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Production of lepton, quark and meson pairs
in peripheral ultrarelativistic heavy ion collisions

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In collaboration with M. Kłusek, W. Schäfer

(Ultra)Peripheral Heavy Ion Collisions

- ① Usual heavy ion collisions - large multiplicities
Ultraperipheral heavy ion collisions - smaller multiplicities
- ② What do we know about them?
There are some theoretical predictions
Experimentally very little is known.
- ③ The dominant process: coherent photon-photon collisions
(increased by large charges of nuclei ($Z_1 e$ and $Z_2 e$))
- ④ Large enhancement (naively: $Z_1^2 Z_2^2$ in the cross section).
- ⑤ But nuclei are not point like → charge form factor.
- ⑥ One can select final state ! ?
- ⑦ Simple final states are interesting.

$$\begin{aligned}AA &\rightarrow A\pi^+\pi^- \\&\gamma\gamma \rightarrow \pi\pi \\AA &\rightarrow A\mu^+\mu^-A \\AA &\rightarrow AQ\bar{Q}A\end{aligned}$$

Contents

- 1 $AA \rightarrow A\rho^0\rho^0A$
- 2 $AA \rightarrow A\pi\pi A$
- 3 $AA \rightarrow A\mu^+\mu^-A$
- 4 $AA \rightarrow AQ\bar{Q}A$
- 5 Other reactions
- 6 Conclusions

Contents

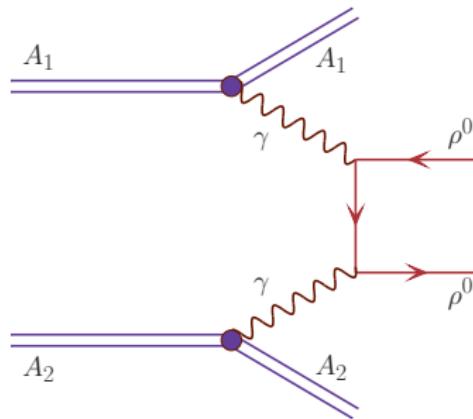
$$AA \rightarrow A\pi^+\pi^-$$

$$\gamma\gamma \rightarrow \pi\pi$$

$$AA \rightarrow A\mu^+\mu^-A$$

$$AA \rightarrow AQ\bar{Q}A$$

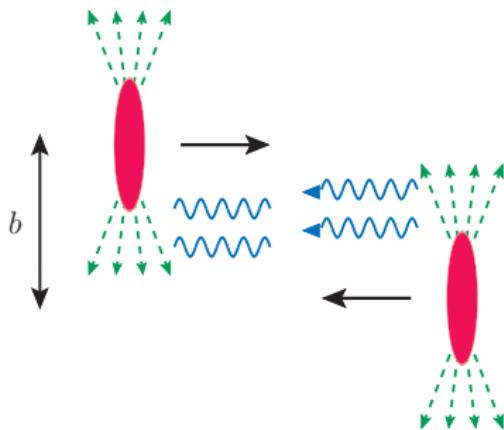
$$AA \rightarrow A\rho^0\rho^0A$$



M. Klusek, W. Schäfer and A. S., Phys. Lett. **B674** (2009) 92.

Accelerator	Nuclei	$\sqrt{s_{NN}}$	γcm
RHIC	Au–Au	200 GeV	107
LHC	Pb–Pb	5.5 TeV	2 932

Equivalent photon approximation (EPA)



The strong electromagnetic field is a source of photons which may interact.

Peripheral collisions:

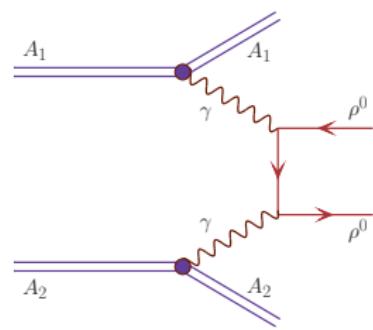
$$b > R_1 + R_2 \cong 14 \text{ fm}$$

Contents
$AA \rightarrow A\pi^+\pi^-$
$\gamma\gamma \rightarrow \pi\pi$
$AA \rightarrow A\mu^+\mu^-A$
$AA \rightarrow AQ\bar{Q}A$

The total cross section in EPA

$$\sigma (AA \rightarrow \rho^0 \rho^0 AA; s_{AA})$$

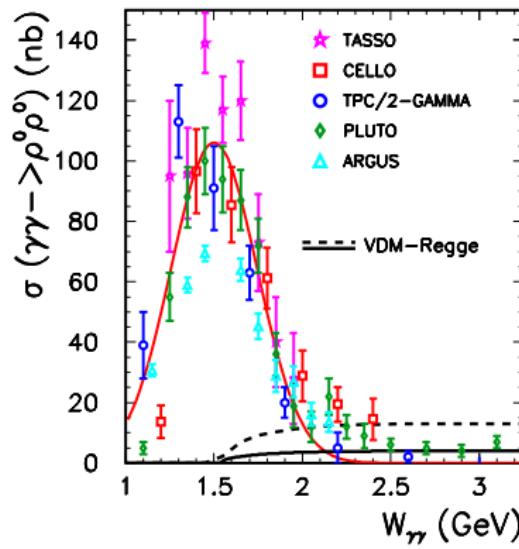
$$= \int \hat{\sigma} (\gamma\gamma \rightarrow \rho^0 \rho^0; x_1 x_2 s_{AA}) dn_{\gamma\gamma} (x_1, x_2, \mathbf{b})$$



- $x_{1,2} = \frac{\omega_{1,2}}{\gamma M_A}$

The elementary cross section

$$\hat{\sigma} (\gamma\gamma \rightarrow \rho^0\rho^0; W_{\gamma\gamma})$$



VDM-Regge model $\Rightarrow \hat{\sigma} (\gamma\gamma \rightarrow \rho^0\rho^0)$

$$\mathcal{M}_{\gamma\gamma \rightarrow \rho^0\rho^0}(\hat{s}, \hat{t}; q_1, q_2) = C_{\gamma \rightarrow \rho^0}^2 \mathcal{M}_{\rho^{0*}\rho^{0*} \rightarrow \rho^0\rho^0}(\hat{s}, \hat{t}; q_1, q_2)$$

- $C_{\gamma \rightarrow \rho^0}^2 = \frac{\alpha_{em}^2}{2.54}$

$$\mathcal{M}_{\rho^{0*}\rho^{0*} \rightarrow \rho^0\rho^0}(\hat{s}, \hat{t}; q_1, q_2) = F(\hat{t}; q_1^2) F(\hat{t}; q_2^2)$$

$$\times \hat{s} \left(\eta_P(\hat{s}, \hat{t}) C_P \left(\frac{\hat{s}}{s_0} \right)^{\alpha_P(\hat{t})-1} + \eta_R(\hat{s}, \hat{t}) C_R \left(\frac{\hat{s}}{s_0} \right)^{\alpha_R(\hat{t})-1} \right)$$

- $\eta_P(\hat{s}, \hat{t} = 0) \cong i$
- $C_P = 8.56 \text{ mb}$
- $\alpha_P(\hat{t}) = 1.088 + 0.25t$
- $\eta_R(\hat{s}, \hat{t} = 0) \cong i - 1$
- $C_R = 13.39 \text{ mb}$
- $\alpha_R(\hat{t}) = 0.5 + 0.9t$

$$F(\hat{t}; q^2) = \exp \left(\frac{B\hat{t}}{4} \right) \cdot \exp \left(\frac{q^2 - m_\rho^2}{2\Lambda^2} \right)$$

- $B \sim 4 \text{ GeV}^{-2}$
- $\Lambda \sim 1 \text{ GeV}$

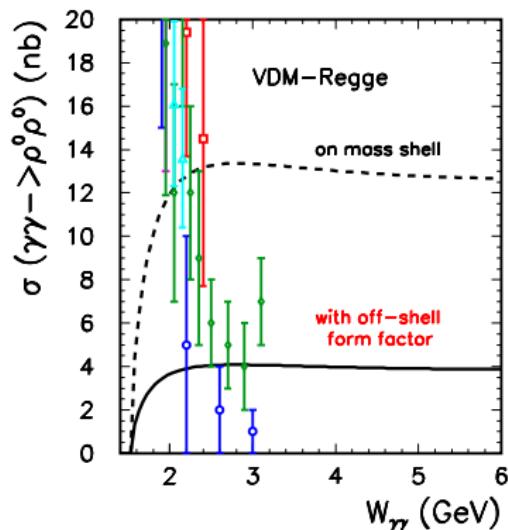
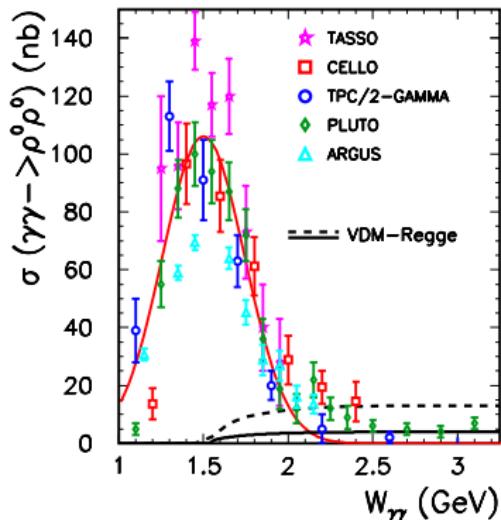
VDM-Regge model

$$\frac{d\hat{\sigma}_{\gamma\gamma \rightarrow \rho^0 \rho^0}}{d\hat{t}} = \frac{1}{16\pi\hat{s}^2} |\mathcal{M}_{\gamma\gamma \rightarrow \rho^0 \rho^0}|^2$$

$$\hat{\sigma}_{\gamma\gamma \rightarrow \rho^0 \rho^0} = \int_{t_{min}(\hat{s})}^{t_{max}(\hat{s})} \frac{d\hat{\sigma}_{\gamma\gamma \rightarrow \rho^0 \rho^0}}{d\hat{t}} d\hat{t}$$

Contents
 $AA \rightarrow A\pi^+\pi^-$
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The elementary cross section



$$\Leftarrow \hat{\sigma}(\gamma\gamma \rightarrow \rho^0\rho^0; W_{\gamma\gamma}) \Rightarrow$$

