

# N-body simulations and dark matter detection

**N-body :**

See e.g : Keres et al [arXiv:1109.4638](#)  
[arxiv:1004.0005](#), Agertz, Teyssier, Moore  
Governato et al [arxiv:0911.2237](#), [arxiv:1106.0499](#)  
review : [arxiv:0801.1023](#), Dolag et al

**links between N-body simulations and dark matter detection:**

Gamma signal and background ([arxiv:11xx.xxxx in progress](#))  
Direct detection ([arxiv:0909.2028](#))  
Cosmic rays ([arxiv:0808.0332](#))  
Gamma and neutrino indirect detection ([arxiv:0801.4673](#))

**Collaboration with** J. Lavalle, F.-S. Ling, R. Teyssier, L. Athanassoula

See also e.g :

Aquarius : gamma ([arXiv:0809.0894](#)), Direct detection ([arXiv:0812.0362](#))  
Via Lactea gamma ([arXiv:0805.4416](#))

...

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**GDR Terascale, CPPM Marseille. 12 october 2011**

# Outline

- **N-body simulations : some basics**
- **Features of dark matter halos and disk galaxies**
- **Consequences for dark matter detection**

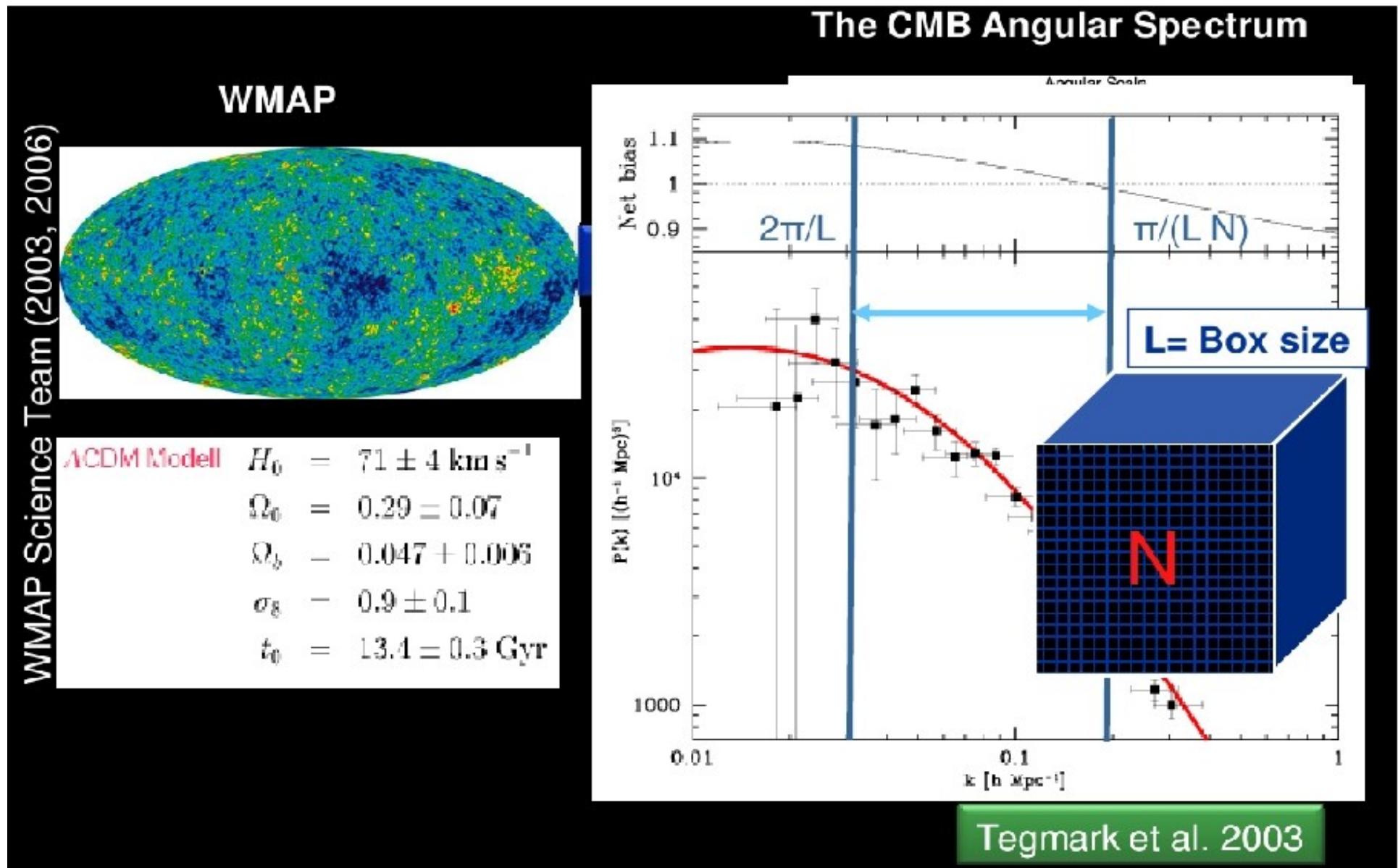
# Introduction

## Hierarchical structure formation scenario

- Cosmological parameters :  $\Omega_\Lambda, \Omega_M, \Omega_b, \sigma_8, H_0, h.$
- Size of the box
- Computer capacity  $\Rightarrow$  Nb of particles  
 $\Rightarrow$  Mass of dark matter particles  $\sim 10^{3-5} M_\odot$

# Introduction

Initial conditions given by CMB power spectrum : WMAP



# Physics

## DARK MATTER (and STARS)

- Gravity : Vlasov and Poisson equations

$$\nabla^2 \Phi = 4\pi G [\rho + (n - 2)\rho_X]$$

## GAS

- Hydrodynamics : Euler equations
- + Gravity

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0,$$

$$\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} = -\nabla \Phi - \frac{\nabla p}{\rho},$$

$$\frac{\partial \varepsilon}{\partial t} + \mathbf{u} \cdot \nabla \varepsilon = -\frac{p}{\rho} \nabla \cdot \mathbf{u},$$

# Physics

## DARK MATTER (and STARS)

- Gravity : Vlasov and Poisson equations

Solved by N-body techniques :  
i.e “particles”

## GAS

- Hydrodynamics : Euler equations
- + Gravity

## 2 approaches :

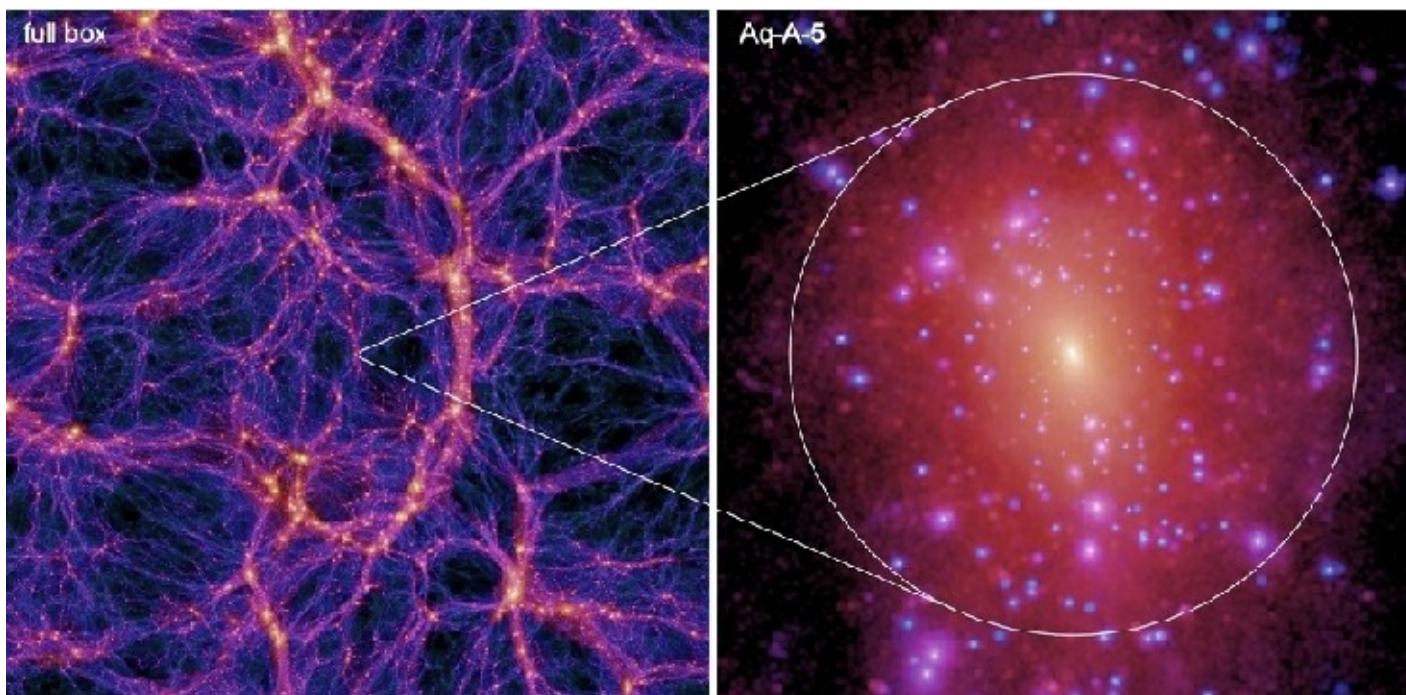
- Lagrangian : fluid=particles (SPH)  
GADGET code (V.Springel)
- Eulerian : fluid=grid (AMR)  
RAMSES code (R.Teyssier)
- “Hybrid”  
AREPO (V.Springel)

# Some results

- NFW, VIA LACTEA I&II, AQUARIUS, GHALO, HORIZON, CLUES, BOLCHOI ...

