

Flavour Physics in an $SO(10)$ Grand Unified Model

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Outline for next 12 minutes

- 1 SUSY-GUTs
- 2 CMM model – a new benchmark scenario
 - Theory
 - Comparison with CMSSM/mSUGRA
 - Phenomenology
- 3 Conclusion

Why do we believe in SUSY-GUTs?

- SM quantum numbers? Charge quantization?
Fermions nicely fit into $SU(5)$ multiplets

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- SO(10): all SM fields per generation + ν_R fit in spinor rep.:

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- GUTs need SUSY:
 - gauge coupling unification
 - hierarchy problem (heavy GUT particles destabilizes electroweak scale)
- But: SUSY flavour & CP problem

Flavour and SUSY GUTs

Flavour mixing:

- (left-handed) quarks: CKM matrix
- neutrinos: PMNS matrix

$$V_{\text{CKM}} = \begin{pmatrix} \bullet & \bullet & \cdot \\ \bullet & \bullet & \cdot \\ \cdot & \cdot & \bullet \end{pmatrix}$$

$$U_{\text{PMNS}} \approx \begin{pmatrix} \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet \end{pmatrix}$$

SU(5) multiplets link quarks to leptons

$$\bar{\mathbf{5}}_1 = \begin{pmatrix} d_R^c \\ d_R^c \\ d_R^c \\ e_L \\ -\nu_e \end{pmatrix}, \quad \bar{\mathbf{5}}_2 = \begin{pmatrix} s_R^c \\ s_R^c \\ s_R^c \\ \mu_L \\ -\nu_\mu \end{pmatrix}, \quad \bar{\mathbf{5}}_3 = \begin{pmatrix} b_R^c \\ b_R^c \\ b_R^c \\ \tau_L \\ -\nu_\tau \end{pmatrix}.$$

Idea of Chang, Masiero, Murayama; Moroi

neutrino mixing angle $\theta_{23} \approx 45^\circ$ induce large $\tilde{b}_R - \tilde{s}_R$ - and $\tilde{\tau}_L - \tilde{\mu}_L$ -mixing
 \Rightarrow new $b_R \rightarrow s_R$ transitions from gluino-squark loops possible

CMM Model

SO(10) gauge theory with superpotential

[Chang, Masiero, Murayama 03]

$$W_Y^{\text{SO}(10)} = \frac{1}{2} \mathbf{16}_i Y_1^{ij} \mathbf{16}_j \mathbf{10}_H + \mathbf{16}_i Y_2^{ij} \mathbf{16}_j \frac{\mathbf{45}_H \mathbf{10}'_H}{2M_{\text{Pl}}} + \mathbf{16}_i Y_N^{ij} \mathbf{16}_j \frac{\overline{\mathbf{16}}_H \overline{\mathbf{16}}_H}{2M_{\text{Pl}}}$$

$$\bullet Y_1^{ij} \rightarrow M_u, M_\nu^D, \quad Y_2^{ij} \rightarrow M_d, M_\ell, \quad Y_N^{ij} \rightarrow M_{\nu R}$$

• Assumptions:

- flavour symmetry (which is exact at M_{Pl}) is broken
- Y_1 and Y_N simultaneously diagonalisable
- breaking via SU(5)

$$\text{SO}(10) \xrightarrow[\langle \mathbf{45}_H \rangle]{\langle \mathbf{16}_H \rangle, \langle \overline{\mathbf{16}}_H \rangle} \text{SU}(5) \xrightarrow{\langle \mathbf{45}_H \rangle} G_{\text{SM}} \xrightarrow{\langle \mathbf{10}_H \rangle, \langle \mathbf{10}'_H \rangle} \text{SU}(3)_C \times \text{U}(1)_{\text{em}}$$

Nonrenormalizable term $\propto Y_2$ term gives naturally small $\tan \beta$ and determines whole flavour structure

Flavour structure CMM model

Key ingredients: weak basis with

$$\boxed{Y_d = Y_\ell^\top} = V_{\text{CKM}}^* \begin{pmatrix} y_d & 0 & 0 \\ 0 & y_s & 0 \\ 0 & 0 & y_b \end{pmatrix} U_D, \quad U_D = U_{\text{PMNS}}^* \text{diag}(1, e^{i\xi}, 1)$$

and right-handed down squark mass matrix:

$$m_{\tilde{d}}^2(M_Z) = \text{diag} \left(m_{\tilde{d}_1}^2, m_{\tilde{d}_1}^2, m_{\tilde{d}_1}^2 (1 - \Delta_{\tilde{d}}) \right)$$

