

EPS HEP 2011

ϕ_2 and ϕ_3 Measurements at Belle

Jeremy Dalseno



Max-Planck-Institut für Physik

Excellence Cluster Universe

jdalseno [at] mpp.mpg.de

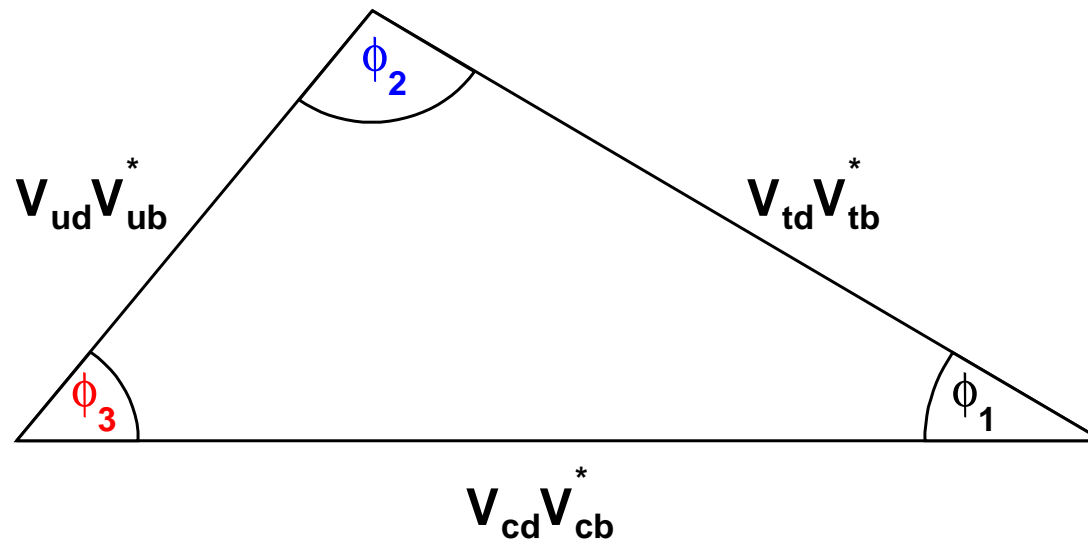
21 July 2011



MAX-PLANCK-GESELLSCHAFT

Outline

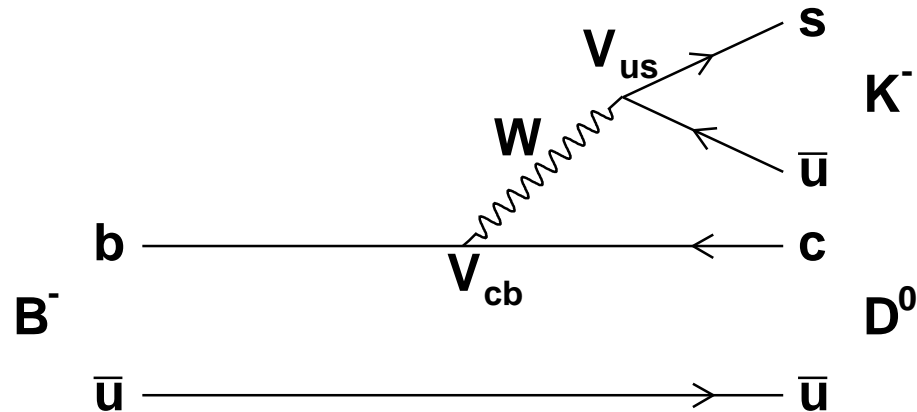
1. $B^- \rightarrow DK^-, D \rightarrow K^+ \pi^-$
2. $B^- \rightarrow DK^-, D \rightarrow K_S^0 \pi^+ \pi^-$
3. $B^0 \rightarrow \pi^+ \pi^-$
4. $B^0 \rightarrow \rho^0 \rho^0$
5. $B^0 \rightarrow a_1(1260)^\pm \pi^\mp$



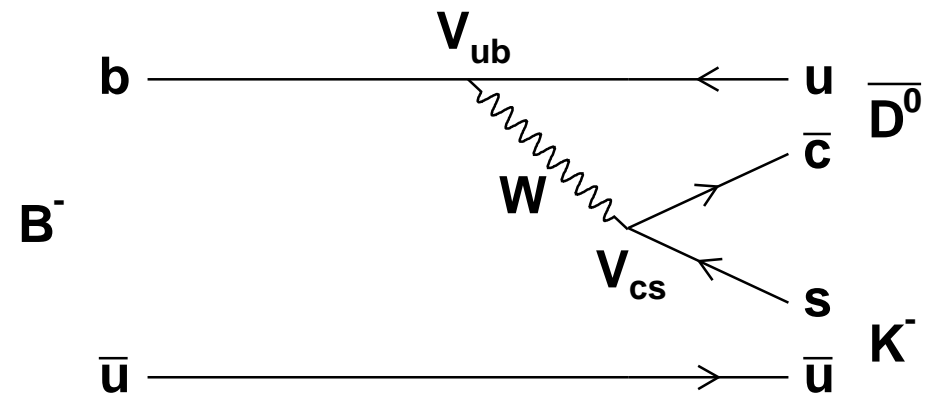
ϕ_3 from B decays

Measure ϕ_3 from interference between 2 diagrams

$$A \propto \lambda^3$$



$$A \propto \lambda^3(\rho - i\eta)$$



where $D \equiv D^0$ or \bar{D}^0 decays to the same final state, $|D\rangle = |D^0\rangle + r_B e^{i\theta} |\bar{D}^0\rangle$

Phase difference, $\theta = \delta_B \pm \phi_3$ for B^\pm

$$\text{Amplitude ratio, } r_B = \frac{A(B^- \rightarrow \bar{D}^0 K^-)}{A(B^- \rightarrow D^0 K^-)}$$

