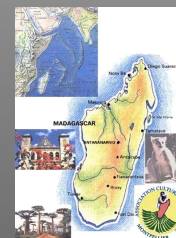




Quantum
Chromo-
Dynamics



QCD & Physique Hadronique

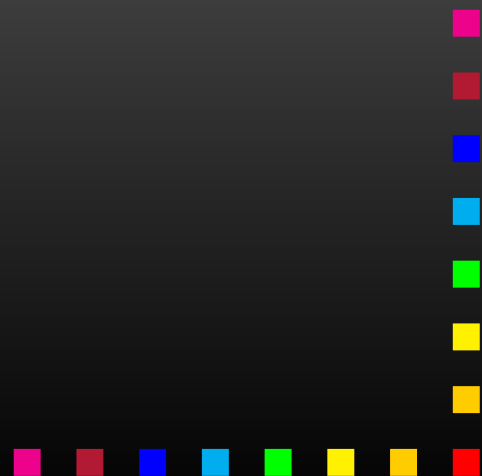
LUPM 11 (10-11 Octobre 2011)
St Martin de Londres (Hérault)

Stephan Narison

CNRS / IN2P3 - LUPM (Montpellier)



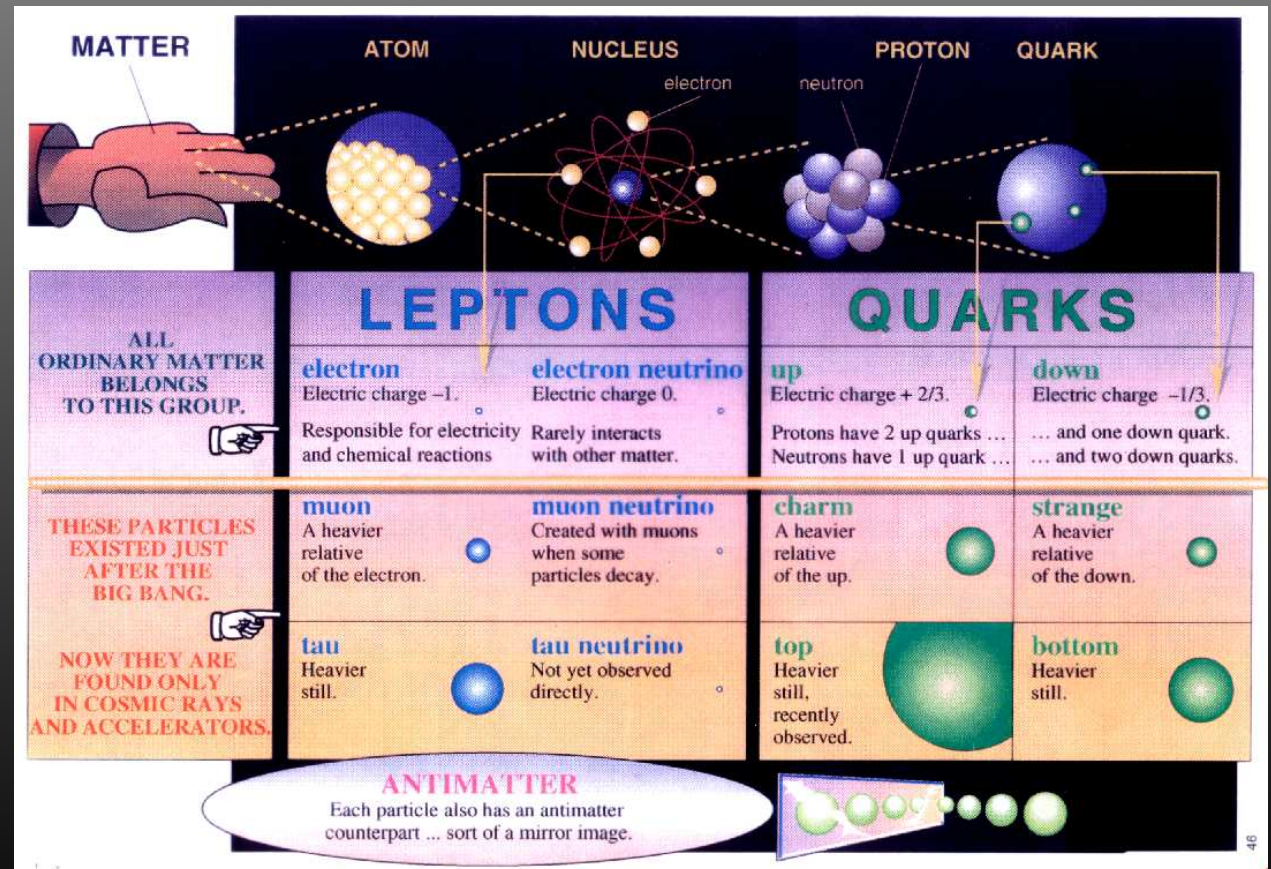
Vers l'Infiniment Petit : Le Modèle Standard



Vers l'Infiniment Petit : Le Modèle Standard

- 6 quarks $\oplus$ 6 leptons constituents

Glashow-Weinberg-Salam : Prix Nobel 1979



- ⇒ • Quelles sont les Forces qui regissent la Nature ?
Forces électromagnétique, faible, forte & gravitation

THE FORCES IN NATURE			
TYPE	INTENSITY OF FORCES (DECREASING ORDER)	BINDING PARTICLE (FIELD QUANTUM)	OCCURS IN :
STRONG NUCLEAR FORCE	~ 1 <i>10^{-13} cm</i>	GLUONS (NO MASS)	ATOMIC NUCLEUS
ELECTRO -MAGNETIC FORCE	$\sim 10^{-3}$	PHOTONS (NO MASS)	ATOMIC SHELL ELECTROTECHNIQUE
WEAK NUCLEAR FORCE	$\sim 10^{-5}$	BOSONS Z^0, W^+, W^- (HEAVY)	RADIOACTIVE BETA DESINTEGRATION
GRAVITATION	$\sim 10^{-38}$	GRAVITONS (?)	HEAVENLY BODIES

