

# Theoretical overview on $t\bar{t}$ and single top

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- I.: **Basic facts about the top**
- II.: **Top-pair production**
- III.: **Single top production**

# Basic facts about top

The essential numbers:

Discovered at the Tevatron in 1995

Mass:

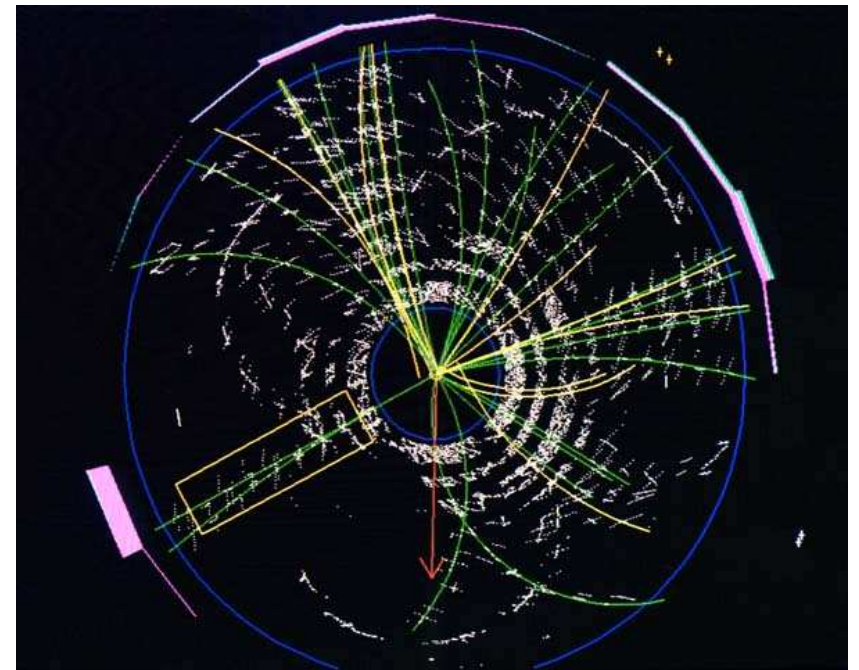
$$m_t = 173.1 \pm 0.6 \pm 1.1 \text{ GeV}$$

Width:

$$\Gamma = 2.0^{+0.7}_{-0.6} \text{ GeV}$$

Branching fraction:

$$\frac{\Gamma(Wb)}{\Gamma(Wq)} = 0.99^{+0.09}_{-0.08}$$



A  $t\bar{t}$  event from CDF.

# Implications

The top quark is special:

- The large top mass sets a hard scale.
- Lifetime shorter than characteristic hadronization time scale.

⇒ Top physics is described by perturbative QCD.

- The top mass is close to the electro-weak breaking scale.

⇒ If there is new physics associated with electro-weak symmetry breaking, top physics is a place to look for.

## Theoretical aspects of the top mass

$$\mathcal{L} = \bar{\Psi}(i\not{D} - m_{\text{bare}})\Psi$$

Renormalisation:

$$m_{\text{bare}} = Z_m m_{\text{renorm}}$$

$Z_m$  and hence  $m_{\text{renorm}}$  depend on the renormalisation scheme !

Conventional choices:

- The  $\overline{\text{MS}}$ -scheme: The  $\overline{\text{MS}}$ -mass  $m_{\overline{\text{MS}}}(\mu)$  is scale-dependent.
- The on-shell-scheme: The mass  $m_{\text{pole}}$  is defined as the pole of the propagator.

In perturbation theory one can convert between different schemes !

# The precision and accuracy on the top mass

With increasing experimental precision, more theoretical issues become relevant:

- The top quark is neither stable nor a colour-singlet.

- This re-introduces non-perturbative effects
- The pole mass is ambiguous by an amount  $O(\Lambda_{\text{QCD}})$ .

Bigi, Shifman, Uraltsev, Vainshtein, '94, Beneke, '94, Smith, Willenbrock, '96, Skands, Wicke, '07

- Experimentally measured are the decay products of the top.