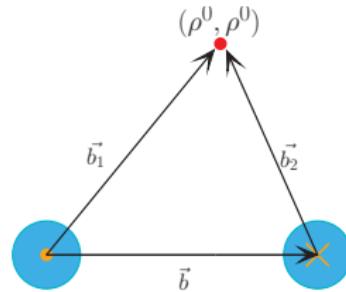
Low-energy (experimental data)

High-energy (VDM-Regge)

Photon flux - continuation of the cross section in EPA

$$dn_{\gamma\gamma}(x_1, x_2, \mathbf{b}) = \int \frac{1}{\pi} d^2 \mathbf{b}_1 |E(x_1, \mathbf{b}_1)|^2 \frac{1}{\pi} d^2 \mathbf{b}_2 |E(x_2, \mathbf{b}_2)|^2$$

$$x \quad S_{abs}^2(\mathbf{b})\delta^{(2)}(\mathbf{b} - \mathbf{b}_1 + \mathbf{b}_2) \frac{d\mathbf{x}_1}{x_1} \frac{d\mathbf{x}_2}{x_2}$$



Photon flux - continuation of the cross section in EPA

$$dn_{\gamma\gamma}(\textcolor{brown}{x}_1, \textcolor{brown}{x}_2, \mathbf{b}) = \int \frac{1}{\pi} d^2 \mathbf{b}_1 |\mathbf{E}(\textcolor{brown}{x}_1, \mathbf{b}_1)|^2 \frac{1}{\pi} d^2 \mathbf{b}_2 |\mathbf{E}(\textcolor{brown}{x}_2, \mathbf{b}_2)|^2$$

$$\times \quad S_{abs}^2(\mathbf{b}) \delta^{(2)}(\mathbf{b} - \mathbf{b}_1 + \mathbf{b}_2) \frac{d\textcolor{brown}{x}_1}{x_1} \frac{d\textcolor{brown}{x}_2}{x_2}$$

- $\mathbf{E}(\textcolor{brown}{x}, \mathbf{b}) = Z \sqrt{4\pi\alpha_{em}} \int \frac{d^2 \mathbf{q}}{(2\pi^2)} e^{-i\mathbf{b}\mathbf{q}} \frac{\mathbf{q}}{\mathbf{q}^2 + \textcolor{brown}{x}^2 M_A^2} F_{em}(\mathbf{q}^2 + \textcolor{brown}{x}^2 M_A^2)$
- $S_{abs}^2(\mathbf{b}) \cong \theta(\mathbf{b} - 2R_A)$
- $\frac{1}{\pi} \int d^2 \mathbf{b} |\mathbf{E}(\textcolor{brown}{x}, \mathbf{b})|^2 = \int d^2 \mathbf{b} N(\omega, \mathbf{b})$
- $d\omega_1 d\omega_2 \rightarrow dW_{\gamma\gamma} dY$

$$AA \rightarrow A\pi^+\pi^-$$

$$\gamma\gamma \rightarrow \pi\pi$$

$$AA \rightarrow A\mu^+\mu^-A$$

$$AA \rightarrow AQ\bar{Q}A$$

The cross section in b-space EPA

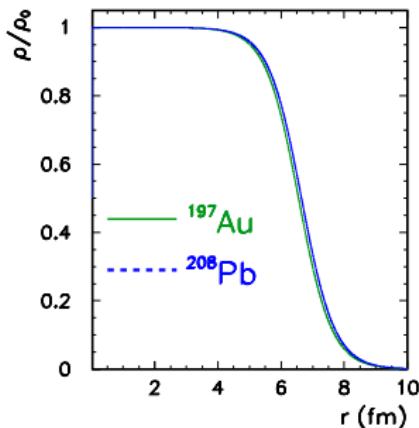
Nuclear cross section – EPA

$$\begin{aligned} & \sigma(AA \rightarrow \rho^0 \rho^0 AA; s_{AA}) = \\ &= \int \hat{\sigma}(\gamma\gamma \rightarrow \rho^0 \rho^0; W_{\gamma\gamma}) \theta(|\mathbf{b}_1 - \mathbf{b}_2| - 2R_A) \\ &\times N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_1) 2\pi b_m db_m d\bar{b}_x d\bar{b}_y \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY \end{aligned}$$

Nucleus charge form factor

REALISTIC F_{em}

$$F(q) = \int \frac{4\pi}{q} \rho(r) \sin(qr) r dr$$



MONOPOLE F_{em}

$$F(q^2) = \frac{\Lambda^2}{\Lambda^2 + q^2}$$

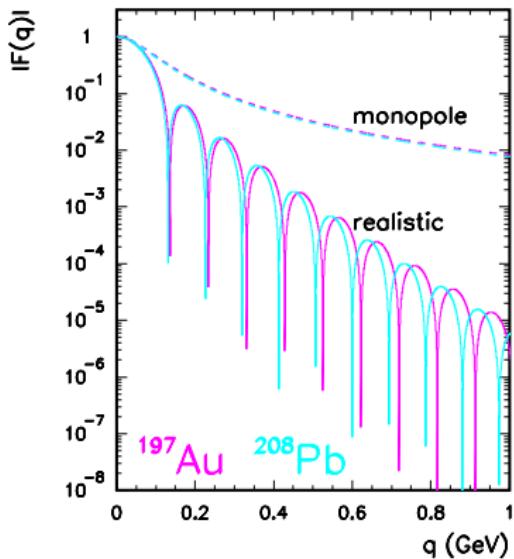
$$\Lambda = \sqrt{\frac{6}{\langle r^2 \rangle}}$$

- $^{197}Au \Rightarrow \sqrt{\langle r^2 \rangle} = 5.3 \text{ fm}, \Lambda = 0.091 \text{ GeV}$,
- $^{208}Pb \Rightarrow \sqrt{\langle r^2 \rangle} = 5.5 \text{ fm}, \Lambda = 0.088 \text{ GeV}$.

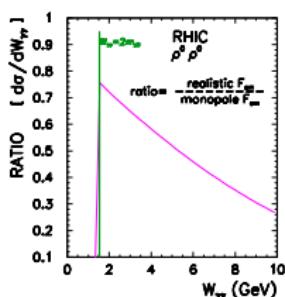
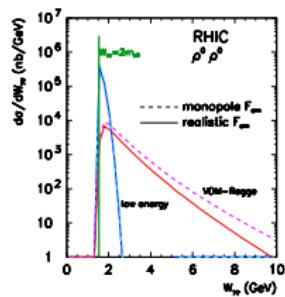
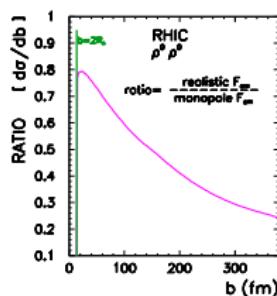
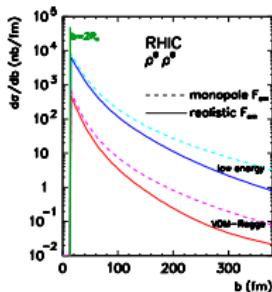
In the literature:

$$\Lambda = (0.08 - 0.09) \text{ GeV}$$

Form factor



RHIC ($AuAu \rightarrow Au \rho^0\rho^0 Au$)



Impact parameter: b .

$$\sigma(F_{em}) = \sigma_{I-e} + \sigma_{VDM-R}$$

$$RATIO = \frac{d\sigma(F_{em}^{REALISTIC})}{d\sigma(F_{em}^{MONPOLE})}$$

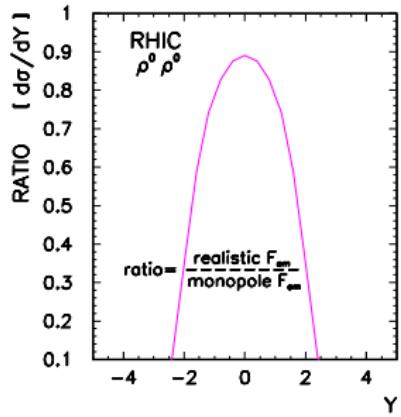
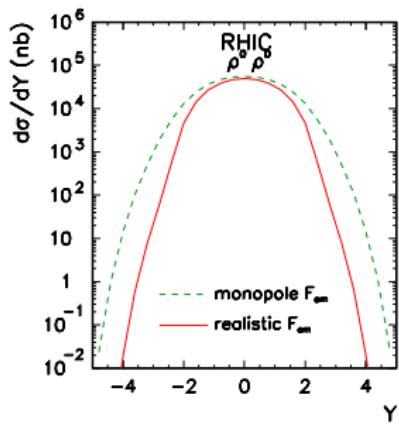
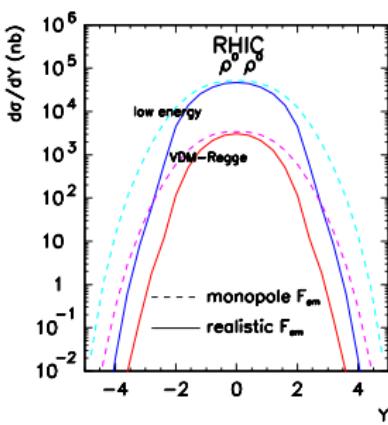
Invariant mass of the $\gamma\gamma$ system: $W_{\gamma\gamma} = M_{\rho^0\rho^0}$.

