

Enhancing lepton flavor violation with the Z-penguin

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Based on work in collaboration with
M. Hirsch and F. Staub

ArXiv:1202.1825 [hep-ph]

Outline of the talk

- $l_i \rightarrow 3l_j$ in the MSSM
- Some mass scaling considerations
- $l_i \rightarrow 3l_j$ in the MSSM revisited
- Beyond MSSM
- Final remarks

$l_i \rightarrow 3l_j$ in the MSSM

In supersymmetry, the additional degrees of freedom provided by the superparticles typically increase the flavor violating signals to observable levels.

The most popular example in the leptonic sector is the radiative decay $\mu \rightarrow e\gamma$ (why the most popular? see later...), but other interesting processes have been studied in the literature. For example:

$$l_i \rightarrow 3l_j$$

- J. Hisano et al., PRD 53 (1996) 2442
- E. Arganda and M.J. Herrero, PRD 73 (2006) 055003

$l_i \rightarrow 3l_j$ in the MSSM

A brief détour...

Experimental limits

$$l_i \rightarrow l_j \gamma$$

$$\text{Br}(\mu \rightarrow e \gamma) < 2.4 \cdot 10^{-12}$$

$$\text{Br}(\tau \rightarrow e \gamma) < 3.3 \cdot 10^{-8}$$

$$\text{Br}(\tau \rightarrow \mu \gamma) < 4.4 \cdot 10^{-8}$$

$$l_i \rightarrow 3l_j$$

$$\text{Br}(\mu \rightarrow 3e) < 1.0 \cdot 10^{-12}$$