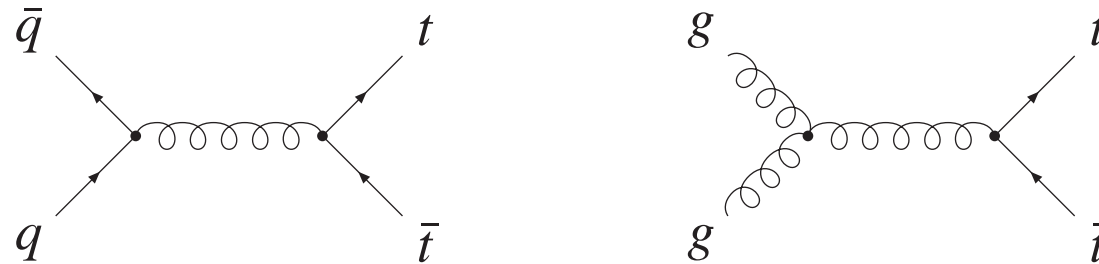
- For top measurements based on reconstruction:  
The  $\overline{\text{MS}}$  mass distorts the Breit-Wigner shape.

**Solution:** Carefully define a short-distance mass, insensitive to non-perturbative effects, and relate the experimental measurement to this short-distance mass.

Fleming, Hoang, Mantry, Stewart, '07

# Top-pair production

The leading-order Feynman diagrams:



The quark-antiquark channel dominates at the Tevatron, while the gluon-gluon channel dominates at the LHC.

We are interested in the **inclusive process**

$$pp \rightarrow t\bar{t} + X$$

as well as the **exclusive processes**

$$pp \rightarrow t\bar{t} + 0 \text{ jets}, \quad pp \rightarrow t\bar{t} + 1 \text{ jet}, \quad pp \rightarrow t\bar{t} + 2 \text{ jets}, \quad \dots$$

# Status of NLO calculations

- $pp \rightarrow t\bar{t}$

Nason, Dawson, Ellis, '88,

Beenakker, Kuijf, van Neerven, Smith, '89,

$$pp \rightarrow b\bar{b}W^+W^-$$

Bevilaqua, Czakon, van Hameren, Papadopoulos, Worek, '10

Denner, Dittmaier, Kallweit, Pozzorini, '10

- $pp \rightarrow t\bar{t} + 1 \text{ jet}$

Dittmaier, Uwer, S.W., '07,

Melnikov, Schulze, '10

- $pp \rightarrow t\bar{t} + 2 \text{ jets}$

Bevilaqua, Czakon, Papadopoulos, Worek, '10

## sub-process $pp \rightarrow t\bar{t} + b\bar{b}$

Bredenstein, Denner, Dittmaier, Pozzorini, '09,

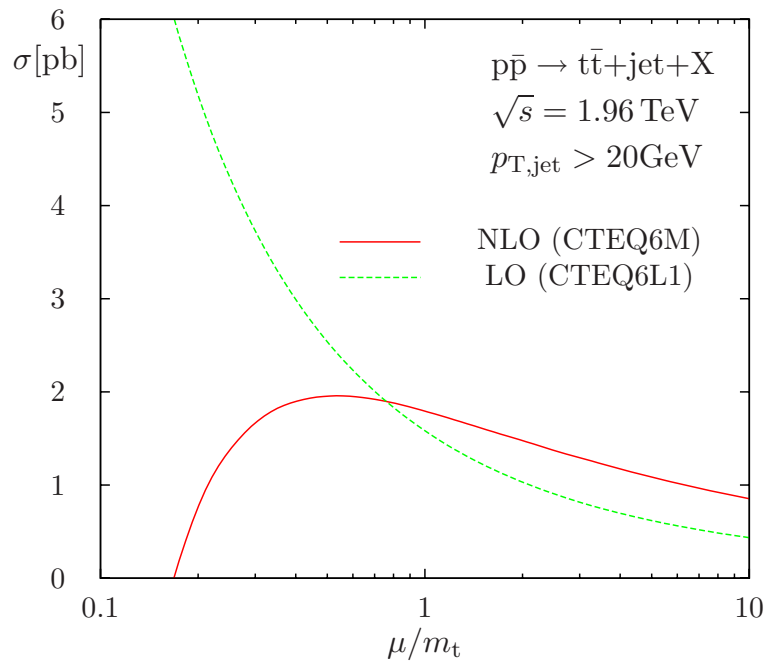
Bevilaqua, Czakon, Papadopoulos, Pittau, Worek, '09

