



# **The 3<sup>rd</sup> generation quarks in warped models : *LHC predictions from LEP/Tevatron anomalies***

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*with*

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PRD 2010 ; PLB 2011

## Outline

*I) Introduction: a warped model*

*II)  $A_{FB}^t$  and  $t\bar{t}$  cross section @ Tevatron*

*III)  $A_{FB}^b$  and EW precision tests @ LEP*

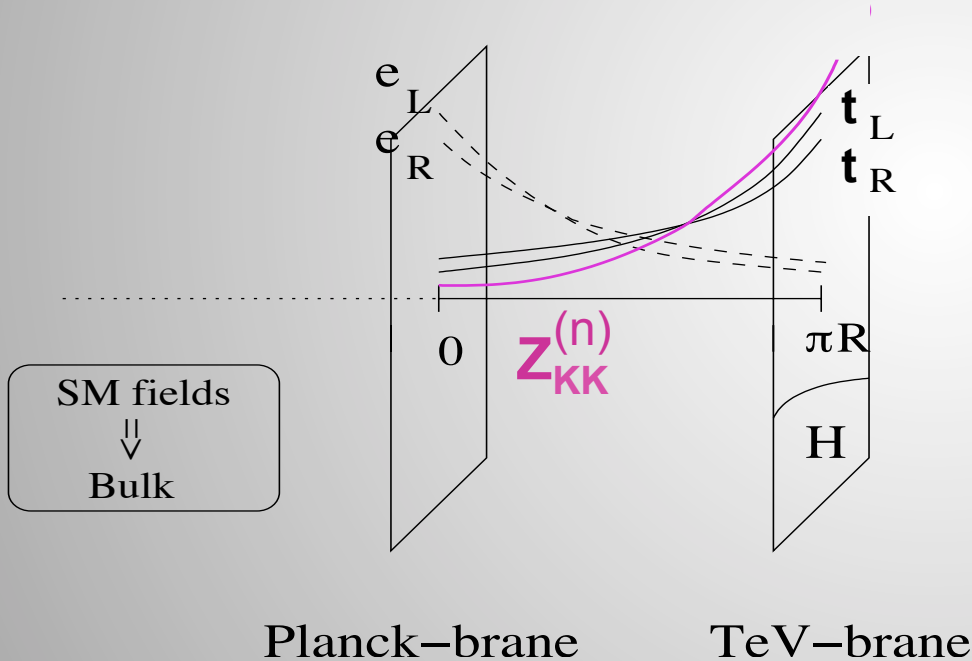
*IV) Constraints and predictions @ LHC*

*V) Other scenarios explaining  $A_{FB}^t$  ?*

*VI) Conclusions*

# 1) Introduction: a warped model

## The Randall-Sundrum (RS) scenario with bulk fields:



- RS addresses the gauge *hierarchy* :

$$M_{grav} \approx TeV \approx Q_{EW}$$

*Randall, Sundrum (1999)*

- RS generates the mass *hierarchies* :

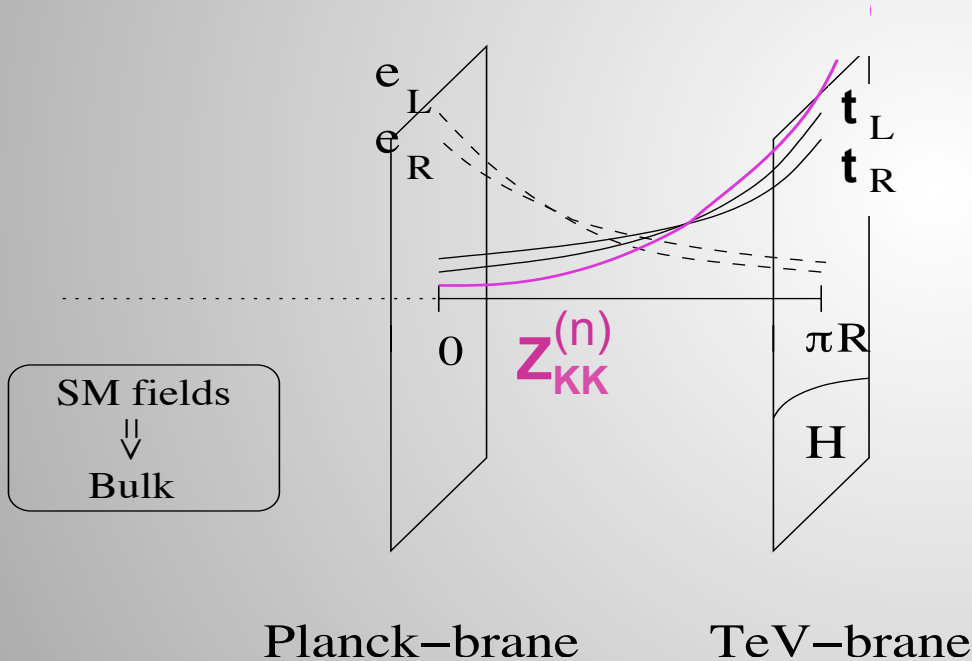
$$m_e \ll m_t$$

*Gherghetta, Pomarol (2000)*

...

# l) Introduction: a warped model

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...

**➡ New Physics effects in the heavy fermion sector !**



**+ attractive features of the RS scenario with bulk fields  
(= dual via AdS/CFT to composite Higgs & top models) :**

- WIMP candidates for the dark matter of universe:  
a LKP stable due to a possible KK-parity (*like in UED*)
- Unification of gauge couplings (*as in ADD*) at high-energies
- *Extra-Dimensions* =  
necessary ingredients for higher-energy string theories

## The EW precision constraints in warped models :

Bulk gauge bosons/fermions mix with their KK excitations

=> tree-level contributions to EW observables

**Ways out** to respect the constraints from EW precision data for  $M_{\text{KK}} \sim \text{TeV}$  :

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**Ways out** to respect the constraints from EW precision data for  $M_{\text{KK}} \sim \text{TeV}$  :

~> **Gauge custodial symmetry in the bulk**

Agashe, Delgado,  
May, Sundrum (2003)

$$\begin{array}{ccc} O(4) & & SU(2)_L \times SU(2)_R \\ \Downarrow & \approx & \Downarrow \\ O(3) & & SU(2)_V \times P_{LR} \end{array}$$

~> **Brane-localized kinetic terms for fermions/gauge fields**

Carena et al. (2002)    Aguila et al. (2003)

~> **Modification of the AdS metric in the vicinity of the IR brane**

Cabrer, Gersdorff, Quiros (2010)

« *Minimal* » representations under  $SU(2)_L \times SU(2)_R \times U(1)_X$ :  $H=(2,2)_0$

$$\begin{pmatrix} t_{1L} & b'_L & q'_{-4/3L} \\ b_{1L} & q''_{-4/3L} & q'_{-7/3L} \end{pmatrix}_{-5/6} \quad (b_R \ q'_{-4/3R})_{-5/6} \quad \begin{pmatrix} q'_{5/3L} & t_{2L} \\ t'_L & b_{2L} \end{pmatrix}_{2/3} \quad (t_R)_{2/3}$$



“custodians”

$$SU(2)_R \longrightarrow U(1)_R$$

$$U(1)_R \times U(1)_X \longrightarrow U(1)_Y$$

$$W_R^3 \quad B_X \longrightarrow B_Y \quad ( + Z'^{KK} )$$

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$Z'$  charges ( $I_{3R}$  isospin) and coupling ( $g_{Z'} \sim 2$ )  $\Rightarrow$   $Zbb$  couplings addressing  $A^b_{FB}$

$t_R$  singlet: no custodian top partners  $\Rightarrow$  possible large  $g^{KK}t\bar{t}$  couplings favor  $A^t_{FB}$

## II) $A_{FB}^t$ and $t\bar{t}$ cross section @ Tevatron

### $A_{FB}^t$ at Tevatron

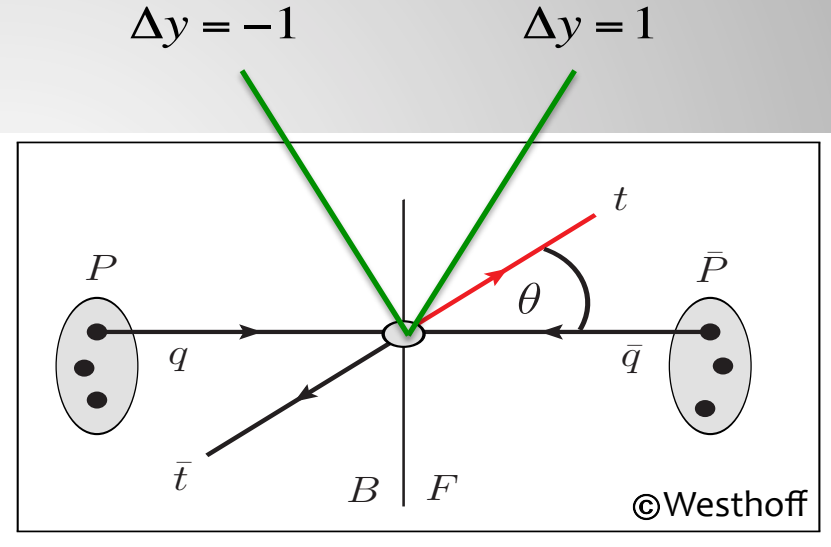
« What is the Forward-Backward asymmetry for the top quark ? »

$\neq 0$  with Parity-violating couplings

$$A_{FB}^t = \frac{\sigma^F - \sigma^B}{\sigma^F + \sigma^B} = \frac{\sigma[\cos \theta_t^* : 0 \rightarrow 1] - \sigma[\cos \theta_t^* : -1 \rightarrow 0]}{\sigma[\cos \theta_t^* : 0 \rightarrow 1] + \sigma[\cos \theta_t^* : -1 \rightarrow 0]} = \frac{\sigma[y_t > 0] - \sigma[y_t < 0]}{\sigma[y_t > 0] + \sigma[y_t < 0]}$$

(  $t\bar{t}$  rest frame )

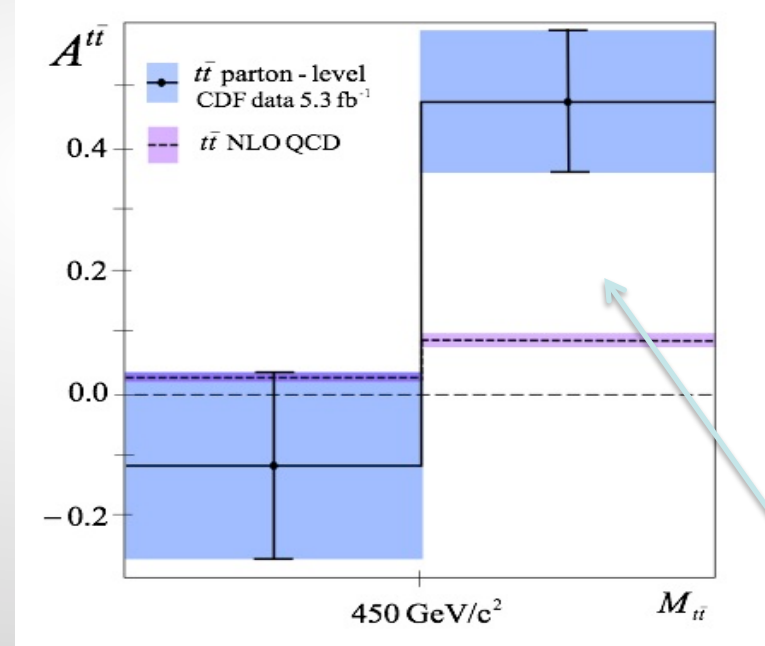
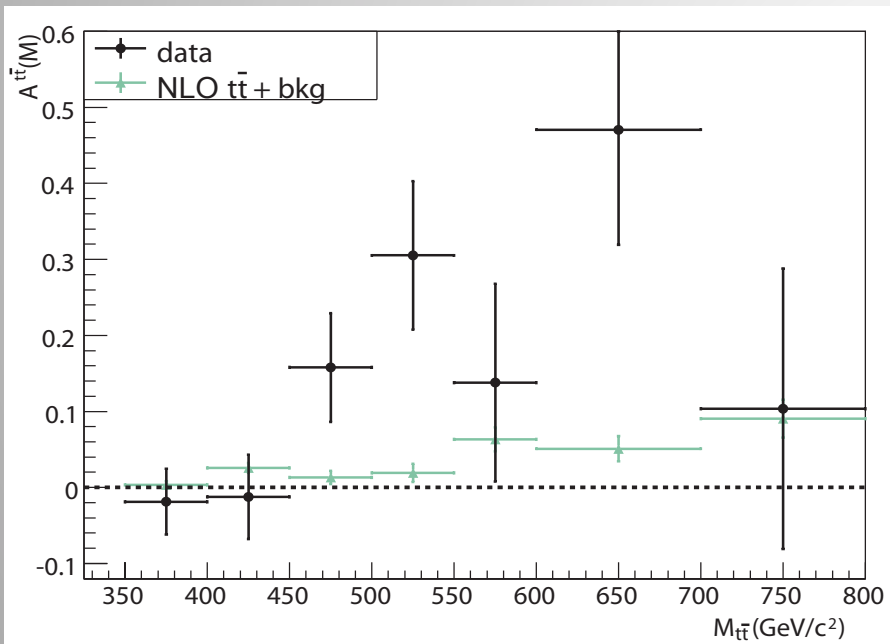
Rapidity :  $y_t = \frac{1}{2} \ln[(E + p_z)/(E - p_z)] = \Delta y/2$



the data we use cause: most recent, unfolded  
and the only ones on rapidity dependence

