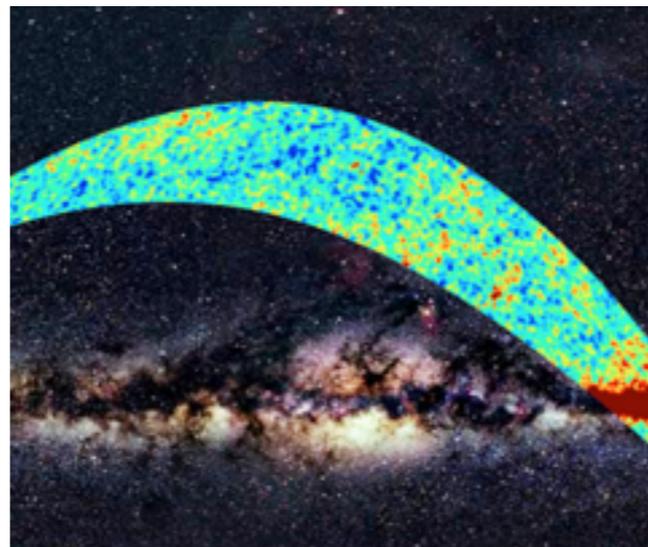
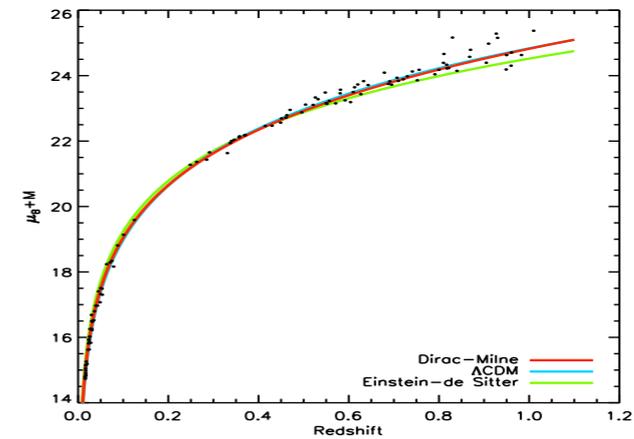
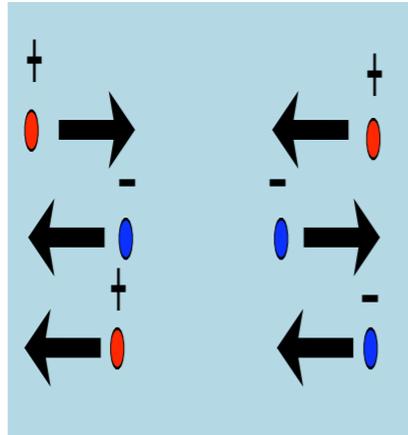


Cosmology of the Dirac-Milne Universe



Aurélien Benoit-Lévy
Institut d'Astrophysique de Paris



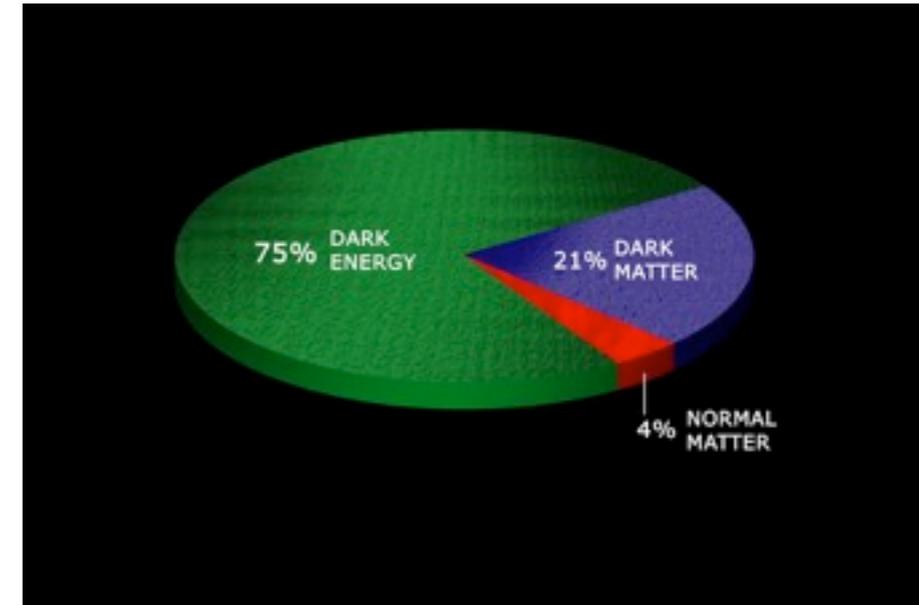
in collaboration with **Gabriel Chardin**

Benoit-Lévy, Chardin, A&A, accepted

Motivation for alternative models



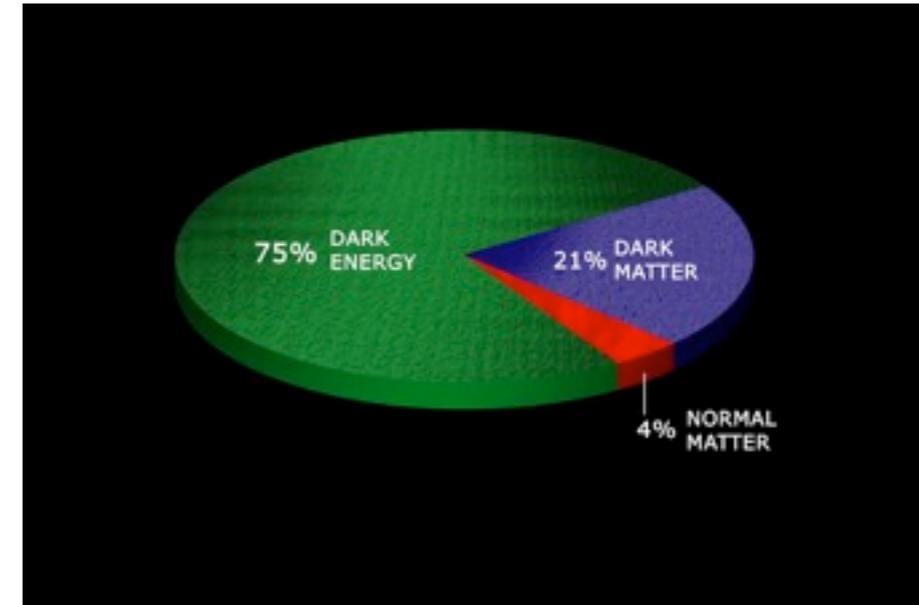
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Motivation for alternative models



