

SUSY developments in FeynRules

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IPHC

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Outline

- 1 Introduction to supersymmetry
- 2 Superspace Module (C. Duhr, B. Fuks)
- 3 Spin 3/2 Project ("Spin 3/2 collaboration")
- 4 Spectrum generator generator (Alloul, De Causmaecker, Fuks, Rausch de Traubenberg)
- 5 Prospects
- 6 Resume

- 1 Introduction to supersymmetry
 - Motivating supersymmetry
 - Superspace and superfield formalism
- 2 Superspace Module (C. Duhr, B. Fuks)
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Supersymmetry as a solution

Standard Model of particle physics

- Is one of the most tested theories in physics
- Has some open questions.

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One of the most popular issues

- Hierarchy problem.
- Dark matter.
- GUT theories.

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Q being a SUSY generator :

$$Q|Boson\rangle = |Fermion\rangle \quad Q|Fermion\rangle = |Boson\rangle$$

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Minimal Supersymmetric Standard Model (MSSM)

- Only one generator (Minimal).
- Quarks \Leftrightarrow Squarks, Leptons \Leftrightarrow Sleptons.
- Gauge/Higgs bosons \Leftrightarrow Gauginos/Higgsinos.

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New particles

- SM-fermion \mapsto new boson.
- SM-boson \mapsto new fermion.

Superspace and superfield formalism

Superspace

A point in superspace is now defined as

$$\phi(x^\mu) \longrightarrow \phi(x^\mu, \theta, \bar{\theta}),$$

$(\theta, \bar{\theta})$: Majorana fermion.

Superfields

Chiral (matter) Superfields

$$\Phi = (\phi, \psi, \dots)$$

ϕ : scalar component

ψ : fermionic component

Vector (gauge) Superfields

$$V = (\lambda, v_\mu, \dots)$$

λ : fermionic component

v_μ : bosonic component

... stand for auxiliary fields.

Susy Lagrangian

- Kinematic terms and gauge interactions for the left-handed (s)quarks in the MSSM

In components (13 terms)

$$D_\mu \tilde{Q}_i^\dagger D^\mu \tilde{Q}^i + \frac{1}{2} (\chi_{Q_i}^j \sigma^\mu D_\mu \bar{\chi}_{Q_i} - D_\mu \chi_{Q_i}^j \sigma^\mu \bar{\chi}_{Q_i}) + F_{Q_i}^\dagger F_{Q_i}^i + i\sqrt{2} \left[\frac{1}{6} g' \tilde{Q}^i \tilde{B} \cdot \tilde{\chi}_{Q_i} + g \tilde{W}^k \tilde{\chi}_{Q_i} \frac{\sigma^k}{2} \tilde{Q}^i + g_s \tilde{G}^a \tilde{\chi}_{Q_i} T^a \tilde{Q}^i + h.c. \right] - g' D_B \tilde{Q}_i^\dagger \tilde{Q}^i - g D_{W^k} \tilde{Q}_i^\dagger \frac{\sigma^k}{2} \tilde{Q}^i - g_s D_{G^a} \tilde{Q}_i^\dagger T^a \tilde{Q}^i$$

Susy Lagrangian

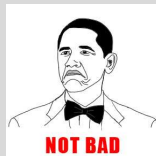
- Kinematic terms and gauge interactions for the left-handed (s)quarks in the MSSM

In components (13 terms)

$$D_\mu \tilde{Q}_i^\dagger D^\mu \tilde{Q}^i + \frac{1}{2} (\chi_Q^i \sigma^\mu D_\mu \bar{\chi}_{Qi} - D_\mu \chi_Q^i \sigma^\mu \bar{\chi}_{Qi}) + F_{Q_i}^\dagger F_{Q_i}^i + i\sqrt{2} \left[\frac{1}{6} g' \tilde{Q}^i \vec{B} \cdot \vec{\chi}_{Qi} + g \vec{W}^k \bar{\chi}_{Qi} \frac{\sigma^k}{2} \tilde{Q}^i + g_s \vec{G}^a \bar{\chi}_{Qi} T^a \tilde{Q}^i + h.c. \right] - g' D_B \tilde{Q}_i^\dagger \tilde{Q}^i - g D_{W^k} \tilde{Q}_i^\dagger \frac{\sigma^k}{2} \tilde{Q}^i - g_s D_{G^a} \tilde{Q}_i^\dagger T^a \tilde{Q}^i$$