# Numerical results on $t\bar{t} + \text{jet}$ production

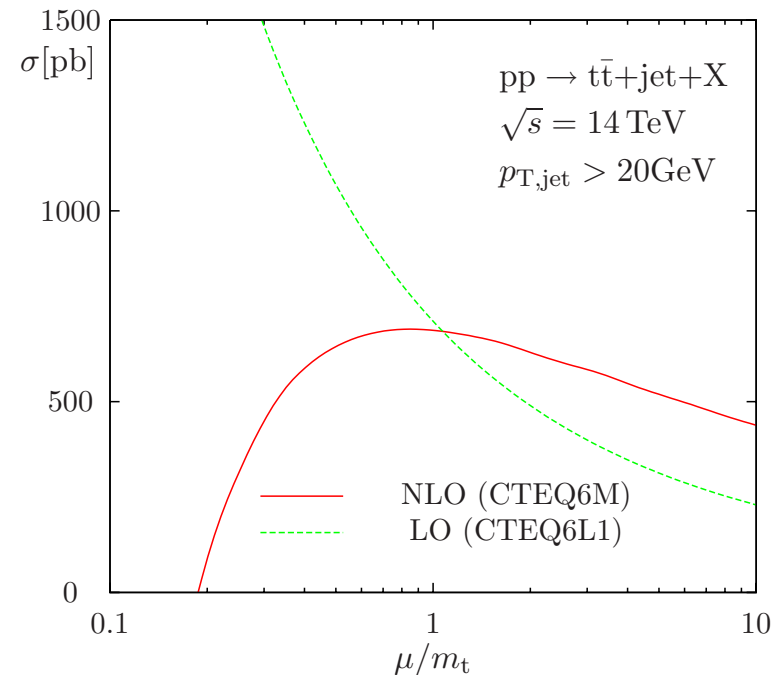
Dependence of the cross section on renormalisation and factorisation scale:

Leading order is proportional to  $\alpha_s^3$  !

Tevatron:



LHC:



Jet definition:  $k_{\perp}$ -algorithm with  $R = 1$  applied to particles other than  $t$  or  $\bar{t}$ .



# Status of NNLO calculations

The  $\alpha_s^4$ -correction to  $pp \rightarrow t\bar{t}$  requires

- The **two-loop amplitudes**  $gg \rightarrow t\bar{t}$ ,  $q\bar{q} \rightarrow t\bar{t}$

work in progress: Czakon, Mitov, Moch,

Bonciani, Ferroglia, Gehrmann, Maitre, von Manteufel, Studerus

- The **squared one-loop amplitudes**  $gg \rightarrow t\bar{t}$ ,  $q\bar{q} \rightarrow t\bar{t}$

Kniehl, Körner, Merebashvili, Rogal, '08,

Anastasiou, Aybat, '08

- A method to **handle the infrared divergences at NNLO**,  
in particular initial state partons and massive partons.

work in progress: Bierenbaum, Czakon, Mitov,

Boughezal, Daleo, Gehrmann, Gehrmann-De Ridder, Luisoni, Monni, Ritzmann,

Glover, Pires

# Resummation

In multi-scale problems there can be large logarithms in the perturbative expansion:

$$\alpha_s^n \ln^j \beta$$

Top-pair production in the threshold region

$$\beta = \sqrt{1 - \frac{4m_t^2}{\hat{s}}}$$

⇒ sum large logarithms to improve perturbation theory

In addition, Coulomb singularities of the form

$$\frac{1}{\beta^k}$$

# NNLL resummation

**Soft gluon resummation** at next-to-next-to-leading logarithmic accuracy:

Moch, Uwer, '08,

Czakon, Mitov, Sterman, '09,

Kidonakis, '10,

Ahrens, Ferroglia, Neubert, Pecjak, Yang, '10,

Beneke, Falgari, Klein, Schwinn, '11

Can **re-expand NNLL** to obtain an “**approximate NNLO**” result.

Differences between the various groups:

- Exact **definition of the resummation variable**.
- Resummation of **soft gluons only** or also **Coulomb terms** ?
- Which **scale dependent parts** are included ?

# NLO with parton showers

Parton showers are **exclusive and resum large logarithms** at LL accuracy.

**Avoid double-counting** when combining NLO calculations with parton showers:  
MC@NLO and POWHEG.

Frixione, Webber, '02, Nason, '04

Convenient tool: POWHEG-BOX

Alioli, Nason, Oleari, Re, '10.

