

# Charmonium and X, Y at Belle

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- X(3872)
  - mass & width determination, BR  $J/\psi\pi^+\pi^-$  mode
  - angular analysis
  - radiative decays
- Y(4260)
  - search in  $J/\psi\pi^0\pi^0$  channel
- $\eta_c$  and  $\eta_c(2S)$ 
  - estimation of the interference effect

# Introduction

B-factories provide a great opportunity to study known charmonium states and discover new ones.

Since 2002 B-factories found more than 10 states that

- probably contain a (c anti-c) pair  $\Rightarrow$  “charmonium-like” states
- have mass above the open charm threshold
- are in poor agreement with the charmonium potential model

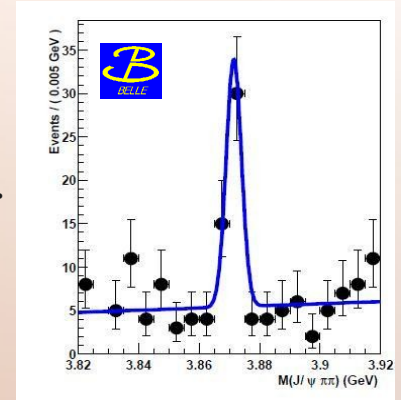
Exotic state models:

- **Multiquark state**
  - Molecule (two loosely bound charm mesons)
  - Tetraquark (tightly bound four-quark state)
- **Hybrid** (state with excited gluonic degrees of freedom)
- **Hadrocharmonium** (charmonium state “coated” by light-hadron matter)
- **Threshold effects**
  - Virtual state at threshold
  - Charmonium state shifted by nearby  $D_{(s)}^{(*)}D_{(s)}^{(*)}$  thresholds

None of these models explains all properties of observed exotic states!

# X(3872)

First observed by Belle[1] in  $B \rightarrow K(J/\psi \pi^+ \pi^-)$ . Mass is close to the  $(D^0 \text{ anti-} D^{*0})$  threshold. Width is less than experimental resolution. Confirmed by BaBar, CDF, and D0.



## Possible interpretations:

- Charmonium state

-  $\chi_{c1}(2P)$   $\longleftrightarrow$  large  $\mathcal{B}(\chi_{c1}(2P) \rightarrow J/\psi \gamma)$  expected

-  $\eta_{c2}$   $\longleftrightarrow$  large width expected

- $D^0 \text{ anti-} D^{*0}$  molecule - **most popular model**  $\longleftrightarrow$  unexplained production in B decays and p anti-p

- (c anti-c) and  $(D^0 \text{ anti-} D^{*0})$  mixture  $\longleftarrow$

- Tetraquark (diquark-diantiquark)  $\longleftrightarrow$  no charged partner of X found

## There are two possibilities for quantum numbers

- $M(\pi^+ \pi^-)$  close to  $\rho$  decay (Belle[2] and CDF[3])  $\oplus$   $X(3872) \rightarrow J/\psi \gamma$  (Belle[4] and Babar[5]) established  $C=+1$
- $X \rightarrow J/\psi \pi^+ \pi^-$  (study by CDF[6])  $\Rightarrow 1^{++}$  or  $2^{-+}$
- $X \rightarrow J/\psi \gamma$  (Belle and Babar[7]) favors  $1^{++}$
- $X \rightarrow J/\psi \pi^+ \pi^- \pi^0$  (BaBar[8]) favors  $2^{-+}$  (?)
- Molecular state model  $\Rightarrow 0^{-+}$  or  $1^{++}$

[1] PRL 91 261001

[2] arXiv:hepex/0505038

[3] PRL 96 102002

[4] arXiv:1105.0177

[5] PRL 102 132001

[6] PRL 98 132002

[7] arXiv:1007.4541

[8] PRD 82 011101

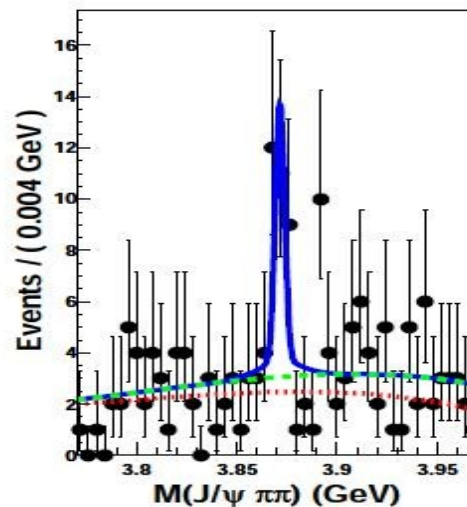
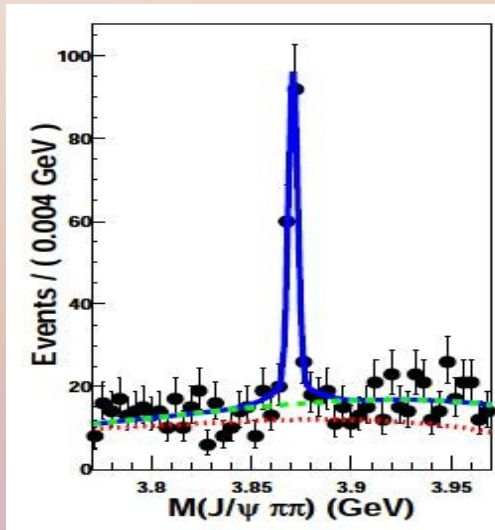
$$X(3872) \rightarrow J/\psi \pi^+ \pi^- \quad (1) \quad \text{arXiv:1107.0163}$$

Full Belle data sample:  $711 \text{ fb}^{-1}$

**Diquark-antidiquark model** predicts mass difference  $\Delta M_X$  on the X mass in the two modes

$B^+ \rightarrow K^+(J/\psi \pi^+ \pi^-)$  and  $B^0 \rightarrow K^0(J/\psi \pi^+ \pi^-)$ .

$B^+ \rightarrow K^+ X$



$B^0 \rightarrow K_S X$

[1] PRD 77 111101(R)

$$\Delta M_X = (-0.69 \pm 0.97 \pm 0.19) \text{ MeV}$$

is consistent with zero  $\Rightarrow$  **same particle**.

$$\Delta M_X = (2.7 \pm 1.6 \pm 0.4) \text{ MeV}$$



$$M_X = (3871.84 \pm 0.27 \pm 0.19) \text{ MeV} \quad \Gamma_X < 1.2 \text{ MeV (90\% CL)}$$

improve the previous  
UL on the width by a  
factor of 2

$$B(B^+ \rightarrow K^+ X) \times B(X \rightarrow J/\psi \pi^+ \pi^-) = (8.61 \pm 0.82 \pm 0.52) \times 10^{-6}$$

$$B(B^0 \rightarrow K^0 X) / B(B^+ \rightarrow K^+ X) = 0.50 \pm 0.14 \pm 0.04$$

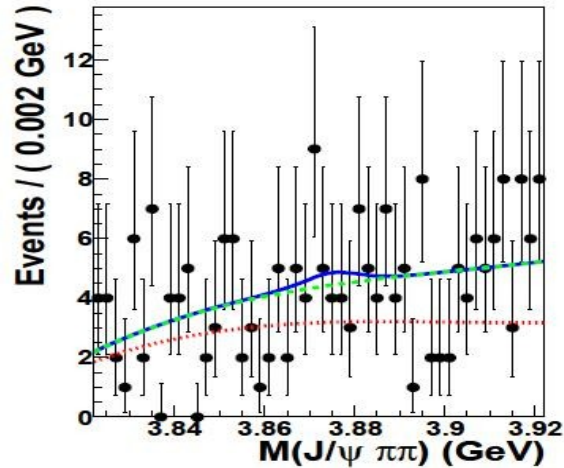
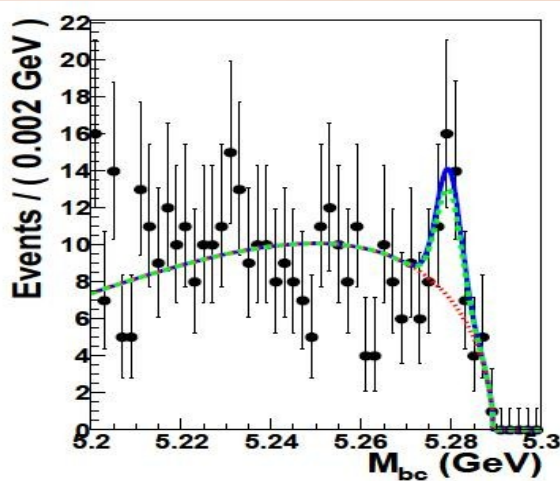
# $X(3872) \rightarrow J/\psi \pi^+ \pi^0$ (2)

Singlet or triplet?

$M_{bc}$

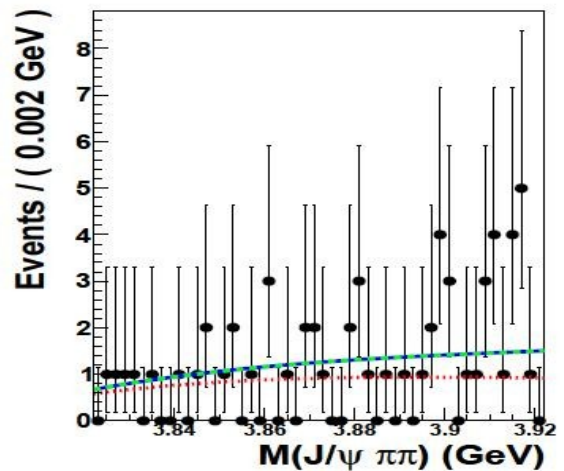
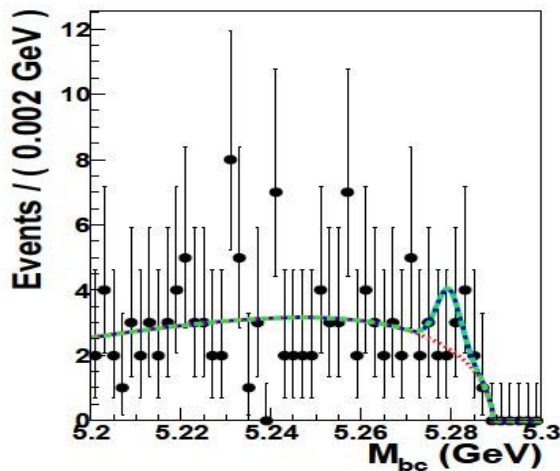
$M(J/\psi \pi \pi)$

$B^0 \rightarrow K^- X^+$



$B^+ \rightarrow K^0 X^+$

+



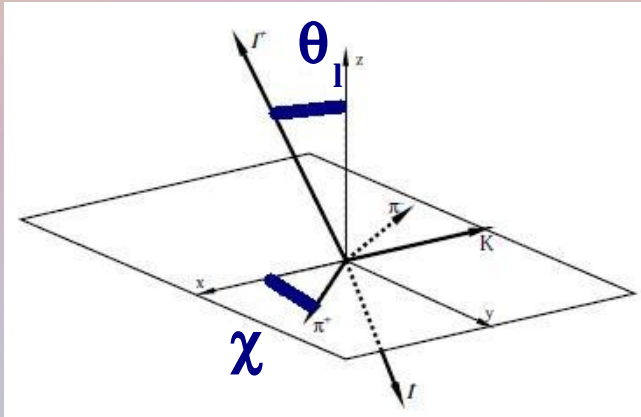
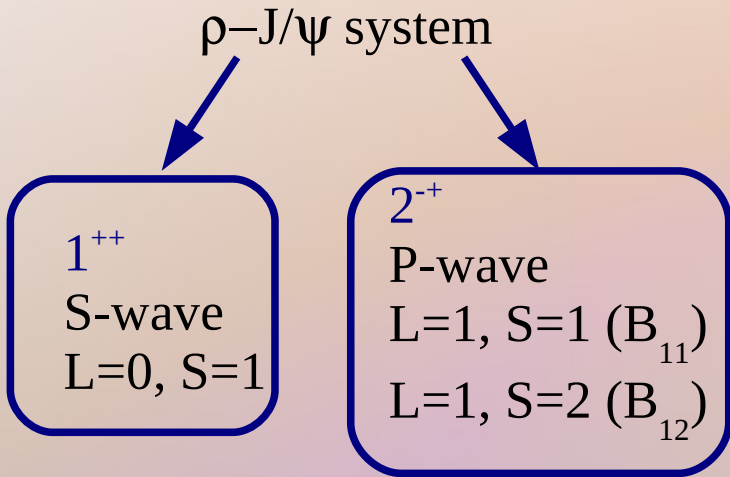
$$\mathcal{B}(B^0 \rightarrow K^- X^+) \times \mathcal{B}(X^+ \rightarrow \rho^+ J/\psi) < 4.2 \times 10^{-6}$$

