



Reconstruction of thermal Sunyaev-Zel'dovich effect with the PLANCK experiment

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Outline

- Introduction

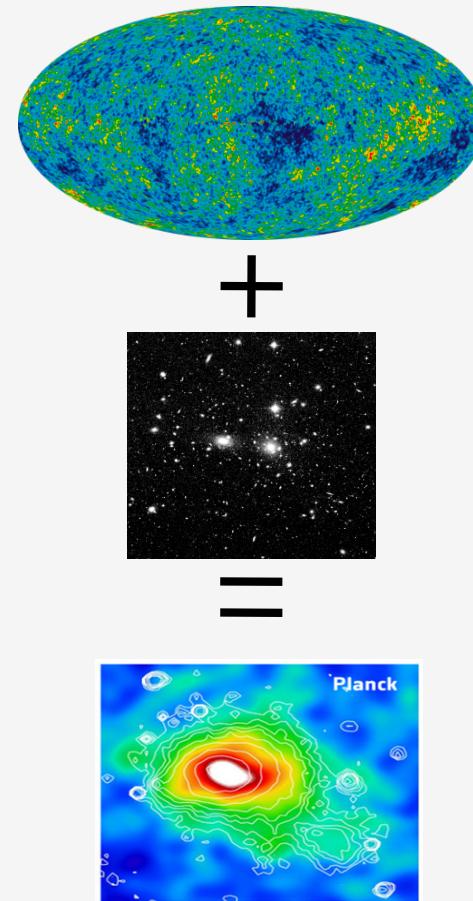
- Cosmic Microwave Background
- Galaxy clusters
- PLANCK experiment

- Extraction of tSZ effect

- MILCA (Hurier et al. 2010)
- Application to simulated data

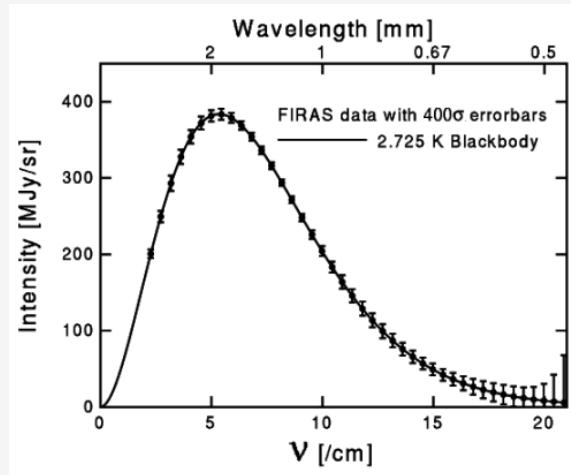
- PLANCK early results

- New clusters discovery
- ESZ catalog



Cosmic microwave background (CMB)

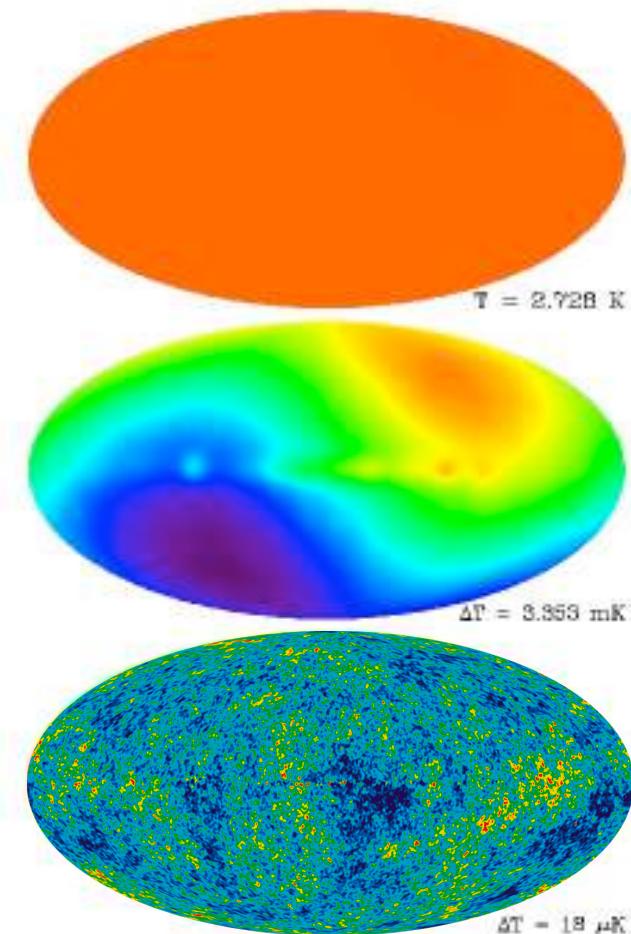
Isotropic and homogenous radiation at 2.725 K



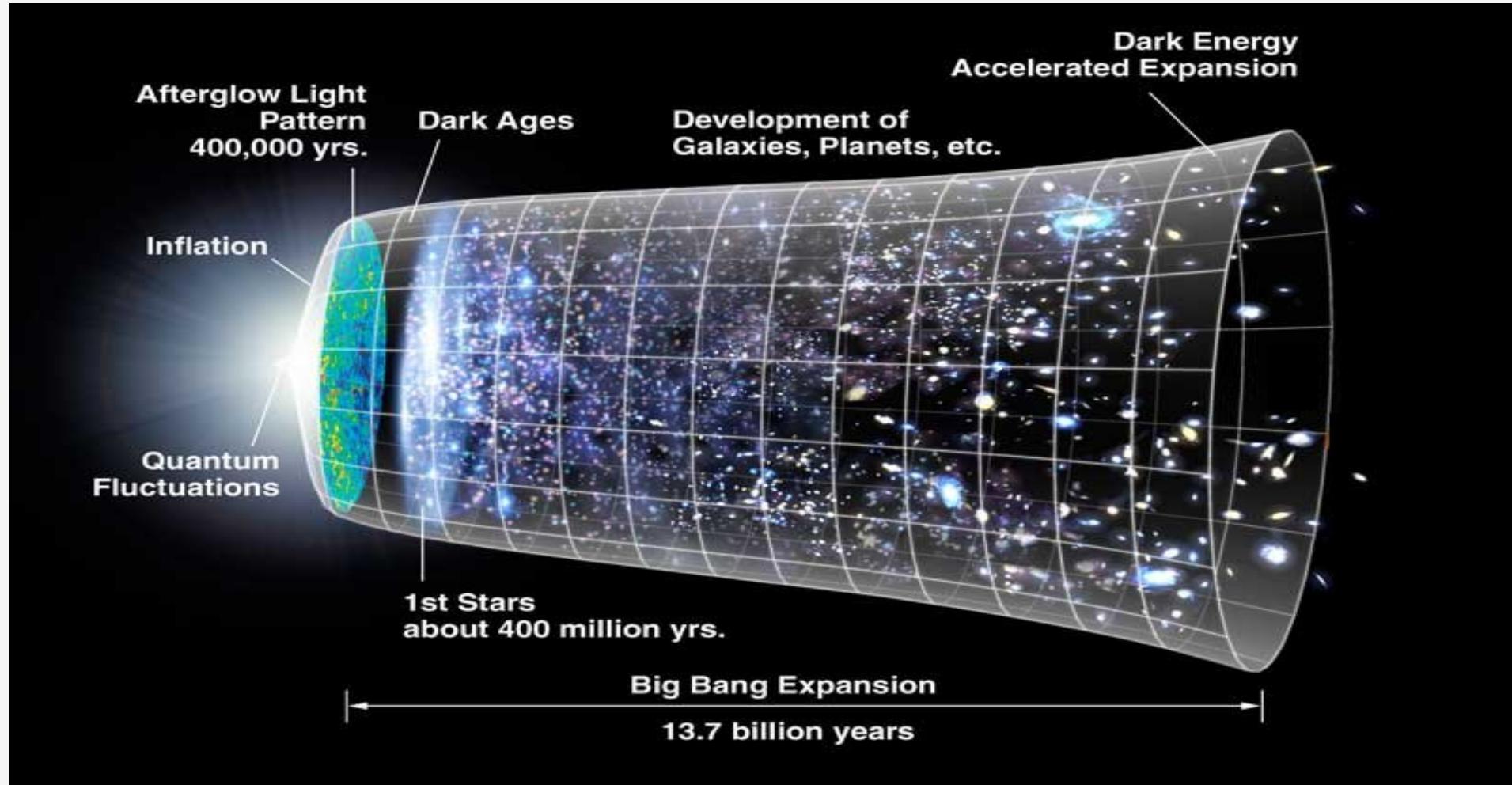
Black body radiation
as measured by COBE

