



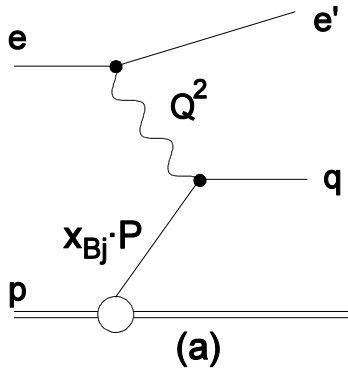
# Jet Production at HERA and Determination of $\alpha_s$ with H1



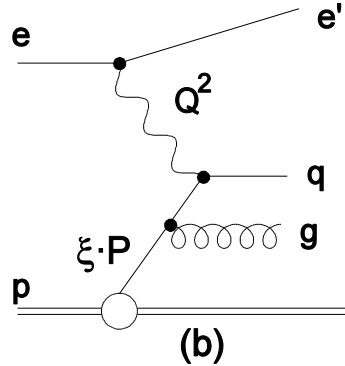
Artem Baghdasaryan DESY / YerPhI

EPS, Grenoble 2011

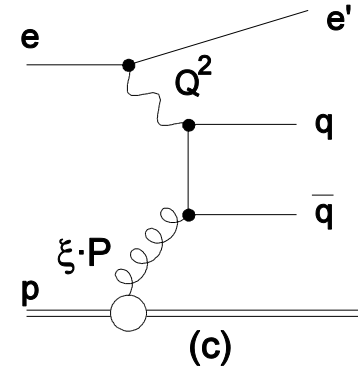
# Jet Production



**Born Level**



**QCD Compton**

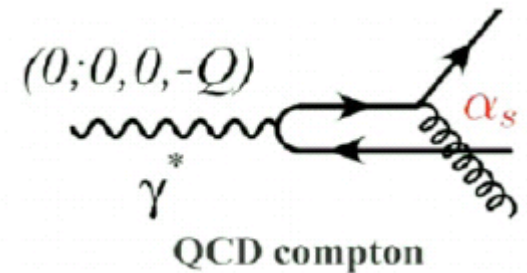
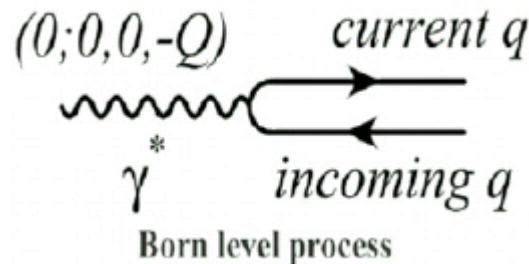


**Boson Gluon Fusion**

$\xi = x_{Bj}(1 + M_{12}^2/Q^2)$  - momentum fraction of struck parton (in LO)

Breit frame ( $2xP + q = 0$ ) is ideal for studying QCD with large  $P_T$ .

In Breit frame processes with low  $P_T$  (Born level contribution, jet contribution from proton remnant, etc) are suppressed



# Jet Measurement at H1

## Neutral Current Phase Space

Low  $Q^2$  (HERA1 (99-00),  $L=43.6/ \text{pb}$ )

High  $Q^2$  (full HERA2,  
 $L=351.6/ \text{pb}$ )

$5 < Q^2 < 100 \text{ GeV}^2$

$150 < Q^2 < 15\,000 \text{ GeV}^2$

$0.2 < y < 0.7$

**Jet Finder: longitudinally invariant infrared & collinear safe  $k_T$  algorithm with merging parameter  $R_0 = 1$  and jet minimal transverse momentum in Breit frame  $P_{\text{TBreit}} = 5 \text{ GeV}$**

## Jet Phase Space

$5 < P_{\text{TBreit}} < 80 \text{ GeV}$

$5 < P_{\text{TBreit}} < 50 \text{ GeV}$

$-1.0 < \eta_{(\text{lab})} < 2.5$

For avoiding problem with singularities additional cut implied on 2- & 3-jet level:  
 $M_{12} > 18 \text{ GeV}$  (Low  $Q^2$ )                       $M_{12} > 16 \text{ GeV}$  (High  $Q^2$ )

### Notation:

$Q^2$  – exchanged boson virtuality

$y$  – inelasticity

$\eta_{(\text{lab})}$  – jet pseudorapidity (laboratory frame)

$M_{12}$  – invariant mass of two leading jets

# NLO Calculations

- NLOJet++ with MSbar scheme for five massless quark flavors
- PDF: CTEQ6.5M (low  $Q^2$ ) and HERAPDF1.5 (high  $Q^2$ ) with  $\alpha_s(M_z) = 0.118$
- NLO corrected for hadronization and  $Z_0$  exchange effects
  - The hadronization correction factor differ from unity
    - less the 10% for inclusive and dijet cross sections
    - less then 20% for trijet and trijet to dijet cross sections ratio
- Scales:  $\mu_f^2 = \mu_r^2 = (Q^2 + P_T^2)/2$
- Theoretical uncertainties  $\Delta\mu_f$  and  $\Delta\mu_r$  estimated by variation of  $\mu_f$  and  $\mu_r$  by a factor 2
- Total scale uncertainty =  $\sqrt{(\Delta\mu_f^2 + \Delta\mu_r^2)}$

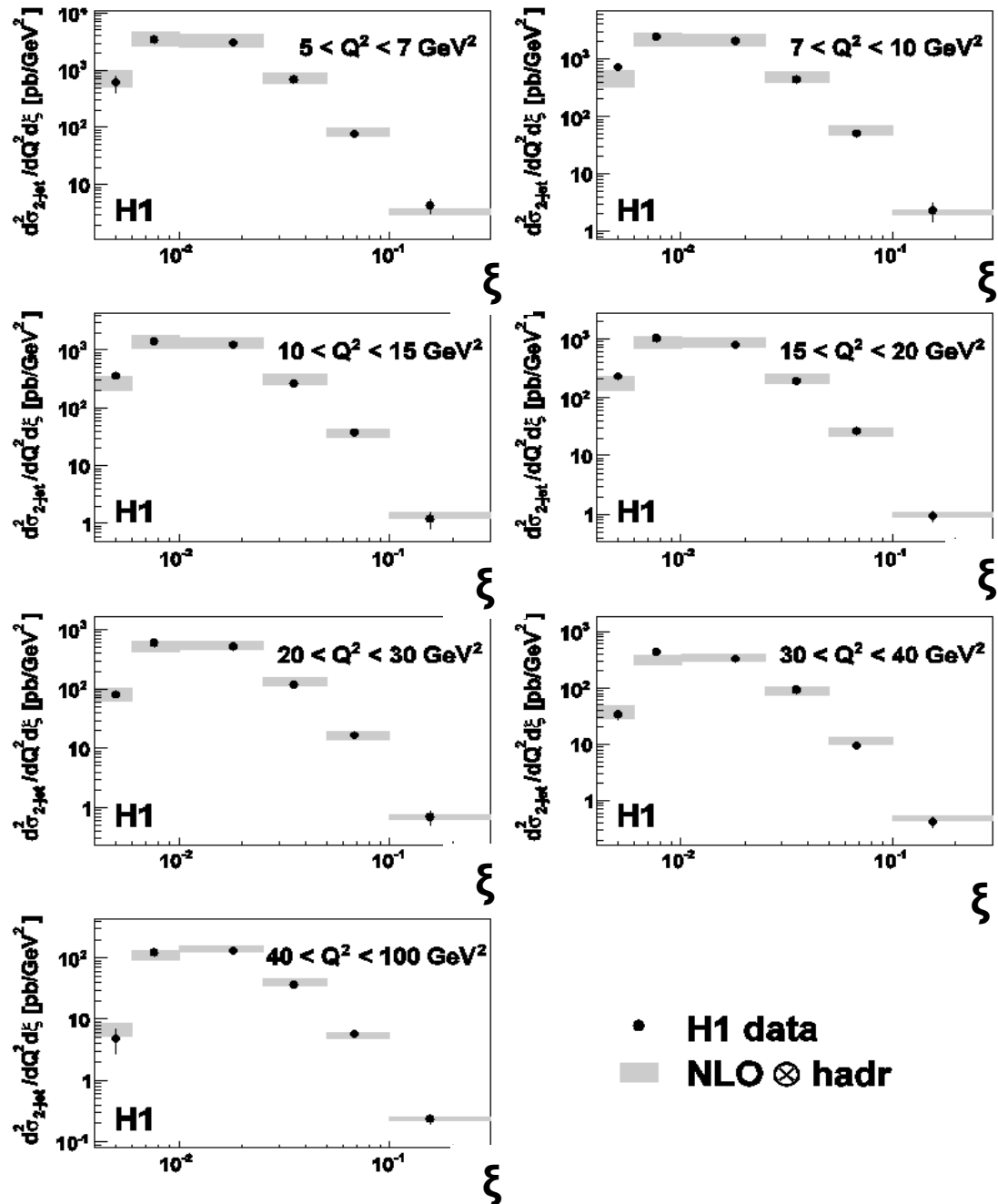
# Cross Sections as function of $Q^2$ and $\xi$ (Low $Q^2$ )

