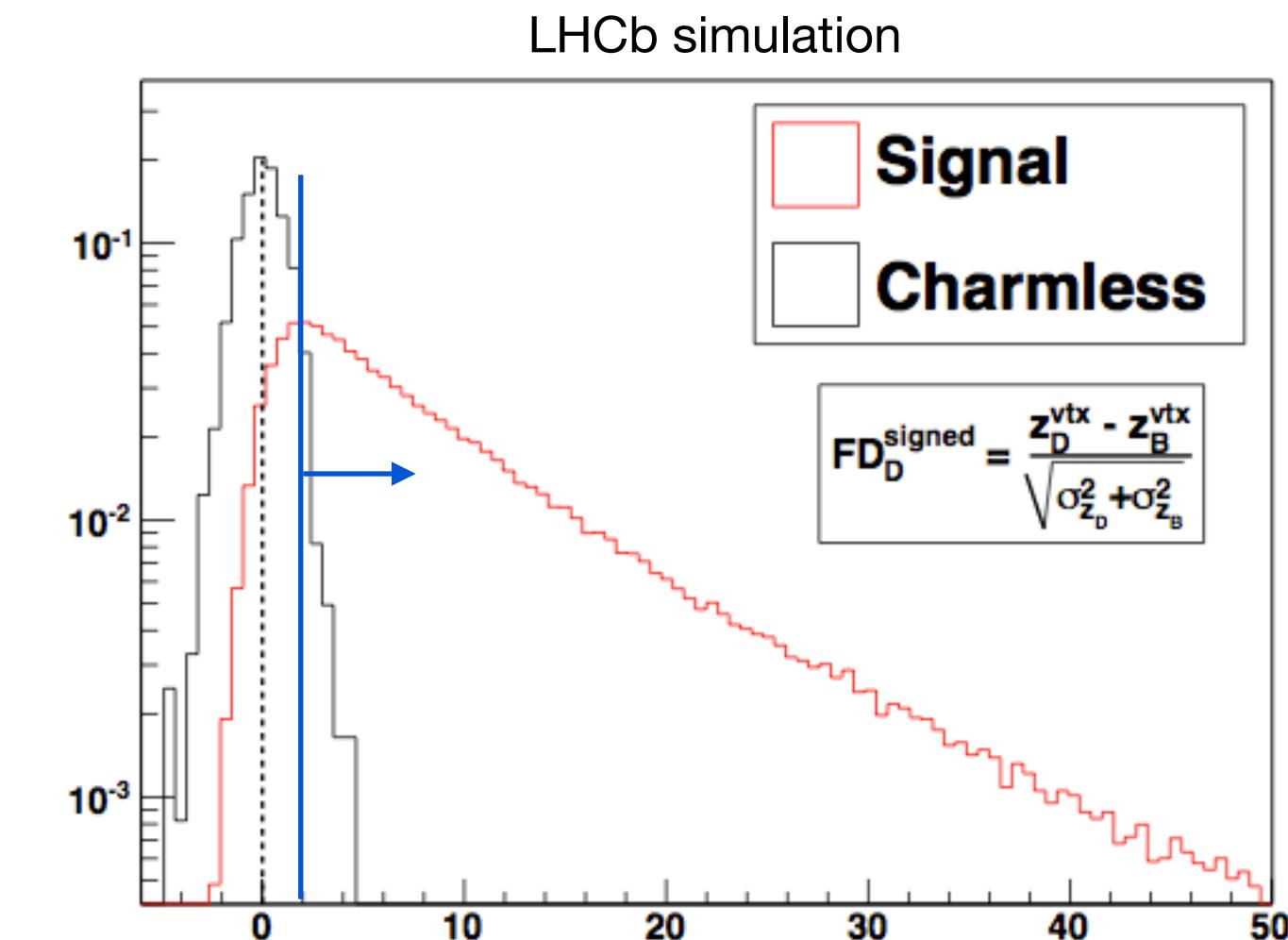
Charmless

$$B^\pm \rightarrow [K\pi]\pi^\pm$$

Cross feed

$$B^\pm \rightarrow [\pi\pi\pi^0]\pi^\pm$$

Part. reco. cross feed



- Thanks to the large boost at LHCb non-true- $D$  backgrounds can be easily removed.
- The above cut is ~85% efficient and removes 97% of zero-lifetime backgrounds