- 95% of our Universe escapes our knowledge
- Dark Energy
 - True cosmological constant: why this value?
 - Vacuum energy: 10^{120} times smaller than expected
 - "Coincidence problem"



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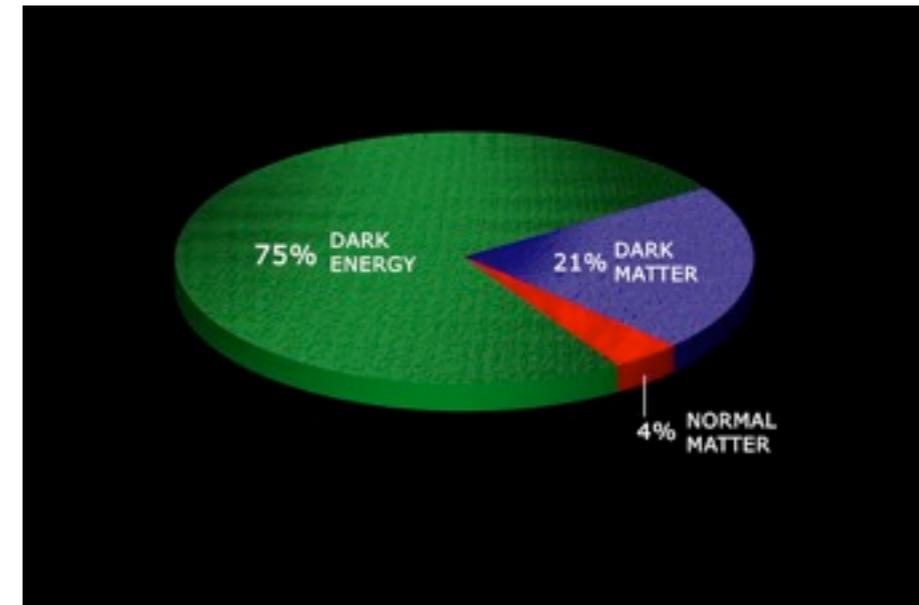
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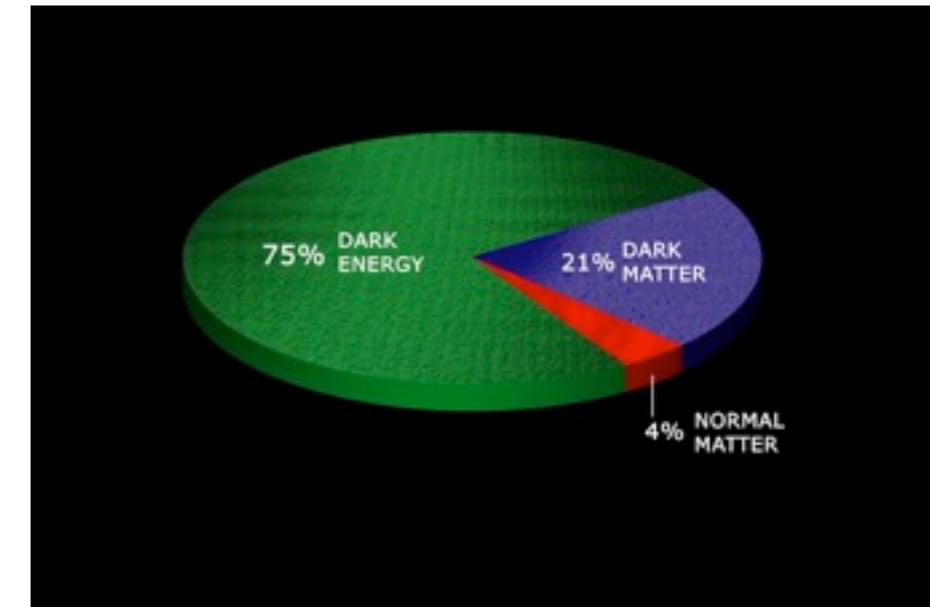
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- **Inflation**

- Introduced to solve horizon and flatness problem

Standard model relies on 3 ingredients which are undetected and /or not understood

Motivation for negative mass



Matter - antimatter symmetric Universe

Antimatter is supposed to have a negative active gravitational mass

Motivation for negative mass



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Antimatter naturally comes as negative mass candidate from Kerr-Newman solution

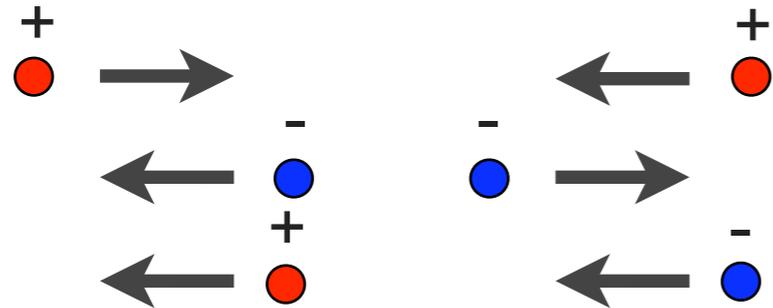
- When $(q, m, ma) = \left(-e, m_e, \frac{\hbar}{2}\right)$ then two \mathbb{R}^4 connected by the annular singularity
- Solution is symmetric under $(r, e, m) \leftrightarrow (-r, -e, -m)$
- In the second space, the solution is seen as having reversed charge and mass (Carter 68)
- This strongly suggests antimatter!
- Also implies that cannot create negative mass as independent degree of freedom