Dipole : produced by the observer velocity in
the CMB referential

Temperature anisotropies strongly depend on
cosmological models



Universe history



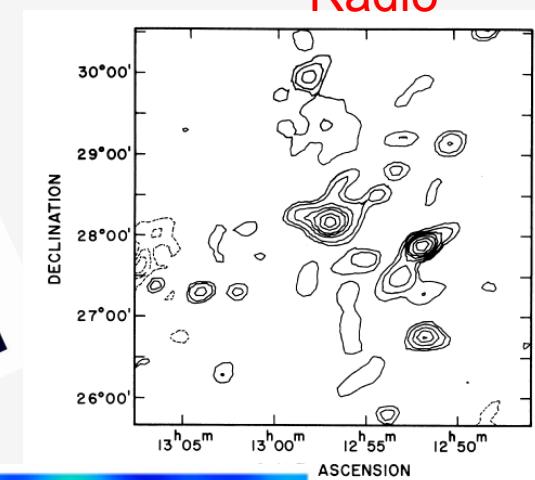
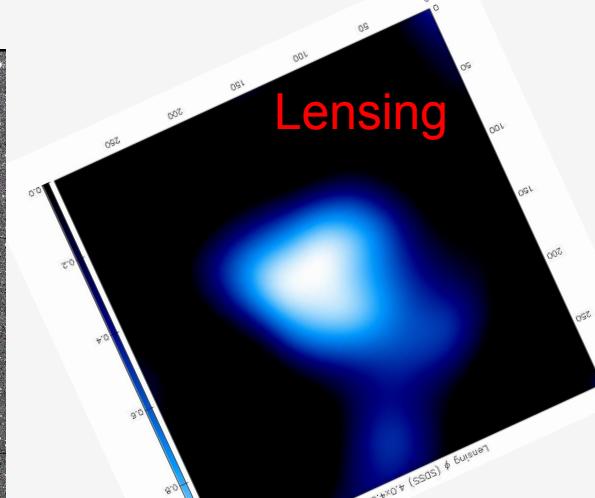
Galaxy clusters

Formation and observables

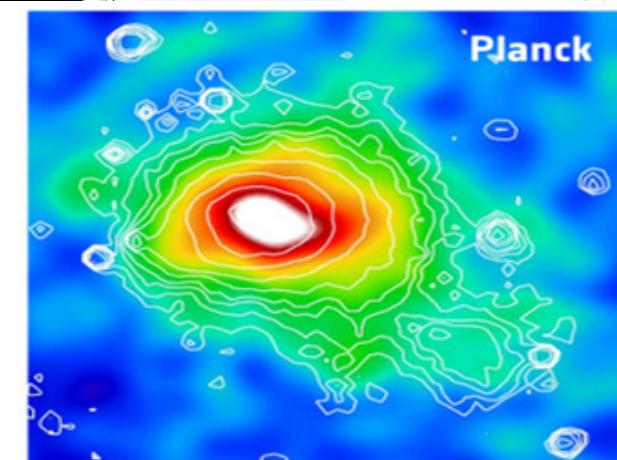
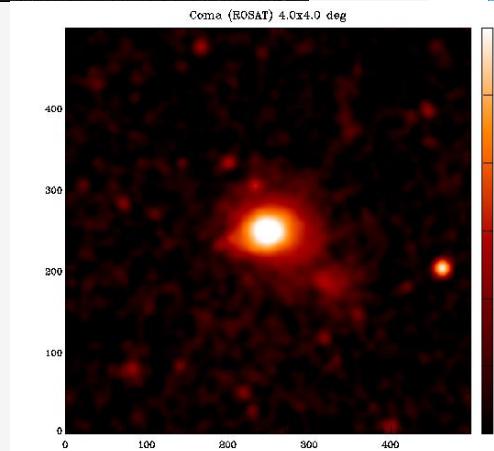
Formation bottom-up model : small structures → large structures

The Coma cluster from different observables

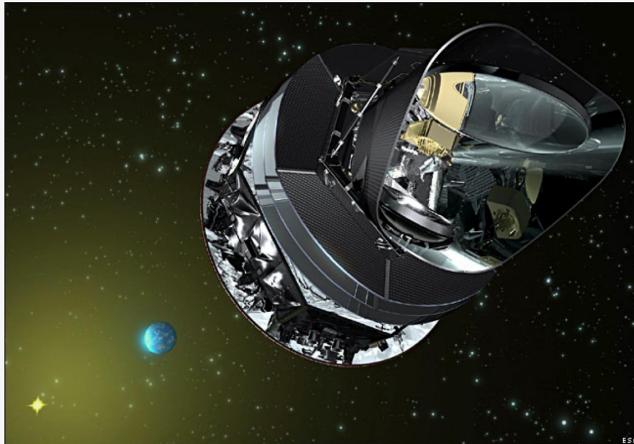
Optique



X-rays



TSZ



The PLANCK experiment

Launch the 14th May 2009
At L2 point of Earth/Solar system

2 instruments :
LFI : radiometers
HFI : bolometers at 0.1 K

Pointing strategy:



9 frequency channels :

LFI : 30, 44, 70 GHz

HFI : 100, 143, 217, 353, 545 and 857 GHz

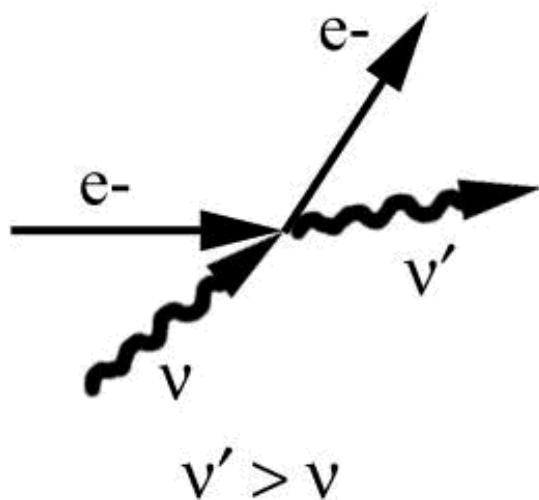
Nominal mission :

2 full sky coverage

Actually : 4th coverage almost completed

Interaction between clusters and CMB: tSZ effect

Inverse Compton scattering



The intensity of tSZ is proportionnal to the integration of the pressure ($T_e n_e$) on the line of sight