RHIC ($Au\ Au \rightarrow Au\ \rho^0\rho^0\ Au$)

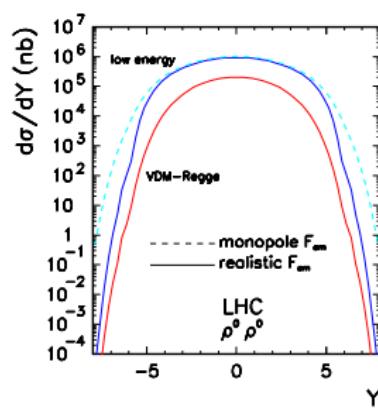
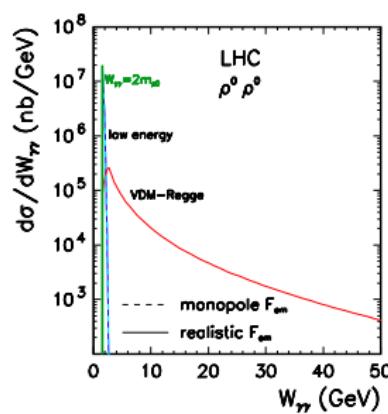
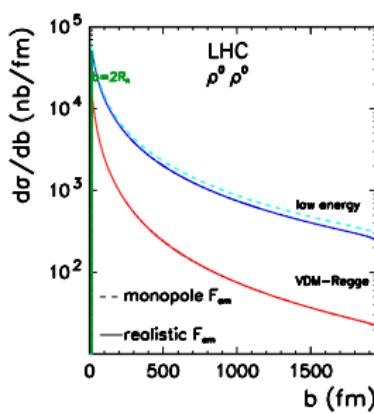
Rapidity of the $\rho^0\rho^0$ pair: $Y = \frac{y_{\rho^0} + y_{\rho^0}}{2}$.

Low-energy+
+VDM-Regge

$$\text{Ratio} = \frac{d\sigma(F_{em}^{REALISTIC})}{d\sigma(F_{em}^{MONOPOLE})}$$

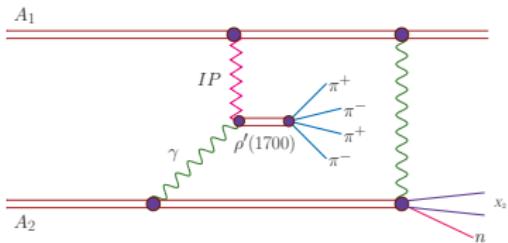
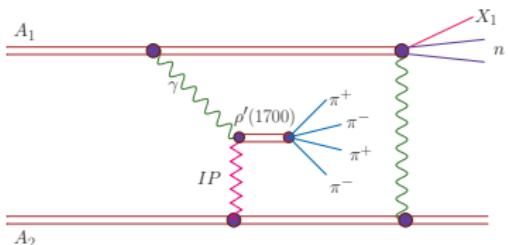
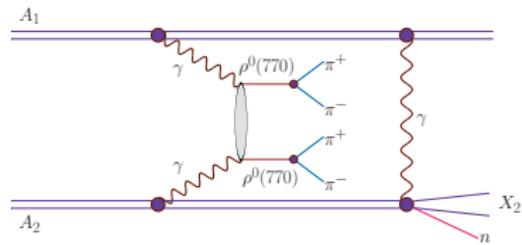
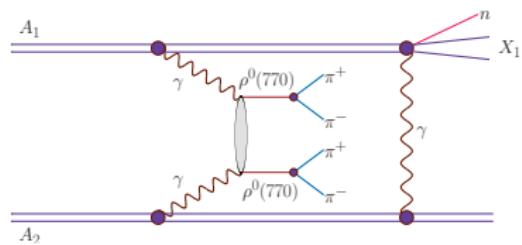


LHC ($Pb\;Pb \rightarrow Pb\;\rho^0\rho^0\;Pb$)

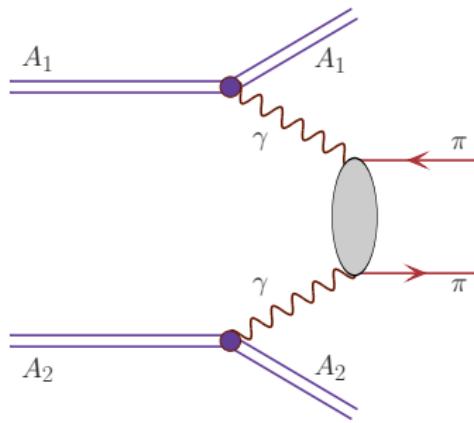


Contents

$$AA \rightarrow A^* A^* \pi^+ \pi^- \pi^+ \pi^-$$



$PbPb \rightarrow PbPb\pi\pi$ at large invariant masses



Accelerator LHC:

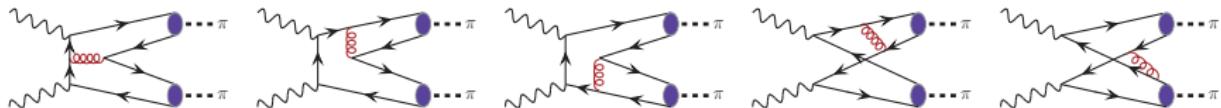
- $\sqrt{s_{NN}} = 3.5 \text{ TeV}$
- $\gamma_{cm} = 2932 \text{ GeV}$

Kłusek-Gawenda, Szczerba, Phys. Lett. B700 (2011) 114004

Elementary cross section for $\gamma\gamma \rightarrow \pi\pi$

The $\gamma\gamma \rightarrow (q\bar{q})(q\bar{q}) \rightarrow \pi\pi$ amplitude in the LO pQCD

$$\begin{aligned}\mathcal{M}(\lambda_1, \lambda_2) &= \int_0^1 dx \int_0^1 dy \phi_\pi(x, \mu_x^2) T_H^{\lambda_1 \lambda_2}(x, y, \mu^2) \phi_\pi(y, \mu_y^2) \\ &\times F_{reg}^{pQCD}(t, u)\end{aligned}$$



- $\mu_x = \min(x, 1-x) \sqrt{s(1-z^2)}$,

- $z = \cos\theta$,

- $F_{reg}^{pQCD}(t, u) = \left[1 - \exp\left(\frac{t-t_m}{\Lambda_{reg}^2}\right)\right] \left[1 - \exp\left(\frac{u-u_m}{\Lambda_{reg}^2}\right)\right]$

The quark distribution amplitude of the pion

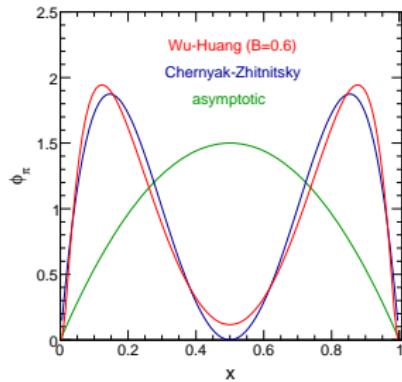
$$\phi_\pi(x, \mu_0^2)_{\text{WH}} = \frac{\sqrt{3}A m_q \beta}{2\sqrt{2}\pi^{3/2} f_\pi} \sqrt{x(1-x)} \left(1 + B \times C_2^{3/2} (2x - 1) \right)$$

$$\times \left(\text{Erf} \left[\sqrt{\frac{m_q^2 + \mu_0^2}{8\beta^2 x(1-x)}} \right] - \text{Erf} \left[\sqrt{\frac{m_q^2}{8\beta^2 x(1-x)}} \right] \right)$$

- $B = 0.6$
- $m_q = 0.3 \text{ GeV}$
- $A = 16.62 \text{ GeV}^{-1}$
- $\beta = 0.745 \text{ GeV}$

$$\phi_\pi(x)_{\text{CZ}} = 30x(1-x)(2x-1)^2$$

$$\phi_\pi(x)_{\text{as}} = 6x(1-x)$$

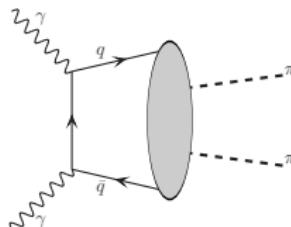


from amplitude to cross section

high energy normalization

$$\sigma(\gamma\gamma \rightarrow \pi\pi) = \int \frac{2\pi}{4 \cdot 64\pi^2 W^2} \frac{p}{q} \sum_{\lambda_1, \lambda_2} |\mathcal{M}(\lambda_1, \lambda_2)|^2 dz$$

Hand-bag model, Diehl-Kroll-Vogt



Hand-bag model:

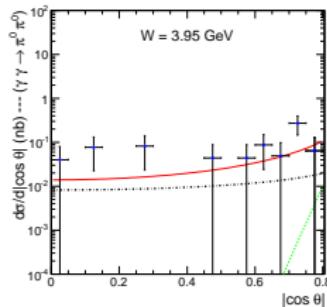
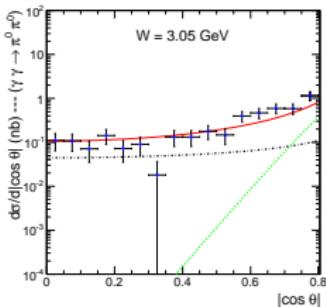
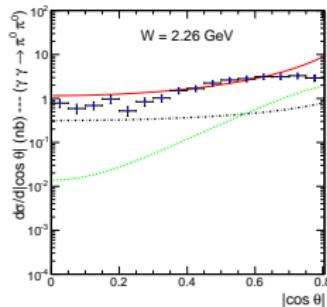
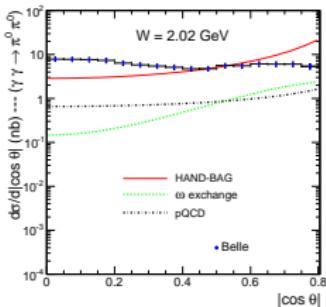
$$\sigma(\gamma\gamma \rightarrow \pi^+\pi^-) = \frac{4\pi\alpha_{em}^2}{s} \left(\frac{\cos\theta_0}{\sin^2\theta_0} + \frac{1}{2} \ln \frac{1+\cos\theta_0}{1-\cos\theta_0} \right) |R_{\pi\pi}(s)|^2$$

$$R_{\pi\pi}(s) = \frac{5}{9s} a_u \left(\frac{s_0}{s} \right)^{n_u} + \frac{1}{9s} a_s \left(\frac{s_0}{s} \right)^{n_s}$$

- $s_0 = 9 \text{ GeV}^2$
- $a_u = 1.375 \text{ GeV}^2$
- $a_s = 0.5025 \text{ GeV}^2$
- $n_u = 0.4175$
- $n_s = 1.195$