First double differential cross section measurements  
 Eur.Phys.J. C67 (2010) 1

Experimental uncertainties ( $< \sim 10\%$ ) dominate by HFS and model uncertainties and are essentially smaller than theoretical ones.

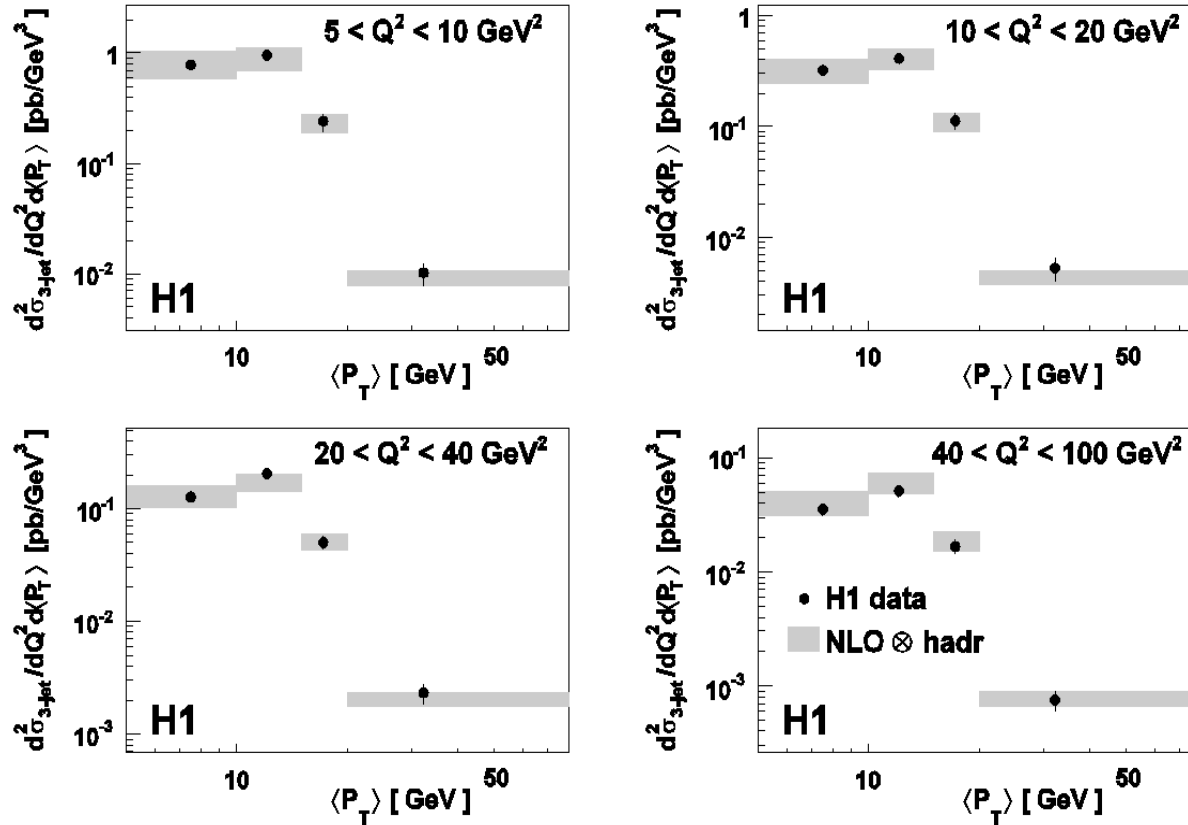
Theoretical uncertainties (up to 30%) dominated by renormalization scale.

2-Jet Cross Section



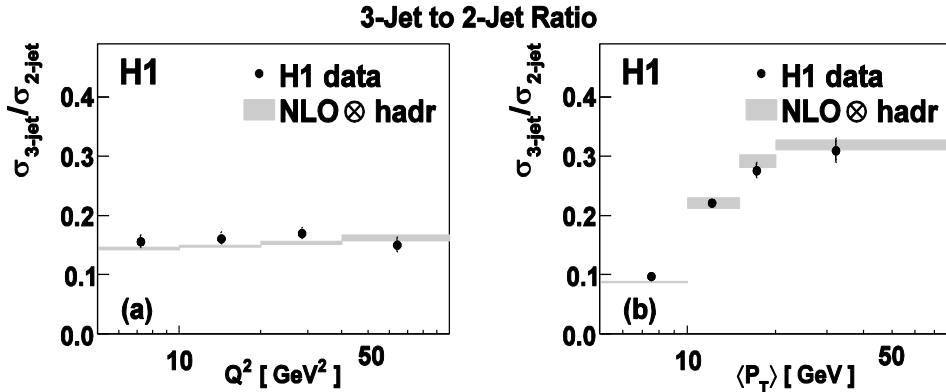
# Trijet Double Differential Cross Sections (Low $Q^2$ )

3-Jet Cross Section



The 3-jet cross section in four  $Q^2$  bins as a function of  $P_T$ . The NLO QCD calculation provides an overall good description of the measured distributions within the quoted theoretical and experimental uncertainties.

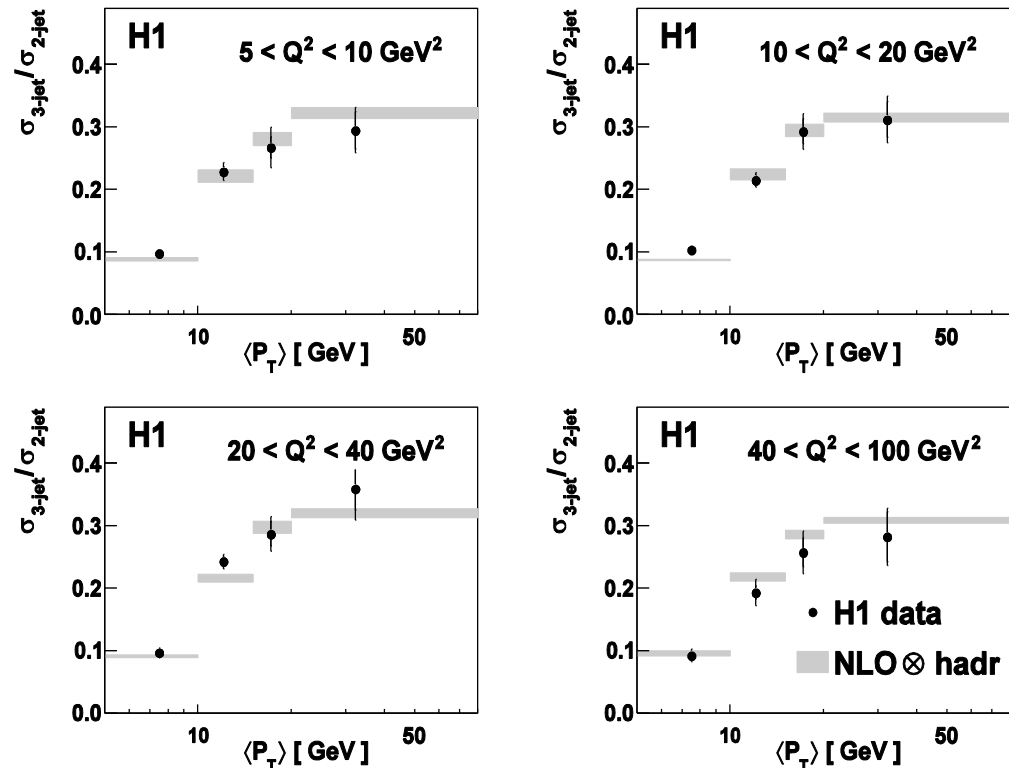
# - 7 - Trijet/Dijet Cross Sections Ratio (Low $Q^2$ )