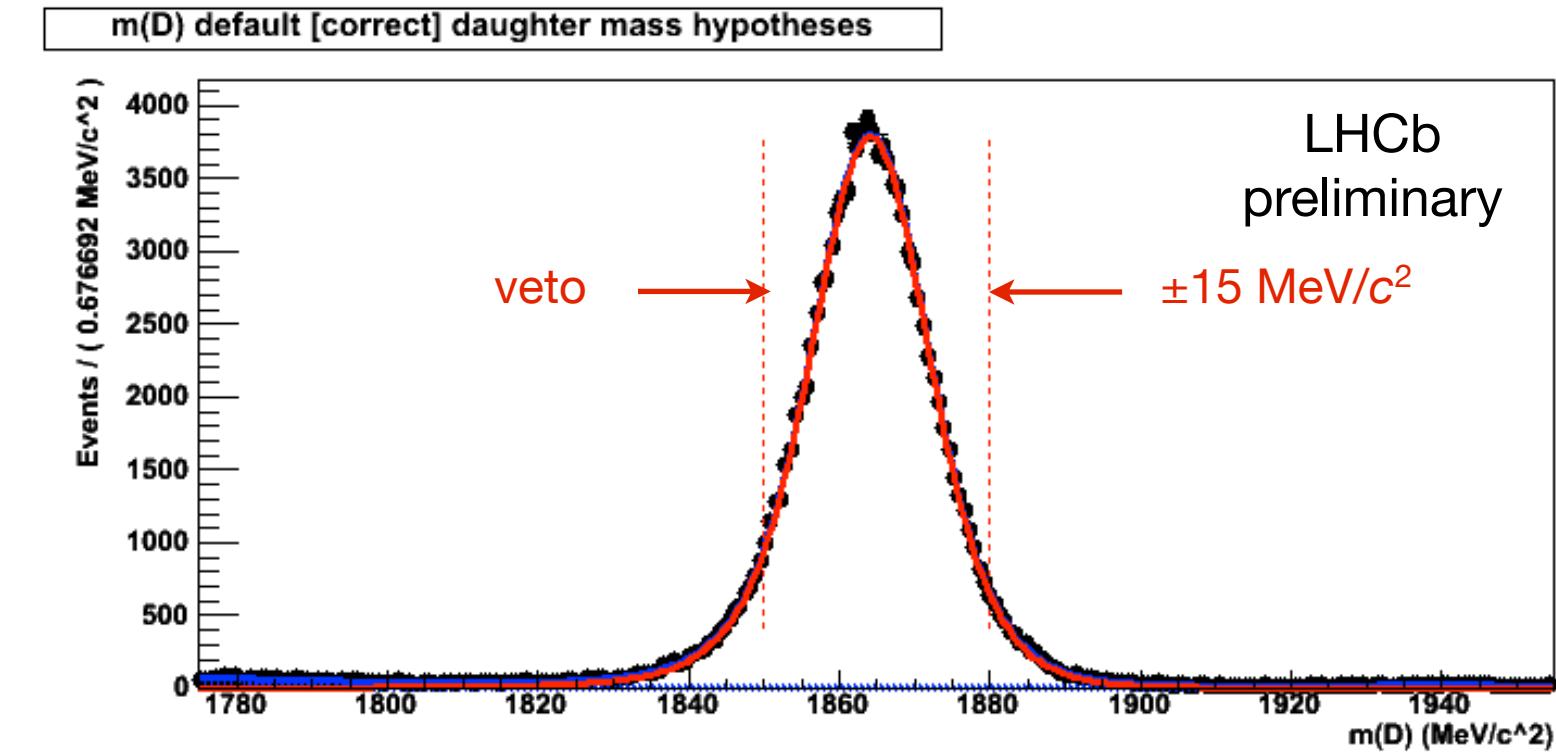
# Favoured mode $\rightarrow$ ADS mode cross feed

