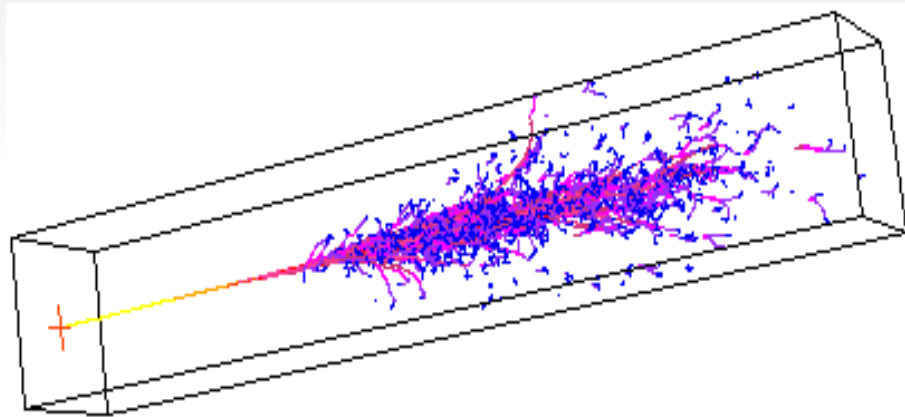


Charged and neutral particle ID with the EMC



Ronald Kunne
IPN Orsay, France
CNRS/IN2P3 – Université Paris Sud



- What are Bayesian classifiers ?
- Charged PID
- Neutral PID

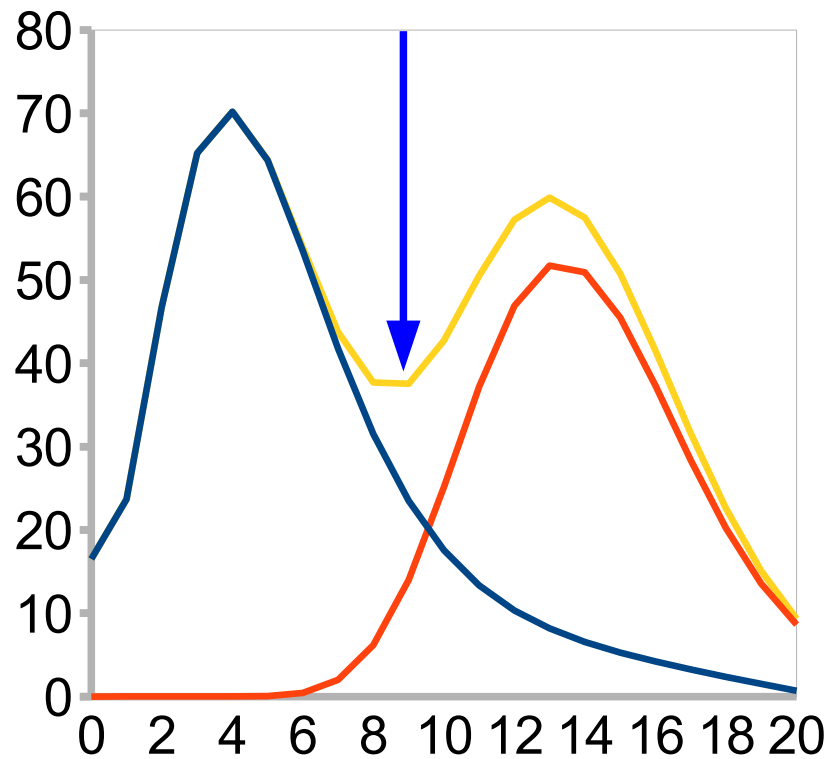


- PandaRoot Version : 12490 (26/6/11)
- externals: may 2011

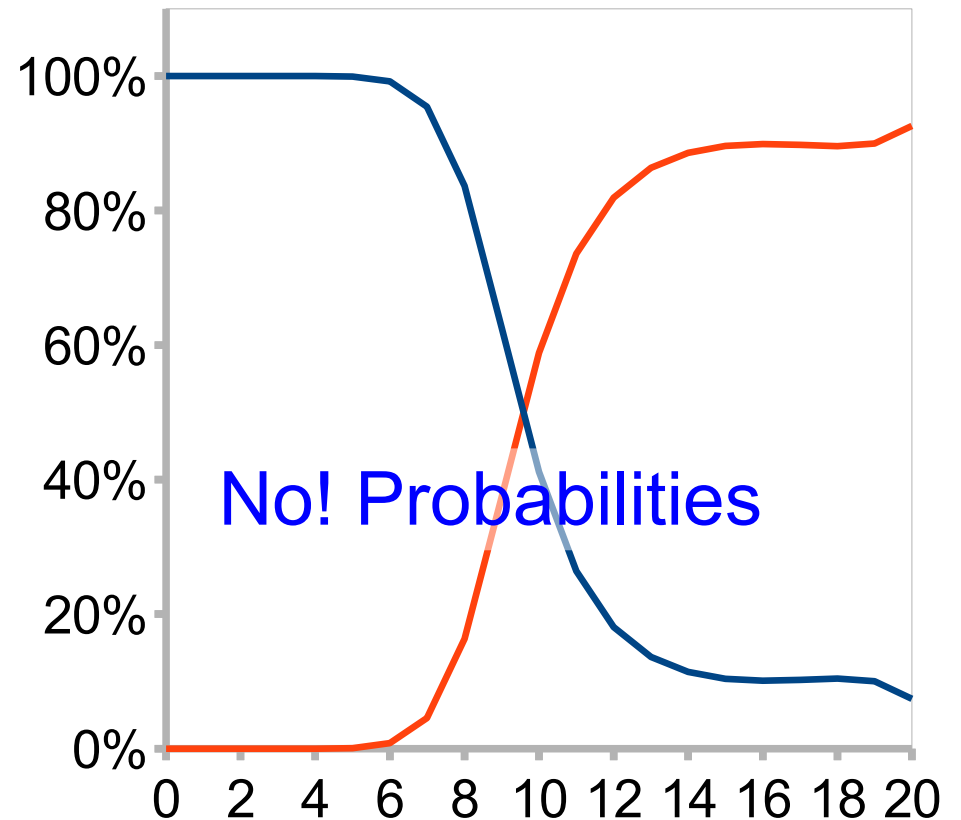
What are Bayesian classifiers ?

Hard cuts are not optimal

Hard cut ?



— apples
— pears
— sum



Enter Bayes' Theorem

$$P(e \mid \text{data}) = \frac{P(\text{data} \mid e) * P(e)}{P(\text{data} \mid e) * P(e) + P(\text{data} \mid \pi) * P(\pi) + \dots}$$

Enter Bayes' Theorem

$$P(e \mid \text{data}) = \frac{P(\text{data} \mid e) * P(e)}{P(\text{data} \mid e) * P(e) + P(\text{data} \mid \pi) * P(\pi) + \dots}$$
$$= \frac{P(\text{data} \mid e)}{P(\text{data} \mid \text{all})} \frac{P(e)}{P(\text{all})}$$

Enter Bayes' Theorem

$$P(e \mid \text{data}) = \frac{P(\text{data} \mid e) * P(e)}{P(\text{data} \mid e) * P(e) + P(\text{data} \mid \pi) * P(\pi) + \dots}$$

$$= \frac{P(\text{data} \mid e)}{P(\text{data} \mid \text{all})} \frac{P(e)}{P(\text{all})} \leftarrow \boxed{= 1}$$

When the data are uncorrelated we can write :

$$P(\text{data} \mid \text{all}) = P(d_1 \mid \text{all}) * P(d_2 \mid \text{all}) * \dots$$

Bayesian classifiers

$P(e \mid \text{data}) =$

$$\frac{P(d_1 \mid e)}{P(d_1 \mid \text{all})} * \frac{P(d_2 \mid e)}{P(d_2 \mid \text{all})} * \frac{P(d_3 \mid e)}{P(d_3 \mid \text{all})} * P(e)$$

Bayes'
factor
(from MC)

From flux,
other data

Very practical !

$P(e \mid \text{data}) =$

$$\frac{P(d_1 \mid e)}{P(d_1 \mid \text{all})} * \frac{P(d_2 \mid e)}{P(d_2 \mid \text{all})} * \frac{P(d_3 \mid e)}{P(d_3 \mid \text{all})} * P(e)$$

