

# Angular analysis of the decay $B_d \rightarrow K^* \mu^+ \mu^-$ at LHCb

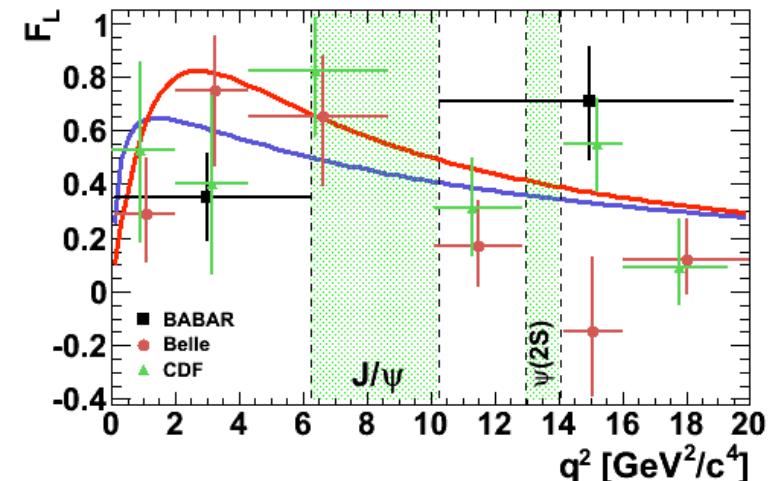
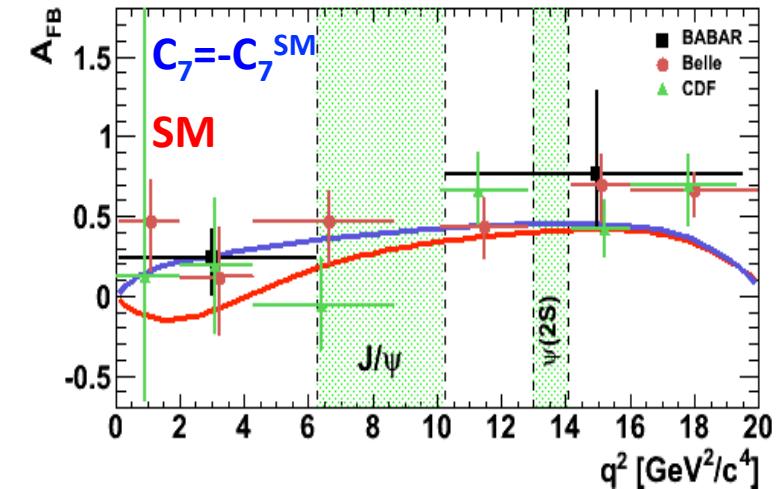
22<sup>nd</sup> July 2011

Mitesh Patel

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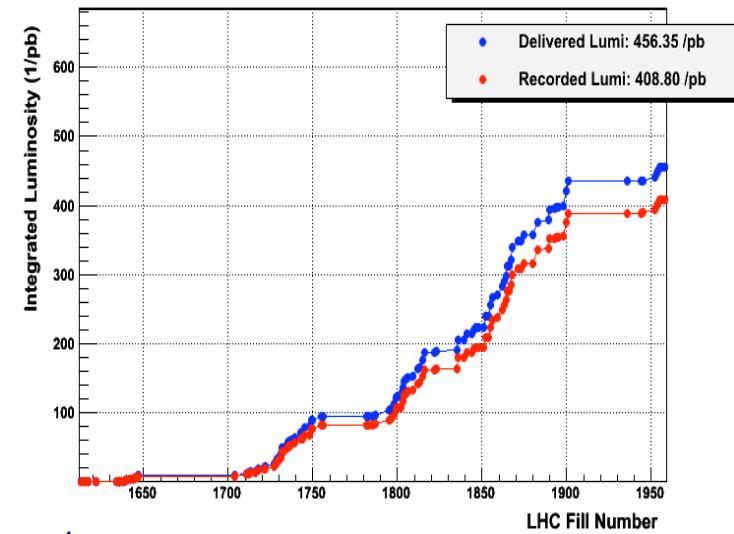
# Introduction

- Flavour changing neutral current decay ( $\rightarrow$ loop), described by 3 angles ( $\theta_l$ ,  $\phi$ ,  $\theta_K$ ) and di- $\mu$  invariant mass  $q^2$
- Sensitive to magnetic and vector and axial semi-leptonic penguin operators
- Many observables where hadronic uncertainties cancel
  - Forward-backward asymmetry  $A_{FB}$  of  $\theta_l$  distribution (zero-crossing point)
- Pre-EPS measurements from Babar, Belle and CDF



# Strategy

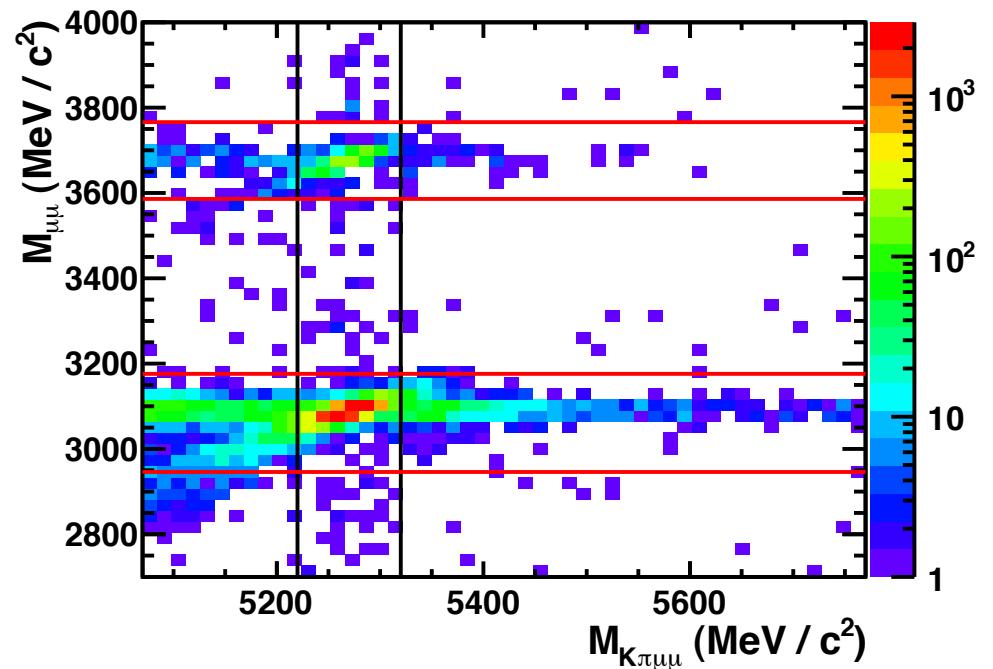
- Select signal events
- Correct for the effect of the reconstruction and selection requirements – “acceptance effect” – using simulation
  - Model independent correction
  - Validate by performing angular analysis of  $B_d \rightarrow K^* J/\psi$  control channel, where physics parameters known from elsewhere
  - Check simulation with a range of control channels
- Fit for observables



- First measurements from LHCb from  $309 \text{ pb}^{-1}$  data taken in 2011
- Focus on theoretically clean angular observables e.g.  $A_{FB}$ ,  $F_L$  and  $d\Gamma/dq^2$