$\Delta_{\tilde{d}} \in [0, 1]$: relative mass splitting; generated by top-Yukawa RG effects

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Rotating Y_d to diagonal form (mass eigenstates) $\Rightarrow \theta_{23} \approx 45^\circ$ enters $m_{\tilde{D}}^2$:

$$m_{\tilde{D}}^2 = U_D m_{\tilde{d}}^2 U_D^\dagger = m_{\tilde{d}_1}^2 \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 - \frac{1}{2} \Delta_{\tilde{d}} & -\frac{1}{2} \Delta_{\tilde{d}} e^{i\xi} \\ 0 & -\frac{1}{2} \Delta_{\tilde{d}} e^{-i\xi} & 1 - \frac{1}{2} \Delta_{\tilde{d}} \end{pmatrix}$$

The CP phase ξ affects CP violation in $B_s - \bar{B}_s$ mixing!

New benchmark scenario?

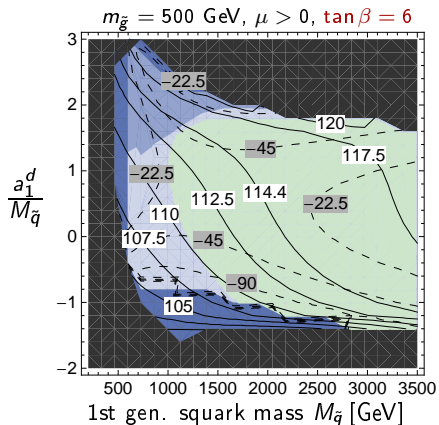
- 7 input parameters at $M_{\text{SO}(10)}$: $m_0^2 \quad m_{\tilde{g}} \quad D \quad a_0 \quad \arg \mu \quad \xi \quad (\tan \beta)$
- alternatively: inputs at M_{ew} : $m_{\tilde{u}_1} \quad m_{\tilde{d}_1} \quad m_{\tilde{g}} \quad a_1^d \quad \arg \mu \quad \xi \quad (\tan \beta)$
- RG evolution: $M_{\text{ew}} \rightarrow M_{\text{Pl}} \rightarrow M_{\text{ew}} \Rightarrow$ find all particle masses, MSSM couplings and calculate observables

generic MSSM	mSUGRA/CMSSM	CMM model
≈ 120 parameters	4 parameters & 1 sign	7 input parameters
SUSY flavour & CP problem	minimize flavour violation ad-hoc	clear flavour structure
no universality	universality at M_{GUT}	universality at M_{Pl} but broken at M_{GUT}
quarks & leptons unrelated		quark-lepton-interplay
Problem: suppress large effects elsewhere	cannot explain current flavour data (e.g. ϕ_s)	can fit ϕ_s and small effects in 1st/2nd gen.

Phenomenology

Global analysis of several observables:

$B_s - \bar{B}_s$ mixing, $b \rightarrow s\gamma$, $\tau \rightarrow \mu\gamma$, m_h (lightest Higgs mass)



black: $m_f^2 < 0$, unstable vacuum

dark blue: excluded by $B_s - \bar{B}_s$

medium blue: excluded by $b \rightarrow s\gamma$

light blue: excluded by $\tau \rightarrow \mu\gamma$

green: compatible with $B_s - \bar{B}_s$, $b \rightarrow s\gamma$, $\tau \rightarrow \mu\gamma$

Higgs mass: ——— 114.4 GeV

ϕ_s in degrees: - - - - - -45°

Generic Results

- flavour effects \propto mass splitting $\Delta_{\tilde{g}}$ (driven by RG effects of y_t)
- $B_s - \bar{B}_s$ mixing: free phase ξ can adjust ϕ_s
- powerful constraint: $m_h \geq 114.4 \text{ GeV} \Rightarrow$ excludes too small $\tan \beta$