The 3-jet cross section normalised to the 2-jet cross section is presented for single differential (on the left)

and for double differential distributions (below).

**3-Jet to 2-Jet Ratio**



This observable benefits from cancellation of the normalisation uncertainties and reduction of the other systematic uncertainties by about 50%.

It is described by the NLO cross section except for the lowest  $P_T$  bin, and shows a reduced sensitivity to the renormalisation scale variation which is done simultaneously for 2-jet and 3-jet cross sections.

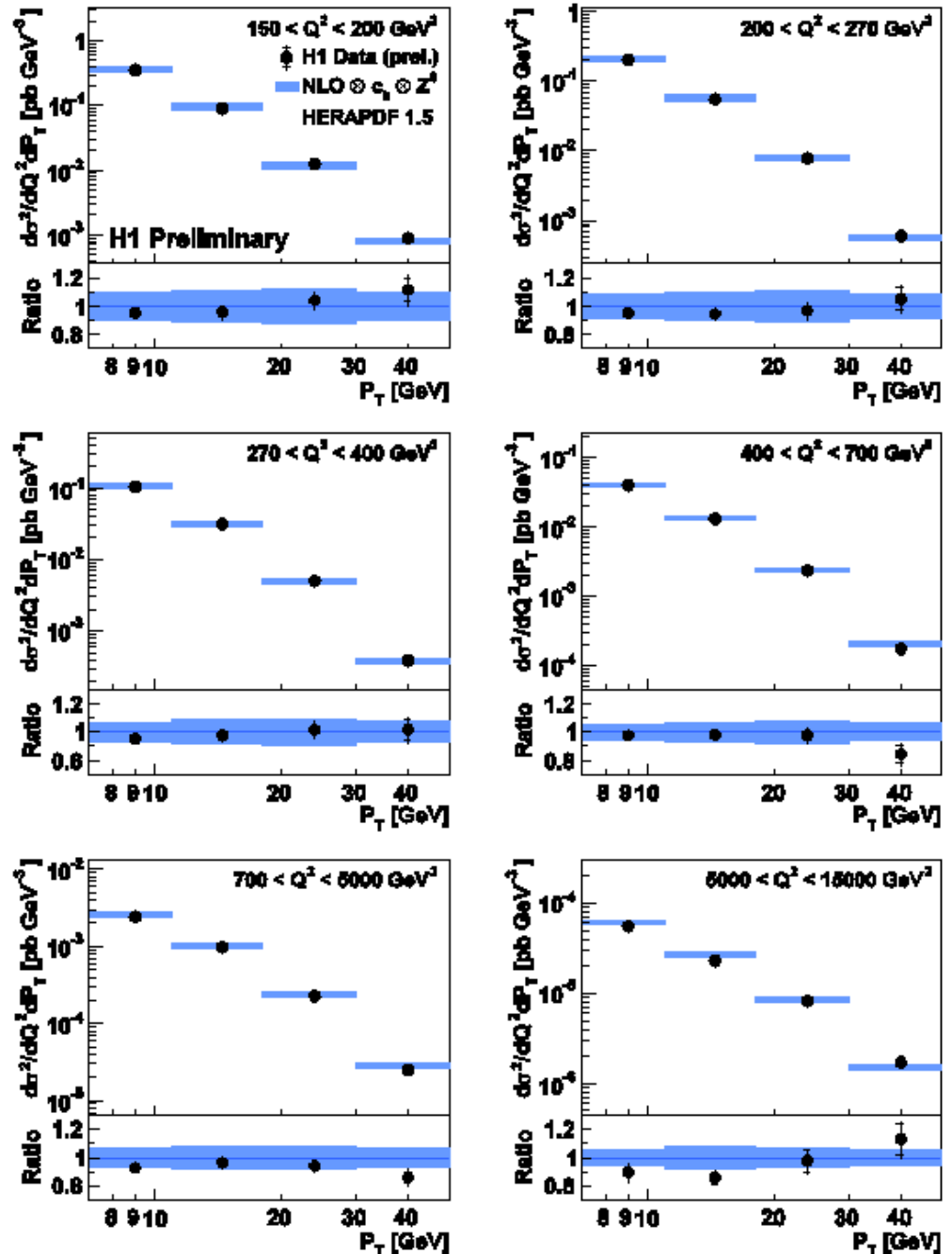
# Double differential Inclusive Jet Cross Sections (High $Q^2$ )

Jet energy scale uncertainty  $\sim 1\%$

Experimental uncertainty of 4-8% about half of the theoretical one.

Data are well described by NLO.

## Inclusive Jet Cross Section





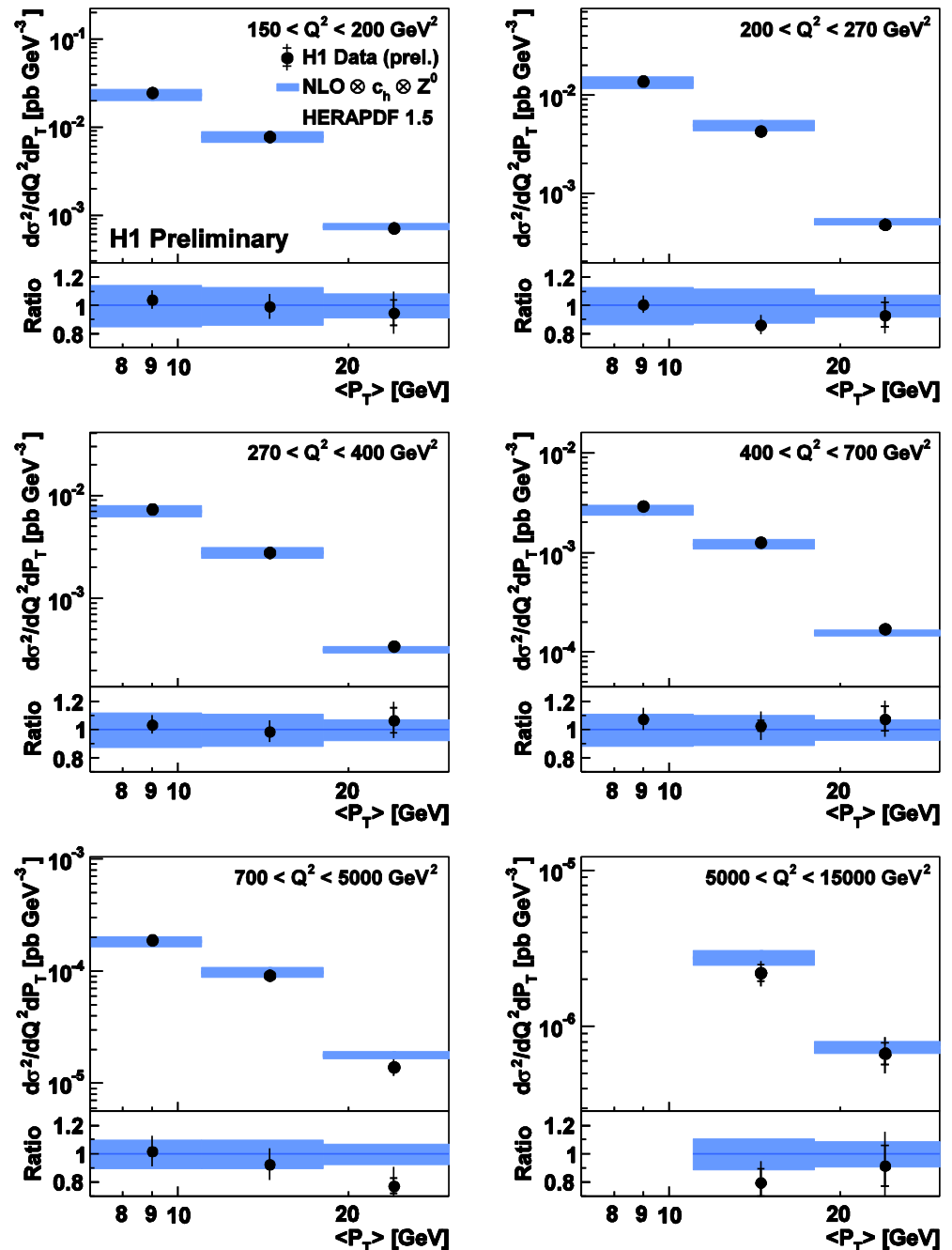
# Double differential Trijet Cross Section (High $Q^2$ )