In superfields (1 term)

$$\left[Q_i^\dagger e^{-2\frac{1}{6}g'V_B} e^{-2gV_{W^k}} \frac{\sigma^k}{2} e^{-2g_s V_{G^a}} \frac{T^a}{2} Q^i \right]_{|\theta \cdot \theta \bar{\theta} \cdot \bar{\theta}}$$



The superspace formalism could be a useful tool for model building

- 1 Introduction to supersymmetry
- 2 Superspace Module (C. Duhr, B. Fuks)
 - Vector superfields
 - Chiral superfields
- 3 Spin 3/2 Project ("Spin 3/2 collaboration")
- 4 Spectrum generator generator (Alloul, De Causmaecker, Fuks, Rausch de Traubenberg)
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Defining Vector superfields

C. Duhr, B. Fuks (CPC '11)

Conventions → Fuks, Rausch de Traubenberg (Ellipses '11)

Vector superfield in the Wess-Zumino gauge

$$V_{W.Z.}(x, \theta, \bar{\theta}) = \theta \sigma^\mu \bar{\theta} v_\mu + i \theta \cdot \theta \bar{\theta} \cdot \bar{\lambda} - i \bar{\theta} \cdot \bar{\theta} \theta \cdot \lambda + \frac{1}{2} \theta \cdot \theta \bar{\theta} \cdot \bar{\theta} D.$$

v_μ gauge vector, $(\lambda, \bar{\lambda})$ Majorana fermion, D auxiliary field.

Declaring the $SU(3)_c$ vector superfield

Model file content	Precisions
VSF[1] == {	Label of the vector superfield
ClassName → GSF	
GaugeBoson → G	must be declared properly
Gaugino → gow	must be declared properly
Indices → {[IndexGluon]}	
}	

Auxiliary fields are automatically generated (not explicitly present).

Vector Langrangians

- Lagrangian associated to the **vector superfields**.
 - **Gauge kinetic terms**.
 - Entirely fixed by gauge and SUSY **invariance**.

Non-abelian groups (abelian limit easy to obtain).

$$\begin{aligned}
 \mathcal{L}_{\text{vector}} &= \frac{1}{16g^2\tau_R} \text{Tr}(W^\alpha W_\alpha)|_{\theta\theta} + \frac{1}{16g^2\tau_R} \text{Tr}(\bar{W}_{\dot{\alpha}} \bar{W}^{\dot{\alpha}})|_{\bar{\theta}\bar{\theta}} \\
 &= -\frac{1}{4} F_{\mu\nu}^a F_a^{\mu\nu} + i\bar{\lambda}_a \bar{\sigma}^\mu D_\mu \lambda^a + \frac{1}{2} D_a D^a
 \end{aligned}$$

Automatic extraction of the vector Lagrangian of a model

all vector superfields

VSFKineticTerms[]

one vector superfield

VSFKineticTerms[GSF]

Defining Chiral superfields

Chiral superfields

$$\Phi(y, \theta) = \phi(y) + \sqrt{2}\phi \cdot \psi(y) - \theta \cdot \theta F(y) \quad \text{with } y^\mu = x^\mu - i\theta\sigma^\mu\bar{\theta}$$

- Describes matter multiplets.
- One scalar field ϕ , one Weyl fermion ψ , one auxiliary field F

Declaring the right-handed quark superfield

Model file content		Precisions
CSF[1] == {		Label of the chiral superfield
ClassName	-> QL	
Chirality	-> Left	
Weyl	-> QLw	must be declared properly
Scalar	-> QLs	must be declared properly
QuantumNumbers	-> { Q -> 2/3}	must be declared properly
Indices	-> { Index[Gen], Index[Colour]}	
}		

Auxiliary fields are automatically generated (not explicitly present).