Same order in λ but receives $\mathcal{O}(0.1)$ from colour suppression

$$B^- \rightarrow D_{\text{Sup}} [K^+ \pi^-] K^-$$

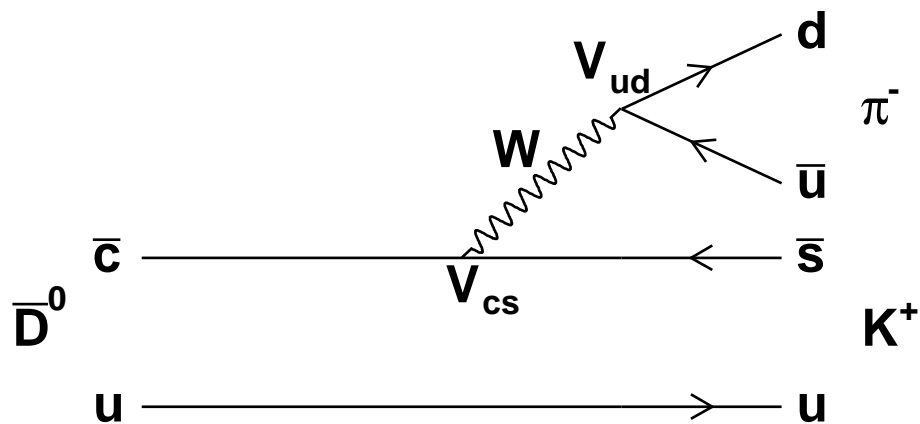
ADS method

D. Atwood, I. Dunietz, and A. Soni, Phys. Rev. Lett. **78**, 3257 (1997); Phys. Rev. D **63**, 036005 (2001)

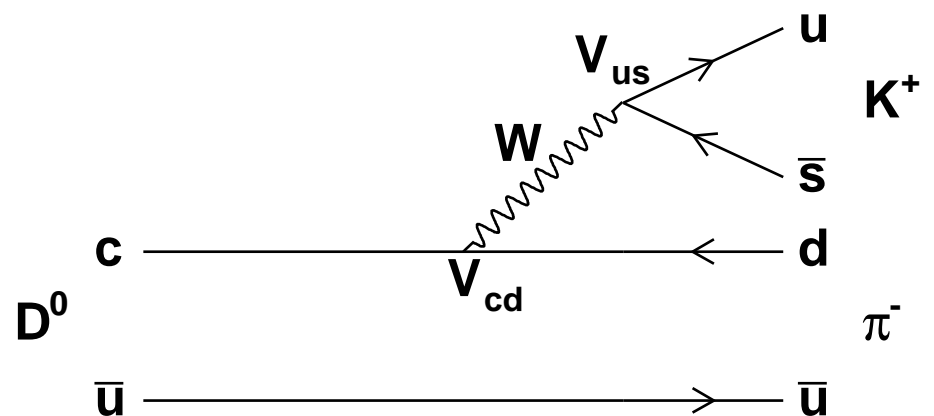
D decays to Cabibbo-favoured and doubly Cabibbo-suppressed same final state

Most promising channel is $D \rightarrow K^+ \pi^-$

Favoured



Suppressed



$$B^- \rightarrow D_{\text{Sup}}[K^+\pi^-]K^-$$

Compare rates of $B^- \rightarrow D_{\text{Fav}}[K^-\pi^+]K^-$ with $B^- \rightarrow D_{\text{Sup}}[K^+\pi^-]K^-$

Measure

$$\mathcal{R}_{DK} \equiv \frac{\mathcal{B}([K^+\pi^-]K^-) + \mathcal{B}([K^-\pi^+]K^+)}{\mathcal{B}([K^-\pi^+]K^-) + \mathcal{B}([K^+\pi^-]K^+)}$$

$$\mathcal{A}_{DK} \equiv \frac{\mathcal{B}([K^+\pi^-]K^-) - \mathcal{B}([K^-\pi^+]K^+)}{\mathcal{B}([K^+\pi^-]K^-) + \mathcal{B}([K^-\pi^+]K^+)}$$

Related to ϕ_3 as

$$\mathcal{R}_{DK} = r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos \phi_3$$

$$\mathcal{A}_{DK} = \frac{2r_B r_D \sin(\delta_B + \delta_D) \sin \phi_3}{\mathcal{R}_{DK}}$$

Amplitude ratio: $r_D = \frac{A(D^0 \rightarrow K^+\pi^-)}{A(\bar{D}^0 \rightarrow K^+\pi^-)}$

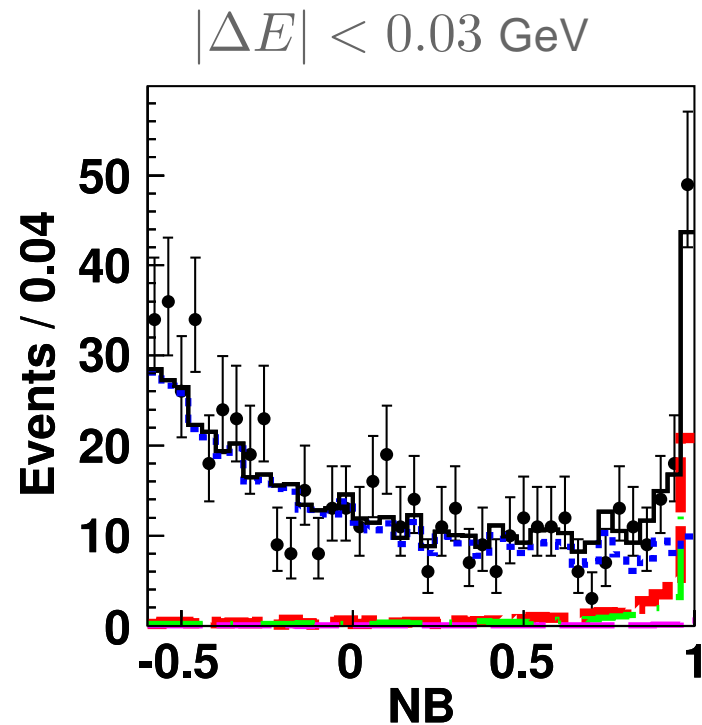
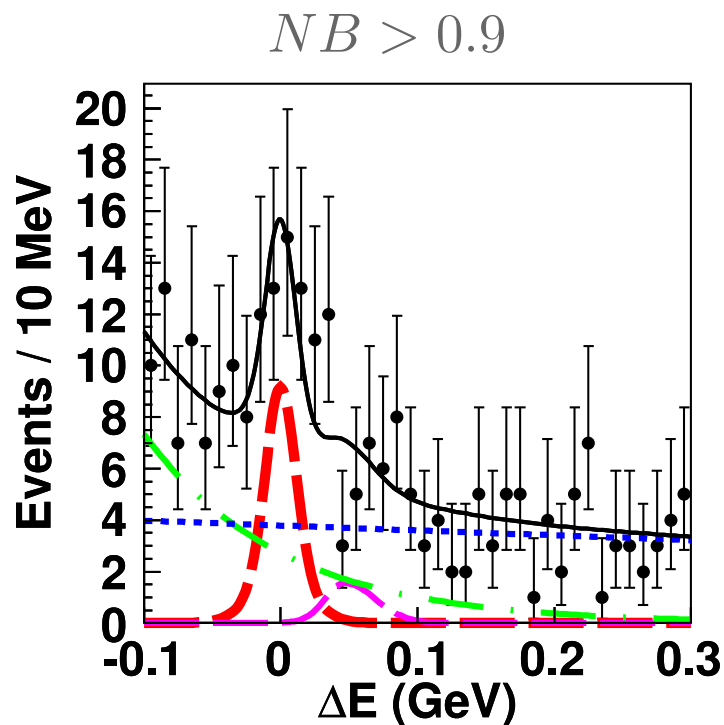
Strong phase difference, δ_D