Electron gaz pressure

Line of sight

$$y = \int_{los} \frac{kT_e}{m_e c^2} n_e(r) \sigma_T dl$$

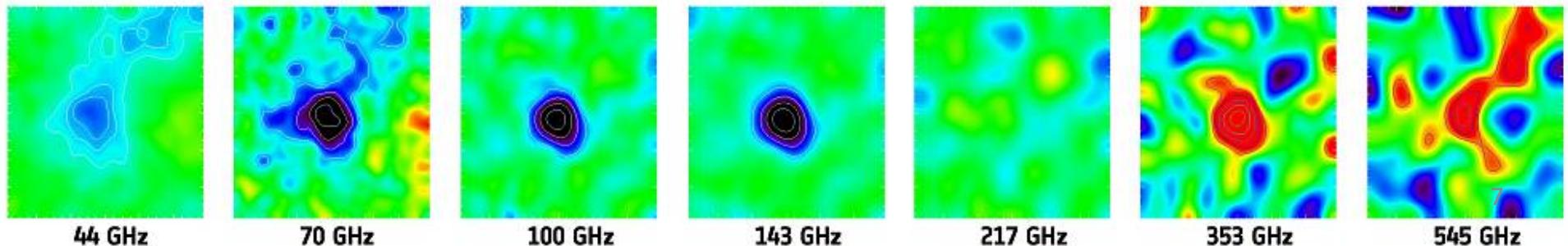
Compton parameter

Thomson scattering

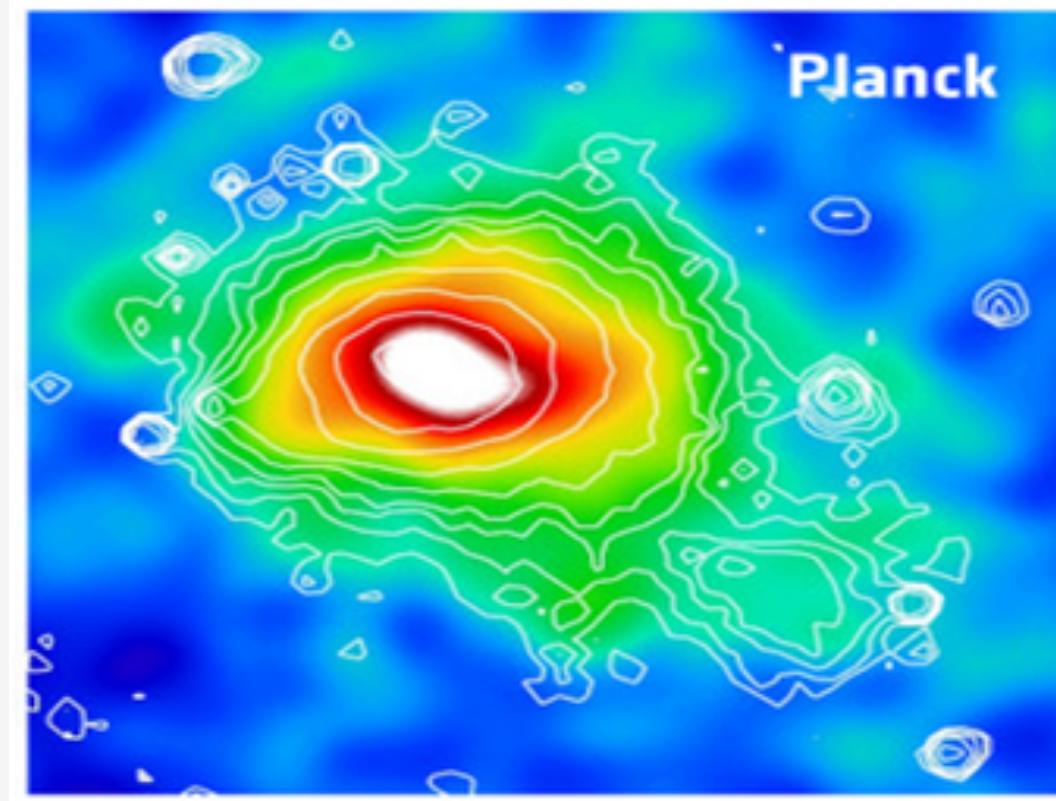
Shift of the electromagnetic spectrum

Frequency dependance $\Delta T = y^* f(v)$

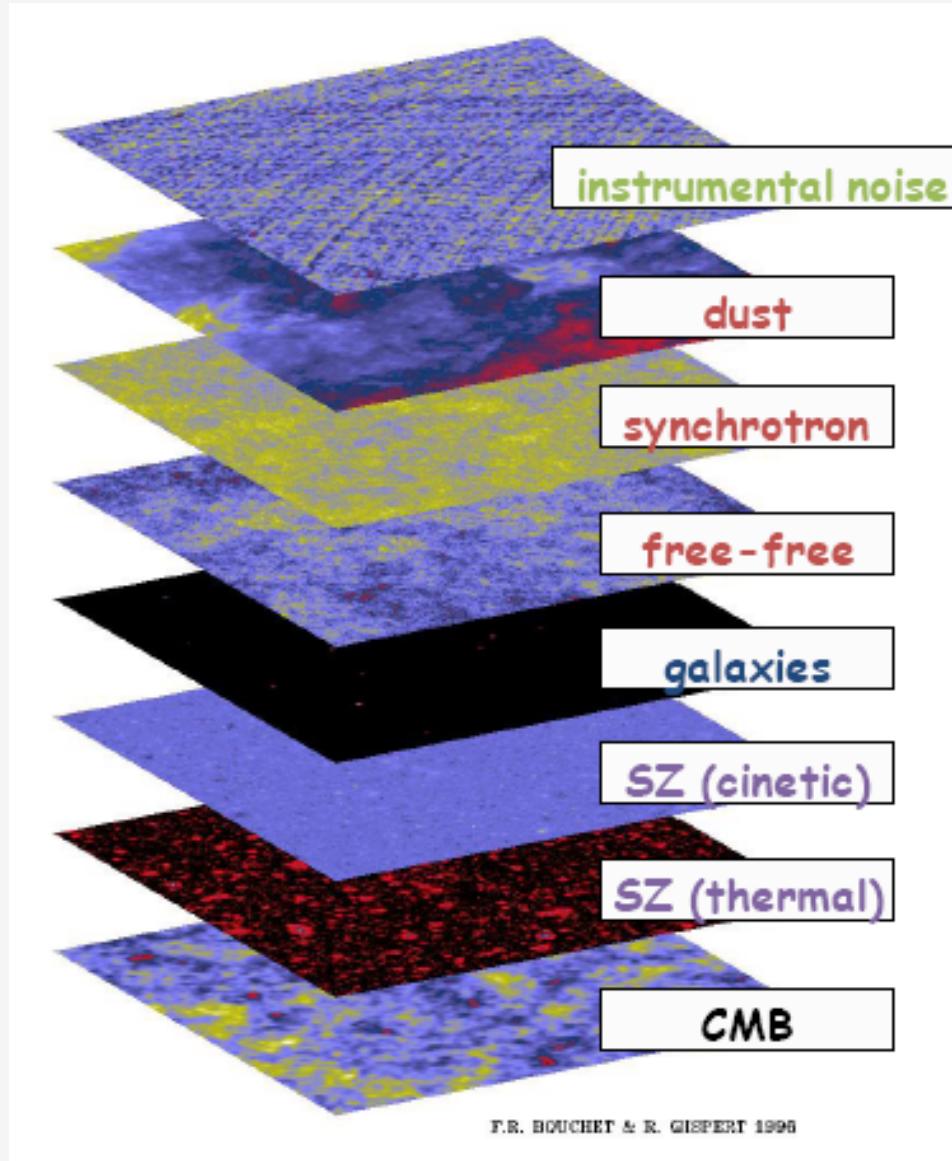
Abell 2319 in PLANCK data (cleaned maps)



Extraction of the tSZ effect



The microwave sky composition



MILCA

Hurier et al. 2010, [arXiv:1007.1149](https://arxiv.org/abs/1007.1149)

MILCA (MODIFIED INTERNAL LINEAR COMBINATION ALGORITHM) :

WE INTEND TO EXTRACT A PHYSICAL COMPONENT FROM A MULTI-FREQUENCY OBSERVATION

Assumption : Each observed channel can be written as a linear combination of several components

1) Constraint on the electromagnetic spectrum of the reconstructed map

2) Constraint(s) on other component(s) spectrum to be removed

3) Reduction of bias by introducing prior information about the noise

Observed maps

$$\mathbf{T} = \mathbf{A} \cdot \mathbf{S} + \mathbf{N}$$

Mixing matrix

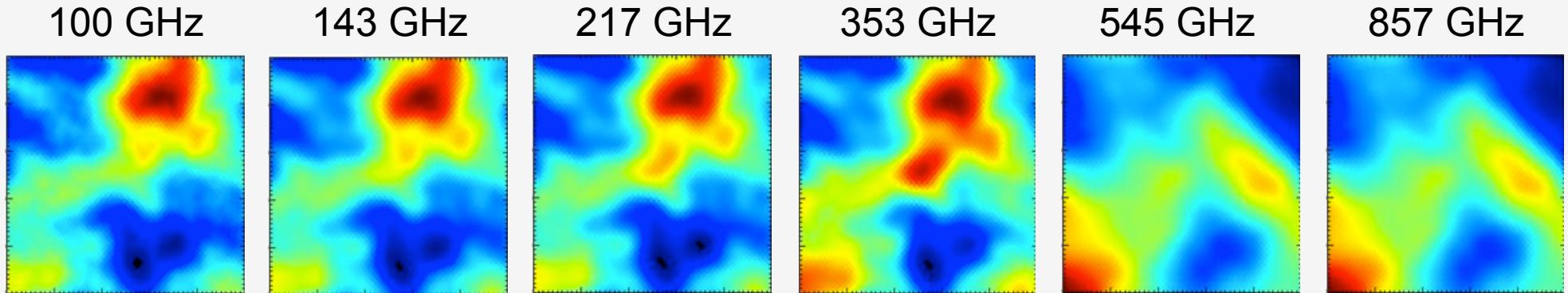
Components maps

Noise

4) Minimization of the covariance matrix in the sub-space of extractible components.