THE EXCHANGE OF PARTICLES IS RESPONSIBLE FOR THE FORCE

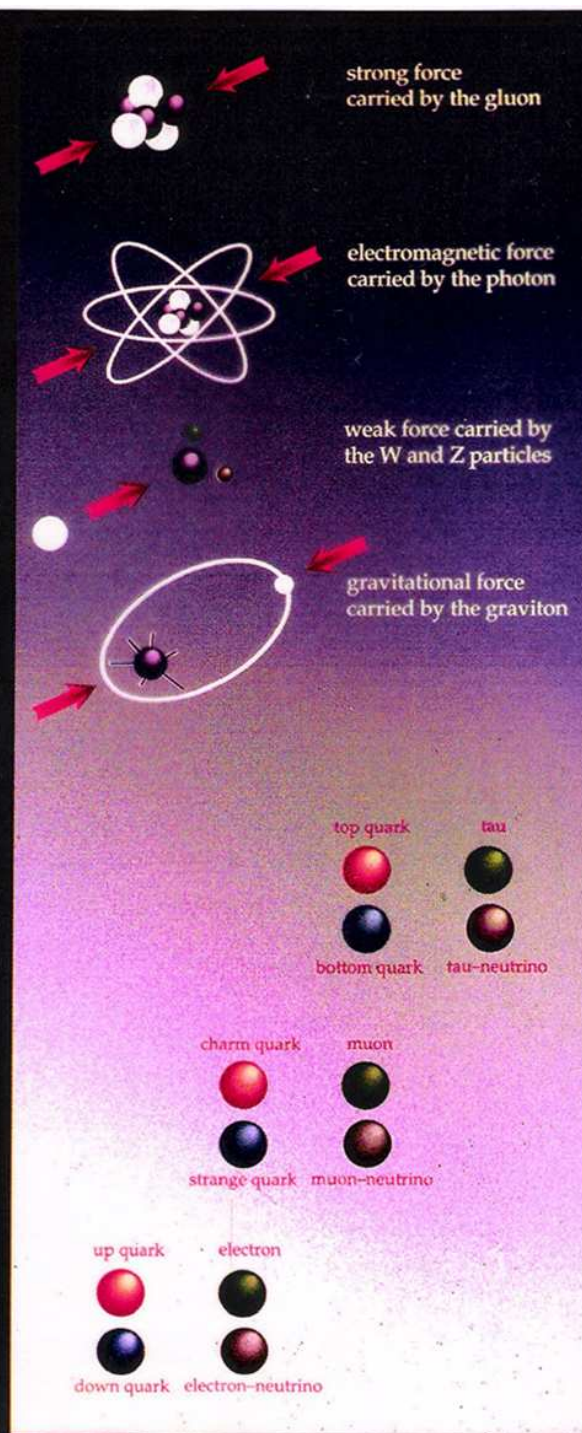
G. t'Hooft-M. Veltman
Prix Nobel 1999



D. Gross, D. Politzer,
F. Wilczek
Prix Nobel 2004



Chromodynamique
Quantique (QCD)



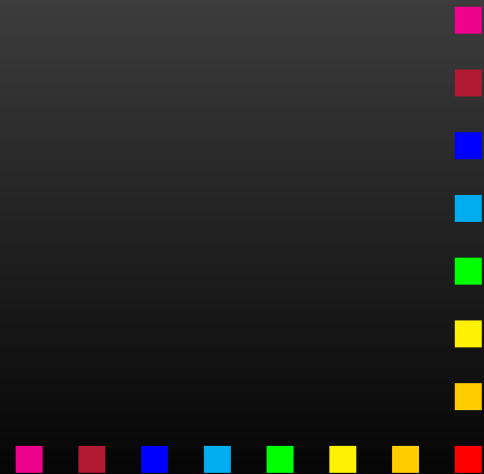
C. Rubbia V. Der Meer
Prix Nobel 1984



⇒ Le Boson de Higgs

1 maillon manquant du **modèle standard**:

La particule de Dieu ?

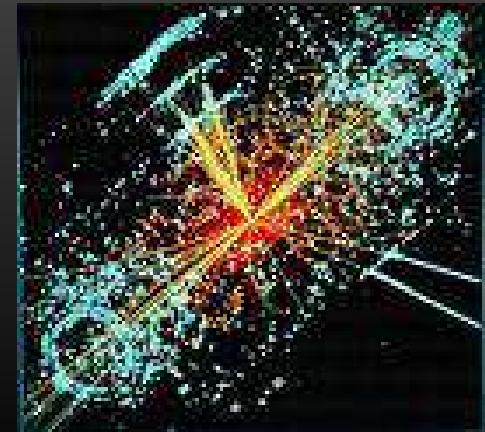
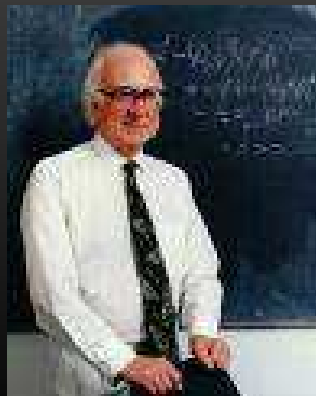


⇒ Le Boson de Higgs

1 maillon manquant du **modèle standard**:

La **particule de Dieu** ?

- Donne des masses aux **quarks**, **leptons**, **bosons de jauge**
- On prédit sa masse **autour de 100 GeV** : **visible au LHC** !
- Sa **(non)** decouverte **est cruciale** pour l'avenir de la **physique**



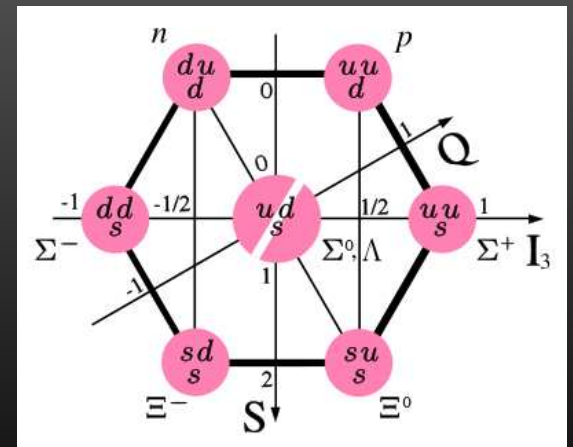
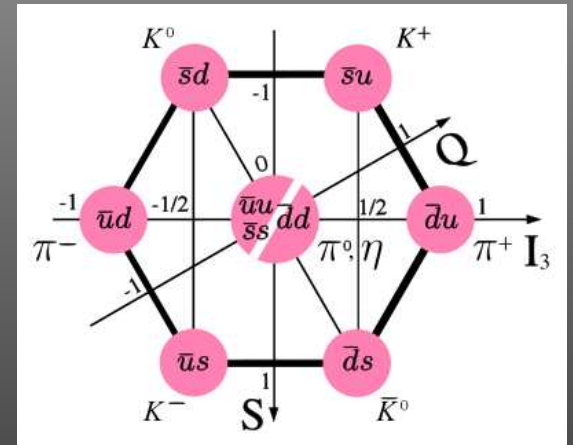


● Les Hadrons des quarks u, d, s ?