No evidence of a charged partner  $X^+$

$$\mathcal{B}(B^+ \rightarrow K^0 X^+) \times \mathcal{B}(X^+ \rightarrow \rho^+ J/\psi) < 6.1 \times 10^{-6}$$

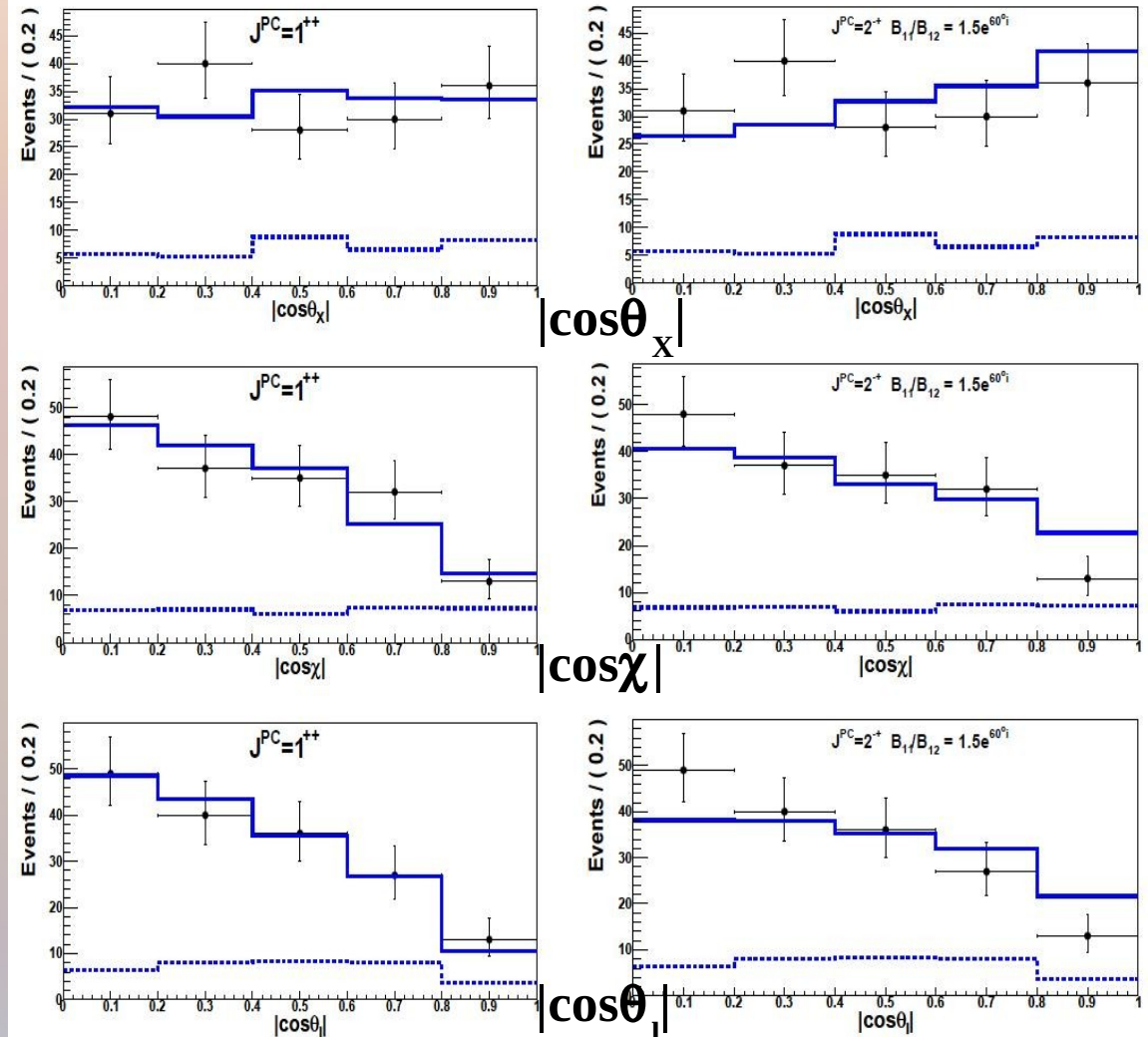
# $X(3872) \rightarrow J/\psi \pi^+ \pi^- \quad (3)$

Angular correlations  $(\theta_x^*, \chi, \theta_1) \Rightarrow 1^{++}$  and  $2^{-+}$  hypotheses are both possible  
(insufficient statistics).



$J^{PC}=1^{++}$

$J^{PC}=2^{-+} \quad B_{11}/B_{12} = 1.5e^{60^\circ i}$



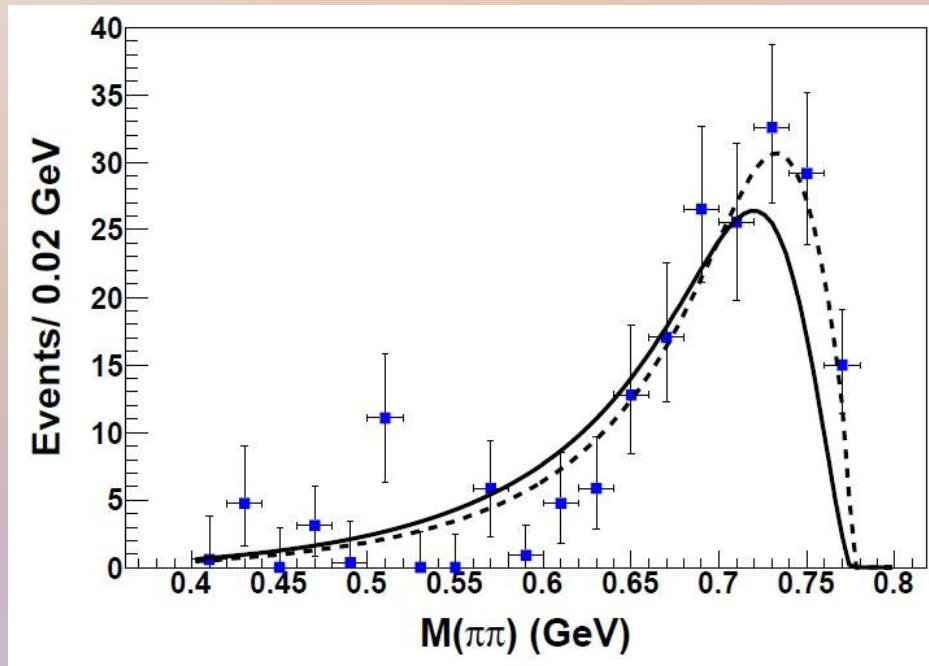
\* b/w  $J/\psi$  and direction opposite to  $K$  in  $X$  restframe

unbinned likelihood fit

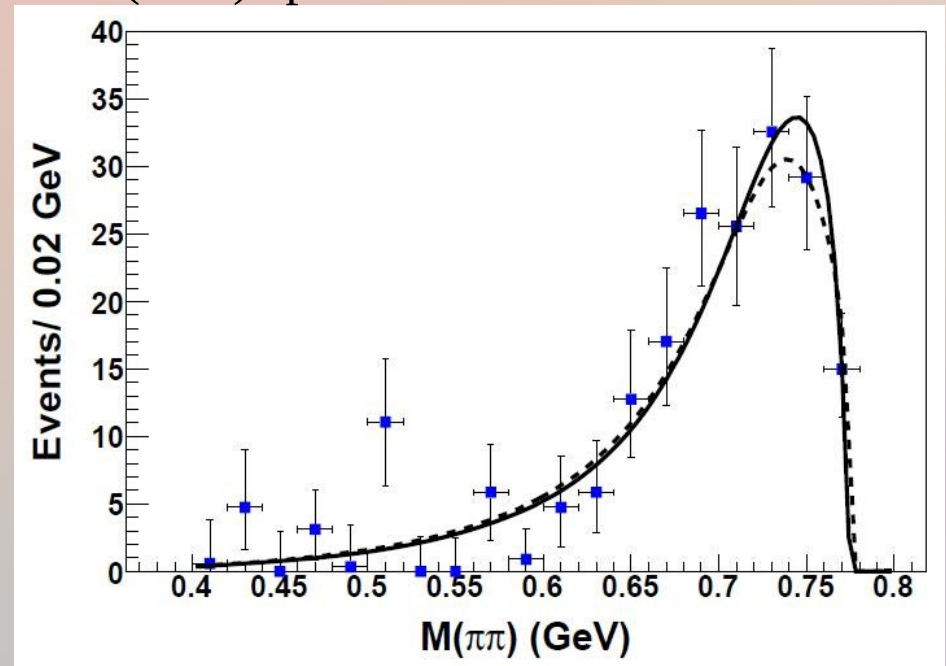
$$X(3872) \rightarrow J/\psi \pi^+ \pi^- \quad (4)$$

Fits to  $M(\pi^+\pi^-)$  distribution taking  $\rho$ - $\omega$  interference into account  
 $\Rightarrow 1^{++}$  and  $2^{-+}$  hypotheses are both possible.

Without of  $\rho$ - $\omega$  interference



With influence of  $\rho$ - $\omega$  interference in  
 $M(\pi^+\pi^-)$  spectrum



S-wave – dashed, P-wave - solid

# $X(3872) \rightarrow J/\psi(\psi')\gamma$

arXiv:1105.0177

Molecular model  $\Rightarrow X \rightarrow \psi'\gamma$  is **highly suppressed** compared to  $X \rightarrow J/\psi\gamma$ .

BaBar[1] results  $\Rightarrow \mathcal{B}(X \rightarrow \psi'\gamma)$  is **3 times larger** than  $\mathcal{B}(X \rightarrow J/\psi\gamma)$ .

Can be an indication of a (c anti-c) admixture (in addition to a  $(D^0 \text{ anti-} D^{*0})$  component).