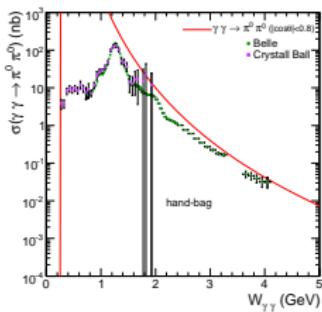
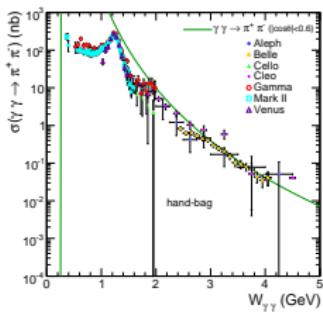
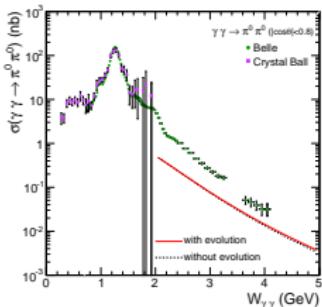
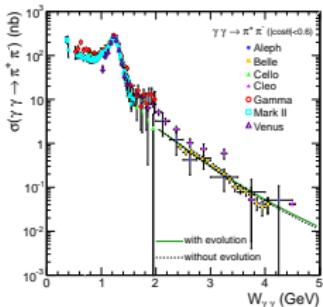
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 $AA \rightarrow A\pi^+\pi^-$
 $\gamma\gamma \rightarrow \pi\pi$
 $AA \rightarrow A\mu^+\mu^-A$
 $AA \rightarrow AQ\bar{Q}A$

$\frac{d\sigma(\gamma\gamma \rightarrow \pi^0\pi^0)}{dz} \implies$ pQCD vs hand-bag vs ω exchange



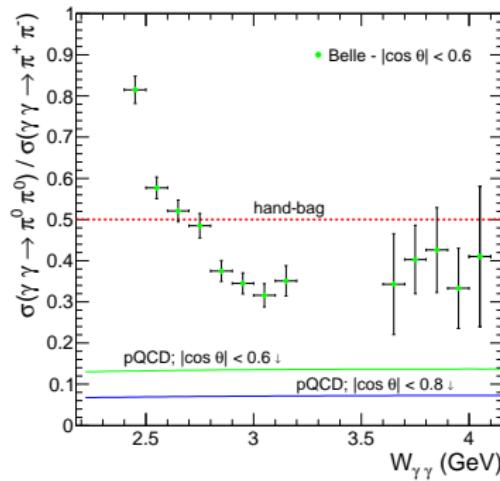
Contents
 $AA \rightarrow A\pi^+\pi^-$
 $\gamma\gamma \rightarrow \pi\pi$
 $AA \rightarrow A\mu^+\mu^-A$
 $AA \rightarrow AQ\bar{Q}A$

$\sigma(\gamma\gamma \rightarrow \pi^+\pi^-)$, $\sigma(\gamma\gamma \rightarrow \pi^0\pi^0) \implies$ pQCD vs hand-bag



Contents
 $AA \rightarrow A\pi^+\pi^-$
 $\gamma\gamma \rightarrow \pi\pi$
 $AA \rightarrow A\mu^+\mu^-A$
 $AA \rightarrow A\bar{Q}Q\bar{A}$

$\sigma(\gamma\gamma \rightarrow \pi^0\pi^0) / \sigma(\gamma\gamma \rightarrow \pi^+\pi^-) \implies$ pQCD vs hand-bag



Contents

$$AA \rightarrow A\pi^+\pi^-$$

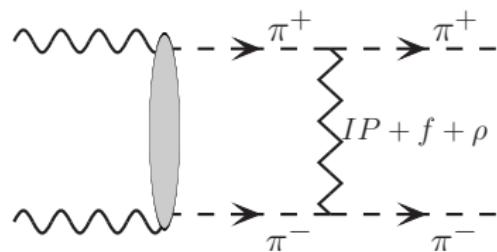
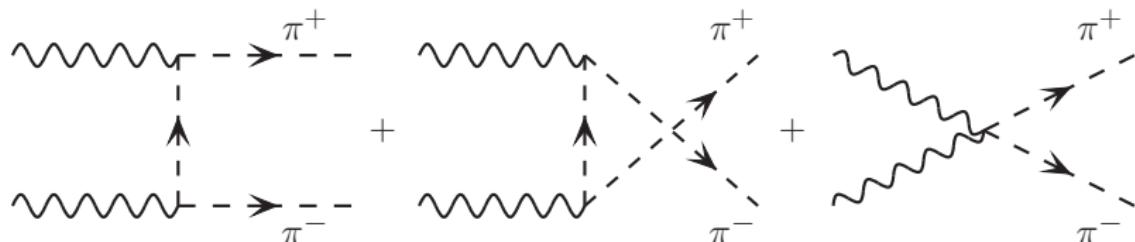
$$\gamma\gamma \rightarrow \pi\pi$$

$$AA \rightarrow A\mu^+\mu^-A$$

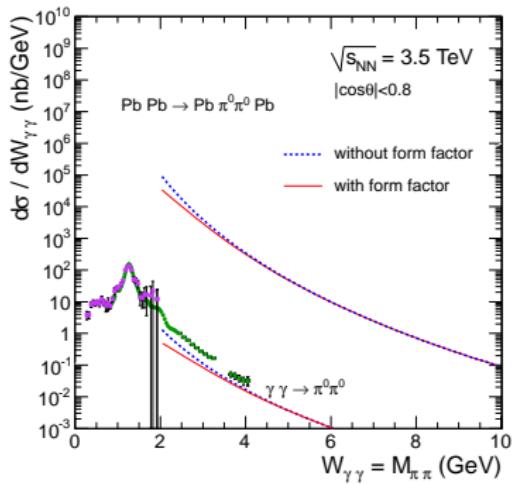
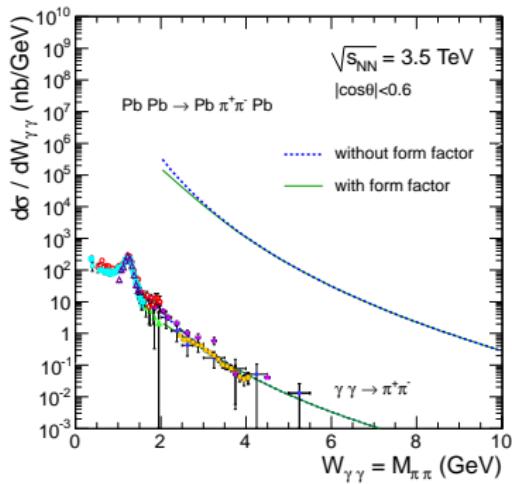
$$AA \rightarrow AQ\bar{Q}A$$

Other mechanisms?

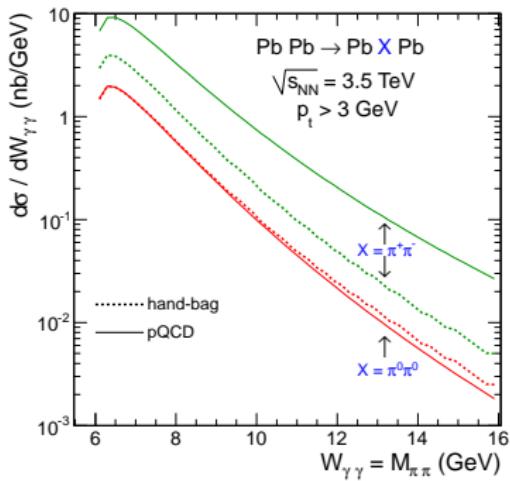
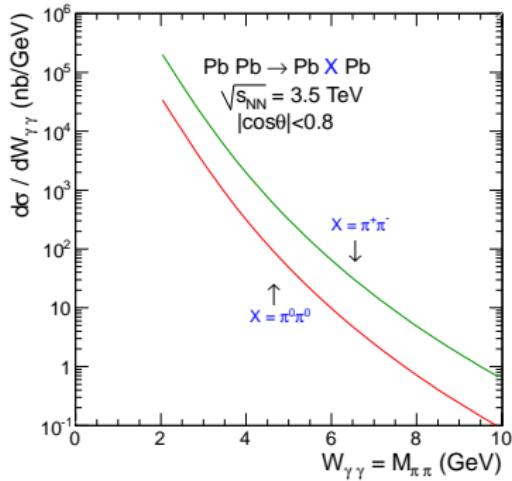
Pion exchange and high-energy pion-pion rescattering



$AA \rightarrow A\pi\pi A$, results



$AA \rightarrow A\pi\pi A$, results



Contents

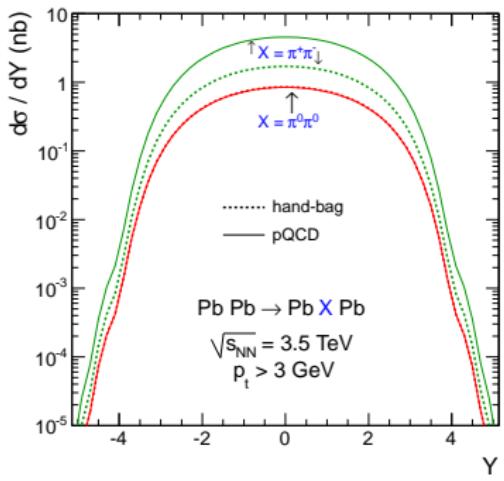
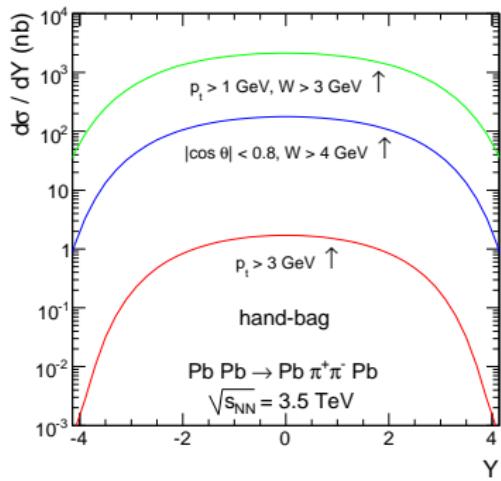
$$AA \rightarrow A\pi^+\pi^-$$

$$\gamma\gamma \rightarrow \pi\pi$$

$$AA \rightarrow A\mu^+\mu^-A$$

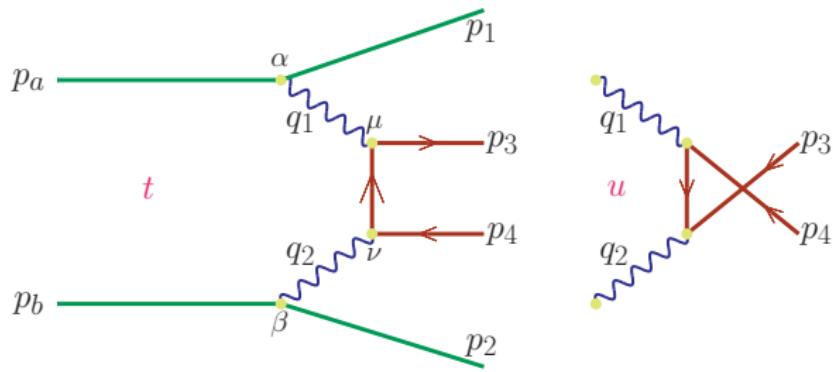
$$AA \rightarrow AQ\bar{Q}A$$

$AA \rightarrow A\pi\pi A$, results



Contents
 $AA \rightarrow A\pi^+\pi^-$
 $\gamma\gamma \rightarrow \pi\pi$
 $AA \rightarrow A\mu^+\mu^-A$
 $AA \rightarrow AQ\bar{Q}A$