$$B^\pm \rightarrow [K\pi] h^\pm$$

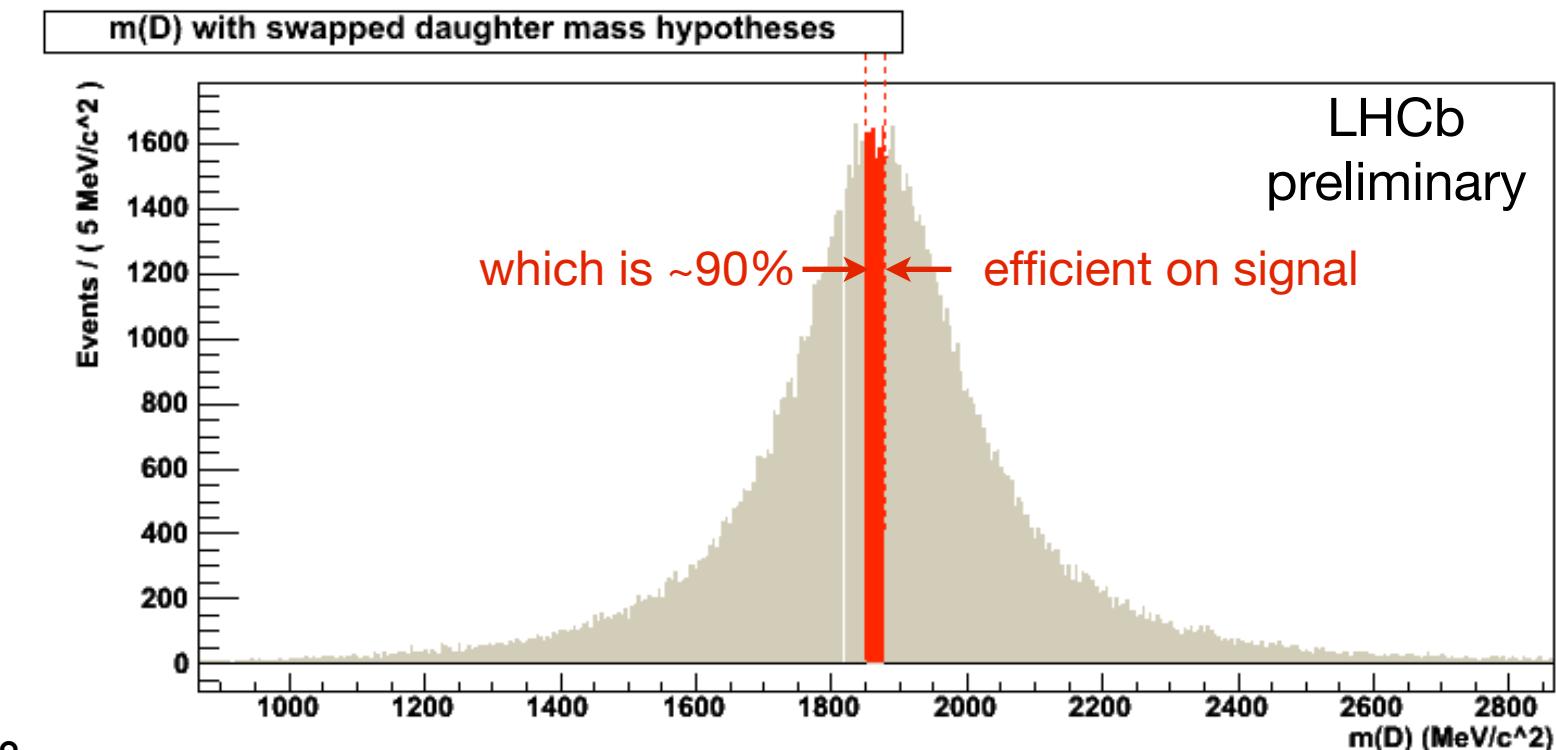
double ↓ misID

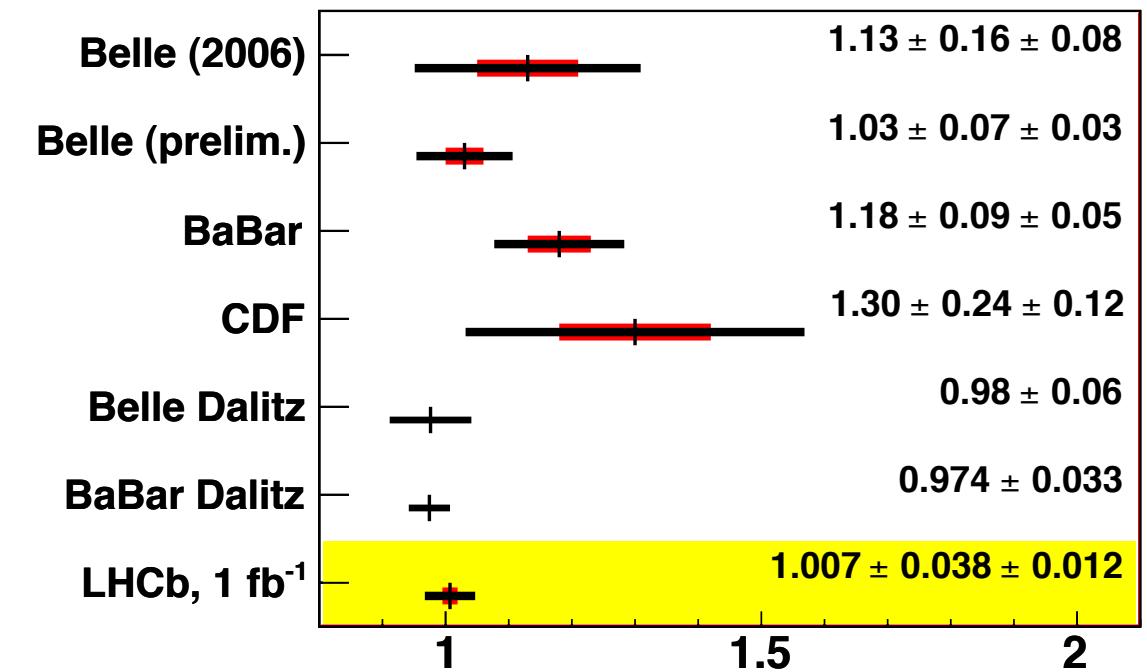
$$B^\pm \rightarrow [\pi K] h^\pm$$

check for by swapping mass hypothesis back

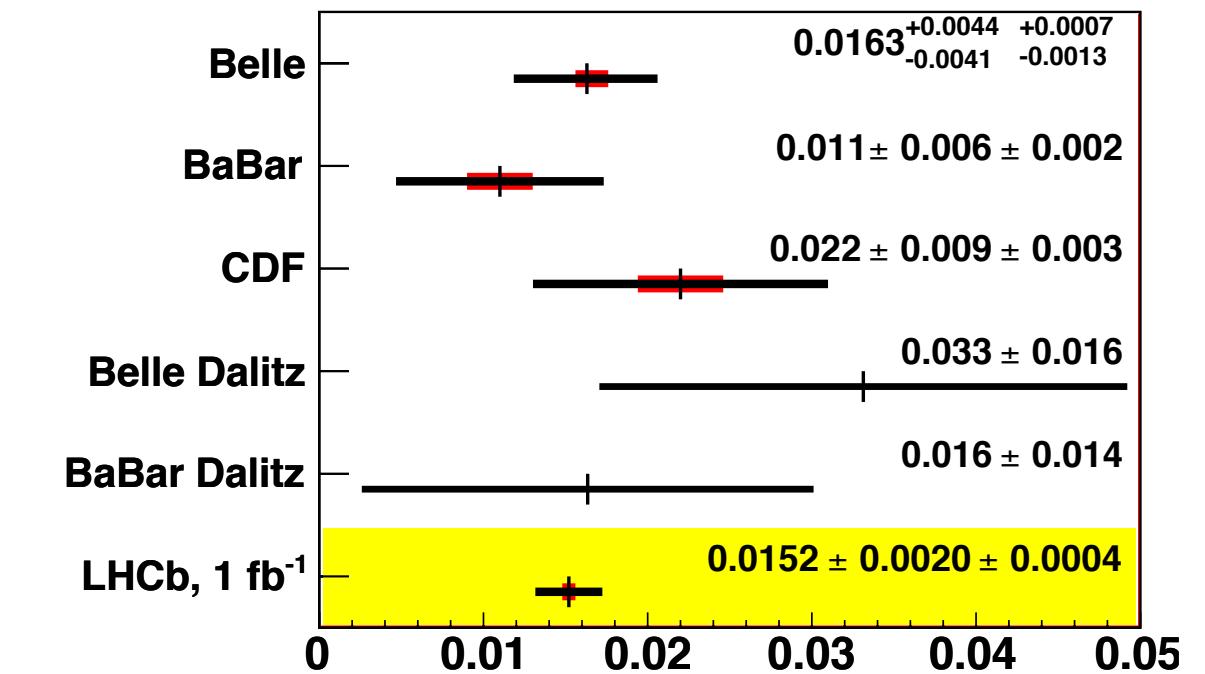


- Combat with PID cuts on the  $D$  daughter tracks.
- But this is not sufficient. A veto is needed.
- After PID cuts and the veto, the expected cross feed rate is  $6 \times 10^{-5}$ .
- This is just **2%** of  $R_{ADS(\pi)}$ .



