

# Heavy Flavours III

FAPPS 2011 at Les Houches  
Emi KOU (LAL/IN2P3)

19/10/2011

# Plan

- 1st lecture: Introduction to flavour physics
  - ★ Weak interaction processes (charges, neutral processes, GIM mechanism)
  - ★ Discovery of CP violation in the K system
  - ★ Measuring oscillation in the B system
- 2nd lecture: Describing oscillations within SM
  - ★ Kobayashi-Maskawa mechanism for CP violation
  - ★ Testing the unitarity of the CKM matrix

# Plan

- 3rd lecture: Searching new physics with flavour physics
  - ★ Some examples (estimating top quark mass, charged Higgs mass in 2HDM, neutral Higgs mass in SUSY)
  - ★ SUSY CP/flavour Problem
  - ★ Hot topics in flavour physics

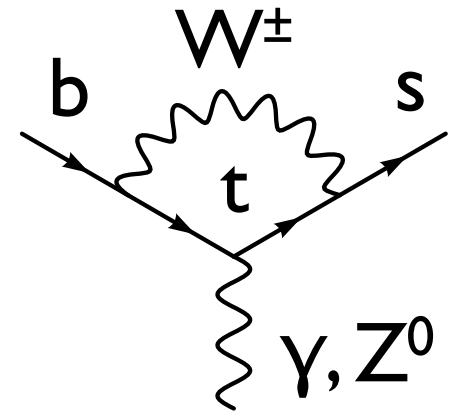
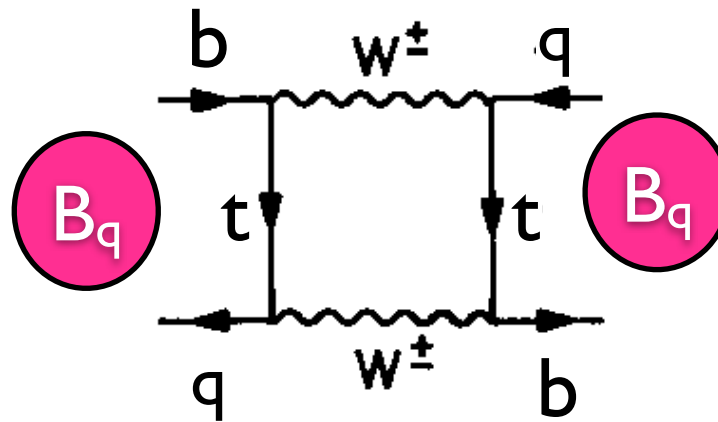
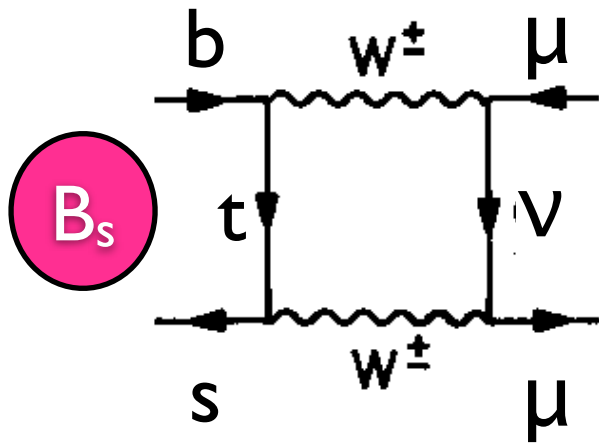
Further reading: “CP Violation” Bigi and Sanda (Cambridge Press)

# New particle searches in flavour physics



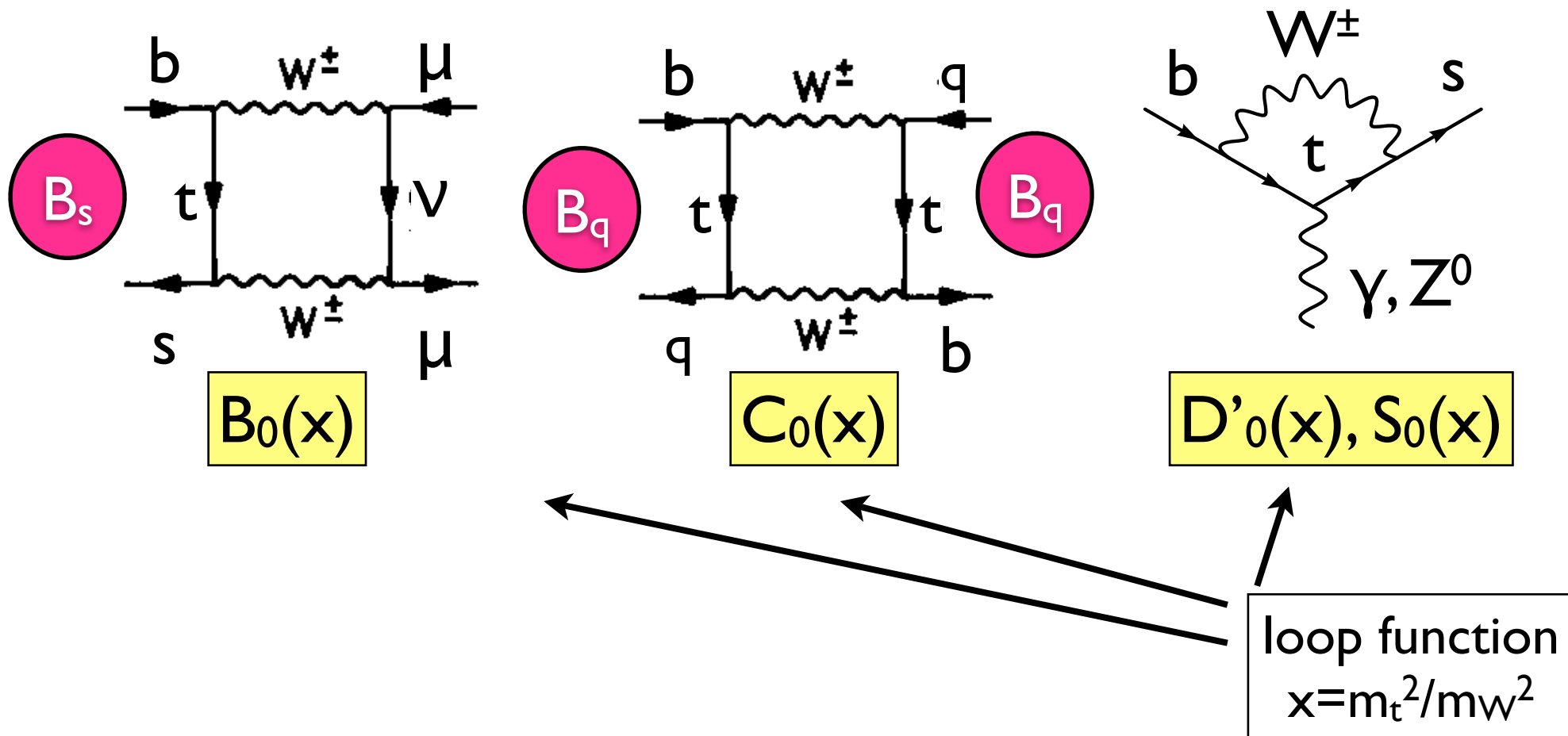


# Searching new particle with loop process





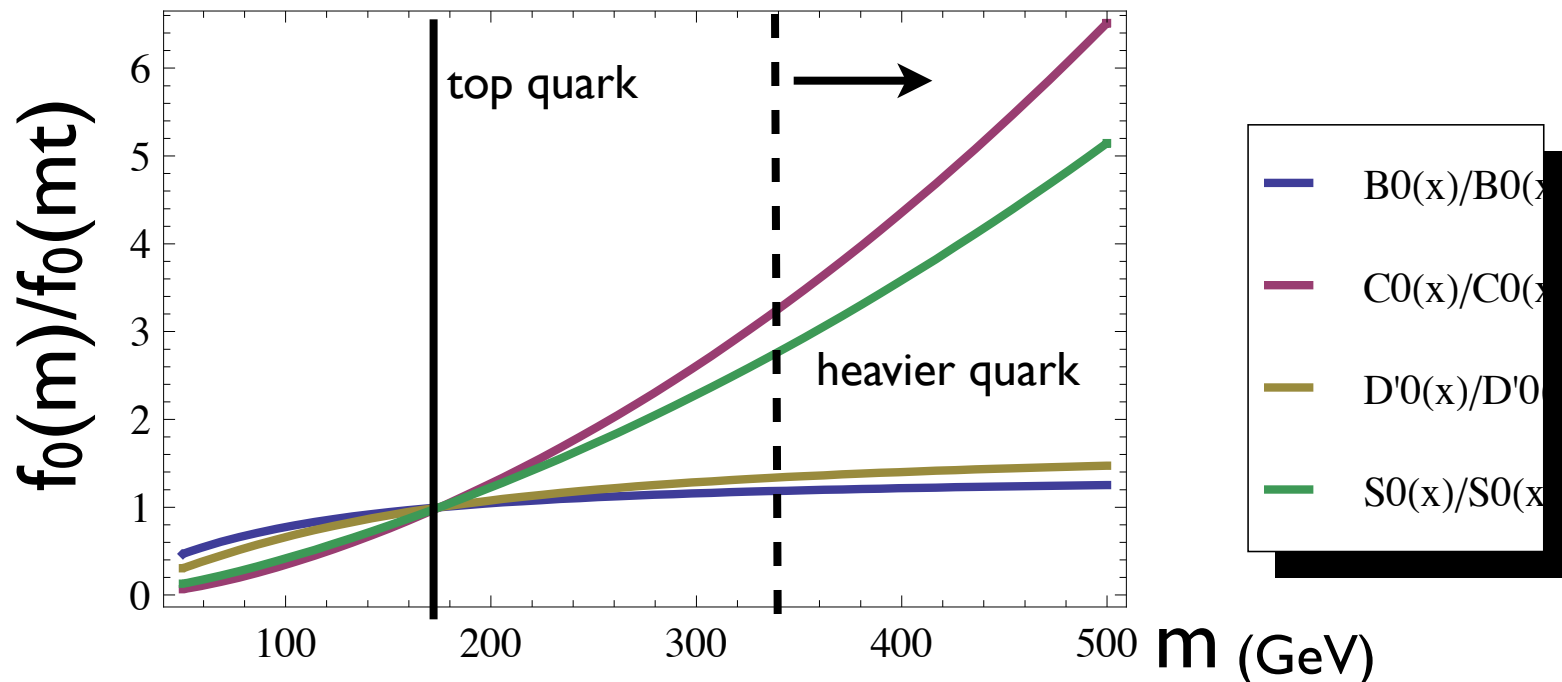
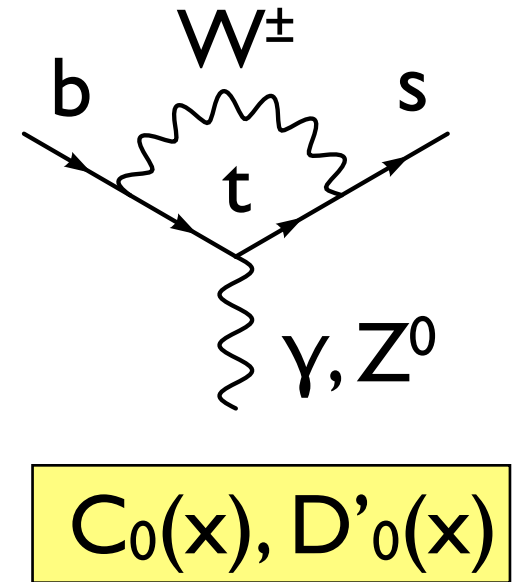
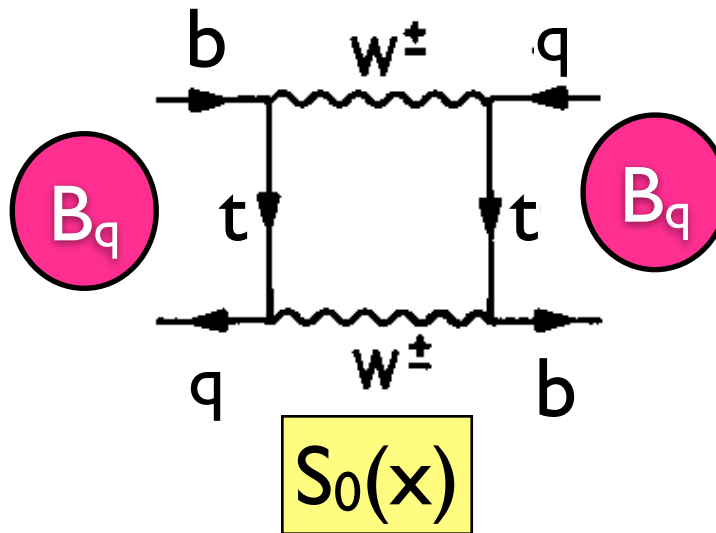
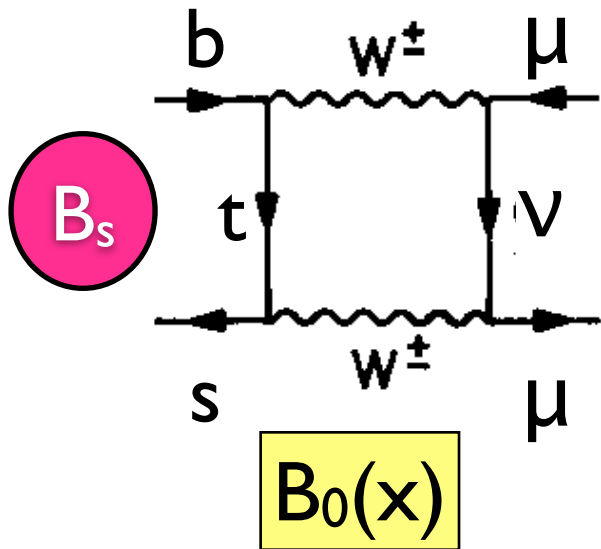
# Searching new particle with loop process