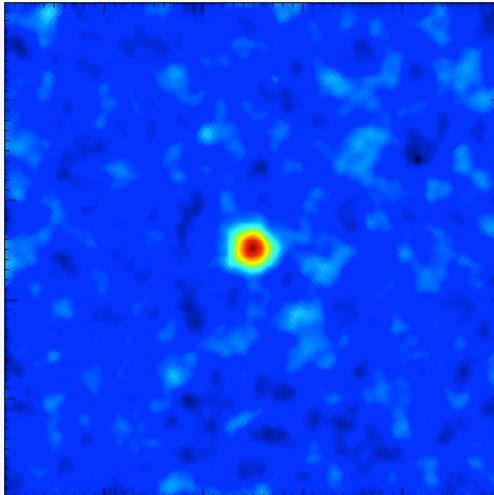
5) Minimization of instrumental noise with remaining degrees of freedom

Reconstruction of tSZ on PLANCK simulations

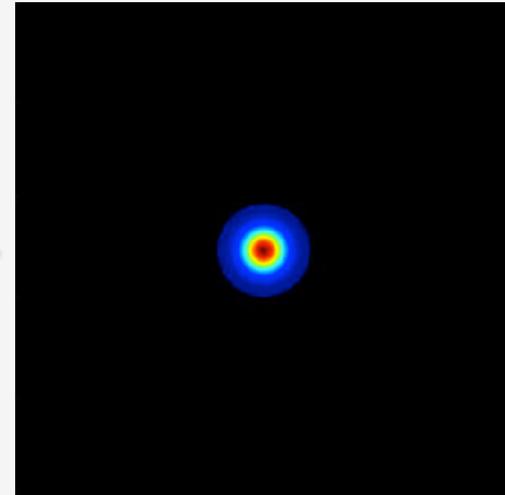


Patch 2 by 2 degrees

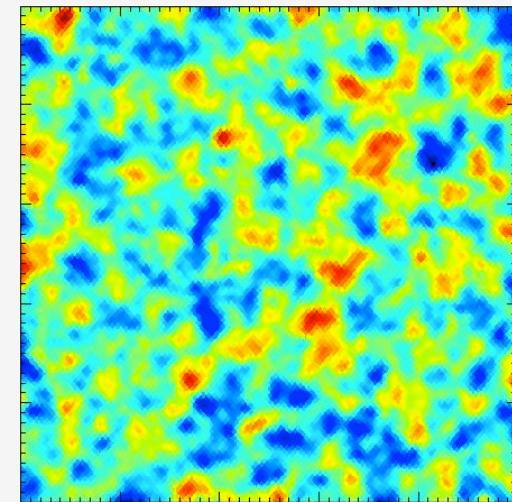
Reconstructed y map



Input y map



Residuals



Estimation of errors

Statistical errors :

- I) Compute noise map using PLANCK scanning strategy
- II) Compute effective hit map for the tSZ constructed map
- III) Compute power spectrum of the noise map
- IV) Perform MC simulation of noise

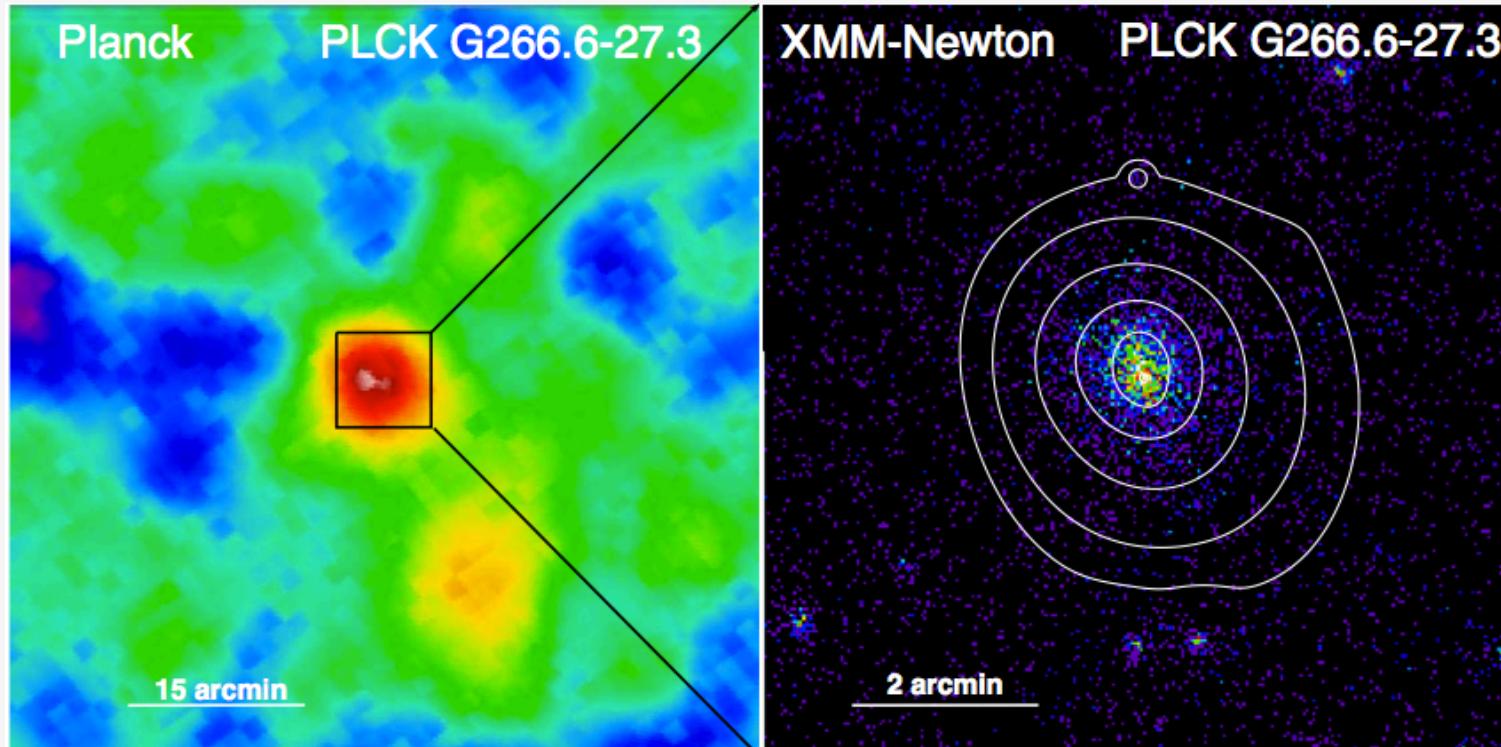
Systematic errors :

- I) Calibration uncertainties
- II) Relativistic correction of tSZ spectrum
- III) Other components residuals

High z cluster detection

Used (in complement of several methods) :

- in the ESZ (PLANCK SZ catalog) validation process
- in the XMM follow up target selection