First double differential trijet cross section measurements at high  $Q^2$ .

Experimental uncertainties dominated by model and HFS uncertainties.

Data are well described by NLO.

### Trijet Cross Section



# $\alpha_s(M_Z)$ Measurements

Extracted  $\alpha_s(M_Z)$  with correlated and uncorrelated errors taken into account

**Inclusive+ Dijet + Trijet without points with  $k = \sigma_{\text{NLO}} / \sigma_{\text{LO}} > 2.5$ ):  
**Eur.Phys.J. C67 (2010) 1****

$$\alpha_s(M_Z) = 0.1160 \pm 0.0014(\text{exp.}) \pm 0.0016(\text{pdf}) \begin{matrix} +0.0093 \\ -0.0077 \end{matrix} (\text{th.})$$

**H1 preliminary 11-032**

**Inclusive jet:**

$$\alpha_s(M_Z) = 0.1190 \pm 0.0021 (\text{exp.}) \pm 0.0020 (\text{pdf}) \begin{matrix} +0.0050 \\ -0.0056 \end{matrix} (\text{th.})$$

**Dijet:**

$$\alpha_s(M_Z) = 0.1146 \pm 0.0022 (\text{exp.}) \pm 0.0021 (\text{pdf}) \begin{matrix} +0.0044 \\ -0.0045 \end{matrix} (\text{th.})$$

**Trijet:**

$$\alpha_s(M_Z) = 0.1196 \pm 0.0016 (\text{exp.}) \pm 0.0010 (\text{pdf}) \begin{matrix} +0.0055 \\ -0.0039 \end{matrix} (\text{th.})$$

Main uncertainties come from theory uncertainties (~4-8%)  
-> theory improvement is desirable

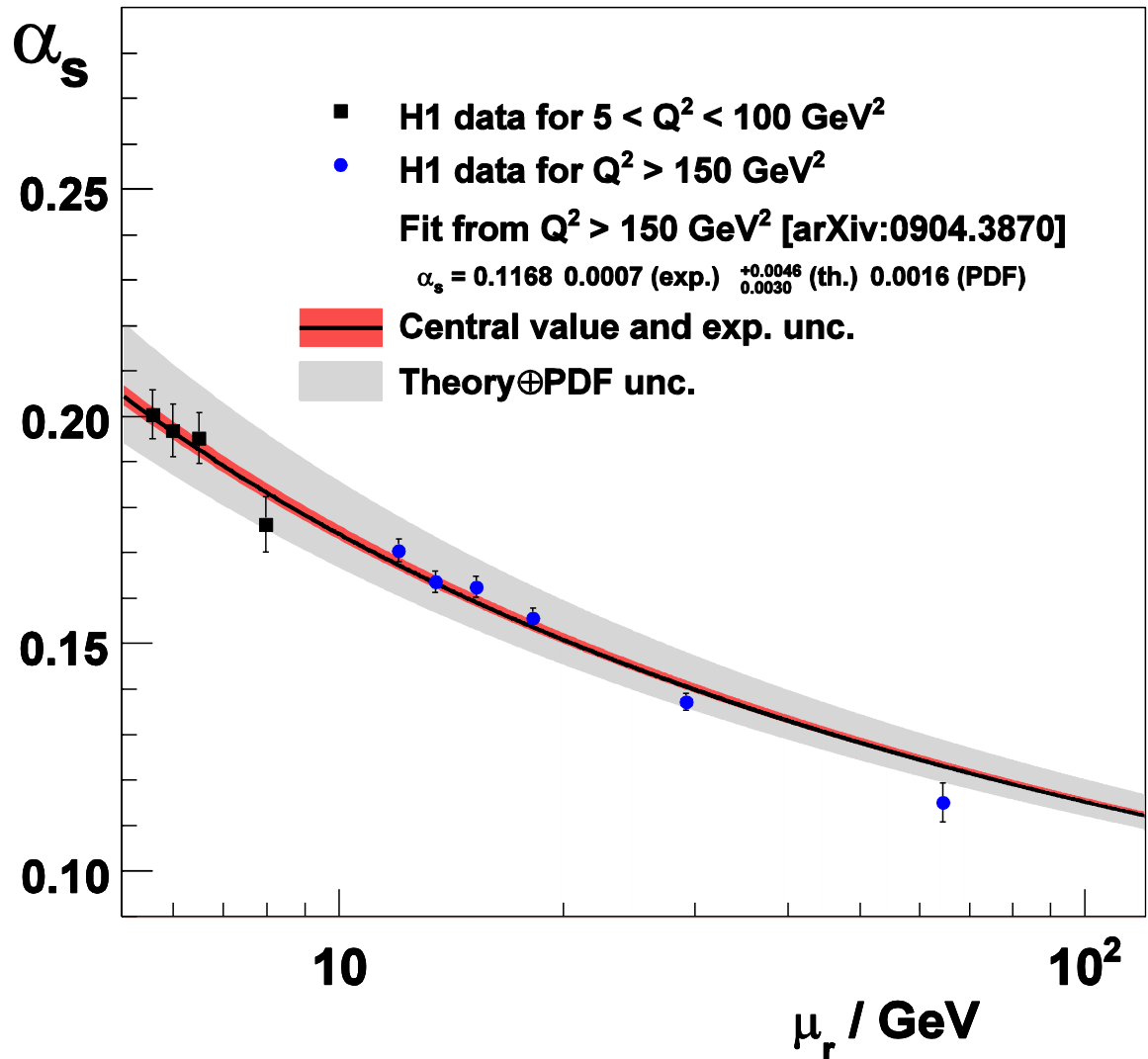
# Running of $\alpha_s(\mu_r)$

Theoretical and experimental uncertainties for high  $Q^2$   $\alpha_s$  (**Eur.Phys.J.C65(2010)363**) extrapolated down to low  $Q^2$ .

Remarkable agreement between extraction of  $\alpha_s(\mu_r)$  at low and high  $Q^2$ .

Nice running of strong coupling between 6 – 70 GeV in single experiment.