$B^- \rightarrow D_{\text{Sup}}[K^+\pi^-]K^-$ Yield

Final data set from Belle, 772 million $B\bar{B}$ pairs

Difficulty in separating small signal from dominant continuum background

Fit ΔE and neural network output (NB) based on event shape



First evidence: 4.1σ significance for suppressed $B^- \rightarrow D_{\text{Sup}}[K^+\pi^-]K^-$

$B^- \rightarrow D_{\text{Sup}}[K^+\pi^-]K^-$ Results

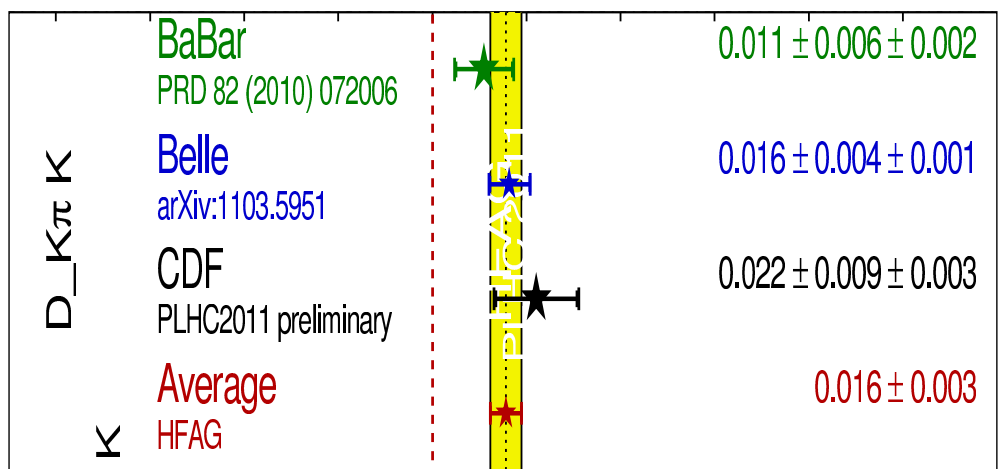
$$\mathcal{R}_{DK} = [1.63_{-0.41}^{+0.44} (\text{stat})_{-0.13}^{+0.07} (\text{syst})] \times 10^{-2}$$

$$\mathcal{A}_{DK} = -0.39_{-0.28}^{+0.26} (\text{stat})_{-0.03}^{+0.04} (\text{syst})$$