Negative mass in General Relativity



“Runaway” solution (Bondi 57)



If antimatter is Bondi-type negative mass, antihydrogen weighting experiments should see antimatter fall as matter

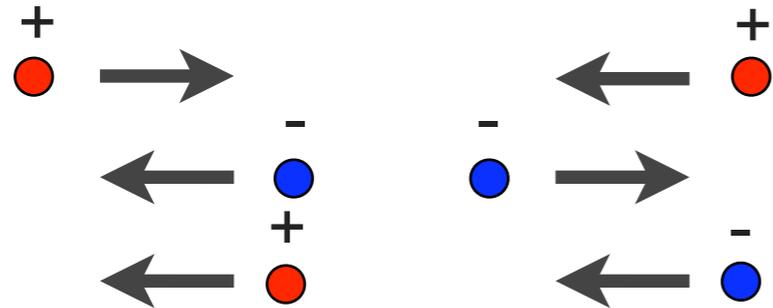
- Corresponds to negative inertial mass
- This would lead to incompatible annihilations

To have a viable cosmology, we need mutual repulsion between matter and antimatter

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To have a viable cosmology, we need mutual repulsion between matter and antimatter

● Electron-hole analogy: antimatter seen as hole. Goes up in a gravitational field.

- “Electron bubble” in superfluid helium; bubble accelerated upwards with $2g$
- Voids in large-scale structures seen as negative density with respect to background density (Dubinski et al. 93, Piran 97). What if background density is null?

Properties of the Dirac-Milne universe



- Flat space-time, open space

$$T_{\mu\nu} = 0 \iff a(t) = t \text{ and } k = -1$$

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	Standard Model	Dirac-Milne	Ratio
T= 170 MeV	3×10^{-5} sec	7 days	1.7×10^{10}
T = 1 MeV	1 sec	3.3 yr	1×10^8
T = 80 keV	~200 sec	41 yr	6.5×10^6
T = 3000 K	380 000 yr	12×10^6 yr	32
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No inflation needed to solve the horizon problem

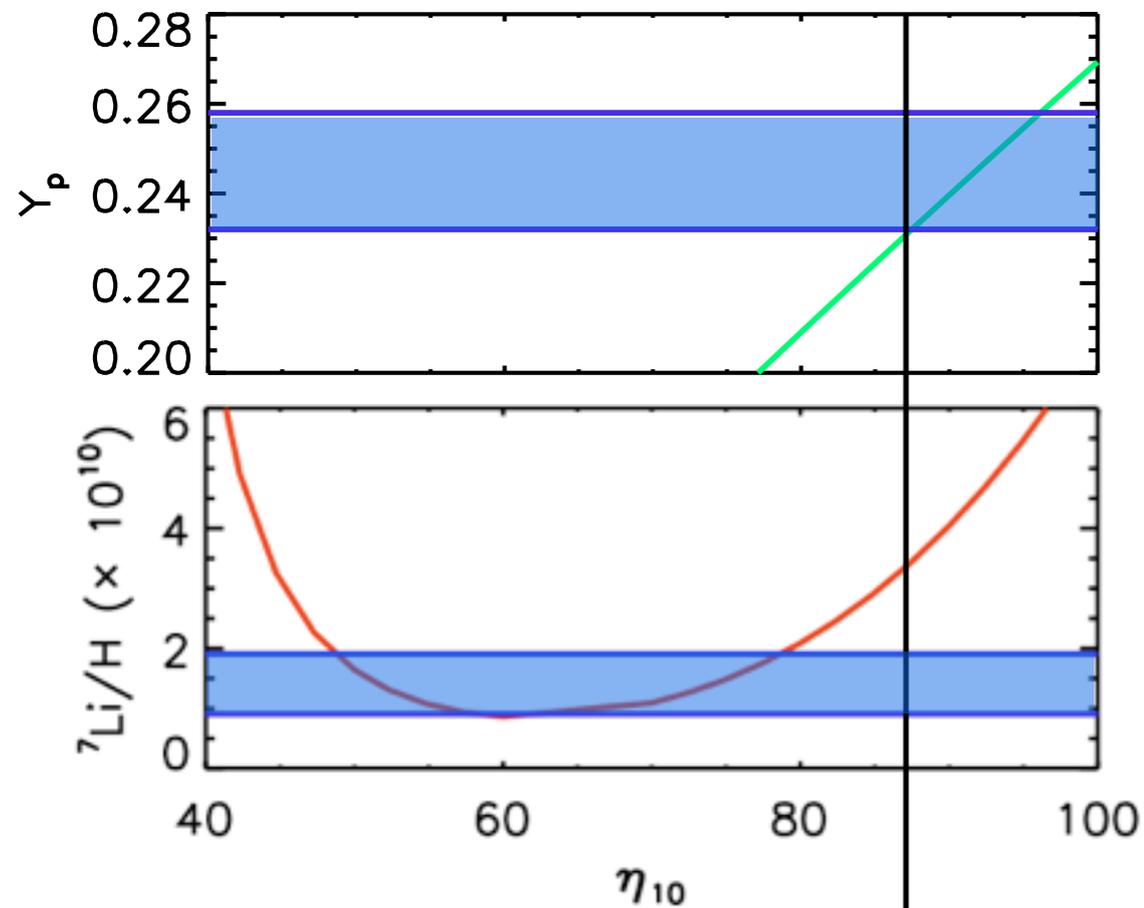
No Dark Energy needed to solve the age problem

Primordial Nucleosynthesis



- Thermal episode : production of ^4He and ^7Li (Lohiya *et al.* 98 & Kaplinghat *et al.* 00, ABL & Chardin 11)