## DARK MATTER only simulations :

- Describe well large scale structure formation : filaments
- Give non smooth dark matter distribution : presence of virialized (sub)structures  
(agreement with Press-Schechter, Sheth-Tormen)  
= CLUMPS



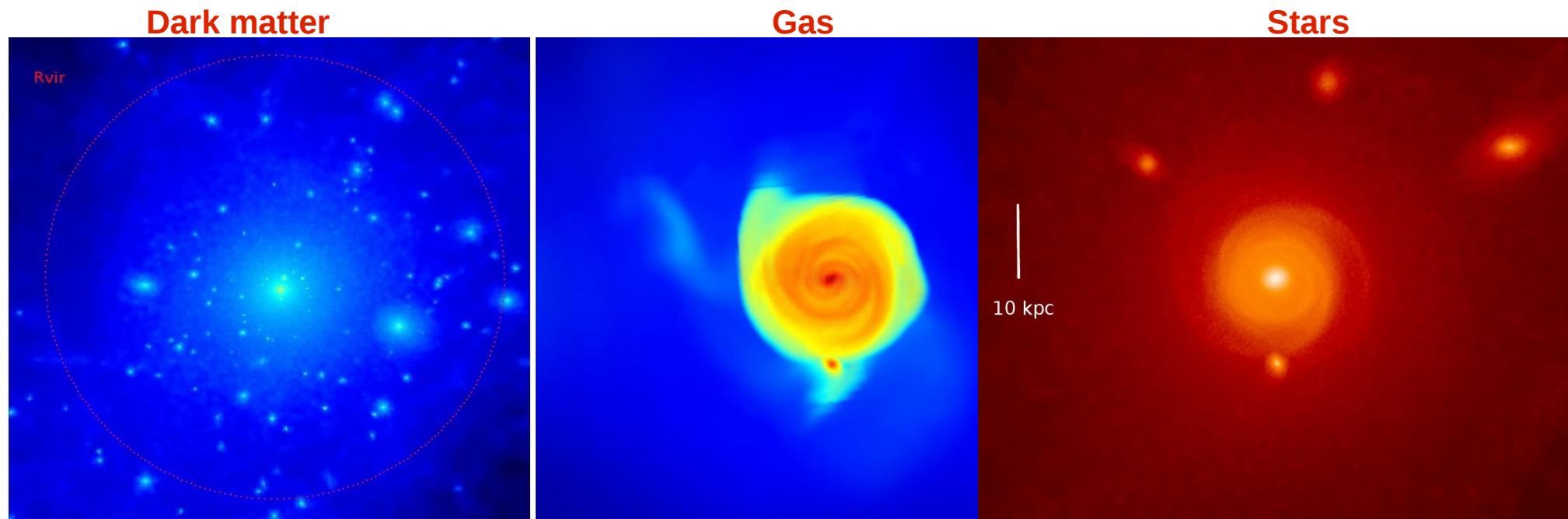
AQUARIUS, Springel et al 2008

# Some results

- NFW, VIA LACTEA I&II, AQUARIUS, GHALO, HORIZON, CLUES ...

## Simulations including gas :

- Filaments
- CLUMPS
- Gas accreted in DM potential  
→ Disk and stars formation



HORIZON project simulation by R.Teyssier

Pictures with Glnemo viewer (Jean-Charles.Lambert@oamp.fr)

# Star formation : recipe

- Infall of cold gas → stars
- Model the gas conversion into stars by a Schmidt law

$$\dot{\rho}_g = -\epsilon_{\text{ff}} \frac{\rho_g}{t_{\text{ff}}} \text{ for } \rho > \rho_0$$

- $t_{\text{ff}}$  free-fall time
- $\rho_0$  threshold density
- $\epsilon_{\text{ff}}$  drive star formation rate

→ Transform gas into star particles

# Supernovae feedback

- Type II SN, relevant for stellar masses  $\sim 8-40 M_{\odot}$
- Represents  $\sim 10\%$  of the mass of a stellar population
- Short lived stars
- $\sim 10\text{-}20$  Myr after the star (particle) creation : explosion
- $\sim 10\%$  of the star (particle) mass is re-injected into the gas
- Energy per explosion  $E_{\text{SNII}} = 10^{51} \text{ erg}$   
→ reheat the gas, can regulate star formation rate

# Clumpy dark matter halos

- Dark matter distribution not smooth : clump spectrum

$$\frac{dN_{cl}}{dM} \propto \left( \frac{M}{M_H} \right)^n$$

typically       $n \sim -1.8 - 2$

Problem :

Number of satellites > observations ... new dwarf galaxies to be discovered ? ... in progress  
satellites without gas and stars (photoionisation, SN feedback)?

# (Cuspy ?) Dark matter Halos

Fit of N-body results :

- **Cusps**

$$\rho_{DM}(r) = \frac{\rho_s}{(r/r_s)^\gamma [1 + (r/r_s)^\alpha]^{(\beta - \gamma)/\alpha}} \quad \rho_{DM}(r) \propto r^{-\gamma} \text{ (small } r)$$

- ★ NFW 1997 :  $\gamma = 1$
- ★ Moore et al 1999 :  $\gamma = 1.5$
- ★ VIA LACTEA (I and II), Diemand et al 2006-2008 :  $\gamma = 1.2$

- **Einasto (AQUARIUS)**

$$\rho_{DM}(r) = \rho_{-2} e^{-\frac{2}{\alpha} [(r/r_{-2})^\alpha - 1]}$$

But : Observations suggest cored profiles, i.e  $\gamma = 0$

# Baryon impacts on dark matter halo

Dark matter profile **steepened or flattened** by baryon processes

- **Adiabatic compression : Blumenthal et al 1986**

Angular momentum and mass conservation :  $M_i(r_i)r_i = [M_b(r_f) + M_{DM}(r_f)]r_f$

- ★  $M_i(r)$  : mass profile of the galactic halo before the cooling of the baryons
- ★  $M_b(r)$  : the baryonic composition of the Milky Way observed now
- ★  $M_{DM}(r)$  : the dark matter component of the halo today (determined iteratively)

$$\text{NFW} : \rho_{DM}(r) \propto r^{-1} \rightarrow r^{-1.5}$$

- **ISM physics : stellar formation, SN feedback ...**

- The response of the DM halo is driven by the **history of assembly** of baryons into a galaxy : *Pedrosa et al* : arxiv:0902.2100
- ISM carefull treatment could lead to shallow profiles on dwarf scale  
*Governato et al* arxiv:0911.2237, *Pontzen & Governato* arxiv:1106.0499

- **Dark disc** : clump accretion by stellar and star disc ... *Read et al* 0902.0009

→ enhancement of DD signal ?  
capture rates in the Sun ? *Bruch et al 2009 vs Ling 2010*

Still debated ...