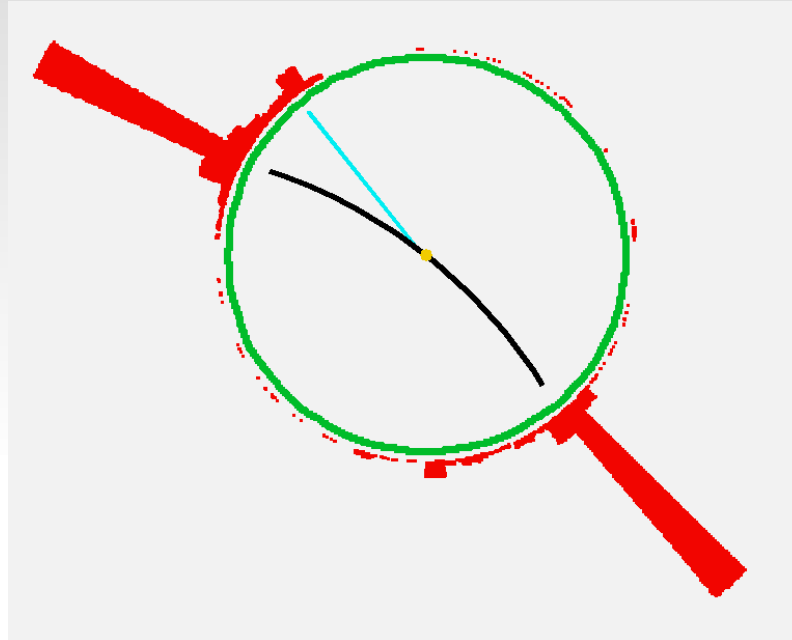
Any number of variables

Classifiers work with correlated data too

Have to take out $E \Rightarrow$ always use (E, z) plane



Charged particle ID

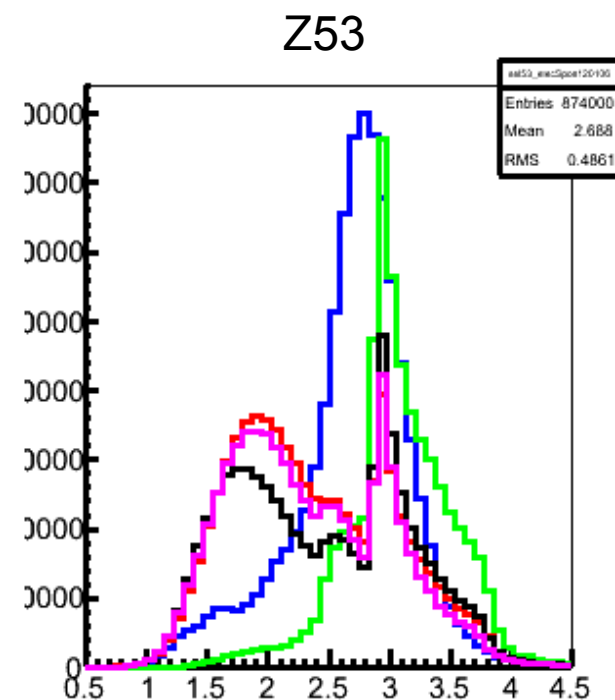
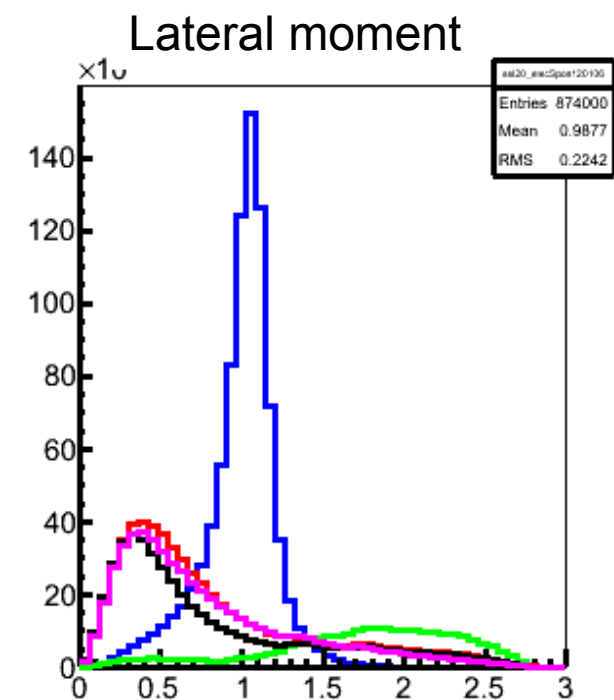
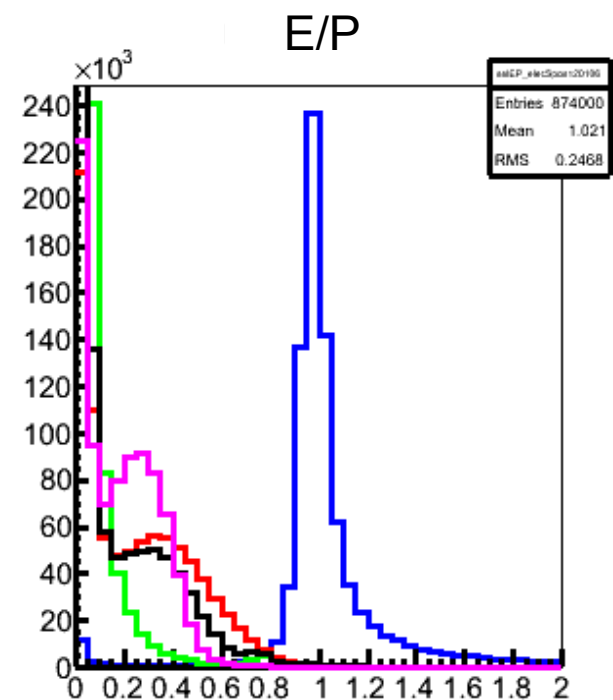
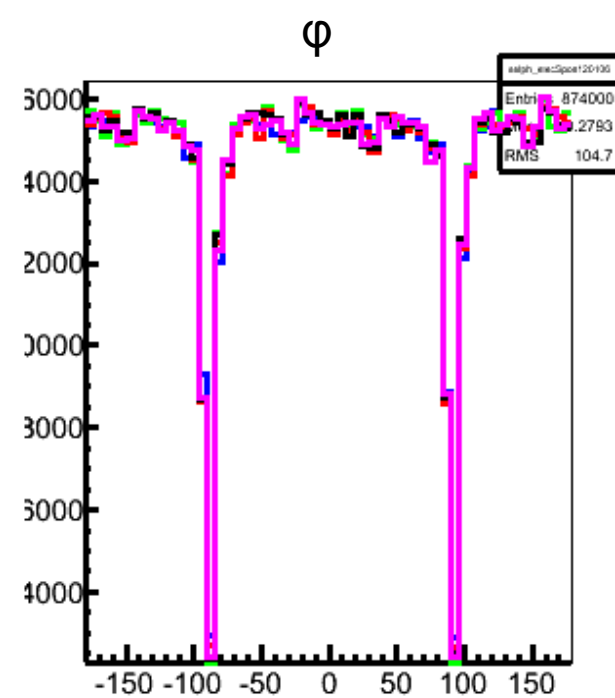
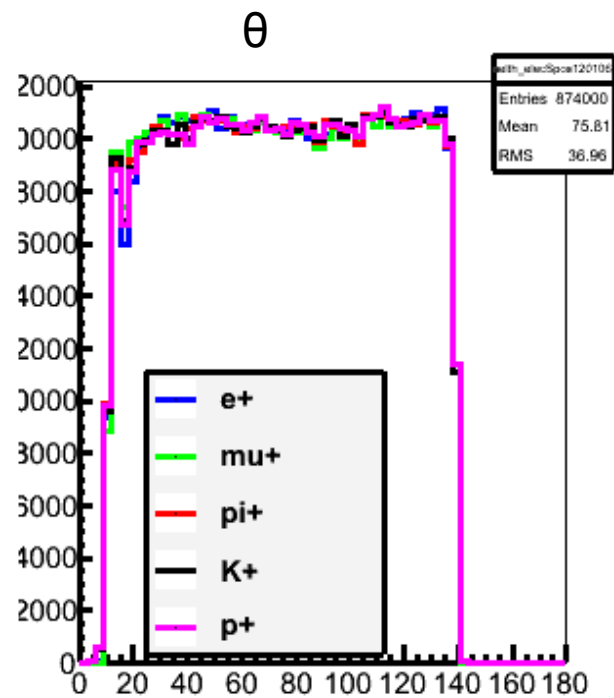
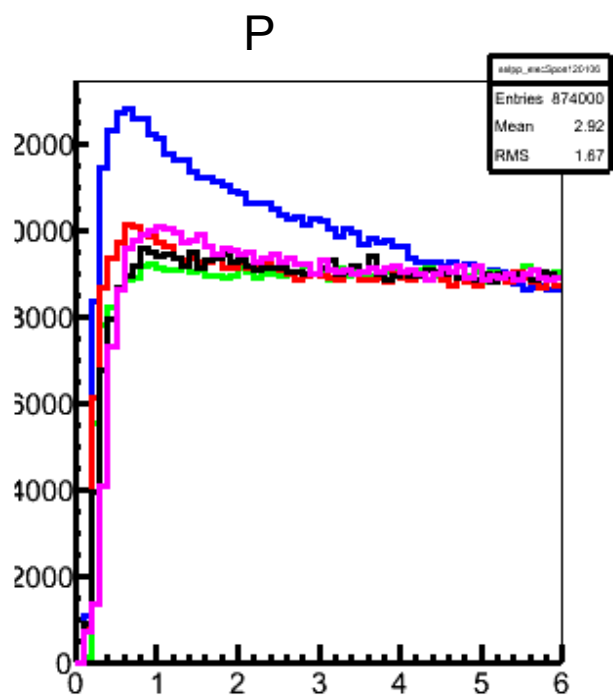


- Problem :
assign PID probabilities to tracks using EMC variables like E/P , Zernike moments

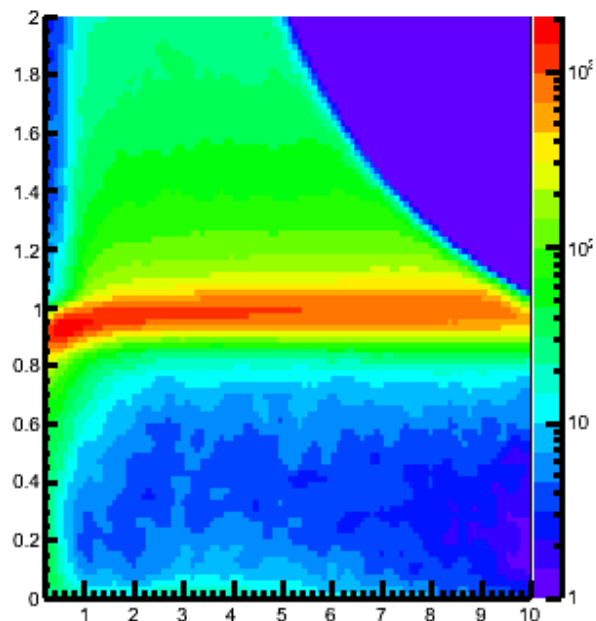
Procedure

- **Generate** e^\pm , μ^\pm , π^\pm , K^\pm , p^\pm tracks, with
 $0.2 < p < 10 \text{ GeV}/c$, $0^\circ < \varphi < 360^\circ$, $5^\circ < \Theta < 140^\circ$
- **Run reconstruction macros** μ hypothesis
- **Save** p_{reco} , φ , Θ , E_{emc} , Lateral moment, Z53, ...
- **Calculate** probabilities
- **Assign** all events using probabilities and **check** result.

