

Microscopic theory of the γ -decay of nuclear giant resonances

Marco Brenna, Gianluca Colò and Pier Francesco Bortignon

14-16 November 2011

<http://arxiv.org/abs/1111.0619>



UNIVERSITÀ
DEGLI STUDI
DI MILANO



Outline

- 1 Theoretical Overview
 - Giant Resonances
 - PVC
- 2 Results
 - Decay to GS
 - Decay to a vibrational state
- 3 Conclusions

Giant Resonances

General features

- Signature of some many-body correlations inside the nucleus
- Nuclear interaction in a given channel
 - Gamow – Teller Resonance \Rightarrow Spin – Isospin interaction
- Parameters of the equation of state of nuclear matter
 - Monopole \Rightarrow Nuclear Compressibility
 - Dipole \Rightarrow Symmetry Energy
 - Quadrupole \Rightarrow Effective mass
- 60-year-studies on GRs (since 1947), two books
 - P.F. Bortignon, A. Bracco, R.A. Broglia, 1998
 - M.N. Harakeh, A. van der Woude, 2001
- Nowadays: more exclusive experiments \Rightarrow γ -decay (LNL-INFN, June 2010)
- Resonances in exotic nuclei (n – rich)

Giant Resonances

General features

- Energy: 10 – 30 MeV
- Width: 2 – 5 MeV
- High fraction of Energy Weighted Sum Rule (EWSR)

Decay of GRs

- Particle emission (neutrons)
- Compound nucleus
- γ -decay

γ -decay

- suppressed with respect to particle decay ($\sim 10^{-3}$)
- extremely sensitive to the resonance multipolarity
- decay to GS: strength of resonances
- decay to low-lying: sensitive to the wavefunctions
- direct decay complementary to inelastic scattering data (based on not well known assumption – reaction model, optical potential)
- compound γ -decay should be taken into account for a comparison with experimental data

Giant Resonances

Theoretical description

RPA...

Microscopically: coherent superposition of p – h excitations



RPA



- Linear response theory
- Fully self - consistent calculations with microscopic interactions (Skyrme, Gogny, RMF)

Giant Resonances

Theoretical description

RPA...

Microscopically: coherent superposition of p – h excitations



RPA



- Linear response theory
- Fully self - consistent calculations with microscopic interactions (Skyrme, Gogny, RMF)

...and Beyond

Some features (as decay to low-lying states) need non-linear term.



Nuclear Field Theory

Bortignon et al.

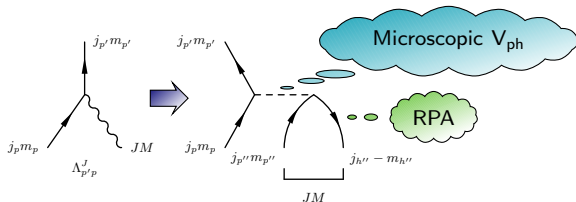
*Phys. Rep.***30**(1977)305



- Perturbative theory
- Interweaving between single-particles and phonons

Particle-Vibration Coupling (PVC) vertex

- In the past: many phenomenological calculations with uncontrolled inputs
- Microscopic calculations are now feasible. From Hartree or Hartree-Fock with V_{eff} (assuming this includes short-range correlations), add PVC on top of it. All calculated using the same Hamiltonian or EDF consistently.



- Pioneering Skyrme calculation by V. Bernard and N. Van Giai in the 80s (neglect of the velocity-dependent part of V_{eff} in the PVC vertex). *Nucl. Phys.* **A348**(1980)75.
- RMF + PVC calculations have been done first by E. Litvinova and P. Ring. More results recently by E. Litvinova and A. Afanasjev.

Particle-Vibration Coupling (PVC) vertex

A consistent study

In the version of PVC implemented here the treatment of the coupling is **exact**, namely we do not wish to make any approximation in the vertex.

$$\langle i || V || j, nJ \rangle = \sqrt{2J+1} \sum_{ph} X_{ph}^{nJ} V_J(ihjp) + (-)^{j_h - j_p + J} Y_{ph}^{nJ} V_J(ipjh)$$

The whole phonon wavefunction is considered, and all the terms of the Skyrme force enter the p-h matrix elements

$$V_J(ihjp) = \sum_{\{m\}} (-)^{j_j - m_j + j_h - m_h} \langle j_j m_j j_j - m_j | JM \rangle \langle j_p m_p j_h - m_h | JM \rangle v_{ihjp}$$