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- degenerate 1st/2nd gen. squark masses & nearly tribimaximal $U_{\text{PMNS}} \Rightarrow$ effects suppressed in $K - \bar{K}$, ϵ_K , $\mu \rightarrow e\gamma$
- realistic GUTs involve dim-5 Yukawa terms to fix $Y_d = Y_\ell^T$ for 1st/2nd gen. \Rightarrow not only $b_R \rightarrow s_R$ but also $b_R \rightarrow d_R$ and $d_R \rightarrow s_R$. Strongly constrained by $K - \bar{K}$ mixing [Trine, Wiesenfeldt, Westhoff 2009]
- Similar constraints can be found from $\mu \rightarrow e\gamma$

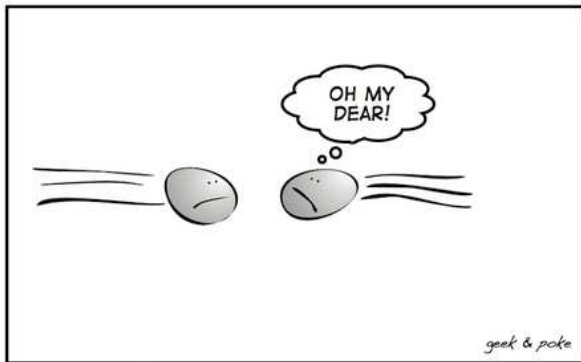
[Ko, Park, Yamaguchi 2008; Borzumati, Yamashita 2009];

[JG, Mertens, Nierste, Wiesenfeldt 2009].

Conclusions

- SUSY GUTs are theoretical well motivated scenarios with correlations between hadronic and leptonic observables
- If large CP violation in $B_s - \bar{B}_s$ mixing is confirmed \Rightarrow physics beyond CMSSM and mSUGRA
- CMM model:
 - large atmospheric mixing angle $\theta_{23} \approx 45^\circ$ induces $b - s$ - and $\tau - \mu$ -transitions
 - free phase ξ can adjust CP violation in $B_s - \bar{B}_s$ mixing
 - only minor effects in $2 \rightarrow 1$ and $3 \rightarrow 1$ transitions
 - extensive RGE analysis to connect Planck-scale and low-energy parameters
 - Higgs potential still has to be worked out
 - new benchmark model?

Thanks for your attention



LATELY INSIDE THE LHC:
2 PROTONS 0.00000000000000000001 SEC BEFORE THE COLLISION

Backup slides

Mass splittings

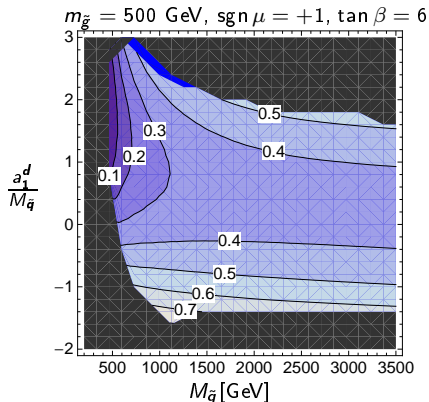
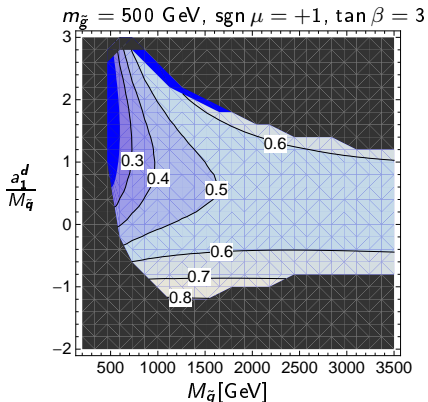


Figure: Relative mass splitting $\Delta_d^{\text{rel}} = 1 - m_{d_3}^2/m_{d_2}^2$ among the bilinear soft terms for the right-handed squarks of the second and third generations with $\tan \beta = 3$ (left) and 6 (right) in the $M_{\tilde{q}}(M_Z) - a_1^d(M_Z)/M_{\tilde{q}}(M_Z)$ plane for $m_{\tilde{g}} = 500 \text{ GeV}$ and $\text{sgn } \mu = +1$.