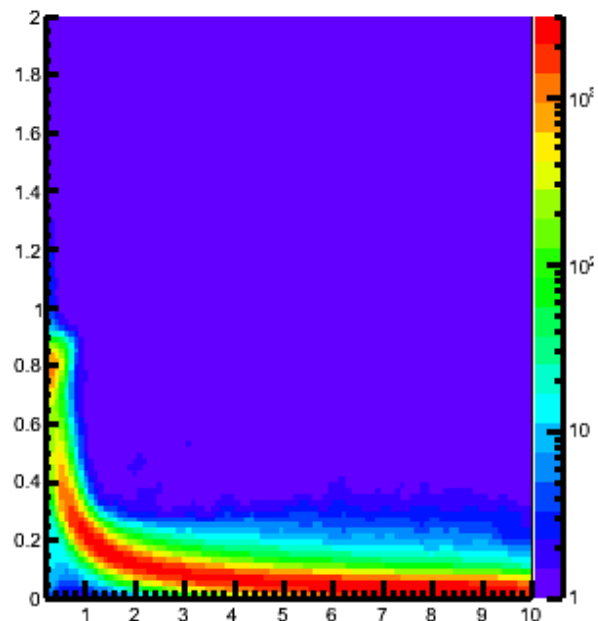




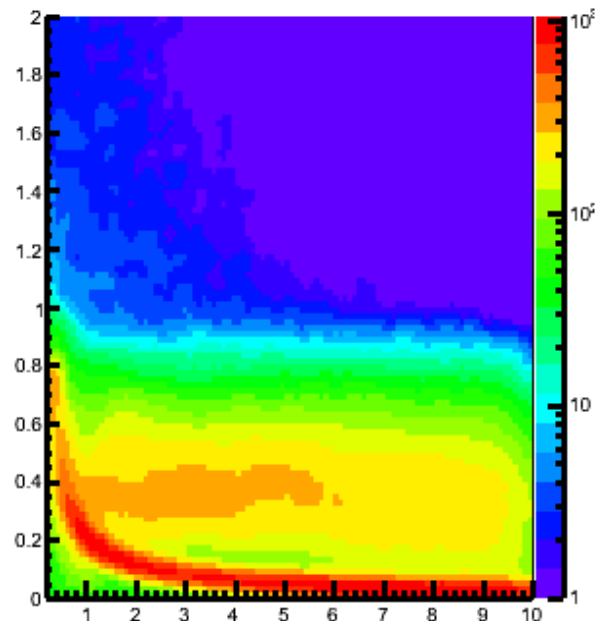
electron +



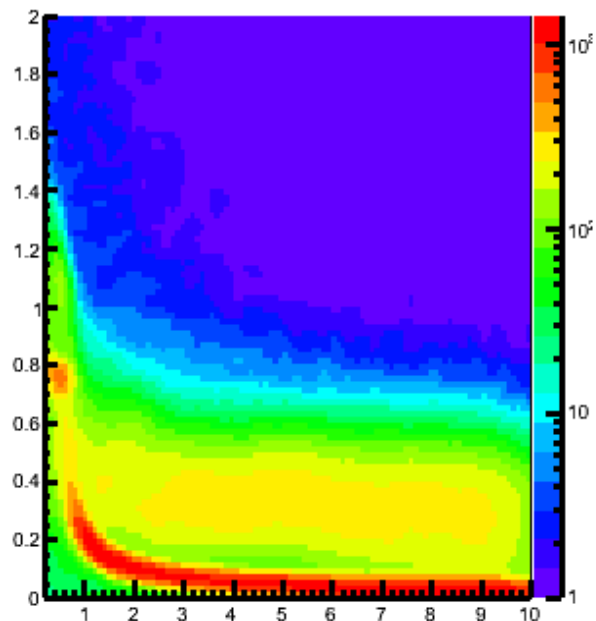
muon +



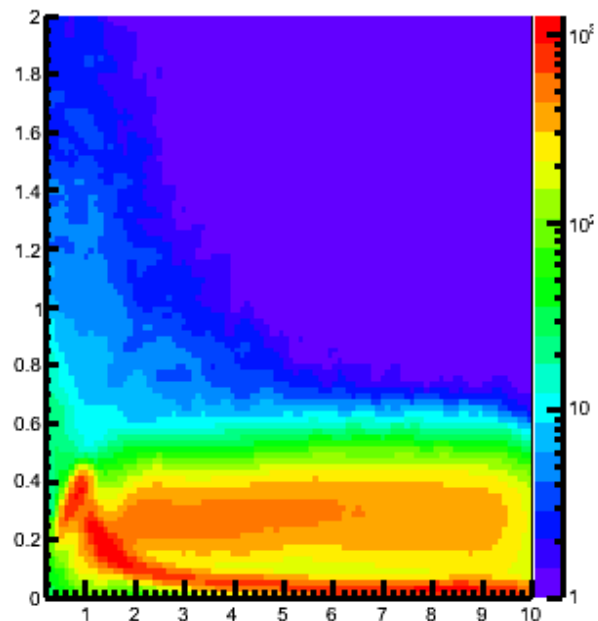
pion +



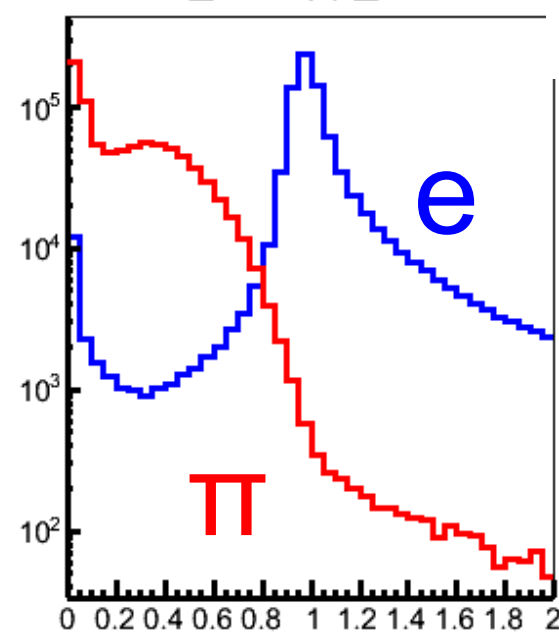
kaon +



proton

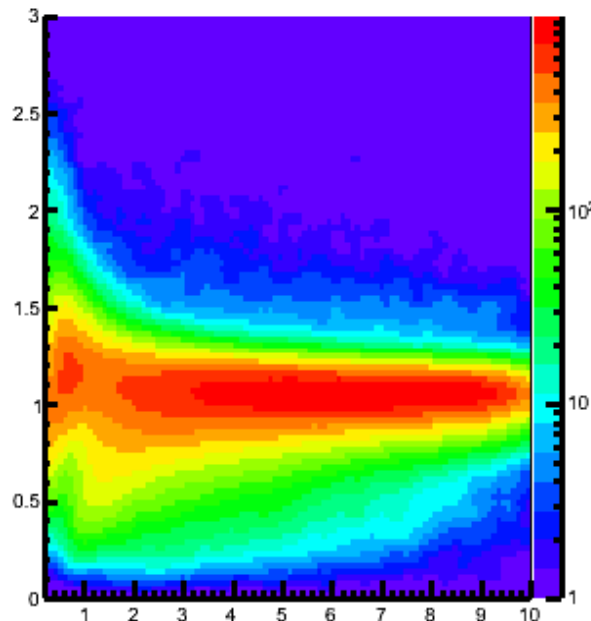


E_emc/pp_reco

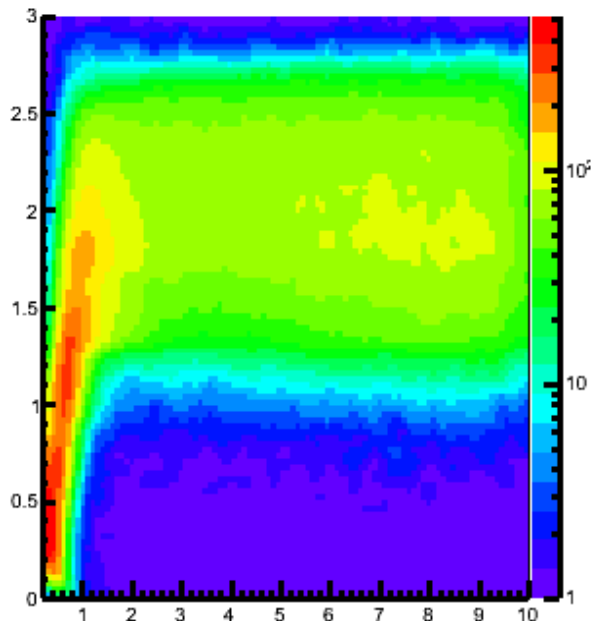


E/p

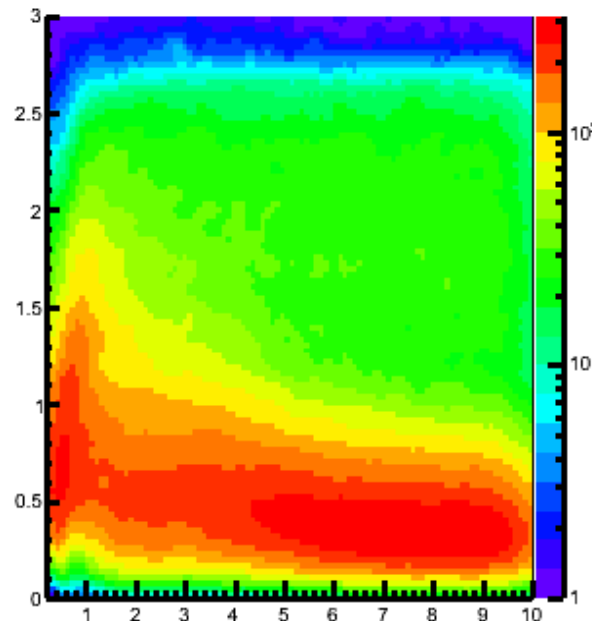
electron +



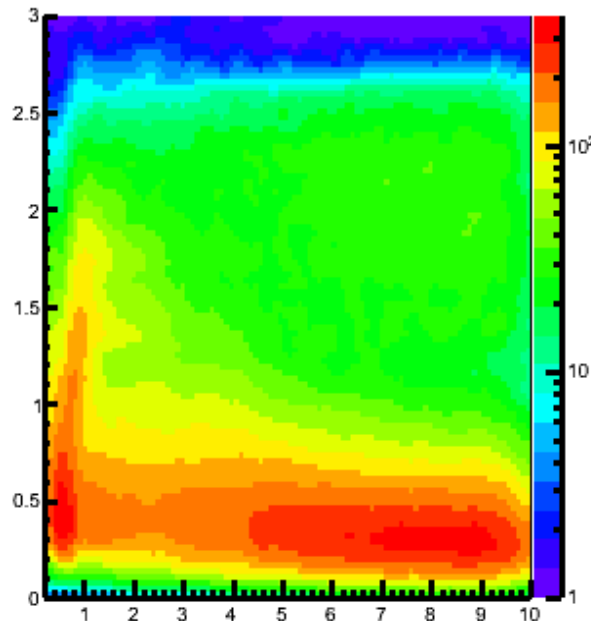
muon +



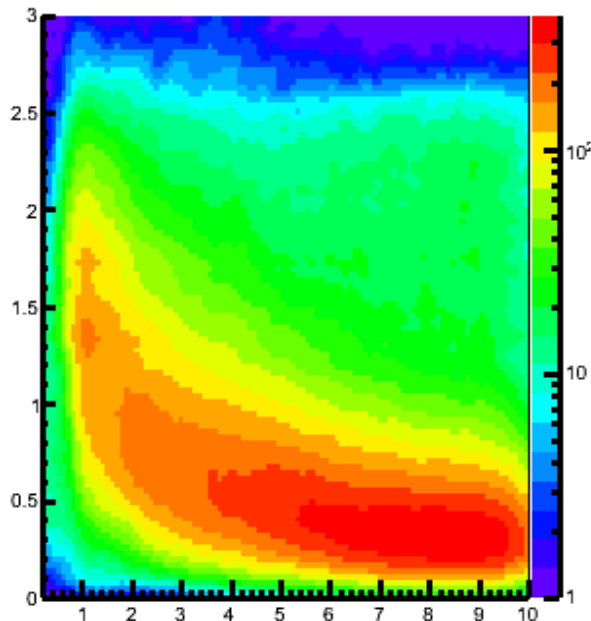
pion +



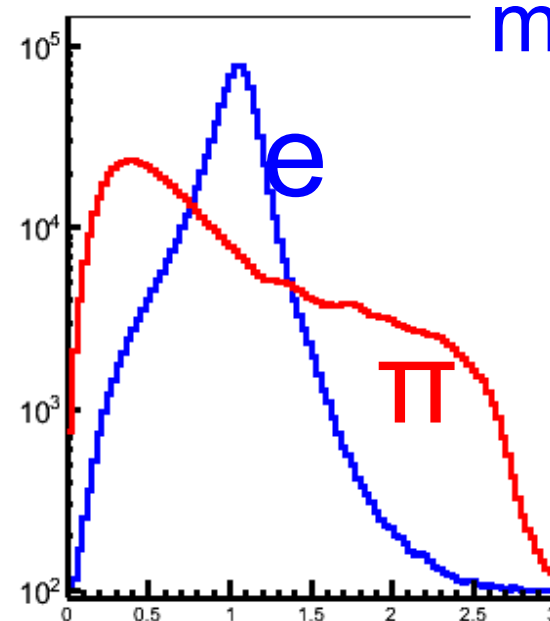
kaon +



proton

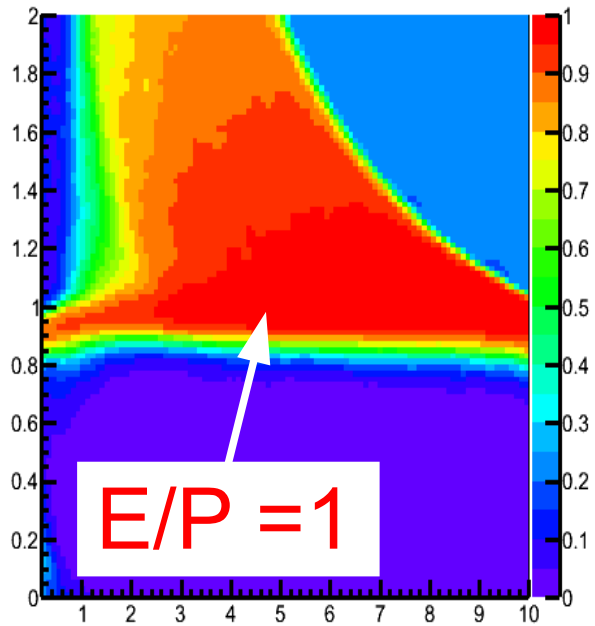


LAT e+ pi+

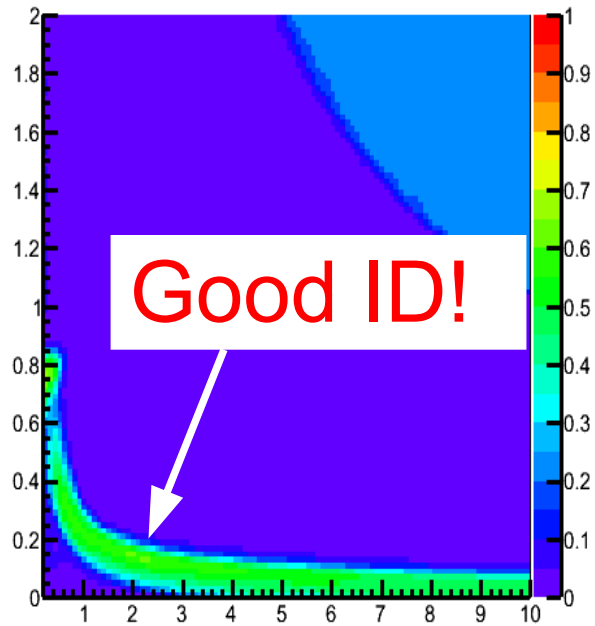


Lateral moment

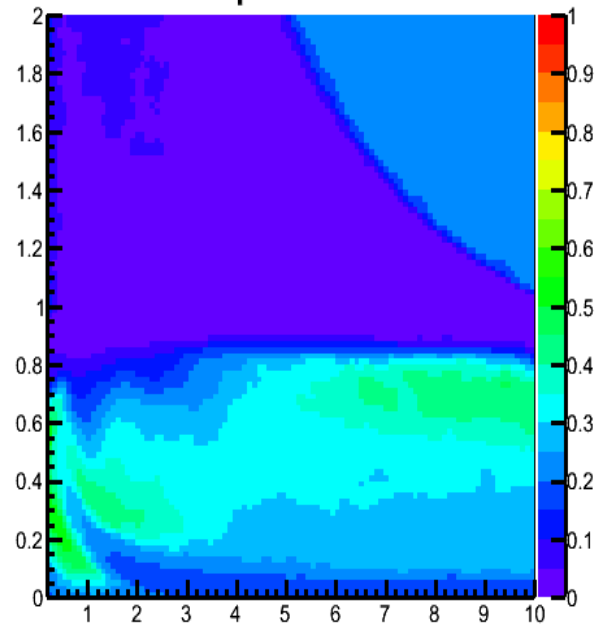
electron -