Used statistics -  $711 \text{ fb}^{-1}$ .

$$\mathcal{B}(B^+ \rightarrow K^+ X) \times \mathcal{B}(X \rightarrow J/\psi\gamma) = (1.78_{-0.44}^{+0.48} \pm 0.12) \times 10^{-6}$$

$$\mathcal{B}(B^+ \rightarrow K^+ X) \times \mathcal{B}(X \rightarrow \psi'\gamma) < 3.45 \times 10^{-6} \text{ (90\% CL)}$$

[1] PRL 102 132001

$$\mathcal{B}(X \rightarrow \psi'\gamma) / \mathcal{B}(X \rightarrow J/\psi\gamma) < 2.1 \text{ (90\% CL)}$$

$$\mathcal{B}(X \rightarrow \psi'\gamma) / \mathcal{B}(X \rightarrow J/\psi\gamma) = 3.4 \pm 1.4$$



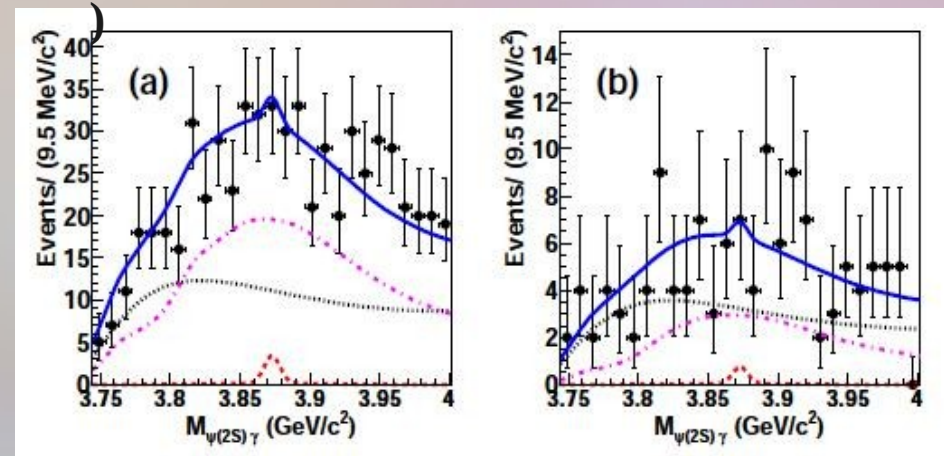
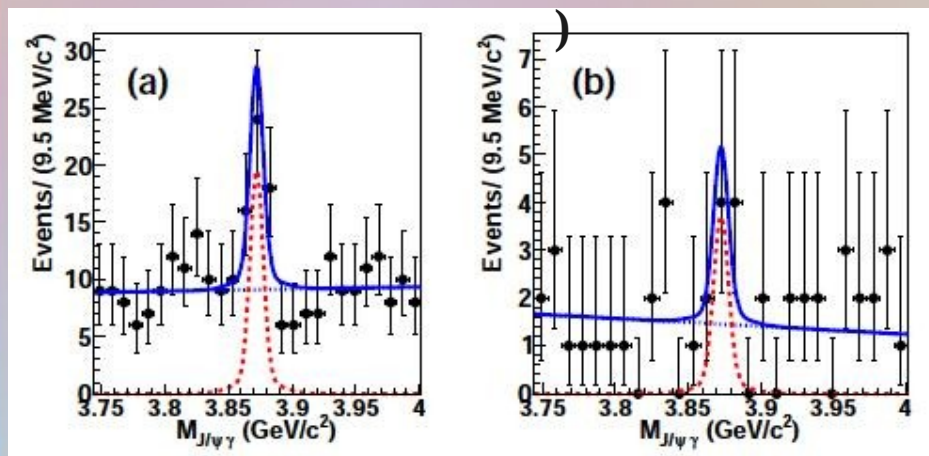
$X$  may not have a large (c anti-c) admixture with a  $(D^0 \text{ anti-} D^{*0})$  molecule.

$B^+ \rightarrow K^+ X(\rightarrow J/\psi\gamma)$

$B^0 \rightarrow K_s^0 X(\rightarrow J/\psi\gamma)$

$B^+ \rightarrow K^+ X(\rightarrow \psi'\gamma)$

$B^0 \rightarrow K_s^0 X(\rightarrow \psi'\gamma)$





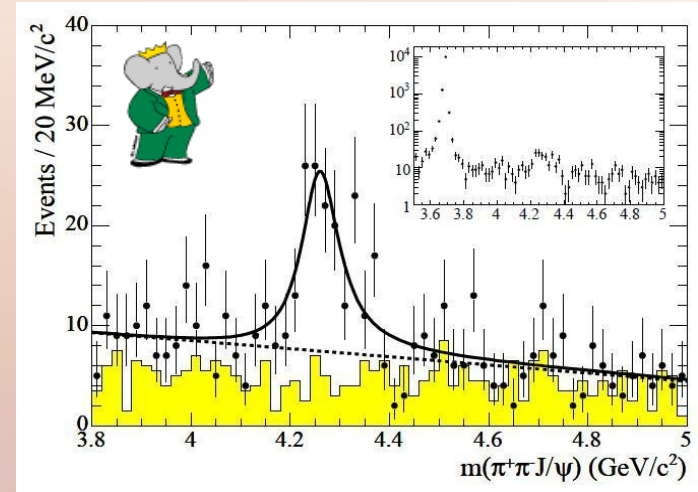
# Y(4260)

First observed by BaBar[1] in 2005 in  $e^+e^- \rightarrow (J/\psi\pi^+\pi^-)\gamma_{\text{ISR}}$ .  
Confirmed by Belle and CLEO.

Production in ISR  $\Rightarrow$  Y(4260) is a  $1^-$  state.

Family of 4 Y resonances (4008, 4260, 4360, 4660) does not fit into the charmonium spectrum.

$\psi(2S)\pi^+\pi^-$



## Possible interpretations:

- Undiscovered  $\psi$  resonances ( $3^3D_1(4560)$ ,  $5^3S_1(4760)$ ,  $4^3D_1(4810)$ )



- Hybrids - most popular model



- Hadrocharmonium
- Tetraquarks
- ( $D$  anti- $D_1$ ) or ( $D^0$  anti- $D^*$ ) molecules
- $f_0(980)\psi(2S)$  molecule for Y(4660)

## Contra:

shifted by  $\sim 300$  MeV ,  
exotic decay channels

Y(4360) and Y(4660) (higher than  $DD^{**}$  threshold) are not seen in  $e^+e^- \rightarrow$  hadrons

[1] PRL 95 142001  
[2] PRL 99 182004

# $Y(4260) \rightarrow J/\psi \pi^0 \pi^0$ (1)

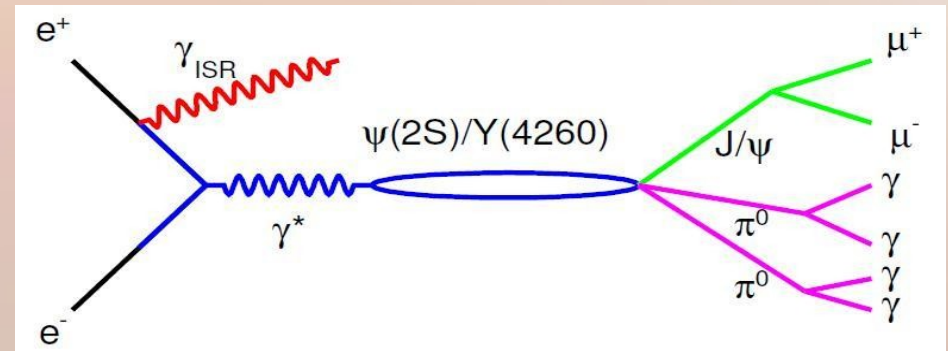
Isospin symmetry  $\Rightarrow$   $Y$  decays to  $(J/\psi \pi^0 \pi^0)$  with half the rate of  $(J/\psi \pi^+ \pi^-)$ .

Large isospin symmetry violation could be a strong evidence of the exotic nature of  $Y$ .

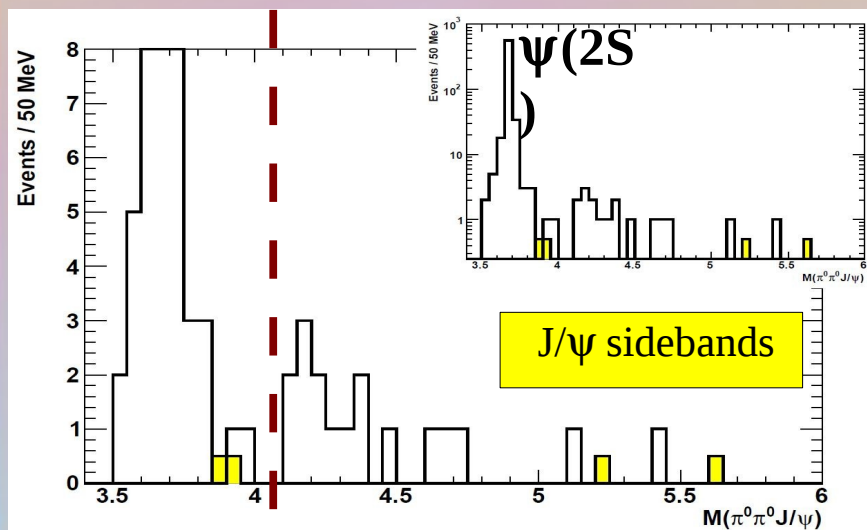
Study of cross-section  $e^+e^- \rightarrow (J/\psi \pi^0 \pi^0) \gamma_{ISR}$  as a function of mass is based on  $790 \text{ fb}^{-1}$ .

## Analysis features:

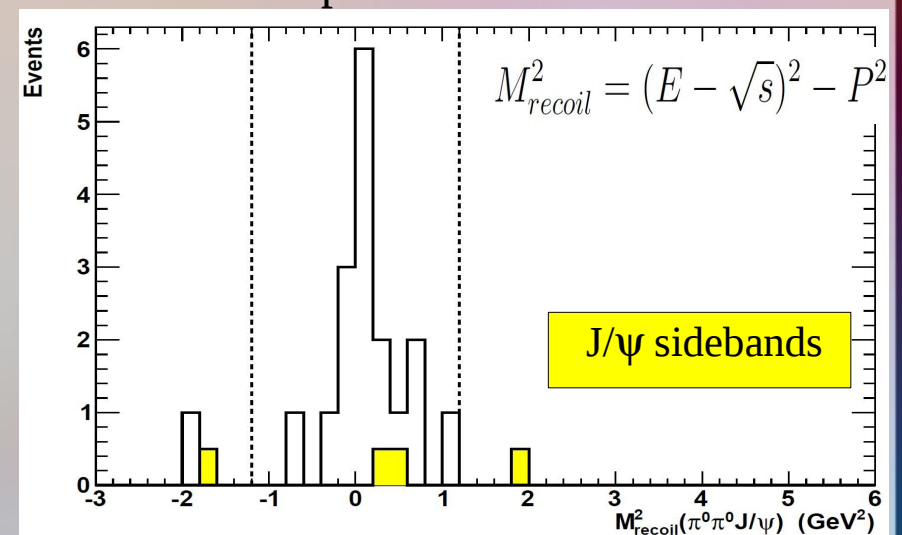
- Require  $\gamma_{ISR}$  (lower backgrounds)
- $J/\psi \rightarrow \mu^+ \mu^-$  ( $J/\psi \rightarrow e^+e^-$  is wiped out by the skim conditions)



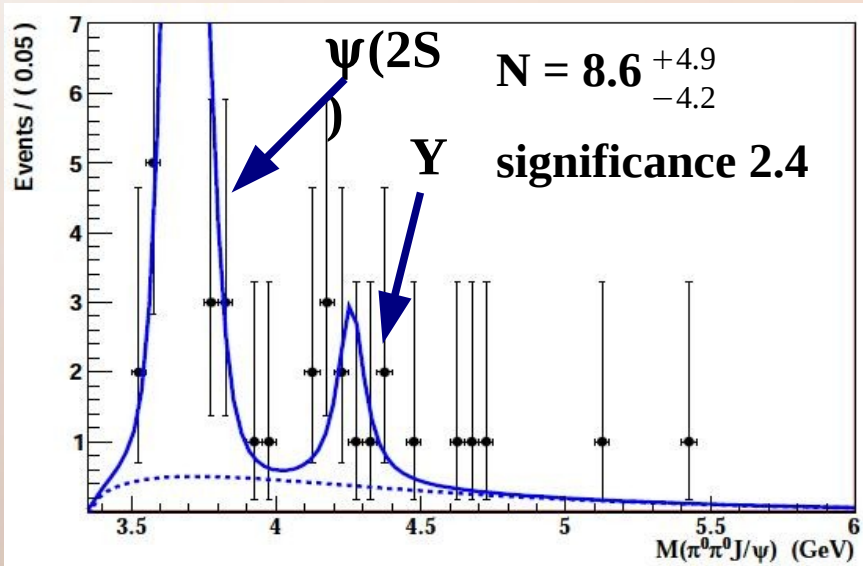
16  $J/\psi \pi^0 \pi^0$  events above 4 GeV.