# CDM Cosmological simulations

**Cosmological N-body simulations with gaz : successful tool  
for disc galaxy formation, works well qualitatively**

- **Nb and dynamics of satellites**
- **Cusp/Core** (*Governato et al arxiv:0911.2237, Pontzen, Governato arxiv:1106.0499*)
- **Angular momentum problem**  
**(bulges too dominant, discs not extended enough)**  
(Agertz, Teyssier, Moore arxiv:1004.0005, Keres et al arxiv:1109.4638)
- **Improvement of ISM physics treatment**

**Realistic and consistent Milky-Way like framework  
for astroparticle calculations ...**

NFW : Navarro Frenk and White ... Frenk supports warm dark matter  
arxiv:1104.2929, arxiv:1105.3474  
<http://www.bbc.co.uk/news/science-environment-14948730>

# Direct detection

Rate :

$$\frac{dR}{dE_R} = \frac{\rho_{DM}}{M_{DM}} \frac{d\sigma}{dE_R} \eta(E_R, t)$$

**Particle and nuclear physics**

$$\frac{d\sigma}{dE_R} = \frac{M_N}{2\mu_n^2} \sigma_n^0 \frac{\left(f_p^2 Z + (A-Z)f_n^2\right)^2}{f_n^2} F^2(E_R)$$

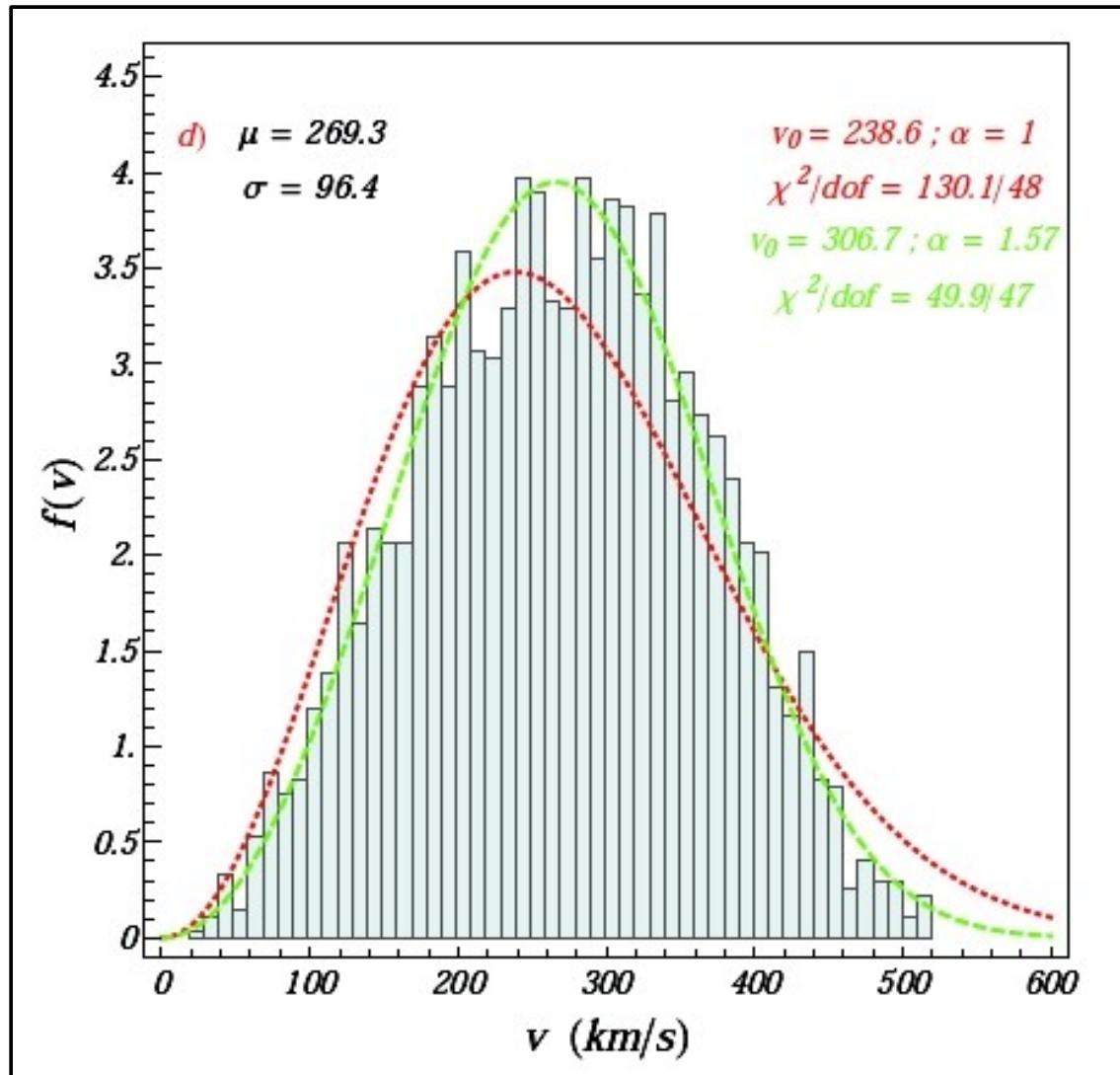
$\rho_{DM}$  : Local dark matter density +

**Astrophysics**

$$\eta = \int d^3\vec{v} \frac{f(\vec{v})}{|\vec{v} - \vec{v}_{\oplus, G}|}$$

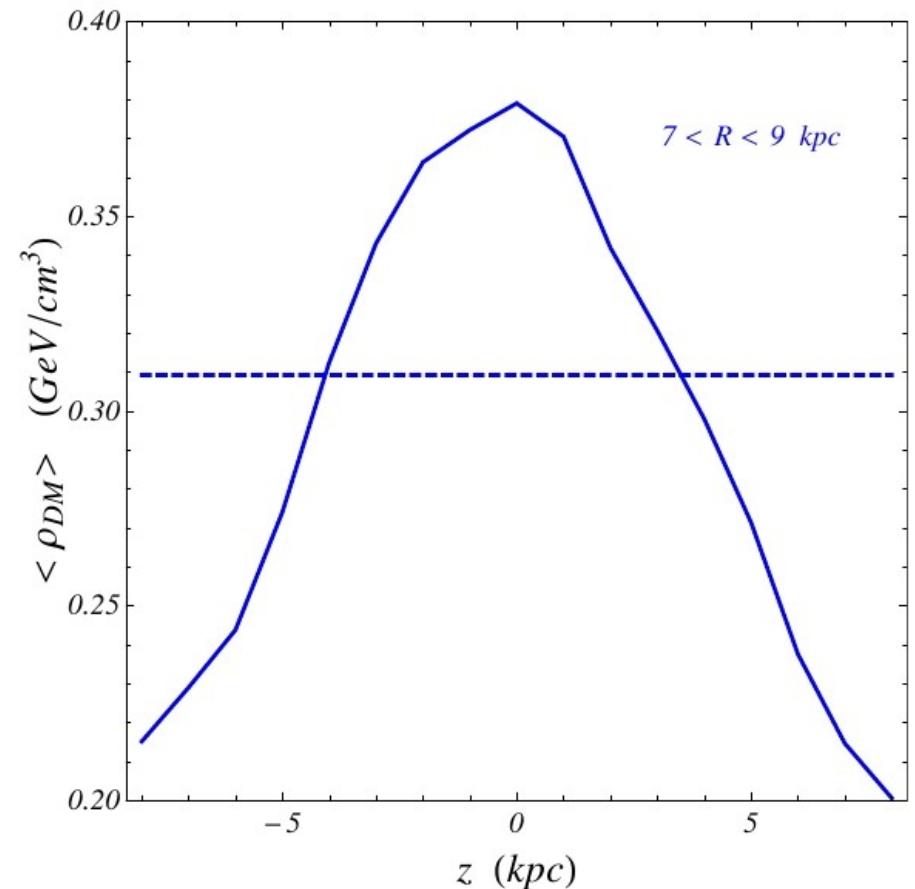
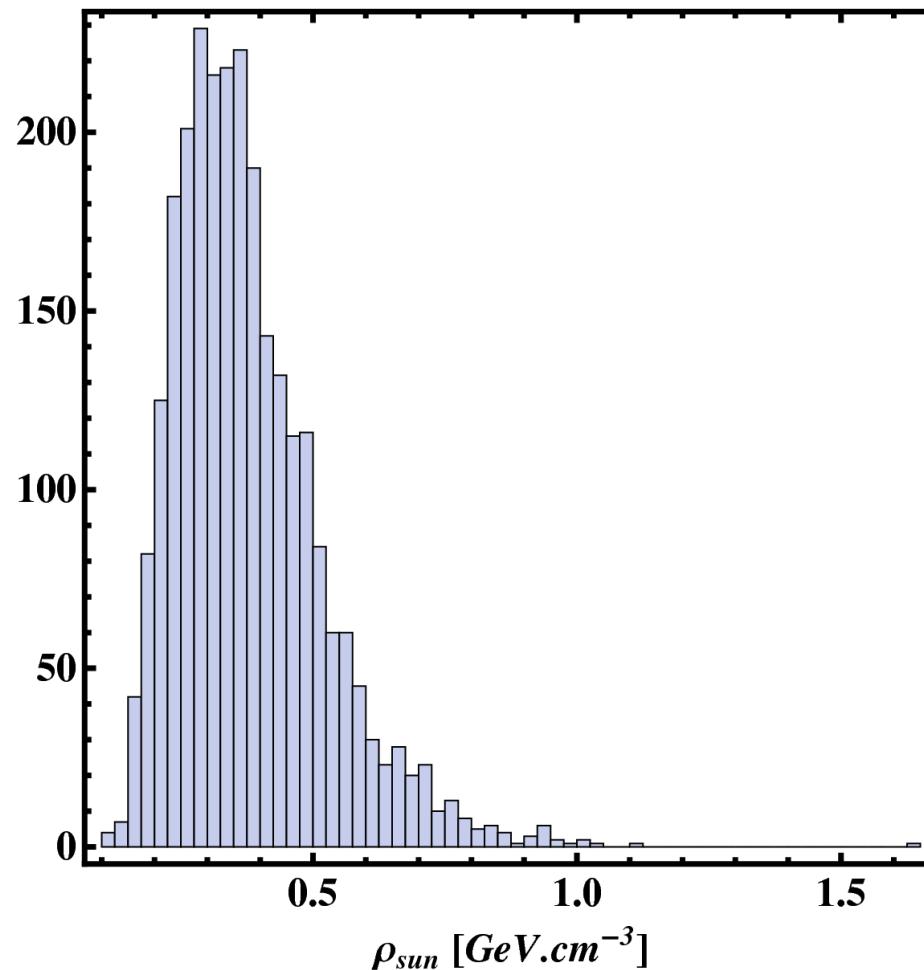
Features  $\neq$  Maxwellian ?  
 Dark disk ?  
 Corotation ?  
 Local density ?