- Modèle des quarks de Gell-Mann (Prix Nobel 1969)

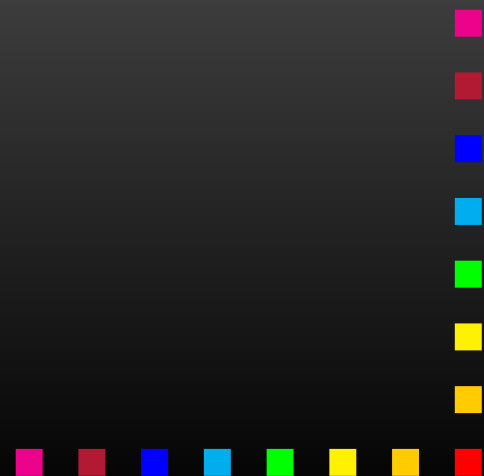
a) Mesons : $\bar{q}_1 q_2$: $M_\pi = 140 \text{ MeV}$

b) Baryons : $q_1 q_2 q_3$: $M_p = 1 \text{ GeV}$



- Décrit maintenant par la Chromodynamique Quantique (QCD):
La théorie de la Couleur

Les Series de Conference Internationales



Les Series de Conference Internationales

- QCD-Montpellier depuis 1985 (Euroconferences 1994-2000)

QCD 10

15th HIGH-ENERGY PHYSICS
INTERNATIONAL CONFERENCE
IN QUANTUM CHROMODYNAMICS (QCD)



25 YEARS OF THE QCD MONTPELLIER
INTERNATIONAL CONFERENCE



SCIENTIFIC PROGRAM

- QCD at Colliders
- Physics of tau-decays and e^+e^-
- Physics of Light Flavours and Glueballs
- Physics of Heavy Flavours
- CP-Violation
- QCD Plasma

INTERNATIONAL COMMITTEE

H. Fritzsch (Munich - DE)
A. Di Giacomo (Pisa - IT)
M. Neubert (Mainz - DE)
A. Pich (Valencia - ES)
E. de Rafael (Marseille - FR)
J.M. Richard (Grenoble - FR)
V.I. Zakharov (Moscow - RU)
K. Zalewski (Cracow - PL).

CONTACT

CHAIRMAN OF THE ORGANIZATION
Stephan Narison
IN2P3/CNRS-Montpellier-France
Email: snarison@gmail.com

QCD SECRETARIAT
Marie Razafindrakoto
Laboratoire de Physique Théorique
et Astroparticules IN2P3/CNRS,
Université de Montpellier 2 - Martin de Londres (10- 11 Octobre 2011) – p. 7/3

- Photo QCD 2010



- HEP-MAD (Antananarivo) depuis 2001

HEP-MAD 11

5th High-Energy Physics International Conference in Madagascar

25-31th august 2011 (Antananarivo)



Scientific program

Physics at LHC and at some other accelerators
QCD (non) perturbative phenomena
Weak decays and CP-violation
Physics beyond the standard model
Astroparticles and neutrino oscillations

International committee

E. Aslanides (Marseille-FR)
J. Ellis (CERN-CH)
A. Di Giacomo (Pisa-IT)
M. Neubert (Mainz-D)
A. Pich (Valencia-ES)
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Chairman of the organization

Stephan Narison (Montpellier-FR)
Laboratoire Univers et Particules de Montpellier (LUPM)
UM2, Place Eugene Bataillon,
34090 Montpellier Cedex 05 FR

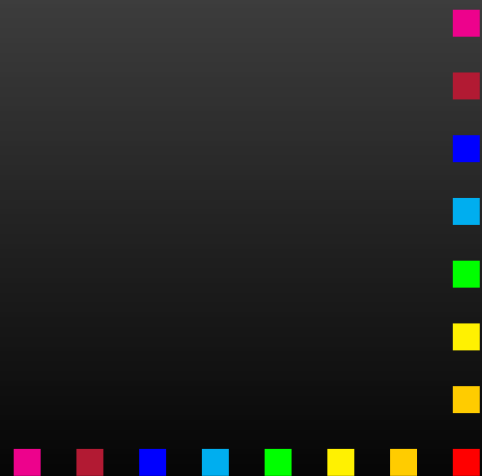
- Photo HEP-MAD 2011



Developpement de l'HEP à Madagascar

- Creation de l'Institut de recherche iHEP-MAD en 2004

Voir le site: <http://www.lpta.univ-montp2.fr/users/qcd/ihepmadtitle.html>



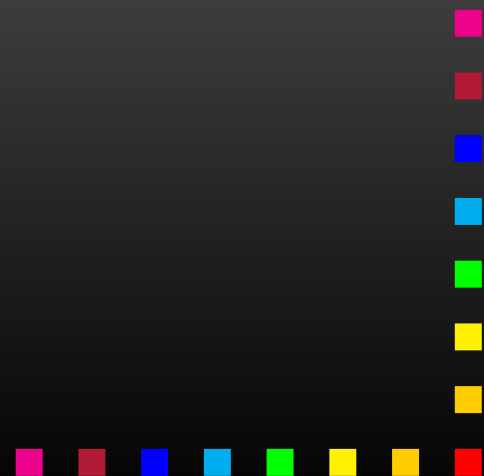
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- Vulgarisation: univs, centres culturels, lycées & collèges, presses,...



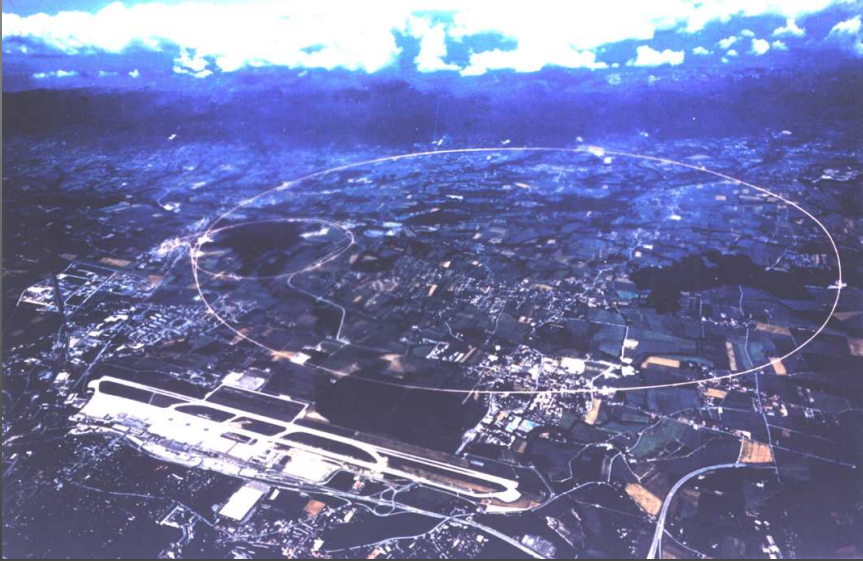
Exploration de l'Infiniment Petit

- Accélérateur des particules: LHC au CERN



Exploration de l'Infiniment Petit

- Accélérateur des particules: LHC au CERN



Tunnel de 27km; 100m au-dessous du sol; Energie de 7000 GeV = 70 fois le LEP = 7 fois le Tevatron (peut fondre 500kg de cuivre); 600 millions de choc proton/proton par sec et 10^{17} pendant toute la durée de l'expérience; Coût: 2.6 Milliards d'Euros + 1.2 Milliard pour le personnel.