Recent application to  $pp \rightarrow t\bar{t} + 1 \text{ jet}$ :

Kardos, Papadopoulos, Trocsanyi, '11

Alioli, Moch, Uwer, '11

## Spin correlations

Within the Standard Model the top decays purely through left-handed weak decay.

In dilepton channel of top-pair production:

Correlation between top and anti-top spins transferred to leptons.

$$\frac{1}{\sigma} \frac{d^2\sigma}{d\cos\theta_l d\cos\theta_{\bar{l}}} = \frac{1}{4} (1 - C \cos\theta_l \cos\theta_{\bar{l}})$$

$$C(D0) = 0.1^{+0.45}_{-0.45}$$

$$C(\text{CDF}) = 0.6 \pm 0.5 \pm 0.2 \quad (\text{EPS 2011})$$

$$C(\text{Theory}) = 0.777^{+0.027}_{-0.042}$$

# The forward-backward asymmetry at the Tevatron

Forward-backward or charge asymmetry in  $q\bar{q} \rightarrow t\bar{t} (+\text{jets})$

Origin: Interference of  $C$ -odd with  $C$ -even parts.

$q\bar{q} \rightarrow t\bar{t}$ : asymmetry appears first at NLO (Kühn, Rodrigo '98).

$A_{FB}$  @ NLO requires NNLO  $p\bar{p} \rightarrow t\bar{t}$

$q\bar{q} \rightarrow t\bar{t} + \text{jet}$ : asymmetry is LO effect (Halzen, Hoyer, Kim, '87, Bowen, Ellis, Rainwater, '05).

$A_{FB}$  @ NLO can be deduced from NLO  $p\bar{p} \rightarrow t\bar{t} + \text{jet}$ .

# The asymmetry for $t\bar{t}$ at the Tevatron

Lab frame:

$$A_{FB}(\text{CDF}) = (15.0 \pm 5.5) \%,$$
$$A_{FB}(\text{Theory}) = (5.8 \pm 0.9) \%,$$

$t\bar{t}$  rest frame:

$$A_{FB}(\text{CDF}) = (20.0 \pm 7.3) \%,$$
$$A_{FB}(\text{D0}) = (19.6 \pm 6.5) \%,$$
$$A_{FB}(\text{Theory}) = (8.7 \pm 1.0) \%,$$

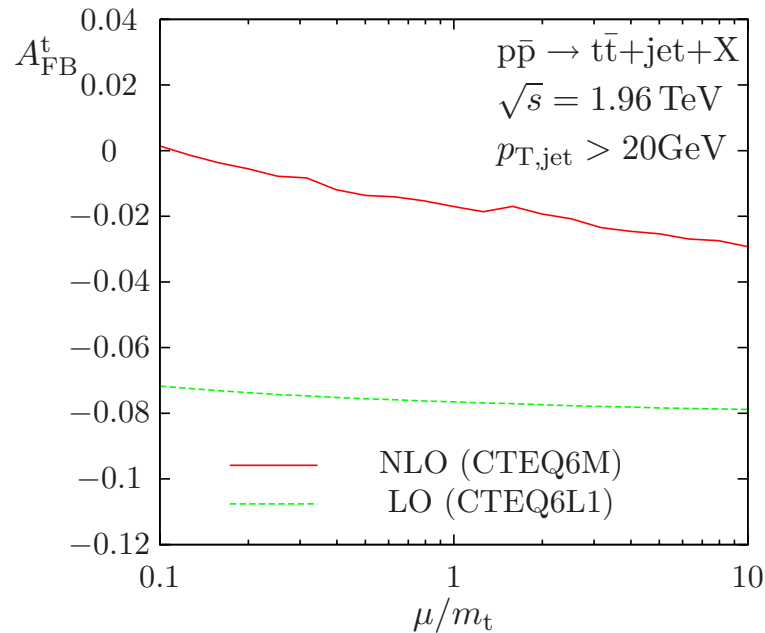
Theory status: LO QCD (from NLO  $p\bar{p} \rightarrow t\bar{t}$ )

electroweak corrections small Hollik, Kollar, '07, Bernreuther, Si, '10, Kühn, Rodrigo, '11,

soft gluon corrections small Kidonakis, '11, Ahrens, Ferroglia, Neubert, Pecjak, Yang, '11

There is a certain tension ...