$M_{recoil}^2$  distribution for events above 4 GeV is consistent with production via ISR.



# $Y(4260) \rightarrow J/\psi \pi^0 \pi^0$ (2)



$$\Gamma_{ee}(\psi(2S)) = (2.30 \pm 0.10) \text{ keV consistent with}$$

$$\Gamma_{ee}(\psi(2S)) = (2.35 \pm 0.04) \text{ keV [PDG]}$$

Y parameters are fixed from PDG.

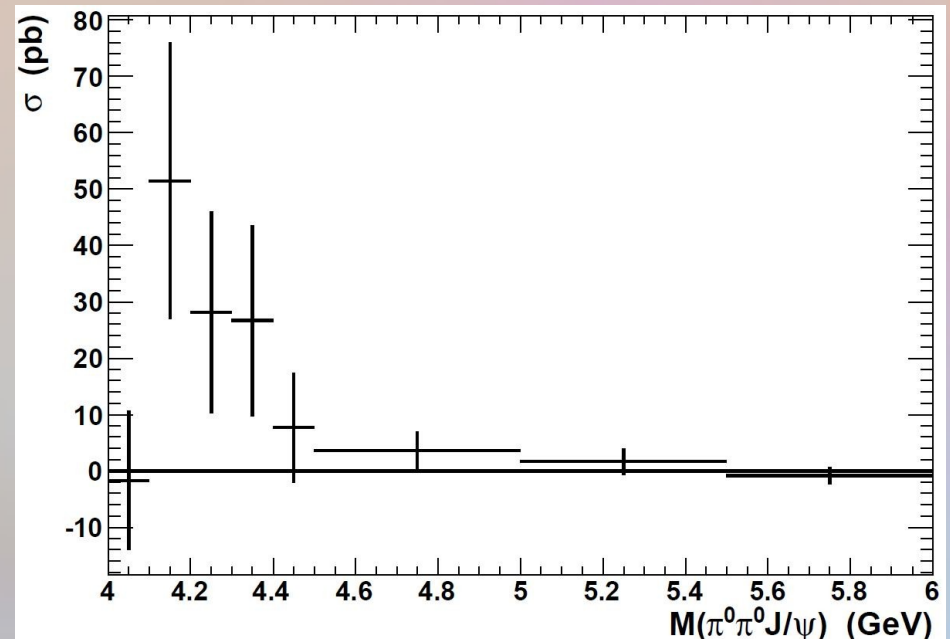
Background:  $(x - x_{\min}) \cdot e^{c(x - x_{\min})}$ ,  $x_{\min} = m_{J/\psi} - 2m_{\pi^0}$

The shape accounts for effective luminosity and efficiency as a function of mass.

$$\Gamma_{ee} \mathcal{B}(J/\psi \pi^0 \pi^0) = (3.19^{+1.82 +0.64}_{-1.53 -0.35}) \text{ eV}$$

$$\Gamma_{ee} \mathcal{B}(J/\psi \pi^+ \pi^-) = 2 \cdot (3.0^{+0.6}_{-0.5}) \text{ eV [PDG]}$$

$\Rightarrow$  consistency with the isospin expectation



$$B^\pm \rightarrow K^\pm (K_S K \pi)^0 \quad (1) \quad \text{arXiv:1105.0978}$$

A large spread of measured  $\eta_c$  and, especially,  $\eta_c(2S)$  parameters.

	<b>BaBar</b> [1][2]	<b>CLEO</b> [3]	<b>Belle</b> [4]
$M(\eta_c)$ , MeV	$2982.2 \pm 0.4 \pm 1.6$	$2981.8 \pm 1.3 \pm 1.5$	$2981.4 \pm 0.5 \pm 0.4$
$\Gamma(\eta_c)$ , MeV	$31.7 \pm 1.2 \pm 0.8$	$24.8 \pm 3.4 \pm 3.5$	$36.6 \pm 1.5 \pm 2.0$
$M(\eta_c(2S))$ , MeV	$3630.8 \pm 3.4 \pm 1.0$	$3642.9 \pm 3.1 \pm 1.5$	$3633.7 \pm 2.3 \pm 1.9$
$\Gamma(\eta_c(2S))$ , MeV	$17.0 \pm 8.3 \pm 2.5$	$6.3 \pm 12.4 \pm 4.0$	$19.1 \pm 6.9 \pm 6.0$

[1] PRD 81 052010

[2] PRL 92 142002

[3] PRL 92 142001

[4] NPPS 184 220

$B^\pm \rightarrow K^\pm (K_S K \pi)^0$  with the (c anti-c) formation from

$(K_S K \pi)^0$  - **signal**

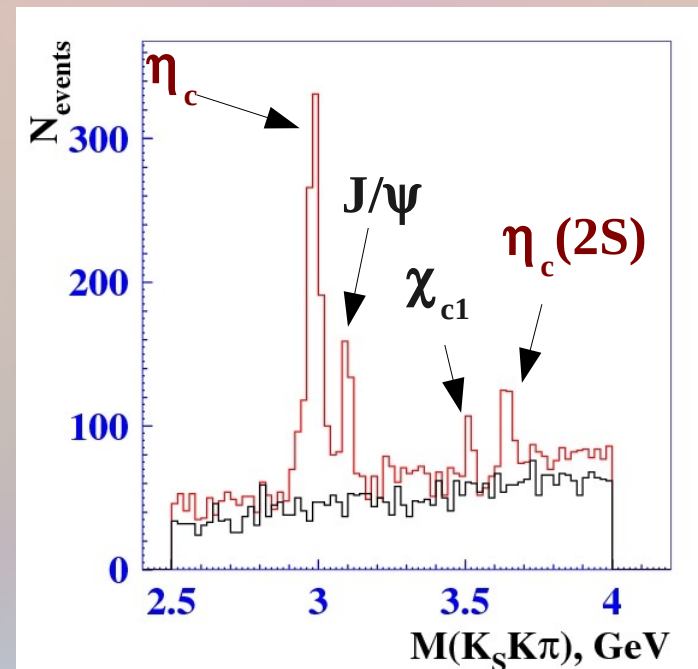
$B^\pm \rightarrow K^\pm (K_S K \pi)^0$  without the (c anti-c) formation –

**non-resonant component**

Same final state  $\Rightarrow$  **interference is inevitable!**

Gives large model uncertainty (>50% for signal yield)

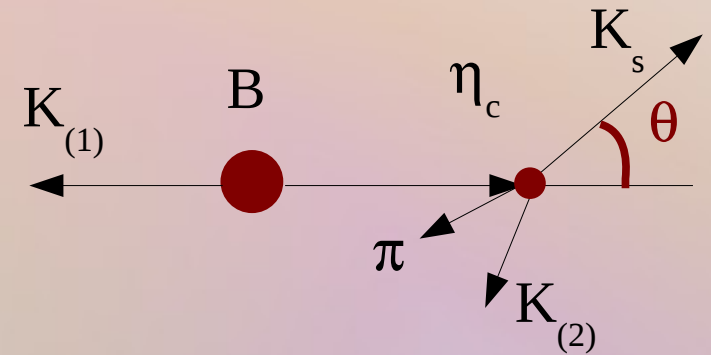
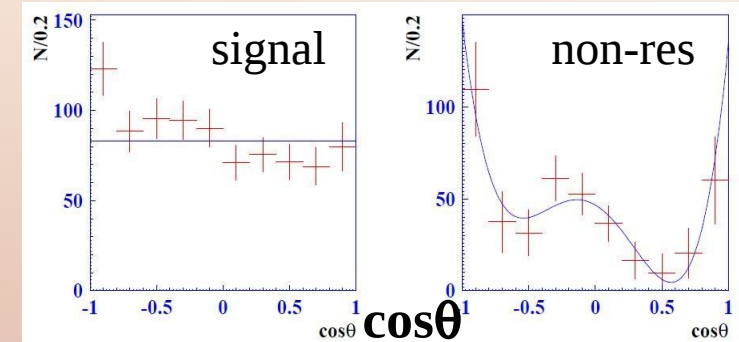
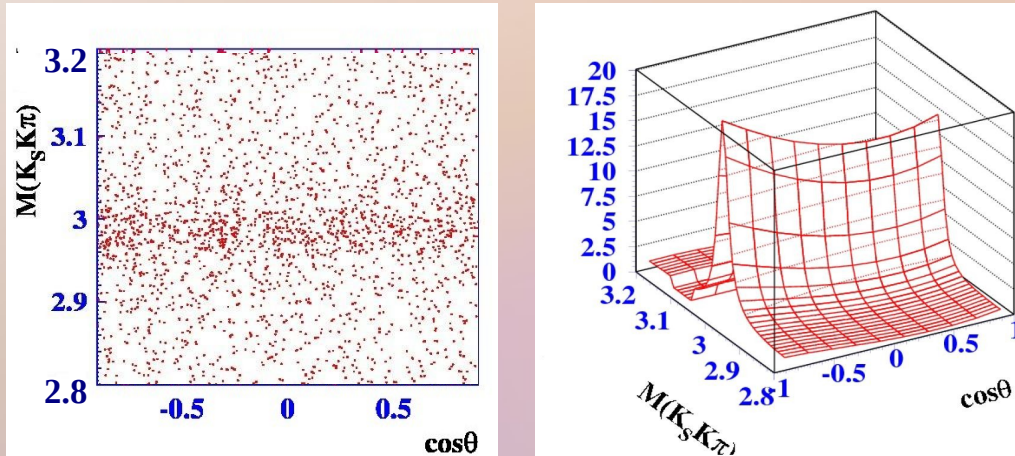
$\Rightarrow$  should be taken into account.



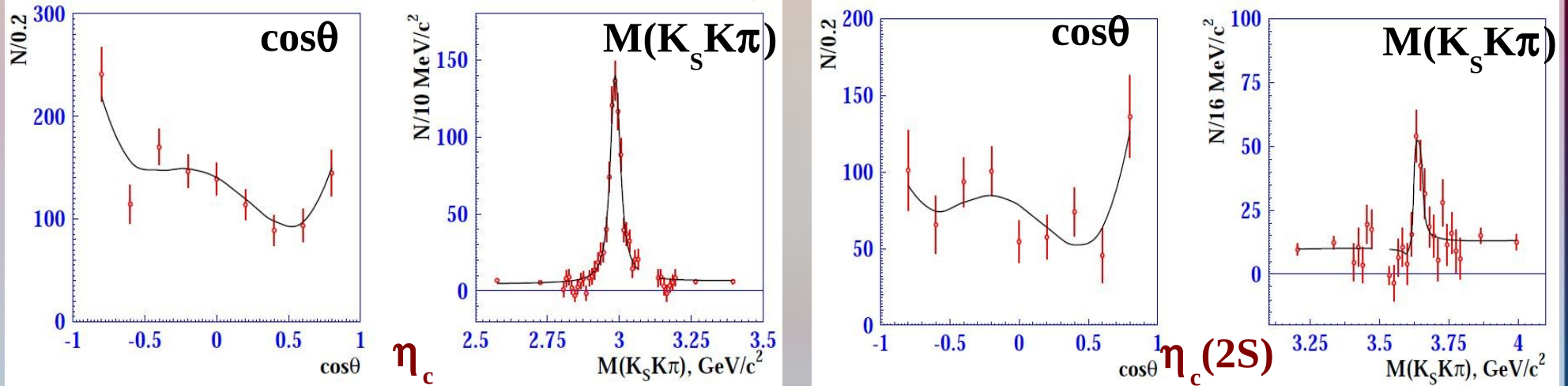
$$B^\pm \rightarrow K^\pm (K_S K \pi)^0 \quad (2)$$

$M(K_S K \pi)$  and  $\cos\theta$  distributions are used to distinguish signal and non-resonant components.