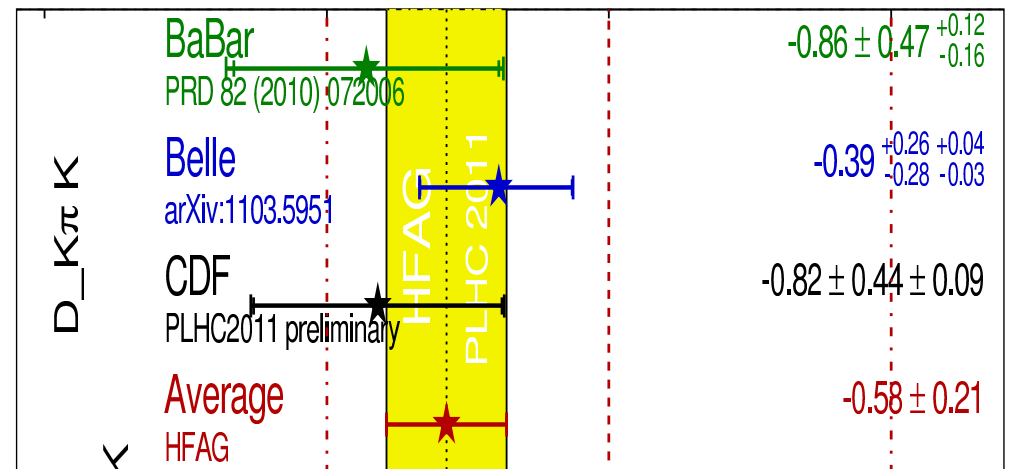
Most precise measurement to date

First evidence for $B^- \rightarrow D_{\text{Sup}}[K^+\pi^-]K^-$

\mathcal{R}_{ADS} Averages **HFAG** PLHC 2011 PRELIMINARY



\mathcal{A}_{ADS} Averages **HFAG** PLHC 2011 PRELIMINARY



$$B^- \rightarrow DK^-, D \rightarrow K_S^0 \pi^+ \pi^-$$

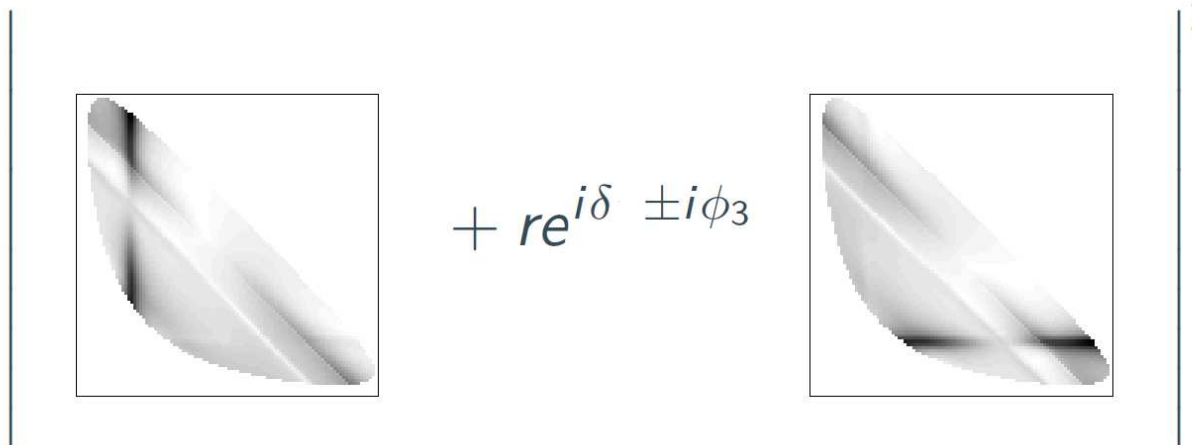
GGSZ method

A. Giri, Yu. Grossman, A. Soffer, J. Zupan, Phys. Rev. D **68**, 054018 (2003)

A. Bondar, Proceedings of BINP Special Analysis Meeting on Dalitz Analysis, 24-26 Sep. 2002, unpublished.

Fit $D \rightarrow K_S^0 \pi^+ \pi^-$ Dalitz plot and directly determine ϕ_3

$$|\mathcal{M}_\pm(m_+^2, m_-^2)|^2 = |f_D(m_+^2, m_-^2) + r_B e^{i(\delta_B \pm \phi_3)} f_D(m_-^2, m_+^2)|^2$$

$$= \left| \left[\text{Dalitz Plot 1} \right] + r e^{i\delta \pm i\phi_3} \left[\text{Dalitz Plot 2} \right] \right|^2$$


Parametrise amplitude as coherent sum of 2-body decays via intermediate resonances

Measure $|f_D|^2$

$$B^- \rightarrow D^{(*)} K^-, D \rightarrow K_S^0 \pi^+ \pi^-$$

Previous Belle measurement

657 million $B\bar{B}$ pairs

Combined results of $B^- \rightarrow DK^-$ and $D^* K^-$, $D^* \rightarrow D\pi^0$, $D\gamma$

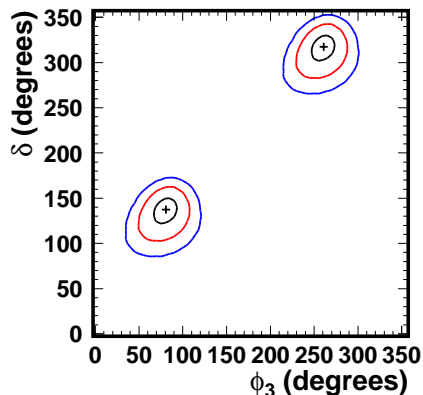
A. Poluektov *et al.* (Belle Collab.), Phys. Rev. D **81**, 112002 (2010)

$$\phi_3 = (78_{-12}^{+11} \text{ (stat)} \pm 4 \text{ (syst)} \pm 9 \text{ (model)})^\circ$$

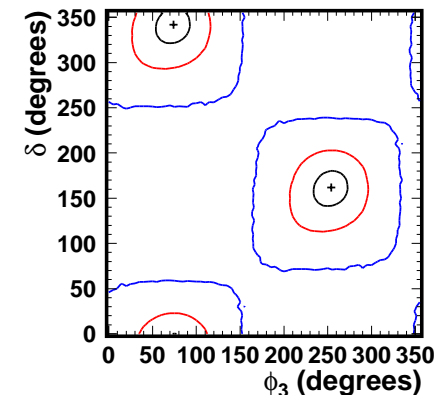
Parametrisation of amplitude $f_D \rightsquigarrow$ model dependence as dominant systematic uncertainty

Would dominate the total uncertainty at LHCb and the next generation B factories

$$B^- \rightarrow DK^-$$



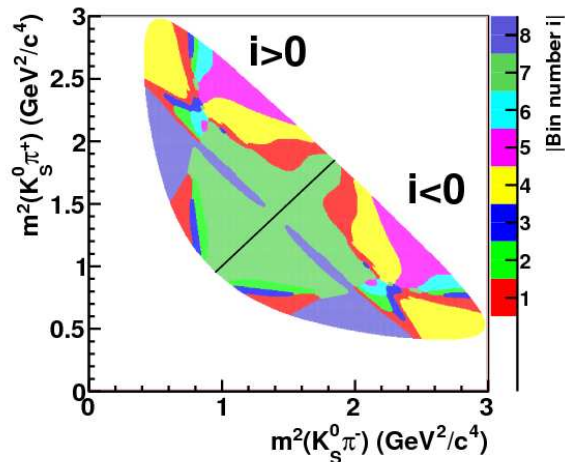
$$B^- \rightarrow D^* K^-$$



Binned Dalitz Plot Method

Use binned Dalitz plot and work with numbers of events in each bin

A. Bondar and A. Poluektov, Eur. Phys. J. C **47**, 347 (2006); Eur. Phys. J. C **55**, 51 (2008).



And compare in a χ^2 fit with

$$N_i^\pm = h_B [K_i + r_B^2 K_{-i} + 2\sqrt{K_i K_{-i}} (x_\pm c_i + y_\pm s_i)]$$

$$x_\pm = r_B \cos(\delta_B \pm \phi_3), y_\pm = r_B \sin(\delta_B \pm \phi_3)$$

N_i^\pm : Expected number of $B^\pm \rightarrow DK^\pm$ events in bin i

K_i : Number of events in bin i determined from a flavour-tagged sample ($D^{*\pm} \rightarrow D\pi^\pm$)

c_i, s_i : related to average strong phase difference in bin i

$$c_i = \langle \cos \Delta\delta_D \rangle_i, s_i = \langle \sin \Delta\delta_D \rangle_i$$