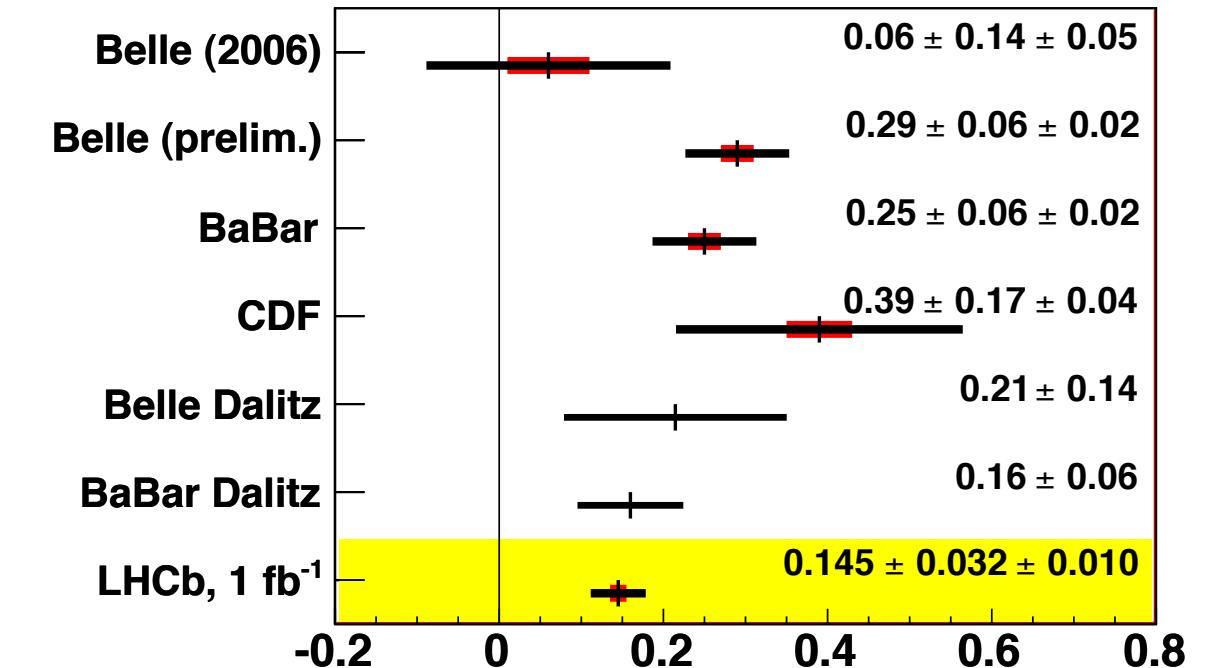


$$R_{CP+} = 1 + r_B^2 + 2r_B \cos \delta_B \cos \gamma$$

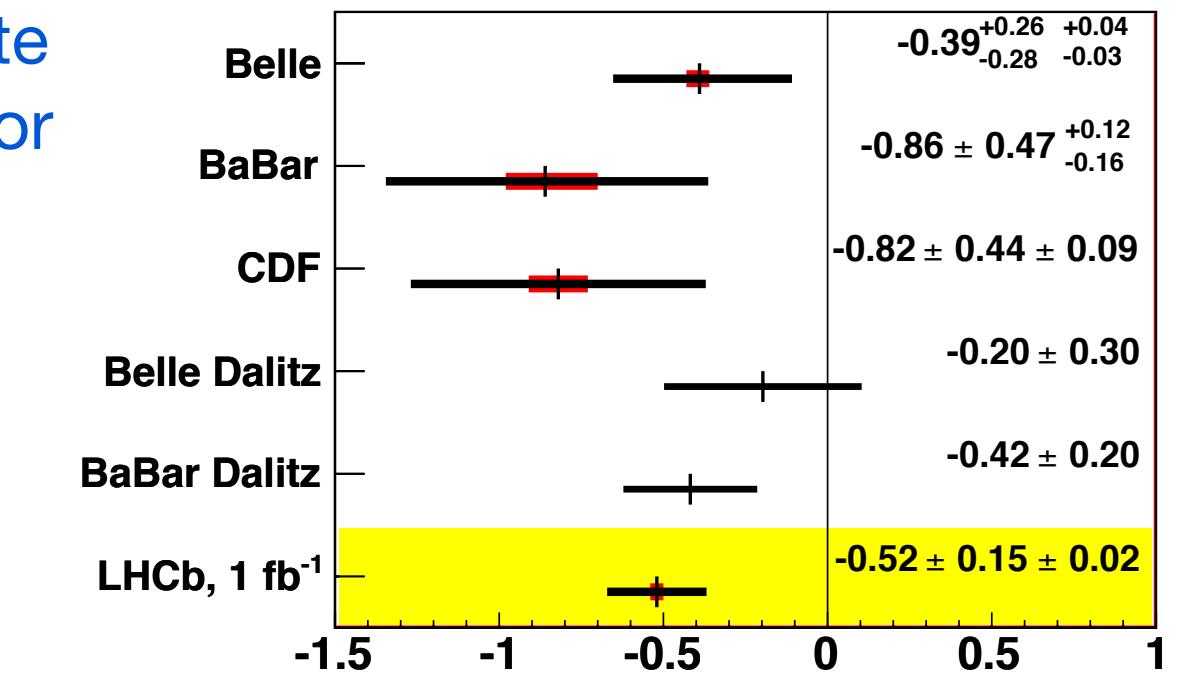


$$R^{ADS} = \frac{r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos \gamma}{1 + (r_B r_D)^2 + 2r_B r_D \cos(\delta_B - \delta_D) \cos \gamma}$$

GGSZ methods measure the underlying parameters,  $r_B, \gamma, \delta$ . From these, we can calculate the four observables for comparison.