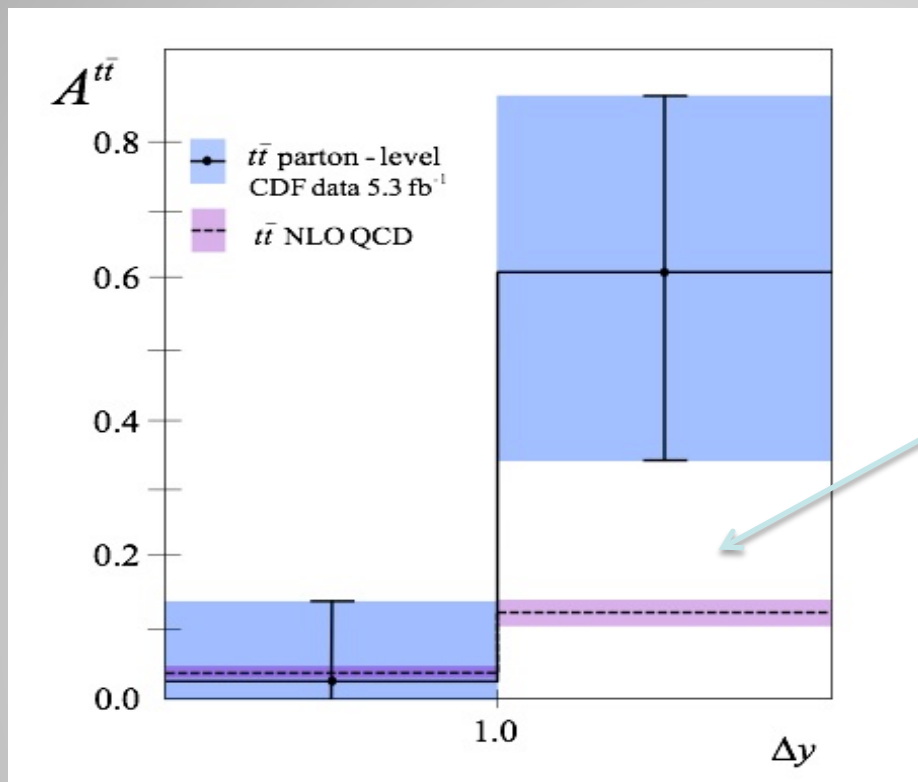
**01-2011** CDF in the lepton+jets channel with  $5.3\text{fb}^{-1}$  :

$A_{\text{FB}}^t = 0.158 \pm 0.075$  (+1.3 sigma from SM prediction)



unfolding

+3.4 standard  
deviations from SM



+1.9 standard  
deviation from SM

$$A_{\text{FB}}^{|\Delta y| < 1} = \frac{N(1 > \Delta y > 0) - N(-1 < \Delta y < 0)}{N(1 > \Delta y > 0) + N(-1 < \Delta y < 0)},$$

$$A_{\text{FB}}^{|\Delta y| > 1} = \frac{N(\Delta y > 1) - N(\Delta y < -1)}{N(\Delta y > 1) + N(\Delta y < -1)}$$

$$|\Delta y| < 3$$



# $A_{FB}^t$ in the considered warped model



+ interferences with SM

(negligible EW gauge contrib.)

$A_{FB}^t$  non-vanishing (Parity violation)  $\left[ \begin{array}{l} g_s Q(c_{t_L}) \neq g_s Q(c_{t_R}) \\ g_s Q(c_{q_L}) \neq g_s Q(c_{q_R}) \end{array} \right. \Rightarrow \left. \begin{array}{l} \text{slightly closer} \\ \text{to TeV-brane :} \\ c_{u_L}, c_{d_L} \lesssim 0.5 \end{array} \right]$

5D mass :  $c k$   $\Rightarrow A_{FB}^t$  significant  $\Rightarrow M_{KK} \sim 1.5 - 2 \text{ TeV}$   $\left. \begin{array}{l} \text{EW tests} \\ \text{not so far} \\ \text{treated in} \\ \text{this setup} \end{array} \right]$

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 \end{array}
 \quad \left. \vphantom{\begin{array}{l} A_{FB}^t \text{ non-vanishing} \\ A_{FB}^t \text{ significant} \end{array}} \right\} \begin{array}{l} \text{EW tests} \\ \text{not so far} \\ \text{treated in} \\ \text{this setup} \end{array}$$

We will show that EW  
fits are OK for :

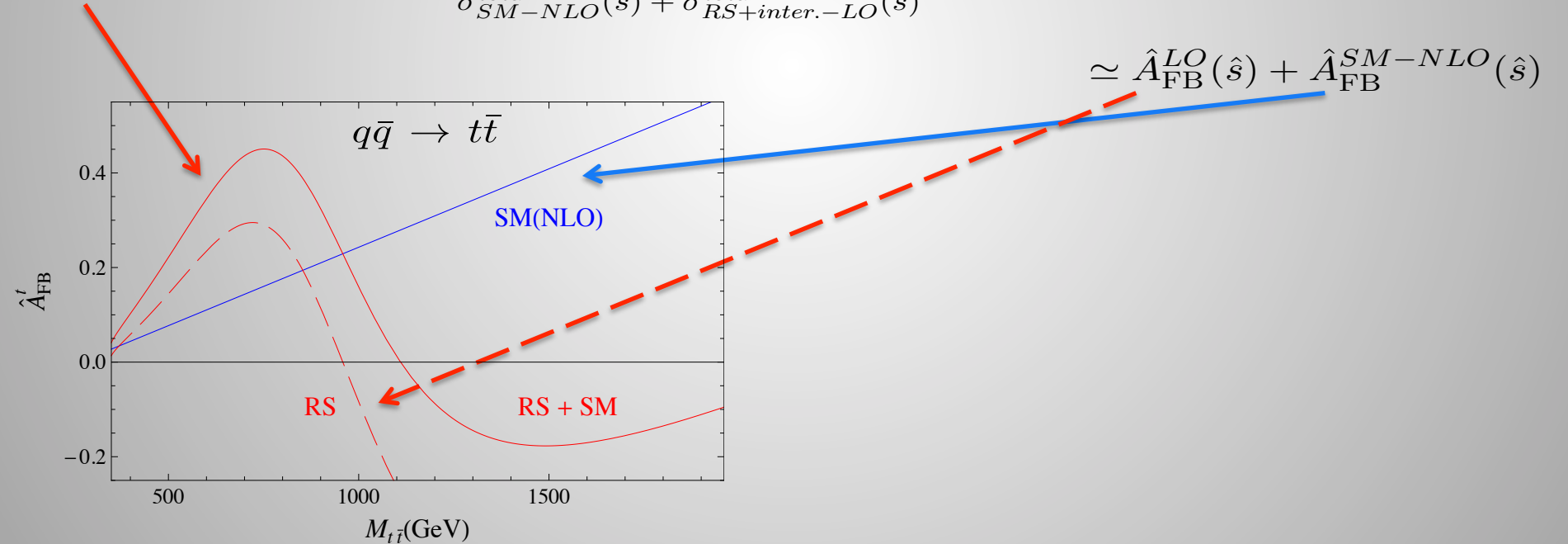
$$\begin{array}{l}
 c_{u/d_L} \sim 0.44, c_{u/d_R} \sim 0.8, c_{c/s_L} \sim 0.6, c_{c_R} \sim 0.6, \\
 c_{s_R} \sim 0.49, c_{t/b_L} \sim 0.51, c_{b_R} \sim 0.53, c_{t_R} \sim -1.3
 \end{array}$$

# Asymmetry at parton level (neglecting 2<sup>nd</sup>/3<sup>rd</sup> generation + gluon initial state)...

$$\hat{A}_{\text{FB}}^{LO}(\hat{s}) = a_q a_t \frac{4\pi\alpha_s^2(\mu_r)}{9} \frac{\beta_t^2}{\hat{\sigma}_{SM-LO}^{\text{total}}(\hat{s}) + \hat{\sigma}_{RS+inter.-LO}^{\text{total}}(\hat{s})} \left[ (\hat{s} - M_{KK}^2) + 2v_q v_t \hat{s} \right]$$

$$\left[ \begin{aligned} a_q &= (Q(c_{q_R}) - Q(c_{q_L}))/2, \\ a_t &= (Q(c_{t_R}) - Q(c_{t_L}))/2, \\ v_q &= (Q(c_{q_R}) + Q(c_{q_L}))/2, \\ v_t &= (Q(c_{t_R}) + Q(c_{t_L}))/2, \end{aligned} \right.$$

$$\hat{A}_{\text{FB}}^{NLO}(\hat{s}) = \frac{(\hat{\sigma}_{SM-NLO}^F(\hat{s}) + \hat{\sigma}_{RS+inter.-LO}^F(\hat{s})) - (\hat{\sigma}_{SM-NLO}^B(\hat{s}) + \hat{\sigma}_{RS+inter.-LO}^B(\hat{s}))}{\hat{\sigma}_{SM-NLO}^{\text{total}}(\hat{s}) + \hat{\sigma}_{RS+inter.-LO}^{\text{total}}(\hat{s})}$$

