

(In)visible Z' and Dark Matter

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Annecy-Le-Vieux - LAPTH - March 15, 2011

E. Dudas, Y. Mambrini, S. Pokorski, A.R.
JHEP 0908:014,2009 – arXiv:0904.1745 [hep-ph]

A. Falkowski, Y. Mambrini, A.R. in progress

N. Bernal, A. Goudelis, A.R. in progress

Extensions of Standard Model

We know that the Standard Model is only an **effective field theory**, there is something more (at least neutrino masses and dark matter).

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Add new space-time structures

ex) Supersymmetry, Extra-dimensions, String Theory,...

Combine the three

The “hidden” sector (heavy matter) communicates with the visible one (the usual Standard Model) through different mechanisms (supersymmetric and/or gravitational interactions, Kaluza-Klein modes, ...), and the extra gauge-group provides a portal among the others to the new physics.

Example: KKLT framework

The presence of an extra U(1) can help to impose the suitable constraints (moduli stabilization, vanishing cosmological constant, TeV superpartner masses), and provide original spectra and dark matter scenarios.

(“D-term induced” uplift [[E.Dudas, Y.Mambrini, S. Pokorski, A.R., M. Trapletti, 08-09](#)])

Forget SUSY and extra-dim:

Only heavy fermions & Extra U(1)_X

Z'-hunter's guide

Hye-Sung Lee <http://sites.google.com/site/zprimeguide/>,
or

P. Langacker, "The Physics of Heavy Z' Gauge Bosons," Rev. Mod. Phys. **81** (2008) 1199
[arXiv:0801.1345 [hep-ph]].

- Sources of U(1)'
- U(1)' Symmetry Breaking at TeV-scale
- Alternative Solutions to the μ -problem
- Challenges in TeV-scale Z' model building
- U(1)' and Proton Decay and also exotic fields
- More Z' Models
- Implications of Z': Gauge boson sector, EWPT sector, CP and FCNC sector, Neutrino sector, Neutralino sector, Sneutrino sector, Baryogenesis sector, Higgs sector, ...

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Hybrid sector

States with SM **and** $U(1)_X$ quantum numbers. They act as a portal between the two previous sector.

A possibility: Kinetic Mixing

Chun et al., Mambrini, 2010

$$\text{SU}(3) \times \text{SU}(2) \times \text{U}(1)_Y \times \text{U}(1)_X$$

$$\mathcal{L} = \frac{1}{4g_Y^2} F_{Y,\mu\nu} F_Y^{\mu\nu} + \frac{1}{4g_X^2} F_{X,\mu\nu} F_X^{\mu\nu} + \delta F_{Y,\mu\nu} F_X^{\mu\nu} + \dots$$

The coefficient δ can be generated at one-loop by the matter in the hybrid sector.

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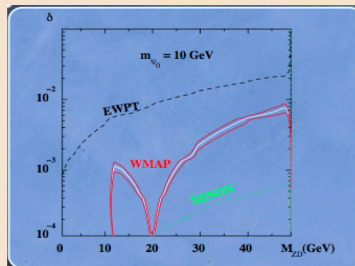
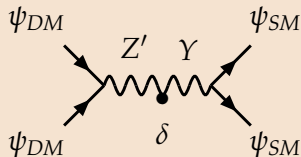
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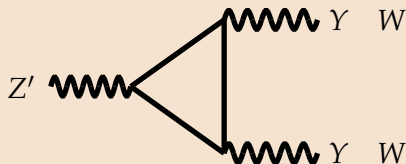
Open a portal on hidden physics

We can have informations for example from the Dark Matter side



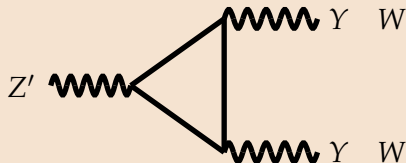
A new portal: The trilinear bosonic couplings

Another possibility



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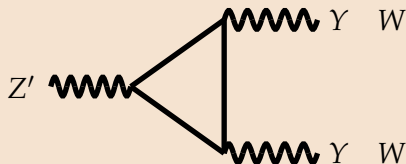


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Z' , and its analysis at LHC (ex: WW-fusion)

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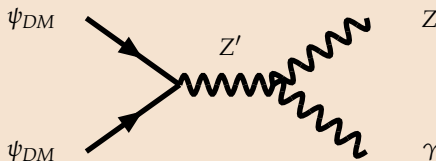
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Dark Matter, and its detection through γ -ray lines



Summary

- 1 Motivations
- 2 Anomalies vs. Decoupling
- 3 Extra U(1)'s
- 4 (In)visible Z' and Dark Matter
- 5 Gamma-ray lines
- 6 Conclusions

From the very beginning...

Whatever extra we want to introduce, the **effective field theory** at low energy has to be compatible with experimental constraints (EW precision data).

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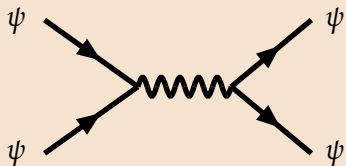
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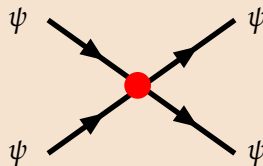
They will reflect the **symmetries** of the UV physics.