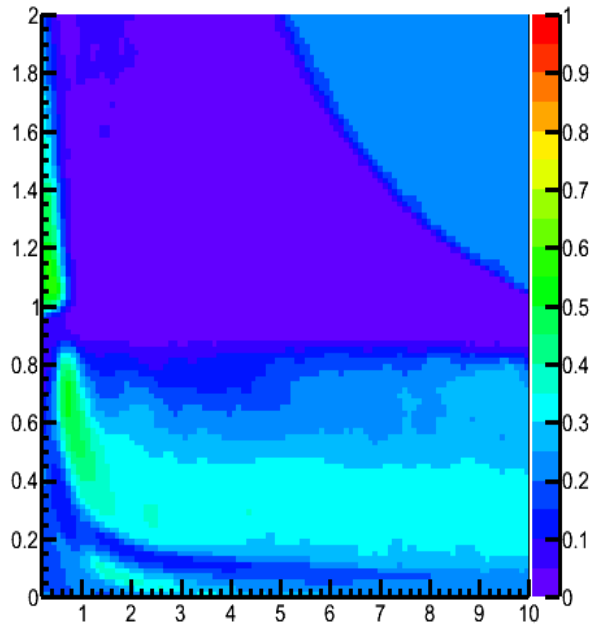
muon -



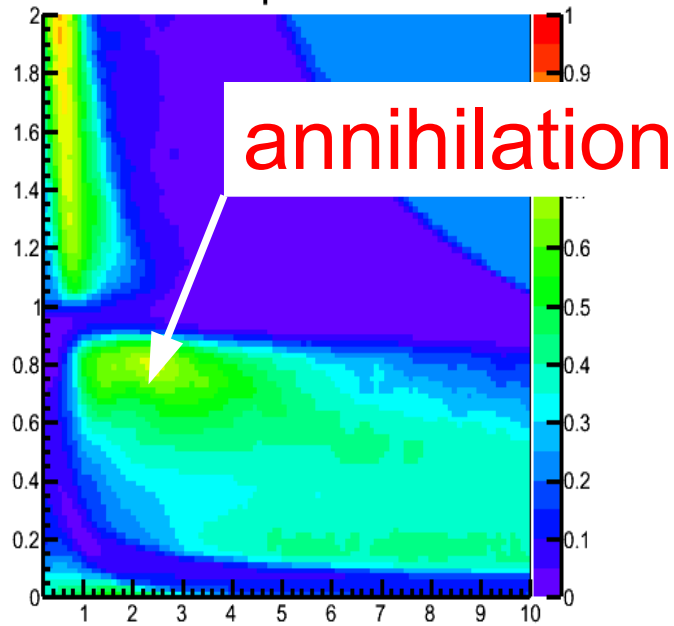
pion -



kaon -



antiproton



Probabilities

Overall efficiencies

MC Input

Reco& PID

	e	μ	π	K	p
e	95	0	2	2	2
μ	0	97	36	41	24
π	2	1	23	15	11
K	1	1	3	5	3
p	2	1	36	37	60

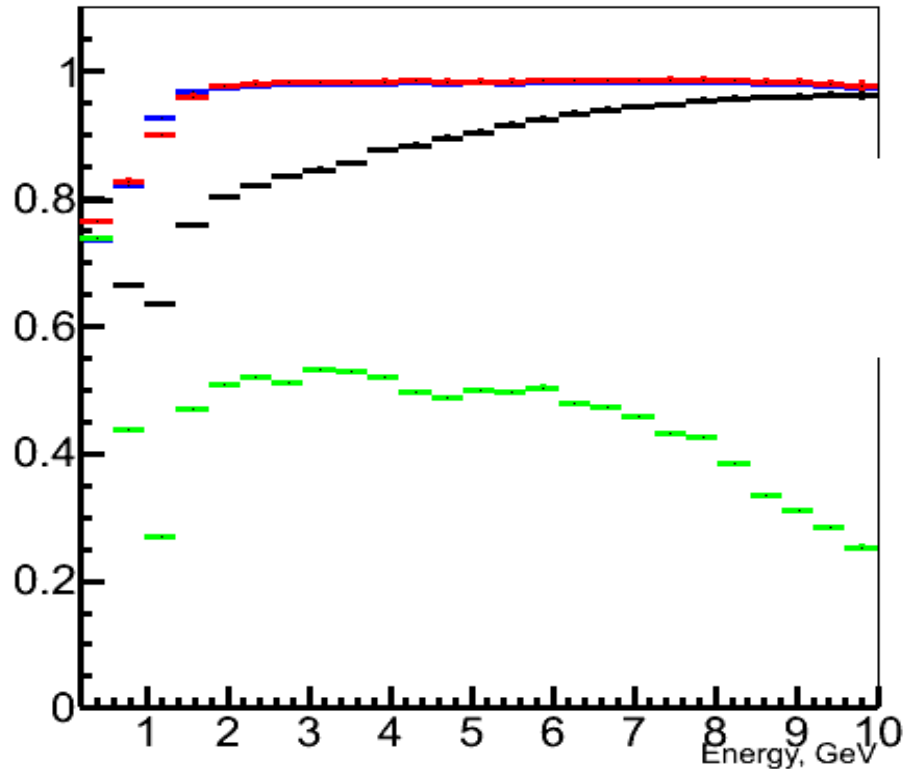
e and μ OK

μ impure

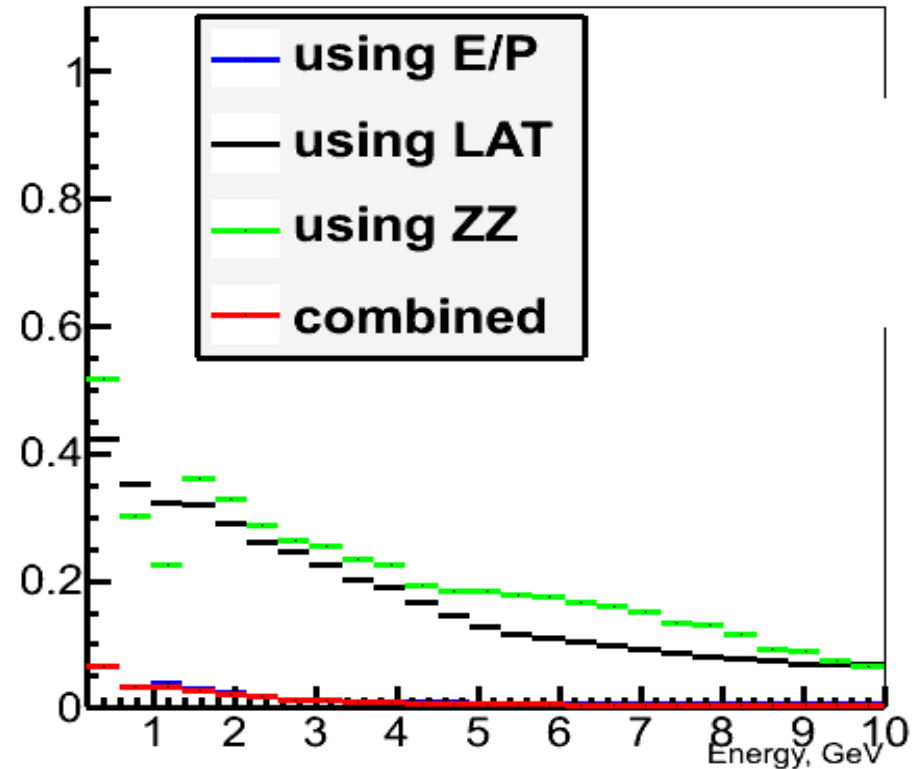
Confusing
the hadrons

Efficiency et impurity

electron efficiency-EP



electron impurity-EP

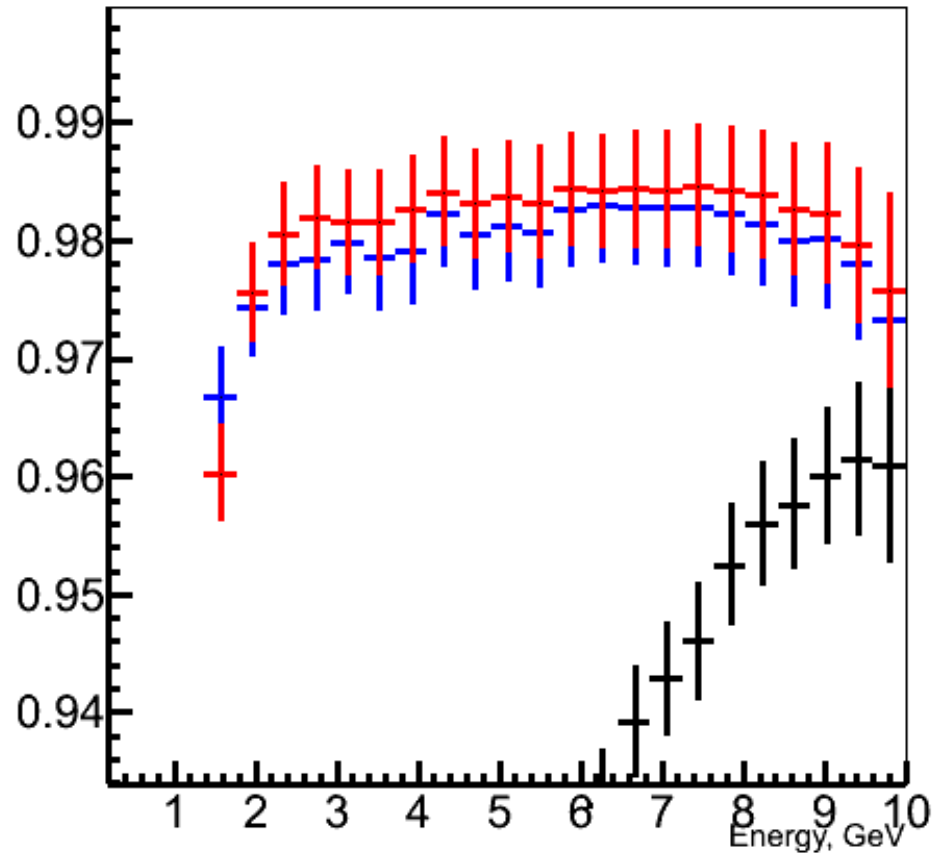


- E/P does most of the job

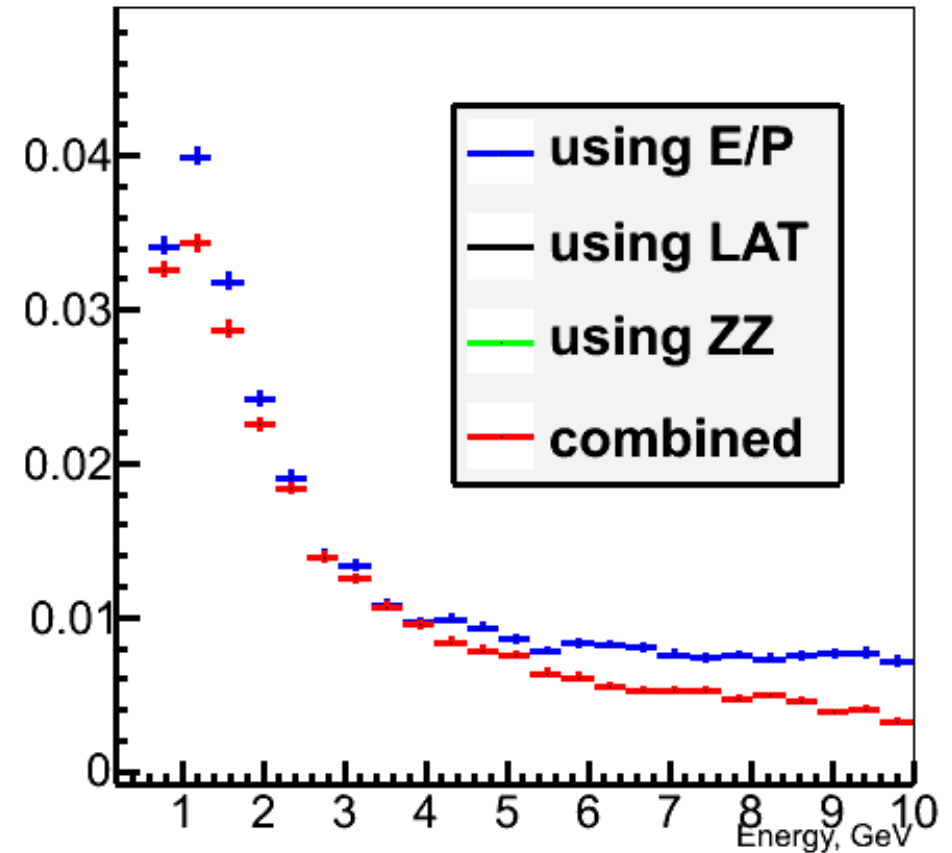
- Low E problematic

Efficiency et impurity

electron efficiency-EP

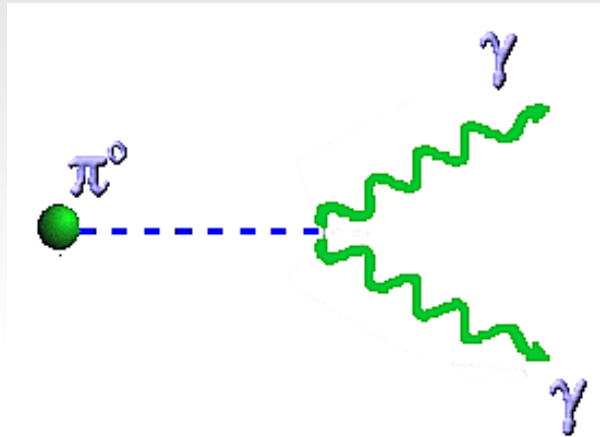


electron impurity-EP



- 98% efficiency above 2 GeV