Indeed, the top quark mass was predicted to be around  $>100$  GeV after the first measurement of  $\Delta M_d$  (1987 by ARGUS Experiment)

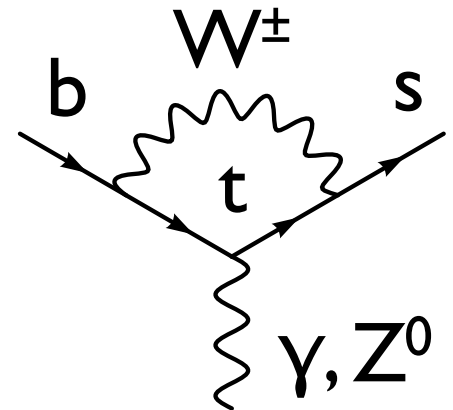
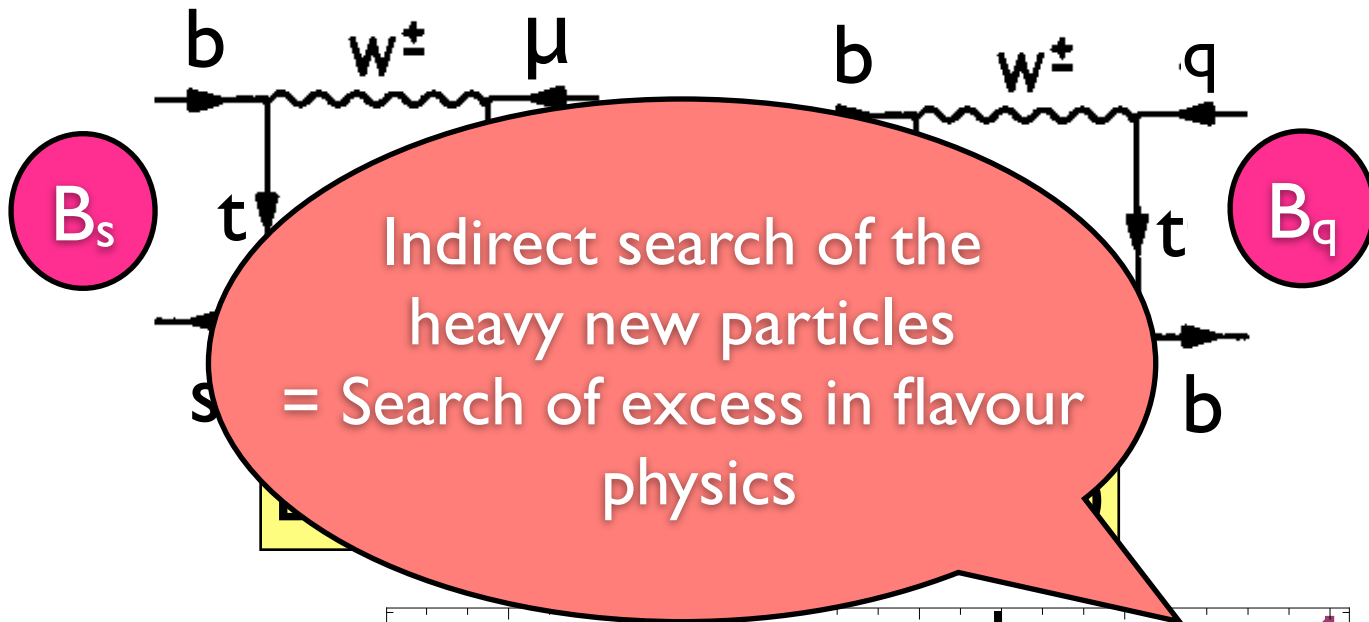


# Searching new particle with loop process

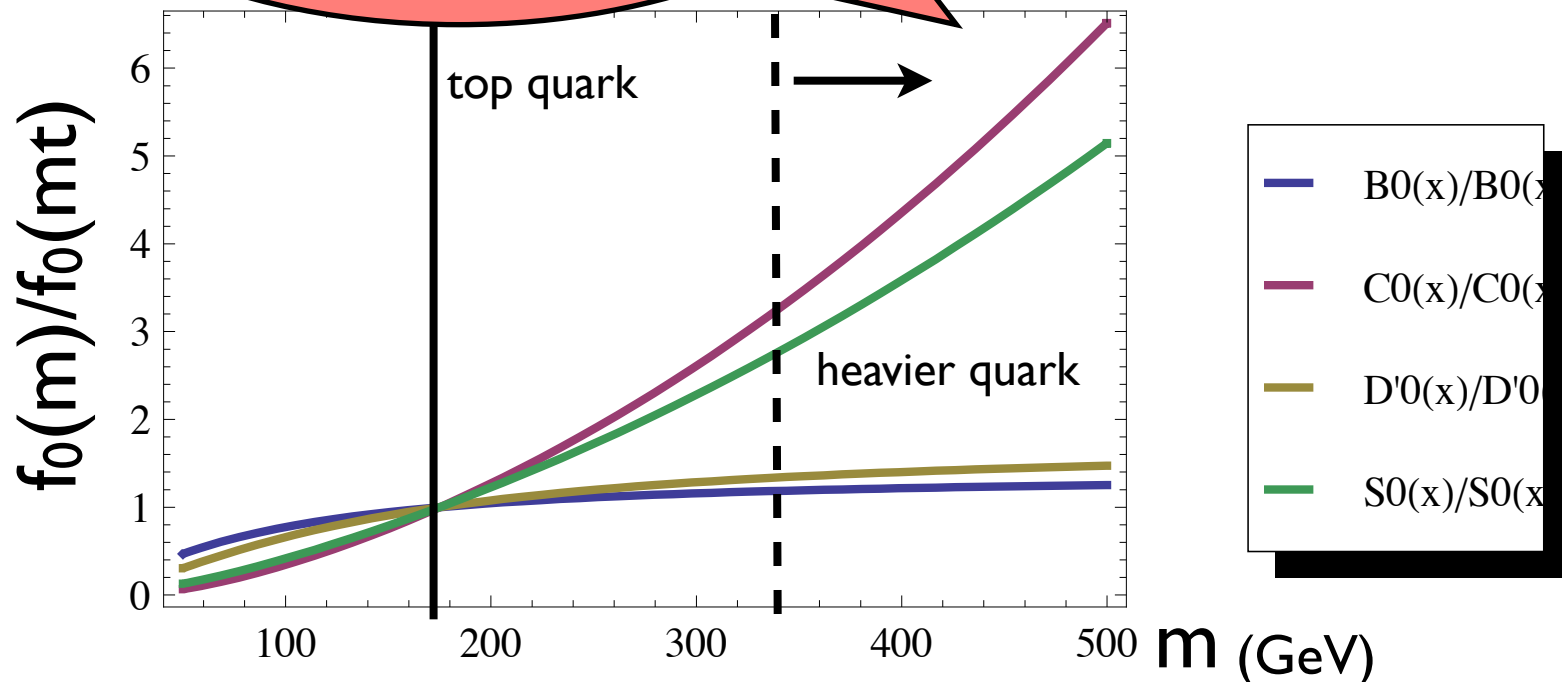




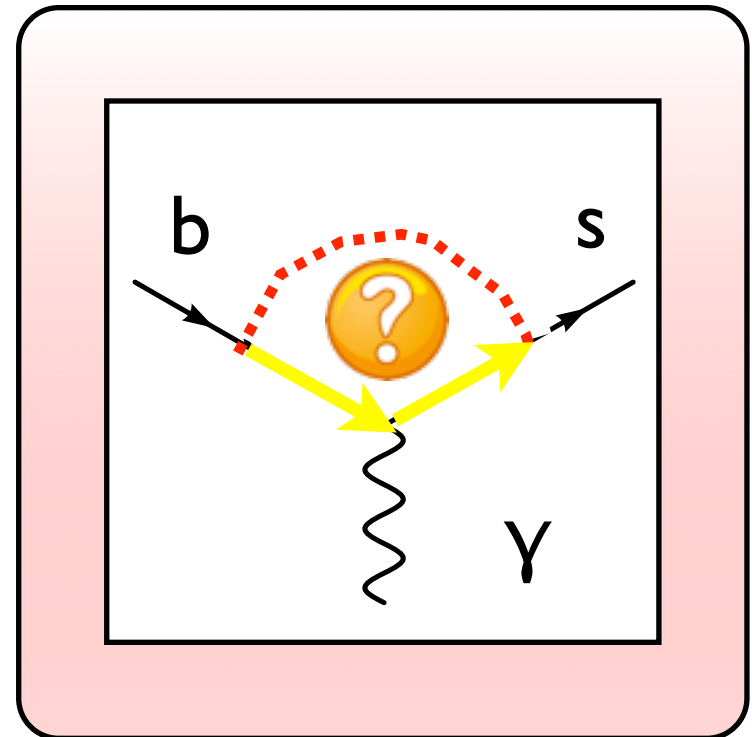
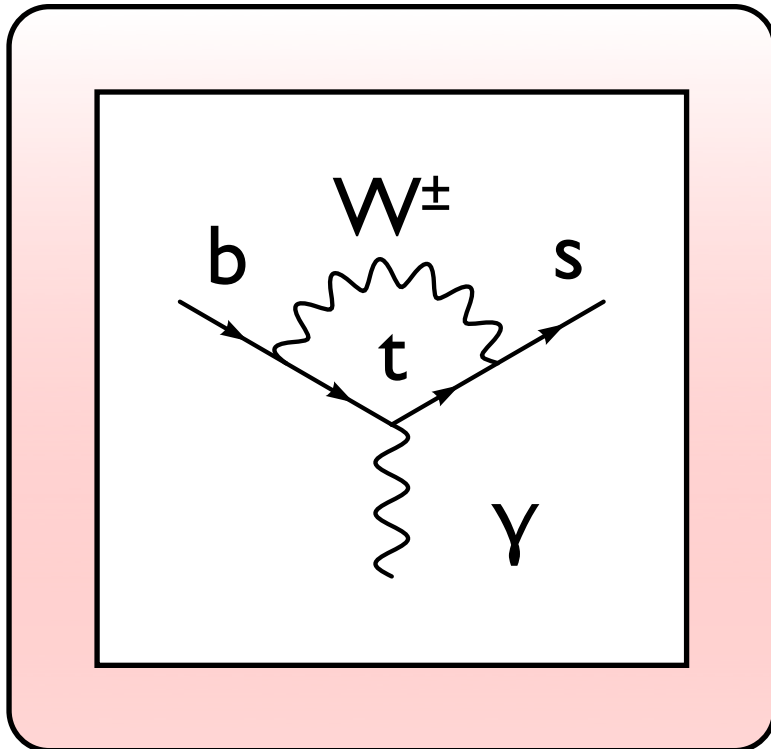
# Searching new particle with loop process



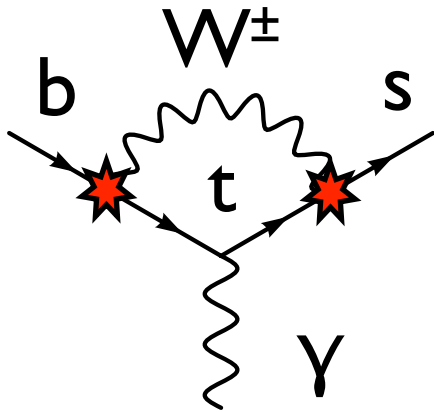
$C_0(x), D'_0(x)$



# New physics contributions to the $b \rightarrow s \gamma$ process



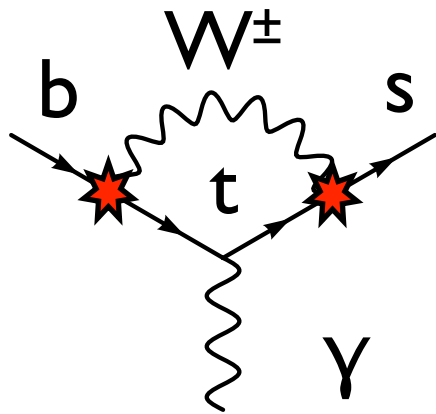
# SM computation of the $b \rightarrow s \gamma$ process



$$\mathcal{L}_{CC} = \frac{g}{\sqrt{2}} (J_\mu^+ W^{-\mu} + J_\mu^- W^{+\mu})$$

$$J_\mu^+ = V_{CKM} \bar{U}_L \gamma_\mu D_L = \sum_{i,j} V_{ij} \bar{u}_i \gamma_\mu (1 - \gamma_5) d_j / 4$$

# SM computation of the $b \rightarrow s \gamma$ process



$$\mathcal{L}_{CC} = \frac{g}{\sqrt{2}} (J_{\mu}^{+} W^{-\mu} + J_{\mu}^{-} W^{+\mu})$$

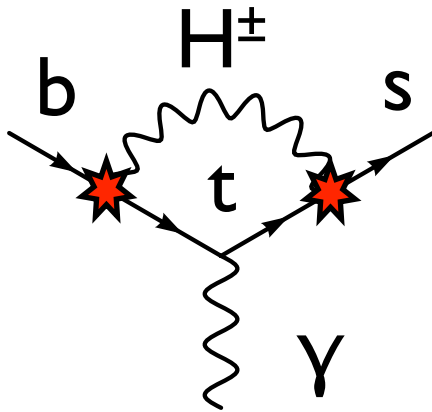
$$J_{\mu}^{+} = V_{CKM} \bar{U}_L \gamma_{\mu} D_L = \sum_{i,j} V_{ij} \bar{u}_i \gamma_{\mu} (1 - \gamma_5) d_j / 4$$

loop function  
 $x = m_t^2 / m_W^2$

$$\bar{b} A_{\mu} s = -i V_{tb} V_{ts}^{*} \frac{G_F e}{8\pi^2 \sqrt{2}} D'_0(x_t) \bar{s} [i \sigma_{\mu\nu} q^{\nu} [m_b (1 + \gamma_5)]] b$$