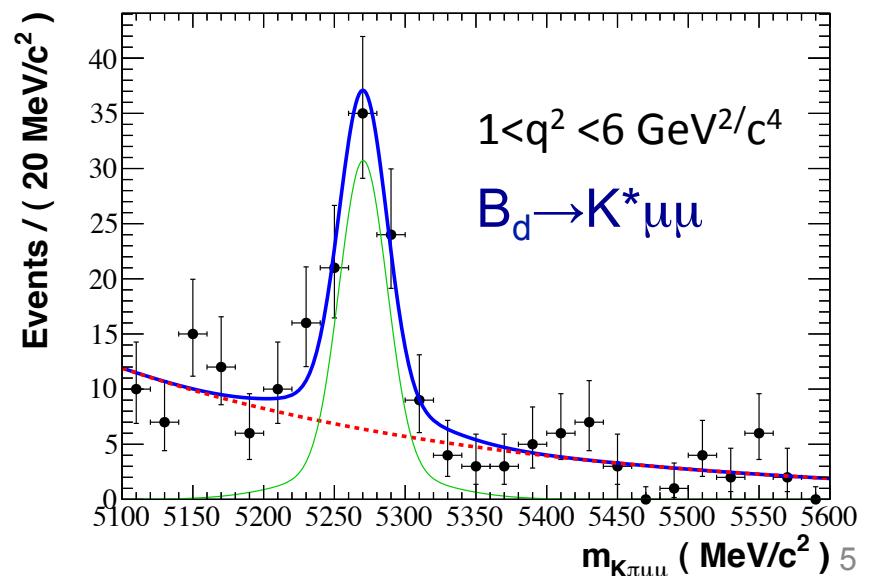
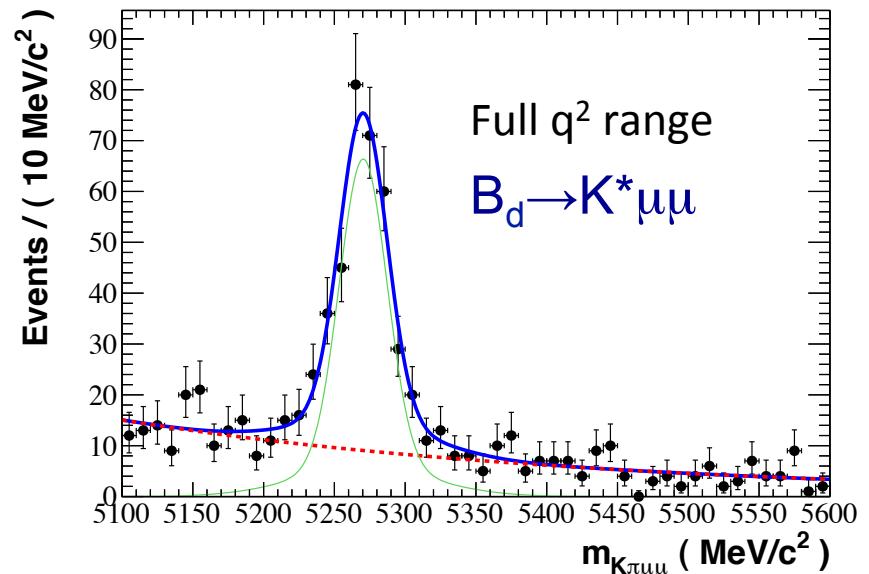
# Selection

- Selection:
  - Remove  $c\bar{c}$  resonances
    - $2946 < m_{\mu\mu} < 3176 \text{ MeV}/c^2$
    - $3586 < m_{\mu\mu} < 3776 \text{ MeV}/c^2$
  - Treat peaking backgrounds with a specific set of criteria ( $\rightarrow$  residual backgrounds  $\sim 3\%$  of signal)
  - Combinatorial backgrounds reduced with a Boosted Decision Tree (BDT) selection
- Use Belle  $q^2$  binning and an (overlapping)  $1 < q^2 < 6 \text{ GeV}^2/c^4$  bin favoured by theorists



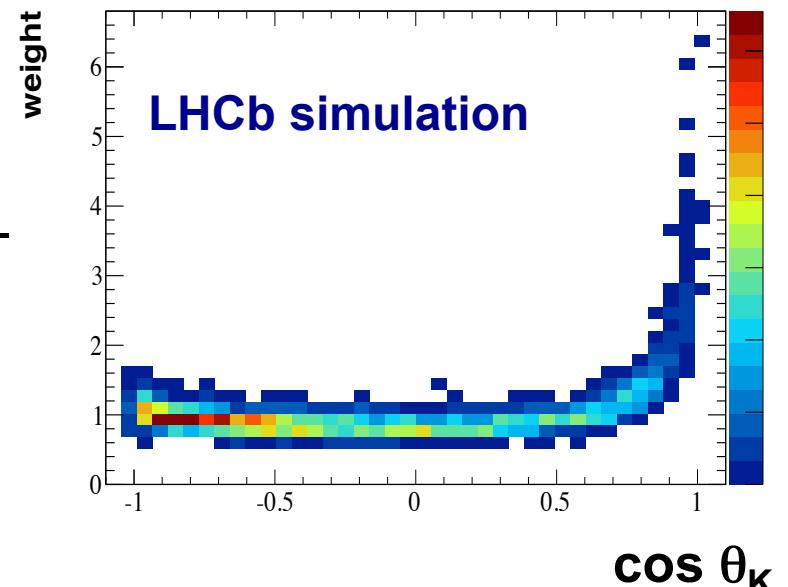
# Boosted Decision Tree

- Train BDT on 2010 data i.e. **totally independent** of 2011 data sample
  - Signal sample –  $B_d \rightarrow K^* J/\psi$  data
  - Bkgrd sample –  $B_d \rightarrow K^* \mu\mu$  mass sideband events
- Resulting selection
  - Background-to-signal ratio  $\sim 0.3$   
Comparable to B-factories
  - Does not induce further biases in  $\cos \theta_L$ ,  $\cos \theta_K$  and  $q^2$  cf reconstruction  
biases introduced are primarily from detector geometry – easy to model



# Acceptance Correction

- Correct angular and  $q^2$  distributions for the effect of the detector and selection
- To be model independent, use an event-by-event weight which is determined **on the basis of the  $\theta_L$ ,  $\theta_K$ ,  $q^2$  of the signal candidates that are found**
- Simulation quality verified with range of control channels ( $B_d \rightarrow K^* J/\psi$ ,  $J/\psi \rightarrow \mu\mu$ ,  $D^* \rightarrow D^0(K\pi)\pi$ )
  - Tracking efficiency
  - Hadron (mis-)identification probabilities
  - Muon (mis-)identification
  - Overall momentum and  $\eta$  distributions