Examples of H.-D. operators

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Fermi theory

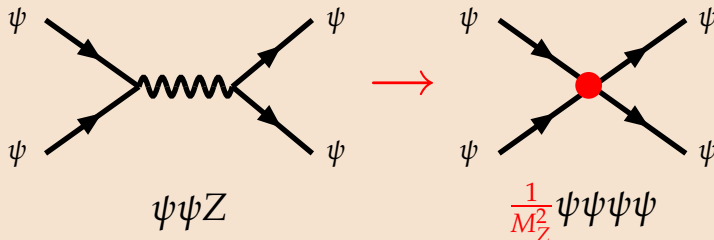


$$\psi\psi Z$$


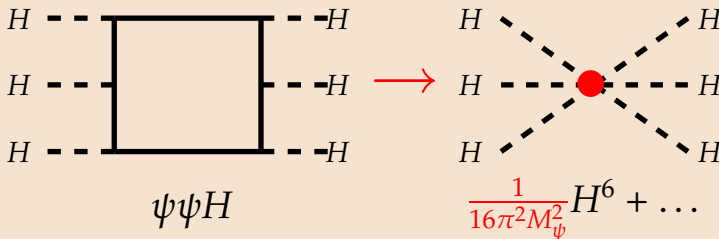
$$\frac{1}{M_Z^2} \psi\psi\psi\psi$$

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Fermi theory



Loop suppressed



4-D. operators

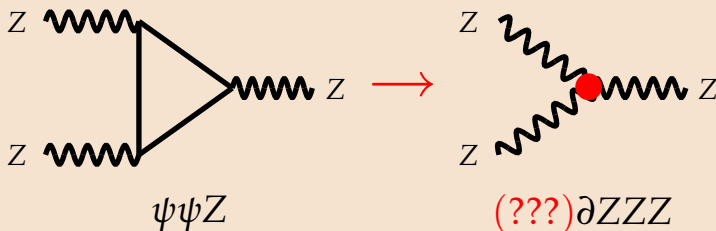
Are there contributions to the 4-dimensional operators coming from heavy particles "integrated out"?

4-D. operators

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Yes, an example is given by the kinetic mixing

In particular, what about: Triangles?



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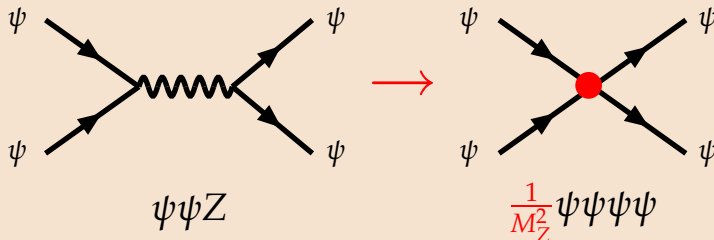
Decoupling “theorem”

T. Appelquist, J. Carazzone, Phys. Rev. D 11 (1975) 2856

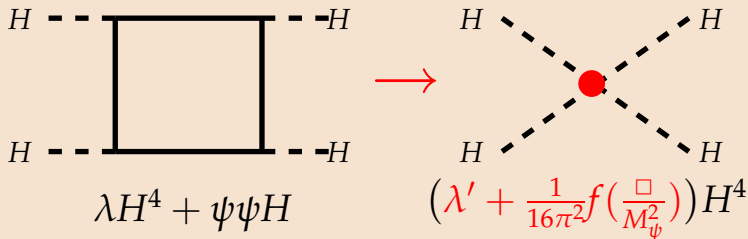
The decoupling theorem states that, in the limit of heavy masses $M_\psi \rightarrow \infty$, the extra terms will have no observable effects. Or, more precisely, those effects from heavy particles are either suppressed by **inverse powers** of M_ψ , or can be **reabsorbed** into renormalizations of couplings, masses, or field strength tensors of the theory.

Again..

Fermi theory



Loop suppressed



Anomalies

Theories in which fermions have **chiral** couplings with gauge fields generically suffer from **anomalies**

Gauge Anomaly

Phenomenon of breaking of gauge symmetries of the classical theory at one-loop level. Anomalies make a theory inconsistent.

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The only way to restore consistency of a theory is to arrange the exact cancellation of anomalies between various chiral sectors of the theory (ex. in SM between quarks and leptons).

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The only way to restore consistency of a theory is to arrange the exact cancellation of anomalies between various chiral sectors of the theory (ex. in SM between quarks and leptons).

Particles involved in anomaly cancellation **may have very different masses** (ex: the mass of the top quark in the SM is much higher than the masses of all other fermions).

Anomalies vs. Decoupling

Gauge invariance should pertain in the theory at all energies

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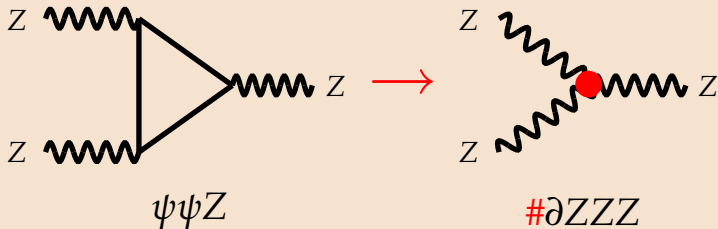
E. D'Hoker, E. Farhi, Nucl. Phys. B248 (1984)

The case of anomaly cancellation presents a notable counterexample to the decoupling theorem:

- anomalous (i.e. gauge-variant) terms in the effective action have topological nature and are therefore scale independent.
- they are not suppressed even at energies much smaller than the masses of the particles producing these terms via loop effects.