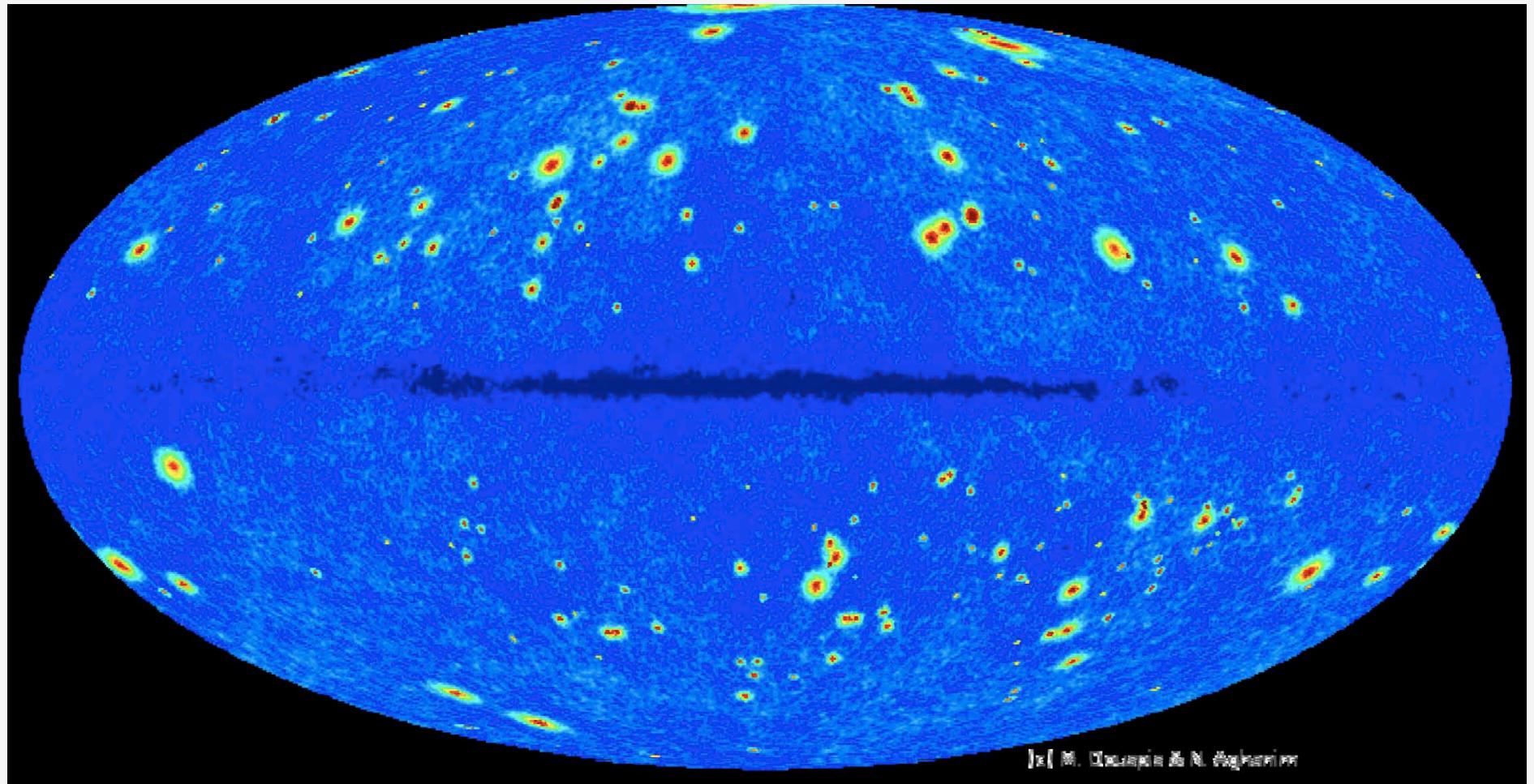


$$Y_{500} = (4.1 \pm 0.9) \times 10^{-4} \text{ arcmin}^2$$

$$z \sim 1$$

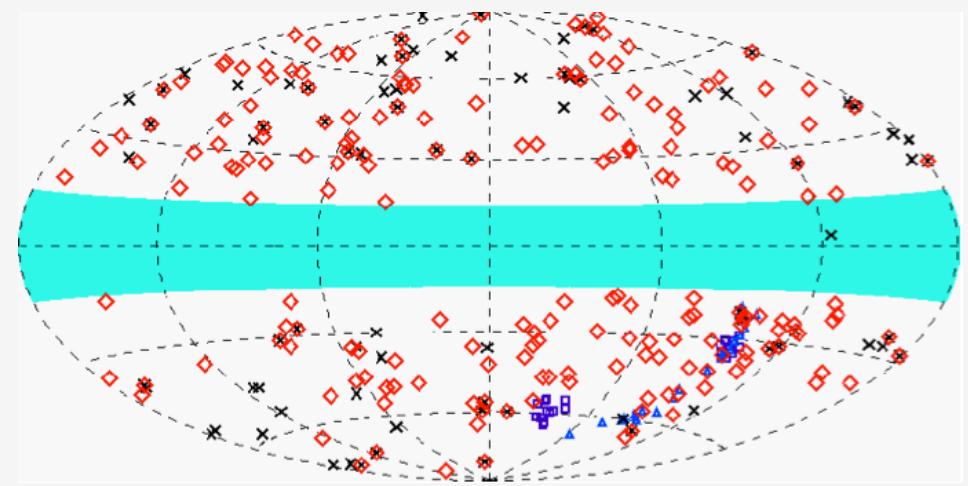
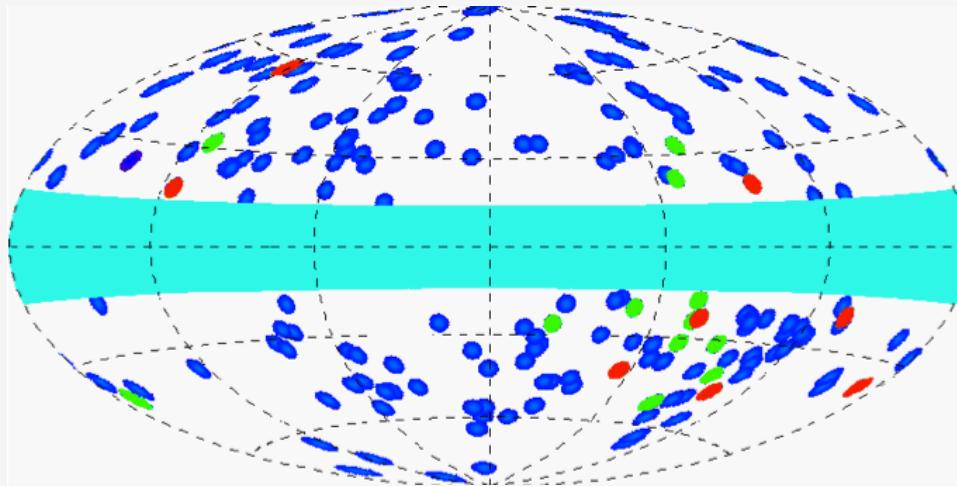
The PLANCK collaboration, arXiv : 1106.1376v2

Detection of tSZ with PLANCK



Early SZ catalog

Ref : The Planck Collaboration 2011 Early paper



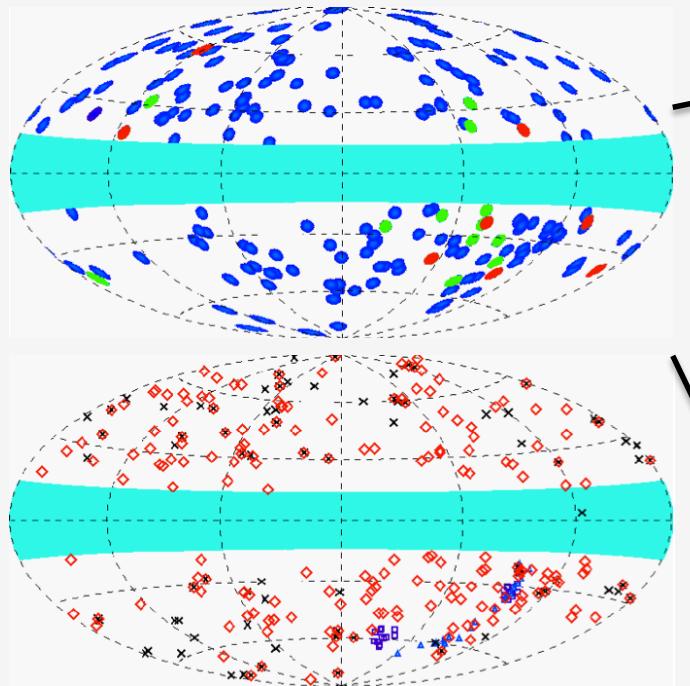
Position of 189 clusters of the catalog :