Matter Lagrangians

- Lagrangian associated to the **chiral superfields**.
 - **Gauge interactions and kinetic terms** for chiral superfields.
 - Entirely fixed by SUSY and gauge **invariance**.

Example for $SU(3)_c \times SU(2)_L \times U(1)_Y$

$$\mathcal{L}_{matter} = [\Phi^\dagger(x, \theta, \bar{\theta}) \exp^{-2y_\Phi g' V_B} \exp^{-2g V_W} \exp^{-2g_s V_G} \Phi(x, \theta, \bar{\theta})]_{|\theta\theta\bar{\theta}\bar{\theta}}$$

(Non-abelian vector superfields contain group representation matrices.)

Automatic extraction of the matter Lagrangian of a model

all chiral superfields `CSFKineticTerms []`

one chiral superfield `CSFKineticTerms [QL]`

Superfield dedicated commands

Superfield Components

Get θ -Component	ThetaComponent [SF]
Get $\theta\theta$ -Component	Theta2Component [SF]
Get $\theta\theta\bar{\theta}\bar{\theta}$ -Component	Theta2Thetabar2Component [SF]

Transformation laws

$$\delta_\epsilon \Phi(x, \theta, \bar{\theta}) = i(\epsilon \cdot Q + \bar{Q} \cdot \bar{\epsilon}) \rightarrow \text{DeltaPhi} = \text{DeltaSUSY}[\text{UR}, \text{eps1}]$$

$$[\delta_\epsilon \Phi(x, \theta, \bar{\theta})]_{|\theta} \rightarrow \text{ThetaComponent}[\text{DeltaSUSY}[\text{UR}, \text{eps1}]]$$

Superfield strength tensor W_α

$$W_\alpha = -\frac{1}{4} \bar{D} \cdot \bar{D} \exp^{2gV} D_\alpha \exp^{-2gV} \quad \text{SuperfieldStrengthL}[\text{SF}, \text{gauge index}]$$

$$\bar{W}_{\dot{\alpha}} = -\frac{1}{4} D \cdot D \exp^{-2gV} \bar{D}_{\dot{\alpha}} \exp^{2gV} \quad \text{SuperfieldStrengthR}[\text{SF}, \text{gauge index}]$$

Full Susy Lagrangian

Gauge Group

Full Susy Lagrangian

Gauge Group

**Vector Superfields
Matter Superfields**

Full Susy Lagrangian

Gauge Group

**Vector Superfields
Matter Superfields**

**Superpotential
Lsoft**

Full Susy Lagrangian

Gauge Group

Vector Superfields
Matter Superfields

Superpotential
 \mathcal{L}_{soft}

AUTOMATIC

$$\mathcal{L} = [\Phi^\dagger e^{-2gV} \Phi]_{|\theta, \theta \bar{\theta}, \bar{\theta}} + \frac{1}{16g^2 \tau_R} \text{Tr}(W^\alpha W_\alpha)_{|\theta, \theta} + \frac{1}{16g^2 \tau_R} \text{Tr}(\bar{W}_{\dot{\alpha}} \bar{W}^{\dot{\alpha}})_{|\bar{\theta}, \bar{\theta}} \\ + W(\Phi)_{|\theta, \theta} + W^*(\Phi^\dagger)_{|\bar{\theta}, \bar{\theta}} + \mathcal{L}_{soft}$$