Measured by CLEO, can also be measured at BES-III

Optimal Binning and CLEO Input

Binned analysis reduces statistical precision of ϕ_3 compared to measuring $|f_D|^2$

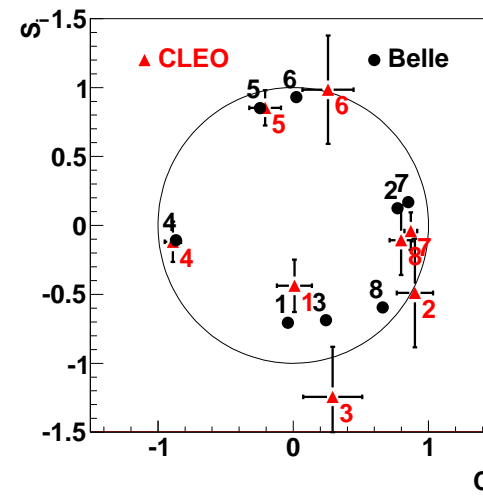
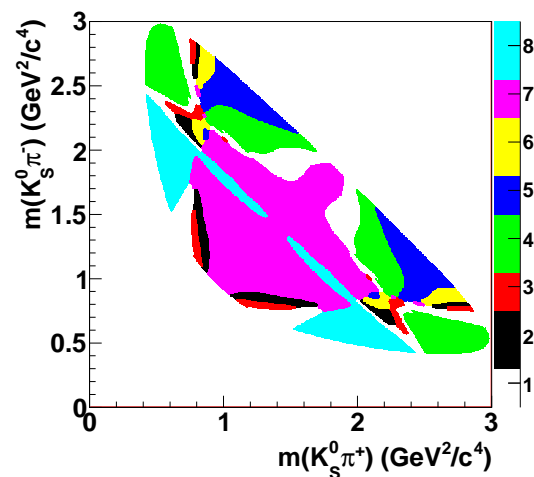
Precision also depends strongly on amplitude behaviour across the bins

Phase difference between D^0 and \bar{D}^0 amplitudes varying as little as possible \Rightarrow better precision

Optimal binning depends on model, ϕ_3 does not

Optimised binning using BaBar 2008 amplitude

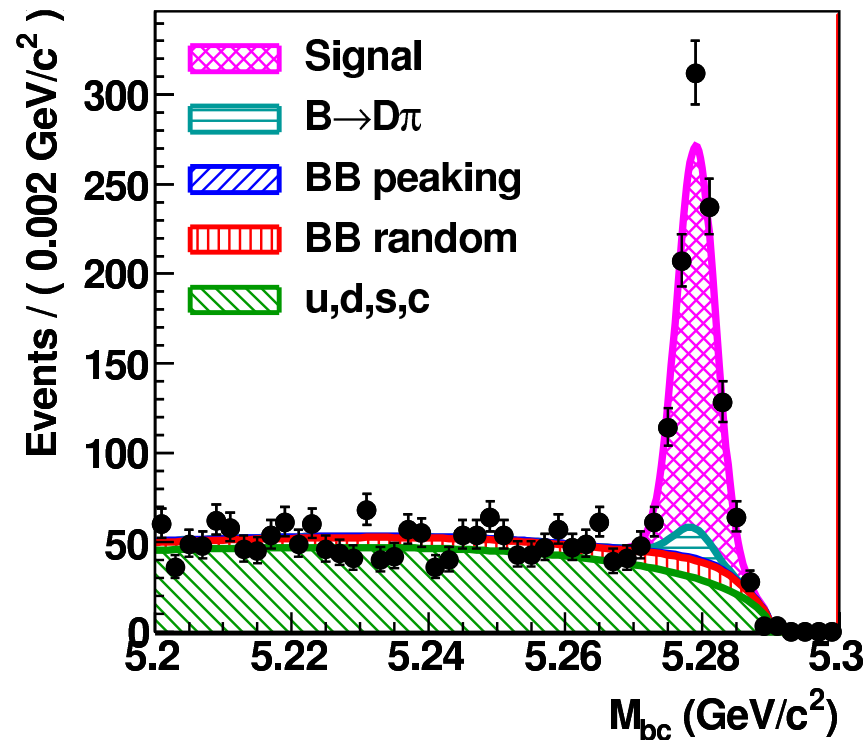
J. Libby *et al.* (CLEO Collab.), Phys. Rev. D **82**, 112006 (2010)