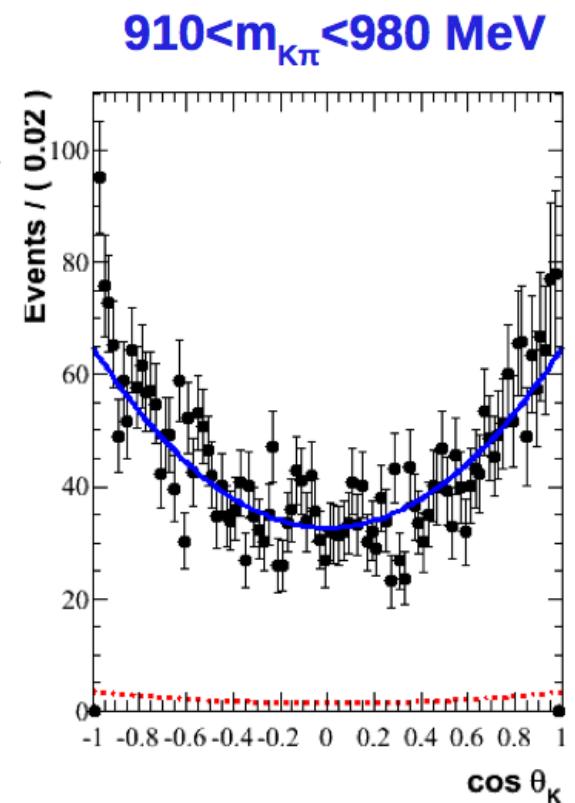


Weight depends on  $\cos \theta_K$

Vast majority of events have weights  $\sim 1$

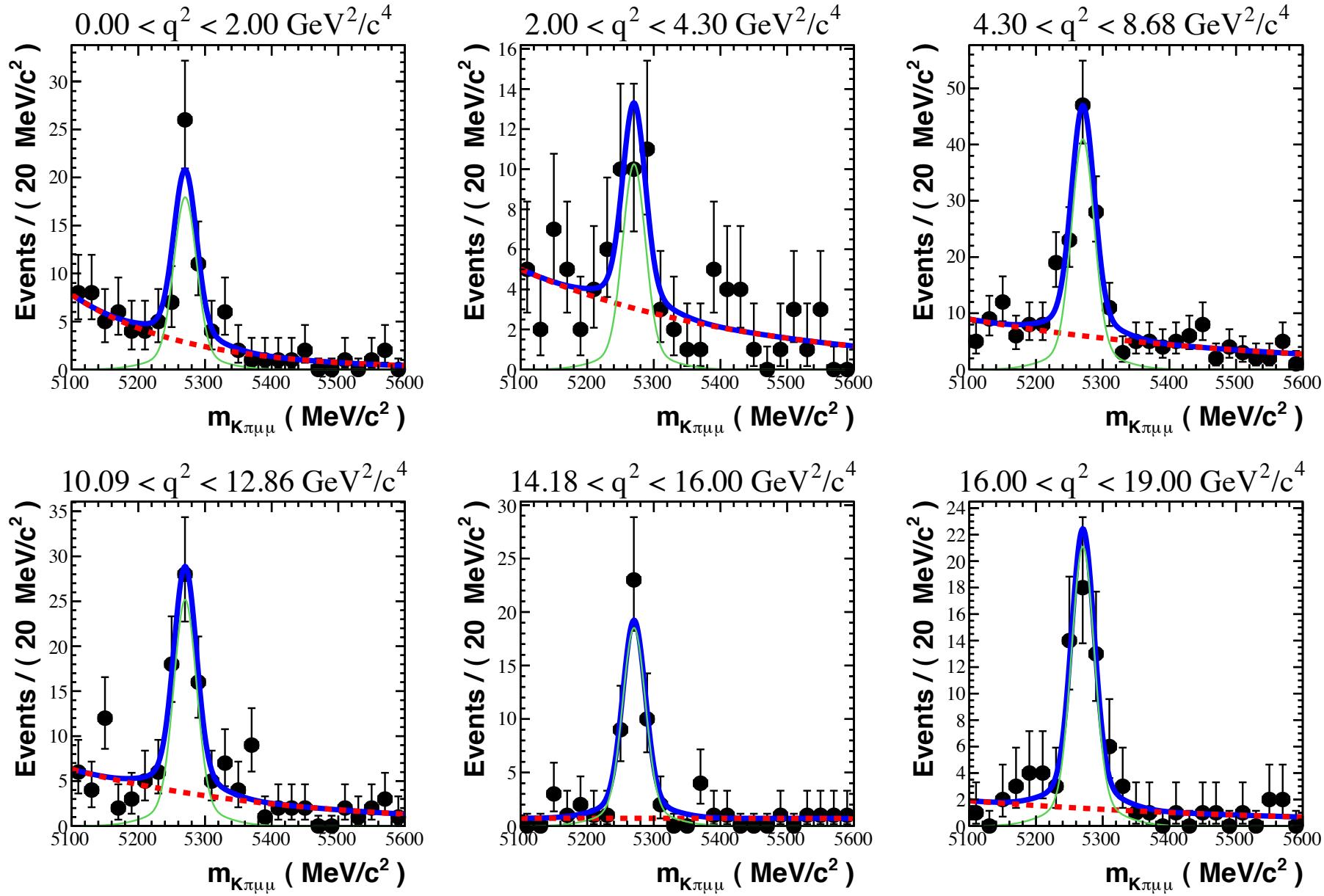
# Fit Procedure and Validation

- Simultaneous fit to the 1d projections of  $\cos \theta_L$ ,  $\cos \theta_K$  and  $m_{K\pi\mu\mu}$  in bins of  $q^2$ 
  - Events weighted according to acceptance correction
  - Use Bayesian approach to construct stat. errors with flat prior over physical region
  - Systematics effects are very small and can be reduced with further data
  - Cross-check with a simple counting approach (don't use angular distributions)
- Validate fitting on  $B_d \rightarrow K^* J/\psi$ 
  - $A_{FB}$  consistent with zero, as expected
  - s-wave contribution induces an asymmetry in  $\cos \theta_K$  distribution,  $A_{FB}^{K}$
  - Acceptance correction makes  $\cos \theta_K$  asymmetric → symmetric
  - Variation of  $A_{FB}^{K}$  with  $m_{K\pi}$  matches BaBar data(\*\*) across  $m_{K\pi}$  range

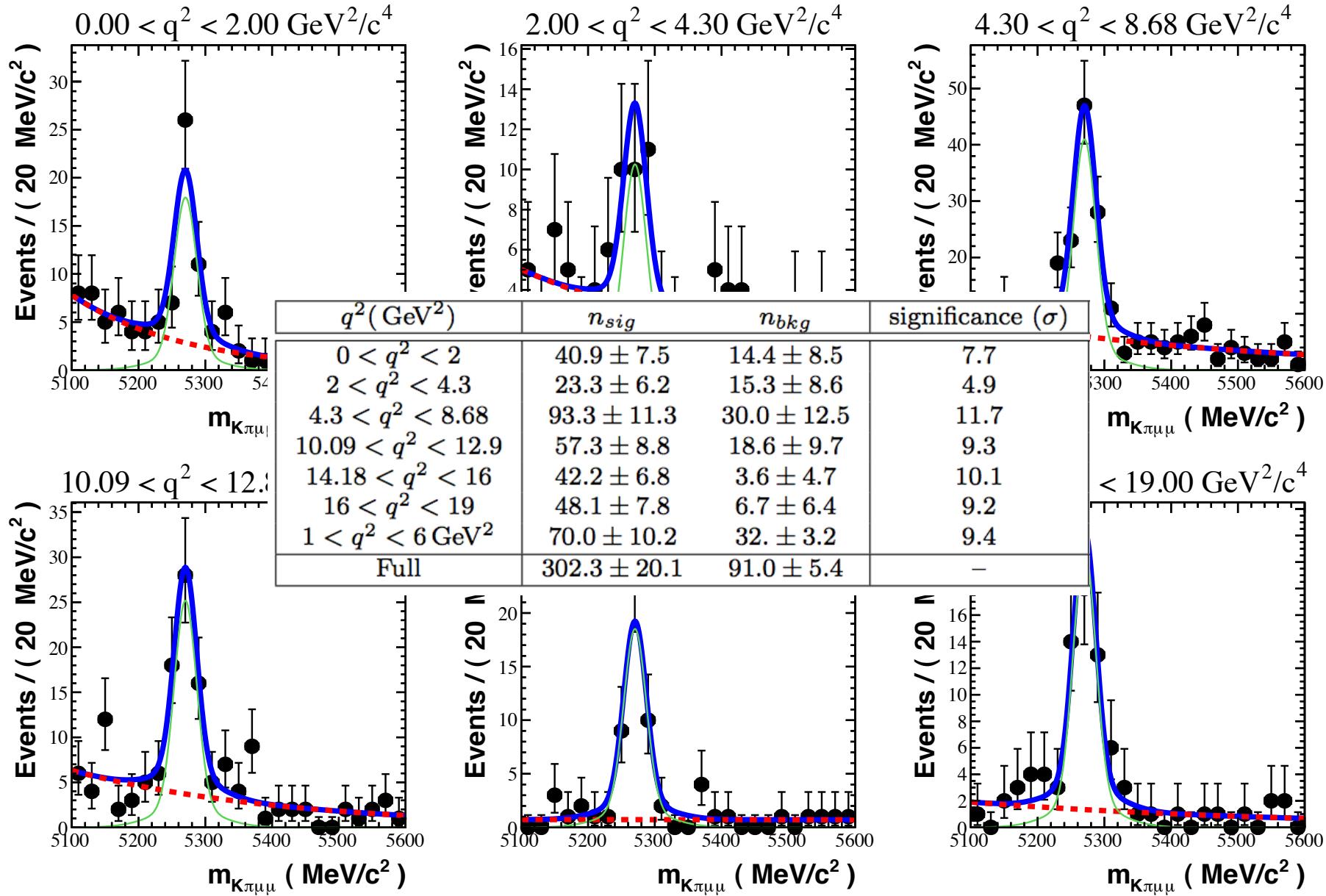


(\*\*) BABAR: PRD 76, 031102 (2007)