FCNC observables

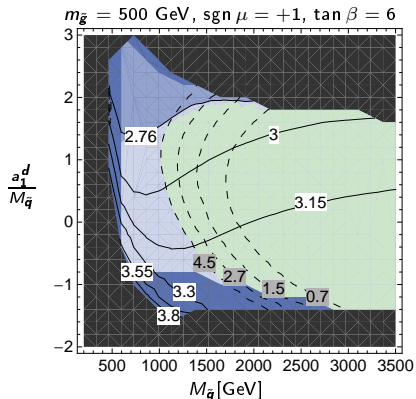
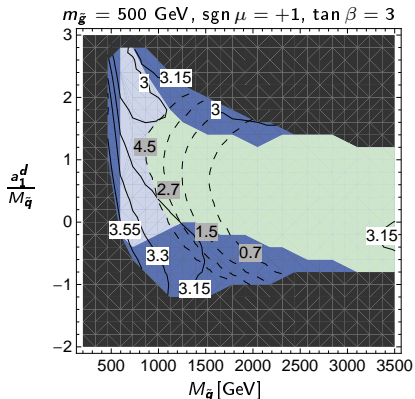
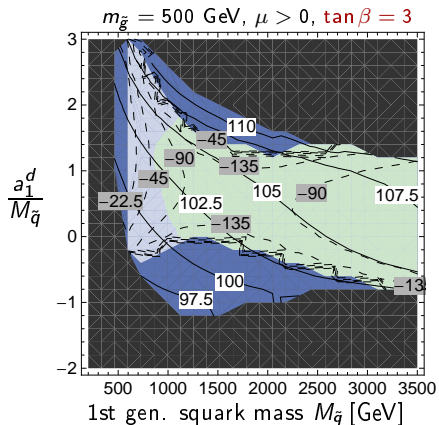


Figure: Correlation of FCNC processes with $\tan \beta = 3$ and $\tan \beta = 6$. $\mathcal{B}(b \rightarrow s\gamma)[10^{-4}]$ solid lines with white labels; $\mathcal{B}(\tau \rightarrow \mu\gamma)[10^{-8}]$ dashed lines with gray labels. Black region: $m_{\tilde{f}}^2 < 0$ or unstable $|0\rangle$; dark blue region: excluded due to $B_s - \bar{B}_s$; medium blue region: consistent with $B_s - \bar{B}_s$ but excluded due to $b \rightarrow s\gamma$; light blue region: consistent with $B_s - \bar{B}_s$ and $b \rightarrow s\gamma$ but inconsistent with $\tau \rightarrow \mu\gamma$; green region: compatible with all three FCNC constraints.

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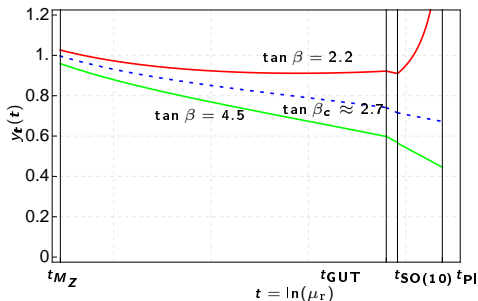
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Perturbativity of y_t



- y_t has a quasi-fixed point $y_t^2/g^2 = 55/56 \simeq 1$ in SO(10) (for $\tan \beta_c \simeq 2.7$)
- $\tan \beta < 2.7 \Rightarrow y_t$ blow-up below M_{PI} ; $\tan \beta > 2.7 \Rightarrow y_t$ stays perturbative
- to test CMM: maximize flavour effects (large $\Delta_{\vec{q}}$, i.e. large y_t , small $\tan \beta$)
- CMM model: $2.7 \lesssim \tan \beta \lesssim 10$

Higgs mass constraint

- For small $\tan\beta$ lower bound from LEP: $m_h \geq 114.4$ GeV
- MSSM: Higgs h^0 tends to be light at tree level: $m_h \leq M_Z |\cos(2\beta)|$
- corrections $\Delta m_h^2 \propto m_t^4 \ln(m_t^2/m_{\tilde{t}}^2) \Rightarrow$ (too) small for large y_t , because of RG evolution (small stop mass $m_{\tilde{t}}^2$)
- larger $\tan\beta$ reduces y_t and size of flavour effects
- could be relaxed by allowing the Higgs multiplets to have different Planck-scale masses from the sfermions (similarly to the non-universal Higgs model (NUHM))

small $\tan\beta$	\Leftrightarrow	large flavor effects	\Leftrightarrow	(too) light h^0
larger $\tan\beta$	\Leftrightarrow	smaller flavor effects	\Leftrightarrow	sufficiently heavy h^0