- 1% impurity per track

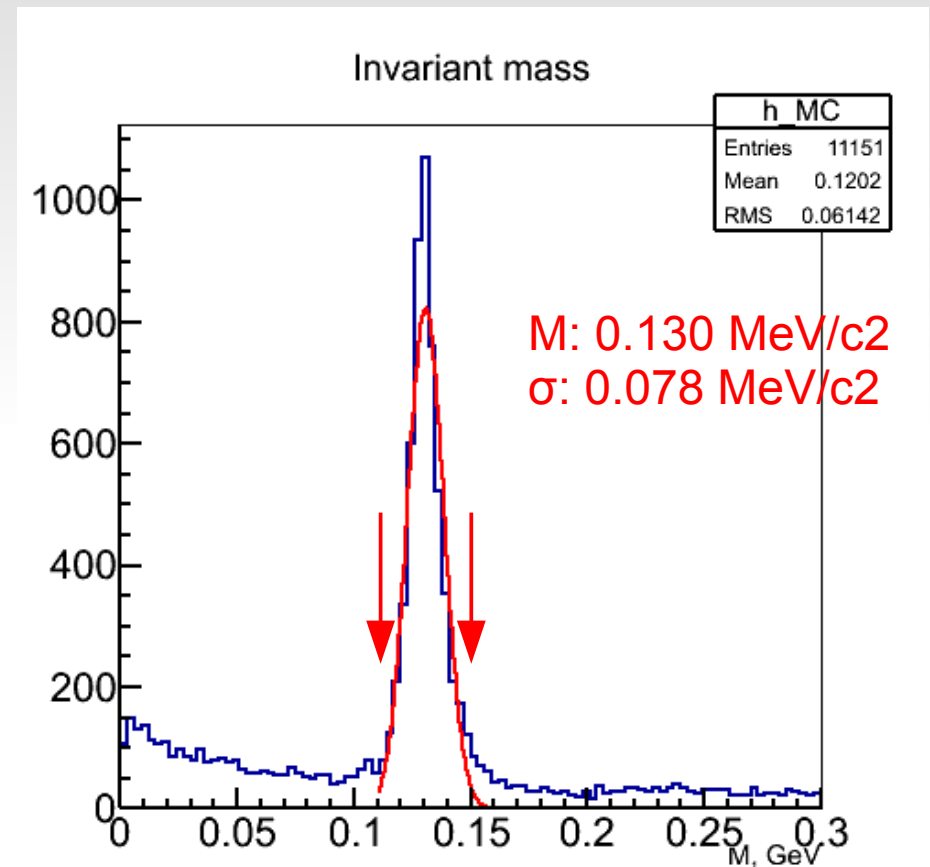
Neutral particle ID



- Problem : π^0 's with small opening angles do not resolve and can not be distinguished from γ 's

Step1 : reconstruction from two γ

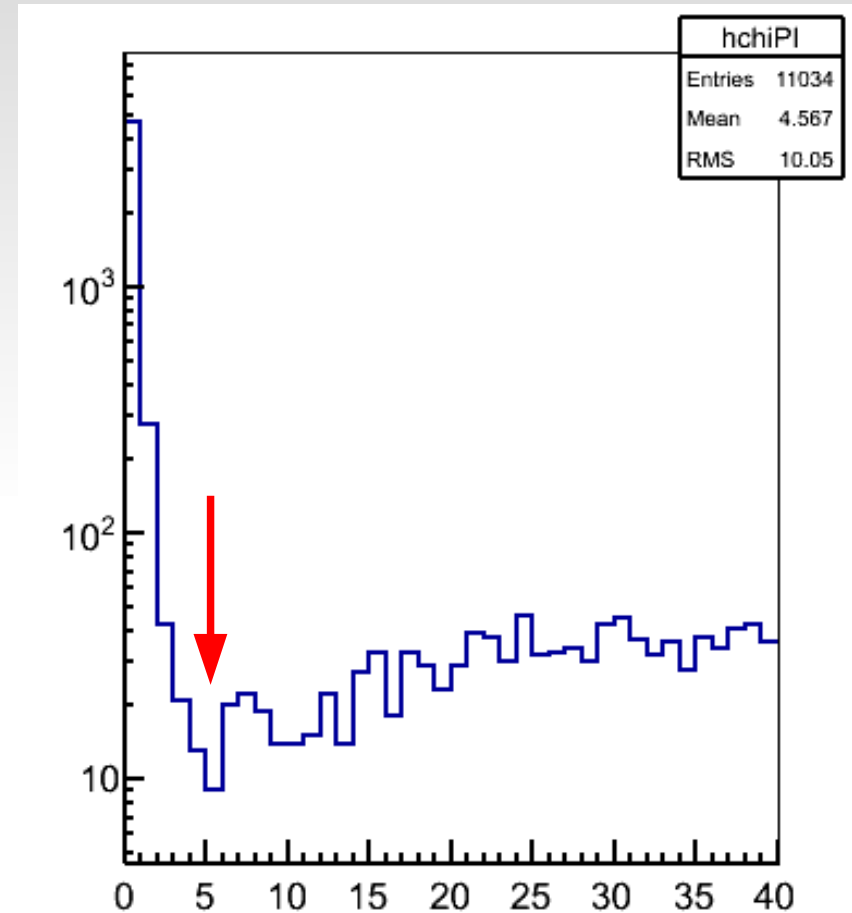
- Reconstruct π^0 's from two bumps using the information available in **PndEmcBump**
- Cut on invariant mass $0.11 < M_{\pi^0} < 0.15 \text{ GeV}$



Correlation
MC π^0 -
reconstructed
 π^0

- Successful reconstruction if $\chi^2 = d\theta^2 + d\phi^2 < 5 \text{ deg}^2$ when compared to MC values

Overall efficiency : About 50%

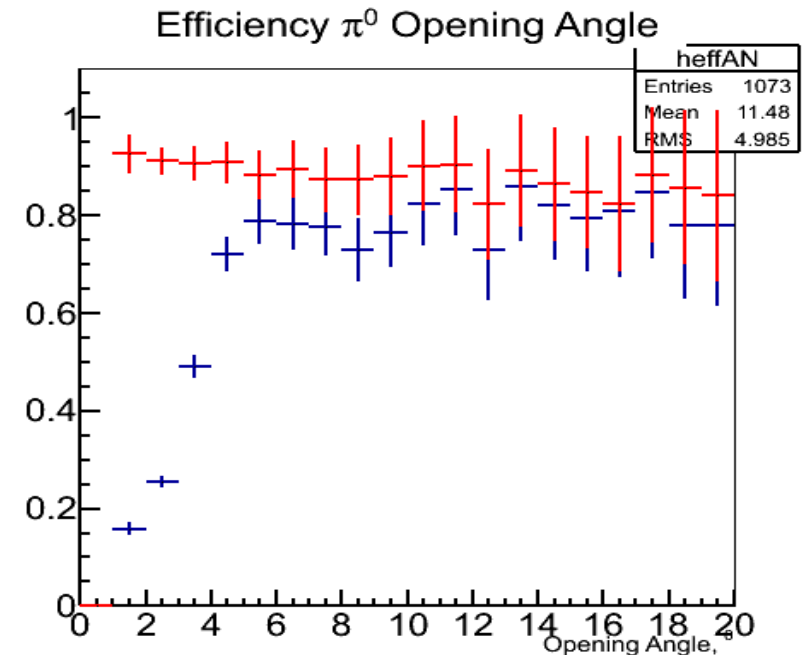
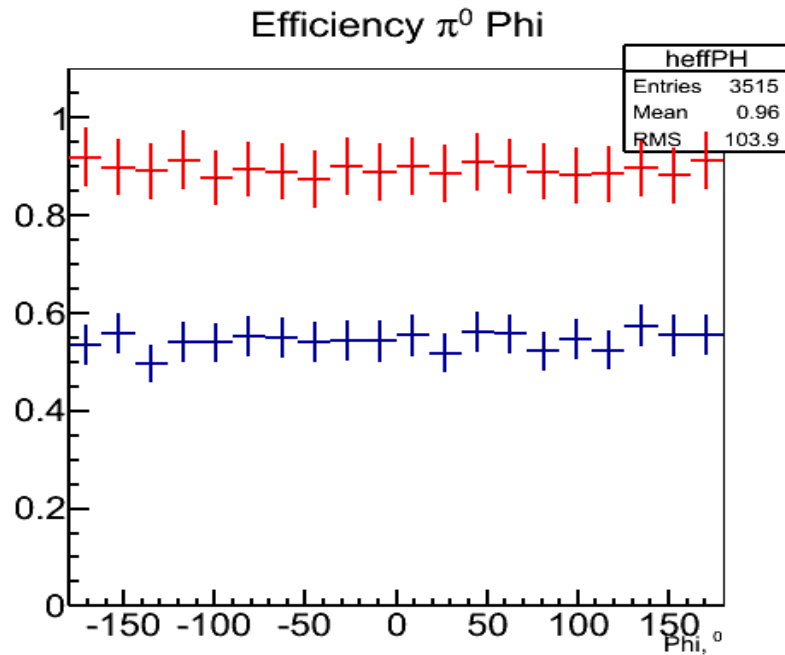
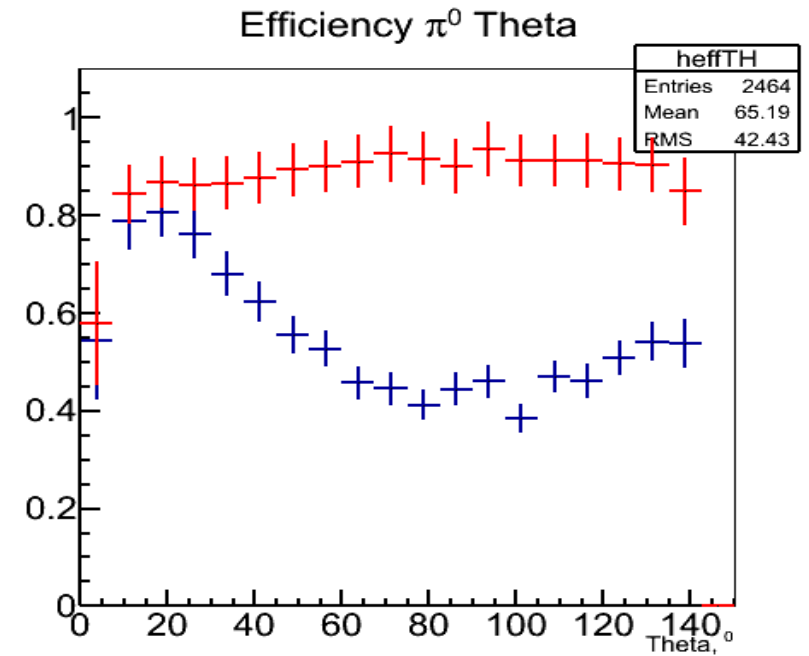
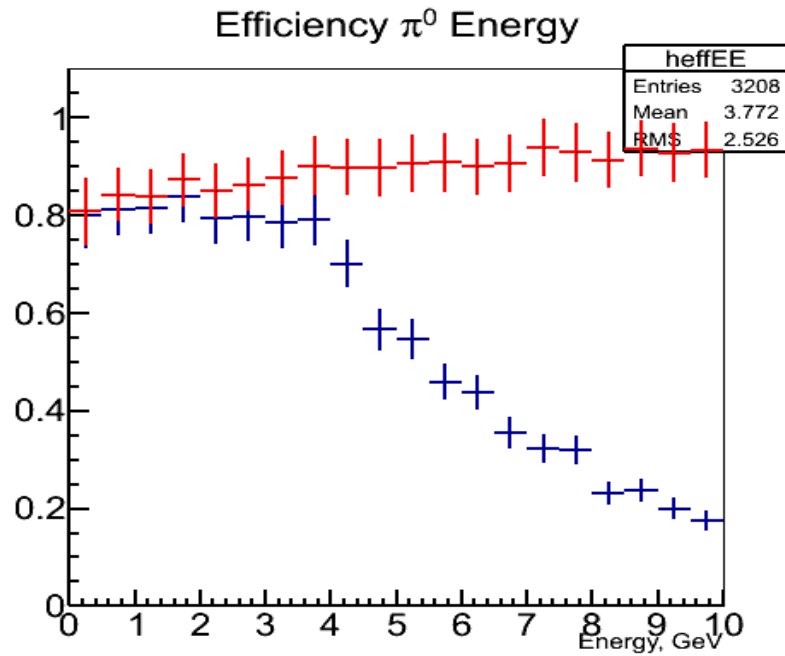