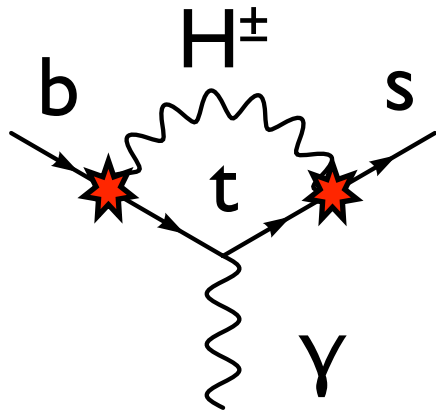
$$D'_0(x_t) = -\frac{(8x_t^3 + 5x_t^2 - 7x_t)}{12(1 - x_t)^3} + \frac{x_t^2(2 - 3x_t)}{2(1 - x_t)^4} \ln x_t$$

# New physics model I: Two Higgs doublet model





# New physics model I: Two Higgs doublet model



$$\mathcal{L} = \frac{g}{2\sqrt{2}M_W} H^\pm [V_{ij}m_{u_i} A_u \bar{u}_i (1 - \gamma_5) d_j + V_{ij}m_{d_j} A_d \bar{u}_i (1 + \gamma_5) d_j]$$

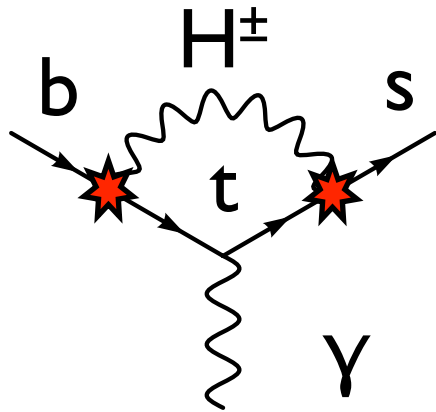
$$\Phi_1 = (\Phi_0, \Phi^+)_1 \rightarrow v_1; \quad \Phi_2 = (\Phi_0, \Phi^+)_2 \rightarrow v_2$$

$$\tan\beta = v_2/v_1, \quad v_1^2 + v_2^2 = v^2$$

$$\text{Type I: } A_u = \cot\beta, A_d = -\cot\beta$$

$$\text{Type II: } A_u = \cot\beta, A_d = \tan\beta$$

# New physics model I: Two Higgs doublet model



$$\mathcal{L} = \frac{g}{2\sqrt{2}M_W} H^\pm [V_{ij}m_{u_i} A_u \bar{u}_i (1 - \gamma_5) d_j + V_{ij}m_{d_j} A_d \bar{u}_i (1 + \gamma_5) d_j]$$

$$\Phi_1 = (\Phi_0, \Phi^+)_1 \rightarrow v_1; \quad \Phi_2 = (\Phi_0, \Phi^+)_2 \rightarrow v_2$$

$$\tan\beta = v_2/v_1, \quad v_1^2 + v_2^2 = v^2$$

$$\text{Type I: } A_u = \cot\beta, A_d = -\cot\beta$$

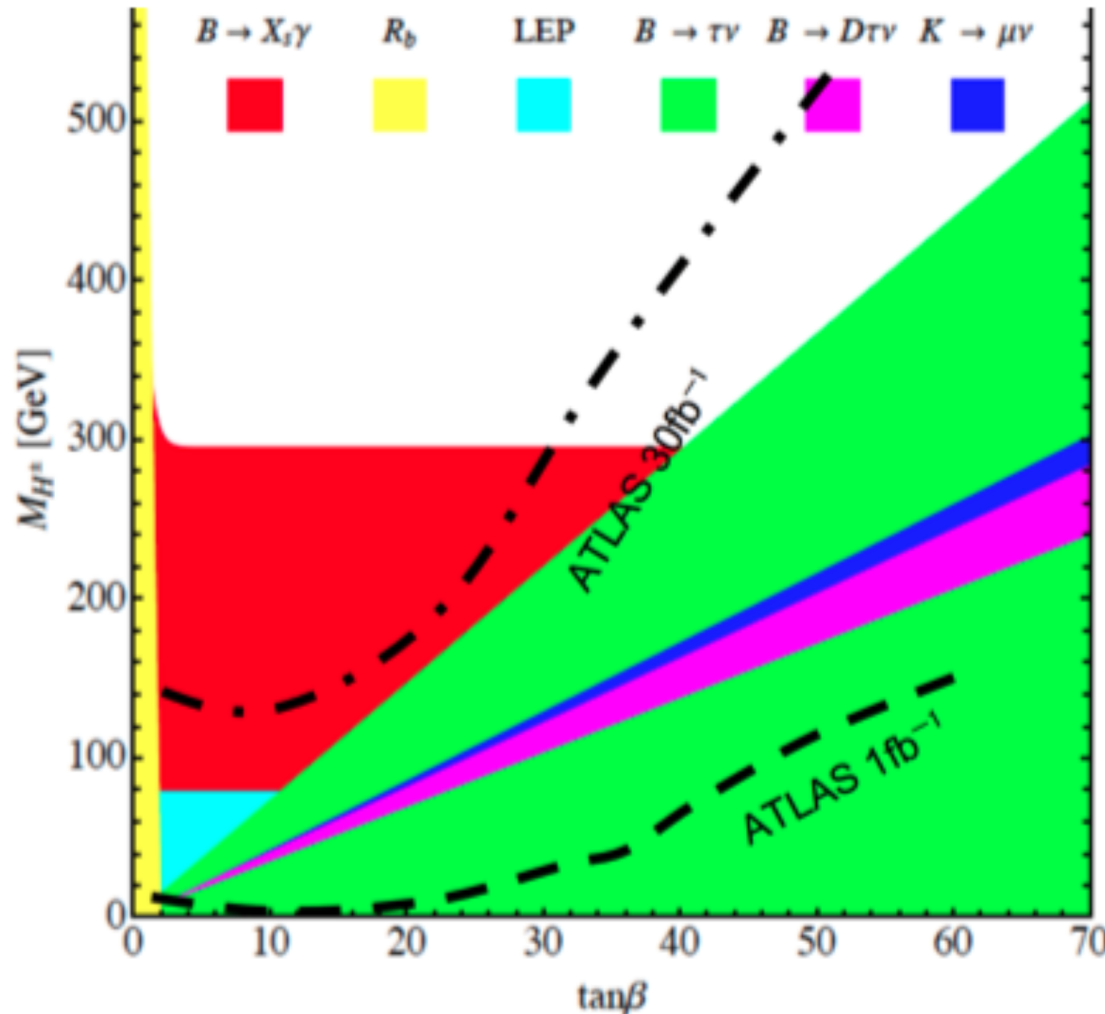
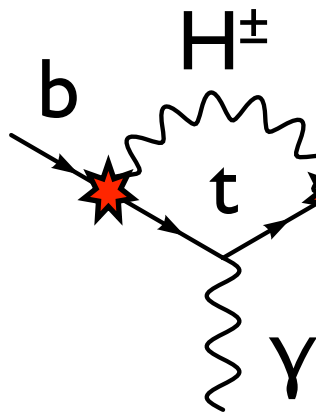
$$\text{Type II: } A_u = \cot\beta, A_d = \tan\beta$$

Now the loop function looks like...

$$c_{7,8}(M_W) = G_{7,8}(m_t^2/M_W^2) + \frac{1}{3\tan^2\beta} G_{7,8}(m_t^2/m_{H^\pm}^2) + \lambda F_{7,8}(m_t^2/m_{H^\pm}^2)$$

The measurement of  $b \rightarrow s \gamma$  can give prediction  
or constraint on the Higgs mass and  $\tan\beta$

# New physics model I: Two Higgs doublet model



$$V_{ij} m_{d_j} A_d \bar{u}_i (1 + \gamma_5) d_j$$

$$(\phi, \Phi^+)_2 \rightarrow v_2$$

$$v_1 = v_2$$

$$-\cot \beta$$

$$-\tan \beta$$

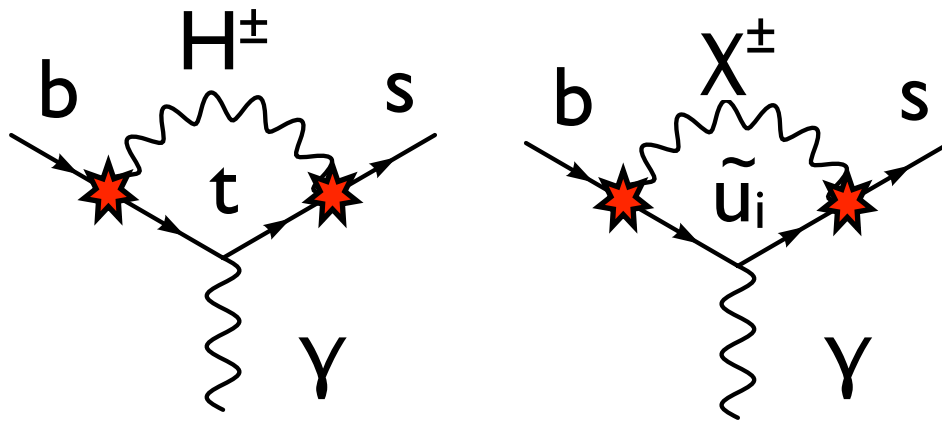
$$F_{7,8}(m_t^2, m_{H^\pm}^2)$$

Now the loop fu

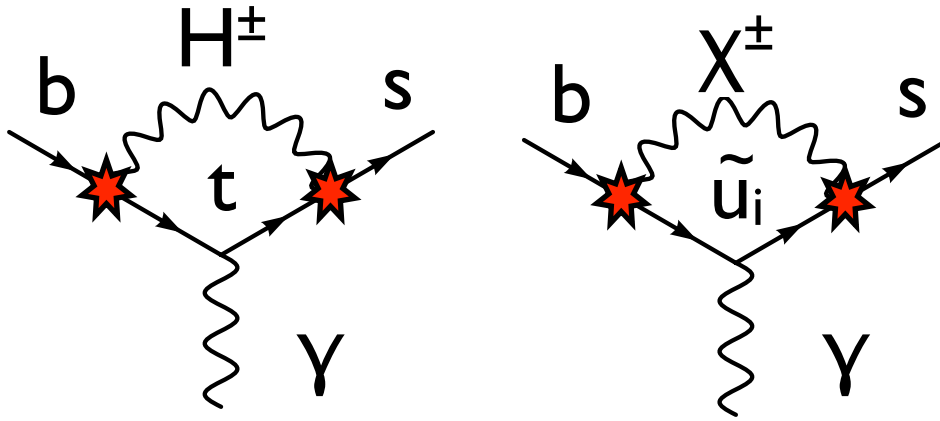
$$c_{7,8}(M_W) = C$$

The measurement of  $b \rightarrow s \gamma$  can give prediction  
or constraint on the Higgs mass and  $\tan \beta$

# New physics model II: Supersymmetry (minimum...)



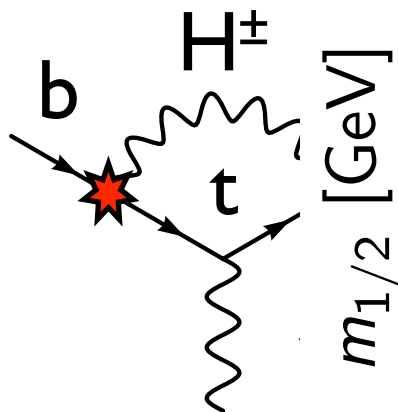
# New physics model II: Supersymmetry (minimum...)



The loop function for chargino diagram looks like...