- Known X-ray clusters
- New clusters, validated in X-ray (19)
- New clusters (8)

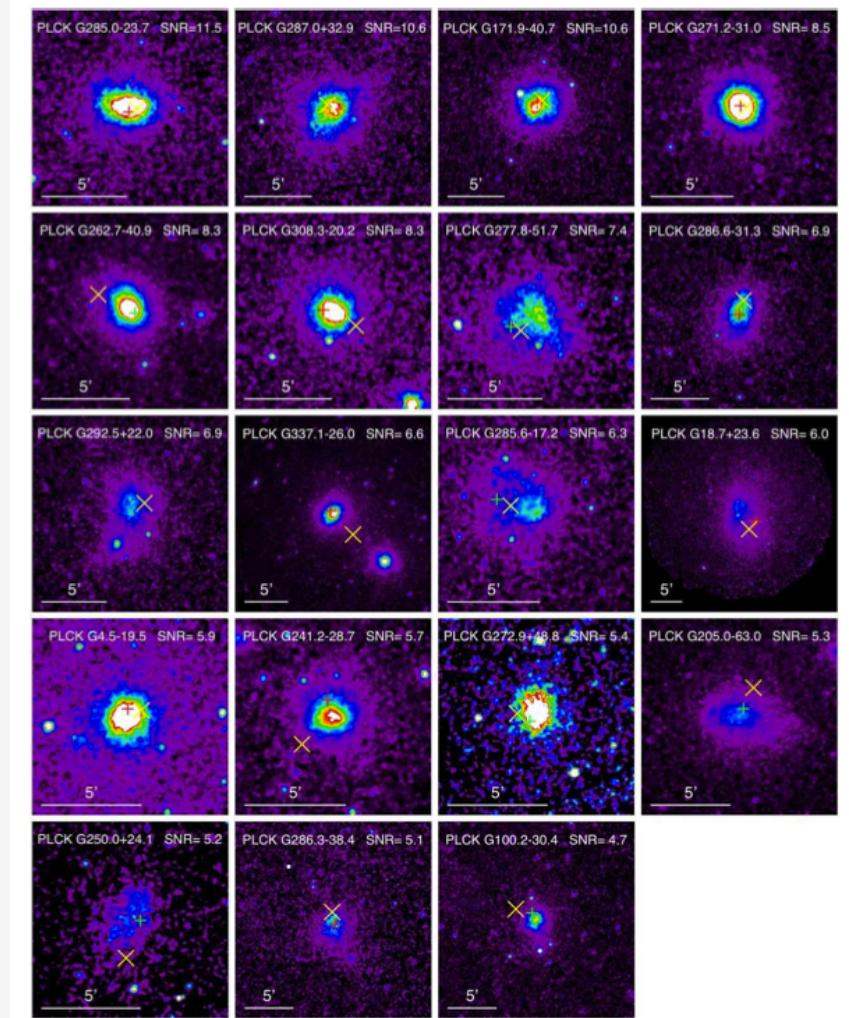
Planck ESZ sample versus other tSZ experiments