2D fit:



Projections:



$$B^{\pm} \rightarrow K^{\pm} (K_S K \pi)^0 \quad (3)$$

$B^{\pm} \rightarrow K^{\pm} \eta_c, \eta_c \rightarrow (K_S K \pi)^0$	
$\mathcal{B} \times \mathcal{B}, 10^{-6}$	$26.7 \pm 1.4(\text{stat})^{+2.9}_{-2.6}(\text{syst}) \pm 4.9(\text{model})$
$M(\eta_c), \text{MeV}$	$2985.4 \pm 1.5(\text{stat})^{+0.2}_{-2.0}(\text{syst})$
$\Gamma(\eta_c), \text{MeV}$	$35.1 \pm 3.1(\text{stat})^{+1.0}_{-1.6}(\text{syst})$
$B^{\pm} \rightarrow K^{\pm} \eta_c(2S), \eta_c(2S) \rightarrow (K_S K \pi)^0$	
$\mathcal{B} \times \mathcal{B}, 10^{-6}$	$3.4^{+2.2}_{-1.5}(\text{stat+model})^{+0.5}_{-0.4}(\text{syst})$
$M(\eta_c(2S)), \text{MeV}$	$3636.1^{+3.9}_{-4.2}(\text{stat+model})^{+0.5}_{-2.0}(\text{syst})$
$\Gamma(\eta_c(2S)), \text{MeV}$	$6.6^{+8.4}_{-5.1}(\text{stat+model})^{+2.6}_{-0.9}(\text{syst})$

Some of the parameters of the 2D fitting function are dependent  $\Rightarrow$  model error.

**The procedure of taking the interference into account:**

- no assumptions about the phase or absolute value of the interference
- significant decrease of model error for  $\mathcal{B}$
- comparable errors (despite the additional model error)

Results are consistent with those obtained in the most accurate measurements.

# Conclusion

- New measurements of X(3872) parameters. UL on the width is significantly reduced.
- A difference in X(3872) masses produced via decays  $B^+ \rightarrow K^+(J/\psi\pi^+\pi^-)$  and  $B^0 \rightarrow K^0(J/\psi\pi^+\pi^-)$  is consistent with zero, which does not corroborate diquark-antidiquark model.
- Study of angular correlations and  $M(\pi^+\pi^-)$  spectrum in  $B^+ \rightarrow K^+(J/\psi\pi^+\pi^-) \Rightarrow$  both  $1^{++}$  or  $2^+$  hypotheses for X(3872) are possible (more statistics is needed).
- No evidence of  $X(3872) \rightarrow \psi'\gamma \Rightarrow$  hypothesis of large (c anti-c) admixture in the X(3872) is not confirmed.
- The value of  $\mathcal{B}(Y(4260) \rightarrow J/\psi\pi^0\pi^0)$  is consistent with the expectation from isospin.
- Parameters of  $\eta_c$  and  $\eta_c(2S)$  have been measured taking into account the interference between signal and non-resonant component.
- B-factories discovered a large number of new charmonium-like states and launched a new era of spectroscopy. Despite the large amount of data that was accumulated, statistics are still insufficient to resolve all the puzzles of exotic states. New Super B-factories are needed!

Backup slides



# $X(3872) \rightarrow J/\psi \pi^+ \pi^-$

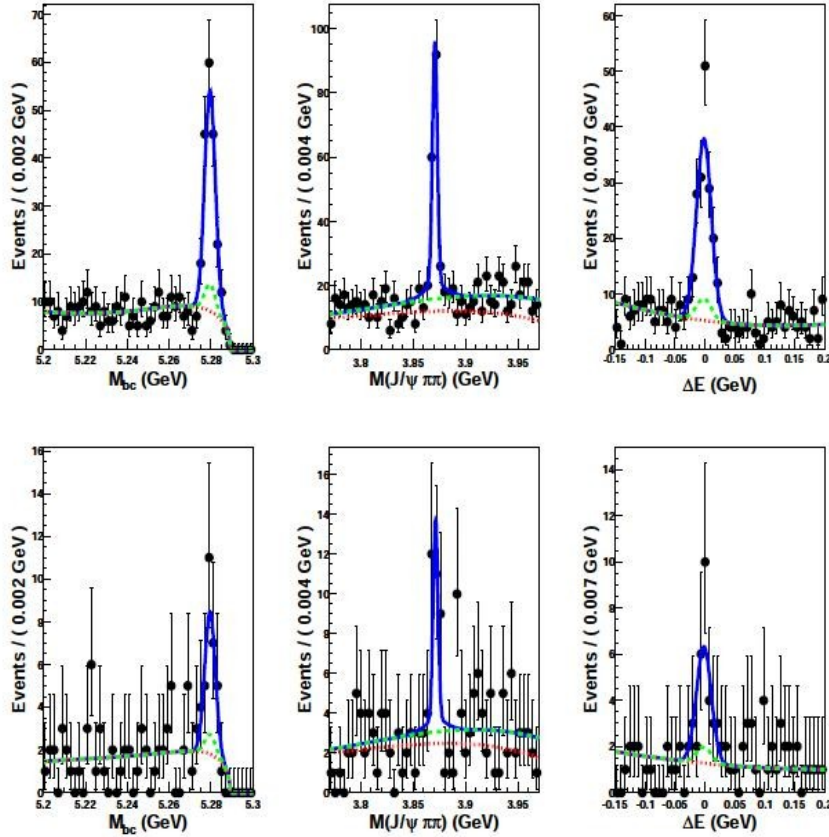


FIG. 2: The  $M_{bc}$  (left),  $M(\pi^+ \pi^- J/\psi)$  (center) and  $\Delta E$  (right) distributions for  $B^+ \rightarrow K^+ X(3872)$  (top) and  $B^0 \rightarrow K_S X(3872)$  (bottom) event candidates within the signal regions of the other two quantities. The curves show the results of the fit described in the text.

TABLE IV: Systematic errors on the mass measurement.

Source	Systematic error (MeV)
$m_{J/\psi}$	0.01
$m_{\psi'}$	0.04
Bias correction	0.16
3-dim. fit model	0.03
MC model dependence	0.09
Quadrature sum	0.19

TABLE V: Systematic errors on the product branching fraction measurement.

Source	$K^+ X(3872)$ (percent)	$K_S X(3872)$ (percent)	$K_S/K^+$ Ratio (percent)
$N_{BB}$	1.4	1.4	-
Secondary BF	1.0	1.0	-
MC statistics	1.0	1.0	1.4
MC model	2.1	2.1	-
Hadron ID	3.7	2.6	1.1
Lepton ID	1.1	1.1	-
Tracking	1.8	1.4	0.4
3-dim. fit model	3.0	5.0	6.0
$K_S$ efficiency	-	4.5	4.5
Quadrature sum	6.0	8.1	7.7

$$\frac{d\Gamma}{d\Omega} = \sum_j \left| \sum_{\lambda_{J/\psi} \lambda_\rho} A_{\lambda_{J/\psi} \lambda_\rho}^{JPC} D_{\lambda_{J/\psi} j}^1(\phi_{J/\psi}, \theta_{J/\psi}) D_{-\lambda_\rho 0}^1(\phi_\rho, \theta_\rho) D_{0(\lambda_{J/\psi} - \lambda_\rho)}^{JX}(\phi_X, \theta_X) \right|^2$$

# $X(3872) \rightarrow J/\psi \pi^+ \pi^-$

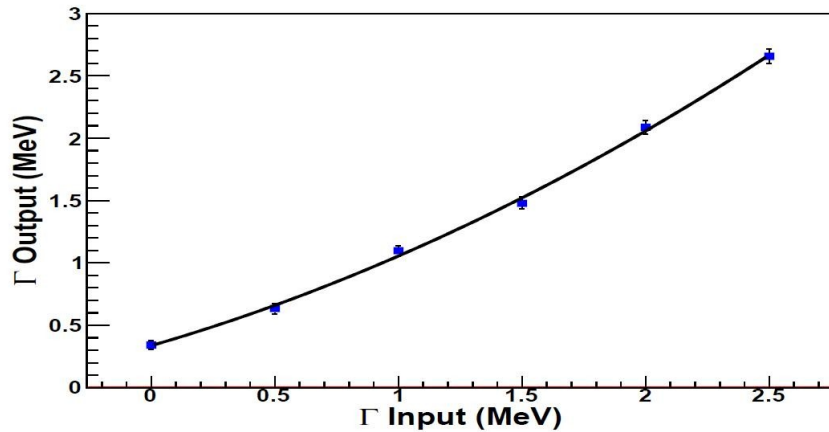


FIG. 3: Fitted values for  $\Gamma_{X(3872)}$  (vertical) versus the MC generator input values (horizontal). The curve is the result of a fit to a second-order polynomial.

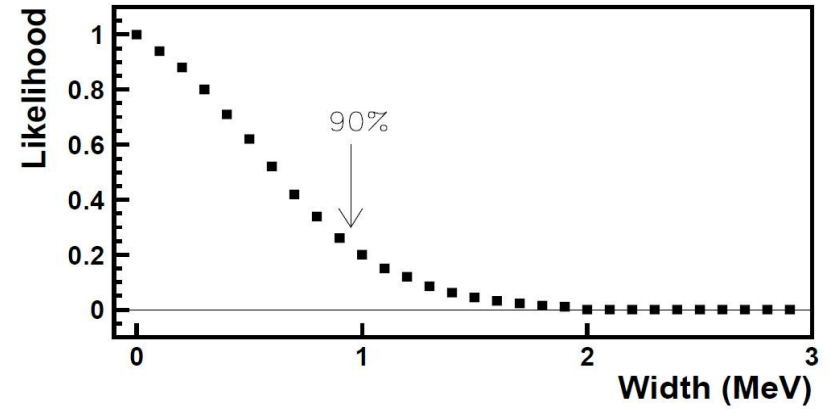


FIG. 4: Likelihood values from the  $\Gamma_{X(3872)}$  scan described in the text. The region of the plot below the arrow contains 90% of the total area under the points.