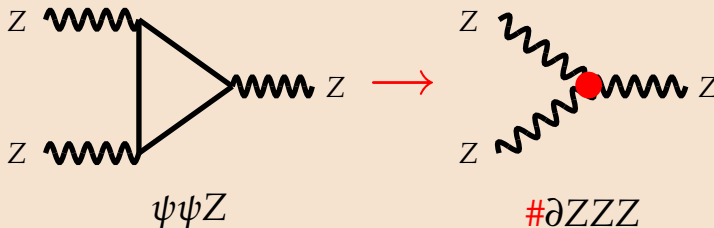
Then...

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There is an effective operators of the form

$$\sim \frac{1}{H^\dagger H} \epsilon^{\mu\nu\rho\sigma} D_\mu \theta_H (H^\dagger D_\nu H - D_\nu H^\dagger H) F_{\rho\sigma}$$

which restores the gauge invariance of the total (tree-level + 1-loop) effective lagrangian.

Focusing on extra U(1)

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Standard Z' theories

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Anomalous Z' theories

There are **some un-canceled** reducible anomalies. They cancel in the underlying theory due to :

- axions with Green-Schwarz type couplings in string theories.
- heavy chiral (wrt Z') fermions in field theory models, which can generate **(non?)-decoupling effects** at low-energy.

Anomalous Z' theories

Anastasopoulos, Bianchi, Dudas, Kiritsis, JHEP 0611 (2006) 057; Coriano et al., ...

Effective action (forgetting kinetic mixing for the moment)

$$\mathcal{S} = - \sum_i \int d^4x \frac{1}{4g_i^2} F_{i,\mu\nu} F_i^{\mu\nu} + \frac{1}{2} \int d^4x \sum_i (\partial_\mu a^i - g_i V_i A_\mu^i)^2$$

$$+ \frac{1}{96\pi^2} C_{ij}^I \epsilon^{\mu\nu\rho\sigma} \int a^I F_{\mu\nu}^i F_{\rho\sigma}^j + \frac{1}{48\pi^2} E_{ij,k} \epsilon^{\mu\nu\rho\sigma} \int A_\mu^i A_\nu^j F_{\rho\sigma}^k .$$

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Stueckelberg mixing terms with axions which render the corresponding gauge fields **massive**.

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Axionic exchanges: nonlocal contributions

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Generalized Chern-Simons terms: “anomalous” three gauge bosons coupling

Stueckelberg mechanism

The Stueckelberg mechanism can be understood as a heavy Higgs mechanism, where an extra Higgs field S takes vev V and then the form:

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This picture is useful when we think to an heavy fermionic sector taking chiral mass. However, one could discuss about Stueckelberg mechanism in more general framework

(Mambrini's paper).

Anomalous three gauge boson couplings

Effective action

$$\begin{aligned} \mathcal{S} = & - \sum_i \int d^4x \frac{1}{4g_i^2} F_{i,\mu\nu} F_i^{\mu\nu} + \frac{1}{2} \int d^4x \sum_i (\partial_\mu a^I - M_i^I A_\mu^i)^2 \\ & + \frac{1}{96\pi^2} C_{ij}^I \epsilon^{\mu\nu\rho\sigma} \int a^I F_{\mu\nu}^i F_{\rho\sigma}^j + \frac{1}{48\pi^2} E_{ij,k} \epsilon^{\mu\nu\rho\sigma} \int A_\mu^i A_\nu^j F_{\rho\sigma}^k . \end{aligned}$$

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Gauge invariance requirement

$$\text{Tr}(Q_i Q_j Q_k) + E_{ij,k} + M_i^I C_{jk}^I = 0$$

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Anomalous three gauge boson couplings

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Our starting point

Notice that it is possible to have standard (anomaly-free) Z' , $\text{Tr}(Q_i Q_j Q_k) = 0$, and non-vanishing anomalous three gauge boson couplings at **low energy**. They have the form

$$d_{ij,k} \epsilon^{\mu\nu\rho\sigma} (\partial a^i - M_i A^i)_\mu (\partial a^j - M_j A^j)_\nu F_{\rho\sigma}^k$$

(In)visible Z' and decoupling of heavy fermions

Definition

(In)visible Z' : extra U(1) massive gauge boson, and:

- All SM fields are **neutral** under Z'
- There is a sector of **heavy fermions** charged both under the SM and Z' , chiral but anomaly-free
- The effects of the heavy fermions are only encoded at low-energy in effective couplings, containing **anomalous three gauge boson couplings**

Warm up: Two Z' 's case

In this case there is a genuine **non-decoupling** effect.

It's easy in fact to write down a gauge invariant operator with 2 **different** covariant derivatives.

The corresponding operator is [with $\theta_i = a_i / (g_i V_i)$]

$$E_{Z'_1 Z'_2, Y} \epsilon^{\mu\nu\rho\sigma} (\partial\theta_1 - Z'_1)_\mu (\partial\theta_2 - Z'_2)_\nu F^Y_{\rho\sigma}$$

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NOTE: I am asking for two extra gauge fields, two extra “Higgs fields”, an extra sector of fermions ... maybe it's not a “simple” extension of the Standard Model.

However: this sector can be **“arbitrarily” heavy**, but its effects on the low-energy theory remain sizeble.

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Subtlety

Calculations in the limit: Yukawa's $\lambda_i \rightarrow \infty$, VEV's V_i finite.