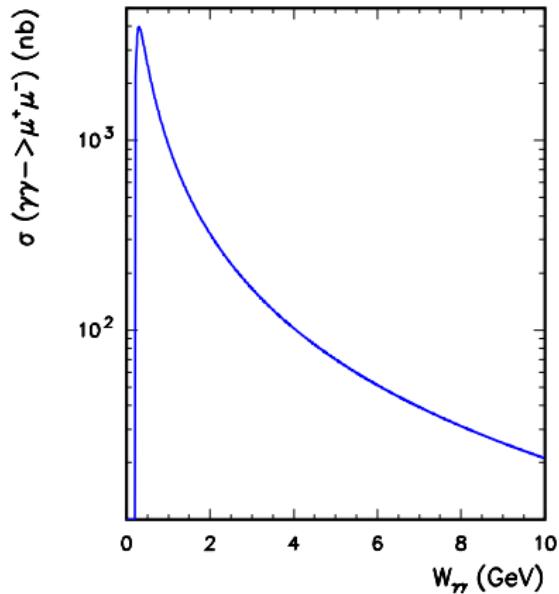
$AA \rightarrow A\mu^+\mu^-A$



Mariola Kłusek-Gawenda and A.S.
 Phys. Rev. C82 (2010) 014904

Contents
 $AA \rightarrow A\pi^+\pi^-$
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$AA \rightarrow A\mu^+\mu^-A$



Momentum-space calculation

$$\begin{aligned}\sigma &= \int \frac{1}{2s} \overline{|\mathcal{M}|^2} (2\pi)^4 \delta^4(p_a + p_b - p_1 - p_2 - p_3 - p_4) \\ &\times \frac{d^3 p_1}{(2\pi)^3 2E_1} \frac{d^3 p_2}{(2\pi)^3 2E_2} \frac{d^3 p_3}{(2\pi)^3 2E_3} \frac{d^3 p_4}{(2\pi)^3 2E_4}. \quad (1)\end{aligned}$$

$$\frac{d^3 p_i}{E_i} = dy_i d^2 p_{it} = dy_i p_{it} dp_{it} d\phi_i. \quad (2)$$

$$\begin{aligned}\sigma &= \int \frac{1}{2s} \overline{|\mathcal{M}|^2} \delta^4(p_a + p_b - p_1 - p_2 - p_3 - p_4) \frac{1}{(2\pi)^8} \frac{1}{2^4} \\ &\times (dy_1 p_{1t} dp_{1t} d\phi_1) (dy_2 p_{2t} dp_{2t} d\phi_2) (dy_3 d^2 p_{3t}) (dy_4 d^2 p_{4t}) \quad (3)\end{aligned}$$

$$\mathbf{p}_m = \mathbf{p}_{3t} - \mathbf{p}_{4t} \quad (4)$$

Momentum-space calculation

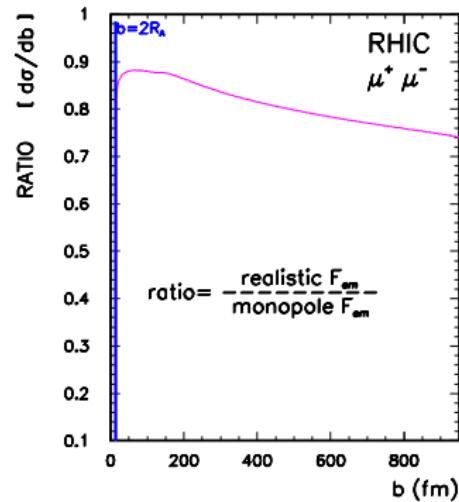
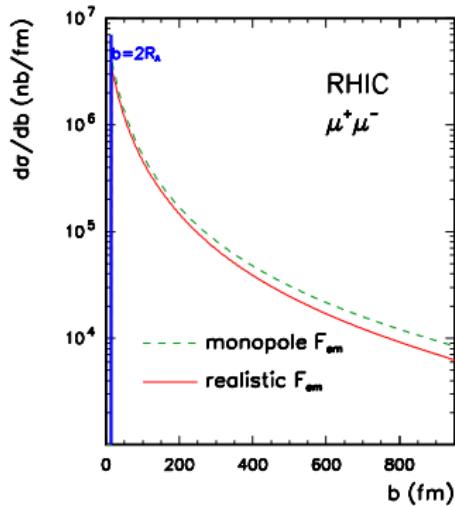
The helicity dependent amplitude of the process can be written as

$$\begin{aligned}
 \mathcal{M}_{\lambda_3, \lambda_4}(t) &= e F(\mathbf{q}_1) (p_a + p_1)^\alpha \frac{-i g_{\alpha\mu}}{q_1^2 + i\varepsilon} \bar{u}(p_3, \lambda_3) i \gamma^\mu \frac{i [(\not{p}_3 - \not{q}_1) + m_\mu]}{(\mathbf{q}_1 - \mathbf{p}_3)^2 - m_\mu^2} \\
 &\times i \gamma^\nu v(p_4, \lambda_4) \frac{-i g_{\nu\beta}}{q_2^2 + i\varepsilon} (p_b + p_2)^\beta e F(\mathbf{q}_2), \tag{5}
 \end{aligned}$$

$$\begin{aligned}
 \mathcal{M}_{\lambda_3, \lambda_4}(u) &= e F(\mathbf{q}_1) (p_a + p_1)^\alpha \frac{-i g_{\alpha\mu}}{q_1^2 + i\varepsilon} \bar{u}(p_3, \lambda_3) i \gamma^\nu \frac{i [(\not{p}_3 - \not{q}_2) + m_\mu]}{(\mathbf{q}_2 - \mathbf{p}_3)^2 - m_\mu^2} \\
 &\times i \gamma^\mu v(p_4, \lambda_4) \frac{-i g_{\nu\beta}}{q_2^2 + i\varepsilon} (p_b + p_2)^\beta e F(\mathbf{q}_2). \tag{6}
 \end{aligned}$$

Finally, one has to calculate the 8-dimensional integral numerically.

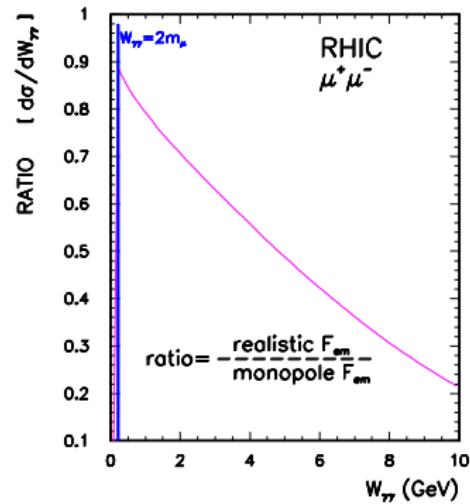
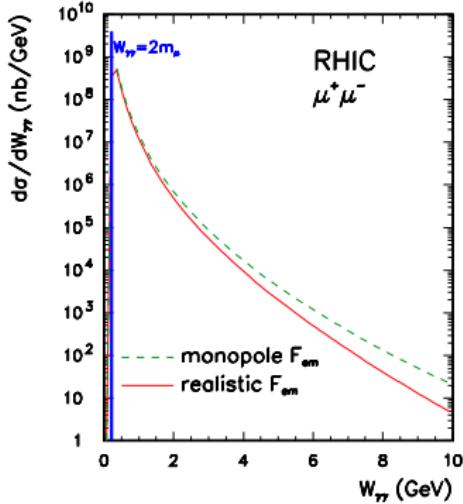
Impact parameter dependence (EPA)



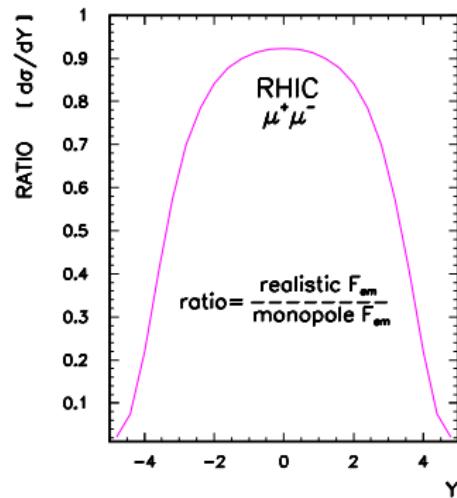
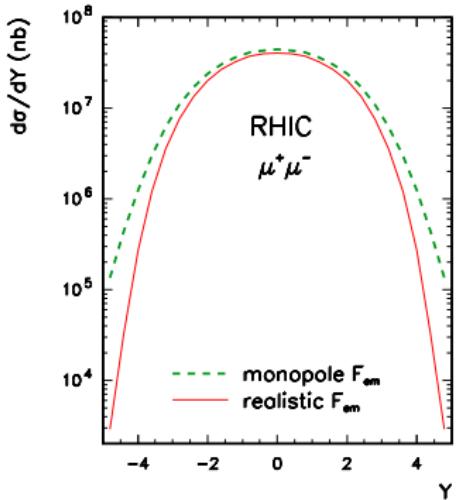
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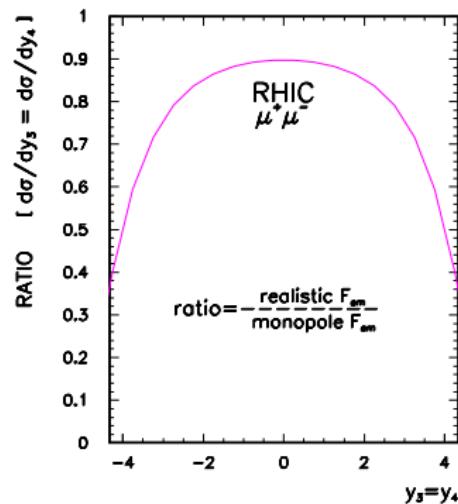
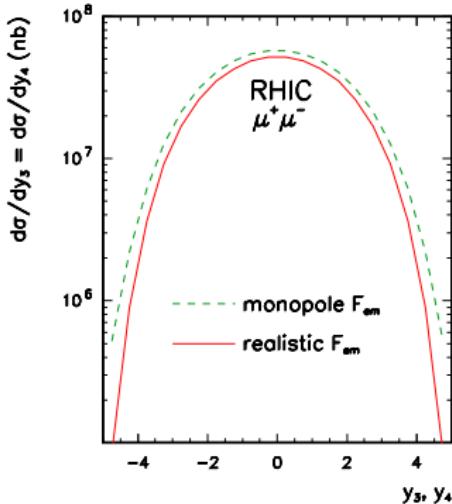
Invariant mass distribution of $\mu^+\mu^-$