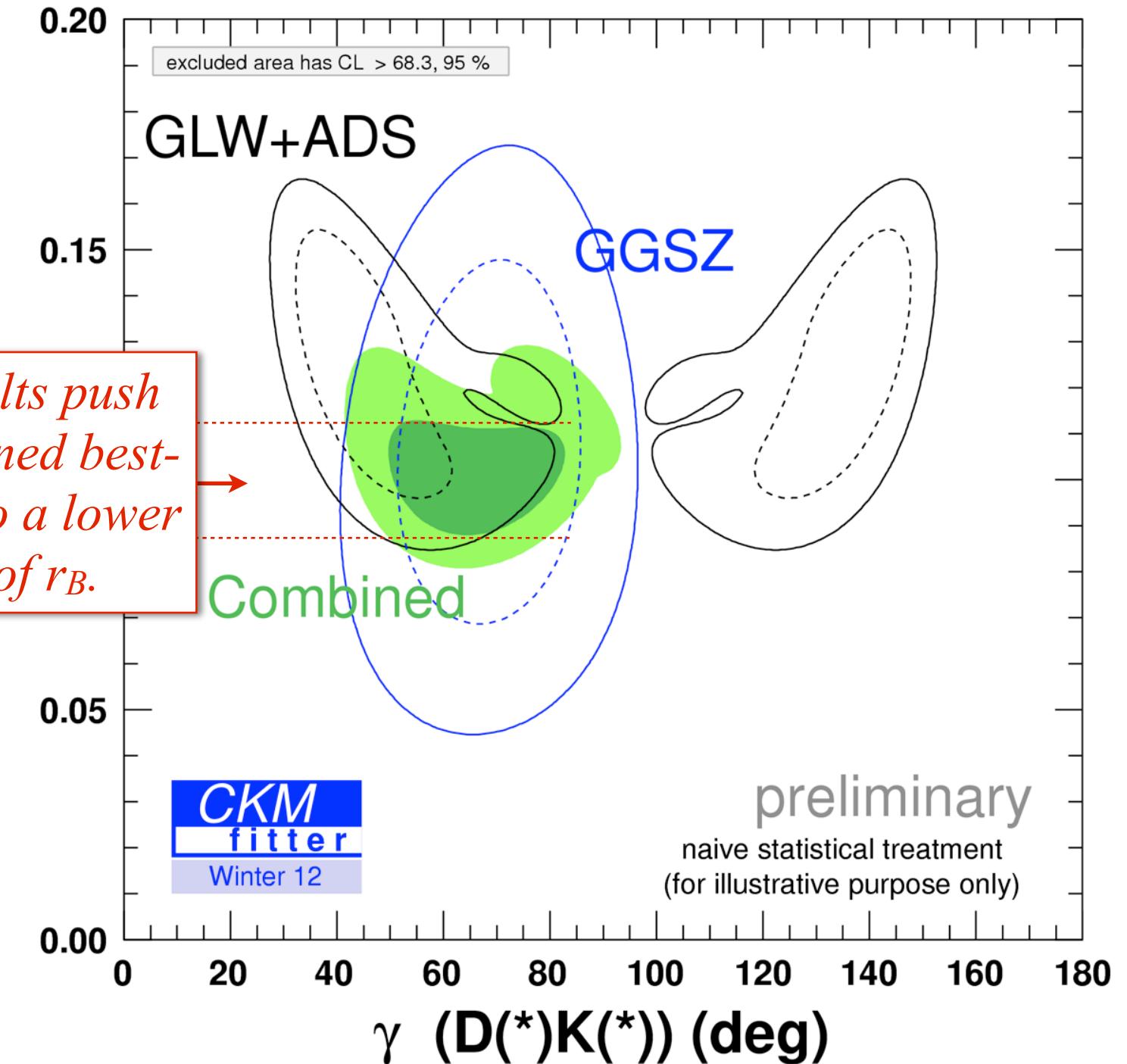
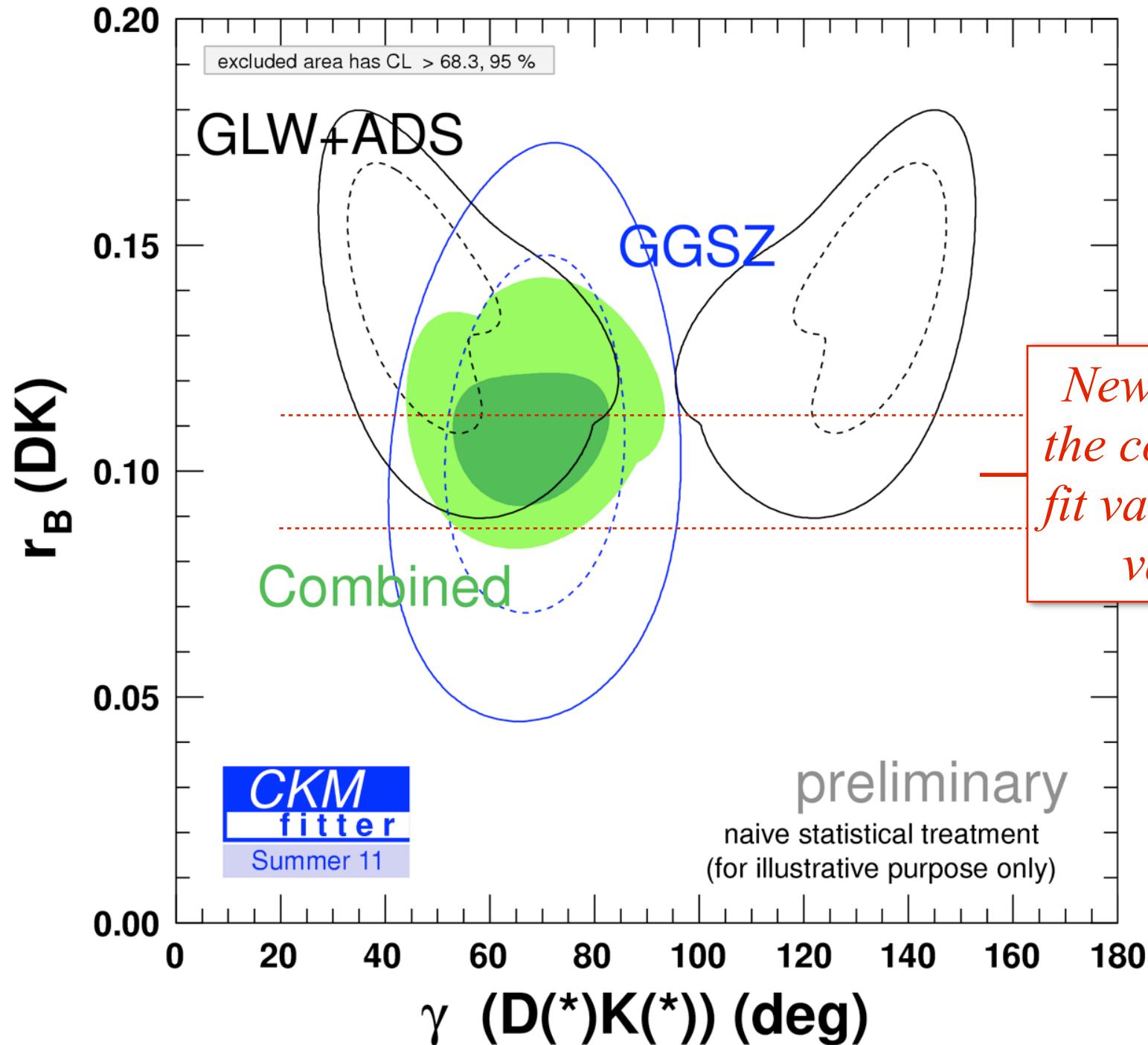