Exploration de l'Infiniment Grand

- Fermi Gamma-ray Space Telescope

Exploration du Cosmos dans la région : 10 keV-300 GeV

- Origine des rayons cosmiques
- Mécanisme de la matière noire
(96% de l'univers!)
- Accélération de Jets de matière
près des trous noirs
- ...



- Telescope HESS High Energy Stereoscopic System
Le site et telescopes de Namibie (Afrique) (de Georges Vasileiadis)

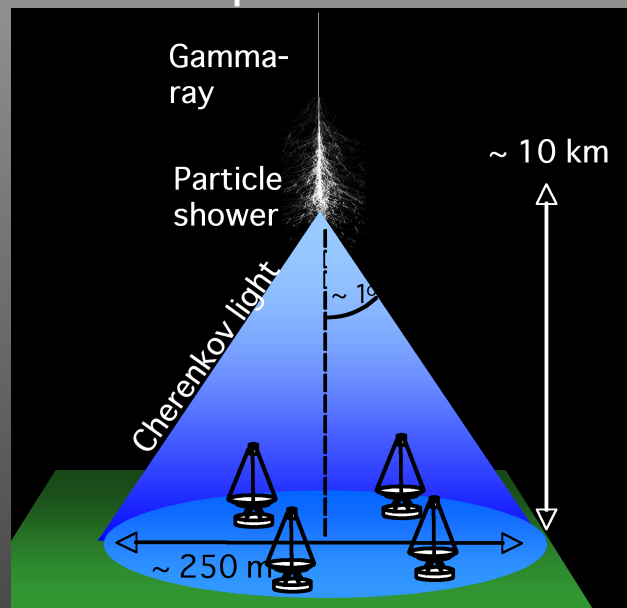


Detection de rayons gamma cosmiques de Hautes Energies (TeV)

$$\gamma \rightarrow e^+ e^-$$

$$e^+ \rightarrow \gamma e^+ \dots$$

$$e^- \rightarrow \gamma e^- \dots$$



provenant des supernova ou du coeur des etoiles près des trous noirs
au centre de la voie lactée à 15 millions d'année-lumière



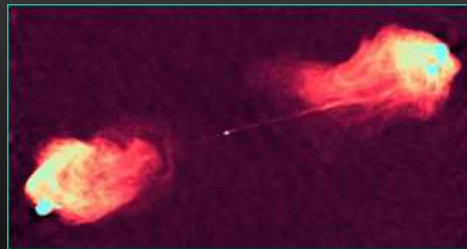
Supernova Cassiopeia

explosion en 1680



Crabe Nebula

explosion en 1054, decouv. en 1989

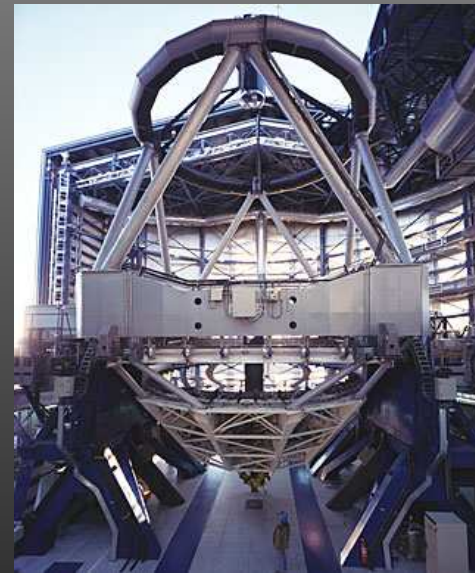


Cygnus A

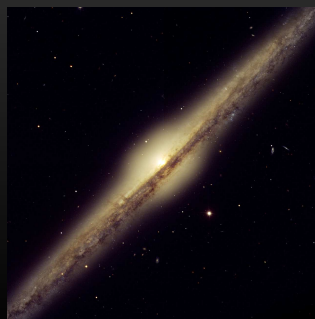
decouv. en 1939

- Telescope ESO European Southern Observatory

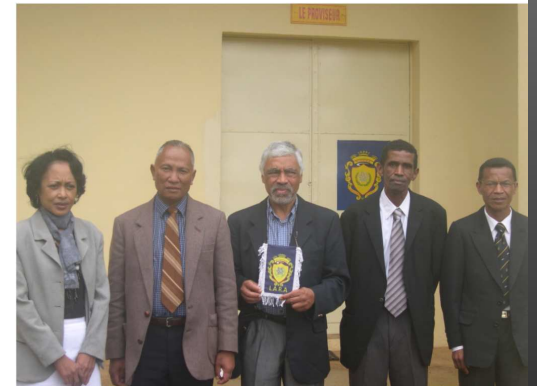
Le site de Paranal: désert de Chili (de Edmond Giraud)



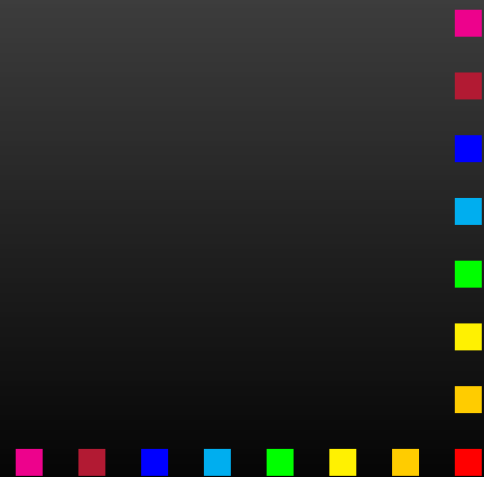
Etude d'amas de galaxies et d'étoiles à 50 millions d'années lumière