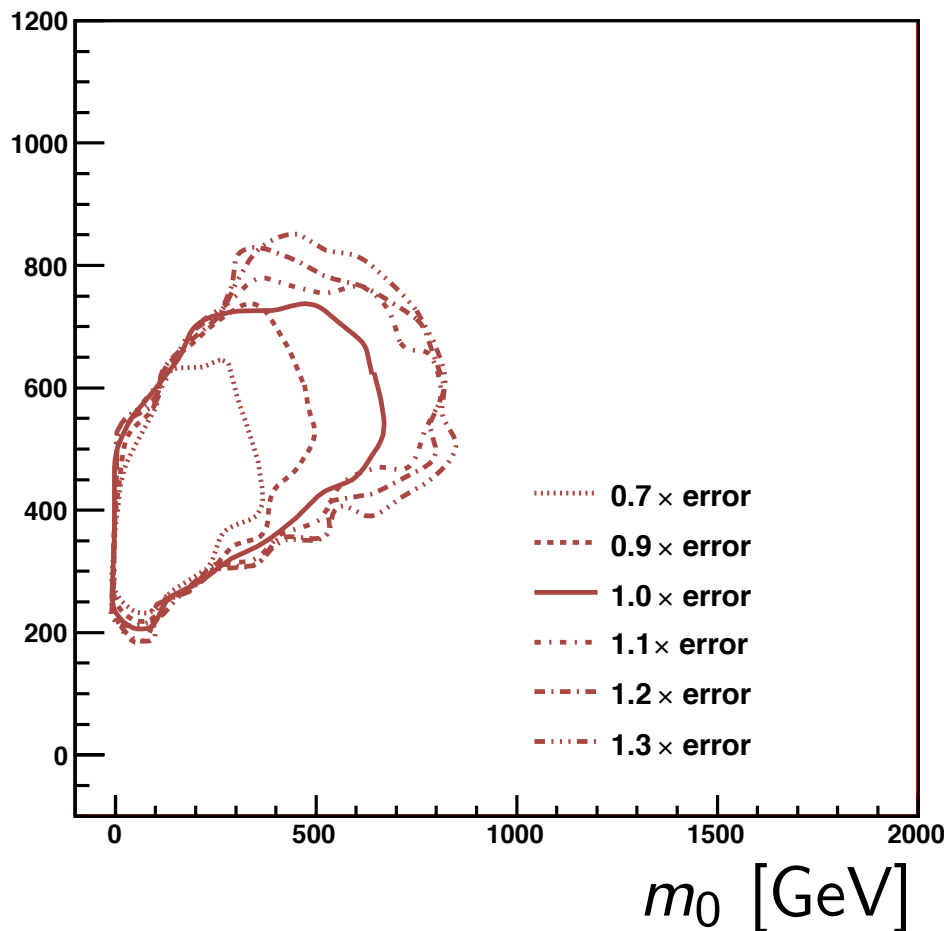
$$\begin{aligned}
 c_{7,8}^{\tilde{\chi}^\pm}(M_W) \simeq & \sum_{j=1}^2 \left\{ \frac{M_W^2}{\tilde{m}_{\chi_j^\pm}^2} |V_{j1}|^2 G_{7,8} \left( \frac{\tilde{m}^2}{\tilde{m}_{\chi_j^\pm}^2} \right) - \frac{M_W U_{j2} V_{j1}}{\tilde{m}_{\chi_j^\pm} \sqrt{2} \cos \beta} H_{7,8} \left( \frac{\tilde{m}^2}{\tilde{m}_{\chi_j^\pm}^2} \right) \right. \\
 & + \sum_{k=1}^2 \left[ -\frac{M_W^2}{\tilde{m}_{\chi_j^\pm}^2} \left| V_{j1} T_{k1} - \frac{m_t V_{j2} T_{k2}}{M_W \sqrt{2} \sin \beta} \right|^2 G_{7,8} \left( \frac{\tilde{m}_{t_k}^2}{\tilde{m}_{\chi_j^\pm}^2} \right) \right. \\
 & \left. \left. + \frac{M_W U_{j2} T_{k1}}{\tilde{m}_{\chi_j^\pm} \sqrt{2} \cos \beta} \left( V_{j1} T_{k1} - \frac{m_t V_{j2} T_{k2}}{M_W \sqrt{2} \sin \beta} \right) H_{7,8} \left( \frac{\tilde{m}^2}{\tilde{m}_{\chi_j^\pm}^2} \right) \right] \right\}
 \end{aligned}$$

# New physics model II: Supersymmetry (minimum...)



The loop function

$$c_{7,8}^{\tilde{\chi}^\pm}(M_W) \simeq$$



$$H_{7,8} \left( \frac{\tilde{m}^2}{\tilde{m}_{\chi_j^\pm}^2} \right) \frac{\tilde{m}_{t_k}^2}{\tilde{n}_{\chi_j^\pm}^2}$$

$$+ \frac{M_W U_{j2} T_{k1}}{\tilde{m}_{\chi_j^\pm} \sqrt{2} \cos \beta} \left( V_{j1} T_{k1} - \frac{m_t V_{j2} T_{k2}}{M_W \sqrt{2} \sin \beta} \right) H_{7,8} \left( \frac{\tilde{m}^2}{\tilde{m}_{\chi_j^\pm}^2} \right) \Bigg] \Bigg\}$$

# SUSY CP/flavour problem

# SUSY CP/flavour problem

SM

- ☒ There is only one source of CP violation.
- ☒ FCNC is suppressed naturally by the GIM mechanism.

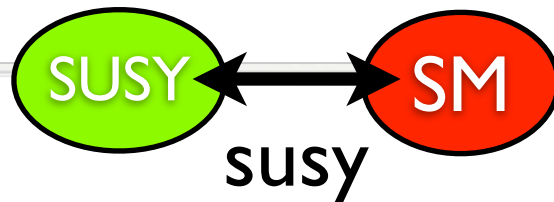
SUSY

- ☒ There is many (too many) sources of CP violation.
- ☒ FCNC can occur since there is, a priori, no GIM mechanism.



# SUSY CP/flavour problem

Names		spin 0	spin 1/2	$SU(3)_C, SU(2)_L, U(1)_Y$
squarks, quarks ( $\times 3$ families)	$Q$	$(\tilde{u}_L \ \tilde{d}_L)$	$(u_L \ d_L)$	$(\mathbf{3}, \mathbf{2}, \frac{1}{6})$
	$\bar{u}$	$\tilde{u}_R^*$	$u_R^\dagger$	$(\bar{\mathbf{3}}, \mathbf{1}, -\frac{2}{3})$
	$\bar{d}$	$\tilde{d}_R^*$	$d_R^\dagger$	$(\bar{\mathbf{3}}, \mathbf{1}, \frac{1}{3})$
sleptons, leptons ( $\times 3$ families)	$L$	$(\tilde{\nu} \ \tilde{e}_L)$	$(\nu \ e_L)$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$
	$\bar{e}$	$\tilde{e}_R^*$	$e_R^\dagger$	$(\mathbf{1}, \mathbf{1}, 1)$
Higgs, higgsinos	$H_u$	$(H_u^+ \ H_u^0)$	$(\tilde{H}_u^+ \ \tilde{H}_u^0)$	$(\mathbf{1}, \mathbf{2}, +\frac{1}{2})$
	$H_d$	$(H_d^0 \ H_d^-)$	$(\tilde{H}_d^0 \ \tilde{H}_d^-)$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$

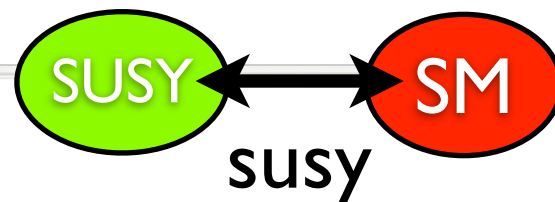


**MSSM**

# SUSY CP/flavour problem

Names		spin 0	spin 1/2	$SU(3)_C, SU(2)_L, U(1)_Y$
squarks, quarks ( $\times 3$ families)	$Q$	$(\tilde{u}_L \ \tilde{d}_L)$	$(u_L \ d_L)$	$(\mathbf{3}, \mathbf{2}, \frac{1}{6})$
				$(\mathbf{1}, \mathbf{2}, -\frac{2}{3})$
sleptons, leptons ( $\times 3$ families)	$e$	$e_R$	$e_R$	$(\mathbf{1}, \mathbf{1}, 1)$
				$(\mathbf{1}, \mathbf{1}, -\frac{1}{2})$
Higgs, higgsinos	$H_u$	$(H_u^+ \ H_u^0)$	$(\tilde{H}_u^+ \ \tilde{H}_u^0)$	$(\mathbf{1}, \mathbf{2}, +\frac{1}{2})$
	$H_d$	$(H_d^0 \ H_d^-)$	$(\tilde{H}_d^0 \ \tilde{H}_d^-)$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$

If Supersymmetry is unbroken\*, the SM particles and their SUSY partners would have the same mass!



**MSSM**

\*The same is true if SUSY is broken spontaneously  $Tr[M_{\text{real scalar}}^2] = 2Tr[M_{\text{chiral fermions}}^2]$

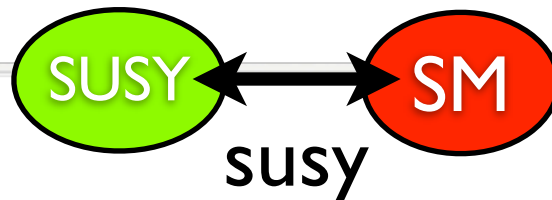
# SUSY CP/flavour problem

Names		spin 0	spin 1/2	$SU(3)_C, SU(2)_L, U(1)_Y$
squarks, quarks	$Q$	$(\tilde{u}_L \ \tilde{d}_L)$	$(u_L \ d_L)$	$(\mathbf{3}, \mathbf{2}, \frac{1}{6})$
( $\times 3$ families)				$(\mathbf{3}, \mathbf{2}, -\frac{2}{3})$
sleptons, leptons	$e$			$(\mathbf{1}, \mathbf{2}, \frac{1}{3})$
( $\times 3$ families)				$(\mathbf{1}, \mathbf{2}, -\frac{1}{3})$
Higgs, higgsinos	$H_u$ $H_d$			

If Supersymmetry is unbroken\*, the SM particles and their SUSY partners

$m_e = m_{\text{selectron}}???$

We would have seen it then!



**MSSM**

\*The same is true if SUSY is broken spontaneously  $Tr[M_{\text{real scalar}}^2] = 2Tr[M_{\text{chiral fermions}}^2]$

# SUSY CP/flavour problem

Names		spin 0	spin 1/2	$SU(3)_C, SU(2)_L, U(1)_Y$
squarks, quarks	$Q$	$(\tilde{u}_L \ \tilde{d}_L)$	$(u_L \ d_L)$	$(\mathbf{3}, \mathbf{2}, \frac{1}{6})$
( $\times 3$ families)				$(\mathbf{3}, \mathbf{2}, -\frac{2}{3})$
sleptons, leptons	$e$			$(\mathbf{1}, \mathbf{2}, \frac{1}{3})$
( $\times 3$ families)				$(\mathbf{1}, \mathbf{2}, -\frac{1}{3})$
Higgs, higgsinos	$H_u$			
	$H_d$			

If Supersymmetry is unbroken\*, the SM particles and their SUSY partners

$m_e = m_{\text{selectron}}???$

**We must break SUSY!!!**

SUSY

\*The same is true if SUSY is broken spontaneously  $Tr[M_{\text{real scalar}}^2] = 2Tr[M_{\text{chiral fermions}}^2]$



# Origin of the SUSY CP/ flavour problem

We must start with most general Soft SUSY breaking term

$$\begin{aligned}\mathcal{L}_{\text{soft}}^{\text{MSSM}} = & -\frac{1}{2}(M_3\tilde{g}\tilde{g} + M_2\tilde{W}\tilde{W} + M_1\tilde{B}\tilde{B}) + c.c. \\ & -(\tilde{u}\mathbf{a}_u\tilde{Q}H_u - \tilde{d}\mathbf{a}_d\tilde{Q}H_d - \tilde{d}\mathbf{a}_d\tilde{L}H_d) + c.c. \\ & -m_{H_u}^2H_u^*H_u - m_{H_d}^2H_d^*H_d - (bH_uH_d + c.c) \\ & -\tilde{Q}^\dagger\mathbf{m}_Q^2\tilde{Q} - \tilde{L}^\dagger\mathbf{m}_L^2\tilde{L} - \tilde{u}\mathbf{m}_u^2\tilde{u}^\dagger - \tilde{d}\mathbf{m}_d^2\tilde{d}^\dagger - \tilde{e}\mathbf{m}_e^2\tilde{e}^\dagger\end{aligned}$$

The SUSY breaking term  
introduces 105 new masses,  
mixings and phases.



# Origin of the SUSY CP/ flavour problem

## Squark mass matrix

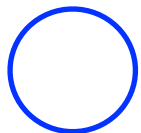
$$V = \tilde{u}_L^\dagger \mathbf{M}_{\mathbf{LL}}^2 \tilde{u}_L + \tilde{u}_R^\dagger \mathbf{M}_{\mathbf{RR}}^2 \tilde{u}_R + \tilde{u}_L^\dagger \mathbf{M}_{\mathbf{LR}}^2 \tilde{u}_R + \tilde{u}_R^\dagger \mathbf{M}_{\mathbf{RL}}^2 \tilde{u}_L$$

$$\mathbf{M}_{\mathbf{LL}}^2 = \left( \frac{1}{2} - \frac{2}{3} \sin^2 \theta_W \right) \frac{g'^2 + g^2}{4} (v_d^2 - v_u^2) \mathbf{1} + v_u^2 \mathbf{y}_u^{*2} + \mathbf{m}_Q^2$$

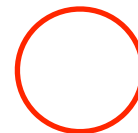
$$\mathbf{M}_{\mathbf{RR}}^2 = \frac{2}{3} \sin^2 \theta_W \frac{g'^2 + g^2}{4} (v_d^2 - v_u^2) \mathbf{1} + v_u^2 \mathbf{y}_u^{*2} + \mathbf{m}_u^2$$

$$\mathbf{M}_{\mathbf{LR}}^2 = -\mu \cot \beta v_u \mathbf{y}_u^* + v_u \mathbf{a}_u^*$$

$$\mathbf{M}_{\mathbf{RL}}^2 = -\mu^* \cot \beta v_u \mathbf{y}_u^* + v_u \mathbf{a}_u^*$$



Terms from spontaneous  
symmetry breaking



Terms from soft SUSY  
breaking



By the way, what is the  
that mixing

Slide from the  
first day...