Reconstruction efficiency

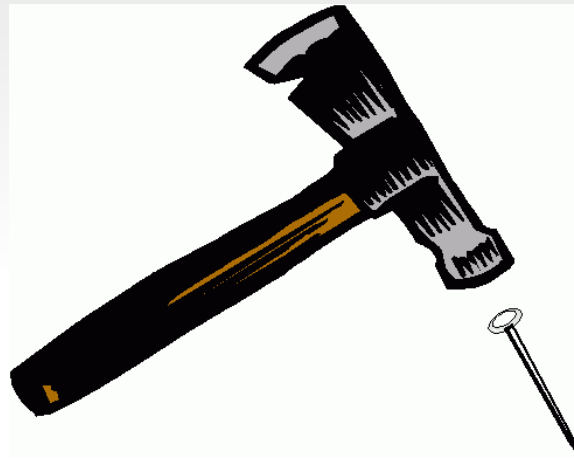
Theoretical efficiency when all unused clusters are taken as π^0 :

About **85%**

Can we recuperate these, without admitting too much gammas?



Step 2 : recuperate unsplit clusters



- Construct **Bayesian classifiers** using the Zernike moments

Cluster Moments

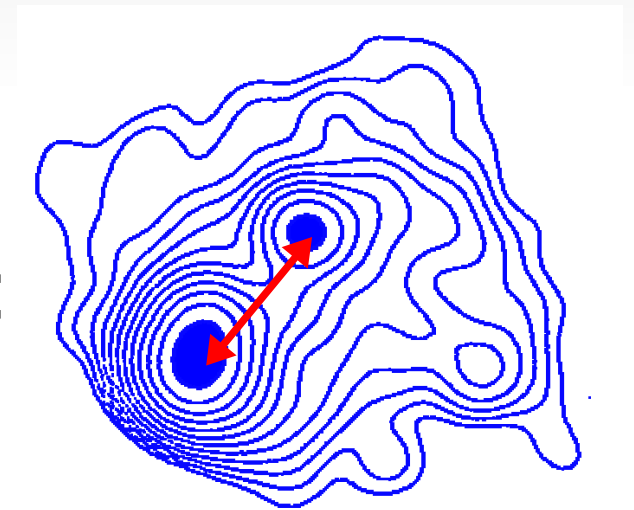
- Two extra "moments" are defined :

- Shower mass : $(\sum E_i)^2 - (\sum p_i)^2$

- Correlated maximum separation :

$$\max [E_i E_j (d\theta_{ij}^2 + d\phi_{ij}^2)]$$

(where the indices run over the cluster hits)



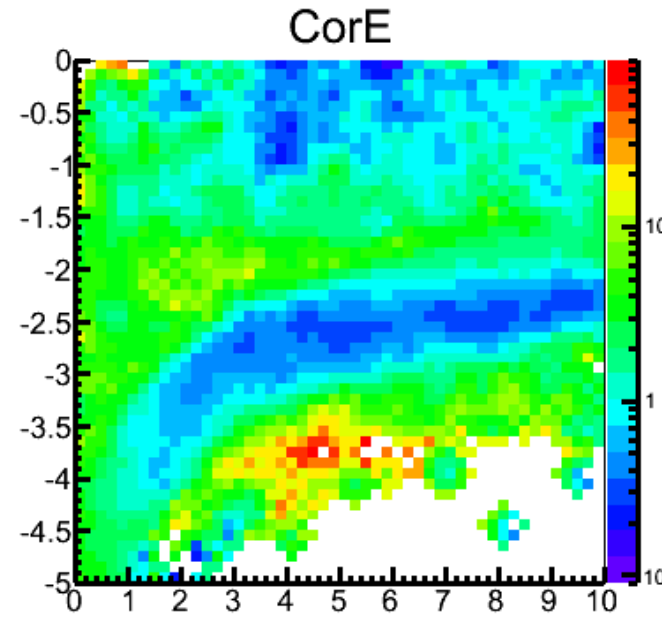
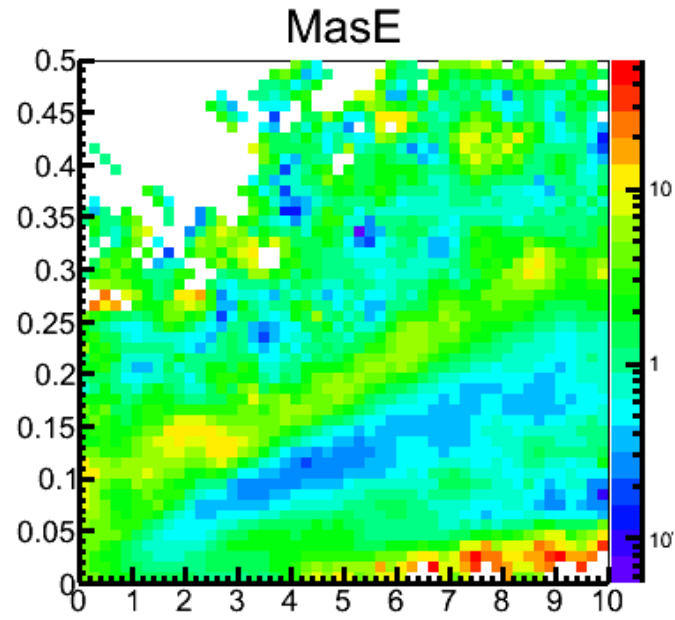
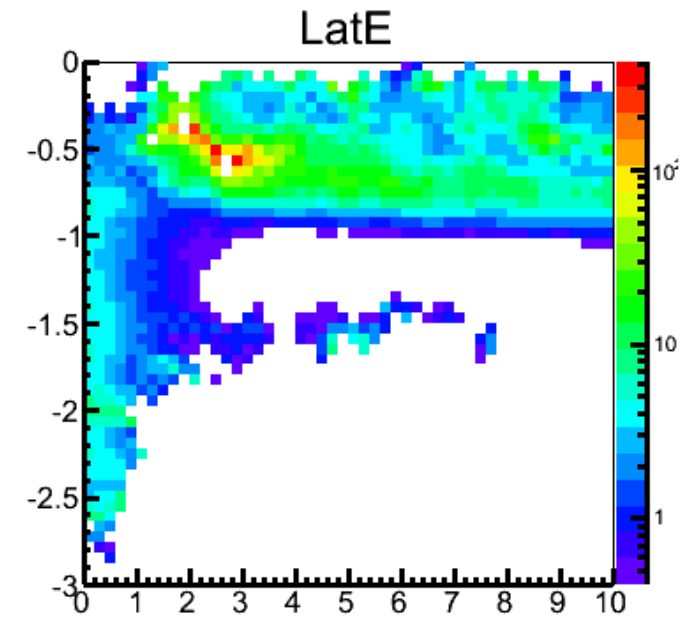
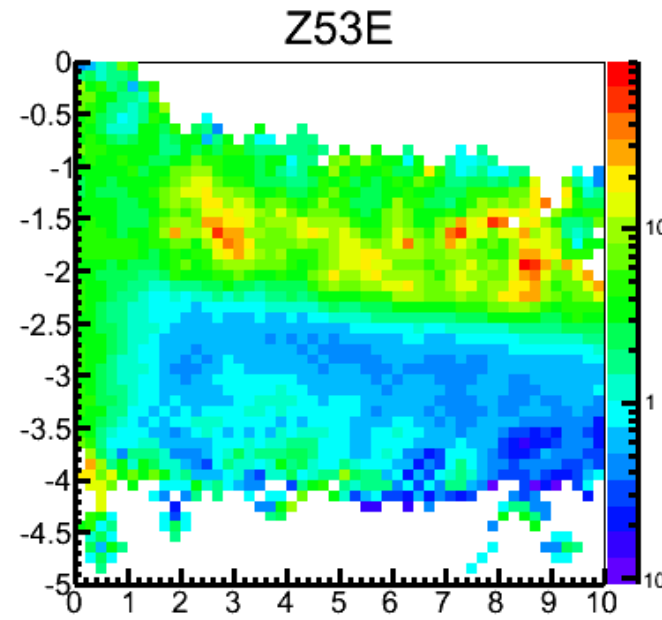
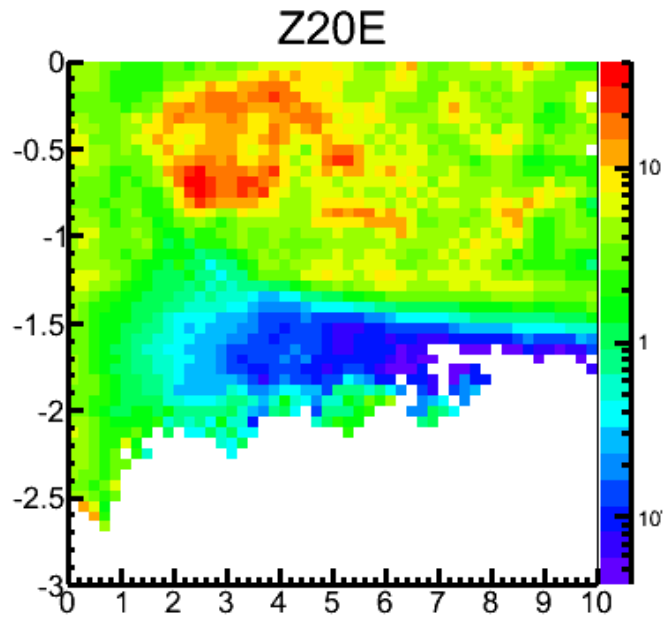
Sixteen moments tested

Z00	Z20	Z40	Z11
Z31	Z51	Z22	Z42
Z62	Z33	Z53	Z44
Z64	LatMom	ShowerMass	CorMax

- Not all moments are efficient classifiers
- Many are correlated between them

Construction of a "Naive" Bayesian classifier

- Procedure :
 - Create 2d-histos with ClusterEnergy E versus moment z for γ and π°
 - $\text{Factor}(E,z) = N(E,z | \pi^\circ) / N(E,z | \gamma)$
 - classifier = $\log(\text{factor1}) + \log(\text{factor2}) + \dots$