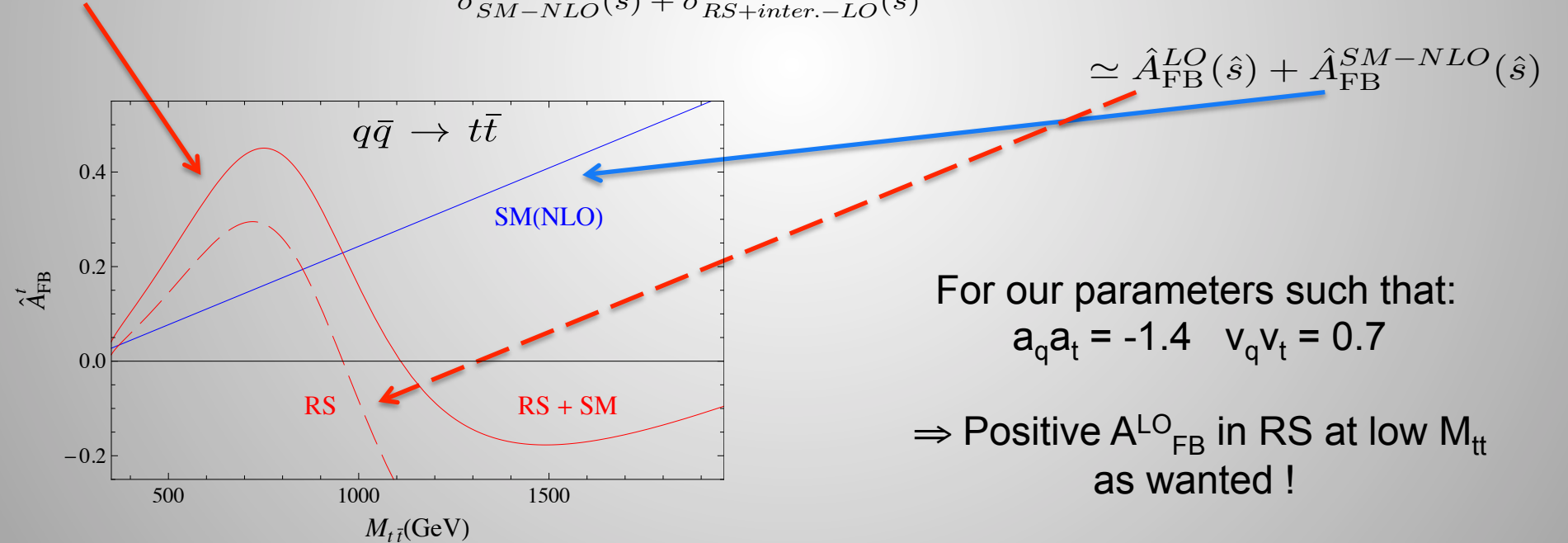


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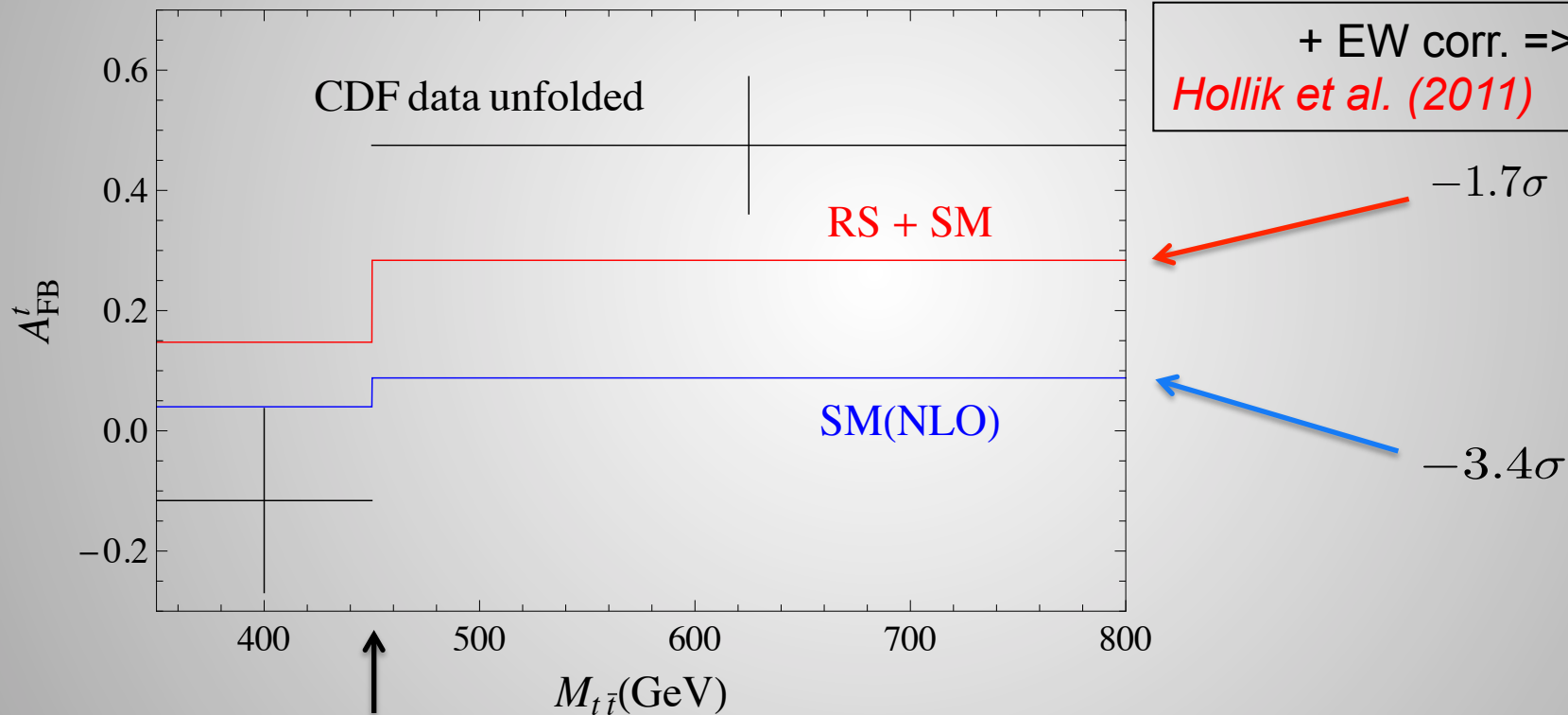
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# Full asymmetry after convolution with MSTW-2008...

$$\mu_f = \mu_r = m_t = 172.5 \text{ GeV}$$

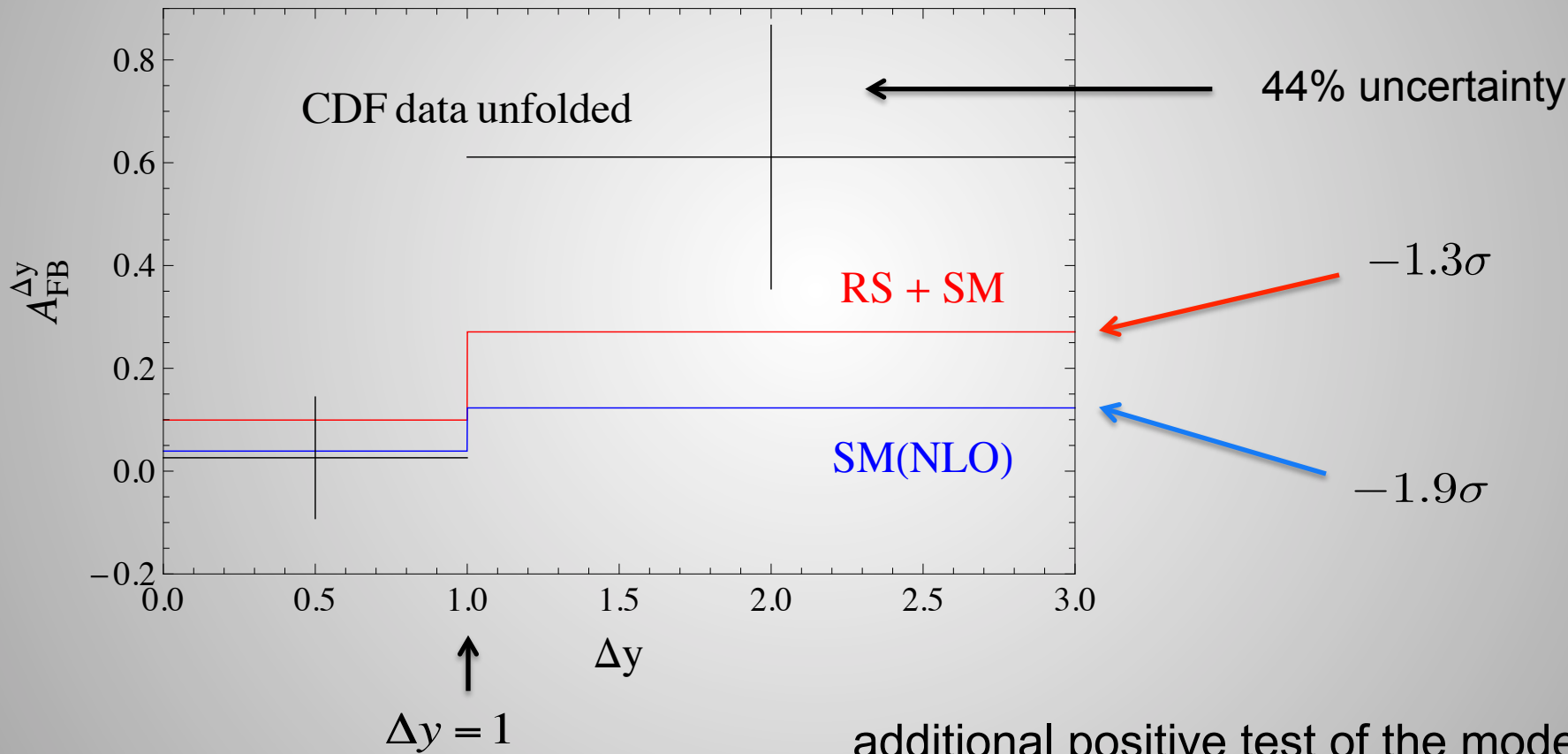


+ EW corr.  $\Rightarrow \sim -1.3\sigma$   
*Hollik et al. (2011)*

rest of the discrepancy : RS @ NLO ?

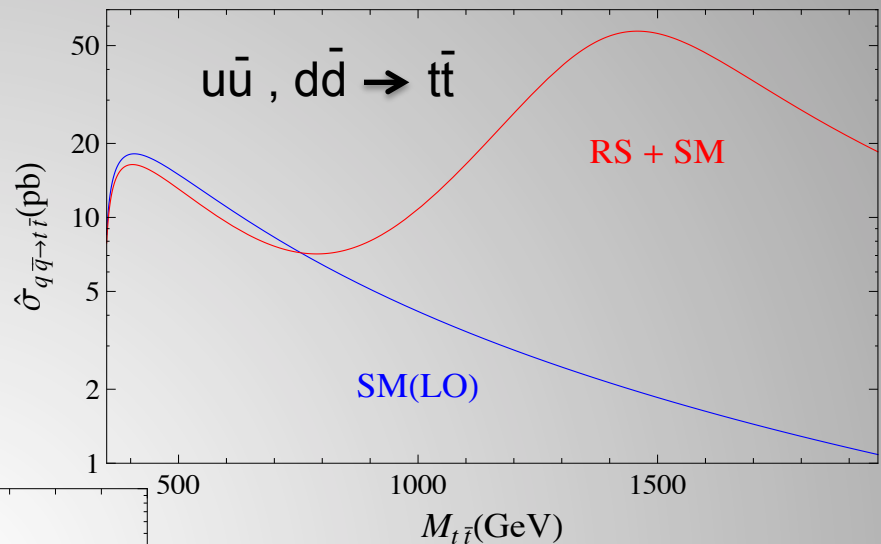
## Full asymmetry as a function of rapidity...

$$\mu_f = \mu_r = m_t = 172.5 \text{ GeV}$$



*One must take care of the differential  $t\bar{t}$  production cross section in good agreement with the SM...*

$$\frac{d\sigma_{SM-NNLO}}{dM_{t\bar{t}}} \left( 1 + \frac{d\sigma_{RS+inter.-LO}}{dM_{t\bar{t}}} / \frac{d\sigma_{SM.-LO}}{dM_{t\bar{t}}} \right)$$



In SM :

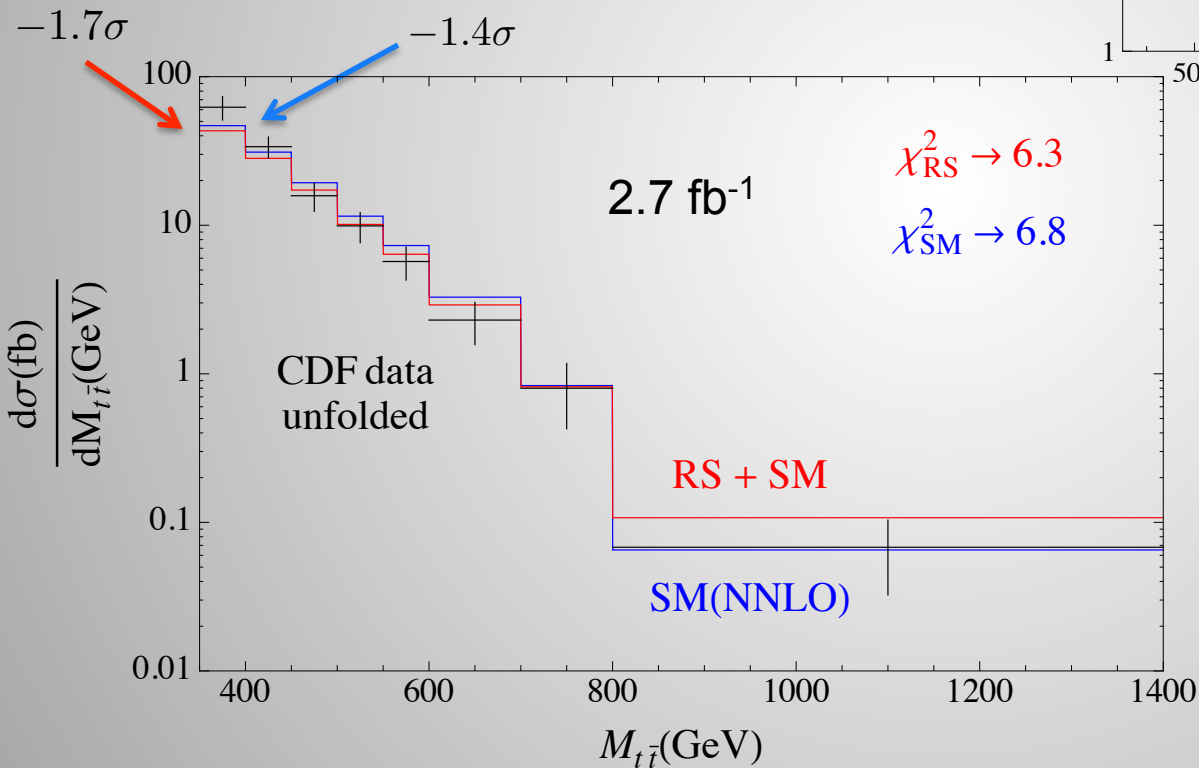
$$\chi_{\text{SM}}^2 / d.o.f. = 6.8 / 8$$

In RS :

$$\chi_{\text{RS}}^2 / d.o.f. = 6.3 / 8$$

$$m_t = 175 \text{ GeV}$$

$$\mu_f = \mu_r = m_t$$



What about the **whole** integrated top quark **asymmetry** and **cross section** ?