Explicit example for the two Z' 's case

Formula in the limit $\lambda_i \rightarrow \infty$, X^i charges of the $(h) =$ heavy spectrum under i group

$$E_{ij,k} = \frac{1}{4} \sum_h (X_L^i X_R^j - X_R^i X_L^j)^{(h)} (X_R^k + X_L^k)^{(h)},$$

It is then easy to find examples of heavy fermionic sectors generating it (l_a fermions Ψ and l_m fermions χ)

	Y	Z'_1	Z'_2
Ψ_L^a	y_a	x_a	z_a
Ψ_R^a	y_a	$x_a - \epsilon_a$	z_a
χ_L^m	y_m	x_m	z_m
χ_R^m	y_m	x_m	$z_m - \epsilon_m$

$$\text{Tr}(Z'_1 Z'_2 Y) = \sum_a l_a \epsilon_a y_a z_a + \sum_m l_m \epsilon_m x_m y_m, \quad E_{Z'_1 Z'_2, Y} = \frac{1}{2} (\sum_a l_a \epsilon_a y_a z_a - \sum_m l_m \epsilon_m x_m y_m)$$

and then

$$\text{Tr}(Z'_1 Z'_2 Y) = 0 \quad \Rightarrow \quad E_{Z'_1 Z'_2, Y} = \sum_a l_a \epsilon_a y_a z_a \neq 0$$

One Z' case

Decoupling

In this case, by symmetry,

$$E_{Z'Z',Y} \epsilon^{\mu\nu\rho\sigma} (\partial\theta_X - Z')_\mu (\partial\theta_X - Z')_\nu F_{\rho\sigma}^Y = 0$$

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In this case, I need to classify the effective operators, using **dimension** and **CP-symmetry**.

NOTE: $U(1)_X$ is realised in the broken phase, but effective operators have to be **SM-invariant**.

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Decoupling

In this case, by symmetry,

$$E_{Z'Z',Y} \epsilon^{\mu\nu\rho\sigma} (\partial\theta_X - Z')_\mu (\partial\theta_X - Z')_\nu F_{\rho\sigma}^Y = 0$$

In this case, I need to classify the effective operators, using **dimension** and **CP-symmetry**.

NOTE: $U(1)_X$ is realised in the broken phase, but effective operators have to be **SM-invariant**.

Heavy fermions at mass scale Λ

- If they are vector-like, effective operators have to preserve charge conjugation C.
Furry's theorem $\rightarrow$ Euler-Heisemberg type $(1/\Lambda^4)F^4 + \dots$
- If they are chiral, effective operators violate C and trilinear coupling are allowed.

One Z' case: CP even operators

- Dimension-four operators :

$$\delta F_{\mu\nu}^Y F^{X\mu\nu} \quad , \quad i\eta \mathcal{D}_\mu \theta_X H^\dagger D_\mu H + c.c.$$

- Dimension-six operators :

$$\begin{aligned} & \frac{1}{\Lambda^2} \left\{ b_1 \text{Tr}(F^X F^Y \tilde{F}^Y) + 2b_2 \text{Tr}(F^X F^W \tilde{F}^W) + b_3 \text{Tr}(F^Y F^X \tilde{F}^X) \right. \\ & + \mathcal{D}^\mu \theta_X \left[i(D^\nu H)^\dagger (\textcolor{red}{c}_1 \tilde{F}_{\mu\nu}^Y + \textcolor{red}{c}_2 \tilde{F}_{\mu\nu}^W + c_3 \tilde{F}_{\mu\nu}^X) H + c.c. \right] \\ & + \partial^\mu \mathcal{D}_\mu \theta_X \left[\textcolor{red}{d}_1 (F^Y \tilde{F}^Y) + 2\textcolor{red}{d}_2 (F^W \tilde{F}^W) + d_3 (F^Y \tilde{F}^X) \right] \\ & \left. + \mathcal{D}_\mu \theta_X \mathcal{D}^\mu \theta_X \left[d_4 (F^Y F^Y) + 2d_5 (F^W F^W) \right] \right\} . \end{aligned}$$

Notation

$$\mathcal{D}_\mu \theta_X = (\partial \theta_X - Z')_\mu$$

$D^\nu H$: SM covariant derivative of Higgs

One Z' case: Trilinear couplings

$$\begin{aligned}
 \Gamma_{\mu\nu\rho}^{Z'\gamma Z}(p_3; p_1, p_2) &= -8 \frac{(d_1 - d_2)}{\Lambda^2} g_X \sin \theta_W \cos \theta_W (p_1 + p_2)^\mu \epsilon_{\nu\rho\sigma\tau} p_2^\sigma p_1^\tau \\
 &\quad - 2 \frac{e g_X}{\cos \theta_W \sin \theta_W} \frac{v^2}{\Lambda^2} [c_1 \cos \theta_W + c_2 \sin \theta_W] \epsilon_{\mu\nu\rho\sigma} p_1^\sigma \\
 \Gamma_{\mu\nu\rho}^{Z'ZZ}(p_3; p_1, p_2) &= -4 \frac{(d_1 \sin^2 \theta_W + d_2 \cos^2 \theta_W)}{\Lambda^2} g_X (p_1 + p_2)^\mu \epsilon_{\nu\rho\sigma\tau} p_2^\sigma p_1^\tau \\
 &\quad - \frac{e g_X}{\cos \theta_W \sin \theta_W} \frac{v^2}{\Lambda^2} [c_2 \cos \theta_W - c_1 \sin \theta_W] \epsilon_{\mu\nu\rho\sigma} (p_2^\sigma - p_1^\sigma) \\
 \Gamma_{\mu\nu\rho}^{Z'W^+W^-}(p_3; p_1, p_2) &= -4 \frac{d_2}{\Lambda^2} g_X (p_1 + p_2)^\mu \epsilon_{\nu\rho\sigma\tau} p_2^\sigma p_1^\tau \\
 &\quad - \frac{e g_X}{\cos \theta_W \sin \theta_W} \frac{v^2}{\Lambda^2} c_2 \epsilon_{\mu\nu\rho\sigma} (p_2^\sigma - p_1^\sigma)
 \end{aligned}$$

Coefficients related to structures

$$c_i \leftrightarrow (v^2 \partial) / \Lambda^2; \quad d_i \leftrightarrow (\partial^3) / \Lambda^2$$

Experimental signatures

How is it possible to experimentally detect such theories with extra $U(1)_X$?