Reliability, robustness

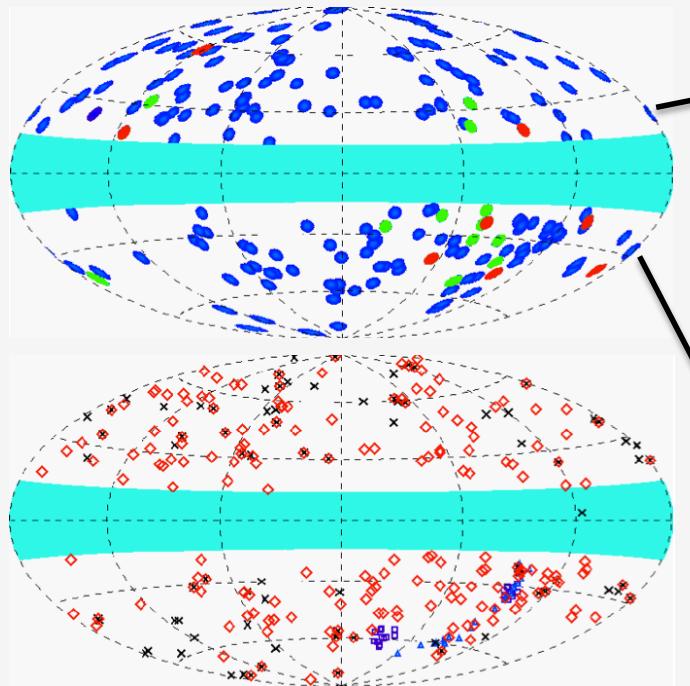
XMM follow up



X-ray counterpart for the 19
 validated clusters discovered
 by PLANCK

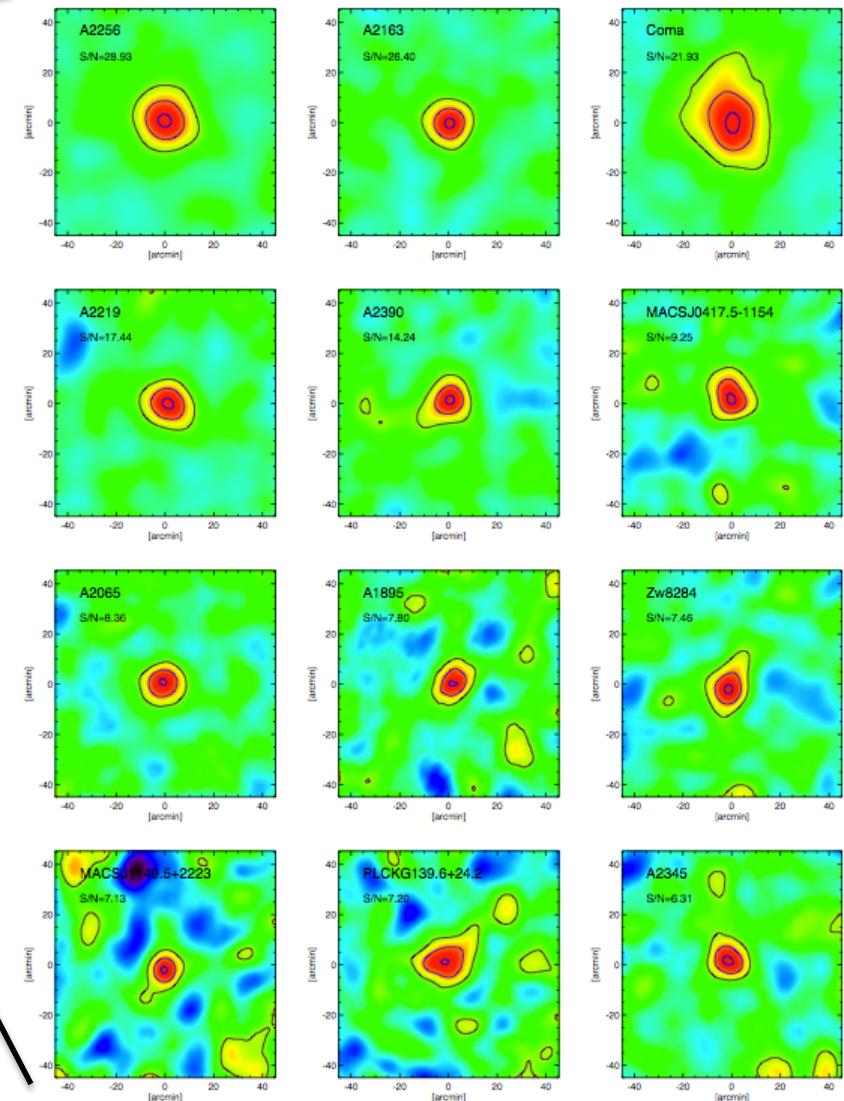


ESZ catalogue



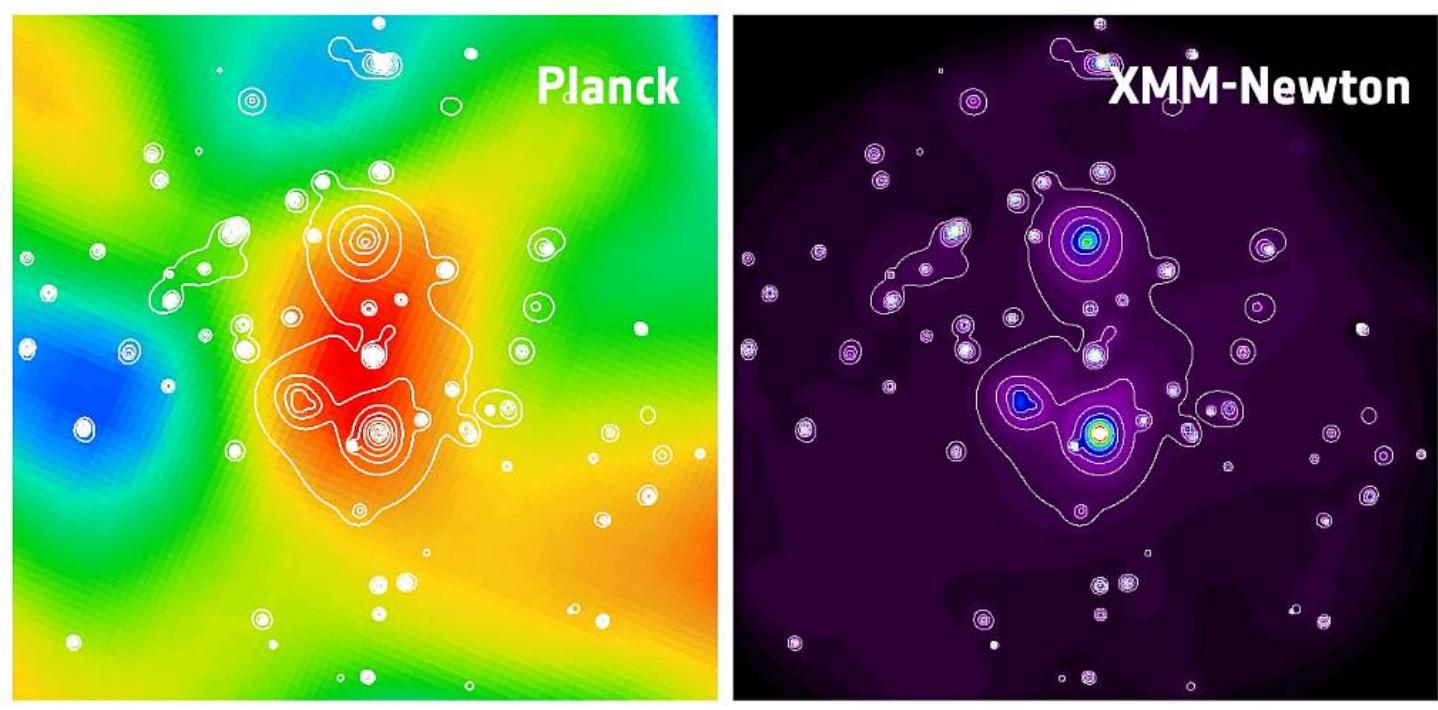
Redshift → Clusters Mass

Mass + selection function →
 Matter power spectrum →
 cosmological parameters

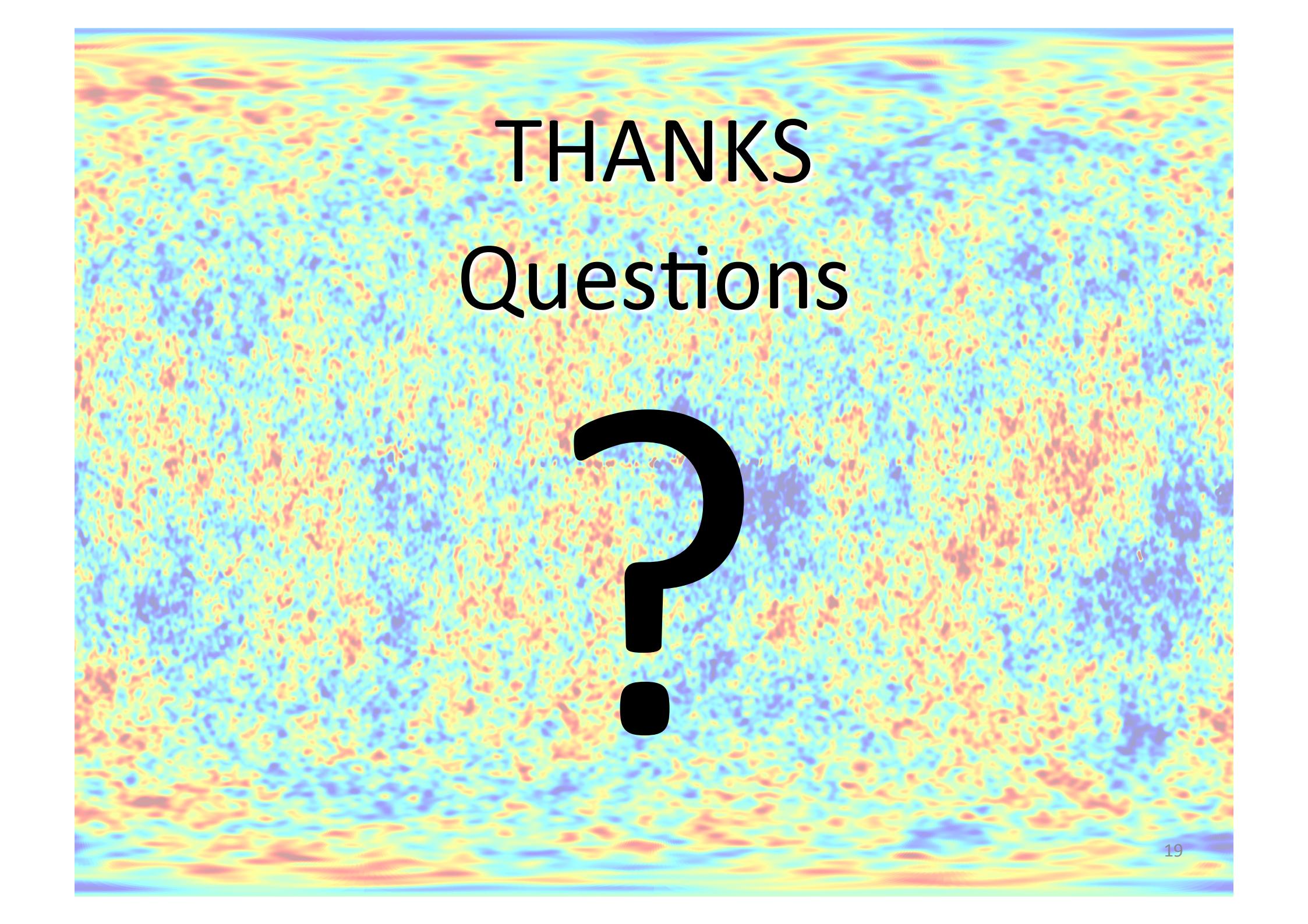


Conclusions

- tSZ effect can be extract with from PLANCK data with high signal to noise ratio and allow the detection of new clusters.



- MILCA allow a low noise, low bias reconstruction of tSZ effect.
- The ESZ sample present a unique dataset of cluster across the full sky with high reliability and high robustness.