Tevatron data [5] :  $0.158 \pm 0.075$

[5] CDF Collaboration

arXiv:1101.0034

SM [NLO] [5] :  $0.058 \pm 0.009 (-1.33\sigma)$

RS+SM :  $0.189 \pm 0.010 (+0.42\sigma)$

 improves



Theoretical (HATHOR):  $\sigma(p\bar{p} \rightarrow t\bar{t}) = 6.62 \pm 1 \text{ pb}$

$\mu_R = \mu_F = m_t = 172.5 \text{ GeV}$

MSTW PDF NNLO

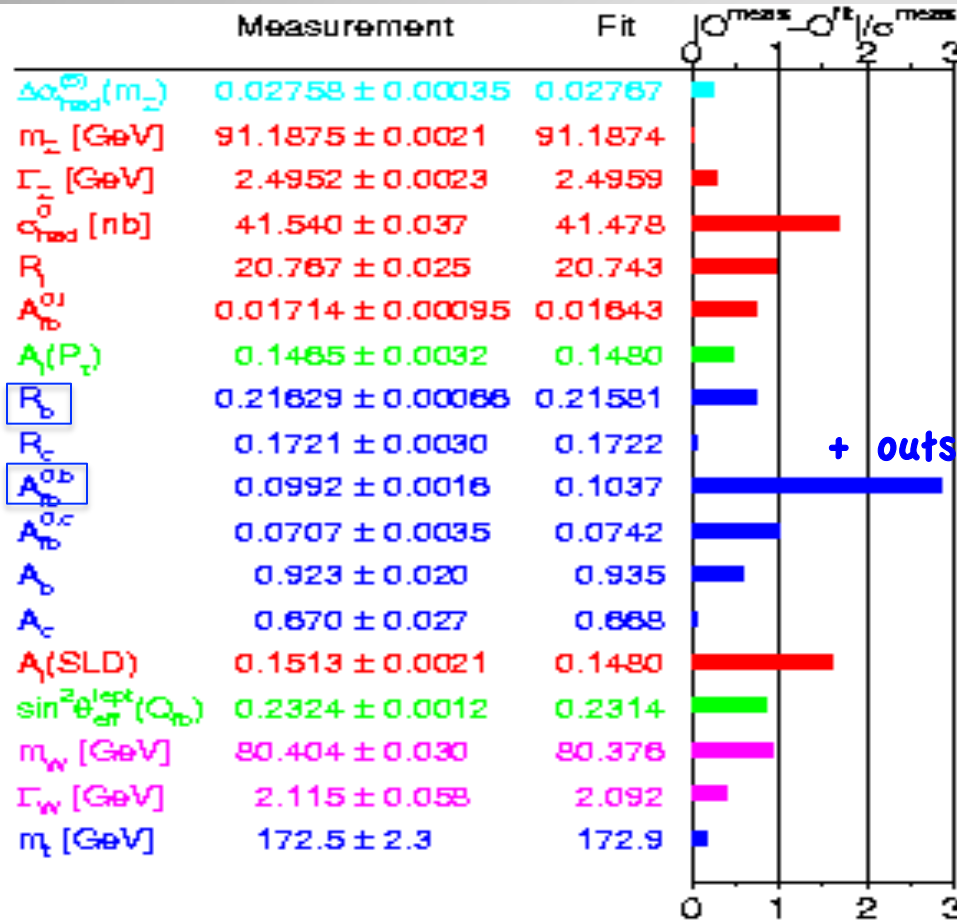
Experimental (Tevatron):  $7.50 \pm 0.48 \text{ pb}$  CDF Collaboration, Note 9913,  
Run II, October 2009.



OK as heavy KK gluon with broad resonance



### III) $A_{FB}^b$ and EW precision tests @ LEP



$A_{FB}^b$  : a NP effect in the b sector ?

$$A_{FB}^b(p\hat{o}le) \equiv \frac{\int_0^{+1} \sigma_{\theta} d \cos \theta - \int_{-1}^0 \sigma_{\theta} d \cos \theta}{\sigma_0(e^+e^- \rightarrow \gamma / Z \rightarrow b\bar{b})}$$

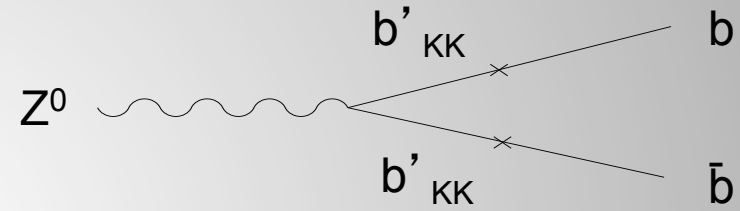
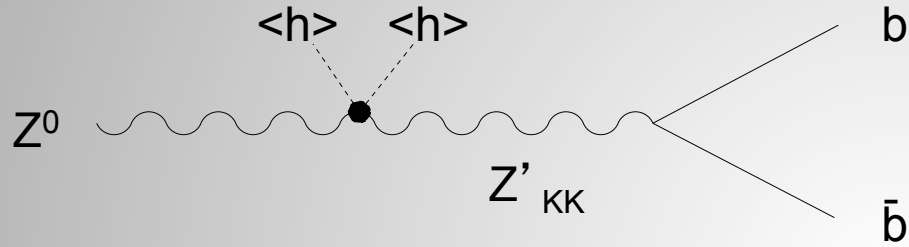
$$= \frac{3}{4} \frac{(Q_Z^{eL})^2 - (Q_Z^{eR})^2}{(Q_Z^{eL})^2 + (Q_Z^{eR})^2} \frac{(Q_Z^{bL})^2 - (Q_Z^{bR})^2}{(Q_Z^{bL})^2 + (Q_Z^{bR})^2}$$

+ outside Z pôle !

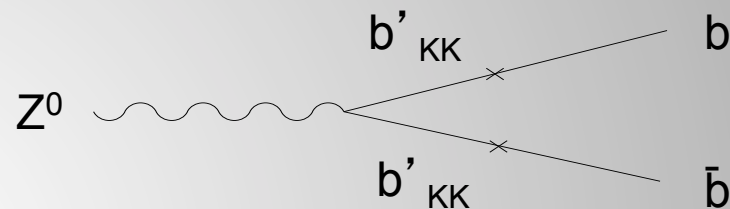
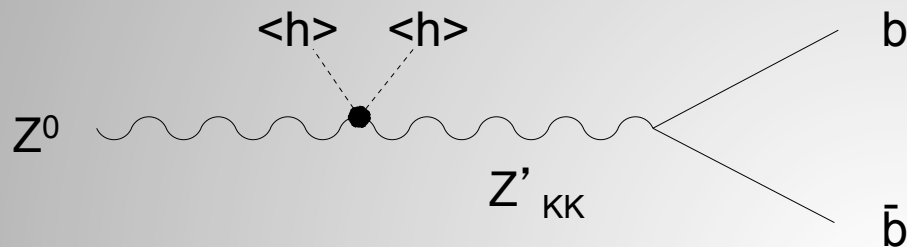
$$R_b \equiv \frac{\Gamma(Z \rightarrow b\bar{b})}{\Gamma(Z \rightarrow \text{hadrons})}$$

$$= \frac{(Q_Z^{bL})^2 + (Q_Z^{bR})^2}{\sum_{q \neq t} [(Q_Z^{qL})^2 + (Q_Z^{qR})^2]}$$

*Interpretation in a generic extra-dimensional model...*  
**(difficult in SUSY)**



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**(difficult in SUSY)**



$$\left| \delta Q_Z^{f_l} \right| \approx 1\%_{00} \ll \left| \delta Q_Z^{b_{L/R}} \right| \approx |-1.5/30\%|$$

$$\text{Coupling } Z_{KK} f_l \bar{f}_l \ll \text{Coupling } Z_{KK} b \bar{b}$$

$\Downarrow$

$$m_{b'}(c_{t_R}) \ll m_{f'}(c_{\text{light}})$$

$$m_t(c_{t_R}) \uparrow \Rightarrow m_{b'}(c_{t_R}) \downarrow$$

$\Downarrow$

**'natural' conditions within the RS model**

# Summary of the EW observables...

Observable	SM	RS
$A_{FB}^b(m_Z)$	$2.7\sigma$	$1.2\sigma$
$R_b$	$0.8\sigma$	$1.2\sigma$
$A_{FB}^c(m_Z)$	$0.9\sigma$	$0.9\sigma$
$R_c$	$0.0\sigma$	$0.5\sigma$
$A_{FB}^s(m_Z)$	$0.6\sigma$	$0.2\sigma$
$\Gamma_{\text{had}}(Z)$	$1.3\sigma$	$1.0\sigma$
$\Gamma_{\text{tot}}(W)$	$0.2\sigma$	$0.2\sigma$
$\langle Q_{FB} \rangle$	$1.1\sigma$	$0.1\sigma$
$C_{1u} + C_{1d}$	$0.2\sigma$	$0.8\sigma$
$C_{1u} - C_{1d}$	$1.1\sigma$	$0.1\sigma$
$\chi^2/d.o.f.$	25.3/17	19.8/17

no more  $A_{FB}^b$  anomaly  
at the  $Z^0$  pole

still fits well

whole fit improved

+ Zuu/Zdd OK from  
Tevatron Run I & II  
& HERA (H1, ZEUS)

## IV) Constraints and predictions @ LHC

### Comparison of the $t\bar{t}$ cross section $\sigma_{t\bar{t}}$

in RS+SM      NNLO       $\mu_F = \mu_R = m_t = 173 \text{ GeV}$        $\sqrt{s} = 7 \text{ TeV}$   
(HATHOR)       $\mathcal{L} = 35 \text{ pb}^{-1}$

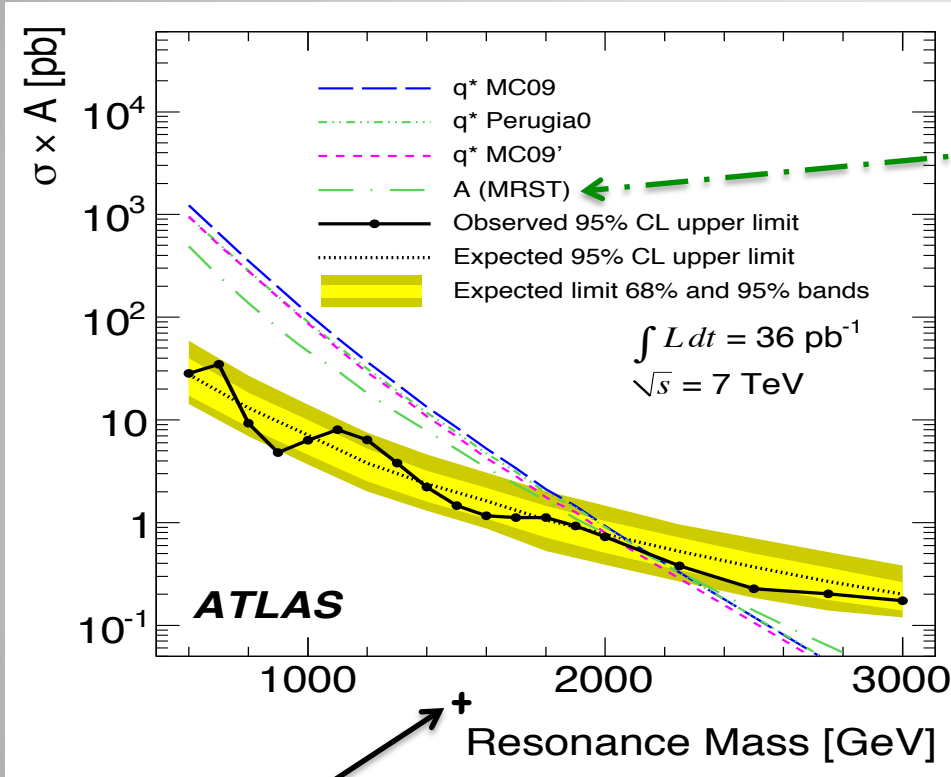
$\sigma(pp \rightarrow t\bar{t})$  at  $-0.86\sigma$       from the ATLAS measurement,  $180 \pm 18.5 \text{ pb}$   
SM at  $-0.81\sigma$

$\sigma(pp \rightarrow t\bar{t})$  at  $+0.36\sigma$       from the CMS measurement,  $158 \pm 19 \text{ pb}$   
SM at  $+0.31\sigma$



OK as major contribution from the gg initial state

# Constraints from dijets



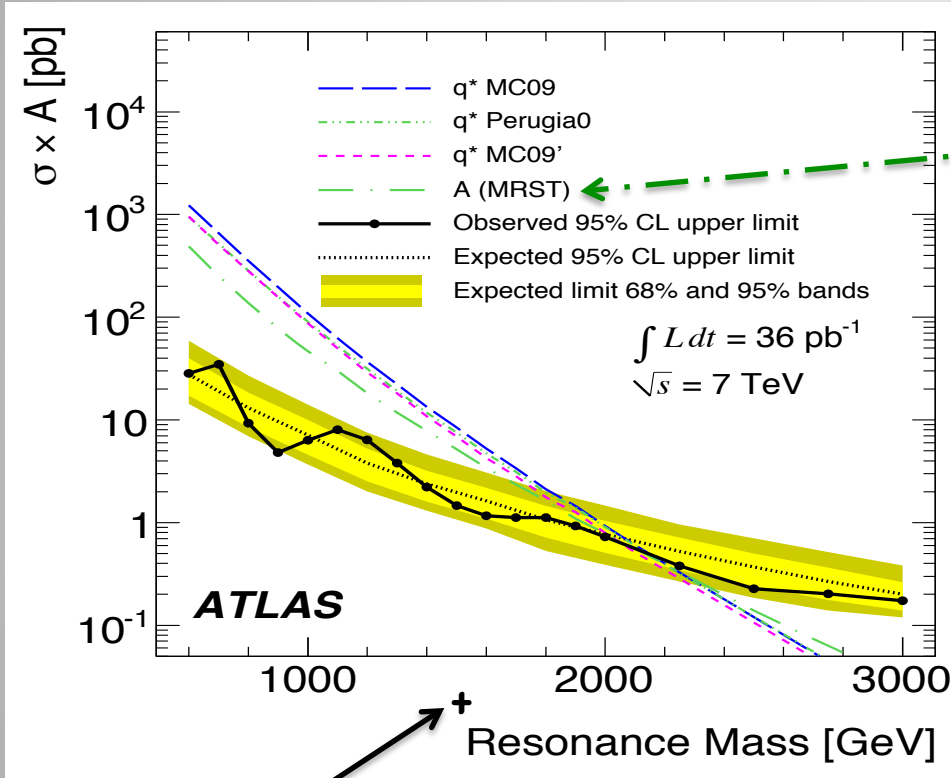
Axigluon -  $SU(3)_L \times SU(3)_R$

*Frampton et al. (1987)*  
*Bagger et al. (1987)*

- ★ now including the width effect between  $0.7 M_{KK}$  and  $1.3 M_{KK}$
- ★ we have also checked the angular distribution constraints

computing the ratio  $RS/A_{\text{Axigluon}}$   
 $\Rightarrow KK$  gluon exchange @ 0.023 pb