Example point

$$M_{\tilde{q}}=1500 \text{ GeV}, m_{\tilde{g}_3}=500 \text{ GeV}, a_1^d(M_Z)/M_{\tilde{q}}=1.5, \arg \mu=0, \tan \beta=6 \quad M_{ew} \xrightarrow{\text{Upward evolution}} M_{Pl}$$

$$a_0=1273 \text{ GeV}, m_0=1430 \text{ GeV}, m_{\tilde{g}}=184 \text{ GeV} \quad M_{Pl} \xrightarrow{\text{SO(10) \& SU(5) RGE}} M_{GUT}$$

$$\hat{A}_{\mathbf{u}}(M_{GUT}) = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 46 \end{pmatrix} \text{ GeV}, \quad \hat{A}_{\mathbf{d}}(M_{GUT}) = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0.3 & -3.5 \end{pmatrix} \text{ GeV},$$

$$\hat{A}_{\nu}(M_{GUT}) = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ -0.0013 & 0.0023 & 43.4 \end{pmatrix} \text{ GeV}, \quad \text{non-universal at } M_{GUT}$$

$$m_{\tilde{\phi}}(M_{GUT}) = \text{diag}(1426, 1426, 1074) \text{ GeV}$$

$$m_{\tilde{\psi}}(M_{GUT}) = \text{diag}(1444, 1444, 1077) \text{ GeV} \quad \xrightarrow{\text{MSSM RGE}}$$

$$m_{\tilde{N}}(M_{GUT}) = \text{diag}(1459, 1459, 1078) \text{ GeV}$$

$$m_{H_u}(M_{GUT}) = 1126 \text{ GeV}, \quad m_{H_d}(M_{GUT}) = 1446 \text{ GeV}$$

$$m_{\tilde{g}}(M_{GUT}) = 211 \text{ GeV}$$

non-universal at M_{GUT}

$$m_{\tilde{g}_1} = 83 \text{ GeV} \quad m_{\tilde{g}_2} = 165 \text{ GeV} \quad \mu = 629 \text{ GeV}$$

$$m_{\tilde{\chi}_i^0} = (640, 632, 159, \underline{81}) \text{ GeV} \quad m_{H_d}^2 = (1432 \text{ GeV})^2$$

$$m_{\tilde{\chi}_i^\pm} = (640, 159) \text{ GeV} \quad m_{H_u}^2 = -(575 \text{ GeV})^2$$

$$M_{\tilde{l}_i} = (1427, 1427, 1074, 1462, 1462, 1095) \text{ GeV}$$

$$M_{\tilde{u}_i} = (1519, 1519, 934, 1501, 1501, 485) \text{ GeV}$$

$$M_{\tilde{d}_i} = (1519, 1519, 908, 1498, 1498, 1164) \text{ GeV}$$

RG evolution

- 2-loop RGE in MSSM, 1-loop RGE in SU(5) and SO(10)
- relate Planck-scale inputs to a set of low-energy inputs:
 - masses of RH up- and down-squarks of 1st gen. $m_{\tilde{u}_1}, m_{\tilde{d}_1}$
 - trilinear term a_1^d of 1st gen.
 - gluino mass $m_{\tilde{g}}$
 - $\arg \mu$ and $\tan \beta$
- RG evolution from M_{ew} to M_{Pl} : find universal soft terms $a_0, m_0, m_{\tilde{g}}$ and D
- RG evolution back to M_{ew} : calculate $|\mu|$ from electroweak symmetry breaking
- Repeat RG evolution: $M_{ew} \rightarrow M_{Pl} \rightarrow M_{ew}$: find all particle masses and MSSM couplings
- adjust CP phase ξ to fit data (enters RGE via U_D) and calculate observables

Universality of SUSY breaking

Assumption of the model:

SUSY is broken flavour blind at $M_{\text{Pl}} \Rightarrow$ Universality of soft- und trilinear terms.
In this sense it is "minimal flavour violating".