	$N_{sig}$	$r_\omega$	$N_{\rho \rightarrow \pi\pi}$	$N_{\omega \rightarrow \pi\pi}$	$N_{\rho-\omega \text{ interf}}$
<i>S</i> -wave	$159 \pm 15$	$0.07 \pm 0.05$	140.9	$0.6 \pm 0.5$	17.8
<i>P</i> -wave	$158 \pm 15$	$0.48^{+0.20}_{-0.14}$	93.2	$3.6^{+1.5}_{-1.1}$	60.0

# $X(3872) \rightarrow J/\psi(\psi')\gamma$

Evidence of  $B \rightarrow K\chi_{c2}$ :  $\mathcal{B}(B^+ \rightarrow K^+\chi_{c2}) / \mathcal{B}(B^+ \rightarrow K^+\chi_{c1}) = (2.25^{+0.73}_{-0.69} \pm 0.17) \times 10^{-2}$   
 more suppressed than expected in theory[2]

[2] NPB 811 155

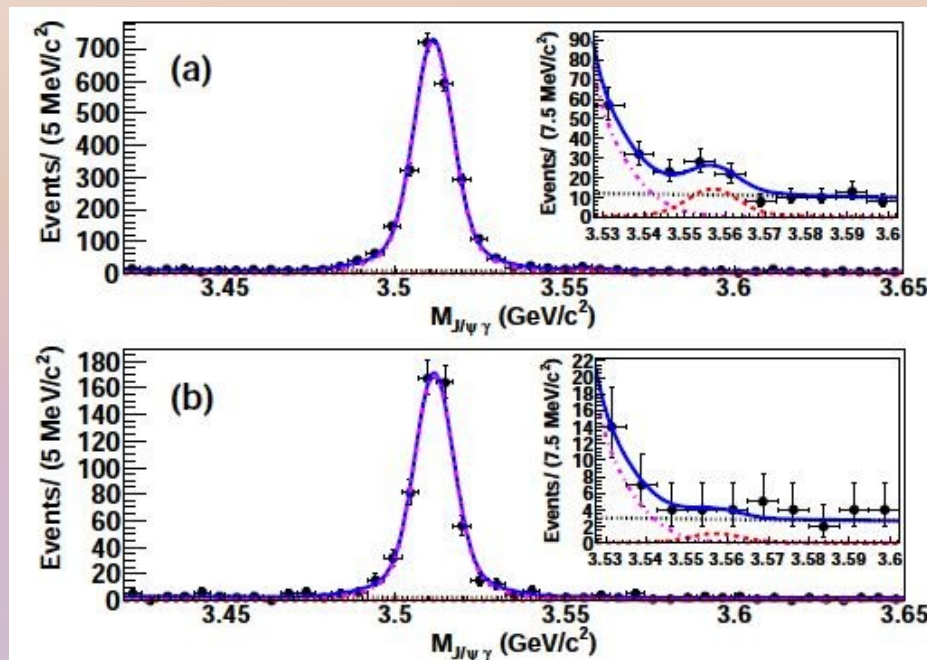


FIG. 1:  $M_{J/\psi\gamma}$  distributions for (a)  $B^+ \rightarrow \chi_{c1,c2}(\rightarrow J/\psi\gamma)K^+$  and (b)  $B^0 \rightarrow \chi_{c1,c2}(\rightarrow J/\psi\gamma)K_S^0$  decays. The curves show the signal (pink dot-dashed for  $\chi_{c1}$  and red dashed for  $\chi_{c2}$ ), and the background component (black dotted) as well as the overall fit (blue solid). The insets show a reduced range of  $M_{J/\psi\gamma}$  and the contribution of the  $B \rightarrow \chi_{c2}K$  peak.

# $Y(4260) \rightarrow J/\psi \pi^0 \pi^0$

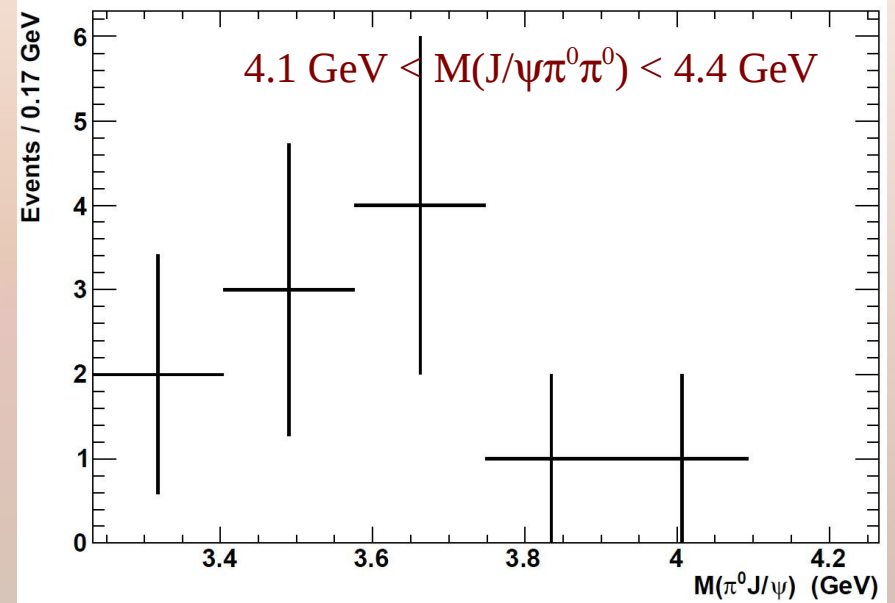
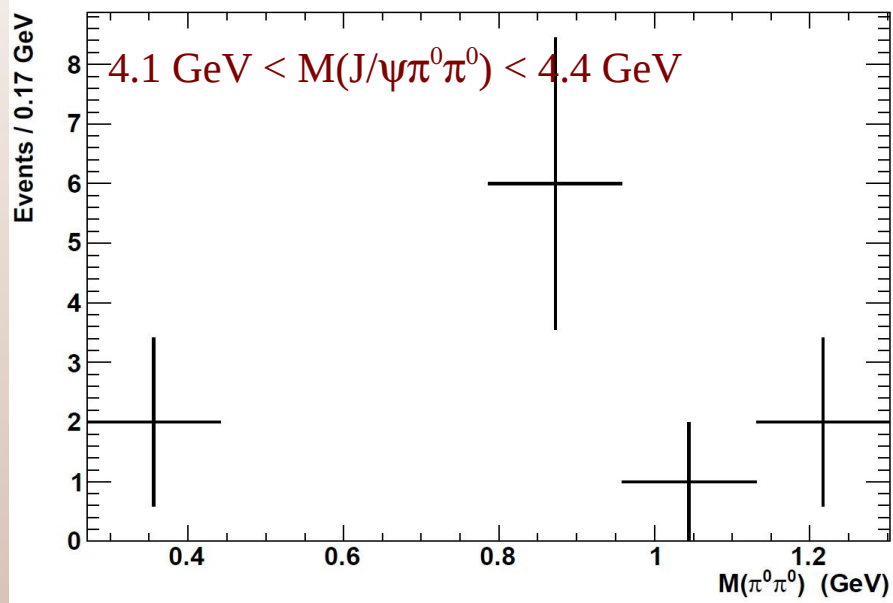


Table 1: Summary of systematic uncertainties.

Source	Error on yield (%)	
Luminosity	$\pm 1.4$	
Branching Fractions	$\pm 1.0$	
MuID	$\pm 2.7$	
Tracking	$\pm 2.0$	
Trigger	$\pm 2.8$	
Cut selection	+3.2	-2.8
$Y(4260)$ mass and width	+5.5	-5.7
Choice of fit function	+18.3	-7.8
Sum in quadrature	+20	-11

Table 2: Results of fit to  $M(\pi^0 \pi^0 J/\psi)$  spectrum. The non-resonant contribution is fit using a falling exponential with threshold function.

Parameter	Value	Positive error	Negative error	Units
$\Gamma_{e^+e^-} \cdot \mathcal{B}(Y(4260) \rightarrow \pi^0 \pi^0 J/\psi)$	3.19	+1.82	-1.53	eV
$N(\psi(2S))$	629	+26	-25	
$\psi(2S)$ mean	3.6842	+0.0005	-0.0005	GeV
$N(1\gamma_{bkg})/N(\psi(2S))$	23	+4	-4	%
$N(> 1\gamma_{bkg})/N(\psi(2S))$	3.6	+3.5	-3.4	%
$N(\text{non-resonant})$	14	+8	-7	
Non-resonant shape parameter	-1.4	+0.7	-0.6	

# $Y(4260) \rightarrow J/\psi \pi^0 \pi^0$

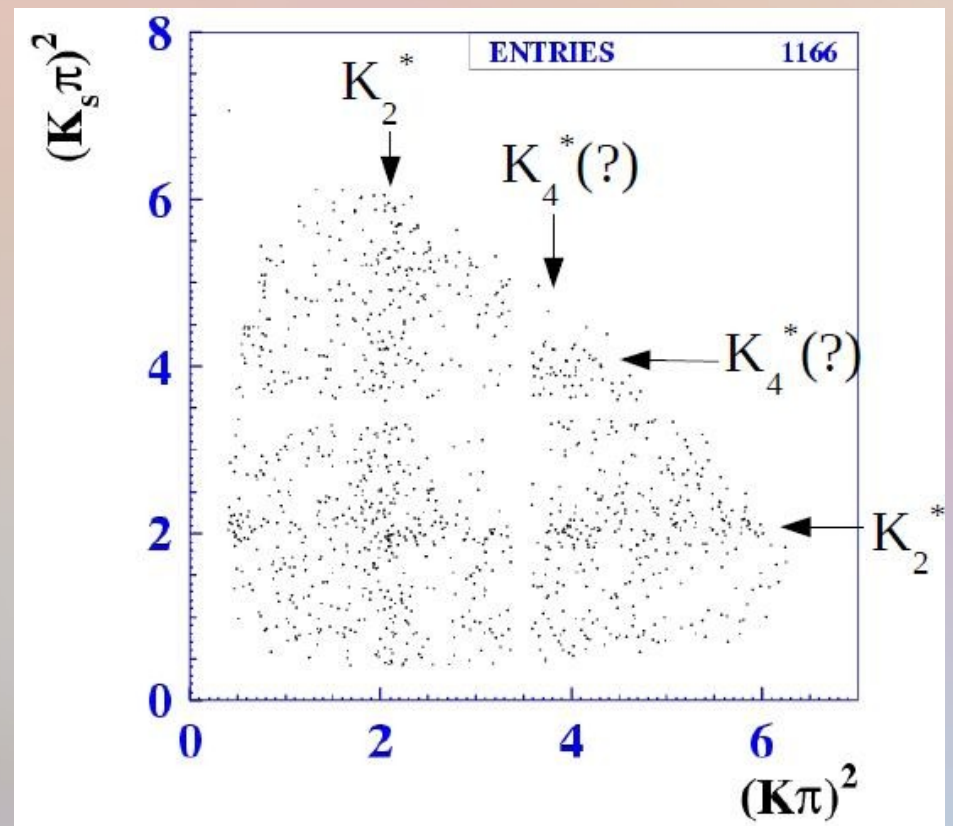
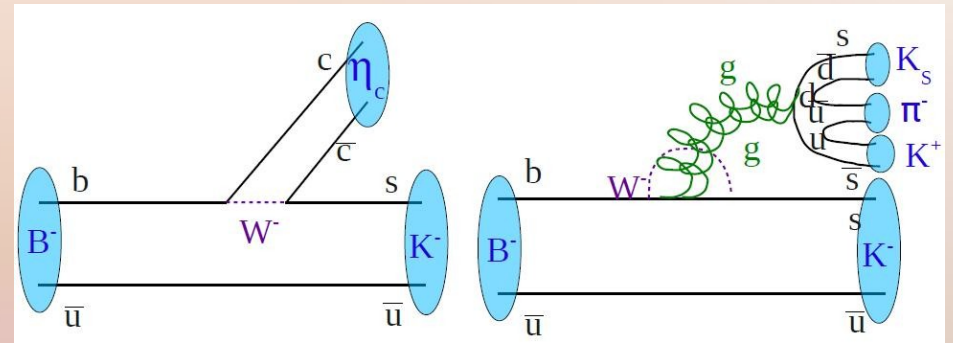
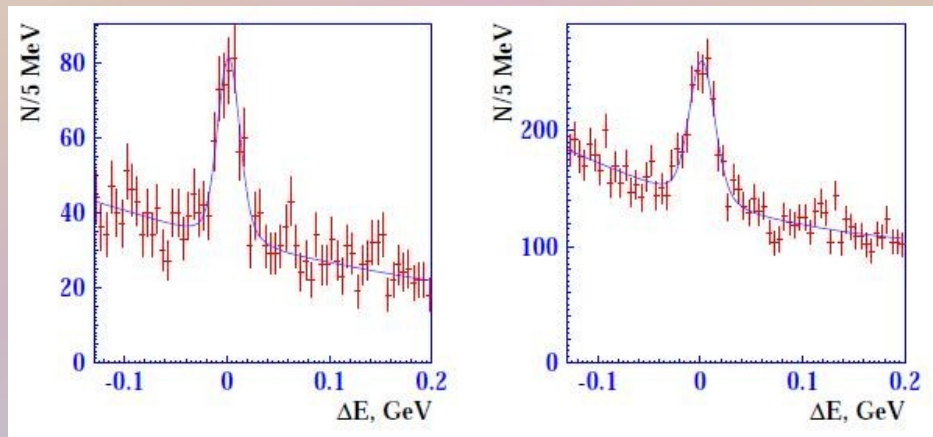
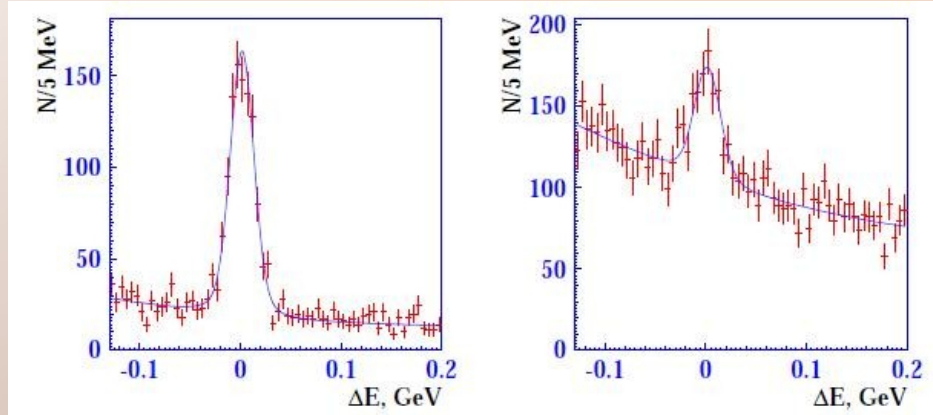
Cuts:

- Events with only two tracks passing track quality cuts
- MuID: One-hard, one-loose selection – require one track with MuID  $> 0.9$ , no MuID cut on other track.  
However if the second tracks has MuID equal to zero: require the track to be in the detector forward of  $\cos(\theta) > -0.85$
- $|M(\mu\mu) - m_{J/\psi}| < 25 \text{ MeV}$  ( $m_{J/\psi}$  is PDG mass)
- $E(\gamma) > 35 \text{ MeV}$ , quite low by Belle standards, with four  $\pi^0$  photons in each event, the smallest energy photon distribution goes to quite low energies
- $|M(\gamma\gamma) - m_{\pi^0}| < 15 \text{ MeV}$  ( $m_{\pi^0}$  is PDG mass)
- $P_{\perp}(\pi^0 \pi^0 J/\psi) \text{ w.r.t. } \gamma_{ISR} < 0.05 \text{ GeV}$ , we require our candidate have the opposite the direction of the ISR photon.
- $|M_{recoil}^2| < 1.2 \text{ GeV}^2$

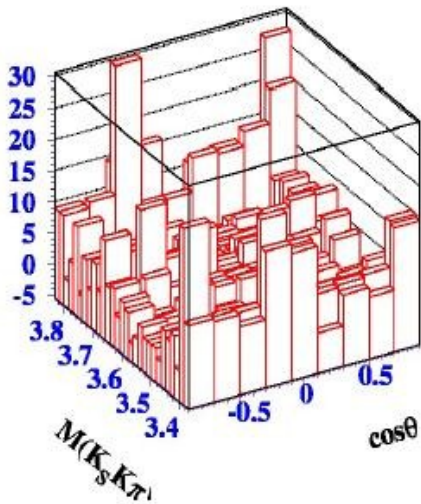
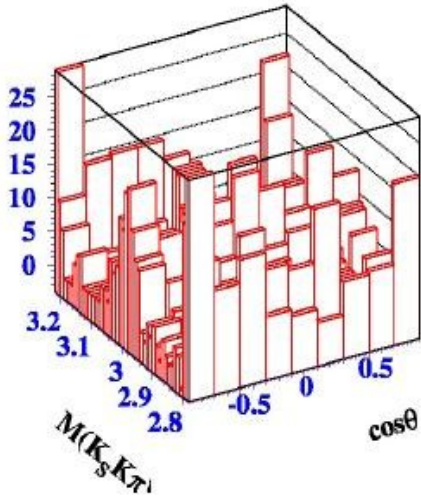
Multiple  $\pi^0$  candidates, for a best candidate selection we minimise the sum of the absolute value of the two  $\pi^0$  decay angles:

$$|\cos(\theta_{\gamma})| = \left| \frac{E(\pi^0)}{P(\pi^0)} \cdot \frac{E(\gamma_1) - E(\gamma_2)}{E(\gamma_1) + E(\gamma_2)} \right|.$$

$$B^{\pm} \rightarrow K^{\pm} (K_S K \pi)^0$$



# $B^\pm \rightarrow K^\pm (K_S K \pi)^0$

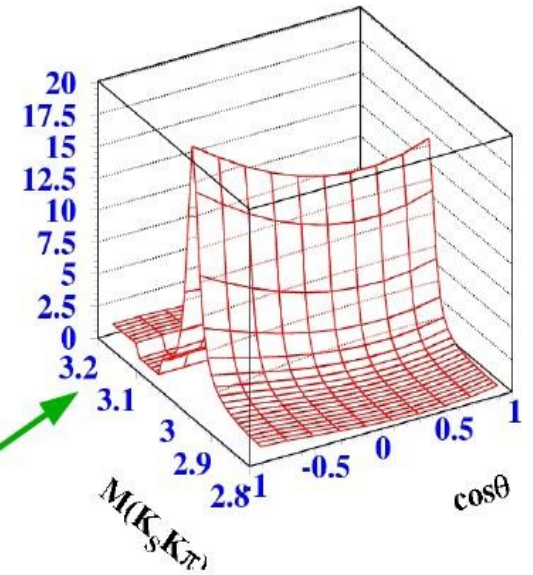


efficiency correction

$$F = (1 + \epsilon_1 x + \epsilon_2 x^2) \cdot \int \left| \underbrace{\left( \frac{\sqrt{N}}{s - M^2 + iM\Gamma} A_\eta(q_1, q_2) + \alpha A_S(q_1, q_2) \right)}_{\eta_c \text{ S-wave signal}} + \underbrace{\beta A_P(q_1, q_2)}_{\text{P-wave non-res}} + \underbrace{\gamma A_D(q_1, q_2)}_{\text{D-wave non-res}} \right|^2 dq_1^2 dq_2^2 d\phi$$

S-wave non-res      P-wave non-res      D-wave non-res

- $x \equiv \cos\theta$
- $s \equiv M(K_S K \pi)$
- $S = \frac{1}{\sqrt{2}}$ ,  $P = \sqrt{\frac{3}{2}} x$ ,  $D = \frac{3}{2} \sqrt{\frac{5}{2}} (x^2 - 1/3)$
- $\int |A_{\eta, S, P, D}(q_1, q_2)|^2 dq_1^2 dq_2^2 d\phi = 1$

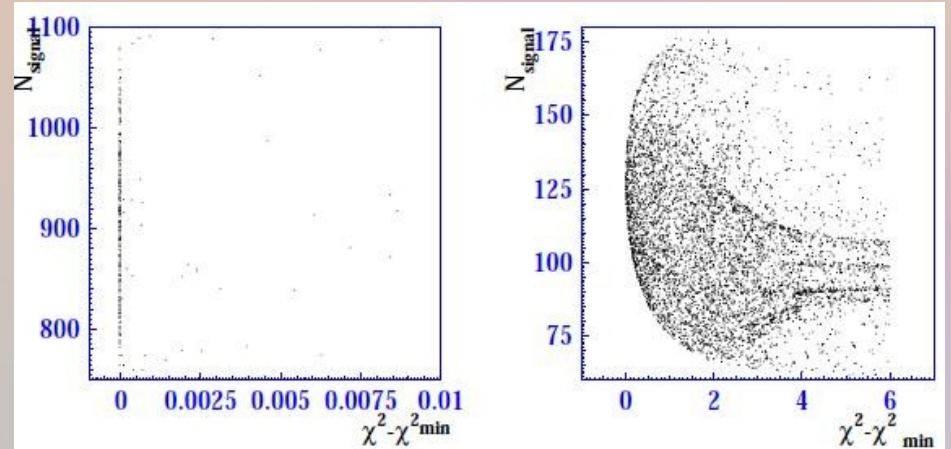


$\eta_c$  region:  $J/\psi$  veto  
 $\eta_c(2S)$  region:  $\chi_{c1}$  veto

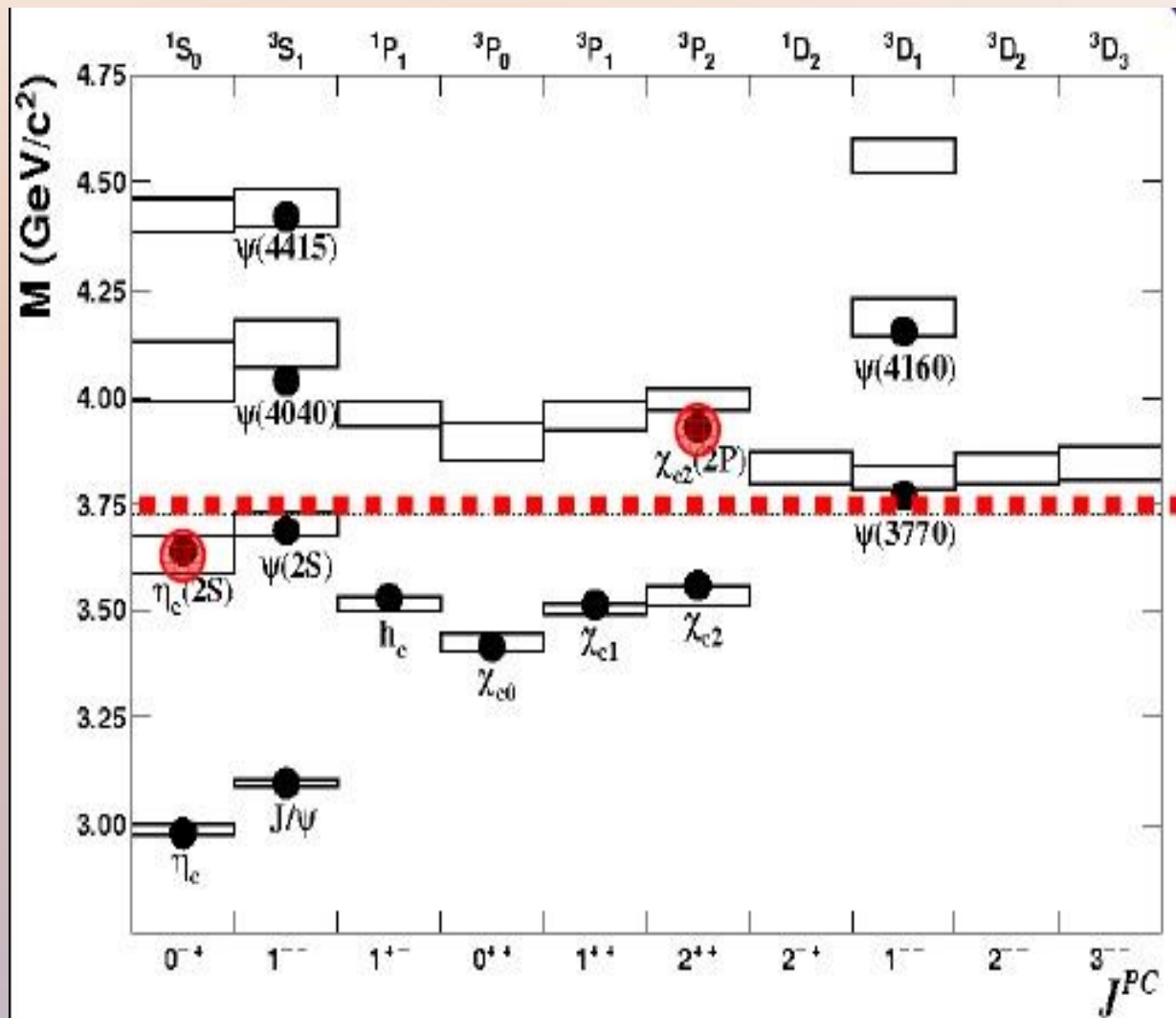
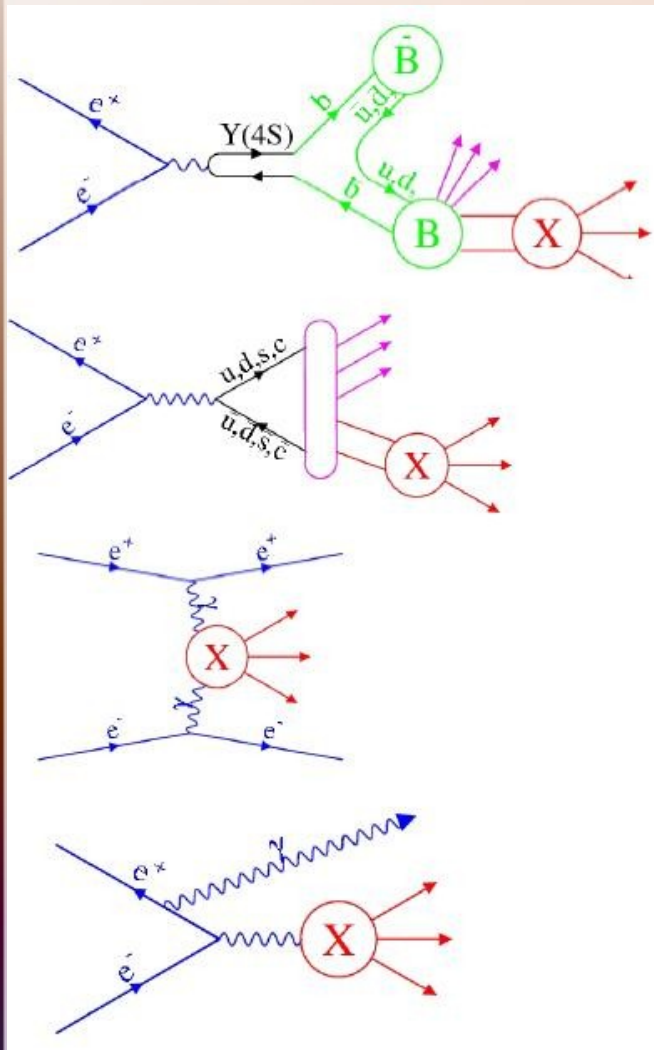
$$B^{\pm} \rightarrow K^{\pm} (K_S K \pi)^0$$