# Dark matter velocity distribution



Signature on direct detection signals

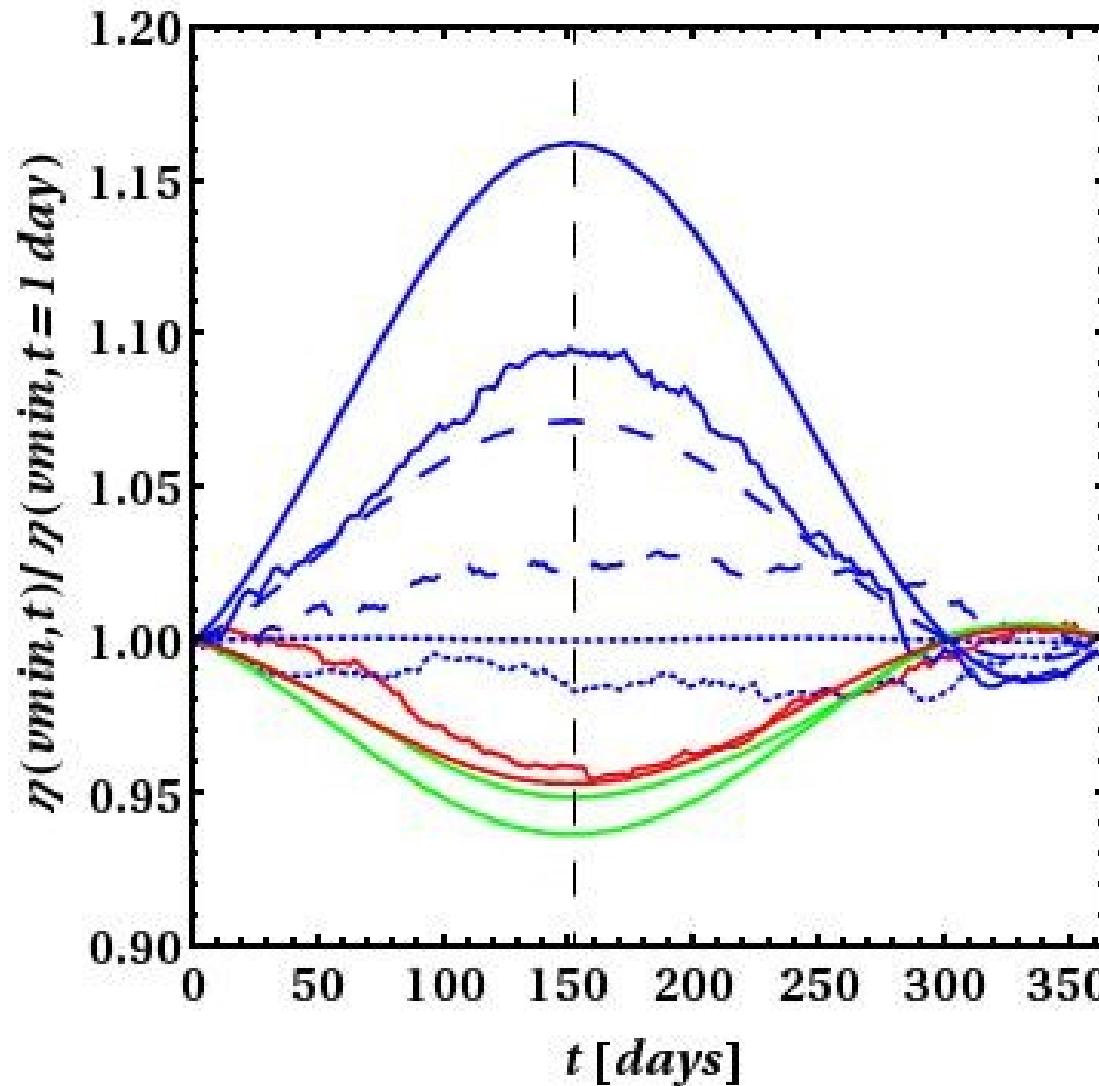
# Local DM density, Dark disk ?



$\text{Mean}(\rho_{\text{sun}}) > 0.3 \text{ GeV.cm}^3$

Enhanced direct detection signal

## Direct detection modulation



Modulation depends on velocity distribution : Maxwellian versus simulation

Directionnal direct detection could distinguish velocity distribution ...  
in progress collab with J. Billard, F. Mayet (Mimac)

# Gamma/neutrino indirect detection

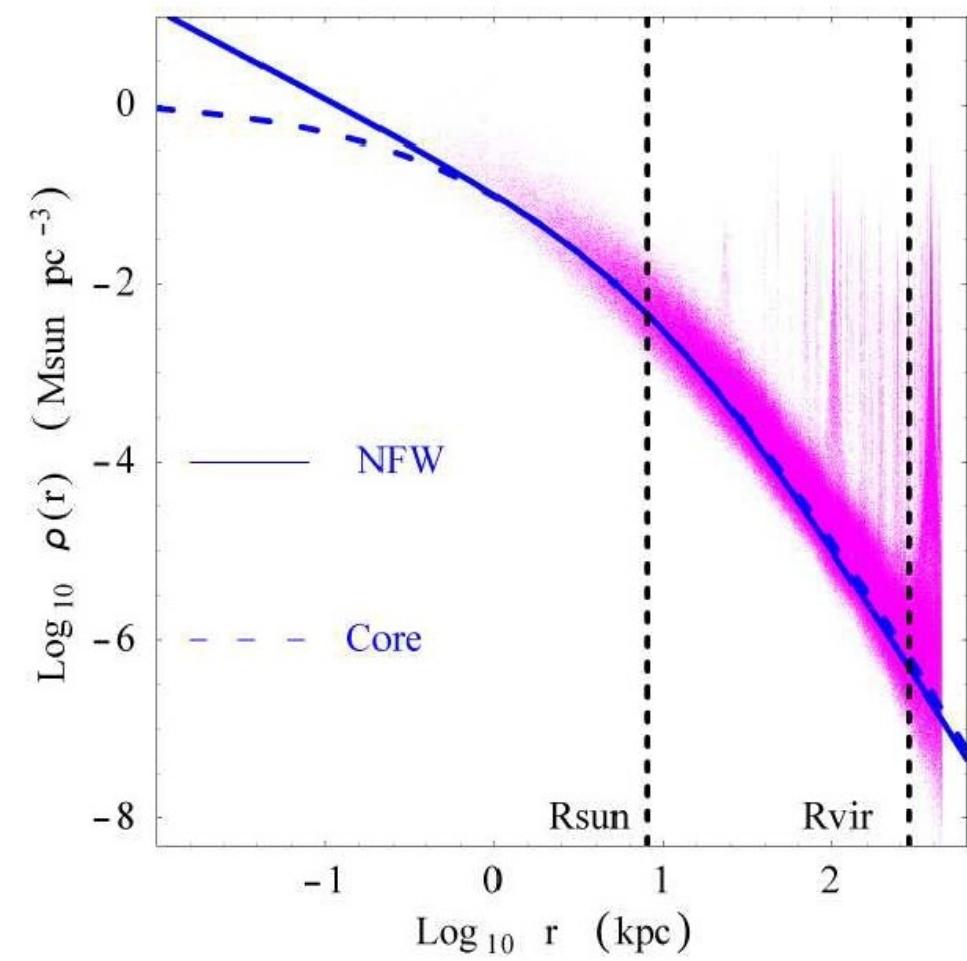
$$\frac{d\Phi_{\gamma,\nu}}{d\Omega} = \underbrace{\frac{1}{4\pi} \frac{1}{\delta} \frac{\langle \sigma v \rangle}{m_{DM}^2} \int_{E_{min}^{\gamma,\nu}}^{E_{max}^{\gamma,\nu}} \sum_i \frac{dN_{\gamma,\nu}^i}{dE_{\gamma,\nu}} BR_i}_{\doteq HEP_{\gamma,\nu}} \underbrace{\int_{l(\vec{\Omega})} \rho_{DM}^2 dl}_{\doteq ASTRO},$$