### $\alpha_s$ from Jet Cross Sections in DIS



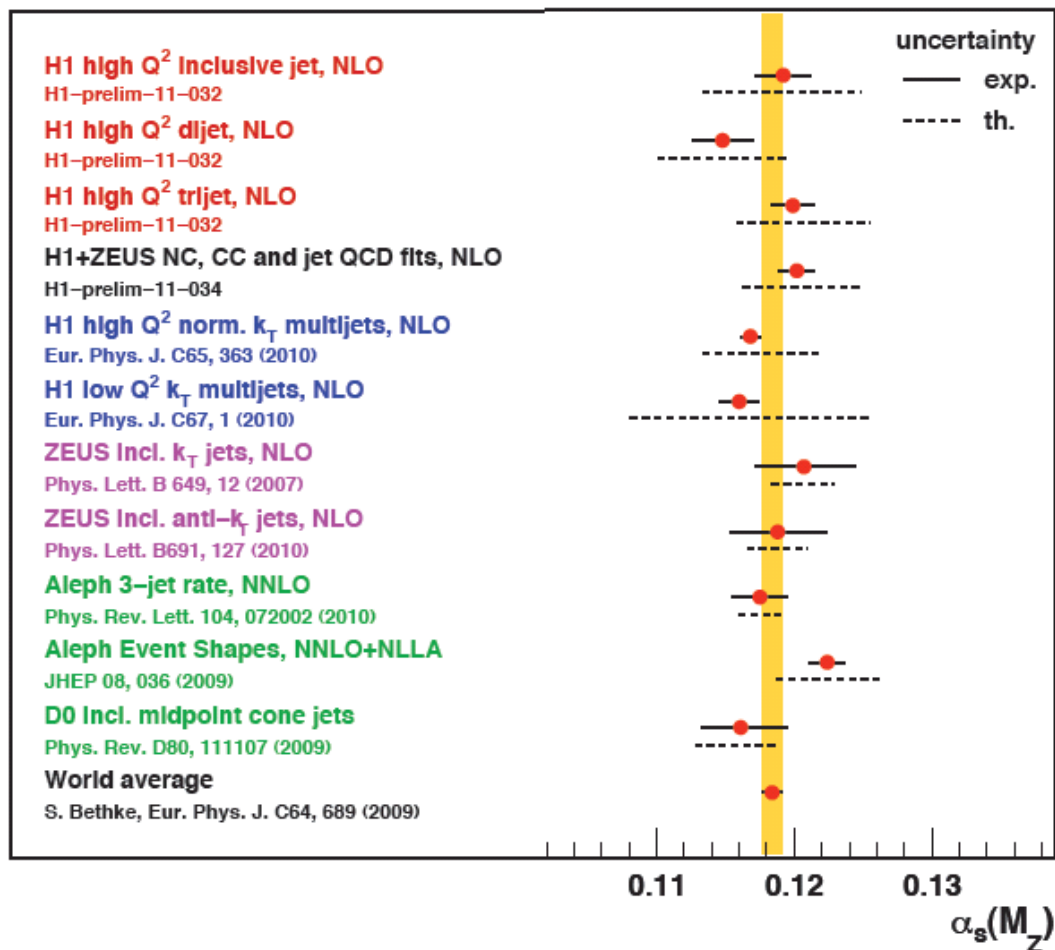
# Summary

High precision measurement of inclusive, dijet, trijet cross sections at low and high  $Q^2$  as well as 3J to 2J cross sections ratio for low  $Q^2$  presented.

All measurements are in good agreement with NLO.

To reduce large theoretical uncertainties calculation of terms beyond NLO necessary.

$\alpha_s(M_Z)$  from jet measurements at HERA are in good agreement between each other and with world average.

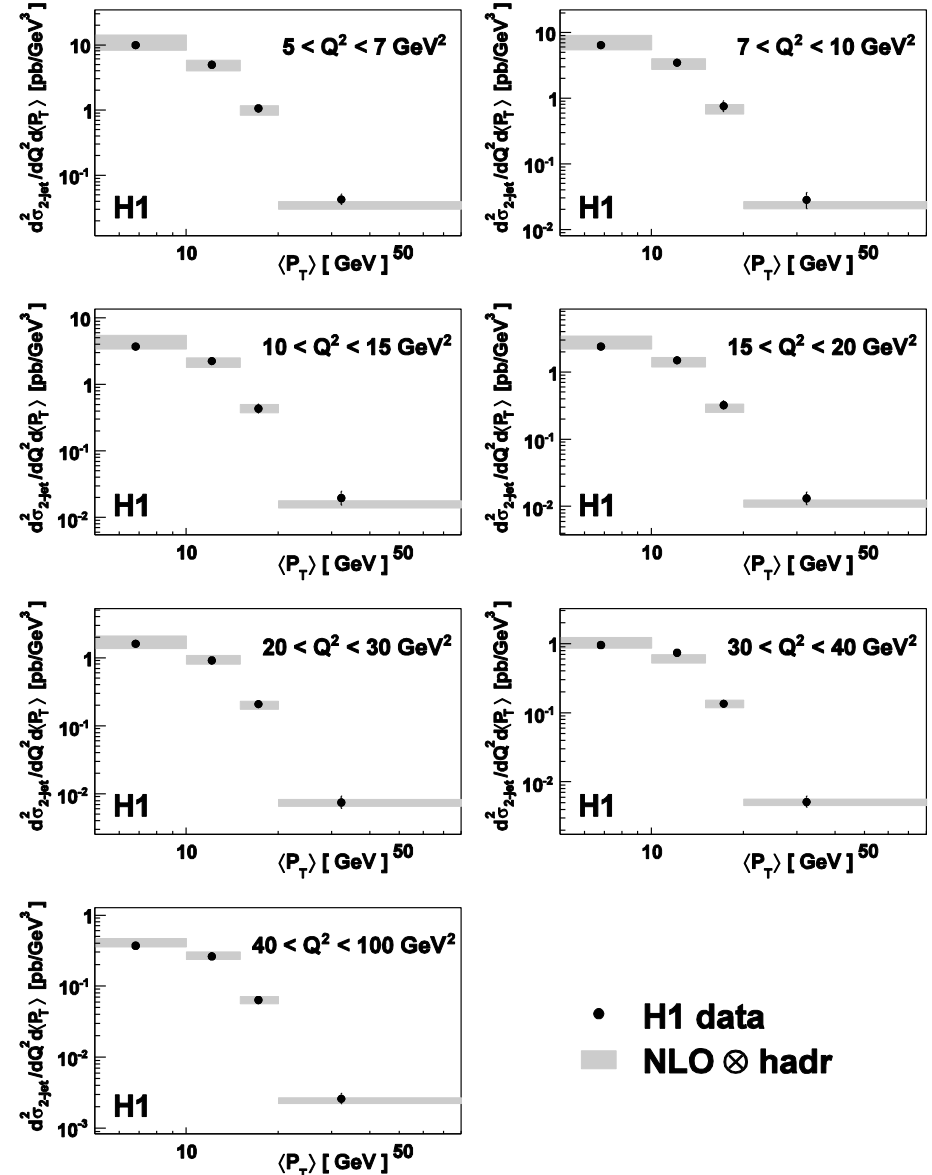
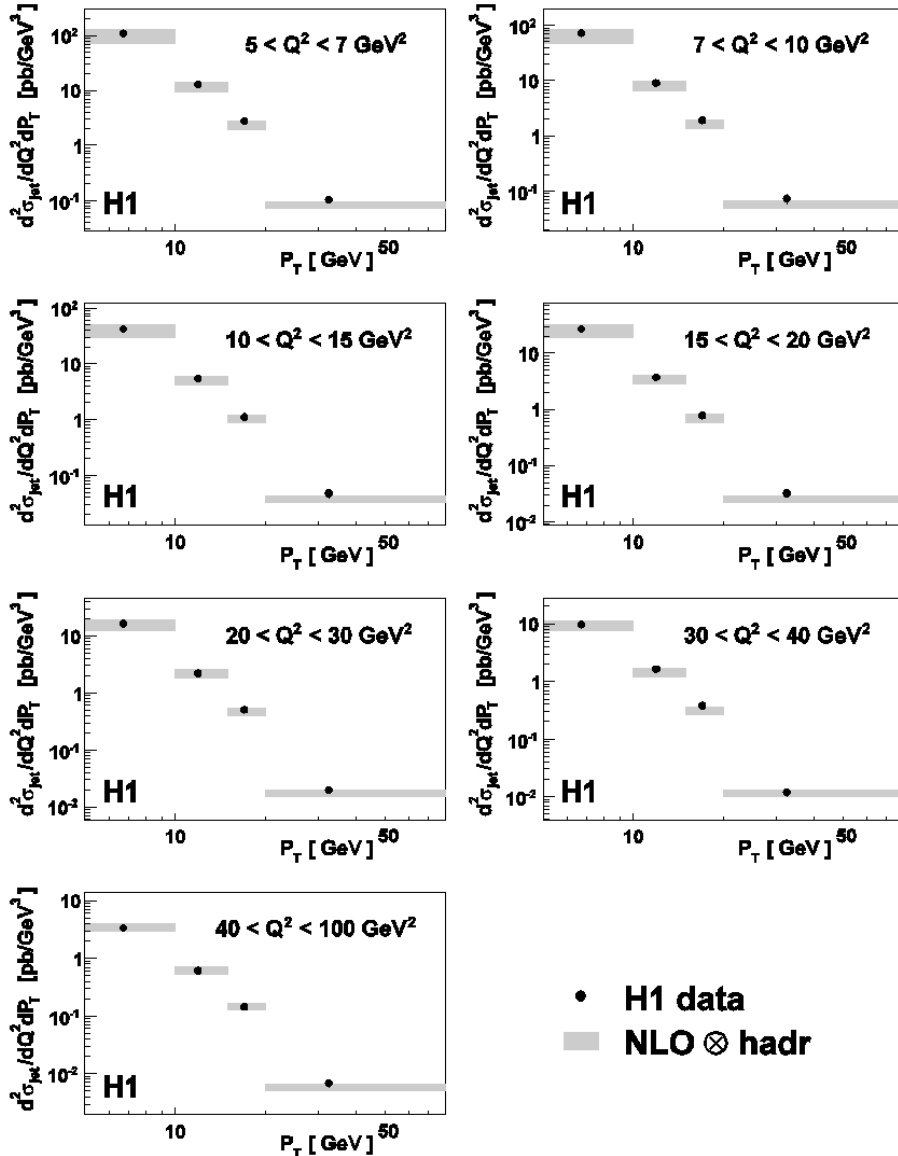


