

DIRECT CP ASYMMETRIES IN HADRONIC D DECAYS

Fu-Sheng Yu

Co-tutors: Prof. Cai-Dian Lu (IHEP, Beijing)
Dr. Emi Kou (LAL, Orsay)

Outline

- ◆ Motivation
- ◆ Branching Ratios
- ◆ Penguin parameterization
- ◆ Predict direct CP asymmetries
- ◆ Summary

Evidence of CPV

- ◆ First evidence of CP violation in charmed meson decays by LHCb, with 3.5σ [PRL. 108 (2012) 111602]

$$\begin{aligned}\Delta A_{CP}^{exp} &\equiv A_{CP}(K^+ K^-) - A_{CP}(\pi^+ \pi^-) \\ &= [-0.82 \pm 0.21(\text{stat}) \pm 0.11(\text{syst})]\%\end{aligned}$$

- ◆ Confirmed by CDF, with 2.7σ [CDF note 10784]

$$\Delta A_{CP} = [-0.62 \pm 0.21(\text{stat}) \pm 0.10(\text{syst})]\%$$

- ◆ Naively expected much smaller in the SM

$$A_{CP}^{dir} \sim \frac{|V_{cb}^* V_{ub}|}{|V_{cs}^* V_{us}|} \frac{\alpha_s}{\pi} \sim 10^{-4}$$

- ◆ Necessary to predict more precisely in the SM.

Dynamics of D decays

- ◆ To predict CPV, we have to well understand the important decay mechanism.
- ◆ At first, branching ratios should be well explained
- *A long-standing puzzle:*

$$R = \frac{Br(D^0 \rightarrow K^+ K^-)}{Br(D^0 \rightarrow \pi^+ \pi^-)} \approx 2.8$$

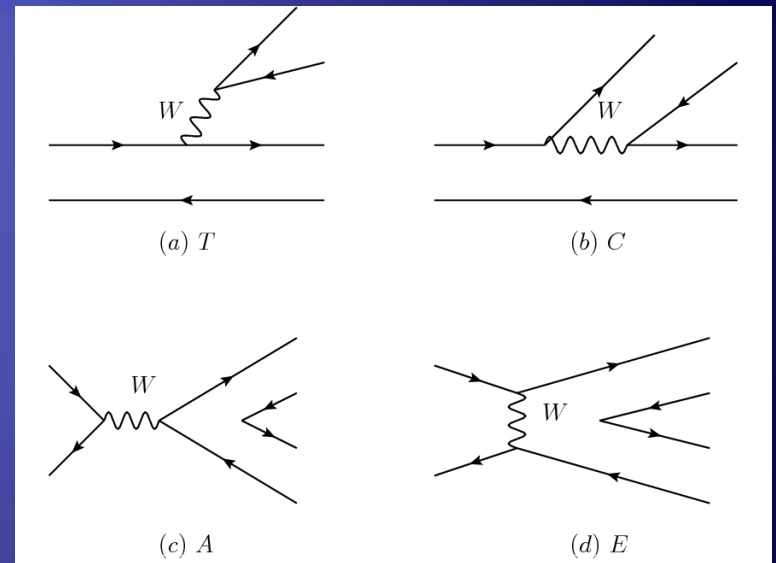
- ◆ $R=1$ in the SU(3) flavor symmetry limit
- ◆ Imply large **SU(3) breaking** effects

Guidelines

- ◆ Framework: topological amplitudes in **factorization** hypothesis:
 - ◆ Short-distance dynamics: Wilson coefficients
 - ◆ Long-distance dynamics: hadronic matrix elements
- ◆ Introduce **non-perturbative** parameters in hadronic matrix elements
 - ◆ Charm mass $m_c \approx 1.3 \text{ GeV}$, not reliable for perturbation in coupling constant and $1/m_c$
- ◆ Include large **SU(3) breaking effects**.

Topological diagrams for BRs

- ◆ According to **weak interactions** and flavor flows
- ◆ Include **all strong interaction** effects, involving FSI
- ◆ This is a **complete set**
- ◆ Topological diagrammatic approach was studied in the flavor $SU(3)$ symmetry limit



[Cheng & Chiang, 2010]

➤ How $SU(3)$ breaking ??