## Diagonalization

$$(\bar{d}, \bar{s}, \bar{b}) \begin{pmatrix} \cdot\cdot & \cdot\cdot & \cdot\cdot \\ \cdot\cdot & (Y_d)^2 & \cdot\cdot \\ \cdot\cdot & \cdot\cdot & \cdot\cdot \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix} \Rightarrow (\bar{\tilde{d}}, \bar{\tilde{s}}, \bar{\tilde{b}}) \begin{pmatrix} m_d^2 & 0 & 0 \\ 0 & m_s^2 & 0 \\ 0 & 0 & m_b^2 \end{pmatrix} \begin{pmatrix} \tilde{d} \\ \tilde{s} \\ \tilde{b} \end{pmatrix}$$

Unitary transformation  
to diagonalize the  
Yukawa matrix

$$U_d (Y_d)^2 U_d^\dagger = (M_d^2)_{diag}$$

Transformation from  
interaction eigen-basis  
to mass eigen-basis

$$U_d \begin{pmatrix} d \\ s \\ b \end{pmatrix} = \begin{pmatrix} \tilde{d} \\ \tilde{s} \\ \tilde{b} \end{pmatrix}$$



# Origin of the SUSY CP/flavour problem

Rotating squark field with the same matrix which diagonalizes quark field

$$U_d \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{weak}} = \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{mass}} \quad \Rightarrow \quad U_d \begin{pmatrix} \tilde{d} \\ \tilde{s} \\ \tilde{b} \end{pmatrix}_{\text{weak}} = \begin{pmatrix} \tilde{d} \\ \tilde{s} \\ \tilde{b} \end{pmatrix}_{\text{mass}}$$

$$V = \tilde{u}_L^\dagger \mathbf{M}_{\mathbf{LL}}^2 \tilde{u}_L + \tilde{u}_R^\dagger \mathbf{M}_{\mathbf{RR}}^2 \tilde{u}_R + \tilde{u}_L^\dagger \mathbf{M}_{\mathbf{LR}}^2 \tilde{u}_R + \tilde{u}_R^\dagger \mathbf{M}_{\mathbf{RL}}^2 \tilde{u}_L$$

$$\mathbf{M}_{\mathbf{LL}}^2 = \left( \frac{1}{2} - \frac{2}{3} \sin^2 \theta_W \right) \frac{g'^2 + g^2}{4} (v_d^2 - v_u^2) \mathbf{1} + v_u^2 \mathbf{y}_u^{*2} + \mathbf{m}_Q^2$$

$$\mathbf{M}_{\mathbf{RR}}^2 = \frac{2}{3} \sin^2 \theta_W \frac{g'^2 + g^2}{4} (v_d^2 - v_u^2) \mathbf{1} + v_u^2 \mathbf{y}_u^{*2} + \mathbf{m}_u^2$$

$$\mathbf{M}_{\mathbf{LR}}^2 = -\mu \cot \beta v_u \mathbf{y}_u^* + v_u \mathbf{a}_u^*$$

$$\mathbf{M}_{\mathbf{RL}}^2 = -\mu^* \cot \beta v_u \mathbf{y}_u^* + v_u \mathbf{a}_u^*$$

The red terms remains non-diagonal.





# Origin of the SUSY CP/flavour problem

Rotating squark field with the same matrix which diagonalizes quark field

$$U_d \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{weak}} = \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{mass}} \quad \Rightarrow \quad U_d \begin{pmatrix} \tilde{d} \\ \tilde{s} \\ \tilde{b} \end{pmatrix}_{\text{weak}} = \begin{pmatrix} \tilde{d} \\ \tilde{s} \\ \tilde{b} \end{pmatrix}_{\text{mass}}$$

$$V = \tilde{u}_L^\dagger \mathbf{M}_{\text{LL}}^2 \tilde{u}_L + \tilde{u}_R^\dagger \mathbf{M}_{\text{RR}}^2 \tilde{u}_R + \tilde{u}_L^\dagger \mathbf{M}_{\text{LR}}^2 \tilde{u}_R + \tilde{u}_R^\dagger \mathbf{M}_{\text{RL}}^2 \tilde{u}_L$$

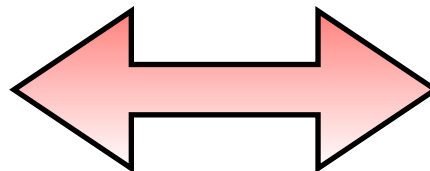
$$\mathbf{M}_{\text{LL}}^2 = \left( \frac{1}{2} - \frac{2}{3} \sin^2 \theta_W \right) \frac{g'^2 + g^2}{4} (v_d^2 - v_u^2) \mathbf{1} + v_u^2 \mathbf{y}_u^{*2} + \mathbf{m}_{\text{Q}}^2$$

$$\mathbf{M}_{\text{RR}}^2 = \frac{2}{3} \sin^2 \theta_W \frac{g'^2 + g^2}{4} (v_d^2 - v_u^2) \mathbf{1} + v_u^2 \mathbf{y}_u^{*2} + \mathbf{m}_{\text{U}}^2$$

$$\mathbf{M}_{\text{LR}}^2 = -\mu \cot \beta v_u \mathbf{y}_u^* + v_u \mathbf{a}_u^*$$

$$\mathbf{M}_{\text{RL}}^2 = -\mu^* \cot \beta v_u \mathbf{y}_u^* + v_u \mathbf{a}_u^*$$

Squark is not on the mass eigen-basis



Flavour mixture in the propagator



# Origin of the SUSY CP/flavour problem

Rotating squark field with the same matrix which diagonalizes quark field

$$U_d \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{weak}} = \begin{pmatrix} d \\ s \\ b \end{pmatrix} = \begin{pmatrix} \tilde{d} \\ \tilde{s} \\ \tilde{b} \end{pmatrix}_{\text{mass}}$$

$\tilde{b}$   $\tilde{s}$

..... **X** .....

**example**

$$V = \tilde{u}_L^\dagger M_{LL}^2 \tilde{u}_L$$

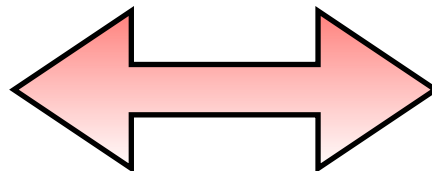
$$M_{LL}^2 = \left( \frac{1}{2} - \frac{2}{3} \sin^2 \theta_W \right) \frac{g^2}{4} \tilde{u}^{*2} + m_Q^2$$

$$M_{RR}^2 = \frac{2}{3} \sin^2 \theta_W \frac{g^2}{4} \tilde{u}^2 + m_{\tilde{u}}^2$$

$$M_{LR}^2 = -\mu \cot \beta v_u \mathbf{y}_u^* + v_u \mathbf{a}_u^*$$

$$M_{RL}^2 = -\mu^* \cot \beta v_u \mathbf{y}_u + v_u \mathbf{a}_u$$

Squark is not on the mass eigen-basis



Flavour mixture in the propagator

# Avoiding SUSY CP/flavour problem I

$$V = \tilde{u}_L^\dagger \mathbf{M}_{LL}^2 \tilde{u}_L + \tilde{u}_R^\dagger \mathbf{M}_{RR}^2 \tilde{u}_R + \tilde{u}_L^\dagger \mathbf{M}_{LR}^2 \tilde{u}_R + \tilde{u}_R^\dagger \mathbf{M}_{RL}^2 \tilde{u}_L$$

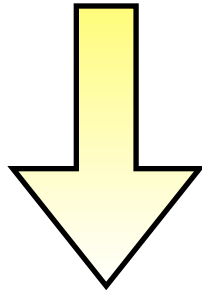
$$\mathbf{M}_{LL}^2 = \left(\frac{1}{2} - \frac{2}{3} \sin^2 \theta_W\right) \frac{g'^2 + g^2}{4} (v_d^2 - v_u^2) \mathbf{1} + v_u^2 \mathbf{y}_u^{*2} + \mathbf{m}_Q^2$$

$$\mathbf{M}_{RR}^2 = \frac{2}{3} \sin^2 \theta_W \frac{g'^2 + g^2}{4} (v_d^2 - v_u^2) \mathbf{1} + v_u^2 \mathbf{y}_u^{*2} + \mathbf{m}_u^2$$

$$\mathbf{M}_{LR}^2 = -\mu \cot \beta v_u \mathbf{y}_u^* + v_u \mathbf{a}_u^*$$

$$\mathbf{M}_{RL}^2 = -\mu^* \cot \beta v_u \mathbf{y}_u^* + v_u \mathbf{a}_u^*$$

**Assumption**



Fix the SUSY breaking parameters so that the red terms can be diagonalized together with the blue terms

$$\mathbf{m}_Q^2 = m_Q^2 \mathbf{1}, \mathbf{m}_L^2 = m_L^2 \mathbf{1}, \mathbf{m}_u^2 = m_u^2 \mathbf{1}, \mathbf{m}_d^2 = m_d^2 \mathbf{1}, \mathbf{m}_e^2 = m_e^2 \mathbf{1}$$

$$\mathbf{a}_u = A_{u0} \mathbf{y}_u, \quad \mathbf{a}_d = A_{u0} \mathbf{y}_d, \quad \mathbf{a}_e = A_{u0} \mathbf{y}_e$$

$$\arg(M_{1\sim 3}), \arg(A_{u0}), \arg(A_{d0}), \arg(A_{e0}) = 0, \text{ or } \pi$$

e.g.  
mSUGRA

# Constraining the Soft SUSY parameters from flavour physics

## Squark mass matrix

$$V = \tilde{u}_L^\dagger \mathbf{M}_{\mathbf{LL}}^2 \tilde{u}_L + \tilde{u}_R^\dagger \mathbf{M}_{\mathbf{RR}}^2 \tilde{u}_R + \tilde{u}_L^\dagger \mathbf{M}_{\mathbf{LR}}^2 \tilde{u}_R + \tilde{u}_R^\dagger \mathbf{M}_{\mathbf{RL}}^2 \tilde{u}_L$$

$$\mathbf{M}_{\mathbf{LL}}^2 = \left(\frac{1}{2} - \frac{2}{3} \sin^2 \theta_W\right) \frac{g'^2 + g^2}{4} (v_d^2 - v_u^2) \mathbf{1} + v_u^2 \mathbf{y}_{\mathbf{u}}^{*2} + \mathbf{m}_{\mathbf{Q}}^2$$

$$\mathbf{M}_{\mathbf{RR}}^2 = \frac{2}{3} \sin^2 \theta_W \frac{g'^2 + g^2}{4} (v_d^2 - v_u^2) \mathbf{1} + v_u^2 \mathbf{y}_{\mathbf{u}}^{*2} + \mathbf{m}_{\mathbf{u}}^2$$

$$\mathbf{M}_{\mathbf{LR}}^2 = -\mu \cot \beta v_u \mathbf{y}_{\mathbf{u}}^* + v_u \mathbf{a}_{\mathbf{u}}^*$$

$$\mathbf{M}_{\mathbf{RL}}^2 = -\mu^* \cot \beta v_u \mathbf{y}_{\mathbf{u}}^* + v_u \mathbf{a}_{\mathbf{u}}^*$$

Instead of (artificially) choosing the parameters, why don't we constrain from the flavour phenomena, first?!

# Constraining the Soft SUSY parameters from flavour physics

$$\mathbf{m}_{AB}^{2\text{SCKM}} = \begin{pmatrix} (m_{AB}^2)_{11} & (\Delta_{AB})_{12} & (\Delta_{AB})_{13} \\ (\Delta_{AB})_{21} & (m_{AB}^2)_{22} & (\Delta_{AB})_{23} \\ (\Delta_{AB})_{31} & (\Delta_{AB})_{32} & (m_{AB}^2)_{33} \end{pmatrix}$$

$$\frac{(\Delta_{AB})_{ij}}{m_{\text{squark}}} \equiv (\delta_{AB})_{ij}$$

Mass Insertion Parameter

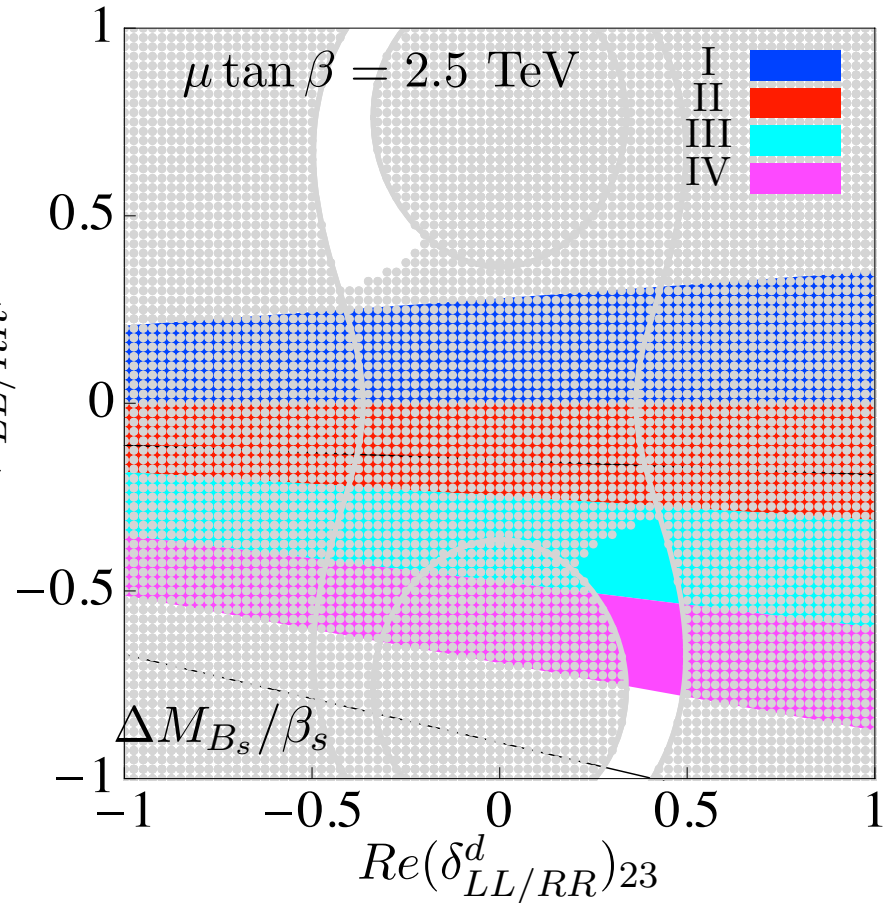
$$(\delta_{AB})_{12} \longrightarrow \Delta m_K, \quad \epsilon, \quad \epsilon'/\epsilon$$

$$(\delta_{AB})_{13} \longrightarrow \Delta m_{B_d}, \quad A_{CP}(B \rightarrow J/\psi K_S),$$