$$\begin{aligned} \mathcal{L}_{\text{soft}} = & -\tilde{16}_i m_{\tilde{16}}^2{}^{ij} \tilde{16}_j - m_{\tilde{10}_H}^2 \mathbf{10}_H^* \mathbf{10}_H - m_{\tilde{10}'_H}^2 \mathbf{10}'_H^* \mathbf{10}'_H \\ & - m_{\tilde{16}_H}^2 \overline{\mathbf{16}}_H^* \overline{\mathbf{16}}_H - m_{\tilde{16}_H}^2 \mathbf{16}_H^* \mathbf{16}_H - m_{\tilde{45}_H}^2 \mathbf{45}_H^* \mathbf{45}_H \\ & - \left(\frac{1}{2} \tilde{16}_i A_1^{ij} \tilde{16}_j \mathbf{10}_H + \frac{1}{2} \tilde{16}_i A_2^{ij} \tilde{16}_j \frac{\mathbf{45}_H \mathbf{10}'_H}{M_{\text{Pl}}} + \frac{1}{2} \tilde{16}_i A_N^{ij} \tilde{16}_j \frac{\overline{\mathbf{16}}_H \overline{\mathbf{16}}_H}{M_{\text{Pl}}} + \text{h.c.} \right), \\ m_{\tilde{16}_i}^2 = & m_0^2 \mathbb{1}, \quad m_{\tilde{10}_H}^2 = m_{\tilde{10}'_H}^2 = m_{\tilde{45}_H}^2 = m_{\tilde{16}_H}^2 = m_0^2, \\ A_1 = & A_0 Y_1, \quad A_2 = A_0 Y_2, \quad A_N = A_0 Y_N, \end{aligned}$$

radiative corrections lead to a nonuniversal sfermion mass matrix at the GUT scale (diagonal in U-basis)

[Hall, Kosteletzky, Raby 86; Barbieri, Hall, Strumia95]

$$\begin{aligned} m_{\tilde{16}_3}^2 &= m_0^2 - \Delta \\ m_{\tilde{16}_1}^2 &\approx m_{\tilde{16}_2}^2 = m_0^2 + \delta \end{aligned}$$

$B_s - \bar{B}_s$ mixing

$$M_{12}^s{}_{\text{CMM}} = \frac{G_F^2 M_W^2 M_{B_s}}{12\pi^2} f_{B_s}^2 \hat{B}_{B_s} (V_{ts}^* V_{tb})^2 (C_L(\mu_b) + C_R(\mu_b))$$

$$C = C_L + e^{-2i\xi} |C_R^{\text{CMM}}|$$

$$f_{B_s} \sqrt{\hat{B}_{B_s}} = (0.2580 \pm 0.0195) \text{ GeV}$$

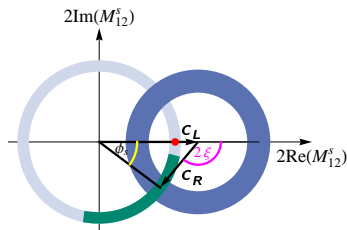


Figure: SM, exp. data, SM+CMM
(Illustration not to scale).

summer 2010:

$$-2\beta_s^{\text{CDF}} \equiv -2\beta_s^{\text{SM}} + \phi_s \in [-1.04, -0.04] \cup [-3.10, -2.16] \quad (68\% \text{ CL})$$

$$\phi_s^{\text{D}\phi} \equiv -2\beta_s^{\text{SM}} + \phi_s = -0.76_{-0.36}^{+0.38}(\text{stat}) \pm 0.02(\text{syst})$$

$$a_{f_s} = -0.0085 \pm 0.0028 \quad (68\% \text{ CL}).$$

Assuming no NP in $a_{f_s}^d$ and naively using a weighted average for $\sin \phi_s$:

$$\sin \phi_s = -0.77 \pm 0.47 \quad (95\% \text{ CL}).$$

Earlier Work

- Barbieri et al 1995:
SO(10) model with small leptonic mixing
- Moroi JHEP **0003** (2000) 019; Phys. Lett. B **493** (2000) 366:
SUSY SU(5) model with right-handed neutrinos, radiative effects due to atmospheric mixing angle
- Harnik et al 2011:
analysis of effective model with large $\tilde{b} - \tilde{s}$ mixing, inspired by the CMM model
- Ciuchini et al 2004, 2007:
SUSY breaking parametrised in mass insertion approximation, SU(5) GUT relations imposed at M_{GUT}