The Matrix Element Method and MadWeight

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J. Alwall, A. Freytas, OM: PRD83:074010 P.Artoisenet, V.Lemaître, F. Maltoni, OM: JHEP 1012:068

## Motivations



- Both LHC and Tevatron search for Higgs and NP !
  - How to identify new particles?
  - How to measure particle properties?
- Especially difficult in presence of missing Energy
- Is there a way to optimise the information which can be extracted from a event sample?



Example 2:



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Example 2:



#### Few

assumptions



assumptions

- Missing transverse momentum
- M\_eff, H\_T
- s Hat Min
- M\_T
- M\_TGEN
- M\_T2 / M\_CT
- M\_T2 (with "kinks")
- M\_T2 / M\_CT ( parallel / perp )
- M\_T2 / M\_CT ( "sub-system" )
- "Polynomial" constraints
- Multi-event polynomial constraints
- Whole dataset variables
- Cross section
- Max Likelihood / Matrix Element

Slíde from Lester: arXív:1004.2732

#### Vague

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#### Fragile

## Outline



- Introduction to Matrix Element re-weighting
- Examples of studies / investigations
  - mass determination : smuon pair production
  - discriminating Hypothesis
  - □ ISR effects: pp > H > W+ W-
  - $\square$  DMEM:  $m_{tt}$  in fully leptonic channel
- Conclusions

## fn's Matrix Element weight



 $\square$  Associate to each experimental event characterised by  $p^{vis}$ , the probability  $\mathcal{P}(p^{vis}|\alpha)$  to be produced and observed following a theoretical assumption  $\alpha$ 

## finis Matrix Element weight

C

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- - $\square |M_{\alpha}(\mathbf{p})|^2 \text{ is the squared matrix element}$  $= W(\mathbf{p}, \mathbf{p}^{vis}) \text{ is the squared matrix element}$
  - $\square W({m p},{m p}^{vis})$  is the transfer function

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- □ Associate to each experimental event characterised by  $p^{vis}$ , the probability  $\mathcal{P}(p^{vis}|\alpha)$ to be produced and observed following a theoretical assumption  $\alpha$  $\mathcal{P}(p^{vis}|\alpha) = \int d\Phi dx_1 dx_2 |M_{\alpha}(p)|^2 W(p, p^{vis})$ 
  - $\square |M_{\alpha}(\boldsymbol{p})|^2$  is the squared matrix element
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  - $\Box \int d\Phi dx_1 dx_2$  is the phase-space integral

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 $\mathcal{P}(\boldsymbol{p}^{vis}|\alpha) = \frac{1}{\sigma_{\alpha}^{vis}} \int d\Phi dx_1 dx_2 |M_{\alpha}(\boldsymbol{p})|^2 W(\boldsymbol{p}, \boldsymbol{p}^{vis})$ 

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- $\Box \int d\Phi dx_1 dx_2$  is the phase-space integral
- $\Box \ \sigma_{\alpha}^{vis}$  is the cross-section (after cuts)

fn's Matrix Element Method



Most common and Important use is to combine those in a Likelihood

$$L(\alpha) = \prod_{i=1}^{N} \mathcal{P}(\boldsymbol{p}_{i}^{vis} | \alpha)$$

fn's Matrix Element Method

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CDF Run II Preliminary 5.6 fb<sup>-1</sup>



Semí-leptonic decay $m_{top} = 173.0 \pm 1.2 {
m GeV}$ 

# **fnscritics of the method**



- The Likelihood methods builds the BEST discriminating variable
- Fully Model dependent
- Transfer Function approximation
  - □ Factorize for each parton
  - Not valid for hard radiation
- D Pure LO approximation
- Strong sensitivity in analysis cut
- $\Box$  Computing time ( $N_{event} * N_{th}$  integrals)



#### B

#### How to evaluate those weights?

 $\mathcal{P}(\boldsymbol{p}^{vis}|\alpha) = \frac{1}{\sigma_{\alpha}} \int d\Phi dx_1 dx_2 |M_{\alpha}(\boldsymbol{p})|^2 W(\boldsymbol{p}, \boldsymbol{p}^{vis})$ 

## Matrix Element weight

How to evaluate those weights?