Consistent treatment of the coupling vertex in the Skyrme framework:

HF single particle states, RPA phonons, microscopic interaction in PVC vertex
 (G. Colò, H. Sagawa, P. F. Bortignon, *Phys. Rev.* **C82**(2010)64307)

γ decay width

$$\Gamma_\gamma(E\lambda; i \rightarrow f) \propto E^{2\lambda+1} B(E\lambda; i \rightarrow f)$$

REDUCED TRANSITION PROBABILITY

$$B(E\lambda; i \rightarrow f) = \frac{1}{2J_i + 1} |\langle J_f \| Q_\lambda^{(E)} \| J_i \rangle|^2$$

ELECTROMAGNETIC OPERATOR (LONG-WAVELENGTH LIMIT)

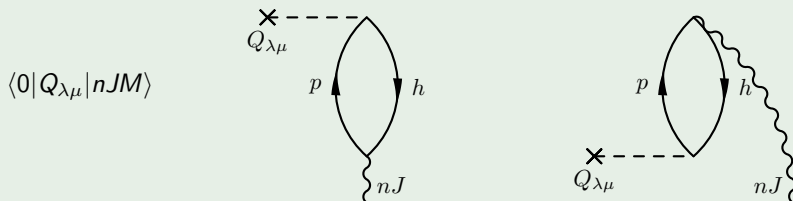
$$Q_{\lambda\mu}^{(E)} = \sum_{i=1}^A e_i^\lambda i^\lambda r_i^\lambda Y_{\lambda\mu}^*(\hat{\mathbf{r}}_i)$$

EFFECTIVE CHARGE DUE TO NUCLEAR RECOIL

$$e_p^\lambda = e \left[\left(1 - \frac{1}{A}\right)^\lambda + (-)^{\lambda} \frac{Z-1}{A^\lambda} \right]$$

$$e_n^\lambda = eZ \left(-\frac{1}{A} \right)^\lambda$$

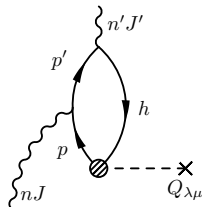
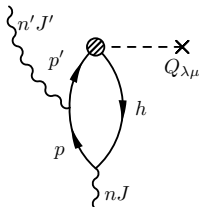
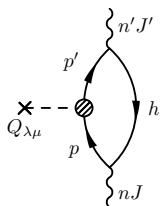
γ decay to the ground state



$$\langle 0 || Q_{\lambda} || nJ \rangle = \sum_{ph} \langle p || Q_{\lambda} || h \rangle \left(\frac{\langle p || V || h, nJ \rangle}{E_J - \epsilon_{ph} + i\eta} - \frac{\langle h || V || p, nJ \rangle}{E_J + \epsilon_{ph} + i\eta'} \right)$$

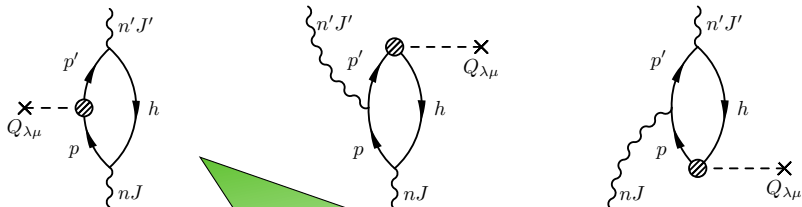
γ decay to low-lying states

NFT necessary: 12 diagrams contribute to the matrix element



γ decay to low-lying states

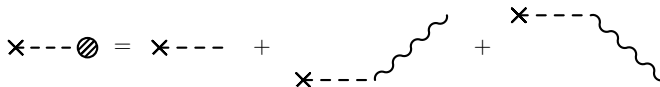
NFT necessary: 12 diagrams contribute to the matrix element



$$\sum_{pp'h} (-)^{J+\lambda+J'+1} \begin{Bmatrix} J & \lambda & J' \\ j_{p'} & j_h & j_p \end{Bmatrix} \frac{\langle p || V || h, nJ \rangle \langle h, mJ' || V || p' \rangle Q_{pp'}^{\lambda pol}}{(E_J - \epsilon_{ph} + i\eta)(E_{J'} - \epsilon_{p'h})}$$