# Constraints from dijets



Axigluon -  $SU(3)_L \times SU(3)_R$

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- ★ now including the width effect between  $0.7 M_{KK}$  and  $1.3 M_{KK}$
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Coupling  $g^{(1)tt} > g^{(1)qq}$

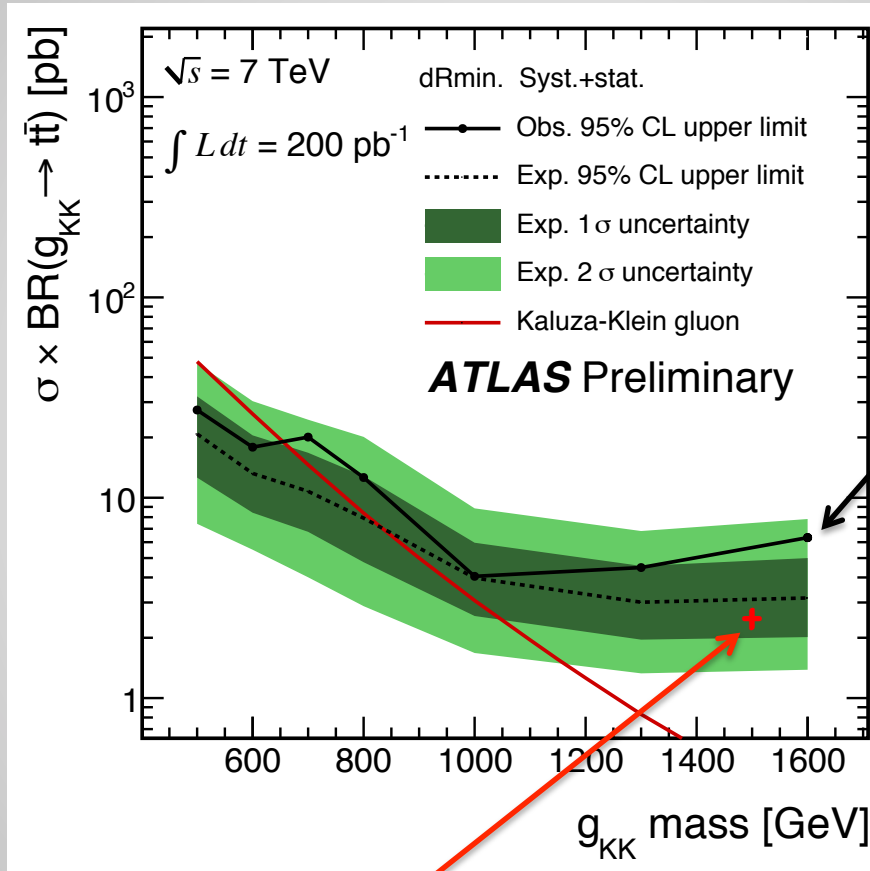


RS addresses  $A_{FB}^t$   
 + passes dijet bounds

computing the ratio RS/Axigluon  
 $\Rightarrow KK$  gluon exchange @ 0.023 pb

# KK gluon searches at LHC

June 5, 2011

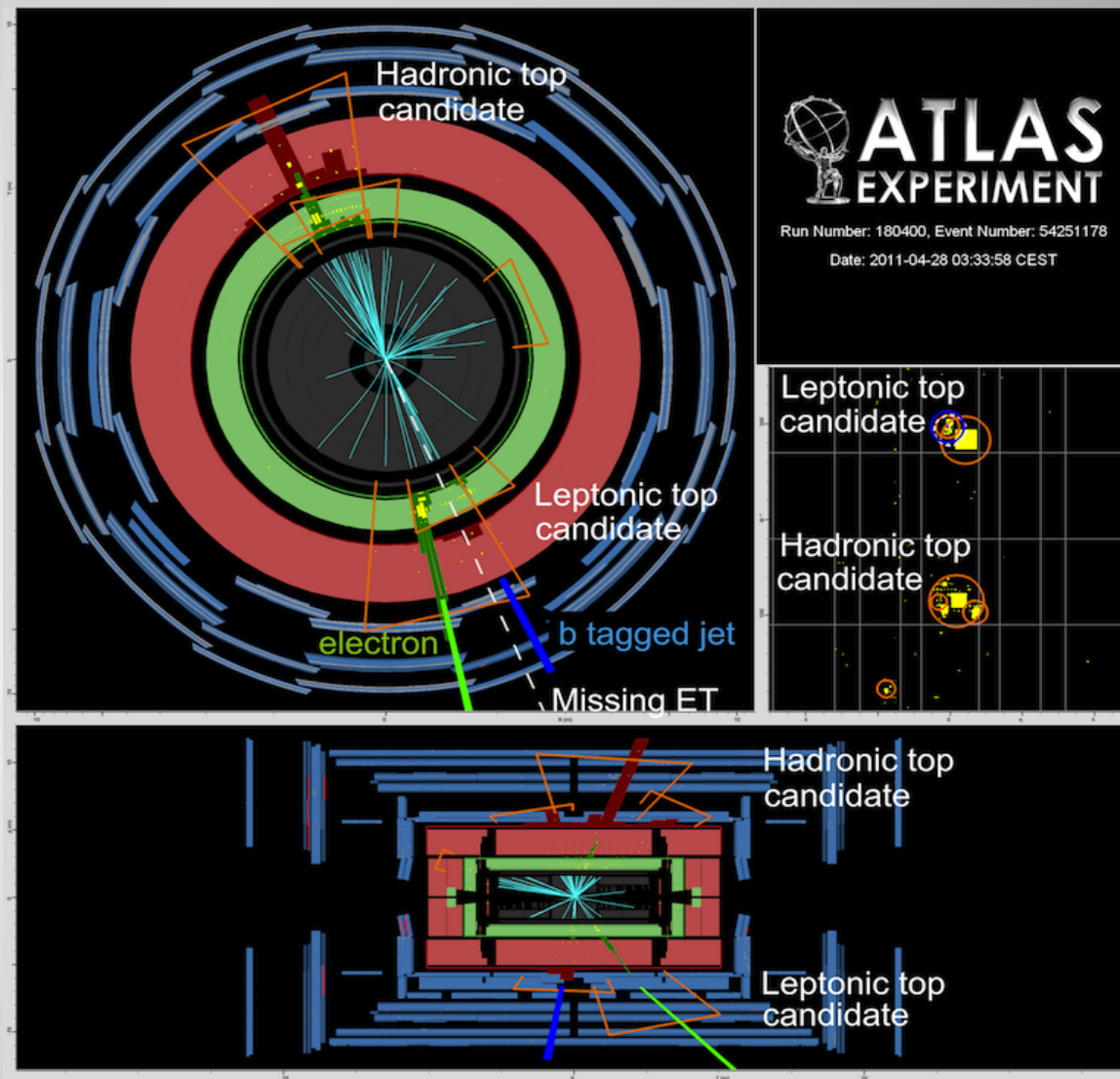


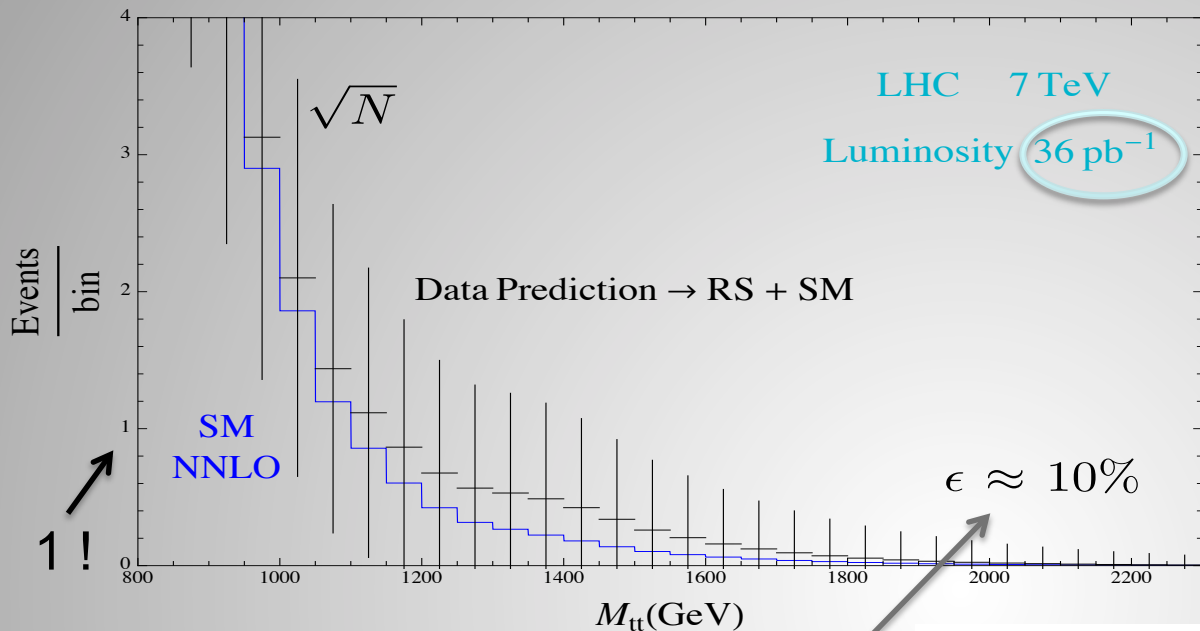
interesting  $\sim 1.5\sigma$  effect  
seen at  $M_{\text{KK}} \sim 1.6 \text{ TeV}$  (!)

rescaling to our KK couplings  
 $\Rightarrow$  KK gluon exchange @ 2.3 pb (conservative due to our larger  $g_{\text{KK}}$  width)



An observed intriguing high-mass ( $M_{t\bar{t}} \sim 1.6\text{TeV}$ ) candidate event with boosted top quarks...



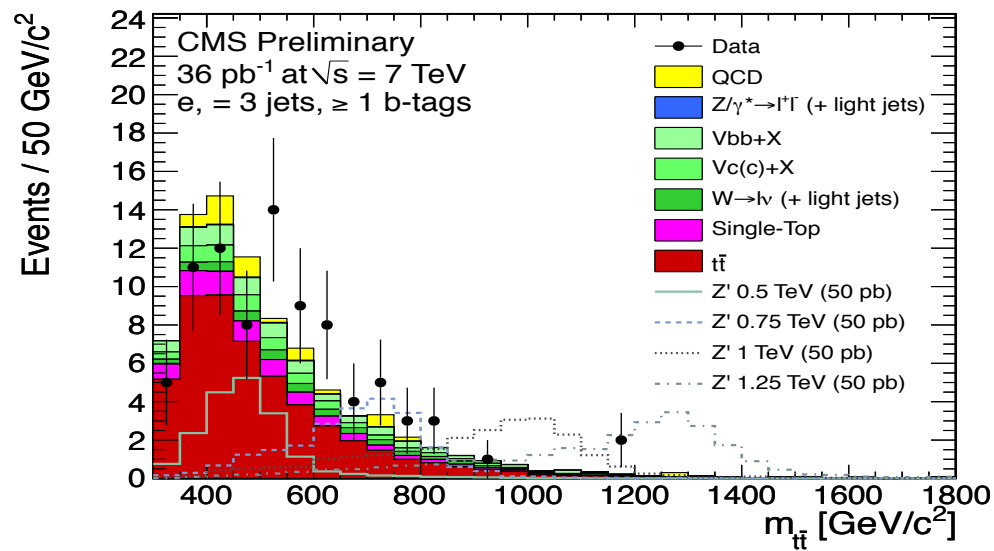


Predictions on the  $M_{t\bar{t}}$  distribution at LHC

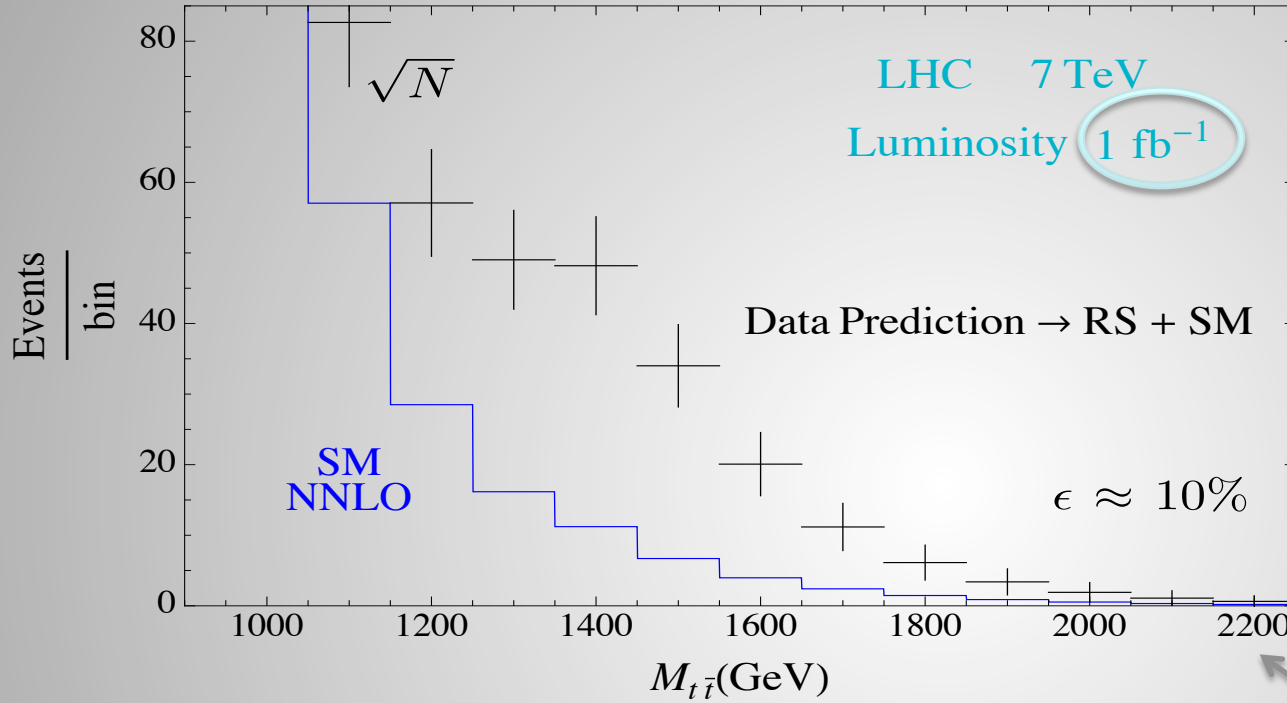
compatible

$t\bar{t}$  reconstruction efficiency taken

$$\mu_f = \mu_r = m_t = 173 \text{ GeV}$$



What does the RS model predicts at the expected luminosity of  $1 \text{ fb}^{-1}$  ?