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If **SM fermions are charged** with respect to the $U(1)_X$ group, and the mass of the new Z' bosons is around the TeV scale, we should be able to see the corresponding **resonance** in the forthcoming runs of LHC; ex) $q\bar{q} \rightarrow Z' \rightarrow f\bar{f}$.

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What happens if the SM fermions are not charged with respect to the $U(1)_X$ group?

(Kumar, Rajaraman, Wells, arXiv:0707.3488 [hep-ph]

Antoniadis, Boyarsky, Espahbodi, Ruchayskiy, Wells, arXiv:0901.0639 [hep-ph]

→ study of LHC detection)

(In)visible Z' as mediator of dark matter annihilation

see also Y. Mambrini, JCAP 0912 (2009) 005

Main Idea

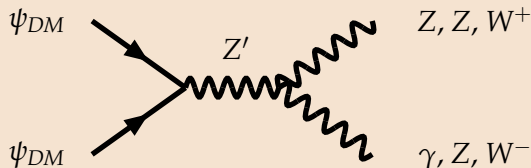
- The **Dark Matter** candidate is the lightest fermion in the sector coupled to Z' but not to SM

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Main Idea

- The **Dark Matter** candidate is the lightest fermion in the sector coupled to Z' but not to SM
- It annihilates into Z , γ , $Z Z$ and $W^+ W^-$, via Z' exchange,

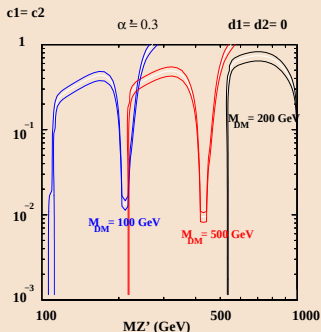


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Main Idea

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- It gives the correct **relic density** [implementing it into CompHEP of **micrOMEGAs**]
- The same diagram produces a **mono-chromatic gamma ray**

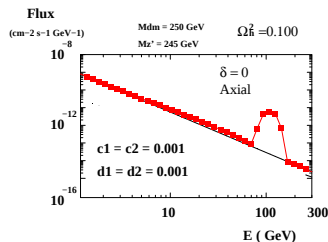
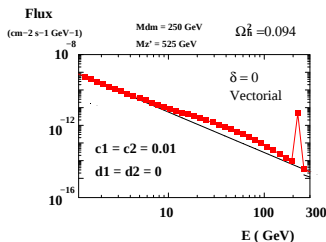
$$E_{\gamma} = M_{DM} \left[1 - \left(\frac{M_Z}{2M_{DM}} \right)^2 \right] ,$$

which could be visible in future experiments.

Crucial point: DM annihilation happens almost at rest.

- There is **NO** $\gamma\gamma$ final state C. N. Yang, Phys. Rev. 77 (1950) 242.

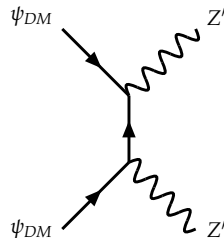
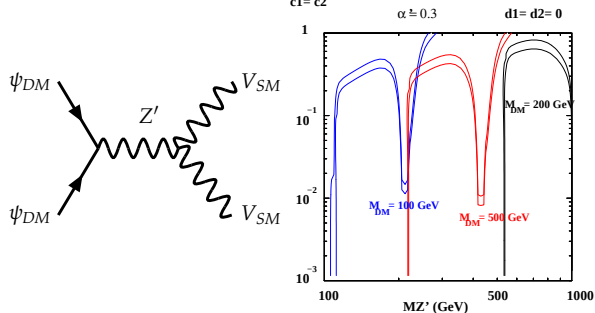
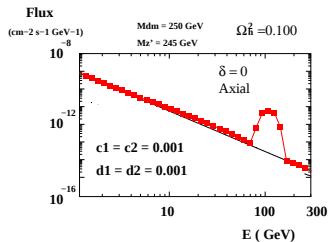
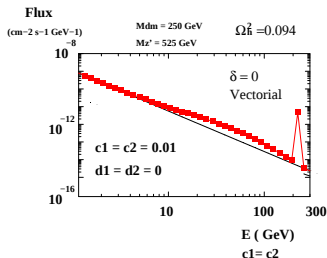
(In)visible Z' as mediator of dark matter annihilation



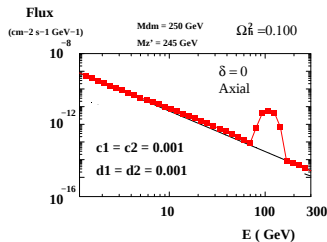
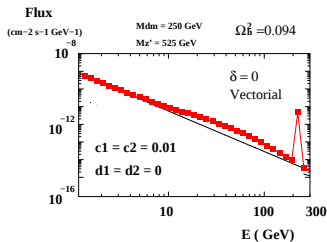
Examples of a gamma-ray differential spectrum (red boxes) for different values of Z' masses at a fixed DM mass $M_{dm} = 250 \text{ GeV}$ and $\Lambda = 1 \text{ TeV}$, in comparison with the background (black line).