$$\text{Br}(\tau \rightarrow 3e) < 2.7 \cdot 10^{-8}$$

$$\text{Br}(\tau \rightarrow 3\mu) < 2.1 \cdot 10^{-8}$$

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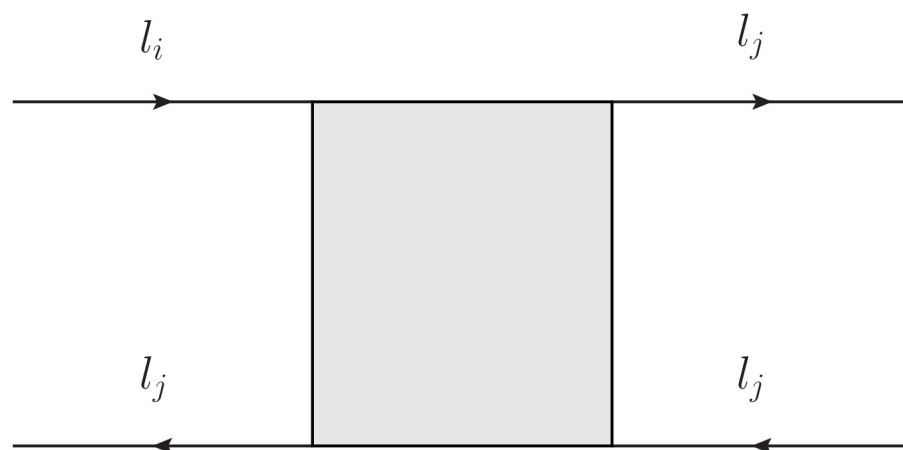
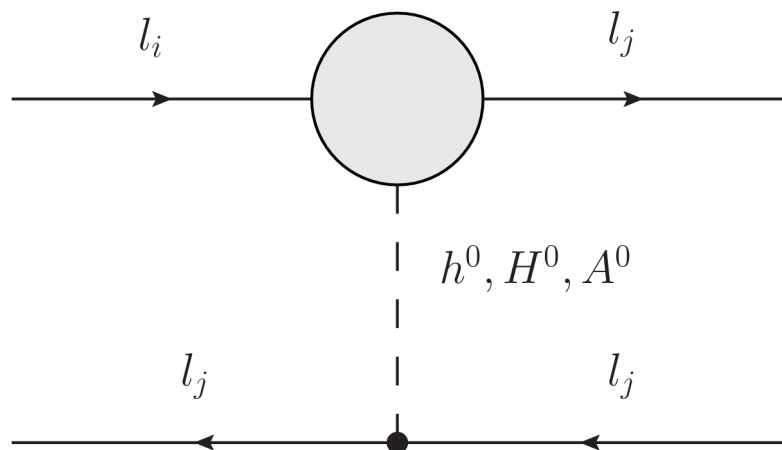
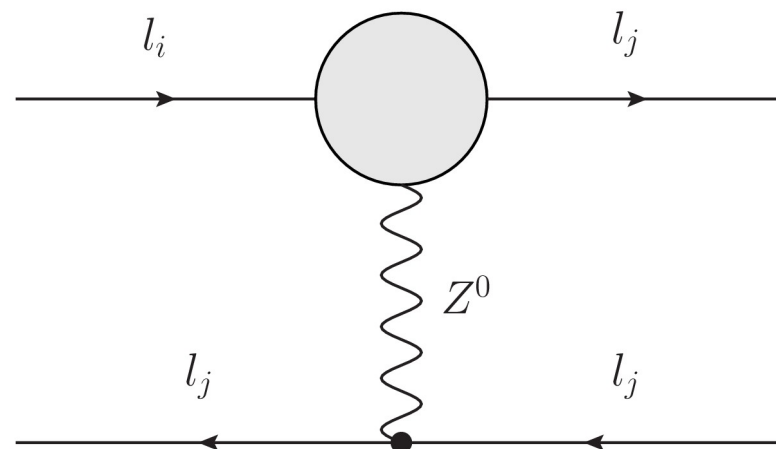
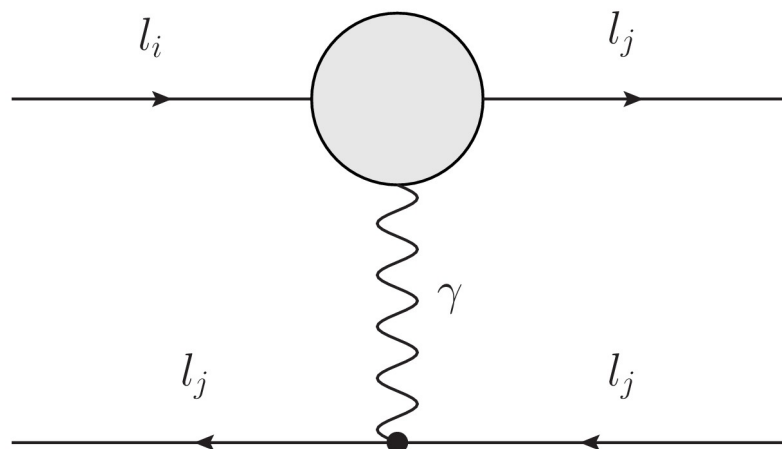
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$l_i \rightarrow 3l_j$ in the MSSM

$$\begin{aligned}
 \Gamma = & \frac{e^4}{512\pi^3} m_{l_j}^5 \left[|A_1^L|^2 + |A_1^R|^2 - 2 (A_1^L A_2^{R*} + A_2^L A_1^{R*} + h.c.) \right. \\
 & + \left(|A_2^L|^2 + |A_2^R|^2 \right) \left(\frac{16}{3} \log \frac{m_{l_j}}{m_{l_i}} - \frac{22}{3} \right) \\
 & + \frac{1}{6} \left(|B_1^L|^2 + |B_1^R|^2 \right) + \frac{1}{3} \left(|\hat{B}_2^L|^2 + |\hat{B}_2^R|^2 \right) \\
 & + \frac{1}{24} \left(|\hat{B}_3^L|^2 + |\hat{B}_3^R|^2 \right) + 6 \left(|B_4^L|^2 + |B_4^R|^2 \right) \\
 & - \frac{1}{2} \left(\hat{B}_3^L B_4^{L*} + \hat{B}_3^R B_4^{R*} + h.c. \right) \\
 & + \frac{1}{3} \left\{ 2 \left(|F_{LL}|^2 + |F_{RR}|^2 \right) + |F_{LR}|^2 + |F_{RL}|^2 \right\} \\
 & \left. + \text{interference terms} \right]
 \end{aligned}$$

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- In most parts of parameter space: **Photon penguins**