..a KK gluon resonance

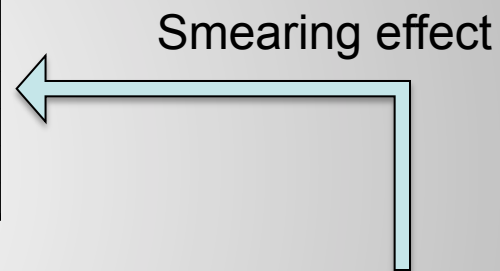
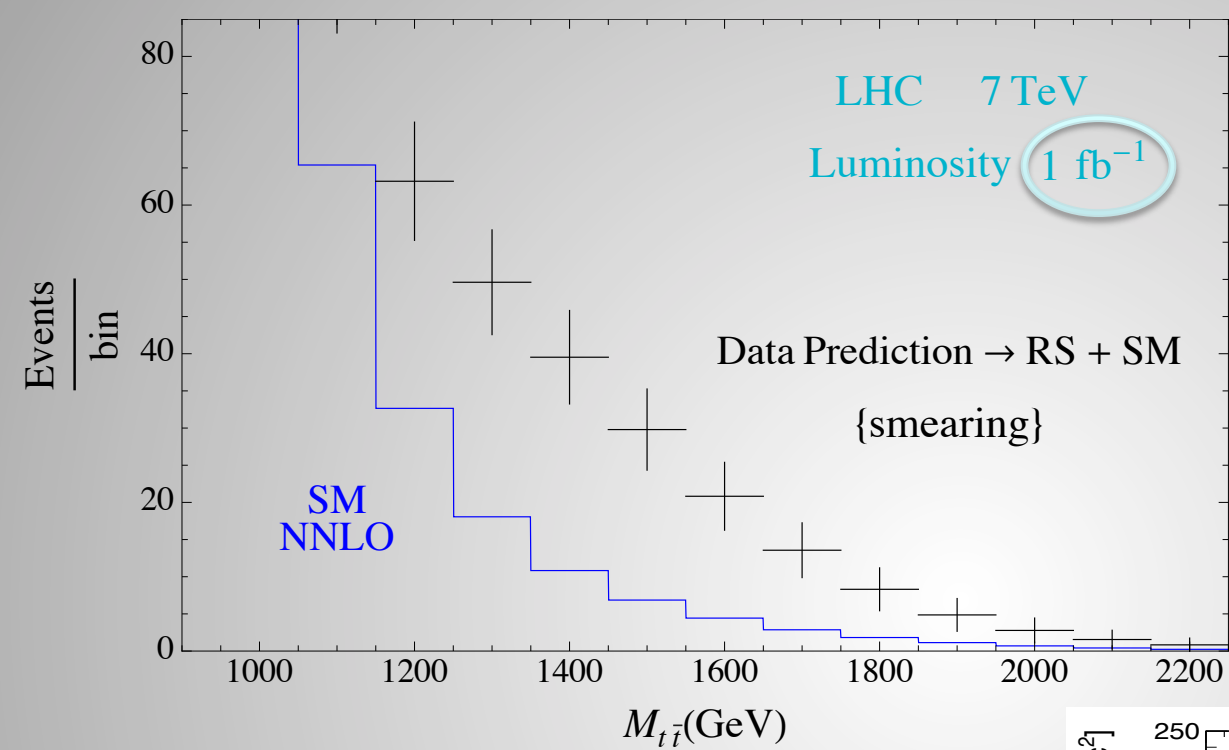
$$\Gamma_{g(1)} \simeq 40\% M_{KK}$$

assuming 100 GeV bins

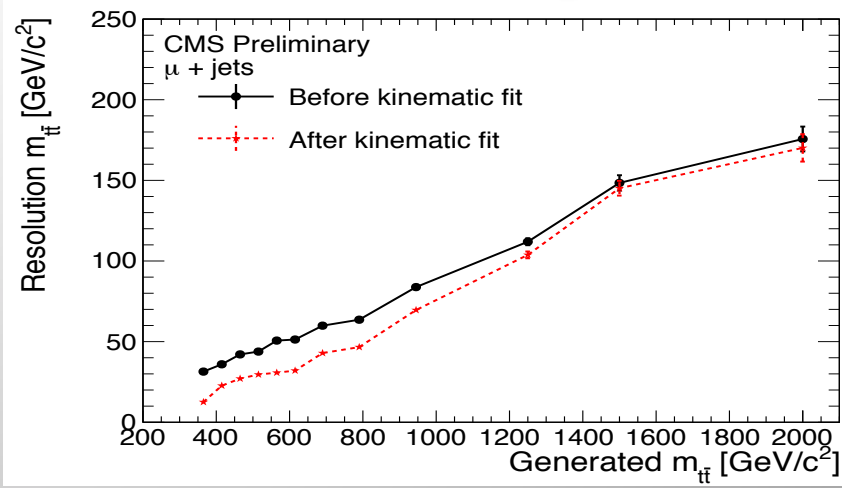
integration of the cross section e.g. over  $[1050, 1750] \text{ GeV}$

$$\text{Signal} / \sqrt{\text{Background}} \simeq 13.9$$

**An excess should be clearly visible.**



**A great excess even simulating  
the  $M_{t\bar{t}}$  experimental resolution:**



## V) Other scenarios explaining $A_{FB}^t$ ?

➡ Messages from the effective operator approach...  
(trying to fit  $A_{FB}^t$  and  $\sigma_{t\bar{t}}$  )

Aguilar-S. et al. (2011)

Delaunay et al. (2011)

Degrande et al. (2011)

Extra **scalar** field – color octet [t-channel] : *impossible*

‘ ‘ – color triplet [t-channel] : *possible (diquark FC couplings)*

Shu et al. (2010), ...

‘ ‘ – color singlet [s- & t-channel] : *difficult*

Giudice et al. (2011)

Extra **vector** boson – color octet [s-channel] : *possible (Axigluon / KK gluon)*

Hewett et al. (2011) / here

‘ ‘ – color singlet [s- & t-channel] :

*tensions as no  $Z', W'$  interferences with the SM contributions (QCD@LO)*

*Possibility: t-chan. exchange of a non-abelian  $Z'$  (with  $Z' u_R t_R$  couplings)*

Jung et al. (2011)

## VI) Conclusions

- ☀ The 'warped paradigm', with theoretical motivations, predicts deviations from SM in the 3<sup>rd</sup> generation sector =>  $A_{FB}^b$ ,  $A_{FB}^t$  = *early indications* ?
- ☀ We suggest a geometrical RS realization addressing both  $A_{FB}^b$  and  $A_{FB}^t$ .
- ☀ The several constraints on the parameter space render this RS scenario quite *predictive on the effects in the  $t\bar{t}$  invariant mass distribution @ LHC*.
- ☀ One must wait for more data (Tevatron, LHC) in order to discriminate between the main  $A_{FB}^t$  interpretations: Z/W', KK gluon, Axigluon, stop...
- ☀ This RS model addressing  $A_{FB}^b$ ,  $A_{FB}^t$  predicts a **KK gluon resonance**  
 $\neq$   
Other RS models usually with light **custodians copiously producible**  
( '*no-lose signal*' theorem in warped pheno. @ LHC )

Back up

Some useful formula's...

$$\cos \theta_t^* = \sqrt{1 + \frac{4m_t^2}{\hat{s} - 4m_t^2}} \tanh y_t$$

$$\frac{1}{\mathcal{D}} = \hat{s} - M_{KK}^2 + i \frac{\hat{s}}{M_{KK}^2} \sum_q \Gamma_{KK}^{g(1) \rightarrow q\bar{q}} M_{KK} \frac{\beta_q [v_q^2 (3 - \beta_q^2)]/2 + a_q^2 \beta_q^2}{v_q^2 + a_q^2}$$

$$\beta_t = \sqrt{1 - 4m_t^2/\hat{s}}$$

$$\sqrt{\hat{s}_0} \simeq \frac{M_{KK}}{(1 + \Gamma_{KK}^2/M_{KK}^2)^{1/4}}$$



$$\frac{d\hat{\sigma}_{RS-LO}}{d\cos\theta_t^*}(\hat{s}) = \frac{\pi\alpha_s^2(\mu_r)\beta_t}{9\hat{s}} \times$$

$$\hat{s}^2|\mathcal{D}|^2 \left[ 8v_q v_t a_q a_t \beta_t \cos\theta^* + (a_q^2 + v_q^2) (v_t^2(2 - \beta_t^2 \sin^2\theta^*) + a_t^2 \beta_t^2(1 + \cos^2\theta^*)) \right]$$

$$\frac{d\hat{\sigma}_{inter.-LO}}{d\cos\theta_t^*}(\hat{s}) = \frac{\pi\alpha_s^2(\mu_r)\beta_t}{9\hat{s}} 4\hat{s}\text{Re}(\mathcal{D}) \left[ v_q v_t \left( 1 - \frac{1}{2}\beta_t^2 \sin^2\theta^* \right) + a_q a_t \beta_t \cos\theta^* \right]$$

$$\left( \left. \frac{d\hat{\sigma}_{SM-LO}}{d\cos\theta_t^*}(\hat{s}) \right|_{q\bar{q}} = \frac{\pi\alpha_s^2(\mu_r)\beta_t}{9\hat{s}} \left\{ 2 - \beta_t^2 \sin^2\theta^* \right\} \right)$$

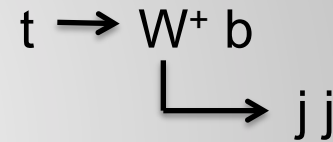
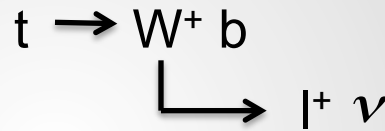
« How is  $A_{\text{FB}}^t$  measured at Tevatron in lepton+jet channels ? »

$$\Delta y = y_t - y_{\bar{t}} \quad y_t = (y_t - y_{\bar{t}})/2$$

$$\Delta y = q(y_l - y_h) = q\Delta y_{lh}$$



in the laboratory frame



$$A_{\text{FB}}^t = \frac{N(\Delta y > 0) - N(\Delta y < 0)}{N(\Delta y > 0) + N(\Delta y < 0)} = \frac{N(q\Delta y_{lh} > 0) - N(q\Delta y_{lh} < 0)}{N(q\Delta y_{lh} > 0) + N(q\Delta y_{lh} < 0)}$$

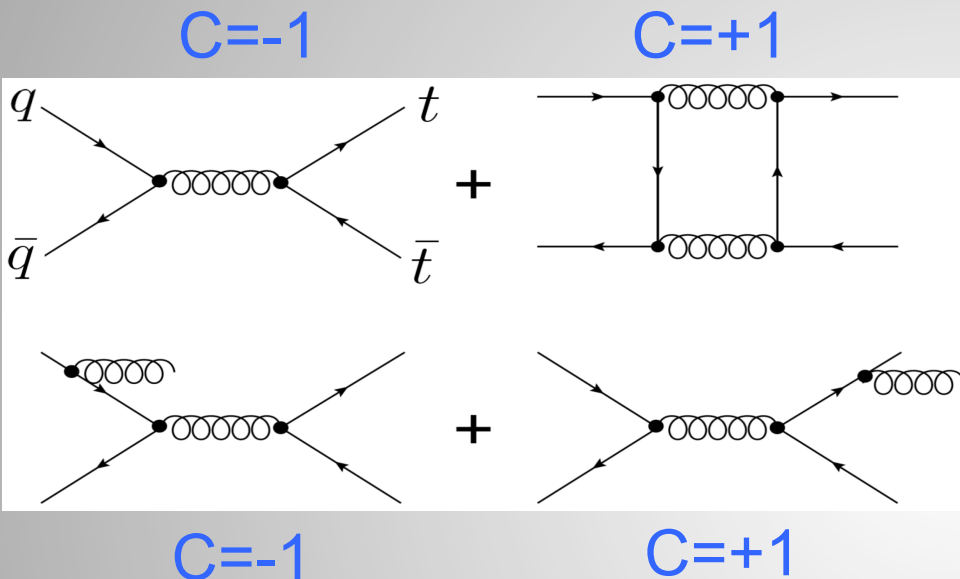
Other asymmetries...