- Late decoupling of weak reactions, lead to ^4He and ^7Li



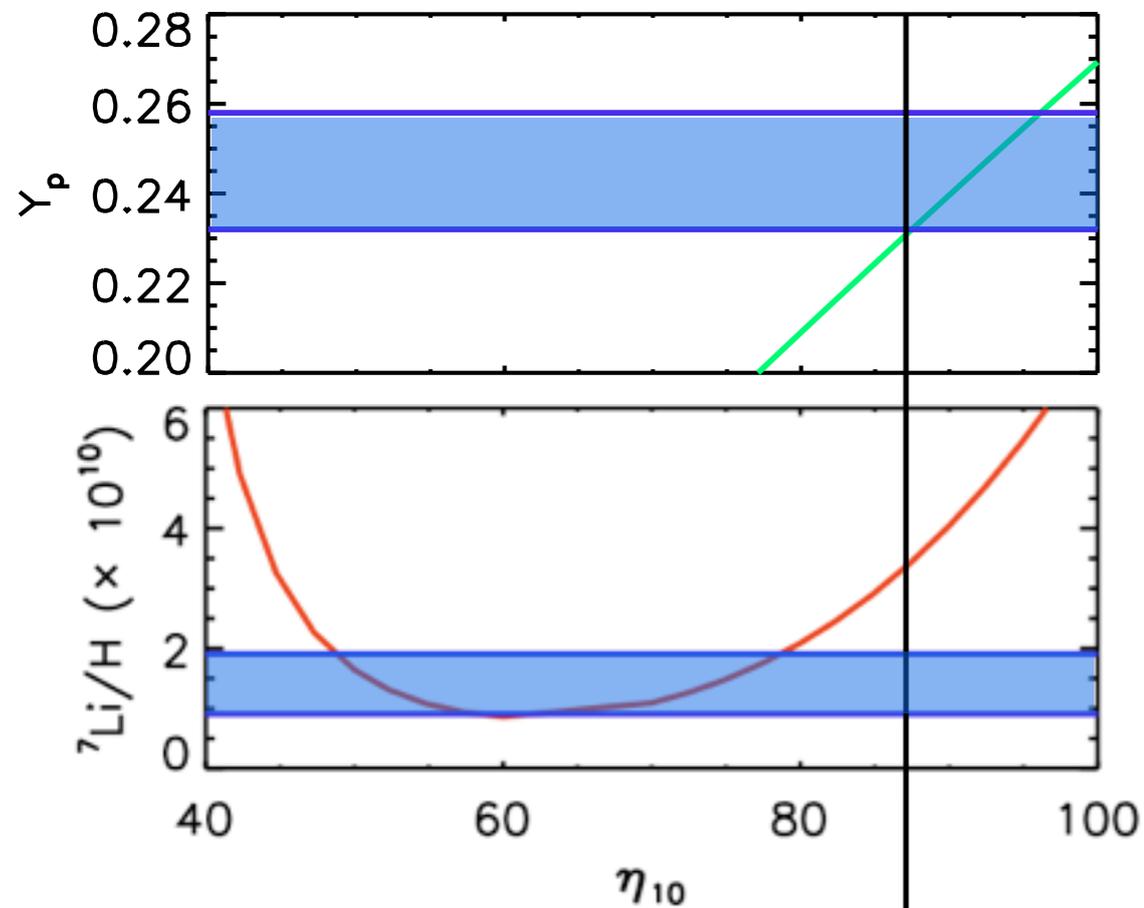
$$\frac{^7\text{Li}}{\text{H}} = 3.45 \times 10^{-10}$$

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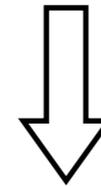
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$$\frac{{}^7\text{Li}}{\text{H}} = 3.45 \times 10^{-10}$$

$$8.8 \times 10^{-9} < \eta < 9.6 \times 10^{-9}$$



No non-baryonic matter is a priori needed

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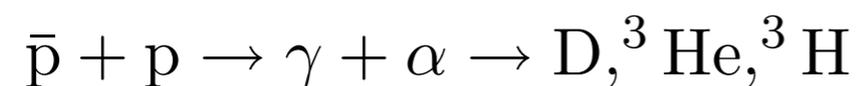


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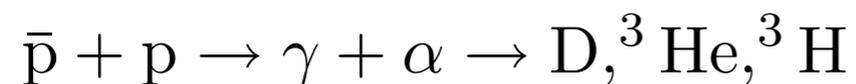