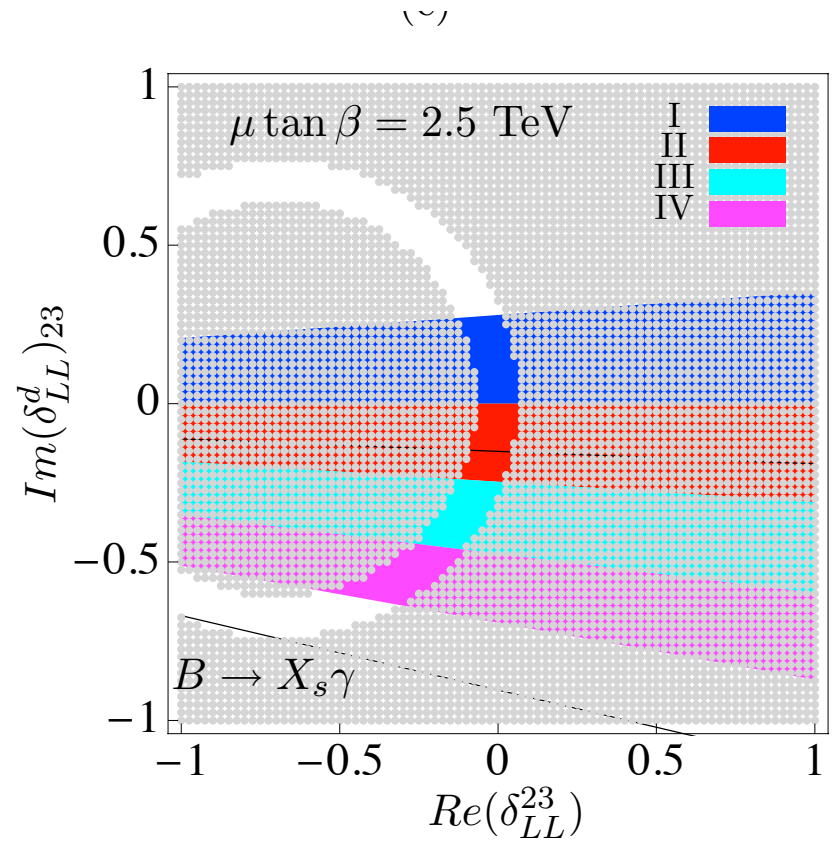
$$(\delta_{AB})_{23} \longrightarrow \Delta m_{B_s}, \quad b \rightarrow s\gamma, \quad A_{CP}(B \rightarrow \phi K_S)$$

*many future measurements*

# $(\delta_{AB})_{23}$ determination



**$B_s$ - $\bar{B}_s$  oscillation**



**$b \rightarrow s \gamma$**

# New particle searches in flavour physics ~hot topics~

$$B_s \rightarrow \mu^+ \mu^-$$

$$A_{SL}^b$$

$$S_{B_s \rightarrow J/\psi \phi} (= \sin 2\beta_s)$$

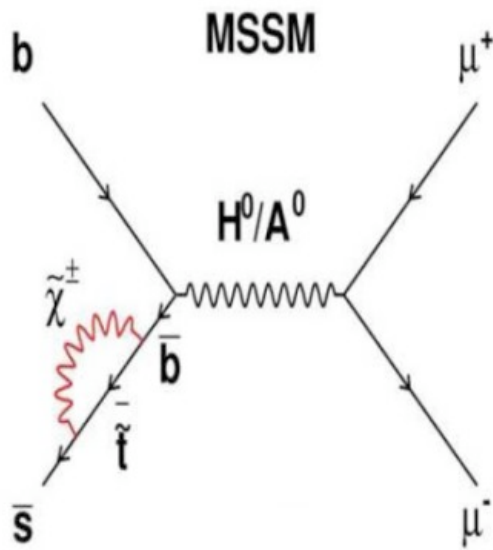
SUSY particle contributions to

$$B_s \rightarrow \mu^+ \mu^-$$



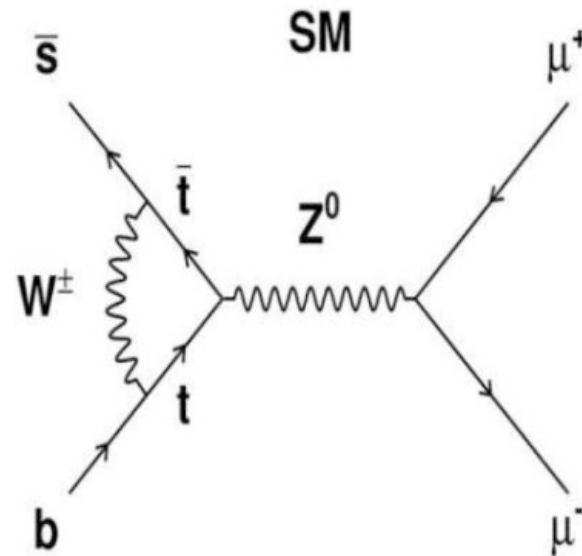
# SUSY particle contributions to

$$B_s \rightarrow \mu^+ \mu^-$$



$$Br(B_s \rightarrow \mu^+ \mu^-)_{\text{MSSM}} = \frac{m_b^2 m_\mu^2 \tan^6 \beta}{M_{A_0}^4}$$

*It could be large if  $\tan\beta$  is large*

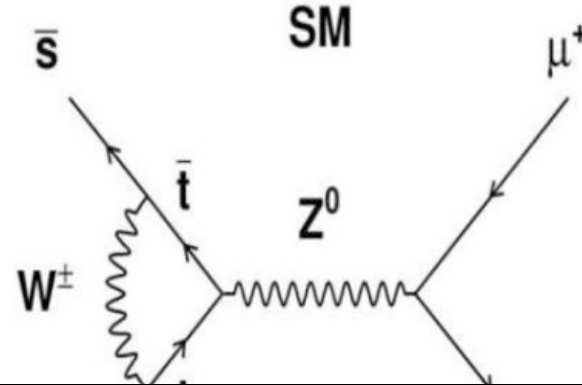
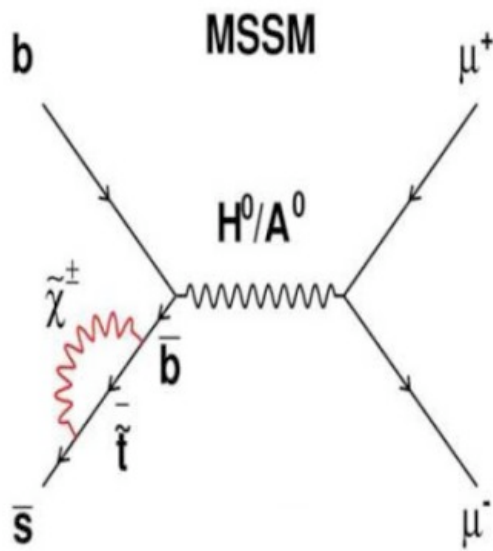


$$Br(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} = (3.2 \pm 0.2) \times 10^{-9}$$

*extremely small!!*

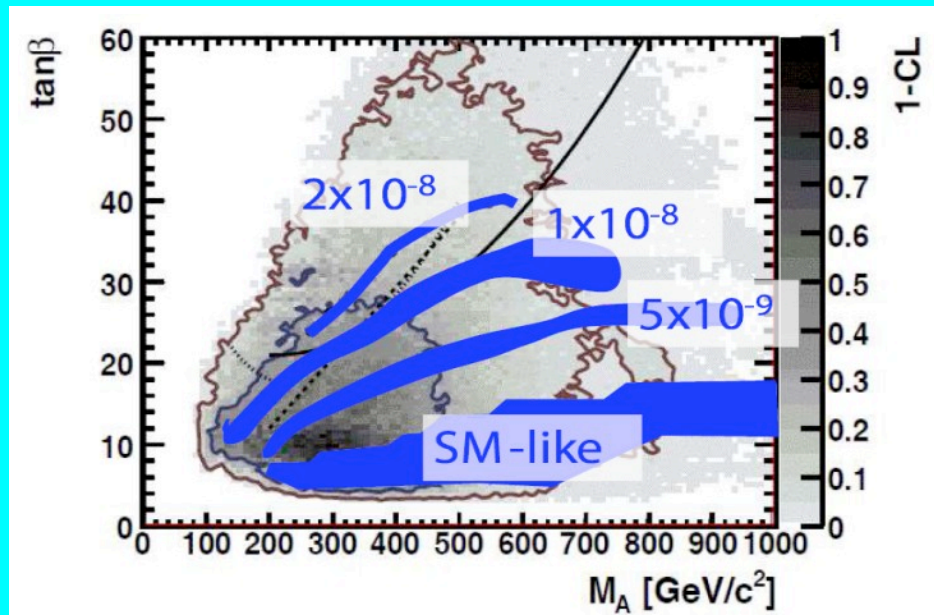
# SUSY particle contributions to

$$B_s \rightarrow \mu^+ \mu^-$$



$$Br(B_s \rightarrow \mu^+ \mu^-)_{\text{MSSM}} = \frac{m_b^2 m_\mu^2 \tan^6 \beta}{M_{A_0}^4}$$

It could be large if  $\tan\beta$  is large



# SUSY particle contributions to

$$B_s \rightarrow \mu^+ \mu^-$$

Excitement in the  
summer 2011!!!

Early summer, CDF ( $7\text{fb}^{-1}$ ) announced...

$$\text{Br}(B_s \rightarrow \mu^+ \mu^-) = (1.8_{-0.9}^{+1.1}) \times 10^{-8}$$

arXiv:1107.2304

CMS  
 $1.14\text{fb}^{-1}$   
(EPS2011)

No significant excess seen

this is  
 $B \rightarrow hh$

	Barrel	Endcap
$N_{\text{signal}}^{\text{exp}}$	$0.80 \pm 0.16$	$0.36 \pm 0.07$
$N_{\text{bg}}^{\text{exp}}$	$0.60 \pm 0.35$	$0.80 \pm 0.40$
$N_{\text{peak}}^{\text{exp}}$	$0.07 \pm 0.02$	$0.04 \pm 0.01$
$N_{\text{obs}}$	2	1

Calculate upper limits using frequentist CLs  
approach and taking  $f_s/f_u = 0.282 \pm 0.037$  [PDG]

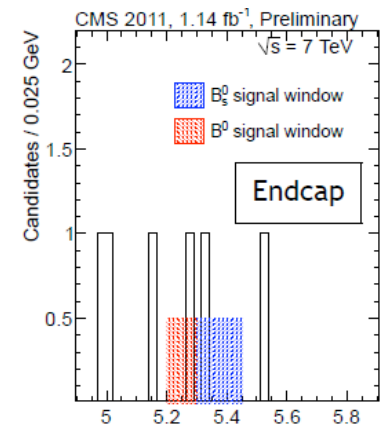
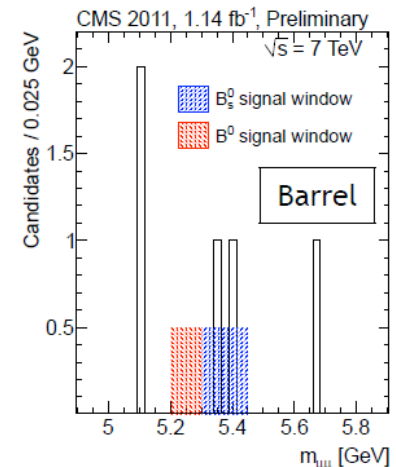
Expected limit at 95% C.L.  
(including presence of SM signal)

$$1.8 \times 10^{-8}$$

Observed limit at 95% (90%) C.L.  
p-value of bckgd only hypothesis

$$1.9 (1.6) \times 10^{-8}$$

$$11\%$$



# SUSY particle contributions to

$$B_s \rightarrow \mu^+ \mu^-$$

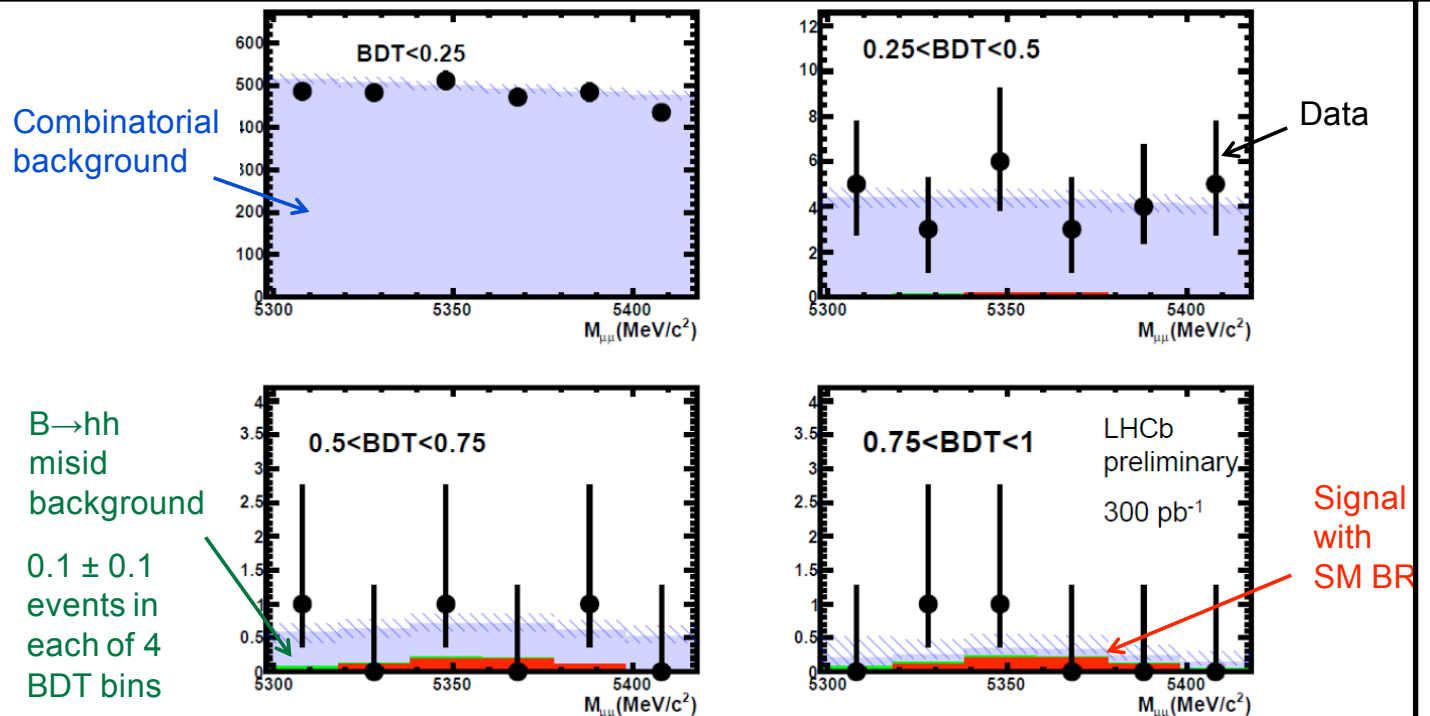
Excitement in the  
summer 2011!!!