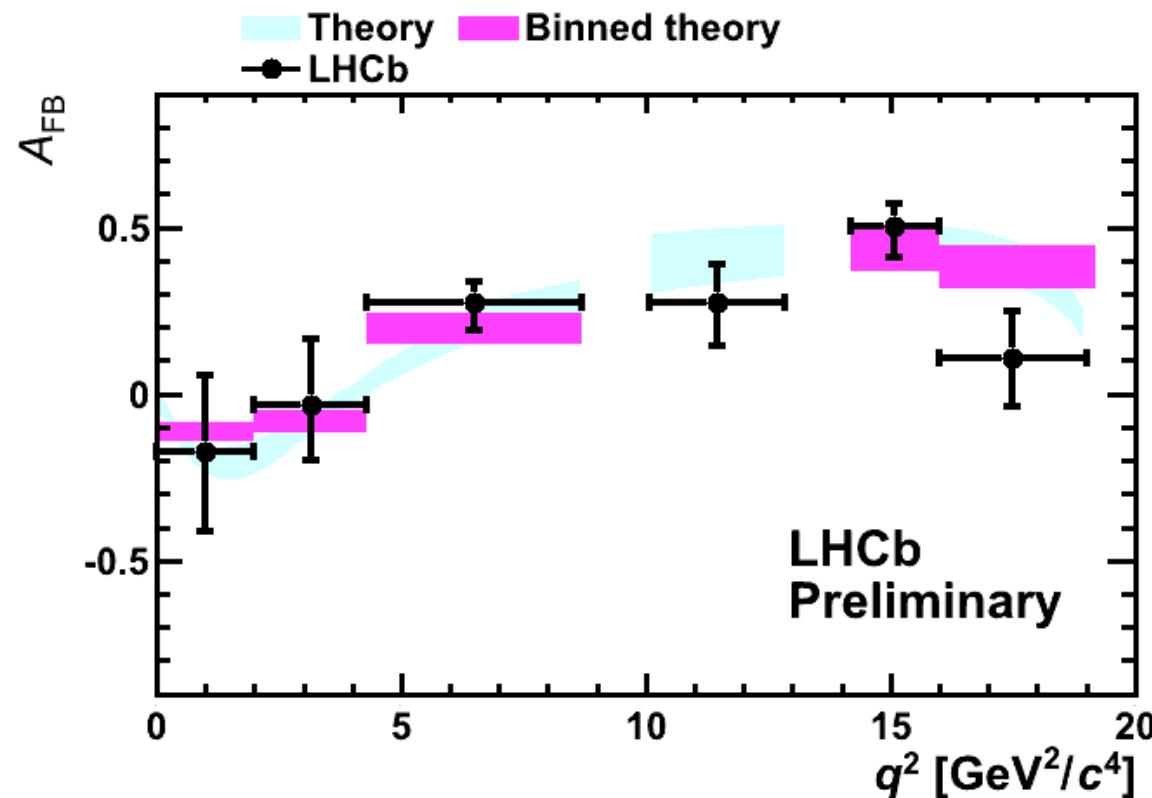
# $B_d \rightarrow K^* \mu\mu$ yields



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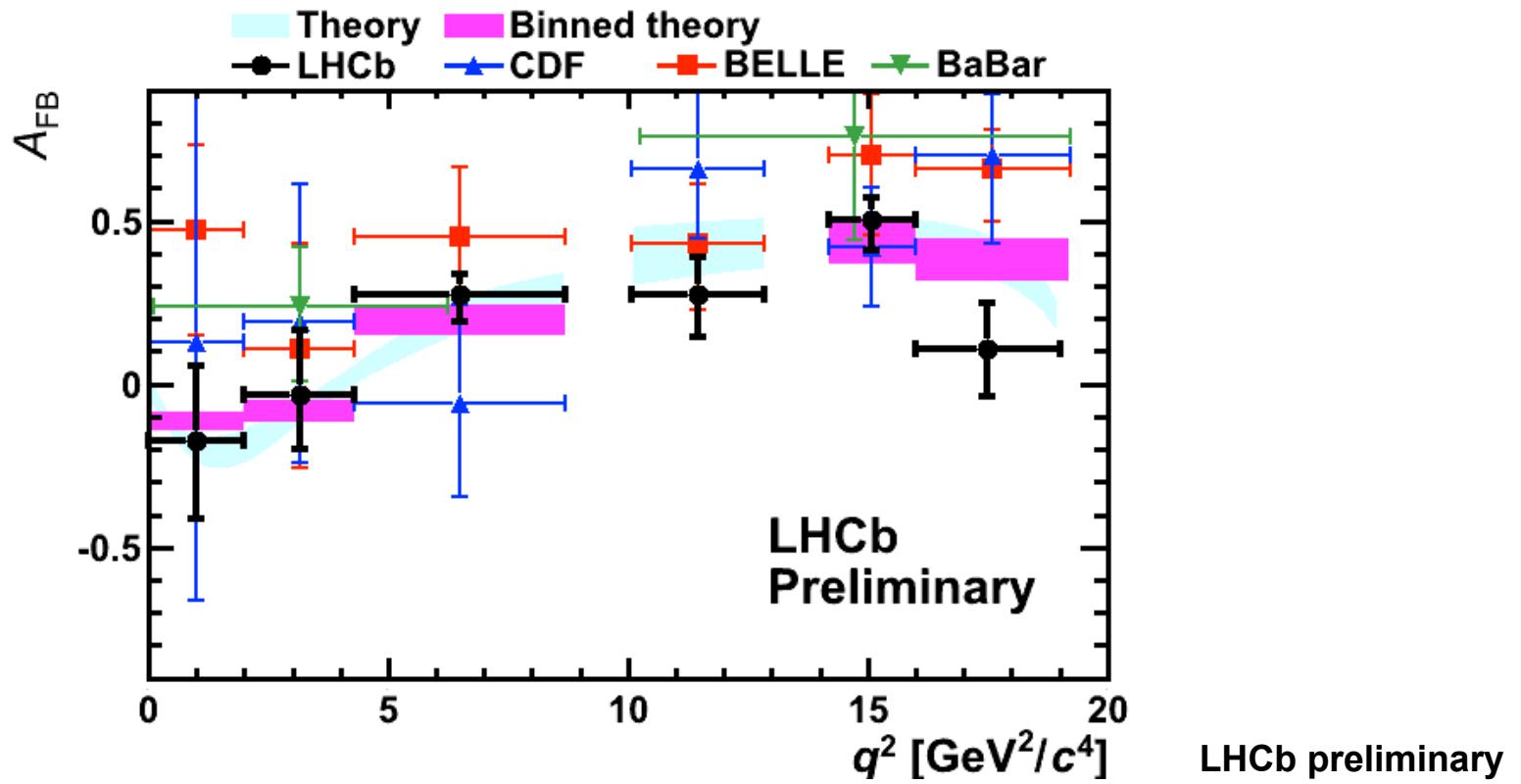