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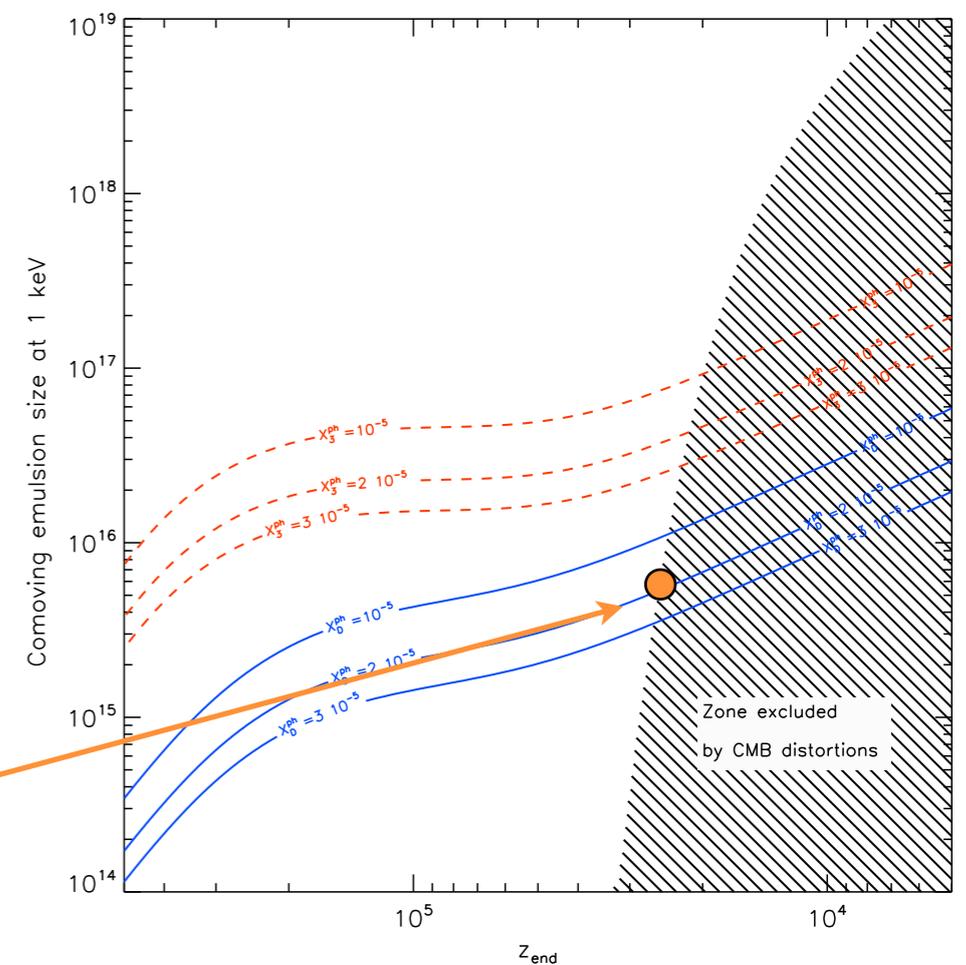
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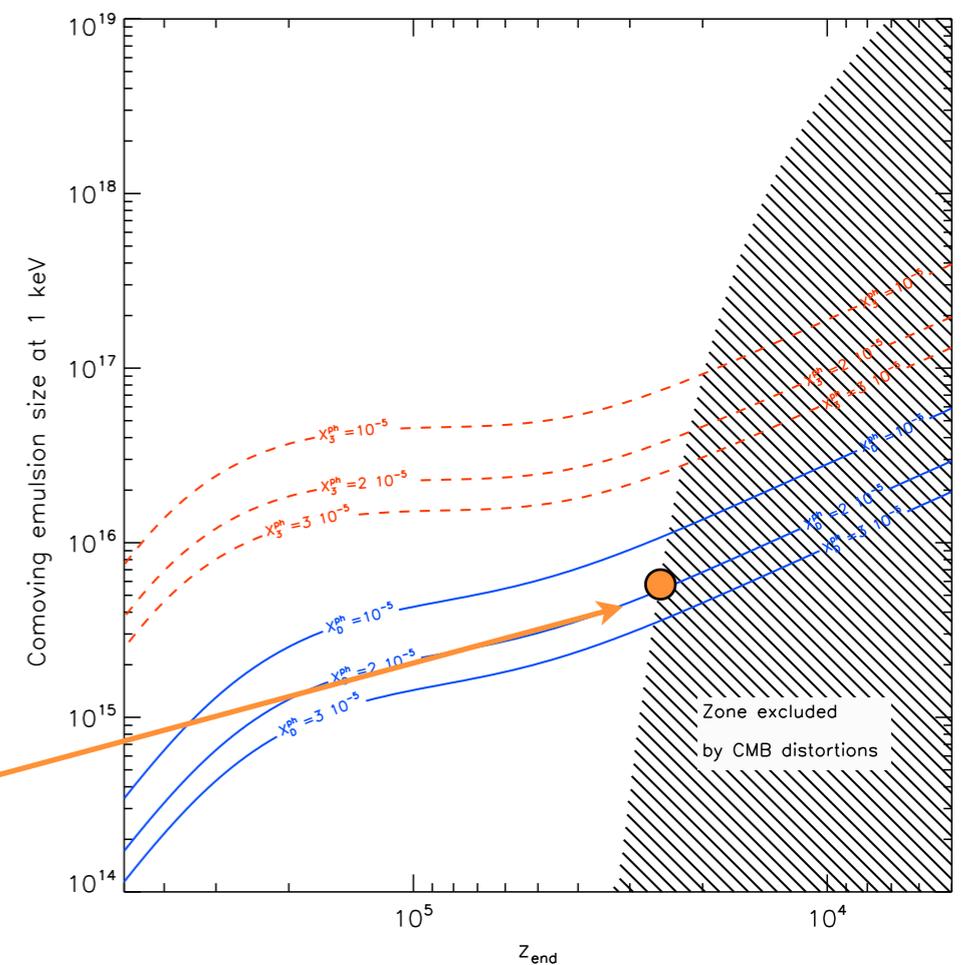
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BBN compatible with D, ^4He , ^7Li tension with ^3He