Mode-dependent dynamics

SU(3) breaking effects

- ◆ **Evolution of Wilson coefficients** depending on masses of decay products
 - Difference of mass ratios $\frac{m_\pi}{m_D}$ VS $\frac{m_K}{m_D}$ $m_K \sim 0.5 \text{ GeV}$
 $m_D \sim 1.8 \text{ GeV}$
 - Especially for the modes with η' involved $M_{\eta'} \sim 1 \text{ GeV}$
- ◆ **Glauber strong phase** associated with **pion** in nonfactorizable amplitudes [H.n Li, S. Mishima, 2009]
 - Pion: as a massless Goldstone boson, and as a $q\bar{q}$ bound state ?

Nambu-Goldstone bosons

- Pion : massless Goldstone boson, and $q\bar{q}$ bound state?
- ♦ **Massless** boson => huge spacetime
=> large separation between $q\bar{q}$
=> **high mass** due to confinement => contradiction!
- ♦ Reconciliation : Tight bound $q\bar{q}$, but multi-parton
=> soft cloud (Lepage, Brodsky 79; Nussinov, Shrock 08; Duraisamy, Kagan 08)
- ♦ **Glauber phase** corresponds to soft cloud [H.n Li, S. Mishima, 09]
- ♦ Pion is unique
- ♦ **SU(3) breaking** effects: distinguish **pions** from other final states





Branching ratios

Include important dynamics
For SU(3) breaking effects

Cabibbo-favored BRs well consistent with data

| Modes | Br(FSI) | Br(diagram) | Br(pole) | Br(exp) | Br(this work) |
|-----------------------------------|---------|-----------------|---------------|-------------------|---------------|
| $D^0 \rightarrow \pi^0 \bar{K}^0$ | 1.35 | 2.36 ± 0.08 | 2.4 ± 0.7 | 2.38 ± 0.09 | 2.37 |
| $D^0 \rightarrow \pi^+ K^-$ | 4.03 | 3.91 ± 0.17 | 3.9 ± 1.0 | 3.891 ± 0.077 | 3.71 |
| $D^0 \rightarrow \bar{K}^0 \eta$ | 0.80 | 0.98 ± 0.05 | 0.8 ± 0.2 | 0.96 ± 0.06 | 1.00 |
| $D^0 \rightarrow \bar{K}^0 \eta'$ | 1.51 | 1.91 ± 0.09 | 1.9 ± 0.3 | 1.90 ± 0.11 | 1.68 |
| $D^+ \rightarrow \pi^+ \bar{K}^0$ | 2.51 | 3.08 ± 0.36 | 3.1 ± 2.0 | 3.074 ± 0.096 | 3.17 |
| $D_S^+ \rightarrow K^+ \bar{K}^0$ | 4.79 | 2.97 ± 0.32 | 3.0 ± 0.9 | 2.98 ± 0.08 | 2.99 |
| $D_S^+ \rightarrow \pi^+ \eta$ | 1.33 | 1.82 ± 0.32 | 1.9 ± 0.5 | 1.84 ± 0.15 | 1.65 |
| $D_S^+ \rightarrow \pi^+ \eta'$ | 5.89 | 3.82 ± 0.36 | 4.6 ± 0.6 | 3.95 ± 0.34 | 3.44 |
| $D_S^+ \rightarrow \pi^+ \pi^0$ | | 0 | 0 | < 0.06 | 0 |