# The forward-backward asymmetry in $t\bar{t} + \text{jet}$



$$\sigma^\pm = \sigma(y_t > 0) \pm \sigma(y_t < 0),$$

$$A_{FB,LO}^t = \frac{\sigma_{LO}^-}{\sigma_{LO}^+},$$

$$A_{FB,NLO}^t = \frac{\sigma_{LO}^-}{\sigma_{LO}^+} \left( 1 + \frac{\delta\sigma_{NLO}^-}{\sigma_{LO}^-} - \frac{\delta\sigma_{NLO}^+}{\sigma_{LO}^+} \right).$$

$$(\mu = \mu_{ren} = \mu_{fact})$$

- $A_{FB,LO}^t = O(\alpha_s^0)$ , i.e. no dependence on  $\mu_{ren}$   
mild dependence on  $\mu_{fact} \ll$  theoretical uncertainty !
- $A_{FB,NLO}^t$  depends on  $\mu_{fact}$  and  $\mu_{ren}$   
asymmetry almost washed out by scale dependence.



## The charge asymmetry at the LHC

No forward-backward asymmetry in the lab frame at the LHC due to symmetric  $pp$  initial state.

But:  $t$  tend to follow initial  $q$ , while  $\bar{t}$  tend to follow initial  $\bar{q}$ .

Initial  $q$ 's tend to have a larger momentum fraction (valence-like) than initial  $\bar{q}$ 's (always sea quarks).

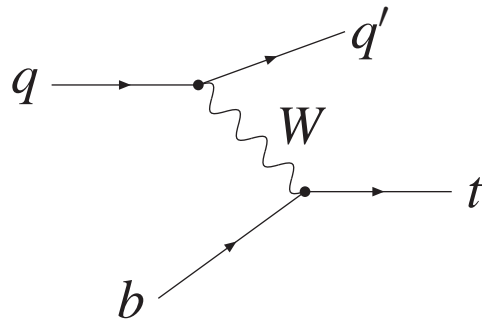
⇒ Rapidity distribution of  $t$  should be broader than the rapidity distribution of  $\bar{t}$ .

Complication: At the LHC  $q\bar{q}$  initial state gives only a small fraction of the events, dominated by  $gg$ .

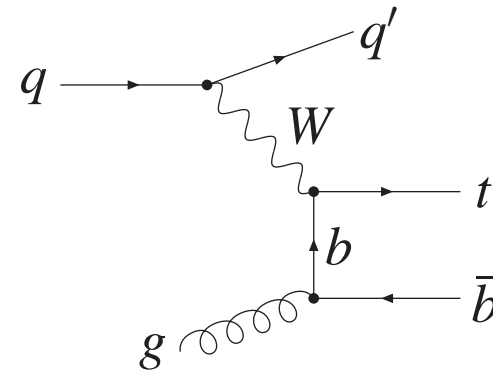
In view of the Tevatron results this measurement should be worth the effort !

# Single top production

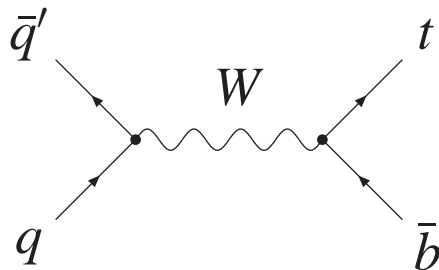
Top quark can also be produced singly by an electroweak  $Wtb$ -vertex:



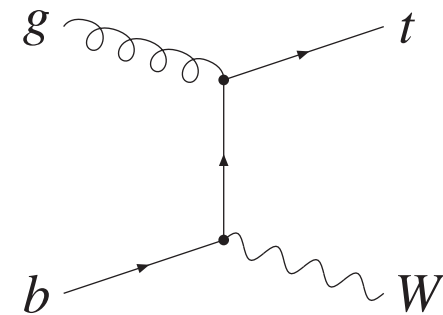
Flavour excitation



$W$ -gluon fusion



s-channel



Associated  $W$ -production

# Single top production

Physics motivation for **single top production**:

- Process sensitive to  $Wtb$  vertex.  
Non-standard couplings can give a hint on physics beyond SM.
- Direct measurement of CKM matrix element  $V_{tb}$ .  
Verification of unitarity of CKM matrix.
- The top quark is produced left-handed.  
Since no hadronization occurs, spin correlations survive in the final decay products.
- The flavour excitation channel can be used to extract the  $b$ -quark density.