$$A_{CP+} = \frac{2r_B \sin \delta_B \sin \gamma}{1 + r_B^2 + 2r_B \cos \delta_B \cos \gamma}$$



$$A^{ADS} = \frac{2r_B r_D \sin(\delta_B + \delta_D) \sin \gamma}{r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos \gamma}$$

Many thanks to the CKMFitter collaboration for absorbing these results



# Dealing with production/detection asymmetries

$B^\pm \rightarrow [K\pi]_D h^\pm$	$A_{CP}((K\pi)_D \pi) = A_{raw}((K\pi)_D \pi) - A_{Prod} - A_K$
	$A_{CP}((K\pi)_D K) = A_{raw}((K\pi)_D K) - A_{Prod} - 2 \times A_K$
$B^\pm \rightarrow [\pi K]_D h^\pm$	$A_{CP}((\pi K)_D \pi) = A_{raw}((\pi K)_D \pi) - A_{Prod} + A_K$
	$A_{CP}((\pi K)_D K) = A_{raw}((\pi K)_D K) - A_{Prod}$
$B^\pm \rightarrow [KK]_D h^\pm$	$A_{CP}((KK)_D \pi) = A_{raw}((KK)_D \pi) - A_{Prod}$
	$A_{CP}((KK)_D K) = A_{raw}((KK)_D K) - A_{Prod} - A_K$
$B^\pm \rightarrow [\pi\pi]_D h^\pm$	$A_{CP}((\pi\pi)_D \pi) = A_{raw}((\pi\pi)_D \pi) - A_{Prod}$
	$A_{CP}((\pi\pi)_D K) = A_{raw}((\pi\pi)_D K) - A_{Prod} - A_K$