$$A_{\text{FB}}^{p\bar{p}} = \frac{\sigma[y_t^{p\bar{p}} > 0] - \sigma[y_t^{p\bar{p}} < 0]}{\sigma[y_t^{p\bar{p}} > 0] + \sigma[y_t^{p\bar{p}} < 0]}$$

$$A_{\text{C}}^t = \frac{\sigma_t[y_t > 0] - \sigma_{\bar{t}}[y_t > 0]}{\sigma_t[y_t > 0] + \sigma_{\bar{t}}[y_t > 0]}$$

$$A_{\text{C}}^t = A_{\text{FB}}^t \Rightarrow CP$$

# Standard Model (QCD) contribution to $A_{FB}^t$



$$A_{FB}^{SM} = \frac{\sigma_{SM-NLO}^F - \sigma_{SM-NLO}^B}{\sigma_{SM-NLO}^F + \sigma_{SM-NLO}^B}$$

(vanishing at LO)

MCFM for SM ( $m_t=172.5\text{GeV}$ , PDF=CTEQ) @ NLO :  $A_{FB}^t = 0.058 \pm 0.009$


Ahrens et al. (2010) obtain ( $m_t=173.1\text{GeV}$ , PDF=MSTW) :

@ NLO :  $A_{FB}^t = 0.067^{+0.006}_{-0.004}$  @ NNLO-approx :  $A_{FB}^t = 0.064^{+0.009}_{-0.007}$   $0.2 < \mu_f / \text{TeV} < 0.8$

=>  $A_{FB}^t [M_{t\bar{t}} > 450\text{GeV}]$  anomaly probably not fully explained by QCD errors  $\sim 0.01$

## Measurements of $A_{FB}^t$ at Tevatron

*now 5.1fb<sup>-1</sup>: see F.Badaud's talk*

**07-2010** D0 in the lepton+jets channel with **(0.9fb<sup>-1</sup> then) 4.3fb<sup>-1</sup>**   
(*ttbar frame, not unfolded = no subtracting bckgrd & effic. + no ttbar level*) :  
 $A_{FB}^t = 0.08 \pm 0.04 \pm 0.01$  **(+1.7 sigma from SM prediction)**

**03-2009** CDF in the lepton+jets channel with **(1.9fb<sup>-1</sup> then) 3.1fb<sup>-1</sup>**  
(*lab frame, unfolded*) :  
 $A_{FB}^t = 0.193 \pm 0.065 \pm 0.024$  **(+2.1 sigma from SM prediction)**

**01-2011** CDF in the dilepton channel with **5.1fb<sup>-1</sup>**  
(*lab frame, unfolded*) :  
 $A_{FB}^t = 0.42 \pm 0.15 \pm 0.05$  **(+2.3 sigma from SM prediction)**  
**(large error => +1.7 sigma from lept.+jets channel)**

(*lab frame, not unfolded*) :  
 $A_{FB}^t (M_{t\bar{t}} < 450 \text{ GeV}) = 0.104 \pm 0.066$  **(+1.6 sigma from SM prediction)**  
 $A_{FB}^t (M_{t\bar{t}} > 450 \text{ GeV}) = 0.212 \pm 0.096$  **(+2.6 sigma from SM prediction)**

The way to compute it...

$$A_{\text{FB}}^t = \frac{(\sigma_{SM}^F + \sigma_{RS}^F + \sigma_{inter.}^F) - (\sigma_{SM}^B + \sigma_{RS}^B + \sigma_{inter.}^B)}{(\sigma_{SM}^F + \sigma_{RS}^F + \sigma_{inter.}^F) + (\sigma_{SM}^B + \sigma_{RS}^B + \sigma_{inter.}^B)}$$

$$\Leftrightarrow A_{\text{FB}}^t = A_{\text{FB}}^{RS} \times R + A_{\text{FB}}^{SM} \times (1 - R)$$

Cao et al. (2010)

with

$$\left\{ \begin{aligned} A_{\text{FB}}^{RS} &= \frac{(\sigma_{RS-LO}^F + \sigma_{inter.-LO}^F) - (\sigma_{RS-LO}^B + \sigma_{inter.-LO}^B)}{(\sigma_{RS-LO}^F + \sigma_{inter.-LO}^F) + (\sigma_{RS-LO}^B + \sigma_{inter.-LO}^B)} \\ R &= \frac{\sigma_{RS-LO}^{\text{total}} + \sigma_{inter.-LO}^{\text{total}}}{\sigma_{SM-LO}^{\text{total}} + \sigma_{RS-LO}^{\text{total}} + \sigma_{inter.-LO}^{\text{total}}} \end{aligned} \right.$$

ex:  $\sigma_{RS-LO}^F = \sigma_{RS-LO}[\cos \theta_t^* : 0 \rightarrow 1] =$

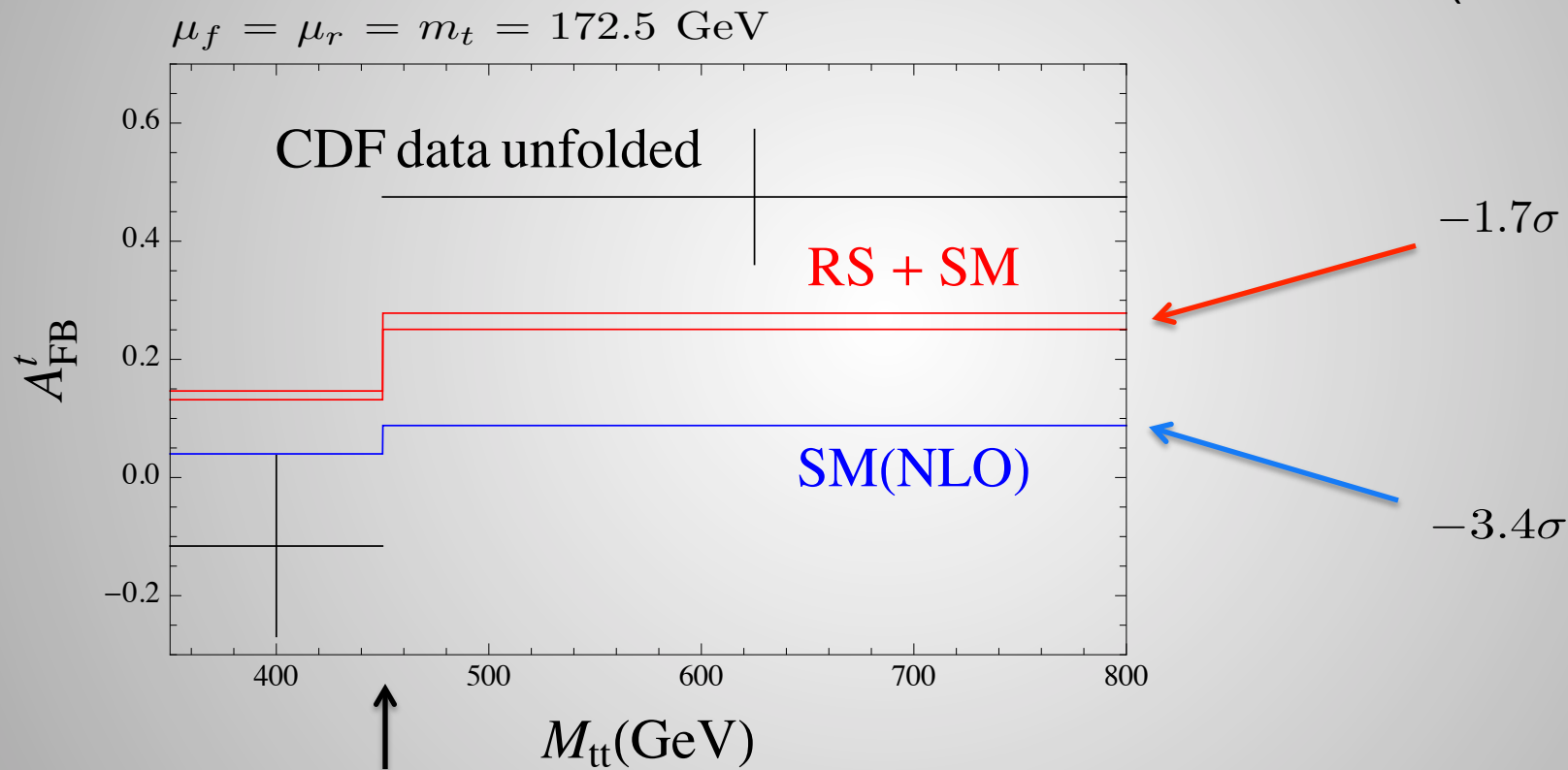
$$\sum_{ij} \int_{\tau_{min}}^{\tau_{max}} d\tau \left[ \int_0^1 d \cos \theta_t^* \left( \frac{d\hat{\sigma}_{RS-LO}}{d \cos \theta_t^*}(\tau s) \right)_{ij} \right] \left\{ \int_{\tau}^1 \frac{dx}{x} f_i(x, \mu_f) f_j\left(\frac{\tau}{x}, \mu_f\right) \right\}$$

$$\tau_{min/max} = \hat{s}_{min/max}/s$$

MSTW-2008-NLO

Looking at the effect of MSTW uncertainties [ $@ 90\%C.L.$ ]...

( $t\bar{t}$ bar frame)



$M_{t\bar{t}} = 450 \text{ GeV}$

no significant dependence as well on  $\mu_f, \mu_r$  and  $m_t$

$$1/(t - M_{KK}^2) \quad -t \leq M_{KK}^2 \quad t = -M_{jj}^2/2 \quad M_{jj} = \sqrt{2}M_{KK} \sim 2 \text{ TeV}$$