# BACKUP

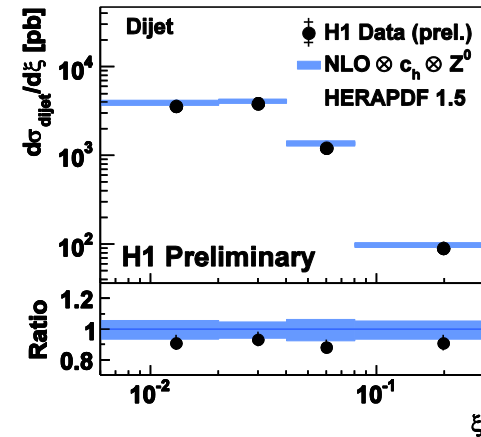
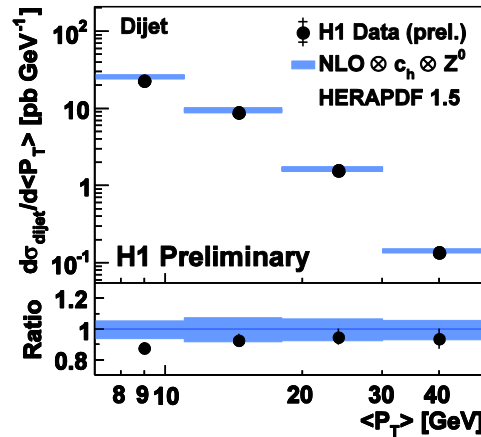
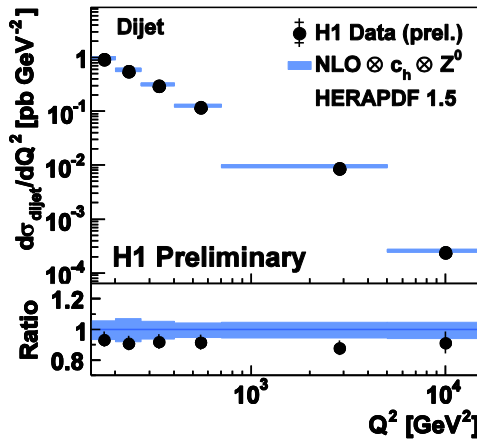
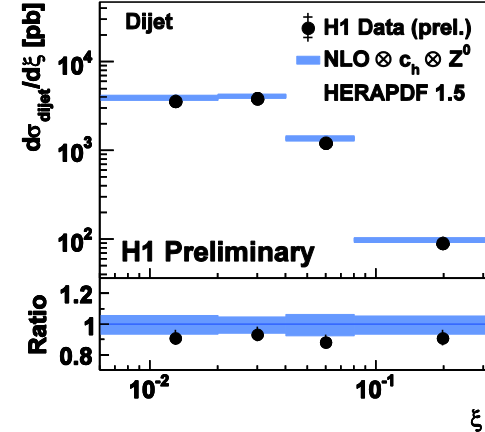
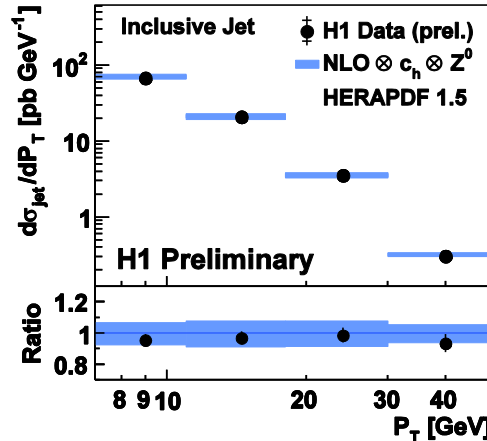
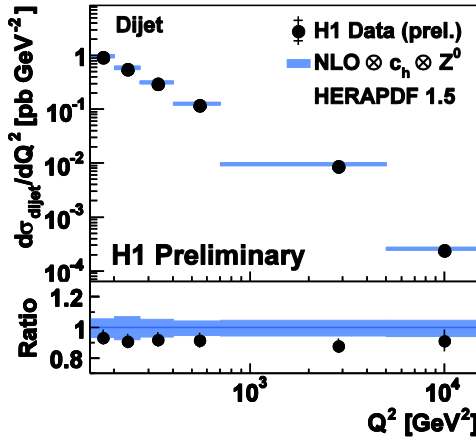
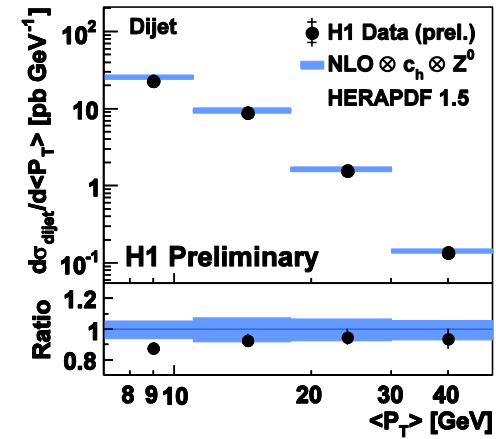
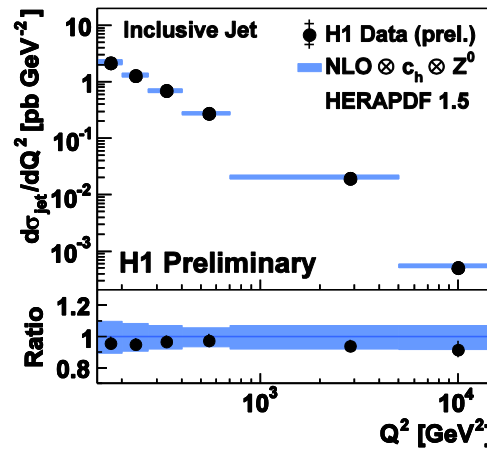
# - 14 - Double differential Dijet Cross Sections Low $Q^2$