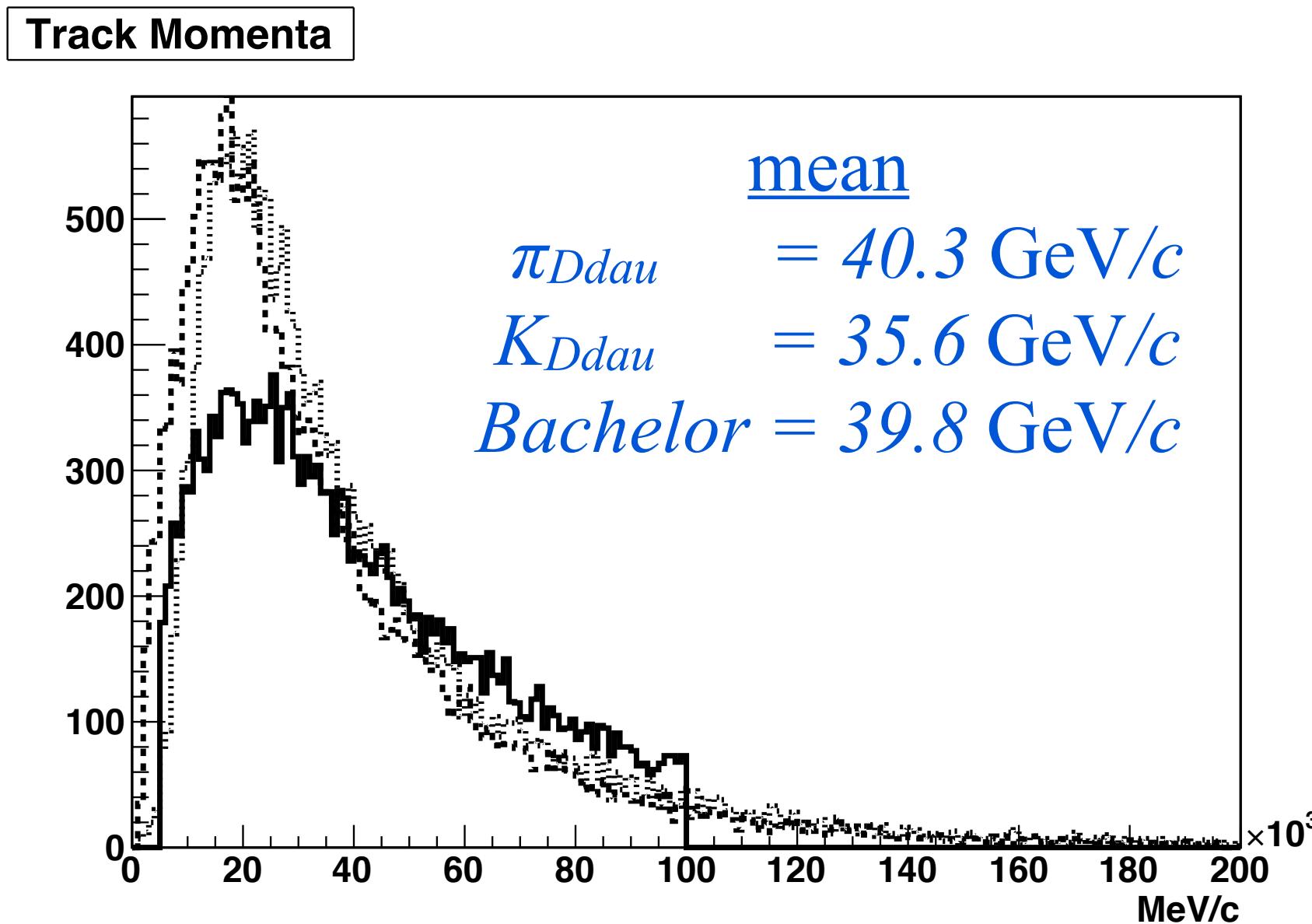
$$\frac{A_{Raw}^{J/\psi K^\pm}}{+A_{PDG}, -0.001 \pm 0.007} = -0.012 \pm 0.004$$



FIXED (%)