# $A_{FB}$ Measurement



Theory predictions from C.Bobeth *et al.*,  
arXiv:1105.0376v2

# $A_{FB}$ Measurement

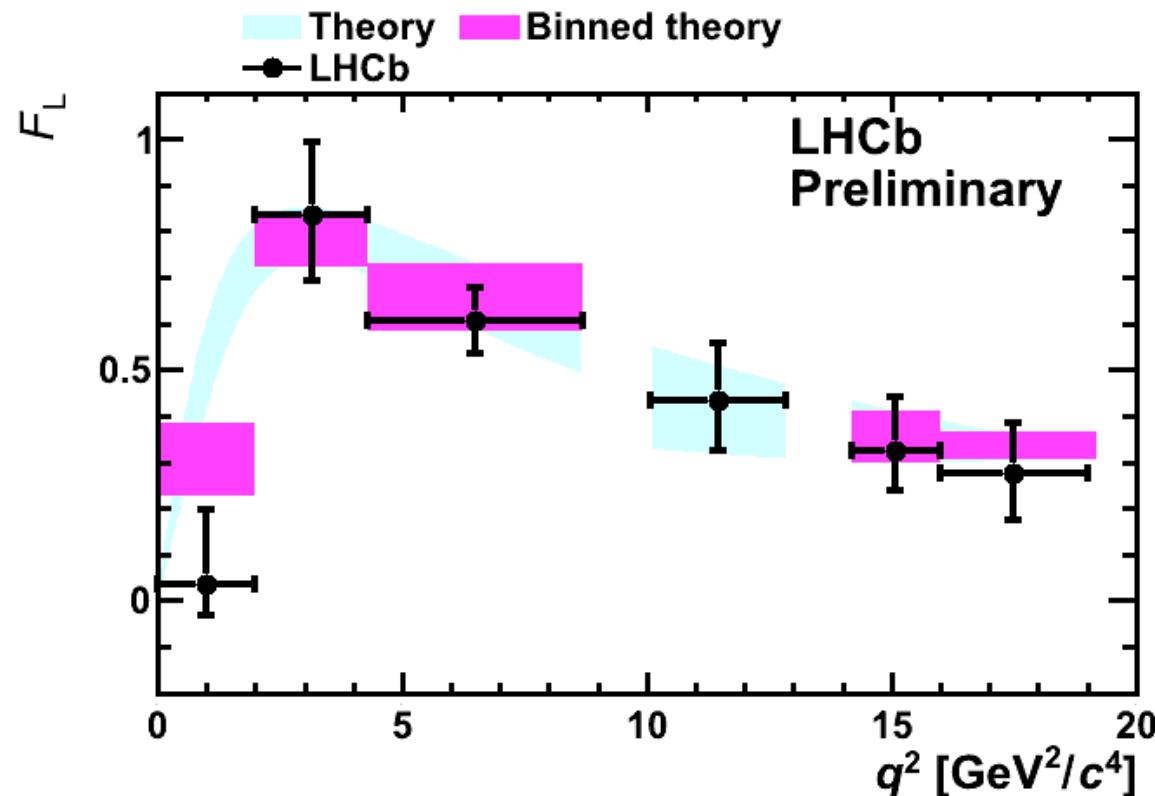


- In  $1 < q^2 < 6 \text{ GeV}^2/\text{c}^4$  bin,
  - $A_{FB} = -0.10 \pm 0.14 \pm 0.05$
  - c.f. Belle  $0.26^{+0.27}_{-0.30} \pm 0.07$

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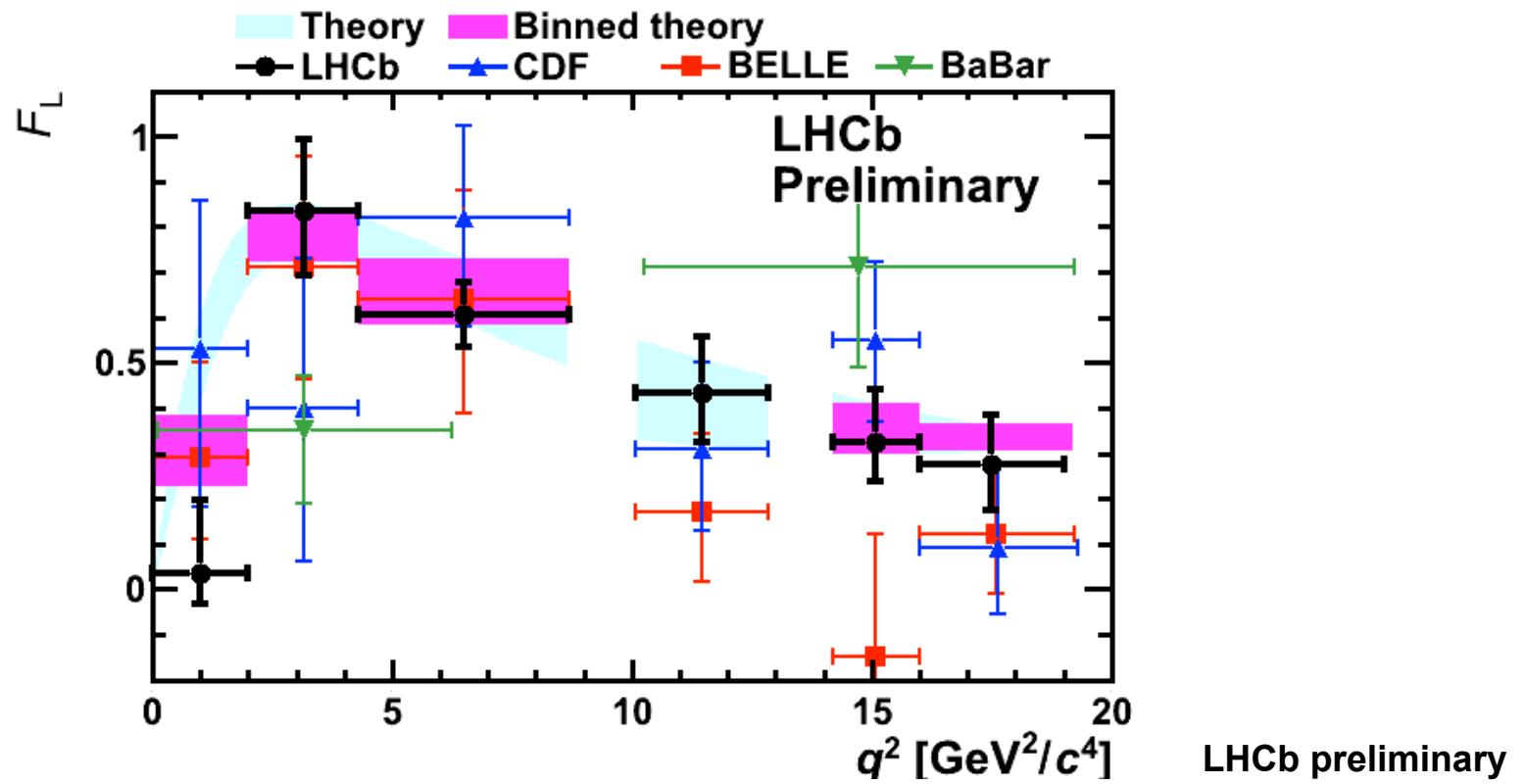
$q^2 (\text{GeV}^2)$	$A_{FB}$	$F_L$	$d\Gamma/dq^2$
$0 < q^2 < 2$	$-0.17^{+0.22}_{-0.23} \pm 0.06$	$0.03^{+0.15}_{-0.03} \pm 0.06$	$0.56 \pm 0.11 \pm 0.03$
$2 < q^2 < 4.3$	$-0.04^{+0.19}_{-0.15} \pm 0.06$	$0.84^{+0.15}_{-0.13} \pm 0.06$	$0.28 \pm 0.08 \pm 0.02$
$4.3 < q^2 < 8.68$	$0.28^{+0.06}_{-0.08} \pm 0.02$	$0.60^{+0.07}_{-0.07} \pm 0.01$	$0.55 \pm 0.07 \pm 0.03$
$10.09 < q^2 < 12.9$	$0.27^{+0.11}_{-0.13} \pm 0.03$	$0.44^{+0.12}_{-0.11} \pm 0.02$	$0.53 \pm 0.09 \pm 0.03$
$14.18 < q^2 < 16$	$0.50^{+0.06}_{-0.09} \pm 0.03$	$0.33^{+0.11}_{-0.08} \pm 0.04$	$0.59 \pm 0.10 \pm 0.03$
$16 < q^2 < 19$	$0.10^{+0.13}_{-0.13} \pm 0.06$	$0.28^{+0.10}_{-0.09} \pm 0.04$	$0.48 \pm 0.08 \pm 0.03$
$1 < q^2 < 6$	$-0.10^{+0.14}_{-0.14} \pm 0.05$	$0.57^{+0.11}_{-0.10} \pm 0.03$	$0.39 \pm 0.06 \pm 0.02$