Cabibbo-suppressed BRs our advantage

| Modes | Br(FSI) | Br(diagram) | Br(pole) | Br(exp) | Br(this work) |
|---------------------------------|---------|-----------------|---------------|-------------------|--|
| $D^0 \rightarrow \pi^+ \pi^-$ | 1.59 | 2.24 ± 0.10 | 2.2 ± 0.5 | 1.45 ± 0.05 | 1.44  |
| $D^0 \rightarrow K^+ K^-$ | 4.56 | 1.92 ± 0.08 | 3.0 ± 0.8 | 4.07 ± 0.10 | 4.19  |
| $D^0 \rightarrow K^0 \bar{K}^0$ | 0.93 | 0 | 0.3 ± 0.1 | 0.320 ± 0.038 | 0.35 |
| $D^0 \rightarrow \pi^0 \pi^0$ | 1.16 | 1.35 ± 0.05 | 0.8 ± 0.2 | 0.81 ± 0.05 | 0.55 |
| $D^0 \rightarrow \pi^0 \eta$ | 0.58 | 0.75 ± 0.02 | 1.1 ± 0.3 | 0.68 ± 0.07 | 0.94 |
| $D^0 \rightarrow \pi^0 \eta'$ | 1.7 | 0.74 ± 0.02 | 0.6 ± 0.2 | 0.91 ± 0.13 | 0.64 |
| $D^0 \rightarrow \eta \eta$ | 1.0 | 1.44 ± 0.08 | 1.3 ± 0.4 | 1.67 ± 0.18 | 1.48 |
| $D^0 \rightarrow \eta \eta'$ | 2.2 | 1.19 ± 0.07 | 1.1 ± 0.1 | 1.05 ± 0.26 | 1.52 |
| $D^+ \rightarrow \pi^+ \pi^0$ | 1.7 | 0.88 ± 0.10 | 1.0 ± 0.5 | 1.18 ± 0.07 | 0.88 |
| $D^+ \rightarrow K^+ \bar{K}^0$ | 8.6 | 5.46 ± 0.53 | 8.4 ± 1.6 | 6.12 ± 0.22 | 5.97 |
| $D^+ \rightarrow \pi^+ \eta$ | 3.6 | 1.48 ± 0.26 | 1.6 ± 1.0 | 3.54 ± 0.21 | 3.37  |
| $D^+ \rightarrow \pi^+ \eta'$ | 7.9 | 3.70 ± 0.37 | 5.5 ± 0.8 | 4.68 ± 0.29 | 4.54  |
| $D_S^+ \rightarrow \pi^0 K^+$ | 1.6 | 0.86 ± 0.09 | 0.5 ± 0.2 | 0.62 ± 0.23 | 0.65 |
| $D_S^+ \rightarrow \pi^+ K^0$ | 4.3 | 2.73 ± 0.26 | 2.8 ± 0.6 | 2.52 ± 0.27 | 2.21 |
| $D_S^+ \rightarrow K^+ \eta$ | 2.7 | 0.78 ± 0.09 | 0.8 ± 0.5 | 1.76 ± 0.36 | 1.00 |
| $D_S^+ \rightarrow K^+ \eta'$ | 5.2 | 1.07 ± 0.17 | 1.4 ± 0.4 | 1.8 ± 0.5 | 1.92 |

Puzzle $D^0 \rightarrow \pi^+ \pi^-$ vs $D^0 \rightarrow K^+ K^-$

- ◆ Revisited: $R_{\text{exp}} = 2.8$, $R = 1$ in SU(3) flavor symmetry

| Modes | Br(FSI) | Br(diagram) | Br(pole) | Br(exp) | Br(this work) |
|-------------------------------|---------|-----------------|---------------|-----------------|---------------|
| $D^0 \rightarrow \pi^+ \pi^-$ | 1.59 | 2.24 ± 0.10 | 2.2 ± 0.5 | 1.45 ± 0.05 | 1.44 |
| $D^0 \rightarrow K^+ K^-$ | 4.56 | 1.92 ± 0.08 | 3.0 ± 0.8 | 4.07 ± 0.10 | 4.19 |

- ◆ Large SU(3) breaking effects
- **Glauber phase** associated with **pions**
 - dominate source of the difference between these two modes

**Must Explain BRs well
otherwise, some important dynamics
may be missed**



**penguin parameterization and
predict direct CP asymmetries**

Direct CP asymmetry

- ◆ Definition:

$$A_{\text{CP}}(f) = \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})}$$

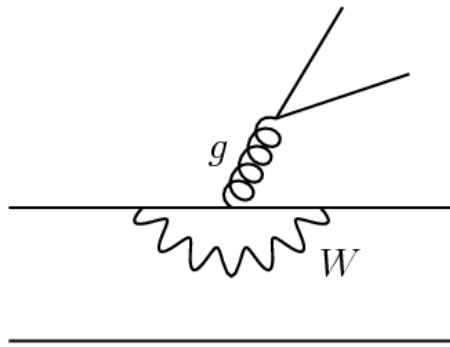
- ◆ Occurs only in singly Cabibbo-suppressed decays
- ◆ Interference of Tree and Penguin contributions