Remember: $c_i \leftrightarrow (v^2 \partial) / \Lambda^2$; $d_i \leftrightarrow (\partial^3) / \Lambda^2 \sim (M_{DM}^2 \partial) / \Lambda^2$

(In)visible Z' as mediator of dark matter annihilation

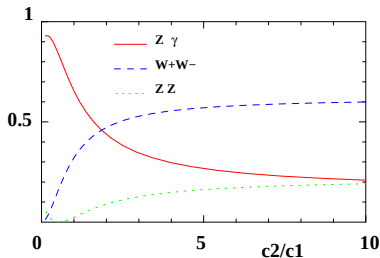


(In)visible Z' as mediator of dark matter annihilation



Branching ratio for $M_{\text{DM}} = 200 \text{ GeV}$,
 $M_{Z'} = 215 \text{ GeV}$ and $d_1 = d_2 = 0$

$\text{Br}(Z')$



Dark Matter detection

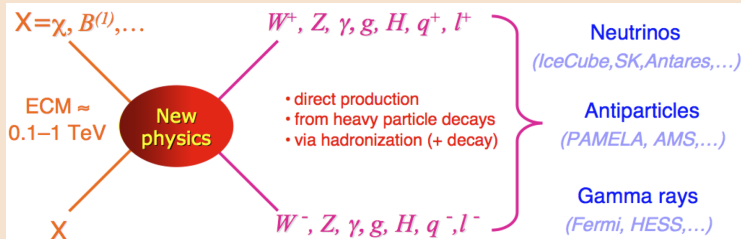
Usual strategies:

Serpico's talk at Planck09

<i>Experiment</i>	<i>Source</i>	<i>Interaction</i>	<i>Channel</i>
<u>Direct</u>	Local (crossing Earth surface)	WIMP-nucleus scattering	Phonons
<u>Indirect</u>	Earth, Sun, Galaxy, Cosmos	WIMP decay/annihilation	γ, ν , Antimatter
<u>Collider</u>	Controlled production	WIMP pair production	$\cancel{e}$

Dark Matter detection

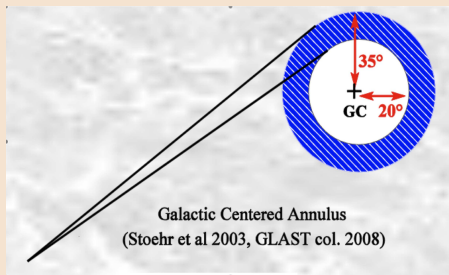
Indirect detection



Target	Advantage	Challenges
Spectral line $E = m_\chi$ anywhere	Smoking gun	Loop process, suppressed, Experimental E-resolution

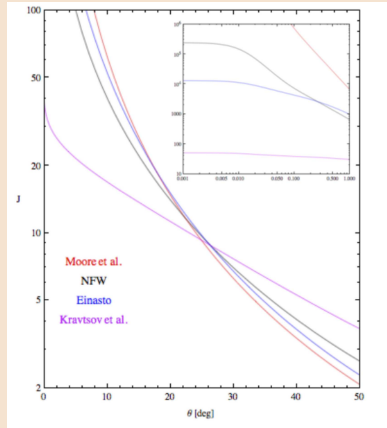
Indirect detection: Observability

Observed region



- Signal to noise ratio increased 12 times with respect to the Galactic Center
- Almost independent of the Galactic Profile

Indirect detection: Observability



Indirect detection: Observability

Parameters

Assuming coefficients of order 1 (natural charges) in front of the different operators, there are essentially **three free mass parameters** for: dark matter, extra gauge boson, heavy fermions.

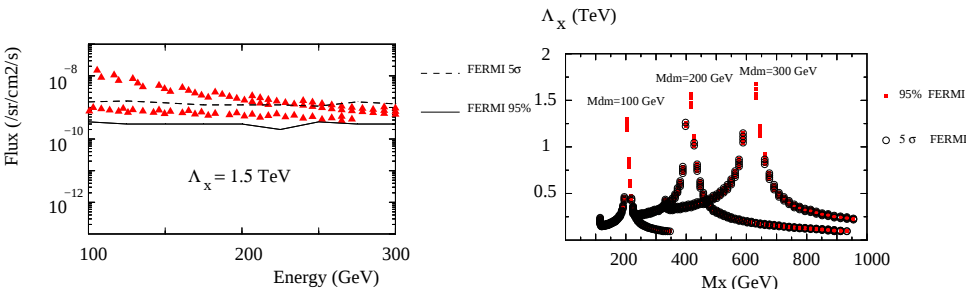
In particular we are interested in the region 100 GeV - few TeV.