J. Hisano et al., PRD 53 (1996) 2442

E. Arganda and M.J. Herrero, PRD 73 (2006) 055003

$$\frac{BR(l_i \rightarrow 3l_j)}{BR(l_j i \rightarrow l_j \gamma)} = \frac{\alpha}{3\pi} \left(\log \frac{m_{l_i}^2}{m_{l_j}^2} - \frac{11}{4} \right) \Rightarrow BR(l_i \rightarrow l_j \gamma) \gg BR(l_i \rightarrow 3l_j)$$

... and that, together with the **good experimental bound**, has made $\mu \rightarrow e\gamma$ so attractive for the pheno community

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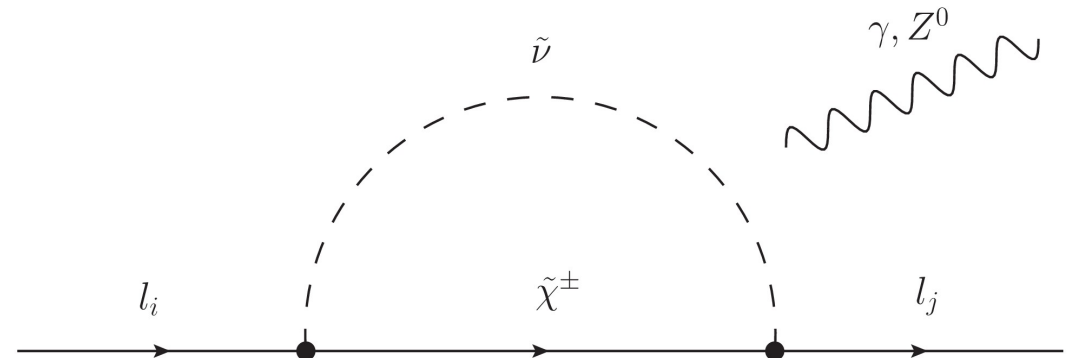
- For large $\tan \beta$ and a light pseudoscalar: **Higgs penguins**

K.S. Babu, C. Kolda, PRL 89 (2002) 241802

Mass scaling considerations

Let us give a more detailed look...

Consider the γ - and Z -penguins originated by chargino-sneutrino loops.



One finds:

$$A_a^{(c)L,R} = \frac{1}{m_{\tilde{\nu}}^2} \mathcal{O}_{A_a}^{L,R} s(x^2)$$

γ -penguin

$$F_X = \frac{1}{g^2 \sin^2 \theta_W m_Z^2} \mathcal{O}_{F_X}^{L,R} t(x^2)$$

Z -penguin

Mass scaling considerations

In fact, the mass scalings

$$A \sim m_{SUSY}^{-2}$$

$$F \sim m_Z^{-2}$$

are quite intuitive. These are the lowest mass scales in the penguins (recall, for example, the H-penguins $\sim m_H^{-2}$)

Then, by doing a very simple estimate...

$$\frac{F}{A} \sim \frac{m_{SUSY}^2}{g^2 \sin^2 \theta_W m_Z^2} \sim 500 \quad \text{for } m_{SUSY} \sim 300 \text{ GeV}$$

And, remember... $\Gamma(l_i \rightarrow 3l_j) \propto A^2, F^2$

Mass scaling considerations

These considerations lead us to the **expectation**

$$F \gg A$$

So...