γ decay to low-lying states

The polarization contribution



Polarization \blacktriangledown

External field partially screened by the interaction with intermediate states

$$Q_{ij}^{\lambda pol} = \langle i || Q_{\lambda} || j \rangle + \sum_{n'} \frac{1}{\sqrt{2\lambda + 1}} \left[\frac{\langle 0 || Q_{\lambda} || n' \lambda \rangle \langle i, n' \lambda || V || j \rangle}{(E_J - E_{J'}) - \hbar\omega_{\lambda} + i\frac{\Gamma_D}{2}} - \frac{\langle i || V || j, n' \lambda \rangle \langle n' \lambda || Q_{\lambda} || 0 \rangle}{(E_J - E_{J'}) + \hbar\omega_{\lambda} + i\frac{\Gamma_D}{2}} \right]$$

Results – ^{208}Pb

- Decay of Isoscalar Giant Quadrupole Resonance (ISGQR) in ^{208}Pb to the ground state and to the first $J^\pi = 3^-$ state
- Experiment at LNL in June 2010 (*Acta Phys. Pol. B***42**(2011)653)
- Consistent approach to the coupling vertex:
 - Single particle states: HF
 - Phonons: self-consistent RPA with Skyrme functional
 - PVC Vertex: microscopic Skyrme interaction
- 4 Skyrme interactions: SLy5, SGII, SkP, LNS
- Submitted to *PRC*, <http://arxiv.org/abs/1111.0619>

$$\begin{aligned}
 V(\mathbf{r}_1, \mathbf{r}_2) = & t_0(1 + x_0 P_\sigma)\delta(\mathbf{r}) + \frac{1}{2}t_1(1 + x_1 P_\sigma)[\mathbf{P}'^2\delta(\mathbf{r}) + \delta(\mathbf{r})\mathbf{P}^2] \\
 & + t_2(1 + x_2 P_\sigma)\mathbf{P}' \cdot \delta(\mathbf{r})\mathbf{P} + \frac{t_3}{6}(1 + x_3 P_\sigma)[\rho(\mathbf{R})]^\sigma \delta(\mathbf{r}) \\
 & + iW_0\boldsymbol{\sigma} \cdot [\mathbf{P}' \times \delta(\mathbf{r})\mathbf{P}]
 \end{aligned}$$


Energy and collectivity of the states

J^π	ISGQR		3^-	
	E [MeV]	EWSR [%]	E [MeV]	$B(E3) \uparrow [10^5 e^2 \cdot \text{fm}^6]$
SLy5	12.28	70	3.62	6.54
SGII	11.72	72	3.14	6.58
SkP	10.28	82	3.29	5.11
LNS	12.10	67	3.19	5.67
Exp.	10.9 \pm 3	100	2.6145 \pm 3	6.11 \pm 9

Experimental data from *NDS108*(2007)1583

Decay to the GS

Interaction	E_{GQR} [MeV]	Γ_γ [eV]	
		RPA	RPA'
SLy5	12.28	231.54	160
SGII	11.72	163.22	138
SkP	10.28	119.18	170
LNS	12.10	176.57	135
Speth et al., <i>PRC</i> 85 (1985)2310	10.60	112 – theor.	
Bortignon et al., <i>PLB</i> 148 (1984)20	11.20	142 – theor.	
Beene et al., <i>PLB</i> 164 (1985)19	11.20	175 – theor.	
Beene et al., <i>PRC</i> 39 (1989)1307	10.60	130 \pm 40 – exp.	

Consistent with experimental value through an energy scaling ($\Delta E = 1$ MeV \Rightarrow increase Γ_γ by 50%) 

Decay to the 3^- state

Interaction	E_{tran} [MeV]	Γ_{γ} [eV]
SLy5	8.66	3.39
SGII	8.58	29.18
SkP	6.99	8.34
LNS	8.90	39.87
Speth et al., <i>PRC</i> 85 (1985)2310	7.99	4.00 – <i>theor.</i>
Bortignon et al., <i>PLB</i> 148 (1984)20	8.59	3.50 – <i>theor.</i>
Beene et al., <i>PRC</i> 39 (1989)1307	7.99	5.00 \pm 5.00 – <i>exp.</i>

Decay to the 3^- state

The SLy5 case

$$\Gamma_\gamma \text{ for a typical ph at 8.5 MeV [eV]} \approx 10^3$$

$$\Gamma_\gamma \text{ [eV]} \quad 3.39$$

Decay to the 3^- state

The SLy5 case

Γ_γ for a typical ph at 8.5 MeV [eV]	$\approx 10^3$
Recoupling	3
Quenching factors	
Γ_γ [eV]	3.39