- Les élèves et les enseignants

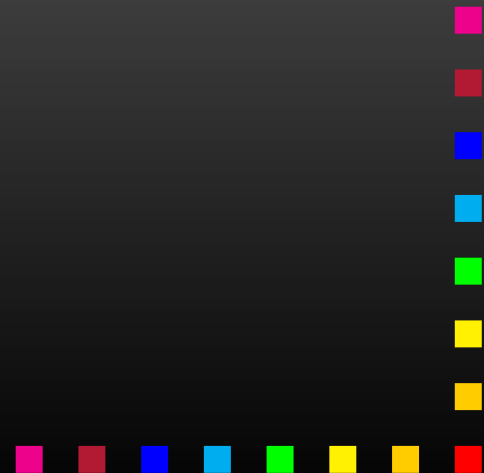


Collaborateurs & Contrats



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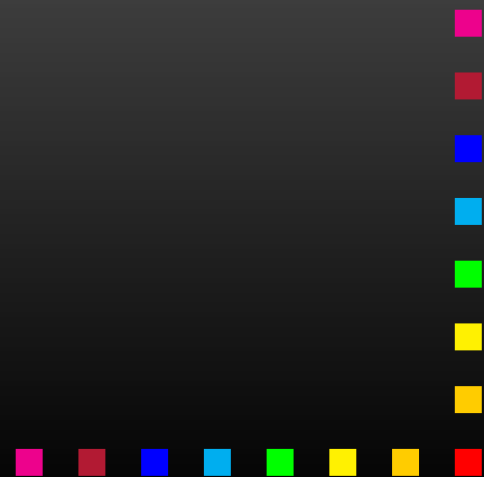
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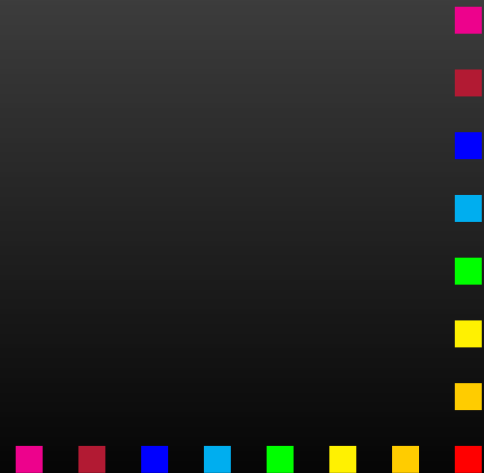
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Q. Zhao (Beijing): Lab. Franco-Chinois

17 Publications en 2009-2011



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Duality between QCD Perturbative Series and Power Corrections.
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- Condensats de gluons, α_s et $m_{c,b}$
Gluon Condensates and $m_b(m_b)$ from Exponential sum rules at Higher Orders.
S. N., e-Print: arXiv:1105.5070 [hep-ph] (2011).
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- Mesons scalaires legers et gluonium
Substructure of the sigma(600) and $f_0(980)$ from gamma-gamma scattering
G. Mennessier, S. N., X.-G. Wang (Beijing), Phys.Lett. B696 (2011) 40-50.
The sigma and $f_0(980)$ from $Ke_4 + \pi - \pi$ scatterings data
G. Mennessier, S. N., X.-G. Wang (Beijing), Phys.Lett.B688:59-66,2010.
Gluonium nature of the $\sigma/f_0(600)$ from its coupling to $K\bar{K}$.
R. Kaminski (Cracow) , G. Mennessier, S. N., Phys.Lett.B680:148-153,2009.

- Baryons lourds

Mass-splittings of triple heavy baryons in QCD

S. N., R. Albuquerque (Montpellier & Sao Paulo) (a paraitre)

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S. N., R. Albuquerque (Montpellier & Sao Paulo), Phys.Lett. B694 (2010) 217-225

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- Hadrons Exotiques: hybrid, tetraquarks, molecules

1^{-+} light exotic mesons in QCD.

S. N. Phys.Lett. B675 (2009) 319-325

1^{--} and 0^{++} heavy tetraquarks and molecules from QCD.

R. Albuquerque, F. Fanomezana, S. N., A. Rabemananjara, C. Zanetti (a paraitre)

Relation between $T_{cc,bb}$ and $X_{c,b}$ from QCD. J.M. Dias, S. N., F.S. Navarra, M.

Nielsen, J.-M. Richard, Phys.Lett. B703 (2011) 274-280

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- Charmonium: desintegration & facteurs de forme

The branching ratio $\psi(3770) \rightarrow J/\psi + \pi^0$ in QCD

Z.-K. Guo, S.N., J.-M. Richard, Q. Zhao (à paraître)

- Quantification sur le cone de lumière, renormalization
Pierre Grangé, E. Werner,...



SVZ Non-Perturbative Sum Rules

alternative to Lattice calculations

♣ One of the Outstanding Discoveries of the 20th century

Shifman Vainshtein Zakharov : Sakurai's price 1999



♡ Bridge between High AND Low energy QCD regions

$$\begin{aligned}\Pi_H(Q^2 \equiv -q^2) &\equiv i \int d^4x \langle 0 | \mathcal{T} J_H(x) J_H^\dagger(0) | 0 \rangle \\ &= \int_{t < \infty} \frac{dt}{t + Q^2 + i\epsilon} \text{Im}\Pi(t) + \text{subtraction terms}\end{aligned}$$

$$QCD\ OPE = EXP\ DATA$$

$J_H(x)$: Hadronic current
 $\bar{\psi}\Gamma\psi, \psi\psi\psi, \alpha_s G^2, g\bar{\psi}G\psi, \bar{\psi}\Gamma_1\psi\bar{\psi}\Gamma_2\psi, \dots$

Different Forms of the Sum Rules

♣ Improvement of the dispersion relation

- Exponential (Borel/Laplace) svz

Moments $\mathcal{L}_i(\tau) = \int_{t_<}^{\infty} dt \exp^{-t\tau} \text{Im}_i \Pi(t)$

Ratio $\mathcal{R}_i(\tau) \equiv -\frac{d}{d\tau} \log \mathcal{L}_i(\tau) \simeq M_{R_i}^2 \equiv \text{Resonance Mass}^2$

Double Ratio $\sqrt{\frac{\mathcal{R}_1}{\mathcal{R}_2}} \simeq \frac{M_{R_1}}{M_{R_2}} \equiv \text{Resonance Mass} - \text{splitting}$

exponential enhances the low energy contribution.

Different Forms of the Sum Rules

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- Moments & FESR

$$\mathcal{M}_n = \int_{t_<}^{t_c} dt t^n \text{Im} \Pi(t)$$

Moments : $n \leq 0$ heavy quarks SVZ

FESR : $n \geq 0$ light quarks Lugunov-Soloviev-Tavkhelidze 67,
Bramon-Etim-Greco 72, Shankar 77, Floratos-SN-de Rafael 79, ...