**THANKS
Questions**

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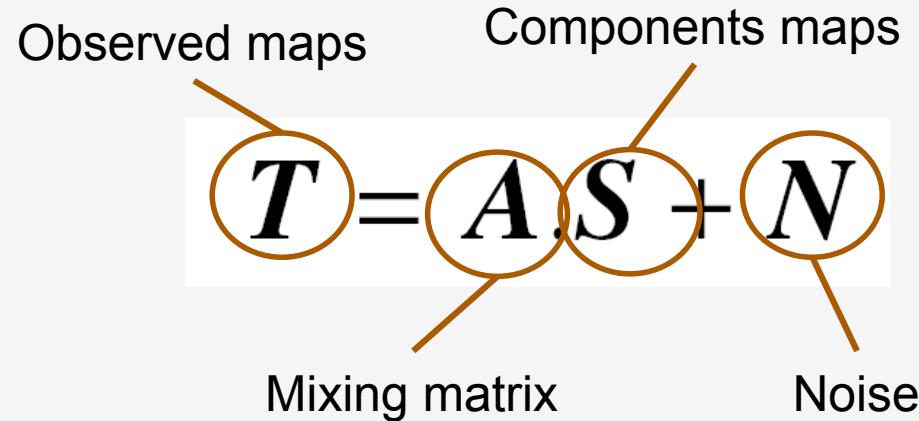
MILCA

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WE INTEND TO EXTRACT A PHYSICAL COMPONENT FROM A MULTI-FREQUENCY OBSERVATION

Assumption : Each observed channel can be written as a linear combination of several components



Detector bandpass

$$A_{ij} = \int F_i(\nu) H_j(\nu) d\nu$$

Component spectrum

MILCA

So far we search a solution in the form of a linear combination of observed channels

$$S_c = \mathbf{w}^T \cdot \mathbf{T},$$

1) Constraint on the electromagnetic spectrum of the reconstructed map

$$g = \sum_i f_i w_i = 1,$$

2) Minimisation of the variance

3) Constraint(s) on other component(s) spectrum to be removed

$$\begin{pmatrix} 2 \cdot C_T & -f \\ f^T & 0 \end{pmatrix} \begin{pmatrix} w \\ \lambda \end{pmatrix} = \begin{pmatrix} \mathbf{0} \\ 1 \end{pmatrix}$$

MILCA

So far we search a solution in the form of a linear combination of observed channels

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Constraint(s)

Reconstructed maps

Observed maps

Covariance matrix

$$\widehat{S}_c = \frac{\mathbf{f}^T \cdot \widehat{\mathbf{C}}_T^{-1} \cdot \mathbf{T}}{\mathbf{f}^T \cdot \widehat{\mathbf{C}}_T^{-1} \cdot \mathbf{f}}$$

MILCA

Covariance matrix
of components

$$\mathbf{C}_T = \mathbf{A} \cdot \mathbf{C}_S \cdot \mathbf{A}^T + \mathbf{C}_N,$$

$$\widehat{\mathbf{S}}_c = \mathbf{S}_c + \frac{1}{(\widehat{\mathbf{C}}_S^{-1})_{cc}} \cdot \sum_{j \neq c} (\widehat{\mathbf{C}}_S^{-1})_{cj} \cdot \mathbf{S}_j$$

Covariance matrix of
observed channels

Noise covariance matrix

$$\widehat{\mathbf{S}}_c = \frac{\mathbf{f}^T \cdot \widehat{\mathbf{C}}_T^{-1}}{\mathbf{f}^T \cdot \widehat{\mathbf{C}}_T^{-1} \cdot \mathbf{f}} \cdot \mathbf{T}$$

Constraint(s) Observed maps
 Reconstructed maps Covariance matrix

MILCA

Covariance matrix
of components

$$\mathbf{C}_T = \mathbf{A} \cdot \mathbf{C}_S \cdot \mathbf{A}^T + \mathbf{C}_N,$$

Covariance matrix of
observed channels

Noise covariance matrix

$$\widehat{\mathbf{S}}_c = \mathbf{S}_c + \frac{1}{(\widehat{\mathbf{C}}_S^{-1})_{cc}} \cdot \sum_{j \neq c} (\widehat{\mathbf{C}}_S^{-1})_{cj} \cdot \mathbf{S}_j$$

Estimation of \mathbf{C}_N :

-Using scan strategy (redundancy)

4) Reduction of bias by introducing
Prior information about the noise

$$\tilde{\mathbf{C}}_T = \mathbf{C}_T - \mathbf{C}_N$$

Constraint(s) Observed maps Covariance matrix

Reconstructed maps

$$\widehat{\mathbf{S}}_c = \frac{\mathbf{f}^T \cdot \widehat{\mathbf{C}}_T^{-1}}{\mathbf{f}^T \cdot \widehat{\mathbf{C}}_T^{-1} \cdot \mathbf{f}} \cdot \mathbf{T}$$

MILCA

Singular value decomposition

$$\tilde{C}_T = U D U^T$$

5) Minimization of the covariance matrix in the sub-space of extractible components.

$$\hat{C}_T = U \begin{bmatrix} D_{i,j} & & & \\ & \ddots & & 0 \\ & & \ddots & \\ 0 & & & 0 \end{bmatrix} U^T$$

Constraint(s) → $\widehat{S}_c = \frac{f^T \cdot \widehat{C}_T^{-1}}{f^T \cdot \widehat{C}_T^{-1} \cdot f} \cdot T$ ← Observed maps
 Reconstructed maps → \widehat{S}_c ← Covariance matrix

MILCA

Singular value decomposition

$$\tilde{C}_T = U D U^T$$

5) Minimization of the covariance matrix in the sub-space of extractible components.

6) Minization of instrumental noise with Remaining degrees of freedom

$$\hat{C}_T = U \begin{bmatrix} D_{i,j} & & & & & & \\ - & - & - & - & - & - & \\ & & & & & & \\ & 0 & & (U^T C_N U)_{i,j} & & & \end{bmatrix} U^T$$

Constraint(s)

Reconstructed maps

Observed maps

Covariance matrix

$$\widehat{S}_c = \frac{f^T \cdot \widehat{C}_T^{-1} \cdot T}{f^T \cdot \widehat{C}_T^{-1} \cdot f}$$

Estimation of statistical errors

Ideal case : white noise assumption

III) Using hit map to determine
the σ by pixel by hit

Erreur syste

I) Compute noise map using
PLANCK scanning strategy

II) Compute effective hit map
for the tSZ constructed map

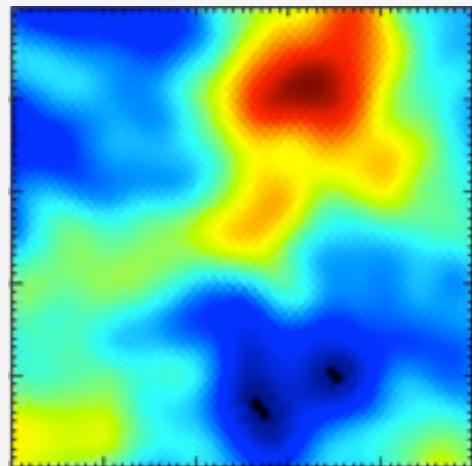
real case : correlated noise

III) Compute power spectrum
of the noise map

IV) Perform MC simulation of
noise

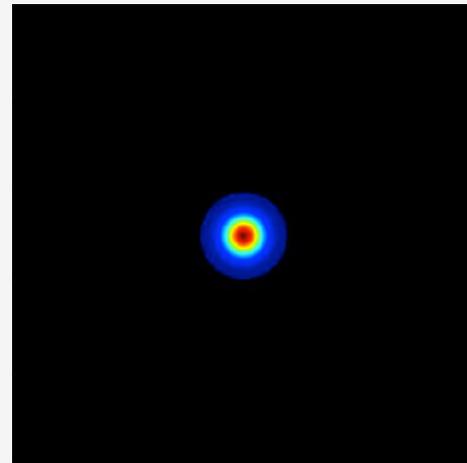
Reconstruction of tSZ on PLANCK simulations

CMB



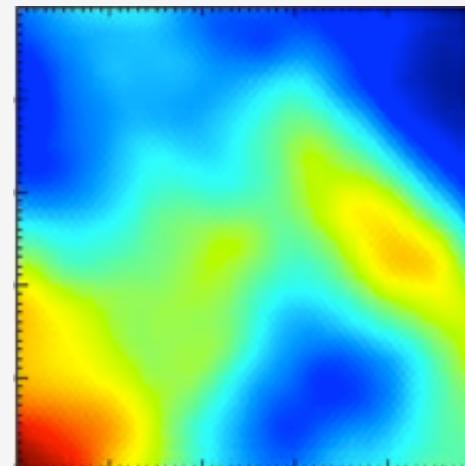
tSZ

$$Y_{500} = 1.3 \cdot 10^{-3} \text{ arcmin}^2$$



Dust

$$(T = 17\text{K}, \beta_d = 1.8)$$



+ NOISE (4 surveys)

All frequency maps are set to a common resolution before performing the separation

New data