Inclusive Jet Cross Section

2-Jet Cross Section

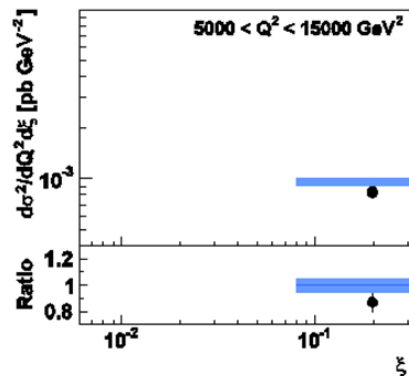
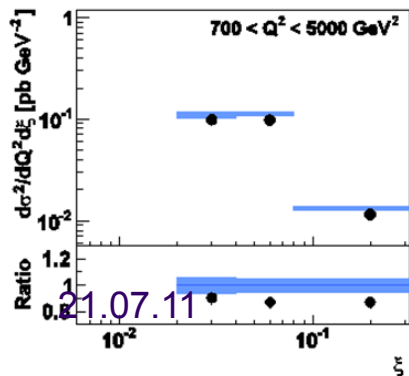
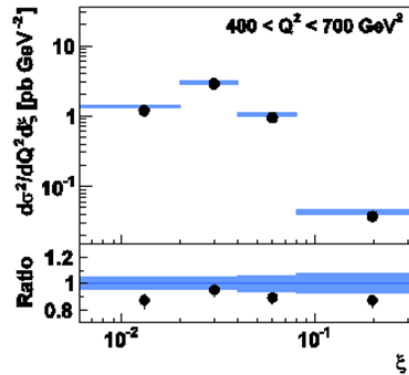
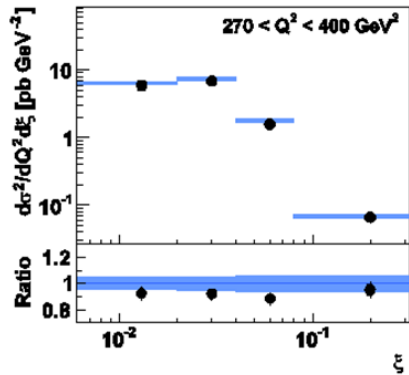
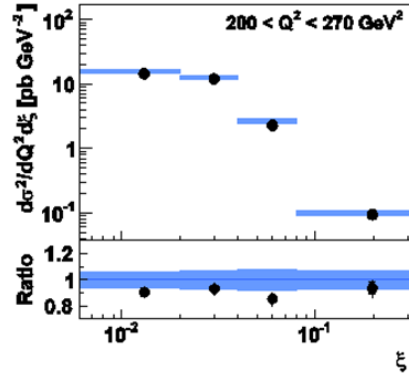
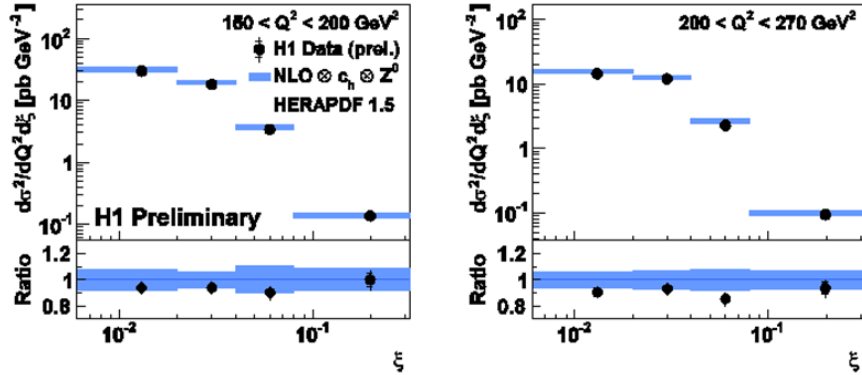


# Single differential Jet Cross Sections (High Q2)

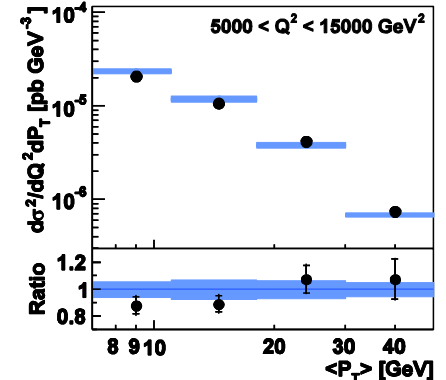
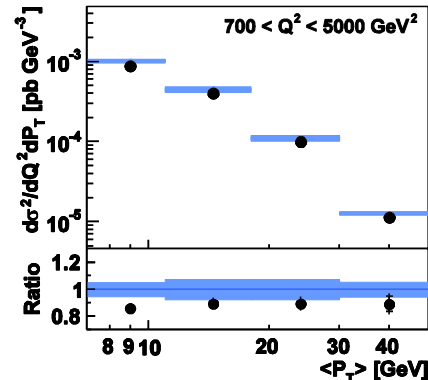
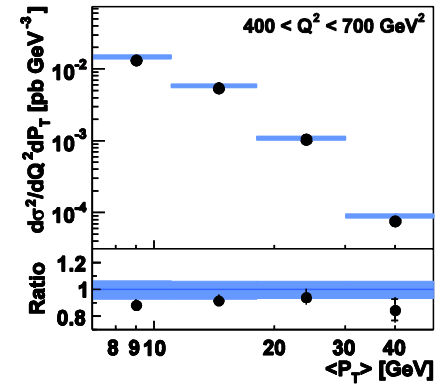
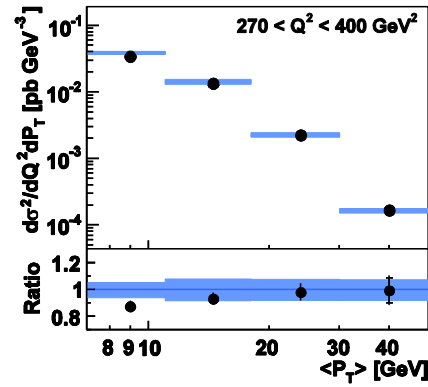
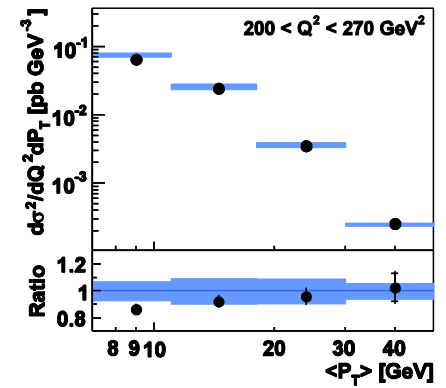
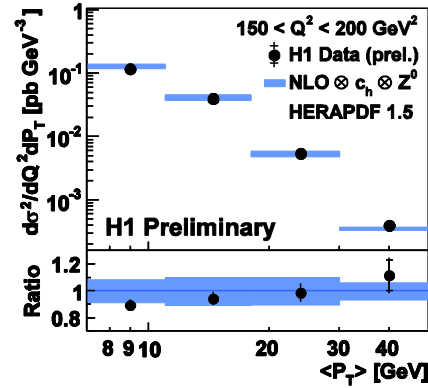