Early summer, CDF ( $7fb^{-1}$ ) announced...

$$Br(B_s \rightarrow \mu^+ \mu^-) = (1.8_{-0.9}^{+1.1}) \times 10^{-8}$$

arXiv:1107.2304

LHCb  
 $300pb^{-1}$   
(EPS2011)

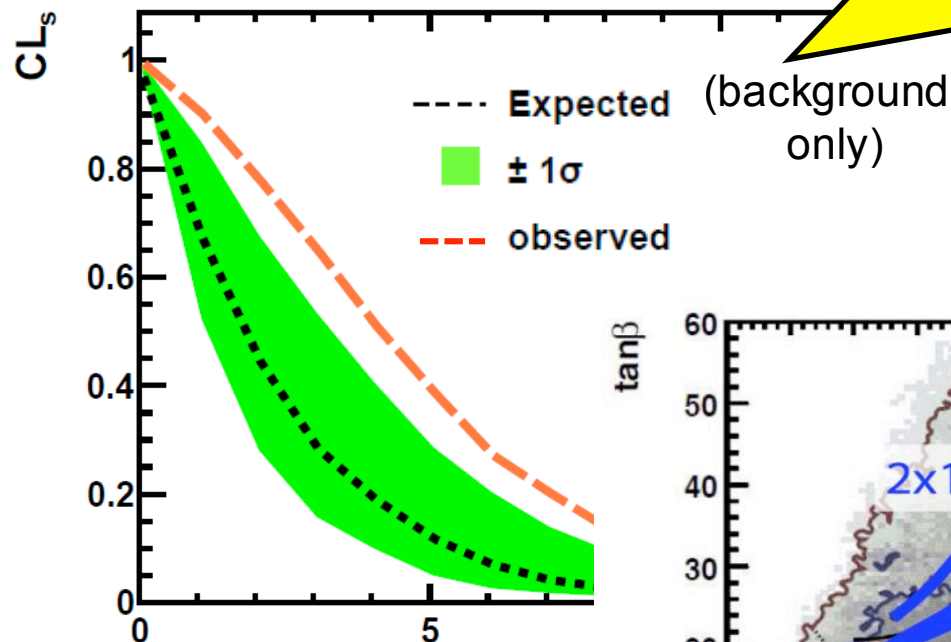


	BDT<0.25	0.25<BDT<0.5	0.5<BDT<0.75	0.75<BDT
Exp.combinatorial	$2968 \pm 69$	$25 \pm 2.5$	$2.99 \pm 0.89$	$0.66 \pm 0.40$
Exp. SM signal	$1.26 \pm 0.13$	$0.61 \pm 0.06$	$0.67 \pm 0.07$	$0.72 \pm 0.07$
Observed	2872	26	3	2

# SUSY particle contributions to

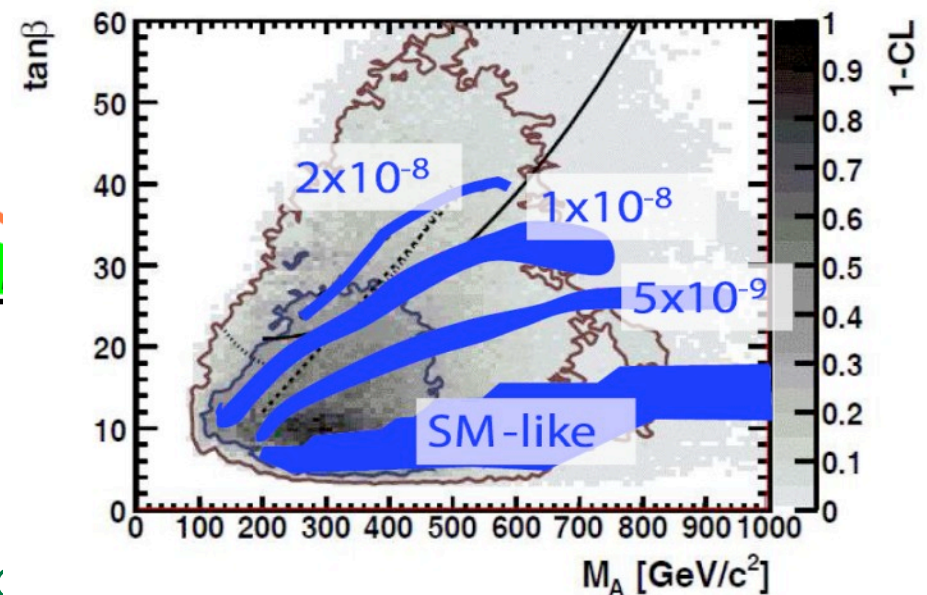
$$B_s \rightarrow \mu^+ \mu^-$$

So far we don't see it.  
But then...



Observed limit at 95% (  
This is 3.4 times the exp

A BR of  $1.8 \times 10^{-8}$  has a  $CL_s$  value of  $\sim 0.3\%$

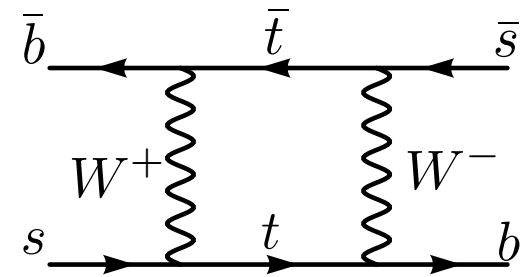
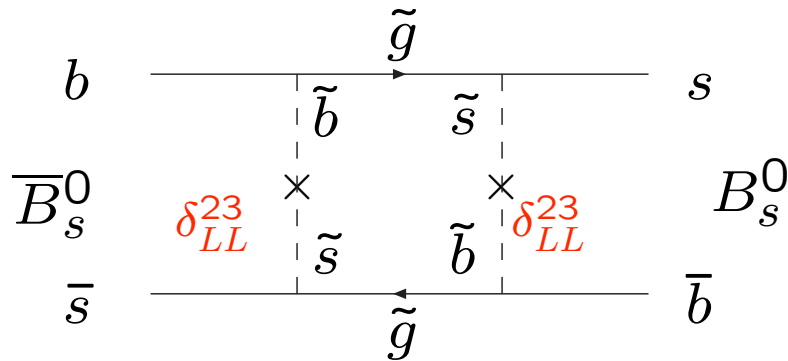


2304

2009-10-17

# New particle contributions to Bs oscillation

# New particle contributions to Bs oscillation



$$S_{J/\psi\phi} = \text{Im} \left[ \underbrace{\frac{q}{p}}_{\text{oscill.}} \underbrace{\frac{A(\overline{B}_s \rightarrow J/\psi\phi)}{A(B_s \rightarrow J/\psi\phi)}}_{\text{decay}} \right]$$

$$\simeq \text{Im} \left[ \underbrace{\frac{\delta_{LL}^{23}}{\delta_{LL}^{23*}}}_{\text{oscill.}} \underbrace{\frac{V_{cb}V_{cs}^*}{V_{cb}^*V_{cs}}}_{\text{decay}} \right]$$

$$= \sin 2\beta_s$$

$\beta_s$  can be large in  
BSM

$$S_{J/\psi\phi} = \text{Im} \left[ \underbrace{\frac{q}{p}}_{\text{oscill.}} \underbrace{\frac{A(\overline{B}_s \rightarrow J/\psi\phi)}{A(B_s \rightarrow J/\psi\phi)}}_{\text{decay}} \right]$$

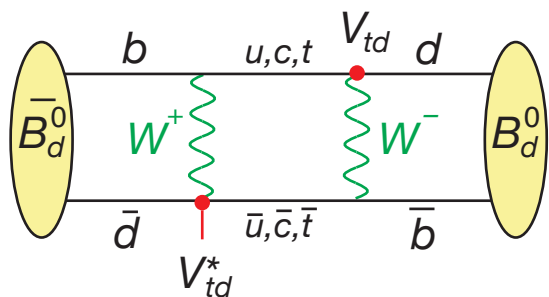
$$= \text{Im} \left[ \underbrace{\frac{V_{tb}V_{ts}^*}{V_{tb}^*V_{ts}}}_{\text{oscill.}} \underbrace{\frac{V_{cb}V_{cs}^*}{V_{cb}^*V_{cs}}}_{\text{decay}} \right]$$

$$= \sin 2\beta_s$$

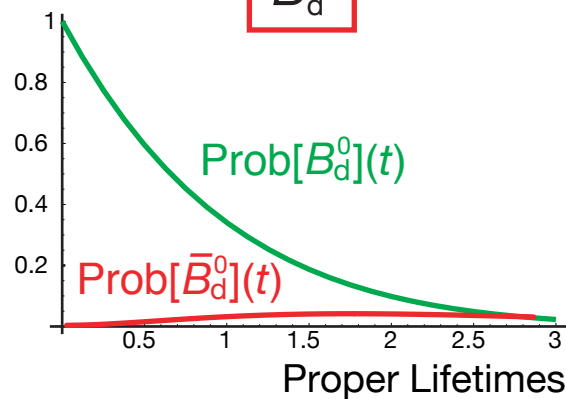
$\beta_s \simeq 1^\circ$  in SM



# Bs oscillation measurement at LHC/Tevatron I: $B_s \rightarrow J/\psi \phi$

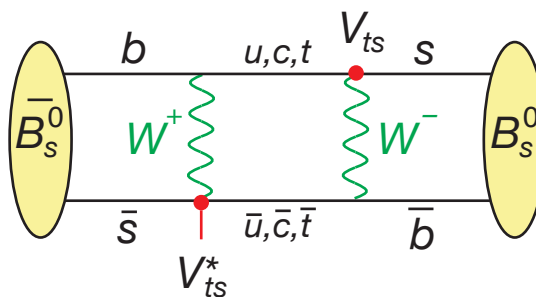


$B_d^0$

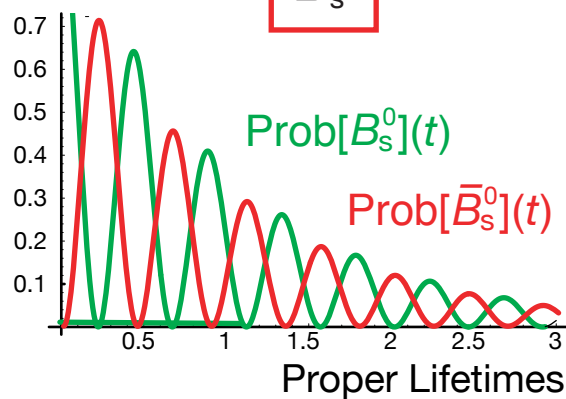


$$x = \frac{\Delta m}{\Gamma} \quad 0.776$$

$$y = \frac{\Delta \Gamma}{2\Gamma} < 0.01^*$$



$B_s^0$



$$26.1 \quad \text{Freq. of oscillation}$$

$$0.05$$

*Difference between the  $B_d/B_s$  system*

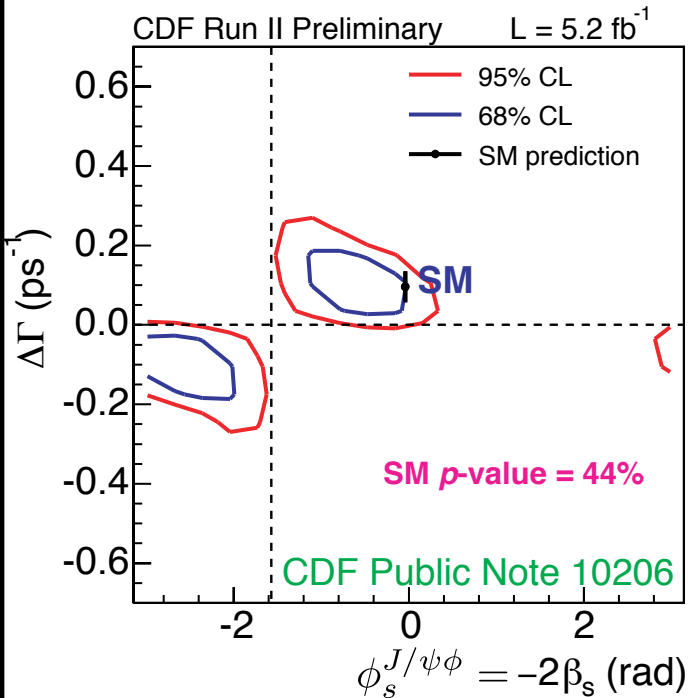
✓  $B_s$  oscillation is much faster (we need more Lorentz boost=LHC/Tevatron!)