$$\cos \theta^* = 0$$

KK gluon produces less than 10% deviation

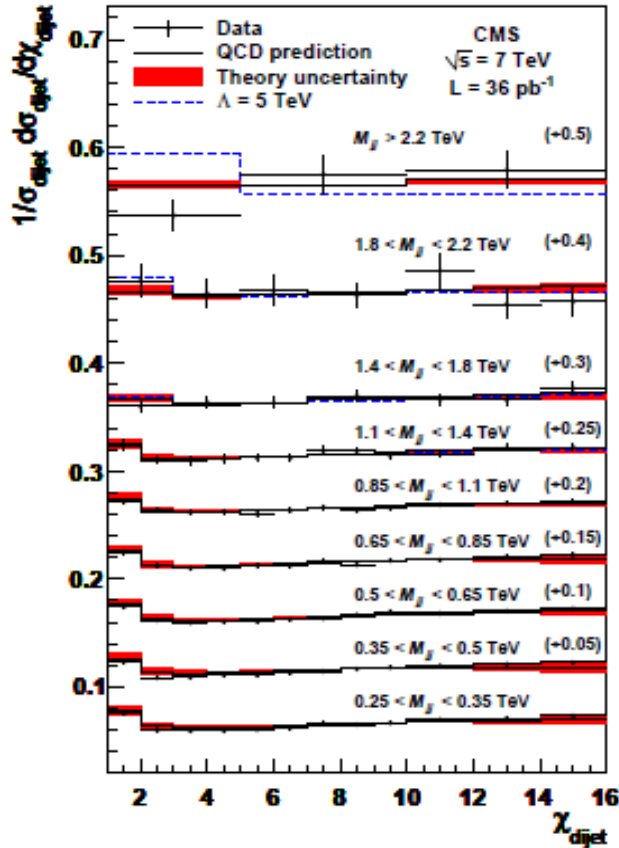
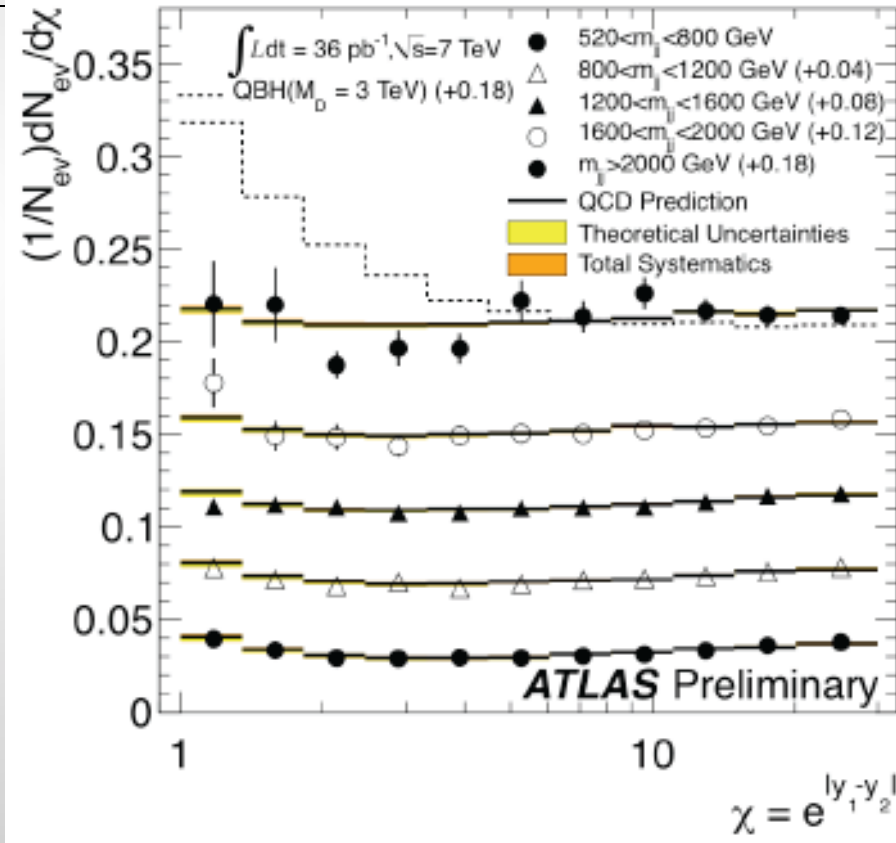
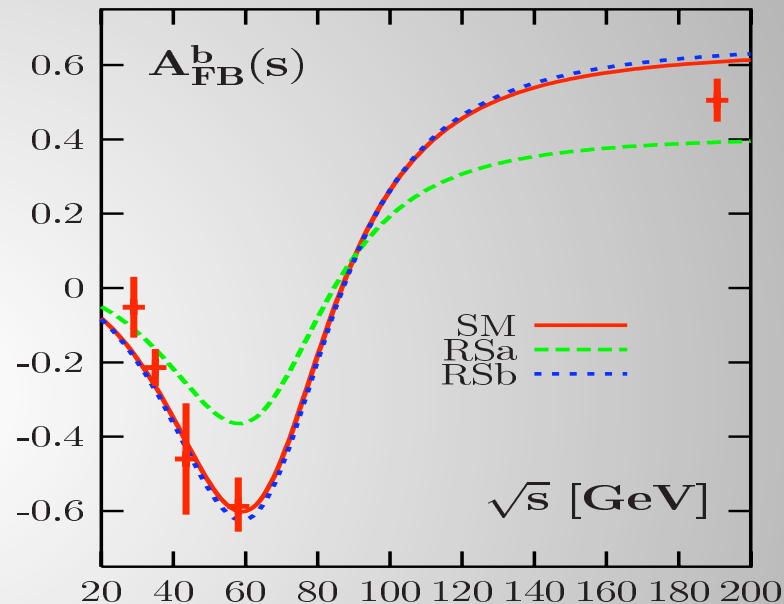
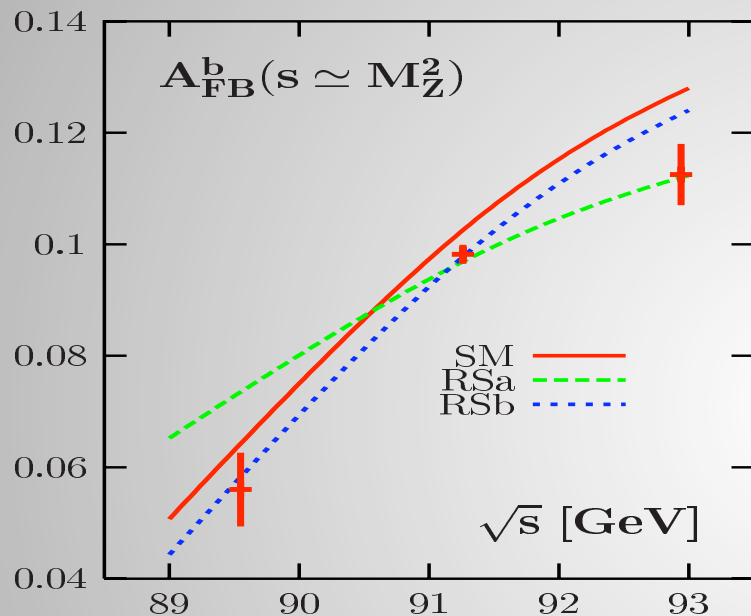


Figure 1: Normalized dijet angular distributions in several  $M_{jj}$  ranges, shifted vertically by the additive amounts given in parentheses in the figure for clarity. The data points include statistical and systematic uncertainties. The results are compared with the predictions of pQCD at NLO (solid histogram) and with the predictions including a contact interaction term of compositeness scale  $\Lambda = 5 \text{ TeV}$  (dashed histogram). The shaded band shows the effect on the NLO pQCD predictions due to  $\mu_r$  and  $\mu_f$  scale variations and PDF uncertainties, as well as the uncertainties from the non-perturbative corrections added in quadrature.



## Global $A_{\text{FB}}^b$ fit @ and off the Z pôle :



$\text{SM} : \chi^2 = 24 \quad \text{RSa} : \chi^2 = 20 \quad \text{RSb} : \chi^2 = 14$

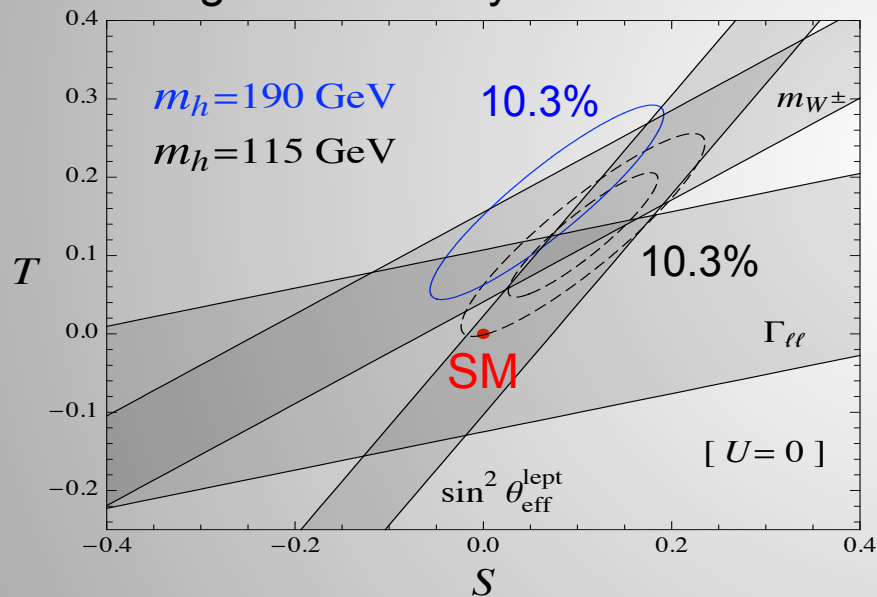
$b_R$  under  $SU(2)_L \times SU(2)_R \times U(1)_X$  :

$$\begin{cases} Q_X = (B-L)/2 \Rightarrow I_R^3 = -1/2 & \text{RSa} \\ Q_X = -5/6 \Rightarrow I_R^3 = +1/2 & \text{RSb} \end{cases}$$



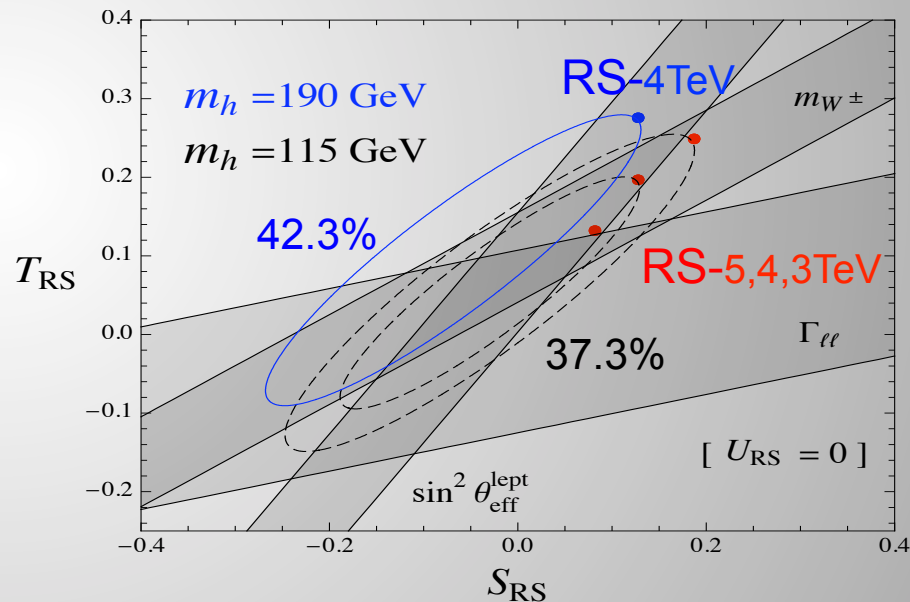
## Improved goodness-of-fit

EW observables are expressed  
in terms of oblique parameters  
encoding the New Physics...



$$\text{p-value } 10.3\% \Leftrightarrow \chi^2/11 = 1.56$$

$$S_{\text{RS}} \simeq 2\pi \left( \frac{2.4v}{M_{KK}} \right)^2 \quad T_{\text{RS}} \simeq k\pi^2 R_c \frac{\tilde{g}^2}{8e^2} \frac{\tilde{M}^2}{k^2} \left( \frac{2.4v}{M_{KK}} \right)^2$$

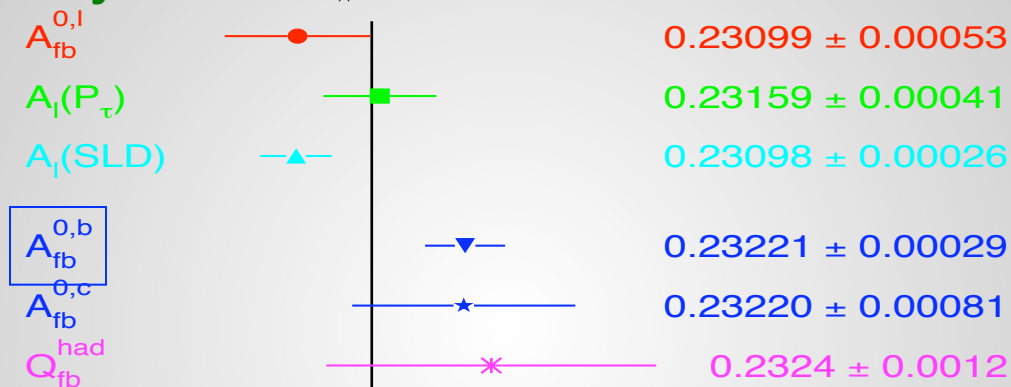


$$\text{p-value } 37.3\% \Leftrightarrow \chi^2/10 = 1.08$$

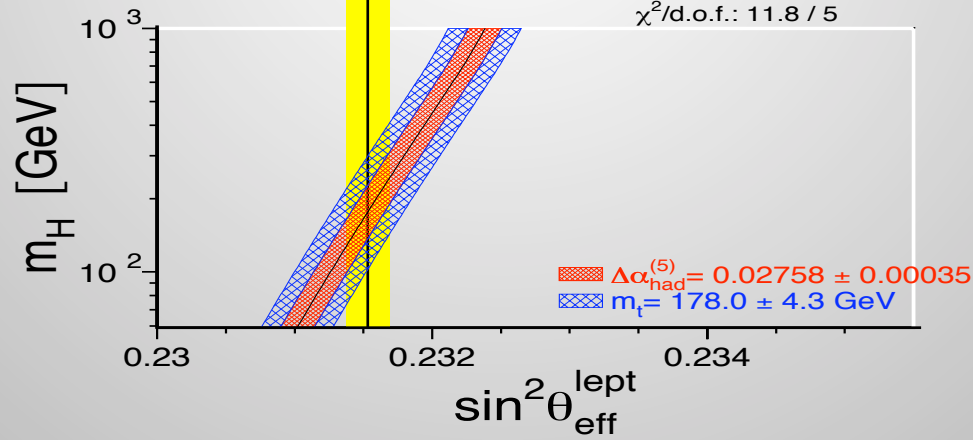
Better quality of fit in RS than in SM cause..

1) positive contribution  $T_{RS}$  (*custodial symmetry breaking*)

2) SM fit degraded by the  $\sin^2 \theta_w$  measurement derived *directly* from  $A_{FB}^b$  :



$\chi^2/\text{d.o.f.}: 11.8 / 5$



SM →

*AdS / CFT correspondance (98') :*

## WARPED H-DIM. SCENARIOS / STRONGLY COUPLED MODELS

<b>5D holographic version</b>	<b>RS with bulk fields</b>	<b>gauge-Higgs unification</b>	<b>Higgsless models</b>
<b>4D dual interpretation</b>	<b>composite Higgs boson</b>	<b>composite Higgs pseudo-Goldstone boson of a global symmetry</b>  <i>(as for little Higgs with <math>T</math> parity)</i>	<b>technicolor models</b>