**Particle physics**                                    **Astrophysics**

Annihilation cross section  
Dark matter mass  
Annihilation induced spectra

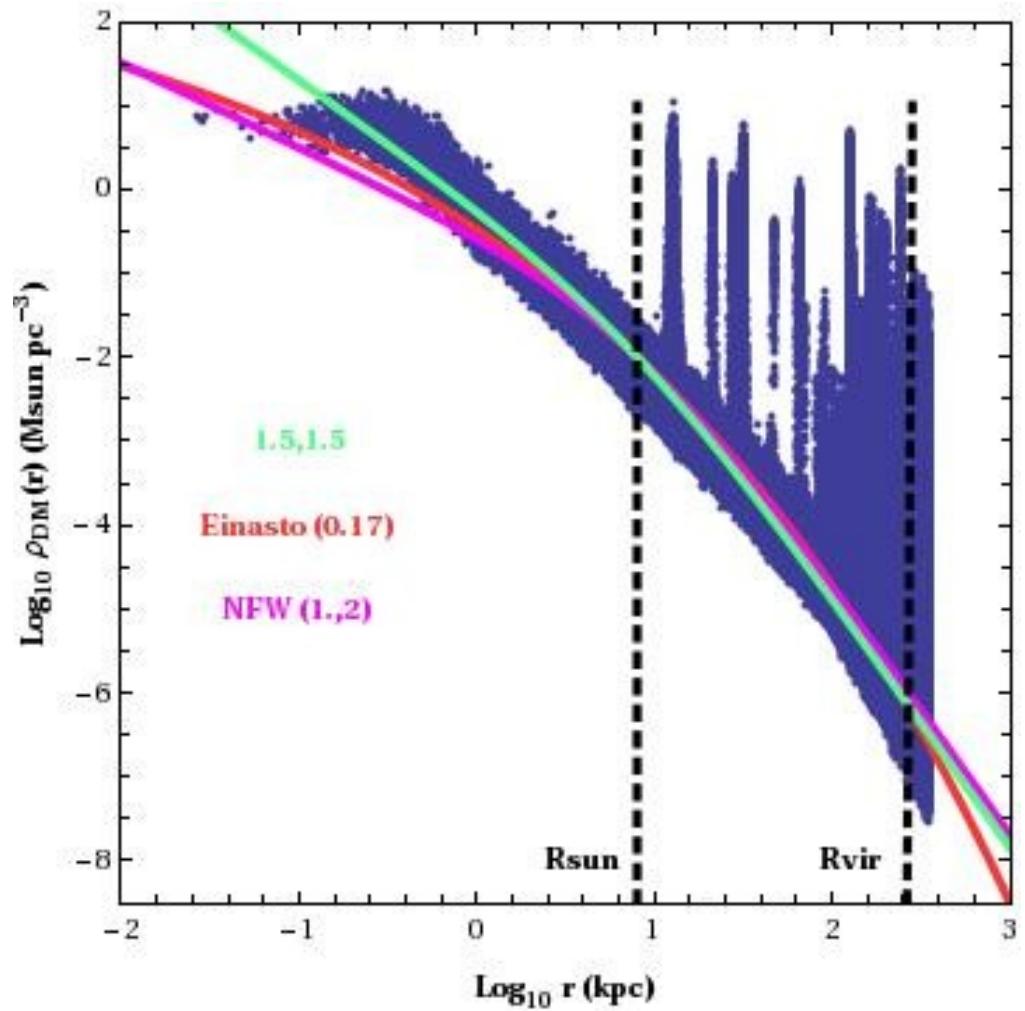
DM distribution:  
  
Features ?  
Cusp ?  
Clump features ?  
Baryons ? (compression ?)  
Feedback ?

## Dark matter density :



Dark matter only

Simulations from the HORIZON project,  
AMR RAMSES code (R. Teyssier)