✓ Non-negligible width difference modify the master formula



# Bs oscillation measurement at LHC/Tevatron I: $B_s \rightarrow J/\psi \phi$

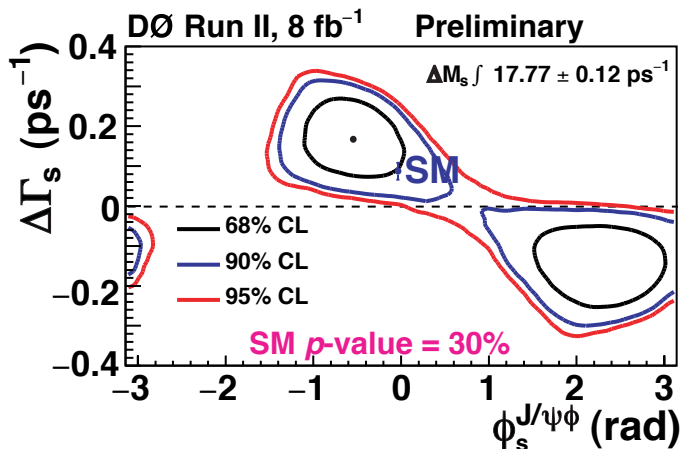
- Constraints in  $(\Delta\Gamma_s, \phi_s)$  plane



Plots all scaled to have identical axis unit sizes

$$\phi_s \in [-3.10, -2.16] \cup [-1.04, -0.04] \text{ 68\% CL}$$

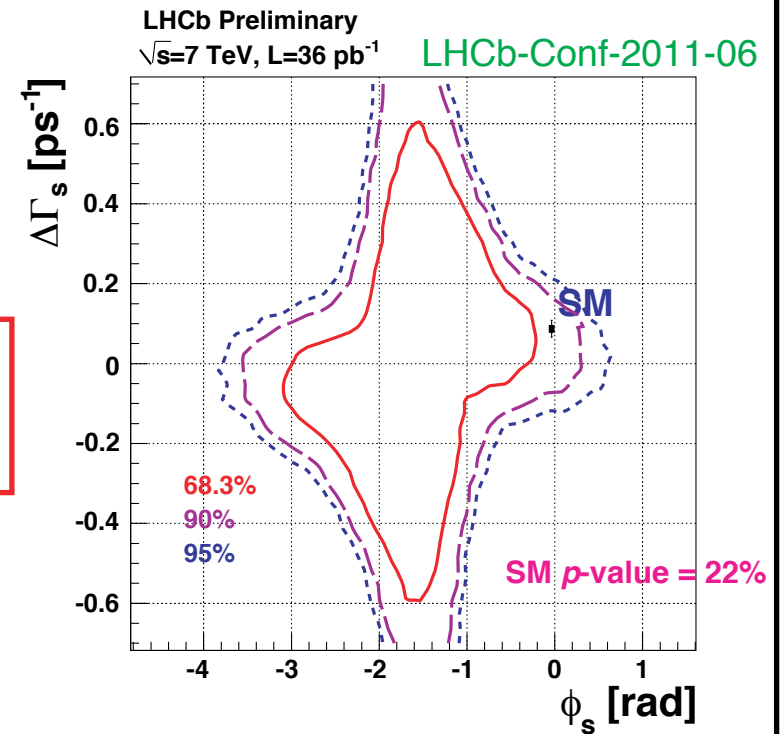
Tevatron: with less data, was previously at  $\gtrsim 2\sigma$  deviation from SM



$$\phi_s = -0.55^{+0.38}_{-0.36}$$

Lenz, Nierste, arXiv:1108.1346

$$\Delta\Gamma_s^{\text{SM}} = 0.087 \pm 0.021 \text{ ps}$$



$$\phi_s \in [-2.7, -0.5] \text{ 68\% CL}$$

LHCb result with 300  $\text{pb}^{-1}$  haven't been published: STAY TUNED!!!

# Bs oscillation measurement at LHC/Tevatron II: dimuon charge asymmetry

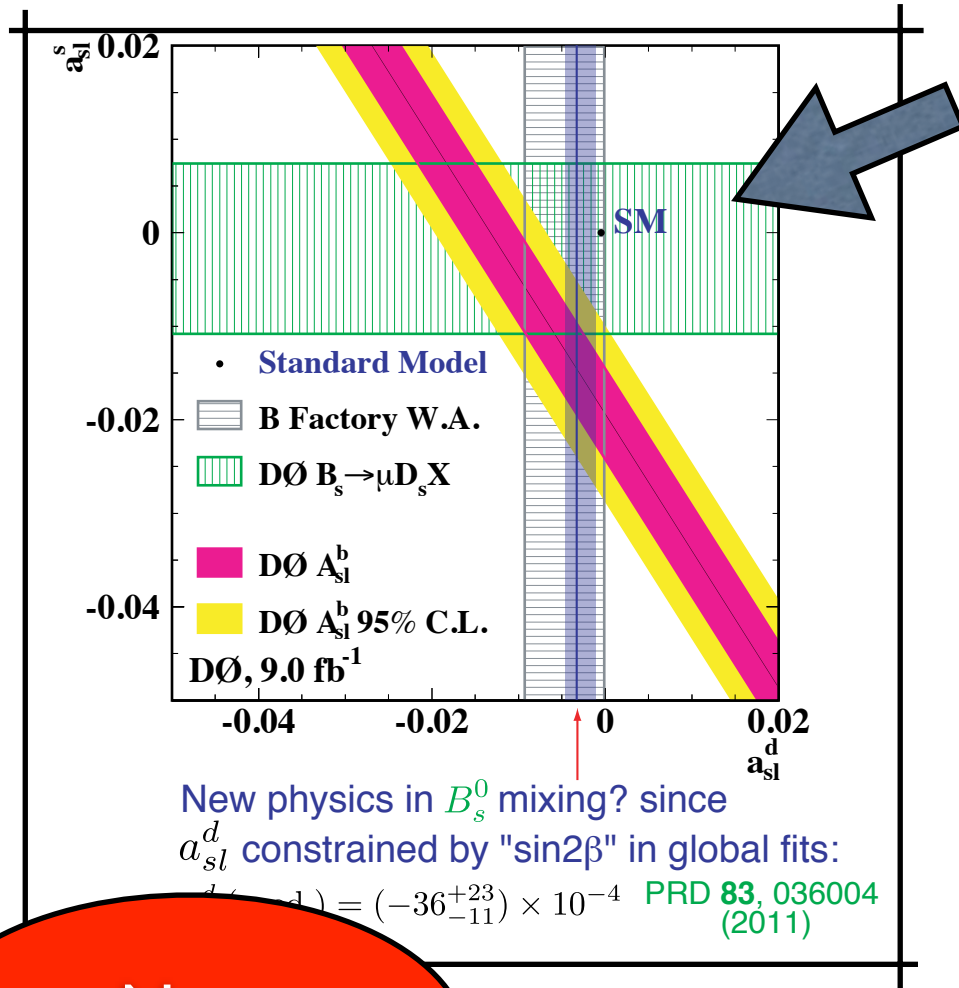


- Measure  $CP$  violation in mixing via

$$A_{sl}^b = \frac{N_b(\mu^+\mu^+) - N_b(\mu^-\mu^-)}{N_b(\mu^+\mu^+) + N_b(\mu^-\mu^-)}$$

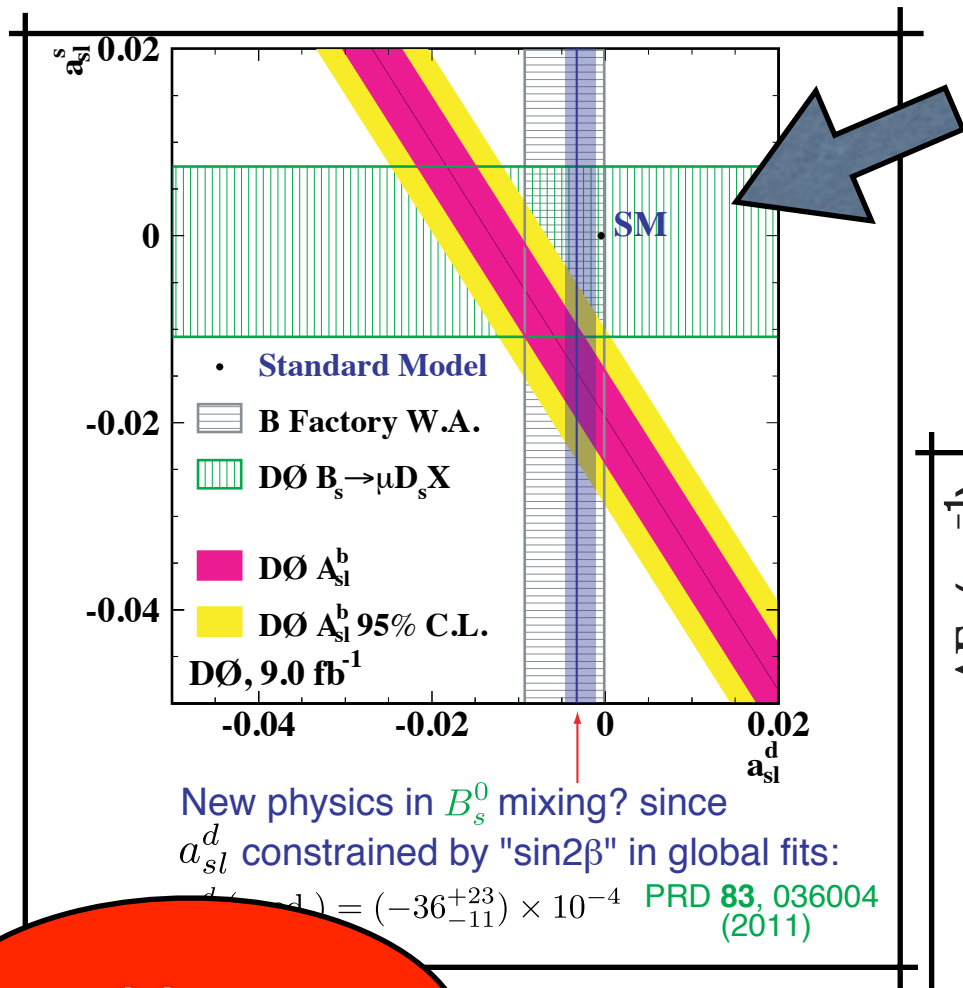
- DØ: Evidence for anomalous dimuon charge asymmetry, (6 fb<sup>-1</sup>, PRL **105**, 081801 (2010))  
3.2σ deviation from  $A_{sl}^b(SM) = (-0.023_{-0.006}^{+0.005})\%$

# Bs oscillation measurement at LHC/Tevatron II: dimuon charge asymmetry



New  
physics!!!!

# Bs oscillation measurement at LHC/Tevatron II: dimuon charge asymmetry

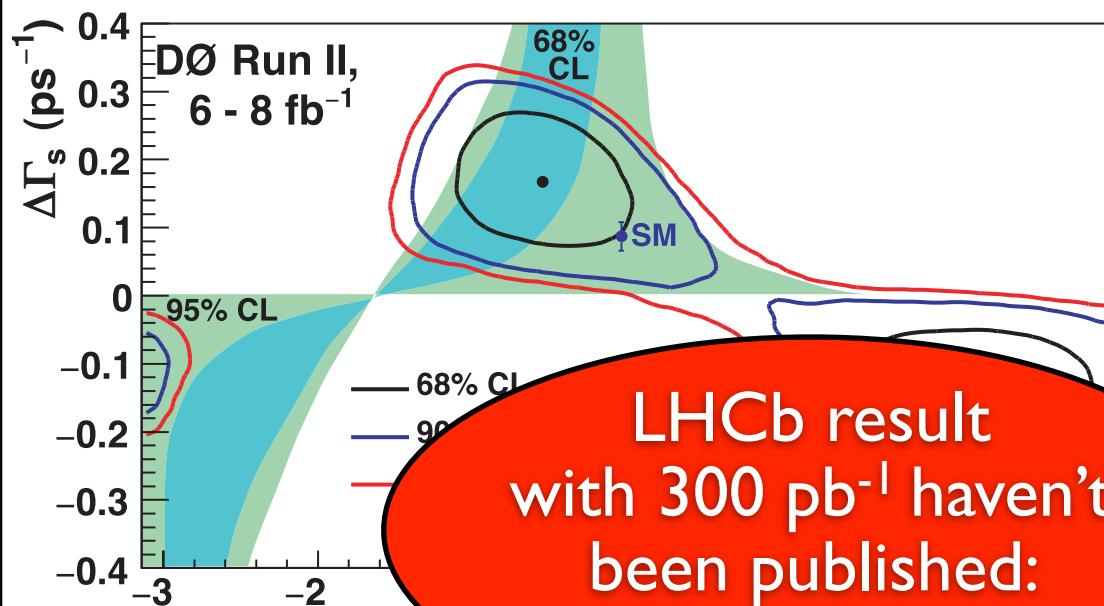


New physics in  $B_s^0$  mixing? since  $a_{sl}^d$  constrained by "sin2β" in global fits:  
 $a_{sl}^d = (-36^{+23}_{-11}) \times 10^{-4}$  PRD 83, 036004 (2011)

New physics!!!!

One can compare to the  $B_s$  oscillation measurement from  $B_s \rightarrow J/\psi \Phi$

$$a_{sl}^s = \frac{|\Gamma_s^{12}|}{|M_s^{12}|} \sin \phi_s = \frac{\Delta \Gamma_s}{\Delta M_s} \tan \phi_s'$$



LHCb result with 300 pb<sup>-1</sup> haven't been published: STAY TUNED!!!