Indirect detection: Observability

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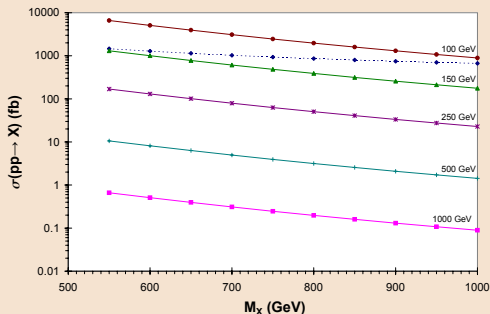
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Indirect detection: Observability

To compare with colliders analysis:

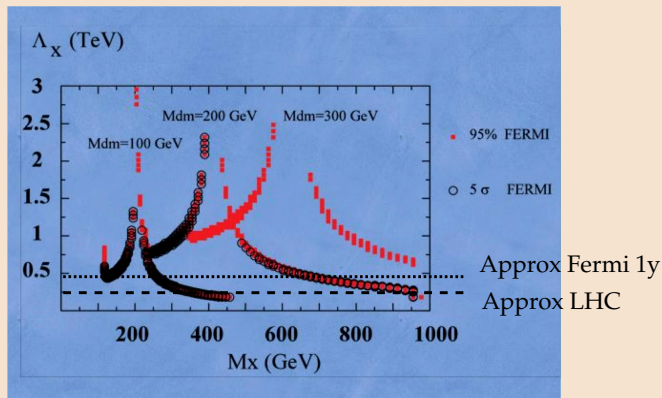


At $\sqrt{s_{pp}} = 14$ TeV LHC as a function of the mass of the extra gauge boson, for different heavy sector scales. The dashed line corresponds to the cross-section required for detection at LHC in the $WW \rightarrow X \rightarrow ZZ \rightarrow 4l$ decay channel.

Kumar, Rajaraman, Wells, Phys. Rev. D 77 (2008) 066011

Indirect detection: Observability

Or looking at the same picture as before:



Kinetic Mixing

Actually the first non-trivial operator one can write is the kinetic mixing between Z' and Y

$$\delta F_{\mu\nu}^{Z'} F^{\mu\nu Y}$$

The possibilities given by this term have been already studied in many papers (see for example [Arkani-Hamed et al. JHEP 0812:104,2008](#)).

Kinetic Mixing

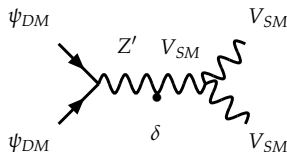
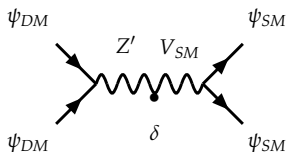
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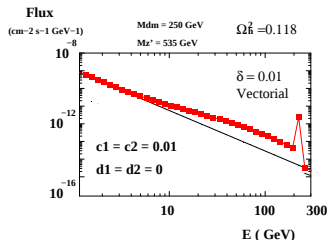
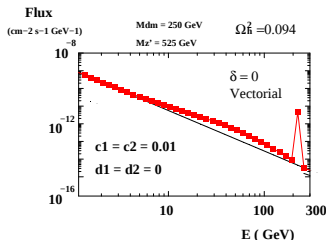
The possibilities given by this term have been already studied in many papers (see for example [Arkani-Hamed et al. JHEP 0812:104,2008](#)).

In our case, it can interplay in two ways:

- If δ is small, it just rotates mass states with respect to the gauge ones ($\rightarrow$ **Milli-charged dark matter**)
- If it is dominant over Z' Z γ coupling, it will tend to lower its effects (namely the gamma line)



Kinetic Mixing



Flux spectrum profile changes when the kinetic mixing term δ is turned on, keeping the good value for relic density.

Kinetic Mixing

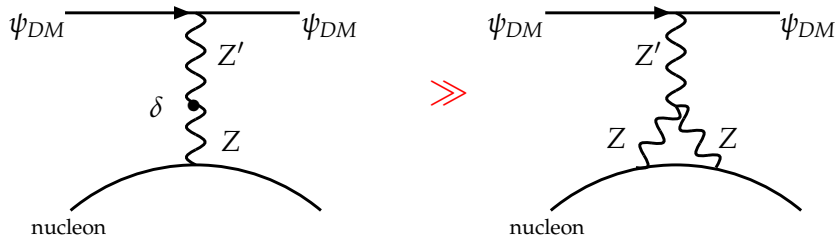
Constraints from direct detection

If the kinetic mixing is turned on, the dark matter annihilates effectively in Z-boson, which can interact with nucleons

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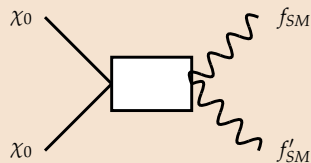
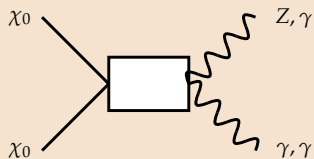


The γ -ray line is still there

For this kind of models, XENON imposes $\delta < 0.01$

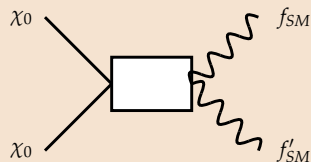
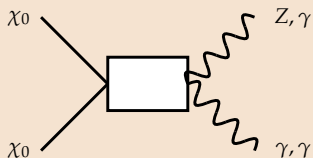
Other possibilities

SUSY/KK



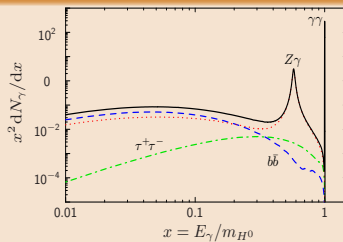
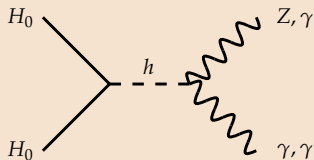
Other possibilities