Type Ia Supernovae



- **Historical discovery of acceleration of expansion**
 - *Riess et al. 98* & *Perlmutter et al. 99* discovered that distant SN Ia are dimmer than expected
 - Interpretation that the expansion is accelerating under the effect of Dark Energy
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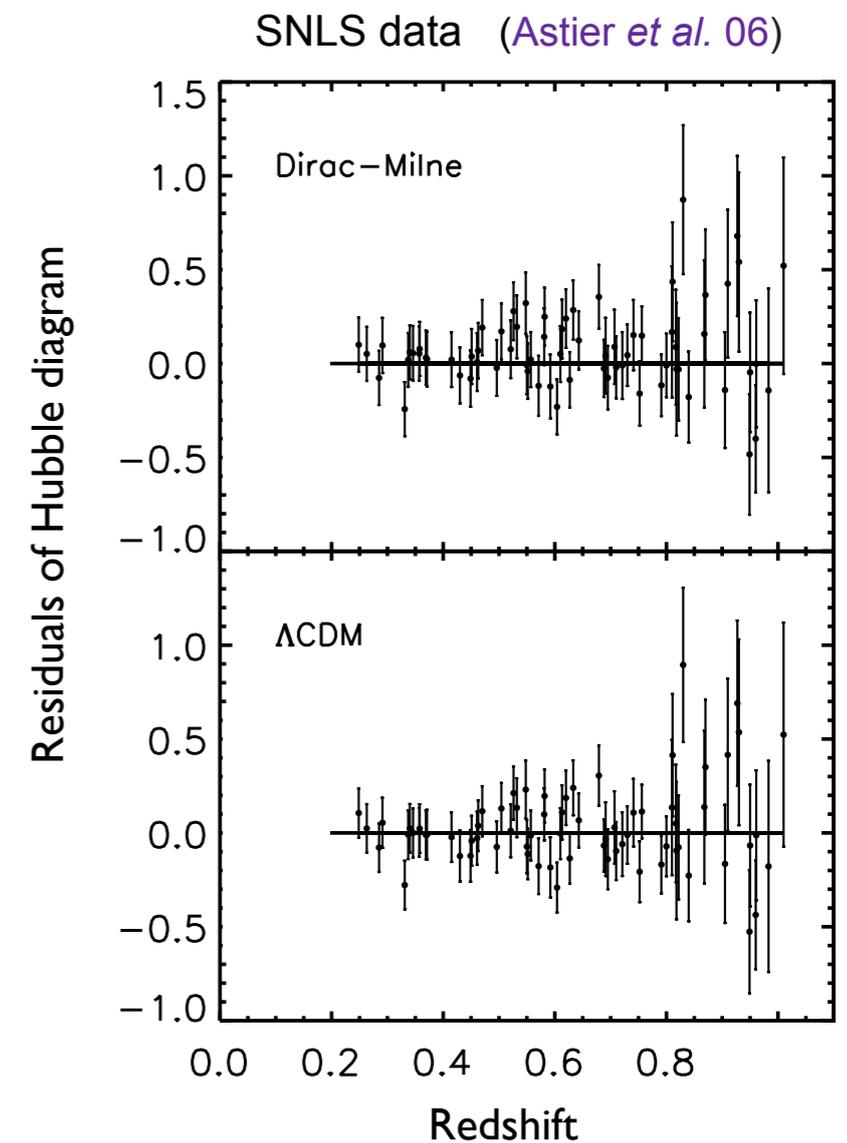


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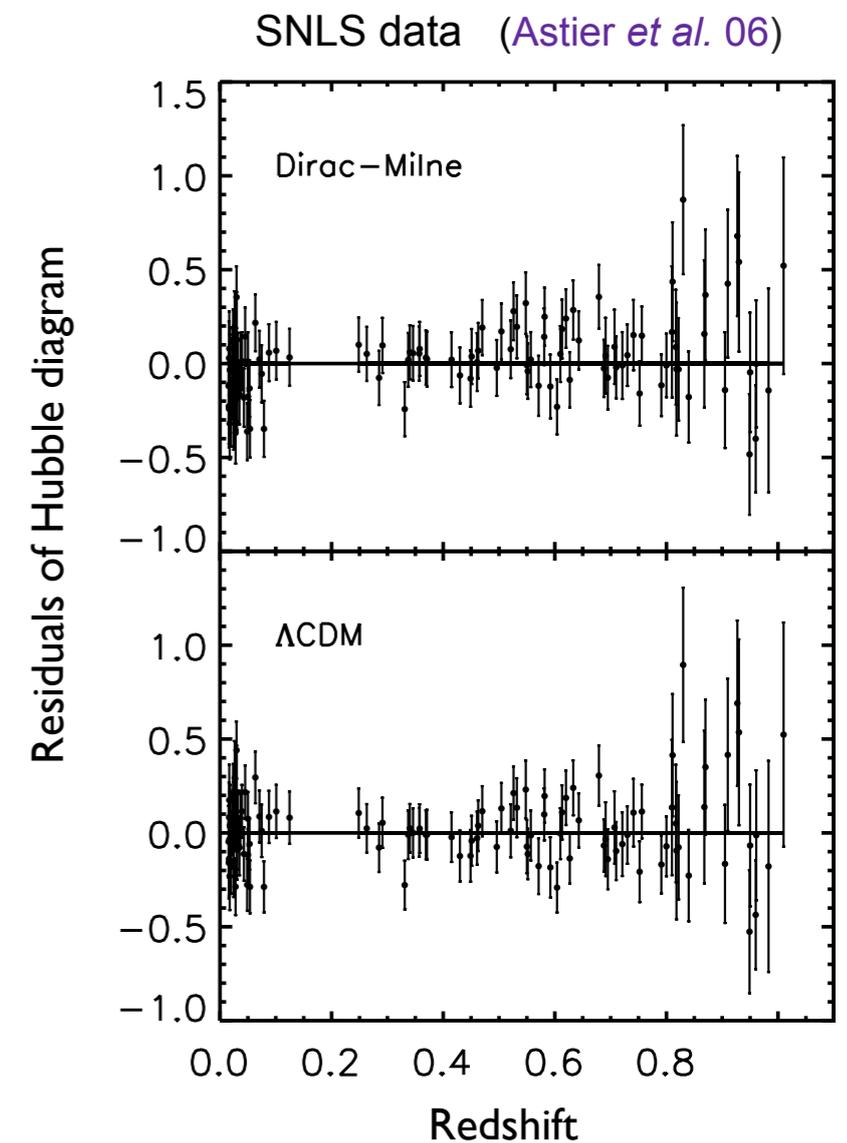