$$\mathcal{A}(D \rightarrow f) = V_{cd}^* V_{ud} T - V_{cb}^* V_{ub} P$$

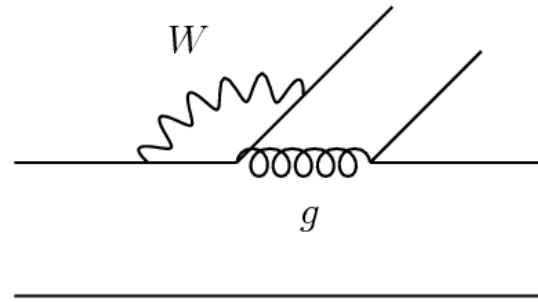
$$V_{CKM} = \begin{pmatrix} 1 - \lambda^2/2 - \lambda^4/8 & \lambda & A\lambda^3(\bar{\rho} - i\bar{\eta}) + A\lambda^5(\bar{\rho} - i\bar{\eta})/2 \\ -\lambda + A^2\lambda^5[1 - 2(\bar{\rho} + i\bar{\eta})]/2 & 1 - \lambda^2/2 - \lambda^4(1 + 4A^2)/8 & A\lambda^2 \\ A\lambda^3(1 - \bar{\rho} - i\bar{\eta}) & -A\lambda^2 + A\lambda^4[1 - 2(\bar{\rho} + i\bar{\eta})]/2 & 1 - A^2\lambda^4/2 \end{pmatrix}$$

Penguin topologies

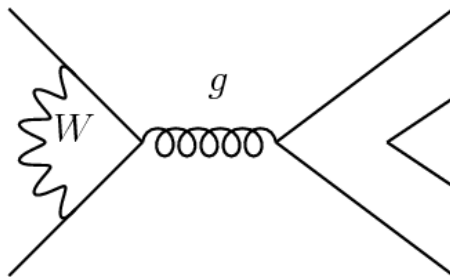
- ◆ All topological penguin diagrams for $D \rightarrow PP$



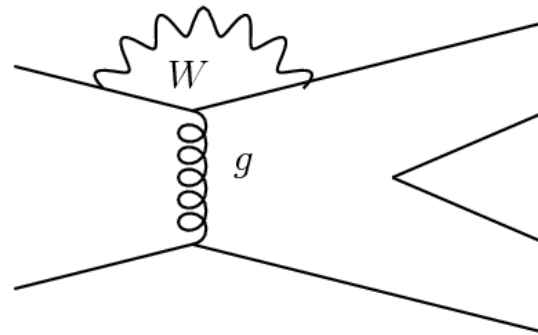
(a) P_T



(b) P_C



(c) P_A



(d) P_F

Penguin parameterization

- ◆ Long-distance hadronic parameters, related to tree level, fixed by the data of branching ratios
- ◆ Combine the short-distance dynamics associated with penguin operators
- ◆ Then predict direct CP asymmetries

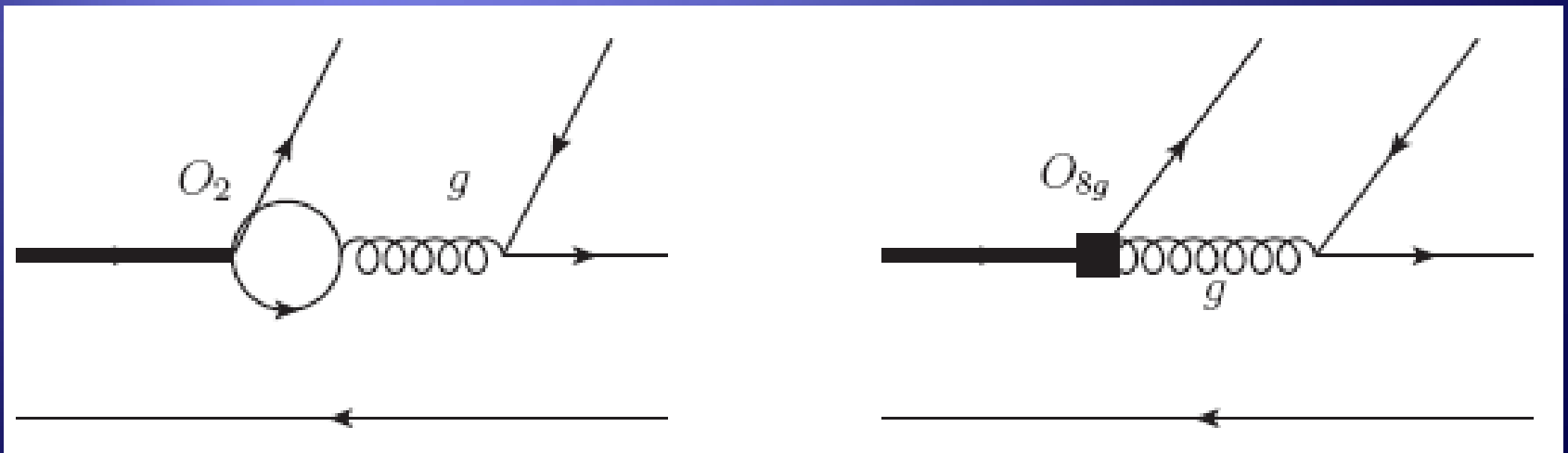
Strategy:

relate penguin to tree

- ◆ At tree level, operators are all $(V-A)(V-A)$
- ◆ For penguins, the hadronic matrix elements with $(V-A)(V-A)$ operators are the same as tree level
- ◆ $(V-A)(V+A)$ can be related to tree by a sign, since either V or A contribute to $D \rightarrow PP$
- ◆ $(S-P)(S+P)$ are different and subtle
- ◆ Related to tree parameters by chiral enhancement, or neglected by power suppression

Quark loops & Magnetic penguin



- ◆ quark loops and magnetic penguin are absorbed into short-distance Wilson coefficients



Predictions

- ◆ Penguin matrix elements are either related to tree matrix elements (fixed by BRs), or factorizable and calculable, or power suppressed, if not able to be related
- ◆ formulate penguin contribution without introducing additional free parameters
- ◆ **Unambiguous** predictions of direct CP asymmetries

Predictions of Direct CP asymmetries

| Modes | $a_{CP}(\text{FSI})$ | $a_{CP}(\text{diagram})$ | a_{CP}^{tree} | $a_{CP}^{\text{tot}} (\times 10^{-3})$ |
|---------------------------------|----------------------|--------------------------|------------------------|---|
| $D^0 \rightarrow \pi^+ \pi^-$ | 0.02 ± 0.01 | 0.86 | 0 | 0.74  |
| $D^0 \rightarrow K^+ K^-$ | 0.13 ± 0.8 | -0.48 | 0 | -0.54  |
| $D^0 \rightarrow \pi^0 \pi^0$ | -0.54 ± 0.31 | 0.85 | 0 | 0.26 |
| $D^0 \rightarrow K^0 \bar{K}^0$ | -0.28 ± 0.16 | 0 | 0.69 | 0.90 |
| $D^0 \rightarrow \pi^0 \eta$ | 1.43 ± 0.83 | -0.16 | -0.29 | -0.61 |
| $D^0 \rightarrow \pi^0 \eta'$ | -0.98 ± 0.47 | -0.01 | 0.43 | 1.67 |
| $D^0 \rightarrow \eta \eta$ | 0.50 ± 0.29 | -0.71 | 0.29 | 0.18 |
| $D^0 \rightarrow \eta \eta'$ | 0.28 ± 0.16 | 0.25 | -0.30 | 0.97 |
| $D^+ \rightarrow \pi^+ \pi^0$ | | 0 | 0 | -0.23 |
| $D^+ \rightarrow K^+ \bar{K}^0$ | -0.51 ± 0.30 | -0.38 | -0.08 | -0.93 |
| $D^+ \rightarrow \pi^+ \eta$ | | -0.65 | -0.46 | 0.63 |
| $D^+ \rightarrow \pi^+ \eta'$ | | 0.41 | 0.30 | 1.28 |
| $D_S^+ \rightarrow \pi^0 K^+$ | | 0.88 | 0.17 | 0.76 |
| $D_S^+ \rightarrow \pi^+ K^0$ | | 0.52 | -0.01 | 0.87 |
| $D_S^+ \rightarrow K^+ \eta$ | | -0.19 | 0.75 | 0.76 |
| $D_S^+ \rightarrow K^+ \eta'$ | | -0.41 | -0.48 | 1.83 |