$A_{Prod} = -0.8 \pm 0.7$
$A_K = -0.5 \pm 0.7$
$A_\pi = 0.0 \pm 0.7$

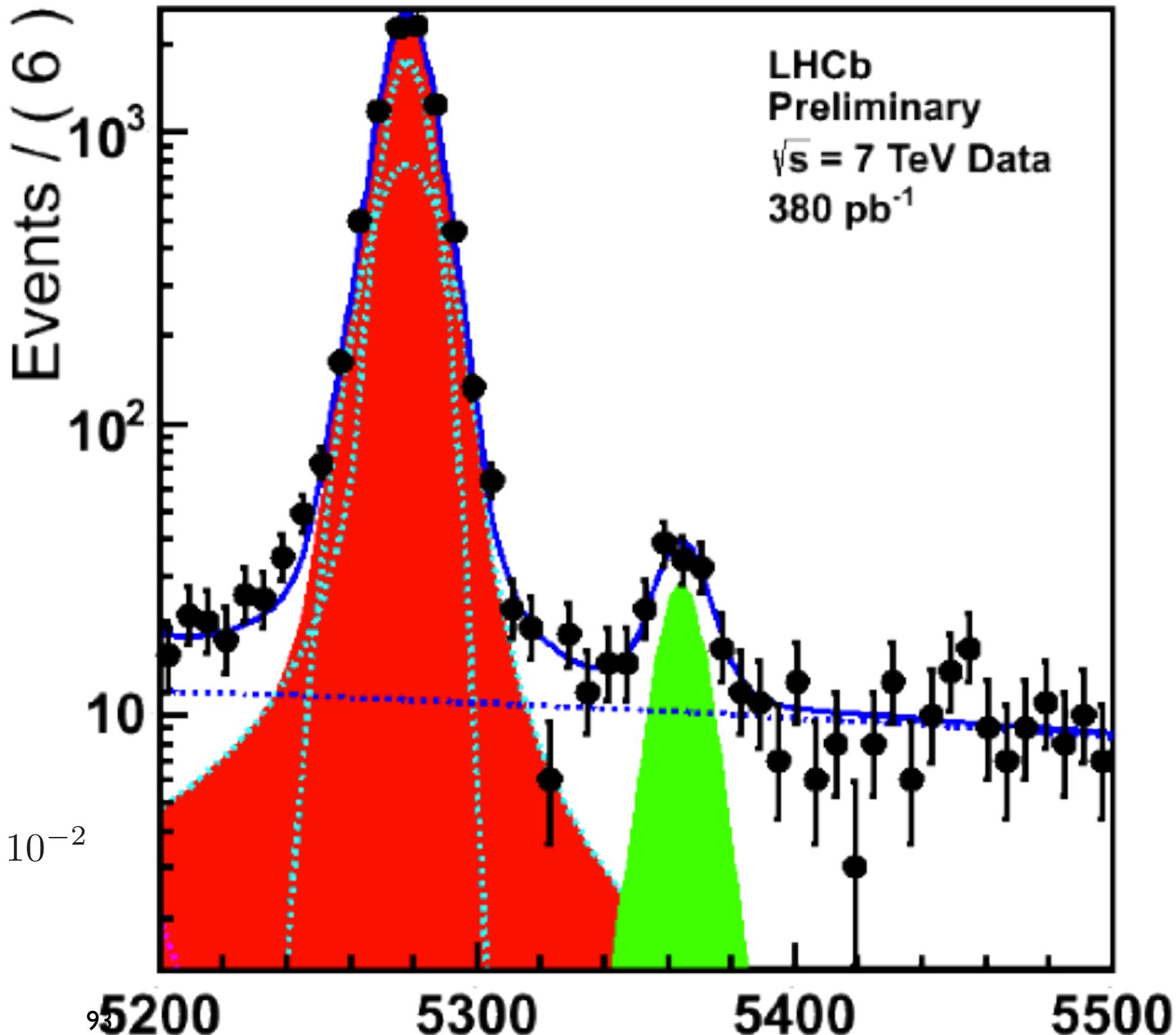
# Track momentum of final sample



# Penguins in $\sin(2\beta)$ : $B_s \rightarrow J/\psi K_S$

- The unitarity triangle shows some tension between  $|V_{ub}|$  and  $\sin(2\beta)$ .
- How much of “ $\sin(2\beta)$ ” is  $\sin(2\beta)$ ? How large are the hadronic penguin contributions?
- Could be eventually deduced by comparing  $B_d \rightarrow J/\psi K_S^0$  and its U-spin partner:  $B_s \rightarrow J/\psi K_S^0$
- First step: confirmation in LHCb dataset.

$$\frac{\mathcal{B}(B_s \rightarrow J/\psi K_S^0)}{\mathcal{B}(B_d \rightarrow J/\psi K_S^0)} = (3.78 \pm 0.58 \pm 0.20 \pm 0.30) \times 10^{-2}$$



DACP elsewhere...

## Experimental status (individual $A_{CP}$ )

Year	Experiment	CP Asymmetry in the decay mode D0 to $\pi^+\pi^-$	$[\Gamma(D0)-\Gamma(D0\bar{b}ar)]/[\Gamma(D0)+\Gamma(D0\bar{b}ar)]$
2010	CDF	<a href="#">M.J. Morello (CDF Collab.), Preprint (CHARM 2010).</a>	+0.0022 ± 0.0024 ± 0.0011
2008	BELLE	<a href="#">M. Staric et al. (BELLE Collab.), Phys. Lett. B 670, 190 (2008).</a>	+0.0043 ± 0.0052 ± 0.0012
2008	BABAR	<a href="#">B. Aubert et al. (BABAR Collab.), Phys. Rev. Lett. 100, 061803 (2008).</a>	-0.0024 ± 0.0052 ± 0.0022
2002	CLEO	<a href="#">S.E. Csorna et al. (CLEO Collab.), Phys. Rev. D 65, 092001 (2002).</a>	+0.019 ± 0.032 ± 0.008
2000	FOCUS	<a href="#">J.M. Link et al. (FOCUS Collab.), Phys. Lett. B 491, 232 (2000).</a>	+0.048 ± 0.039 ± 0.025
1998	E791	<a href="#">E.M. Aitala et al. (E791 Collab.), Phys. Lett. B 421, 405 (1998).</a>	-0.049 ± 0.078 ± 0.030
.	.	COMBOS average	+0.0020 ± 0.0022

Year	Experiment	CP Asymmetry in the decay mode D0 to $K^+K^-$	$[\Gamma(D0)-\Gamma(D0\bar{b}ar)]/[\Gamma(D0)+\Gamma(D0\bar{b}ar)]$
2011	CDF	<a href="#">A. Di Canto (CDF Collab.), Preprint (BEAUTY 2011).</a>	-0.0024 ± 0.0022 ± 0.0010
2008	BELLE	<a href="#">M. Staric et al. (BELLE Collab.), Phys. Lett. B 670, 190 (2008).</a>	-0.0043 ± 0.0030 ± 0.0011
2008	BABAR	<a href="#">B. Aubert et al. (BABAR Collab.), Phys. Rev. Lett. 100, 061803 (2008).</a>	+0.0000 ± 0.0034 ± 0.0013
2002	CLEO	<a href="#">S.E. Csorna et al. (CLEO Collab.), Phys. Rev. D 65, 092001 (2002).</a>	+0.000 ± 0.022 ± 0.008
2000	FOCUS	<a href="#">J.M. Link et al. (FOCUS Collab.), Phys. Lett. B 491, 232 (2000).</a>	-0.001 ± 0.022 ± 0.015
1998	E791	<a href="#">E.M. Aitala et al. (E791 Collab.), Phys. Lett. B 421, 405 (1998).</a>	-0.010 ± 0.049 ± 0.012
1995	CLEO	<a href="#">J.E. Bartelt et al. (CLEO Collab.), Phys. Rev. D 52, 4860 (1995).</a>	+0.080 ± 0.061
1994	E687	<a href="#">P.L. Frabetti et al. (E687 Collab.), Phys. Rev. D 50, 2953 (1994).</a>	+0.024 ± 0.084
.	.	COMBOS average	-0.0023 ± 0.0017