\mathcal{L}_{soft} is the soft-susy breaking lagrangian

Lagrangian commands

Total Lagrangian

```
Theta2Thetabar2Component[CSFKineticTerms[]] +  
Theta2Component[VSFKineticTerms[] + Superpot] +  
Thetabar2Component[VSFKineticTerms[] + HC[Superpot]] +  
LSoft
```

Eliminating the auxiliary fields

```
lagr = SolveEqMotionD[lagr]  
lagr = SolveEqMotionF[lagr]
```

Back to four-component fermions

```
Usual FEYNRULES routine.  
lagr = WeylToDirac[lagr]
```

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 - FEYNRULES side
 - Interface side
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Theory expectations

FeynRules-superfield can be used to extract Goldstino Lagrangian

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FeynRules-superfield can be used to extract Goldstino Lagrangian

- Variation of the SUSY Lagrangian (using FEYNRULES)

Using the supercharges

$$\delta_\epsilon \mathcal{L} = \partial_\mu K^\mu$$

Using Noether theorem

$$\delta_\epsilon \mathcal{L} = \partial_\mu \left[\frac{\delta \mathcal{L}}{\delta (\partial_\mu X)} \delta_\epsilon X \right]$$

- Result to be reproduced

$$J^\mu = \sqrt{2} D_\nu \phi_i^\dagger \sigma^\nu \bar{\sigma}^\mu \psi^i + i\sqrt{2} \sigma^\mu \bar{\psi}_i W^{*i} - \frac{i}{2} \sigma^\rho \bar{\sigma}^\nu \sigma^\mu \bar{\lambda}_a F_{\nu\rho}^a + g \phi_i^\dagger \sigma^\mu \bar{\lambda} \phi^i$$

- Supercurrent conservation \Rightarrow Goldstino (ψ_1) interaction Lagrangian

$$\mathcal{L} = \frac{1}{2\sqrt{2}} \frac{1}{\langle F^1 \rangle} \psi^1 \cdot \partial_\mu J + \frac{1}{2\sqrt{2}} \frac{1}{\langle F_1^\dagger \rangle} \bar{\psi}^1 \cdot \partial_\mu \bar{J}$$

FEYNRULES implementation

Declare Goldstino

Model file content	Precisions
<pre>CSF[100] == { ClassName -> GLDSF Chirality -> Left Weyl -> GLDw Scalar -> GLDs }</pre>	<p>Label of the chiral superfield</p> <p>must be declared properly</p> <p>must be declared properly</p>

Rarita-Schwinger field

→ **Not** a superfield

⇒ Only declared in `M$ClassesDescription` with classe name `RW`

Supercurrent

```
JJ = SuperCurrent[Lvector,Lchiral,Lsuperpot,spin index,lorentz index];
```

Interfaces

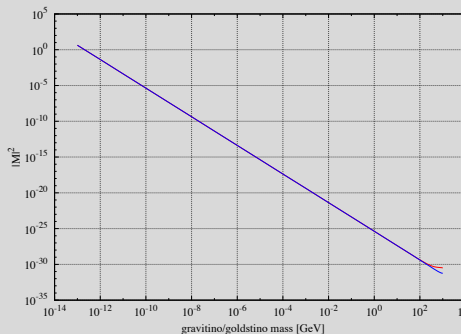
Working Interfaces

CALCHEP, MG5 (UFO)