# - 16 - Double differential Dijet Cross Section (High Q<sup>2</sup>)

Dijet Cross Section



Dijet Cross Section

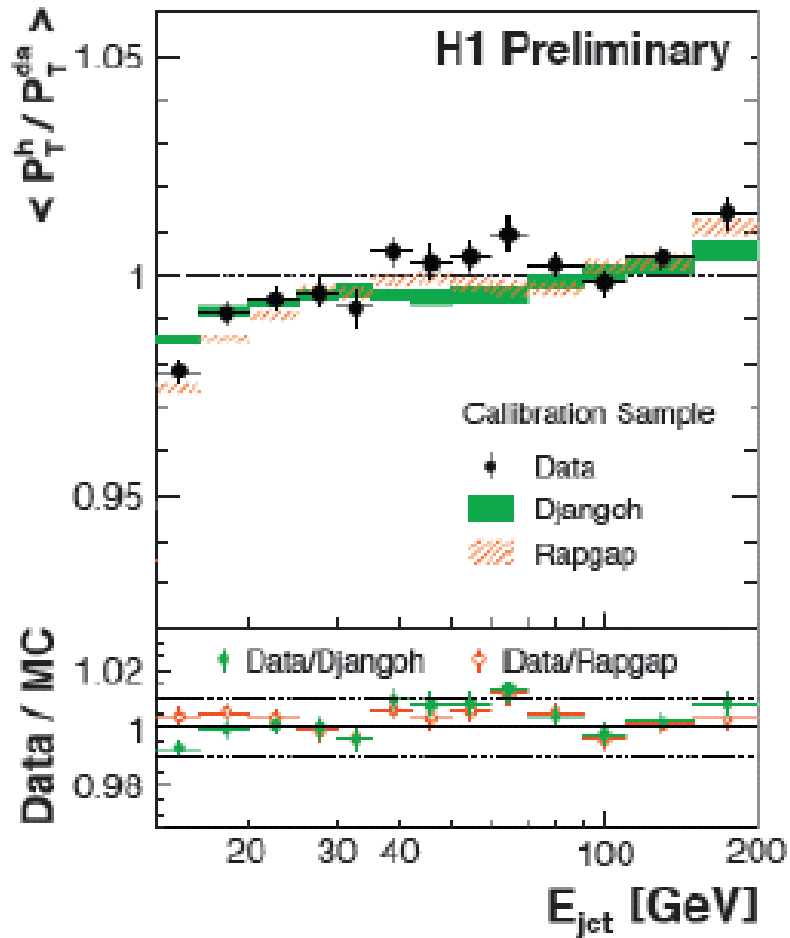


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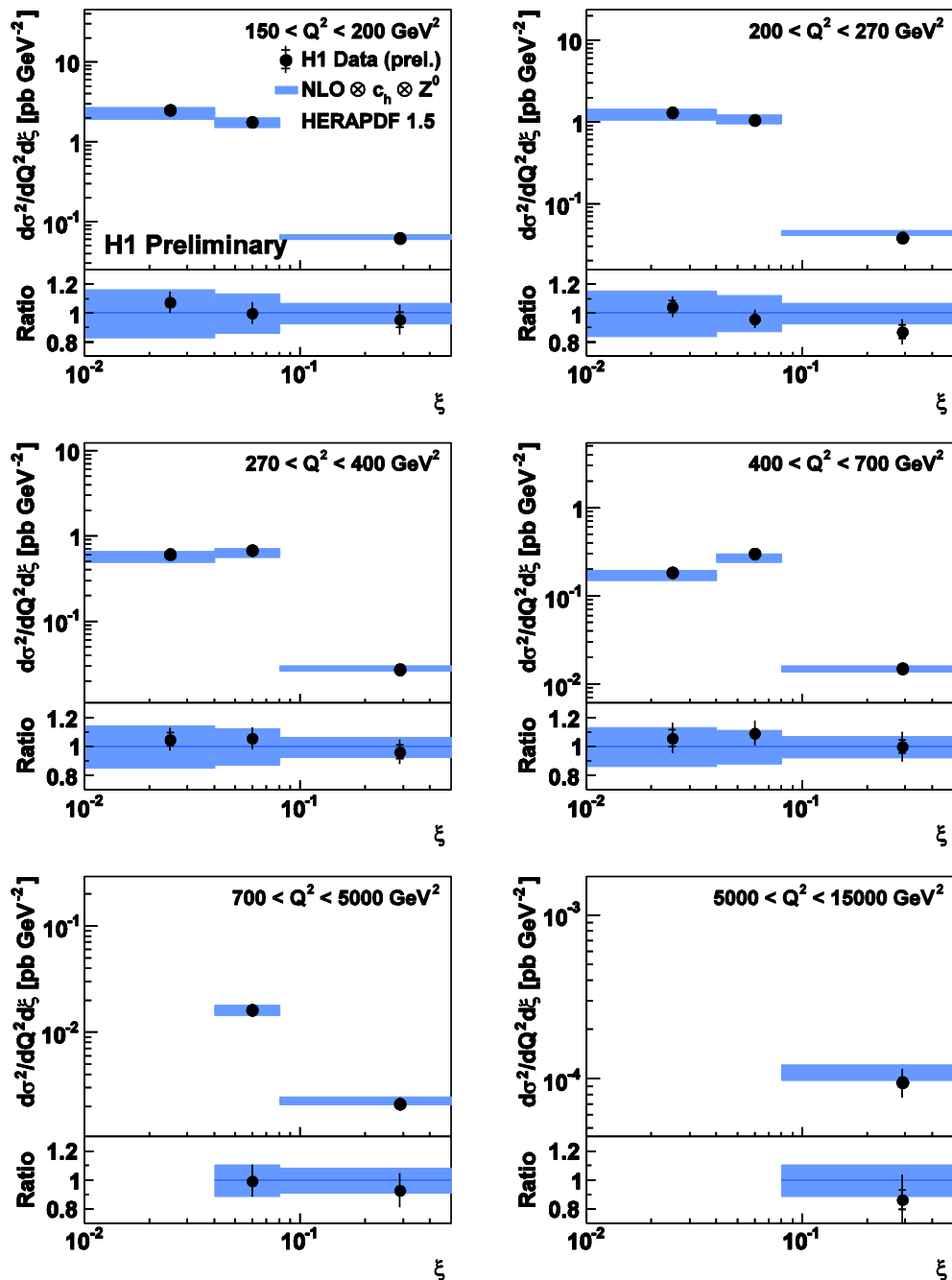


# Double Differential Trijet Cross Sections

- 17 -



## Trijet Cross Section



# $\alpha_s(M_Z)$ Fit

Minimise  $\chi^2(\alpha_s(M_Z))$  defined as:

$$\chi^2 = \vec{V}^T \cdot M^{-1} \cdot \vec{V} + \sum_k \epsilon_k^2$$

*correlated version of  $\sum(\text{difference/error})^2$*

*penalty term for fitted systematics  
"Hessian" method*

$$M = M^{\text{stat.}} + M^{\text{uncor.}}$$

*correlated for some bins*      *uncorrelated systematics*

$$V_i = \sigma_i^{\text{exp.}} - \sigma_i^{\text{theo.}} \left( 1 - \sum_k \Delta_{ik} \epsilon_k \right)$$

*bin #*      *correlated systematical error #k*      *parameter in fit, pull  
"Hessian" method*

Exp. uncertainty of fit defined as  $\alpha_s$  interval upto minimum  $\chi^2+1$