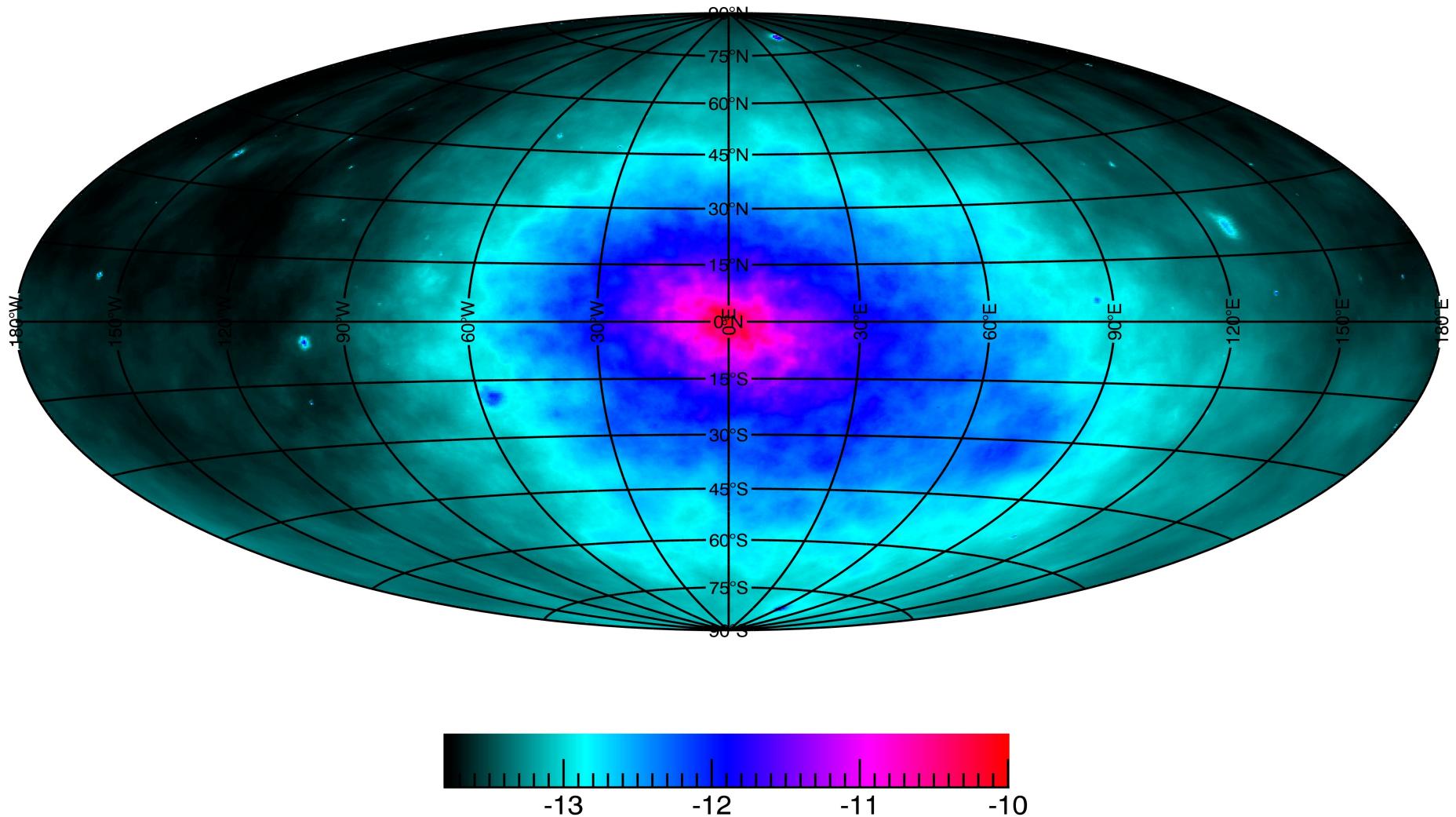


Dark matter+ baryons

Adiabatic compression  
Strong cusp

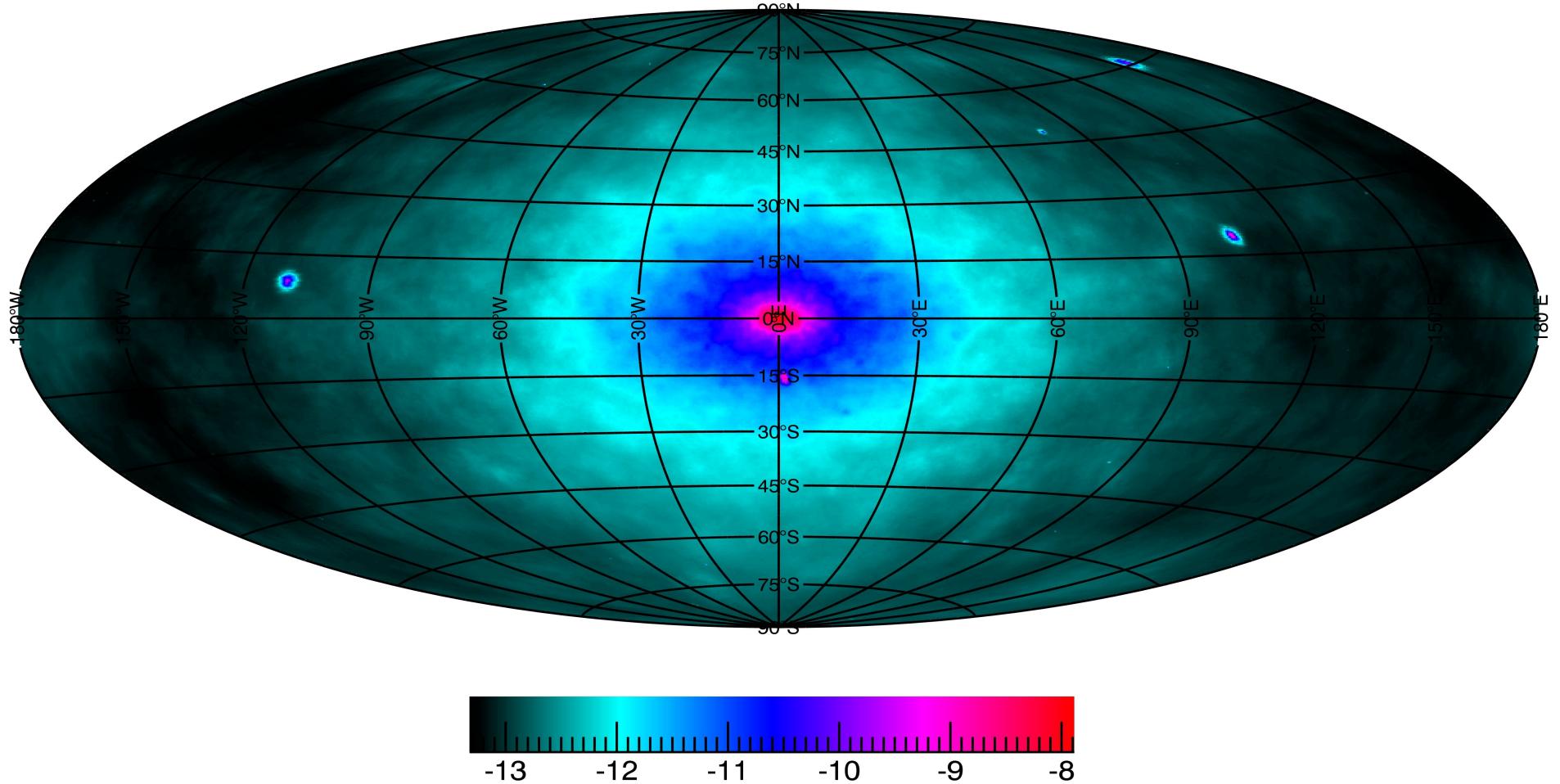
# Gamma skymap : Dark matter contribution

## N-body simulation : dark matter only



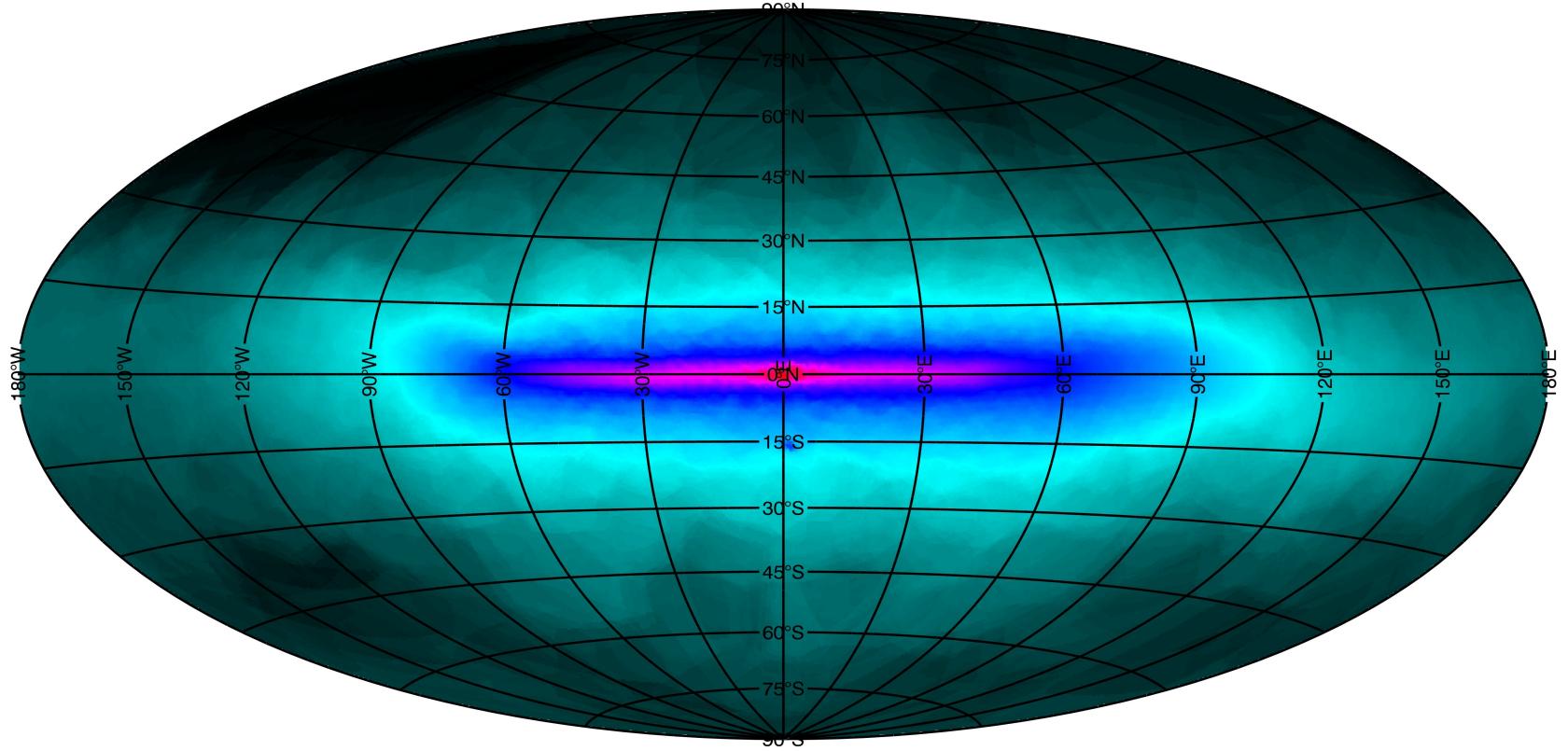
+ standard thermal (HEP+cosmo) scenario  
Gammas : FERMI, HESS ~ -10  
Neutrinos : KM3Net GC ~ -9

# Gamma skymap : Dark matter contribution N-body simulation : dark matter + baryons



- ~ 2 orders of magnitude higher fluxes in central region
- Very high astrophysics contribution → HEP scenarios
- Possible conflict with observations FERMI, HESS ...
- Depend on background ...

# Gamma skymap : $\pi^0$ Background N-body simulation : dark matter + baryons



star distribution → SNII explosion → cosmic rays  
Gas distribution → CR spallation → gamma fluxes

To be compared with Fermi ...