Source	$B^{\pm} \rightarrow K^{\pm} (K_S K \pi)^0$	
	$\eta_c$	$\eta_c(2S)$
Number of $B\bar{B}$ pairs	1.3	1.3
$\mathcal{B}(K_S \rightarrow \pi^+ \pi^-)$	0.1	0.1
Model efficiency dependence	+8.6 -6.7	+2.0 -1.5
Background approximation	—	+2.3
Bin size	-3.3	+13.3 -3.9
$\Delta E$ cut	-2.2	+2.3
Detector resolution	+1.1	+4.7 -8.6
$M_{inv}$ efficiency dependence	+2.2	+0.8
Track reconstruction	3	3
$K^{\pm}$ identification	1.6	1.6
$\pi^{\pm}$ identification	1.5	1.5
$K_S$ reconstruction	4.4	4.4
Total, %	+10.7 -9.8	+15.8 -11.9

Source	$\eta_c$		$\eta_c(2S)$	
	Mass	Width	Mass	Width
Background approximation	—	—	+0.2	-0.1
Bin size	+0.2	-1.0	-1.1	+2.4
Detector resolution	-0.1	+1.0 -1.2	+0.5 -0.1	+1.8 -0.9
Scale uncertainty	-2.0	—	-1.7	—
Total, $\text{MeV}/c^2$	+0.2 -2.0	+1.0 -1.6	+0.5 -2.0	+2.6 -0.9

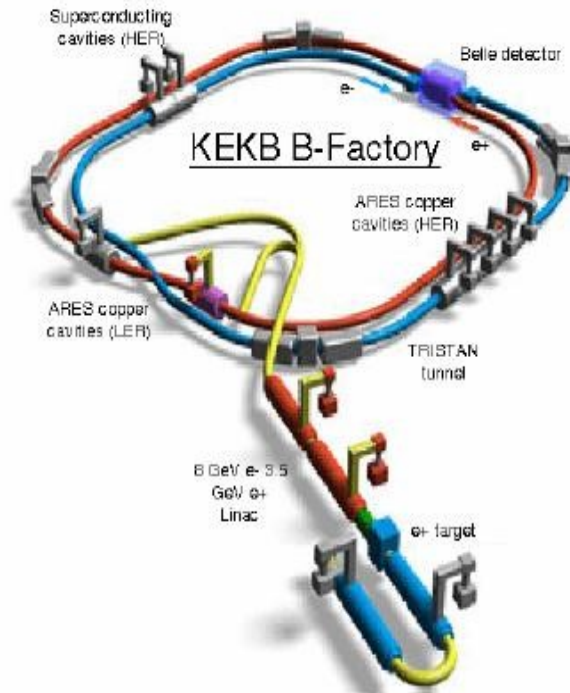
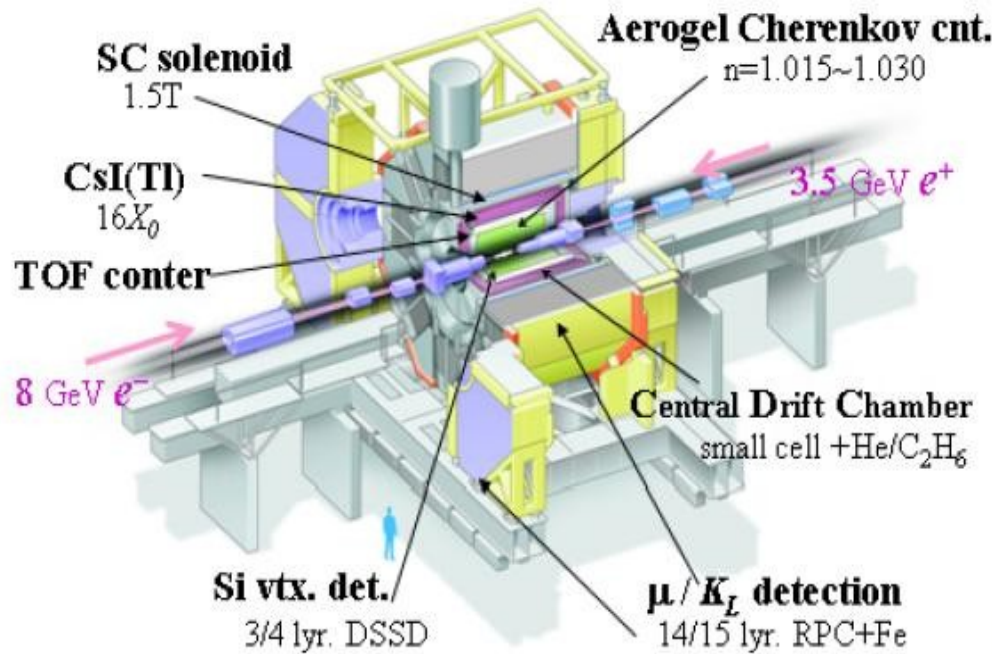






State	M (MeV)	$\Gamma$ (MeV)	$J^{PC}$	Process (mode)	Experiment
<b>B-decays</b>					
$\eta_c(2S)$	$3637 \pm 4$	$14 \pm 7$	$0^{-+}$	$K(K_S^0 K^- \pi^+)$	Belle(2002), BaBar, CLEO
X(3872)	$3871.52 \pm 0.20$	$1.3 \pm 0.6$	$1^{++}$	$K(\pi^+ \pi^- J/\psi)$ $K(D^{*0} \bar{D}^0), \dots$	Belle(2003), BaBar, CDF, D0
Y(3940)	$3915.7 \pm 4.2$	$41 \pm 12$	$0/2^{?+}$	$K(\omega J/\psi)$	Belle(2004), BaBar
$Z_1(4050)^+$	$4051^{+24}_{-43}$	$82^{+51}_{-55}$	?	$K(\pi^+ \chi_{c1}(1P))$	Belle (2008)
$Z_2(4250)^+$	$4248^{+185}_{-45}$	$177^{+321}_{-72}$	?	$K(\pi^+ \chi_{c1}(1P))$	Belle (2008)
$Z(4430)^+$	$4443^{+24}_{-18}$	$107^{+113}_{-71}$	?	$K(\pi^+ \psi(2S))$	Belle (2007)
<b>Double charmonium</b>					
X(3940)	$3942^{+9}_{-8}$	$37^{+27}_{-17}$	$?^{?+}$	$J/\psi(D\bar{D}^*)$	Belle (2007)
X(4160)	$4156^{+29}_{-25}$	$139^{+113}_{-65}$	$?^{?+}$	$J/\psi(D^* \bar{D}^*)$	Belle (2007)
<b>ISR</b>					
Y(4008)	$4008^{+121}_{-49}$	$226 \pm 97$	$1^{--}$	$(\pi^+ \pi^- J/\psi)$	Belle (2007)
Y(4260)	$4263 \pm 5$	$108 \pm 14$	$1^{--}$	$(\pi^+ \pi^- J/\psi)$	BaBar (2005), Belle, CLEO
Y(4360)	$4353 \pm 11$	$96 \pm 42$	$1^{--}$	$(\pi^+ \pi^- \psi(2S))$	BaBar (2007), Belle
X(4630)	$4634^{+9}_{-11}$	$92^{+41}_{-32}$	$1^{--}$	$(\Lambda_c \Lambda_c)$	Belle (2007)
Y(4660)	$4664 \pm 12$	$48 \pm 15$	$1^{--}$	$(\pi^+ \pi^- \psi(2S))$	Belle (2007)
<b>Two photons</b>					
$\chi_{c2}(2P)$	$3927.2 \pm 2.6$	$24.1 \pm 6.1$	$2^{++}$	$(D\bar{D})$	Belle(2005), BaBar
X(3915)	$3914 \pm 4$	$23^{+10}_{-13}$	$0, 2^{++}$	$(\omega J/\psi)$	Belle(2009)
X(4350)	$4350.6^{+4.6}_{-5.1}$	$13.3^{+18.4}_{-10.0}$	$0, 2^{++}$	$(\phi J/\psi)$	Belle(2009)
<b>Energy scan and <math>\Upsilon</math> transitions</b>					
$\eta_b(1S)$	$9390.7 \pm 2.9$	?	$0^{-+}$	$\gamma + (\dots)$	BaBar(2008), CLEO
$Y_b$	$10889.6 \pm 2.3$	$54.7^{+8.6}_{-7.8}$	$1^{--}$	$\pi^+ \pi^- \Upsilon(nS)$	Belle (2008)

# Belle Detector



- $3.5 \text{ GeV } e^+ \times 8.0 \text{ GeV } e^-$ .
- $\mathcal{L}_{\text{max}} = 2.1 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
- Continuous injection  
→  $1.1 \text{ fb}^{-1} / \text{day}$ .
- $\int \mathcal{L} dt \approx 1 \text{ ab}^{-1}$