→ working

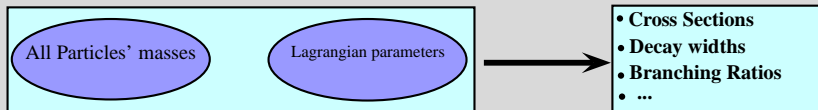
Numerical codes

On-going validation

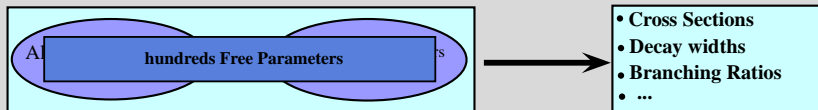


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 - Motivations
 - Renormalization Group Equations
 - Scalar Potential and mass matrices
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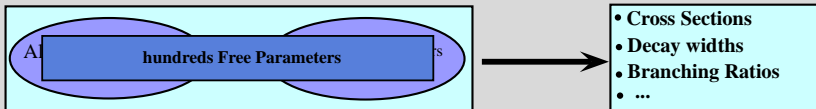
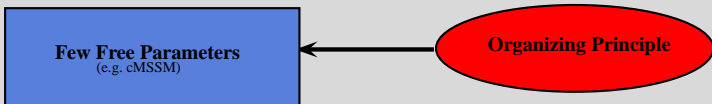
What are Susy theories phenomenological implications?



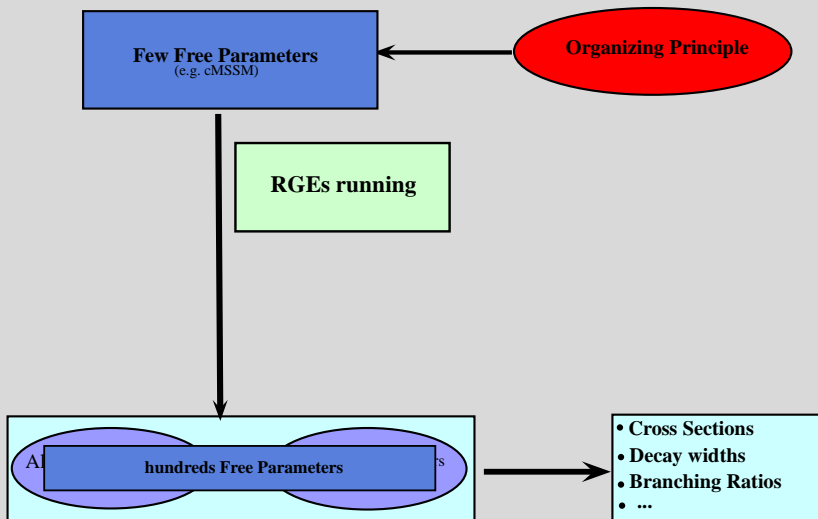
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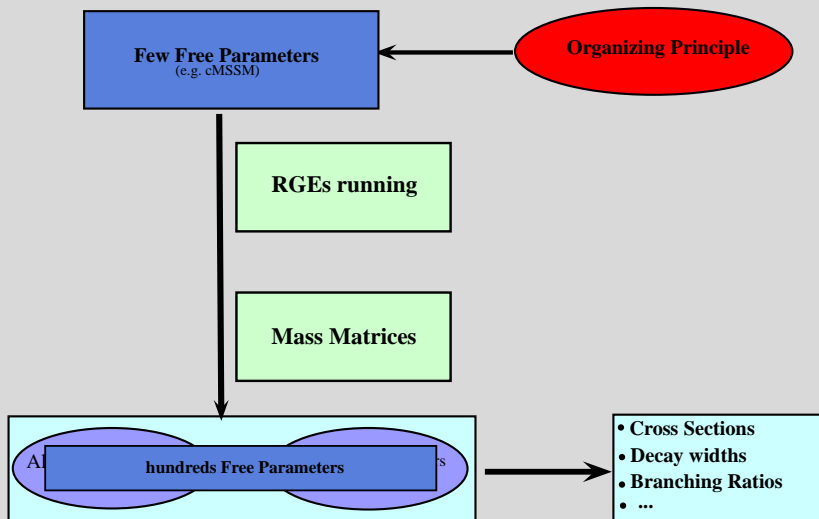
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Obtaining the RGEs

Alloul, Fuks, Raush de Trautenberg (Les Houches '11 Proceedings)

New way of defining the superpotential

Ex : Up-type quarks couplings

```
yu[ff1, ff2] UR[ff1, cc1] SUDot[QL[aa, ff2, cc1],HU[aa],aa]
```