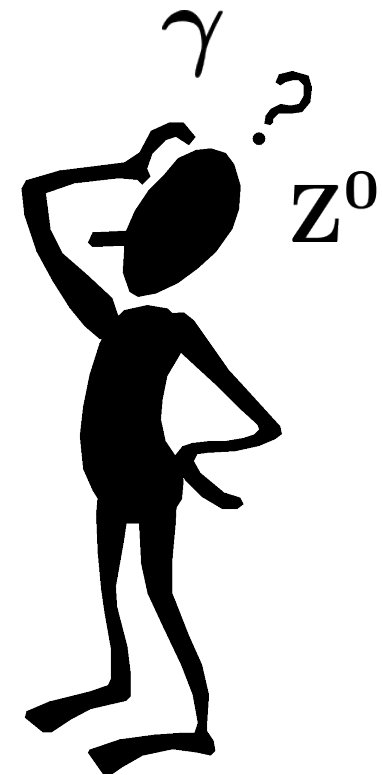
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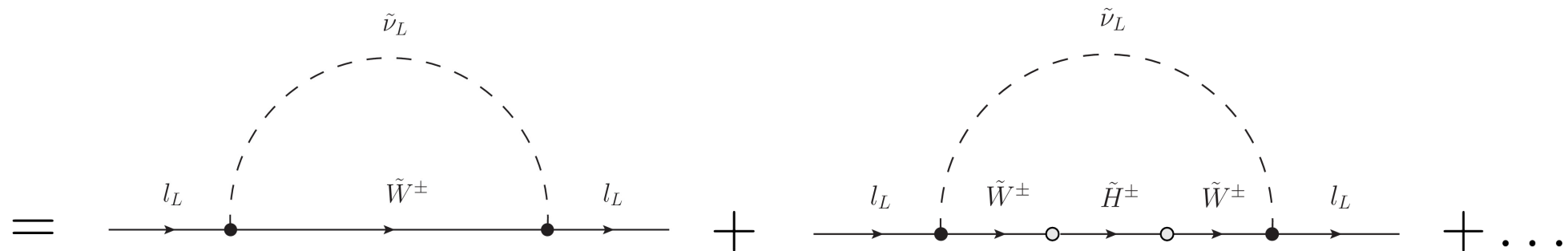
Why the Z-penguins are not the dominant contribution in the MSSM?



$l_i \rightarrow 3l_j$ in the MSSM revisited

Consider F_L , dominant contribution within the Z-penguins, obtained when the external leptons are L-handed and make an expansion on the **chargino mixing angle**.

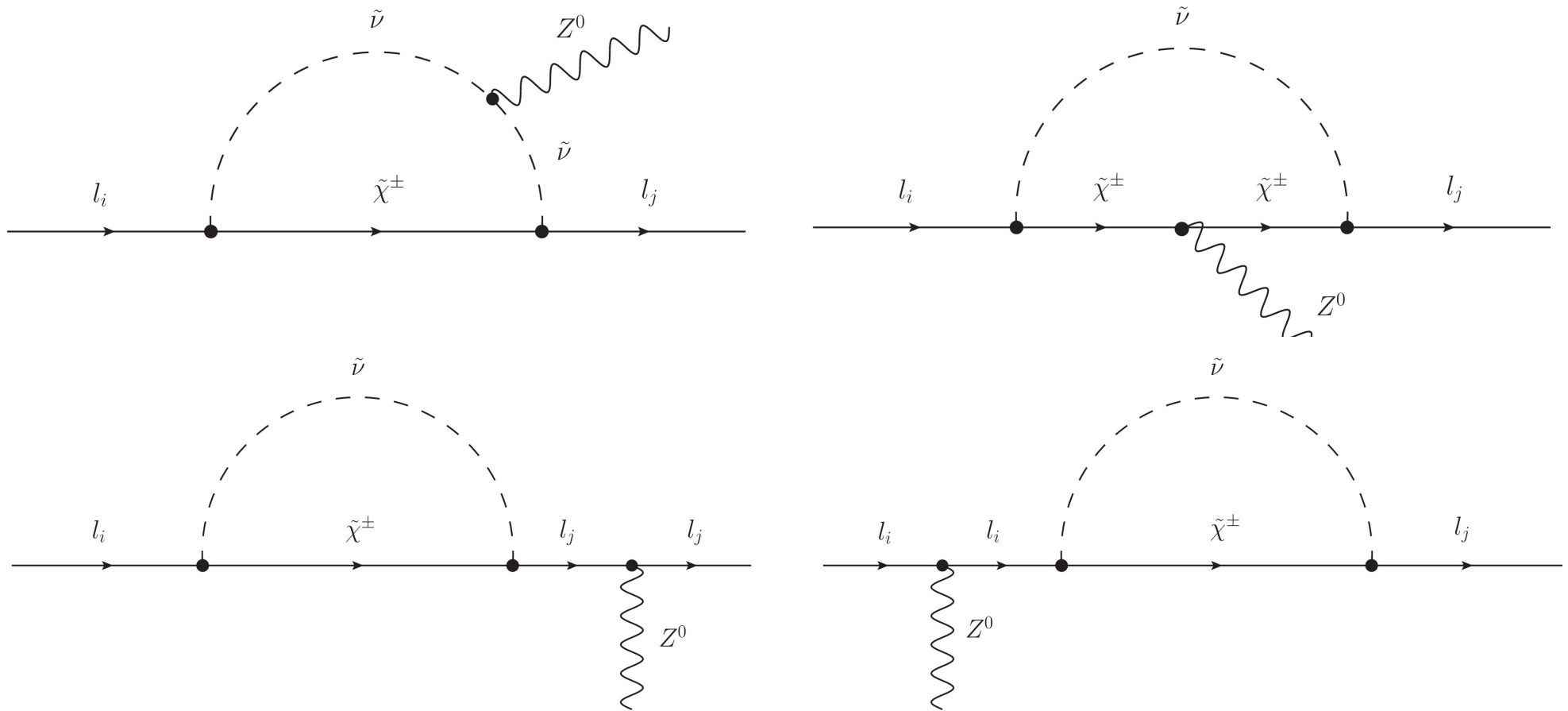
$$F_L = F_L^{(0)} + \theta_{\tilde{\chi}^\pm}^2 F_L^{(2)} + \dots$$