Decay to the 3^- state

The SLy5 case

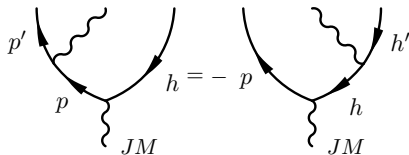
Γ_γ for a typical ph at 8.5 MeV [eV]		$\approx 10^3$
Quenching factors	Recoupling	3
	$\pi - \nu$ cancellation	3
Γ_γ [eV]		3.39

$$Q_{ij} = \left(\tau_z - \frac{N - Z}{A} \right)_j \langle i || r^\lambda Y_\lambda || j \rangle$$

Decay to the 3^- state

The SLy5 case

Γ_γ for a typical ph at 8.5 MeV [eV]		$\approx 10^3$
Quenching factors	Recoupling	3
	$\pi - \nu$ cancellation	3
	$p - h$ cancellation	3 - 4
Γ_γ [eV]		3.39



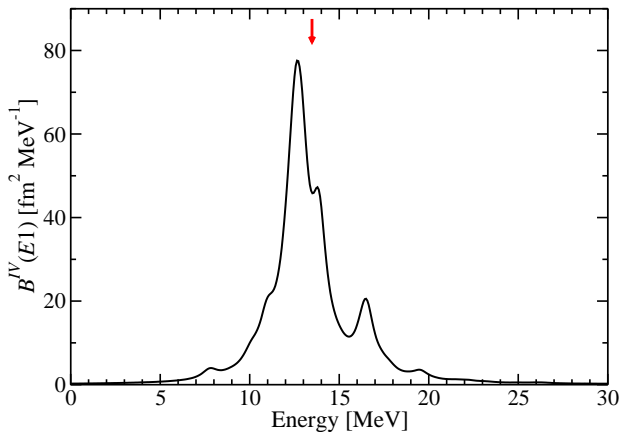
Conclusions ▶

- Microscopic and consistent treatment of the γ decay
- γ decay width to the GS not so able to discriminate between models
- γ decay width to the 3^- very sensitive to the interaction used
 - Dipole states
- Comparison with the experiment at LNL – INFN (June 2010)
- Other closed shell nuclei: ^{90}Zr (LNL - 2010),...
- PDR?

Backup Slides

The dipole isovector strength

[◀ Back to Conclusions](#)

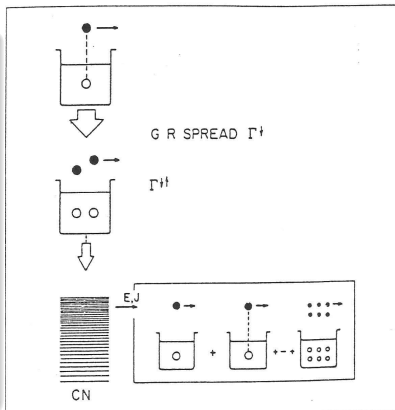


The decay of the compound nucleus

$$\langle \Gamma_{\gamma 0}^{CN} \rangle = \frac{X(\lambda) b_{E\lambda}(E) \left(\frac{E}{\hbar c}\right)^{2\lambda+1}}{\rho_I(E)}$$

$$X(\lambda) = \frac{8\pi(\lambda + 1)}{\lambda[(2\lambda + 1)!!]^2}$$

- $\rho_I(E)$ density of compound states with spin I at energy E
- $b_{E\lambda}(E)$ reduced transition probability per unit energy



Bohr – Mottelson model

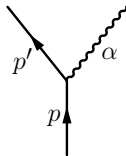
◀ Back to PVC

In the original Bohr-Mottelson model, the phonons are treated as fluctuations δU of the mean field U and their properties are taken from experiment.

$$R = R_0 \left(1 + \sum_{\lambda\mu} \alpha_{\lambda\mu}(t) Y_{\lambda\mu}^*(\hat{r}) \right) \quad \Rightarrow \quad U(\mathbf{r} - \mathbf{R}) = U(\mathbf{r} - \mathbf{R}_0) + \delta U$$

$$\delta U = -R_0 \frac{\partial U}{\partial r} \sum_{\lambda\mu} \alpha_{\lambda\mu} Y_{\lambda\mu}^*$$

$$\langle n_\alpha = 1, p' | \delta U | p \rangle$$



$$\Gamma_{\gamma}(Ej; i \rightarrow f) = \frac{8\pi(2j+1)}{j[(2j+1)!!]^2} \left(\frac{E}{\hbar c}\right)^{2j+1} B(Ej; i \rightarrow f)$$