# Status of NLO calculations

- **s-channel and t-channel:**

Stelzer, Sullivan, Willenbrock, '98, Harris, Laenen, Phaf, Sullivan, S.W., '02, Cao, Schwienhorst, Yuan, '04,  
Campbell, Ellis, Tramontana, '04, Campbell, Frederix, Maltoni, Tramontano, '09,  
Falgari, Giannuzzi, Mellor, Signer, '11

- **Associated  $W$ -production:**

Campbell, Tramontana, '05, Frixione, Laenen, Motylinski, Webber, White, '08

- **Resummation:**

Kidonakis, '10, Zhu, Li, Wang, Zhang, '10

- **MC@NLO:**

Frixione, Laenen, Motylinski, Webber, '05

- **POWHEG:**

Alioli, Nason, Oleari, Re, '09

## The CKM matrix element $V_{tb}$

$V_{tb}$  is known indirectly from unitarity

$$|V_{ub}|^2 + |V_{cb}|^2 + |V_{tb}|^2 = 1$$

to a very high precision:  $|V_{tb}| = 0.9990 - 0.9993$

No way to measure  $|V_{tb}|$  directly to this precision !

Sideremark: From top-pair production at the Tevatron:

$$\frac{BR(t \rightarrow Wb)}{BR(t \rightarrow Wq)} = \frac{|V_{tb}|^2}{|V_{td}|^2 + |V_{ts}|^2 + |V_{tb}|^2} = 0.99^{+0.09}_{-0.08}$$

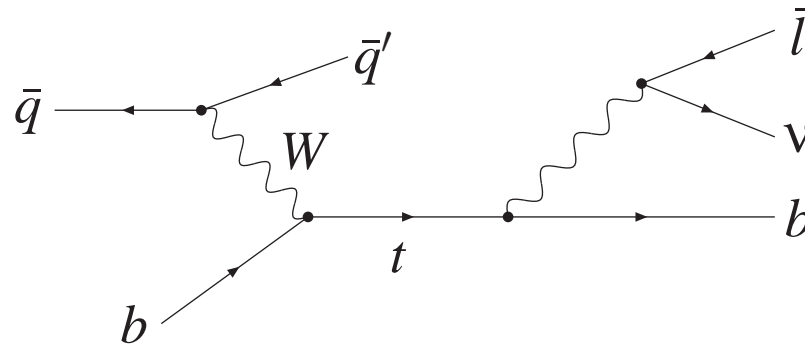
If we do not assume three generations, then it follows only

$$|V_{tb}| \gg |V_{ts}|, |V_{td}|$$

**Single top production:** Direct measurement of  $|V_{tb}|$  without any assumptions on the number of generations.

# Spin correlations

At the electroweak  $Wtb$ -vertex the **top quark is produced left-handed**.



Since no hadronization occurs, **spin correlations survive** in the final decay products.

Of particular importance is the **angle between the lepton  $\bar{l}$  and the light-quark jet  $\bar{q}'$** .

Jezabek, Kühn, '94

Mahlon, Parke, '97

van der Heide, Laenen, Phaf, S.W., '00

## Angular correlations

In W-gluon fusion or flavour excitation the top quark is highly polarized along the direction of the  $\bar{d}$ -quark. In addition the  $u$ -quark density is the largest among the quark densities. Look at the quantity

$$a = \frac{1}{2} (1 + \cos \theta_{q\bar{l}})$$

where  $\theta_{q\bar{l}}$  is the angle between the light quark jet and the charged lepton.

In the rest frame of the top:

$$\frac{d\sigma}{da} = \sigma(2Pa + (1 - P)),$$

The slope of this distribution is given by

$$2P_{\text{signal}}\sigma_{\text{signal}} + 2P_{\text{background}}\sigma_{\text{background}}$$

# Summary

- Top physics is a very active field in theory.
- Top mass is very close to the electroweak symmetry breaking scale.
- The value of the top mass is essential for many precision measurements.
- Angular distributions are very interesting:
  - Spin correlations in top-pair production and single top.
  - Charge asymmetry at Tevatron and LHC.