Pair rapidity distribution

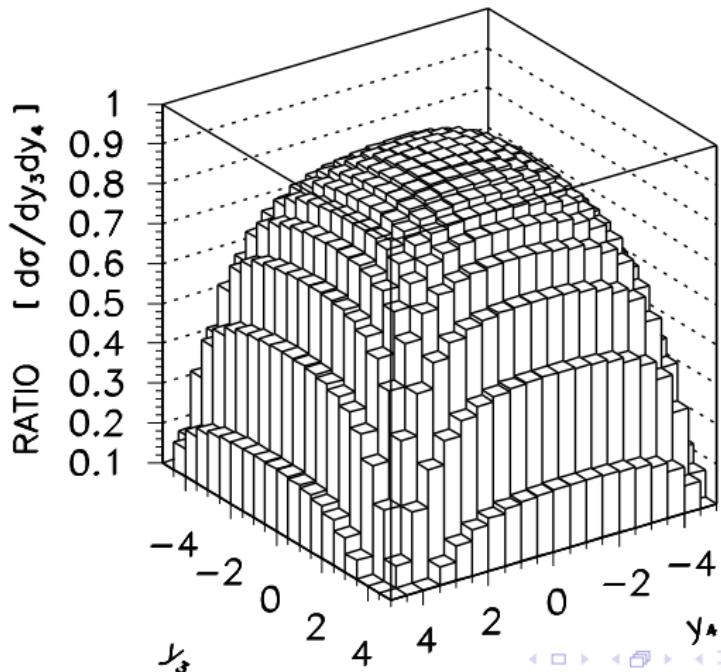


Rapidity distribution of muons



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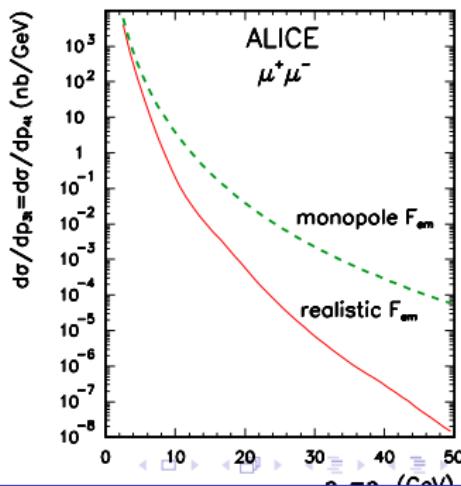
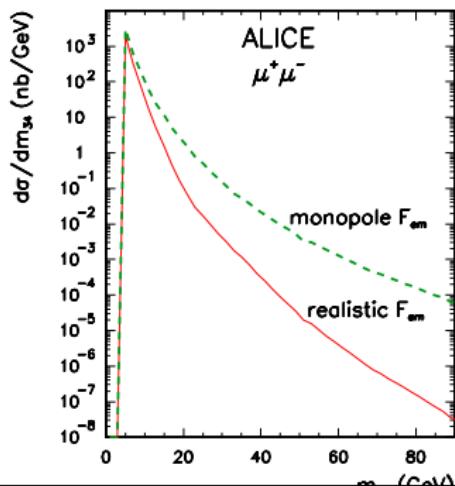
Distribution in $y_{\mu^+}y_{\mu^-}$



Predictions for ALICE

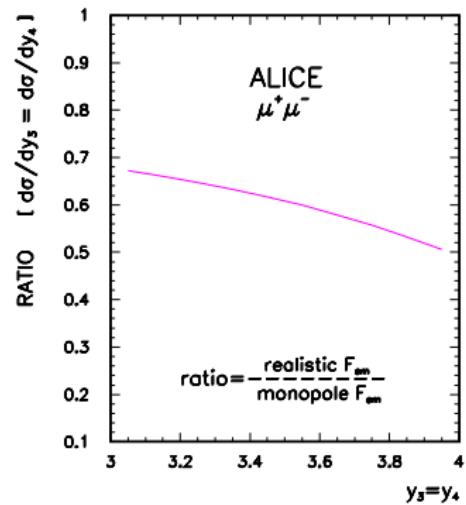
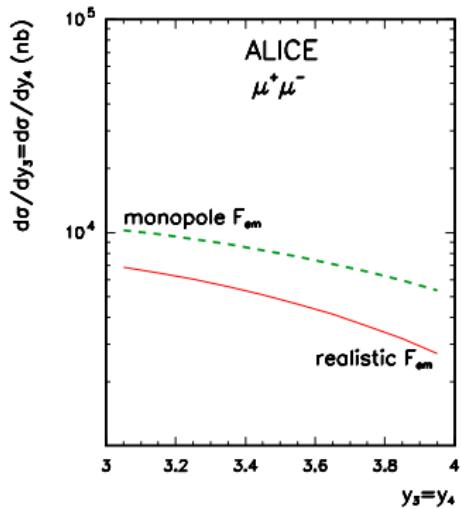
ALICE

- $p_{3t}, p_{4t} \geq 2 \text{ GeV}$
- $(y_3, y_4) = (3, 4)$



Contents
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 $AA \rightarrow AQ\bar{Q}A$

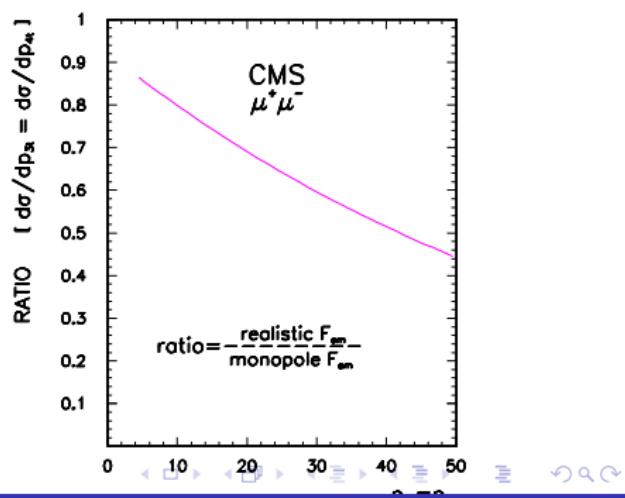
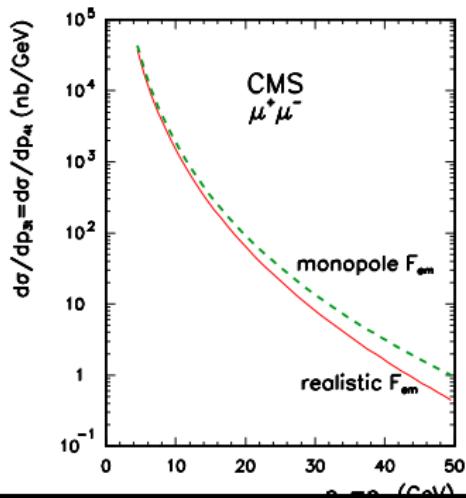
Predictions for ALICE



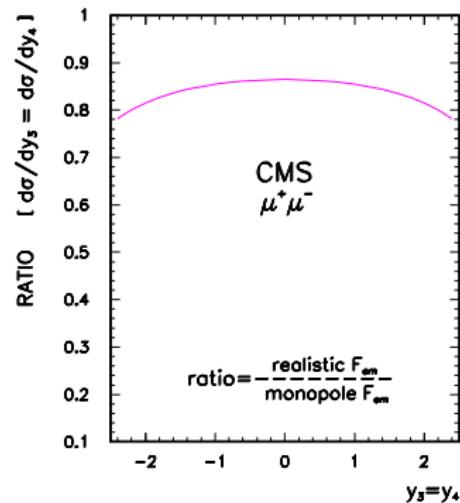
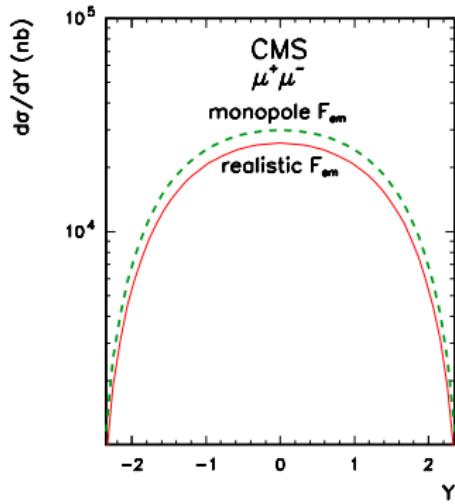
Predictions for CMS