# $F_L$ Measurement



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# $F_L$ Measurement

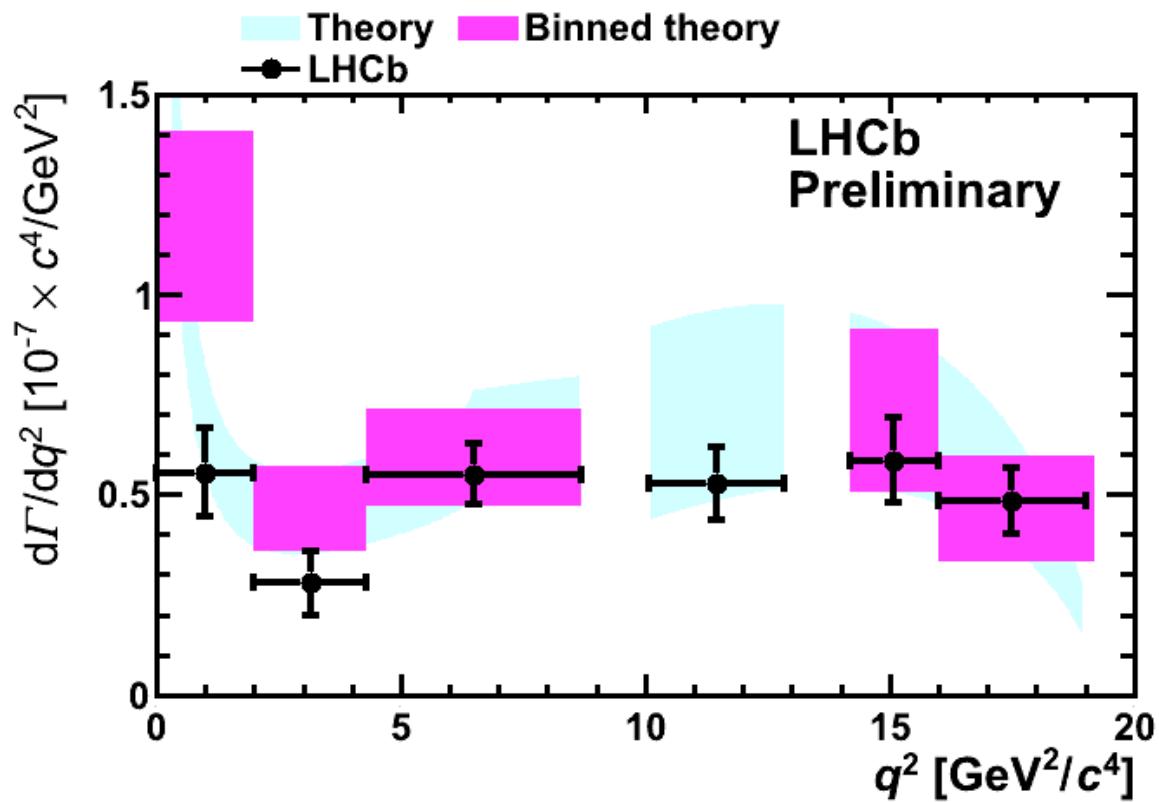


- In  $1 < q^2 < 6$  GeV $^2/c^4$  bin,
  - $F_L = 0.57^{+0.11}_{-0.10} \pm 0.03$
  - c.f. Belle  $0.67 \pm 0.23 \pm 0.07$

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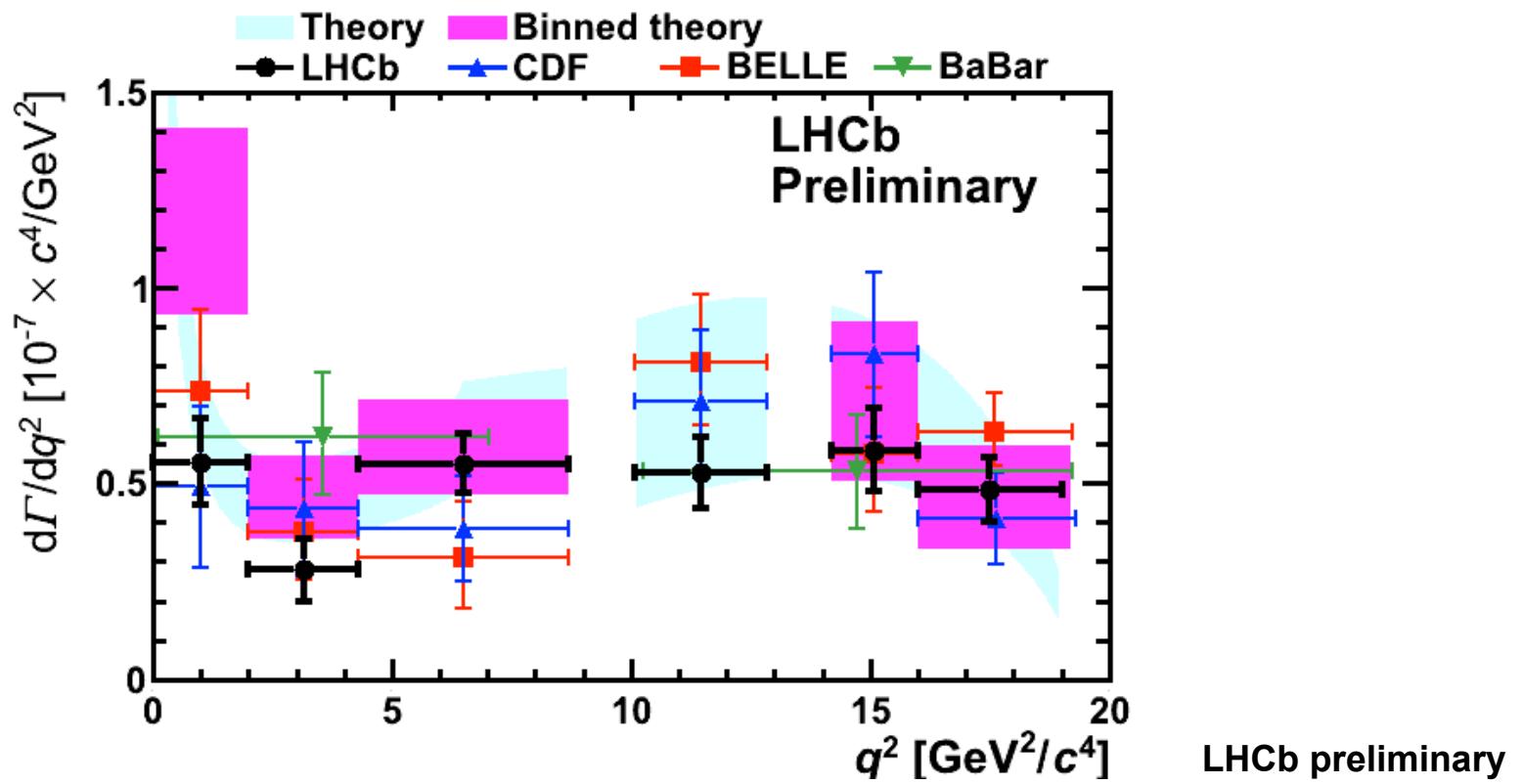
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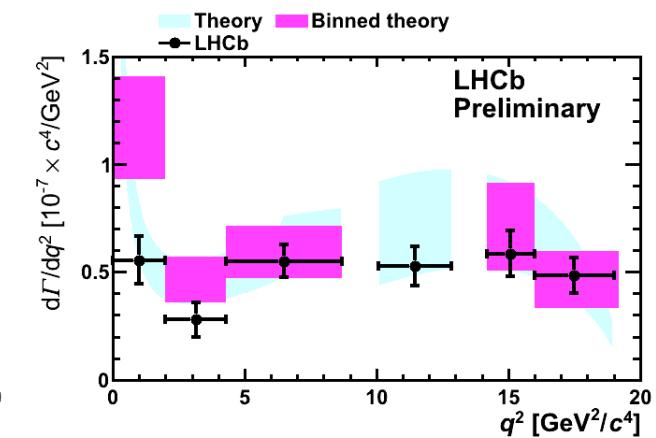
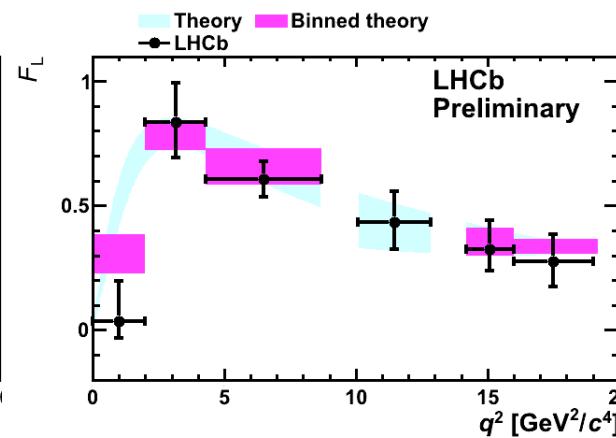
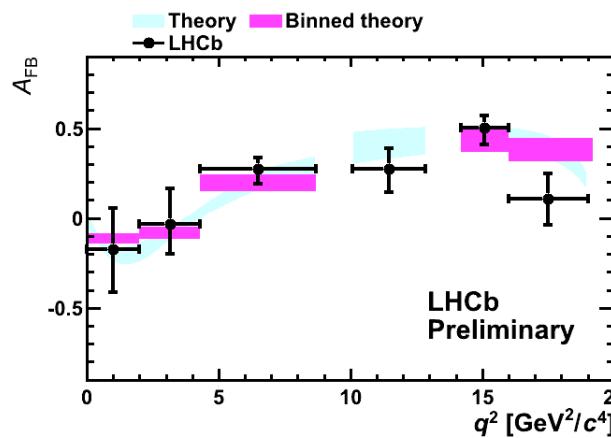