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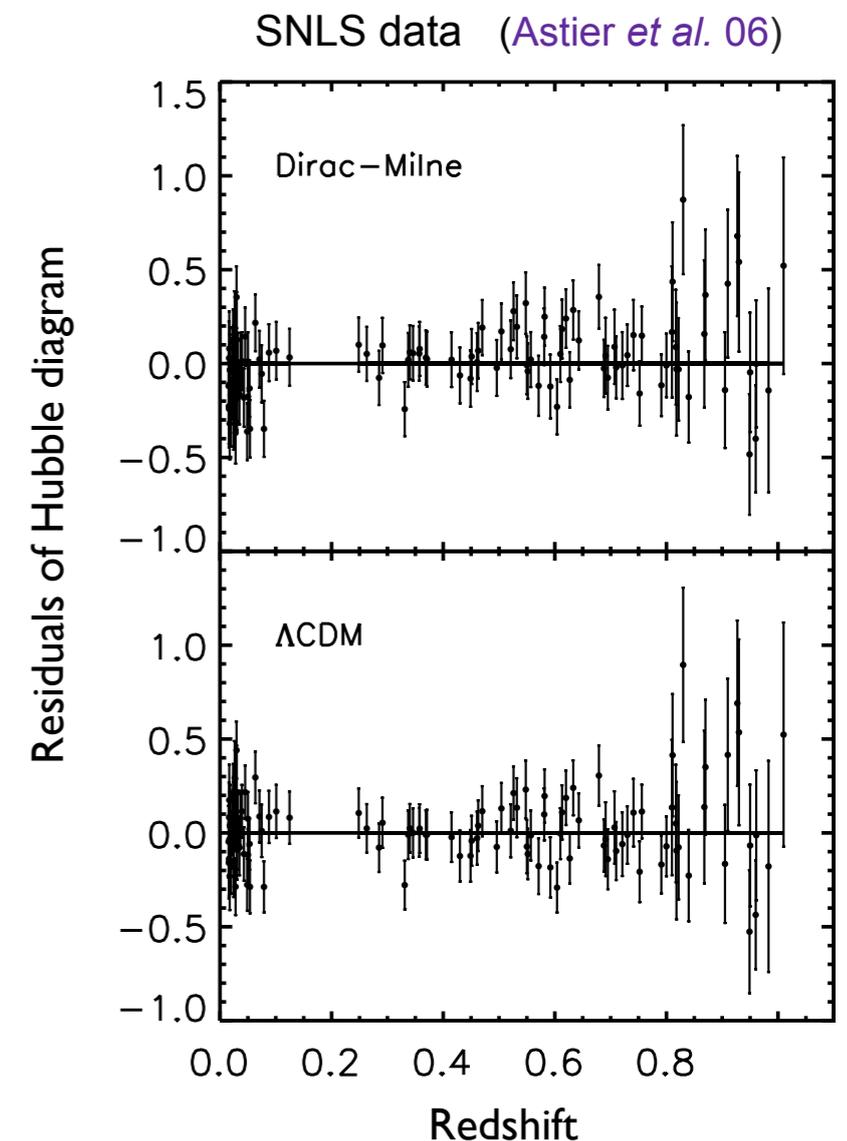
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- Nearby SN Ia are crucial
- An offset on low-z SNe Ia by $\Delta m = 0.06$ mag makes the χ^2 equal

[Kowalski et al. 08](#) estimate $\sigma_{\text{sys}}=0.04$ mag

Dirac-Milne universe
close to best-fit

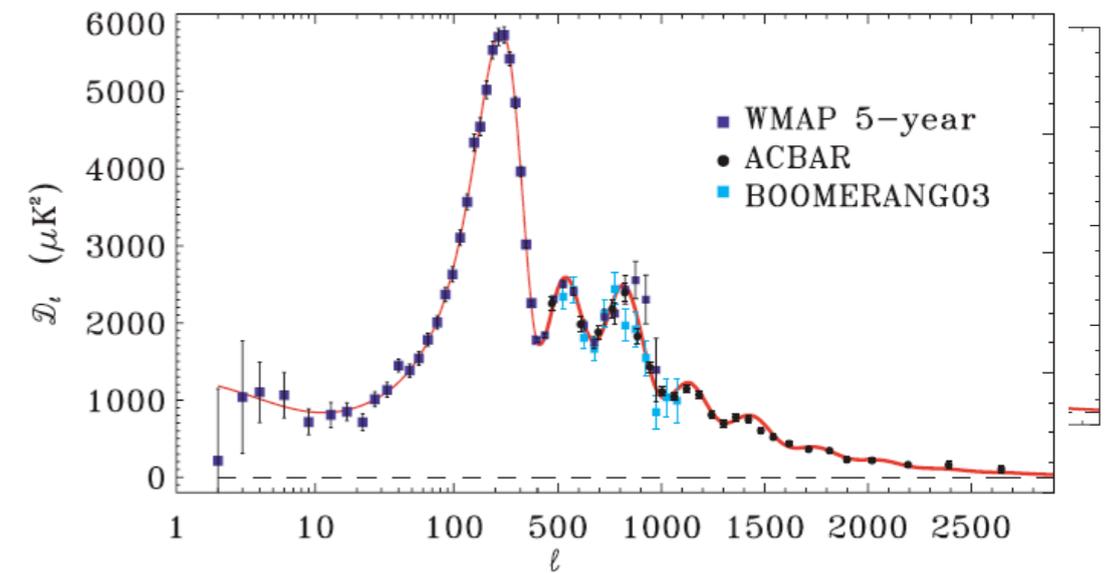


First steps on Cosmic Microwave Background

● CMB: major test of cosmological models

- First peak corresponds to acoustic scale given by sound horizon seen on last scattering surface.

$$\theta = \frac{r_s}{d_A}$$



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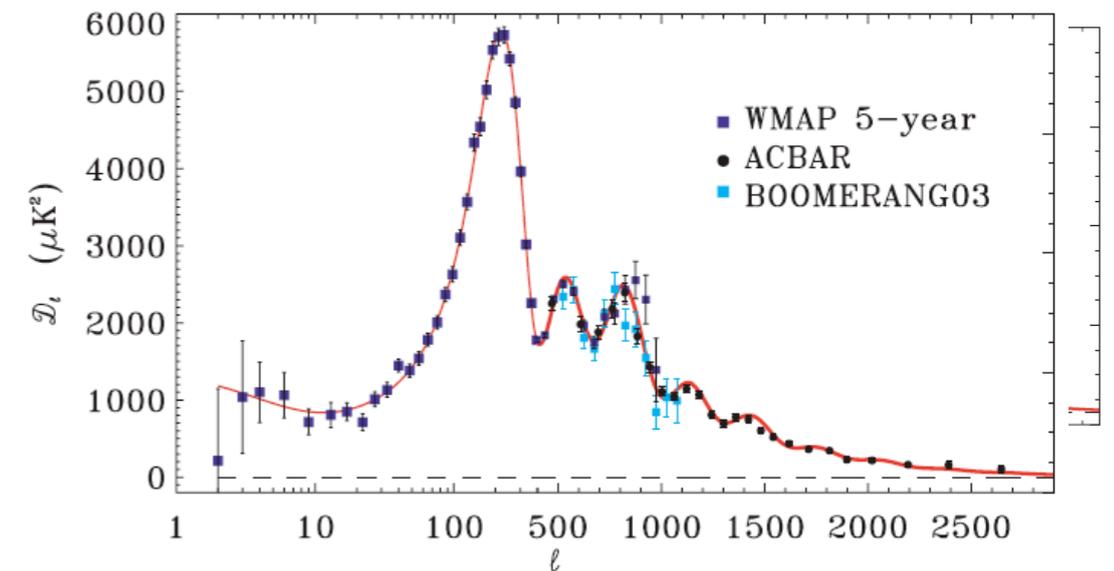
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$$d_A(z) = H_0^{-1} \frac{1}{1+z} \sinh(\ln(1+z)) \quad \text{is 163 times larger than in } \Lambda\text{CDM.}$$