Important: There is no order 1!

$l_i \rightarrow 3l_j$ in the MSSM revisited

$$\mathbf{F} = \mathbf{F}_1 + \mathbf{F}_2 + \mathbf{F}_3 + \mathbf{F}_4$$



$l_i \rightarrow 3l_j$ in the MSSM revisited

When you sum the four diagrams that contribute to $F_L^{(0)}$:

$$\begin{aligned} F_L^{(0)} &= F_{L,1}^{(0)} + F_{L,2}^{(0)} + F_{L,3}^{(0)} + F_{L,4}^{(0)} \\ &= \frac{1}{2}g^3 c_W Z_V^{ki} Z_V^{kj*} X_1^k + \frac{1}{2}g^2 g' s_W Z_V^{ki} Z_V^{kj*} X_2^k \end{aligned}$$

X_1^k and X_2^k are combinations of PV functions, with **different combinations of chargino and sneutrino masses**. However, one finds that the masses **cancel out** and they just become numerical constants. Therefore...

$l_i \rightarrow 3l_j$ in the MSSM revisited

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$$\Rightarrow F_L^{(0)} \propto \sum_k Z_V^{ki} Z_V^{kj*} = 0 \quad \text{It vanishes exactly!}$$

Side comment: This cancellation was also found in Lunghi et al. Nucl. Phys. B 568 (2000) 120 when looking into $B \rightarrow X_s l^+ l^-$ in supersymmetry

Beyond the MSSM

In **conclusion**, the **Z-penguins** are not dominant in the MSSM because the leading-order term vanishes and the first non-zero contribution is suppressed by two chargino insertions. This cancellation is not found in the **photon penguins**.

How can we **break the cancellation**?

- Additional states that mix with the sneutrinos
- New lepton couplings

$l_i \rightarrow 3l_j$ can be greatly enhanced!

Beyond the MSSM

Example 1: Supersymmetric inverse seesaw.

Example 2: MSSM + Trilinear R-parity violation

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Example 2: MSSM + Trilinear R-parity violation

$$W_R = W_{MSSM} + \frac{1}{2} \lambda_{ijk} \hat{L}_i \hat{L}_j \hat{E}_k^c$$

- Sneutrino-lepton loops are also possible in this case
- The new couplings break the cancellation since

$$\sum_k Z_V^{ki} Z_V^{kj*} \lambda_{jki} \lambda_{jkj} \neq 0$$

Great **enhancement** due to Z-boson penguins!