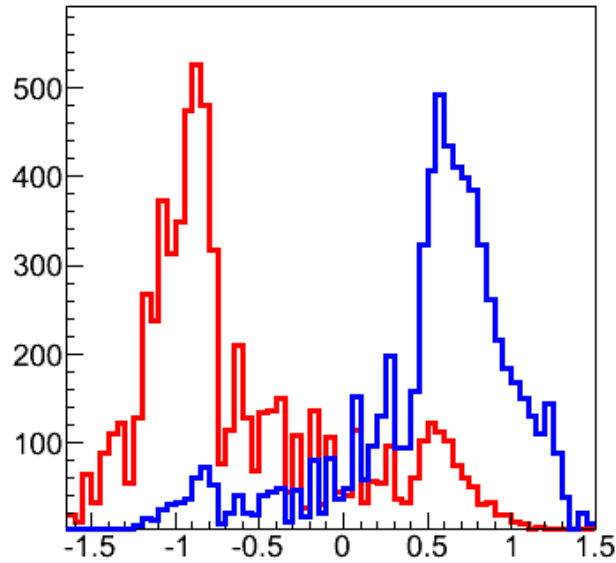
Factor (E,z)

Blue : more γ than π^0

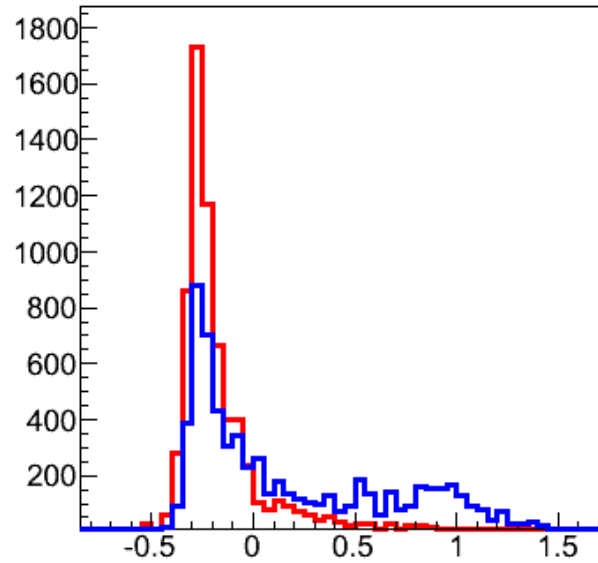
Red : more π^0 than γ

Green : about equal

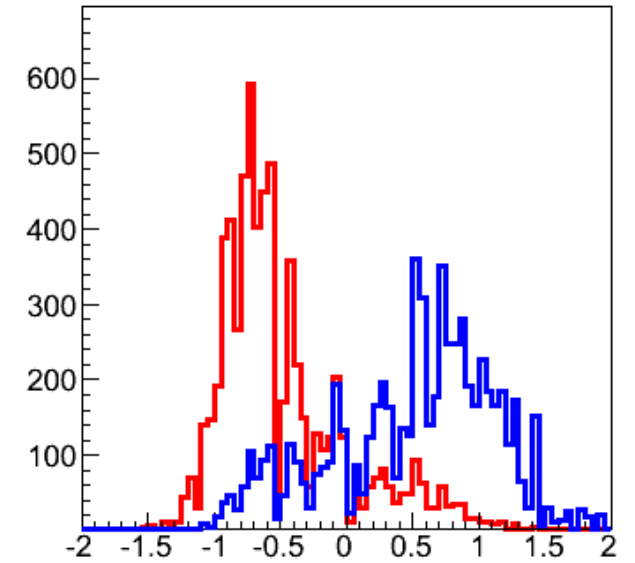
Z20



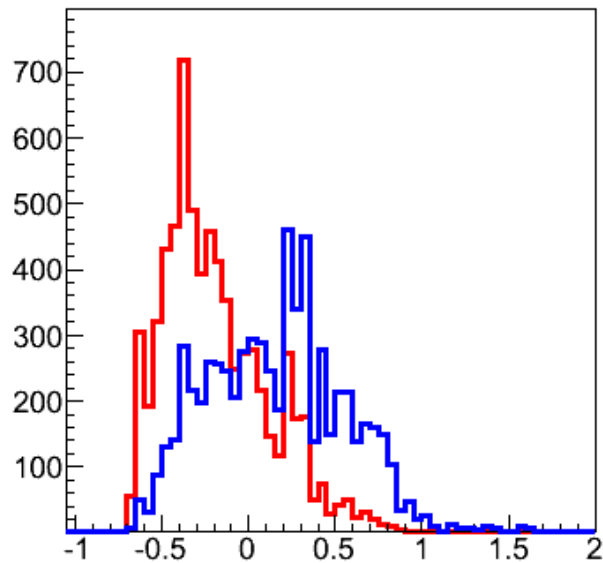
Z53



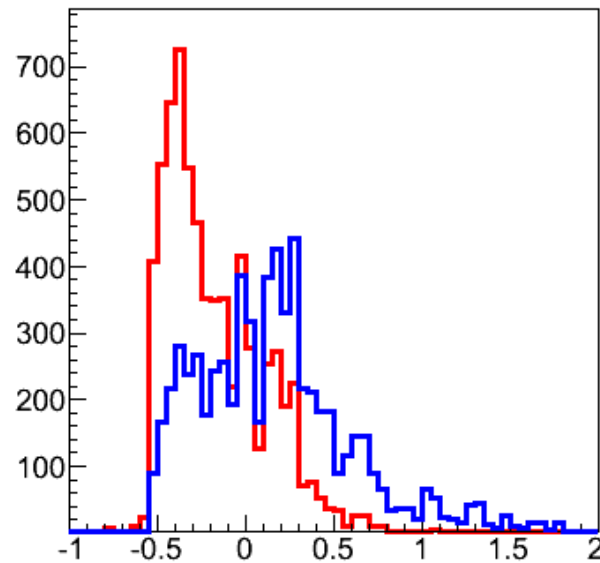
Lat



Mas



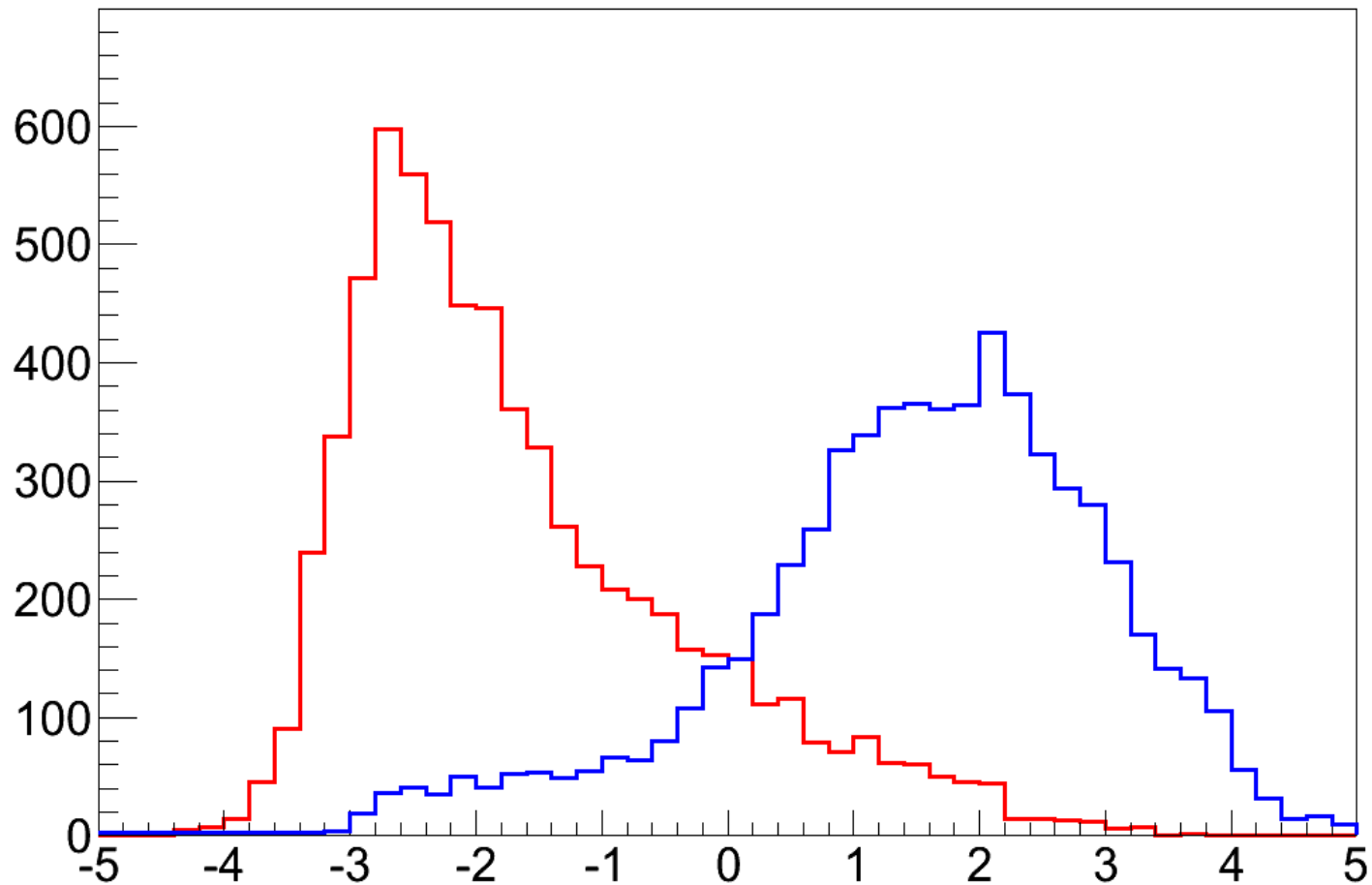
Cor



events as function
of log(factor)