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Superpotential

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```

```
graph TD; A["New way of defining the superpotential  
Ex : Up-type quarks couplings  
yu[ff1, ff2] UR[ff1, cc1] SUDot[QL[aa, ff2, cc1],HU[aa],aa]"] --> B((Superpotential)); A --> C((LSoft));
```

Superpotential

LSoft

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Ex : Up-type quarks couplings

```
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```



RGEs

```
RGE[LSoft, Superpotential]
```

Output from InSuRGE

Gauge coupling constants @ 2loop level

$$\frac{\partial}{\partial t} [g'] = \frac{199 (g')^2 g_s^5}{6400 \pi^4} + \frac{11 g_s^7}{160 \pi^4} + \frac{27 g_s^5 g_w^2}{1280 \pi^4} + \frac{33 (g')^3}{80 \pi^2} - \frac{7 g_s^3 (Y^d)_{\text{GEN}\$1, \text{GEN}\$2}^{**} Y^d_{\text{GEN}\$1, \text{GEN}\$2}}{640 \pi^4} - \frac{9 g_s^3 (Y^e)_{\text{GEN}\$1, \text{GEN}\$2}^{**} Y^e_{\text{GEN}\$1, \text{GEN}\$2}}{640 \pi^4} - \frac{13 g_s^3 (Y^u)_{\text{GEN}\$1, \text{GEN}\$2}^{**} Y^u_{\text{GEN}\$1, \text{GEN}\$2}}{640 \pi^4}$$

$$\frac{\partial}{\partial t} [g_w] = \frac{g_w^5}{64 \pi^4} + \frac{9 (g')^2 g_w^5}{1280 \pi^4} + \frac{3 g_s^2 g_w^5}{32 \pi^4} + \frac{21 g_w^7}{256 \pi^4} + \frac{g_w^3}{16 \pi^2} - \frac{3 g_w^3 (Y^d)_{\text{GEN}\$1, \text{GEN}\$2}^{**} Y^d_{\text{GEN}\$1, \text{GEN}\$2}}{128 \pi^4} - \frac{g_w^3 (Y^e)_{\text{GEN}\$1, \text{GEN}\$2}^{**} Y^e_{\text{GEN}\$1, \text{GEN}\$2}}{128 \pi^4} - \frac{3 g_w^3 (Y^u)_{\text{GEN}\$1, \text{GEN}\$2}^{**} Y^u_{\text{GEN}\$1, \text{GEN}\$2}}{128 \pi^4}$$

$$\frac{\partial}{\partial t} [g_s] = -\frac{9 g_s^5}{128 \pi^4} + \frac{11 (g')^2 g_s^5}{1280 \pi^4} + \frac{g_s^7}{8 \pi^4} + \frac{9 g_s^5 g_w^2}{256 \pi^4} - \frac{3 g_s^3 (Y^d)_{\text{GEN}\$1, \text{GEN}\$2}^{**} Y^d_{\text{GEN}\$1, \text{GEN}\$2}}{16 \pi^2} - \frac{g_s^3 (Y^u)_{\text{GEN}\$1, \text{GEN}\$2}^{**} Y^u_{\text{GEN}\$1, \text{GEN}\$2}}{64 \pi^4} - \frac{g_s^3 (Y^u)_{\text{GEN}\$1, \text{GEN}\$2}^{**} Y^u_{\text{GEN}\$1, \text{GEN}\$2}}{64 \pi^4}$$

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$$\frac{9 g_s^3 (Y^e)^{**}}{640 \pi^4} Y^{e, \text{GEN}\$1, \text{GEN}\$2} Y^{e, \text{GEN}\$1, \text{GEN}\$2} - \frac{13 g_s^3 (Y^u)^{**}}{640 \pi^4} Y^{u, \text{GEN}\$1, \text{GEN}\$2} Y^{u, \text{GEN}\$1, \text{GEN}\$2}$$

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$$\frac{g_w^3 (Y^e)^{**}}{128 \pi^4} Y^{e, \text{GEN}\$1, \text{GEN}\$2} Y^{e, \text{GEN}\$1, \text{GEN}\$2} - \frac{g_w^3 (Y^u)^{**}}{128 \pi^4} Y^{u, \text{GEN}\$1, \text{GEN}\$2} Y^{u, \text{GEN}\$1, \text{GEN}\$2}$$

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Validated against MSSM, NMSSM and RPV

RGEs Dedicated Commands

Gauge Constants RGEs