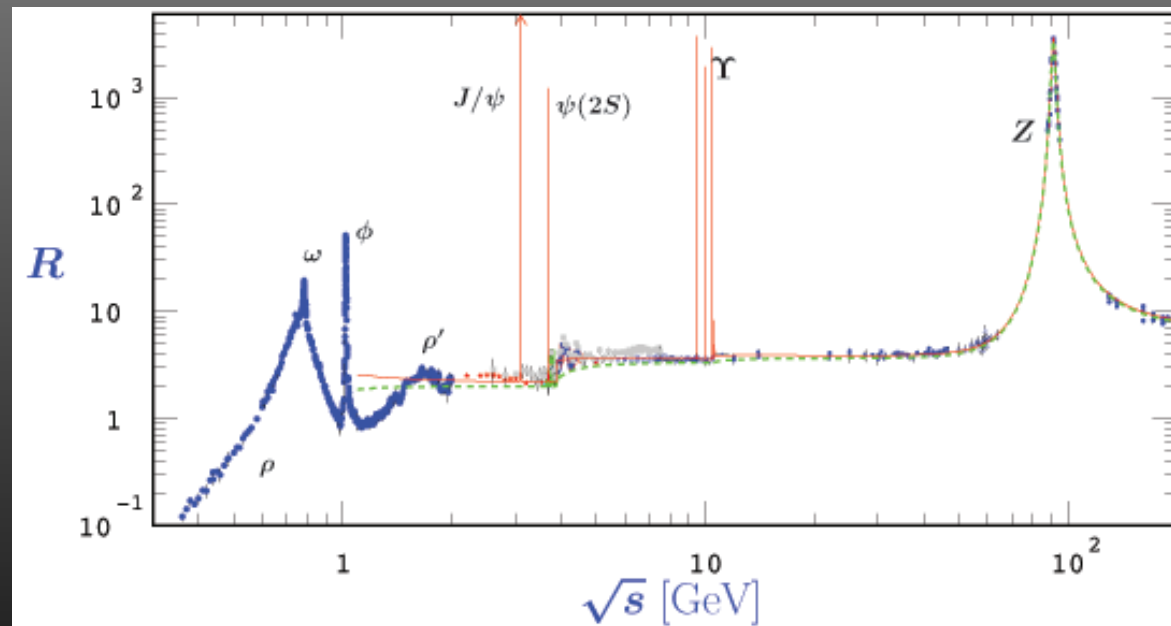
not accurate for extracting power corrections : $\neq$ of large numbers

The Adler function in e^+e^-

♣ $D(Q^2)$ measurable in $e^+e^- \rightarrow \gamma, Z \rightarrow \text{Hadrons}$ process

$$D(Q^2) \equiv -Q^2 \frac{d}{dQ^2} \Pi(Q^2) = \frac{1}{12\pi^2} \int_{t_<}^{\infty} ds \frac{R(s)}{(s+Q^2)^2}$$

DM2, LEP, CLEO, BABAR, BELLE, BES



B. Richter, S. Ting

Prix Nobel 1976 : decouverte du J/ψ



The SVZ-OPE for the Adler function

♣ $D(Q^2)$ known in QCD using the SVZ-OPE

$$D(Q^2) \equiv -Q^2 \frac{d}{dQ^2} \Pi(Q^2) = \sum_{p=0,1,2,\dots} \frac{C_{2p} \langle 0 | O_{2p} | 0 \rangle}{Q^{2p}}$$

The SVZ-OPE for the Adler function

- ♣ $D(Q^2)$ known in QCD using the SVZ-OPE

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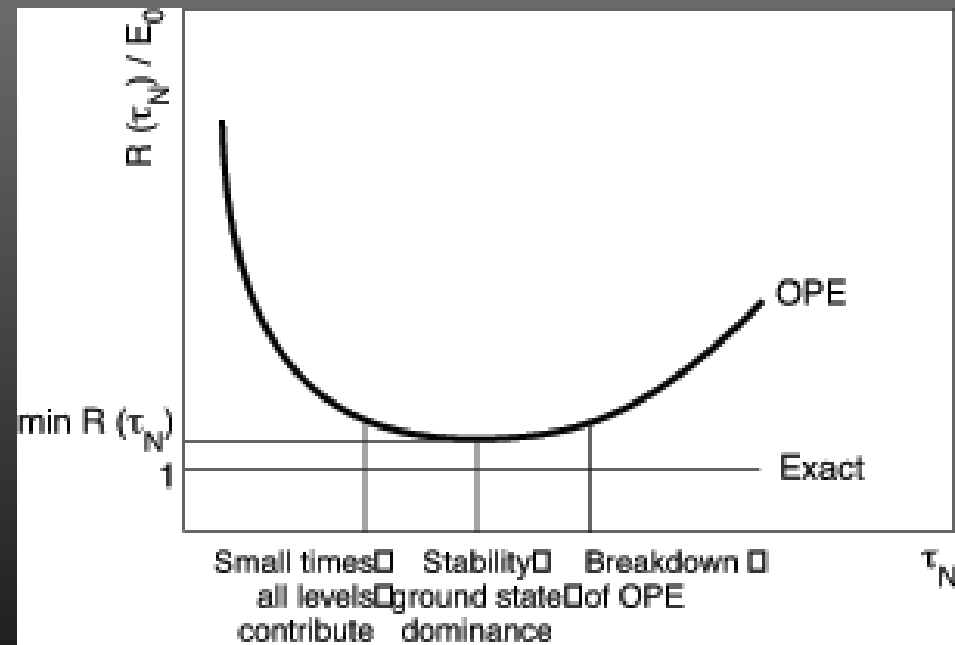
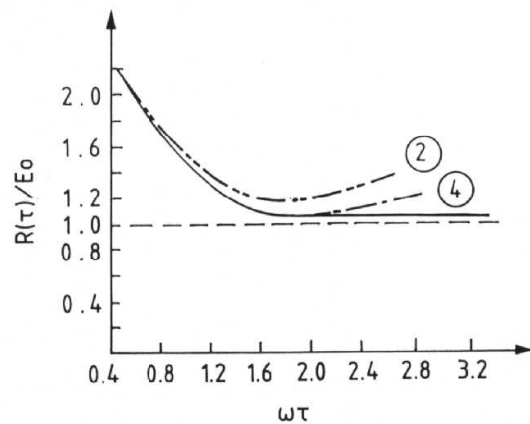
- ◇ Anatomy of the OPE in terms of QCD parameters