Beyond the MSSM

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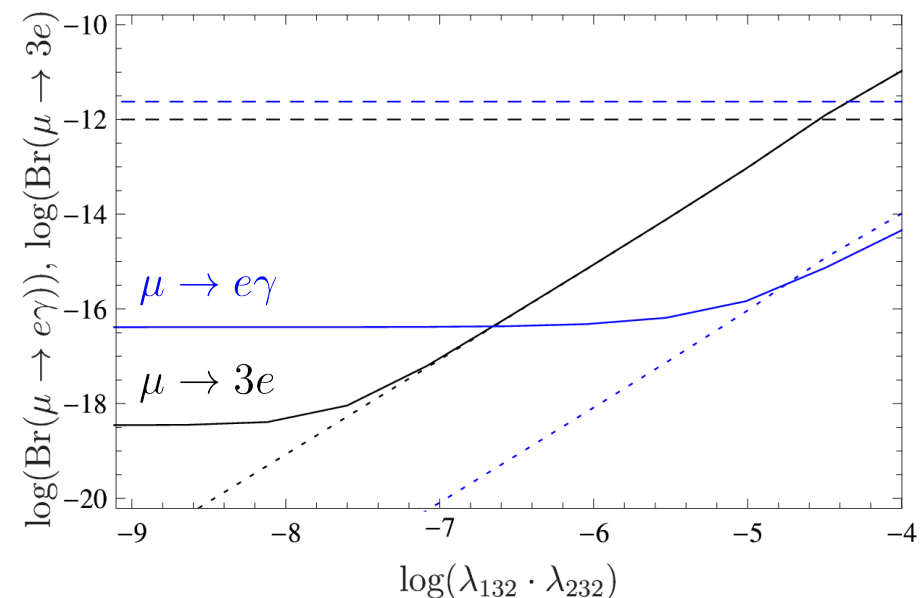
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Bound in the literature: $\lambda_{132} \cdot \lambda_{232} \lesssim 0.2$

3 orders of magnitude improvement!

Final remarks

- In the MSSM the Z-penguin contribution to $l_i \rightarrow 3l_j$ is usually neglected or regarded as sub-dominant. And that's totally correct!
- However, in many extensions of the lepton sector the Z-penguin becomes dominant, enhancing the signal by many orders of magnitude.
- In fact, one can easily find $BR(\mu \rightarrow 3e) \gg BR(\mu \rightarrow e\gamma)$
- $BR(\mu \rightarrow 3e)$ can be the most constraining observable!
- LFV studies should be re-considered and bounds re-evaluated.



Thank you!

Backup slides

Photon penguin contributions

E. Arganda and M.J. Herrero, PRD 73 (2006) 055003

$$A_a^{L,R} = A_a^{(n)L,R} + A_a^{(c)L,R}, \quad a = 1, 2$$

$$A_1^{(n)L} = \frac{1}{576\pi^2} N_{iAX}^R N_{jAX}^{R*} \frac{1}{m_{\tilde{l}_X}^2} \frac{2 - 9x_{AX} + 18x_{AX}^2 - 11x_A^3 + 6x_{AX}^3 \log x_{AX}}{(1 - x_{AX})^4}$$

$$\begin{aligned} A_2^{(n)L} = & \frac{1}{32\pi^2} \frac{1}{m_{\tilde{l}_X}^2} \left[N_{iAX}^L N_{jAX}^{L*} \frac{1 - 6x_{AX} + 3x_{AX}^2 + 2x_{AX}^3 - 6x_{AX}^2 \log x_{AX}}{6(1 - x_{AX})^4} \right. \\ & + N_{iAX}^R N_{jAX}^{R*} \frac{m_{l_i}}{m_{l_j}} \frac{1 - 6x_{AX} + 3x_{AX}^2 + 2x_{AX}^3 - 6x_{AX}^2 \log x_{AX}}{6(1 - x_{AX})^4} \\ & \left. + N_{iAX}^L N_{jAX}^{R*} \frac{m_{\tilde{\chi}_A^0}}{m_{l_j}} \frac{1 - x_{AX}^2 + 2x_{AX} \log x_{AX}}{(1 - x_{AX})^3} \right] \end{aligned}$$

$$A_a^{(n)R} = A_a^{(n)L} \Big|_{L \leftrightarrow R}$$

$$\text{where } x_{AX} = m_{\tilde{\chi}_A^0}^2 / m_{\tilde{l}_X}^2$$

Photon penguin contributions

E. Arganda and M.J. Herrero, PRD 73 (2006) 055003

$$A_1^{(c)L} = -\frac{1}{576\pi^2} C_{iAX}^R C_{jAX}^{R*} \frac{1}{m_{\tilde{\nu}_X}^2} \frac{16 - 45x_{AX} + 36x_{AX}^2 - 7x_A^3 + 6(2 - 3x_{AX}) \log x_{AX}}{(1 - x_{AX})^4}$$