Difference of CP asymmetries

- ◆ The prediction in the SM

$$\Delta A_{CP}^{SM} \equiv A_{CP}(K^+K^-) - A_{CP}(\pi^+\pi^-) = -0.13\%$$

- ◆ Enhanced from naively expectation in SM 10^{-4}
- ◆ LHCb $\Delta A_{CP} = [-0.82 \pm 0.24]\%$
- ◆ CDF $\Delta A_{CP} = [-0.62 \pm 0.23]\%$
- ◆ The prediction is still smaller than experimental measurements
- ◆ If CPV remains the current central value ($\sim 1\%$), may be a signal of new physics


Summary

- ◆ Explain branching ratios at tree level
- ◆ Parameterize penguin contributions, related to tree amplitudes under factorization hypothesis
 - ◆ Fix hadronic parameters using data of branching ratios
 - ◆ Combine short-distance dynamics associated with penguin operators
- ◆ Unambiguous predictions of direct CP asymmetries in $D \rightarrow PP$ in the SM
- ◆ Especially $\Delta A_{CP}^{SM} = -0.13\%$
- ◆ Much smaller than LHCb and CDF measurements

THANK YOU!

Improvement of BRs involving η'

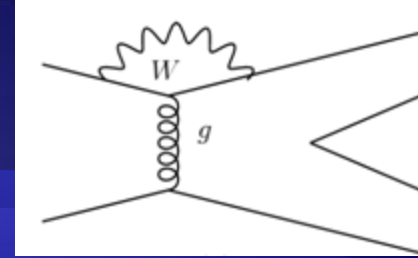
- Benefited from the scale-dependent Wilson coefficients, predictions with all the η' involved modes are improved, compared to the pole model and diagrammatic approach

| Modes | Br(FSI) | Br(diagrammatic) | Br(pole) | Br(exp) | Br(this work) |
|-----------------------------------|---------|------------------|---------------|-----------------|--|
| $D^0 \rightarrow \bar{K}^0 \eta'$ | 1.51 | 1.91 ± 0.09 | 1.9 ± 0.3 | 1.90 ± 0.11 | 1.84 |
| $D_S^+ \rightarrow \pi^+ \eta'$ | 5.89 | 3.82 ± 0.36 | 4.6 ± 0.6 | 3.95 ± 0.34 | 3.25 |
| $D^0 \rightarrow \pi^0 \eta'$ | 1.7 | 0.74 ± 0.02 | 0.6 ± 0.2 | 0.91 ± 0.13 | 0.70 |
| $D^0 \rightarrow \eta \eta'$ | 2.2 | 1.19 ± 0.07 | 1.1 ± 0.1 | 1.05 ± 0.26 | 1.58 |
| $D^+ \rightarrow \pi^+ \eta'$ | 7.9 | 3.70 ± 0.37 | 5.5 ± 0.8 | 4.68 ± 0.29 | 4.78  |
| $D_S^+ \rightarrow K^+ \eta'$ | 5.2 | 1.07 ± 0.17 | 1.4 ± 0.4 | 1.8 ± 0.5 | 1.67 |
| $D^+ \rightarrow K^+ \eta'$ | | 0.91 ± 0.17 | 1.0 ± 0.1 | 1.76 ± 0.22 | 1.07 |

Penguin operators

$$\begin{aligned} O_3 &= \sum_{q'=u,d,s} (\bar{u}_\alpha c_\alpha)_{V-A} (\bar{q}'_\beta q'_\beta)_{V-A}, & (\mathbf{V-A})(\mathbf{V-A}) \\ O_4 &= \sum_{q'=u,d,s} (\bar{u}_\alpha c_\beta)_{V-A} (\bar{q}'_\beta q'_\alpha)_{V-A}, \\ O_5 &= \sum_{q'=u,d,s} (\bar{u}_\alpha c_\alpha)_{V-A} (\bar{q}'_\beta q'_\beta)_{V+A}, & (\mathbf{V-A})(\mathbf{V+A}) \\ O_6 &= \sum_{q'=u,d,s} (\bar{u}_\alpha c_\beta)_{V-A} (\bar{q}'_\beta q'_\alpha)_{V+A} & (\mathbf{S+P})(\mathbf{S-P}) \end{aligned}$$

Penguin exchange annihilation amplitude



- ◆ The hadronic matrix elements with the operators of $(S-P)(S+P)$ are absent in tree level
- ◆ No helicity suppression for $(S-P)(S+P)$, so their contributions can not be neglected
- ◆ Can not use the hadronic parameters at tree level
- ◆ Assumed to be dominated by scalar resonances