one would expect a tiny angle!

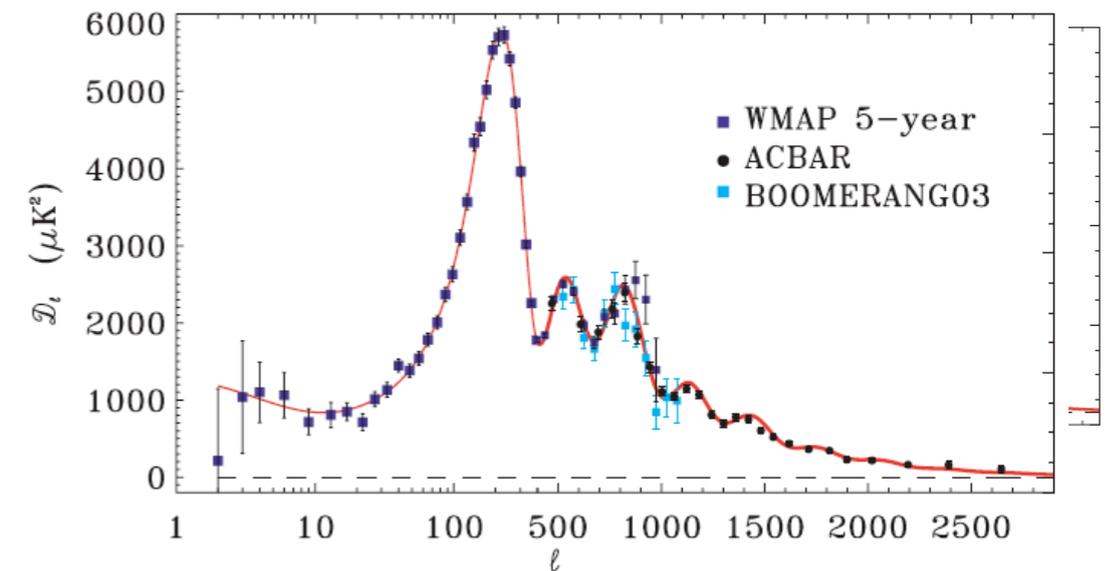
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Integrating from 40 MeV to ~7 eV (end of annihilation, cf BBN) yields acoustic scale around 1° !

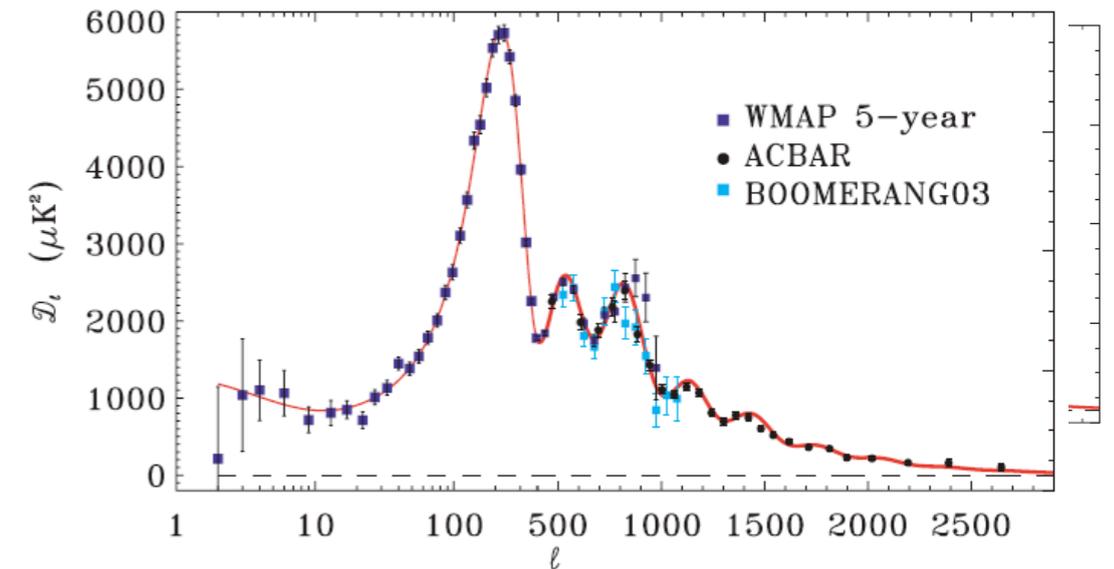
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**Acoustic scale
naturally emerges at 1°**

Conclusion



● Dirac-Milne universe

- Symmetric matter - antimatter universe
- Antimatter is supposed to have a negative active gravitational mass

● In fair agreement with studied cosmological tests

- Thermal primordial nucleosynthesis of ^4He and ^7Li
Secondary production of D can constrain size of the matter-antimatter emulsion
 ^3He production too high
- Taken at face value, SNe Ia data favour accelerating universe
Dirac-Milne universe requires reasonable systematic errors
- Acoustic scale naturally expected at the degree scale in CMB

● Still, many uncovered issues

- Disagreement on Baryonic Acoustic Oscillations (BAO)
- Structure formation
- CMB anisotropies
- ...