```
GaugeCouplingsRGE[SPMS,NLoop->1]
```

Gaugino Masses RGEs

```
GauginoMassesRGE[SPMS,SoftMS,NLoop->2]
```

Superpotential RGEs

```
SuperpotentialRGE[SPMS,NLoop->2]
```

LSoft RGEs

```
ScaSoftRGE[SoftNMS, SPNMS]
```

Number of loops

NLoop default value is set to 2

Not available yet for ScaSoftRGE.

Mass Matrices

Inspired by FR '10 work.

To have a mass spectrum

- Calculate the lagrangian without any rotation into mass eigenstates.
- Need to know which field acquires a vev ?
- Need to know which fields mix together ?

Implementation in FeynRules

- New `ExpandIndices` function (to avoid field rotations)
- New declarations in model file \rightarrow vevs and field mixings
- **Tree level in progress**
- Radiative corrections planned in near future

Preliminary results

```
In[57]:= GetMassMatrices[lagr]
```

The Lagrangian you entered contains physical fields, make sure these don't come from a previous field rotation. Calculations have been however performed.

Calculations took 35.8097

seconds to be performed. Results are stored in the variable MassMatrices

```
In[58]:= MassMatrices[[7, 2]].MatrixForm[MassMatrices[[7, 3]].MassMatrices[[7, 4]]
```