Nezri, Lavalle, Teyssier ... soon on arxiv

# Cosmic rays

collaboration with J. Lavalle

$$\vec{\nabla} \left[ K(E) \vec{\nabla} \mathcal{N}_{\text{cr}} - \vec{V}_{\text{conv}} \mathcal{N}_{\text{cr}} \right] + \frac{\partial}{\partial E} \left[ b(E) \mathcal{N}_{\text{cr}} + K_{EE} \frac{\partial}{\partial E} \mathcal{N}_{\text{cr}} \right] + \Gamma(E) \mathcal{N}_{\text{cr}} + Q = 0$$

$$Q \propto \int_{E_{thr}}^{m_{DM}} dE_i \sum_f b_f \frac{dN_i^j}{dE_i} \left( \frac{\langle \sigma v \rangle}{m_{DM}^2} \right) \times \underbrace{\int \rho_{DM}^2(r) dV}$$

**Positrons :**

$$\lambda_D = \left\{ \frac{4K_0\tau_E}{1-\delta} (\epsilon^{\delta-1} - \epsilon_S^{\delta-1}) \right\}^{1/2}$$

High / Low energies : come from local environment  
and depend on fluctuations

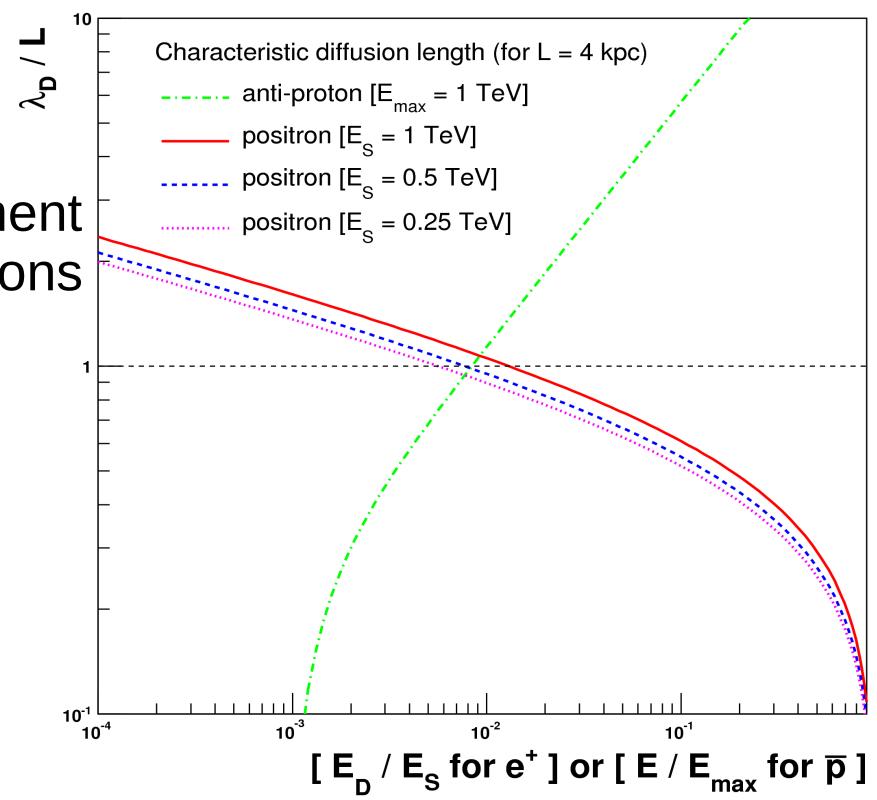
Low / High energies : large volume,  
smooth the fluctuations

**Antiprotons :**

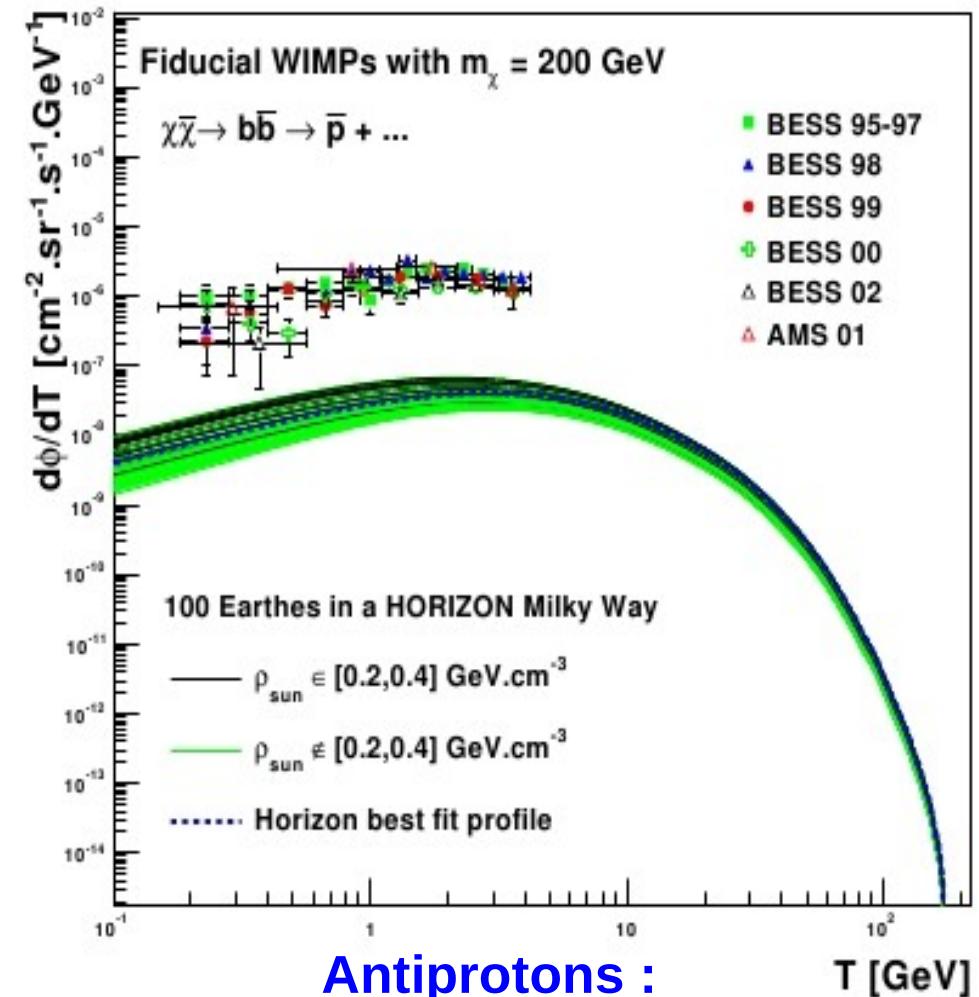
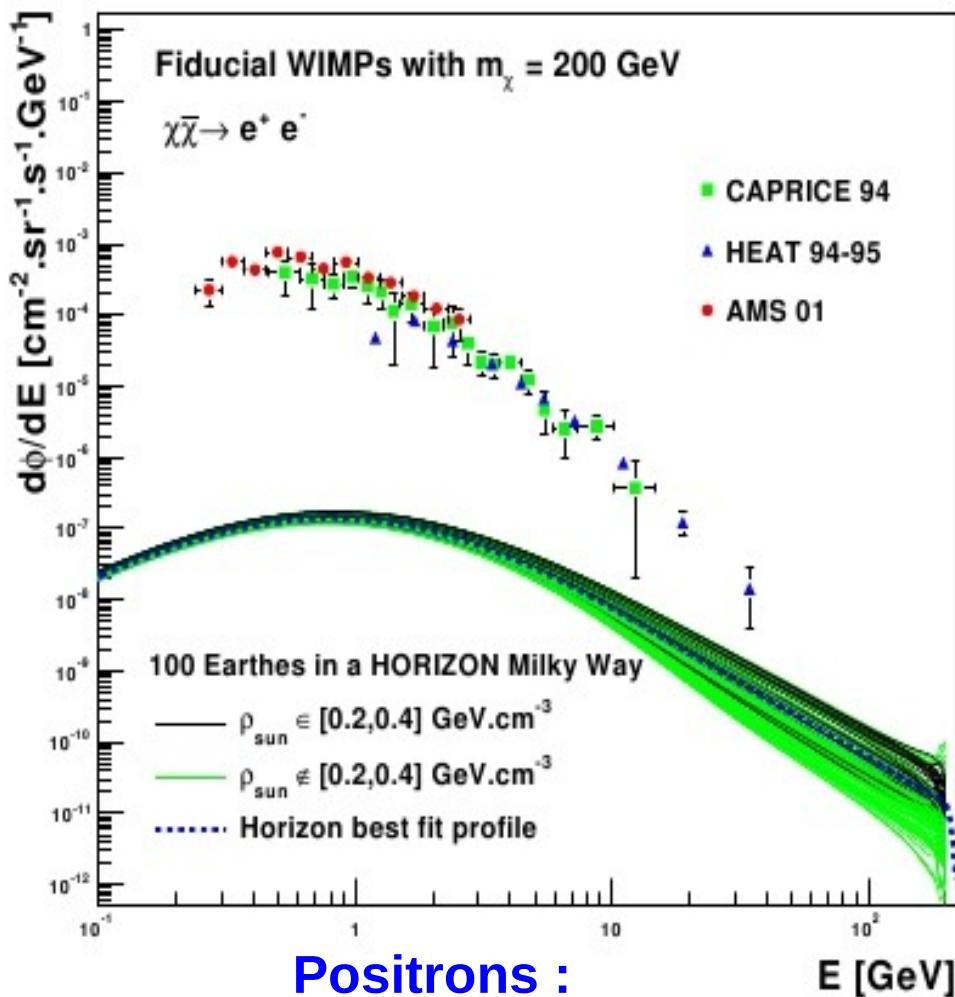
$$\Lambda_D = \frac{K(E)}{V_{\text{conv}}}$$