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# Conclusions

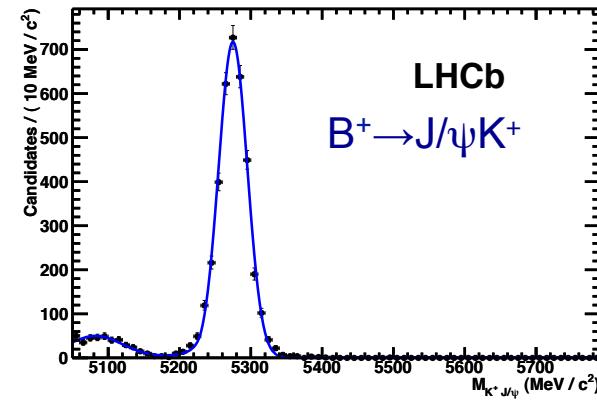
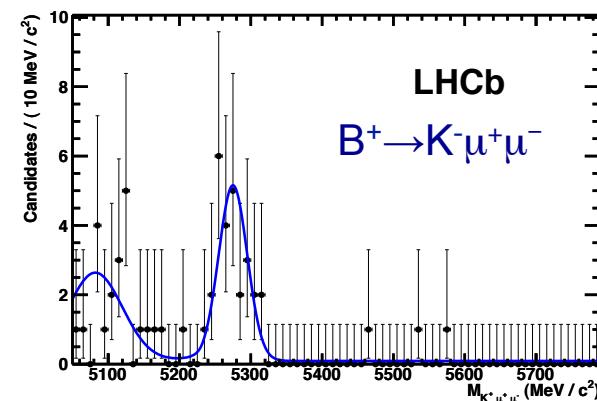
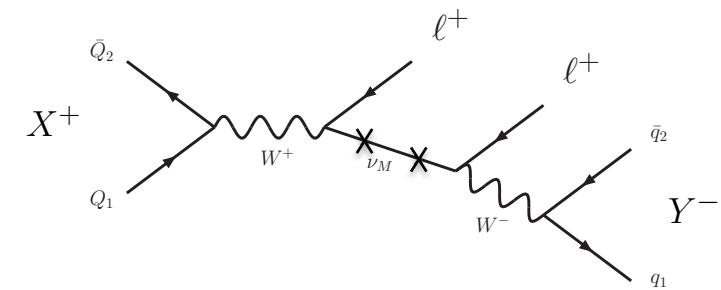
- Angular analysis of  $B_d \rightarrow K^* \mu^+ \mu^-$ 
  - $A_{FB}$ ,  $F_L$  and  $d\Gamma/dq^2$  measured as function of  $q^2$  with  $309\text{pb}^{-1}$  of LHCb data taken in 2011
  - All three measurements show good agreement with the SM, no evidence for a large asymmetry in the low  $q^2$  region as hinted at by previous experiments
  - Errors smaller than previous measurements and are statistically dominated



# Backup

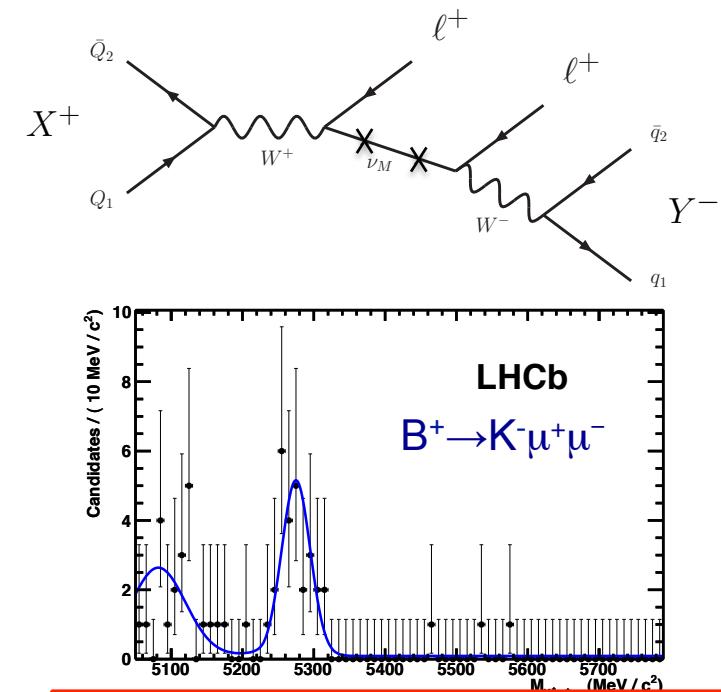
# Search for $B^+ \rightarrow \pi^- \mu^+ \mu^+$ and $B^+ \rightarrow K^- \mu^+ \mu^+$

- Lepton Flavour Violating decays
  - ( $\Delta L=2$ ) strictly forbidden in SM
  - Sterile Majorana  $\nu$  of mass  $O(1\text{GeV}/c^2)$  could enhance BR significantly
- Analysis Strategy
  - Tight selection, use ‘opposite sign’  $B^+ \rightarrow K^- \mu^+ \mu^-$  decays as a proxy for signal
  - Normalise to  $B^+ \rightarrow J/\psi K^+$
  - Detector performance measured from control channels used to estimate peaking bkgrd
- Observed signal / background
  - <0.3 (0.1) bkgrd evts expected in  $\pi \mu \mu$  ( $K \mu \mu$ )
  - **Zero events observed in both signal and mass sideband regions**



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Observed limit @ 90% CL  
 $\text{BR}(B^+ \rightarrow K^- \mu^+ \mu^+) < 4.3 \times 10^{-8}$   
 $\text{BR}(B^+ \rightarrow \pi^- \mu^+ \mu^+) < 4.5 \times 10^{-8}$

Factor 40(30) improvement  
cf previous best limit (CLEO)