```
Out[58]= {bow, wow3, hdw1, huw2}.
```

$$\begin{pmatrix} M_1 & 0 & -\frac{1}{2} i g' v_d & \frac{1}{2} i g' v_u \\ 0 & M_2 & \frac{1}{2} i g_w v_d & -\frac{1}{2} i g_w v_u \\ -\frac{1}{2} i g' v_d & \frac{1}{2} i g_w v_d & 0 & -\mu \\ \frac{1}{2} i g' v_u & -\frac{1}{2} i g_w v_u & -\mu & 0 \end{pmatrix} \cdot \{bow, wow_3, hdw_1, huw_2\}$$

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Future evolutions

RGEs

- 1 Loop OK
- 2 Loop in progress

Future evolutions

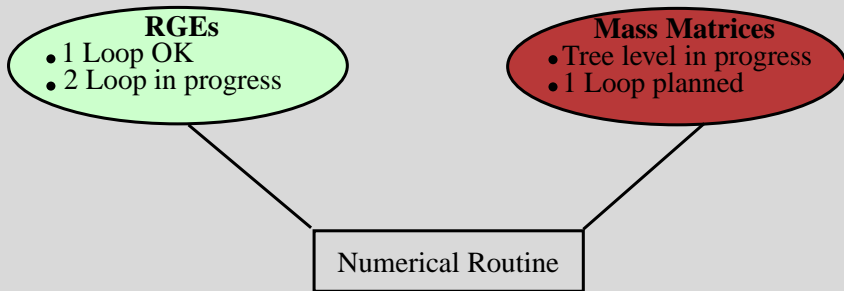
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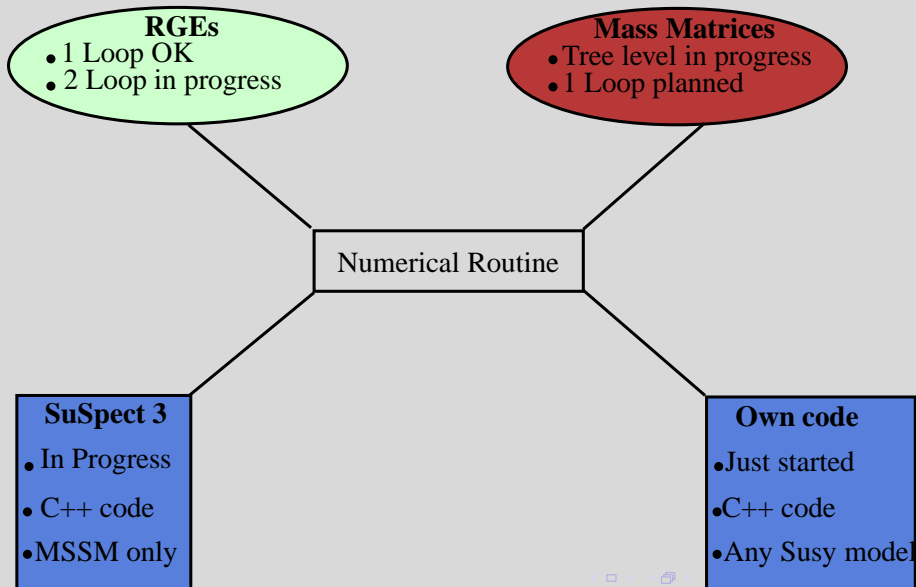
Mass Matrices

- Tree level in progress
- 1 Loop planned

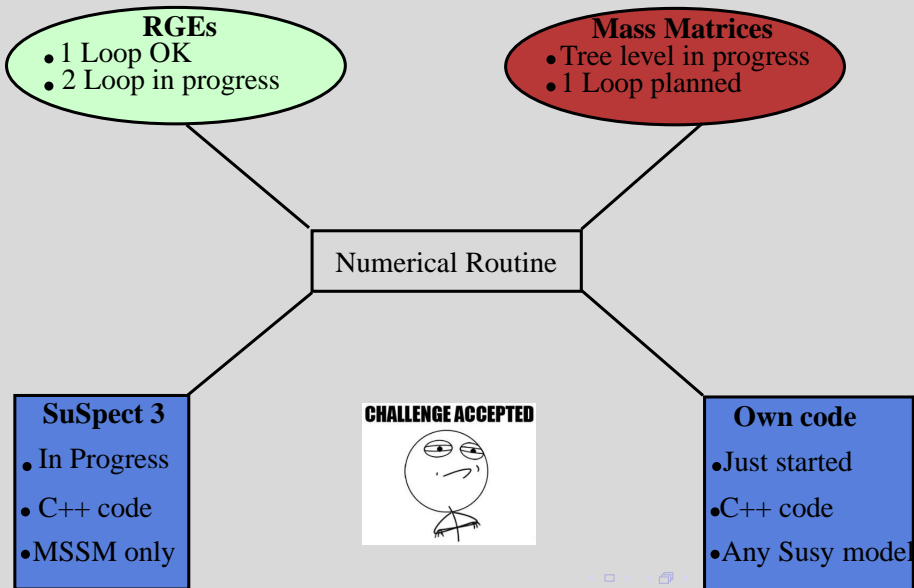
Future evolutions



Future evolutions



Future evolutions



- 1 Introduction to supersymmetry
- 2 Superspace Module (C. Duhr, B. Fuks)
- 3 Spin 3/2 Project ("Spin 3/2 collaboration")
- 4 Spectrum generator generator (Alloul, De Causmaecker, Fuks, Rausch de Traubenberg)
- 5 Prospects
- 6 Resume

Conclusion

Achieved work

- Superfields (since a long time ago).
- Spin 3/2 project.
- RGEs @ 1 loop and (partial) 2loop.

On-going work

- Spin 3/2 numerical validation.
- Complete RGEs @ 2loop.
- Scalar potential and mass matrices diagonalization @ 1loop.

Thank You !