Particle physics

Astrophysics



## Astrophysical uncertainties :



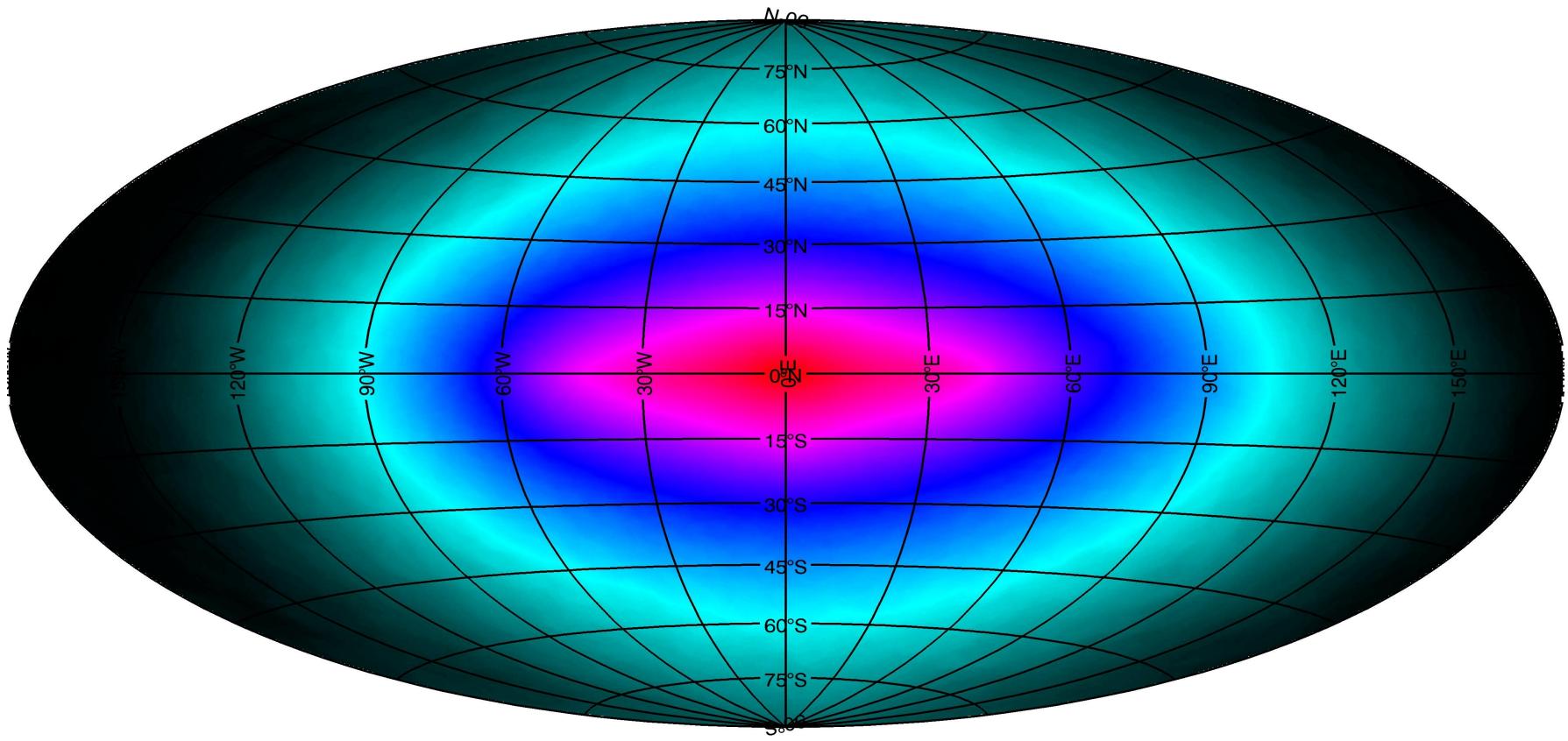
## Cosmic rays in N-body framework :

Quantify the uncertainties related to local dark matter density

Use also the gas distribution to calculate signal and background (in progress)  
Also use magnetic field distribution of simulations (future work)

# Cosmic rays

## N-body simulation : dark matter + baryons



**star distribution → SNII explosion → cosmic rays distribution**

Nezri, Lavalle, Teyssier ... in progress

# Summary-Conclusion

- **Cosmological N-body simulations with gaz : successful tool for galaxy formation**
- **Nb and dynamics of satellites**
- **Cusp/Core** (*Governato et al arxiv:0911.2237*)
- **Angular momentum problem**  
**(bulges too dominant, discs not extended enough)**  
(Agertz, Teyssier, Moore arxiv:1004.0005, Keres et al arxiv:1109.4638)  
→ **too concentrated objects**
- **Improvement of ISM physics treatment**

- **Very consistent framework for dark matter detection and astroparticle calculations**
- **Dark matter signals (DD,  $\gamma$ ,  $v$ , CR)**
- **Backgrounds from gas, stars and ISM physics**

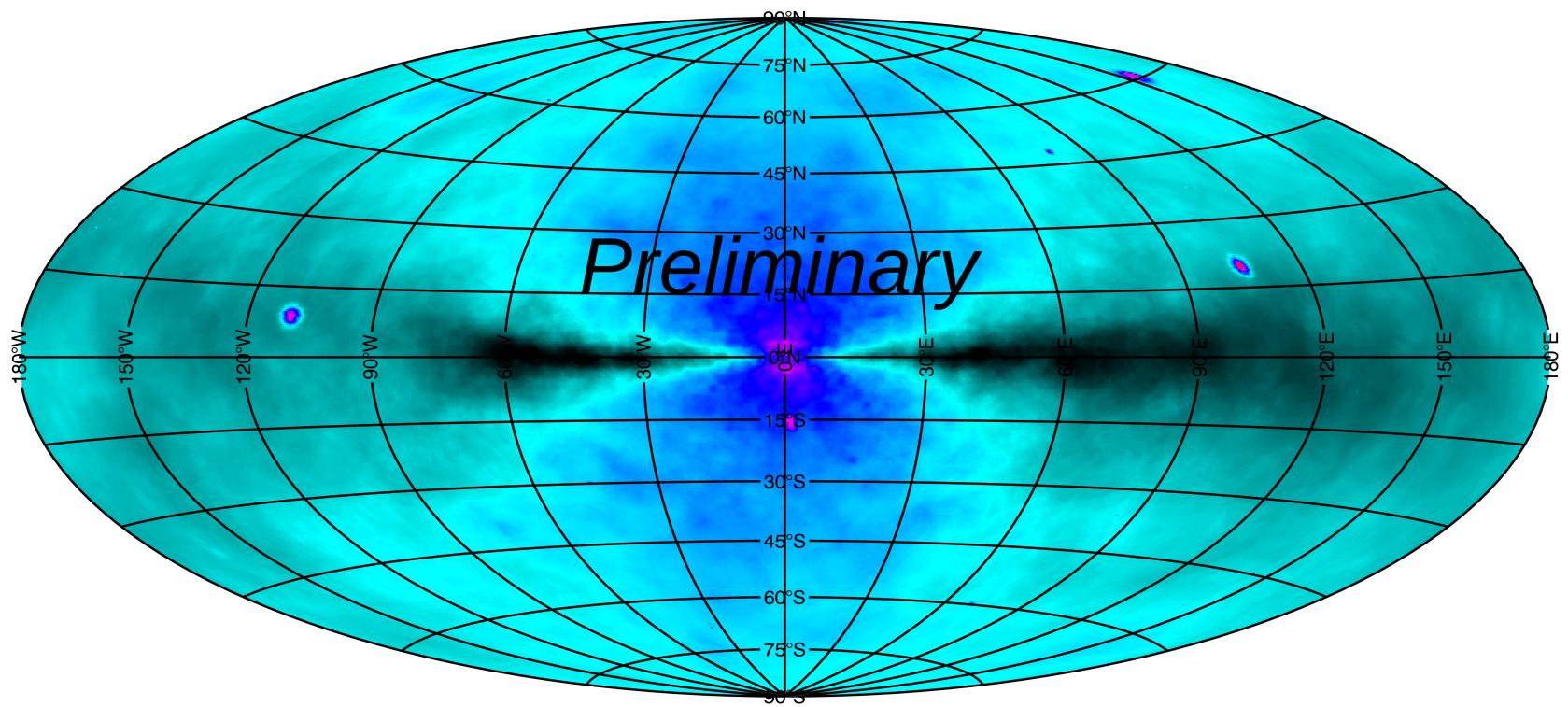
Nezri, Lavalle, Teyssier soon on arxiv... + future works  
starting a Ph D thesis : Pol Mollitor

Interface between N-body codes (Gadget, Ramses, Arepo ...) and astroparticle codes (Micromegas, Darksusy, Galprop, Usine ...)

# Thanks

# Gamma skymap : DM versus $\pi^0$ Background

N-body simulation : dark matter + baryons



Signal / background

Fermi bubbles ...

Nezri, Lavalle, Teyssier ... soon on arxiv