 $\mathcal{P}(\boldsymbol{p}^{vis}|\alpha) = \frac{1}{\sigma_{\alpha}} \int d\Phi dx_1 dx_2 |M_{\alpha}(\boldsymbol{p})|^2 (W(\boldsymbol{p}, \boldsymbol{p}^{vis}))$ 

Fit from MC tuned to the detector resolution 



has it's own Transfer functions  $W(\boldsymbol{x}, \boldsymbol{y}) \approx \prod_{i=1}^{\infty} \frac{1}{\sqrt{2\pi\sigma_i}} e^{-\frac{(x_i - y_i)^2}{2\sigma_i^2}}$ 

Forbíds any addítíonal jets and therefore NLO.

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How to evaluate those weights?

- $\mathcal{P}(\boldsymbol{p}^{vis}|\alpha) = \frac{1}{\sigma_{\alpha}} \int d\Phi dx_1 dx_2 \mathcal{M}_{\alpha}(\boldsymbol{p})^2 \mathcal{W}(\boldsymbol{p}, \boldsymbol{p}^{vis})$
- Fit from MC tuned to the detector resolution
- Use of matrix-element generator: MadGraph 4

## fn's Matrix Element weight





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How to evaluate those weights?

$$\mathcal{P}(\boldsymbol{p}^{vis}|\alpha) = \frac{1}{\sigma_{\alpha}} (d\Phi dx_1 dx_2) M_{\alpha}(\boldsymbol{p})|^2 W(\boldsymbol{p}, \boldsymbol{p}^{vis})$$

Difficult point: Numerical Integration

## fn's Matrix Element weight



# fn's Monte-Carlo Integration

The choice of the parameterisation has a strong impact on the efficiency



The adaptive Monte-Carlo Technique picks point in interesting areas
 The technique is efficient

## this Monte-Carlo Integration

The choice of the parametrization has a strong impact on the efficiency



## The adaptive Monte-Carlo Techniques picks points everywhere

INE UNLEARAL CONVERMES SLOWLA

# fn's Monte-Carlo Integration

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The adaptive Monte-Carlo Techniques picks point in interesting areas

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□ First Example: dí-leptonic top quark pair



□ degrees of freedom 16

- 2: pdf
  - □ 3 x 6: final states
  - -4: energy-momentum conservation

] peaks 16

- 4: Bréit-Wigner
- □ 3 x 4: visible particles























□ Second Example: semí-leptoníc top quark paír







Second Example: semí-leptoníc top quark paír



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□ Second Example: semí-leptoníc top quark paír



![](_page_34_Picture_0.jpeg)

![](_page_34_Figure_2.jpeg)

Second Example: semí-leptoníc top quark paír

![](_page_34_Figure_4.jpeg)

## fn's Matrix Element weight

![](_page_35_Figure_1.jpeg)


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MADWEIGHT

P. Artoisenet, V. Lemaître, F. Maltoni, OM: JHEP 1012:068



### MadWeight



fully hadronic / leptonic process

w production

semi-leptonic top quark pair

Fully leptonic top quark pair



### MadWeight



Higss production decaying in W

W+W-production

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### MadWeight



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### □ Examples of studies / investigations

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- discriminating Hypothesis
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- mass determination : smuon pair production
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### Main effect: induce a total transverse momentum

J. Alwall, A. Freytas, OM: PRD83:074010

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27/34





Study the ISR on Higgs production at LHC (14 TeV) at parton level (no hadronization)













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## **fnsDifferential Cross Section**





**OM: UCL Thesis** 

31/34

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## **fnsDifferential Cross Section**





#### We use the full inference



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### **DMEM Validation**








# DMEM



What if the sample is not a SM one? For example if a heavy Z exists (600 GeV).







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## Matrix Element Re-Weighting: path to precise measurement





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- Improves Kinematical Fitting Method





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#### Backup slide





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# MadWeight



- the phase-space is split into blocks, each of them is associated to a specific local change of variables
- 12 blocks, í.e. 12 analytic changes of variables have been defined in our code.
- Madweight finds automatically
  - the optimal partition of the PS into blocks
  - computes the weights using the corresponding PS parametrisation











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