Blue : π^0
Red : γ

Bayesian classifier = $\sum \log(\text{factor})$



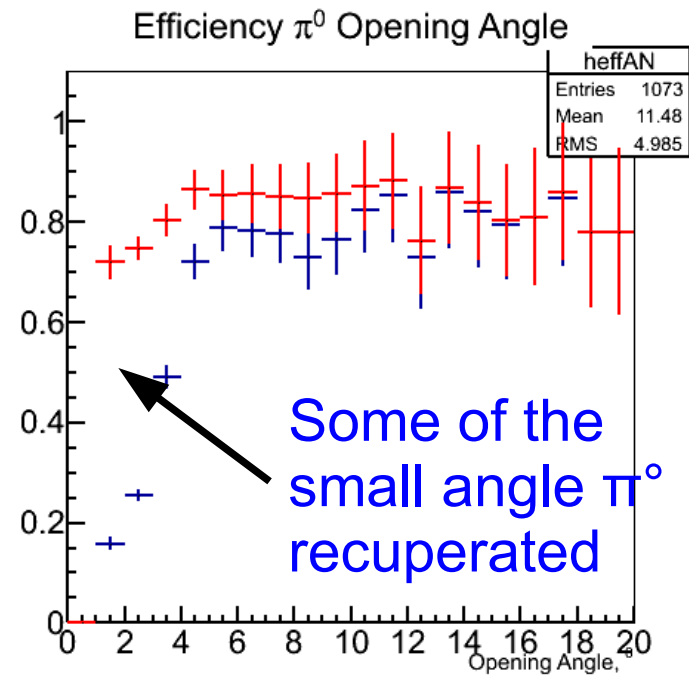
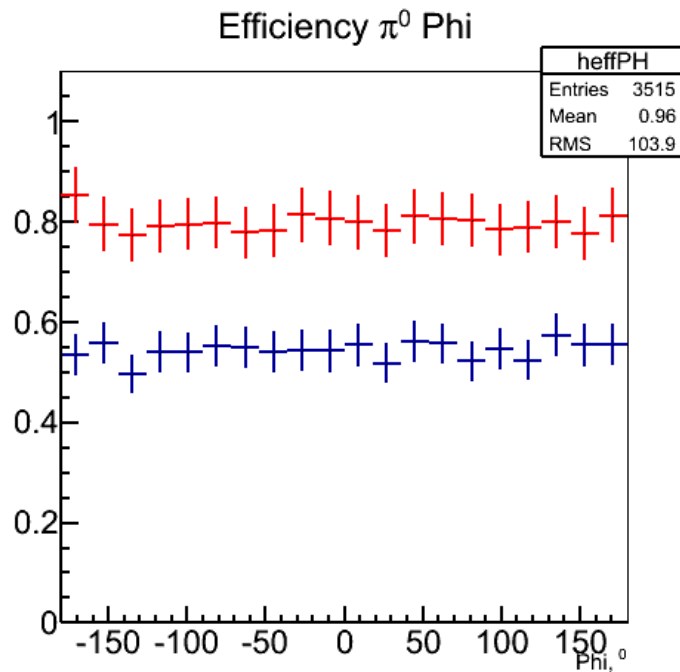
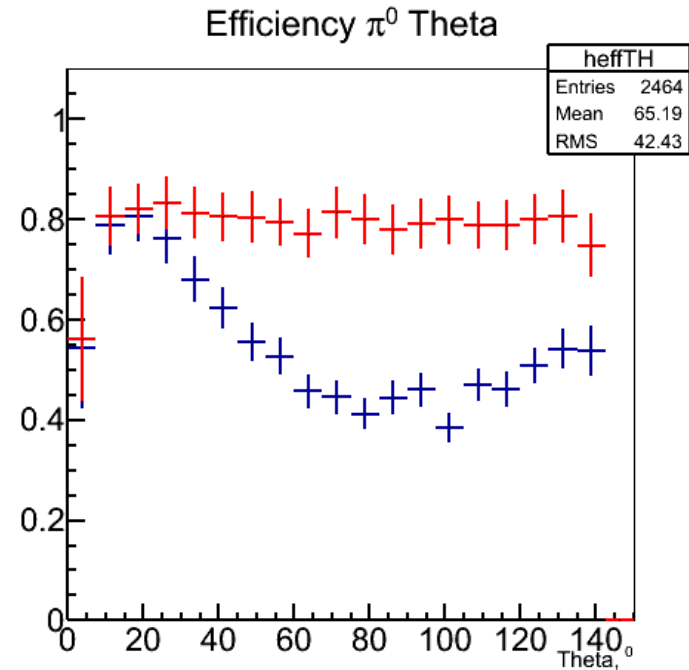
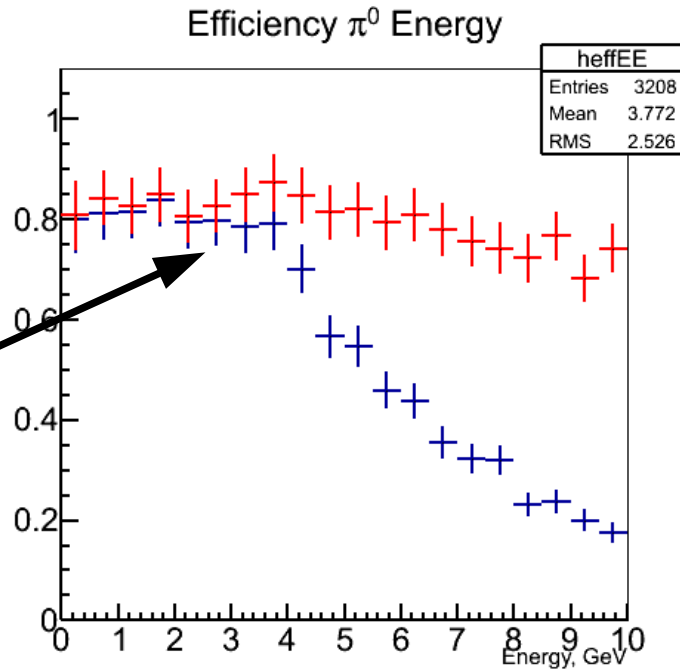
events
as function of
Bayesian
classifier

Blue : π^0
Red : γ

Efficiency π^0 :
five moments

Not needed
below 4GeV/c

80% total
efficiency

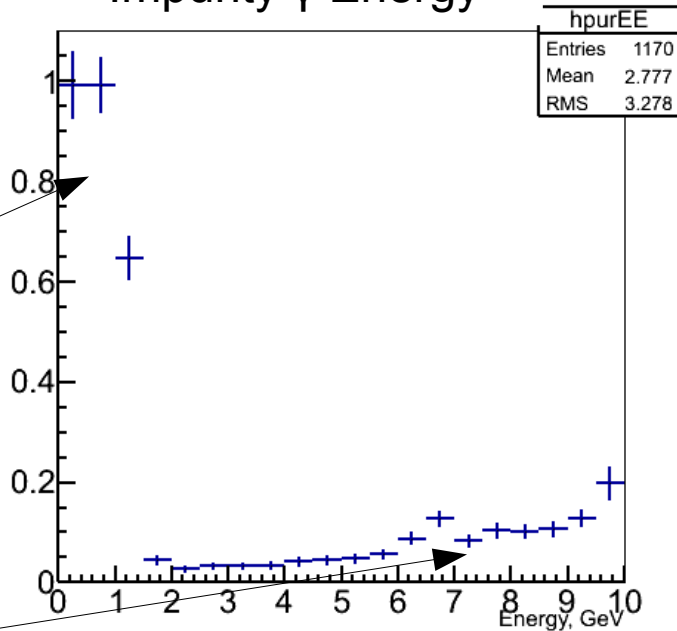


Impurity from gammas

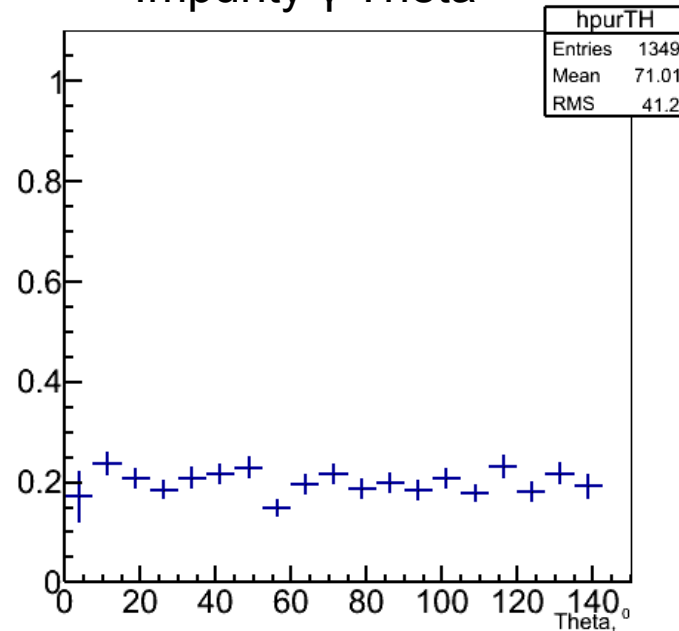
Harmful below 2 GeV/c

5-20% above 2 GeV/c

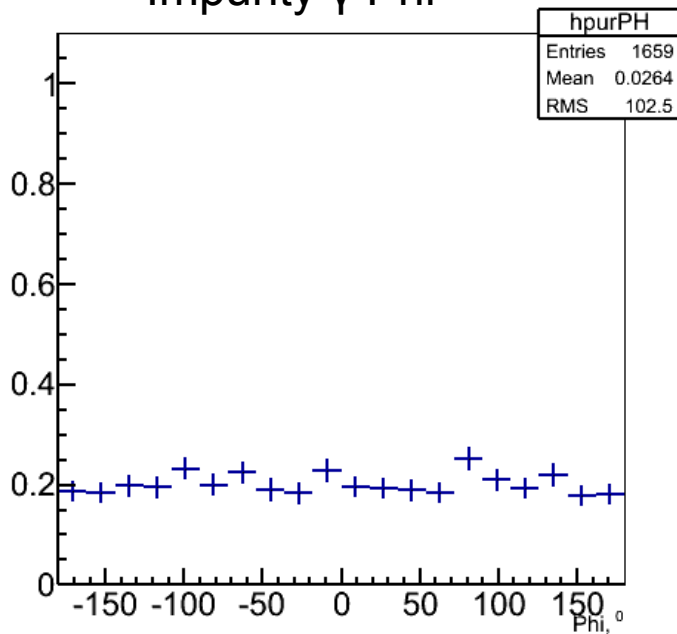
Impurity γ Energy



Impurity γ Theta



Impurity γ Phi



Fraction of γ accepted as π^0

Conclusions

- Charged particle ID:
 - Bayesian classifiers combine E/P , LatMom, Z53
 - 98% efficiency for e and μ , above 2 GeV/c
 - 1% impurity for π , above 3 GeV/c
- π^0 reconstruction using bumps :
 - loss due to unresolved clusters, can be recuperated with cluster moments
 - price to pay : 5-20% of the single γ pass the test

Thank you for
your attention !



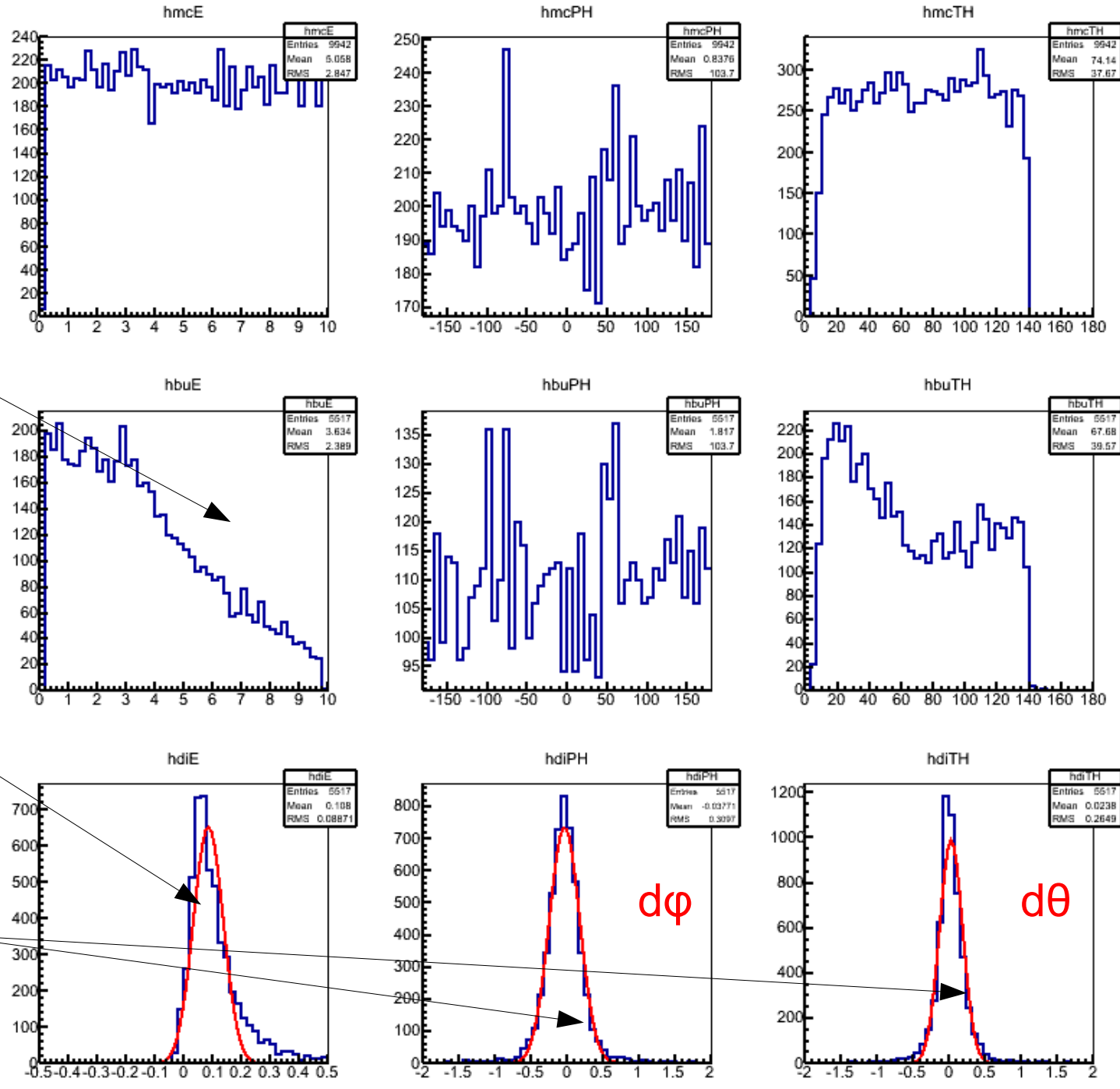
Correlation
MC π^0 -
reconstructed
 π^0

Losses !

10K
events

Using
Bump
energies

$\chi^2 = d\theta^2 + d\phi^2 < 5$



MC

Reco

Residu