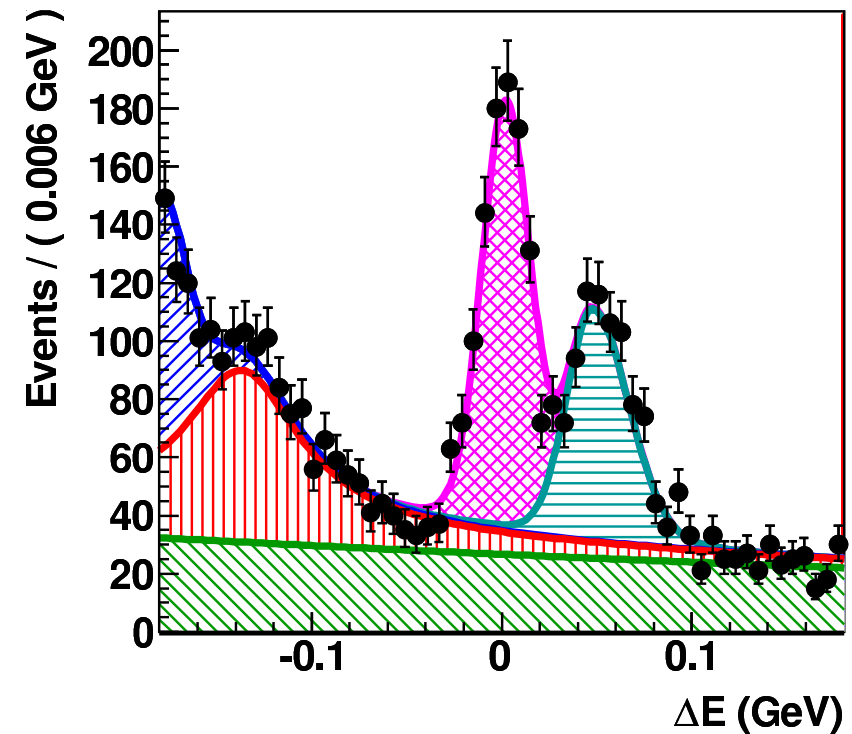
$B^- \rightarrow D[K_S^0 \pi^+ \pi^-] K^-$ Signal Yield

Final data set from Belle, 772 million $B\bar{B}$ pairs

$\cos\theta_{\text{thr}} < 0.8, |\Delta E| < 0.03 \text{ GeV}$



$\cos\theta_{\text{thr}} < 0.8, M_{bc} > 5.27 \text{ GeV}/c^2$



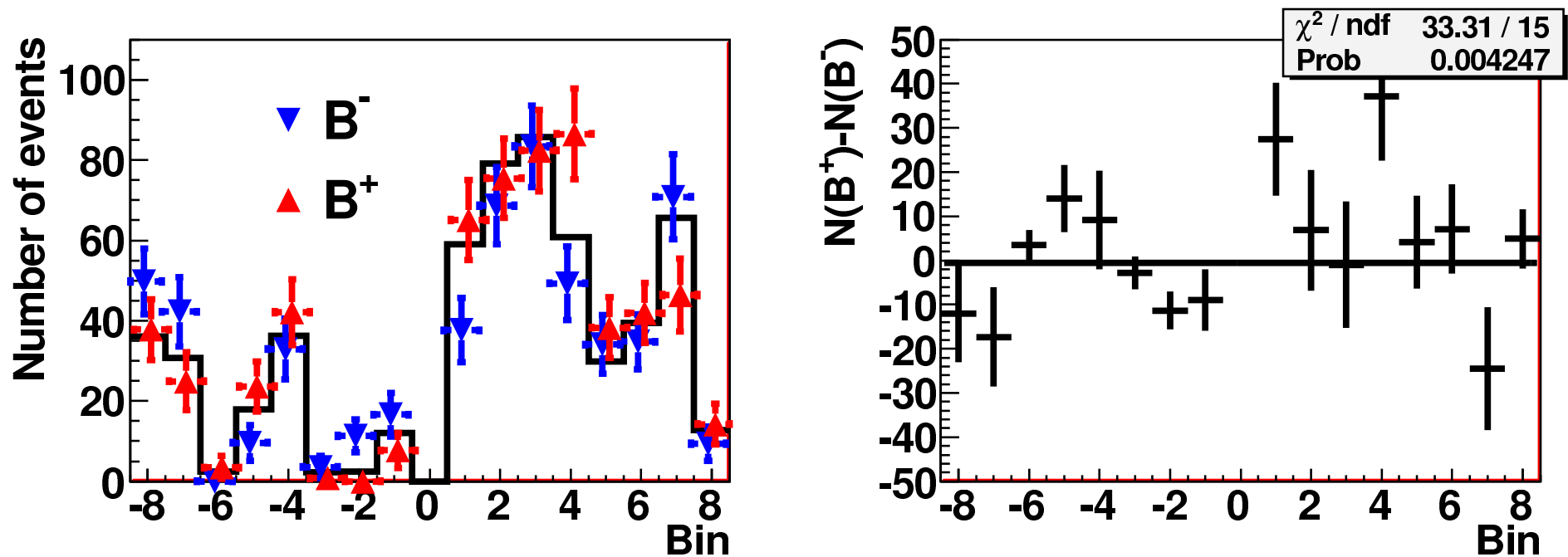
Signal yield: 1176 ± 43 events

$B^- \rightarrow D[K_S^0 \pi^+ \pi^-] K^-$ Asymmetry

Now determine signal yield in optimised Dalitz plot bins

Perform χ^2 fit to compare with expected signal yield determined from

$$N_i^\pm = h_B [K_i + r_B^2 K_{-i} + 2\sqrt{K_i K_{-i}}(x_\pm c_i + y_\pm s_i)]$$