- $p = 0$: usual PT series ($a_s \equiv \alpha_s/\pi$):
 $C_0 \equiv \sum_n c_n \alpha_s^n = 1 + a_s + 1.640 a_s^2 + 6.371 a_s^3 + 49.076 a_s^4 +$
 $\Delta_N \equiv \sum_{n>N} c_n \alpha_s^n$??
- $p = 1$: $\bar{m}_q^2$: small corrections
- $p = 2$: $\langle \alpha_s G^2 \rangle$, $m_q \langle \bar{\psi}_q \psi_q \rangle$: gluon and quark condensates
- $p = 3$: $\alpha_s \langle \bar{\psi}_q \psi_q \rangle^2$: four-quark condensates

Theoretical Progresses

♣ 1st Step

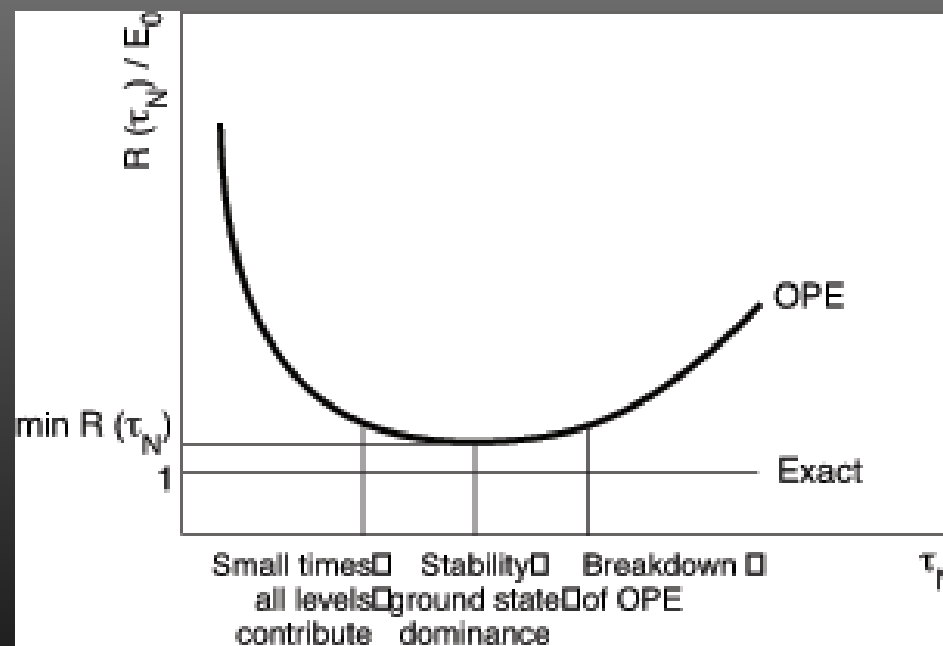
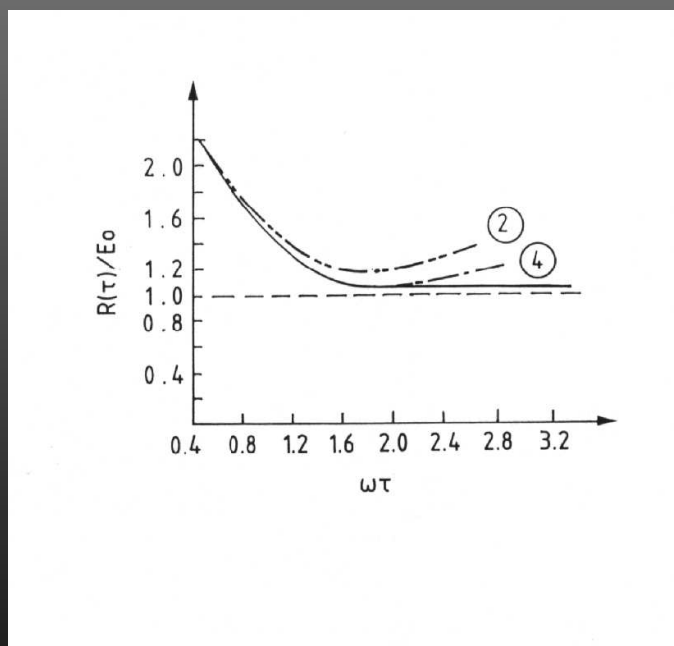
- Quant. Mec. & Non-Rel. Bell-Bertlmann (BB), NSVZ 81



Theoretical Progresses

♣ 1st Step

- Quant. Mec. & Non-Rel. Bell-Bertlmann (BB), NSVZ 81



- Radiative corrections into Exponential SR :
Inverse Laplace **NOT** Borel transform SN- de Rafael 1981



2nd Step

- Mixing of operators under renormalization
Tarrach 82, Espriu-Tarrach 82, SN-Tarrach 83,...
- Absorption of Mass singularities into the quark condensate
Becchi-SN-de Rafael-Yndurain (BNRY) 81, Broadhurst-Generalis (BG) 84,
Bagan-Latorre-Pascual 86, BNP 92, Jamin-Munz 95,
Chetyrkin-Steinhauser 01
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Nikolaev-Radyushkin (NR) 83, BG 84, Bagan-Pascual-Tarrach 85,...
- Higher order PT corrections Chetyrkin et al...





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3rd step

- ChPT constraints on the pion spectral function
Bijnens-Prades-de Rafael 95
- Question on duality violation for spectral function
Shifman 00, Cata-Golterman-Peris 09, G-Alonso-Prades-Pich, de Rafael,



Large order terms: $\Delta_N \equiv \sum_{n>N} c_n \alpha_s^n$

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- $c_n \sim \left(\frac{c_{n-1}}{c_{n-2}} \right) c_{n-1} : \neq$ pert. calc. to $O(\alpha_s^4)$ Chetyrkin et al. ;
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♠ Dual to $1/Q^2$ from a tachyonic gluon mass at short distance ?

- $\sum_{n>N} c_n \alpha_s^n \simeq C a_s \lambda^2 / Q^2 \quad \lambda^2 \leq 0 : \quad N \approx 10$ Lattice
Zakharov-Gubarev-Polikarpov, Chetyrkin-SN-Zakharov 95, SN-Zakharov 09
- Short PT series + power corrections $\equiv$ long PT series.

Traditional Hadron Phenomenology

♣ Impressive wide areas of applications: **kalashnikov** !