- Search for  $B^+ \rightarrow \pi^- \mu^+ \mu^+$ ,  $B^+ \rightarrow K^- \mu^+ \mu^+$ 
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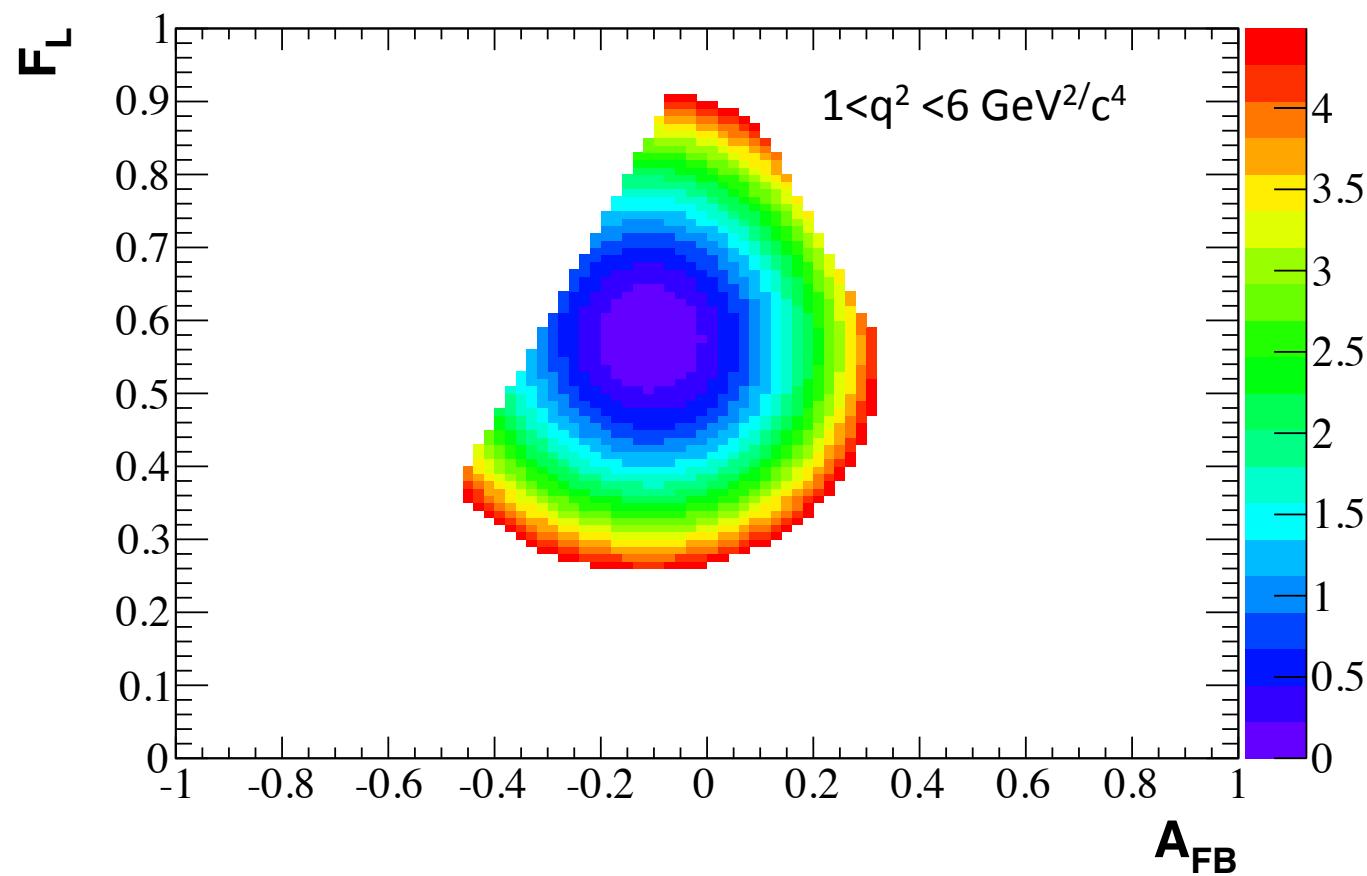
# Peaking Backgrounds

- A number of vetos are introduced to deal with peaking bkgrds e.g.
  - $B_s \rightarrow \phi \mu^+ \mu^-$  with  $K \rightarrow \pi$
  - $B_d \rightarrow K^* J/\psi$  with  $\pi(K) \rightarrow \mu$  and  $\mu \rightarrow \pi(K)$  swaps [evades  $J/\psi$  vetos]
  - $B_d \rightarrow K^* \mu^+ \mu^-$  with  $K \rightarrow \pi$  and  $\pi \rightarrow K$Completely negligible impact on signal
- Residual background (after application of BDT selection also) :

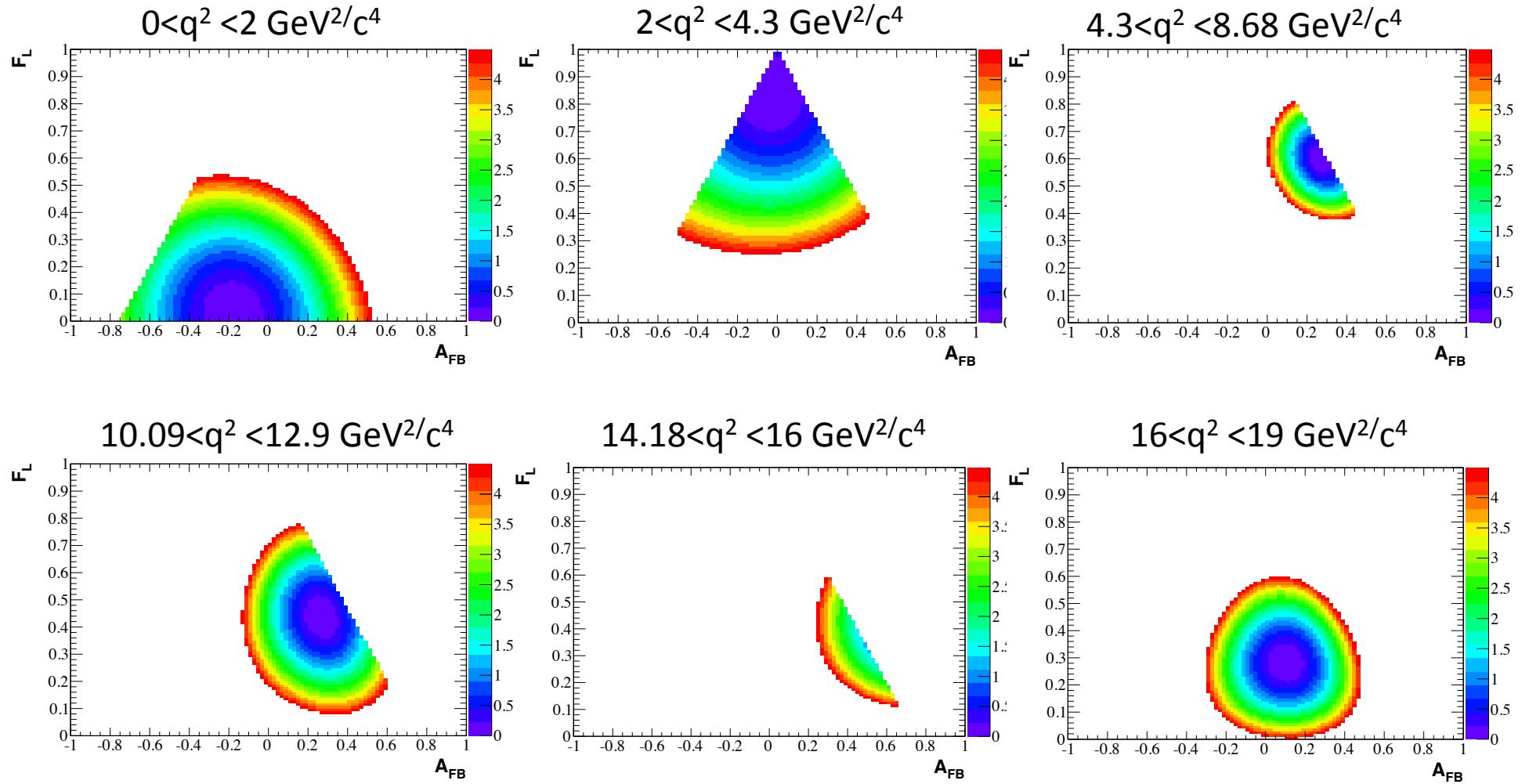
Source	Quantity	Signal Loss (%)
$B_s \rightarrow \phi \mu^+ \mu^-$	2.3	0.1
$B^0 \rightarrow K^{*0} J/\psi$	0.7	0.1
$B^0 \rightarrow K^{*0} \mu^+ \mu^-$	1.2	0.3
Total	4.2	0.5

→ residual background is ~3% of signal – only ~0.7% of this can affect asymmetry -  $B_d \rightarrow K^* \mu^+ \mu^-$  background flips B and B

# Likelihoods



# Likelihoods



# Errors and Physical Region

- Angular equations → pdf negative if  $A_{FB} < 3/4(1-F_L)$
- Statistical errors
  - Use Bayesian approach to construct errors with flat prior over physical region
    - The central value quoted is that with the largest likelihood
    - Errors estimated by performing a profile-likelihood scan over the plane and integrating a 68% CL region of the likelihood distribution
- Systematics effects are small and can be reduced with further data