$$\begin{aligned} A_2^{(c)L} = & -\frac{1}{32\pi^2} \frac{1}{m_{\tilde{\nu}_X}^2} \left[C_{iAX}^L C_{jAX}^{L*} \frac{2 + 3x_{AX} - 6x_{AX}^2 + x_{AX}^3 + 6x_{AX} \log x_{AX}}{6(1 - x_{AX})^4} \right. \\ & + C_{iAX}^R C_{jAX}^{R*} \frac{m_{l_i}}{m_{l_j}} \frac{2 + 3x_{AX} - 6x_{AX}^2 + x_{AX}^3 + 6x_{AX} \log x_{AX}}{6(1 - x_{AX})^4} \\ & \left. + C_{iAX}^L C_{jAX}^{R*} \frac{m_{\tilde{\chi}_A^-}}{m_{l_j}} \frac{-3 + 4x_{AX} - x_{AX}^2 - 2 \log x_{AX}}{(1 - x_{AX})^3} \right] \end{aligned}$$

$$A_a^{(c)R} = A_a^{(c)L} \Big|_{L \leftrightarrow R}$$

$$\text{where } x_{AX} = m_{\tilde{\chi}_A^-}^2 / m_{\tilde{\nu}_X}^2$$

Z-penguin contributions

E. Arganda and M.J. Herrero, PRD 73 (2006) 055003

$$F_{L(R)} = F_{L(R)}^{(n)} + F_{L(R)}^{(c)}$$

$$\begin{aligned}
 F_L^{(n)} &= -\frac{1}{16\pi^2} \left\{ N_{iBX}^R N_{jAX}^{R*} \left[2E_{BA}^{R(n)} C_{24}(m_{\tilde{l}_X}^2, m_{\tilde{\chi}_A^0}^2, m_{\tilde{\chi}_B^0}^2) - E_{BA}^{L(n)} m_{\tilde{\chi}_A^0} m_{\tilde{\chi}_B^0} C_0(m_{\tilde{l}_X}^2, m_{\tilde{\chi}_A^0}^2, m_{\tilde{\chi}_B^0}^2) \right] \right. \\
 &\quad \left. + N_{iAX}^R N_{jAY}^{R*} \left[2Q_{XY}^{\tilde{l}} C_{24}(m_{\tilde{\chi}_A^0}^2, m_{\tilde{l}_X}^2, m_{\tilde{l}_Y}^2) \right] + N_{iAX}^R N_{jAX}^{R*} \left[Z_L^{(l)} B_1(m_{\tilde{\chi}_A^0}^2, m_{\tilde{l}_X}^2) \right] \right\} \\
 F_R^{(n)} &= F_L^{(n)} \Big|_{L \leftrightarrow R} \\
 F_L^{(c)} &= -\frac{1}{16\pi^2} \left\{ C_{iBX}^R C_{jAX}^{R*} \left[2E_{BA}^{R(c)} C_{24}(m_{\tilde{\nu}_X}^2, m_{\tilde{\chi}_A^-}^2, m_{\tilde{\chi}_B^-}^2) - E_{BA}^{L(c)} m_{\tilde{\chi}_A^-} m_{\tilde{\chi}_B^-} C_0(m_{\tilde{\nu}_X}^2, m_{\tilde{\chi}_A^-}^2, m_{\tilde{\chi}_B^-}^2) \right] \right. \\
 &\quad \left. + C_{iAX}^R C_{jAY}^{R*} \left[2Q_{XY}^{\tilde{\nu}} C_{24}(m_{\tilde{\chi}_A^-}^2, m_{\tilde{\nu}_X}^2, m_{\tilde{\nu}_Y}^2) \right] + C_{iAX}^R C_{jAX}^{R*} \left[Z_L^{(l)} B_1(m_{\tilde{\chi}_A^-}^2, m_{\tilde{\nu}_X}^2) \right] \right\} \\
 F_R^{(c)} &= F_L^{(c)} \Big|_{L \leftrightarrow R}
 \end{aligned}$$

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However, note that in the decay width one has

$$\begin{aligned}F_{LL} &= \frac{F_L Z_L^{(l)}}{g^2 \sin^2 \theta_W m_Z^2} \\F_{RR} &= F_{LL}|_{L \leftrightarrow R} \\F_{LR} &= \frac{F_L Z_R^{(l)}}{g^2 \sin^2 \theta_W m_Z^2} \\F_{RL} &= F_{LR}|_{L \leftrightarrow R}\end{aligned}$$