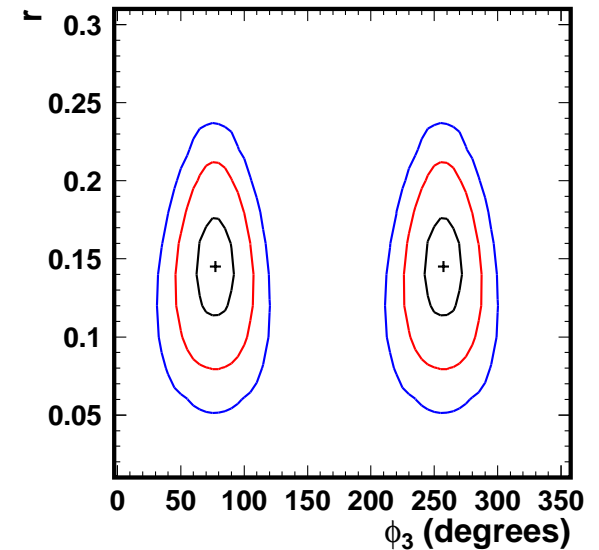
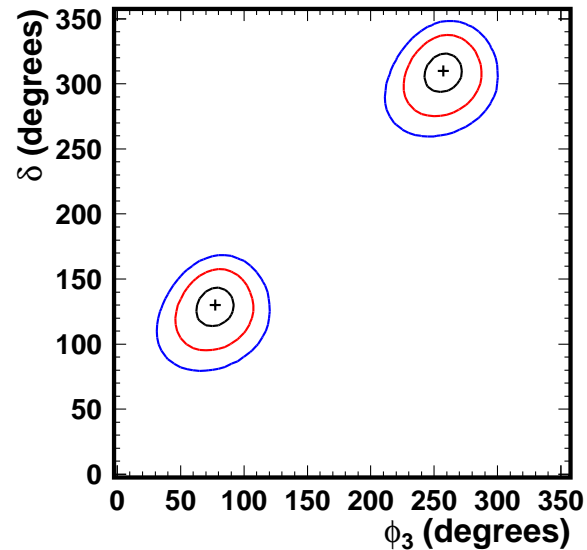
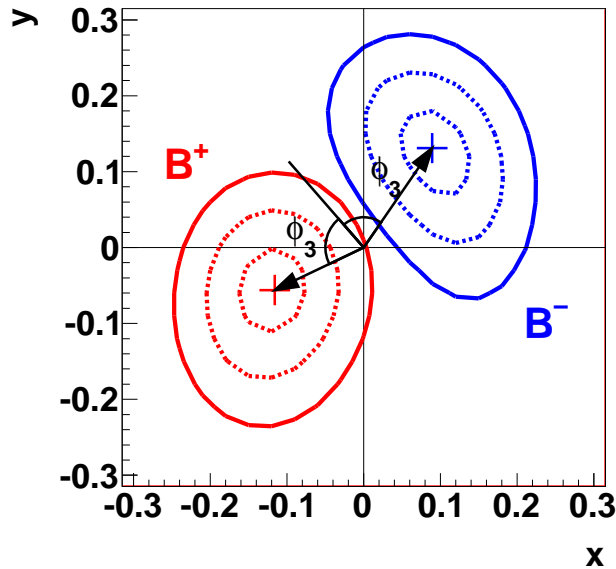


Significant CP asymmetry can be seen

0.4% probability of statistical fluctuation

$B^- \rightarrow D[K_S^0 \pi^+ \pi^-] K^- \phi_3$ Constraint

x_{\pm} and y_{\pm} determined in the fit, constrain ϕ_3 , r_B and δ_B



$$\phi_3 = (77.3_{-14.9}^{+15.1} \pm 4.2 \pm 4.3)^\circ \text{ cf. } \phi_3 = (78_{-12}^{+11} (\text{stat}) \pm 4 (\text{syst}) \pm 9 (\text{model}))^\circ$$

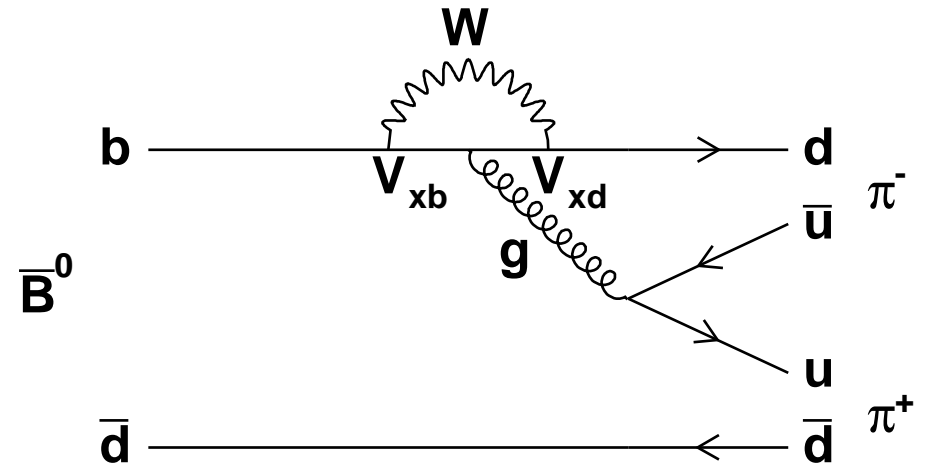
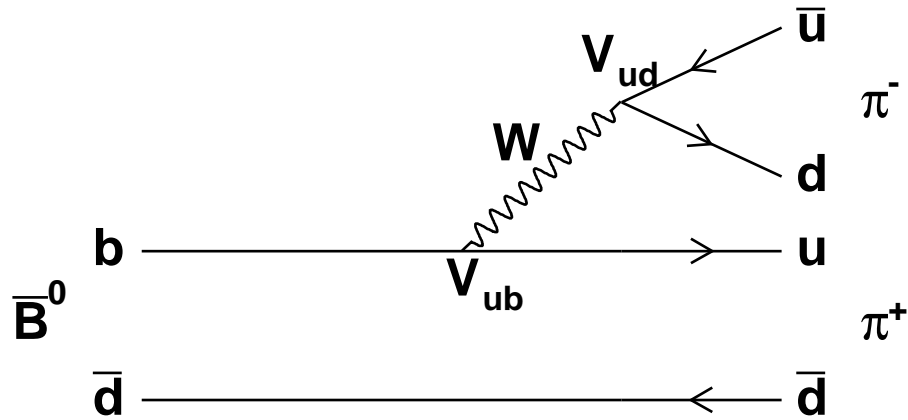
$$r_B = 0.145 \pm 0.030 \pm 0.011 \pm 0.011$$

$$\delta_B = (129.9 \pm 15.0 \pm 3.9 \pm 4.7)^\circ$$

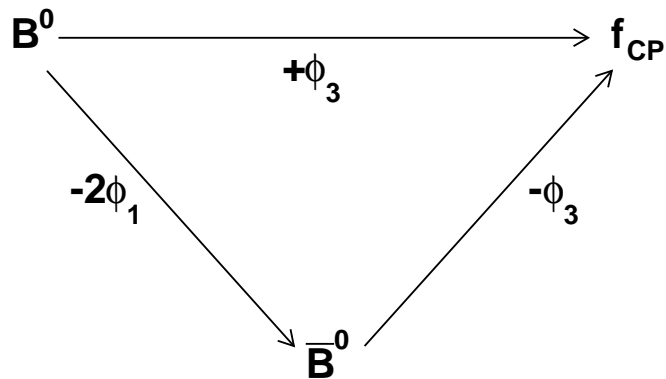
1st error - statistical, 2nd - systematic, 3rd - c_i, s_i precision