SUSY/KK



Inert Higgs

Gustafsson et al, Phys. Rev. Lett. 99, 041301 (2007)

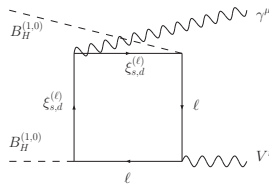
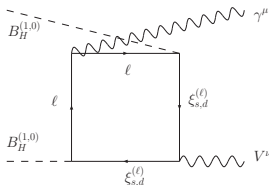
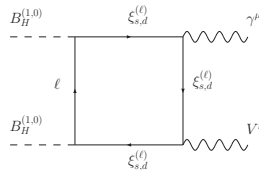
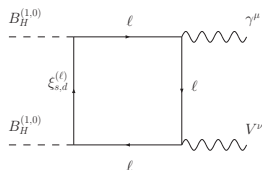


WIMP Forest: The Chiral Square

Bertone et al., Phys. Rev. D 80 (2009) 023512

6dim-model.

Scenario characterized by three lines ($V = \gamma, Z, KK - exc.$). The two lines at and around the dark matter (LKP), and a line at much lower energies that is clearly distinguishable from the other ones.

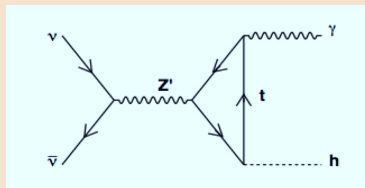


Or again:

Higgs in space!

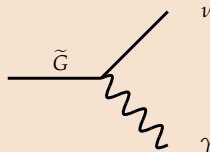
Jackson et al. JCAP 1004 (2010) 004

Like us, but also a line:



Decaying dark matter

Bertone et al. JCAP 0711 (2007) 003



From Yann Mambrini's talk

Here the summary of some different known possibilities concerning γ -ray lines from dark matter.

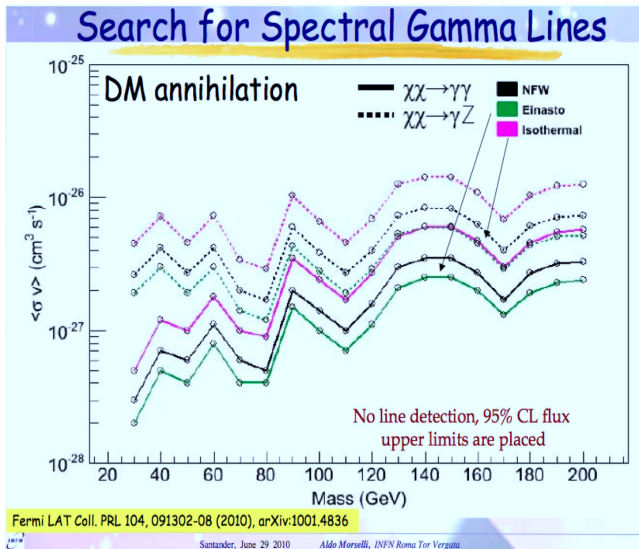
Masse	Direct detection	Indirect detection	LHC
SUSY/KK	Yes	No line	Yes
Chiral Square	Yes	3 lines	?
Inert HiggsModel	Yes	2 lines	Yes
Milli-charged	Yes	No line	Yes
(In)visible X	No	1 line	No

What do experimental data say?

FERMI results (after 1 year data taking) in the region 30-200 GeV

The limits on $\langle\sigma v\rangle_{\gamma\gamma}$ ($\langle\sigma v\rangle_{\gamma Z}$) shown in Table I are about one or more orders of magnitude weaker than the cross-sections expected for a typical thermal WIMP. However, there are several models in the literature that predict larger cross-sections and are constrained by these results. A WIMP produced non-thermally may have a much larger annihilation cross-section than a thermally produced WIMP and still produce the required DM relic density. An example is the “Wino LSP” model [19] that explains the recent positron measurement by PAMELA [37], and predicts $\langle\sigma v\rangle_{\gamma Z} \simeq 1.4 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$ at $E_\gamma \sim 170 \text{ GeV}$. Our results disfavor this model by about a factor of $\sim 2 - 5$, depending on the dark matter halo profile (see Table I). Other models that are partially

What do experimental data say?



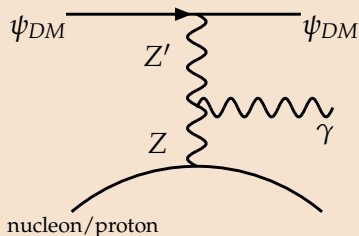
Conclusions & Outlook

- Three gauge boson "**anomalous**" **vertices** can connect an otherwise invisible Z' to SM.
- The diagram generating the correct relic density also generates **one visible gamma-ray line**.
- There is no $\gamma\gamma$ final state, differently from SUSY neutralino and inert Higgs scalars (but sensitivity ...).
- It would be interesting to analyze more generally the **non-decoupling effects** of heavy chiral fermions : for two Z' is there a **violation of the decoupling "theorem"** ?
[N.Bernal, A.Goudelis, A.R.]

Conclusions & Outlook

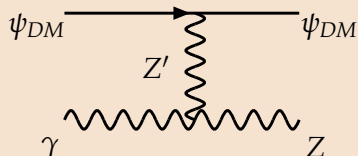
New possible funny effects:

A.Falkowski, Y.Mambrini, A.R.



Direct Detection + γ -ray?

Scattering with proton (in clouds) + γ -ray?



Scattering with photons with Z-production?