CMS

- $p_{3t}, p_{4t} > 4 \text{ GeV}$
- $|y_3, y_4| < 2.5$



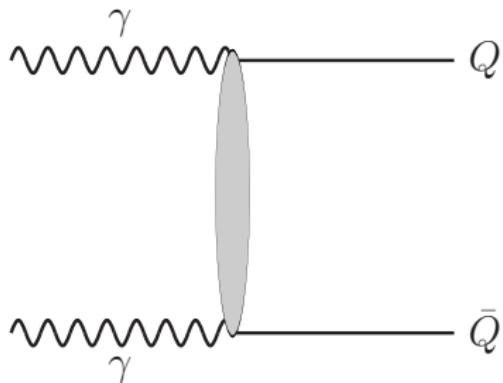
Predictions for CMS



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$$AA \rightarrow AQ\bar{Q}A$$

The mechanism analogous to dilepton production



In fact two diagrams (t and u channel quark exchanges) in the Born approximation

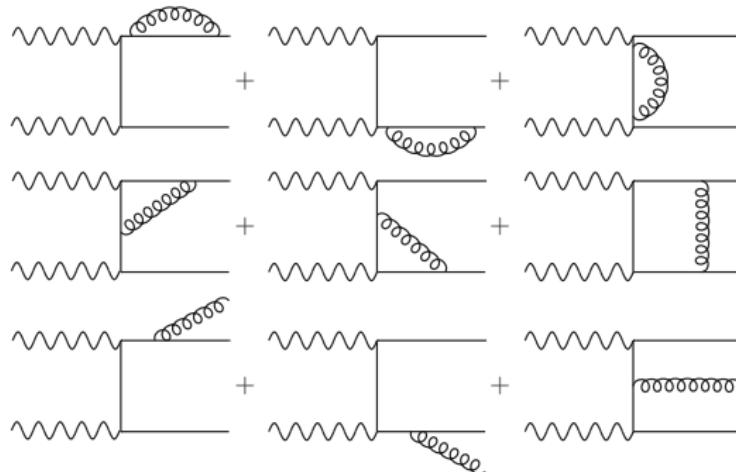
M. Kłusek-Gawenda, A.S., M. Machado and V. Serbo,
arXiv:1011.1191, Phys. Rev. C83 (2011) 024903.

Other mechanisms, QCD corrections

In reality not quarks but **mesons** could be measured.

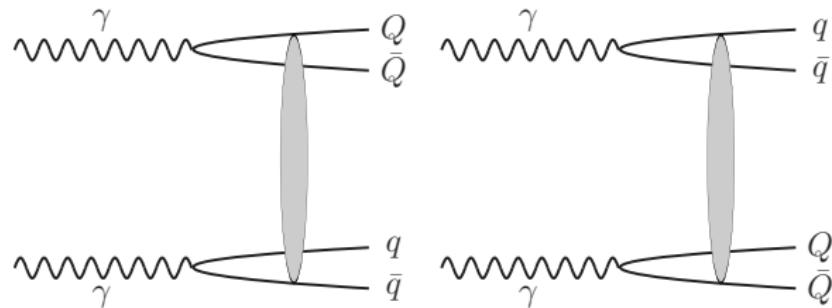
D or B mesons are associated with a few pions/kaons.

Therefore other mechanisms **leading to similar final state** have to be included.



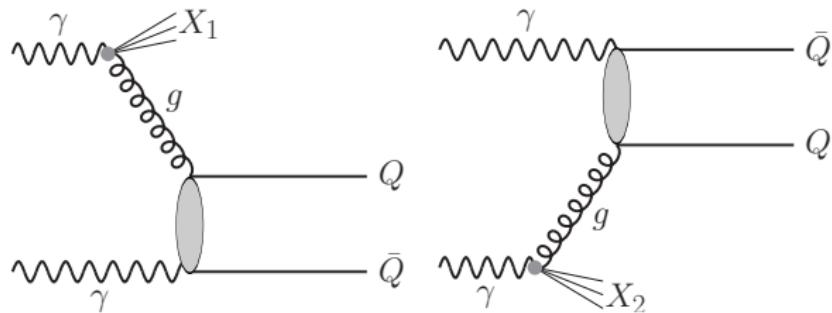
Four-quark component

Two heavy quark/antiquark, two light quark/antiquark



Single-resolved mechanisms

One photon fluctuates to a **partonic state** with **parton distributions**.



Elementary cross sections

LO (Born) term:

$$\sigma_{\gamma\gamma \rightarrow Q\bar{Q}}^{direct}(W_{\gamma\gamma}) = N_c e_Q^4 \frac{4\pi\alpha_{em}^2}{W_{\gamma\gamma}^2}$$

$$\times \left\{ 2 \ln \left[\frac{W_{\gamma\gamma}}{2m_Q} (1 + v) \right] \left(1 + \frac{4m_Q^2 W_{\gamma\gamma}^2 - 8m_Q^4}{W_{\gamma\gamma}^4} \right) - \left(1 + \frac{4m_Q^2 W_{\gamma\gamma}^2}{W_{\gamma\gamma}^4} \right) \right.$$

NLO corrections:

$$\sigma_{\gamma\gamma \rightarrow Q\bar{Q}(g)}^{QCD}(W_{\gamma\gamma}) = N_c e_Q^4 \frac{2\pi\alpha_{em}^2}{W_{\gamma\gamma}^2} C_F \frac{\alpha_s}{\pi} f^{(1)}. \quad (8)$$

function f was calculated by: **Kniehl-Kotikov-Merebashvili-Veretin, 2009**

Elementary cross sections, 4-quark component

Four-quark component in the dipole-dipole scattering approach based on a saturation approach (Kwieciński-Motyka) with extrapolation down to the threshold (Szczurek)

$$\begin{aligned}\sigma_{\gamma\gamma \rightarrow Q\bar{Q}}^{4q}(W_{\gamma\gamma}) &= \sum_{f_2 \neq Q} \int \left| \Phi^{Q\bar{Q}}(\rho_1, z_1) \right|^2 \left| \Phi^{f_2\bar{f}_2}(\rho_2, z_2) \right|^2 \sigma_{dd}(\rho_1, \rho_2, x_{Qf}) d^2\rho \\ &+ \sum_{f_1 \neq Q} \int \left| \Phi^{f_1\bar{f}_1}(\rho_1, z_1) \right|^2 \left| \Phi^{Q\bar{Q}}(\rho_2, z_2) \right|^2 \sigma_{dd}(\rho_1, \rho_2, x_{fQ}) d^2\rho\end{aligned}$$

where $\Phi^{Q\bar{Q}}(\rho, z)$ are the quark – antiquark wave functions of the photons in the mixed representation and σ_{dd} is the dipole–dipole cross section.

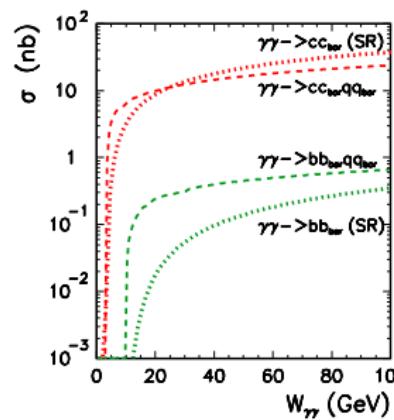
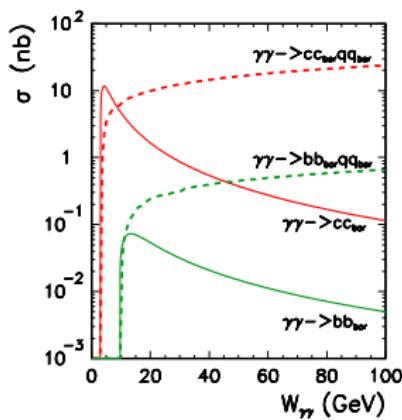
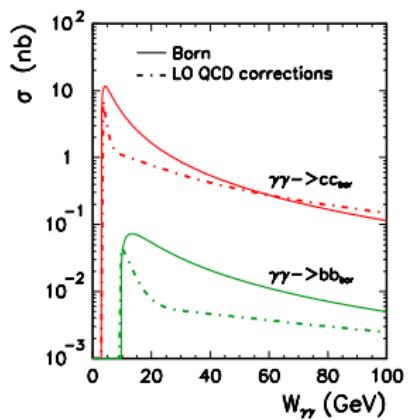
Elementary cross sections

single resolved component

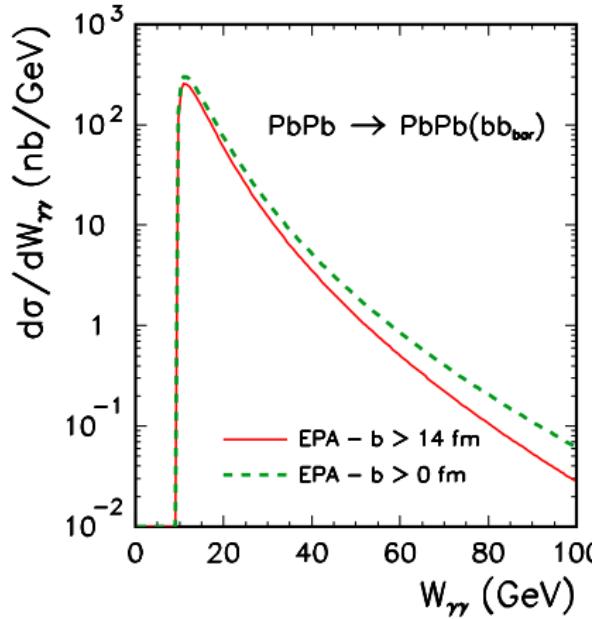
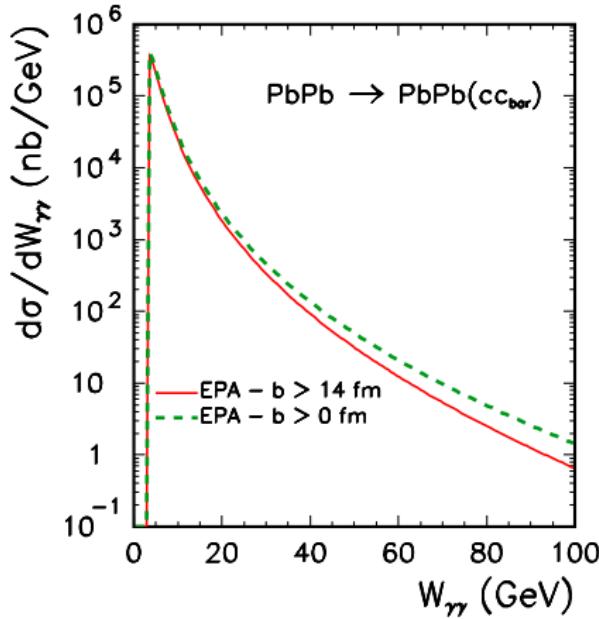
$$\begin{aligned}\sigma_{1-res}(s) &= \int dx_1 \left[g_1(x_1, \mu^2) \hat{\sigma}_{g\gamma \rightarrow Q\bar{Q}}(\hat{s} = x_1 s) \right] \\ &+ \int dx_2 \left[g_2(x_2, \mu^2) \hat{\sigma}_{\gamma g \rightarrow Q\bar{Q}}(\hat{s} = x_2 s) \right], \quad (10)\end{aligned}$$

where g_1 and g_2 are gluon distributions in photon 1 or photon 2 and $\hat{\sigma}_{g\gamma \rightarrow Q\bar{Q}}$ and $\hat{\sigma}_{\gamma g \rightarrow Q\bar{Q}}$ are elementary cross sections. In our evaluation we take the GVR1992 gluon distributions in photon.