Precision comparable to previous measurement with $B^- \rightarrow DK^-$ only

$b \rightarrow u \bar{u} d$



V_{ub} carries the phase $e^{-i\phi_3}$



For tree amplitude,

The phase difference is $-2\phi_1 - \phi_3 - \phi_3$

Assuming a closed triangle, $2\phi_1 + 2\phi_3 = 2\pi - 2\phi_2$

Expect $\mathcal{A}_{CP} = 0$, $\mathcal{S}_{CP} = \sin 2\phi_2$

Departure from these in presence of penguin contribution

ϕ_2 Status

$B^0 \rightarrow \pi^+ \pi^-$, $B^0 \rightarrow \rho^0 \rho^0$ and $B^0 \rightarrow a_1(1260)^\pm \pi^\mp$ are ongoing analyses

Based on final data set from Belle, 772 million $B\bar{B}$ pairs

Data reprocessing with new tracking algorithm to improve detection efficiency

$B^0 \rightarrow \pi^+ \pi^-$

Parameter	Expected statistical uncertainty (772M)	Previous statistical uncertainty (535M)
\mathcal{A}_{CP}	0.06	0.08
\mathcal{S}_{CP}	0.08	0.10

Also expected to be the most precise measurement

$B^0 \rightarrow \rho^0 \rho^0$

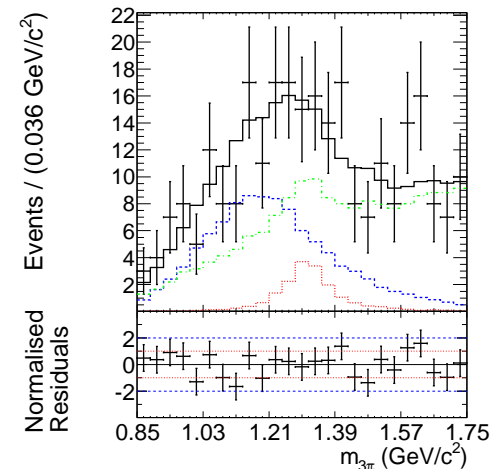
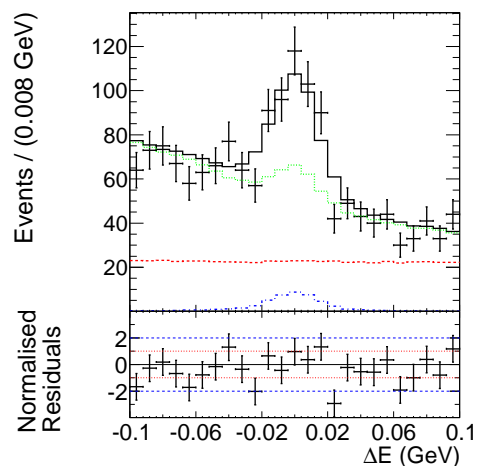
Parameter	Expected statistical uncertainty	World Average statistical uncertainty
\mathcal{B}	46%	38%
f_L	0.24	0.15

Halved statistical uncertainty over previous measurement \Rightarrow Improved upper limit at least

ϕ_2 Status

$$B^0 \rightarrow a_1(1260)^\pm \pi^\mp$$

Statistical uncertainty on branching fraction $\sim 7\%$ cf. world average $\sim 11\%$



Based on yield of 1445 ± 101 events, expected statistical uncertainties

Parameter	Expected statistical uncertainty	World Average statistical uncertainty
\mathcal{A}_{CP}	0.05	0.07
\mathcal{C}_{CP}	0.10	0.15
\mathcal{S}_{CP}	0.12	0.21

Expected to be the most precise measurement

Summary

First evidence for $B^- \rightarrow D_{\text{Sup}}[K^+\pi^-]K^-$

Most precise measurement of ADS observables \mathcal{R}_{DK} and \mathcal{A}_{DK}

First ϕ_3 measurement with binned Dalitz plot analysis

$$\phi_3 = (77.3_{-14.9}^{+15.1} \pm 4.2 \pm 4.3)^\circ$$

Model-dependent result dominates the world average

Precision comparable to model-dependent analysis with $B^- \rightarrow DK^-$ only

Final results on ϕ_2 related modes expected soon

$B^0 \rightarrow \pi^+\pi^-$ and $B^0 \rightarrow a_1(1260)^\pm\pi^\mp$ should dominate the world averages

If no signal found, $B^0 \rightarrow \rho^0\rho^0$ upper limit expected improve at least, should impact on ϕ_2

Backup

Measuring c_i, s_i

Can be obtained in $\psi(3770) \rightarrow D^0 \bar{D}^0$ decays

Coherent D^0 and \bar{D}^0 pairs produced

If both D^0 and \bar{D}^0 decay to $K_S^0 \pi^+ \pi^-$,

$$N_{ij} = K_i K_{-j} + K_{-i} K_j - 2\sqrt{K_i K_{-i} K_j K_{-j}}(c_i c_j + s_i s_j)$$

N_{ij} : Number of events in bin i (j) for $D_{1(2)} \rightarrow K_S^0 \pi^+ \pi^-$

Constrain c_i, s_i

If one D decays to a CP eigenstate while the other decays to $K_S^0 \pi^+ \pi^-$,

$$N_i = K_i + K_{-i} - 2\sqrt{K_i K_{-i}} c_i$$

N_i : Number of events in bin i for $D \rightarrow K_S^0 \pi^+ \pi^-$

Constrain c_i only