- ρ meson, gluon condensate, charm mass since 1979: SVZ
- Meson spectroscopy since Reinders-Rubinstein-Yazaki 81
- Light quark masses since Becchi-SN-de Rafael-Yndurain 81, SN-Paver-de Rafael-Treleani 83,...
- Corrections to π and K PCAC SN 81, Dominguez-de Rafael 87, SN book 89, ...
- Heavy quark masses since SVZ 79, SN 87, Chetyrkin et al, Ioffe-Zyabiyuk, SN 10,...
- Light Baryons since 1981: Ioffe, Dosch et al.
- Heavy Baryons Bagan-Chabab-Dosch-SN 92-93, Albuquerque et al., Chinese groups,...
- Gluonium since Novikov SVZ 80, SN 83, SN-Veneziano 89
- Light Hybrids Latorre-Pascual-SN 87, Chetyrkin-SN 00, SN 09
- Heavy Hybrids Govaerts-Reinders-Rubinstein-Weyers 85, SN-book 04
- Four-quarks, molecules Latorre-Pascual 85, SN 86; Sao Paulo, Chinese,...; Matheus-SN-Nielsen-Richard 07
- Hadronic decays Vertex Navarra et al... Light Cone De Fazio
- τ -decay BNP 92, Pich-Lediberder, Prades-Pich, G.-Alonso, Valenzuela
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♡ SN books : WSC 89, Cambridge 04



PT QCD parameters



Param	Values	Sources
QCD coupling		
$\alpha_s(M_Z)$	0.1192(10)	τ -decay SN 09 [0.1191(27) Z-width] 0.1189(10) average (Bethke, PDG)
Running Q. Masses [MeV] $O(\alpha_s^3)$		
$\overline{m}_u(2 \text{ GeV})$	(2.8 ± 0.2)	average SN09
$\overline{m}_d(2 \text{ GeV})$	(5.1 ± 0.2)	"
$\overline{m}_s(2 \text{ GeV})$	(96.1 ± 4.8)	"
$\overline{m}_c(m_c)$	(1261 ± 16)	J/ψ Q^2 -mom SN10, SN11
$\overline{m}_b(m_b)$	(4177 ± 11)	Υ Q^2 & Exp-mom SN10, SN11



SVZ power corrections SNB 04 Chap. 27



d	NPQCD param.	Values [GeV] ^d	Sources
3	$\frac{1}{2}\langle\bar{u}u + \bar{d}d\rangle(2)$	$-(0.254 \pm .015)^3$	(pseudo)scal,
	GMOR: $\delta_\pi \times 10^{-2}$	5 ± 0.5 (6.2 ± 1.6)	LSR (less sens α_s) FESR
	$\langle\bar{d}d\rangle/\langle\bar{u}u\rangle$	$1 - 9 \times 10^{-3}$	non-norm. ord.(pseudo)scal,
	$\langle\bar{s}s\rangle/\langle\bar{d}d\rangle$	0.74 ± 0.03	non-norm. ord.(pseudo)scal ⊕ light & heavy baryons e^+e^- , $\Upsilon - \eta_b$, J/ψ LSR
4	$\langle\alpha_s G^2\rangle$	$(7 \pm 1)10^{-2}$	
	Lattice	Adriano 85, Rakow 09	τ : unconvulsive
5	$g\langle\bar{\psi}\sigma_{\mu\nu}\frac{\lambda^a}{2}\psi G_a^{\mu\nu}\rangle$	$M_0^2 = (0.80 \pm 0.02)$	Light baryons, B , B^*
	$\equiv M_0^2\alpha_s^{1/3}\beta_1\langle\bar{\psi}\psi\rangle$		
6	$g^3 f_{abc}\langle G^a G^b G^c\rangle$	$(8.2 \pm 1.0)\langle\alpha_s G^2\rangle$	J/ψ -LSR SN10
	$\rho\alpha_s\langle\bar{\psi}\psi\rangle^2$	$(4.5 \pm 0.3)10^{-4}$	$\rho = 2.1 \pm 0.2$



Correlated Estimate of $1/Q^2$

♣ $1/Q^2$ —term : tachyonic gluon mass SN95a, 95b, 09

Channels	$-(\alpha_s/\pi)\lambda^2$ in $\text{GeV}^2 \times 10^2$
e^+e^- data	
$\mathcal{R}(\tau)$	6.5 ± 0.5
π—sum rule	
$\mathcal{L}_\pi$	12 ± 6
Average	7 ± 3
τ-decay : large $\beta - \sum_1^4$ PT series	
Fixed Order PT	2.6 ± 0.8
Contour Improved	5.9 ± 0.8

Effect of $1/Q^2$ on α_s from τ -decays

◇ α_s from τ -decay **SN09**

$$R_\tau \equiv \frac{\Gamma(\tau \rightarrow \nu_\tau + \text{hadrons} |_{\Delta S=0})}{\Gamma(\tau \rightarrow l + \bar{\nu}_l + \nu_\tau)}$$

$$= 3|V_{ud}|^2 S_{EW} (1 + \delta^{(0)} + \delta'_{EW} + \delta_m^{(2)} + \delta_{svz} + \delta_{NST})$$

Corrections	Size $\times 10^3$
$\delta_{svz} = \sum_4^8 \delta^{(D)}$	$-(7.8 \pm 1.0)$
$\delta_{ST} \equiv \delta_{svz} + \delta_m^{(2)} + \delta_\pi + \delta_{a_0}$	$-(10.9 \pm 1.1)$
δ_{inst}	$-(0.7 \pm 2.7)/20$
δ_{DV}	$-(15 \pm 9)$ Cata-Golterman-Peris
$\delta_{tach} \equiv \text{large } \beta - \sum_1^4 PT$	(17 ± 5) FO
	(39 ± 5) CI
$\delta_{NST} \equiv \delta_{inst} + \delta_{DV} + \delta_{tach}$	(2.0 ± 9.4) FO
	(24.0 ± 10.6) CI

$$R_{\tau,V+A}|_{exp} = 3.479 \pm 0.011 \quad \Rightarrow$$

$$\alpha_s(M_\tau) = 0.3276(34)_{ex}(10)_{st}(85)_{nst} \quad \text{FO}$$

$$= 0.3221(48)_{ex}(14)_{st}(121)_{nst} \quad \text{CI}$$



PT	$\alpha_s(M_\tau)$	$\alpha_s(M_Z)$	Ref.
FO	0.3276 (34) _{ex} (86) _{th}	0.1195 (4) _{ex} (10) _{th} (2) _{ev}	SN 09
CI	0.3221 (48) _{ex} (122) _{th}	0.1188 (6) _{ex} (15) _{th} (2) _{ev}	
$\langle \rangle$	0.3249 (29) _{ex} (75) _{th}	0.1192 (4) _{ex} (9) _{th} (2) _{ev}	
Z		0.1191 (27) _{ex} (2) _{th}	BCK, DAVIER et al.
$\langle \rangle$		0.1189 (10)	BETHKE, PDG

Conclusions & Future Developments

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- ◇ **$1/Q^2$ term:** a possible way to parametrize Large order PT series
- ♡ **$1/Q^2$ term:** seems to improve many existing phenomenology