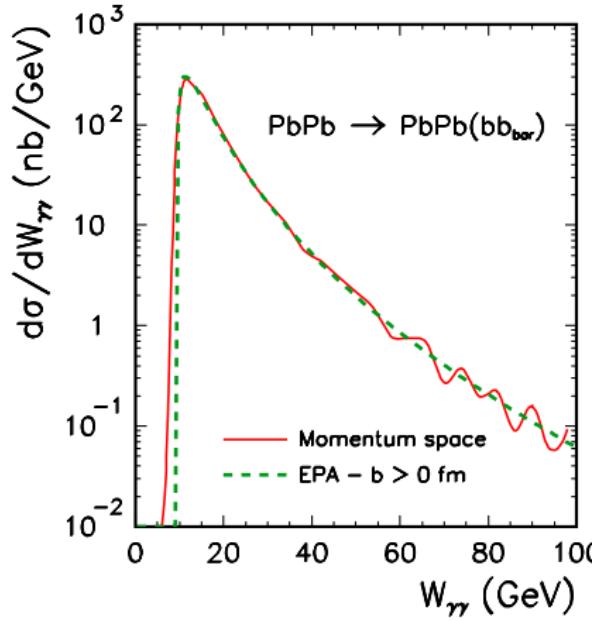
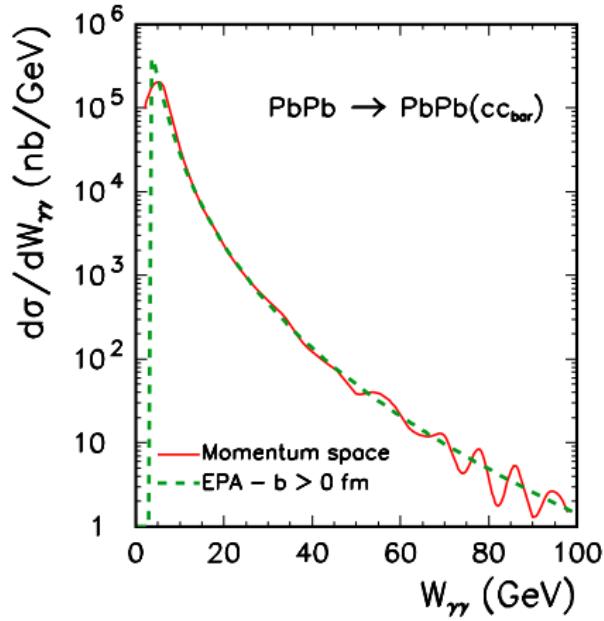
Elementary cross sections, results



$W_{\gamma\gamma}$ -dependence of the nuclear cross section

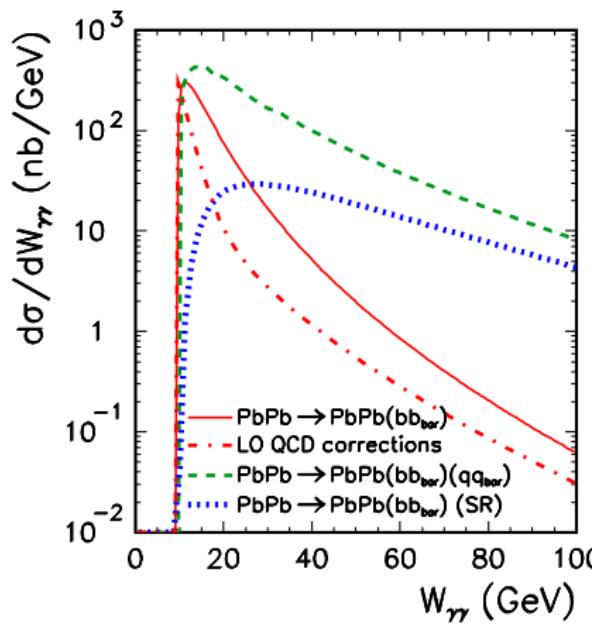
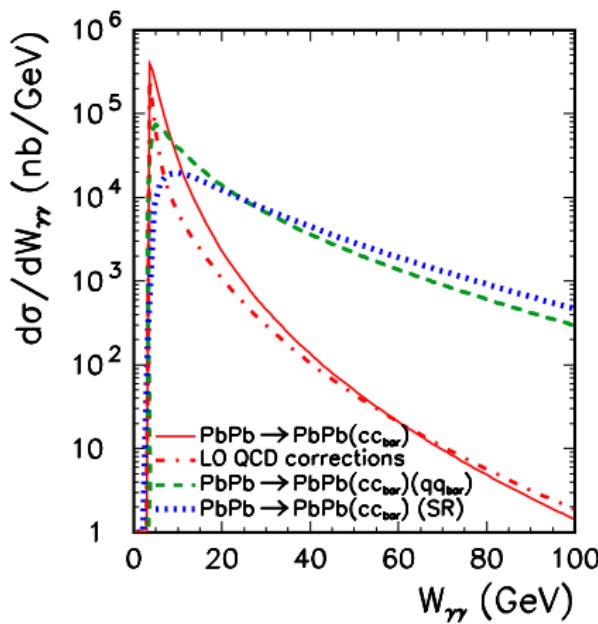


$W_{\gamma\gamma}$ -dependence, EPA vs exact



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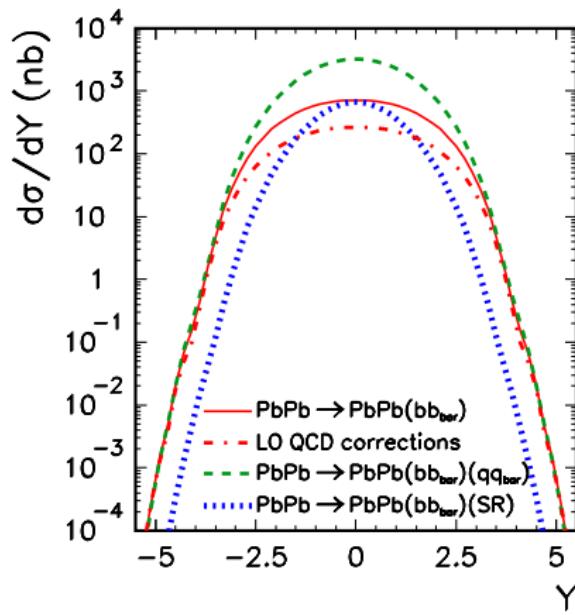
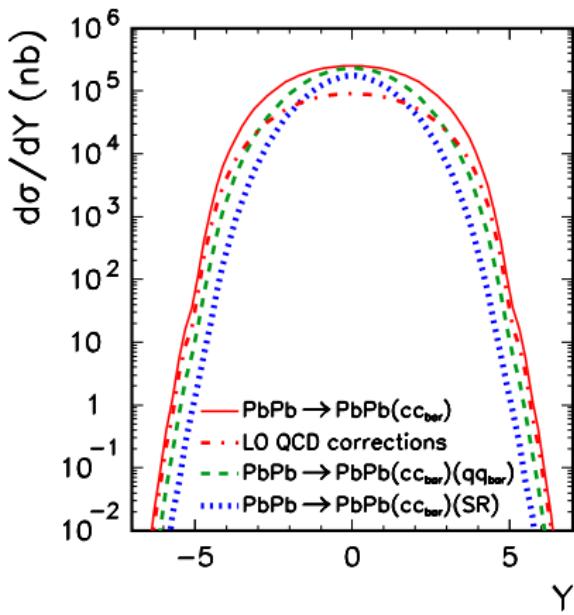
$W_{\gamma\gamma}$ -dependence, components



Contents
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 $AA \rightarrow AQ\bar{Q}A$

Rapidity distribution

Rapidity of the whole system



Total cross sections

Tablica: Partial contributions of different mechanisms.

	σ_{tot}	Born	QCD-corrections	4-quark	Single-resolved
$c\bar{c}$	2.47 mb	42.5 %	14.6 %	27.1 %	15.8 %
bb	$10.83 \mu b$	18.9 %	7.7 %	64.5 %	8.9 %

Other processes

- ① $AA \rightarrow A\pi^+\pi^-A$ at low $M_{\pi\pi}$

$AA \rightarrow A\pi^0\pi^0A$ at low $M_{\pi\pi}$

Easy for a measurement (ALICE)

- ② $AA \rightarrow AD^+D^-A$

$AA \rightarrow AD^0\bar{D}^0A$

Testing pQCD and distribution amplitudes

Luszczak-Szczurek, Phys. Lett. **B700** (2011) 116.

- ③ $AA \rightarrow AW^+W^-A$

Anomalous triple and quartic boson couplings? Not possible

- ④ $AA \rightarrow AJ/\Psi J/\Psi A$

Testing heavy-quark approaches.

General summary

- ① Sizeable cross sections for different processes.
- ② Cross sections smaller than in the literature
Realistic charge distribution, absorptive geometrical effects
- ③ The role of competitive **diffractive processes** leading to the same final state has to be explored
Strikman, Gay Ducati, Machado
- ④ Experimental feasibility of several processes should be studied.
- ⑤ Potential for this type of studies should be better explored.